



# Top mass measurements in ATLAS and CMS

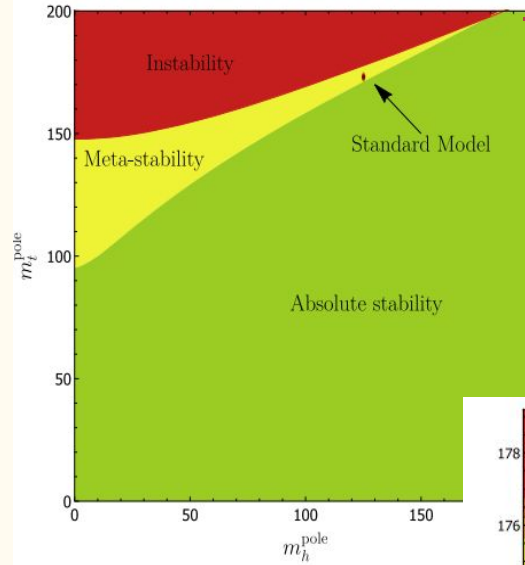
—  
Marco Vanadia on behalf of the ATLAS and CMS collaborations  
INFN Rome Tor Vergata

*Blois*

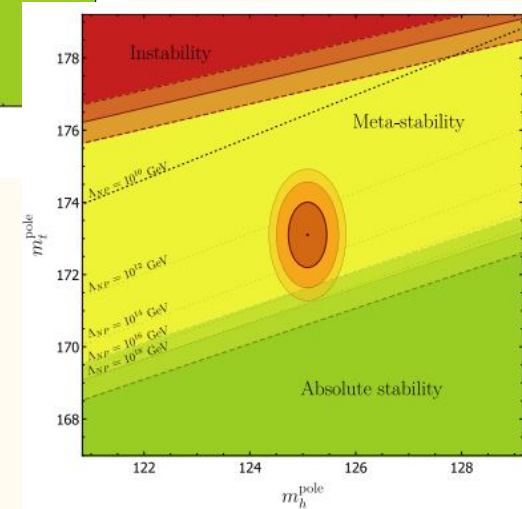
*5/6/2019*

# Top mass: why we care

- $m_t \sim 172.5$  GeV
  - heaviest elementary particle
- critical input for EW precision tests
- crucial interplay with the Higgs
  - vacuum stability
  - quartic coupling
- cosmological consequences
  - e.g. Universe lifetime, see [PhysRevD.97.056006](#)
- challenging for experiments and theory
  - ambiguities on  $m_t$  interpretation at  $O(\Lambda_{\text{QCD}})$   
(see e.g. review [arXiv:1903.0657](#))

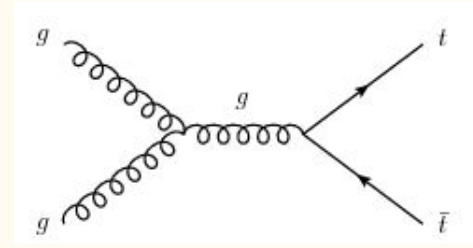


[PhysRevD.97.056006](#)



# Top mass measurement at the LHC

- Lots of data:
  - $\sigma_{tt} \sim 830 \text{ pb @ } 13 \text{ TeV}$  (180 @ 7 TeV, 250 @ 8 TeV)
  - $\sim 140/\text{fb}$  per experiment @ 13 TeV (4 @ 7 TeV, 20 @ 8 TeV)
- Direct measurements:
  - observable dependent on  $m_t$
  - problem: measurement of “ $m_t^{\text{MC}}$ ” due to color
- Indirect measurements:
  - property  $f(m_t^{\text{pole}})$  (e.g. cross section) + theory  $\rightarrow m_t(\text{scheme})$
  - problem: uncertainties in fixed-order calculations due to soft radiation, non-perturbative effects, ...
- Many decay channels, many experimental observables  $\rightarrow$  combination

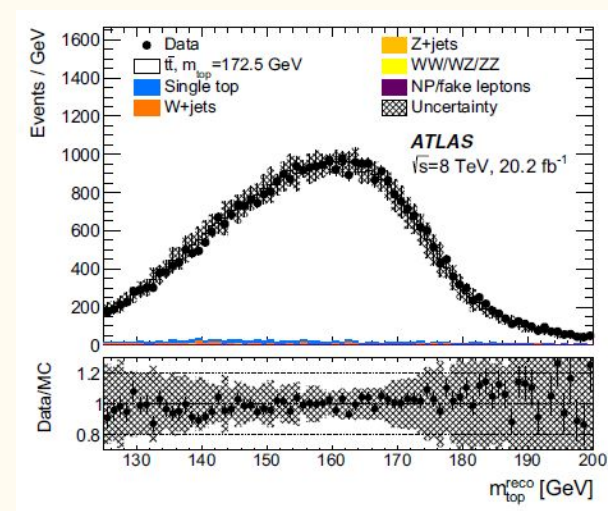
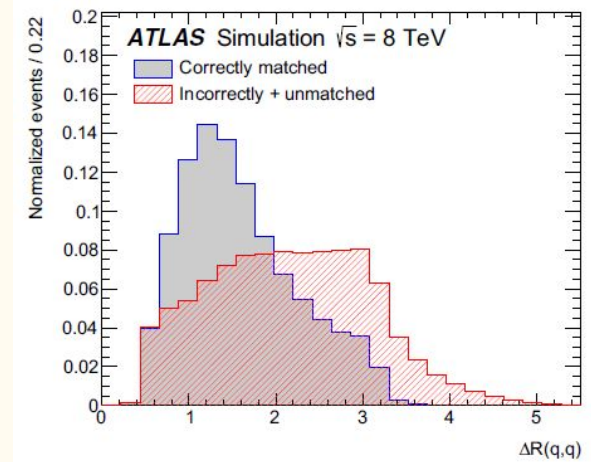


**Top Pair Decay Channels**

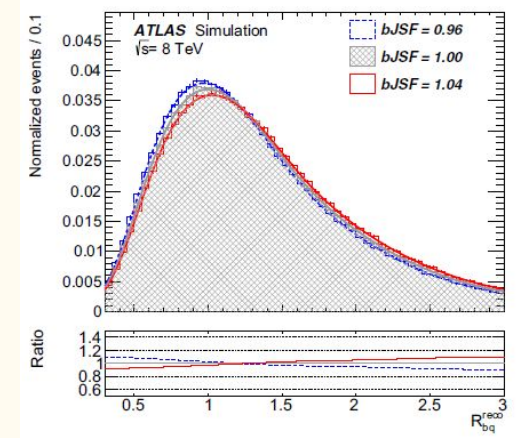
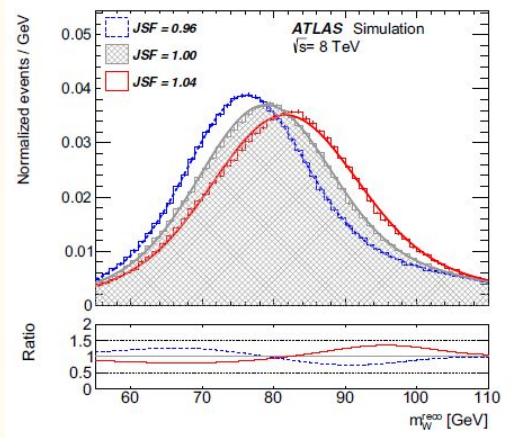
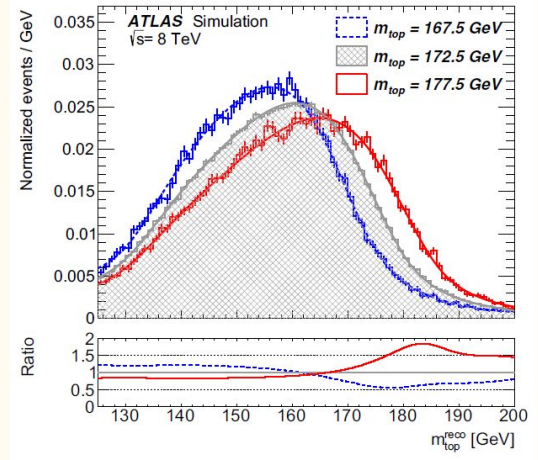
$c\bar{s}$	electron+jets	muon+jets	tau+jets	all-hadronic	
$u\bar{d}$					
$\tau^-$	tau+jets				
$\mu^-$	muon+jets				
$e^-$	electron+jets				
$W$ decay	$e^+$	$\mu^+$	$\tau^+$		$u\bar{d}$

# $\ell + \text{jets}$ channel: ATLAS 8 TeV

- 1 high-pt isolated e/mu,  $\geq 4$  jets,  $\equiv 2$  b-jets
- Topology reconstruction: KLFitter
- $L(m_t^{\text{reco}})$  maximised to assign jets to partons
- observables:
  - $m_{\text{top}}^{\text{reco}}$
  - $m_W^{\text{reco}} \rightarrow$  Jet Energy Scale
  - $R_{\text{bq}}^{\text{reco}} = (p_T^{\text{b-lep}} + p_T^{\text{b-had}}) / (p_T^{\text{q1}} + p_T^{\text{q2}}) \rightarrow$  b-Jet Energy Scale
- selection on BDT score
  - kinematics used against wrong topological reconstruction



- 3-dimensional template fit to the 3 observables, templates as a function of  $m_t^{MC}$



$m_{top} = 172.08 \pm 0.39$  (stat) GeV,  
 $JSF = 1.005 \pm 0.001$  (stat), and  
 $bJSF = 1.008 \pm 0.005$  (stat).

$m_{top} = 172.08 \pm 0.39$  (stat)  $\pm 0.82$  (syst) GeV

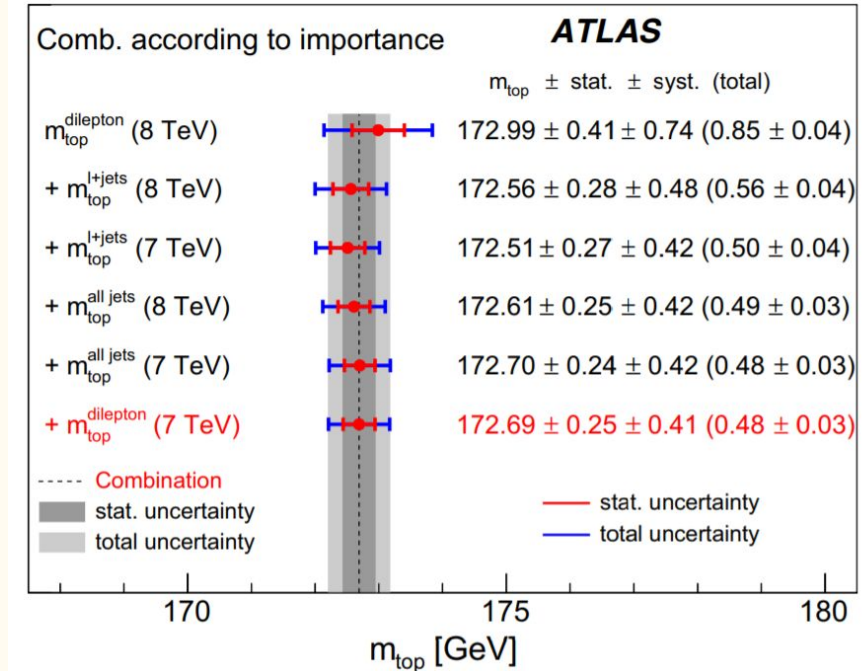
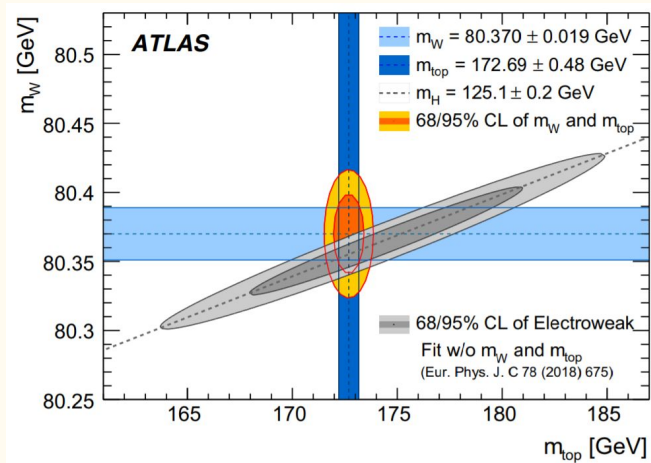
Dominant systematics:

- Jet Energy Scale: 0.58 GeV
- b-tagging: 0.38 GeV

Anti-correlation of systematics in different analyses -> combination!

