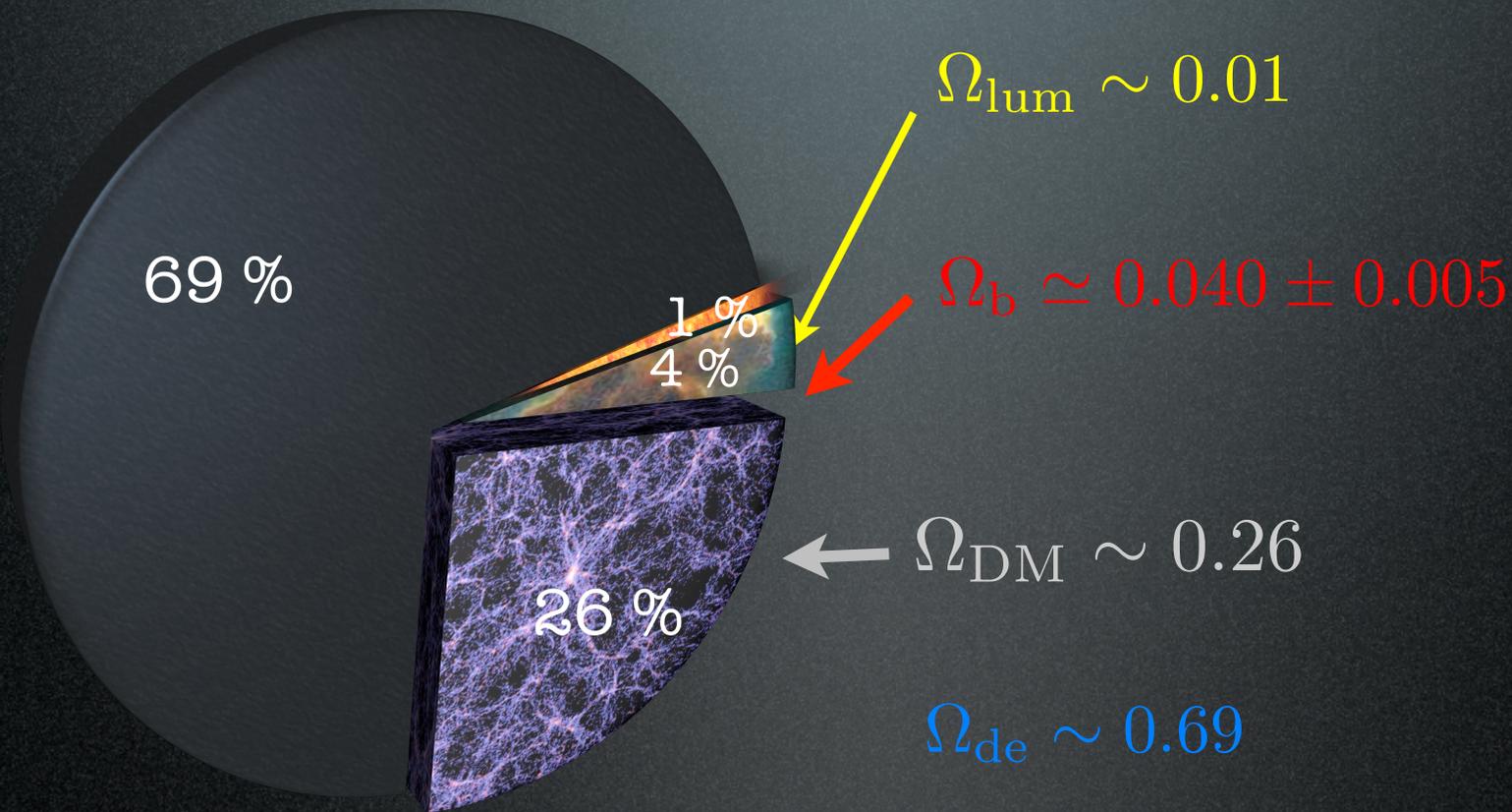


Energia Oscura *(Dark Energy)*

How do we know that
Dark Energy is out there?

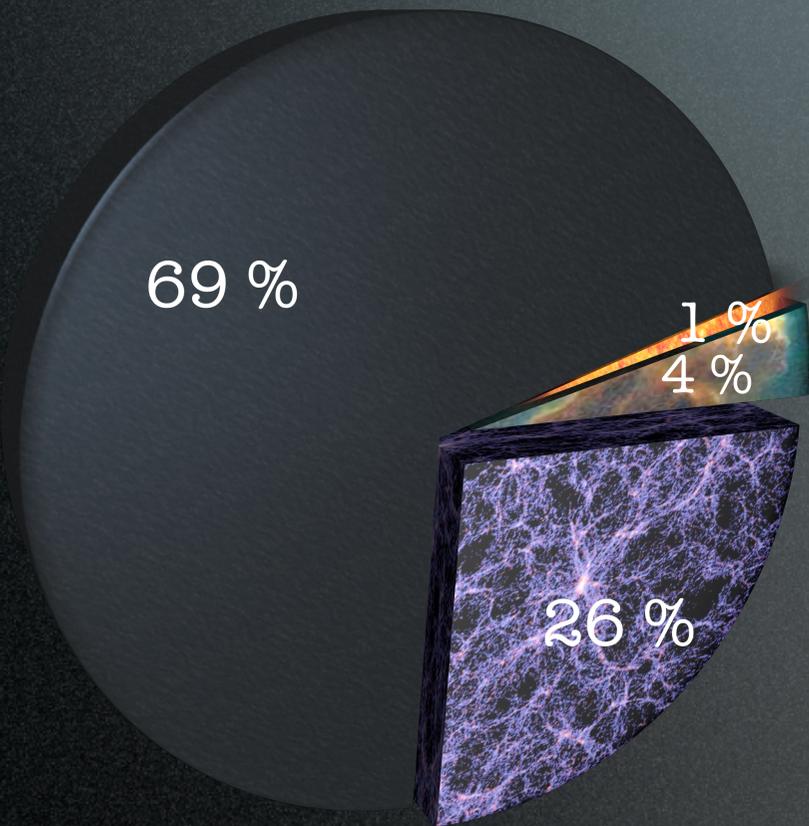
The cosmic inventory

Most of the Universe is Dark



The cosmic inventory

'Definition' of Dark Energy:



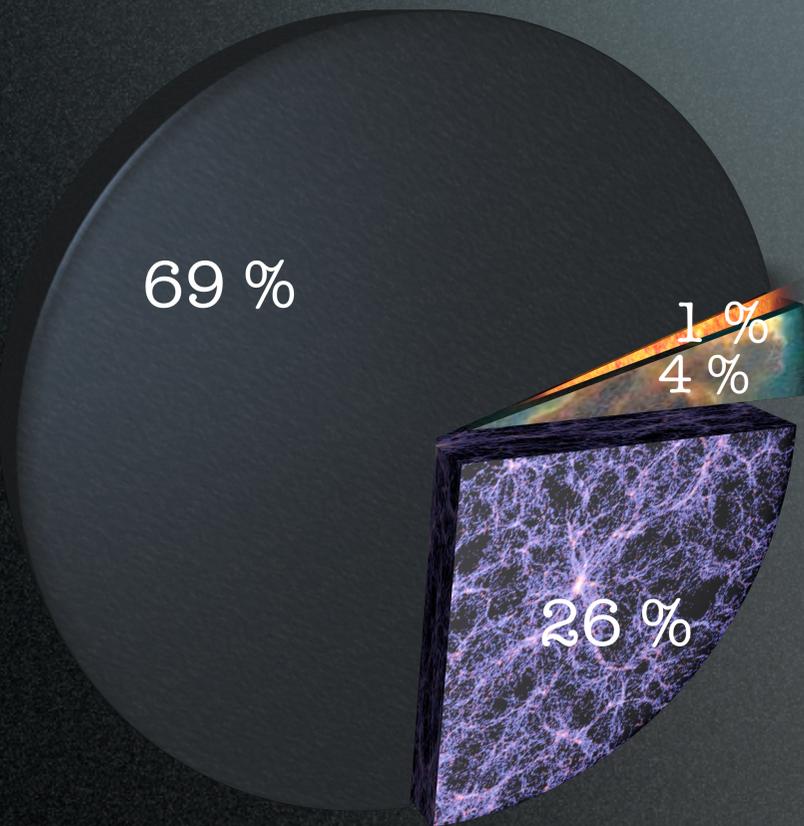
The cosmic inventory

'Definition' of Dark Energy:

