



# The WHIZARD Generator for Lepton Colliders



Jürgen R. Reuter, DESY





# WHIZARD: Introduction / Technical Facts

WHIZARD v2.6.4 (23.08.2018)

<http://whizard.hepforge.org>

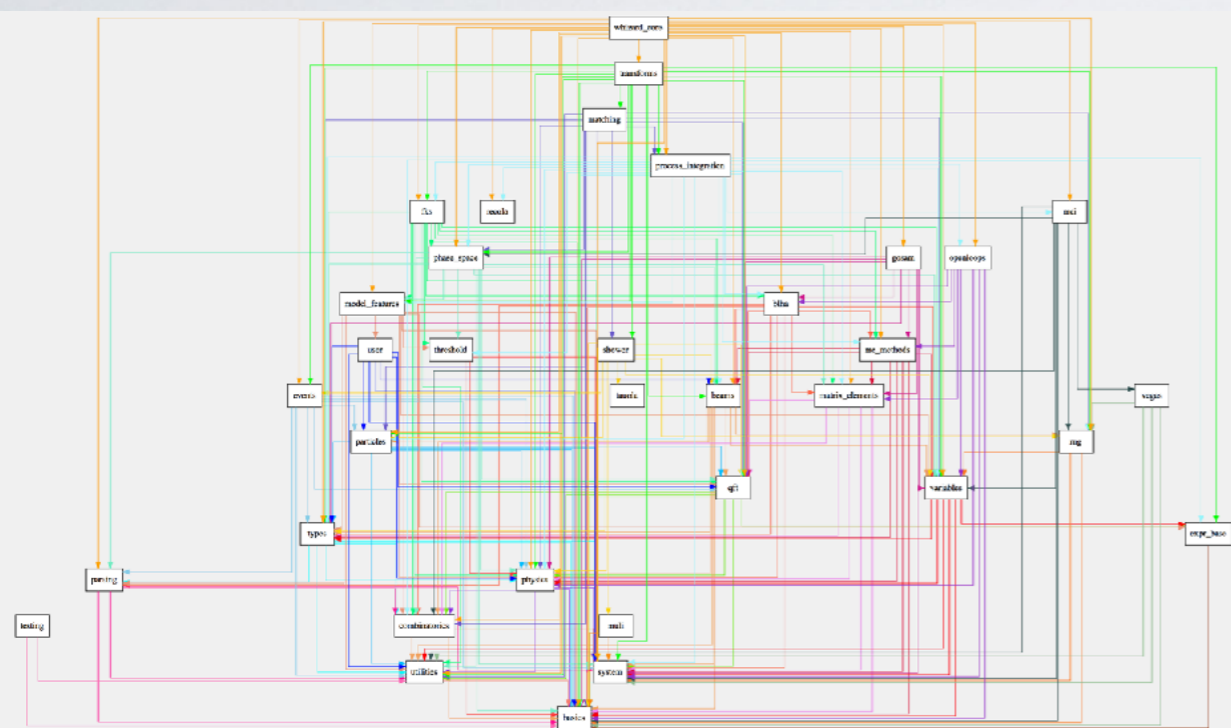
<whizard@desy.de>

WHIZARD Team: *Wolfgang Kilian, Thorsten Ohl, JRR*

*Simon Braß/Nils Kreher/Vincent Rothe/So Young Shim/Pascal Stienemeier/Zhijie Zhao*

## PUBLICATIONS

General WHIZARD reference: EPJ C71 (2011) 1742, arXiv:0708.4241  
 O' Mega (ME generator): LC-TOOL (2001) 040; arXiv:hep-ph/0102195  
 VAMP (MC integrator): CPC 120 (1999) 13; arXiv:hep-ph/9806432  
 CIRCE (beamstrahlung): CPC 101 (1997) 269; arXiv:hep-ph/9607454  
 Parton shower: JHEP 1204 (2012) 013; arXiv:1112.1039  
 Color flow formalism: JHEP 1210 (2012) 022; arXiv:1206.3700  
 NLO capabilities: JHEP 1612 (2016) 075; arXiv:1609.03390  
 Parallelization of MEs: CPC 196 (2015) 58; arXiv:1411.3834  
 POWHEG matching: EPS-HEP (2015) 317; arXiv:1510.02739



- Programming Languages: Fortran2008 (gfortran  $\geq 5.1.0$ ), OCaml ( $\geq 3.12.0$ )
- Standard installation: `configure <FLAGS>, make, [make check], make install`
- Installed centrally, production runs in specific workspaces
- Large self test suite, unit tests [module tests], regression testing
- **Continuous integration system (gitlab CI @ Siegen)**





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WHIZARD v2.7.0 (21.01.2019)

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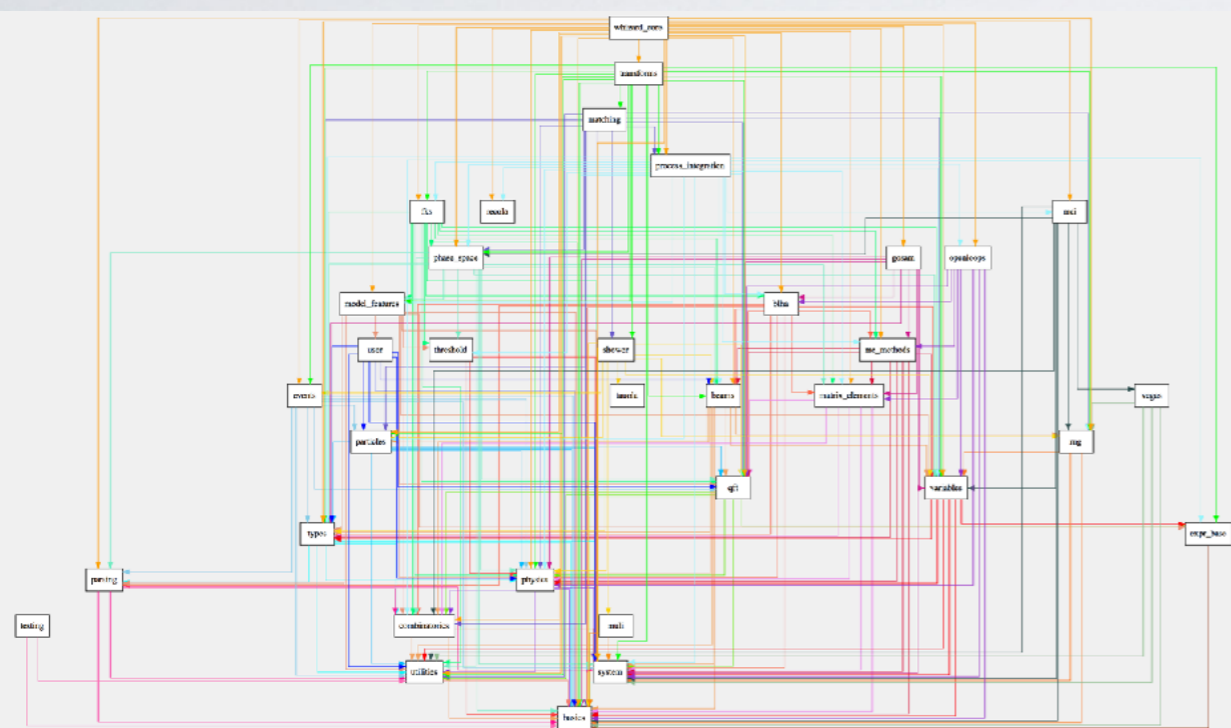
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# WHIZARD: Past and recent timeline (I)

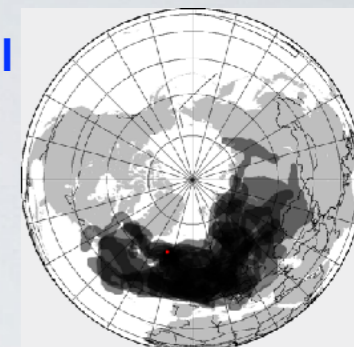
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- Milestone: first-ever multi-leg implementation of MSSM v1.25 [2003]
- Color flow formalism [ $\approx$ 2005]
- Used for many TESLA studies and most ILC CDR and TDR, CLIC CDR and detector Lol studies (versions v1.24, v1.50, v1.95) [ $\approx$  2002–2013]
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Eyjafjallajökull





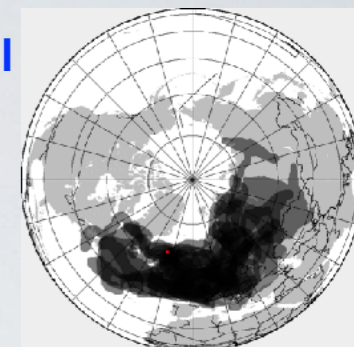
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**Major refactoring phase I: LHC physics  $\rightarrow$  v2.0.0** [ $\approx$  2007–2010; **38 months**]

Validation inside ATLAS and CMS [ $\approx$ 2011–2014]

**Refactoring phase II: NLO automation / maintainability  $\rightarrow$  v2.2.0**  
[ $\approx$  2012–2014; **18 months**]

Strong interest of CEPC group for CEPC simulations [ $\approx$  2013 — now] [Talk by Manqi Ruan](#)

04/2015, ALCW'15 Tokyo: LC generator group endorsed v2.2 for new mass productions

FCC-ee interest in simulations: [ca. spring 2016]

**Refactoring phase III: first NLO implementation overhaul** [2016; **3 months**]

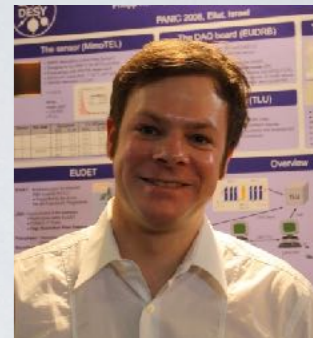
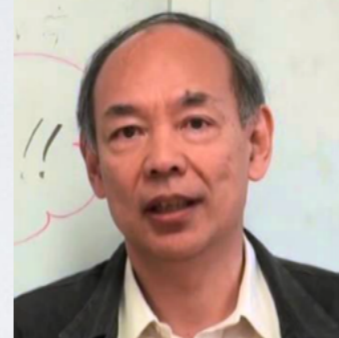
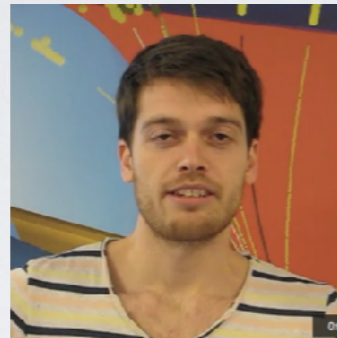




# WHIZARD: Past and recent timeline (II)

Final validation for  $e^+e^-$  physics between v1.95 & v2 [until end of 2017, partially mid 2018]

Special thanks to: [beam spectra, photon background, event formats, shower/hadronization, tau decays]



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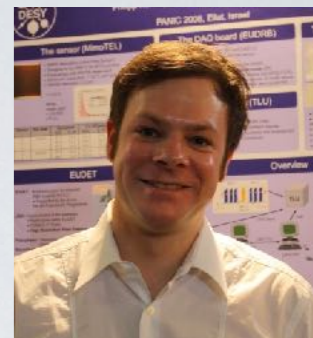
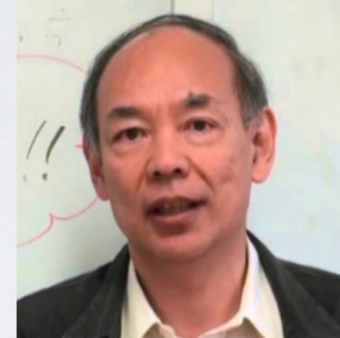
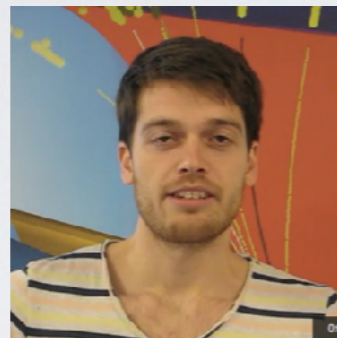
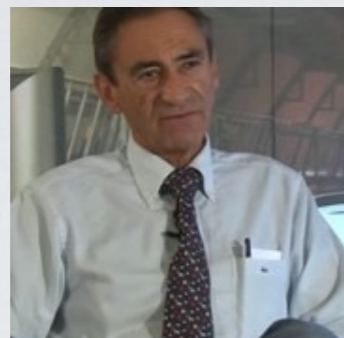




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- 01/2018, CERN, LC generator meeting: **only trivial minor, ready for mass production**
- Refactoring phase IV:** core data structure overhaul: NLO [fall 2018; **ca. 2-3months**]  
[dust-layer buried students, total-code-no-man-wasteland alarm]
- Preparation phase for WHIZARD 3.0.0 started: ... PARALLEL TO ...**  
Work on: [NLO QCD final validation; structure functions; NLO EW; shower and matching/merging]
- (Technical) refactoring phase V:** **code modernization (submodules etc: gfortran 6.1+ )**  
[mid / end of 2019; when NAG debugging compiler support ready]









- Universal event generator for lepton and hadron colliders (SM and BSM physics)
- Tree ME generator 0' Mega **optimized ME generator** 
- Generator/simulation tool for lepton collider beam spectra: CIRCE1/2
- Interfaces to external packages: FastJet, GoSam, GuineaPig(++), HepMC, HOPPET, LCIO, LHAPDF(5/6), LoopTools, OpenLoops, PYTHIA6 [internal], PYTHIA8, RecoLa, StdHep [internal], Tauola [internal]
- Event formats: LHE, StdHEP, HepMC, LCIO + several ASCII


 Scattering processes and [auto-] decays

```
integral (br_hZA_redef) = 200 keV
```

 Factorized processes with spin correlations [variants: no correlations, definite helicity, **predefined branching ratios**]

 Scripting language for the steering: SINDARIN

είσαλο ιαόραζ αρϷο·  
όϷαρπιο λόραζ Ϸοιο

 **Beam structure:** polarization, asymmetric beams, crossing angle, structured beams, decays

```
beams = e1, E1
beams_pol_density = @(-1), @(+1)
beams_pol_fraction = 80%, 30%
```

```
beams = p, pbar => lhpdf
$lhpdf = "NNPDF3"
```

```
beams = e1, E1 => circe2 => isr => ewa
```





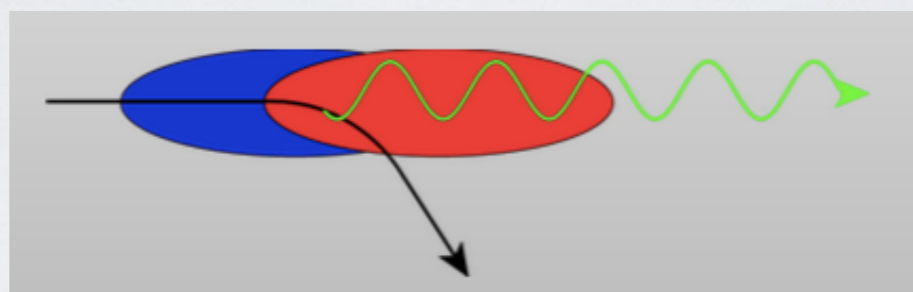
# $e^+e^-$ Beamspectra



# $e^+e^-$ Beamspectra

- High-energy  $e^+e^-$  colliders need to achieve extreme luminosities
- **Price for limited AC power: high bunch charges and tiny cross sections**
- Dense beams generate strong EM fields: deflect particles in other bunch (**beamstrahlung**)

$$L \approx \frac{N}{4\pi\sigma_x\sigma_y} \frac{\eta P_{AC}}{E_{CM}}$$

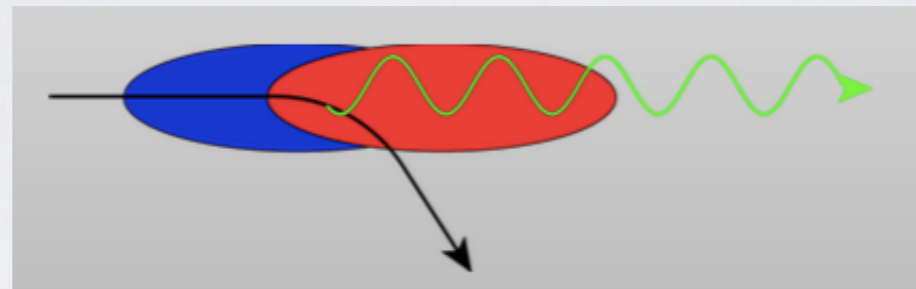




# e<sup>+</sup>e<sup>-</sup> Beamspectra

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### Index of /circe\_files/CLIC

Name	Last modified	Size	Description
Parent Directory	-	-	-
0.5TeVeeMapPB0.67E0.0Mi0.30.circe	06-Jul-2016 17:03	6.0M	
0.5TeVegMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	6.0M	
0.5TeVgeMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	6.0M	
0.5TeVggMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	3.9M	
0.35TeVeeMapPB0.67E0.0Mi0.30.circe	06-Jul-2016 17:02	6.0M	
0.35TeVegMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:02	6.0M	
0.35TeVgeMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	6.0M	
0.35TeVggMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	3.9M	
0.38TeVeeMapPB0.67E0.0Mi0.30.circe	23-Jun-2017 16:02	14M	
0.38TeVegMapPB0.67E0.0Mi0.0.circe	23-Jun-2017 16:02	9.0M	
0.38TeVgeMapPB0.67E0.0Mi0.0.circe	23-Jun-2017 16:02	9.0M	
0.38TeVggMapPB0.67E0.0Mi0.0.circe	23-Jun-2017 16:02	3.9M	
1.4TeVeeMapPB0.67E0.0Mi0.15.circe	06-Jul-2016 17:03	35M	
1.4TeVegMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:03	15M	
1.4TeVgeMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:04	7.8M	
1.4TeVggMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:04	15M	
3TeVeeMapN100.circe	06-Jul-2016 17:04	1.0M	
3TeVeeMapPB0.67E0.0Mi0.15.circe	06-Jul-2016 17:04	24M	
3TeVegMapN100.circe	06-Jul-2016 17:04	521K	
3TeVegMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:04	12M	
3TeVgeMapN100.circe	06-Jul-2016 17:04	1.0M	
3TeVgeMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:04	24M	
3TeVggMapN100.circe	06-Jul-2016 17:05	273K	
3TeVggMapPB0.67E0.0Mi0.0.circe	06-Jul-2016 17:05	6.1M	

### Index of /circe\_files/TESLA

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Parent Directory	-	-	-
teslagg_500.circe	29-Jul-2016 13:20	1.1M	
teslagg_500_polavg.circe	29-Jul-2016 13:20	270K	

### Index of /circe\_files/ILC

Name	Last modified	Size	Description
Parent Directory	-	-	-
ilc200ee_nobeamsread.circe	29-Jul-2016 13:20	1.0M	
ilc230ee_nobeamsread.circe	29-Jul-2016 13:20	1.0M	
ilc250ee_nobeamsread.circe	29-Jul-2016 13:20	1.0M	
ilc350ee_nobeamsread.circe	29-Jul-2016 13:20	1.0M	
ilc500ee_nobeamsread.circe	29-Jul-2016 13:20	1.0M	

### Index of /circe\_files/CEPC

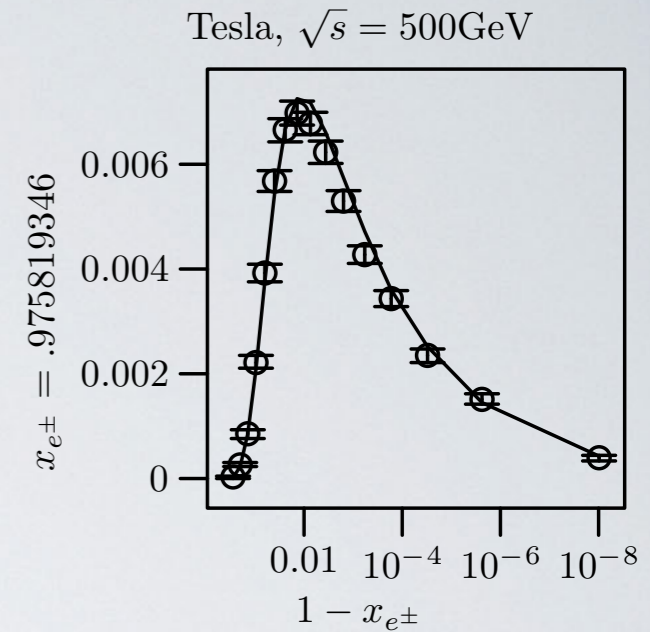
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cepc240.circe	29-Jul-2016 13:20	252K	
cepc250.circe	29-Jul-2016 13:20	252K	





# Lepton Collider Beam Simulation

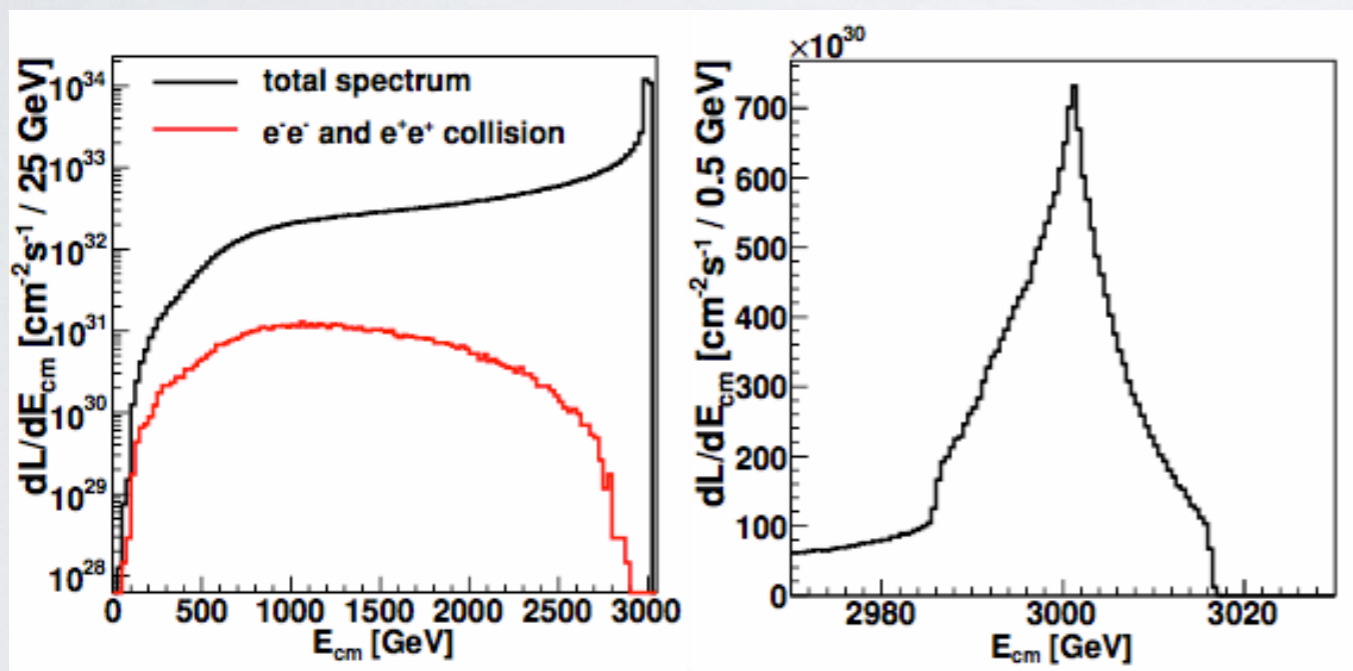
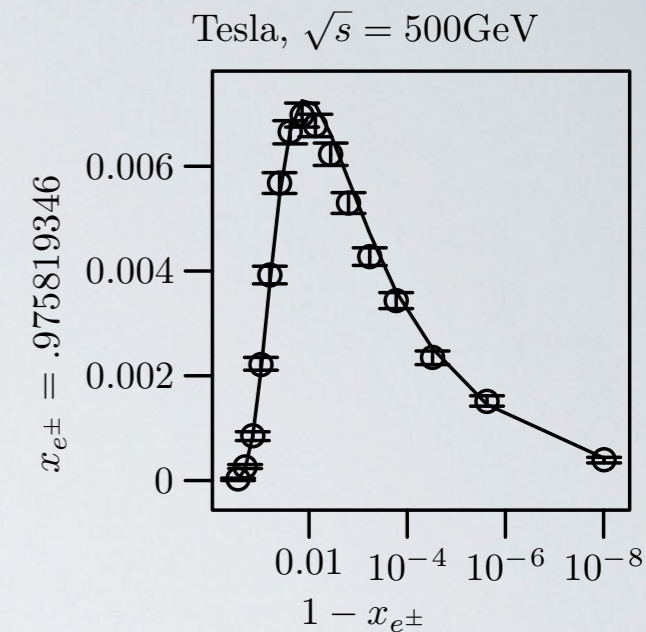
- Adapt GuineaPig beam spectra for WHIZARD v2
- For WHIZARD v1.95 simulations done by Lumilinker [T. Barklow]
- TESLA/SLC spectra were rather simple
- Fits with 6 or 7 parameters possible [CIRCE1]
- **Beams not factorizable:**  $D_{B_1 B_2}(x_1, x_2) \neq D_{B_1}(x_1) \cdot D_{B_2}(x_2)$
- **No simple power law:**  $D_{B_1 B_2}(x_1, x_2) \neq x_1^{\alpha_1} (1 - x_1)^{\beta_1} x_2^{\alpha_2} (1 - x_2)^{\beta_2}$





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Dalena/Esbjerg/Schulte [LCWS 2011]

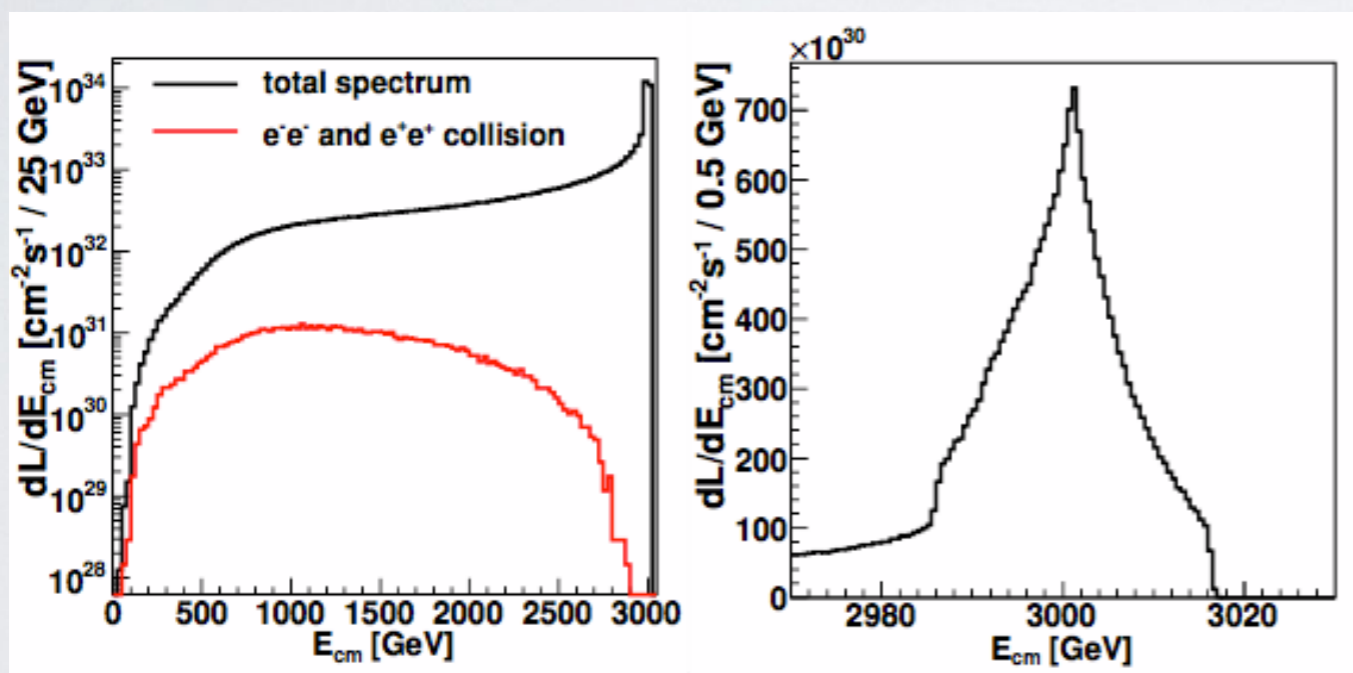
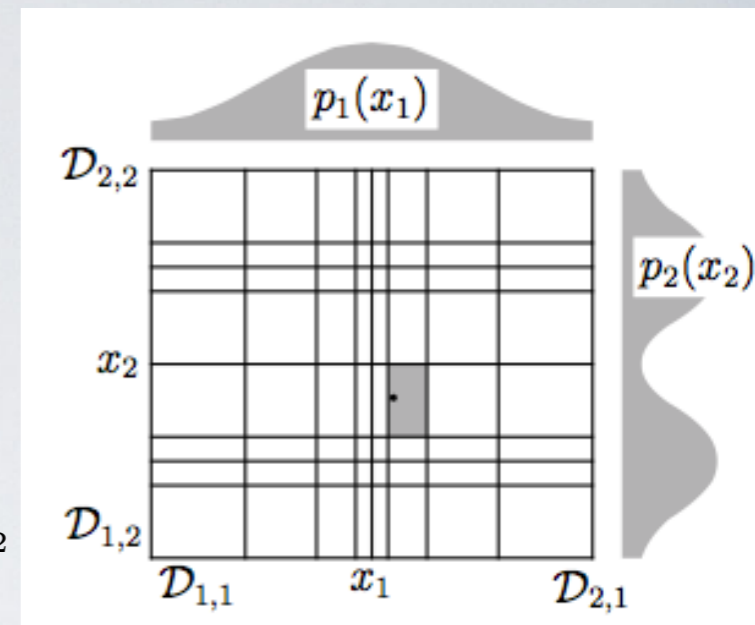
Tails @ CLIC much more complicated (wakefields)





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## CIRCE2 algorithm (WHIZARD 2.2.5, 02/15)

- Adapt **2D factorized variable width histogram** to steep part of distribution
- Smooth correlated fluctuations with moderate **Gaussian filter** [suppresses artifacts from limited GuineaPig statistics]
- Smooth **continuum/boundary bins separately** [avoid artificial beam energy spread]





## 1. Run Guinea-Pig++ with

```
do_lumi=7;num_lumi=100000000;num_lumi_eg=100000000;num_lumi_gg=100000000;
```

to produce `lumi.[eg][eg].out` with  $(E_1, E_2)$  pairs.

[Large event numbers, as Guinea-Pig++ will produce only a small fraction!]

