

MANCHESTER  
1824

University of Manchester

BESIII

# Open Charm at BESIII

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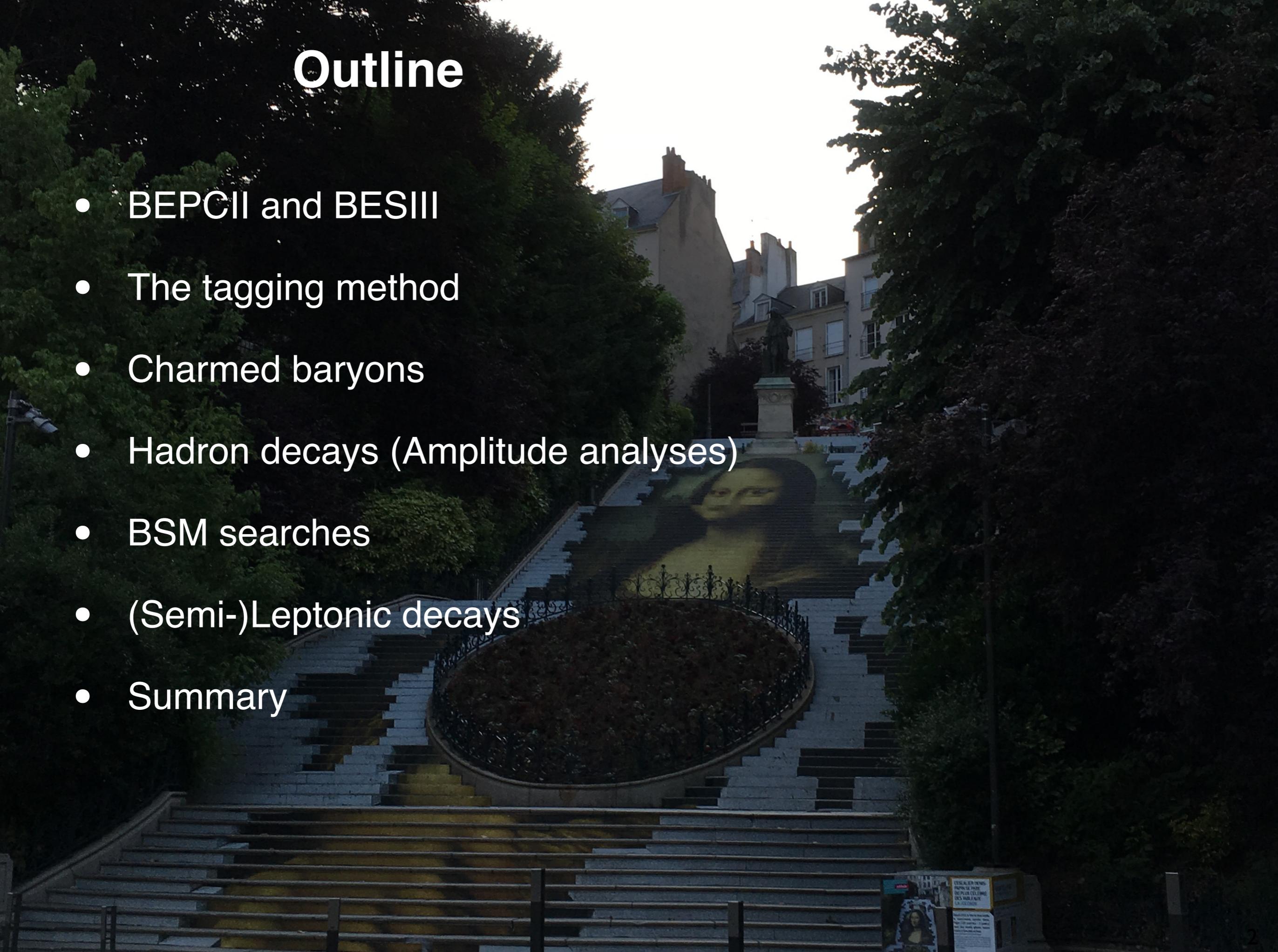
on behalf of the BESIII collaboration

31st Rencontres de Blois, June 2-7, 2019, Blois

THE  
ROYAL  
SOCIETY

# Outline

- BEPCII and BESIII
- The tagging method
- Charmed baryons
- Hadron decays (Amplitude analyses)
- BSM searches
- (Semi-)Leptonic decays
- Summary

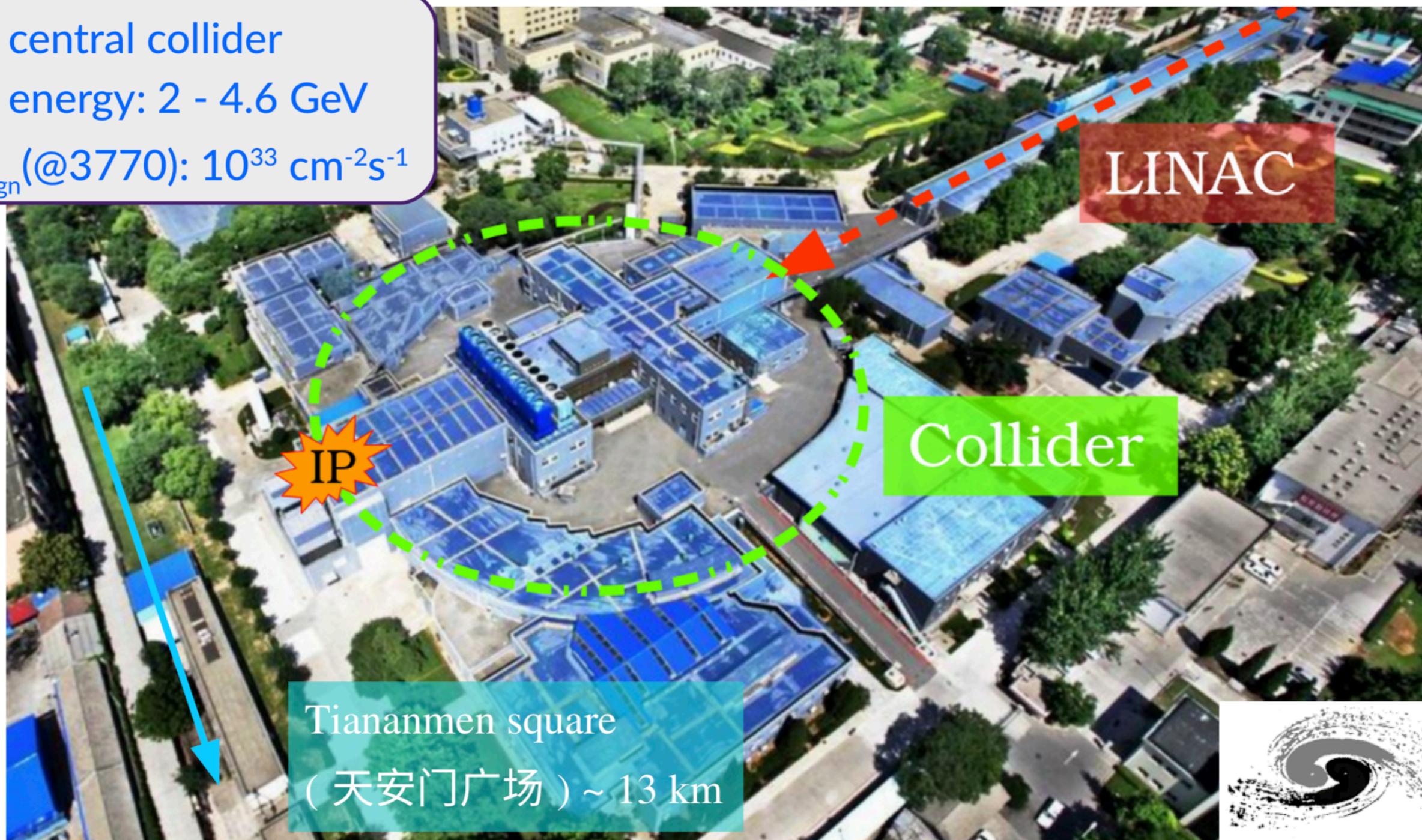


# BEPCII @ IHEP (Beijing, PRC)

$e^+e^-$  central collider

CM energy: 2 - 4.6 GeV

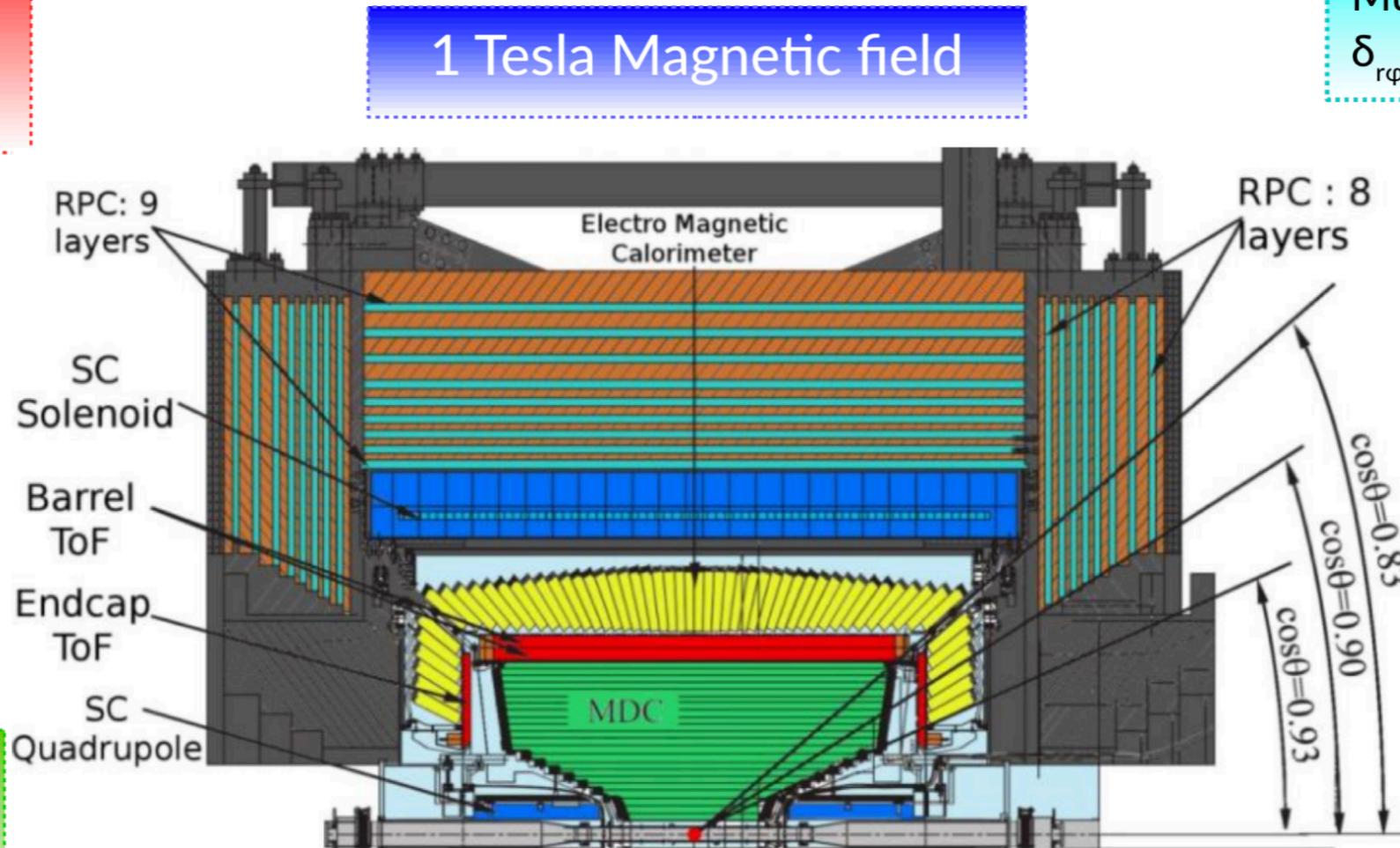
$L_{\text{design}} (@3770): 10^{33} \text{ cm}^{-2}\text{s}^{-1}$



# BESIII @ BEPCII

Time Of Flight:  
 $\sigma_t$  (barrel) = 90 ps  
 $\sigma_t$  (endcap) = 110 ps

Muon counters:  
 $\delta_{r\phi} = 1.4 \text{ cm} - 1.7 \text{ cm}$



Electromagnetic  
 Calorimeter:  
 $dE/\sqrt{E} (1 \text{ GeV}) = 2.5 \%$

Main Drift Chamber:  
 $\sigma_x (1 \text{ GeV}/c) \sim 130 \mu\text{m}$   
 $dp/p (1 \text{ GeV}/c) = 0.5 \%$