Einstein equations

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3p)$$

pressure
density
the 'size' of the Universe



The cosmic inventory

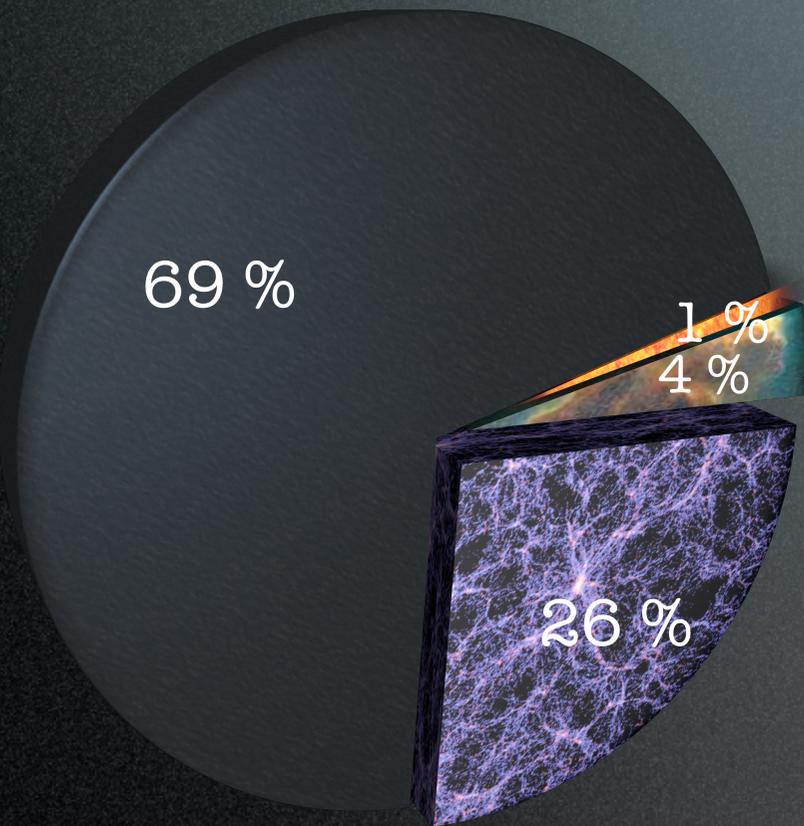
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⇒ acceleration!



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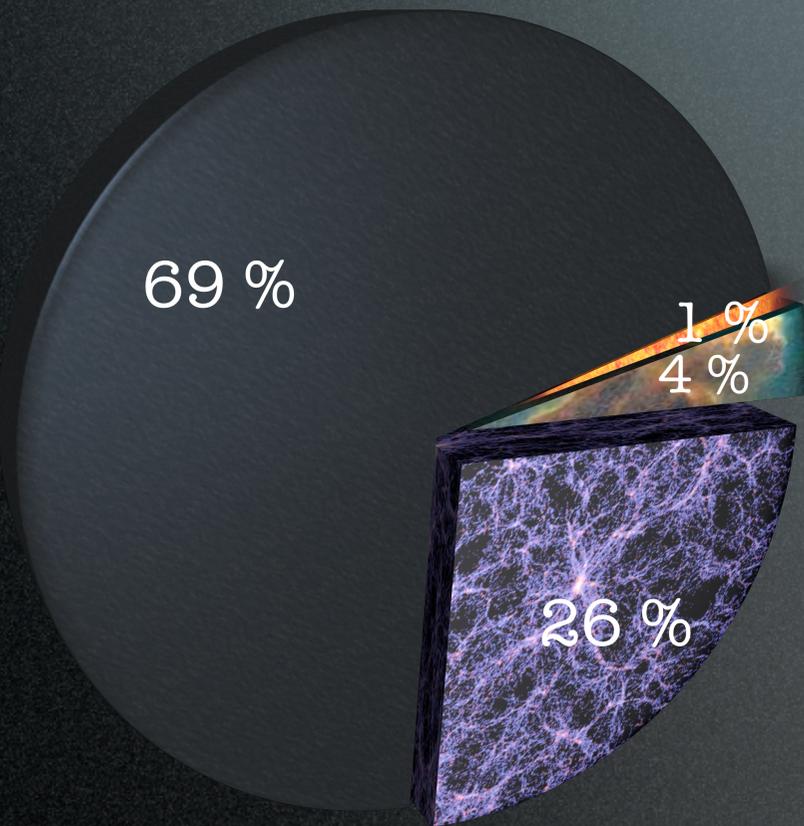
⇒ **acceleration!**

special case:

$$\rho = -p \text{ i.e. } w = -1$$

cosmological constant Λ

(constant as $\rho_i \propto (1+z)^{3(1+w_i)} \rightsquigarrow \text{const}$)



The Evidence for DE

1) Supernovae type Ia:
'standard candles'

$$\mathcal{L} = 4\pi F d_L^2$$

Luminosity ('known') Flux ('measured') Distance



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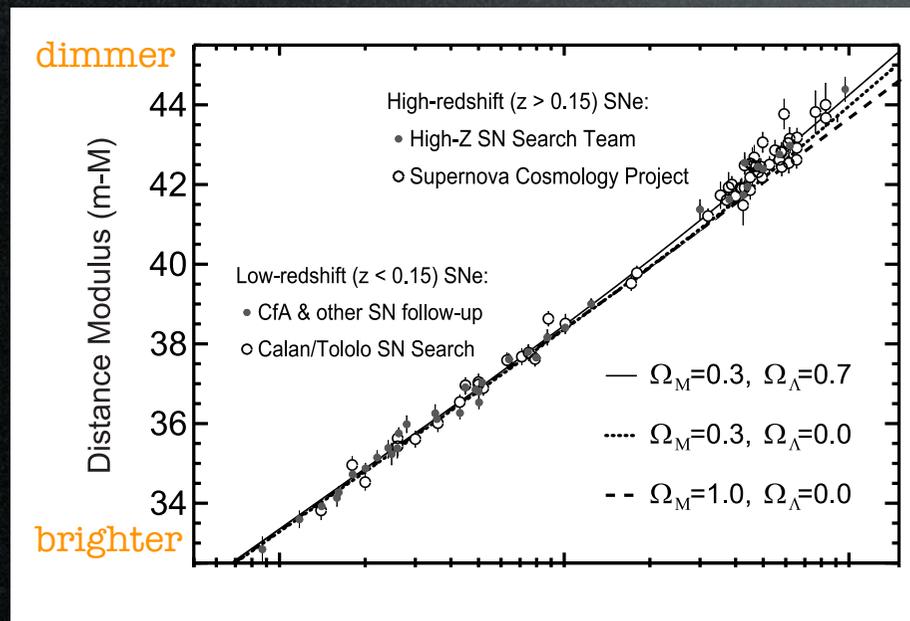


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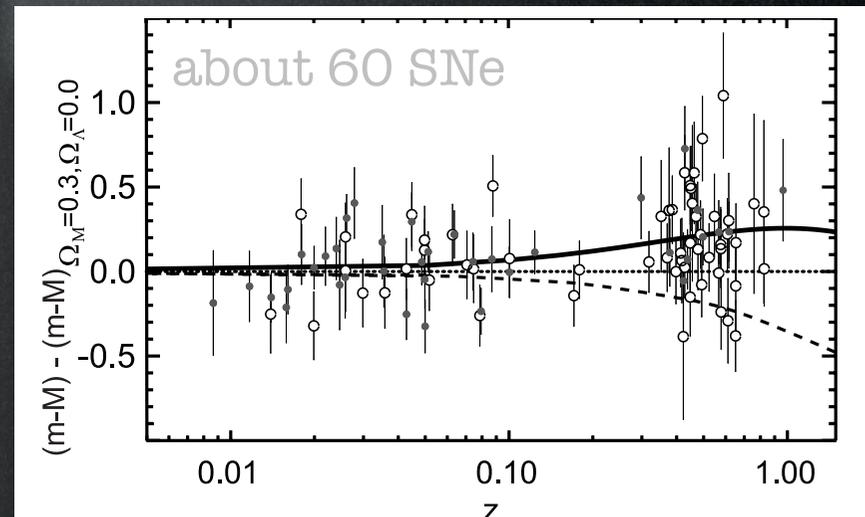
1) Supernovae type Ia: 'standard candles'

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 d_L ← "Distance"



Perlmutter et al., 1999, *Astrophys. J.* 517
 Riess et al., 1998, *Astron. J.* 116