## 2. Run `circe2_tool.opt` with steering file

```
{ file="ilc500/beams.circe" # to be loaded by WHIZARD
  { design="ILC" roots=500 bins=100 scale=250 # E in [0,1]
    { pid/1=electron pid/2=positron pol=0 # unpolarized e-/e+
      events="ilc500/lumi.ee.out" columns=2 # <= Guinea-Pig
      lumi = 1564.763360 # <= Guinea-Pig
      iterations = 10 # adapting bins
      smooth = 5 [0,1) [0,1) # Gaussian filter 5 bins
      smooth = 5 [1] [0,1) smooth = 5 [0,1) [1] } } }
```

to produce correlated beam description

## 3. Run WHIZARD with SINDARIN input:

```
beams = e1, E1 => circe2
$circe2_file = "ilc500.circe"
$circe2_design = "ILC"
?circe_polarized = false
```

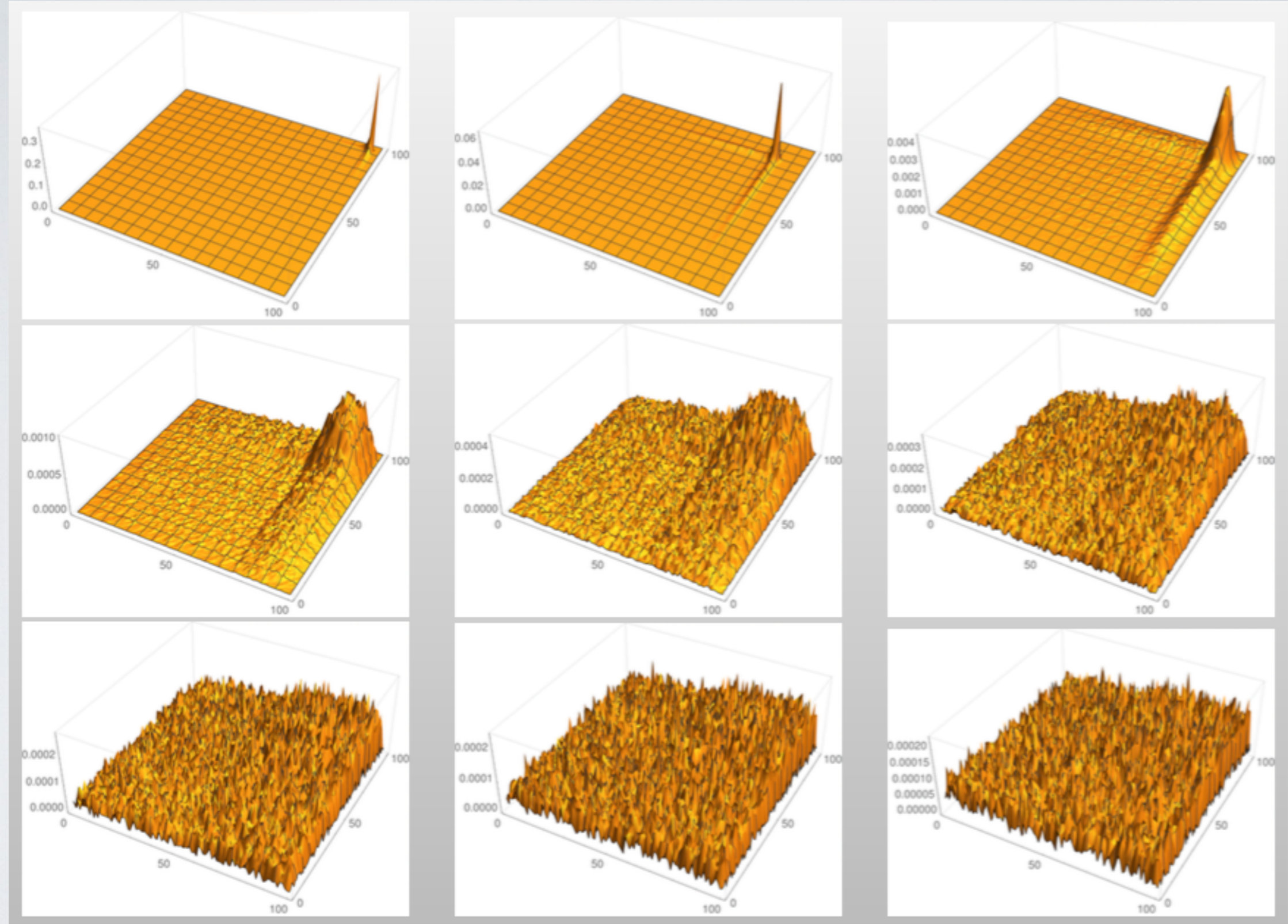
### 3 simulation options

1. Unpolarized simulation with unpol. spectra
2. Pol. simulation: unpol. spectra + pol. beams
3. Polarized spectrum with helicity luminosities





# Iterations of Beam Spectrum

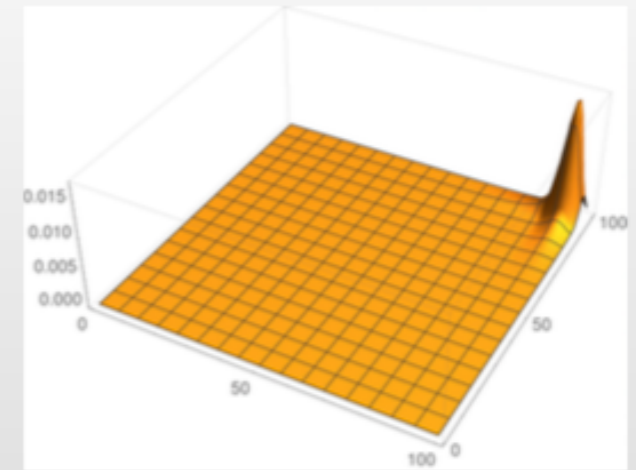
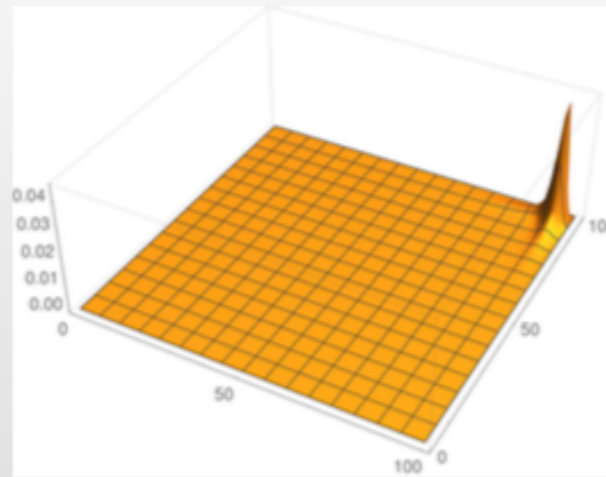
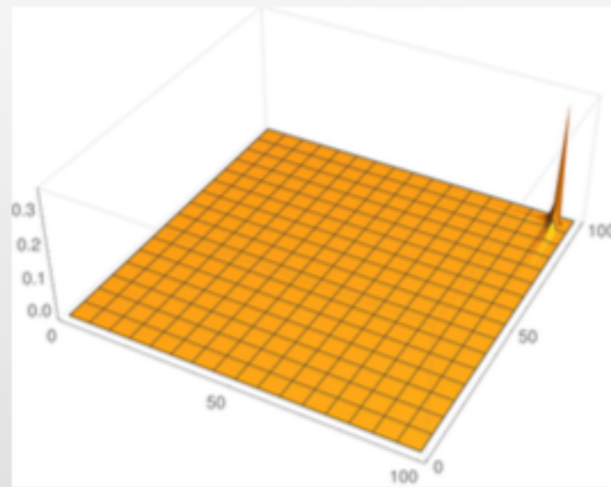


(171,306 GuineaPig events in 10,000 bins)

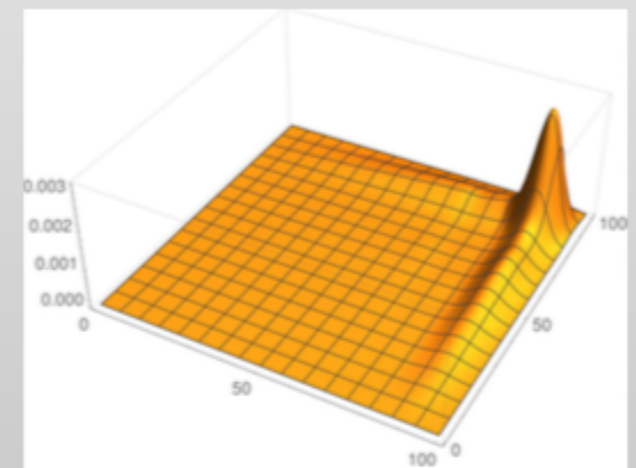
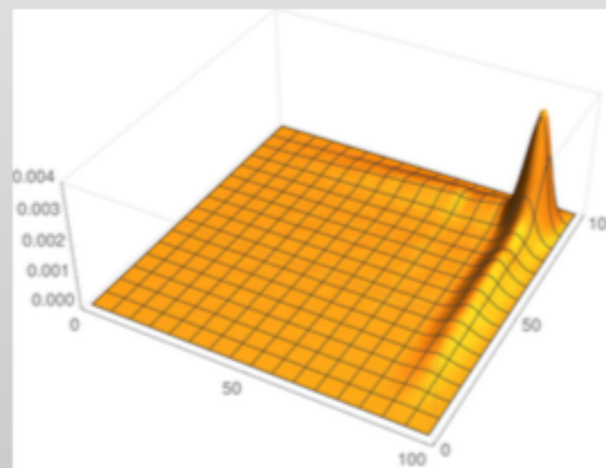
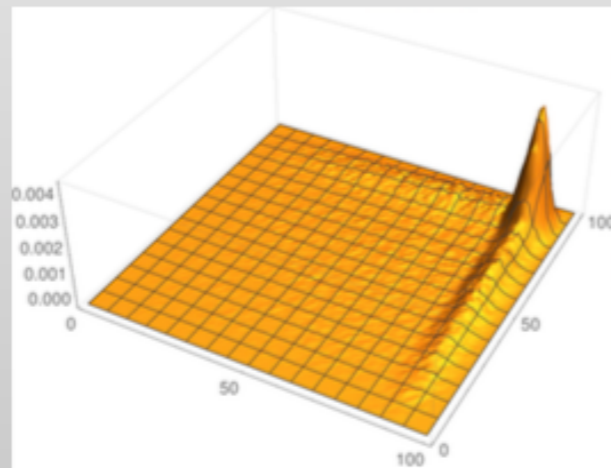


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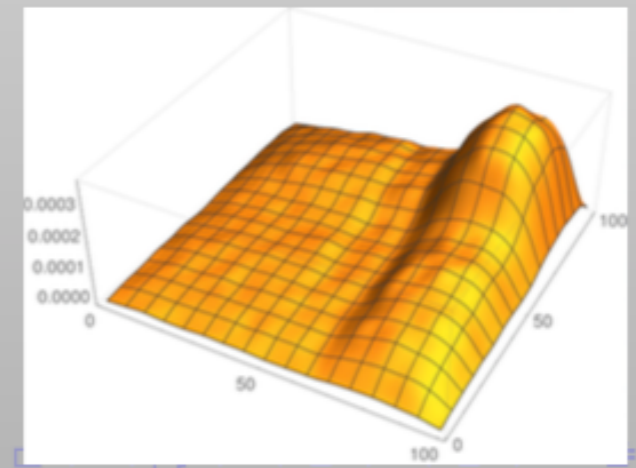
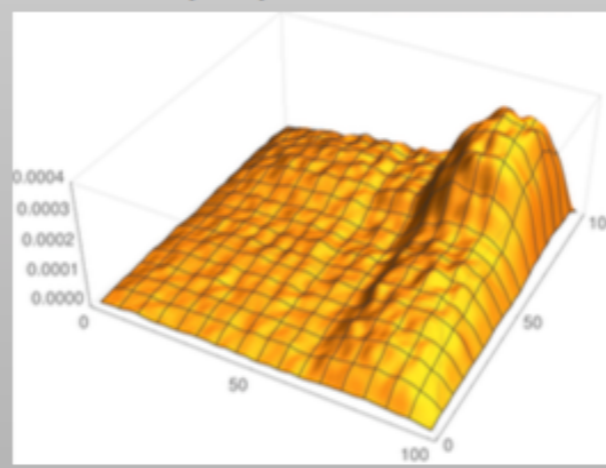
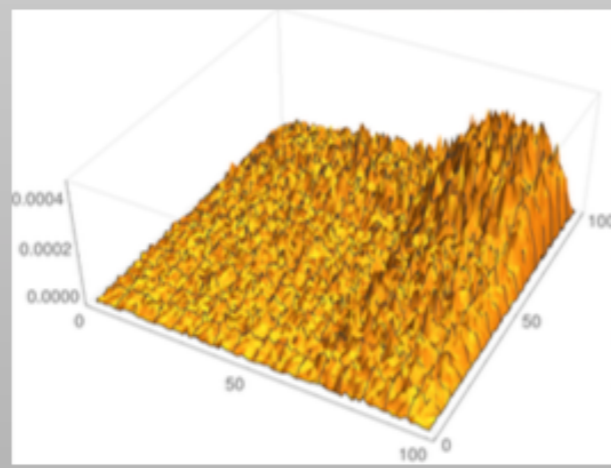
► **iterations** = 0 and **smooth** = 0, 3, 5:



► **iterations** = 2 and **smooth** = 0, 3, 5:



► **iterations** = 4 and **smooth** = 0, 3, 5:





# Inclusive Lepton Collider ISR included

Soft exponentiation to all orders

$$\epsilon = \frac{\alpha}{\pi} q_e^2 \ln \left( \frac{s}{m^2} \right) \quad \text{Gribov/Lipatov, 1971}$$

$$f_0(x) = \epsilon \cdot (1 - x)^{-1+\epsilon}$$

Hard-collinear photons up to 3rd QED order



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Hard-collinear photons up to 3rd QED order

Kuraev/Fadin, 1983; Skrzypek/Jadach, 1991

$$g_3(\epsilon) = 1 + \frac{3}{4}\epsilon + \frac{27 - 8\pi^2}{96}\epsilon^2 + \frac{27 - 24\pi^2 + 128\zeta(3)}{384}\epsilon^3$$

$$\begin{aligned} f_3(x) = & g_3(\epsilon) f_0(x) - \frac{\epsilon}{2}(1+x) \\ & - \frac{\epsilon^2}{8} \left( \frac{1+3x^2}{1-x} \ln x + 4(1+x) \ln(1-x) + 5+x \right) \\ & - \frac{\epsilon^3}{48} \left( (1+x) [6 \text{Li}_2(x) + 12 \ln^2(1-x) - 3\pi^2] + 6(x+5) \ln(1-x) \right. \\ & \quad \left. + \frac{1}{1-x} \left[ \frac{3}{2}(1+8x+3x^2) \ln x + 12(1+x^2) \ln x \ln(1-x) \right. \right. \\ & \quad \left. \left. - \frac{1}{2}(1+7x^2) \ln^2 x + \frac{1}{4}(39-24x-15x^2) \right] \right) \end{aligned}$$

$$\zeta(3) = 1.20205690315959428539973816151 \dots$$



# Inclusive Lepton Collider ISR included

Soft exponentiation to all orders

$$\epsilon = \frac{\alpha}{\pi} q_e^2 \ln\left(\frac{s}{m^2}\right) \quad \text{Gribov/Lipatov, 1971}$$

$$f_0(x) = \epsilon \cdot (1-x)^{-1+\epsilon}$$

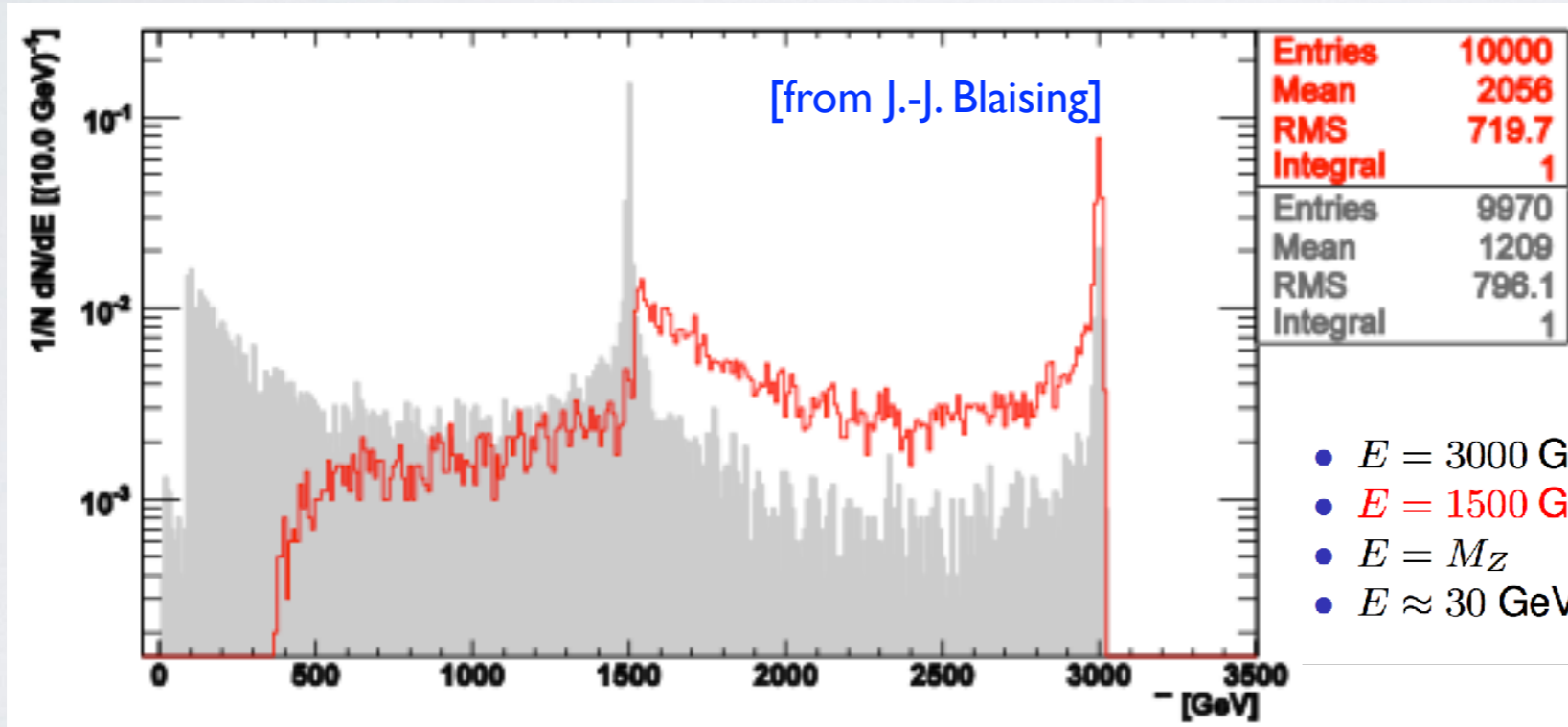
Hard-collinear photons up to 3rd QED order

Kuraev/Fadin, 1983; Skrzypek/Jadach, 1991

$$g_3(\epsilon) = 1 + \frac{3}{4}\epsilon + \frac{27 - 8\pi^2}{96}\epsilon^2 + \frac{27 - 24\pi^2 + 128\zeta(3)}{384}\epsilon^3$$

$$f_3(x) = g_3(\epsilon) f_0(x) - \frac{\epsilon}{2}(1+x) - \frac{\epsilon^2}{8} \left( \frac{1+3x^2}{1-x} \ln x + 4(1+x) \ln(1-x) + 5+x \right) - \frac{\epsilon^3}{48} \left( (1+x) [6\text{Li}_2(x) + 12\ln^2(1-x) - 3\pi^2] + 6(x+5) \ln(1-x) + \frac{1}{1-x} \left[ \frac{3}{2}(1+8x+3x^2) \ln x + 12(1+x^2) \ln x \ln(1-x) - \frac{1}{2}(1+7x^2) \ln^2 x + \frac{1}{4}(39-24x-15x^2) \right] \right)$$

$$\zeta(3) = 1.20205690315959428539973816151\dots$$



- $E = 3000 \text{ GeV}$  (luminosity spectrum peak)
- $E = 1500 \text{ GeV}$  ( $Z$  peak and lumi spectrum)
- $E = M_Z$  ( $Z$  resonance)
- $E \approx 30 \text{ GeV}$  (due to  $e^+e^- \rightarrow \gamma^* \rightarrow b\bar{b}$ )



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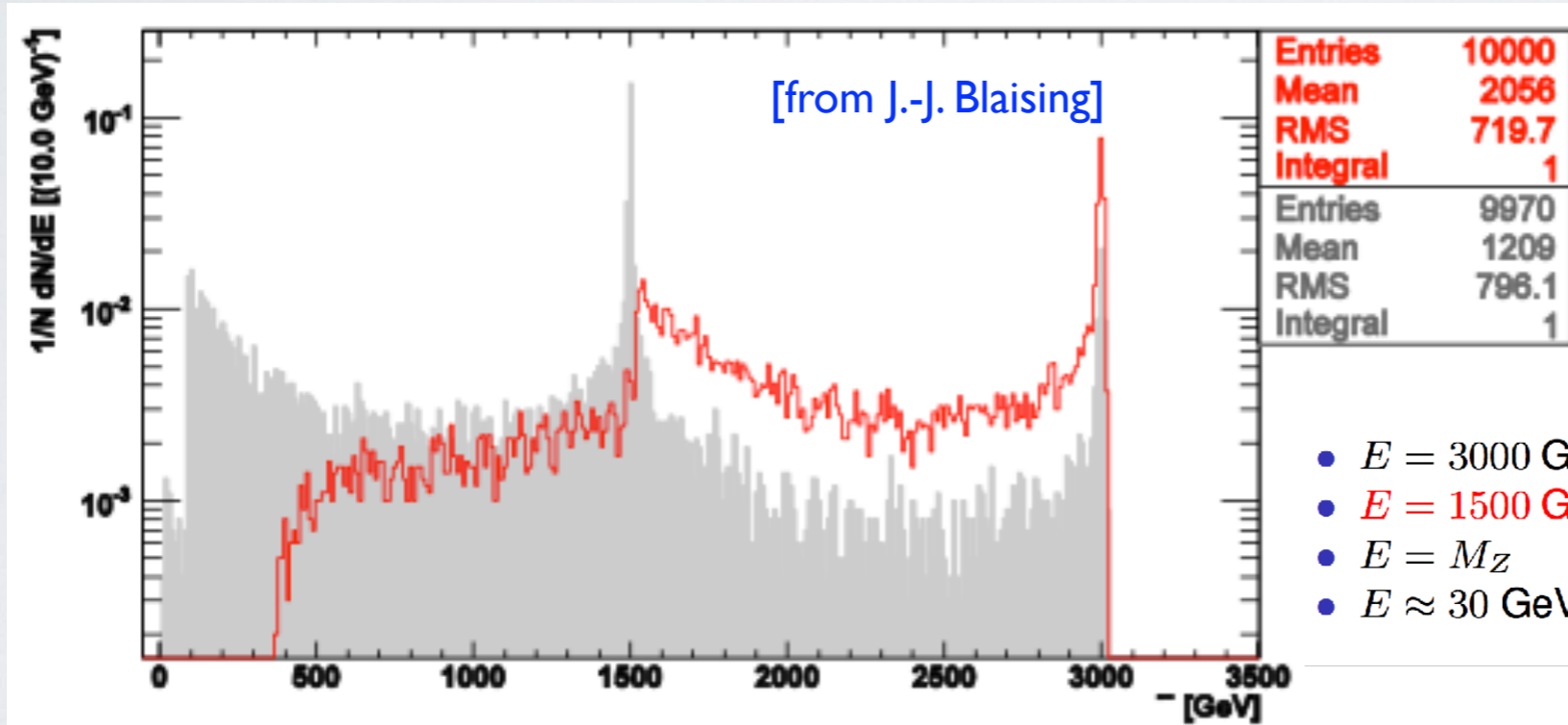
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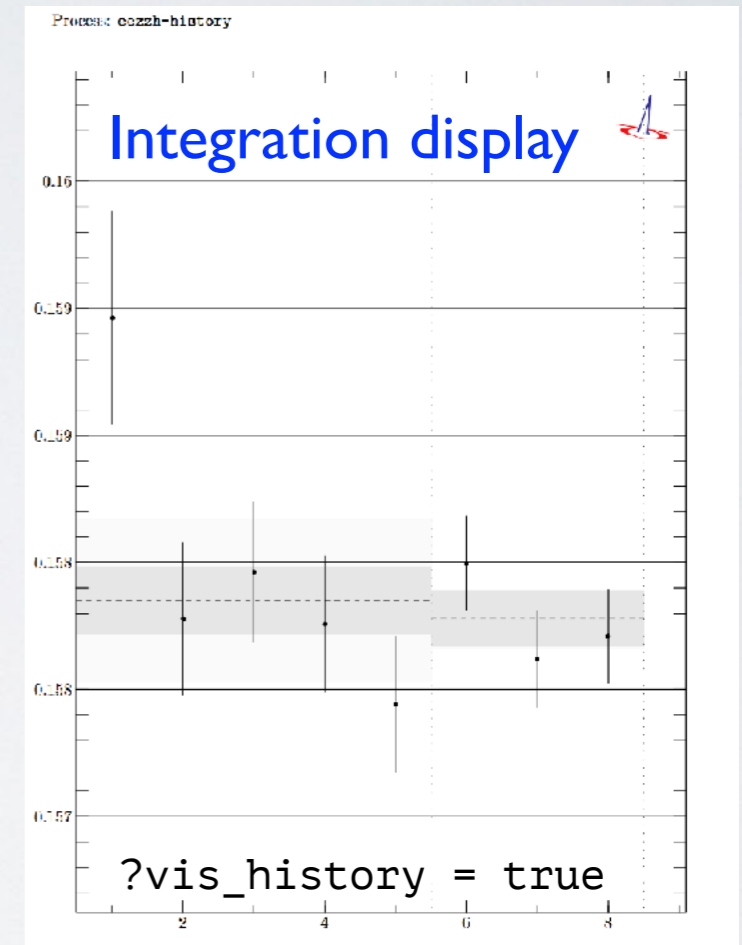
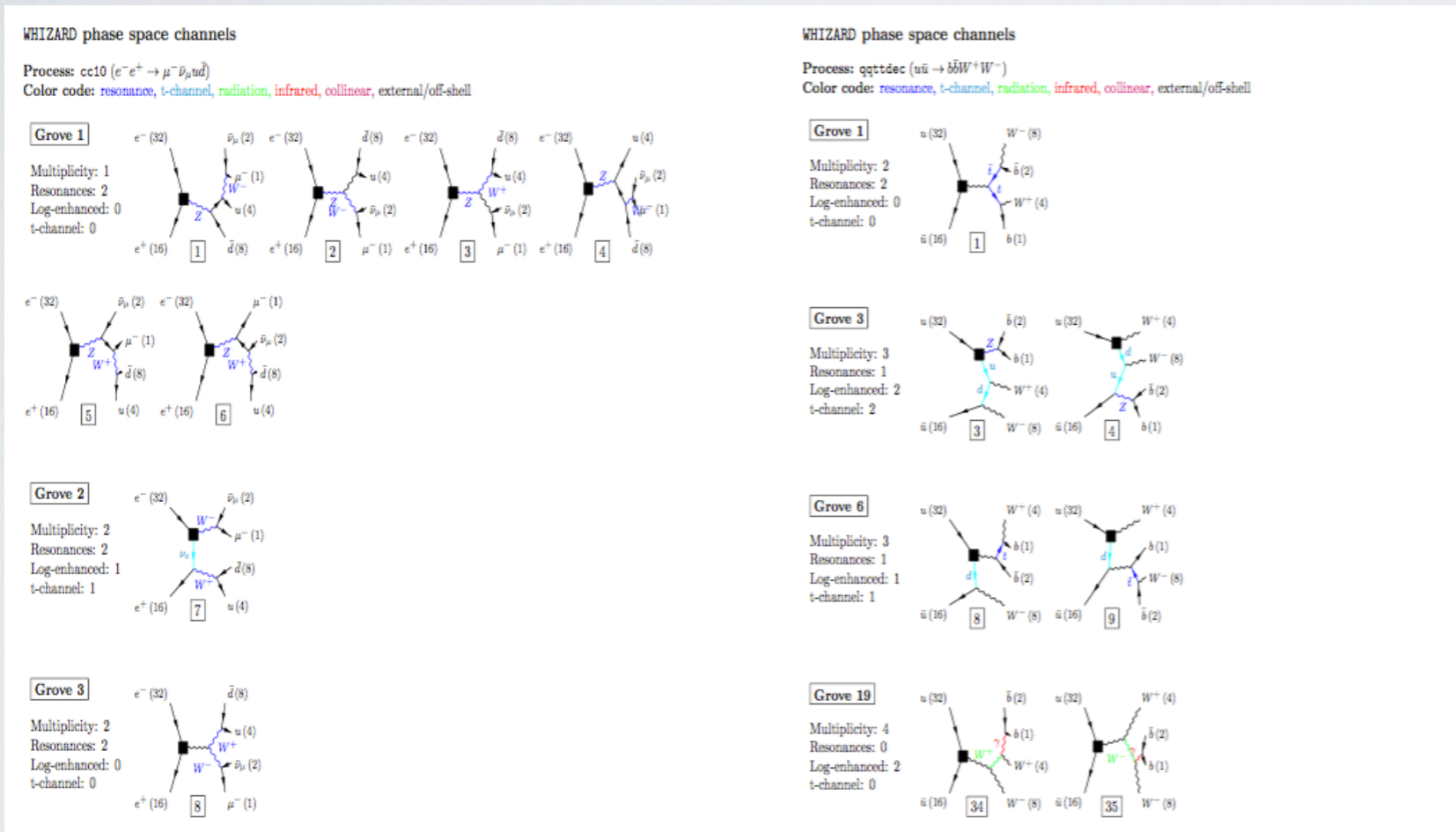
- One explicit ISR photon / beam: ISR/EPA handler generates physical  $p_T$  distributions
- Explicit matching needed: heuristic procedures LO — *tbd* for NLO !



# Phase Space Integration

- VAMP : adaptive multi-channel Monte Carlo integrator
- VAMP2 : fully MPI-parallelized version, using RNG stream generator

**WHIZARD algorithm:** heuristics to classify phase-space topology, adaptive multi-channel mapping  $\implies$  resonant, t-channel, radiation, infrared, collinear, off-shell



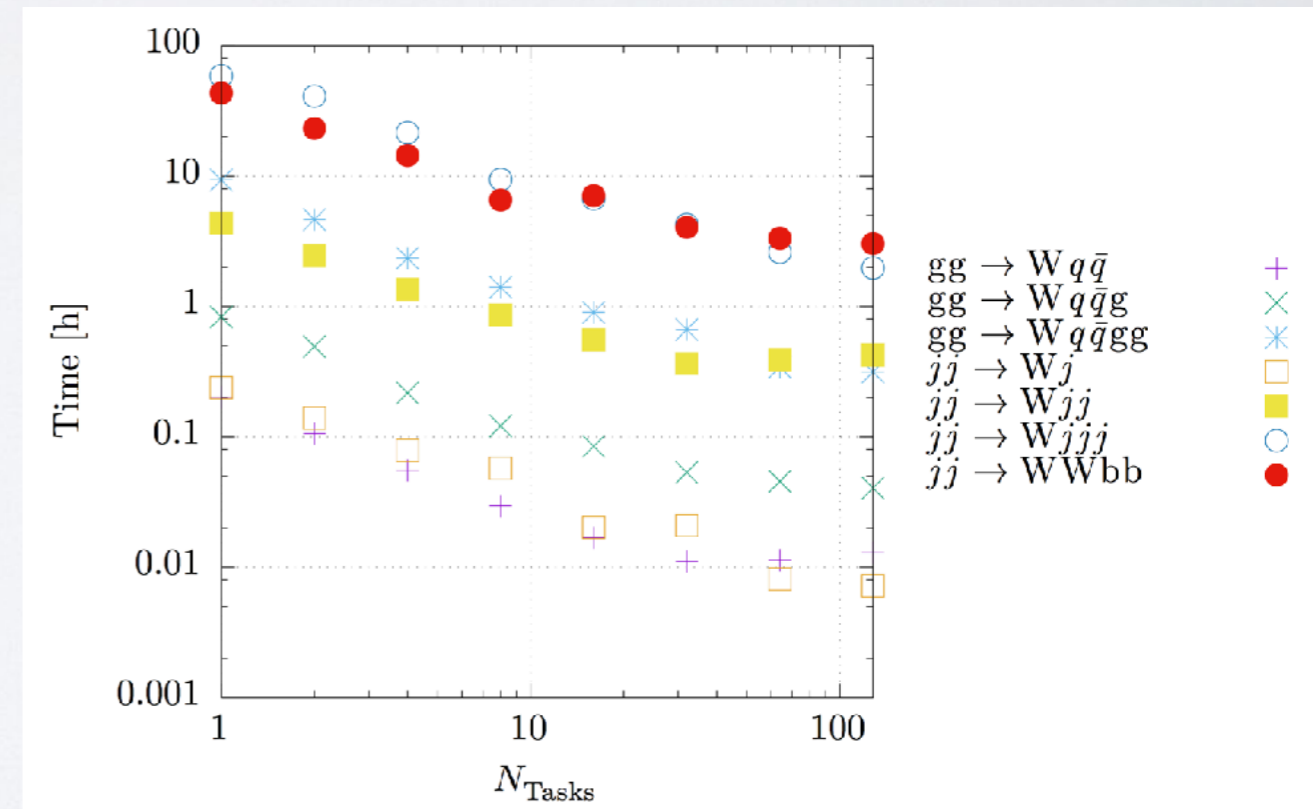
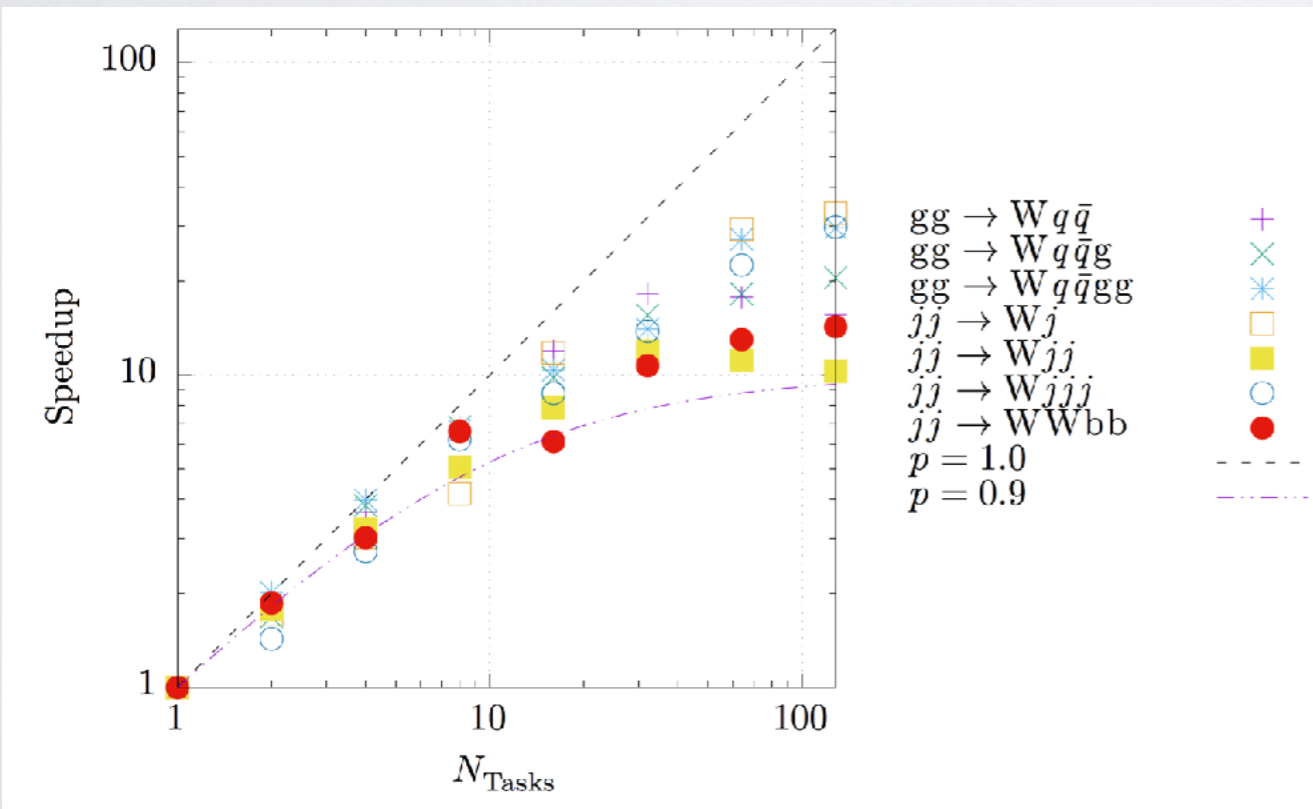
Complicated processes: **factorization into production and decay** with the unstable option

Resonance-aware factorization for NLO processes and parton showers (e.g.  $e^+e^- \rightarrow jjjj$ )





- Event generation trivially parallelizable
- Major bottleneck: adaptive phase space integration (generation of grids)**
- Parallelization of integration: OMP multi-threading for different helicities since long
- NEW (after v2.5.0/2.6.4): MPI parallelization (using OpenMPI or MPICH)**
- Distributes workers over multiple cores, grid adaption needs non-trivial communication
- Amdahl's law:  $s = \frac{1}{1-p+\frac{p}{N}}$
- Speedups of 10 to 30, saturation at  $O(100)$  tasks
- Integration times go down from weeks to hours! [can do also parallel event generation]**



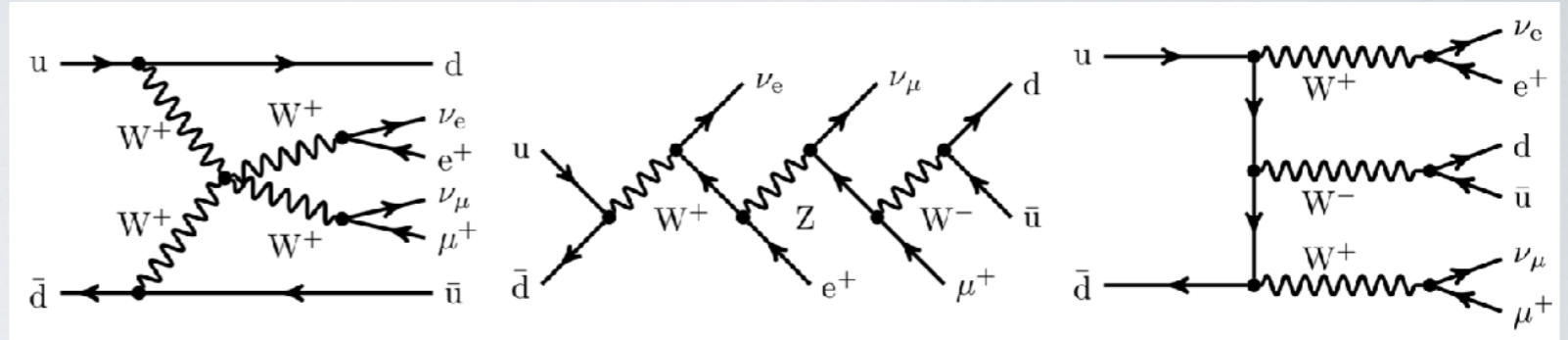




# LHC VBS: Comparison LO & LO+PS

Ballestrero et al., 1803.07943

Order	$\mathcal{O}(\alpha^6)$	$\mathcal{O}(\alpha_s^2\alpha^4)$	$\mathcal{O}(\alpha_s\alpha^5)$
$\sigma[\text{fb}]$	$2.292 \pm 0.002$	$1.477 \pm 0.001$	$0.223 \pm 0.003$

