

# Learning representations of irregular particle-detector geometry with distance-weighted graph networks

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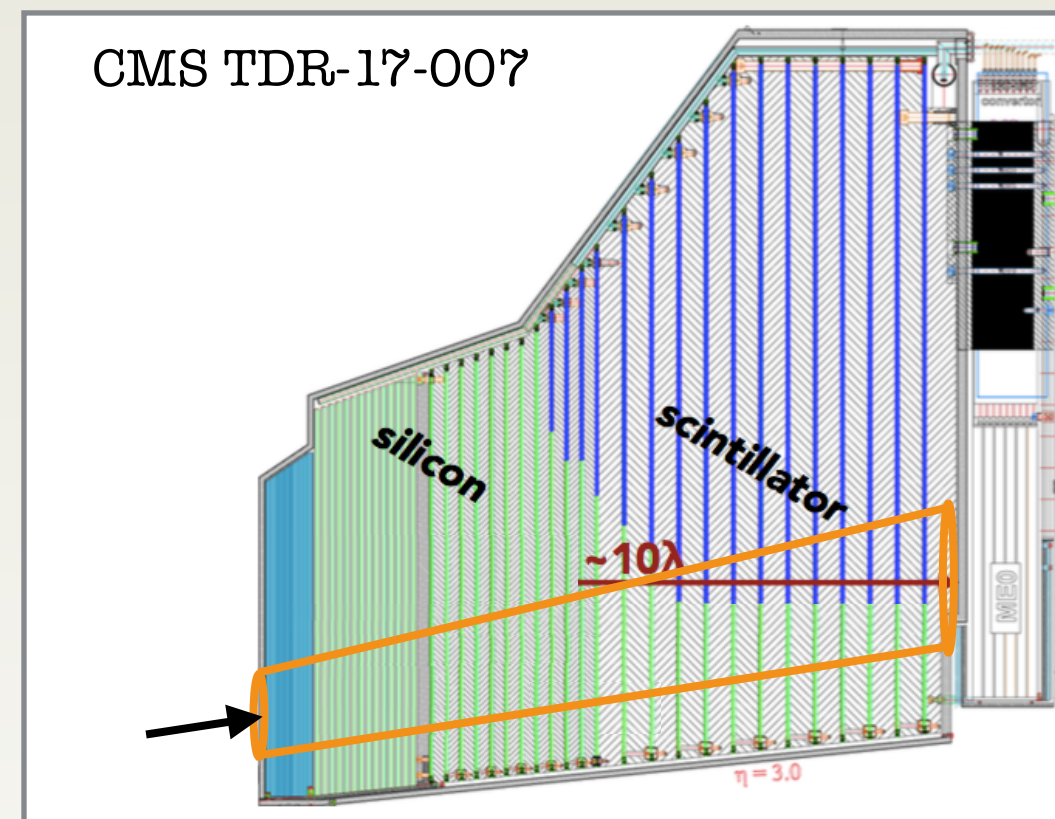
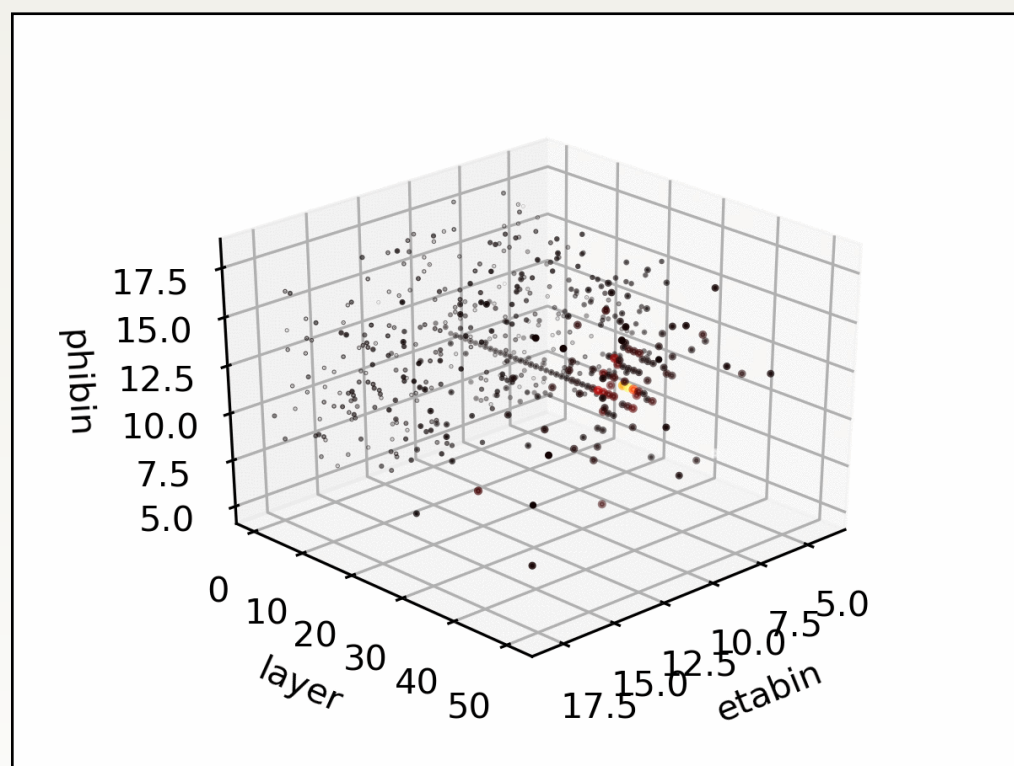
17.4.2019



1: CERN

2: National University of Sciences and Technology, Islamabad

- Example: HGCal produces 3D shower images
  - Space
  - Energy (+time) as colour
- Large number of inputs: 6M channels



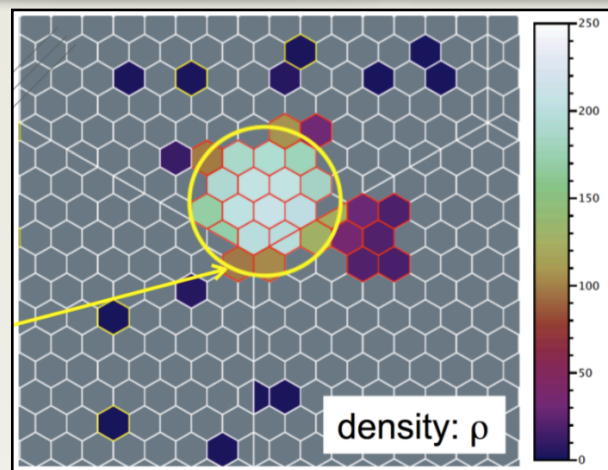
## • Tasks:

- Identify showers in noise
- Identify particle type from shower shape
- Measure energy

