

$e^+e^- \rightarrow \gamma\gamma$ at large angle for FCC-ee luminometry

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with M. Chiesa, G. Montagna, O. Nicosini, F. Piccinini

- ↪ Introduction
- ↪ $e^+e^- \rightarrow \gamma\gamma$ at large angle at FCC-ee for luminometry
 - ↪ Why $e^+e^- \rightarrow \gamma\gamma$? Advantages and disadvantages (theoretical point of view)
- ↪ The BabaYaga event generator
 - ↪ Sketch of its theoretical formulation
- ↪ Exploratory study and phenomenology of QED/EWK radiative corrections (NLO and higher orders)
- ↪ A few considerations on achievable theoretical accuracy
- ↪ Conclusions

Reference processes for luminosity

- Instead of getting the luminosity from machine parameters, it's more effective and precise to exploit the relation

$$\sigma = \frac{N}{L} \quad \rightarrow \quad L = \frac{N_{\text{ref}}}{\sigma_{\text{theory}}} \quad \frac{\delta L}{L} = \frac{\delta N_{\text{ref}}}{N_{\text{ref}}} \oplus \frac{\delta \sigma_{\text{theory}}}{\sigma_{\text{theory}}}$$

- Reference (*normalization*) processes are required to have a clean topology, high statistics and **be calculable with high theoretical accuracy**
- QED processes are golden processes to push theo. accuracy at the [sub-]permill level
 - ★ At LEP: small-angle $e^+e^- \rightarrow e^+e^-$ (Bhabha)
(mainly t -channel γ exchange, tiny Z “contamination”)
 - ★ At flavour factories: large-angle QED processes
Bhabha, $e^+e^- \rightarrow \gamma\gamma$, $e^+e^- \rightarrow \mu^+\mu^-$
- At FCC-ee, Bhabha will still be the reference process, $e^+e^- \rightarrow \gamma\gamma$ worth being studied

S. Jadach *et al.*, arXiv:1812.01004 [hep-ph] and A. Blondel *et al.*, arXiv:1809.01830 [hep-ph]

↪ **Inclusion of Radiative Corrections is mandatory (in particular QED RC)**

↪ **Fully-fledged Monte Carlo event generators needed**

- Fully-exclusive generator developed for QED processes at flavour factories
- It simulates **Bhabha**, $e^+e^- \rightarrow \mu^+\mu^-$, $e^+e^- \rightarrow \gamma\gamma$ at large angles
- Theoretical accuracy at 0.1% (or slightly better) for integrated cross sections for luminosity monitoring
- Based on an *in-house* implementation of a **QED Parton-Shower**, *consistently matched with exact QED NLO RCs*
 - ↪ An arbitrary number of (extra) photons can be generated
- The same QED PS & NLO matching framework successfully applied also to Drell-Yan processes (**HORACE**) and $H \rightarrow 4\ell$ (**Hto4l**)

CMCC *et al.*, JHEP 0710 (2007) 109; CMCC *et al.*, JHEP 0612 (2006) 016; S. Boselli *et al.*, JHEP 1506 (2015) 023
- ★ One of the few generators to implement $e^+e^- \rightarrow \gamma\gamma$, with exact QED NLO & resummation (to the best of my knowledge)

see also S. Eidelman *et al.*, EPJC **71** (2011) 1597 (MCGPJ generator)

★ Webpage

<http://www.pv.infn.it/hepcomplex/babayaga.html>

or better ask the authors!

★ BabaYaga core references:

- Barzè *et al.*, Eur. Phys. J. C **71** (2011) 1680
- Balossini *et al.*, Phys. Lett. **663** (2008) 209
- Balossini *et al.*, Nucl. Phys. **B758** (2006) 227
- CMCC *et al.*, Nucl. Phys. Proc. Suppl. **131** (2004) 48
- CMCC, Phys. Lett. B **520** (2001) 16
- CMCC *et al.*, Nucl. Phys. B **584** (2000) 459

BabaYaga with a dark photon

BabaYaga@NLO for $e^+e^- \rightarrow \gamma\gamma$

BabaYaga@NLO for Bhabha

BabaYaga@NLO

improved PS BabaYaga

BabaYaga

★ Related work:

- S. Actis *et al.*
“Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data”, Eur. Phys. J. C **66** (2010) 585
Report of the Working Group on Radiative Corrections and Monte Carlo Generators for Low Energies
- CMCC *et al.*, JHEP **1107** (2011) 126
NNLO massive pair corrections

Why $e^+e^- \rightarrow \gamma\gamma$ at FCC-ee? Pros and cons

see also M. Dam's talks at this workshop on Tuesday,
at FCC-ee week, Rome, April 2016

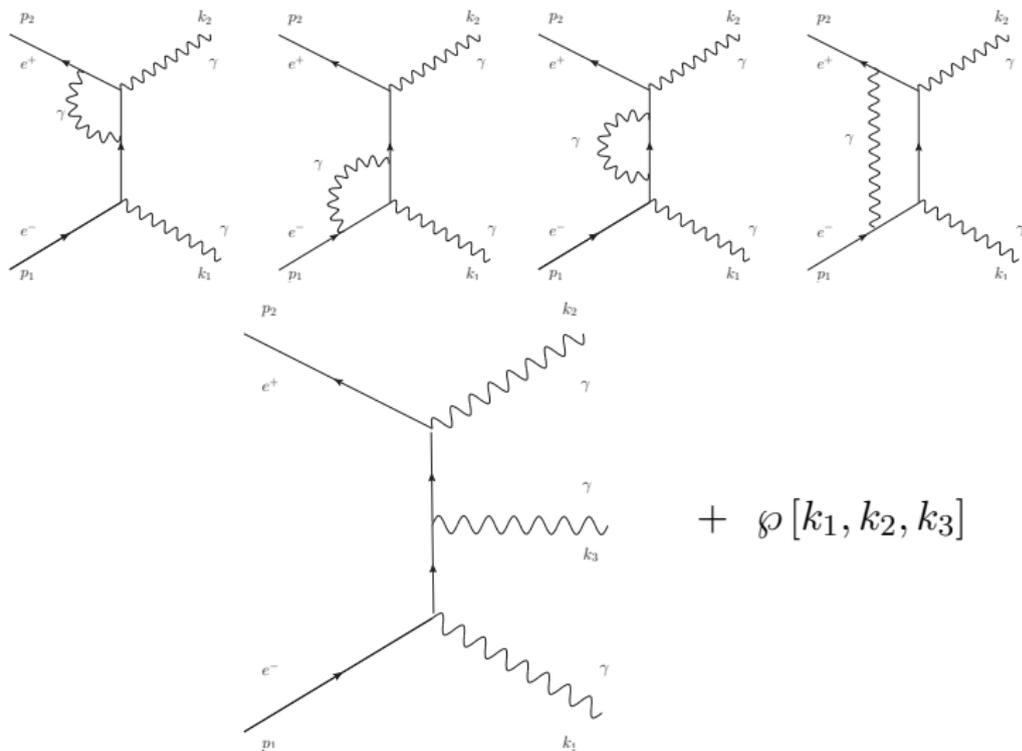
and at 10th FCC-ee physics workshop, CERN, February 2016