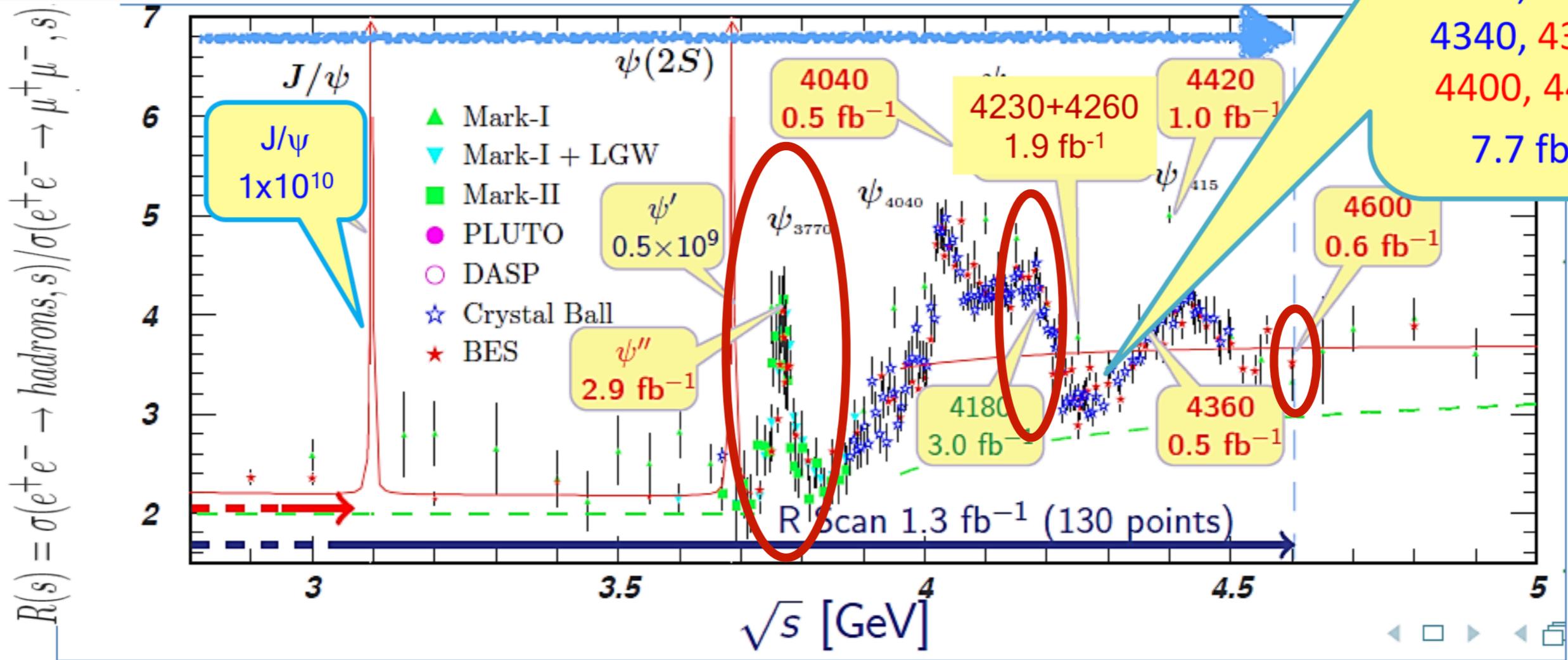
hermetic

barrel  $|\cos\theta| < 0.83$

endcap  $0.85 < |\cos\theta| < 0.93$

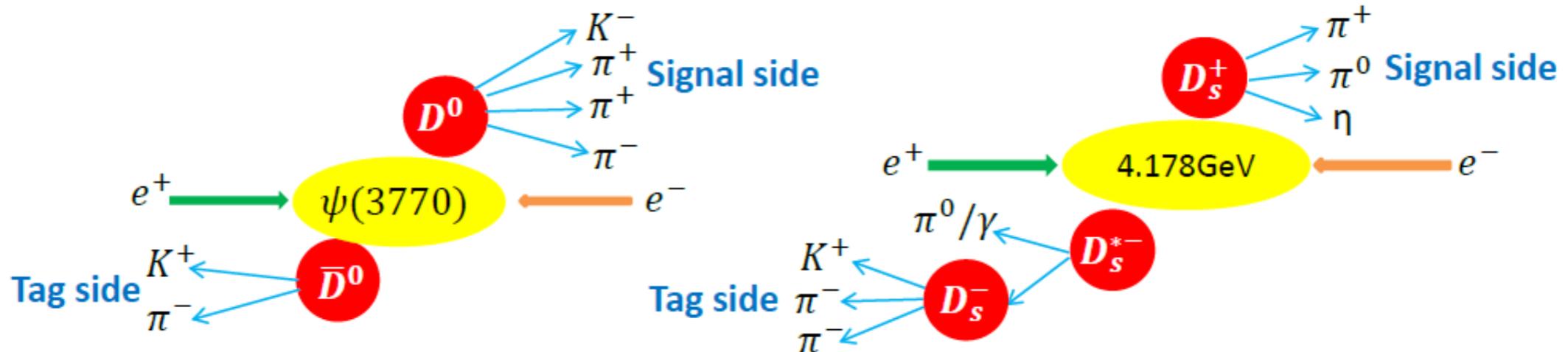
# Collected datasets

Optimised for flavour physics in the tau-charm region



# Tagging method for charm@threshold

- Single tag: fully reconstruct the signal  $D_{(s)}$ ,  $\Lambda_c$
- Double tag:
  - Fully reconstruct the tag  $D_{(s)}$ ,  $\Lambda_c$  taking advantage of kinematic constraints
  - Search for the signal mode in the recoil system
  - Possible to measure absolute Branching Fraction



@ threshold = full kinematic constraint of the decays

Excellent for neutral and invisible particles

$$\Delta E = E_D - E_{\text{Beam}}$$

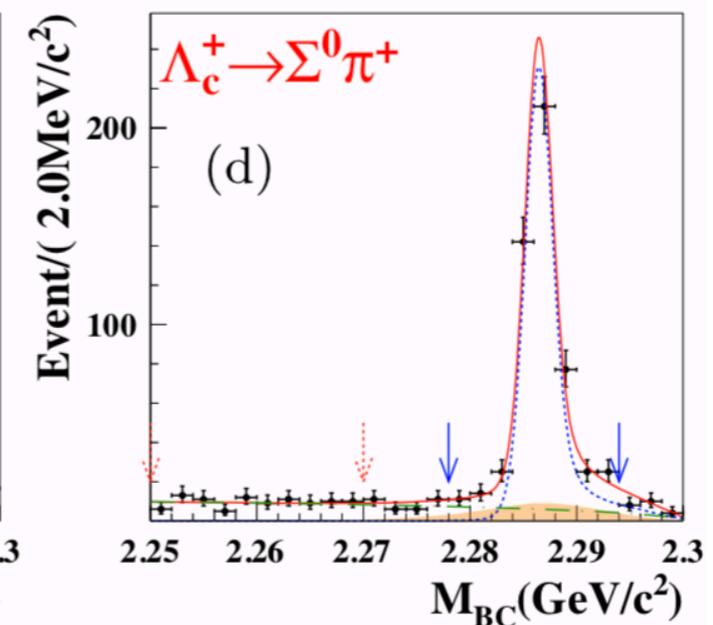
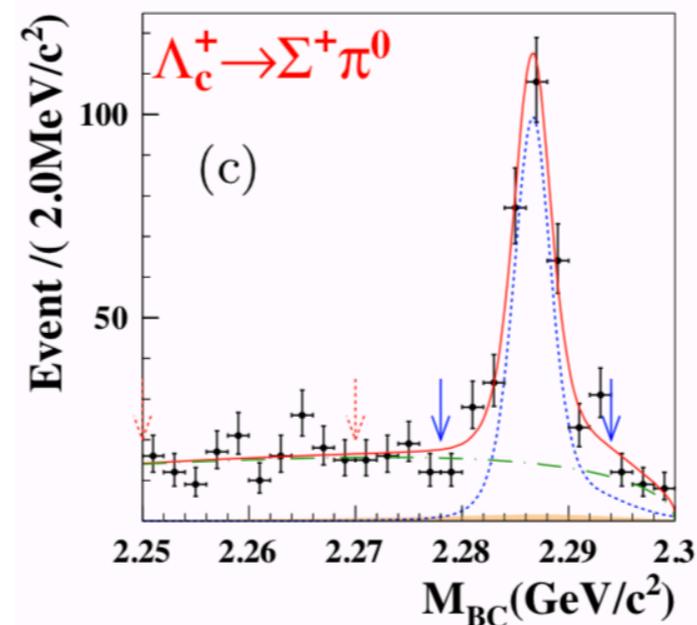
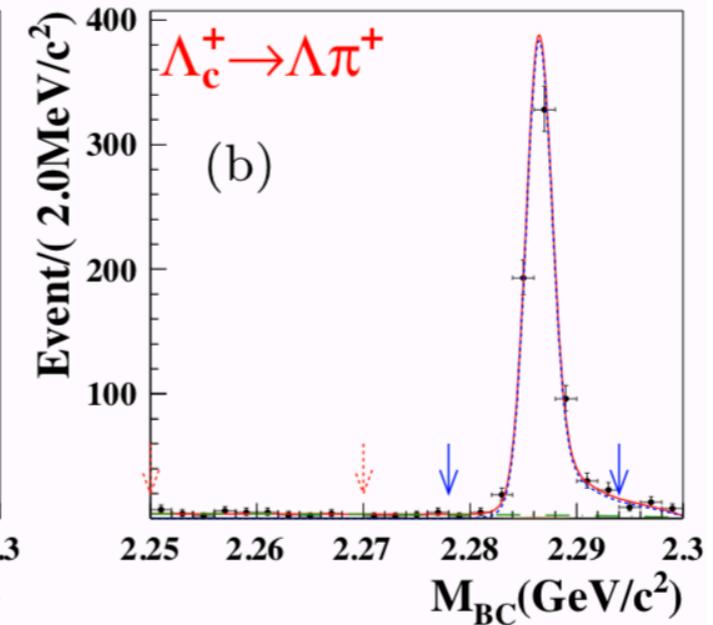
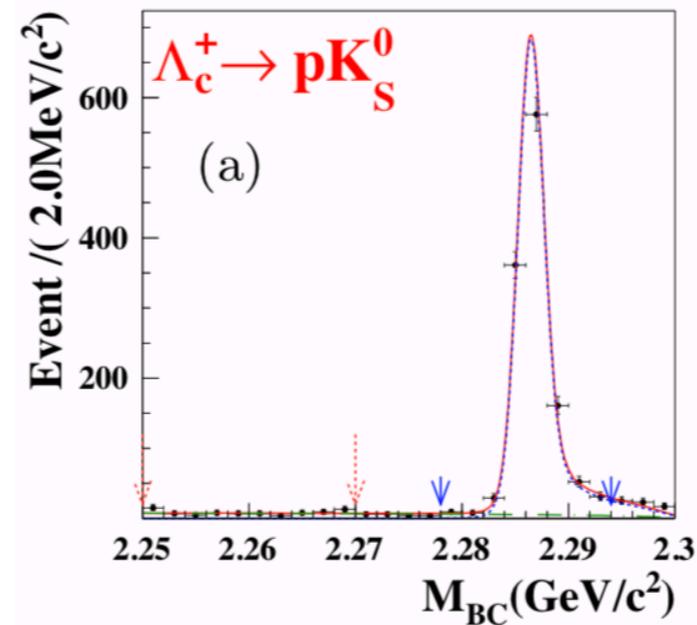
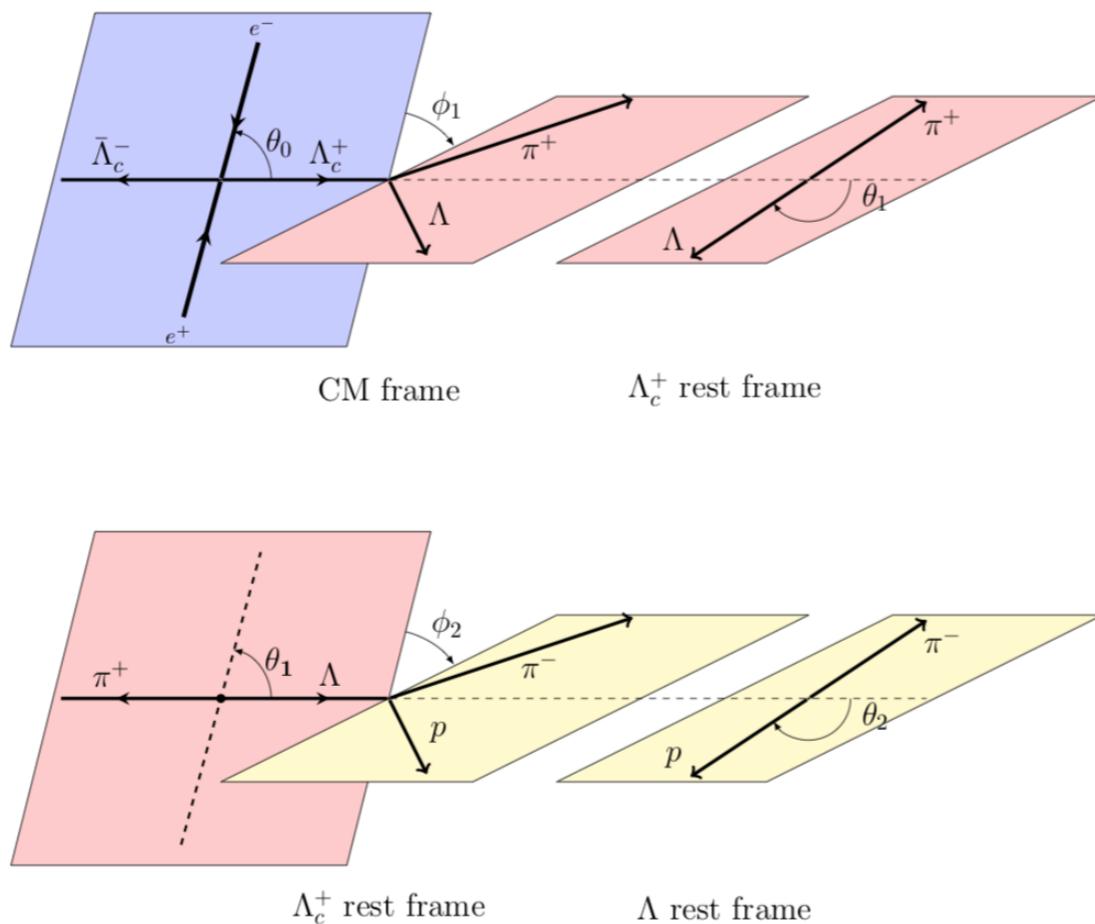
$$M_{\text{BC}} = \sqrt{E_{\text{Beam}}^2 - p_D^2}$$

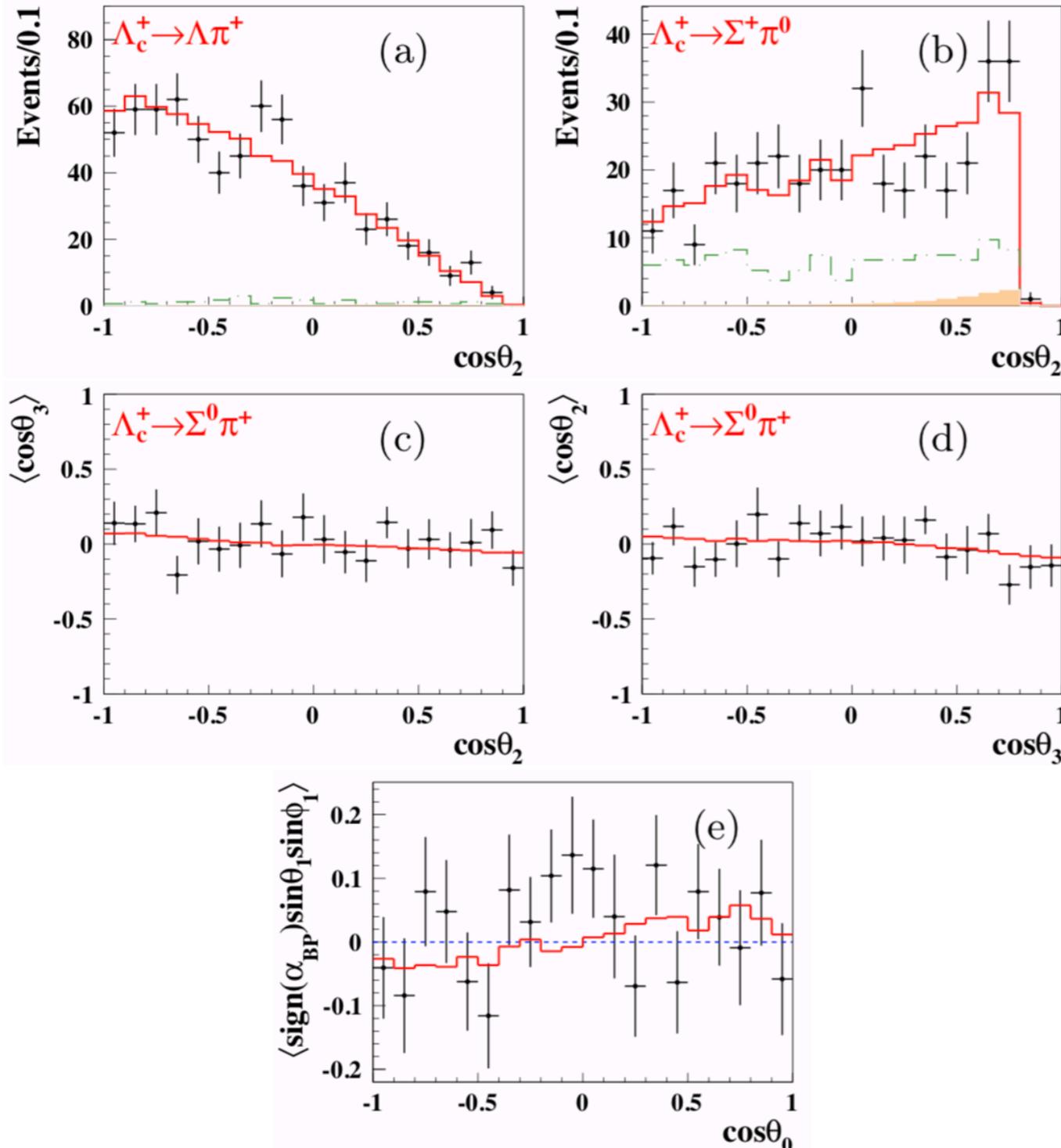
# Weak Decay Asymmetries of $\Lambda_c^+ \rightarrow pK_S^0$ , $\Lambda\pi^+$ , $\Sigma^+\pi^0$ , and $\Sigma^0\pi^+$