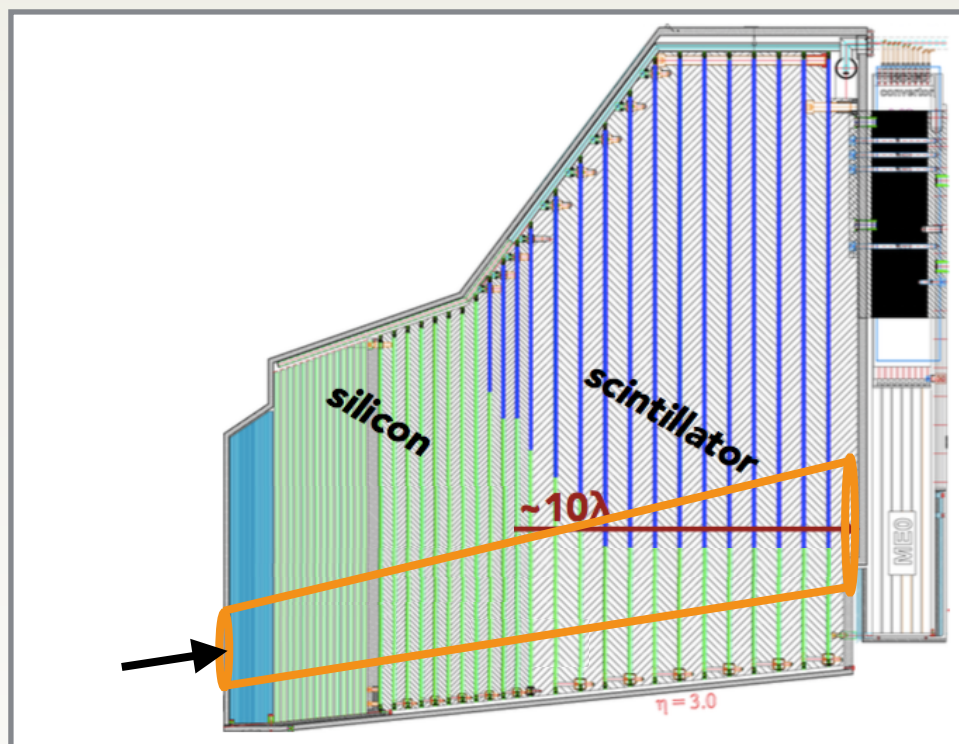
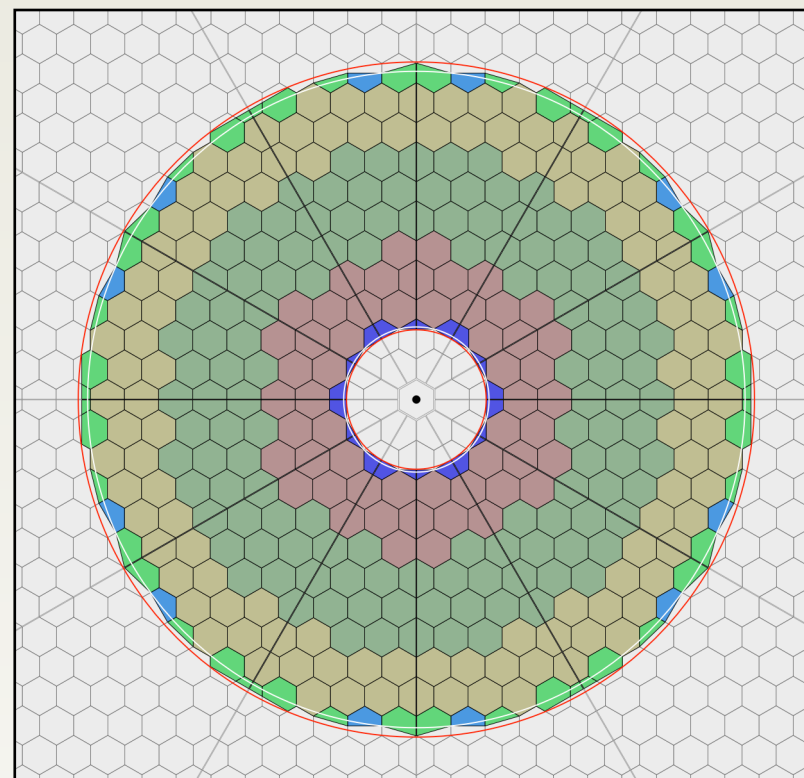
**strong similarity  
to pattern  
recognition/  
computer vision**

→ Using translation invariance,  
CNNs seem natural choice

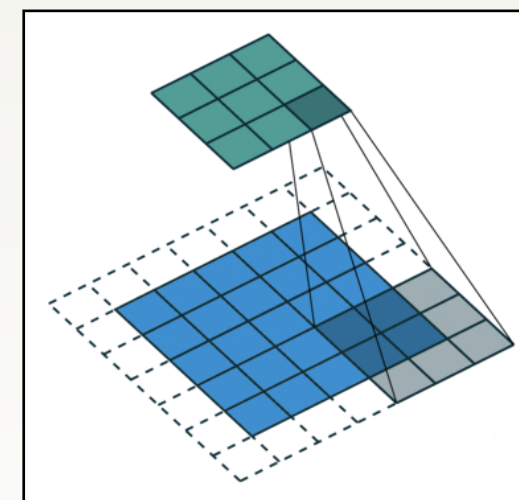
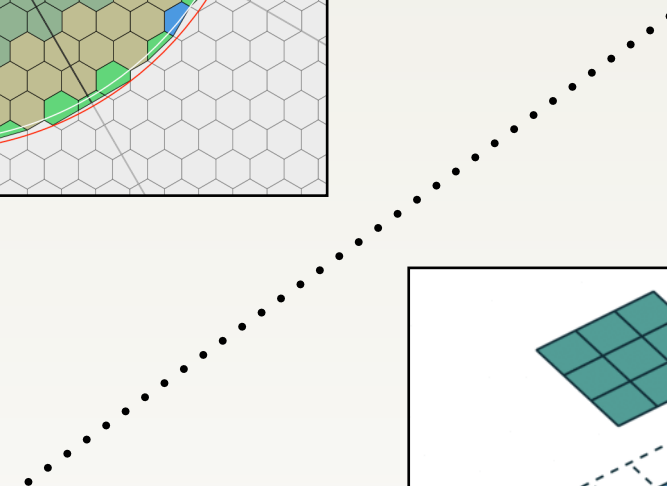
# Detectors: General Problem



CMS TDR-17-007



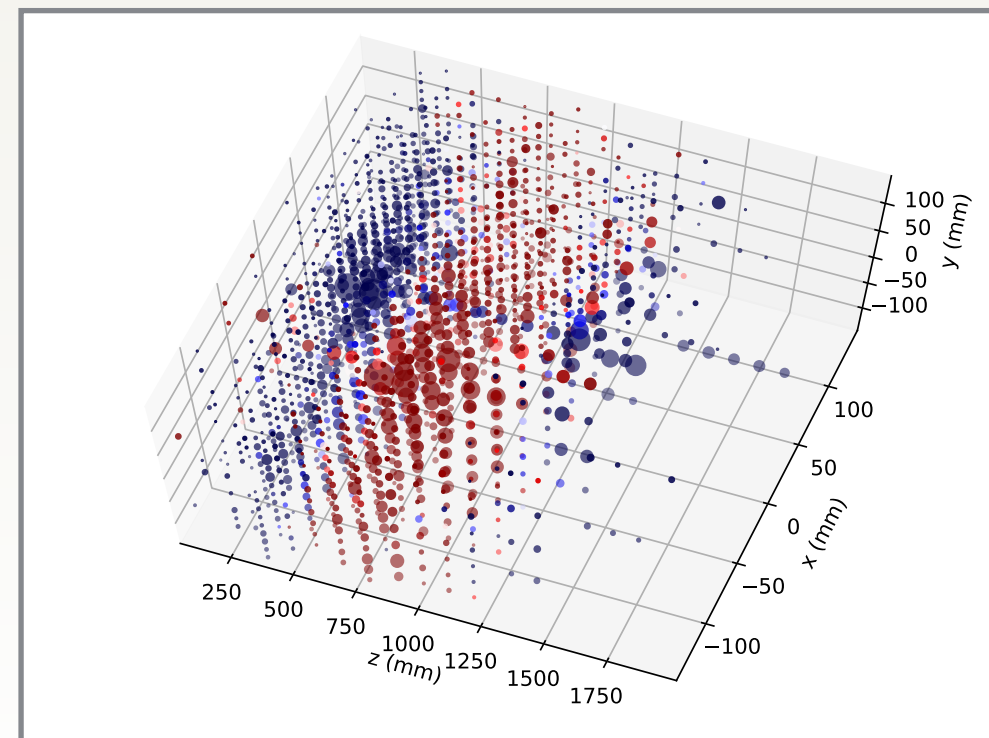
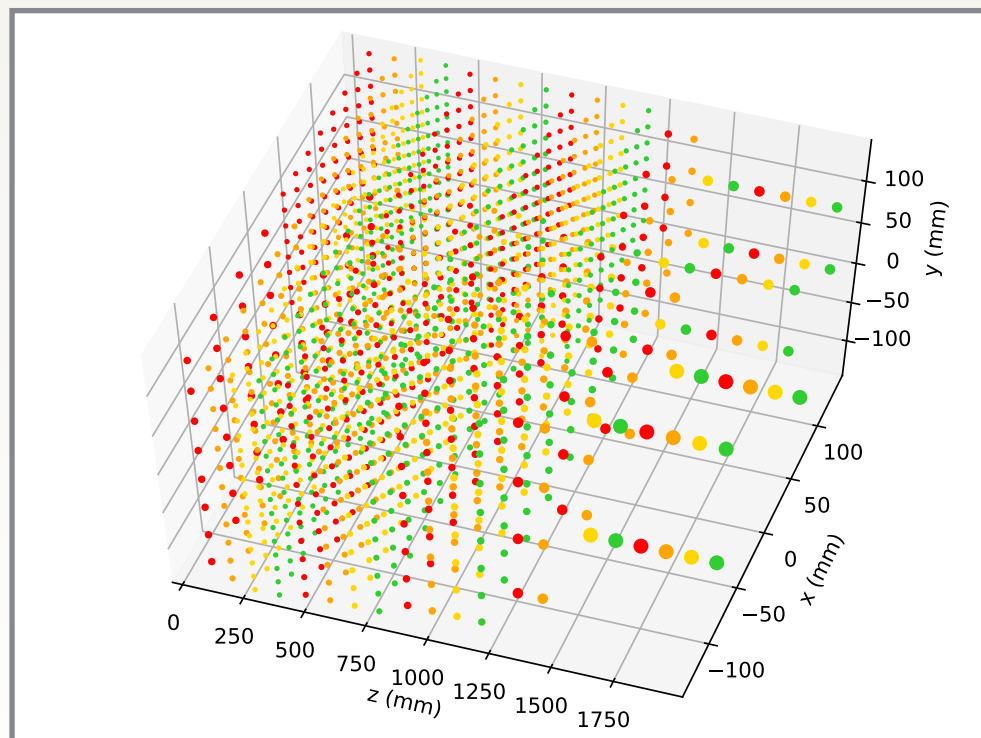
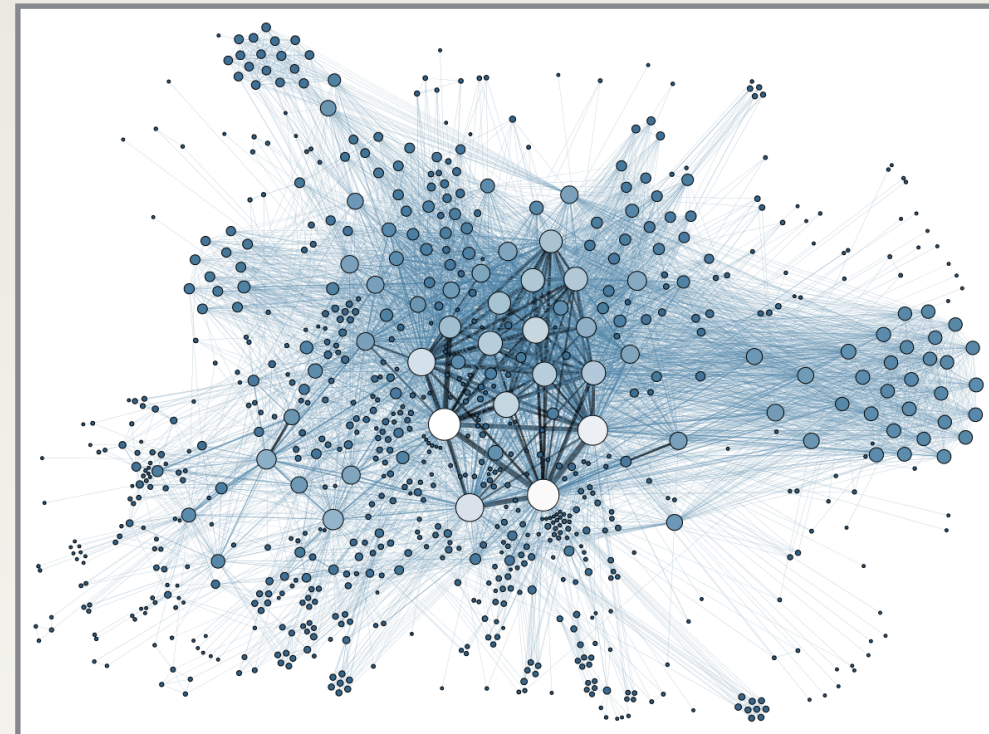
- Irregular geometry: physics driven
- Sparse showers