P. Janot's presentation at FCC-ee Joint Accelerator-Physics meeting, June 2015

my talk at FCC (TLEP) workshop (TLEP9), Pisa, February 2015

- ✓ at LO, purely QED process, *at any energy*
- ✓ at NLO, weak corrections (loops with Z & W^\pm), but not fermionic loops yet (in particular, *no hadronic loops*)
- ✓ hadronic vacuum polarization (**and its uncertainty**) enters only at NNLO (2-loops, order α^2)
- ✗ Large Bhabha background: at Z pole huge, much better at higher energies [*see later*]
- ✗ At NNLO less explored than Bhabha, but modern 2-loop techniques can be straightforwardly used
- ✗ Lack of independent MC codes for cross-checks/validation

NLO QED diagrams



virtual (+soft) RC from F.A. Berends & R. Kleiss, NPB 186 (1981) 22
 real RC calculated with the help of Vermaseren's FORM

Simulation setup & cross sections

→ 4 “standard” cms energy points: $\sqrt{s} = 91, 160, 240, 365$ GeV

→ Only QED corrections (NLO & higher orders) [weak & hadronic RC discussed later]

- [1] Full phase space, i.e. **no cuts**

- [2] (Acceptance) cuts:

at least two γ 's with: $20^\circ < \theta_\gamma < 160^\circ \quad \wedge \quad E_\gamma \geq 0.25 \times \sqrt{s}$

- [1] without cuts

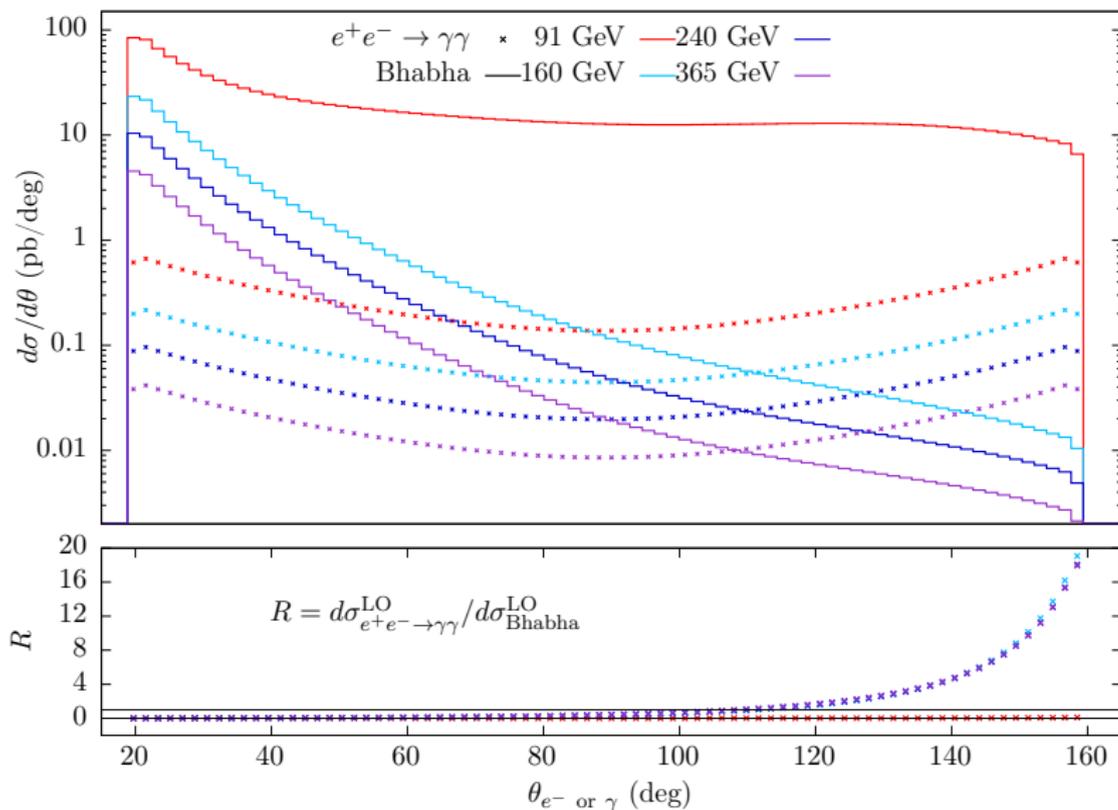
\sqrt{s} (GeV)	LO (pb)	NLO (pb)	w h.o. (pb)	stat. acc.*
91	364.68	447.27 [+23%]	445.6(9) [-0.46%]	$3.9 \cdot 10^{-6}$
160	123.71	154.37 [+25%]	153.2(2) [-0.95%]	$2.3 \cdot 10^{-5}$
240	56.816	71.809 [+26%]	71.07(6) [-1.30%]	$5.3 \cdot 10^{-5}$
365	25.385	32.515 [+28%]	32.09(2) [-1.67%]	$1.4 \cdot 10^{-4}$