567 pb<sup>-1</sup> @ 4600 MeV

[arXiv:1905.04707](https://arxiv.org/abs/1905.04707)

- Measure the weak asymmetry  $\alpha_{BP}^+ \equiv \frac{2\text{Re}(s \cdot p)}{|s|^2 + |p|^2}$  via a full angular analysis carried out simultaneously on the 4 signal modes
- Single tag method





Decay asymmetry parameters  $\alpha^+$ :

$\Lambda_c^+ \rightarrow p K_S^0$ :  $0.18 \pm 0.43(\text{stat}) \pm 0.14(\text{syst})$  ★ new

$\Lambda_c^+ \rightarrow \Lambda \pi^+$ :  $-0.80 \pm 0.11(\text{stat}) \pm 0.02(\text{syst})$

$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$ :  $-0.57 \pm 0.10(\text{stat}) \pm 0.07(\text{syst})$  ★ best

$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$ :  $-0.73 \pm 0.17(\text{stat}) \pm 0.07(\text{syst})$  ★ new

$\alpha^+_{\Sigma^+ \pi^0}$ : negative sign rules out several positive predictions

$\alpha^+_{\Sigma \pi}$  results agree well: hyperon isospin symmetry

First study of  $\Lambda_c$  transverse polarisation

$$\mathcal{P}_T(\cos \theta_0) \equiv \sqrt{1 - \alpha_0^2} \cos \theta_0 \sin \theta_0 \sin \Delta_0$$

in unpolarised  $e^+e^-$  collisions

$$\sin \Delta_0 = -0.28 \pm 0.13 \pm 0.03$$

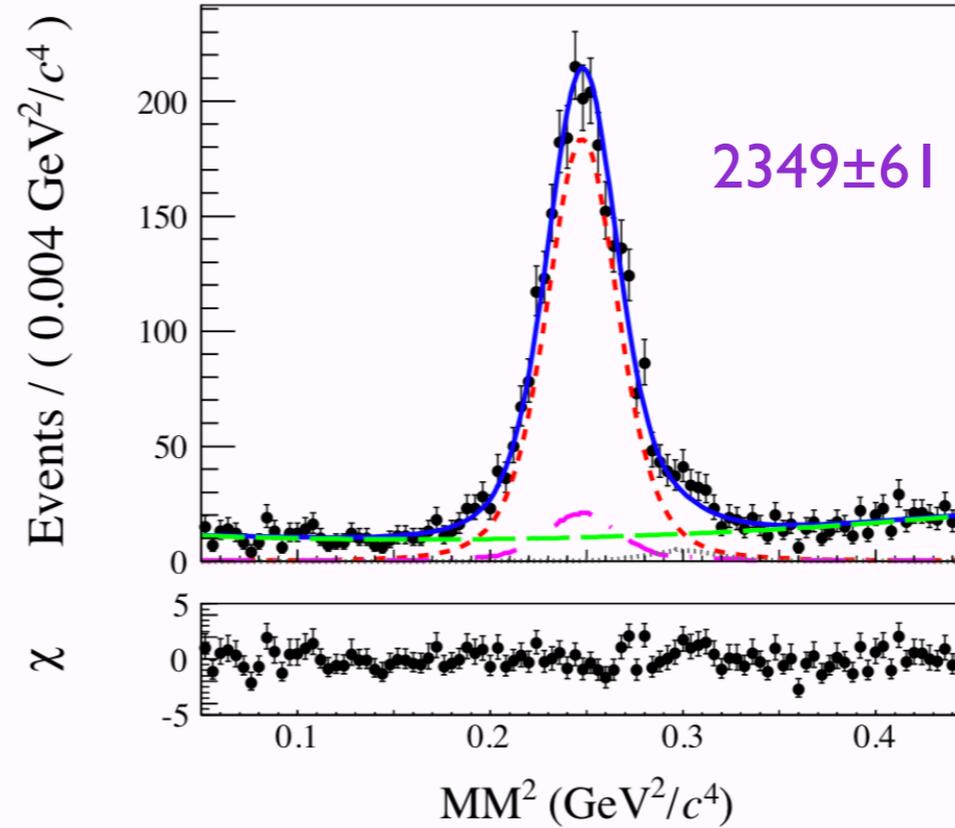
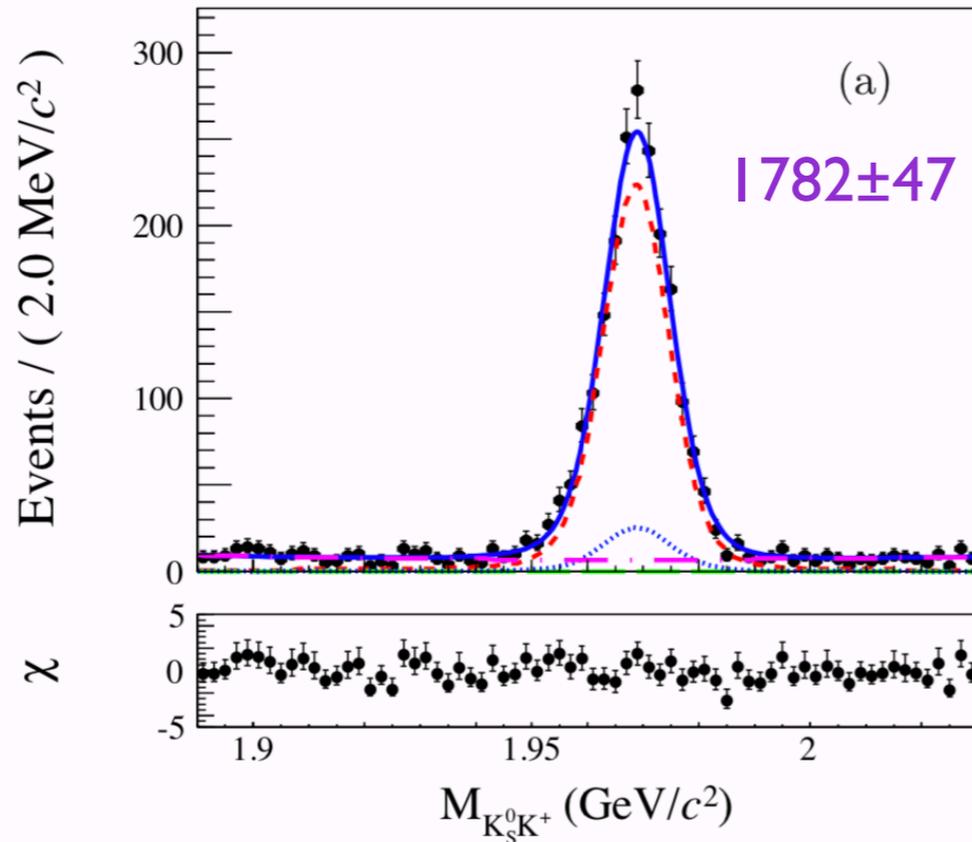
Effect with a  $2.1\sigma$  statistical significance

# Study of the Decays $D_s^+ \rightarrow K_S^0 K^+$ and $K_L^0 K^+$

3.19 fb<sup>-1</sup> @ 4178 MeV

arXiv:1903.04164

- Double tag analysis  $e^+e^- \rightarrow D_s^{*\pm} D_s^\mp \rightarrow \gamma D_s^+ D_s^-$



Tag mode
$K^+ K^- \pi^-$
$K^- \pi^+ \pi^-$
$\pi^+ \pi^- \pi^-$
$K^+ K^- \pi^- \pi^0$
$\pi^- \eta'_{\gamma\rho^0}$
$\rho^- \eta$
$K_S^0 K^- \pi^+ \pi^-$
$K_S^0 K^+ \pi^- \pi^-$
$K_S^0 K^- \pi^0$
$K_S^0 K_S^0 \pi^-$
$\pi^- \eta$
$\pi^- \eta'_{\pi^+ \pi^- \eta}$
$\pi^- \eta_{\pi^+ \pi^- \pi^0}$

$$\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) = (1.425 \pm 0.038_{\text{stat.}} \pm 0.031_{\text{syst.}})\% \quad \mathcal{B}(D_s^+ \rightarrow K_L^0 K^+) = (1.485 \pm 0.039_{\text{stat.}} \pm 0.046_{\text{syst.}})\%$$

$$A_{\text{CP}}(D_s^+ \rightarrow K_S^0 K^+) = (0.6 \pm 2.8(\text{stat}) \pm 0.6(\text{syst}))\%$$

$$A_{\text{CP}}(D_s^+ \rightarrow K_L^0 K^+) = (-1.1 \pm 2.6(\text{stat}) \pm 0.6(\text{syst}))\%$$

## $K_S$ - $K_L$ asymmetry

$$\frac{\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) - \mathcal{B}(D_s^+ \rightarrow K_L^0 K^+)}{\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) + \mathcal{B}(D_s^+ \rightarrow K_L^0 K^+)} = (-2.1 \pm 1.9_{\text{stat.}} \pm 1.6_{\text{syst.}})\%$$

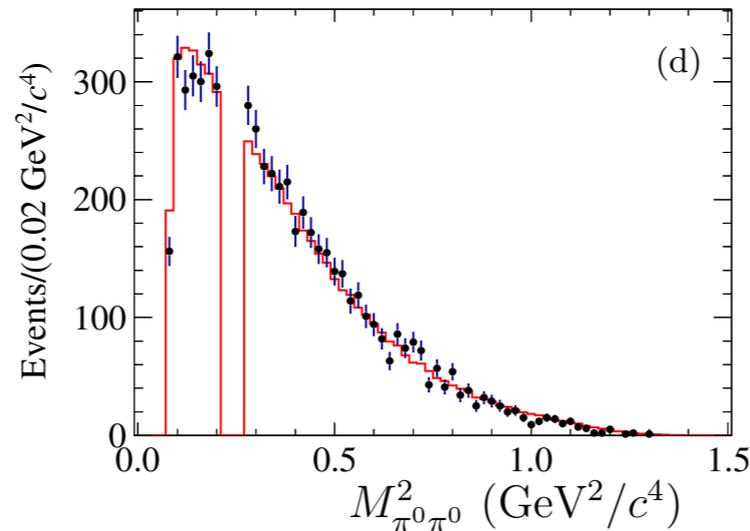
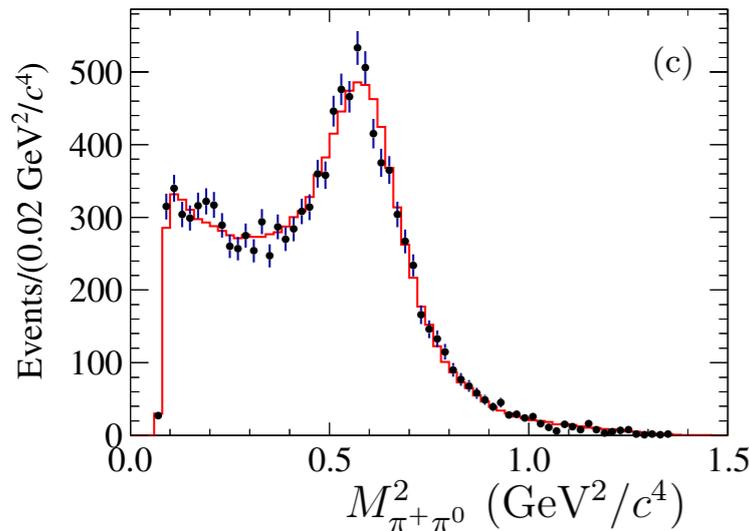
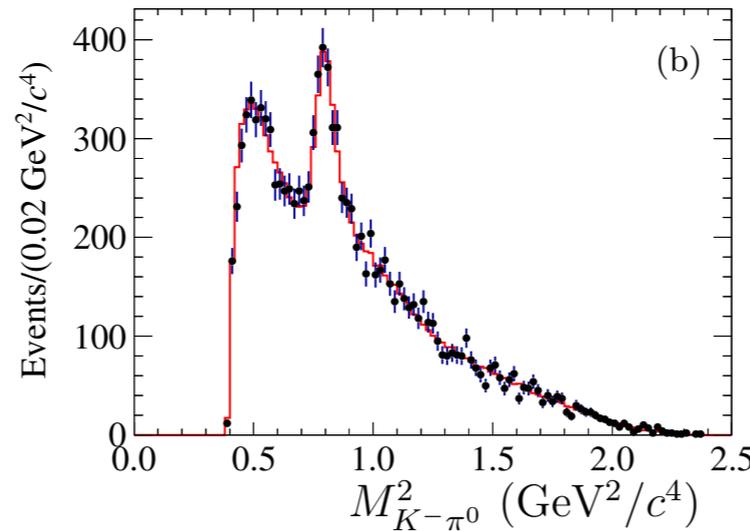
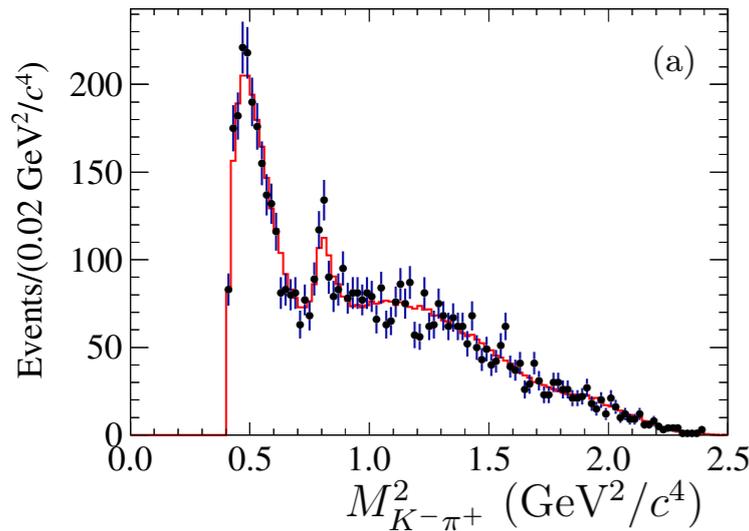
# Amplitude Analysis of $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$

2.93 fb<sup>-1</sup> @ 3773 MeV

[arXiv:1903.06316](https://arxiv.org/abs/1903.06316)

- Double tag analysis: tag mode:  $\bar{D}^0 \rightarrow K^+ \pi^-$
  - 6100 events with 99% purity used for amplitude analysis
  - $B(D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0) = (8.86 \pm 0.13(\text{stat}) \pm 0.19(\text{syst}))\%$
- First measurement of  $D^0 \rightarrow K \pi \pi \pi$  with more than one  $\pi^0$