- Uniform, regular pixel size in all dimensions

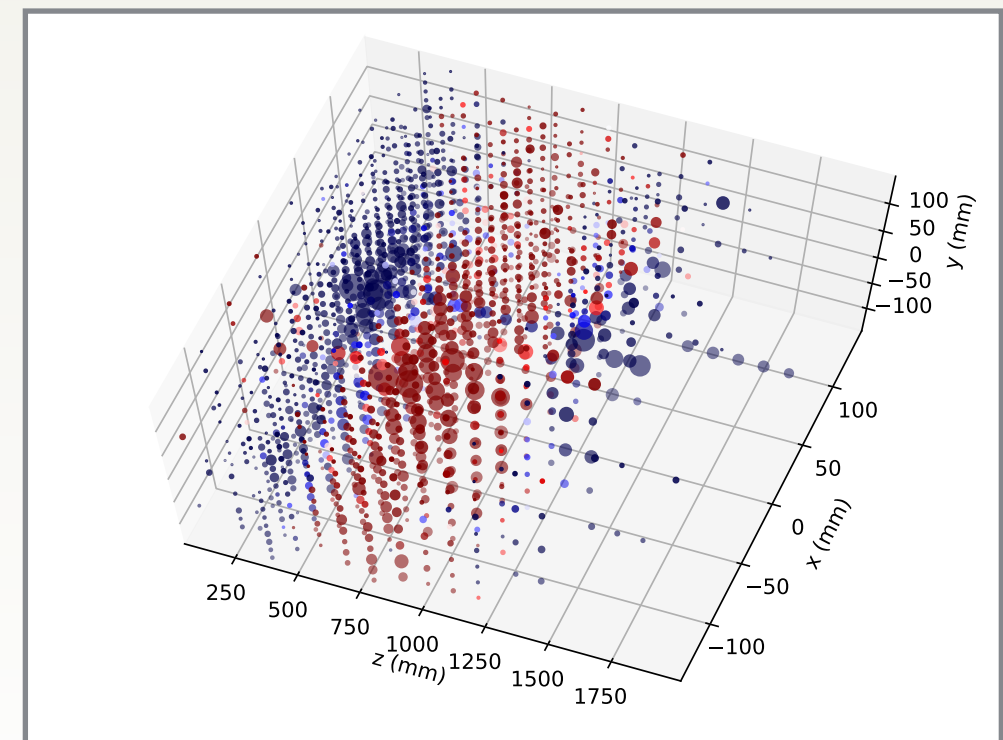
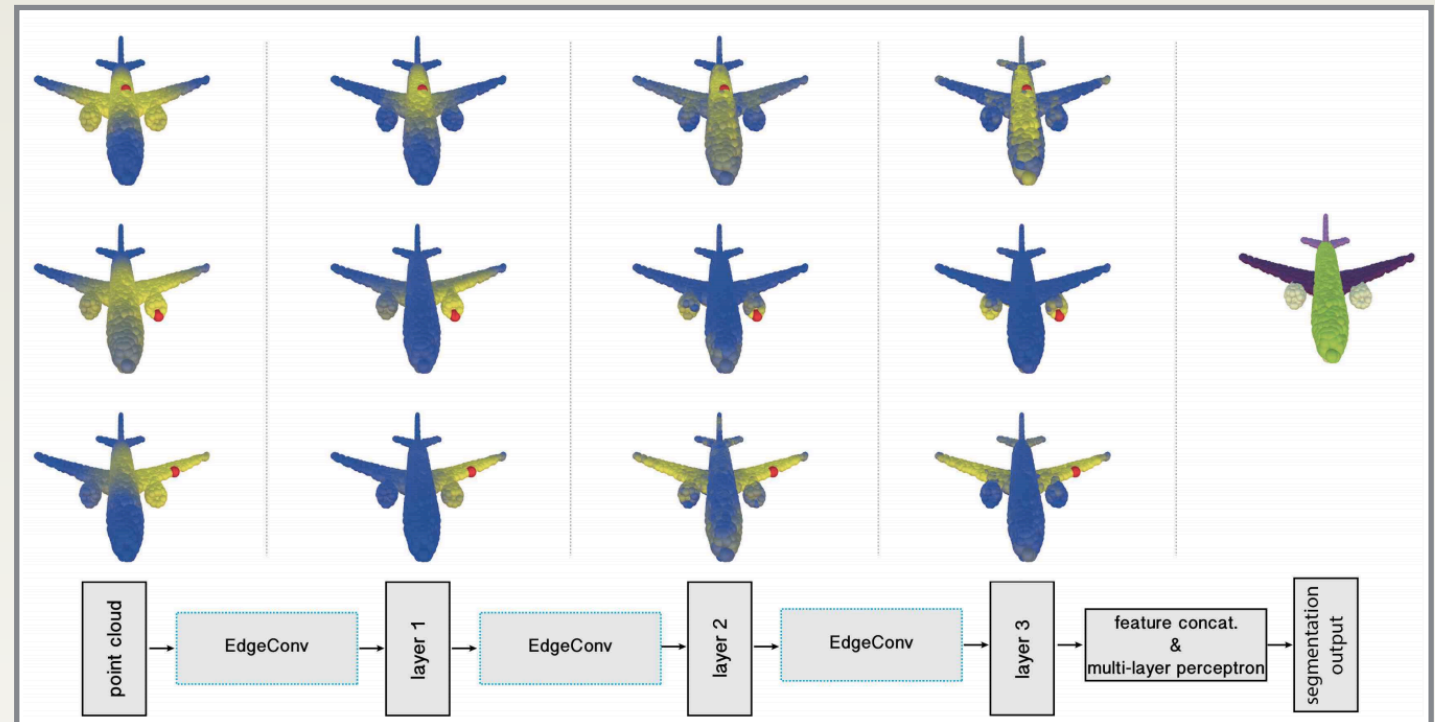