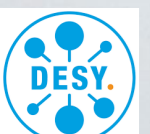
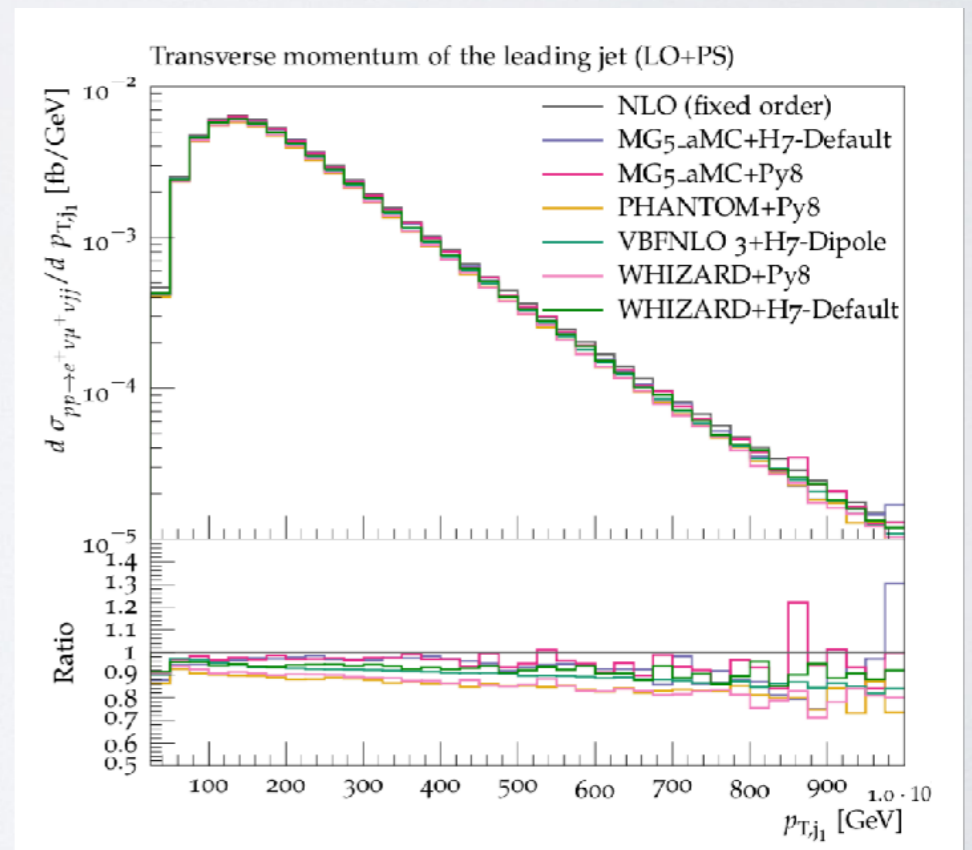
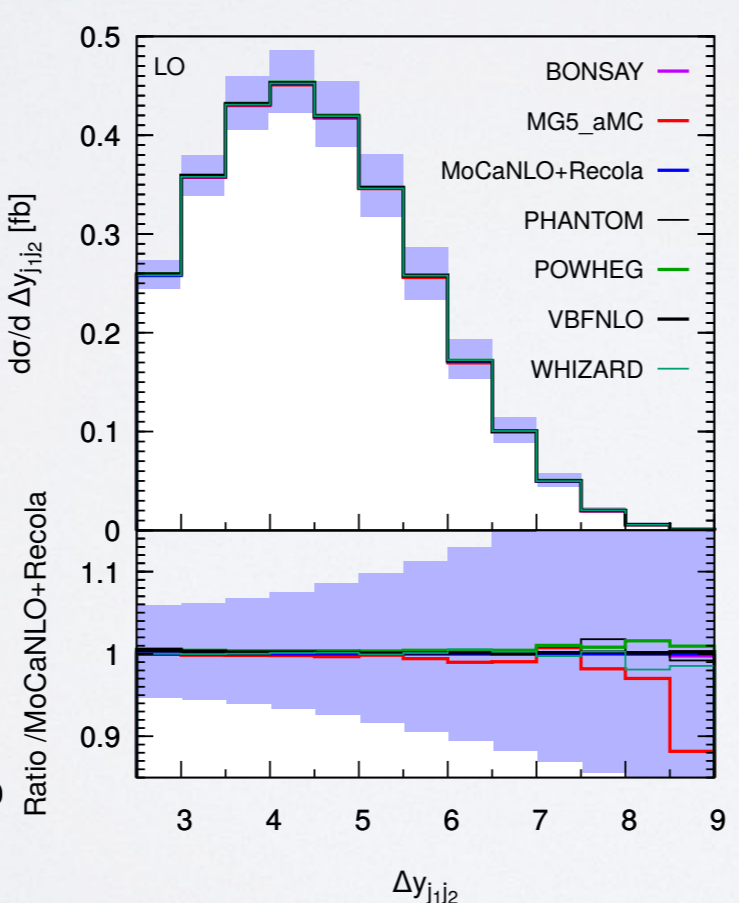
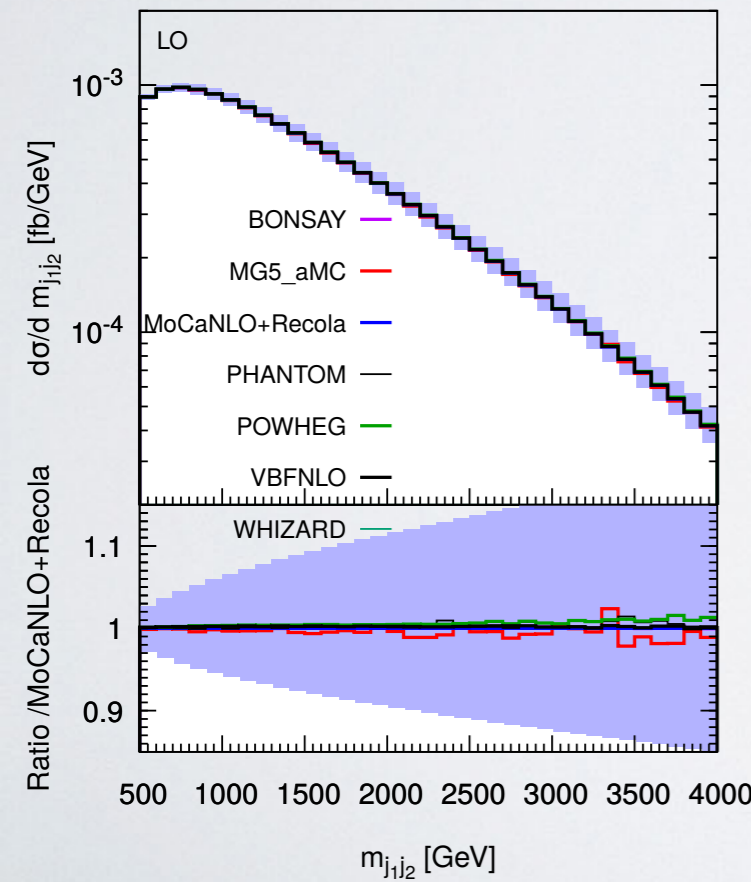


Code	$\sigma[\text{fb}]$
BONSAY	$1.43636 \pm 0.00002$
MG5_AMC	$1.4304 \pm 0.0007$
MoCaNLO+RECOLA	$1.43476 \pm 0.00009$
PHANTOM	$1.4374 \pm 0.0006$
POWHEG-BOX	$1.44092 \pm 0.00009$
VBFNLO	$1.43796 \pm 0.00005$
LO WHIZARD	$1.4381 \pm 0.0002$

$p_{T,\ell} > 20 \text{ GeV}$     $|y_\ell| < 2.5$     $\Delta R_{\ell\ell} > 0.3$   
 $p_{T,\text{miss}} > 40 \text{ GeV}$   
 Anti- $k_T$  jets with  $R = 0.4$ :  
 $p_{T,j} > 30 \text{ GeV}$     $|y_j| < 4.5$     $\Delta R_{\ell j} > 0.3$   
 $m_{jj} > 500 \text{ GeV}$     $|\Delta y_{jj}| > 2.5$

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MG5_AMC+PYTHIA8, $\Gamma_{\text{resc}}$	$1.275 \pm 0.003$
MG5_AMC+HERWIG7, $\Gamma_{\text{resc}}$	$1.266 \pm 0.003$
PHANTOM+PYTHIA8	$1.235 \pm 0.001$
PHANTOM+HERWIG7	$1.258 \pm 0.001$
VBFNLO+HERWIG7-DIPOLE	$1.3001 \pm 0.0002$
WHIZARD+PYTHIA8	$1.229 \pm 0.001$

LO+PS

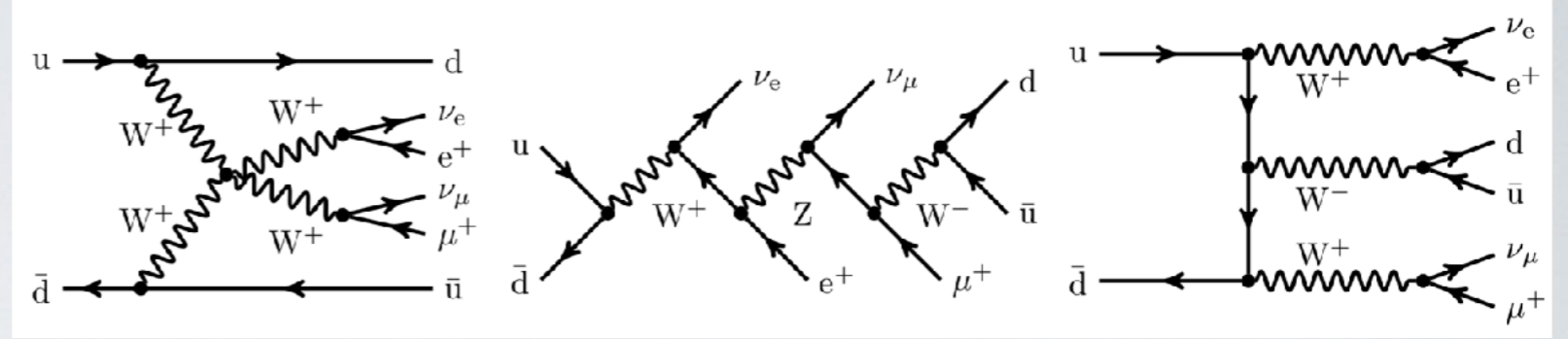




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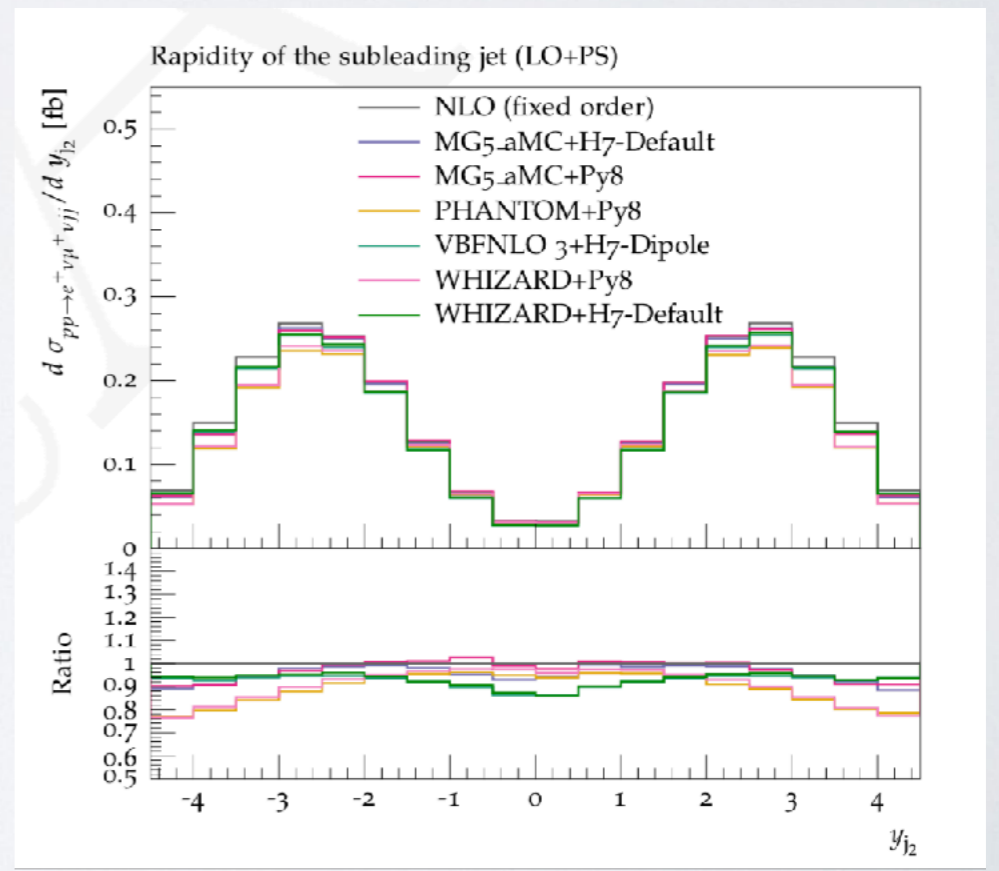
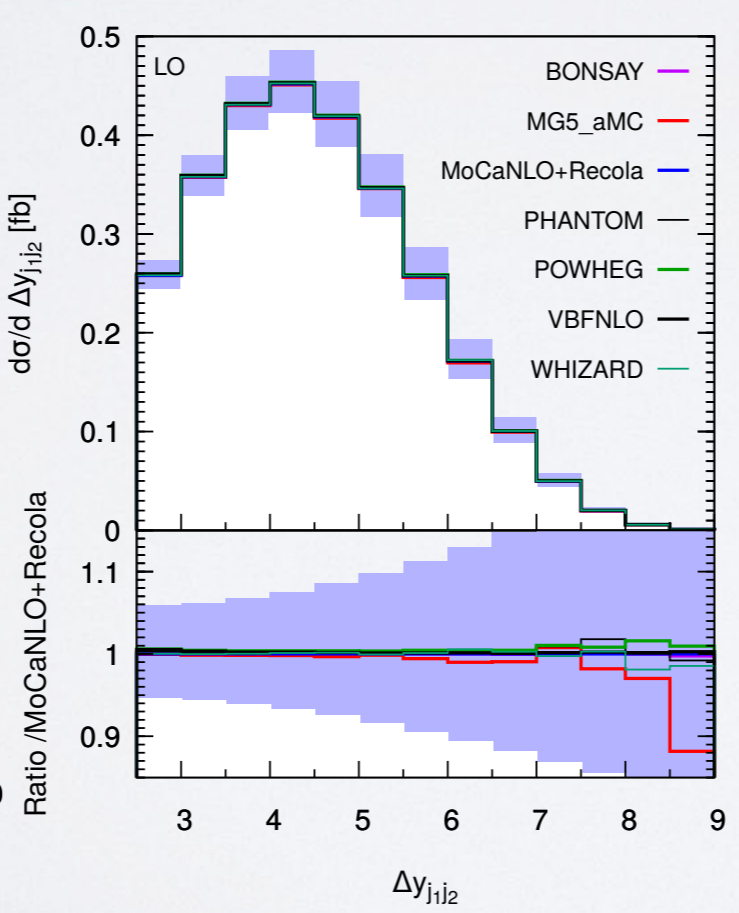
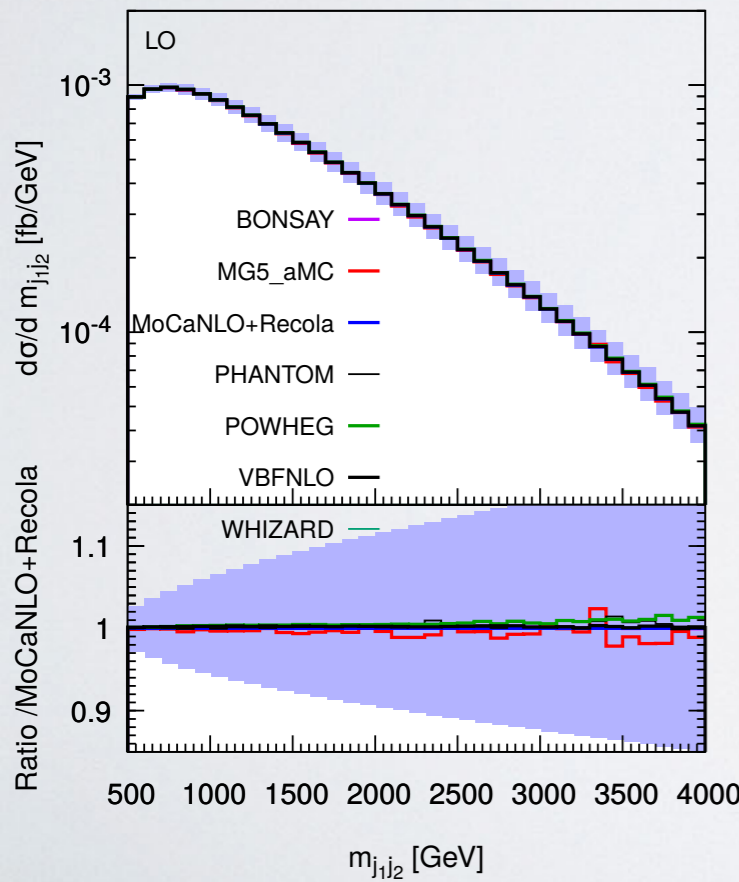


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LO+PS

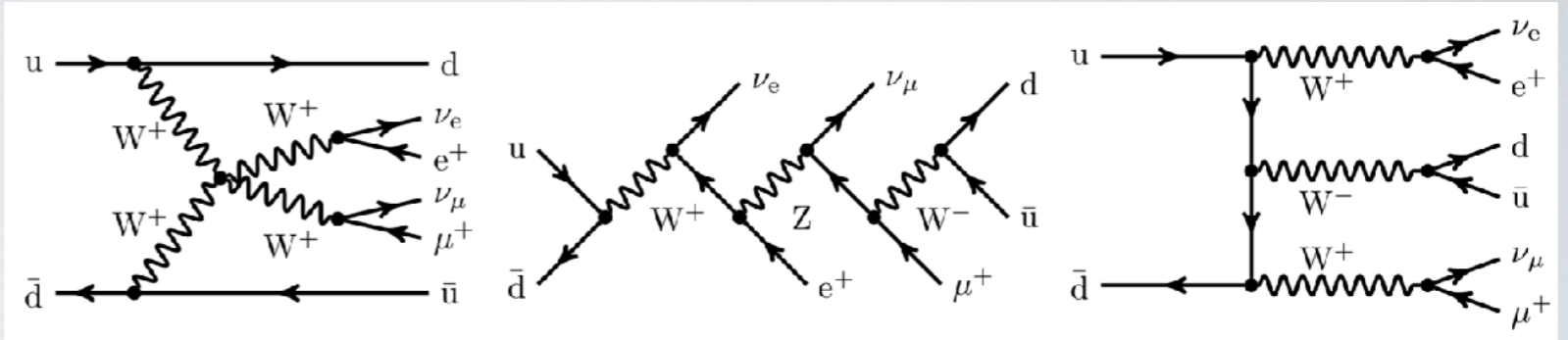




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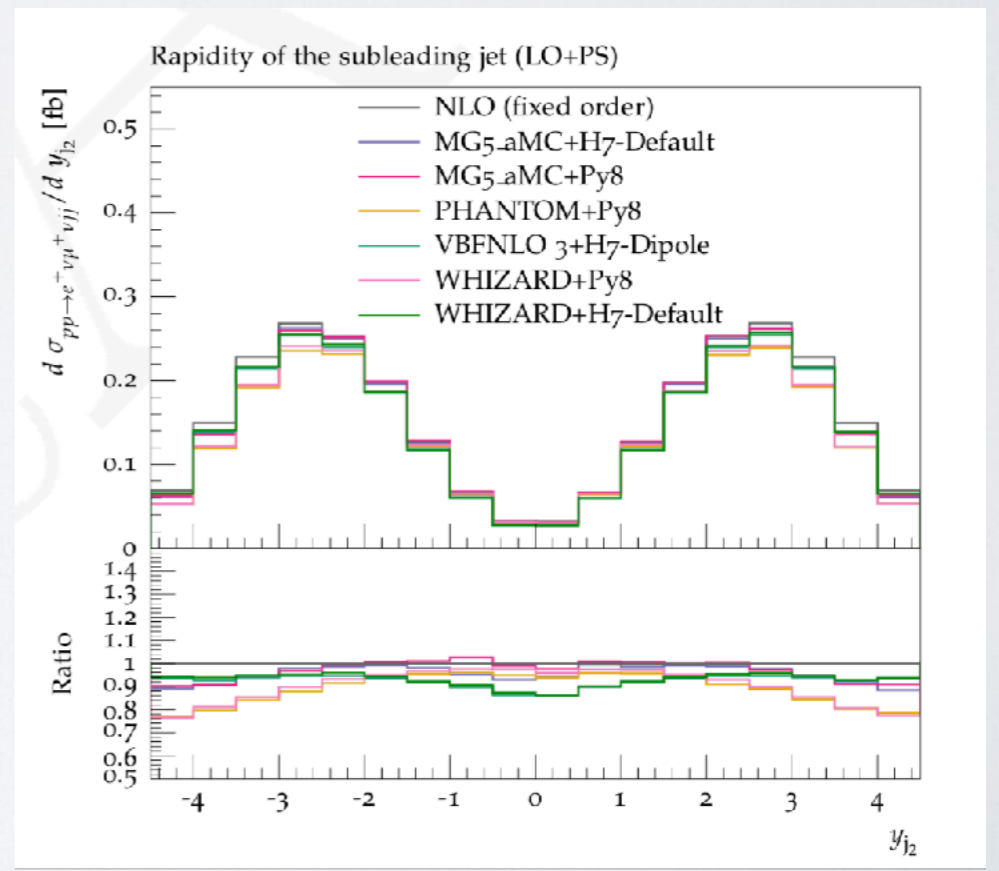
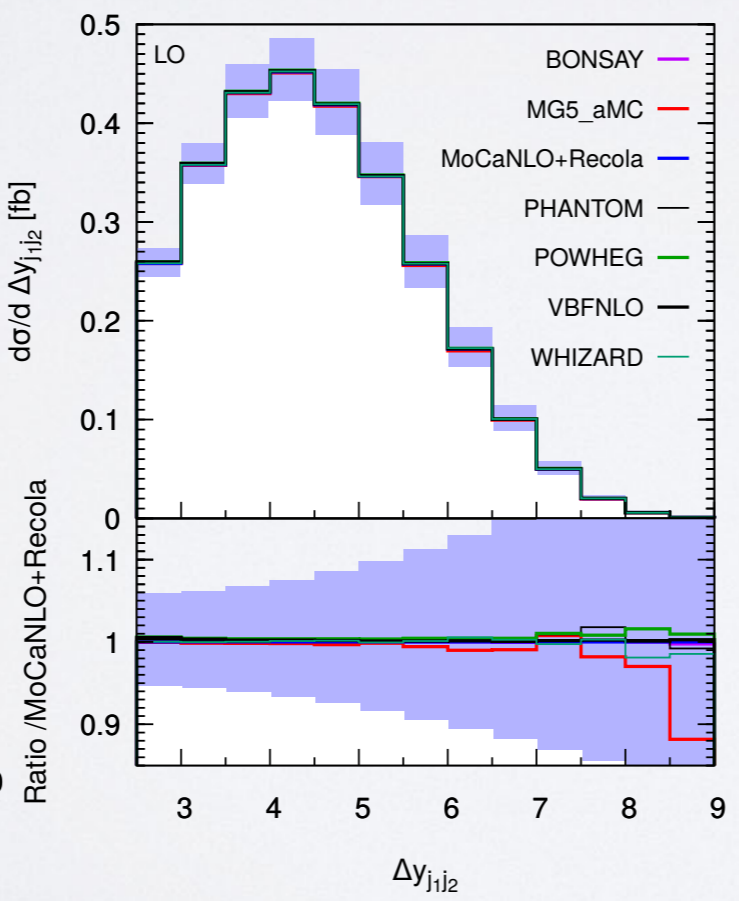
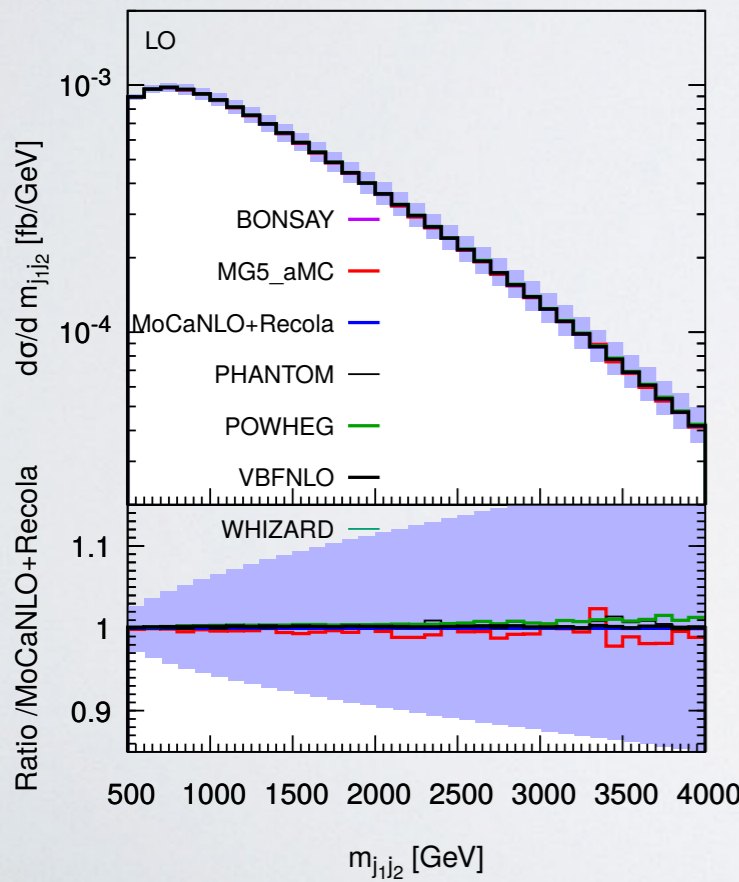
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MG5_AMC+HERWIG7, $\Gamma_{\text{resc}}$ , $\Gamma_{\text{resc}}$	$1.266 \pm 0.003$
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**First official use of MPI-parallelized phase space & first published application of WHIZARD & HERWIG showering**

LO+PS





WHIZARD cannot only do scattering processes, but also decays

Example Energy distribution electron in muon decay:

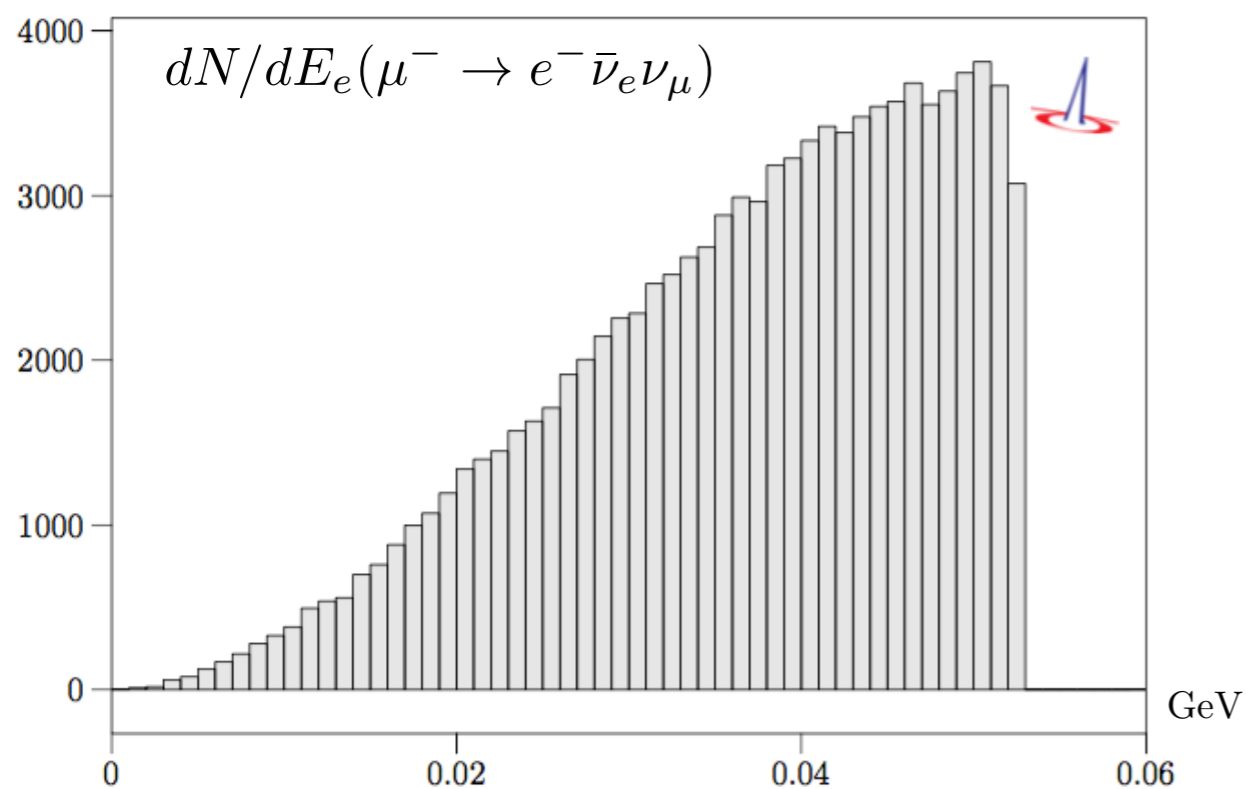
```
model = SM
process mudec = e2 => e1, N1, n2
integrate (mudec)

histogram e_e1 (0, 60 MeV, 1 MeV)
analysis = record e_e1 (eval E [e1])

n_events = 100000

simulate (mudec)

compile_analysis { $out_file = "test.dat" }
```





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```

## Automatic integration of particle decays

```

auto_decays_multiplicity = 2
?auto_decays_radiative = false

unstable Wp () { ?auto_decays = true }

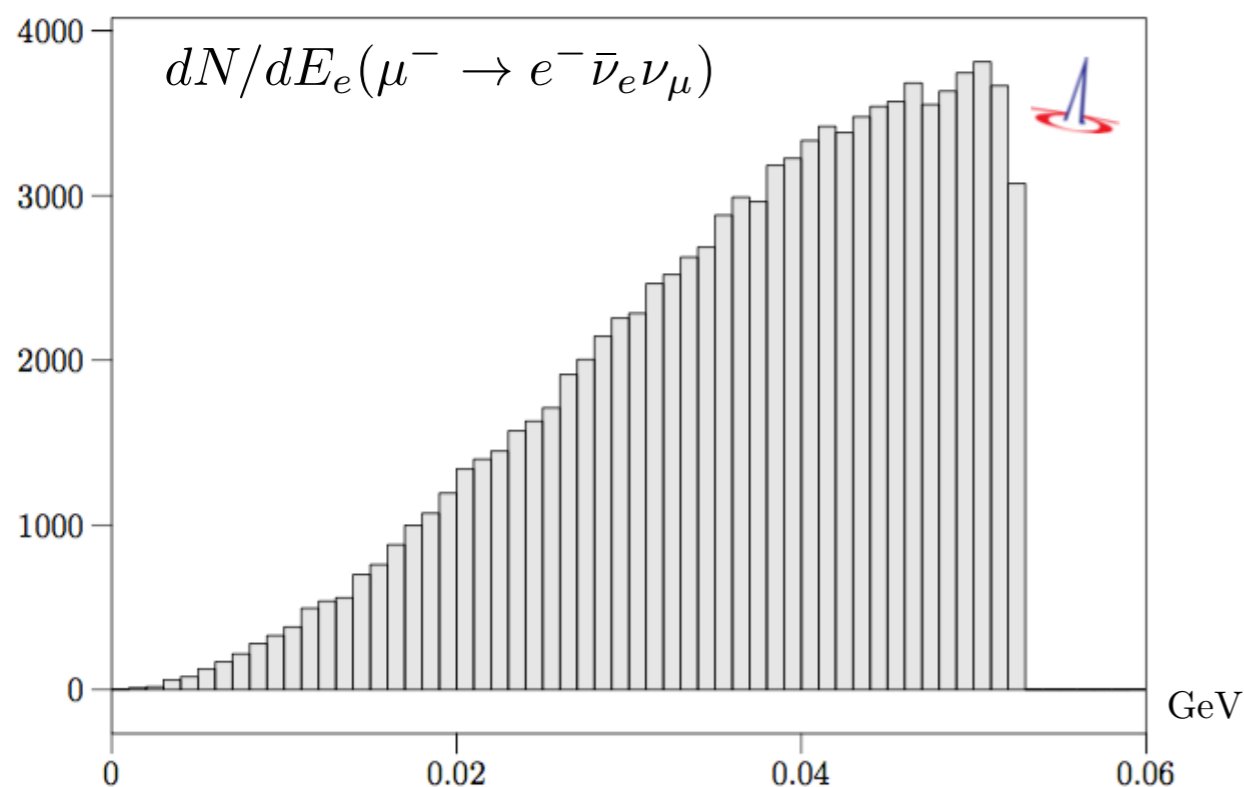
```

It	Calls	Integral[GeV]	Error[GeV]	Err[%]	Acc	Eff[%]
1	100	2.2756406E-01	0.00E+00	0.00	0.00*	100.00
1	100	2.2756406E-01	0.00E+00	0.00	0.00	100.00

```

Unstable particle W+: computed branching ratios:
decay_p24_1: 3.3337068E-01  dbar, u
decay_p24_2: 3.3325864E-01  sbar, c
decay_p24_3: 1.1112356E-01  e+, nue
decay_p24_4: 1.1112356E-01  mu+, numu
decay_p24_5: 1.1112356E-01  tau+, nutau
Total width = 2.0478471E+00 GeV (computed)
              = 2.0490000E+00 GeV (preset)
Decay options: helicity treated exactly

```



Preset branching ratios possible:

```
integral (br_hZA_redef) = 200 keV
```



**Event formats:** conventions for outputting details of the events

```
sample_format = hepmc
sample_format = lhef {$lhef_version = "3.0"}
sample_format = stdhep, stdhep_up, stdhep_ev4
sample_format = ascii, debug, mokka, lha
sample_format = lcio
simulate (<process>)
```

- External format, ASCII: HepMC [[Dobbs/Hansen, 2001](#)]
- External format, binary: LCIO [[Gaede, 2003](#)]
- Internal formats, binary: StdHEP [[Lebrun, 1990](#)]
- Internal formats, ASCII: LHA, LHEF [[Alwall et al., 2006](#)]