Dominant uncertainties after the combination:

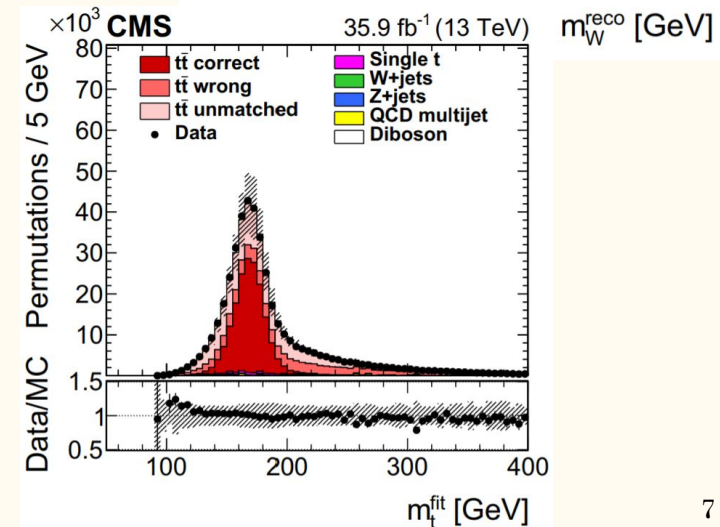
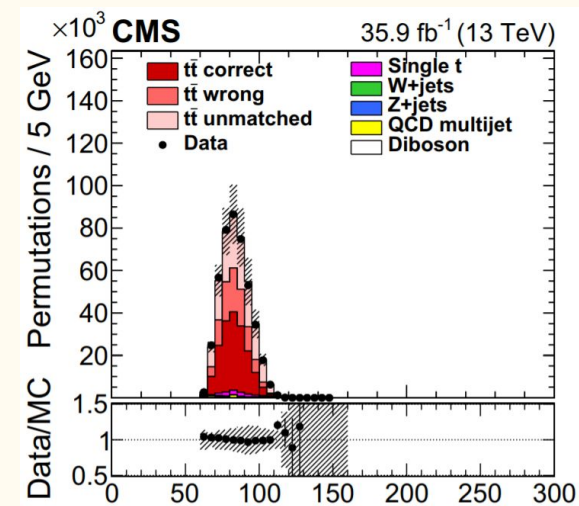
- ME generator: 0.12 GeV
  - aMC@NLO vs Powheg
- Jet Energy Scale: 0.22 GeV
- b-Jet Energy Scale: 0.17 GeV
- b-tagging: 0.17 GeV



# $\ell$ +jets channel: CMS 13 TeV

- 1 high-pt isolated e/mu,  $\geq 4$  jets, exactly 2 b-jets
- kinematic fit: 2 combinations of b-jets with light-jets with 2 solutions for  $p_{\text{longitudinal}}^{\nu} \rightarrow 4$  permutations
- permutations weighted by  $P=e^{-\chi^2/2}$ ,  $P>0.2$  applied
- background ( $\sim 4\%$ ) from MC
- Ideogram method
  - $m_t^{\text{fit}}$  and JSF PDFs from MC
    - $W \rightarrow qq' \rightarrow \text{JSF}$
  - likelihood fit in data
  - 1D fit (JSF=1), 2D fit (JSF free), hybrid (gaus. prior on JSF)

[Eur. Phys. J. C 78 \(2018\) 891](#)



# $\ell + \text{jets}$ channel: CMS 13 TeV

Eur. Phys. J. C 78 (2018) 891

Results:

$$m_t^{\text{hyb}} = 172.25 \pm 0.08 \text{ (stat+JSF)} \pm 0.62 \text{ (syst)} \text{ GeV,}$$

$$\text{JSF}^{\text{hyb}} = 0.996 \pm 0.001 \text{ (stat)} \pm 0.008 \text{ (syst).}$$

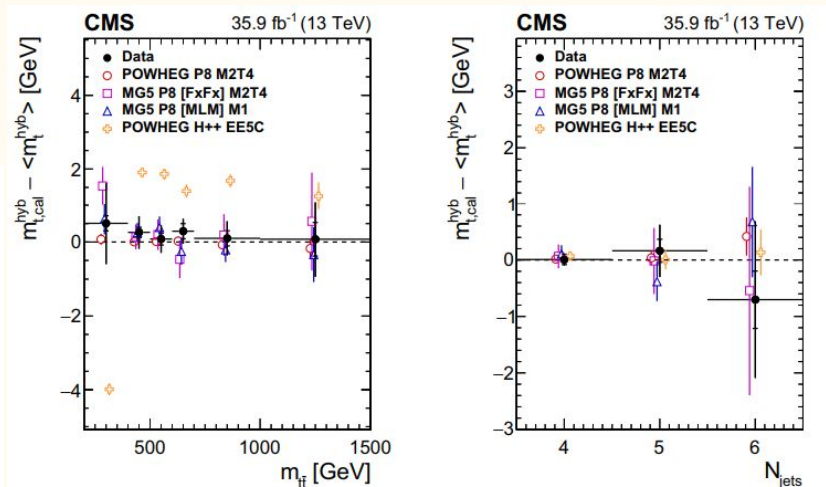
- Jet Energy Corrections  $\rightarrow$  0.18 GeV
- Jet Energy Resolution  $\rightarrow$  0.12 GeV
- JEC Flavor response  $\rightarrow$  0.39 GeV

- First top mass on Run-2 data
- First test of new generation of NLO generators

- b-jet modelling  $\rightarrow$  0.12 GeV
- Generator  $\rightarrow$  0.20 GeV
- FSR scale in parton shower  $\rightarrow$  0.13 GeV
- color reconnection  $\rightarrow$  0.31 GeV

Comparison of different MC models on differential  $m_t$  measurements as a function of several quantities

Model	$\chi^2$ probability							
	$p_T^{\text{t, had}}$	$m_{\bar{t}t}$	$p_T^{\bar{t}}$	$N_{\text{jets}}$	$p_T^{\text{b, had}}$	$ \eta^{\text{b, had}} $	$\Delta R_{b\bar{b}}$	$\Delta R_{q\bar{q}'}$
POWHEG P8 M2T4	0.68	0.94	0.91	0.71	0.98	0.60	0.61	0.70
MG5 P8 [FxFx] M2T4	0.98	0.78	0.93	0.94	0.80	0.35	0.94	0.91
MG5 P8 [MLM] M1	0.48	0.84	0.99	0.41	0.98	0.17	0.71	0.61
POWHEG H++ EE5C	0.07	$2 \times 10^{-13}$	0.52	0.72	$2 \times 10^{-4}$	0.55	0.36	$2 \times 10^{-5}$
POWHEG P8 ERD on	0.75	0.99	0.83	0.53	0.95	0.64	0.38	0.96
POWHEG P8 QCD inspired	0.80	0.94	0.94	0.66	0.99	0.71	0.49	0.90
POWHEG P8 gluon move	0.87	0.94	0.93	0.72	0.93	0.51	0.59	0.93





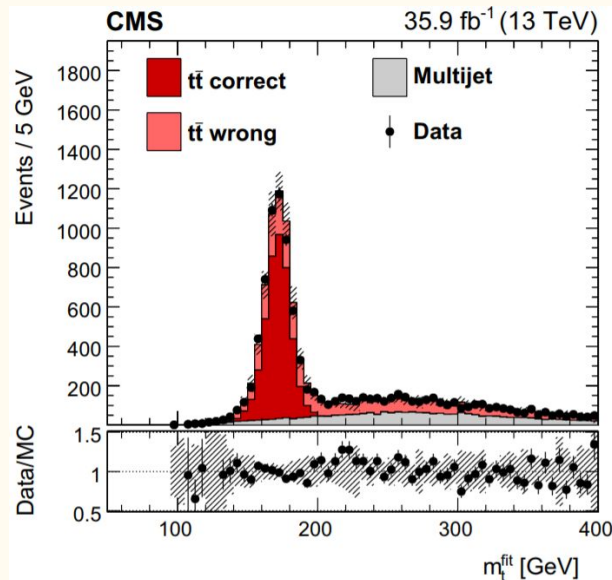
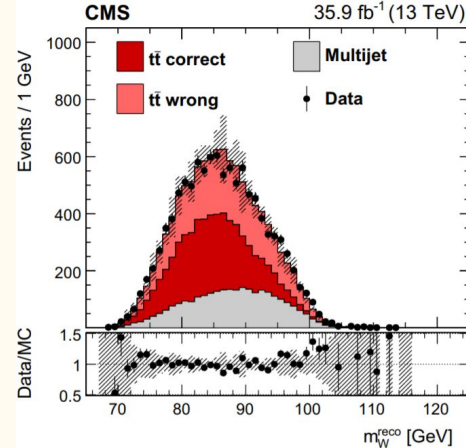
# all-had channel: CMS 13 TeV

- $\geq 6$  jets,  $\geq 2$  b-tagged jets,  $\Delta R_{bb} > 2$
- kinematic fit, analogous to  $l+jets$ 
  - multijet bkg (25%) from events with 0 b-jets
- ideogram method, analogous to  $l+jets$
- best result from hybrid method

$$m_t^{\text{hyb}} = 172.34 \pm 0.20 (\text{stat+JSF}) \pm 0.70 (\text{syst}) \text{ GeV}$$

$$\text{JSF}^{\text{hyb}} = 0.997 \pm 0.002 (\text{stat}) \pm 0.007 (\text{syst}).$$

- dominant uncertainties:
  - Jet Energy Corrections  $\rightarrow 0.15$  GeV
  - JEC Flavor Response  $\rightarrow 0.34$  GeV
  - ME/PS matching  $\rightarrow 0.24$  GeV
  - ISR PS scale  $\rightarrow 0.12$  GeV
  - FSR PS scale  $\rightarrow 0.18$  GeV
  - Color reconnection  $\rightarrow 0.36$  GeV



[Eur. Phys. J. C 79 \(2019\) 313](#)

# all-had+l-jets: CMS 13 TeV

Same method for both channels  $\rightarrow$  combined likelihood

$$\mathcal{L}(m_t, \text{JSF}) = \mathcal{L}_A(m_t, \text{JSF}) \mathcal{L}_L(m_t, \text{JSF}).$$

$$m_t^{\text{hyb}} = 172.26 \pm 0.07 (\text{stat+JSF}) \pm 0.61 (\text{syst}) \text{ GeV}$$

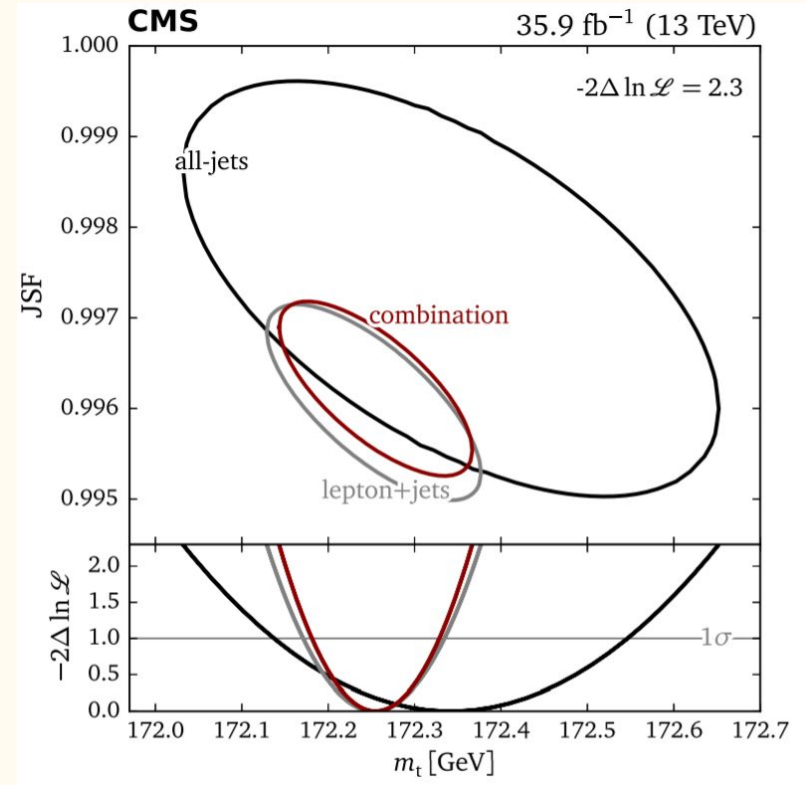
$$\text{JSF}^{\text{hyb}} = 0.996 \pm 0.001 (\text{stat}) \pm 0.007 (\text{syst})$$