- Using graph neural networks for reconstruction
  - Invariant w.r.t. order of inputs
  - Do not depend on a regular geometry
  - In particularly interesting: **dynamic graph networks** learning space transformations
- Studying approaches for segmentation (clustering)
- Here in a simplified irregular calorimeter
  - Full Tungsten, no absorber, directly consider energy deposits
  - Sensor size and quantity changes with layer and x,y



# Clustering / Segmentation

- Clustering is more than (just) segmentation: need to identify fractions rather than classify a set of points
- However, proposal for segmentation of point clouds: DGCNN [1] similar to our problem
  - Irregular points / sensors
  - Identifying one shower in presence of others
  - Proven very powerful
- DGCNN (a.k.a EdgeConv layers)
  - Transform features per vertex
  - Calculate L2 distance between vertices with new features
  - Select N neighbours and edges (just difference between features, absolute coord.)
  - Transform edge features
  - Select maximum activation of transformed edge features as new vertex features (max pool in edges)
  - Propagate this information to next layer



[1] arXiv:1801.07829



# EdgeConv in practice

- DGCNN (a.k.a EdgeConv layers)

- ▶ Transform features per vertex
- ▶ Calculate L2 distance between vertices with new features
- ▶ Select N neighbours and edges  
(just difference between features, absolute coord.)
- ▶ Transform edge features
- ▶ Select maximum activation of transformed edge features  
as new vertex features (max pool in edges)

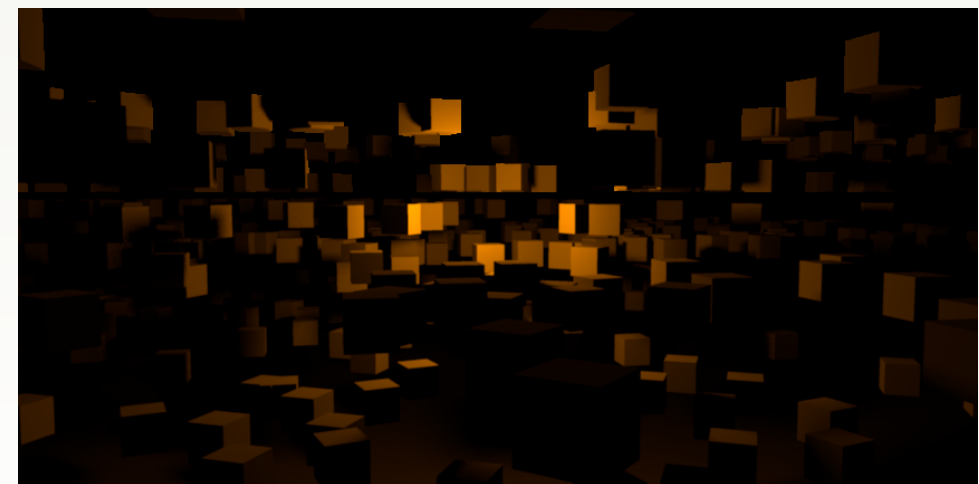
- ▶  $B \times V \times F \rightarrow B \times V \times F'$  ( $F' = 64$ )
- ▶  $\mathbf{B} \times \mathbf{V} \times \mathbf{V} \times \mathbf{F}' \rightarrow B \times V \times V \times 1$
- ▶  $B \times V \times N \times F'$
- ▶  $(\mathbf{B} \times \mathbf{V} \times \mathbf{N} \times \mathbf{F}' \rightarrow \mathbf{B} \times \mathbf{V} \times \mathbf{N} \times \mathbf{F}'')^t$
- ▶  $B \times V \times N \times F'' \rightarrow B \times V \times F''$

- Many resource intense steps

- ▶ Our training/inference resources are very limited
- ▶ We also need a fast network for triggering applications
- ▶ Our inputs are more complex: coordinate features and also measured features  
(e.g. energy in a sensor)

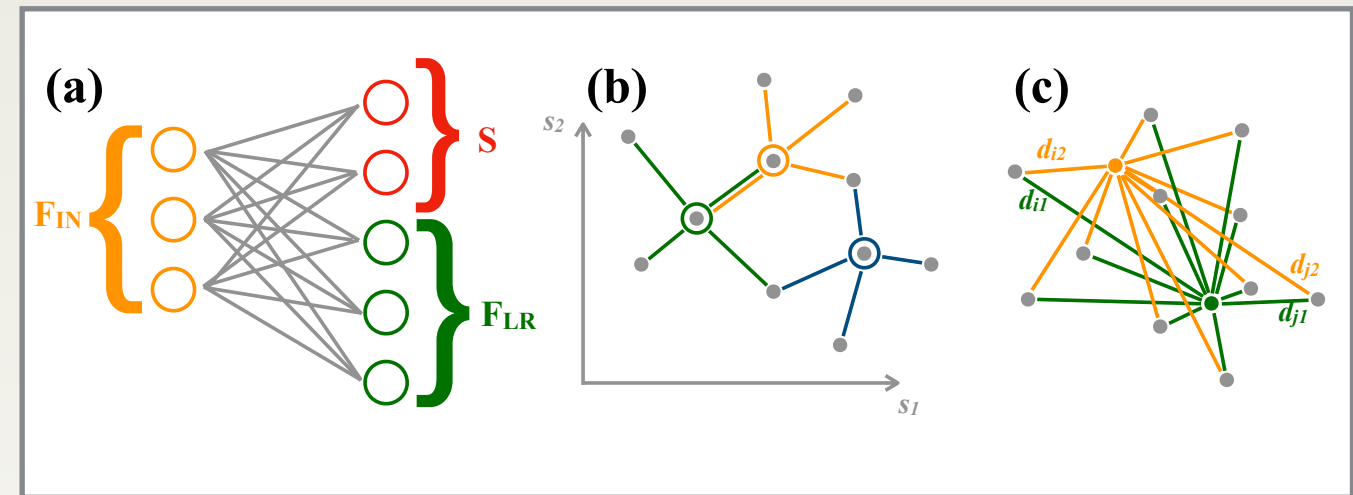
- Build new network layers: GravNet and GarNet

- ▶ Allow for learnable space representation
- ▶ Split coordinate space and 'other feature' space
- ▶ Aggregate features from vertices
- ▶ Evaluate distances in coordinate space and apply as weights to features when aggregating
  - ▶ Creates gradient w.r.t. distances



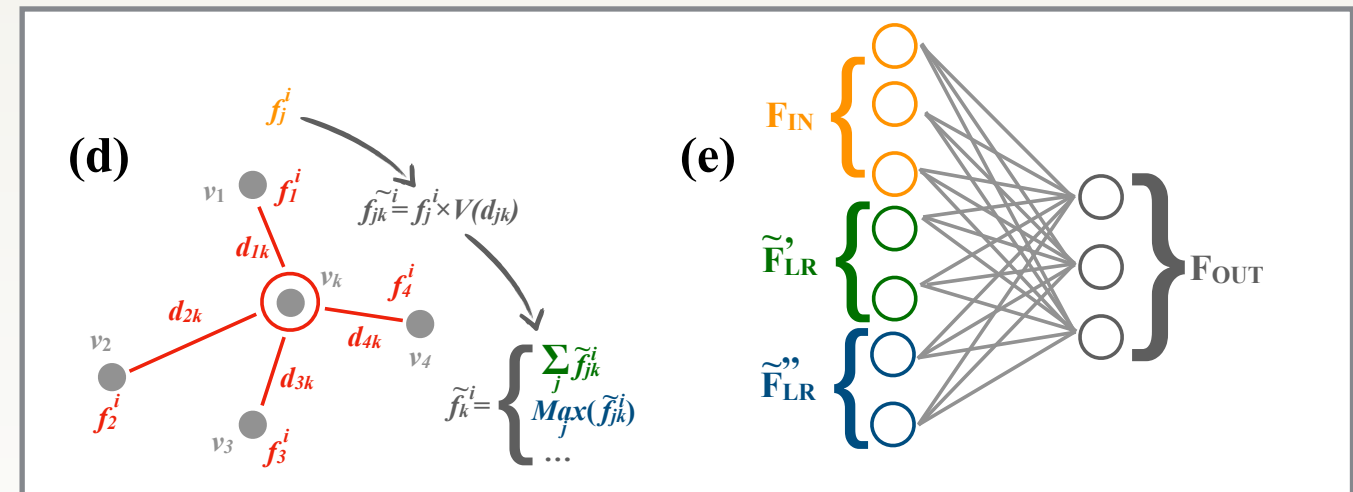
## • GravNet

- ▶ Project to coordinate and feature space **(a)**
- ▶ Select N neighbours using coordinate space **(b)**
- ▶ Scale neighbour features with distance **(d)**
  - ▶ (small distance = large weight)
- ▶ Select maximum and mean of scaled features **(d)**
  - ▶ Improves convergence significantly
- ▶ Mix with original vertex information **(e)**