- [2] with cuts

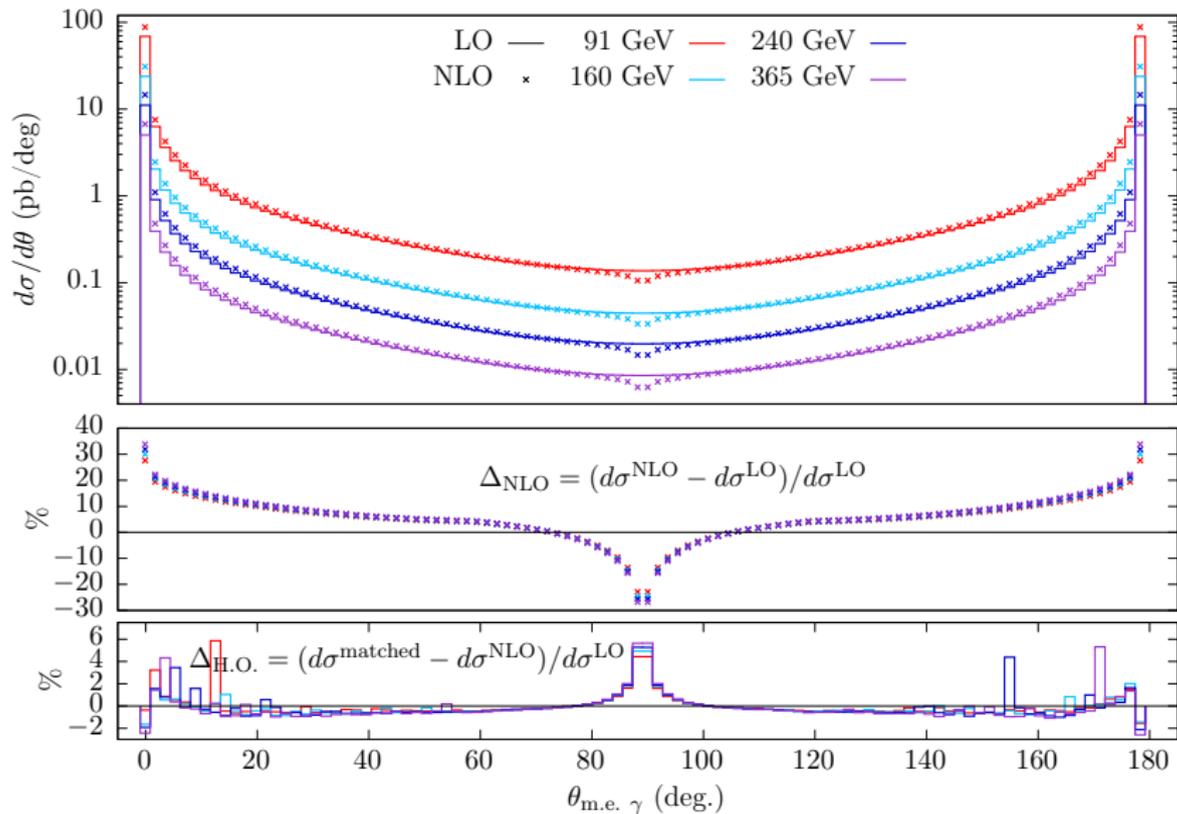
\sqrt{s} (GeV)	LO (pb)	NLO (pb)	w h.o. (pb)	Bhabha LO (pb)
91	39.821	41.043 [+3.07%]	40.868(3) [-0.44%]	2625.9 [66 × $\sigma^{\gamma\gamma}$]
160	12.881	13.291 [+3.18%]	13.228(1) [-0.49%]	259.98 [20 × $\sigma^{\gamma\gamma}$]
240	5.7250	5.9120 [+3.26%]	5.884(2) [-0.49%]	115.77 [20 × $\sigma^{\gamma\gamma}$]
365	2.4752	2.5582 [+3.35%]	2.5436(2) [-0.59%]	50.373 [20 × $\sigma^{\gamma\gamma}$]

* Assuming integrated luminosities as in Tab. 1 of A. Blondel *et al.*, arXiv:1809.01830 [hep-ph]

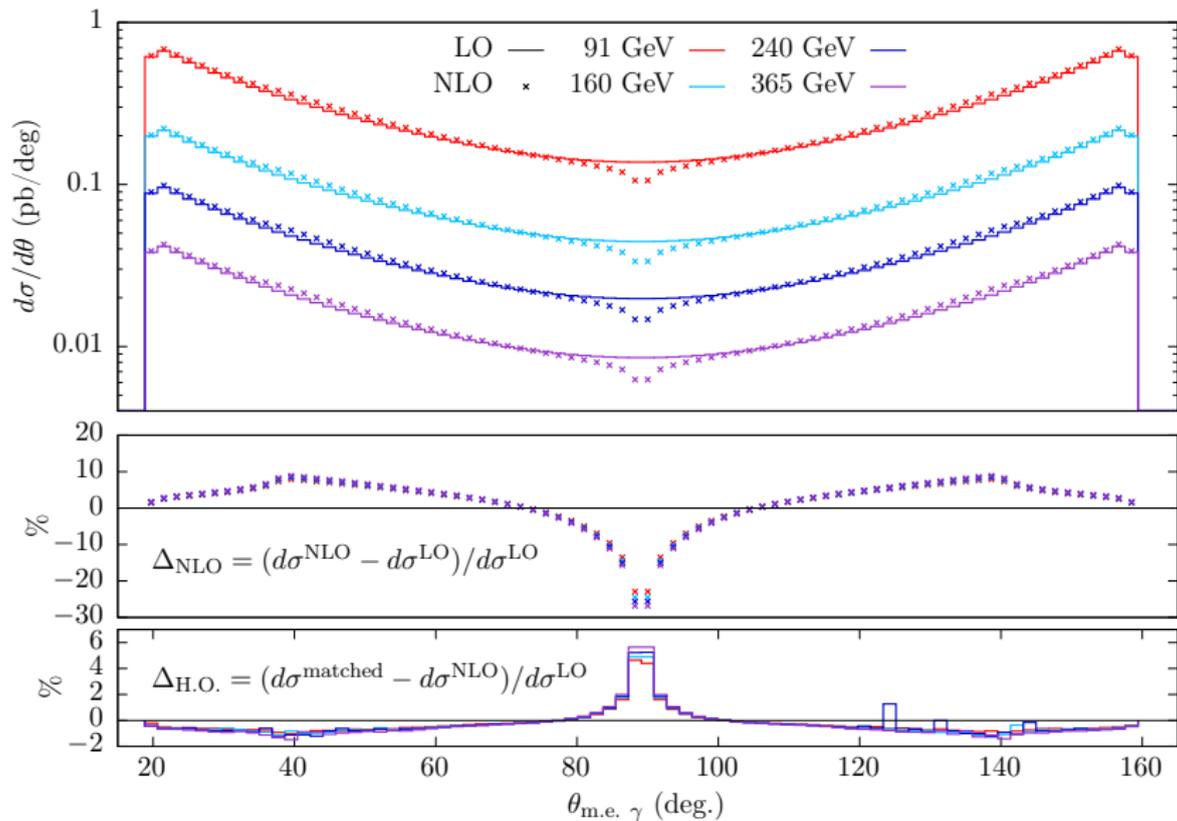
$e^+e^- \rightarrow \gamma\gamma$ vs Bhabha (at LO, with acceptance cuts)