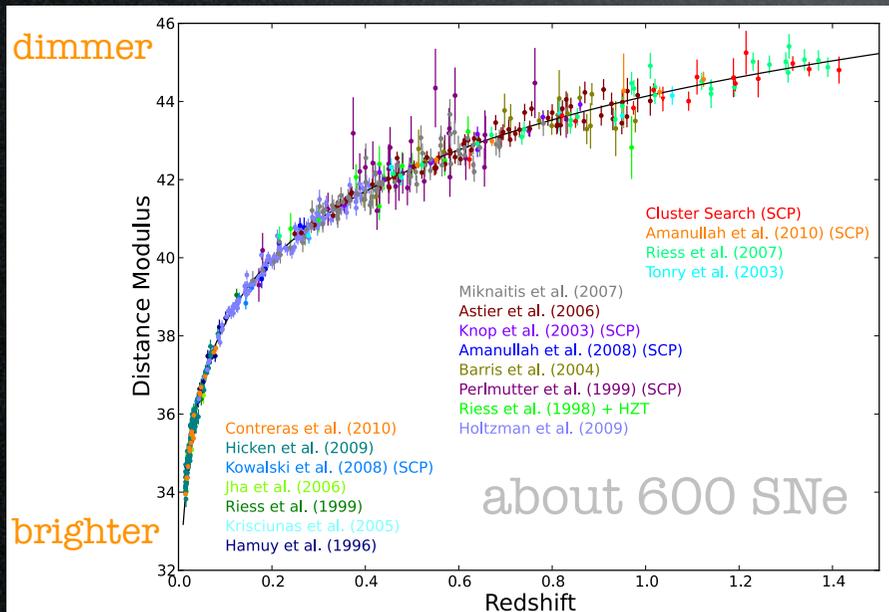


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Suzuki et al., 1105.3470

Bottom line:
 distant SNe appear **dimmer**
 than predicted in a Universe
 without DE,
 the Universe has **accelerated**
 in the past 5 Gyr

The Evidence for DE

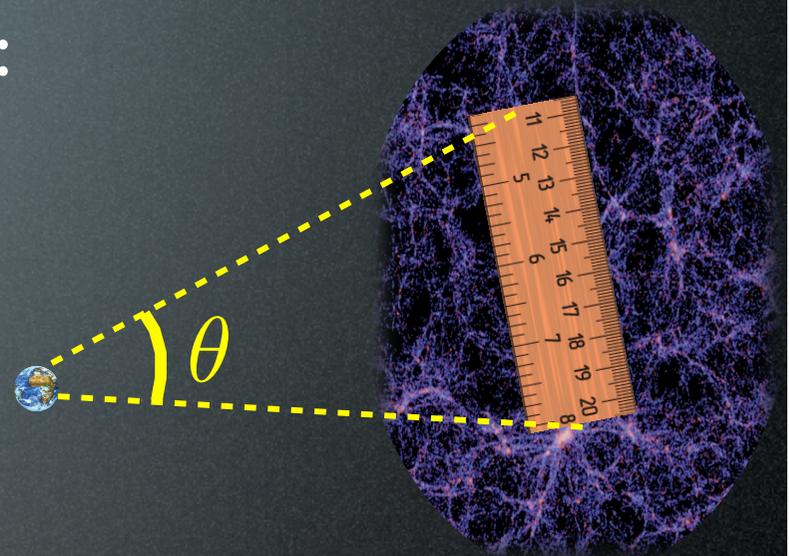
2) Baryon Acoustic Oscillations: 'standard ruler'

$$L = \theta d_A$$

L ← Length ('known')

θ ← Angle ('measured')

d_A ← Angular distance ('unknown')



The Evidence for DE

2) Baryon Acoustic Oscillations:

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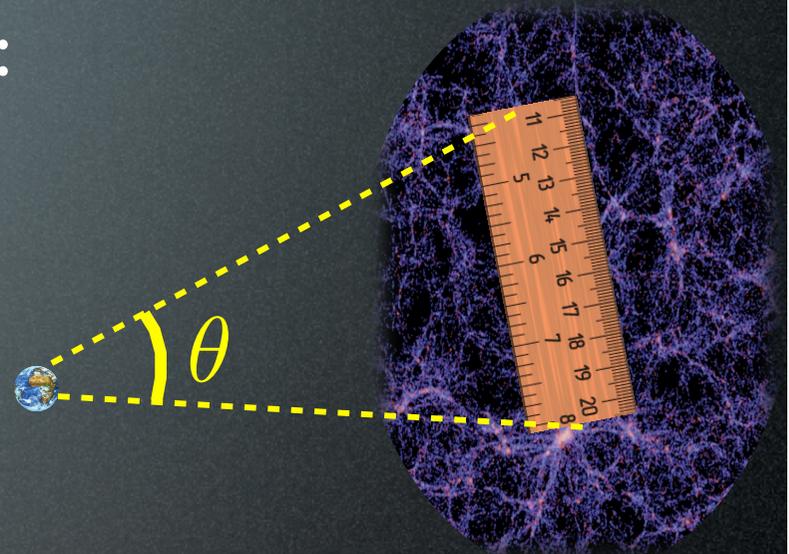
$$L = \theta d_A = \theta \frac{\chi}{1+z}$$

Length
(‘known’)

comoving distance
(‘unknown’)

$$\chi(z) = \int_0^z \frac{dz'}{H(z')} = \int_0^z \frac{dz'}{H_0 \sqrt{\Omega_M(1+z')^3 + \Omega_\Lambda}}$$

so L as fnc of z and Ω_M, Ω_Λ



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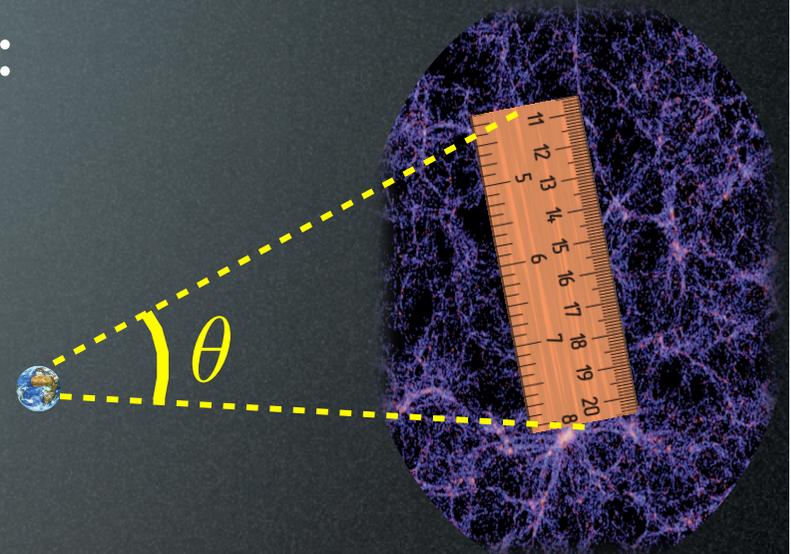
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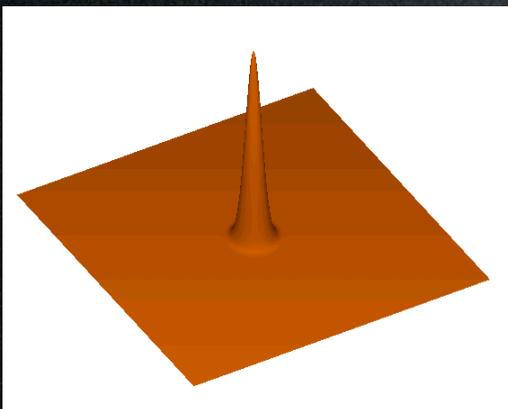
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What is the ‘ruler’?