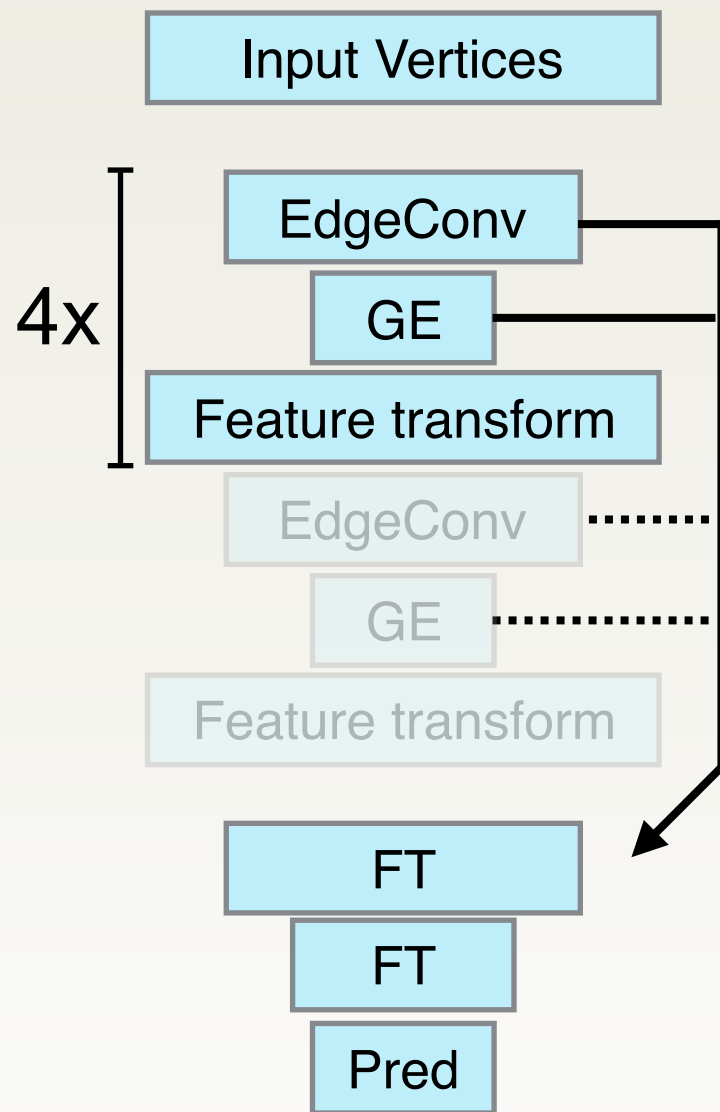


## • GarNet:

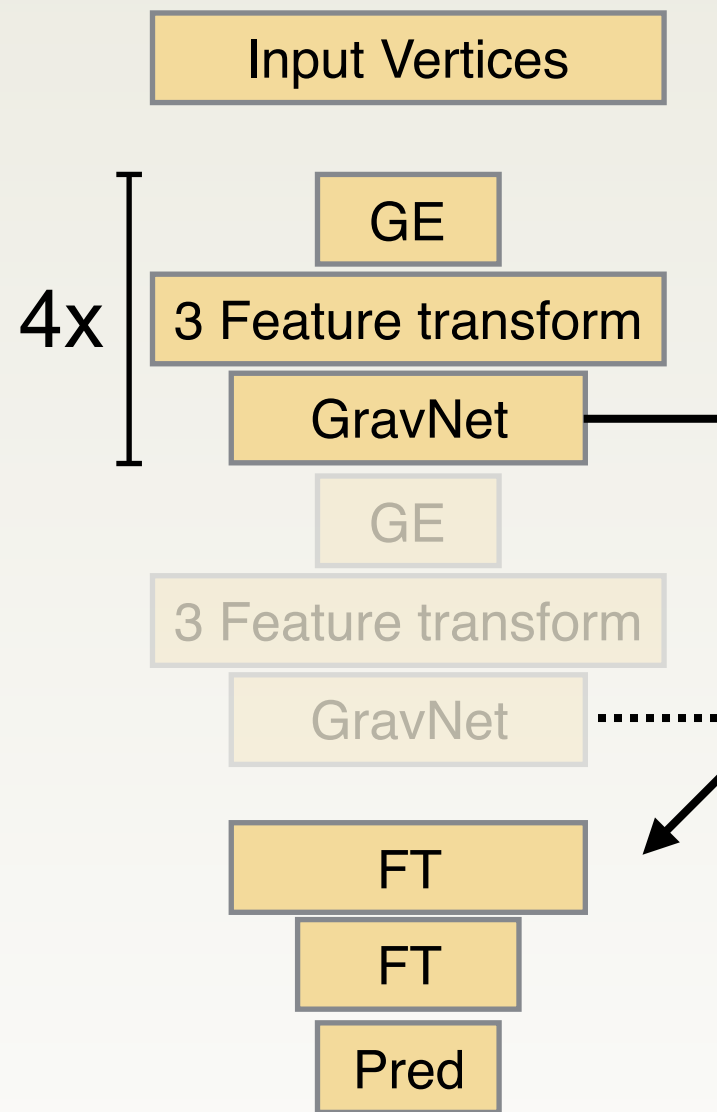
- ▶ Project to coordinate and feature space **(a)**
- ▶ Interpret coordinates as distances to aggregators **(c)**
- ▶ Use distance weights to aggregate mean and max **(d)**
- ▶ Expand back to all vertices using same distance weights **(d)**
- ▶ Mix with original vertex information **(e)**



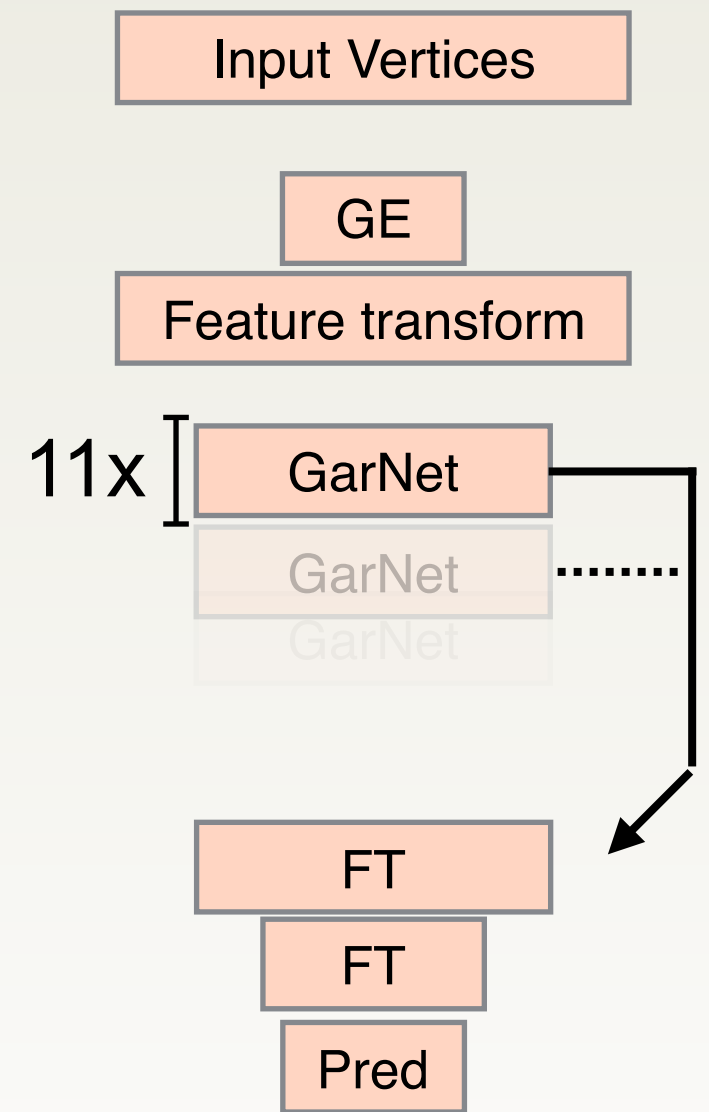
## “DGCNN”



## GravNet



## GarNet



- Similar total depth (counting all trainable transformations)
- All models approx 100k free parameters



# Dataset and Training

- Segmentation

- ▶ 16M events
- ▶ Charged pions ( $E = 10 - 100$  GeV)
  - ▶ Most complex showers
- ▶ Shot at  $x, y = [-5, 5]$  cm (random),  $z = -5$  cm
- ▶ 2 particles per event

