



SUPER-WEAK FORCE AND NEUTRINO MASSES

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based on 1812.11189

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OUTLINE

1. Status of particle physics

2. $U(1)_Z$ extension of SM

3. UV behavior of the model

Status of particle physics: energy frontier

LEP, LHC: SM describes final states of particle collisions precisely [see amazing ATLAS and CMS contributions Wednesday before lunch]

SM is unstable

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Degrassi et al., arXiv:1205.6497

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Status of particle physics: energy frontier

- LEP, LHC: SM describes final states of particle collisions precisely
- SM is unstable
- No proven sign of new physics beyond SM at colliders* (only exclusion limits)

*There are some indications below discovery significance (such as lepton flavor non-universality in meson decays)

• Universe at large scale described precisely by cosmological SM: Λ CDM ($\Omega_m = 0.3$) [Planck etc]

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 Inflation of the early, accelerated expansion of the present Universe [Planck, SNa1 etc]₆

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Nature is neutral, which is closer to honest

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 There are many extensions proposed, often with the aim of predicting some observable effect at the LHC – but there are none so far, so may give up

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SM is highly efficient – let us stick to efficiency the only exception of economical description is the relatively large number of arbitrary Yukawa couplings

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gauge and gravity anomaly cancellation and

gauge invariant Yukawa terms for neutrino mass generation 9

Fermions

fermion fields:

$$\begin{split} \psi_{q,1}^{f} &= \begin{pmatrix} U^{f} \\ D^{f} \end{pmatrix}_{\mathrm{L}} & \psi_{q,2}^{f} = U_{\mathrm{R}}^{f}, & \psi_{q,3}^{f} = D_{\mathrm{R}}^{f} \\ \psi_{l,1}^{f} &= \begin{pmatrix} \nu^{f} \\ \ell^{f} \end{pmatrix}_{\mathrm{L}} & \psi_{l,2}^{f} = \nu_{\mathrm{R}}^{f}, & \psi_{l,3}^{f} = \ell_{\mathrm{R}}^{f} \\ \psi_{\mathrm{L/R}} &\equiv \psi_{\mp} = \frac{1}{2} \left(1 \mp \gamma_{5} \right) \psi \equiv P_{\mathrm{L/R}} \psi \end{split}$$

where

(v_L can v_R can also be Majorana neutrinos, embedded into different Dirac spinors)

Scalars

Scalar for Φ complex SU(2)_L doublet and χ
 complex singlet:

 $\mathcal{L}_{\phi,\chi} = [D_{\mu}^{(\phi)}\phi]^* D^{(\phi)\mu}\phi + [D_{\mu}^{(\chi)}\chi]^* D^{(\chi)\mu}\chi - V(\phi,\chi)$ with scalar potential

$$V(\phi, \chi) = V_0 - \mu_{\phi}^2 |\phi|^2 - \mu_{\chi}^2 |\chi|^2 + (|\phi|^2, |\chi|^2) \begin{pmatrix} \lambda_{\phi} & \frac{\lambda}{2} \\ \frac{\lambda}{2} & \lambda_{\chi} \end{pmatrix} \begin{pmatrix} |\phi|^2 \\ |\chi|^2 \end{pmatrix}$$

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• After SSB, $G \rightarrow SU(3)_c \times U(1)_{QED}$:

$$\phi = \frac{1}{\sqrt{2}} e^{\mathbf{i} \mathbf{T} \cdot \boldsymbol{\xi}(x)/v} \begin{pmatrix} 0\\ v+h'(x) \end{pmatrix} \& \ \chi(x) = \frac{1}{\sqrt{2}} e^{\mathbf{i} \eta(x)/w} \left(w+s'(x) \right)_{\mathbf{11}}$$

Fermion-scalar interactions

Standard Yukawa terms:

$$\mathcal{L}_{Y} = -\left[c_{D}\left(\bar{U}, \bar{D}\right)_{L} \begin{pmatrix}\phi^{(+)}\\\phi^{(0)}\end{pmatrix} D_{R} + c_{U}\left(\bar{U}, \bar{D}\right)_{L} \begin{pmatrix}\phi^{(0)*}\\-\phi^{(+)*}\end{pmatrix} U_{R} + c_{\ell}\left(\bar{\nu}_{\ell}, \bar{\ell}\right)_{L} \begin{pmatrix}\phi^{(+)}\\\phi^{(0)}\end{pmatrix} \ell_{R}\right] + h.c.$$

lead to fermion masses after SSB:

$$\mathcal{L}_{\mathrm{Y}} = -\left(1 + \frac{h(x)}{v}\right) \left[\bar{D}_{\mathrm{L}} M_D D_{\mathrm{R}} + \bar{U}_{\mathrm{L}} M_U U_{\mathrm{R}} + \bar{\ell}_{\mathrm{L}} M_\ell \ell_{\mathrm{R}}\right] + \mathrm{h.c.}$$