Dominant uncertainties:

- Jet Energy Corrections  $\rightarrow$  0.17 GeV
- JEC Flavor Response  $\rightarrow$  0.37 GeV
- Color reconnection modelling  $\rightarrow$  0.33 GeV
- ME generator  $\rightarrow$  0.21 GeV
- FSR PS scale  $\rightarrow$  0.12 GeV

Dilepton channels: see BACKUP and Ref.:

- [PLB 761 \(2016\) 350](#)
- [Phys. Rev. D 96, 032002](#)

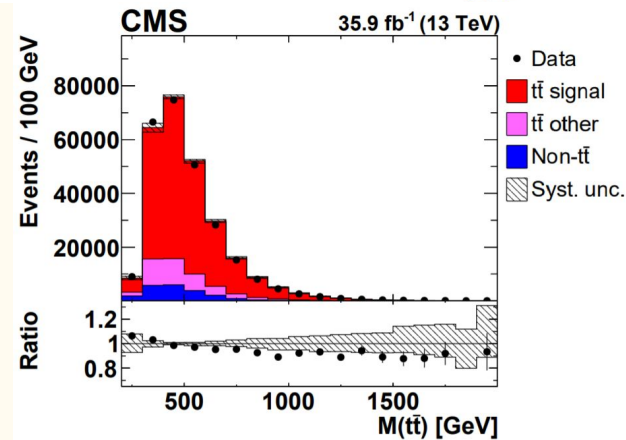
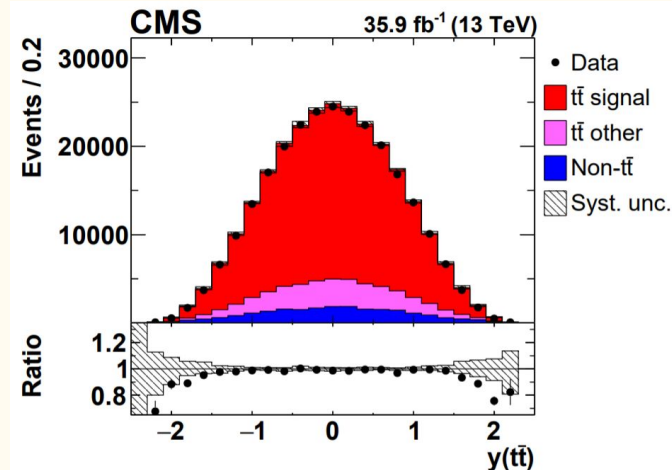


# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV

measure  $\sigma_{t\bar{t}}$   $\rightarrow$  sensitive to  $m_t^{\text{pole}}$

- 2 isolated el/mu, opposite charge
- $\geq 2$  jets,  $\geq 1$  b-tagged jet
- kinematic reconstruction:
  - invariant masses constraints imposed
  - toys with smeared momentum for each event to recover events with no solutions
  - toys weighted using expected spectra
- modified algorithm for  $m_t^{\text{pole}}$  measurement
  - $\nu\nu$  reconstruction without imposing  $m_t$  as constraint

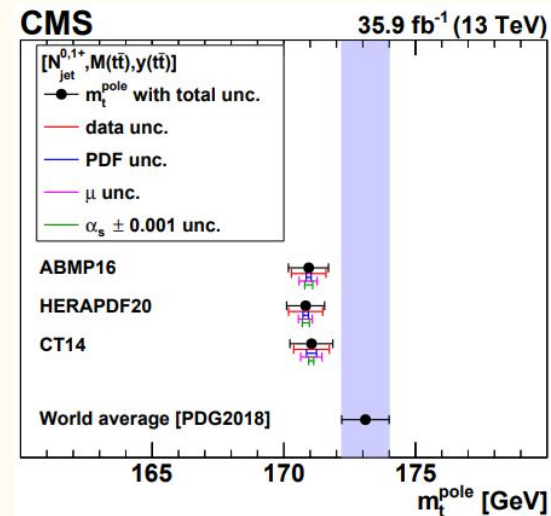
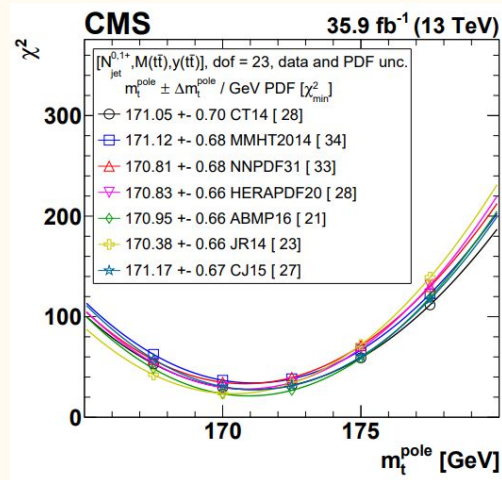
[arXiv:1904.05237](https://arxiv.org/abs/1904.05237)



# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV

arXiv:1904.05237

- measurement unfolded to parton-level differential  $\sigma$
- $\alpha_s$  and  $m_t^{\text{pole}}$  from  $\sigma(N_{\text{jets}}, M_{\text{tt}}, y_{\text{tt}})$  vs fixed-order NLO calculations
- $m_t^{\text{pole}}$  measurement from  $\chi^2$  of pred. vs data for different hyp.
- JES is dominant exp. uncert.



Final measurement: simultaneous PDF,  $\alpha_s$ ,  $m_t^{\text{pole}}$  NLO fit including HERA DIS data

$$m_t^{\text{pole}} = 170.5 \pm 0.7(\text{fit}) \pm 0.1(\text{model})_{-0.1}^{+0.0}(\text{param}) \pm 0.3(\text{scale}) \text{ GeV} = 170.5 \pm 0.8(\text{total}) \text{ GeV}.$$

# Indirect: $m_t^{\text{pole}}$ in $tt+1$ jet, ATLAS 8 TeV

[arXiv:1905.02302](https://arxiv.org/abs/1905.02302)

- 1 isolated e/mu,  $\geq 5$  jets, =2 b-tagged
- $p_T^{\text{miss}} \rightarrow p_T^{\nu}$ , then  $m_W$  constraint imposed
- Ws and b-jets  $\rightarrow$  top,  $|m_t^{\text{lep}} - m_t^{\text{had}}|$  minimised
- leading jet not used for tops  $\rightarrow$  ISR candidate
- observable sensitive to  $m_t^{\text{pole}}$ :

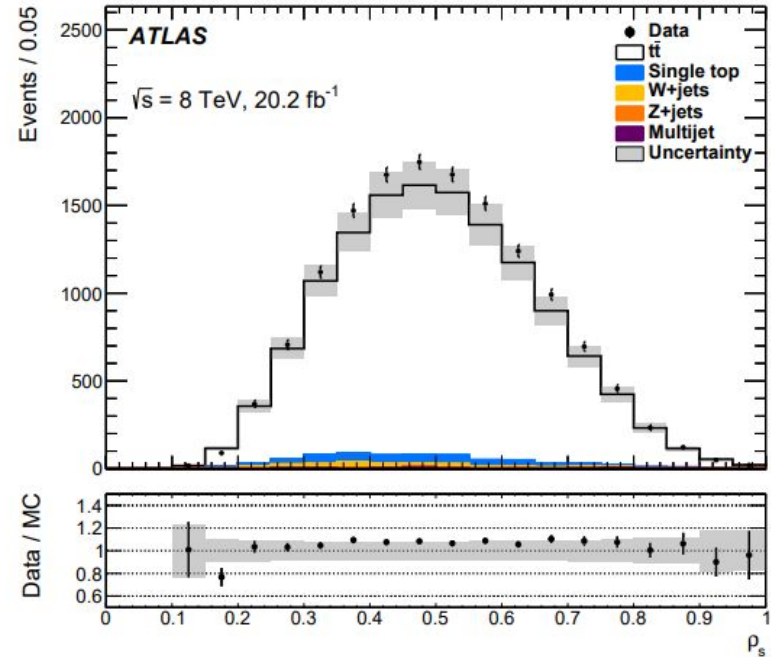
$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \cdot \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}$$

with

$$\rho_s = 2m_0 / m_{t\bar{t}+1\text{-jet}}$$

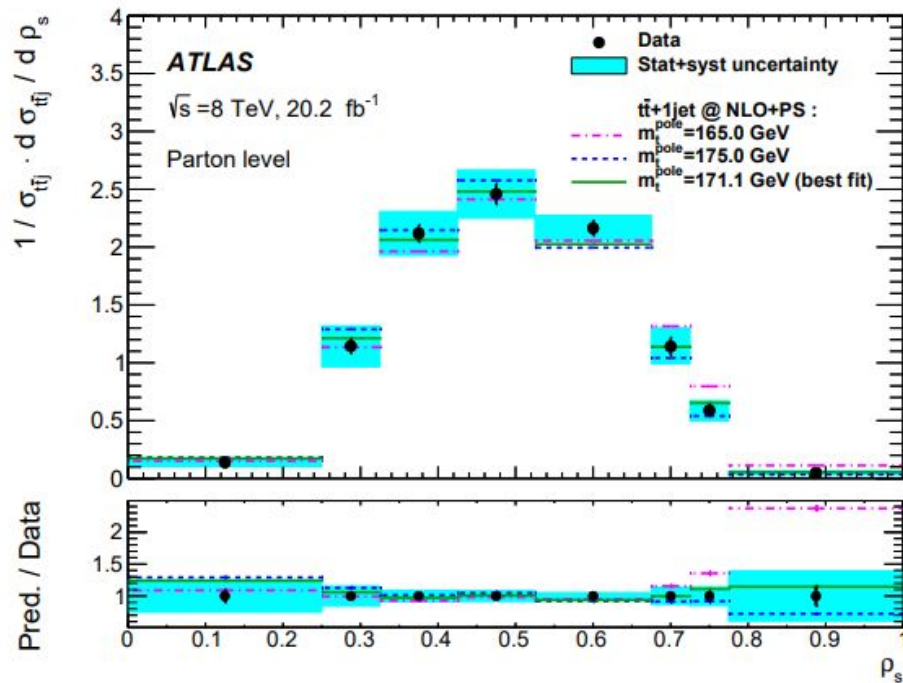
constant

invariant mass of  
 $tt+1$  jet system



# Indirect: $m_t^{\text{pole}}$ in $tt+1$ jet, ATLAS 8 TeV

[arXiv:1905.02302](https://arxiv.org/abs/1905.02302)



- Data unfolded to parton level
- $m_t^{\text{pole}}$  extracted with  $\chi^2$  minimization vs NLO+PS fixed order predictions
- Dominant uncertainties:
  - JES, JER
  - PS and hadronization
  - Color reconnection
  - Other modelling (e.g. UE)
  - Scale and PDF (theo)