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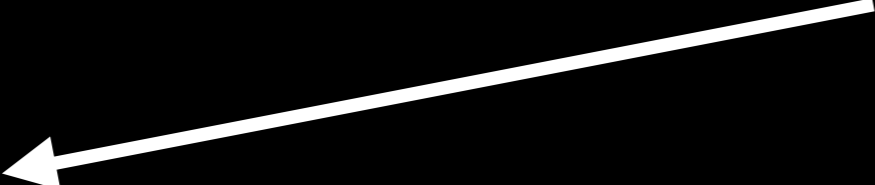
## LCIO Format (LC I/O, particle-flow motivated): (ASCII transcription from binary)

```

=====
Event : 1 - run: 0 - timestamp [...]
=====
date: [...]
detector : unknown
event parameters:
parameter Event Number [int]: 1,
parameter ProcessID [int]: 1,
parameter Run ID [int]: 0,
parameter beamPDG0 [int]: 11,
parameter beamPDG1 [int]: -11,
parameter Energy [float]: 500,
parameter Pol0 [float]: 0,
parameter Pol1 [float]: 0,
parameter _weight [float]: 1,
parameter alphaQCD [float]: 0.1178,
parameter crossSection [float]: 338.482,
parameter crossSectionError [float]: 7.2328,
parameter scale [float]: 500,
parameter BeamSpectrum [string]: ,
parameter processName [string]: lcio_5_p,
collection name : MCParticle
parameters:
----- print out of MCParticle collection -----
flag: 0x0
simulator status bits: [sbvtcls] s: created in simulation b: backscatter v: vertex is not endpoint of parent t: decayed in tracker c: decayed in
calorimeter l: has left detector s: stopped o: overlay
[ id ] index | PDG | px, py, pz | energy | gen | [simstat] | vertex x,y,z | mass | charge | spin | colorflow | [par] - [dau]
[00000004] 0 | 11 | 0.00e+00, 0.00e+00, 2.50e+02 | 2.50e+02 | 3 | [ 0 ] | 0.0, 0.0, 0.0 | 5.11e-04 | -1.00e+00 | 0.0, 0.0, 0.0 | (0, 0) | [] - [2,3]
[00000005] 1 | -11 | 0.00e+00, 0.00e+00, -2.50e+02 | 2.50e+02 | 3 | [ 0 ] | 0.0, 0.0, 0.0 | 5.11e-04 | 1.00e+00 | 0.0, 0.0, 0.0 | (0, 0) | [] - [2,3]
[00000006] 2 | 13 | 1.42e+02, 1.99e+02, -5.22e+01 | 2.50e+02 | 1 | [ 0 ] | 0.0, 0.0, 0.0 | 1.06e-01 | -1.00e+00 | 0.0, 0.0, 1.0 | (0, 0) | [0,1] - []
[00000007] 3 | -13 | -1.42e+02, -1.99e+02, 5.22e+01 | 2.50e+02 | 1 | [ 0 ] | 0.0, 0.0, 0.0 | 1.06e-01 | 1.00e+00 | 0.0, 0.0, -1.0 | (0, 0) | [0,1] - []

```

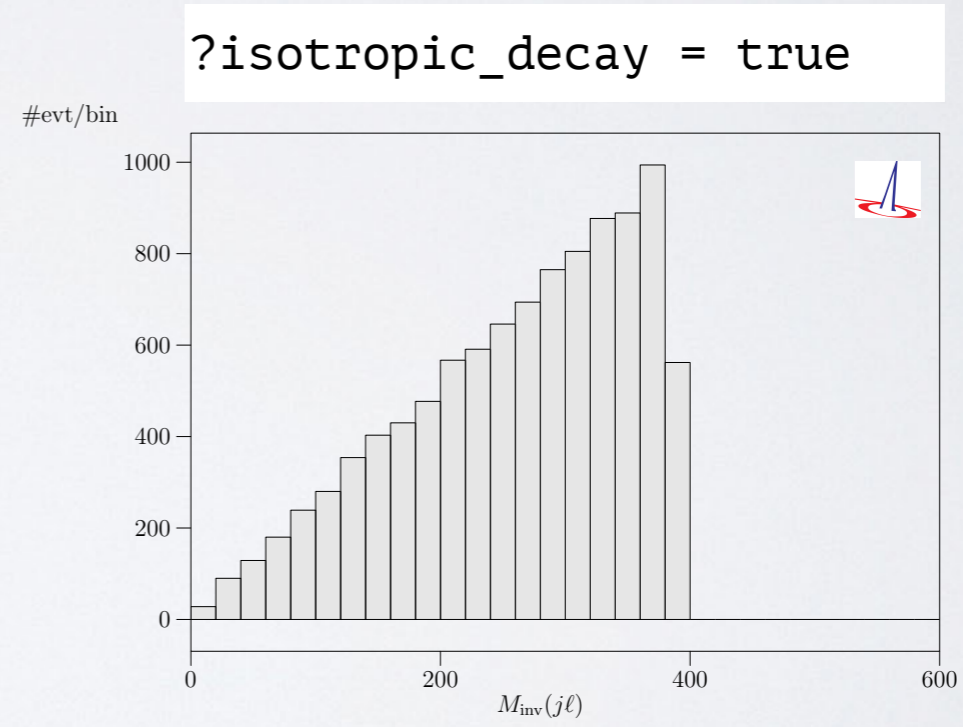
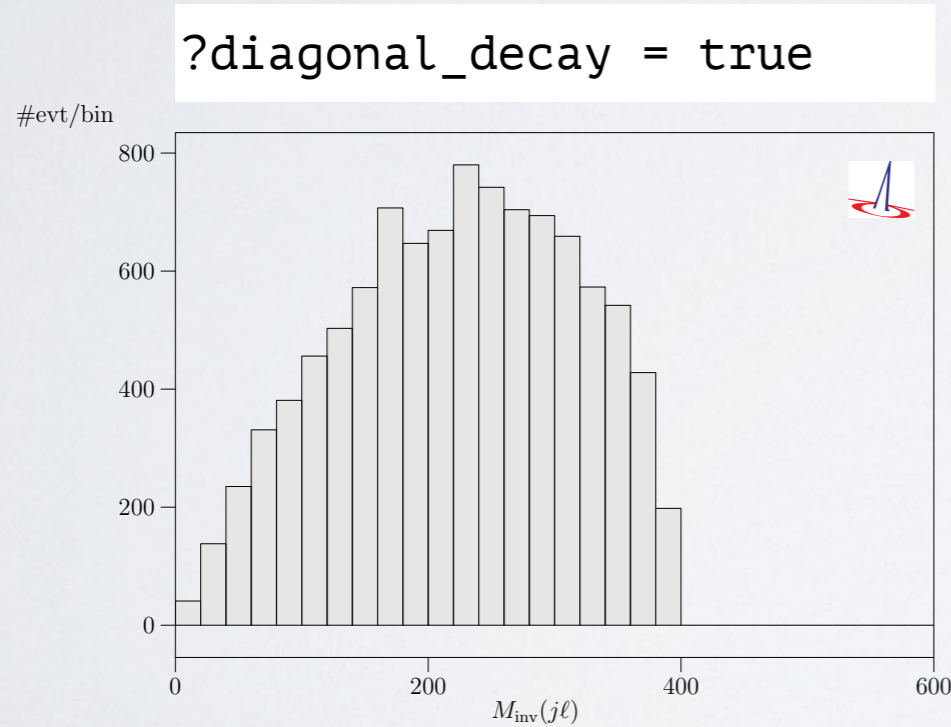
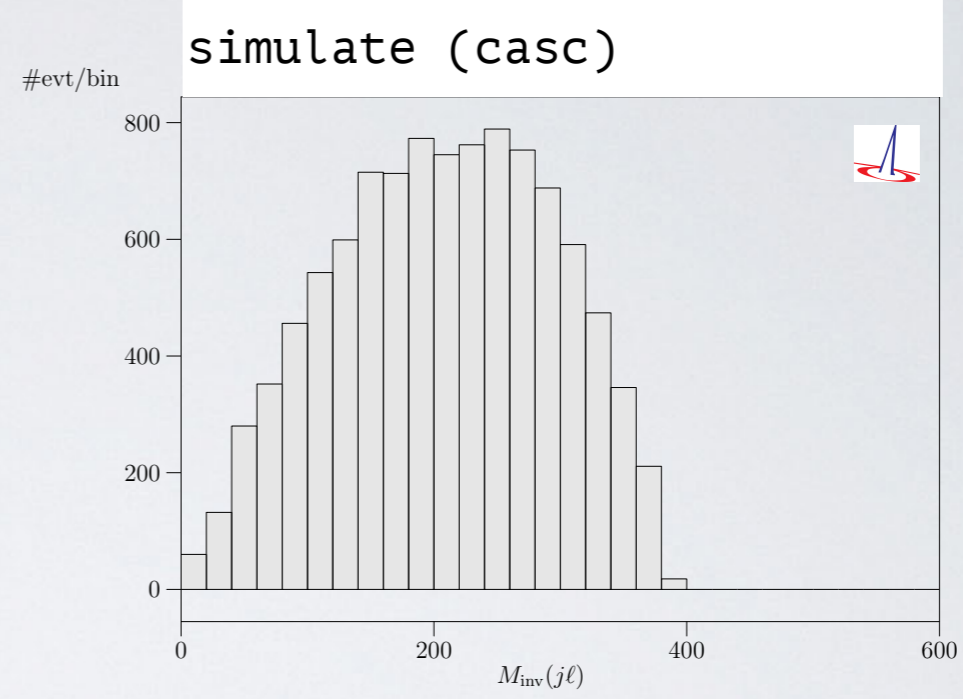
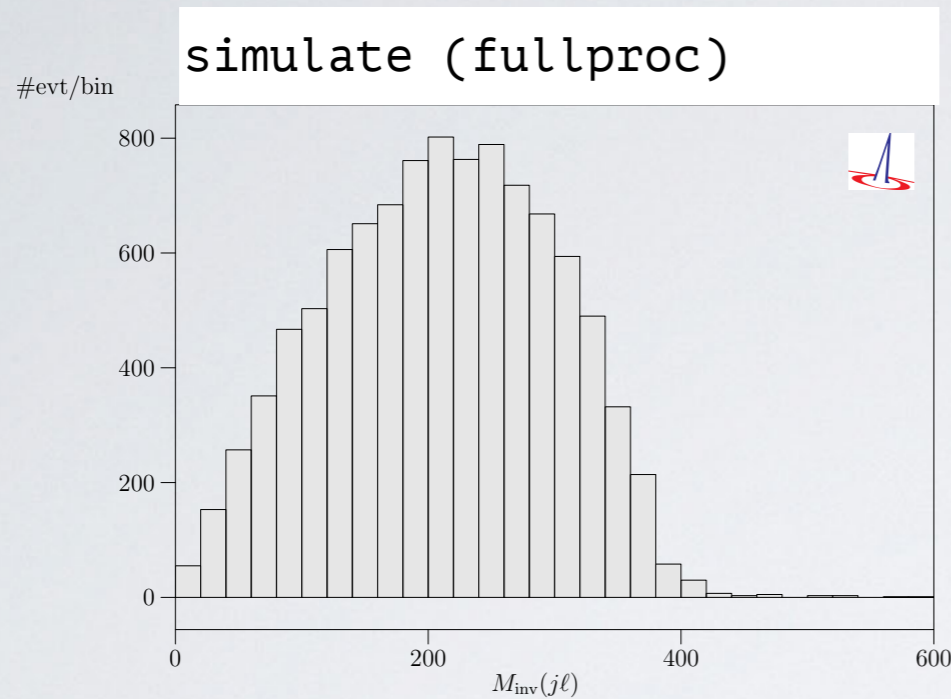
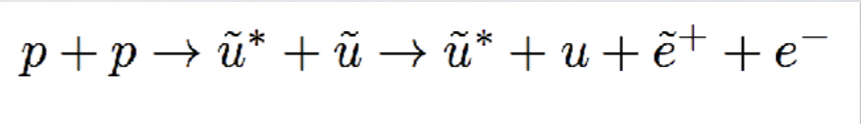
Event header information as agreed upon with LC Gen Group





# Spin Correlation and Polarization in Cascades

Cascade decay, factorize production and decay

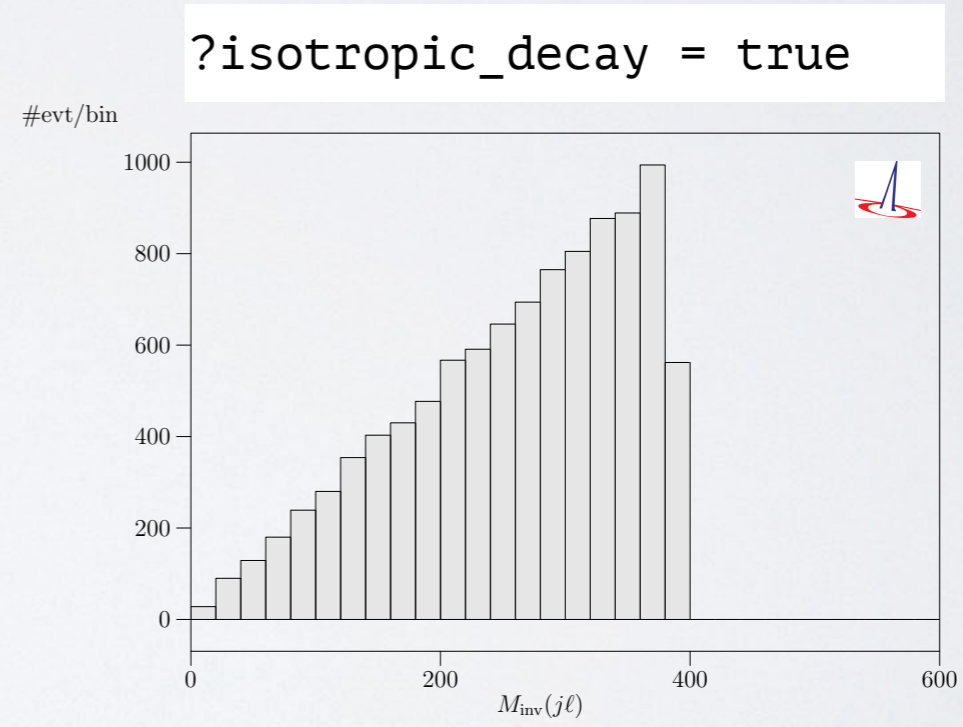
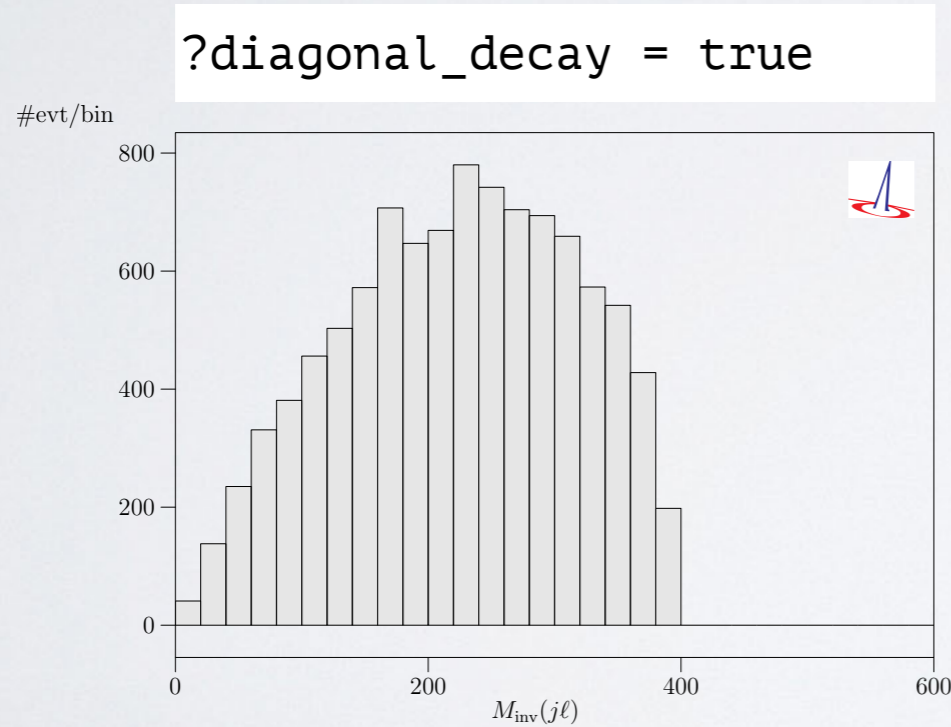
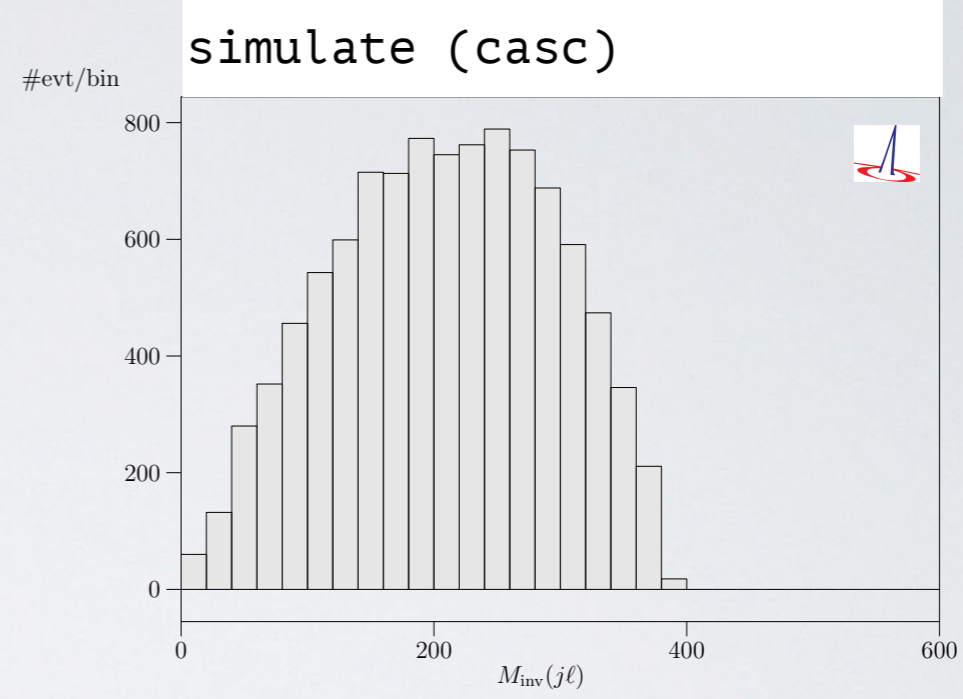
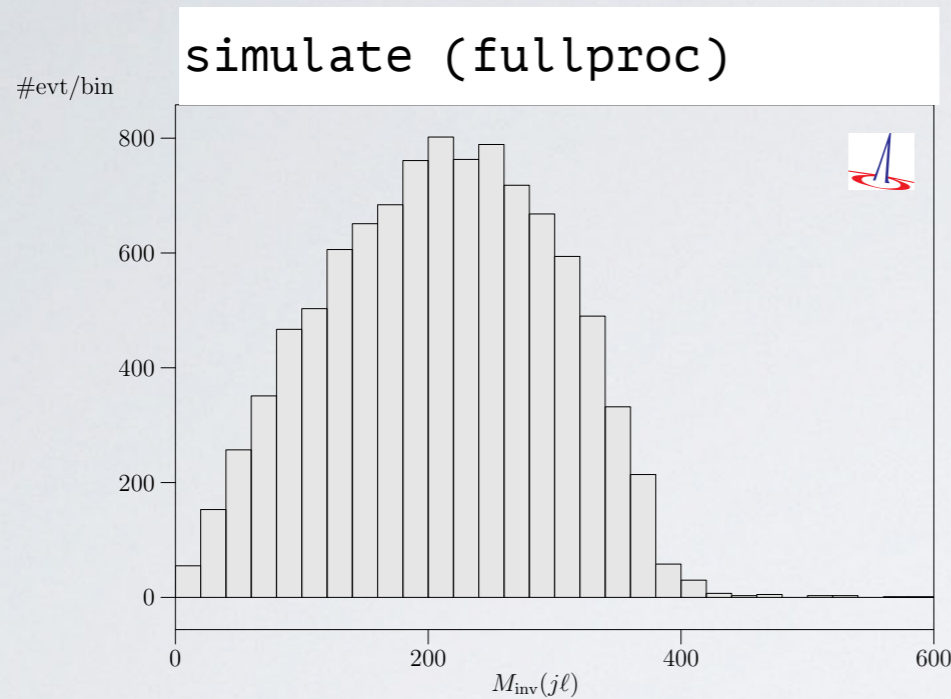
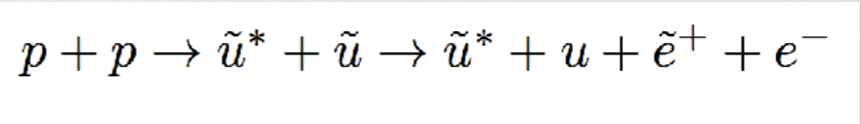






# Spin Correlation and Polarization in Cascades

Cascade decay, factorize production and decay



Possibility to select specific helicity in decays!

unstable "W+" { decay\_helicity = 0 }





```
?resonance_history = true  
resonance_on_shell_limit = 4  
resonance_on_shell_turnoff = 1  
resonance_background_factor = 1e-10
```

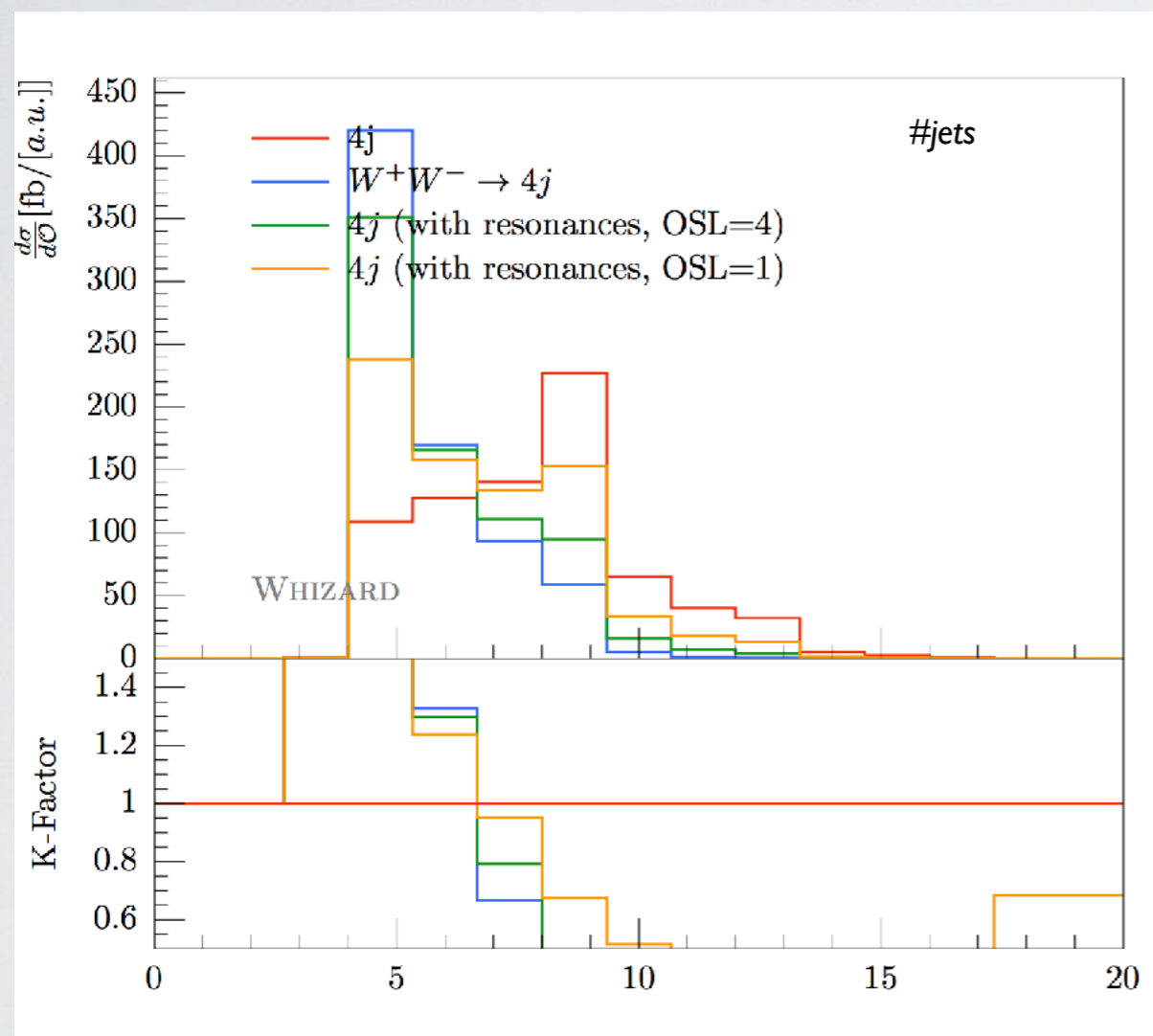
- **Problem:**  $e^+e^- \rightarrow jjjj$  not dominated by highest  $\alpha_s$  power,  
but by resonances  $e^+e^- \rightarrow WW/ZZ \rightarrow (jj)(jj)$
- **Solution:** proper merging with resonant subprocesses by means of resonance histories
- WHIZARD v2.6.0: **option to set resonance histories**



# Keep resonances in ME-PS merging

```
?resonance_history = true
resonance_on_shell_limit = 4
resonance_on_shell_turnoff = 1
resonance_background_factor = 1e-10
```

- Problem:**  $e^+e^- \rightarrow jjjj$  not dominated by highest  $\alpha_s$  power, but by resonances  $e^+e^- \rightarrow WW/ZZ \rightarrow (jj)(jj)$
- Solution:** proper merging with resonant subprocesses by means of resonance histories
- WHIZARD v2.6.0: **option to set resonance histories**

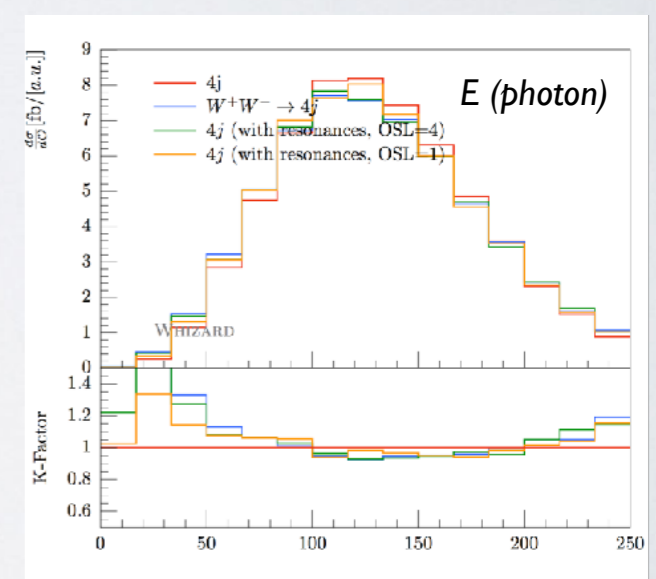
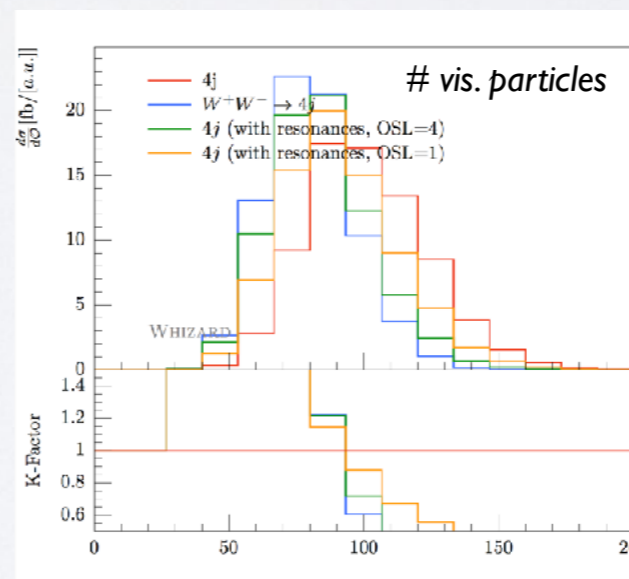
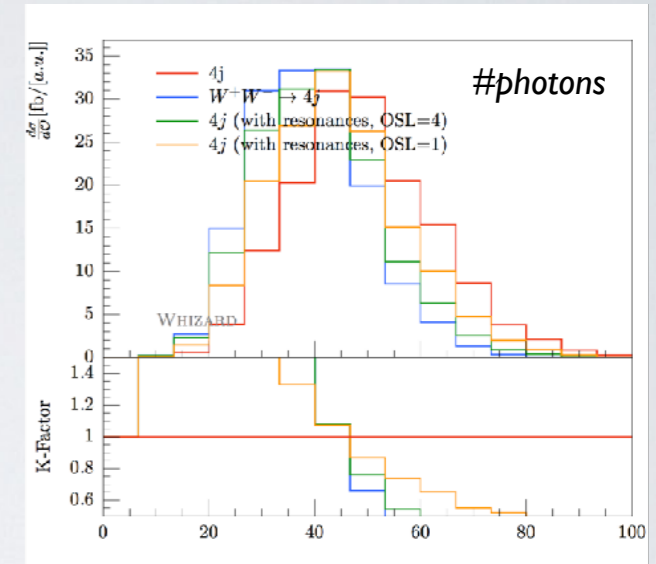
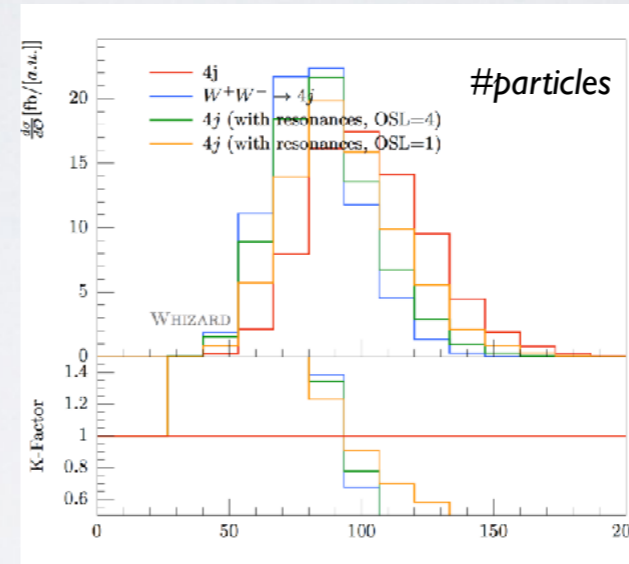
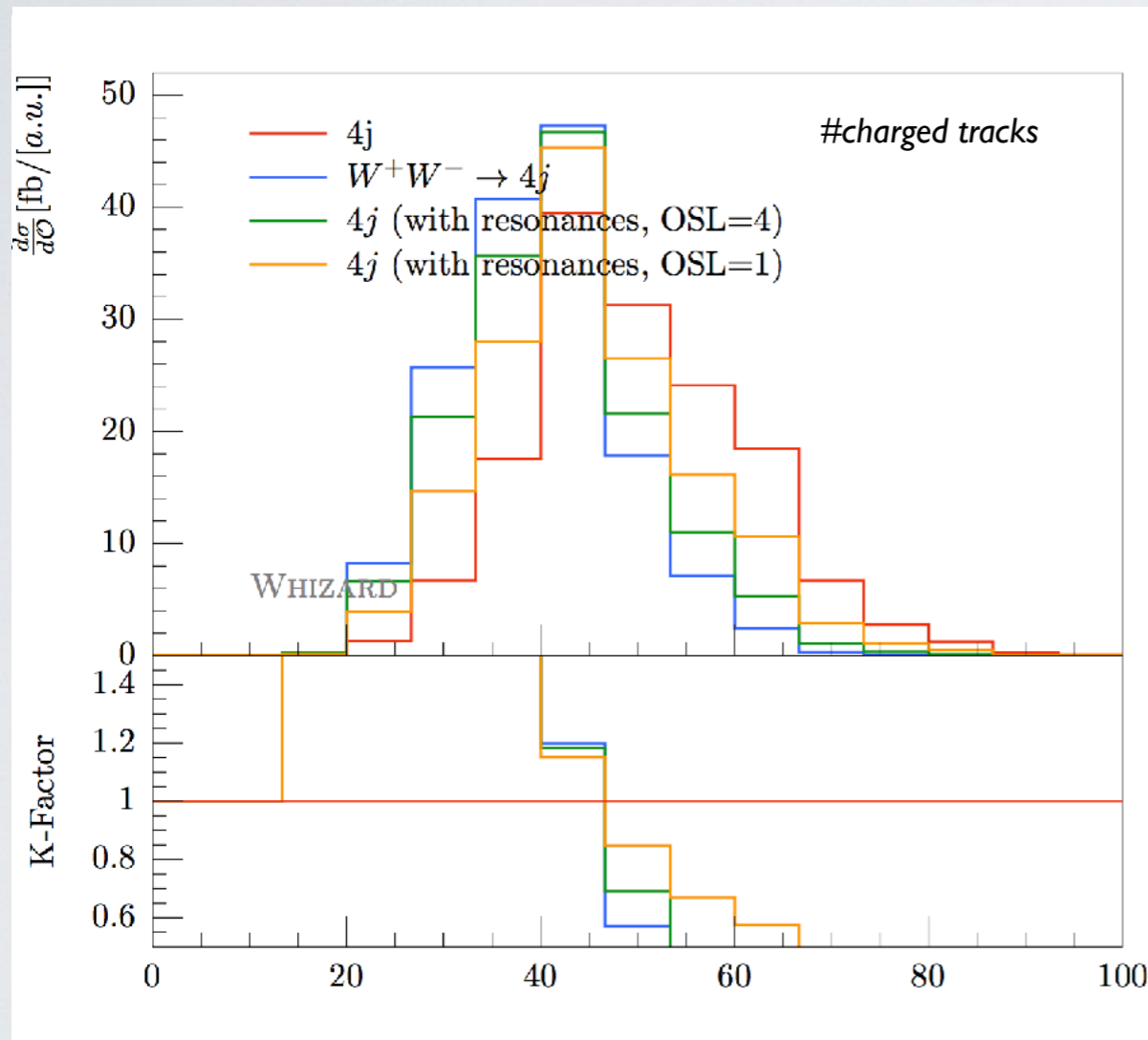