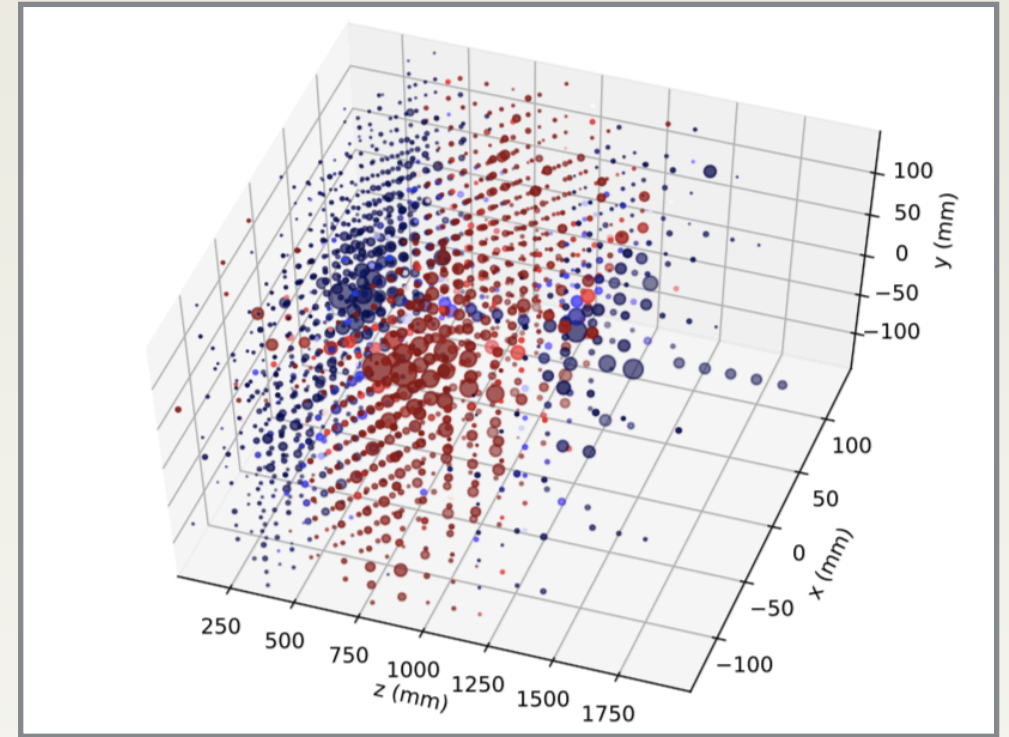
- Calorimeter

- ▶ Tungsten
- ▶ 30 cm x 30 cm x 2m
- ▶ In total 2102 sensors

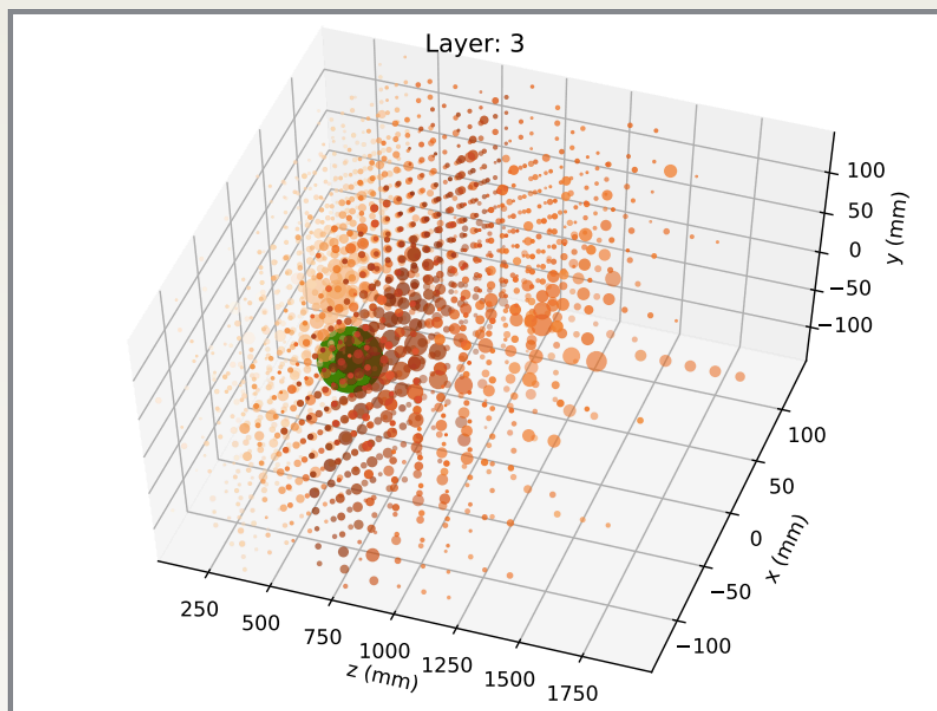
- Training

- ▶ Using exponentially decaying learning rates starting around 0.0003
- ▶ No dropout
  - ▶ With about 100k parameters no overtraining
- ▶ Batch normalisation
- ▶ Minimize:

$$L = \sum_k \frac{\sum_i \sqrt{E_i t_{ki}} (p_{ki} - t_{ki})^2}{\sum_i \sqrt{E_i t_{ki}}},$$

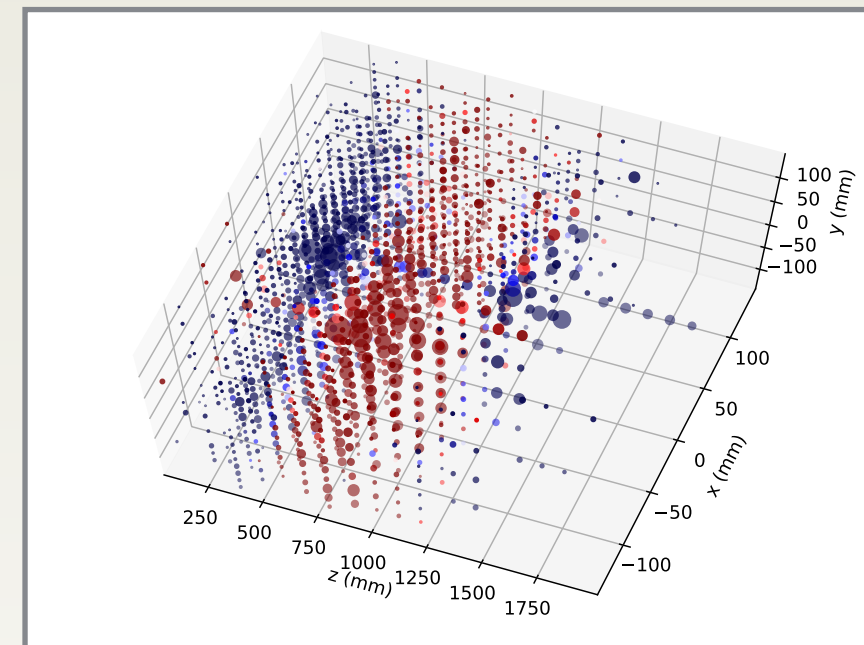


- Use distances to visualise perception of the DNN
  - Here GravNet

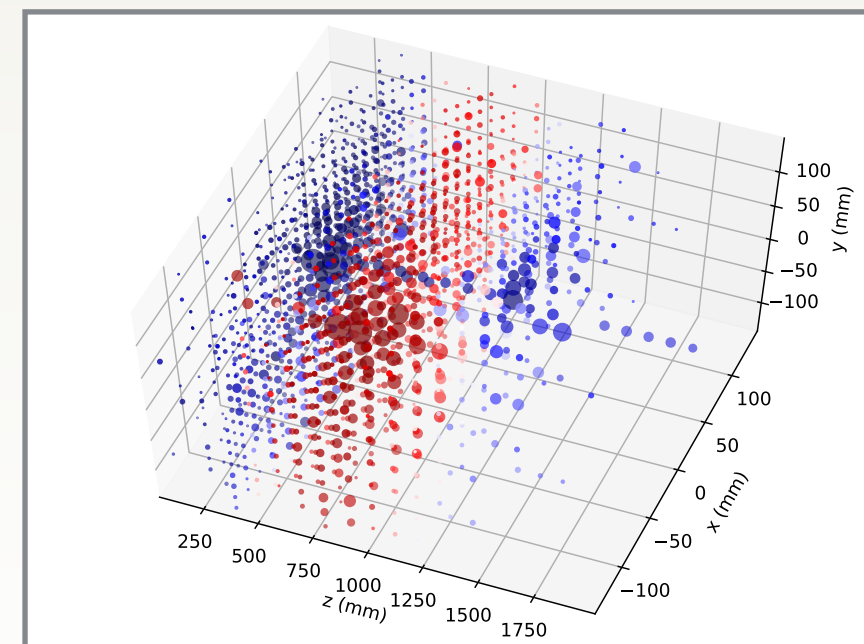


- Showers are successfully reconstructed
  - Connecting **tracks** are identified
  - EM/hadronic components are **linked**
  - Fractions are separated