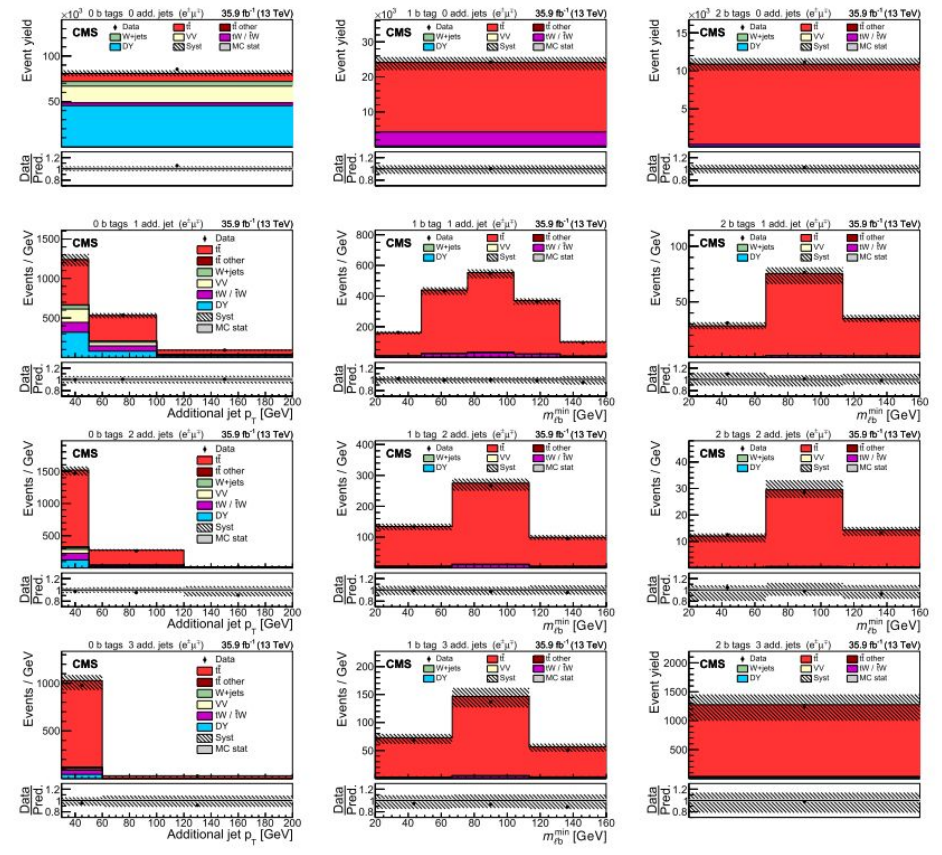
$$m_t^{\text{pole}} = 171.1 \pm 0.4(\text{stat}) \pm 0.9(\text{syst}) {}^{+0.7}_{-0.3}(\text{theo}) \text{ GeV}$$

→  
 $\overline{\text{MS}}$

$$m_t(m_t) = 162.9 \pm 0.5(\text{stat}) \pm 1.0(\text{syst}) {}^{+2.1}_{-1.2}(\text{theo}) \text{ GeV}$$

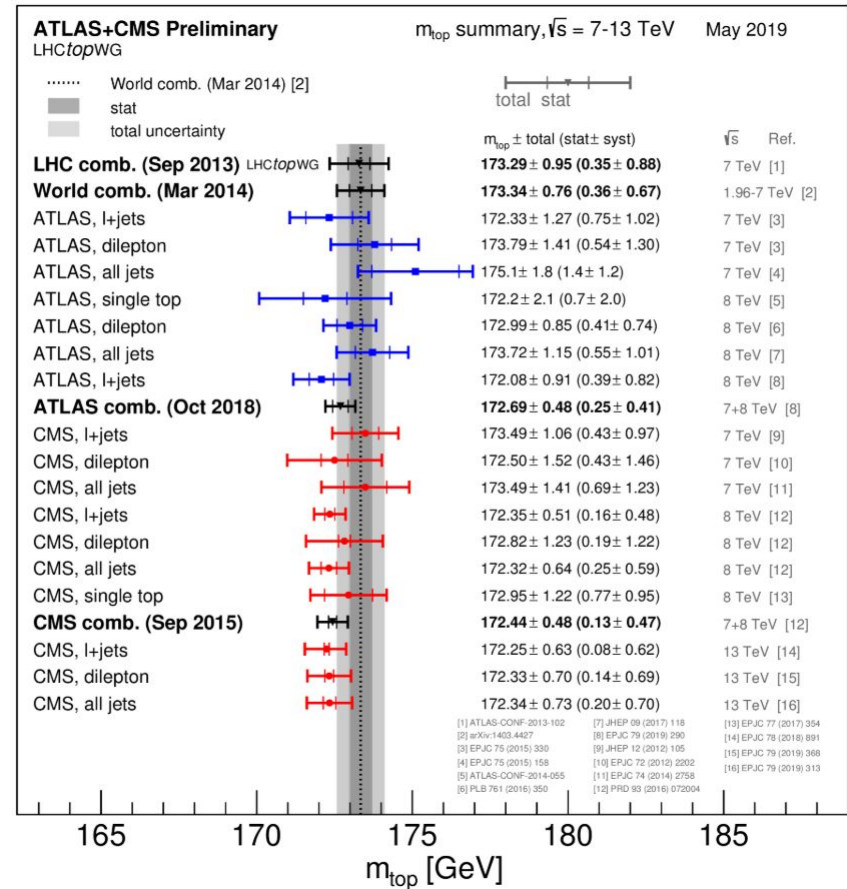
# Direct/Indirect: CMS dilepton 13 TeV

- $e\mu$  channel (opposite charge)
- 12 event categories in function of  $N_{b\text{-jets}}, N_{\text{nonb-jets}}$
- $L(\sigma_{tt}, m_t^{\text{MC}})$  fit to observables (depending on region):
  - $N_{\text{events}}$
  - $m_{lb}^{\text{min}}$  for  $\geq 1$  b-jet
  - smallest non-bjet  $p_{Tj}$
- results  $\sigma_{tt} = 815 \pm 2 \text{ (stat)} \pm 29 \text{ (syst)} \pm 20 \text{ (lumi)} \text{ pb}$ ,  
 $m_t^{\text{MC}} = 172.33 \pm 0.14 \text{ (stat)}^{+0.66}_{-0.72} \text{ (syst)} \text{ GeV}$ .
- dominant uncertainty: JES 0.57 GeV
- $m_t^{\text{pole}}$  and  $m_t(\text{MS-bar})$  are also measured



# Conclusion

- Direct measurements  $< 500$  MeV uncertainty on  $m_t^{\text{MC}}$
- Indirect measurements  $< 1$  GeV uncertainty on  $m_t^{\text{pole}}$
- How to improve:
  - combining
  - jet uncertainties
  - $t\bar{t}$  MC modelling
- We need theory:
  - $m_t^{\text{MC}} \leftrightarrow m_t^{\text{pole}} \leftrightarrow m_t(\text{MS-bar})$  known up to 4-loops 1502.01030
  - scale dependency of simulations/calculations
- Lots of data and new channels to explore
  - MC stat is also a challenge



summary of ATLAS and CMS direct measurements



# BACKUP



# ATLAS

D0  $\sigma_{\text{incl.}}^{\text{tt}}$ ,  $\sqrt{s}= 1.96$  TeV  
PRD 94, 092004 (2016)



$$m_t^{\text{pole}} \pm \Delta^{\text{tot}}$$
$$172.8^{+3.4}_{-3.2} \text{ GeV}$$

CMS  $\sigma_{\text{incl.}}^{\text{tt}}$ , NNPDF3.0,  $\sqrt{s}= 7+8$  TeV  
JHEP 08 (2016) 029



$$173.8^{+1.7}_{-1.8} \text{ GeV}$$

CMS  $\sigma_{\text{incl.}}^{\text{tt}}$ ,  $\sqrt{s}= 13$  TeV  
JHEP 09 (2017) 051



$$170.6^{+2.7}_{-2.7} \text{ GeV}$$

CMS  $\sigma_{\text{diff.}}^{\text{tt}}$ ,  $\sqrt{s}= 13$  TeV  
arXiv:1904.05237



$$170.5^{+0.8}_{-0.8} \text{ GeV}$$

ATLAS  $\sigma_{\text{diff.}}^{\text{tt}}$ ,  $\sqrt{s}= 8$  TeV  
EPJC 77 (2017) 804



$$173.2^{+1.6}_{-1.6} \text{ GeV}$$

ATLAS  $\sigma_{\text{incl.}}^{\text{tt}}$ ,  $\sqrt{s}= 7+8$  TeV  
EPJC 74 (2014) 3109



$$172.9^{+2.5}_{-2.6} \text{ GeV}$$

ATLAS  $\sigma_{\text{diff.}}^{\text{tt}+1 \text{ jet}}$ ,  $\sqrt{s}= 7$  TeV  
JHEP 10 (2015) 121

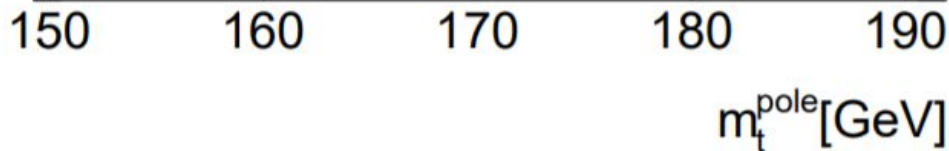


$$173.7^{+2.3}_{-2.1} \text{ GeV}$$

ATLAS  $\sigma_{\text{diff.}}^{\text{tt}+1 \text{ jet}}$ ,  $\sqrt{s}= 8$  TeV  
*this analysis*



$$171.1^{+1.2}_{-1.1} \text{ GeV}$$



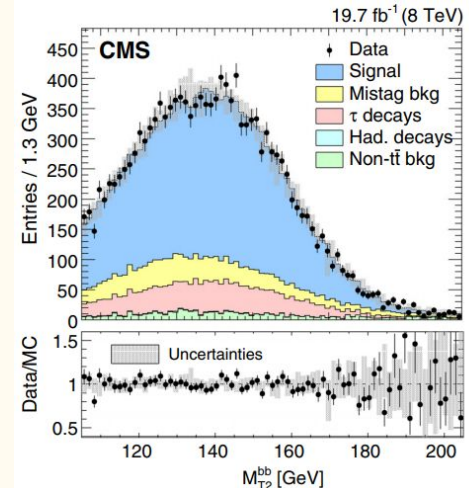
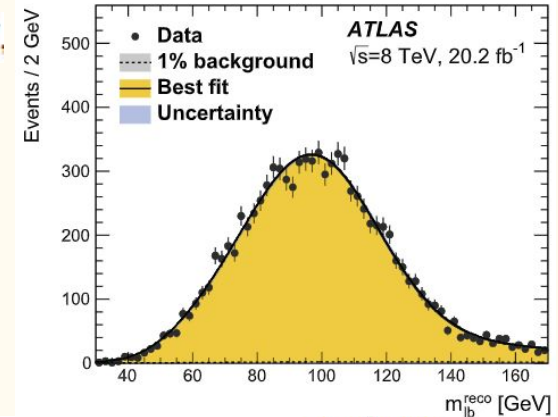
from

[arXiv:1905.02302](https://arxiv.org/abs/1905.02302)

# Dilepton channel:

- 8 TeV result from ATLAS  $m_{top} = 172.99 \pm 0.41$  (stat)  $\pm 0.74$  (syst) GeV,
  - template fit to  $m_{lb}$ , dominant uncertainties:
    - hadronization modelling  $\rightarrow 0.22$  GeV
    - ISR/FSR modelling  $\rightarrow 0.23$  GeV
    - JES  $\rightarrow 0.54$  GeV
    - b-JES  $\rightarrow 0.30$  GeV
- 8 TeV result from CMS  $172.22 \pm 0.18$ (stat)  $^{+0.89}_{-0.93}$ (syst) GeV.
  - template fit to  $m_{lb}$  and  $M_{T2}$  (modified transverse mass)
  - 1D (JSF, correction to jet calibration, =1),  
2D fit ( $m_t$  and JSF), hybrid (linear combination)
  - dominant uncertainties:
    - JES  $\rightarrow 0.46$  GeV
    - b-fragmentation  $\rightarrow 0.40$  GeV
    - top  $p_T$   $\rightarrow 0.51$  GeV
    - hard scattering scale  $\rightarrow 0.47$  GeV
    - matching scale  $\rightarrow 0.31$  GeV

some of these  
are very  
asymmetric  
up/down

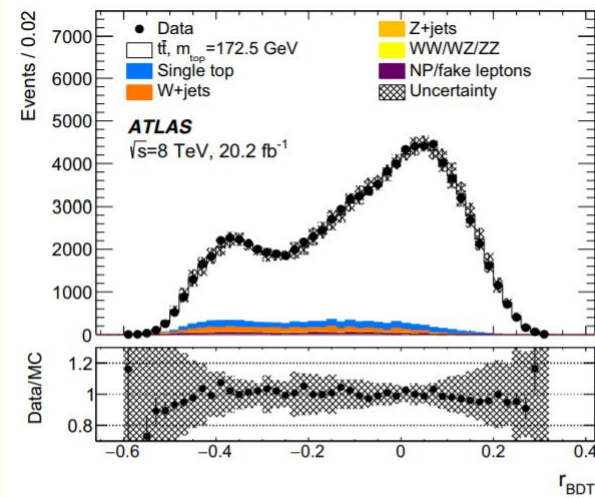
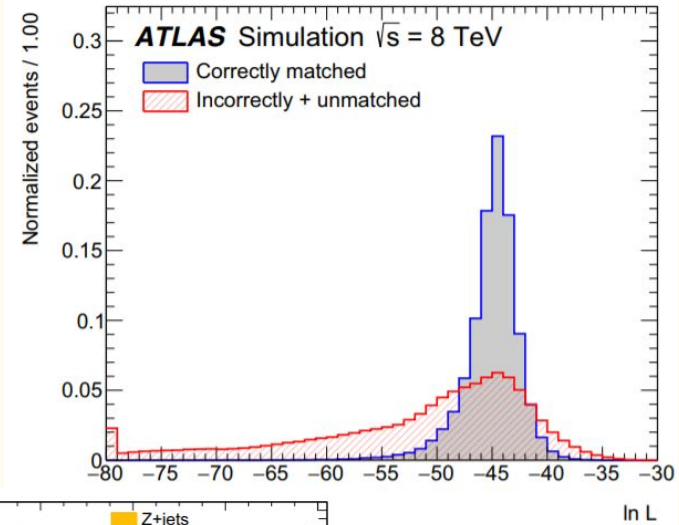