# Keep resonances in ME-PS merging

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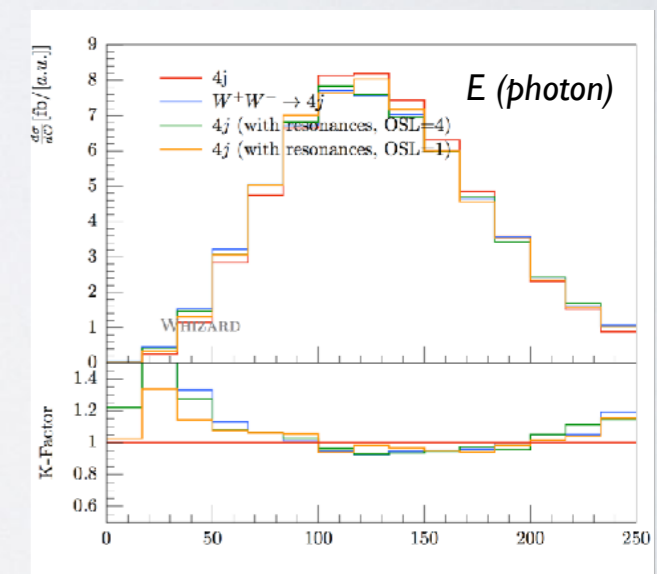
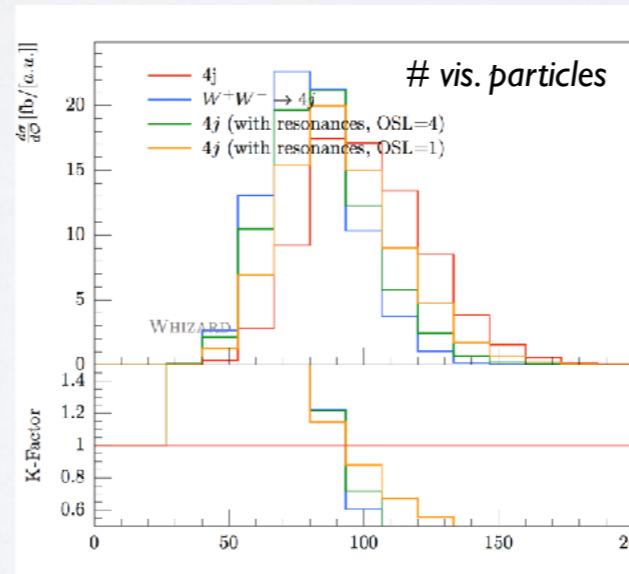
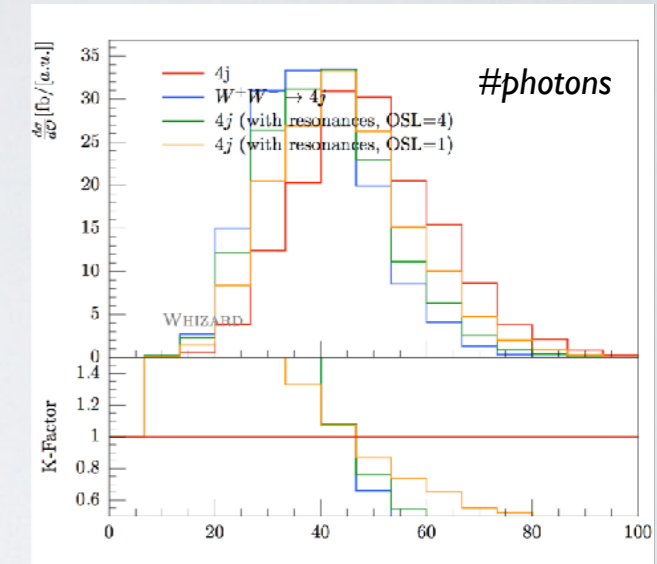
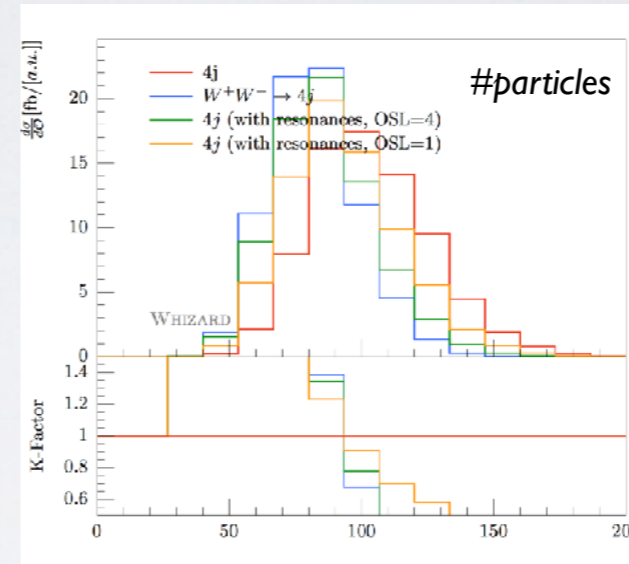
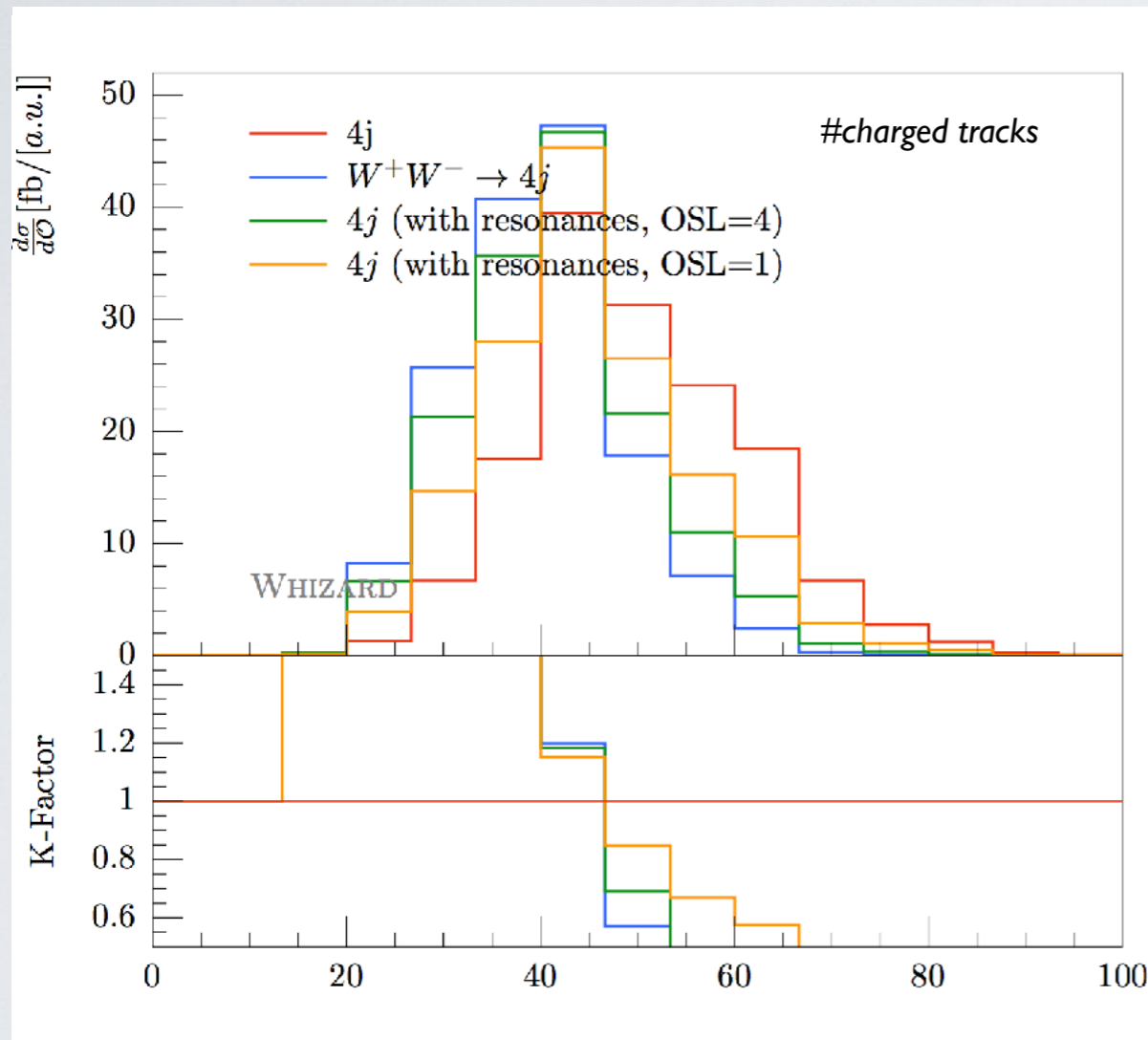




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- WHIZARD v2.6.0: **option to set resonance histories**



- LC Generator Group started first tests on  $e^+e^- \rightarrow 6j$  ; includes tests with resonant  $H \rightarrow bb$





MODEL TYPE	with CKM matrix	trivial CKM
Yukawa test model	---	Test
QED with $e, \mu, \tau, \gamma$	---	QED
QCD with $d, u, s, c, b, t, g$	---	QCD
Standard Model	SM_CKM	SM
SM with anomalous gauge couplings	SM_ac_CKM	SM_ac
SM with $Hgg, H\gamma\gamma, H\mu\mu, He^+e^-$	SM_Higgs_CKM	SM_Higgs
SM with bosonic dim-6 operators	---	SM_dim6
SM with charge 4/3 top	---	SM_top
SM with anomalous top couplings	---	SM_top_anom
SM with anomalous Higgs couplings	---	SM_rx/NoH_rx/SM_ul
SM extensions for $VV$ scattering	---	SSC/AltH/SSC_2/SSC_AltT
SM with $Z'$	---	Zprime
Two-Higgs Doublet Model	THDM_CKM	THDM
Higgs Singlet Extension	---	HSExt
MSSM	MSSM_CKM	MSSM
MSSM with gravitinos	---	MSSM_Grav
NMSSM	NMSSM_CKM	NMSSM
extended SUSY models	---	PSSSM
Littlest Higgs	---	Littlest
Littlest Higgs with ungauged $U(1)$	---	Littlest_Eta
Littlest Higgs with $T$ parity	---	Littlest_Tpar
Simplest Little Higgs (anomaly-free)	---	Simplest
Simplest Little Higgs (universal)	---	Simplest_univ
SM with graviton	---	Xdim
UED	---	UED
“SQED” with gravitino	---	GravTest
Augmentable SM template	---	Template

- Automated models: interface to SARAH/BSM Toolbox [Staub, 0909.2863](#); [Ohl/Porod/Staub/Speckner, 1109.5147](#)
- Automated models: interface to FeynRules [Christensen/Duhr](#); [Christensen/Duhr/Fuks/JRR/Speckner, 1010.3251](#)



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- **Automated models: UFO interface** [new WHIZARD/0' Mega model format]





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by So Young Shim  
heavily used  
for CLIC  
Yellow Report  
multi-boson  
studies  
(VVV + VBS)

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- Automated models: **UFO interface** [new WHIZARD/0' Mega model format]





```
model = SM (ufo)
```

UFO file is assumed to be in working directory OR

```
model = SM (ufo ("<my UFO path>"))
```

UFO file is in user-specified directory

```
=====
WHIZARD 2.5.1
=====
| Reading model file '/Users/reuter/local/share/whizard/models/SM.mdl'
| Preloaded model: SM
| Process library 'default_lib': initialized
| Preloaded library: default_lib
| Reading model file '/Users/reuter/local/share/whizard/models/SM_hadrons.mdl'
| Reading commands from file 'ufo_2.sin'
| Model: Generating model 'SM' from UFO sources
| Model: Searching for UFO sources in working directory
| Model: Found UFO sources for model 'SM'
| Model: Model file 'SM.ufo.mdl' generated
| Reading model file 'SM.ufo.mdl'
```

```
| Switching to model 'SM' (generated from UFO source)
```

All the setup works the same as for intrinsic models

Old FeynRules / SARAH interface will get deprecated

kept at the moment for user backwards compatibility

All SM-like models/scalar extensions already supported

Higher-dim. operators, general Lorentz/color structures is work in progress



Working NLO interfaces to:

- ★ GoSam [N. Greiner, G. Heinrich, J. v. Soden-Fraunhofen et al.]
- ★ OpenLoops [F. Cascioli, J. Lindert, P. Maierhöfer, S. Pozzorini]
- ★ Recola [A. Denner, L. Hofer, J.-N. Lang, S. Uccirati]

NLO QCD (massless & massive) fully supported

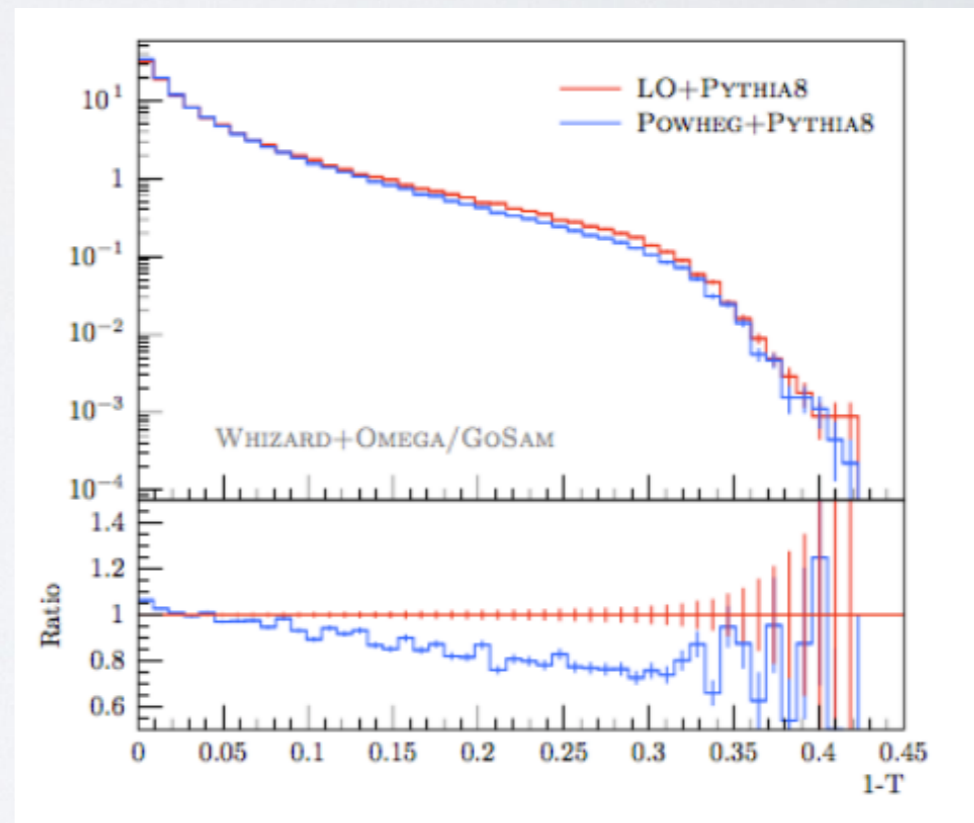
List of validated NLO QCD processes

```
alpha_power = 2
alphas_power = 0

process eett = e1,E1 => t, tbar
  { nlo_calculation = "full" }
```

- $e^+e^- \rightarrow jj$
- $e^+e^- \rightarrow jjj$
- $e^+e^- \rightarrow \ell^+\ell^-jj$
- $e^+e^- \rightarrow \ell^+\nu_\ell jj$
- $e^+e^- \rightarrow t\bar{t}$
- $e^+e^- \rightarrow t\bar{t}\bar{t}$
- $e^+e^- \rightarrow t\bar{t}W^+jj$
- $e^+e^- \rightarrow tW^-b$
- $e^+e^- \rightarrow W^+W^-b\bar{b}, \ell^+\ell^-\nu_\ell\bar{\nu}_\ell b\bar{b}$
- $e^+e^- \rightarrow b\bar{b}\ell^+\ell^-$
- $e^+e^- \rightarrow t\bar{t}H$
- $e^+e^- \rightarrow W^+W^-b\bar{b}H, \ell^+\ell^-\nu_\ell\bar{\nu}_\ell b\bar{b}H$
- $pp \rightarrow \ell^+\ell^-$
- $pp \rightarrow \ell\nu$
- $pp \rightarrow ZZ$

- FKS subtraction [Frixione/Kunszt/Signer, hep-ph/9512328]
- Resonance-aware treatment [Ježo/Nason, 1509.09071]
- Virtual MEs external
- Real and virtual subtraction terms internal
- NLO decays available for the NLO processes
- Fixed order events for plotting (weighted)
- Automated POWHEG damping and matching
- NLO QCD: final validation      NLO EW started
- New refactoring phase (3rd + 4th NLO refactoring)



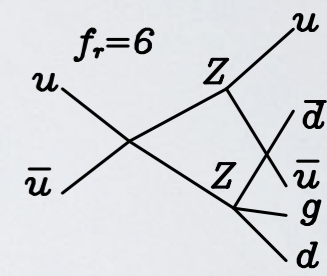
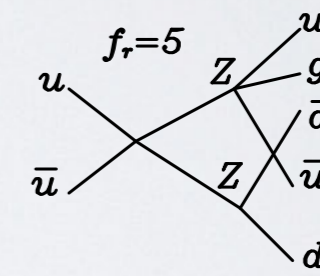
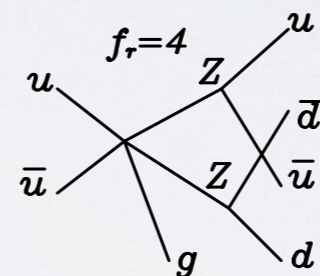
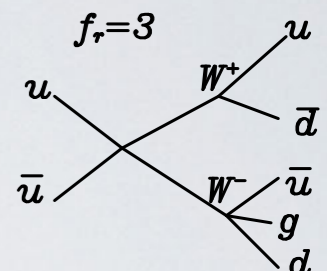
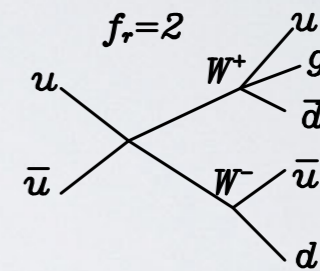
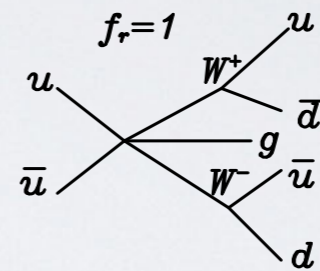
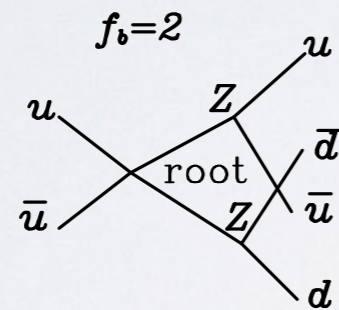
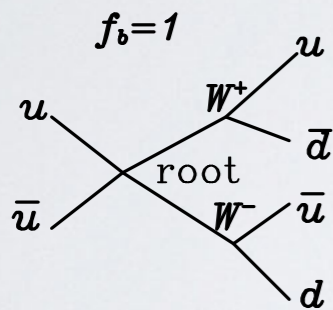


- Amplitudes (except for pure QCD/QED) contain **resonances** ( $Z, W, H, t$ )
- In general: resonance masses *not* respected by modified kinematics of subtraction terms**
- Collinear (and soft) radiation can lead to mismatch between Born and subtraction terms
- Algorithm to include resonance histories** [[Ježo/Nason, 1509.09071](#)]
- Avoids double logarithms in the resonances' width
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- Separate treatment of Born and real terms,**  
soft mismatch [, collinear mismatch]



# Resonance mappings for NLO processes

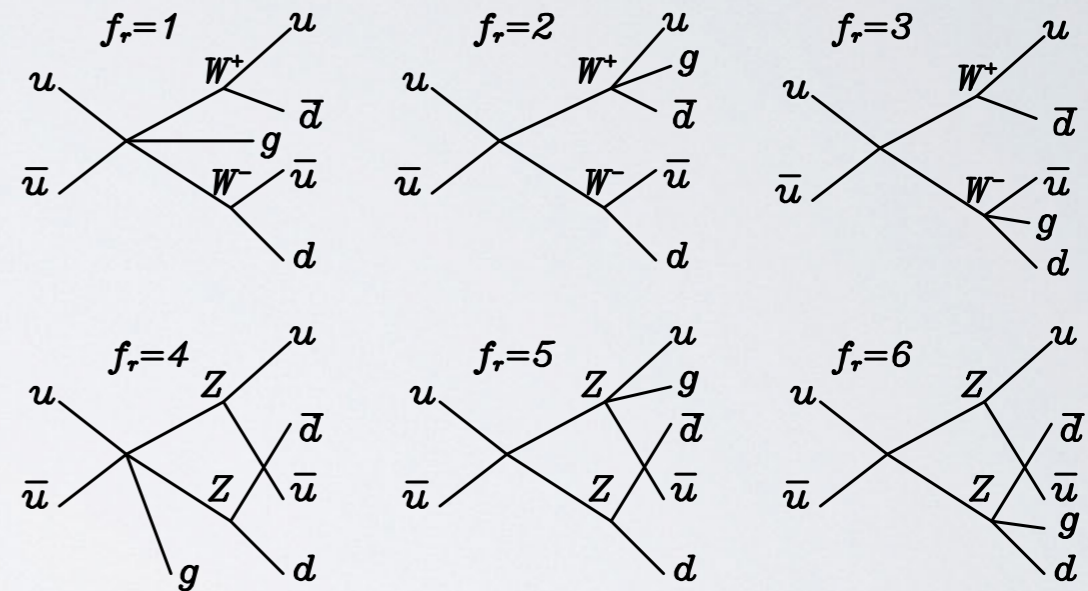
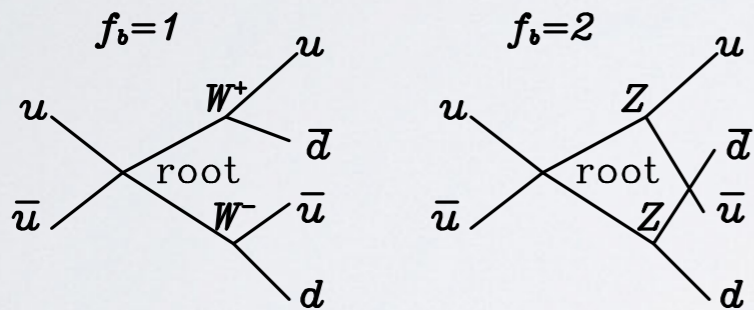
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WHIZARD complete automatic implementation: example  $e^+ e^- \rightarrow \mu\mu bb$  (ZZ, ZH histories)

It	Calls	Integral[fb]	Error[fb]	Err[%]	Acc	Eff[%]	Chi2	N[It]
1	11988	9.6811847E+00	6.42E+00	66.30	72.60*	0.65		
2	11959	2.8539703E+00	2.35E-01	8.25	9.02*	0.69		
3	11936	2.4907574E+00	6.54E-01	26.25	28.68	0.35		
4	11908	2.7695559E+00	9.67E-01	34.91	38.09	0.30		
5	11874	2.4346151E+00	4.82E-01	19.80	21.57*	0.74		
5	59665	2.7539078E+00	1.97E-01	7.15	17.47	0.74	0.49	5

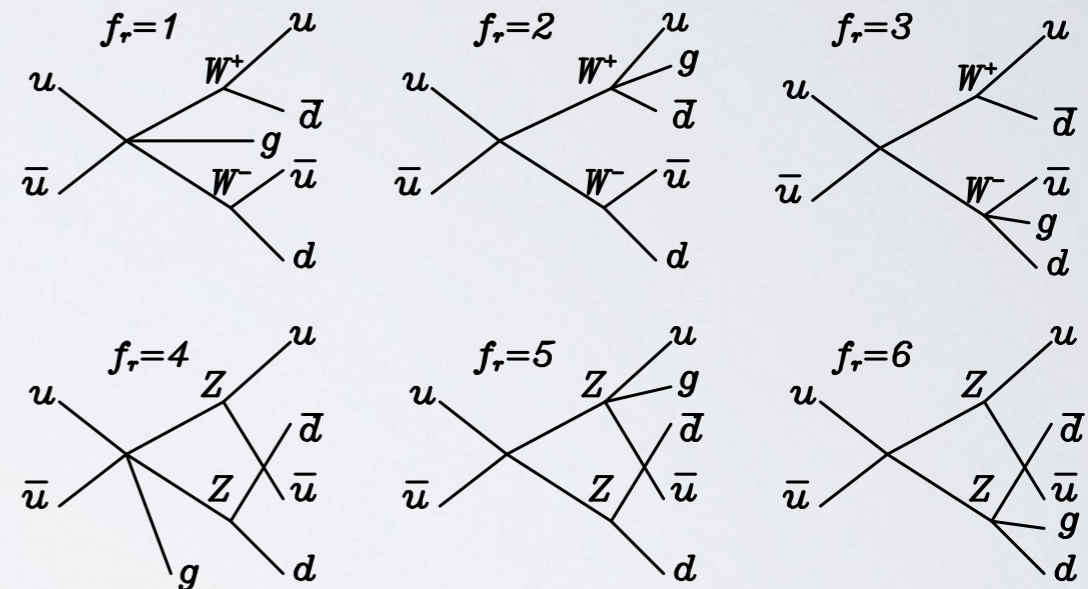
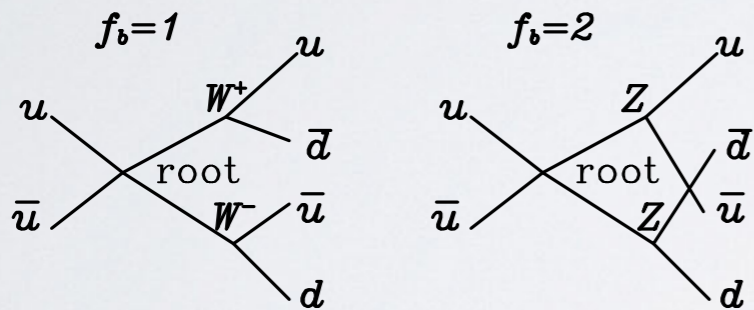
standard FKS





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standard FKS

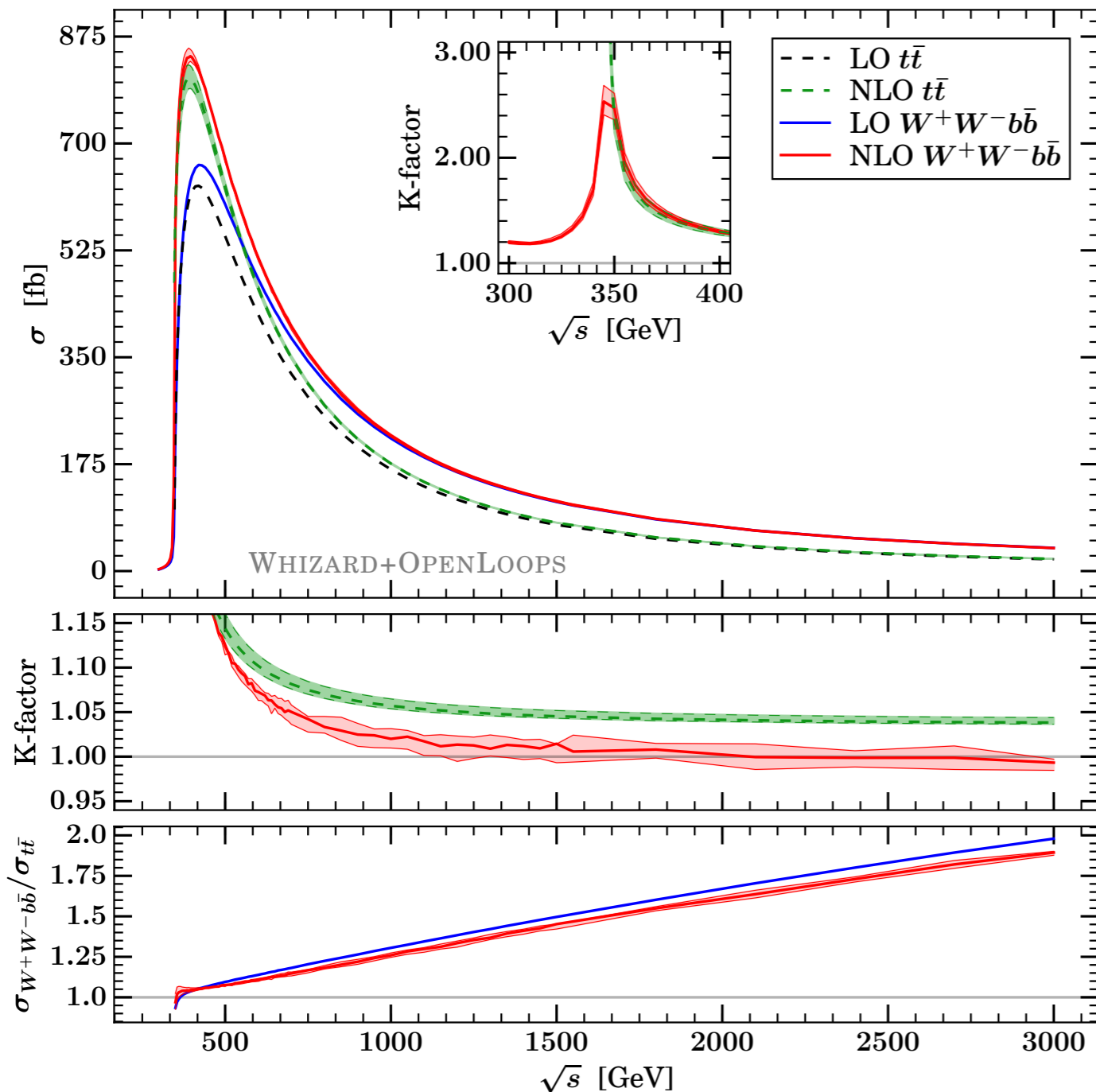
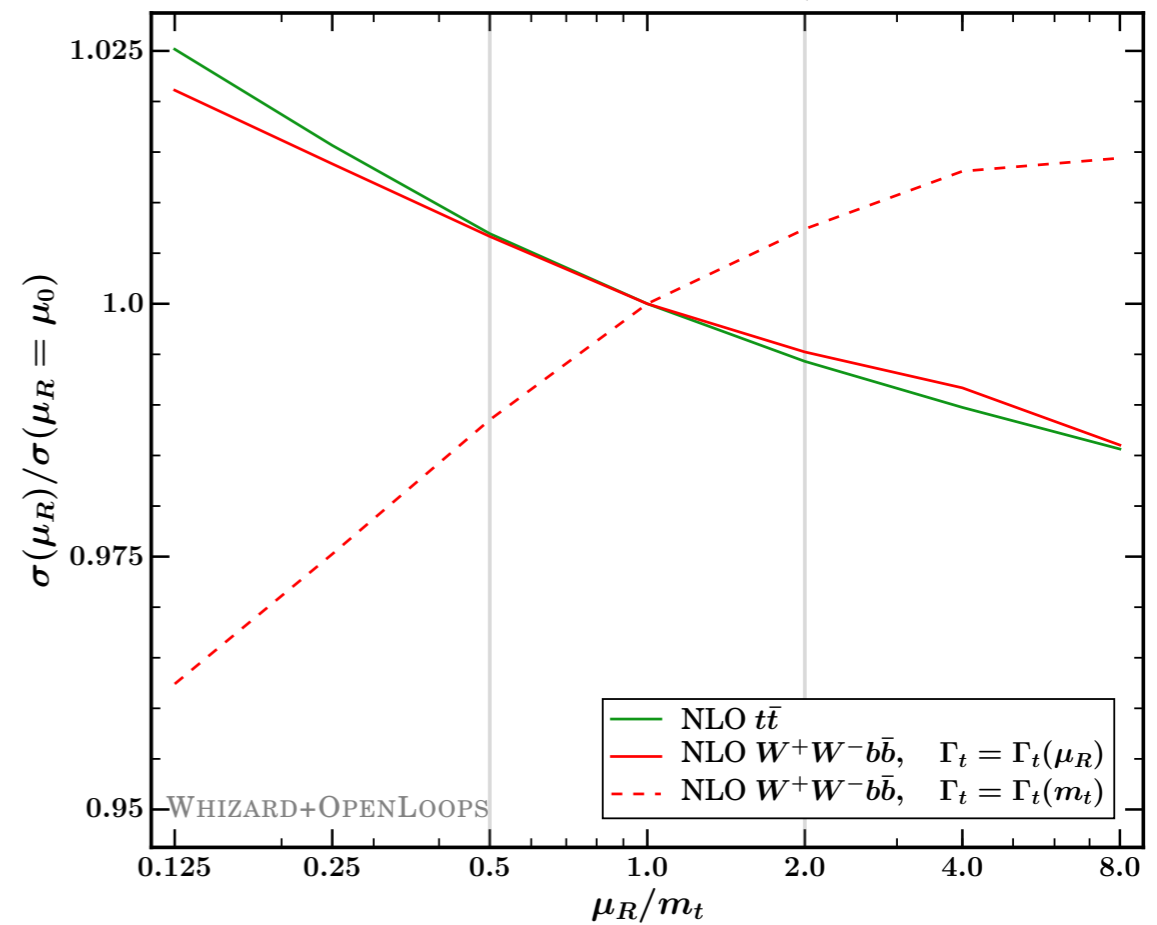
It	Calls	Integral[fb]	Error[fb]	Err[%]	Acc	Eff[%]	Chi2	N[It]
1	11988	2.9057032E+00	8.35E-02	2.87	3.15*	7.90		
2	11962	2.8591952E+00	5.20E-02	1.82	1.99*	10.91		
3	11936	2.9277880E+00	4.09E-02	1.40	1.52*	14.48		
4	11902	2.8512337E+00	3.98E-02	1.40	1.52*	13.70		
5	11874	2.8855399E+00	3.87E-02	1.34	1.46*	17.15		
5	59662	2.8842006E+00	2.04E-02	0.71	1.72	17.15	0.53	5

FKS with resonance mappings





# NLO QCD Results for off-shell $e^+e^- \rightarrow t\bar{t}$

 $e^+e^- \rightarrow t\bar{t}$  and  $e^+e^- \rightarrow W^+W^-b\bar{b}$  $e^+e^- \rightarrow t\bar{t}$  and  $e^+e^- \rightarrow W^+W^-b\bar{b}$  at  $\sqrt{s} = 800$  GeV