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• Neutrino Yukawa terms $(z_{\chi} = -2z_{\nu_{\mathrm{R}}})$: $\mathcal{L}_{\mathrm{Y}}^{\nu} = -\sum_{i,j} \left((c_{\nu})_{ij} \overline{L}_{i,\mathrm{L}} \cdot \tilde{\phi} \nu_{j,\mathrm{R}} + \frac{1}{2} (c_{\mathrm{R}})_{ij} \overline{\nu_{i,\mathrm{R}}^{c}} \nu_{j,\mathrm{R}} \chi \right) + \mathrm{h.c.}$ 12

After SSB neutrino mass terms appear

$$\mathcal{L}_{\mathbf{Y}}^{\nu} = -\frac{1}{2} \sum_{i,j} \left[\left(\overline{\nu_{\mathbf{L}}}, \ \overline{\nu_{\mathbf{R}}^c} \right)_i M(h,s)_{ij} \left(\begin{array}{c} \nu_{\mathbf{L}}^c \\ \nu_{\mathbf{R}} \end{array} \right)_j + \text{h.c.} \right]$$

where

$$M(h,s)_{ij} = \begin{pmatrix} 0 & m_{\rm D} \left(1+\frac{h}{v}\right) \\ m_{\rm D} \left(1+\frac{h}{v}\right) & M_{\rm M} \left(1+\frac{s}{w}\right) \end{pmatrix}_{ij}$$

6x6 symmetric matrix (*m*_D complex, *M*_M real)

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but v_L and v_R have the same q-numbers, can mix, leading to see-saw l

Effective light neutrino masses

If $m_i << M_j$, can integrate out the heavy neutrinos

$$\mathcal{L}_{\mathrm{dim}-5}^{\nu} = -\frac{1}{2} \sum_{i} m_{\mathrm{M},i} \left(1 + \frac{h}{v}\right)^{2} \left(\overline{\nu_{i,\mathrm{L}}^{\prime c}} \nu_{i,\mathrm{L}}^{\prime} + \mathrm{h.c.}\right)^{2}$$

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where $m_{\mathrm{M},i} = \frac{m_i^2}{M_i}$ are Majorana masses

if $m_i \sim O(100 \text{keV})$ and $M_j \sim O(100 \text{GeV})$, then

 $m_{M,i} \sim O(0.1 eV)$

Mixing in the neutral gauge sector

$$\begin{pmatrix} W_{\mu}^{3} \\ B_{\mu}' \\ Z_{\mu}' \end{pmatrix} = \underline{M}(\sin\theta_{\rm W}, \sin\theta_{\rm T}) \begin{pmatrix} Z_{\mu}^{0} \\ T_{\mu} \\ A_{\mu} \end{pmatrix}$$

QED current remains unchanged:

$$\mathcal{L}_{\text{QED}} = -eA_{\mu}J^{\mu}_{\text{em}}, \quad J^{\mu}_{\text{em}} = \sum_{f=1}^{3}\sum_{j=1}^{3}e_{j}\left(\overline{\psi}^{f}_{q,j}(x)\gamma^{\mu}\psi^{f}_{q,j}(x) + \overline{\psi}^{f}_{l,j}(x)\gamma^{\mu}\psi^{f}_{l,j}(x)\right)$$

Neutral current interactions

$$\mathcal{L}_{Z^0} = -eZ^0_\mu \Big(\cos\theta_T J^\mu_{Z^0} + \sin\theta_T J^\mu_T\Big) = -eZ^0_\mu J^\mu_{Z^0} + O(\theta_T)$$
$$\mathcal{L}_T = -eT_\mu \Big(\sin\theta_T J^\mu_{Z^0} + \cos\theta_T J^\mu_T\Big) = -eT_\mu J^\mu_T + O(\theta_T)$$

current with Z⁰ remains unchanged:

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but mixes with new current of new couplings: $J_{\rm T}^{\mu} = \sum_{f=1}^{3} \sum_{j=1}^{3} \frac{\gamma'_{Z} r_{j} + \gamma'_{ZY} y_{j}}{\sin \theta_{\rm W}} \Big(\overline{\psi}_{q,j}^{f}(x) \gamma^{\mu} \psi_{q,j}^{f}(x) + \overline{\psi}_{l,j}^{f}(x) \gamma^{\mu} \psi_{l,j}^{f}(x) \Big)$

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- The second scalar together with the established BEH field may be the source of inflation.