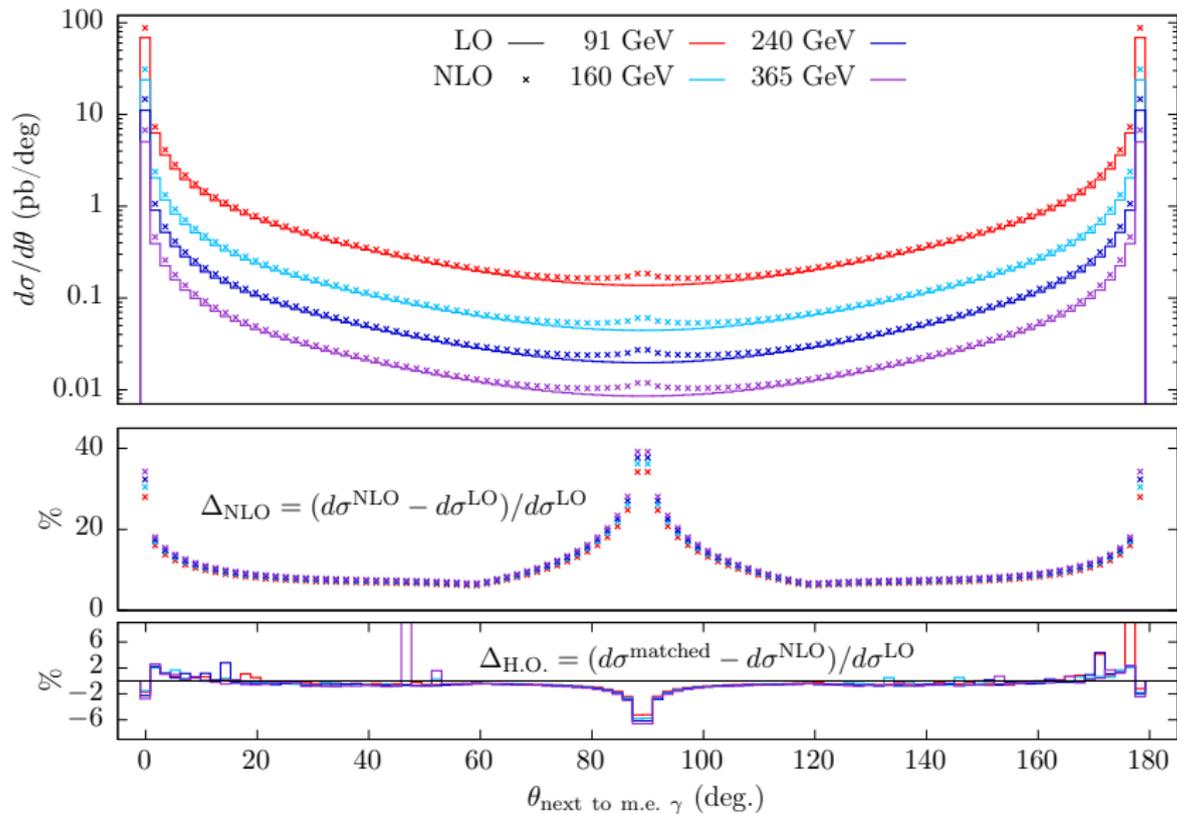
Most energetic γ angle (without cuts)



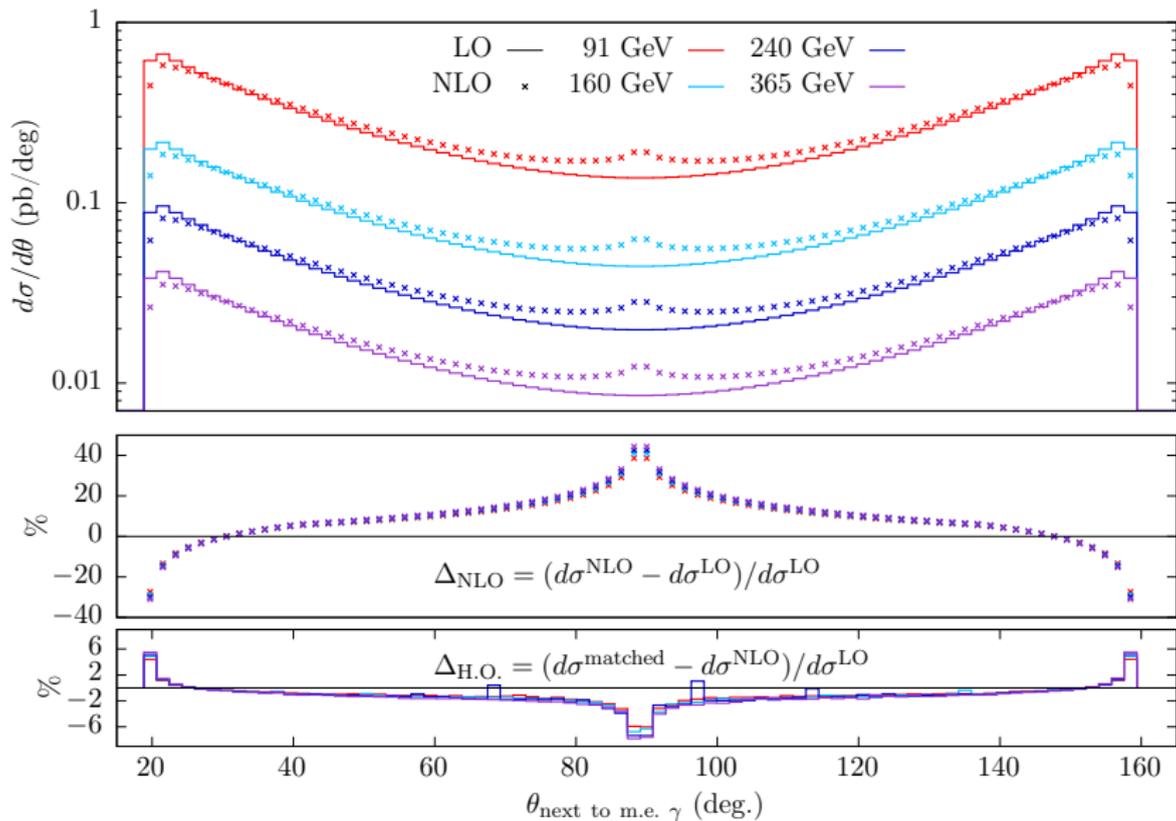
Most energetic γ angle (with acceptance cuts)