Truth - for reference



Prediction

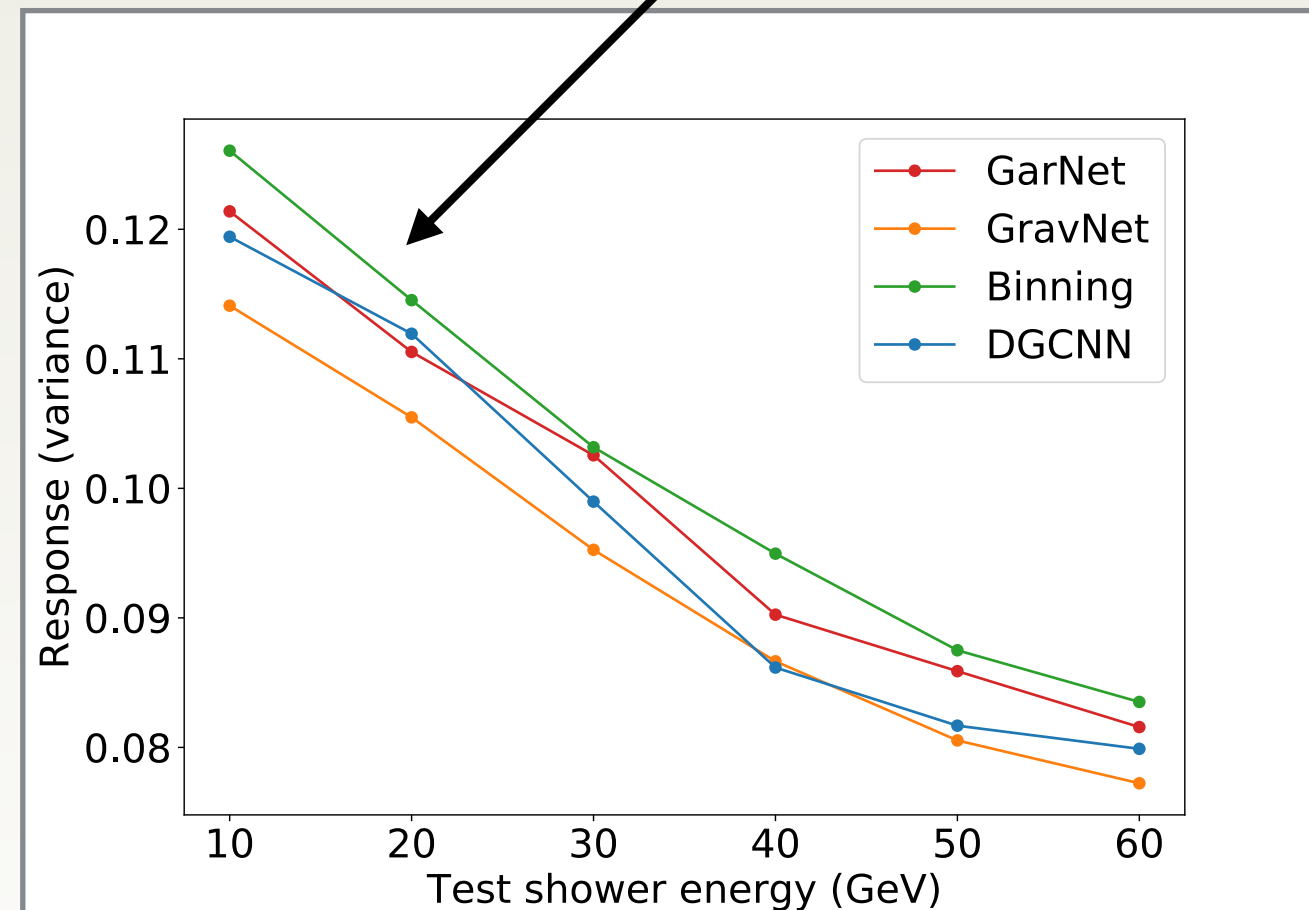
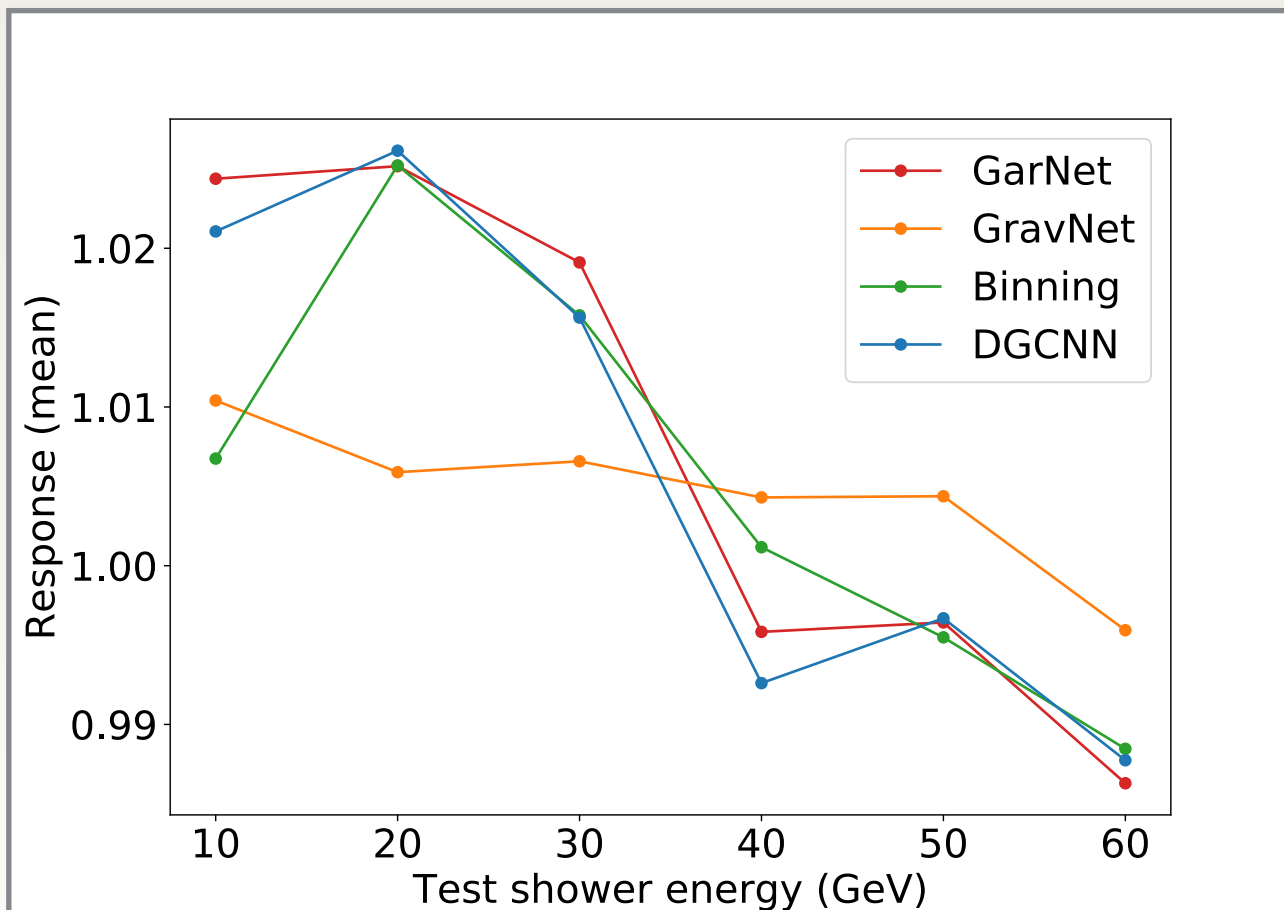