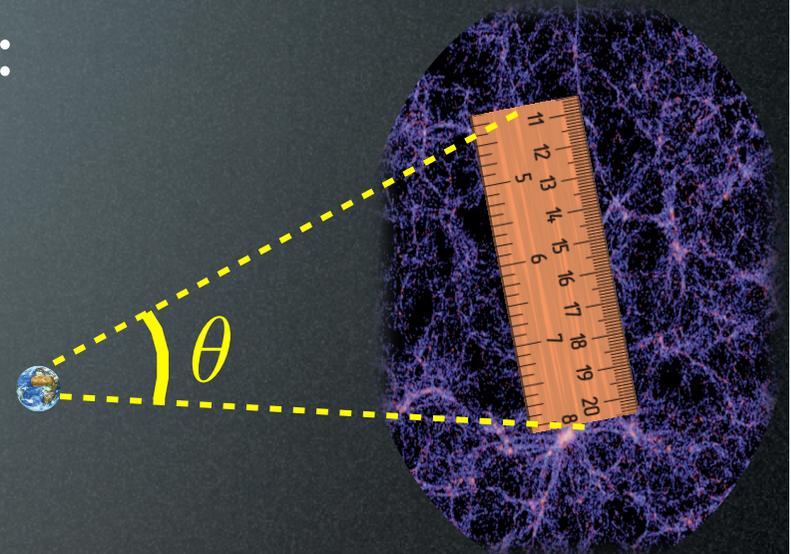
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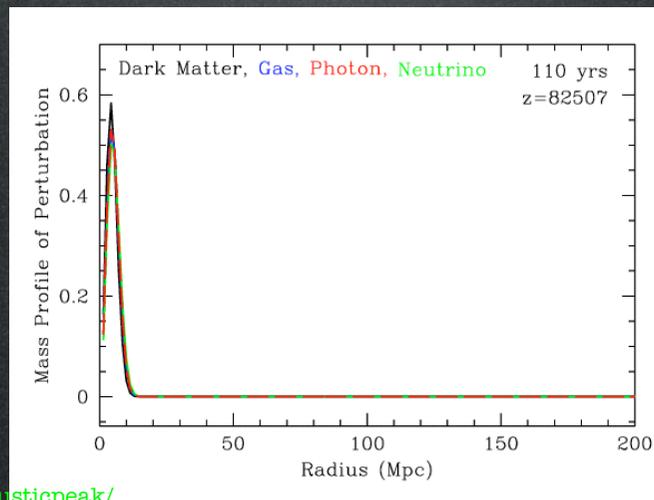
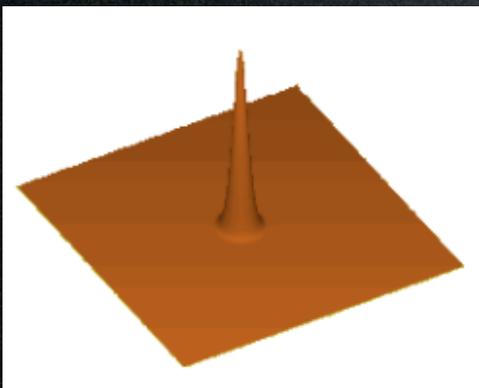
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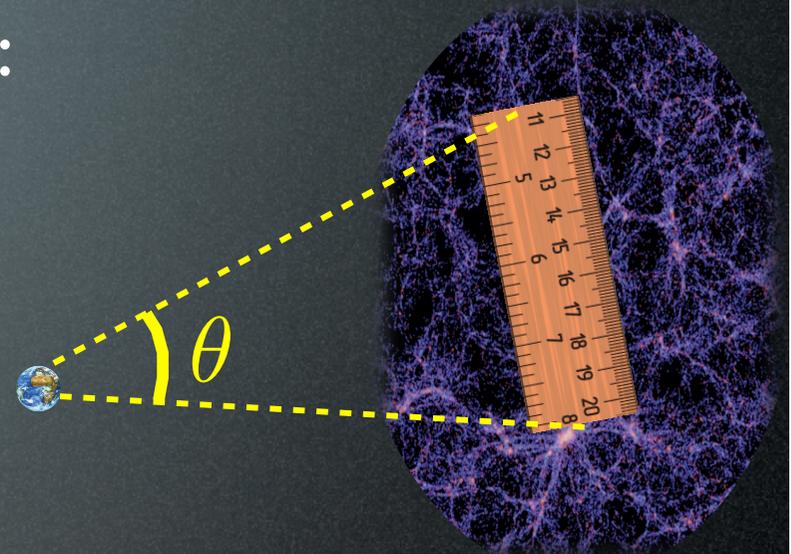
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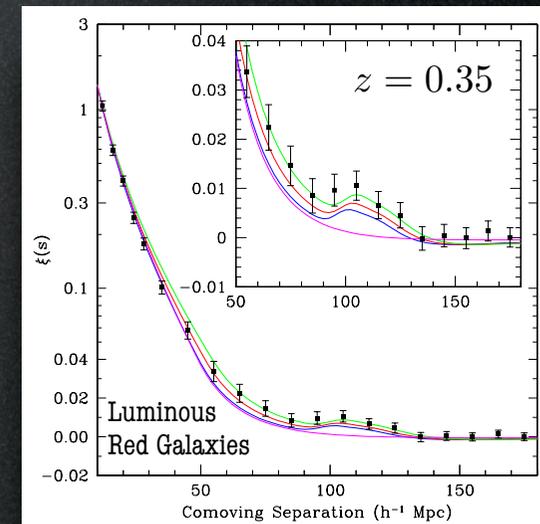
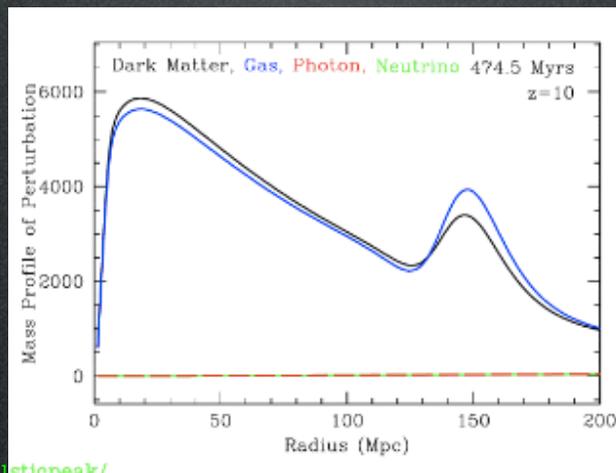
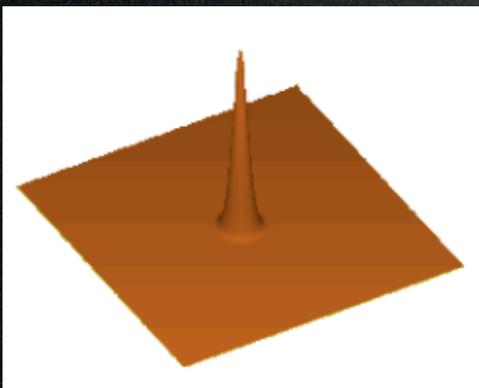
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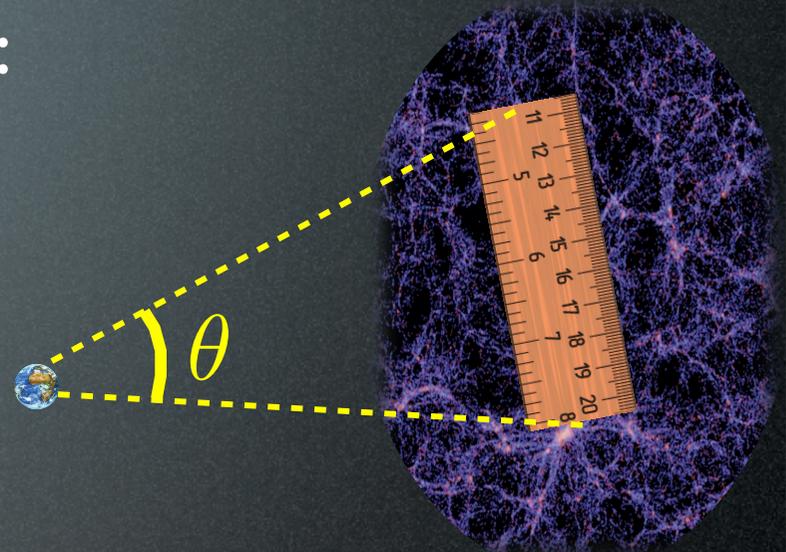
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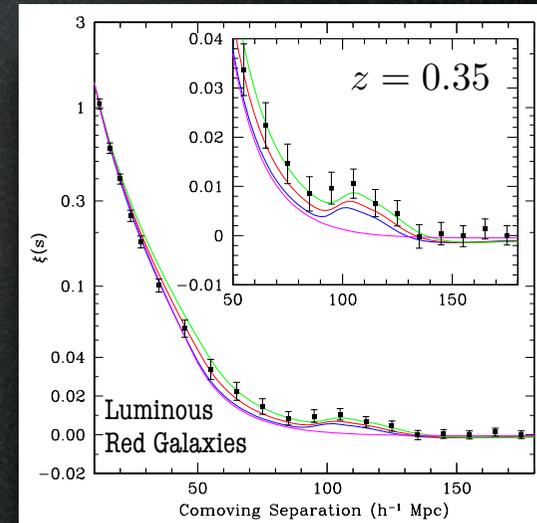
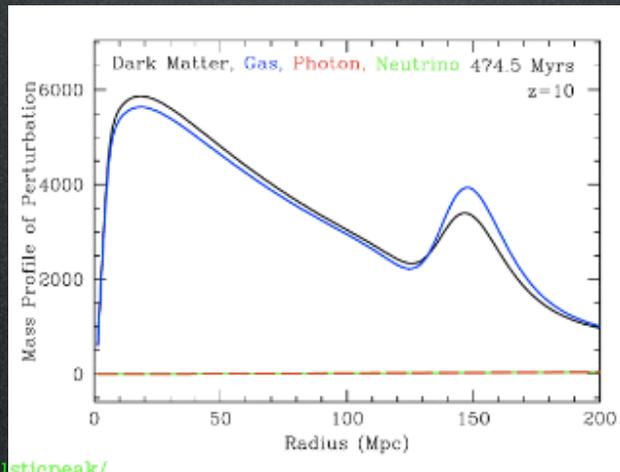
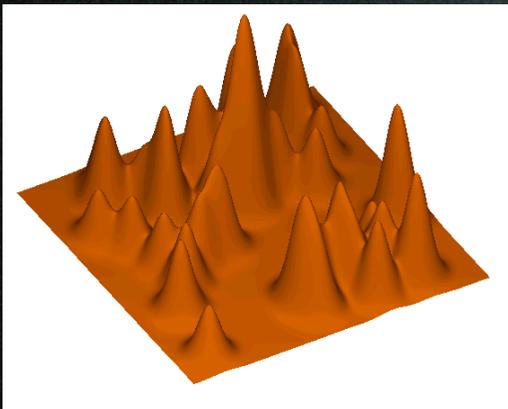
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What is the 'ruler'? A **pinch** in the **galaxy distribution**