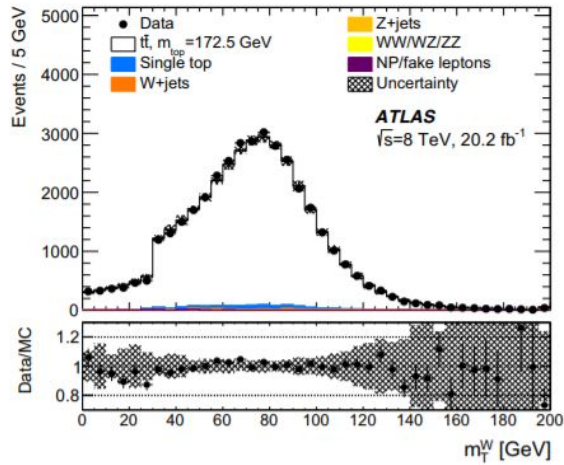
# $\ell$ +jets channel: ATLAS 8 TeV

## BDT

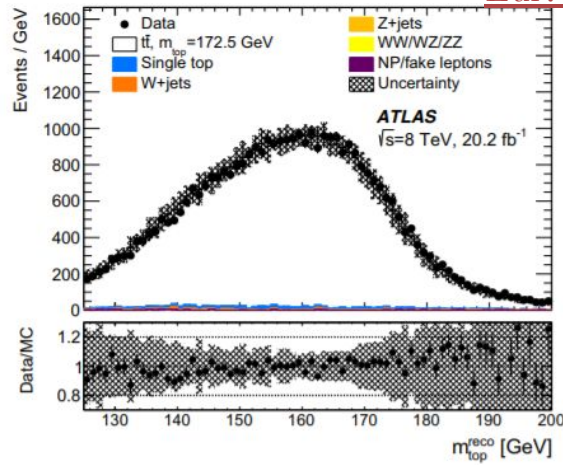
**Table 2** The input variables to the BDT algorithm sorted by their separation

Separation (%)	Description
31	Logarithm of the event likelihood of the best permutation, $\ln L$
13	$\Delta R$ of the two untagged jets $q_1$ and $q_2$ from the hadronically decaying $W$ boson, $\Delta R(q, q)$
5.0	$p_T$ of the hadronically decaying $W$ boson
4.3	$p_T$ of the hadronically decaying top quark
4.2	Relative event probability of the best permutation
2.0	$p_T$ of the reconstructed $t\bar{t}$ system
1.7	$p_T$ of the semi-leptonically decaying top quark
1.2	Transverse mass of the leptonically decaying $W$ boson
0.3	$p_T$ of the leptonically decaying $W$ boson
0.3	Number of jets
0.2	$\Delta R$ of the reconstructed $b$ -tagged jets
0.2	Missing transverse momentum
0.1	$p_T$ of the lepton

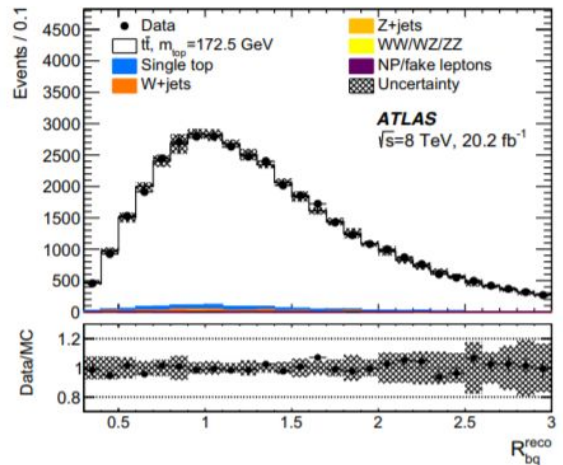
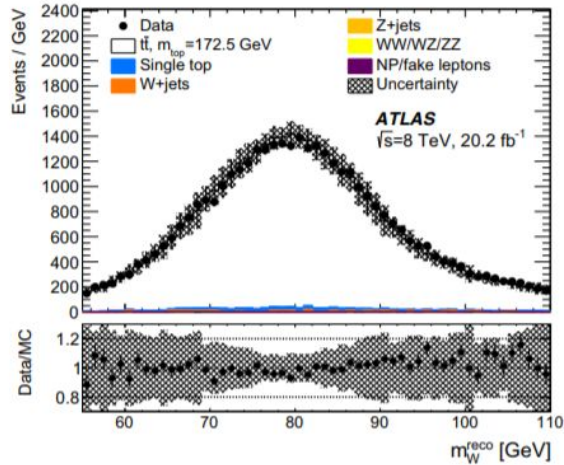




(a) W boson transverse mass



(b) Reconstructed top quark mass



# $\ell + \text{jets}$ channel: ATLAS 8 TeV

unbinned LH on  $i=1\dots N$  events

$$\begin{aligned}
& L_{\text{shape}}^{\ell+\text{jets}}(m_{\text{top}}, \text{JSF}, \text{bJSF}, f_{\text{bkg}}) \\
&= \prod_{i=1}^N P_{\text{top}}(m_{\text{top}}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}, f_{\text{bkg}}) \\
&\quad \times P_W(m_W^{\text{reco},i} | \text{JSF}, f_{\text{bkg}}) \\
&\quad \times P_{R_{bq}}(R_{bq}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}, f_{\text{bkg}}),
\end{aligned}$$

$$\begin{aligned}
& P_{\text{top}}(m_{\text{top}}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}, f_{\text{bkg}}) \\
&= (1 - f_{\text{bkg}}) \cdot P_{\text{top}}^{\text{sig}}(m_{\text{top}}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}) \\
&\quad + f_{\text{bkg}} \cdot P_{\text{top}}^{\text{bkg}}(m_{\text{top}}^{\text{reco},i} | \text{JSF}, \text{bJSF}),
\end{aligned}$$

$$\begin{aligned}
& P_W(m_W^{\text{reco},i} | \text{JSF}, f_{\text{bkg}}) \\
&= (1 - f_{\text{bkg}}) \cdot P_W^{\text{sig}}(m_W^{\text{reco},i} | \text{JSF}) \\
&\quad + f_{\text{bkg}} \cdot P_W^{\text{bkg}}(m_W^{\text{reco},i} | \text{JSF}), \quad \text{and}
\end{aligned}$$

$$\begin{aligned}
& P_{R_{bq}}(R_{bq}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}, f_{\text{bkg}}) \\
&= (1 - f_{\text{bkg}}) \cdot P_{R_{bq}}^{\text{sig}}(R_{bq}^{\text{reco},i} | m_{\text{top}}, \text{JSF}, \text{bJSF}) \\
&\quad + f_{\text{bkg}} \cdot P_{R_{bq}}^{\text{bkg}}(R_{bq}^{\text{reco},i} | \text{bJSF})
\end{aligned}$$

$\ell + \text{jets}$  channel:  
**ATLAS 8 TeV**  
 fit

Event selection	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$	
	Standard	Standard	BDT
$m_{\text{top}}$ result [GeV]	172.33	171.90	172.08
Statistics	0.75	0.38	0.39
– Stat. comp. ( $m_{\text{top}}$ )	0.23	0.12	0.11
– Stat. comp. (JSF)	0.25	0.11	0.11
– Stat. comp. (bJSF)	0.67	0.34	0.35
Method	$0.11 \pm 0.10$	$0.04 \pm 0.11$	$0.13 \pm 0.11$
Signal Monte Carlo generator	$0.22 \pm 0.21$	$0.50 \pm 0.17$	$0.16 \pm 0.17$
Hadronization	$0.18 \pm 0.12$	$0.05 \pm 0.10$	$0.15 \pm 0.10$
Initial- and final-state QCD radiation	$0.32 \pm 0.06$	$0.28 \pm 0.11$	$0.08 \pm 0.11$
Underlying event	$0.15 \pm 0.07$	$0.08 \pm 0.15$	$0.08 \pm 0.15$
Colour reconnection	$0.11 \pm 0.07$	$0.37 \pm 0.15$	$0.19 \pm 0.15$
Parton distribution function	$0.25 \pm 0.00$	$0.08 \pm 0.00$	$0.09 \pm 0.00$
Background normalization	$0.10 \pm 0.00$	$0.04 \pm 0.00$	$0.08 \pm 0.00$
$W$ +jets shape	$0.29 \pm 0.00$	$0.05 \pm 0.00$	$0.11 \pm 0.00$
Fake leptons shape	$0.05 \pm 0.00$	0	0
Jet energy scale	$0.58 \pm 0.11$	$0.63 \pm 0.02$	$0.54 \pm 0.02$
Relative $b$ -to-light-jet energy scale	$0.06 \pm 0.03$	$0.05 \pm 0.01$	$0.03 \pm 0.01$
Jet energy resolution	$0.22 \pm 0.11$	$0.23 \pm 0.03$	$0.20 \pm 0.04$
Jet reconstruction efficiency	$0.12 \pm 0.00$	$0.04 \pm 0.01$	$0.02 \pm 0.01$
Jet vertex fraction	$0.01 \pm 0.00$	$0.13 \pm 0.01$	$0.09 \pm 0.01$
$b$ -tagging	$0.50 \pm 0.00$	$0.37 \pm 0.00$	$0.38 \pm 0.00$
Leptons	$0.04 \pm 0.00$	$0.16 \pm 0.01$	$0.16 \pm 0.01$
Missing transverse momentum	$0.15 \pm 0.04$	$0.08 \pm 0.01$	$0.05 \pm 0.01$
Pile-up	$0.02 \pm 0.01$	$0.14 \pm 0.01$	$0.15 \pm 0.01$
Total systematic uncertainty	$1.04 \pm 0.08$	$1.07 \pm 0.10$	$0.82 \pm 0.06$
Total	$1.28 \pm 0.08$	$1.13 \pm 0.10$	$0.91 \pm 0.06$

# $\ell$ +jets channel: ATLAS 8 TeV uncertainties

# $\ell + \text{jets}$ channel: CMS 13 TeV, ideogram method

$$\mathcal{L}(\text{sample}|m_t, \text{JSF}) = P(\text{JSF}) \prod_{\text{events}} \left( \sum_{i=1}^n P_{\text{gof}}(i) \times \left[ \sum_j f_j P_j(m_{t,i}^{\text{fit}}|m_t, \text{JSF}) P_j(m_{W,i}^{\text{reco}}|m_t, \text{JSF}) \right] \right)^{w_{\text{evt}}}$$

$i$ = $i$ -th permutation in one event

$j$ =correct permutation, uncorrect permutation, unmatched

- PDFs from samples with 7 different  $m_t$  and 5 different JSF values
- method bias estimated with pseudo-experiments and corrected