# Quantitative Results

- Focus on the overlap region, only (20-80 % overlap)
- Define energy response

$$R_k = \frac{\sum_i E_i p_{ik}}{\sum_i E_i t_{ik}}$$

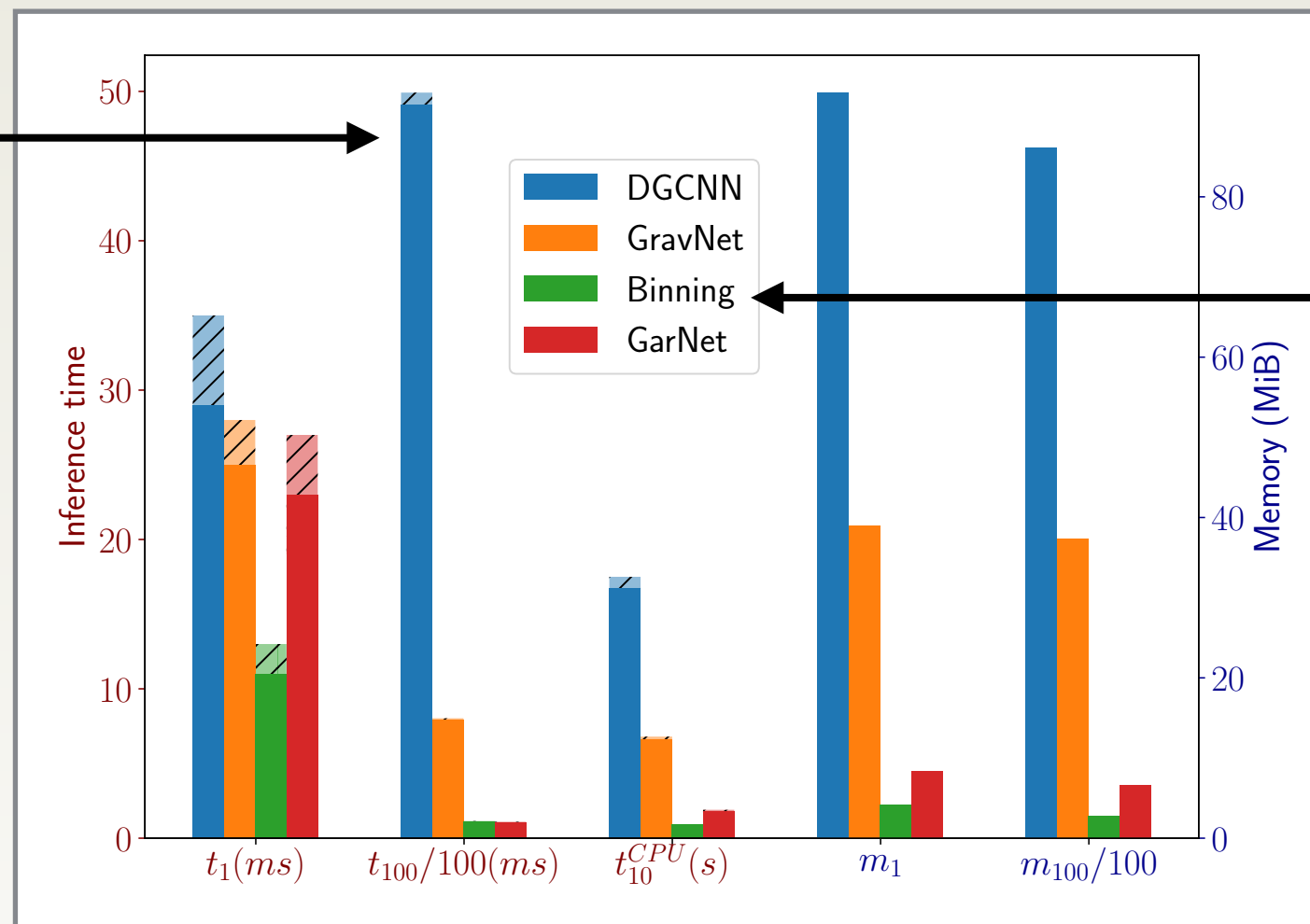
CNN approach  
for comparison



- The graph network based approaches outperform the CNN approach
  - More natural presentation of the detector
- The GravNet model outperforms all approaches



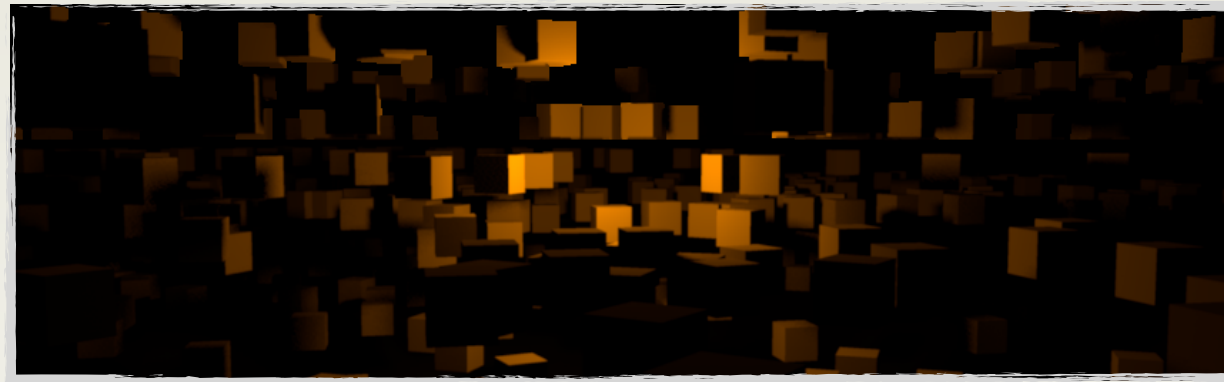
proposal  
from ML literature



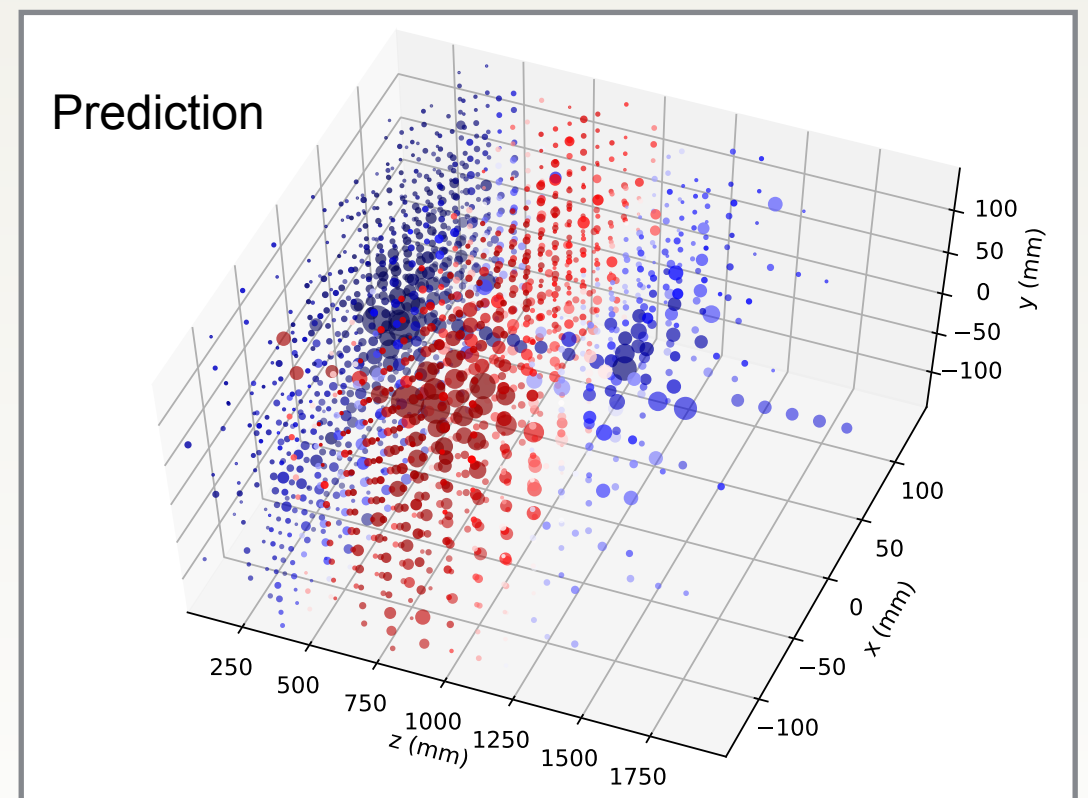
CNN approach  
for comparison

- GravNet better performing and lower resource requirements than proposal from literature (DGCNN)
- GarNet very fast, developed with trigger application in mind
  - CNNs profit from highly optimised code and show worse performance and adaptation power to irregular geometries
  - Room for more improvement, e.g. taking more advantage of sparsity

# Summary



- Presented graph neural network based approaches for clustering / shower segmentation
- Two new graph neural network layer proposals
  - Based on distance weighting in coordinate space
  - Reduced resource requirements
  - Better performance than suggestions in the literature
- Not limited to clustering
  - Currently studying tracking applications
  - Could be interesting for jet tagging/lepton isolation
- Tensorflow & Keras implementation  
<https://github.com/jkiesele/calographNN>
  - Individual ready-to-use layers and full models



S.R. Qasim, JK, Y. Iiyama, M. Pierini  
 arXiv:1902.07987, submitted to EPJC