Credibility requirement

Is there any region of the parameter space of the model that is not excluded by experimental results, both established in standard model phenomenology and elsewhere?

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Answer is not immediate, extensive studies are needed



An immediate objection(?): such neutral gauge bosons are excluded

new searches will be sensitive to masses below 1 MeV [e.g. SENSEI: 1804.00088]



An imme contribution of the

le: boson to aμ

using the new neutral currents:

$$\Delta a_{\mu} = a_{\mu}^{(T+SM)} - a_{\mu}^{(SM)} = a_{\mu}^{(Z^{0})} - a_{\mu}^{(Z^{0})}(0,0) + a_{\mu}^{(T^{0})}$$
where

$$a_{\mu}^{(\mathbb{Z}^{0})}(h_{f},\theta_{T}) = \frac{G_{\mathrm{F}}m_{\mu}^{2}}{6\sqrt{2}\pi^{2}} \left[2\sin\theta_{\mathrm{W}}(h_{f}\cos\theta_{\mathrm{W}}\sin\theta_{T} - \sin\theta_{\mathrm{W}}\cos\theta_{T}) \\ \times \left(2\sin\theta_{\mathrm{W}}(h_{f}\cos\theta_{\mathrm{W}}\sin\theta_{T} - \sin\theta_{\mathrm{W}}\cos\theta_{T}) + \cos\theta_{T} \right) - \cos^{2}\theta_{T} \right] \\ a_{\mu}^{(\mathrm{T}^{0})}(h_{f},\theta_{T}) = \frac{G_{\mathrm{F}}m_{\mu}^{2}}{6\sqrt{2}\pi^{2}} \frac{M_{\mathbb{Z}^{0}}^{2}}{M_{\mathrm{T}^{0}}^{2}} \left[2\sin\theta_{\mathrm{W}}(h_{f}\cos\theta_{\mathrm{W}}\cos\theta_{T} + \sin\theta_{\mathrm{W}}\sin\theta_{T}) \\ \times \left(2\sin\theta_{\mathrm{W}}(h_{f}\cos\theta_{\mathrm{W}}\cos\theta_{T} + \sin\theta_{\mathrm{W}}\sin\theta_{T}) - \sin^{2}\theta_{T} \right) \right] \\ \times \left(2\sin\theta_{\mathrm{W}}(h_{f}\cos\theta_{\mathrm{W}}\cos\theta_{T} + \sin\theta_{\mathrm{W}}\sin\theta_{T}) - \sin^{2}\theta_{T} \right) \right]$$

An immediate example: contribution of the new gauge boson to a_μ





with Zoltán Péli

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Perturbative RG flows

- New couplings are small, hence can use PT
- All β-functions derived at one loop (slightly differ for Dirac or Majorana neutrinos)
- Constrain scalar couplings by assuming that the new model remains stable up to $M_{\rm P1}$
- Among new couplings the flow is most sensitive to the largest neutrino Yukawa coupling (c_v)

Initial values set at m_t

$$g_Y(m_t) = \sqrt{\frac{3}{5}} \times 0.4626$$
, $g_L(m_t) = 0.6477$, $g_3(m_t) = 1.166$,
 $c_t(m_t) = 0.9379$, $\mu_{\phi}(m_t) = 131.5 \,\text{GeV}$, $\lambda_{\phi}(m_t) = 0.1259$.

allowed regions at fixed values of the largest neutrino Yukawa coupling c_v for both Dirac and Majorana neutrinos

Scalar parameters allowed for stability



Scalar parameters allowed for stability with Majorana neutrinos



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The parameter space vanishes rapidly above $c_v = 1$ The parameter space disappears completely for $c_t = 1$

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- U(1)_Z extension has the potential of explaining all known results
- Anomaly cancellation and neutrino mass generation mechanism are used to fix the Z-charges up to reasonable assumptions
- Parameter space can be constrained from and should be confronted with existing experimental results