The dominant amplitude is  $K^- a_1(1260)^+$



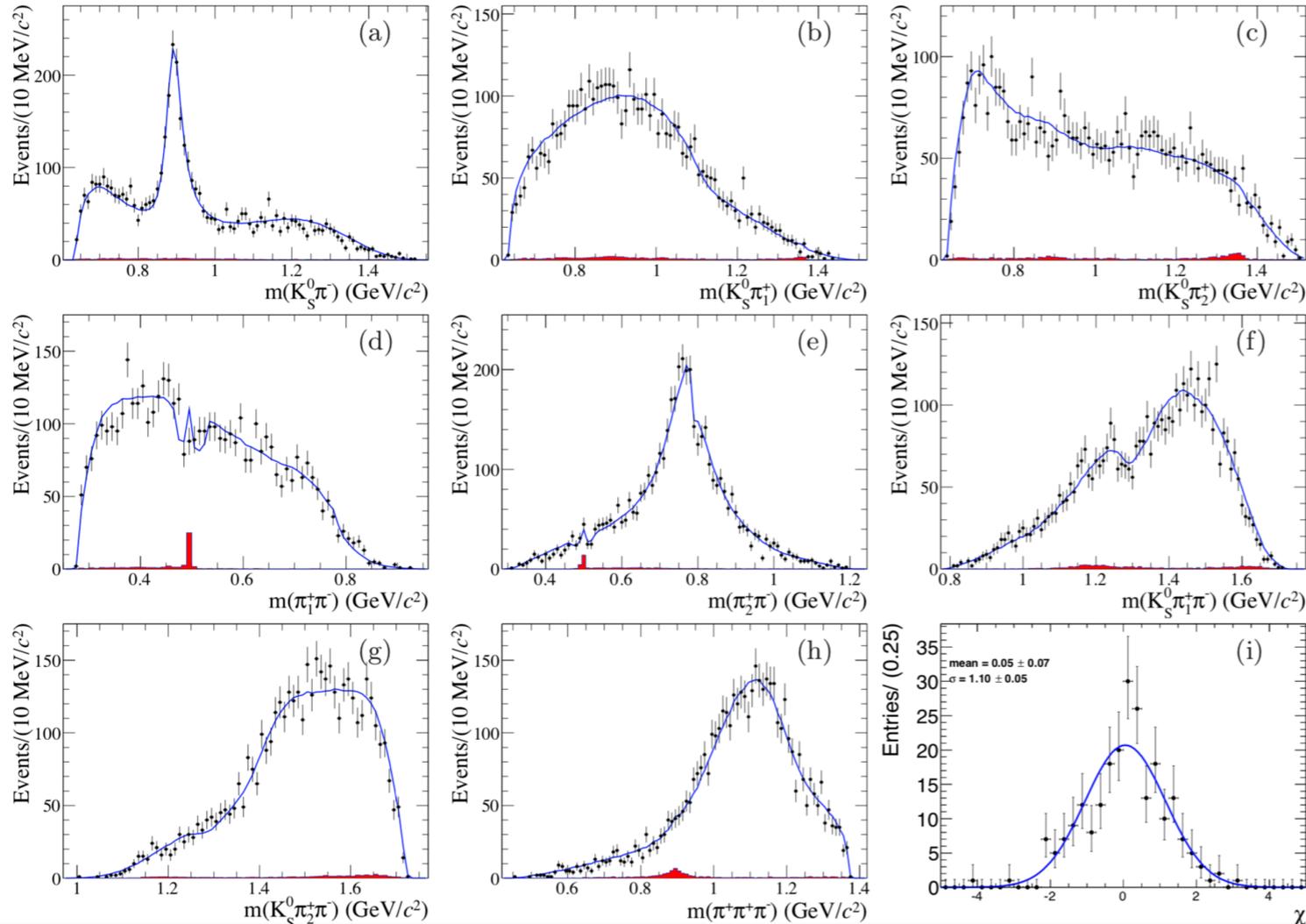
Amplitude mode	FF (%)	Phase ( $\phi$ )	Significance ( $\sigma$ )
$D \rightarrow SS$			
$D \rightarrow (K^- \pi^+)_{S\text{-wave}}(\pi^0 \pi^0)_S$	$6.92 \pm 1.44 \pm 2.86$	$-0.75 \pm 0.15 \pm 0.47$	$> 10$
$D \rightarrow (K^- \pi^0)_{S\text{-wave}}(\pi^+ \pi^0)_S$	$4.18 \pm 1.02 \pm 1.77$	$-2.90 \pm 0.19 \pm 0.47$	6.0
$D \rightarrow AP, A \rightarrow VP$			
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [S]$	$28.36 \pm 2.50 \pm 3.53$	0 (fixed)	$> 10$
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [D]$	$0.68 \pm 0.29 \pm 0.30$	$-2.05 \pm 0.17 \pm 0.25$	6.1
$D \rightarrow K_1(1270)^- \pi^+, K^{*-} \pi^0 [S]$	$0.15 \pm 0.09 \pm 0.15$	$1.84 \pm 0.34 \pm 0.43$	4.9
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [S]$	$0.39 \pm 0.18 \pm 0.30$	$-1.55 \pm 0.20 \pm 0.26$	4.8
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [D]$	$0.11 \pm 0.11 \pm 0.11$	$-1.35 \pm 0.43 \pm 0.48$	4.0
$D \rightarrow K_1(1270)^0 \pi^0, K^- \rho^+ [S]$	$2.71 \pm 0.38 \pm 0.29$	$-2.07 \pm 0.09 \pm 0.20$	$> 10$
$D \rightarrow (K^{*-} \pi^0)_A \pi^+, K^{*-} \pi^0 [S]$	$1.85 \pm 0.62 \pm 1.11$	$1.93 \pm 0.10 \pm 0.15$	7.8
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [S]$	$3.13 \pm 0.45 \pm 0.58$	$0.44 \pm 0.12 \pm 0.21$	$> 10$
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [D]$	$0.46 \pm 0.17 \pm 0.29$	$-1.84 \pm 0.26 \pm 0.42$	5.9
$D \rightarrow (\rho^+ K^-)_A \pi^0, K^- \rho^+ [D]$	$0.75 \pm 0.40 \pm 0.60$	$0.64 \pm 0.36 \pm 0.53$	5.1
$D \rightarrow AP, A \rightarrow SP$			
$D \rightarrow ((K^- \pi^+)_{S\text{-wave}} \pi^0)_A \pi^0$	$1.99 \pm 1.08 \pm 1.55$	$-0.02 \pm 0.25 \pm 0.53$	7.0
$D \rightarrow VS$			
$D \rightarrow (K^- \pi^0)_{S\text{-wave}} \rho^+$	$14.63 \pm 1.70 \pm 2.41$	$-2.39 \pm 0.11 \pm 0.35$	$> 10$
$D \rightarrow K^{*-} (\pi^+ \pi^0)_S$	$0.80 \pm 0.38 \pm 0.26$	$1.59 \pm 0.19 \pm 0.24$	4.1
$D \rightarrow K^{*0} (\pi^0 \pi^0)_S$	$0.12 \pm 0.12 \pm 0.12$	$1.45 \pm 0.48 \pm 0.51$	4.1
$D \rightarrow VP, V \rightarrow VP$			
$D \rightarrow (K^{*-} \pi^+)_V \pi^0$	$2.25 \pm 0.43 \pm 0.45$	$0.52 \pm 0.12 \pm 0.17$	$> 10$
$D \rightarrow VV$			
$D \rightarrow K^{*-} \rho^+ [S]$	$5.15 \pm 0.75 \pm 1.28$	$1.24 \pm 0.11 \pm 0.23$	$> 10$
$D \rightarrow K^{*-} \rho^+ [P]$	$3.25 \pm 0.55 \pm 0.41$	$-2.89 \pm 0.10 \pm 0.18$	$> 10$
$D \rightarrow K^{*-} \rho^+ [D]$	$10.90 \pm 1.53 \pm 2.36$	$2.41 \pm 0.08 \pm 0.16$	$> 10$
$D \rightarrow (K^- \pi^0)_V \rho^+ [P]$	$0.36 \pm 0.19 \pm 0.27$	$-0.94 \pm 0.19 \pm 0.28$	5.7
$D \rightarrow (K^- \pi^0)_V \rho^+ [D]$	$2.13 \pm 0.56 \pm 0.92$	$-1.93 \pm 0.22 \pm 0.25$	$> 10$
$D \rightarrow K^{*-} (\pi^+ \pi^0)_V [D]$	$1.66 \pm 0.52 \pm 0.61$	$-1.17 \pm 0.20 \pm 0.39$	7.6
$D \rightarrow (K^- \pi^0)_V (\pi^+ \pi^0)_V [S]$	$5.17 \pm 1.91 \pm 1.82$	$-1.74 \pm 0.20 \pm 0.31$	7.6
$D \rightarrow TS$			
$D \rightarrow (K^- \pi^+)_{S\text{-wave}}(\pi^0 \pi^0)_T$	$0.30 \pm 0.21 \pm 0.30$	$-2.93 \pm 0.31 \pm 0.82$	5.8
$D \rightarrow (K^- \pi^0)_{S\text{-wave}}(\pi^+ \pi^0)_T$	$0.14 \pm 0.12 \pm 0.10$	$2.23 \pm 0.38 \pm 0.65$	4.0

# Amplitude analysis of $D^+ \rightarrow K^0_S \pi^+ \pi^+ \pi^-$

2.93 fb<sup>-1</sup> @ 3773 MeV

[arXiv:1901.05936](https://arxiv.org/abs/1901.05936)

- Double tag analysis: tag mode  $D^- \rightarrow K^+ \pi^- \pi^-$
- 4559 events with 97.5% purity used for amplitude analysis
- BF of the components determined as well, with significantly improved precision



The dominant amplitude is  $K^0_S a_1(1260)^+$

Comparing with  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ : larger contribution for  $D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+$  by an order of magnitude

Amplitude	Significance ( $\sigma$ )	Phase	FF
$D^+ \rightarrow K^0_S a_1(1260)^+ (\rho^0 \pi^+ [S])$	> 10	0.0 (fixed)	$0.384 \pm 0.021 \pm 0.029$
$D^+ \rightarrow K^0_S a_1(1260)^+ (\rho^0 \pi^+ [D])$	4.3	$-1.55 \pm 0.16 \pm 0.22$	$0.004 \pm 0.002 \pm 0.001$
$D^+ \rightarrow K^0_S a_1(1260)^+ (\rho^0 \pi^+)$	-	-	$0.403 \pm 0.021 \pm 0.029$
$D^+ \rightarrow K^0_S a_1(1260)^+ (f_0(500) \pi^+)$	> 10	$-1.82 \pm 0.08 \pm 0.10$	$0.055 \pm 0.007 \pm 0.017$
$D^+ \rightarrow \bar{K}_1(1400)^0 (K^{*-} \pi^+ [S]) \pi^+$	> 10	$-2.68 \pm 0.05 \pm 0.07$	$0.221 \pm 0.012 \pm 0.018$
$D^+ \rightarrow \bar{K}_1(1400)^0 (K^{*-} \pi^+ [D]) \pi^+$	> 10	$-2.24 \pm 0.10 \pm 0.07$	$0.015 \pm 0.002 \pm 0.001$
$D^+ \rightarrow \bar{K}_1(1400)^0 (K^{*-} \pi^+)$	-	-	$0.216 \pm 0.012 \pm 0.011$
$D^+ \rightarrow \bar{K}_1(1270)^0 (K^0_S \rho^0 [S]) \pi^+$	9.7	$-0.56 \pm 0.09 \pm 0.11$	$0.024 \pm 0.003 \pm 0.007$
$D^+ \rightarrow \bar{K}(1460)^0 (K^{*-} \pi^+) \pi^+$	> 10	$-2.50 \pm 0.07 \pm 0.06$	$0.068 \pm 0.006 \pm 0.002$
$D^+ \rightarrow \bar{K}(1460)^0 (K^0_S \rho^0) \pi^+$	6.1	$-2.65 \pm 0.18 \pm 0.25$	$0.008 \pm 0.002 \pm 0.005$
$D^+ \rightarrow \bar{K}_1(1650)^0 (K^{*-} \pi^+ [S]) \pi^+$	6.5	$0.95 \pm 0.14 \pm 0.22$	$0.016 \pm 0.004 \pm 0.009$
$D^+ \rightarrow (K^0_S \rho^0 [S])_A \pi^+$	> 10	$-1.88 \pm 0.08 \pm 0.05$	$0.057 \pm 0.007 \pm 0.023$
$D^+ \rightarrow (K^0_S \rho^0 [D])_A \pi^+$	7.0	$2.77 \pm 0.12 \pm 0.14$	$0.008 \pm 0.002 \pm 0.001$
$D^+ \rightarrow (K^0_S \rho^0)_A \pi^+$	-	-	$0.064 \pm 0.007 \pm 0.030$
$D^+ \rightarrow (K^0_S (\pi^+ \pi^-)_S)_A \pi^+$	> 10	$-3.08 \pm 0.06 \pm 0.04$	$0.064 \pm 0.005 \pm 0.007$
$D^+ \rightarrow ((K^0_S \pi^+)_S - \text{wave } \pi^-)_P \pi^+$	> 10	$2.10 \pm 0.08 \pm 0.28$	$0.017 \pm 0.003 \pm 0.004$
$D^+ \rightarrow K^0_S \pi^+ \pi^+ \pi^-$ non-resonance	-	-	$0.081 \pm 0.006 \pm 0.006$

# Amplitude analysis of $D_s^+ \rightarrow \pi^+ \pi^0 \eta$ and ...

3.19 fb<sup>-1</sup> @ 4178 MeV

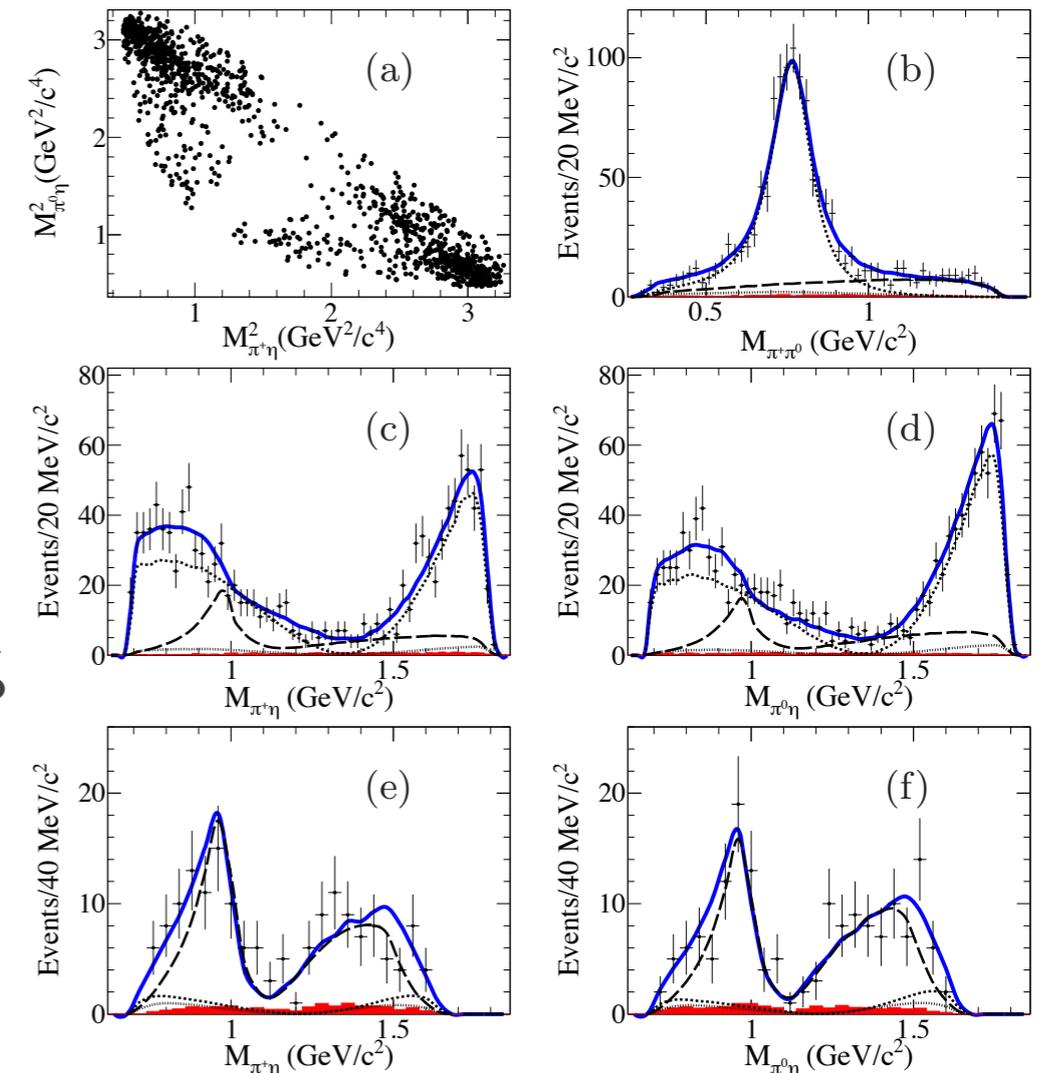
[arXiv:1903.04118](https://arxiv.org/abs/1903.04118)