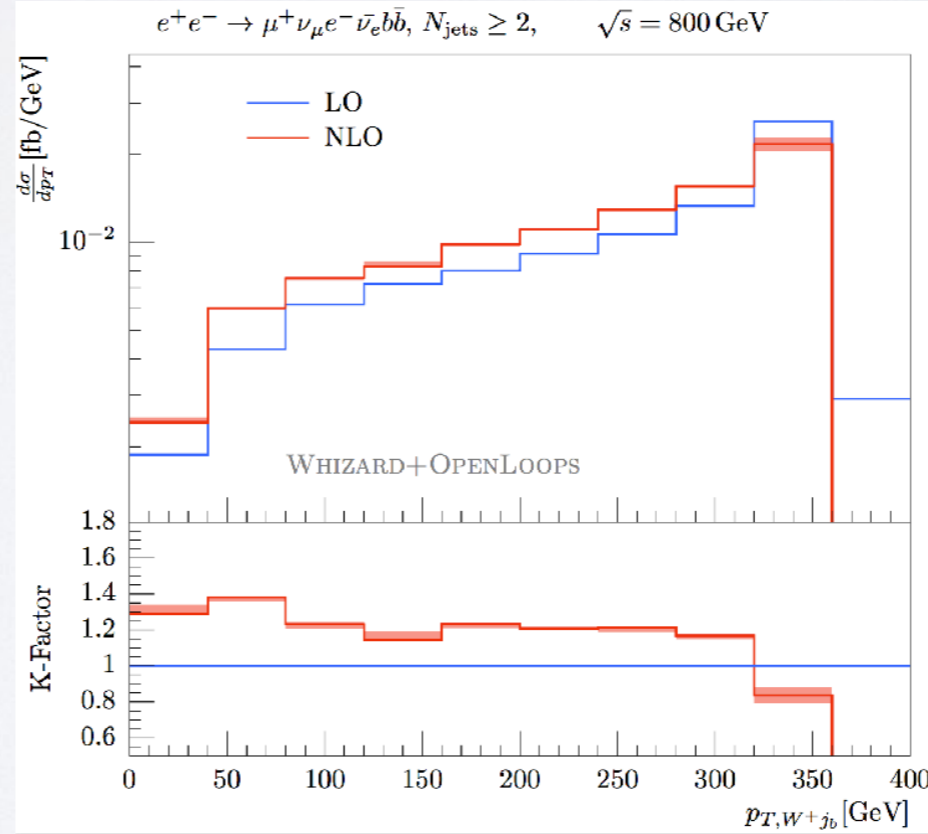
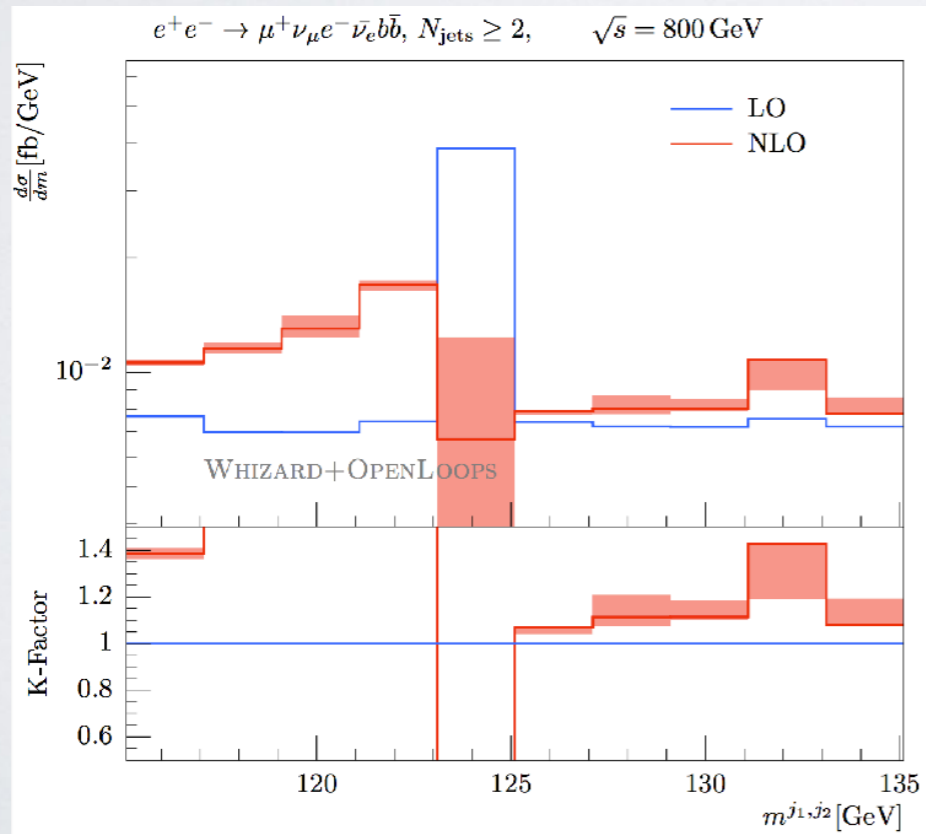
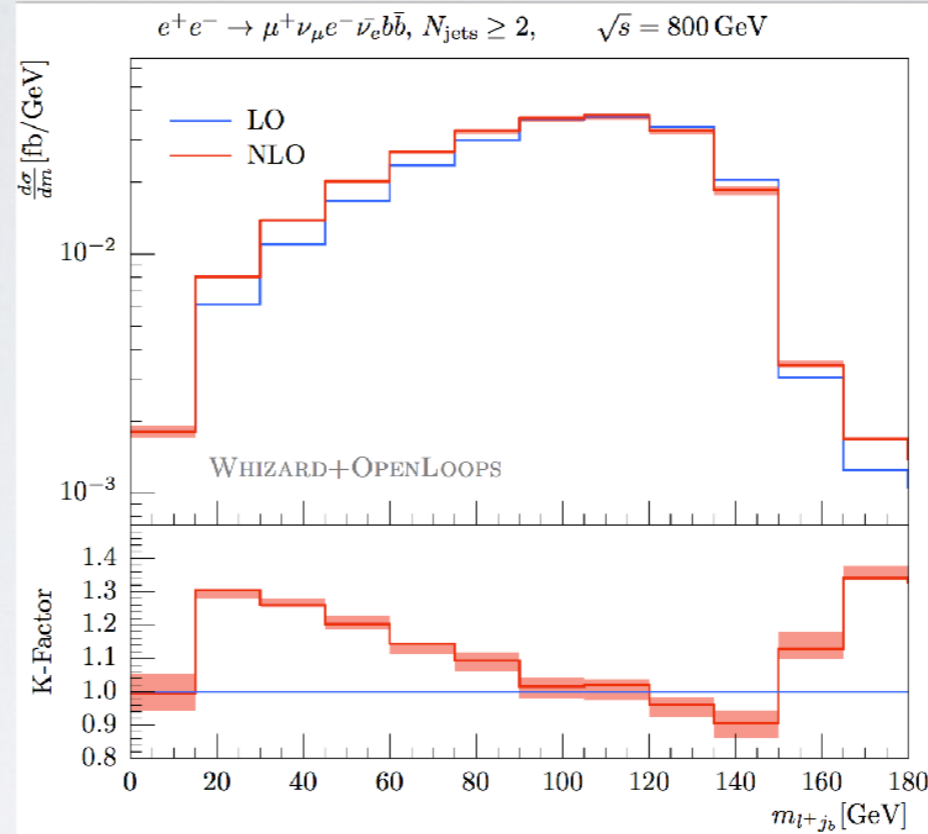
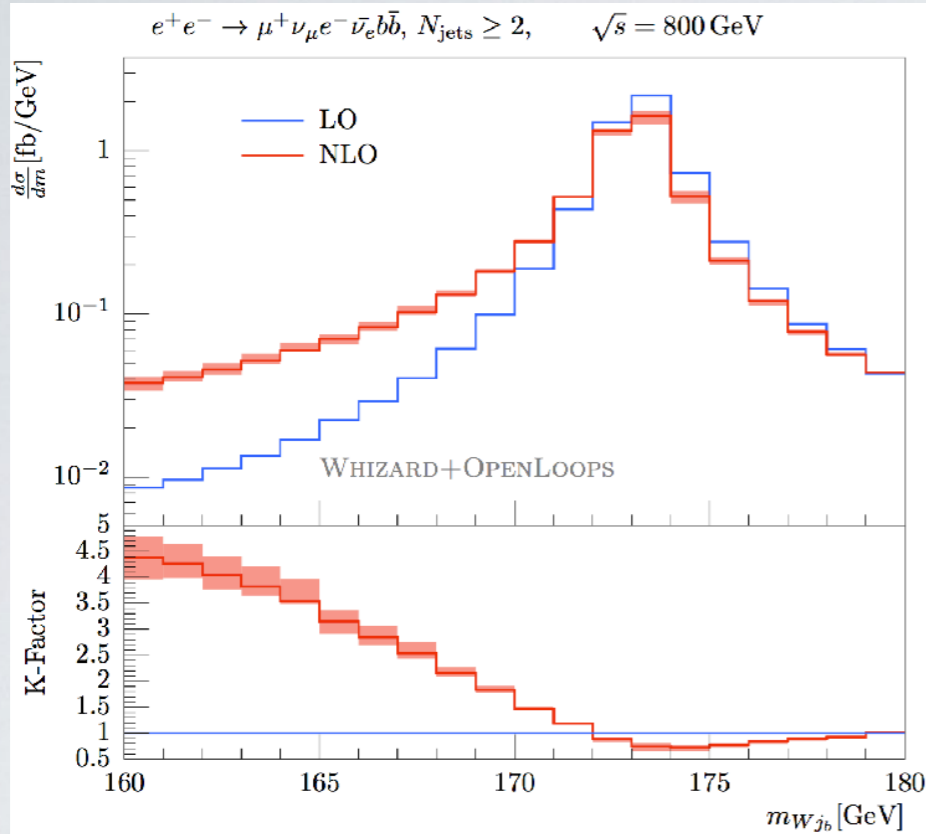
$\sqrt{s}$ [GeV]	$e^+e^- \rightarrow t\bar{t}$			$e^+e^- \rightarrow W^+W^-b\bar{b}$		
	$\sigma^{\text{LO}}$ [fb]	$\sigma^{\text{NLO}}$ [fb]	K-factor	$\sigma^{\text{LO}}$ [fb]	$\sigma^{\text{NLO}}$ [fb]	K-factor
500	548.4	$627.4^{+1.4\%}_{-0.9\%}$	1.14	600.7	$675.1^{+0.4\%}_{-0.8\%}$	1.12
800	253.1	$270.9^{+0.8\%}_{-0.4\%}$	1.07	310.2	$320.7^{+1.1\%}_{-0.7\%}$	1.03
1000	166.4	$175.9^{+0.7\%}_{-0.3\%}$	1.06	217.2	$221.6^{+1.1\%}_{-1.0\%}$	1.02
1400	86.62	$90.66^{+0.6\%}_{-0.2\%}$	1.05	126.4	$127.9^{+0.7\%}_{-1.5\%}$	1.01
3000	19.14	$19.87^{+0.5\%}_{-0.2\%}$	1.04	37.89	$37.63^{+0.4\%}_{-0.9\%}$	0.993

Chokouf /Kilian/Lindert/Pozzorini/JRR/Weiss, 1609.03390





# Differential Results for off-shell $e^+e^- \rightarrow tt$



$$m_t^2 = m_W^2 + \frac{2\langle m_{ljb}^2 \rangle}{1 - \langle \cos \theta_{ljb} \rangle}$$

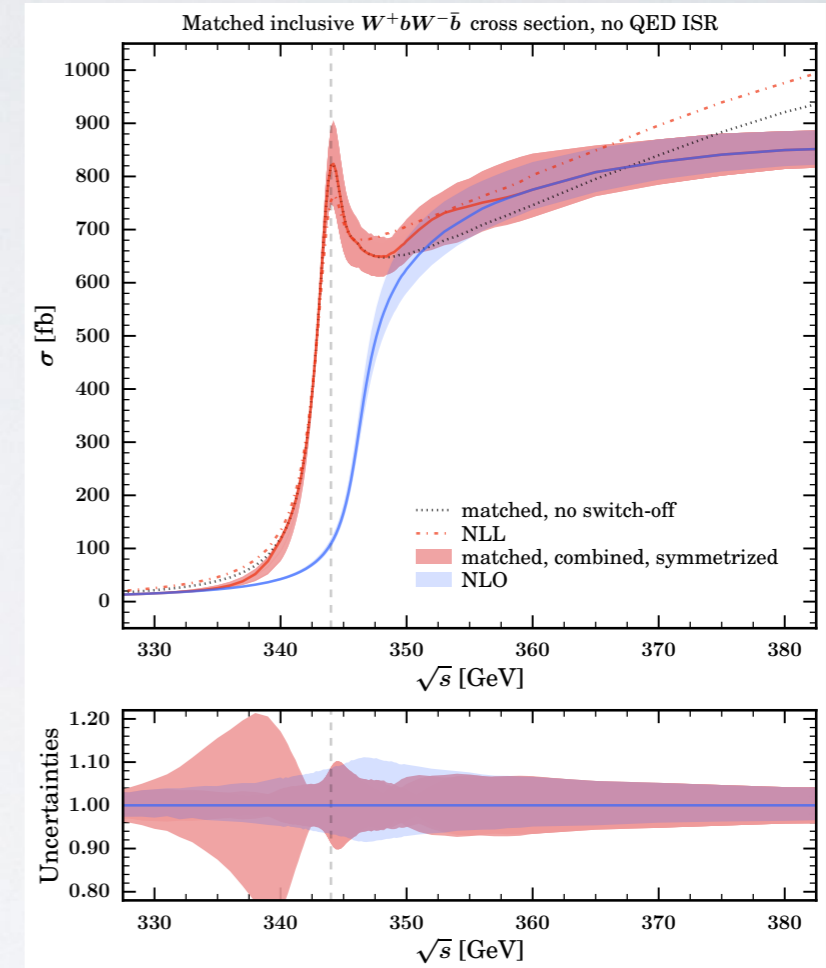
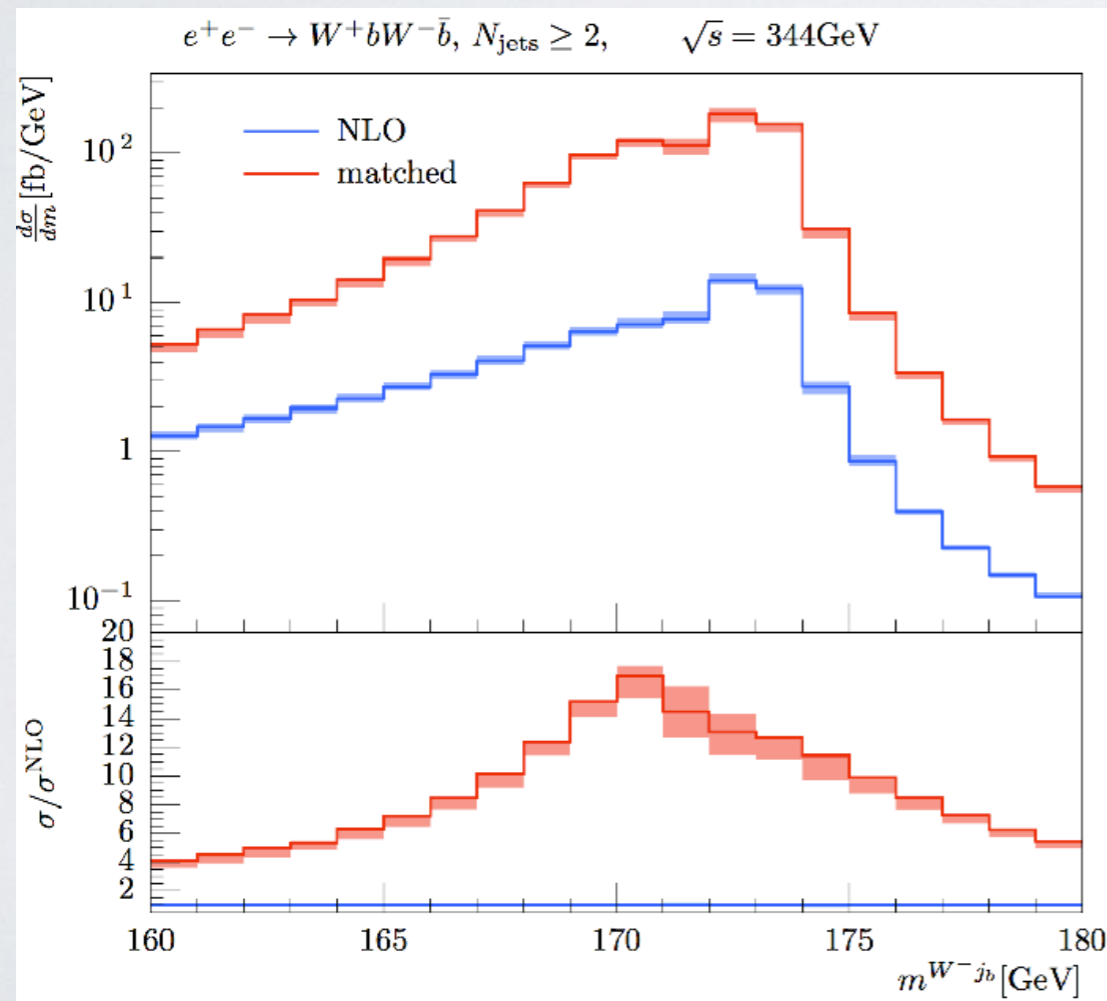






# Top Threshold/Continuum in WHIZARD

- Top threshold scan best-known method to measure top quark mass,  $\Delta M \sim 30\text{-}70 \text{ MeV}$
- Continuum top production best-known method to measure top couplings
- WHIZARD provides special model for top threshold
- Matches threshold resummation with NLO QCD
- Allows for (almost) fully exclusive final states



Chokouf /Hoang/Kilian/JRR/Stahlhofen/Teubner/Weiss,  
1712.02220 [JHEP 1803(2018)184]

Allows to study top mass dependence of  
differential distributions at threshold

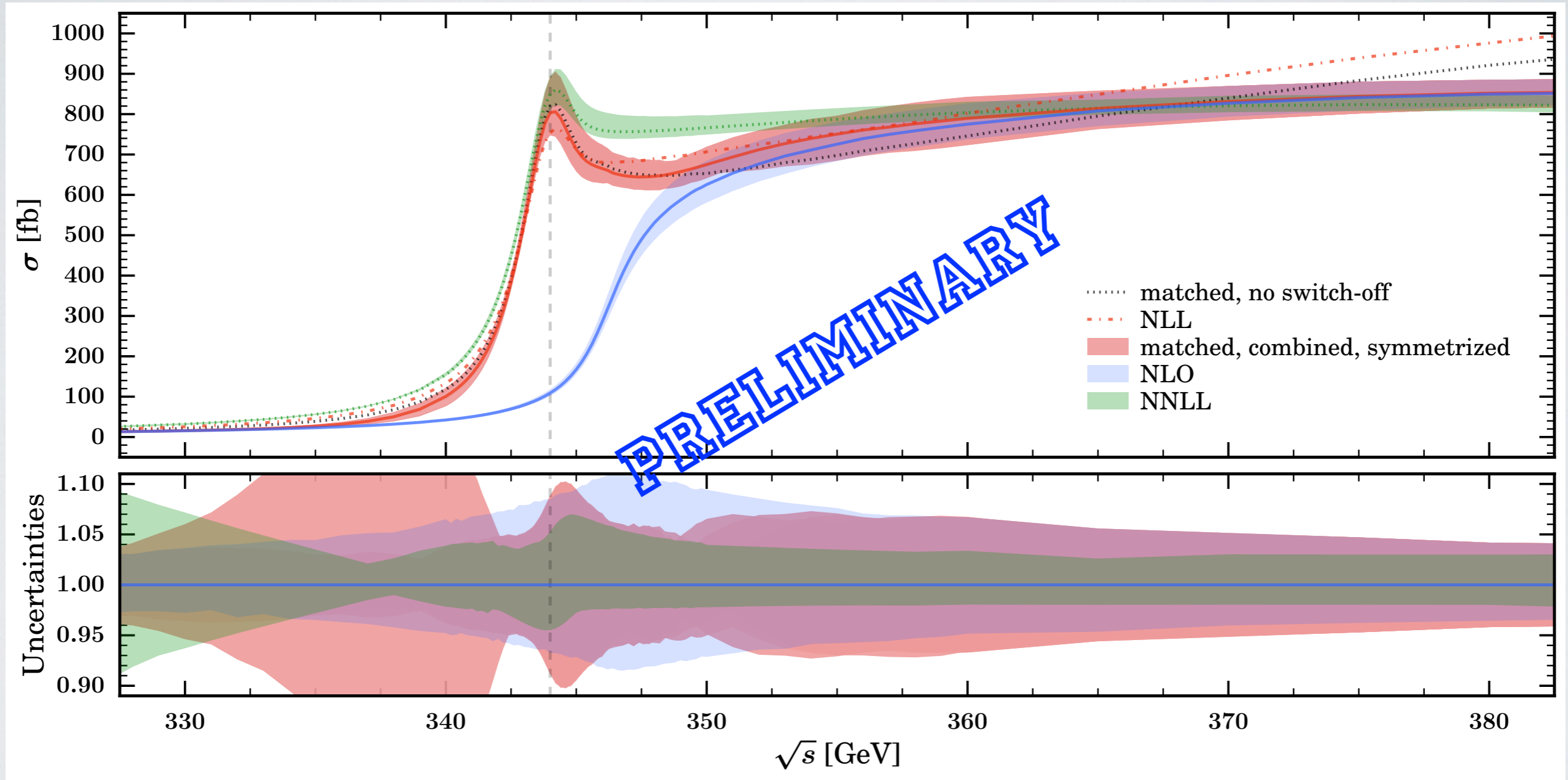




# Future Work ...

Next steps: higher QCD order, EW corrections (ISR matching!!), soft gluons ... ..

$$e^+e^- \rightarrow W^+bW^-\bar{b}$$





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- No intermediate files: direct communication between event records
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```

=====
Running self-test: whizard_lha
-----
Running test: whizard_lha_1
----- LHA initialization information -----
beam  kind  energy pdfgrp pdfset
A     2212  6500.000  -1    -1
B     2212  6500.000  -1    -1

Event weighting strategy = -3

Processes, with strategy-dependent cross section info
number  xsec (pb)  xerr (pb)  xmax (pb)
1       1.0000e+00  5.0000e-02  1.0000e+00
2       1.2000e+00  6.0000e-02  1.0000e+00
3       1.4000e+00  7.0000e-02  1.0000e+00
4       1.6000e+00  8.0000e-02  1.0000e+00
5       1.8000e+00  9.0000e-02  1.0000e+00

----- End LHA initialization information -----
... success.
Running test: whizard_lha_2
----- LHA initialization information -----
beam  kind  energy pdfgrp pdfset
A     2212  6500.000  -1    -1
B     2212  6500.000  -1    -1

Event weighting strategy = -3

Processes, with strategy-dependent cross section info
number  xsec (pb)  xerr (pb)  xmax (pb)
1       1.0000e+00  5.0000e-02  1.0000e+00

----- End LHA initialization information -----
----- LHA event information and listing -----

process =      1  weight =  1.0000e+00  scale =  1.0000e+03 (GeV)
           alpha_em =  7.8740e-03  alpha_strong =  1.0000e-01

Participating Particles
no  id  stat  mothers  colours  p_x  p_y  p_z  e  m  tau  spin
1   2011  -9    0  0  0.000  0.000  0.000  1.000  1.000  0.000  0.000
2   2012  -9    0  0  0.000  0.000  0.000  2.000  2.000  0.000  0.000
3    11  -1    1  0  0.000  0.000  0.000  4.000  4.000  0.000  0.000
4    12  -1    2  0  0.000  0.000  0.000  6.000  6.000  0.000  0.000
5    91   3    1  0  0.000  0.000  0.000  3.000  3.000  0.000  0.000
6    92   3    2  0  0.000  0.000  0.000  5.000  5.000  0.000  0.000
7     3   1    3  4  0.000  0.000  0.000  7.000  7.000  0.000  0.000
8     4   1    3  4  0.000  0.000  0.000  8.000  8.000  0.000  0.000
9     5   1    3  4  0.000  0.000  0.000  9.000  9.000  0.000  0.000

----- End LHA event information and listing -----

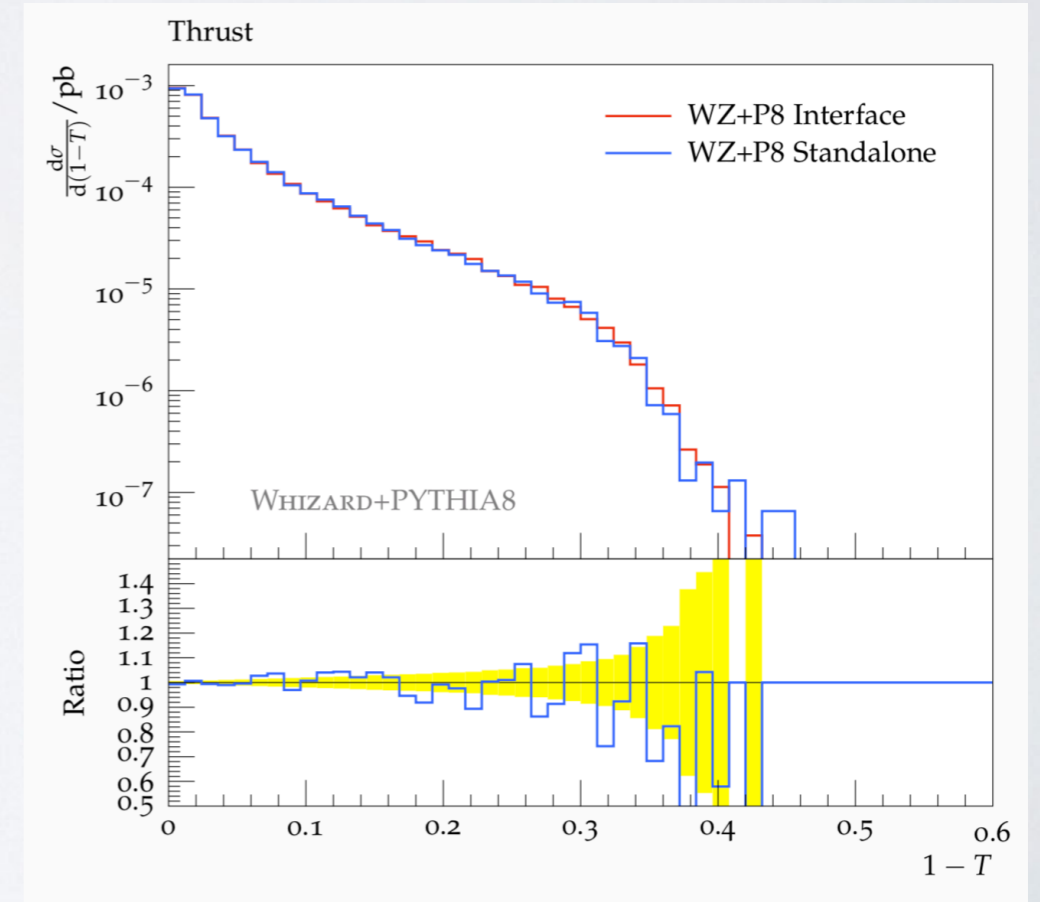
```

```

$shower_method = "PYTHIA8"
$hadronization_method = "PYTHIA8"

```

Allows to use the PYTHIA8 toolbox for matching





- ▶ Implemented by Wolfgang Kilian [on sabbatical at CERN w. CLICdp 03/2018-08/2018]
- ▶ Workspace subdirectory for GRID communication: job ID
- ▶ Pack and unpack features: transfers whole directories, relies on tar

```
./whizard --job_id "42" or
```

[actually for the integration grids!]

```
./whizard -J "42"
```

```
$grid_path = "<afs/.../>"
```

```
./whizard script1_tar.sin --pack my_workspace
```

script1\_tar.sin contains `$compile_workspace = "my_workspace"`

On the remote machine, you can run this with

```
./whizard script2_tar.sin --unpack my_workspace.tgz
```



- WHIZARD 2.7.0 event generator for collider physics (ee, pp, ep)
- High-multiplicity SM hard processes ( $2 \rightarrow 10$  etc.)
- Allows to simulate all possible BSM models
- Strong focus on  $e^+e^-$  physics: beam spectra,  $e^+e^-$  ISR, LCIO, polarizations
- NLO QCD (almost) done  $\rightarrow$  WHIZARD 3.0 [EW validation started]
- **NEW:**
  - ✓ UFO models: [WIP: still waiting for general Lorentz structures]
  - ✓ MPI parallel integration
  - ✓ Possibility to pre-set branching ratios for factorized processes
  - ✓ Resonance matching to parton shower
  - ✓ Fully integrated PYTHIA8 interface
  - ✓ Batch mode / gridpack functionality





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WE'RE HAPPY TO ACCOMODATE SPECIFIC DEMANDS OF FCC-EE COMMUNITY



# BACKUP







## Beam polarization, ILC-like setup

```
beams = e1, E1
beams_pol_density = @(-1), @(+1)
beams_pol_fraction = 80%, 30%
```

## Polarized decays: longitudinal Z

```
process zee = Z => e1, E1
beams = Z
beams_pol_density = @(0)
```

## Scan over polarizations

```
scan int h1 = (-1,1) {
  scan int h2 = (-1,1) {
    beams_pol_density = @(h1), @(h2)
    integrate (proc)
  }
}
```

## Asymmetric beams

```
beams = e1, E1
beams_momentum = 100 GeV, 900 GeV
```

## Beams with crossing angle

```
beams_momentum = 250 GeV, 250 GeV
beams_theta = 0, 10 degree
```

## Beams with rotated crossing angle

```
beams_momentum = 250 GeV, 250 GeV
beams_theta = 0, 10 degree
beams_phi = 0, 45 degree
```

## Structure functions (also concatenated)

```
beams = p, p => pdf_builtin
$pdf_builtin_set = "mmht2014lo"
```

```
beams = p, pbar => lhpdf
```

```
beams = e, p => none, pdf_builtin
```

```
beams = e1, E1 => circe1
$circe1_acc = "TESLA"
?circe1_generate = false
circe1_mapping_slope = 2
```

```
beams = e1, E1 => circe2 => isr => ewa
```

```
beams = e1, E1 => beam_events
$beam_events_file = "uniform_spread_2.5%.dat"
```



## Beam polarization

Spin $j$	Particle type	possible $m$ values
0	Scalar boson	0
1/2	Spinor	+1, -1
1	(Massive) Vector boson	+1, (0), -1
3/2	(Massive) Vectorspinor	+2, (+1), (-1), -2
2	(Massive) Tensor	+2, (+1), (0), (-1), -2

```
beams_pol_density = @(<spin entries>), @(<spin entries>)\nbeams_pol_fraction = <degree beam 1>, <degree beam 2>
```

## Different density matrices

```
beams_pol_density = @()
```

Unpolarized beams

$$\rho = \frac{1}{|m|} \mathbb{I}$$

$$\begin{aligned} |m| = 2 & \quad \text{massless} \\ |m| = 2j + 1 & \quad \text{massive} \end{aligned}$$

```
beams_pol_density = @(\pm j)\nbeams_pol_fraction = f
```

Circular polarization

$$\rho = \text{diag} \left( \frac{1 \pm f}{2}, 0, \dots, 0, \frac{1 \mp f}{2} \right)$$

```
beams_pol_density = @(\theta)\nbeams_pol_fraction = f
```

Longitudinal polarization (massive)

$$\rho = \text{diag} \left( \frac{1-f}{|m|}, \dots, \frac{1-f}{|m|}, \frac{1+f(|m|-1)}{|m|}, \frac{1-f}{|m|}, \dots, \frac{1-f}{|m|} \right)$$

```
beams_pol_density = @(\j, -j, j:-j:\exp(-I*\phi))\nbeams_pol_fraction = f
```

Transversal polarization (along an axis)

$$\rho = \begin{pmatrix} 1 & 0 & \dots & \dots & \frac{f}{2} e^{-i\phi} \\ 0 & 0 & \ddots & & 0 \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ 0 & & \ddots & 0 & 0 \\ \frac{f}{2} e^{i\phi} & \dots & \dots & 0 & 1 \end{pmatrix}$$

```
beams_pol_density = @(\j:j:1-\cos(\theta),\nj:-j:\sin(\theta)*\exp(-I*\phi), -j:-j:1+\cos(\theta))\nbeams_pol_fraction = f
```

Polarization along arbitrary axis ( $\theta, \Phi$ )

$$\rho = \frac{1}{2} \cdot \begin{pmatrix} 1 - f \cos \theta & 0 & \dots & \dots & f \sin \theta e^{-i\phi} \\ 0 & 0 & \ddots & & 0 \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ 0 & & \ddots & 0 & 0 \\ f \sin \theta e^{i\phi} & \dots & \dots & 0 & 1 + f \cos \theta \end{pmatrix}$$