	2D approach		1D approach	Hybrid	
	$\delta m_t^{2D}$ [GeV]	$\delta \text{JSF}^{2D}$ [%]	$\delta m_t^{1D}$ [GeV]	$\delta m_t^{\text{hyb}}$ [GeV]	$\delta \text{JSF}^{\text{hyb}}$ [%]
<i>Experimental uncertainties</i>					
Method calibration	0.05	<0.1	0.05	0.05	<0.1
JEC (quad. sum)	0.13	0.2	0.83	0.18	0.3
– InterCalibration	(–0.02)	(<0.1)	(+0.16)	(+0.04)	(<0.1)
– MPFIInSitu	(–0.01)	(<0.1)	(+0.23)	(+0.07)	(<0.1)
– Uncorrelated	(–0.13)	(+0.2)	(+0.78)	(+0.16)	(+0.3)
Jet energy resolution	–0.20	+0.3	+0.09	–0.12	+0.2
b tagging	+0.03	<0.1	+0.01	+0.03	<0.1
Pileup	–0.08	+0.1	+0.02	–0.05	+0.1
Non- $\bar{t}$ background	+0.04	–0.1	–0.02	+0.02	–0.1
<i>Modeling uncertainties</i>					
JEC Flavor (linear sum)	–0.42	+0.1	–0.31	–0.39	<0.1
– light quarks (uds)	(+0.10)	(–0.1)	(–0.01)	(+0.06)	(–0.1)
– charm	(+0.02)	(<0.1)	(–0.01)	(+0.01)	(<0.1)
– bottom	(–0.32)	(<0.1)	(–0.31)	(–0.32)	(<0.1)
– gluon	(–0.22)	(+0.3)	(+0.02)	(–0.15)	(+0.2)
b jet modeling (quad. sum)	0.13	0.1	0.09	0.12	<0.1
– b frag. Bowler–Lund	(–0.07)	(+0.1)	(–0.01)	(–0.05)	(<0.1)
– b frag. Peterson	(+0.04)	(<0.1)	(+0.05)	(+0.04)	(<0.1)
– semileptonic B decays	(+0.11)	(<0.1)	(+0.08)	(+0.10)	(<0.1)
PDF	0.02	<0.1	0.02	0.02	<0.1
Ren. and fact. scales	0.02	0.1	0.02	0.01	<0.1
ME/PS matching	–0.08 ± 0.09	+0.1	+0.03 ± 0.05	–0.05 ± 0.07	+0.1
ME generator	+0.15 ± 0.23	+0.2	+0.32 ± 0.14	+0.20 ± 0.19	+0.1
ISR PS scale	+0.07 ± 0.09	+0.1	+0.10 ± 0.05	+0.06 ± 0.07	<0.1
FSR PS scale	+0.24 ± 0.06	–0.4	–0.22 ± 0.04	+0.13 ± 0.05	–0.3
Top quark $p_T$	+0.02	–0.1	–0.06	–0.01	–0.1
Underlying event	–0.10 ± 0.08	+0.1	+0.01 ± 0.05	–0.07 ± 0.07	+0.1
Early resonance decays	–0.22 ± 0.09	+0.8	+0.42 ± 0.05	–0.03 ± 0.07	+0.5
Color reconnection	+0.34 ± 0.09	–0.1	+0.23 ± 0.06	+0.31 ± 0.08	–0.1
<b>Total systematic</b>	<b>0.75</b>	<b>1.1</b>	<b>1.10</b>	<b>0.62</b>	<b>0.8</b>
Statistical (expected)	0.09	0.1	0.06	0.08	0.1
<b>Total (expected)</b>	<b>0.76</b>	<b>1.1</b>	<b>1.10</b>	<b>0.63</b>	<b>0.8</b>

# $\ell$ +jets channel: CMS 13 TeV

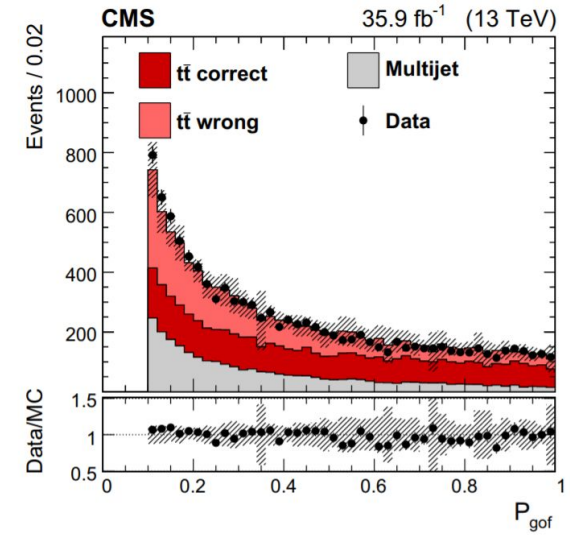
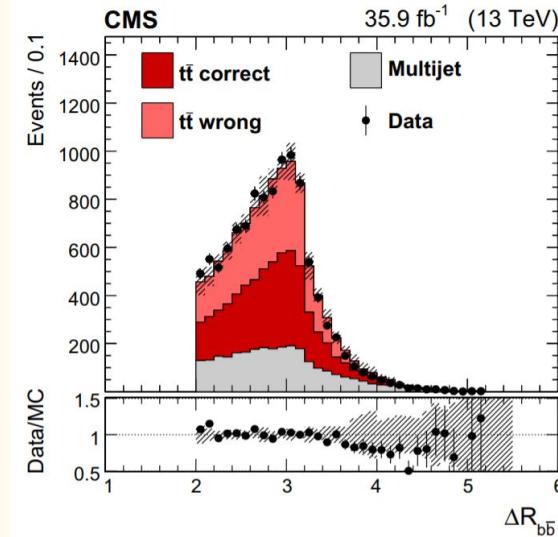
[Eur. Phys. J. C 78 \(2018\) 891](#)

# AllHad CMS 13 TeV: kinematic fit

$$\chi^2 = \sum_{j \in \text{jets}} \left[ \frac{(p_{Tj}^{\text{reco}} - p_{Tj}^{\text{fit}})^2}{\sigma_{p_{Tj}}^2} + \frac{(\eta_j^{\text{reco}} - \eta_j^{\text{fit}})^2}{\sigma_{\eta_j}^2} + \frac{(\phi_j^{\text{reco}} - \phi_j^{\text{fit}})^2}{\sigma_{\phi_j}^2} \right]$$

$$P_{\text{gof}} \equiv 1 - \text{erf} \left( \sqrt{\frac{\chi^2}{2}} \right) + \sqrt{\frac{2\chi^2}{\pi}} e^{-\chi^2/2}$$

- all parton-jets assignments tested
- only b-jets used as candidate for b-quarks
- equivalent choices not considered separately
- only permutation with best  $\chi^2$  kept
- $P_{\text{gof}} > 0.1$  required



# AllHad CMS 13 TeV: ideogram method

$$\mathcal{L}(m_t, \text{JSF}) = P(\text{sample}|m_t, \text{JSF})$$

$$= \prod_{\text{events}} P(\text{event}|m_t, \text{JSF})$$

$$= \prod_{\text{events}} P(m_t^{\text{fit}}, m_W^{\text{reco}}|m_t, \text{JSF})$$

multiplied by P(JSF) prior  
where appropriate

$$P(m_t^{\text{fit}}, m_W^{\text{reco}}|m_t, \text{JSF}) \quad j=\text{correct, wrong}$$

$$= f_{\text{sig}} P(m_t^{\text{fit}}, m_W^{\text{reco}}|m_t, \text{JSF})$$

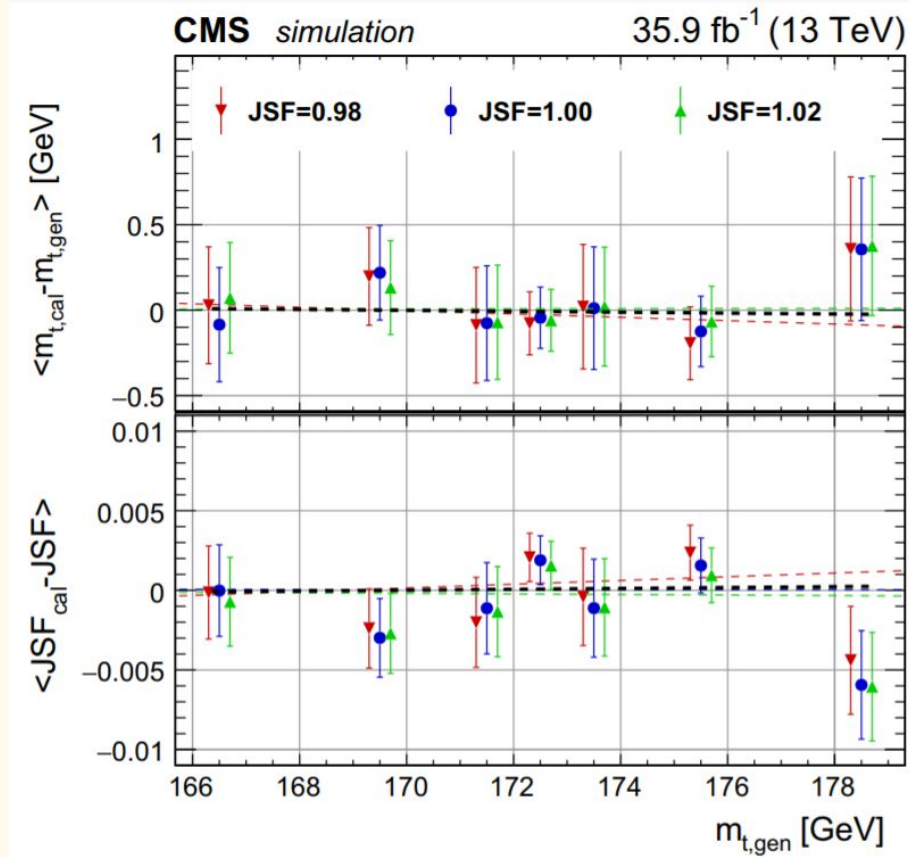
$$+ (1 - f_{\text{sig}}) P_{\text{bkg}}(m_t^{\text{fit}}, m_W^{\text{reco}})$$

$$= f_{\text{sig}} \sum_j f_j P_j(m_t^{\text{fit}}|m_t, \text{JSF}) P_j(m_W^{\text{reco}}|m_t, \text{JSF})$$

$$+ (1 - f_{\text{sig}}) P_{\text{bkg}}(m_t^{\text{fit}}) P_{\text{bkg}}(m_W^{\text{reco}}),$$

- signal PDF from analytic functions, parameters from simultaneous fit to samples with 7 different  $m_t$  and 5 different input JSF
- bkg shape from spline interpolation as a function of  $m_t^{\text{fit}}$  and  $m_W^{\text{reco}}$ , but independent from  $m_t$  and JSF
- signal fraction and correct perm. fraction are free parameters
- for hybrid method, width of gaussian prior on JSF optimised to minimize uncertainty

# AllHad CMS 13 TeV: ideogram method



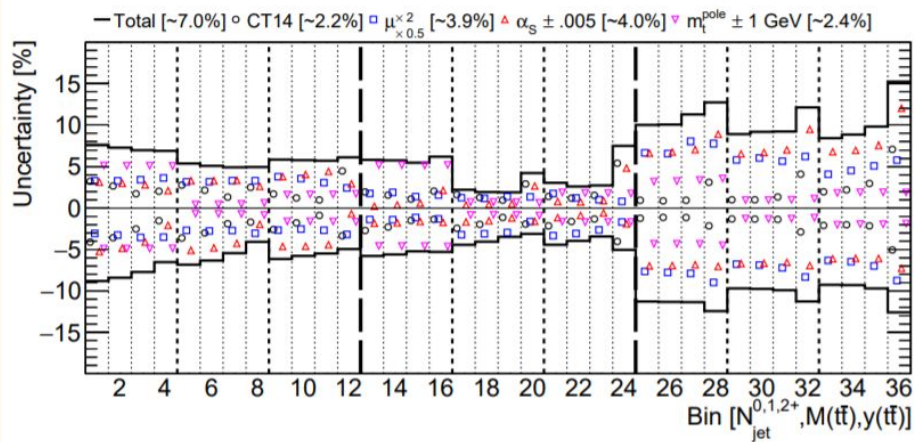
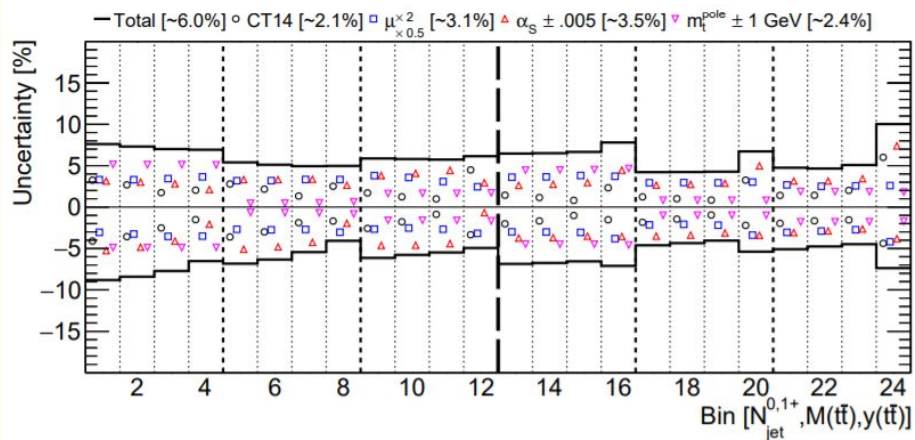
# AllHad CMS 13 TeV