The Evidence for DE

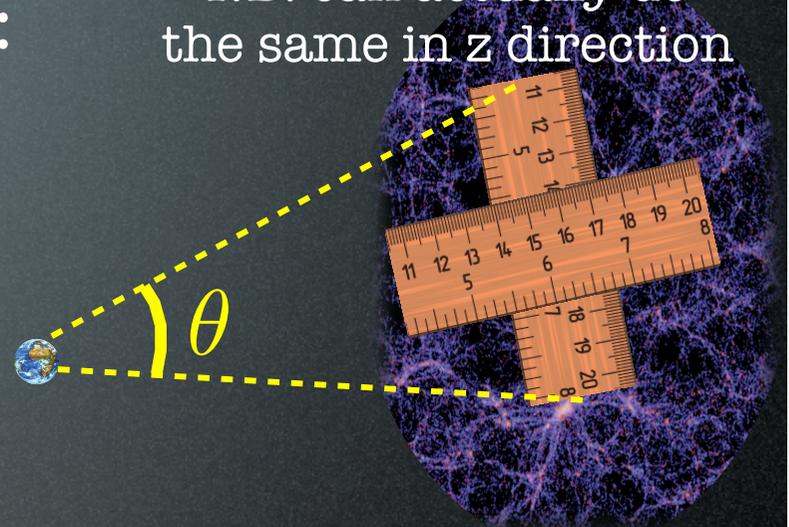
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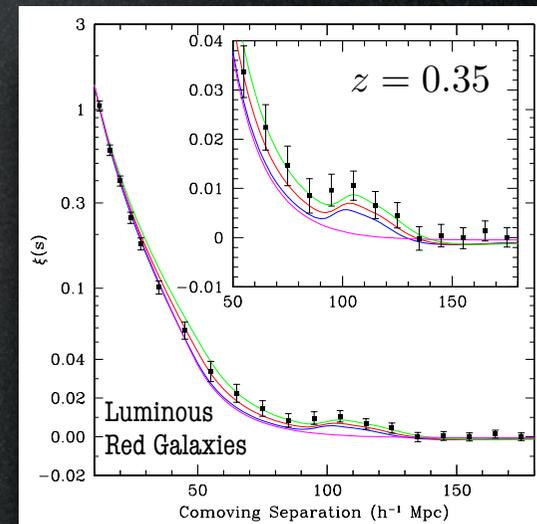
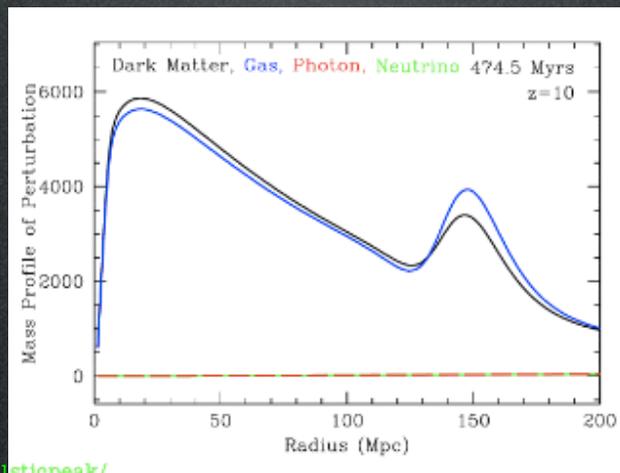
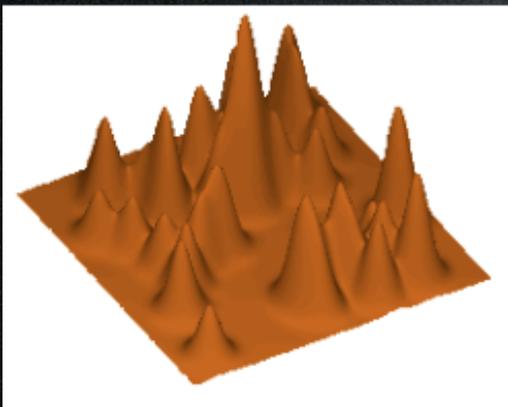
NB: can actually do the same in z direction



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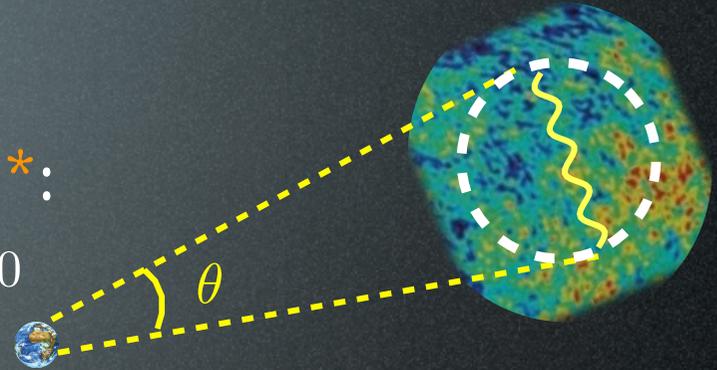
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In principle: another 'standard ruler' *:

the size of the sound horizon at $z \simeq 1100$

$$r_s = \int c_s d\tau \quad c_s \simeq c/\sqrt{3}$$



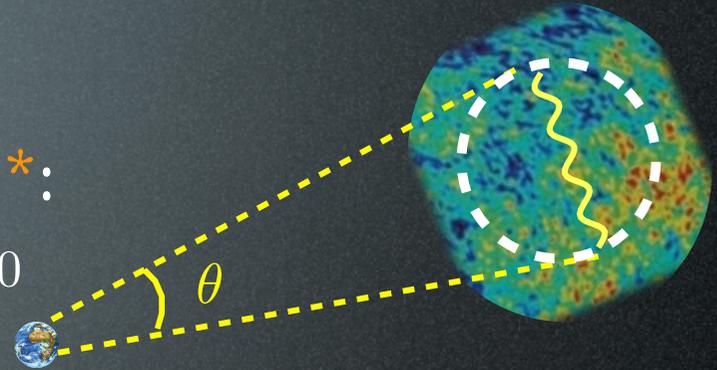
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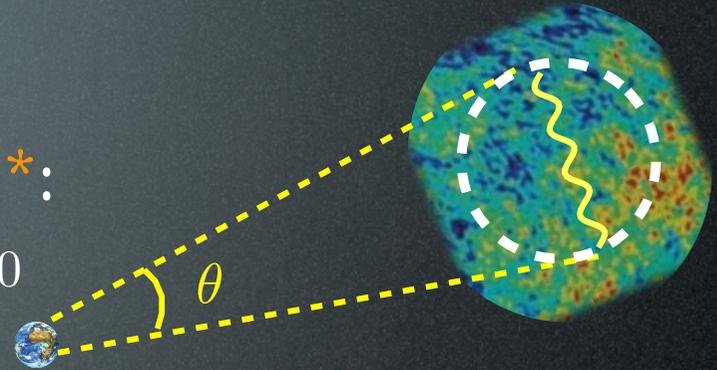
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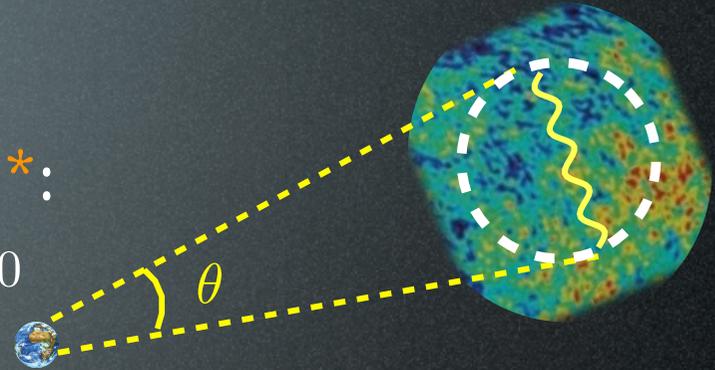
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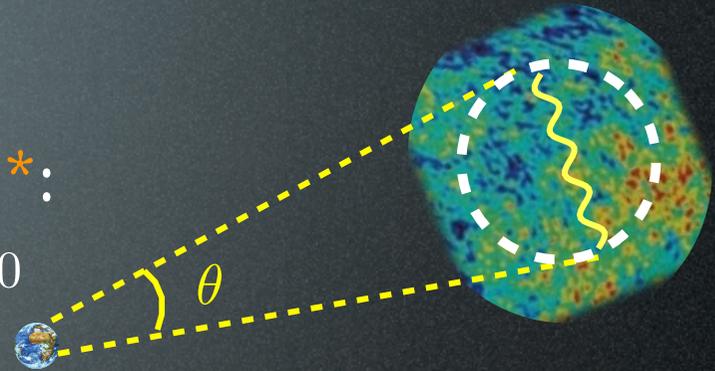
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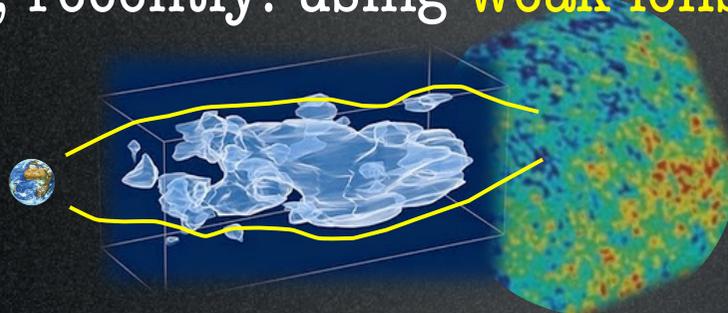


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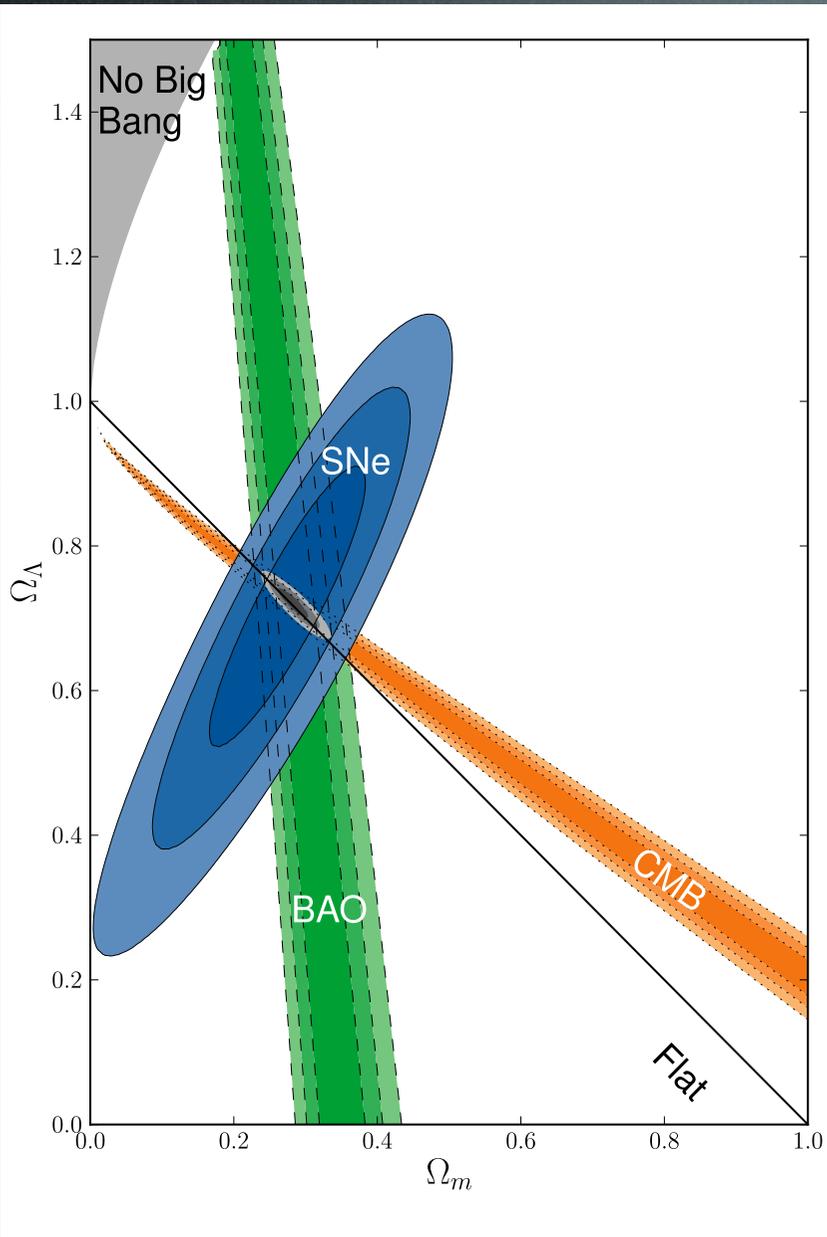
Moreover, recently: using **weak lensing** of CMB light