- Double tag analysis: tag modes  $D_s^- \rightarrow K^0 S K^-$ ;  $D_s^- \rightarrow K^+ K^- \pi^-$ ;  $D_s^- \rightarrow K^0 S K^- \pi^0$ ;  $D_s^- \rightarrow K^+ K^- \pi^- \pi^0$ ;  $D_s^- \rightarrow K^0 S K^- \pi^- \pi^-$ ;  $D_s^- \rightarrow \pi^- \eta$
- 1239 events with 97.7% purity used for amplitude analysis

## First amplitude analysis

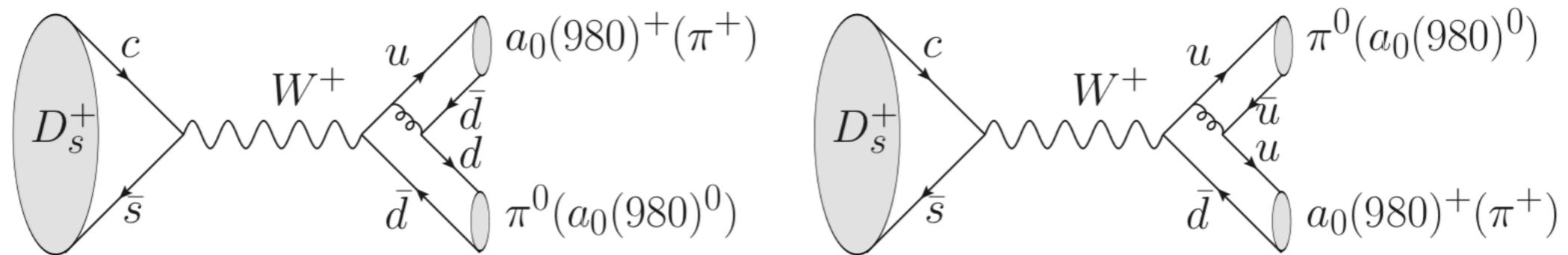
Amplitude	$\phi_n$ (rad)	FF <sub>n</sub>
$D_s^+ \rightarrow \rho^+ \eta$	0.0 (fixed)	$0.783 \pm 0.050 \pm 0.021$
$D_s^+ \rightarrow (\pi^+ \pi^0)_V \eta$	$0.612 \pm 0.172 \pm 0.342$	$0.054 \pm 0.021 \pm 0.025$
$D_s^+ \rightarrow a_0(980) \pi$	$2.794 \pm 0.087 \pm 0.044$	$0.232 \pm 0.023 \pm 0.033$

$B(D_s^+ \rightarrow \pi^+ \pi^0 \eta) = (9.50 \pm 0.28(\text{stat}) \pm 0.41(\text{syst}))\%$   
Best precision measurement



# ... a first observation of the pure W-annihilation decays $D_s^+ \rightarrow a_0(980)^+ \pi^0$ and $D_s^+ \rightarrow a_0(980)^0 \pi^+$

[arXiv:1903.04118](https://arxiv.org/abs/1903.04118)



First observation with a statistical significance  $16.2 \sigma$

$$\mathcal{B}(D_s^+ \rightarrow a_0(980)^{+(0)} \pi^{0(+)}, a_0(980)^{+(0)} \rightarrow \pi^{+(0)} \eta) = (1.46 \pm 0.15_{\text{stat.}} \pm 0.23_{\text{sys.}})\%$$

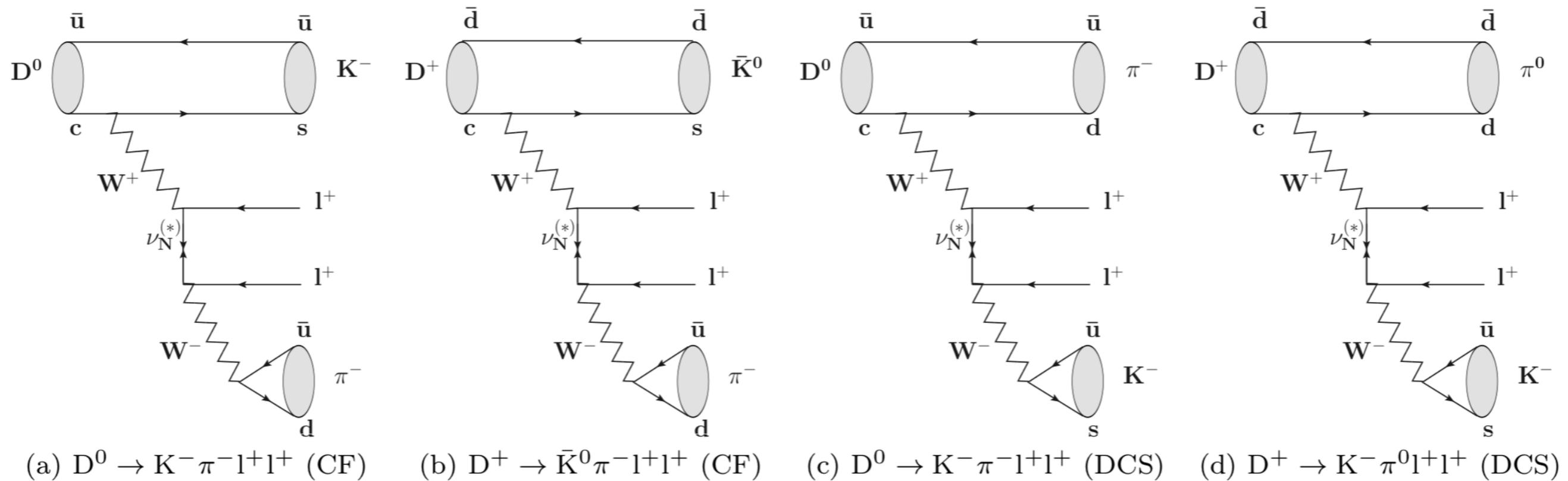
An order of magnitude larger than other W-annihilation decays

# Search for heavy Majorana neutrino in lepton number violating decays of $D \rightarrow K \pi e^+ e^+$

2.93 fb<sup>-1</sup> @ 3773 MeV

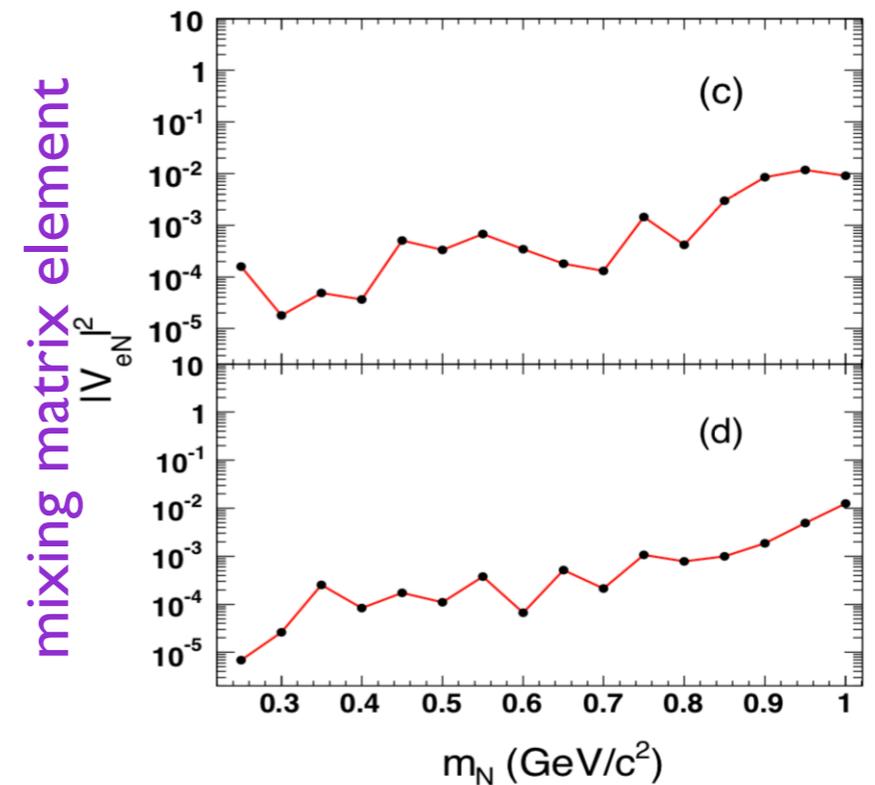
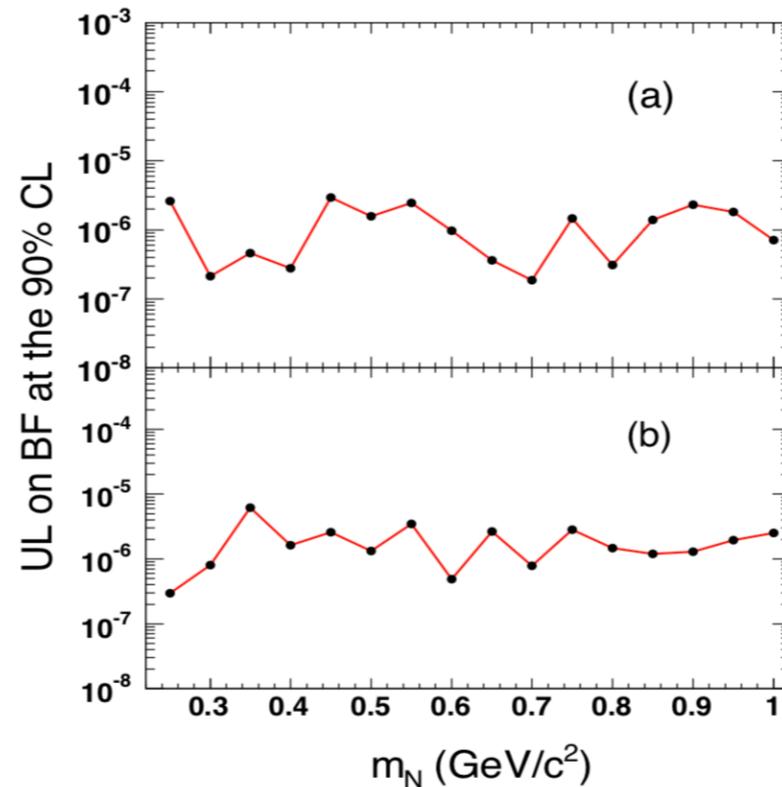
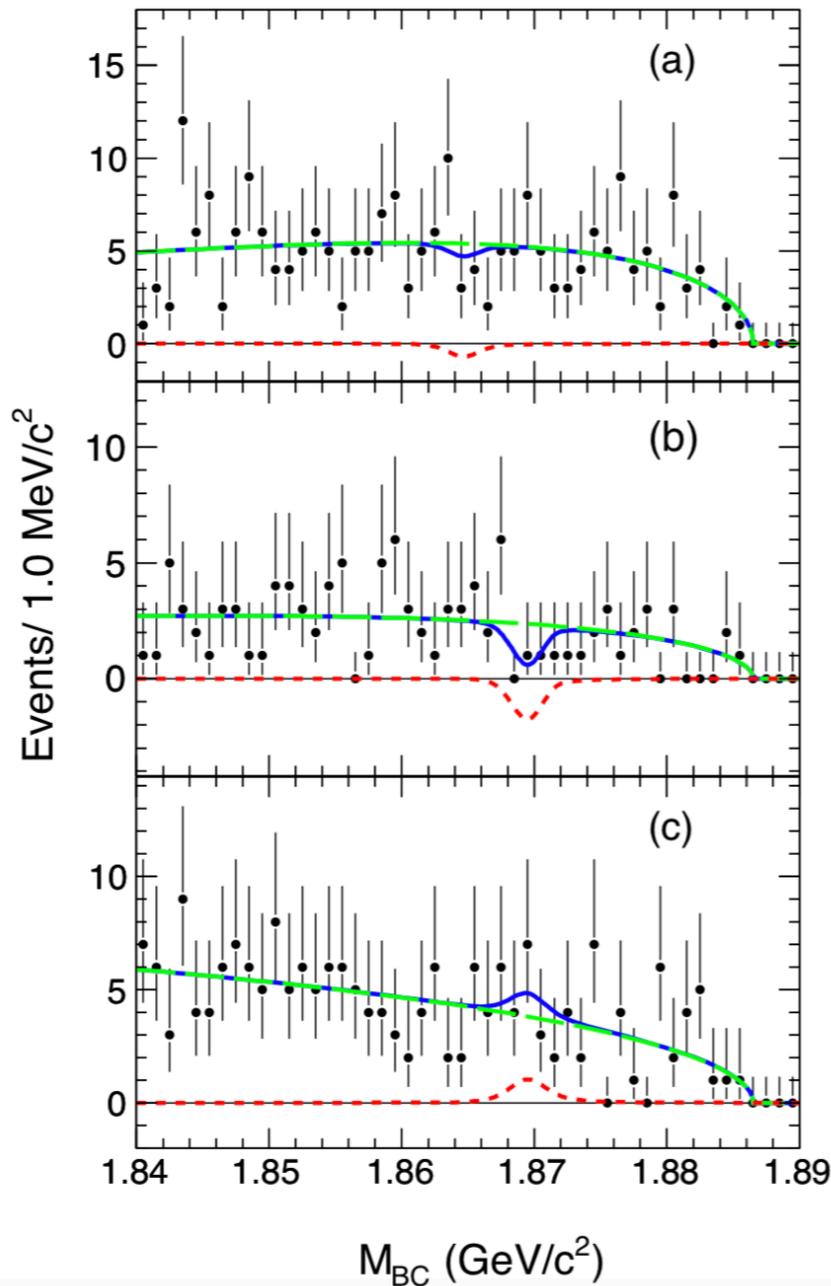
[arXiv:1902.02450](https://arxiv.org/abs/1902.02450)

- Single tag analysis
- See-saw mechanism  $m_\nu \sim y_\nu^2 v^2 / m_N$
- LNV process: exchange a single Majorana neutrino



