

```
dave@walnuts:~$ grep -i "eft" /usr/share/dict/british-english
```

```
Left
bereft
chieftain
chieftain's
chieftains
cleft
cleft's
clefts
deft
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deftest
deftly
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leftmost
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leftover's
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lefts
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lefty
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wefts
dave@walnuts:~$ █
```

Basis construction and translation with DEFT

see B. Grippaios & DS, arXiv:1807.07546, code here

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Introduction

DEFT takes as input a set of fields and their irreps under a set of $SU(N)$ -like symmetries. *In principle*, it can output:

- ▶ a list of all the contractions of products of these fields which are invariant under the symmetries, to a given order;
- ▶ a list of the redundancies between these operators (Fierz, IBPs, EOMs, &c.);
- ▶ an arbitrary operator basis;
- ▶ a matrix to convert into and between arbitrary operator bases.

This talk:

1. a look under the hood;
2. the extant obstacles to the practical use of DEFT.

'Monomial operators'

a product of fields; each field may have some covariant derivatives

In DEFT's internal machinery, all operators are expressed as linear combinations of 'monomial operators'.

$$\delta_{\dot{\gamma}}^{\dot{\alpha}} \delta_{\dot{\delta}}^{\dot{\beta}} \epsilon_{ab} \epsilon^{de} \delta_B^A$$

invariants are L-C epsilons and Kron. deltas

$$H^b \bar{Q}_{LeA}^{\dot{\gamma}} d_R^{\dot{\delta}B} \bar{W}_{\dot{\alpha}\dot{\beta}d}^a$$

$$\bar{W}_d^a \delta_a^d \equiv 0$$

$$\bar{W}_{\dot{\alpha}\dot{\beta}} \epsilon^{\dot{\alpha}\dot{\beta}} \equiv 0$$

Irreps of $SU(N)$ -like symmetries encoded by upper and lower fundamental indices.

Lagrangian redundancies

- Fierz relations $\epsilon^{\dots}\epsilon_{\dots} = \sum \delta^{\cdot}\delta^{\cdot} \dots \delta^{\cdot}$ (also Schouten identities)

$$\epsilon^{\dot{\alpha}\dot{\beta}} \bar{H}_a e_R^\alpha D_{\alpha\dot{\beta}} D_{\beta\dot{\alpha}} L_L^{\beta a} - \epsilon^{\dot{\alpha}\dot{\beta}} \bar{H}_a e_R^\alpha D_{\beta\dot{\beta}} D_{\alpha\dot{\alpha}} L_L^{\beta a} + \epsilon_{\alpha\beta} \epsilon^{\gamma\delta} \epsilon^{\dot{\alpha}\dot{\beta}} \bar{H}_a e_R^\beta D_{\delta\dot{\beta}} D_{\gamma\dot{\alpha}} L_L^{\alpha a} = 0$$

- IBPs

$$-\epsilon^{\dot{\alpha}\dot{\beta}} D_{\alpha\dot{\beta}} \bar{L}_{Lb}^{\dot{\gamma}} L_L^{\alpha a} \bar{W}_{\dot{\alpha}\dot{\gamma}a}^b - \epsilon^{\dot{\alpha}\dot{\beta}} \bar{L}_{Lb}^{\dot{\gamma}} D_{\alpha\dot{\beta}} L_L^{\alpha a} \bar{W}_{\dot{\alpha}\dot{\gamma}a}^b + \epsilon^{\dot{\alpha}\dot{\beta}} \bar{L}_{Lb}^{\dot{\gamma}} L_L^{\alpha a} D_{\alpha\dot{\beta}} \bar{W}_{\dot{\beta}\dot{\gamma}a}^b = 0$$

- Commuting derivatives

$$-\frac{1}{2} ig' \epsilon^{\alpha\beta} B_{\beta\gamma} D_{\alpha\dot{\alpha}} e_R^\gamma e_R^{\dot{\alpha}} + \frac{1}{2} ig' \epsilon^{\dot{\alpha}\dot{\beta}} \bar{B}_{\dot{\beta}\dot{\gamma}} D_{\alpha\dot{\alpha}} e_R^\alpha e_R^{\dot{\gamma}} - \epsilon^{\alpha\beta} \epsilon^{\dot{\alpha}\dot{\beta}} D_{\gamma\dot{\beta}} D_{\beta\dot{\gamma}} D_{\alpha\dot{\alpha}} e_R^\gamma e_R^{\dot{\gamma}} + \epsilon^{\alpha\beta} \epsilon^{\dot{\alpha}\dot{\beta}} D_{\beta\dot{\gamma}} D_{\gamma\dot{\beta}} D_{\alpha\dot{\alpha}} e_R^\gamma e_R^{\dot{\gamma}} = 0$$

EOM relations²

Local field redefinitions don't affect S -matrix elements

$$\phi(x) \rightarrow \phi(x) + \frac{U[\phi](x)}{\Lambda^2} \implies S_4 + \frac{S_6}{\Lambda^2} \rightarrow S_4 + \frac{1}{\Lambda^2} \left(S_6 + \int dx U \frac{\delta S_4}{\delta \phi} \right) + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$$