```
beams_pol_density = @(\j:j:h_j, j-1:j-1:h_{j-1}, \dots, -j:-j:h_{-j})
```

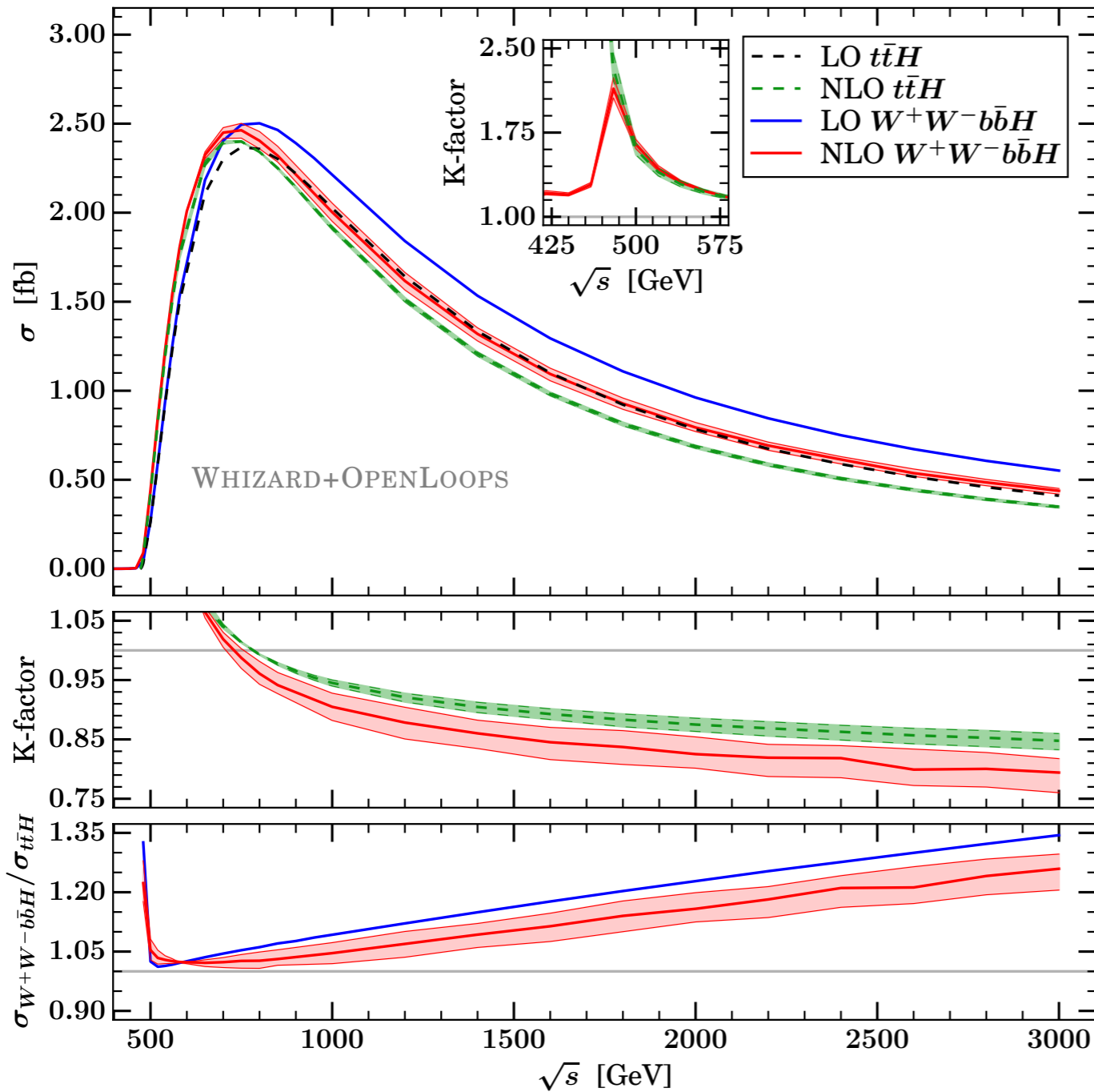
```
beams_pol_density = @(\{m:m':x_{m,m'}\})
```

Diagonal / arbitrary density matrices



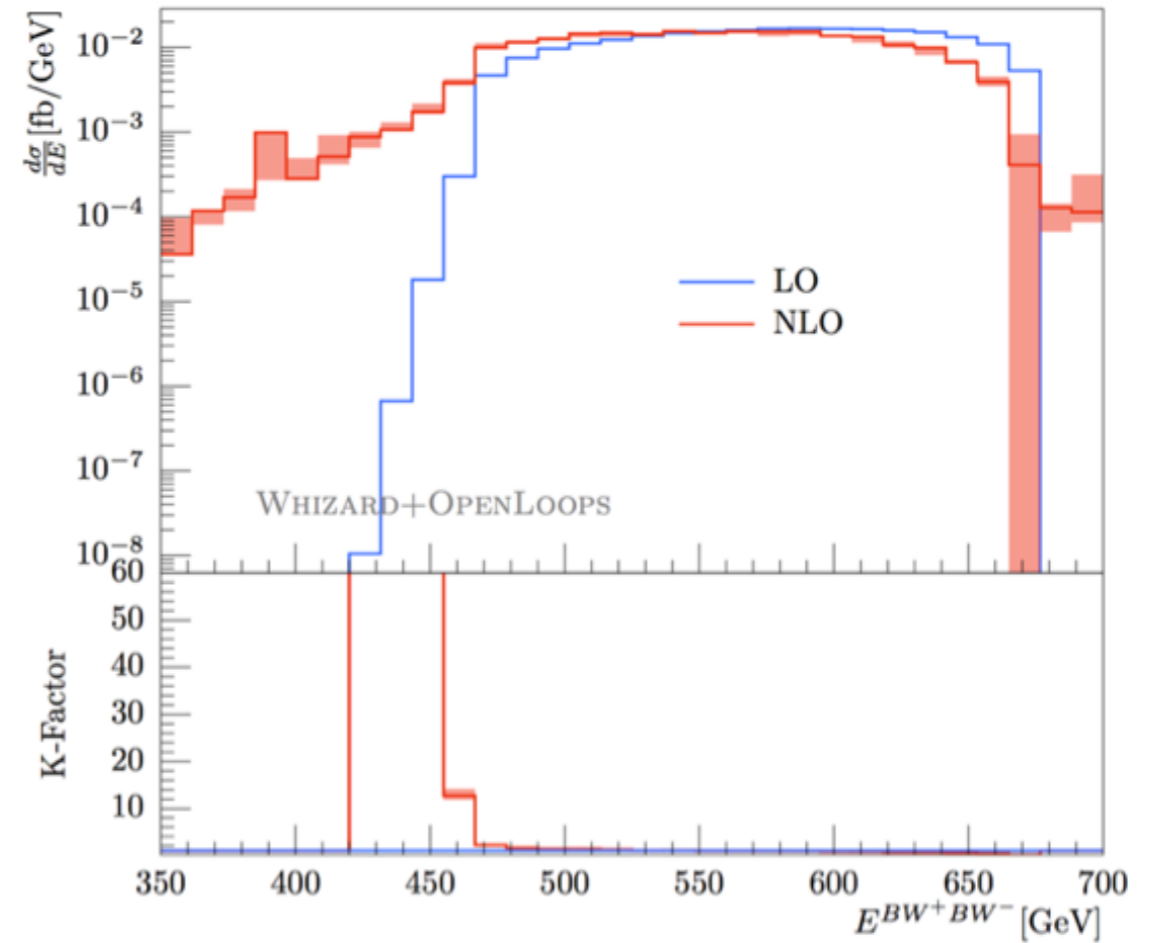
# NLO QCD Results for off-shell $e^+e^- \rightarrow ttH$

$e^+e^- \rightarrow t\bar{t}H$  and  $e^+e^- \rightarrow W^+W^-b\bar{b}H$



Chokoufé/Kilian/Lindert/Pozzorini/JRR/Weiss, 1609.03390

$e^+e^- \rightarrow W^+bW^-b\bar{b}H, N_{\text{jets}} \geq 2, \sqrt{s} = 800\text{GeV}$

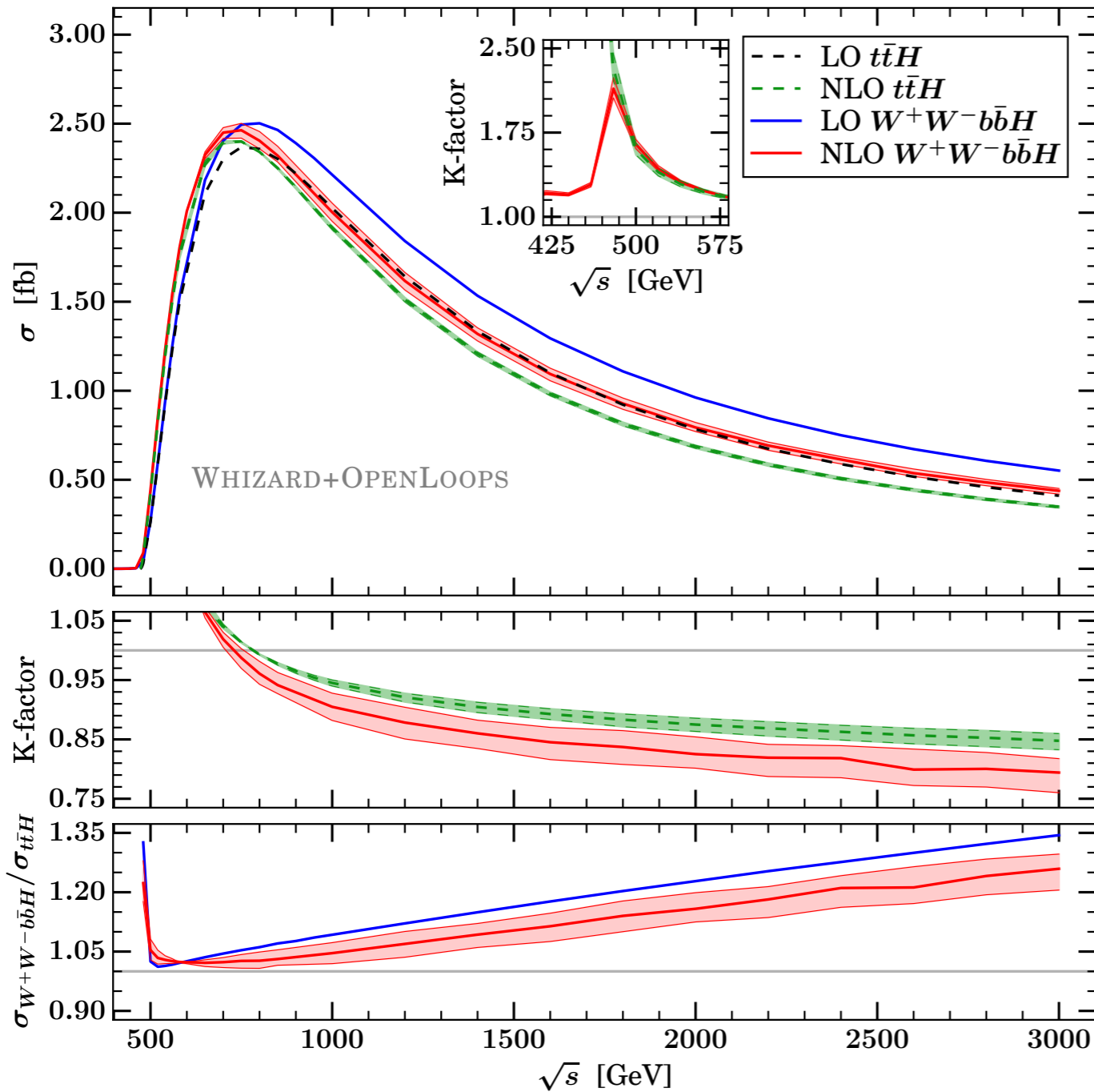


$\sqrt{s}$ [GeV]	$e^+e^- \rightarrow t\bar{t}H$			$e^+e^- \rightarrow W^+W^-b\bar{b}H$		
	$\sigma^{\text{LO}}$ [fb]	$\sigma^{\text{NLO}}$ [fb]	K-factor	$\sigma^{\text{LO}}$ [fb]	$\sigma^{\text{NLO}}$ [fb]	K-factor
500	0.26	$0.42^{+3.6\%}_{-3.1\%}$	1.60	0.27	$0.44^{+2.6\%}_{-2.4\%}$	1.63
800	2.36	$2.34^{+0.1\%}_{-0.1\%}$	0.99	2.50	$2.40^{+2.1\%}_{-1.9\%}$	0.96
1000	2.02	$1.91^{+0.5\%}_{-0.5\%}$	0.95	2.21	$2.00^{+2.5\%}_{-2.5\%}$	0.90
1400	1.33	$1.21^{+0.9\%}_{-1.0\%}$	0.90	1.53	$1.32^{+2.6\%}_{-3.0\%}$	0.86
3000	0.41	$0.35^{+1.4\%}_{-1.8\%}$	0.84	0.55	$0.44^{+2.9\%}_{-4.3\%}$	0.79

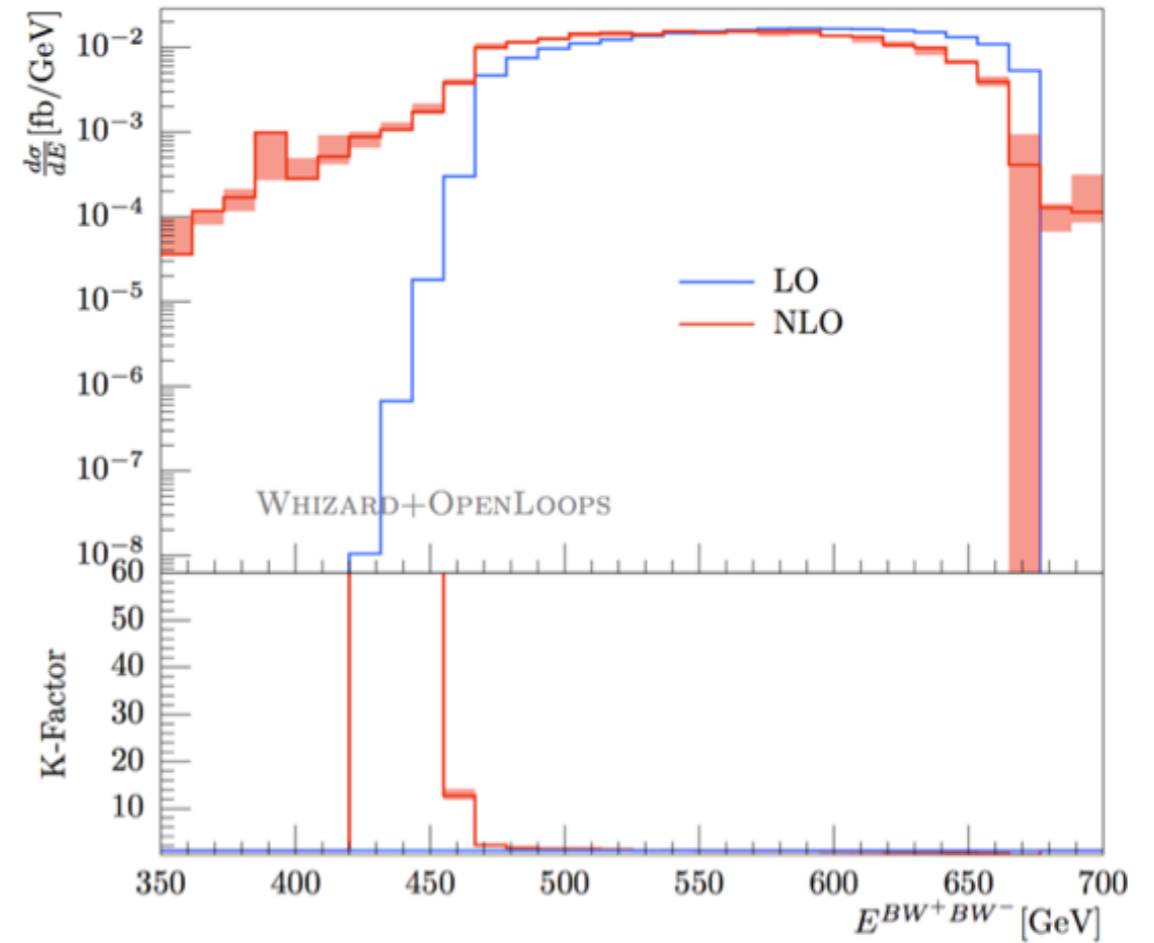




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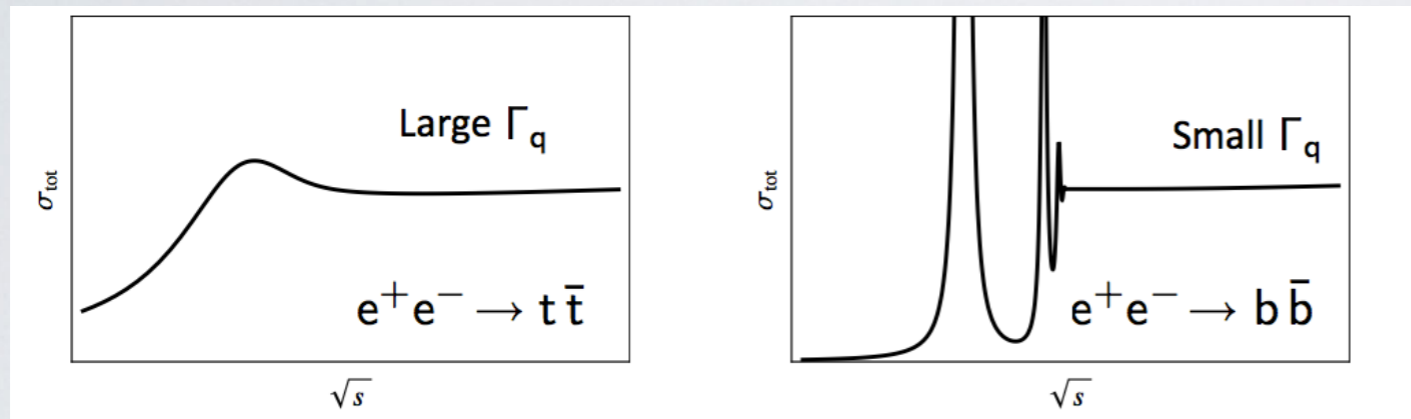




# Top Threshold/Continuum at lepton colliders

- Top threshold scan best-known method to measure top quark mass,  $\Delta M \sim 30\text{-}70 \text{ MeV}$
- Continuum top production best-known method to measure top couplings

Heavy quark production at lepton colliders, qualitatively:

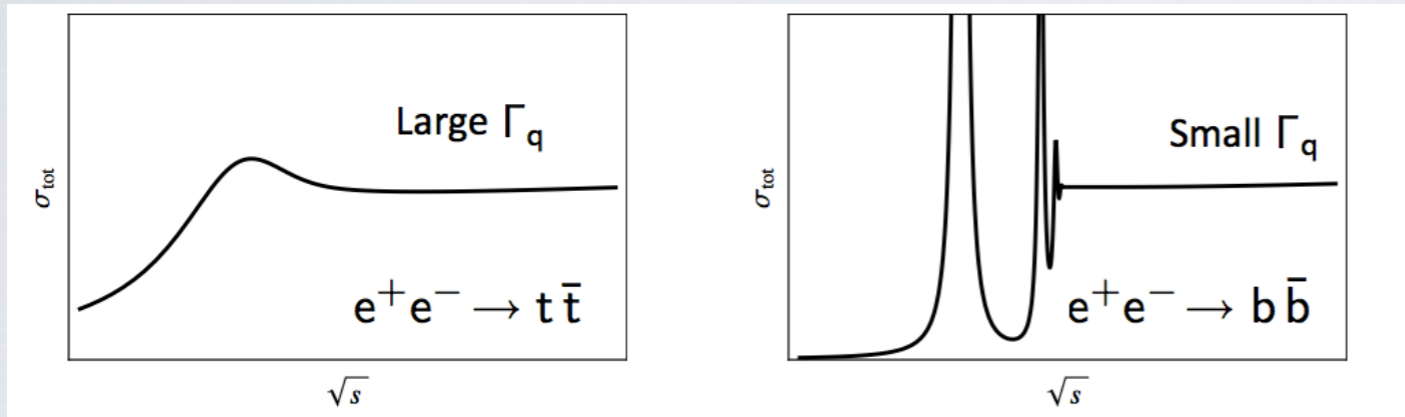




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error source	$\Delta m_t^{\text{PS}}$ [MeV]
stat. error (200 fb <sup>-1</sup> )	13
theory (NNNLO scale variations, PS scheme)	40
parametric ( $\alpha_s$ , current WA)	35
non-resonant contributions (such as single top)	< 40
residual background / selection efficiency	10 – 20
luminosity spectrum uncertainty	< 10
beam energy uncertainty	< 17
combined theory & parametric	30 – 50
combined experimental & backgrounds	25 – 50
total (stat. + syst.)	40 – 75

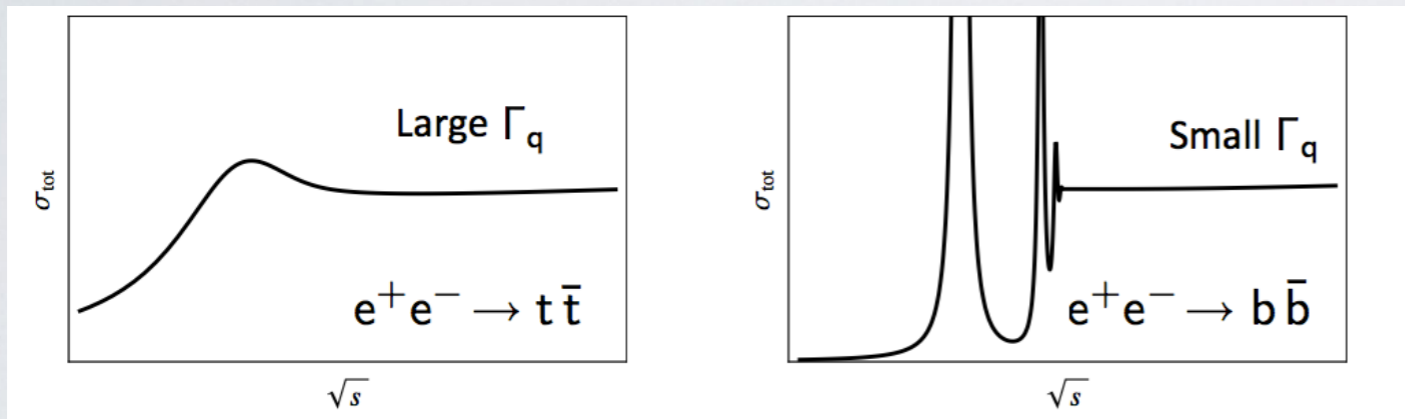
from 1702.05333



# Top Threshold/Continuum at lepton colliders

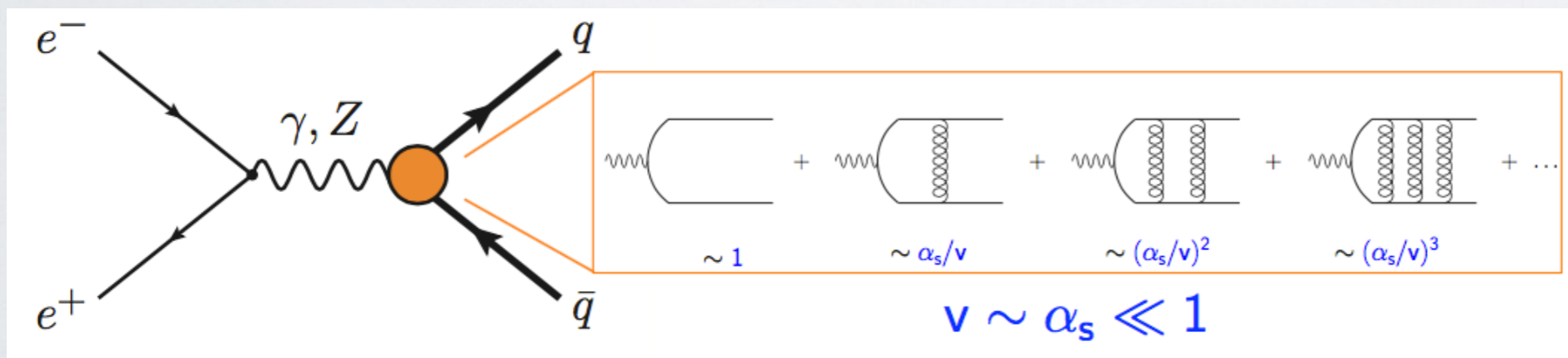
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Threshold region: top velocity  $v \sim \alpha_s \ll 1$  non-relativistic EFT: (v)NRQCD from 1702.05333



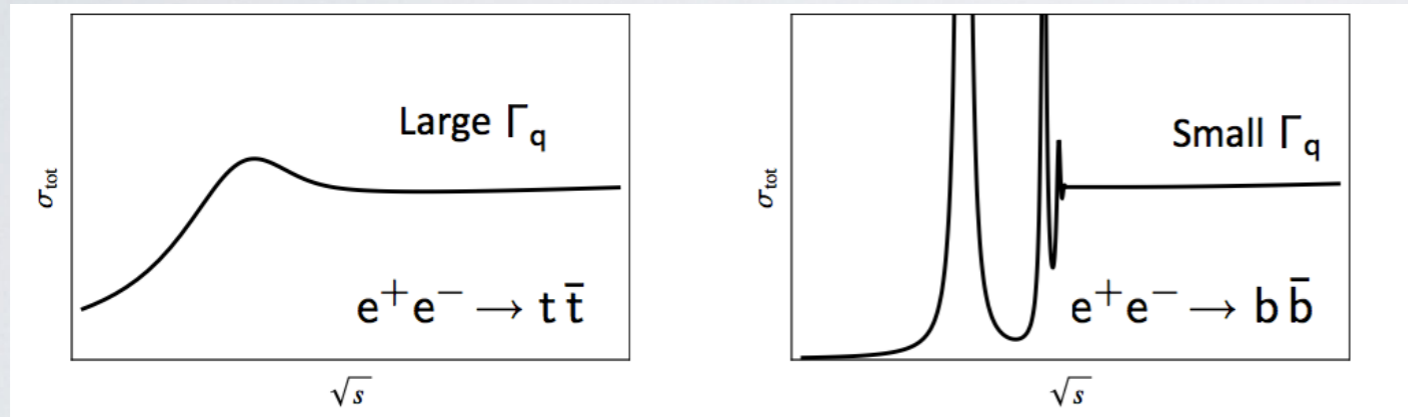
Continuum region: “standard” fixed-order QCD



# Top Threshold/Continuum at lepton colliders

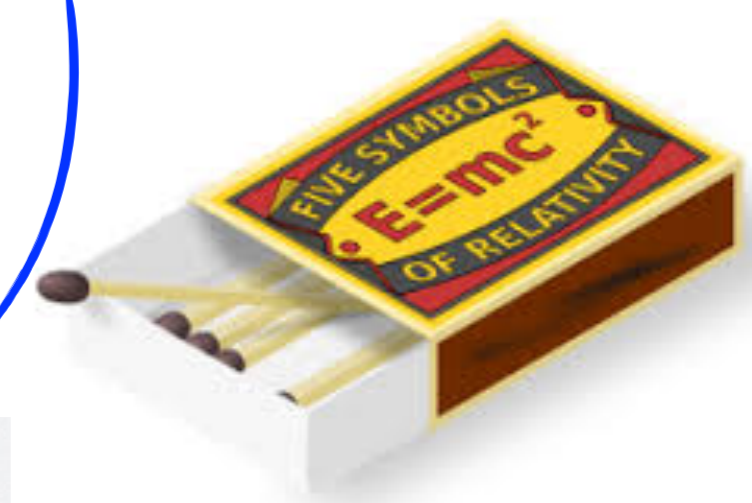
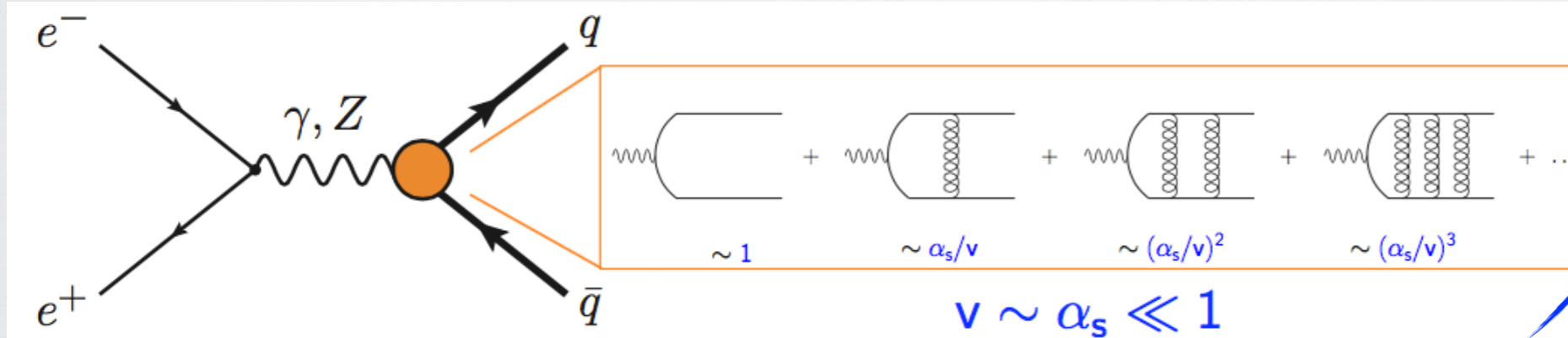
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MATCH



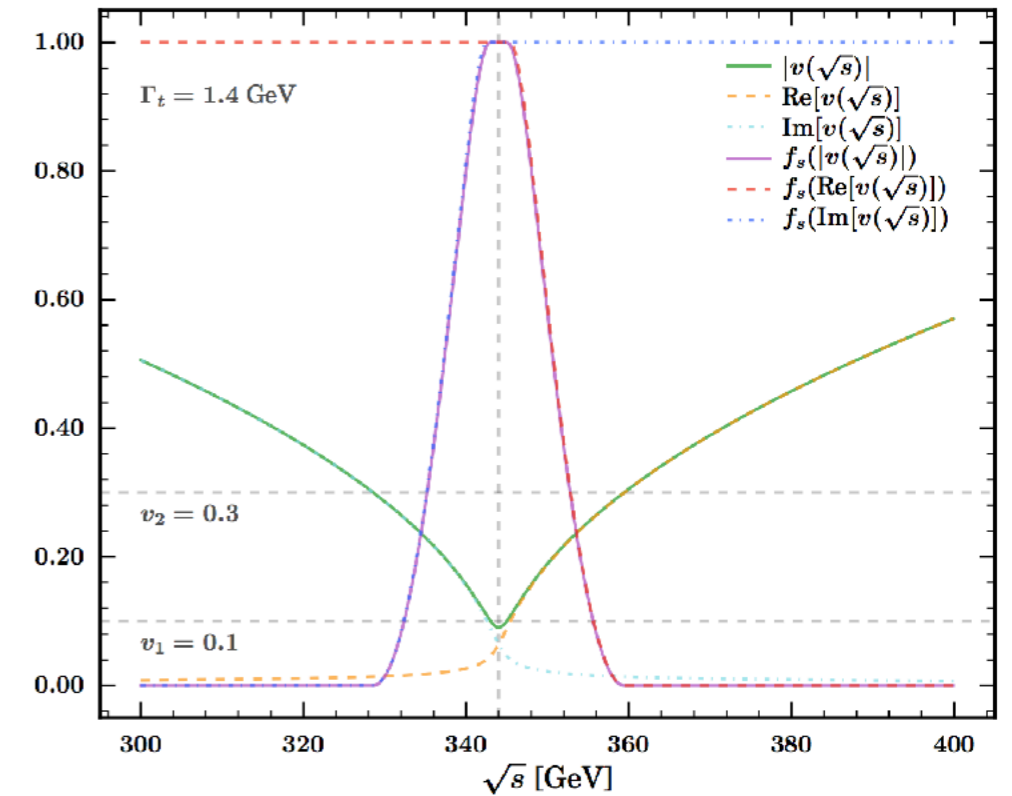




# Top threshold: validation and matching

- Transition region between relativistic and resummation effects

$$\begin{aligned}
 \sigma_{\text{NLO+NLL}} = & \sigma_{\text{NLO}} + \left( \tilde{F}_{\text{NLL}} - \tilde{F}_{\text{NLL}}^{\text{exp}} \right) \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \rightarrow \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} W^+ \\ \phantom{W^+} \\ \phantom{W^+} \\ W^- \end{array} \right) \left( \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \right) \\