# Upper limits

Different Majorana neutrino mass assumptions  $m_N$  in the decays  
 $D^0 \rightarrow K^- e^+ \nu_N (\pi^- e^+)$  and  $D^+ \rightarrow K^0_S e^+ \nu_N (\pi^- e^+)$



$$B(D^0 \rightarrow K^- \pi^- e^+ e^+) < 2.7 \times 10^{-6} \text{ @90\% CL}$$

$$B(D^+ \rightarrow K^0_S \pi e^+ e^+) < 3.3 \times 10^{-6} \text{ @90\% CL}$$

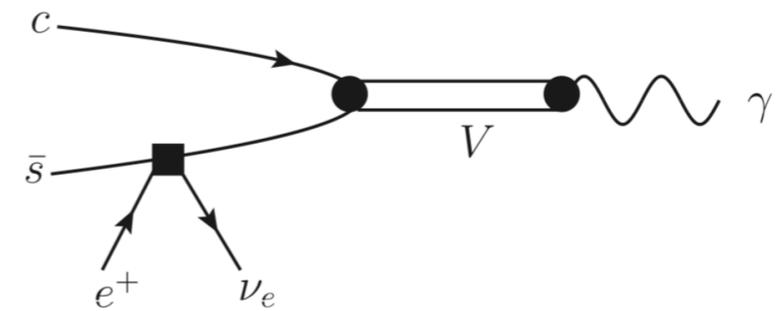
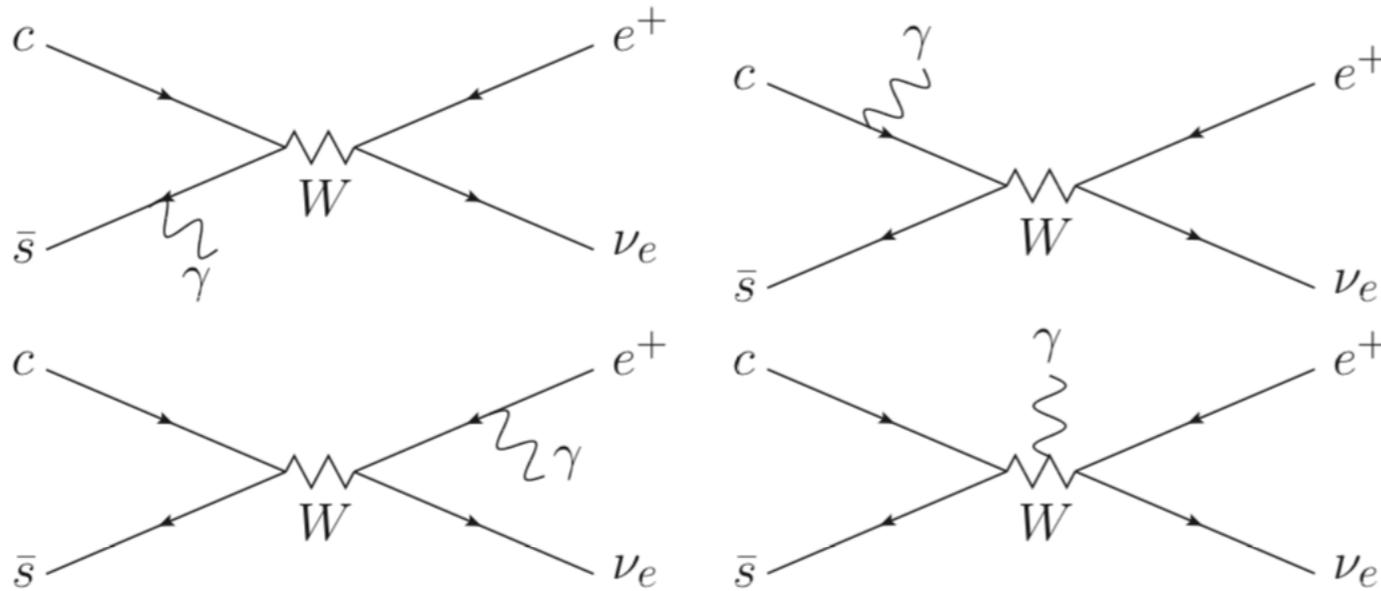
$$B(D^+ \rightarrow K^- \pi^0 e^+ e^+) < 8.5 \times 10^{-6} \text{ @90\% CL}$$

# First search for the decay $D_s^+ \rightarrow \gamma e^+ \nu_e$

3.19 fb<sup>-1</sup> @ 4178 MeV

Phys. Rev. D 99, 072002 (2019) [arXiv:1902.03351](https://arxiv.org/abs/1902.03351)

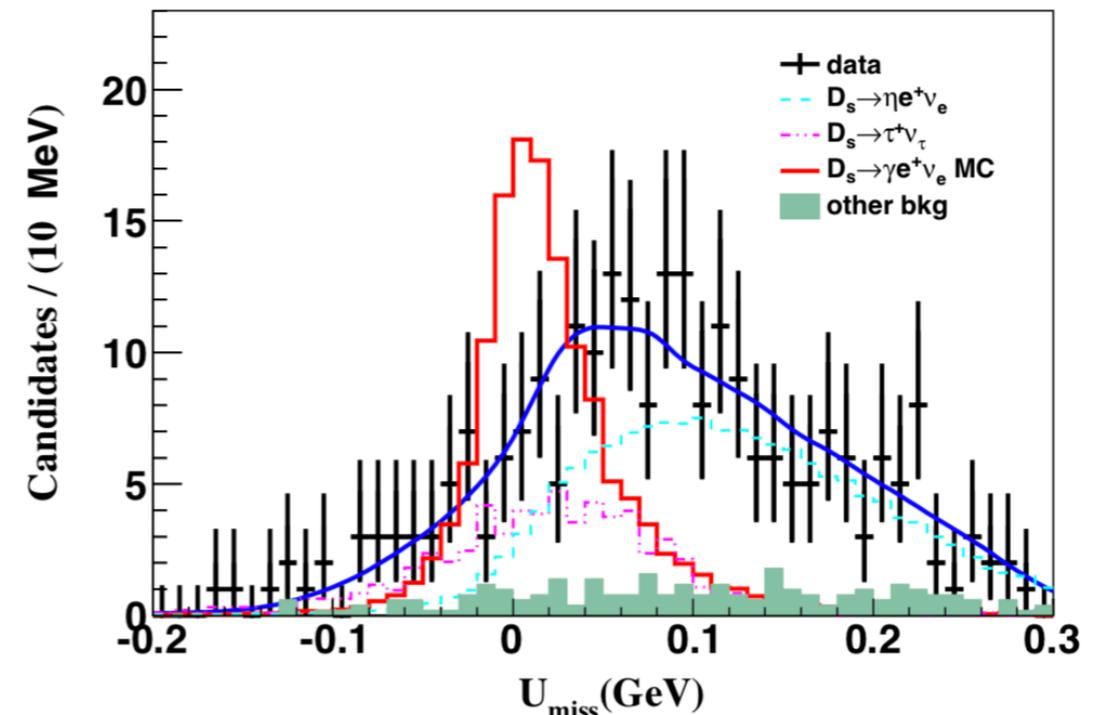
No helicity suppression. The BFs are predicted to be in the range  $10^{-5}$ - $10^{-3}$  in various models.



Long distance contribution via vector meson suggested by Yang and Yang, Mod. Phys. Lett. A 27, 1250120 (2012) may further enhance the BF

Double tag analysis with 14 tag modes

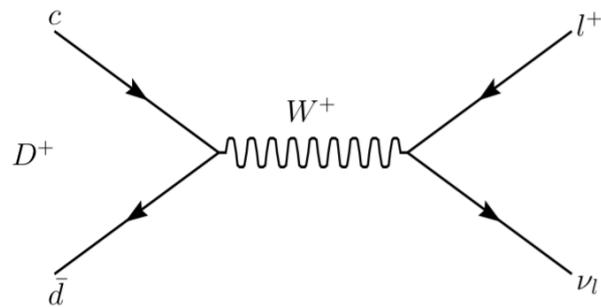
- |                              |  |
|------------------------------|--|
| $K^+ K^- \pi^-$              | $K_S^0 K^-$                                  |
| $\pi^+ \pi^- \pi^-$          | $K_S^0 K^- \pi^0$                            |
| $K^- \pi^+ \pi^-$            | $K_S^0 K^+ \pi^- \pi^-$                      |
| $K^+ K^- \pi^- \pi^0$        | $\eta_{\gamma\gamma} \pi^-$                  |
| $K_S^0 K^- \pi^+ \pi^-$      | $K_S^0 K_S^0 \pi^-$                          |
| $\eta'_{\gamma\rho^0} \pi^-$ | $\eta_{\pi^0} \pi^+ \pi^- \pi^-$             |
| $\eta_{\gamma\gamma} \rho^-$ | $\eta'_{\eta\gamma\gamma} \pi^+ \pi^- \pi^-$ |



Upper limit  $B(D_s^+ \rightarrow \gamma e^+ \nu_e) < 1.3 \times 10^{-4}$  at the 90% C.L.

# Search for $D^+ \rightarrow \tau^+ \nu_\tau$

2.93 fb<sup>-1</sup> @ 3773 MeV



$$\Gamma(D^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2}{8\pi} f_{D^+}^2 |V_{cd}|^2 m_\ell^2 M_{D^+} \left(1 - \frac{m_\ell^2}{M_{D^+}^2}\right)^2$$

BF < 1.2 × 10<sup>-3</sup> @ 90% CL by CLEO with 818 pb<sup>-1</sup>  
PRD 78, 052003(2008)

- Double tag analysis

Tag modes, $i$
$K^+ \pi^- \pi^-$
$K^+ \pi^- \pi^- \pi^0$
$K_S^0 \pi^-$
$K_S^0 \pi^- \pi^0$
$K_S^0 \pi^- \pi^- \pi^+$
$K^+ K^- \pi^-$

137 ± 27 events

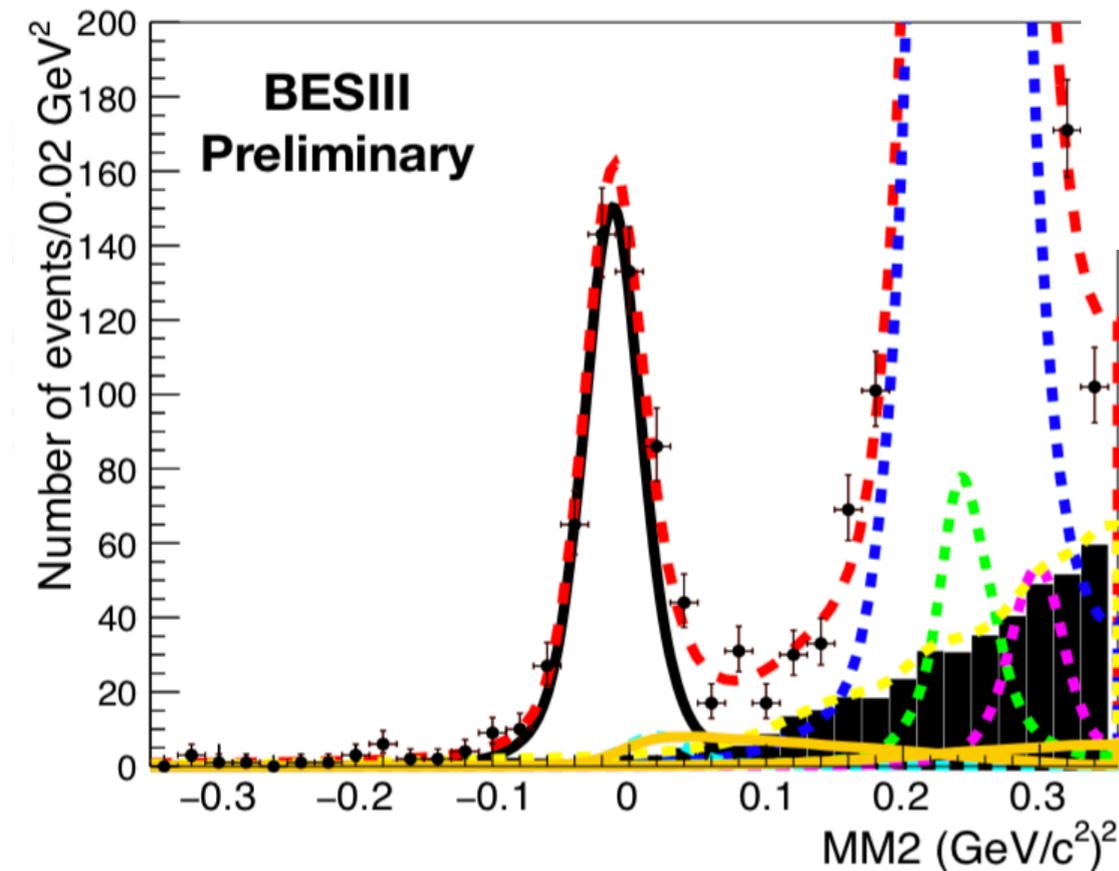
First evidence with  
> 4σ significance

$$\mathcal{B}(D^+ \rightarrow \tau^+ \nu_\tau) = \frac{N_{DT}}{\mathcal{B}(\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau) \cdot \sum_i N_{tag}^i \cdot (\epsilon_{DT}^i / \epsilon_{tag}^i)}$$

$$\mathcal{B}(D^+ \rightarrow \tau^+ \nu_\tau) = (1.20 \pm 0.24_{stat}) \times 10^{-3}$$

$$f_{D^+} |V_{cd}| = 50.4 \pm 5.0_{stat} \text{ MeV}$$

$$R_{\tau/\mu} = \Gamma(D^+ \rightarrow \tau^+ \nu_\tau) / \Gamma(D^+ \rightarrow \mu^+ \nu_\mu) = 3.21 \pm 0.64, \text{ SM prediction is } 2.66 \pm 0.01$$



# Other recent results on hadronic decays and charm baryons

- M. Ablikim *et al.* (BESIII collaboration), [Measurement of the absolute branching fractions of  \$\Lambda\_c^+ \rightarrow \Lambda \eta \pi^+\$  and  \$\Sigma\(1385\)^+ \eta\$](#) , Phys. Rev. D 99, 032010 (2019), [arXiv:1812.10731](#)
- M. Ablikim *et al.* (BESIII collaboration), [Evidence for the decays of  \$\Lambda\_c^+ \rightarrow \Sigma^+ \eta\$  and  \$\Sigma^+ \eta'\$](#) , [arXiv:1811.08028](#)
- M. Ablikim *et al.* (BESIII collaboration), [Measurements of the absolute branching fractions and CP asymmetries for  \$D^+ \rightarrow K^0\_{S,L} K\(\pi^0\)\$](#) , Phys. Rev. D 99, 032002 (2019), [arXiv:1812.05400](#)
- M. Ablikim *et al.* (BESIII collaboration), [Observation of  \$D^+\_s \rightarrow p \bar{n}\$  and confirmation of its large branching fraction](#), Phys. Rev. D 99, 031101 (2019), [arXiv:1811.00752](#)
- M. Ablikim *et al.* (BESIII collaboration), [Observation of the W-Annihilation Decay  \$D^+\_s \rightarrow \omega \pi^+\$  and Evidence for  \$D^+\_s \rightarrow \omega K^+\$](#) , Phys. Rev. D 99, 091101 (2019), [arXiv:1811.00392](#)