$$\Omega_{\Lambda} = 0.61^{+0.14}_{-0.06}$$

Sherwin et al., ACT Atacama Cosmology
Telescope, 1105.0419

The Evidence for DE



- complementarity
- concordance

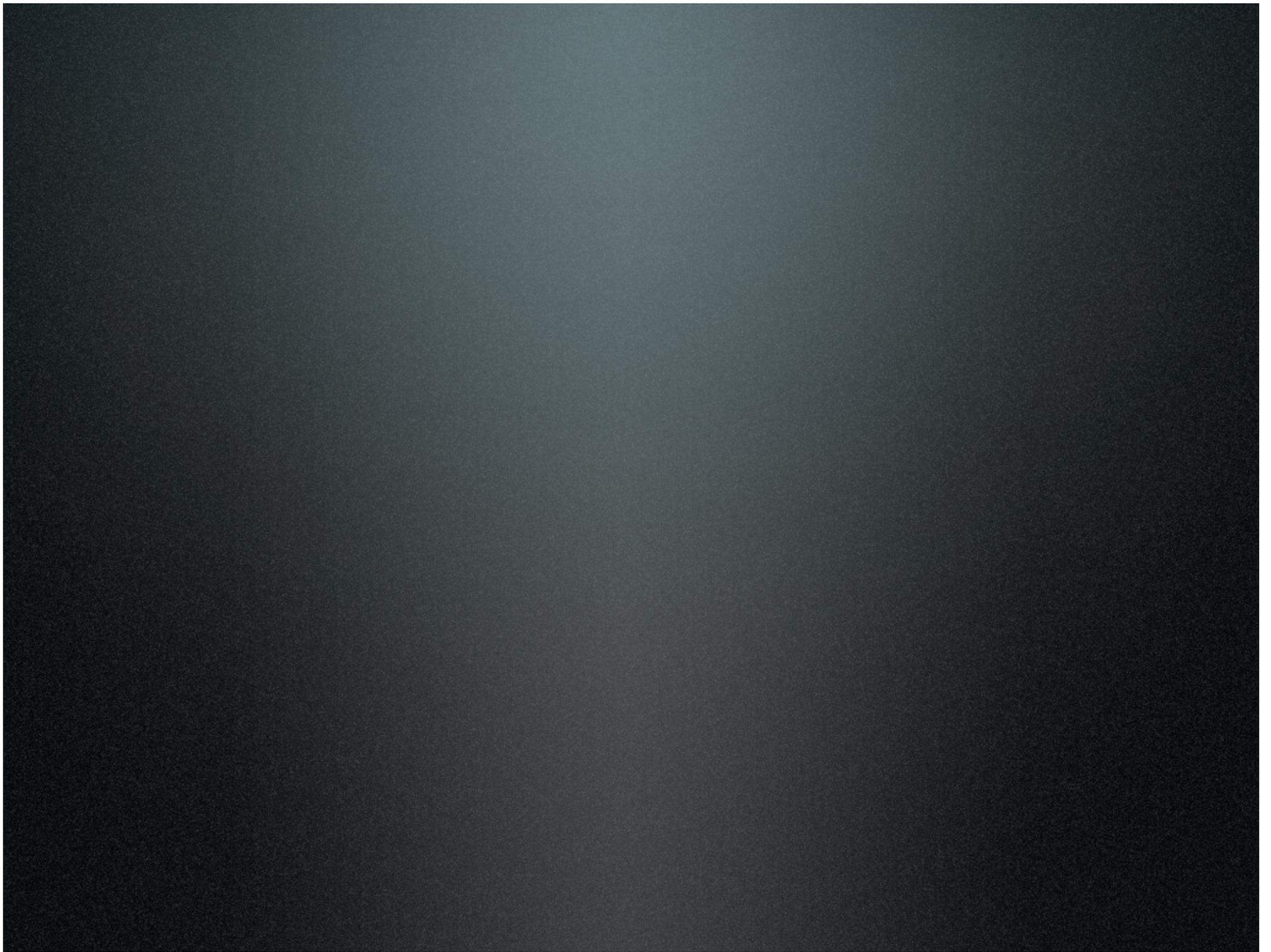
$$\Omega_\Lambda = 0.725 \pm 0.016$$

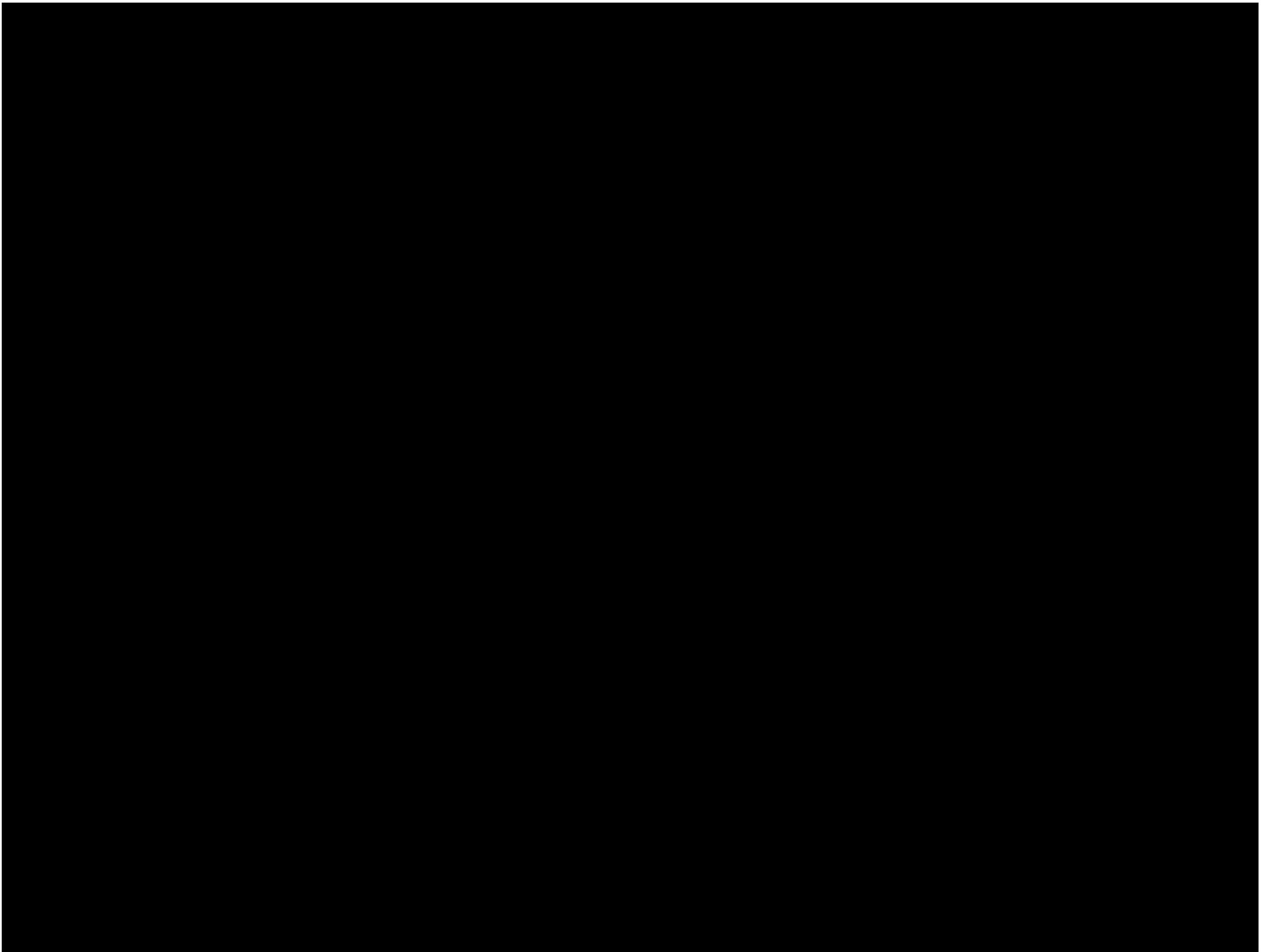
$$\Omega_M = 0.274 \pm 0.007$$

Komatsu et al., WMAP7, 1001.4538

- Other probes played / will play a role:
- cluster counts
 - weak lensing...

What do we know of the
(particle physics) properties
of Dark Energy?





Nature of DE

Λ cosmological constant, $w = -1$

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measured value $\rho_\Lambda = 2.5 \cdot 10^{-47} \text{ GeV}^4$

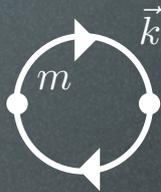
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$\simeq \sum_{\text{particles}} \frac{g_i k_{\text{max}}^4}{16 \pi^2}$



The diagram shows a circular loop with two dots on the left and right sides. The left dot is labeled 'm'. The right dot is labeled with a vector 'k' above it. Two arrows on the loop indicate a clockwise direction of travel.

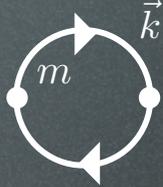
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The diagram shows a circular loop with two dots on the left and right sides. The word 'm' is written inside the loop. An arrow on the top part of the loop points to the right, and an arrow on the bottom part points to the left. A vector arrow labeled 'k' points from the center of the loop towards the top-right.

if $k_{\text{max}} \sim M_{\text{Pl}}$ $\rho_\Lambda \sim 10^{74} \text{ GeV}^4$

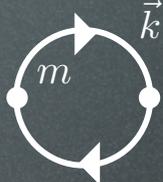
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if $k_{\text{max}} \sim M_{\text{Pl}}$ $\rho_\Lambda \sim 10^{74} \text{ GeV}^4$

121 orders
of magnitude!!

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The worst fine tuning problem. Ever.

Nature of DE

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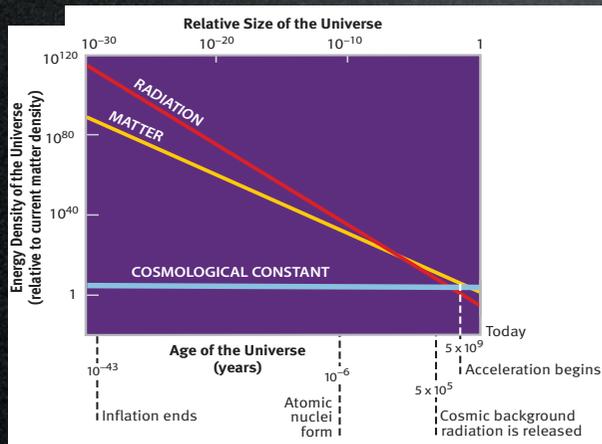
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evolution in time



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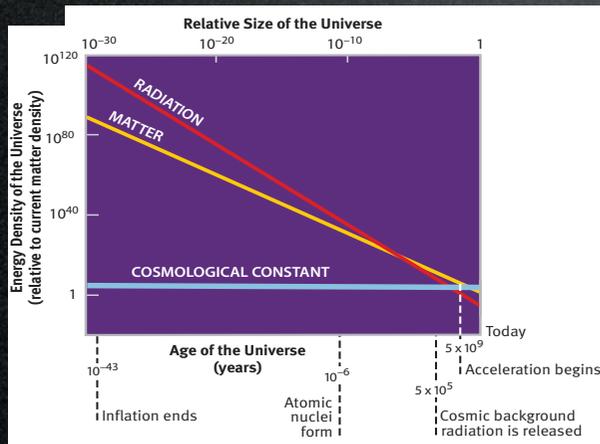
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Why now?
Coincidence problem.