 & + \left| \tilde{F}_{\text{NLL}} \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \rightarrow \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \right|^2 \\
 & + \left\{ \tilde{F}_{\text{NLL}} \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \rightarrow \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} W^+ \\ \phantom{W^+} \\ \phantom{W^+} \\ W^- \end{array} \right) \left( \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \right) \right. \\
 & \left. + \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \rightarrow \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} W^+ \\ \phantom{W^+} \\ \phantom{W^+} \\ W^- \end{array} \right) \left( \begin{array}{c} b \\ \phantom{b} \\ \phantom{b} \\ \bar{b} \end{array} \right) \left( \begin{array}{c} e^+ \\ \phantom{e^+} \\ \phantom{e^+} \\ e^- \end{array} \right) \right. \\
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 \end{aligned}$$



$$\begin{aligned}
 \sigma_{\text{matched}} = & \sigma_{\text{FO}}[\alpha_H] + \sigma_{\text{NRQCD}}^{\text{full}}[f_s \alpha_H, f_s \alpha_S, f_s \alpha_{US}] \\
 & - \sigma_{\text{NRQCD}}^{\text{expanded}}[f_s \alpha_H, f_s \alpha_H],
 \end{aligned}$$

Smoothstep matching function:

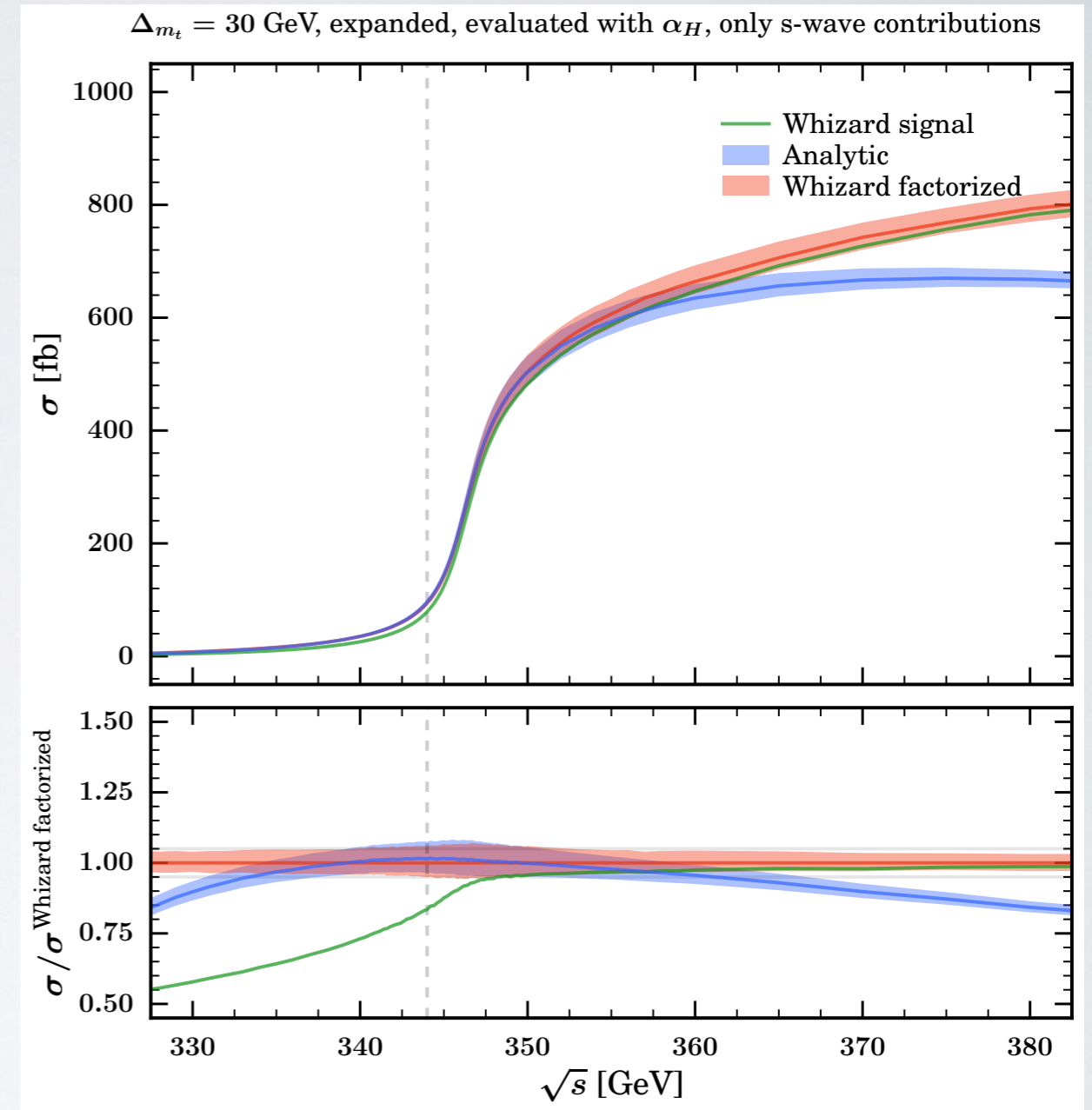
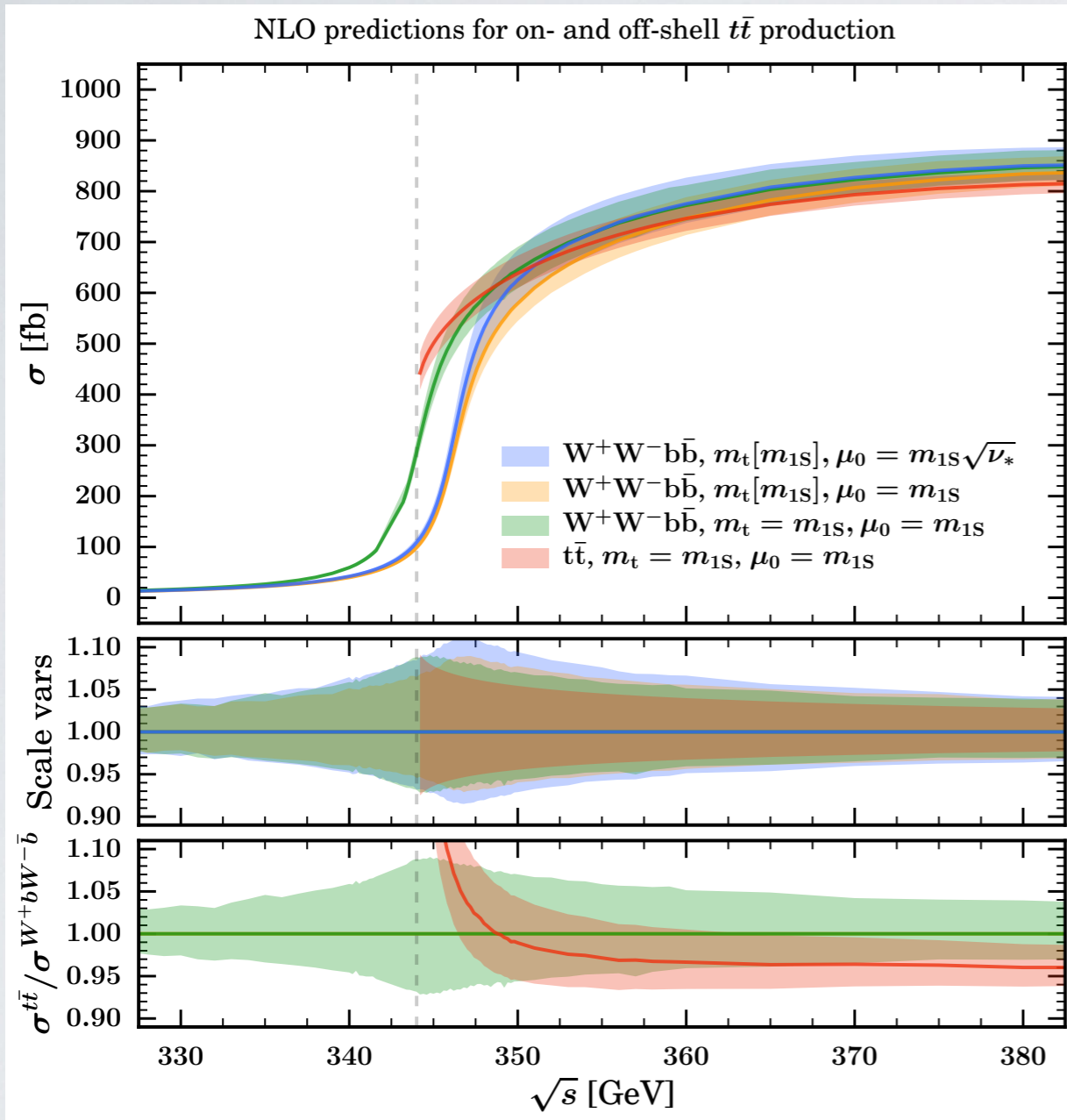
$$f_s(v) = \begin{cases} 1 & v < v_1 \\ 1 - 3 \left( \frac{v-v_1}{v_2-v_1} \right)^2 - 2 \left( \frac{v-v_1}{v_2-v_1} \right)^3 & v_1 \leq v \leq v_2 \\ 0 & v > v_2 \end{cases}$$

Chokouf /Hoang/Kilian/JRR/Stahlhofen/  
Teubner/Weiss, 1712.02220





# Top threshold: validation and matching



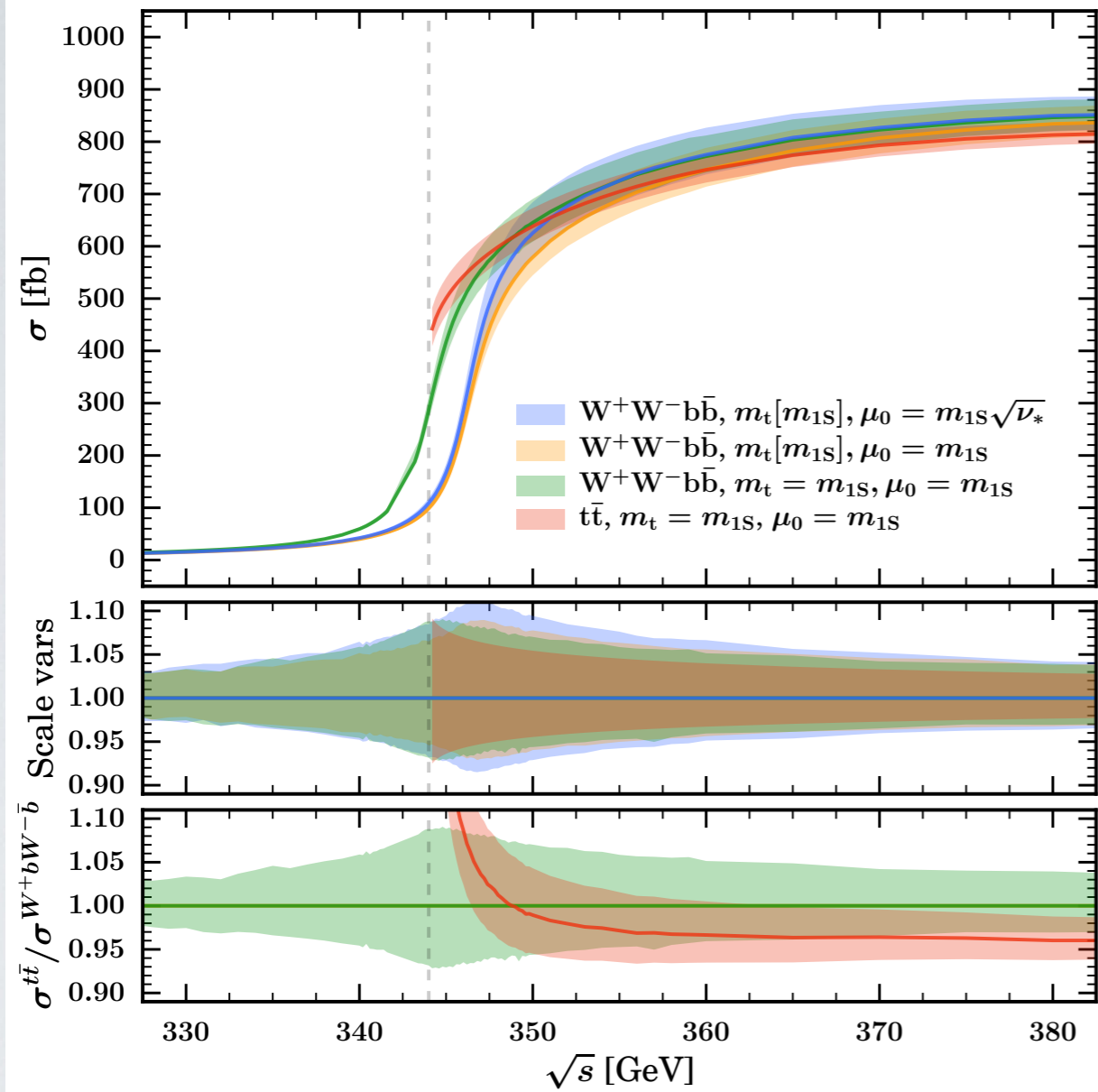
Bach/Chokouf /Hoang/Kilian/JRR/Stahlhofen/Teubner/Weiss, 1712.02220



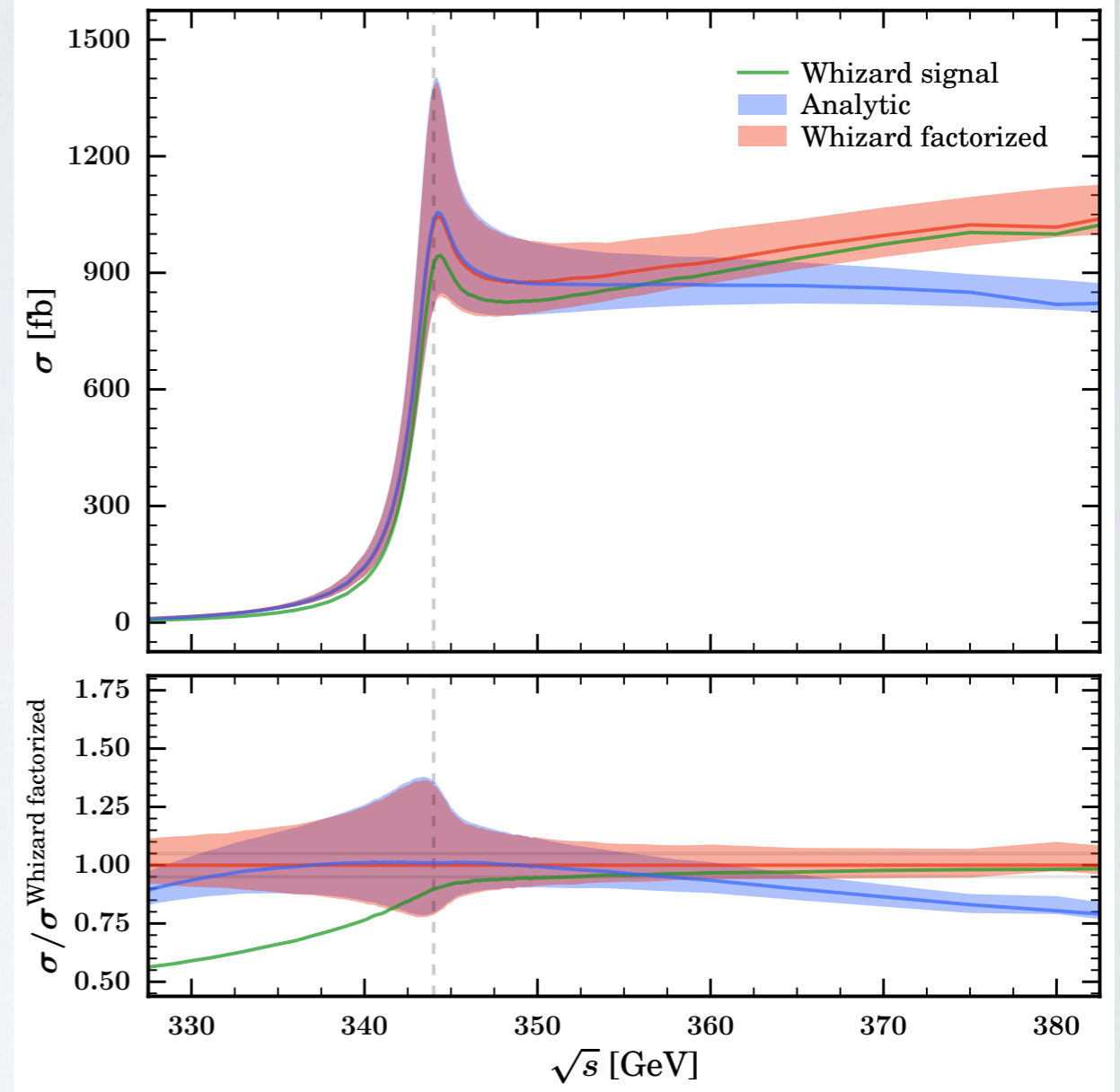


# Top threshold: validation and matching

NLO predictions for on- and off-shell  $t\bar{t}$  production



$\Delta_{m_t} = 30$  GeV, LL, only s-wave contributions



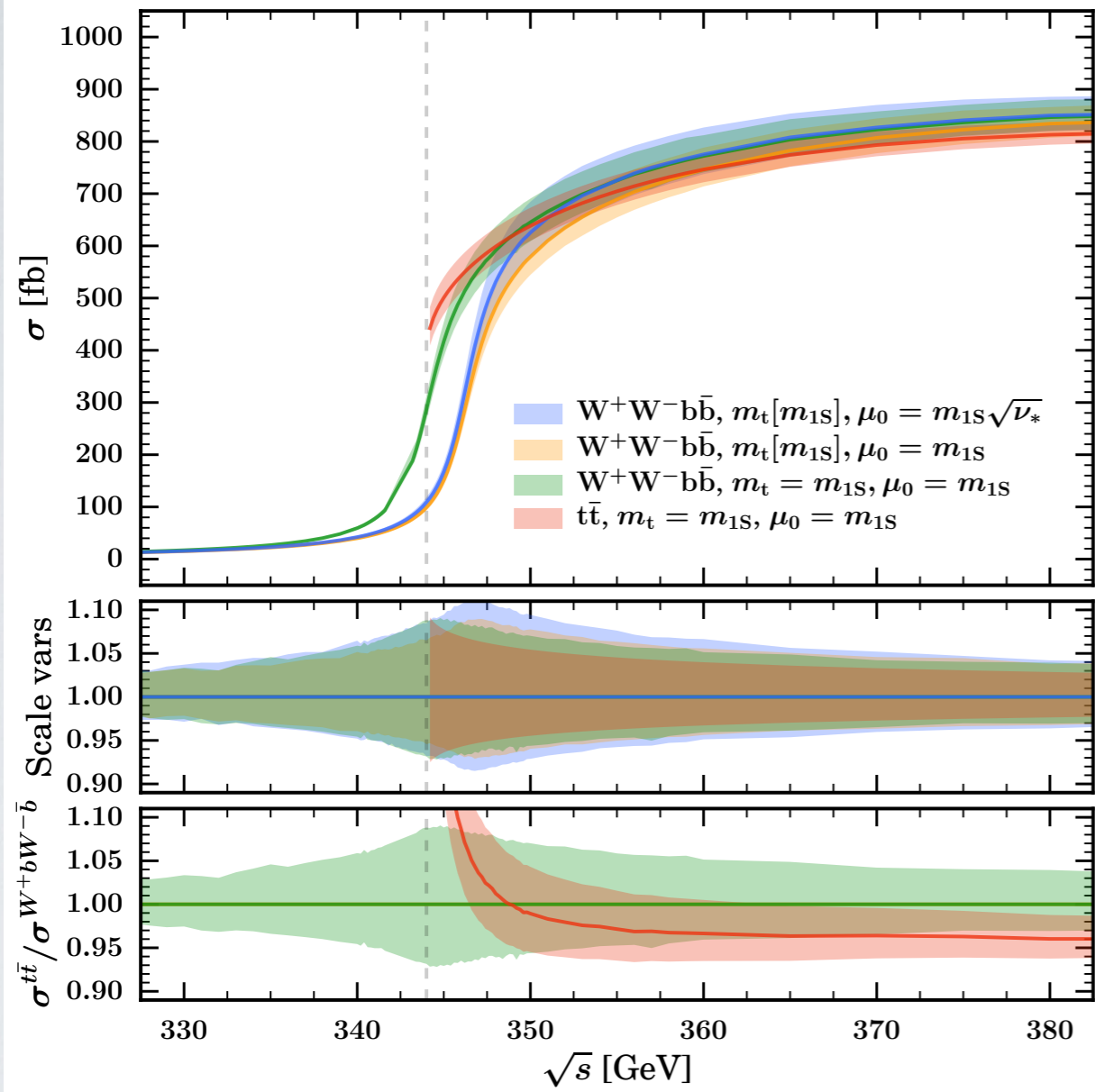
Bach/Chokouf /Hoang/Kilian/JRR/Stahlhofen/Teubner/Weiss, 1712.02220



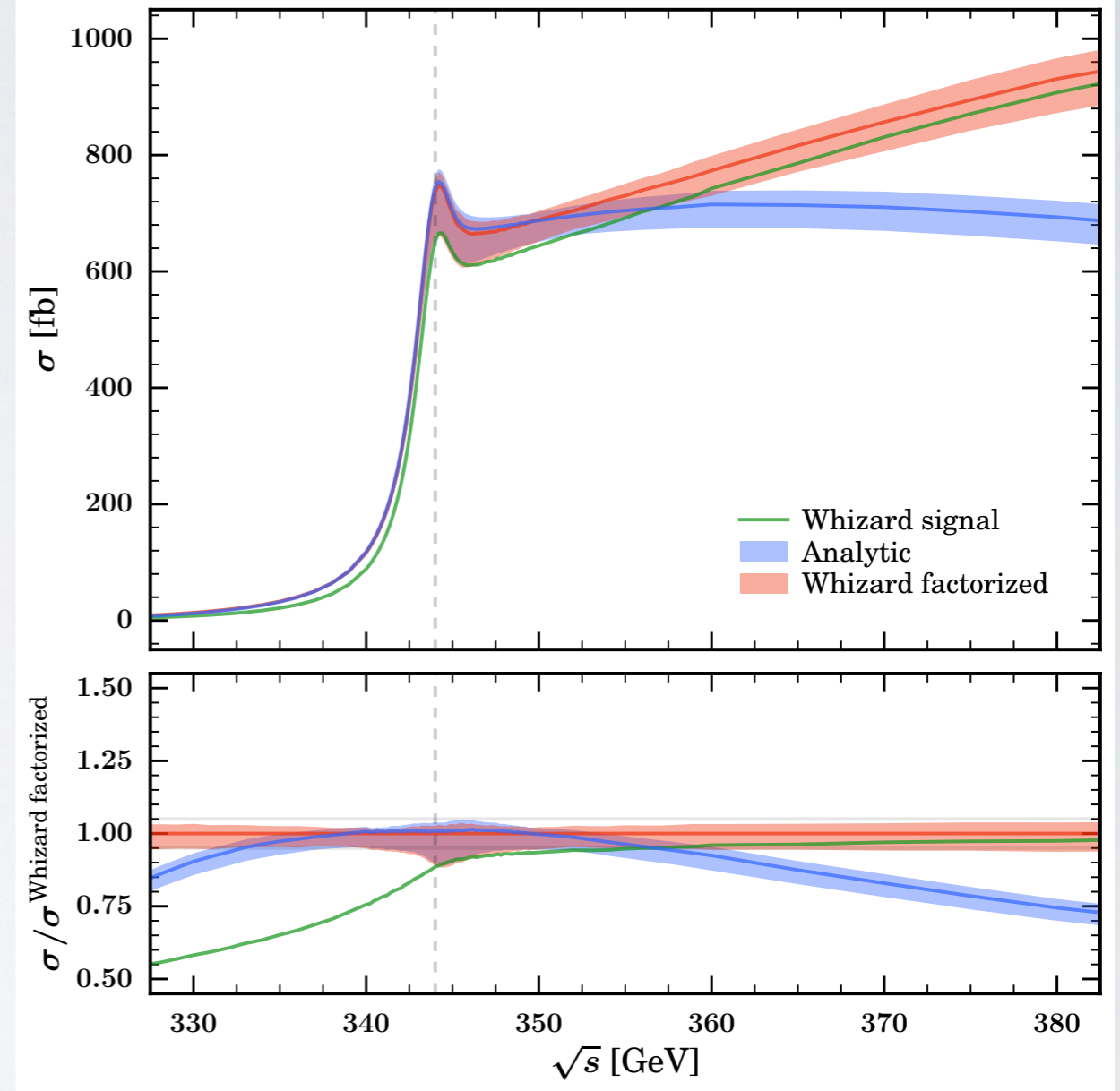


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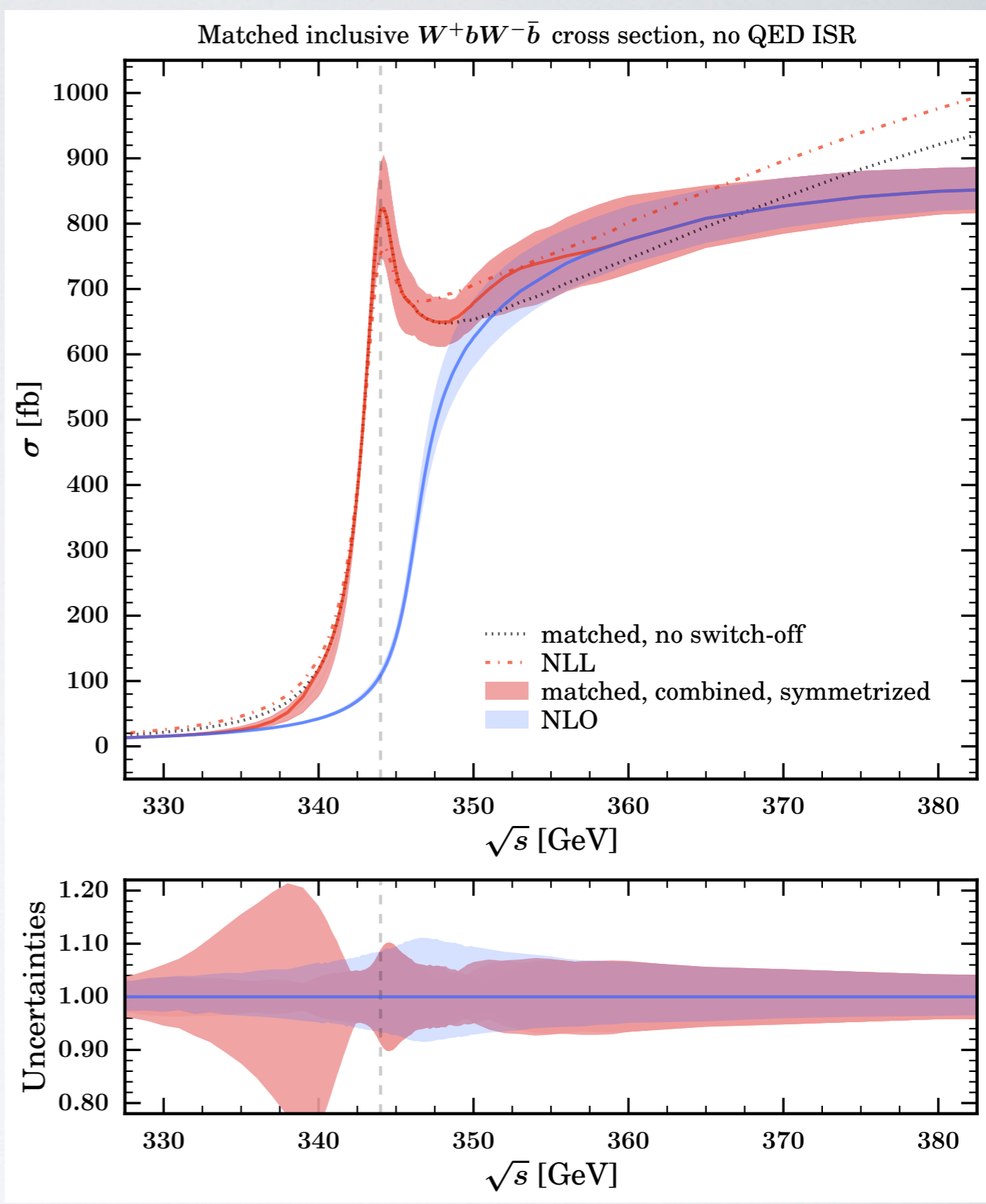
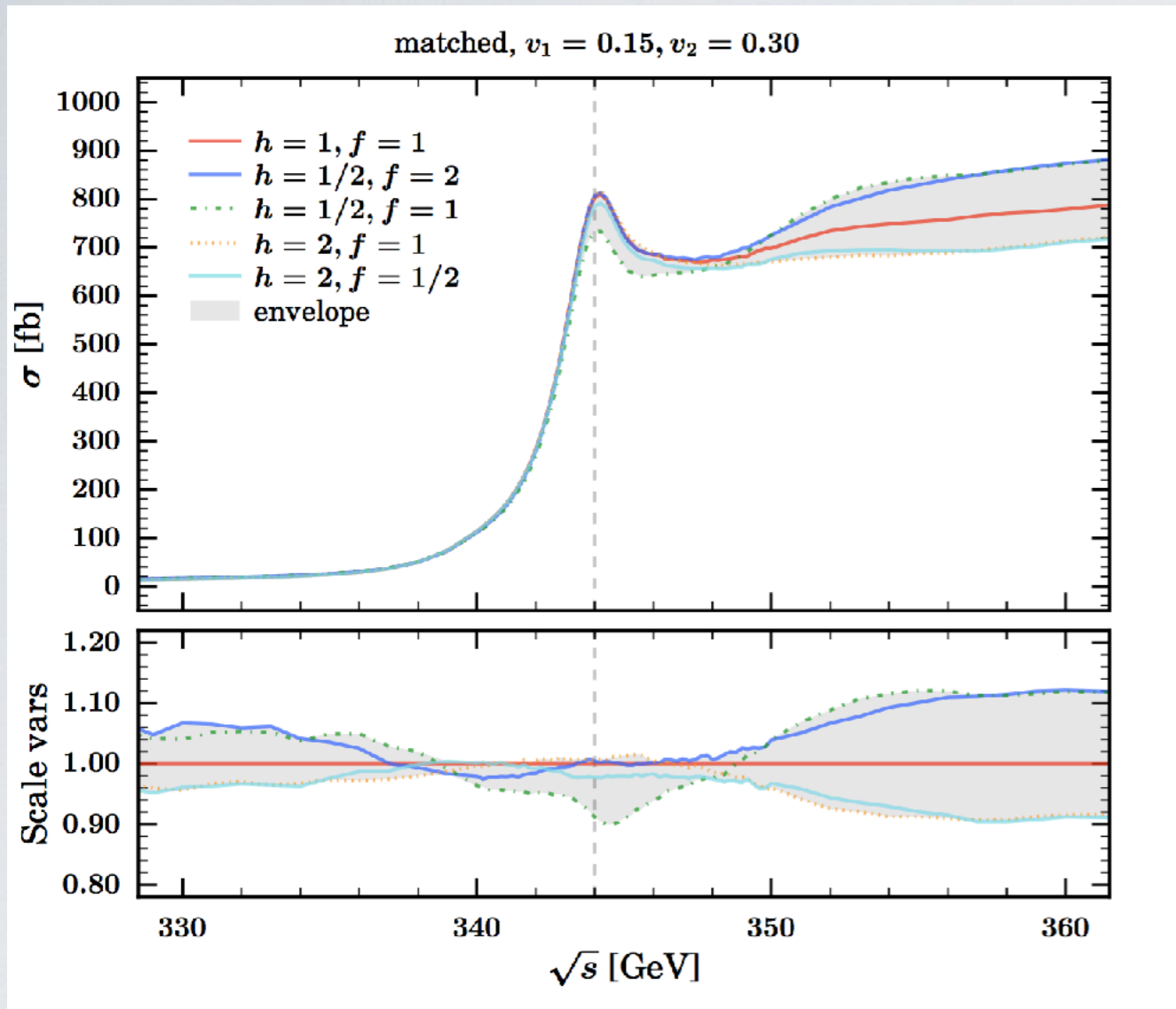


Bach/Chokouf /Hoang/Kilian/JRR/Stahlhofen/Teubner/Weiss, 1712.02220





# Matching threshold NLL to continuum NLO



Total uncertainty:  $h$ - $f$  variation band and matching [switch-off function]

Symmetrization of error bands:

$$\sigma_{\max} = \max \left[ \max_{i \in \text{HF}} \sigma_i, \sigma_0 + (\sigma_0 - \min_{i \in \text{HF}} \sigma_i) \right]$$

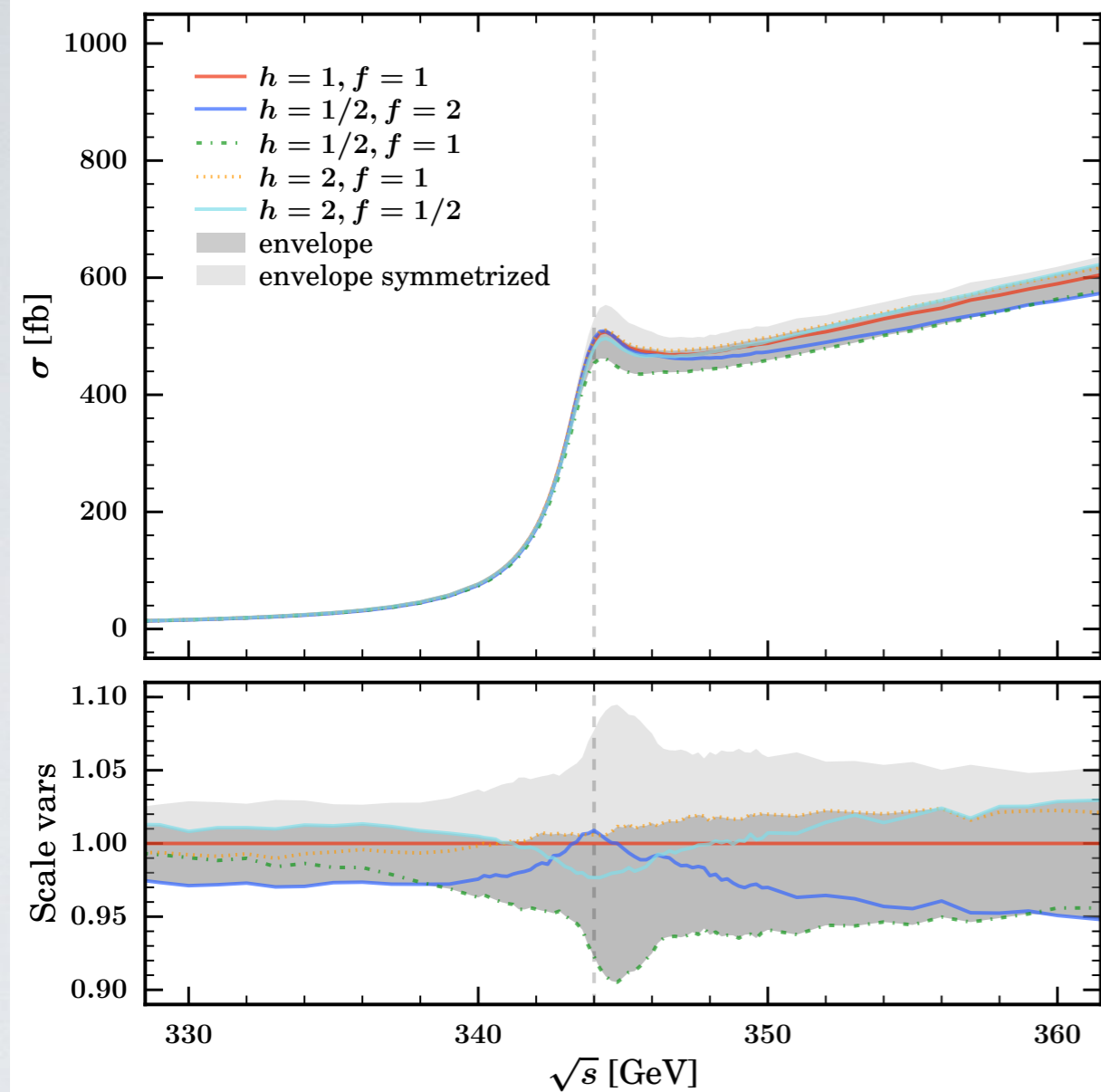
$$\sigma_{\min} = \min \left[ \min_{i \in \text{HF}} \sigma_i, \sigma_0 - (\max_{i \in \text{HF}} \sigma_i - \sigma_0) \right]$$



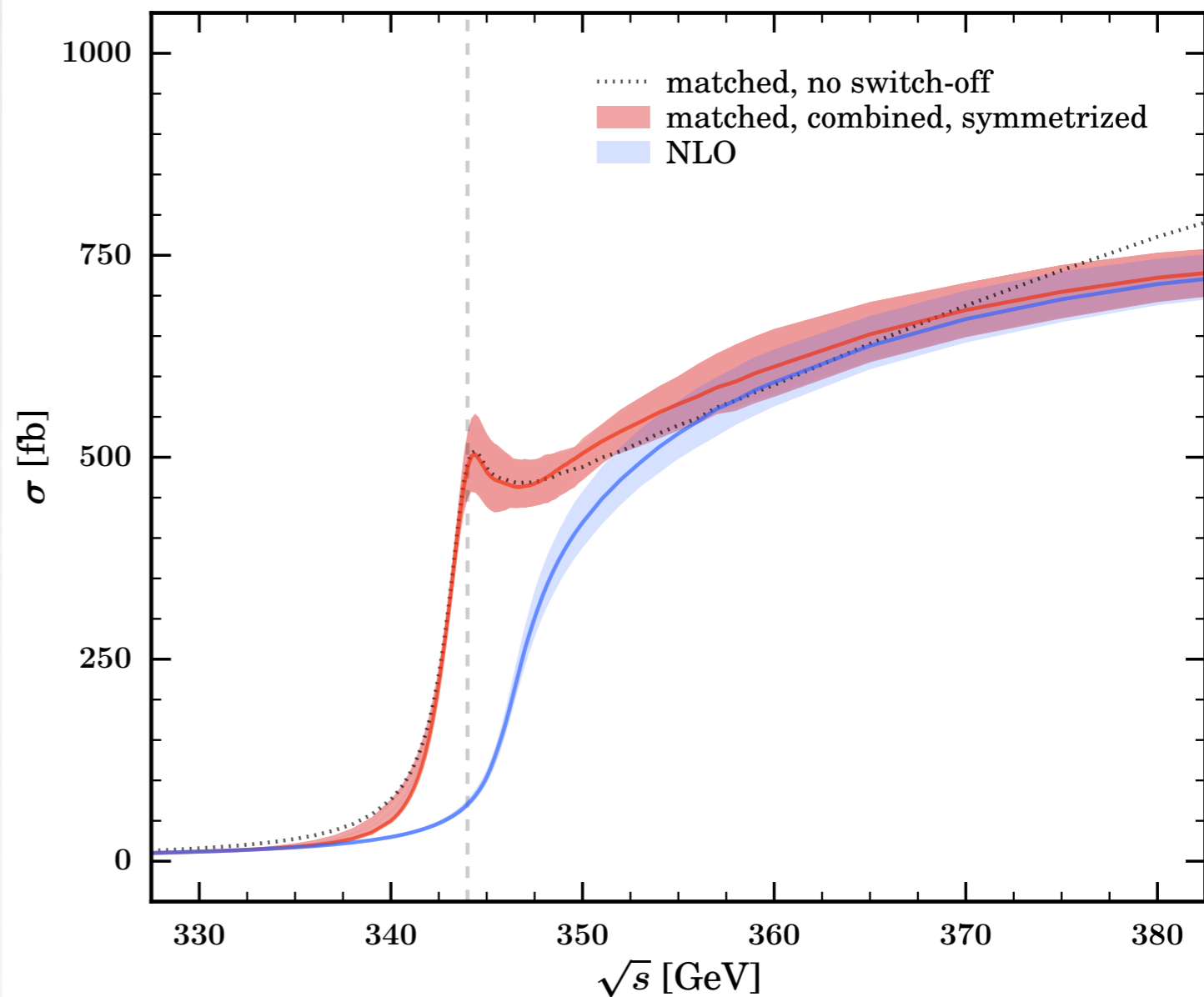


# Threshold matching with QED ISR

matched, no switch-off



Matched inclusive  $W^+bW^-\bar{b}$  cross section, with QED ISR





# Matched threshold differential distributions