# Other recent results on (semi-)leptonic decays

- M. Ablikim *et al.* (BESIII collaboration), [Measurement of the Dynamics of the Decays  \$D\_s^+ \rightarrow \eta^{\(\prime\)} e^+ \nu\_e\$](#) , Phys. Rev. Lett. 122, 121801 (2019) [arXiv:1901.02133](#)
- M. Ablikim *et al.* (BESIII collaboration), [Study of the decay  \$D^0 \rightarrow \bar{K}^0 \pi^- e^+ \nu\_e\$](#) , Phys. Rev. D 99, 011103 (2019), [arXiv:1811.11349](#)
- M. Ablikim *et al.* (BESIII collaboration), [Determination of the pseudoscalar decay constant  \$f\_{D\_s^+}\$  via  \$D\_s^+ \rightarrow \mu^+ \nu\_\mu\$](#) , Phys. Rev. Lett. 122, 071802 (2019), [arXiv:1811.10890](#)
- M. Ablikim *et al.* (BESIII collaboration), [First measurement of the form factors in  \$D\_s^+ \rightarrow K^0 e^+ \nu\_e\$  and  \$D\_s^+ \rightarrow K^{\*0} e^+ \nu\_e\$  decays](#), Phys. Rev. Lett. 122, 061801 (2019), [arXiv:1811.02911](#)
- M. Ablikim *et al.* (BESIII collaboration), [Study of the  \$D^0 \rightarrow K^- \mu^+ \nu\_\mu\$  dynamics and test of lepton flavor universality with  \$D^0 \rightarrow K^- \ell^+ \nu\_\ell\$  decays](#), Phys. Rev. Lett. 122, 011804 (2019), [arXiv:1810.03127](#)
- M. Ablikim *et al.* (BESIII collaboration), [Observation of  \$D^+ \rightarrow f\_0\(500\) e^+ \nu\_e\$  and Improved Measurements of  \$D \rightarrow \rho e^+ \nu\_e\$](#) , Phys. Rev. Lett. 122, 062001 (2019), [arXiv:1809.06496](#)

# Summary

- Very rich charm programme @ BESIII
- The unique tagging technique allows for absolute BF measurements, rare decays searches
- Very high purity charm samples for amplitude analyses
- A lot of new results: either a completely new results or significantly improving previous measurements

# BACKUP

# Variables & systematics $\Lambda_c^+ \rightarrow BP$ decays

$$\frac{dN}{d \cos \theta_2} \propto 1 + \alpha_{\Lambda \pi^+ (\Sigma^+ \pi^0)}^+ \alpha_{\Lambda (\Sigma^+)} \cos \theta_2$$

$$\langle \cos \theta_i \rangle = -\frac{1}{6} \alpha_{\Sigma^0 \pi^+}^+ \alpha_{\Lambda} \cos \theta_j$$

$$\mathcal{W} \propto 1 + \alpha_0 \cos^2 \theta_0 + \mathcal{P}_T \alpha_{BP}^+ \sin \theta_1 \sin \phi_1$$

$$\langle \sin \theta_1 \sin \phi_1 \rangle = \frac{\int_0^{2\pi} \int_{-1}^1 \sin \theta_1 \sin \phi_1 \mathcal{W} d \cos \theta_1 d \phi_1}{\int_0^{2\pi} \int_{-1}^1 \mathcal{W} d \cos \theta_1 d \phi_1}$$

Source	$\alpha_A^+$	$\alpha_B^+$	$\alpha_C^+$	$\alpha_D^+$	$\sin \Delta_0$	$\Delta_1^B$	$\Delta_1^C$	$\Delta_1^D$
Reconstruction	0.00	0.00	0.00	0.01	0.00	0.8	0.0	0.0
$\pi^0 \pi^0$ veto	0.01	0.00	0.01	0.00	0.00	0.0	0.2	0.0
$\Delta E$ signal region	0.07	0.01	0.02	0.05	0.02	0.3	0.1	0.1
$M_{BC}$ signal region	0.12	0.01	0.05	0.02	0.02	0.5	0.4	0.1
Bkg subtraction	0.03	0.01	0.05	0.04	0.02	0.3	0.3	0.0
<b>Total</b>	<b>0.14</b>	<b>0.02</b>	<b>0.07</b>	<b>0.07</b>	<b>0.03</b>	<b>1.0</b>	<b>0.6</b>	<b>0.2</b>

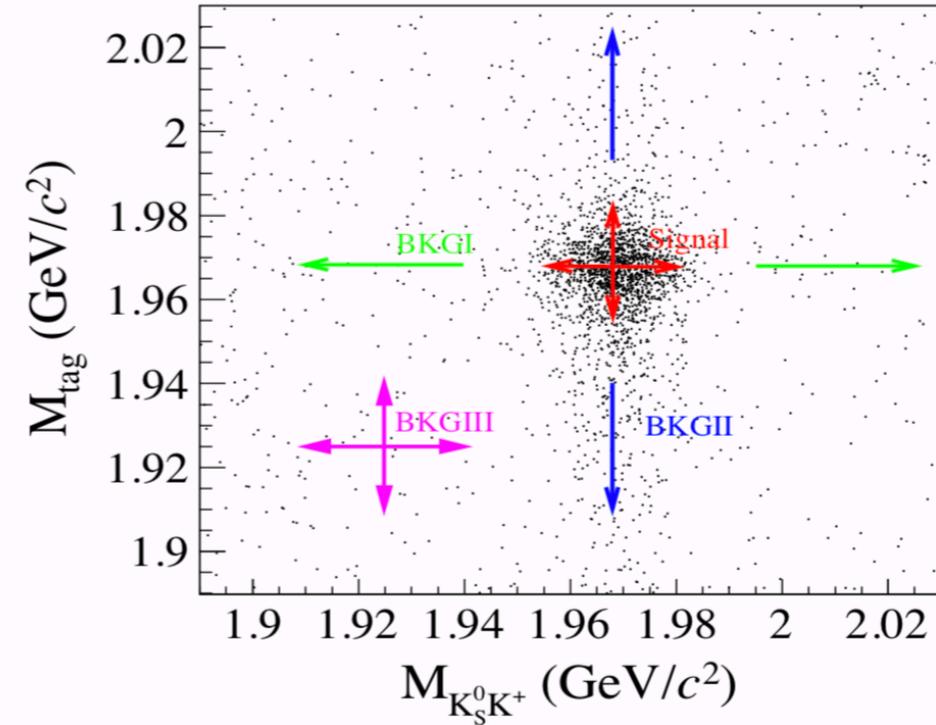
# Systematics for $D_s^+ \rightarrow K_S^0 K^+$ and $K_L^0 K^+$

$$MM^2 = (P_{e^+e^-} - P_{D_s^-} - P_\gamma - P_{K^+})^2$$

$$N_{ST}^i = 2 \times N_{D_s^{*\pm} D_s^\mp} \times \mathcal{B}_{\text{tag}}^i \times \epsilon_{ST}^i$$

$$N_{DT}^i = 2 \times N_{D_s^{*\pm} D_s^\mp} \times \mathcal{B}_{\text{tag}}^i \times \mathcal{B}_{\text{sig}} \times \epsilon_{DT}^i$$

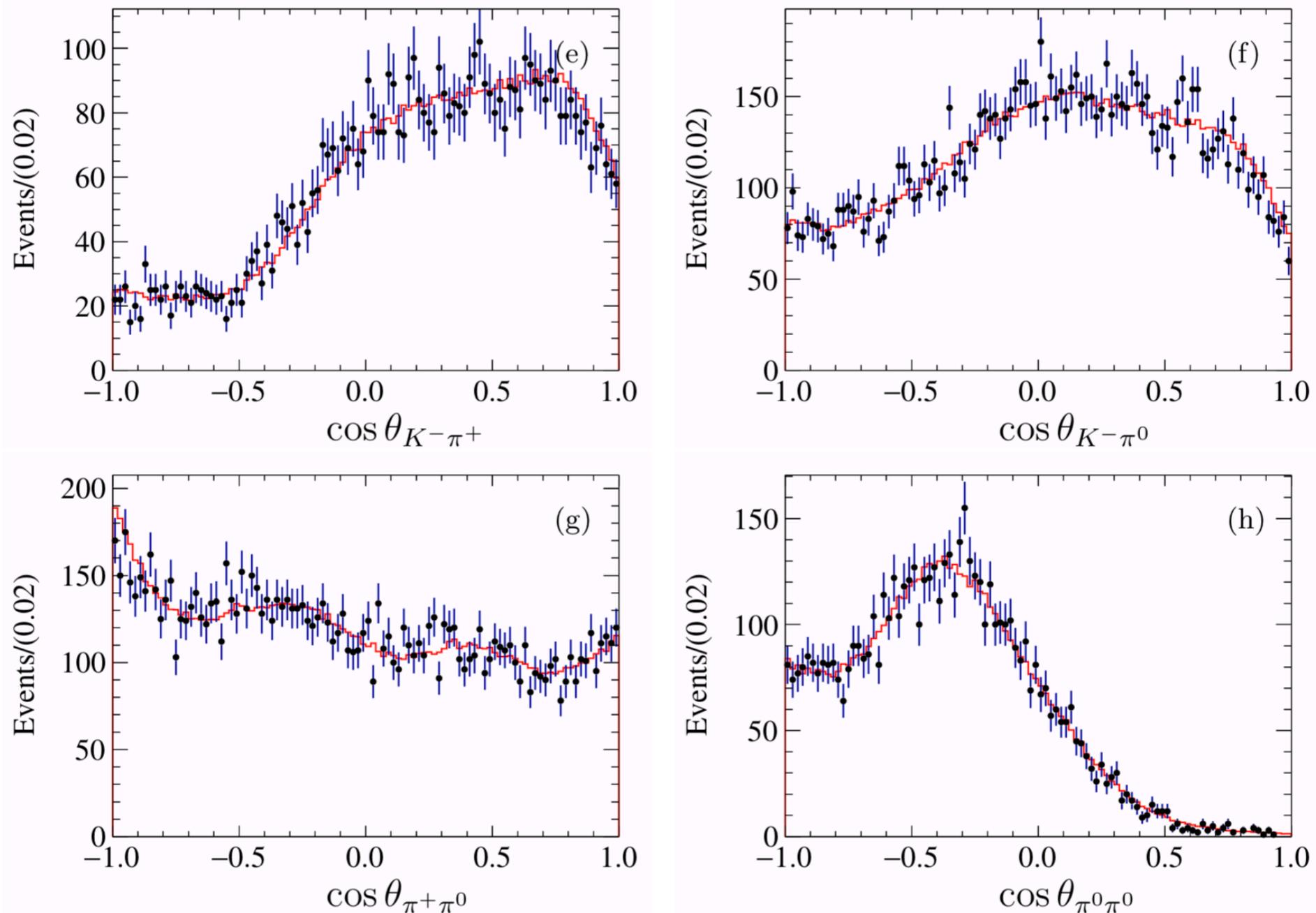
$$\mathcal{B}_{\text{sig}} = \frac{N_{DT}^{\text{tot}}}{\sum_i N_{ST}^i \times \epsilon_{DT}^i / \epsilon_{ST}^i}$$



Source	$\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+)$	$\mathcal{B}(D_s^+ \rightarrow K_L^0 K^+)$	$R(D_s^+ \rightarrow K_{S,L}^0 K^+)$	$A_{CP}(D_s^\pm \rightarrow K_S^0 K^\pm)$	$A_{CP}(D_s^\pm \rightarrow K_L^0 K^\pm)$
$K^+/K^-$ tracking	0.5	0.5	-	0.4	0.4
$K^+/K^-$ PID	0.5	0.5	-	0.4	0.4
$K_S^0$ reconstruction	1.5	-	0.7	-	-
Photon selection and kinematic fit	-	2.0	1.0	-	-
Extra photon energy requirement	-	0.6	0.3	-	-
Extra charged track requirement	0.6	0.6	-	-	-
ST $M(D_s)$ fit	0.9	0.9	-	-	-
DT fit	0.8	-	0.4	-	-
$MM^2$ fit	-	1.5	0.7	-	-
MC statistics	0.3	0.3	0.2	0.2	0.2
Effect of $\mathcal{B}(D_s^* \rightarrow \gamma D_s)$	-	0.7	0.3	-	-
Effect of $e^+e^- \rightarrow D_s^+ D_s^-$	-	0.4	0.2	-	-
Tag-side bias	0.3	0.5	0.3	-	-
total	2.2	3.1	1.6	0.6	0.6

# Amplitude Analysis of $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$

- cosines of helicity angles



# Systematics for $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$

TABLE IV. FF systematic uncertainties (in units of statistical standard deviations) for: (I) the amplitude model, (II) background, (III) experimental effects, and (IV) fit bias. The total uncertainty is obtained by adding all contributions in quadrature.

Amplitude mode	I	II	III	IV	Total
$D \rightarrow SS$					
$D \rightarrow (K^- \pi^+)_S (\pi^0 \pi^0)_S$	1.518	1.258	0.072	0.235	1.987
$D \rightarrow (K^- \pi^0)_S (\pi^+ \pi^0)_S$	1.524	0.835	0.078	0.004	1.740
$D \rightarrow AP, A \rightarrow VP$					
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [S]$	1.293	0.436	0.030	0.363	1.412
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [D]$	0.938	0.368	0.024	0.284	1.046
$D \rightarrow K_1(1270)^- \pi^+, K^{*-} \pi^0 [S]$	1.643	1.175	0.160	0.182	2.035
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [S]$	1.562	0.567	0.034	0.036	1.662
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [D]$	0.989	0.541	0.035	0.068	1.201
$D \rightarrow K_1(1270)^0 \pi^0, K^- \rho^+ [S]$	0.713	0.221	0.098	0.172	0.772
$D \rightarrow (K^{*-} \pi^0)_A \pi^+, K^{*-} \pi^0 [S]$	1.253	1.254	0.076	0.237	1.790
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [S]$	1.145	0.524	0.022	0.162	1.278
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [D]$	0.865	1.468	0.052	0.106	1.708
$D \rightarrow (\rho^+ K^-)_A \pi^0, K^- \rho^+ [D]$	1.249	0.812	0.084	0.186	1.504
$D \rightarrow AP, A \rightarrow SP$					
$D \rightarrow ((K^- \pi^+)_S \pi^0)_A \pi^0$	1.377	0.372	0.102	0.164	1.439
$D \rightarrow VS$					
$D \rightarrow (K^- \pi^0)_S \rho^+$	1.308	0.252	0.070	0.476	1.416
$D \rightarrow K^{*-} (\pi^+ \pi^0)_S$	0.381	0.549	0.023	0.166	0.689
$D \rightarrow K^{*0} (\pi^0 \pi^0)_S$	0.880	0.417	0.078	0.232	1.005
$D \rightarrow VP, V \rightarrow VP$					
$D \rightarrow (K^{*-} \pi^+)_V \pi^0$	0.688	0.752	0.033	0.273	1.056
$D \rightarrow VV$					
$D \rightarrow K^{*-} \rho^+ [S]$	0.980	1.354	0.059	0.371	1.713
$D \rightarrow K^{*-} \rho^+ [P]$	0.425	0.506	0.031	0.348	0.747
$D \rightarrow K^{*-} \rho^+ [D]$	1.365	0.598	0.049	0.398	1.543
$D \rightarrow (K^- \pi^0)_V \rho^+ [P]$	0.695	1.223	0.027	0.140	1.414
$D \rightarrow (K^- \pi^0)_V \rho^+ [D]$	1.335	0.848	0.237	0.401	1.649
$D \rightarrow K^{*-} (\pi^+ \pi^0)_V [D]$	0.751	0.894	0.049	0.074	1.171
$D \rightarrow (K^- \pi^0)_V (\pi^+ \pi^0)_V [S]$	0.818	0.443	0.046	0.211	0.955
$D \rightarrow TS$					
$D \rightarrow (K^- \pi^+)_S (\pi^0 \pi^0)_T$	1.171	0.936	0.084	0.273	1.528
$D \rightarrow (K^- \pi^0)_S (\pi^+ \pi^0)_T$	0.803	0.188	0.068	0.018	0.828

TABLE V. Phase,  $\phi$ , systematic uncertainties (in units of statistical standard deviations) for: (I) the amplitude model, (II) background, (III) experimental effects, and (IV) fit bias. The total uncertainty is obtained by adding all contributions in quadrature.

