

# **Early-Universe Simulations of the Cosmological Axion**

**Malte Buschmann  
University of Michigan**

**7/15/2019  
CERN**

**arXiv:1906.00967**

**MB, Joshua W Foster, Benjamin R Safdi**



**National Energy Research  
Scientific Computing Center**

# Post- vs Pre-inflationary scenario

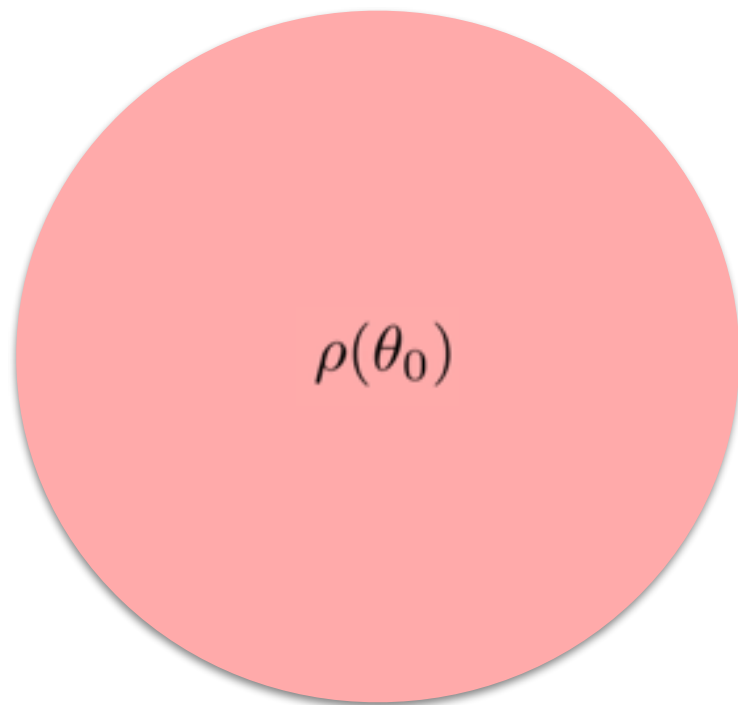
Two different scenarios can be considered:  
Breaking the PQ symmetry **before** or **after** inflation



# Post- vs Pre-inflationary scenario

Two different scenarios can be considered:  
Breaking the PQ symmetry **before** or **after** inflation

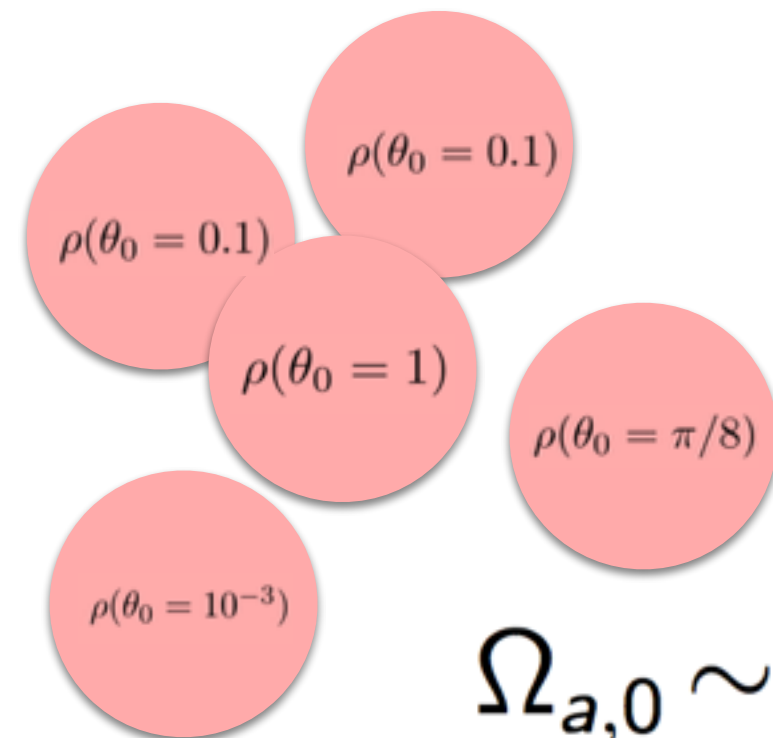
**before inflation:**



$$\Omega_{a,0} \sim \theta_0^2$$

two free parameters:  
 $\theta_0$  ,  $f_a$

**after inflation:**



$$\Omega_{a,0} \sim \langle \theta_0^2 \rangle$$

one free parameter:  $f_a$   
inhomogeneous at small scales

# Post- vs Pre-inflationary scenario

Two different scenarios can be considered:  
Breaking the PQ symmetry **before** or **after** inflation

## Focus of this discussion!

### Main goals:

1. Obtain **axion mass** with which correct relic abundance is reached
2. Characterise **inhomogeneities**

**after inflation:**

$$\rho(\theta_0 = 0.1)$$

$$\rho(\theta_0 = 0.1)$$

$$\rho(\theta_0 = 1)$$

$$\rho(\theta_0 = \pi/8)$$

$$\rho(\theta_0 = 10^{-3})$$

$$\Omega_{a,0} \sim \langle \theta_0^2 \rangle$$

one free parameter:  $f_a$   
inhomogeneous at small scales



time (not to scale)