	2D		1D	Hybrid	
	$\delta m_{\tau}^{2D}$ [GeV]	$\delta JSF^{2D}$ [%]	$\delta m_{\tau}^{1D}$ [GeV]	$\delta m_{\tau}^{hyb}$ [GeV]	$\delta JSF^{hyb}$ [%]
<i>Experimental uncertainties</i>					
Method calibration	0.06	0.2	0.06	0.06	0.2
JEC (quad. sum)	0.18	0.3	0.73	0.15	0.2
Intercalibration	-0.04	-0.1	+0.12	-0.04	-0.1
MPPInSitu	-0.03	0.0	+0.22	+0.08	+0.1
Uncorrelated	-0.17	-0.3	+0.69	+0.12	+0.2
Jet energy resolution	-0.09	+0.2	+0.09	-0.04	+0.1
b tagging	0.02	0.0	0.01	0.02	0.0
Pileup	-0.06	+0.1	0.00	-0.04	+0.1
Background	0.10	0.1	0.03	0.07	0.1
Trigger	+0.04	-0.1	-0.04	+0.02	-0.1
<i>Modeling uncertainties</i>					
JEC flavor (linear sum)	-0.35	+0.1	-0.31	-0.34	0.0
Light quarks (uds)	+0.10	-0.1	-0.01	+0.07	-0.1
Charm	+0.03	0.0	-0.01	+0.02	0.0
Bottom	-0.29	0.0	-0.29	-0.29	0.0
Gluon	-0.19	+0.2	+0.03	-0.13	+0.2
b jet modeling (quad. sum)	0.09	0.0	0.09	0.09	0.0
b frag. Bowler-Lund	-0.07	0.0	-0.07	-0.07	0.0
b frag. Peterson	-0.05	0.0	-0.04	-0.05	0.0
Semileptonic b hadron decays	-0.03	0.0	-0.03	-0.03	0.0
PDF	0.01	0.0	0.01	0.01	0.0
Ren. and fact. scales	0.05	0.0	0.04	0.04	0.0
ME/PS matching	+0.32 ± 0.20	-0.3	-0.05 ± 0.14	+0.24 ± 0.18	-0.2
ISR PS scale	+0.17 ± 0.17	-0.2	+0.13 ± 0.12	+0.12 ± 0.14	-0.1
FSR PS scale	+0.22 ± 0.12	-0.2	+0.11 ± 0.08	+0.18 ± 0.11	-0.1
Top quark $p_T$	+0.03	0.0	+0.02	+0.03	0.0
Underlying event	+0.16 ± 0.19	-0.3	-0.07 ± 0.14	+0.10 ± 0.17	-0.2
Early resonance decays	+0.02 ± 0.28	+0.4	+0.38 ± 0.19	+0.13 ± 0.24	+0.3
CR modeling (max. shift)	+0.41 ± 0.29	-0.4	-0.43 ± 0.20	-0.36 ± 0.25	-0.3
"gluon move" (ERD on)	+0.41 ± 0.29	-0.4	+0.10 ± 0.20	+0.32 ± 0.25	-0.3
"QCD inspired" (ERD on)	-0.32 ± 0.29	-0.1	-0.43 ± 0.20	-0.36 ± 0.25	-0.1
Total systematic	0.81	0.9	1.03	0.70	0.7
Statistical (expected)	0.21	0.2	0.16	0.20	0.1
Total (expected)	0.83	0.9	1.04	0.72	0.7

# AllHad/l+jets CMS 13 TeV

	$\delta m_{\tau}^{\text{hyb}}$ [GeV]		
	All-jets	$\ell$ +jets	Combination
<i>Experimental uncertainties</i>			
Method calibration	0.06	0.05	0.03
JEC (quad. sum)	0.15	0.18	0.17
Intercalibration	-0.04	+0.04	+0.04
MPFInSitu	+0.08	+0.07	+0.07
Uncorrelated	+0.12	+0.16	+0.15
Jet energy resolution	-0.04	-0.12	-0.10
b tagging	0.02	0.03	0.02
Pileup	-0.04	-0.05	-0.05
All-jets background	0.07	-	0.01
All-jets trigger	+0.02	-	+0.01
$\ell$ +jets background	-	+0.02	-0.01
<i>Modeling uncertainties</i>			
JEC flavor (linear sum)	-0.34	-0.39	-0.37
light quarks (uds)	+0.07	+0.06	+0.07
charm	+0.02	+0.01	+0.02
bottom	-0.29	-0.32	-0.31
gluon	-0.13	-0.15	-0.15
b jet modeling (quad. sum)	0.09	0.12	0.06
b frag. Bowler-Lund	-0.07	-0.05	-0.05
b frag. Peterson	-0.05	+0.04	-0.02
semileptonic b hadron decays	-0.03	+0.10	-0.04
PDF	0.01	0.02	0.01
Ren. and fact. scales	0.04	0.01	0.01
ME/PS matching	+0.24	-0.07	+0.07
ME generator	-	+0.20	+0.21
ISR PS scale	+0.14	+0.07	+0.07
FSR PS scale	+0.18	+0.13	+0.12
Top quark $p_T$	+0.03	-0.01	-0.01
Underlying event	+0.17	-0.07	-0.06
Early resonance decays	+0.24	-0.07	-0.07
CR modeling (max. shift)	-0.36	+0.31	+0.33
"gluon move" (ERD on)	+0.32	+0.31	+0.33
"QCD inspired" (ERD on)	-0.36	-0.13	-0.14
Total systematic	0.70	0.62	0.61
Statistical (expected)	0.20	0.08	0.07
Total (expected)	0.72	0.63	0.61

# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV



# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV

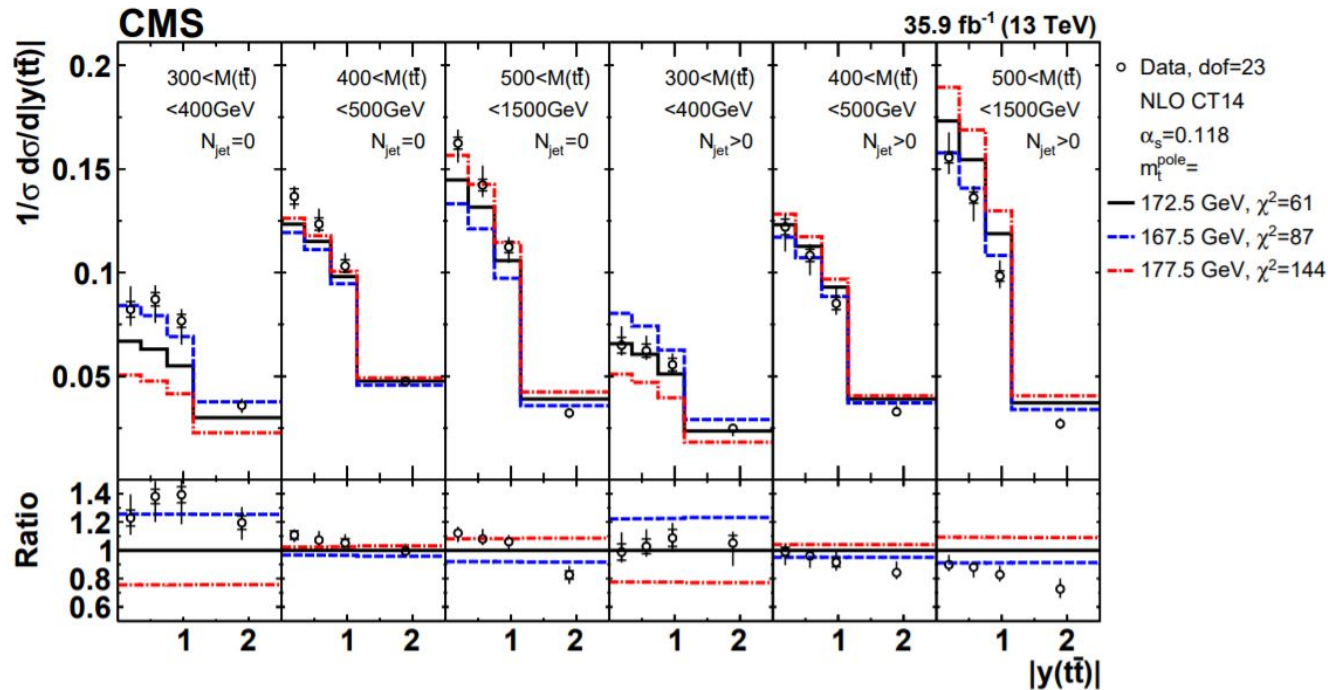


Figure 16: Comparison of the measured  $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$  cross sections to NLO predictions obtained using different  $m_t^{\text{pole}}$  values (further details can be found in Fig. 3). For each theoretical prediction, values of  $\chi^2$  and dof for the comparison to the data are reported.