Amplitude mode	I	II	III	IV	Total
$D \rightarrow SS$					
$D \rightarrow (K^- \pi^+)_S (\pi^0 \pi^0)_S$	3.137	0.093	0.043	0.030	3.139
$D \rightarrow (K^- \pi^0)_S (\pi^+ \pi^0)_S$	2.330	0.850	0.044	0.109	2.483
$D \rightarrow AP, A \rightarrow VP$					
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [S]$	0.000	0.000	0.000	0.000	0.000
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0 [D]$	1.194	0.761	0.081	0.479	1.497
$D \rightarrow K_1(1270)^- \pi^+, K^{*-} \pi^0 [S]$	0.953	0.820	0.054	0.124	1.264
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [S]$	1.051	0.556	0.029	0.565	1.316
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0 [D]$	1.002	0.483	0.045	0.121	1.120
$D \rightarrow K_1(1270)^0 \pi^0, K^- \rho^+ [S]$	2.007	0.188	0.079	0.847	2.188
$D \rightarrow (K^{*-} \pi^0)_A \pi^+, K^{*-} \pi^0 [S]$	1.208	0.706	0.048	0.455	1.472
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [S]$	1.711	0.365	0.053	0.214	1.750
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0 [D]$	1.501	0.605	0.051	0.187	1.630
$D \rightarrow (\rho^+ K^-)_A \pi^0, K^- \rho^+ [D]$	1.195	0.613	0.133	0.611	1.482
$D \rightarrow AP, A \rightarrow SP$					
$D \rightarrow ((K^- \pi^+)_S \pi^0)_A \pi^0$	2.039	0.410	0.045	0.446	2.127
$D \rightarrow VS$					
$D \rightarrow (K^- \pi^0)_S \rho^+$	3.159	0.471	0.053	0.216	3.201
$D \rightarrow K^{*-} (\pi^+ \pi^0)_S$	1.207	0.258	0.045	0.156	1.245
$D \rightarrow K^{*0} (\pi^0 \pi^0)_S$	0.938	0.476	0.062	0.116	1.060
$D \rightarrow VP, V \rightarrow VP$					
$D \rightarrow (K^{*-} \pi^+)_V \pi^0$	1.260	0.471	0.032	0.490	1.432
$D \rightarrow VV$					
$D \rightarrow K^{*-} \rho^+ [S]$	1.995	0.154	0.070	0.712	2.125
$D \rightarrow K^{*-} \rho^+ [P]$	1.612	0.214	0.035	0.864	1.842
$D \rightarrow K^{*-} \rho^+ [D]$	1.586	1.108	0.051	0.588	2.022
$D \rightarrow (K^- \pi^0)_V \rho^+ [P]$	1.429	0.324	0.023	0.128	1.471
$D \rightarrow (K^- \pi^0)_V \rho^+ [D]$	0.401	0.832	0.133	0.666	1.146
$D \rightarrow K^{*-} (\pi^+ \pi^0)_V [D]$	1.445	1.313	0.040	0.190	1.962
$D \rightarrow (K^- \pi^0)_V (\pi^+ \pi^0)_V [S]$	1.354	0.213	0.041	0.726	1.551
$D \rightarrow TS$					
$D \rightarrow (K^- \pi^+)_S (\pi^0 \pi^0)_T$	2.544	0.724	0.057	0.189	2.653
$D \rightarrow (K^- \pi^0)_S (\pi^+ \pi^0)_T$	1.533	0.718	0.050	0.135	1.699

# Systematic uncertainties for $D_s^+ \rightarrow \pi^+ \pi^0 \eta$

Systematic uncertainties for the amplitude analysis are considered from five sources: (I) line-shape parameterizations of the resonances, (II) fixed parameters in the amplitudes, (III) the background level and distribution in the Dalitz plot, (IV) experimental effects, and (V) the fitter performance. We determine these systematic un-

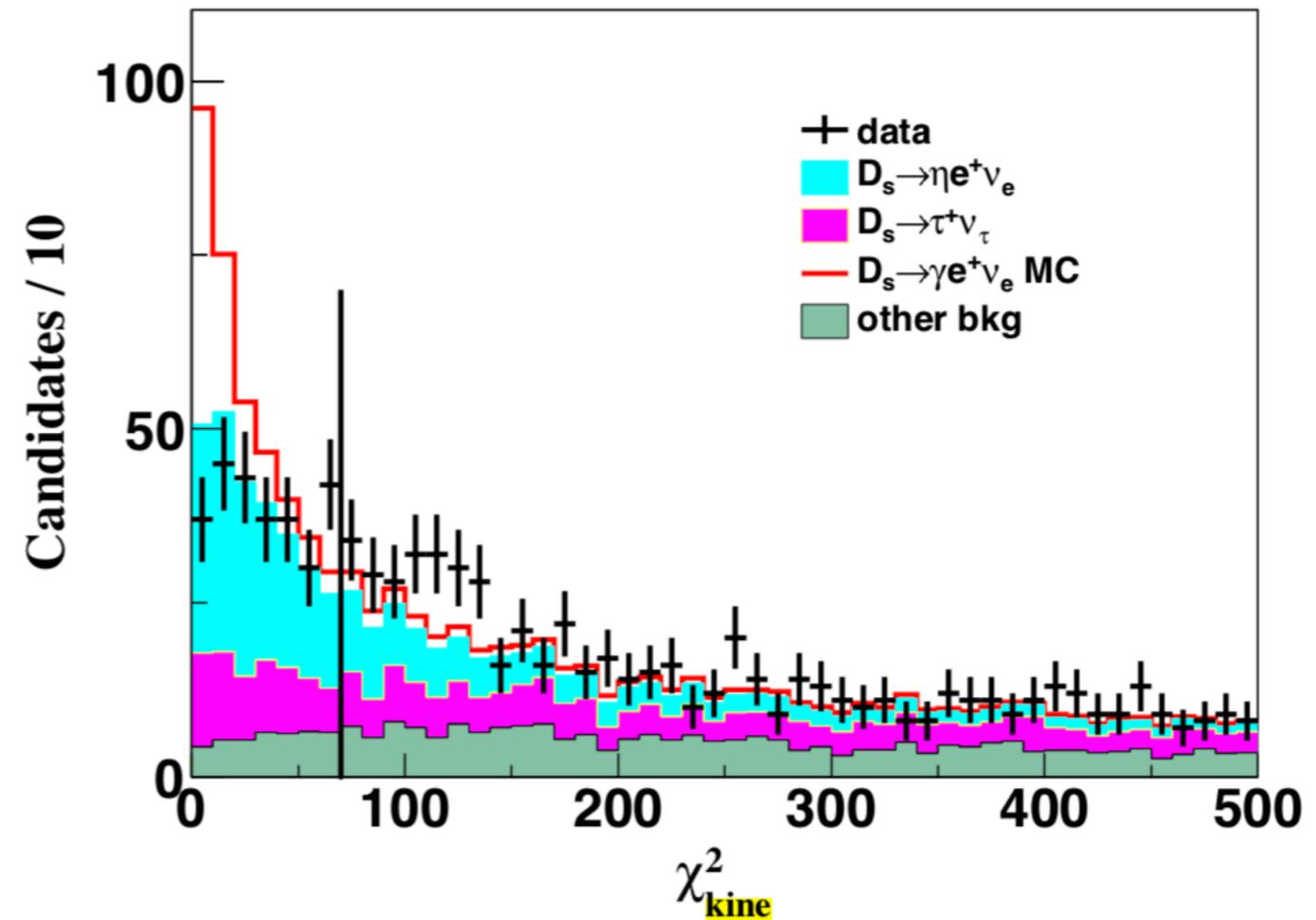
Amplitude		Source					Total
		I	II	III	IV	V	
$D_s^+ \rightarrow \rho^+ \eta$	FF	0.06	0.34	0.13	0.12	0.15	0.41
$D_s^+ \rightarrow (\pi^+ \pi^0)_V \eta$	$\phi$	—	1.97	0.18	0.03	0.17	1.99
	FF	0.61	1.03	0.12	0.06	0.08	1.21
$D_s^+ \rightarrow a_0(980) \pi$	$\phi$	—	0.41	0.07	0.28	0.09	0.51
	FF	0.58	1.31	0.02	0.06	0.11	1.45

# Systematic uncertainties for $D \rightarrow K\pi e^+e^-$

Source	Relative systematic uncertainty (%)		
	$D^0 \rightarrow K^- \pi^- e^+ e^-$	$D^+ \rightarrow K_S^0 \pi^- e^+ e^-$	$D^+ \rightarrow K^- \pi^0 e^+ e^-$
$e$ Tracking	2.0	2.0	2.0
$e$ PID	2.0	2.0	2.0
$K/\pi$ Tracking	2.0	1.0	1.0
$K/\pi$ PID	1.0	0.5	0.5
$K_S^0$ selection	–	1.5	–
$\pi^0$ selection	–	–	2.0
$N_{D\bar{D}}$	1.0	0.9	0.9
Cited BF	–	0.1	0.0
$\Delta E$ requirement	0.7	0.7	0.4
FSR recovery	0.6	0.8	0.6
Efficiency modeling	3.6	4.3	4.7
Fitting $M_{BC}$	...	...	...
Total	5.3	5.7	6.1

# Systematic uncertainties for $D_s^+ \rightarrow \gamma e^+ \nu_e$

Source	Relative uncertainty (%)
ST yields	0.4
Form factor model	11
$e^+$ tracking & PID	0.4
Photon selection	1
$E_{\gamma}^{\text{max}}$	1.1
$N_{\text{char}}^{\text{extra}}$	0.9
$\chi_{\text{kine}}^2$	11
FSR	0.3
$U_{\text{miss}}$ fit	10
Tag bias	0.5
Total	18.6



# Systematic uncertainties: $D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$

TABLE V. Systematic uncertainties of FFs for amplitudes and components. The different sources include (I) masses and widths of the intermediate resonances, (II) effective radius of intermediate resonances and  $D^+$ , (III) parameters in the  $K_S^0 \pi^+$   $S$ -wave parameterization, (IV) parameters in  $\rho - \omega$  mixing parameterization, (V) line shape of the  $f_0(500)$ , (VI) effect from peaking background, (VII) effect from general background, and (VIII) fit procedure.

Amplitude and component	Source ( $\sigma_{\text{stat}}$ )								total
	I	II	III	IV	V	VI	VII	VIII	
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+ [S])$	0.299	0.831	0.496	0.069	0.877	0.215	0.023	0.143	1.367
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+ [D])$	0.137	0.335	0.032	0.078	0.014	0.028	0.054	0.085	0.386
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+)$	0.301	0.885	0.529	0.054	0.870	0.217	0.014	0.125	1.406
$D^+ \rightarrow K_S^0 a_1(1260)^+ (f_0(500) \pi^+)$	0.534	0.538	2.369	0.050	0.553	0.215	0.097	0.085	2.410
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+ (K^{*-} \pi^+ [S])$	1.260	0.094	0.306	0.003	0.093	0.177	0.174	0.060	1.328
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+ (K^{*-} \pi^+ [D])$	0.286	0.099	0.216	0.007	0.041	0.027	0.042	0.078	0.386
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+ (K^{*-} \pi^+)$	0.857	0.078	0.221	0.002	0.066	0.123	0.119	0.063	0.910
$D^+ \rightarrow \bar{K}_1(1270)^0 \pi^+ (K_S^0 \rho^0 [S])$	1.151	0.274	1.511	0.071	0.480	0.172	0.061	0.086	1.990
$D^+ \rightarrow \bar{K}(1460)^0 (K^{*-} \pi^+) \pi^+$	0.288	0.081	0.162	0.001	0.048	0.016	0.016	0.071	0.351
$D^+ \rightarrow \bar{K}(1460)^0 (K_S^0 \rho^0) \pi^+$	0.365	0.546	2.288	0.044	0.374	0.194	0.153	0.058	2.423
$D^+ \rightarrow \bar{K}_1(1650)^0 \pi^+ (K^{*-} \pi^+ [S])$	1.836	0.862	0.077	0.007	0.164	0.095	0.195	0.063	2.049
$D^+ \rightarrow (K_S^0 \rho^0 [S])_A \pi^+$	0.644	0.758	3.139	0.036	0.124	0.154	0.037	0.058	3.300
$D^+ \rightarrow (K_S^0 \rho^0 [D])_A \pi^+$	0.188	0.248	0.334	0.044	0.010	0.072	0.001	0.092	0.474
$D^+ \rightarrow (K_S^0 \rho^0)_A \pi^+$	0.863	0.876	4.287	0.031	0.131	0.236	0.066	0.078	4.469
$D^+ \rightarrow (K_S^0 (\pi^+ \pi^-)_S)_A \pi^+$	0.751	0.318	0.933	0.035	0.243	0.548	0.363	0.149	1.432
$D^+ \rightarrow ((K_S^0 \pi^+)_{S\text{-wave}} \pi^-)_P \pi^+$	0.347	0.073	1.422	0.014	0.128	0.259	0.039	0.086	1.497
$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$ non-resonance	0.604	0.256	0.191	0.025	0.153	0.580	0.327	0.078	0.969

TABLE IV. Systematic uncertainties of phases for amplitudes. The different sources include (I) masses and widths of the intermediate resonances, (II) effective radius of intermediate resonances and  $D^+$ , (III) parameters in the  $K_S^0 \pi^+$   $S$ -wave parameterization, (IV) parameters in the  $\rho - \omega$  mixing parameterization, (V) line shape of the  $f_0(500)$ , (VI) effect from peaking background, (VII) effect from general background, and (VIII) fit procedure.

Amplitude	Source ( $\sigma_{\text{stat}}$ )								total
	I	II	III	IV	V	VI	VII	VIII	
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+ [D])$	0.317	0.413	1.221	0.059	0.273	0.042	0.057	0.061	1.412
$D^+ \rightarrow K_S^0 a_1(1260)^+ (f_0(500) \pi^+)$	0.265	0.343	1.110	0.262	-	0.220	0.058	0.071	1.243
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+ (K^{*-} \pi^+ [S])$	0.872	0.362	1.006	0.131	0.257	0.003	0.051	0.058	1.412
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+ (K^{*-} \pi^+ [D])$	0.393	0.252	0.451	0.068	0.062	0.001	0.097	0.149	0.679
$D^+ \rightarrow \bar{K}_1(1270)^0 \pi^+ (K_S^0 \rho^0 [S])$	1.135	0.349	0.123	0.021	0.012	0.131	0.121	0.121	1.213
$D^+ \rightarrow \bar{K}(1460)^0 (K^{*-} \pi^+) \pi^+$	0.786	0.032	0.152	0.049	0.128	0.028	0.092	0.054	0.820
$D^+ \rightarrow \bar{K}(1460)^0 (K_S^0 \rho^0) \pi^+$	0.573	0.022	1.249	0.023	0.261	0.070	0.062	0.139	1.409
$D^+ \rightarrow \bar{K}_1(1650)^0 \pi^+ (K^{*-} \pi^+ [S])$	1.171	0.166	0.948	0.026	0.089	0.066	0.118	0.051	1.526
$D^+ \rightarrow (K_S^0 \rho^0 [S])_A \pi^+$	0.539	0.307	0.217	0.015	0.061	0.007	0.115	0.050	0.672
$D^+ \rightarrow (K_S^0 \rho^0 [D])_A \pi^+$	0.173	0.278	1.057	0.038	0.273	0.045	0.057	0.100	1.147
$D^+ \rightarrow (K_S^0 (\pi^+ \pi^-)_S)_A \pi^+$	0.254	0.508	0.442	0.072	0.010	0.058	0.092	0.050	0.733
$D^+ \rightarrow ((K_S^0 \pi^+)_{S\text{-wave}} \pi^-)_P \pi^+$	0.142	0.226	3.309	0.083	0.192	0.027	0.059	0.125	3.330