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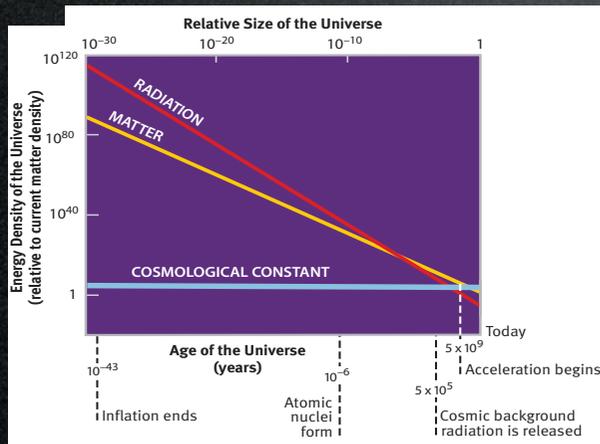
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Why now?
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Anthropism?
Multiverse?

Nature of DE

Φ 'quintessence', $w > -1$

Nature of DE

Φ 'quintessence', $w > -1$

$$\rho_{\Phi} = \frac{1}{2}\dot{\Phi}^2 + V$$

$$p_{\Phi} = \frac{1}{2}\dot{\Phi}^2 - V$$

$$w_{\Phi} = -1 + \frac{\dot{\Phi}^2}{\dot{\Phi}^2 + 2V}$$

so if $\dot{\Phi} \ll V \rightarrow$ Dark Energy

Nature of DE

Φ 'quintessence', $w > -1$

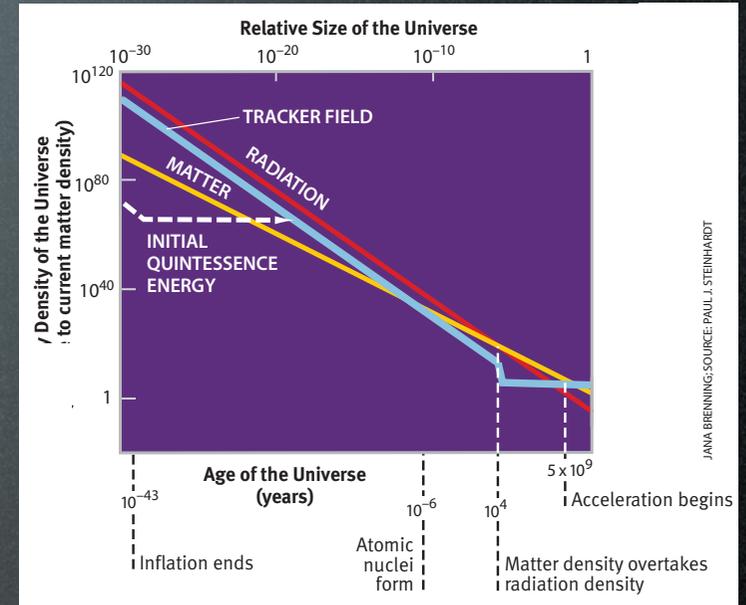
evolution in time

$$\rho_{\Phi} = \frac{1}{2} \dot{\Phi}^2 + V$$

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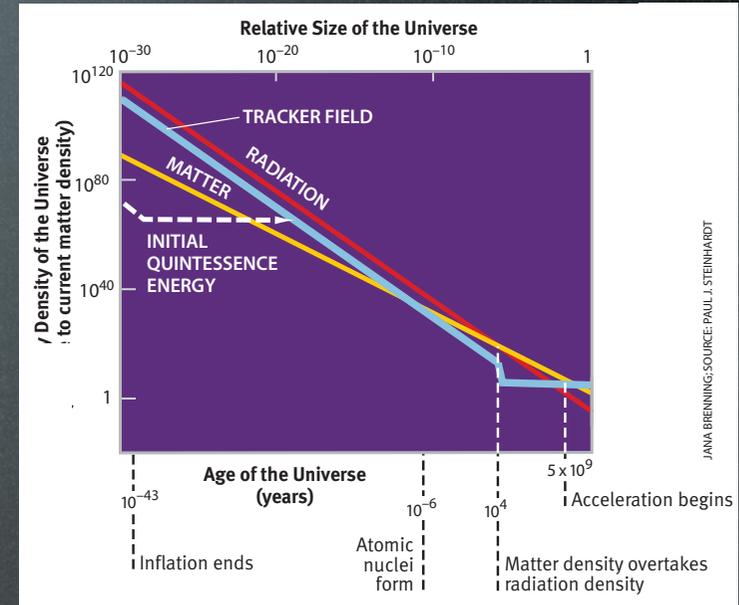
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Ostriker and Steinhard, Scientific American 2000

Modified Gravity (f(R), DGP...)

Nature of DE

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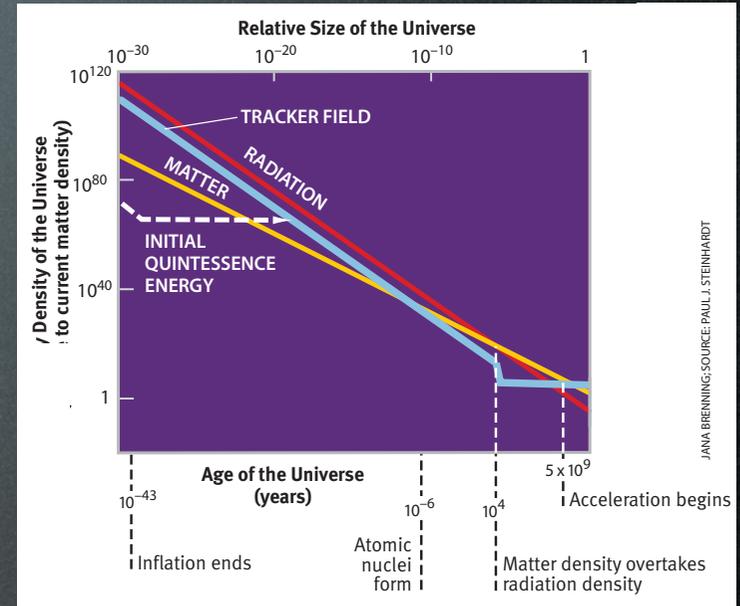
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Modified Gravity (f(R), DGP...)

Swiss cheese, local voids...



Nature of DE

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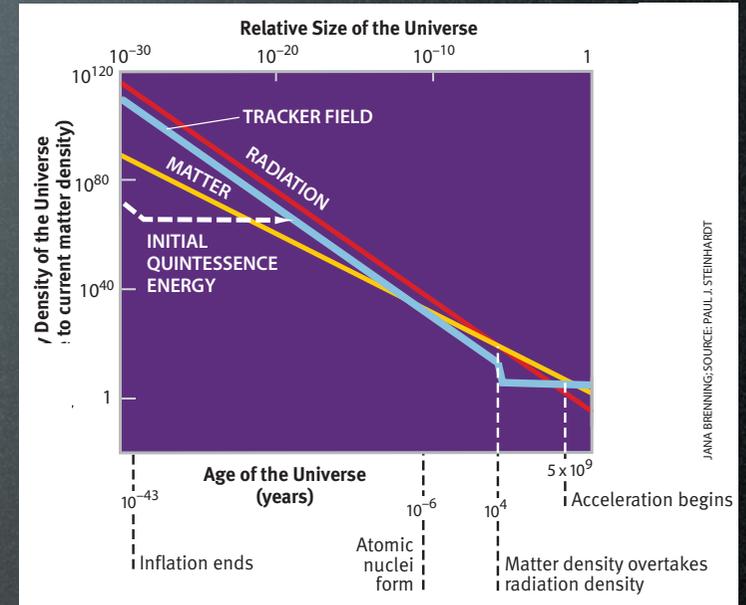
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