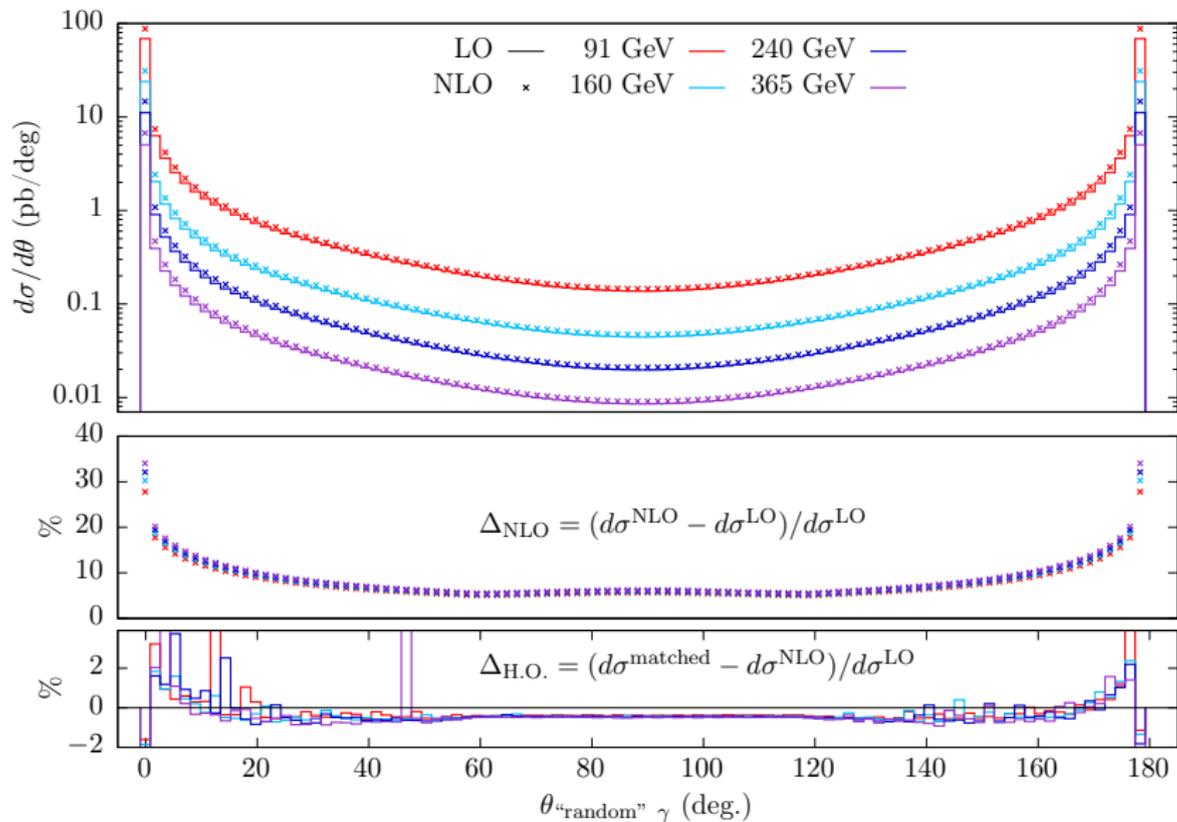
Next to most energetic γ angle (without cuts)



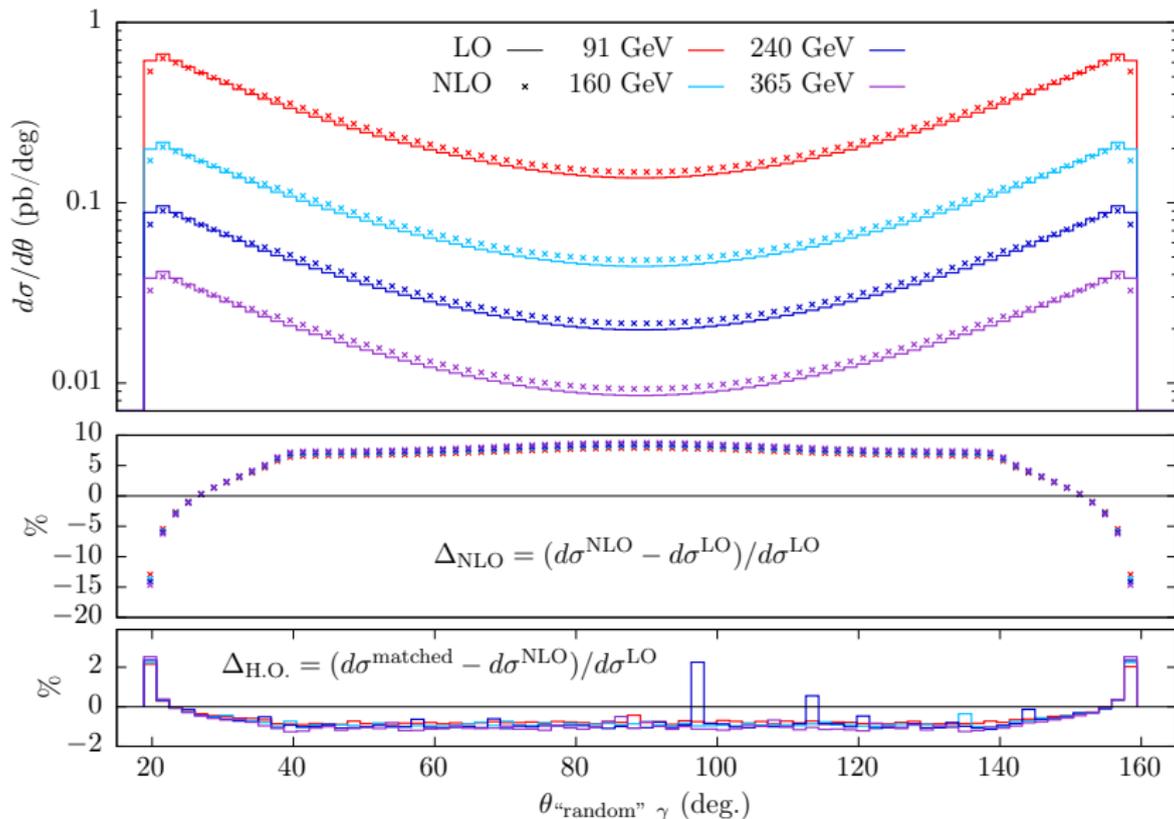
Next to most energetic γ angle (with acceptance cuts)