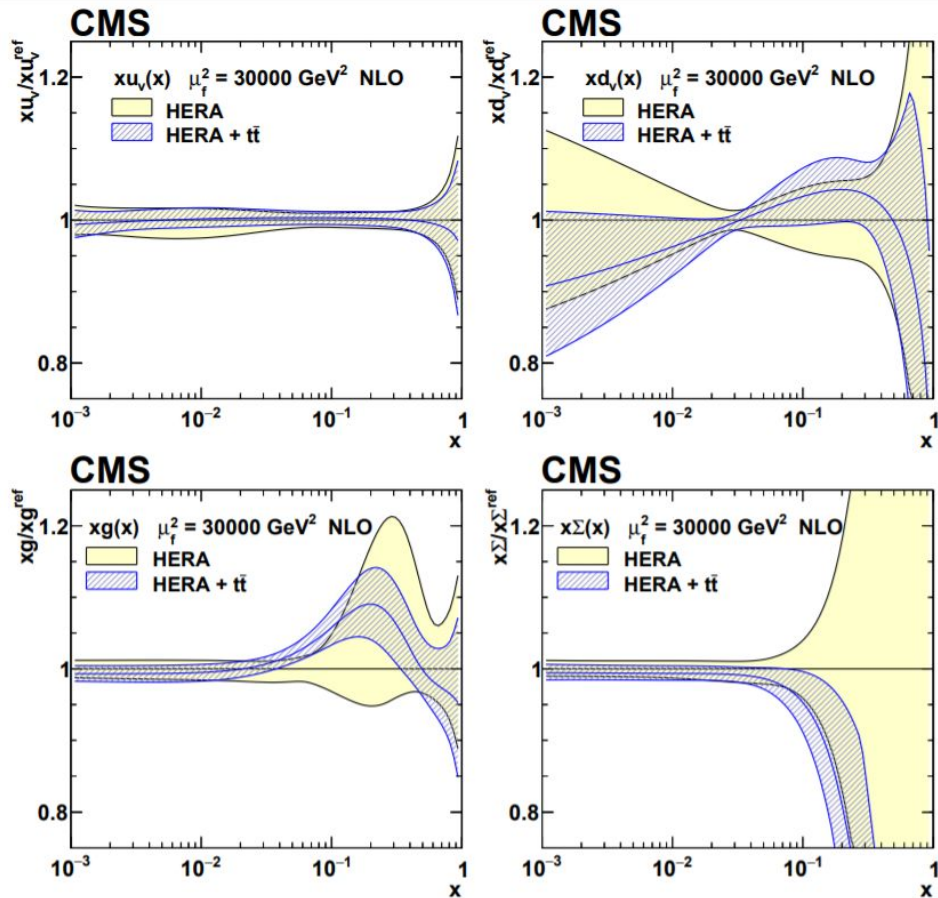


# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV

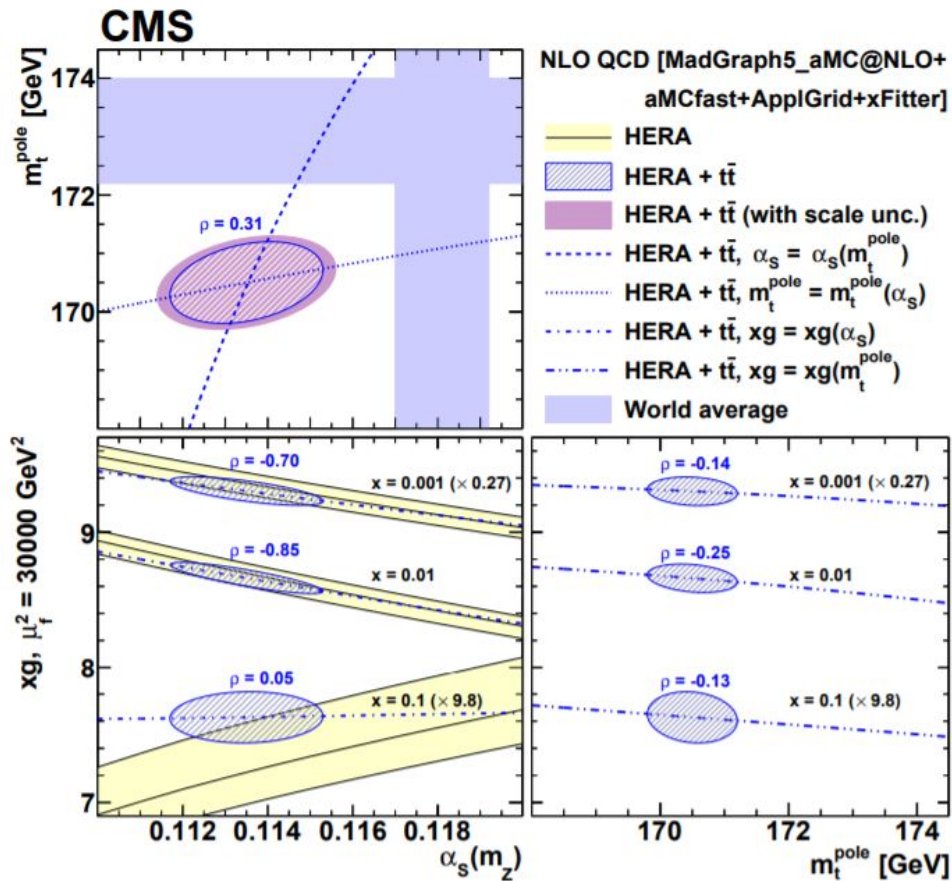
Table 2: The individual contributions to the uncertainties for the  $\alpha_S(m_Z)$  and  $m_t^{\text{pole}}$  determination.

Parameter	Variation	$\alpha_S(m_Z)$	$m_t^{\text{pole}}$ [GeV]
Fit uncertainty			
Total	$\Delta\chi^2 = 1$	$\pm 0.0016$	$\pm 0.7$
Model uncertainty			
$f_s$	$f_s = 0.5$	+0.0001	0.0
$f_s$	$f_s = 0.3$	0.0000	0.0
$Q_{\text{min}}^2$	$Q_{\text{min}}^2 = 5.0 \text{ GeV}^2$	+0.0002	+0.1
$Q_{\text{min}}^2$	$Q_{\text{min}}^2 = 2.5 \text{ GeV}^2$	-0.0004	-0.1
$M_c$	$M_c = 1.49 \text{ GeV}$	+0.0001	0.0
$M_c$	$M_c = 1.37 \text{ GeV}$	0.0000	0.0
Total		+0.0002 -0.0004	+0.1 -0.1
PDF parametrisation uncertainty			
$\mu_{f,0}^2$	$\mu_{f,0}^2 = 2.2 \text{ GeV}^2$	-0.0001	0.0
$\mu_{f,0}^2$	$\mu_{f,0}^2 = 1.6 \text{ GeV}^2$	+0.0002	0.0
$A'_g$	set to 0	+0.0002	-0.1
$E_g$	set to 0	+0.0008	0.0
Total		+0.0008 -0.0001	-0.1
Scale uncertainty			
$\mu_r$ variation	$\mu_r = H$	+0.0004	-0.2
$\mu_r$ variation	$\mu_r = H/4$	+0.0007	+0.1
$\mu_f$ variation	$\mu_f = H$	-0.0002	+0.3
$\mu_f$ variation	$\mu_f = H/4$	+0.0001	-0.3
$\mu_{r,f}$ variation	$\mu_{r,f} = H$	+0.0004	+0.1
$\mu_{r,f}$ variation	$\mu_{r,f} = H/4$	+0.0011	-0.2
alternative $\mu_{r,f}$	$\mu_{r,f} = H/2$	-0.0005	+0.1
Total		+0.0011 -0.0005	+0.3 -0.3

# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV



# Indirect: $m_t^{\text{pole}}$ in dilepton events, CMS 13 TeV



[arXiv:1904.05237](https://arxiv.org/abs/1904.05237)

# Indirect: $m_t^{\text{pole}}$ in $t\bar{t}+1$ jet, ATLAS 8 TeV

[arXiv:1905.02302](https://arxiv.org/abs/1905.02302)

Mass scheme	$m_t^{\text{pole}}$ [GeV]	$m_t(m_t)$ [GeV]
<b>Value</b>	<b>171.1</b>	<b>162.9</b>
<b>Statistical uncertainty</b>	<b>0.4</b>	<b>0.5</b>
<i>Simulation uncertainties</i>		
Shower and hadronisation	0.4	0.3
Colour reconnection	0.4	0.4
Underlying event	0.3	0.2
Signal Monte Carlo generator	0.2	0.2
Proton PDF	0.2	0.2
Initial- and final-state radiation	0.2	0.2
Monte Carlo statistics	0.2	0.2
Background	<0.1	<0.1
<i>Detector response uncertainties</i>		
Jet energy scale (including $b$ -jets)	0.4	0.4
Jet energy resolution	0.2	0.2
Missing transverse momentum	0.1	0.1
$b$ -tagging efficiency and mistag	0.1	0.1
Jet reconstruction efficiency	<0.1	<0.1
Lepton	<0.1	<0.1
<i>Method uncertainties</i>		
Unfolding modelling	0.2	0.2
Fit parameterisation	0.2	0.2
<b>Total experimental systematic</b>	<b>0.9</b>	<b>1.0</b>
Scale variations	(+0.6, -0.2)	(+2.1, -1.2)
Theory PDF $\oplus\alpha_s$	0.2	0.4
<b>Total theory uncertainty</b>	<b>(+0.7, -0.3)</b>	<b>(+2.1, -1.2)</b>
<b>Total uncertainty</b>	<b>(+1.2, -1.1)</b>	<b>(+2.3, -1.6)</b>

$$\chi^2 = \sum_{i,j} \left[ \mathcal{R}_{\text{data}}^{t\bar{t}+1\text{-jet}} - \mathcal{R}_{\text{NLO+PS}}^{t\bar{t}+1\text{-jet}}(m_t^{\text{pole}}) \right]_i [V^{-1}]_{ij} \left[ \mathcal{R}_{\text{data}}^{t\bar{t}+1\text{-jet}} - \mathcal{R}_{\text{NLO+PS}}^{t\bar{t}+1\text{-jet}}(m_t^{\text{pole}}) \right]_j$$

$i,j=\text{bins}$

# Direct/Indirect: CMS dilepton 13 Tev

Source	Uncertainty (%)
Trigger	0.4
Lepton ident./isolation	2.2
Muon momentum scale	0.2
Electron momentum scale	0.2
Jet energy scale	0.7
Jet energy resolution	0.5
b tagging	0.3
Pileup	0.3
$t\bar{t}$ ME scale	0.5
$tW$ ME scale	0.7
DY ME scale	0.2
NLO generator	1.2
PDF	1.1
$m_t^{\text{MC}}$	0.4
Top quark $p_T$	0.5
ME/PS matching	0.2
UE tune	0.3
$t\bar{t}$ ISR scale	0.4
$tW$ ISR scale	0.4
$t\bar{t}$ FSR scale	1.1
$tW$ FSR scale	0.2
b quark fragmentation	1.0
b hadron BF	0.2
Colour reconnection	0.4
DY background	0.8
$tW$ background	1.1
Diboson background	0.3
W+jets background	0.3
$t\bar{t}$ background	0.2
Statistical	0.2
Integrated luminosity	2.5
MC statistical	1.2
Total $\sigma_{t\bar{t}}^{\text{th}}$ uncertainty	4.2
Extrapolation uncertainties	
$t\bar{t}$ ME scale	$\mp_{-0.1}^{0.4}$
PDF	$\pm_{0.6}^{0.8}$
Top quark $p_T$	$\pm_{0.3}^{0.2}$
$t\bar{t}$ ISR scale	$\mp_{-0.1}^{0.2}$
$t\bar{t}$ FSR scale	$\pm_{0.1}^{0.1}$
UE tune	$<0.1$
$m_t^{\text{MC}}$	$\mp_{0.3}^{0.2}$
Total $\sigma_{t\bar{t}}$ uncertainty	$+4.3$ $-4.2$

Source	Uncertainty (GeV)
Trigger	0.02
Lepton ident./isolation	0.02
Muon momentum scale	0.03
Electron momentum scale	0.10
Jet energy scale	0.57
Jet energy resolution	0.09
b tagging	0.12
Pileup	0.09
$t\bar{t}$ ME scale	0.18
$tW$ ME scale	0.02
DY ME scale	0.06
NLO generator	0.14
PDF	0.05
$\sigma_{t\bar{t}}$	0.09
Top quark $p_T$	0.04
ME/PS matching	0.16
UE tune	0.03
$t\bar{t}$ ISR scale	0.16
$tW$ ISR scale	0.02
$t\bar{t}$ FSR scale	0.07
$tW$ FSR scale	0.02
b quark fragmentation	0.11
b hadron BF	0.07
Colour reconnection	0.17
DY background	0.24
$tW$ background	0.13
Diboson background	0.02
W+jets background	0.04
$t\bar{t}$ background	0.02
Statistical	0.14
MC statistical	0.36
Total $m_t^{\text{MC}}$ uncertainty	$+0.68$ $-0.73$

**Table 6** Values of  $m_t(m_t)$  obtained from the comparison of the  $\sigma_{t\bar{t}}$  measurement with the NNLO predictions using different PDF sets. The first uncertainty shown comes from the experimental, PDF, and  $\alpha_S(m_Z)$  uncertainties, and the second from the variation in the renormalization and factorization scales

PDF set	$m_t(m_t)$ (GeV)
ABMP16	$161.6 \pm 1.6$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
NNPDF3.1	$164.5 \pm 1.6$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
CT14	$165.0 \pm 1.8$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
MMHT14	$164.9 \pm 1.8$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.1}$ (scale)

**Table 7** Values of  $m_t^{\text{pole}}$  obtained by comparing the  $\sigma_{t\bar{t}}$  measurement with predictions at NNLO+NNLL using different PDF sets

PDF set	$m_t^{\text{pole}}$ (GeV)
ABMP16	$169.9 \pm 1.8$ (fit + PDF + $\alpha_S$ ) $^{+0.8}_{-1.2}$ (scale)
NNPDF3.1	$173.2 \pm 1.9$ (fit + PDF + $\alpha_S$ ) $^{+0.9}_{-1.3}$ (scale)
CT14	$173.7 \pm 2.0$ (fit + PDF + $\alpha_S$ ) $^{+0.9}_{-1.4}$ (scale)
MMHT14	$173.6 \pm 1.9$ (fit + PDF + $\alpha_S$ ) $^{+0.9}_{-1.4}$ (scale)