We calculate the **marginal EOM**, whose parts plus the **remainder** we find in higher dimensional terms¹

$$\begin{aligned} & -\frac{1}{2} \epsilon_{\alpha\beta} \epsilon^{\gamma\delta} \epsilon^{\dot{\alpha}\dot{\beta}} \epsilon_{ab} D_{\delta\dot{\beta}} D_{\gamma\dot{\alpha}} H^b Q_L^{\beta a A} \bar{u}_{R A}^{\alpha} \\ & + y_e^{\dagger} \epsilon_{\alpha\beta} \epsilon_{\gamma\delta} \epsilon_{ab} \bar{e}_R^{\delta} L_L^{\gamma b} Q_L^{\beta a A} \bar{u}_{R A}^{\alpha} + y_u \epsilon_{\alpha\beta} \epsilon_{\dot{\alpha}\dot{\beta}} \bar{Q}_{L a B}^{\dot{\beta}} Q_L^{\beta a A} \bar{u}_{R A}^{\alpha} u_R^{\dot{\alpha} B} \\ & + y_d^{\dagger} \epsilon_{\alpha\beta} \epsilon_{\gamma\delta} \epsilon_{ab} Q_L^{\delta b A} Q_L^{\beta a B} \bar{u}_{R B}^{\alpha} \bar{d}_{R A}^{\gamma} - 2\lambda \epsilon_{\alpha\beta} \epsilon_{ab} \bar{H}_d H^b H^d Q_L^{\beta a A} \bar{u}_{R A}^{\alpha} \end{aligned}$$

= operators of different dimension, which we ignore

¹taking care over the **contractions** between the two

²Because they look similar, we include Bianchi identities $D_{\mu} \tilde{F}^{\mu\nu} = 0$ in this class.

Put all the relations in a matrix

Each relation is a vector of Wilson coefficients $\sum_i c_i \mathcal{O}_i = 0$.
Collect these as the rows of a matrix.

$$\begin{array}{r} \begin{array}{cccccc} & c_1 & c_2 & c_3 & & c_N \\ & \downarrow & \downarrow & \downarrow & & \downarrow \\ \text{relation 1} \rightarrow & i & 0 & y_u & 0 & \dots & 0 \\ \text{relation 2} \rightarrow & 1 & 0 & 0 & 1 & \dots & g_s \\ & \vdots & & & & & \\ & \cdot & & & & & \\ & \cdot & & & & & \end{array} \end{array}$$

The rest is linear algebra, for which we use `sympy`. We've checked the ranks of these matrices for various subsets and simple extensions of the one generation SM, using Hilbert series methods.

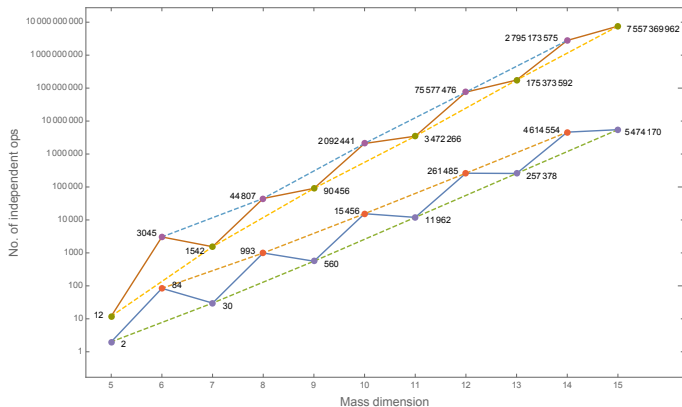
Reducing to a non-redundant basis

1. Perform column operations to express the relations in terms of the coefficients of the operators we want to keep, $\{B_1, B_2\}$, and the ones we want to eliminate, $\{R_1, R_2, R_3\}$
2. Perform row operations to reduce to the following form

$$\begin{array}{ccccc} c_{R_1} & c_{R_2} & c_{R_3} & c_{B_1} & c_{B_2} \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ \left(\begin{array}{ccc|cc} 1 & 0 & 0 & * & * \\ 0 & 1 & 0 & * & * \\ 0 & 0 & 1 & * & * \\ \hline 0 & 0 & 0 & 0 & 0 \end{array} \right) \end{array}$$

Iff. the matrix can be put in this form, $\{B_1, B_2\}$ is a valid basis.

DEFT presently runs out of steam pretty quickly



(From Henning, Lu, Melia, Murayama arXiv:1512.03433)

For the one generation Standard Model on a laptop:

- ▶ ~ 45 minutes to generate dim 6 operators and convert from Warsaw to SILH basis
- ▶ ~ 1 day to generate a basis of dim 8 operators

#TODO

- ▶ **Generational indices** Leave them uncontracted or contracted with 0-dimensional spurions in the irreps of the flavour symmetries
- ▶ **Convert between invariants** $\gamma^\mu, \lambda^A, \dots \leftrightarrow \epsilon, \delta$
- ▶ **Interfaces** Print-out to FeynRules, ... (although note built-in AllYourBases module)
- ▶ **SM in broken phase** Substitute B, W, H for A, Z, W, h
- ▶ **Transdimensional interactions** Expand EOM relations to higher orders. Systematically calculate corrections to lower order params.
- ▶ **Tabulate higher irreps of $SU(N)$** Currently has the rules for (anti)-fundamental, adjoint and all-symmetric tensors
- ▶ **Refactoring** Speed-ups, especially in row reduction methods and memory management

SM applications?

- ▶ **Matching** Matching a UV theory to the SMEFT is typically done off-shell. One needs to define a ‘Green’s function basis’ and expressions to convert into the usual ‘S-matrix bases’.
- ▶ **Phenomenology of $d > 6$** Can study novel processes and define precisely the validity of the EFT expansion.

Summary

Fields and symmetries in, operators and bases out. In particular, it's been tested against existing results for the one-generation Standard Model.

DEFT is very much a 'proof of concept'. All feedback welcome!