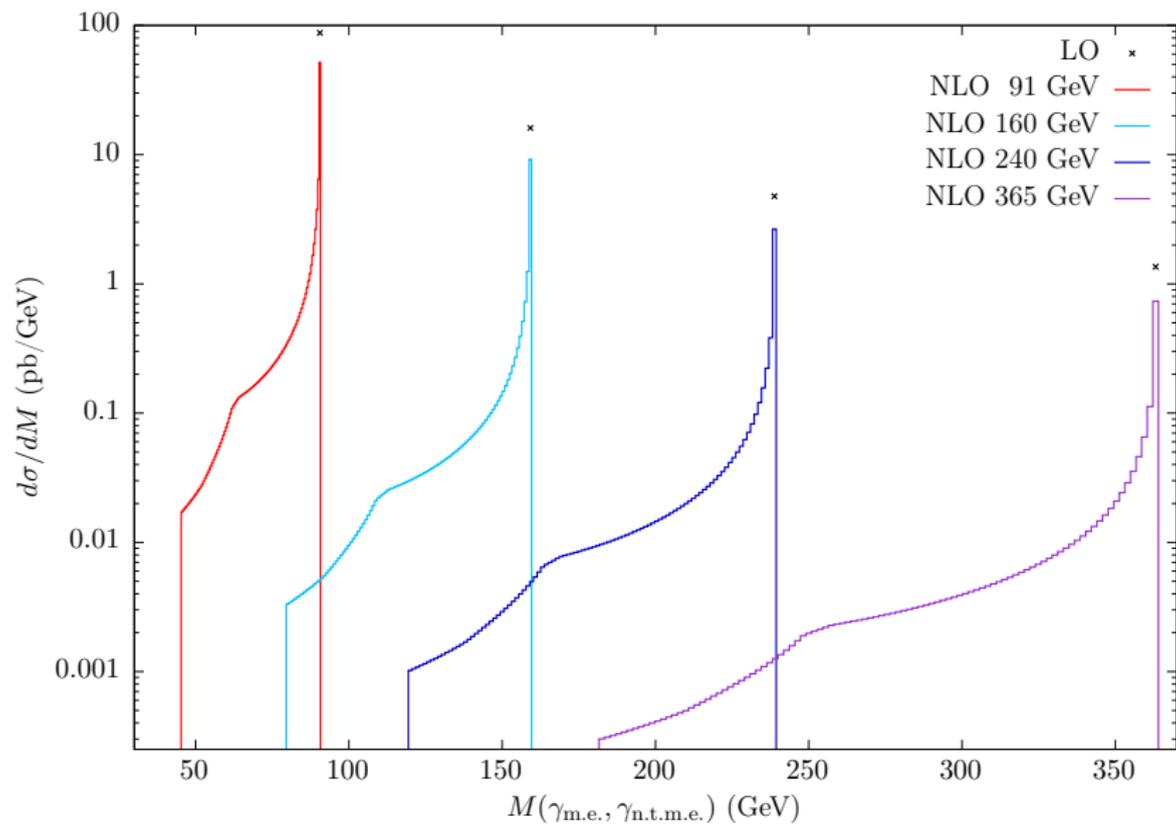
“Randomized” γ angle (without cuts)



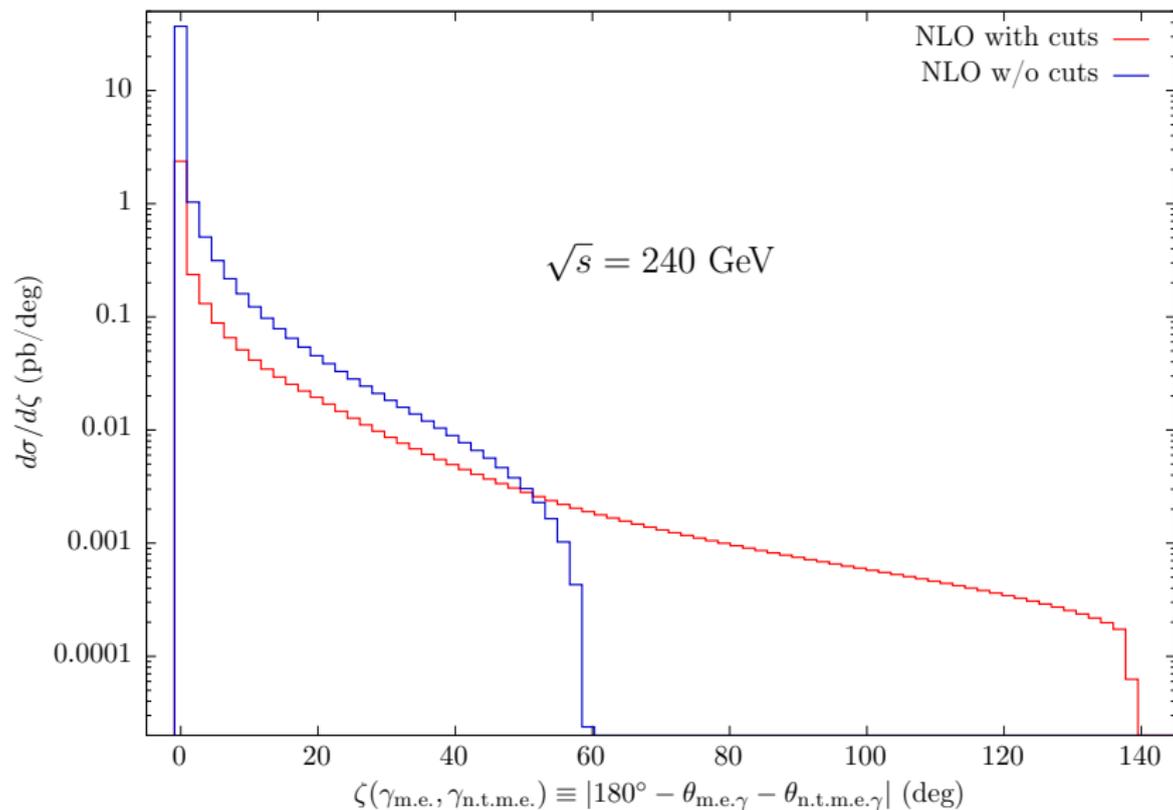
“Randomized” γ angle (with acceptance cuts)



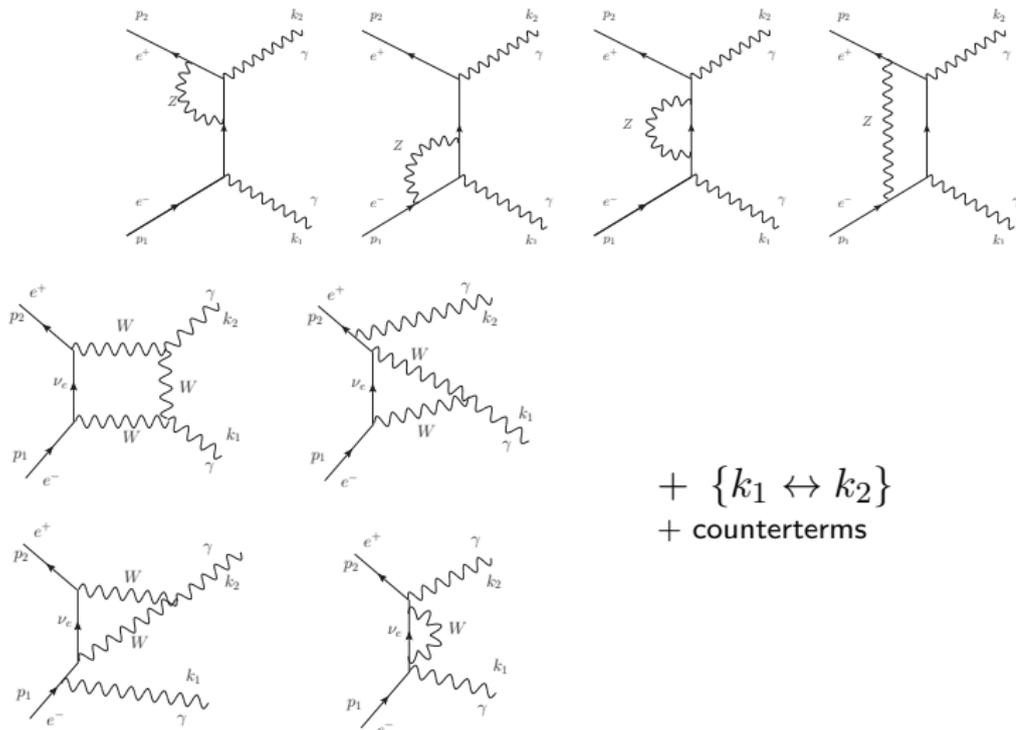
Invariant mass distribution at NLO (with cuts)



Acollinearity distribution at NLO



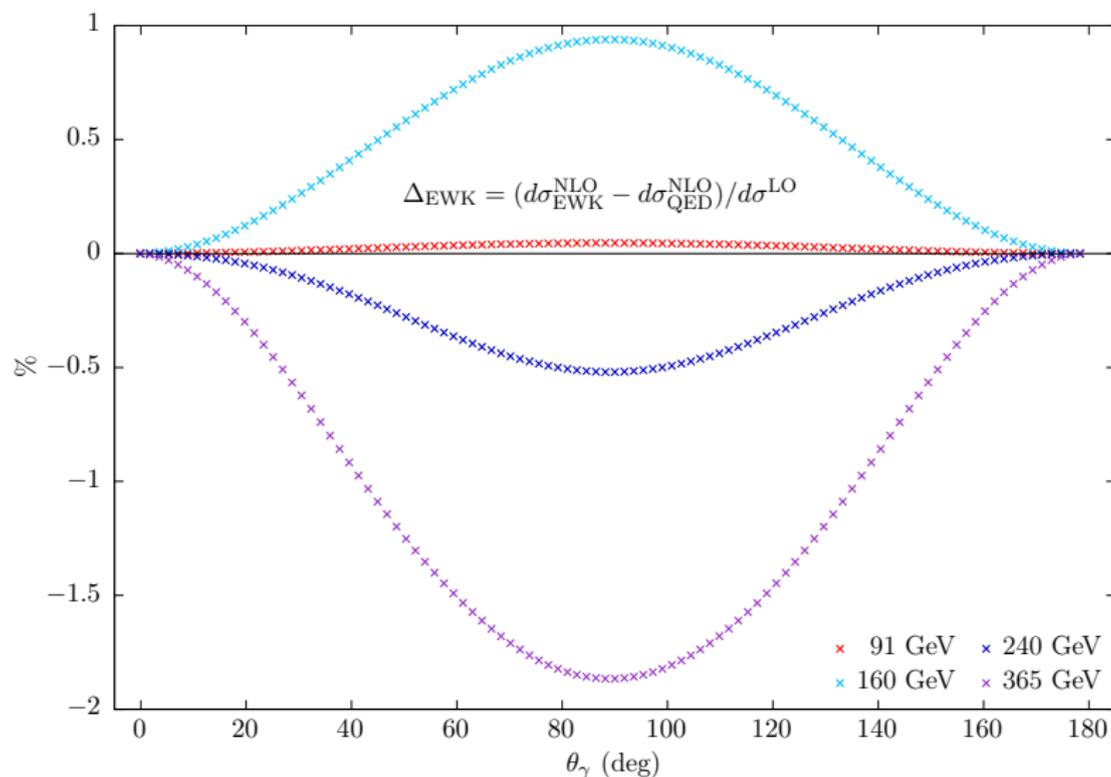
NLO virtual weak diagrams



→ Calculated in the on-shell (complex mass) scheme with the help of Reco1a-1.3.6

S. Actis *et al.*, JHEP 04:037, 2013

S. Actis *et al.*, CPC 214:140–173, 2017



- at higher energies, weak RCs get of the same order of QED h.o.

Rough estimate of (NNLO) VP hadronic corrections (and uncertainties)

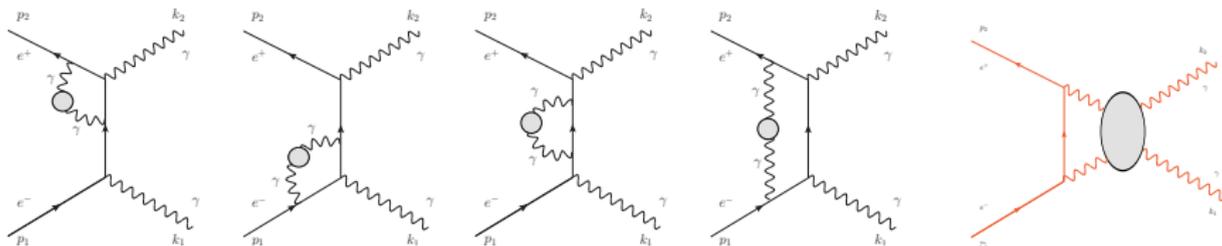
↪ for Bhabha, $\Delta\alpha_{had}$ uncertainty affects [today] the theoretical accuracy at $\mathcal{O}(10^{-4})$, entering at NLO

see Tables 2 & 3 of S. Jadach *et al.*, arXiv:1812.01004 [hep-ph] and A. Blondel *et al.*, arXiv:1809.01830 [hep-ph]

F. Jegerlehner's talk at this workshop on Tuesday

↪ for $e^+e^- \rightarrow \gamma\gamma$ it enters only at NNLO

[and also light-by-light graphs contribute!]



$$\sigma_{\Delta\alpha_{had}}^{\text{NNLO}} \pm \delta\sigma \stackrel{\text{very naive!}}{\approx} (\sigma_{\text{QED}}^{\text{NLO}} - \sigma^{\text{LO}}) \times [\Delta\alpha_{had}(s) \pm \delta\Delta\alpha_{had}]$$

\sqrt{s} (GeV)	$\Delta\alpha_{had}(s)^\dagger$	$\delta\sigma/\sigma_{LO}$ [1]	$\delta\sigma/\sigma_{LO}$ [2]
91	$(276.7 \pm 1.2) \cdot 10^{-4}$	$2.8 \cdot 10^{-5}$	$3.7 \cdot 10^{-6}$
160	$(309.1 \pm 1.2) \cdot 10^{-4}$	$3.0 \cdot 10^{-5}$	$3.8 \cdot 10^{-6}$
240	$(333.2 \pm 1.2) \cdot 10^{-4}$	$3.1 \cdot 10^{-5}$	$3.9 \cdot 10^{-6}$
365	$(358.5 \pm 1.2) \cdot 10^{-4}$	$3.4 \cdot 10^{-5}$	$4.0 \cdot 10^{-6}$

[†]from F. Jegerlehner's recent `hadr5n16.f`

- The process $e^+e^- \rightarrow \gamma\gamma$ at large-angle is worth being studied as monitor for luminosity at FCC-ee
- On the theoretical side:
 - NLO QED RCs affect differential cross sections at the 10 – 20% level
 - QED higher-order RCs lie in the % range
 - EWK RCs get larger at higher energies, and lie in the % range
 - Hadronic VP enters only at NNLO, its uncertainty is (likely) negligible
- With **complete NNLO at hand, matched with QED h.o. resummation**, can $e^+e^- \rightarrow \gamma\gamma$ theoretical accuracy be controlled at/better than the 10^{-4} level?
Perhaps better than small-angle Bhabha?

SPARES

Theory of QED corrections into Monte Carlo generators

- ★ The most precise MC generators include **exact $\mathcal{O}(\alpha)$ (NLO) photonic corrections matched with higher-order leading logarithmic contributions [multiple photon corrections]**

[+ **vacuum polarization**, using a data driven routine for the calculation of the non-perturbative $\Delta\alpha_{\text{had}}^{(5)}(q^2)$ hadronic contribution]

- ★ Common methods used to account for multiple photon corrections are the **analytical collinear QED Structure Functions (SF)**, **YFS exponentiation** and **QED Parton Shower (PS)**

- The QED PS [implemented in **BabaYaga/BabaYaga@NLO**] is an **exact MC solution** of the QED DGLAP equation for the non-singlet electron SF $D(x, Q^2)$

$$Q^2 \frac{\partial}{\partial Q^2} D(x, Q^2) = \frac{\alpha}{2\pi} \int_x^1 \frac{dt}{t} P_+(t) D\left(\frac{x}{t}, Q^2\right)$$

- The PS solution can be cast into the form

$$D(x, Q^2) = \Pi(Q^2) \sum_{n=0}^{\infty} \int \frac{\delta(x-x_1 \cdots x_n)}{n!} \prod_{i=0}^n \left[\frac{\alpha}{2\pi} P(x_i) L dx_i \right]$$

→ $\Pi(Q^2) \equiv e^{-\frac{\alpha}{2\pi} LI_+}$ Sudakov form factor, $I_+ \equiv \int_0^{1-\epsilon} P(x) dx$, $L \equiv \ln Q^2/m^2$ collinear log,

ϵ soft-hard separator and Q^2 virtuality scale

→ the kinematics of the photon emissions can be recovered → **exclusive photons generation**

- The accuracy is improved by **matching exact NLO with higher-order leading log corrections**

★ **theoretical error starts at $\mathcal{O}(\alpha^2)$ (NNLO) QED corrections**, for all QED channels [Bhabha, $\gamma\gamma$ and $\mu^+\mu^-$]

Exact $\mathcal{O}(\alpha)$ (NLO) soft+virtual (SV) corrections and hard-bremsstrahlung (H) matrix elements can be combined with QED PS *via* a matching procedure

- $d\sigma_{PS}^{\infty} = \Pi(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} |\mathcal{M}_{n,PS}|^2 d\Phi_n$
- $d\sigma_{PS}^{\alpha} = [1 + C_{\alpha,PS}] |\mathcal{M}_0|^2 d\Phi_2 + |\mathcal{M}_{1,PS}|^2 d\Phi_3 \equiv d\sigma_{PS}^{SV}(\varepsilon) + d\sigma_{PS}^H(\varepsilon)$
- $d\sigma_{NLO}^{\alpha} = [1 + C_{\alpha}] |\mathcal{M}_0|^2 d\Phi_2 + |\mathcal{M}_1|^2 d\Phi_3 \equiv d\sigma_{NLO}^{SV}(\varepsilon) + d\sigma_{NLO}^H(\varepsilon)$
- $F_{SV} = 1 + (C_{\alpha} - C_{\alpha,PS}) \quad F_H = 1 + \frac{|\mathcal{M}_1|^2 - |\mathcal{M}_{1,PS}|^2}{|\mathcal{M}_{1,PS}|^2}$

$$d\sigma_{\text{matched}}^{\infty} = F_{SV} \Pi(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} \left(\prod_{i=0}^n F_{H,i} \right) |\mathcal{M}_{n,PS}|^2 d\Phi_n$$

$d\Phi_n$ is the **exact** phase space for n final-state particles
(2 fermions + an arbitrary number of photons)

- F_{SV} and $F_{H,i}$ are infrared/collinear safe and account for missing $\mathcal{O}(\alpha)$ non-logs, avoiding double counting of leading-logs
- $[\sigma_{matched}^\infty]_{\mathcal{O}(\alpha)} = \sigma_{\text{NLO}}^\alpha$
- resummation of higher orders LL (PS) contributions is preserved
- the cross section is still fully differential in the momenta of the final state particles (e^+ , e^- and $n\gamma$)
(F 's correction factors are applied on an event-by-event basis)
- as a by-product, part of photonic $\alpha^2 L$ included by means of terms of the type $F_{SV | H,i} \otimes$ [leading-logs]

G. Montagna et al., **PLB** 385 (1996)

- the theoretical error is shifted to $\mathcal{O}(\alpha^2)$ (NNLO, 2 loop) not infrared, singly collinear terms: very naively and roughly (for photonic corrections)

$$\frac{1}{2}\alpha^2 L \equiv \frac{1}{2}\alpha^2 \log \frac{s}{m_e^2} \sim 5 \times 10^{-4}$$

“Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data”

- It is extremely important to compare independent calculations/implementations/codes, in order to
 - asses the technical precision, spot bugs (with the same th. ingredients)
 - estimate the theoretical error when including partial/incomplete higher-order corrections
- E.g. comparison BabaYaga@NLO vs. Bhwide at KLOE

S. Jadach et al. PLB 390 (1997) 298