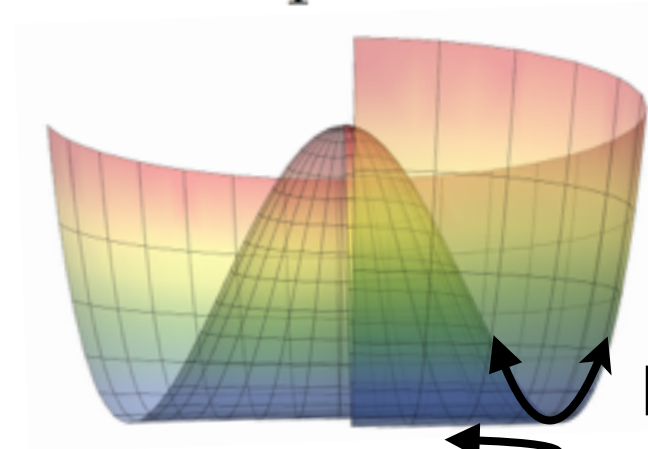
Inflation

simulation

PQ transition

@  $T \approx f_a$

$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2$$



radial mode  
axion

time (not to scale)

simulation

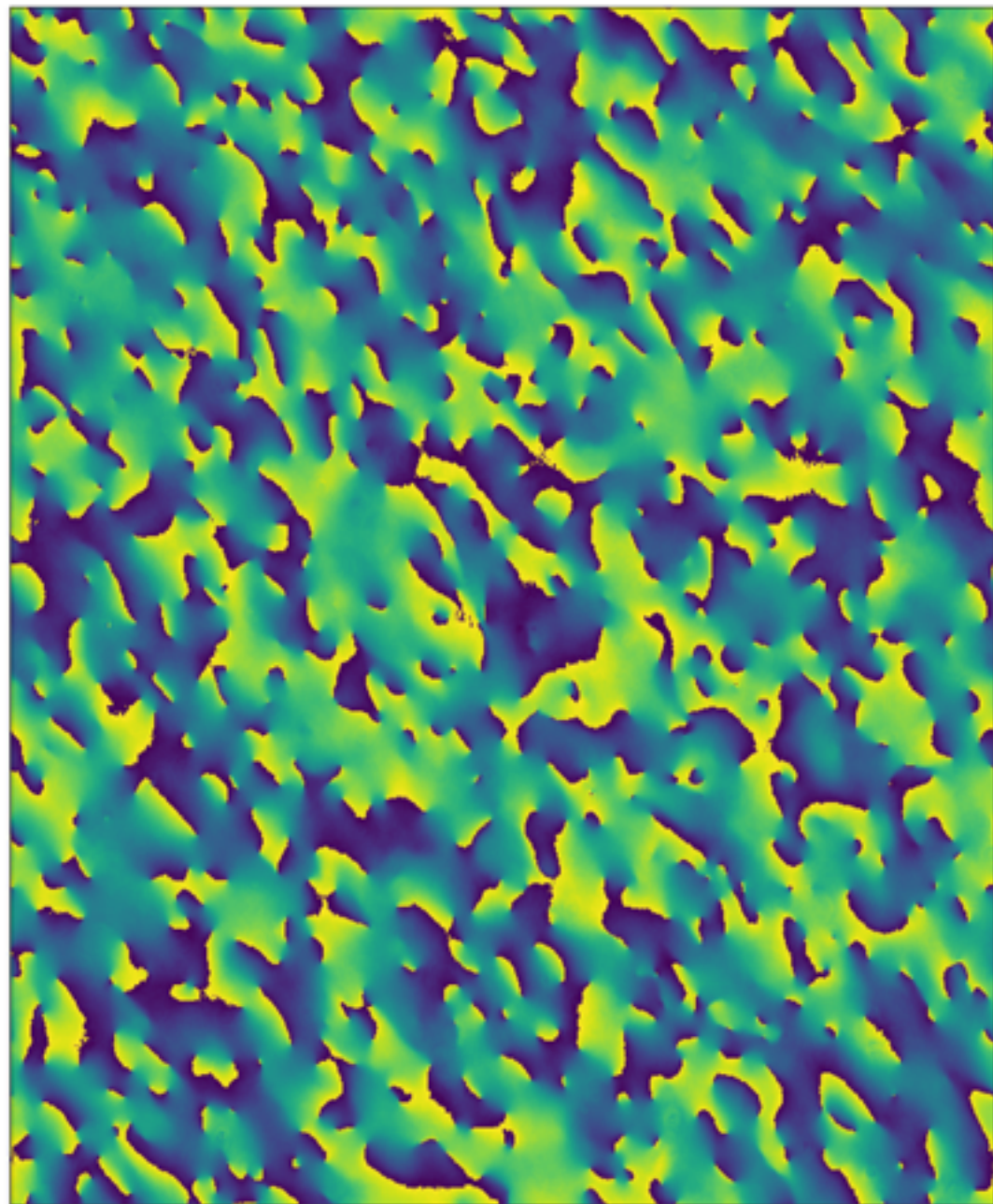
Inflation

thermal spec.

PQ transition

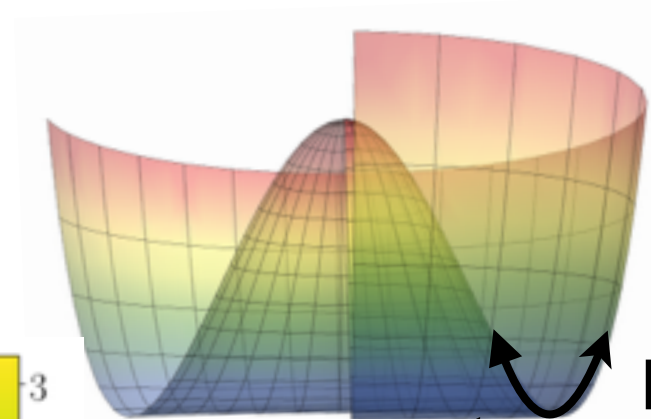
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radial @ vev



MB, Foster, Safdi (1906:00967)

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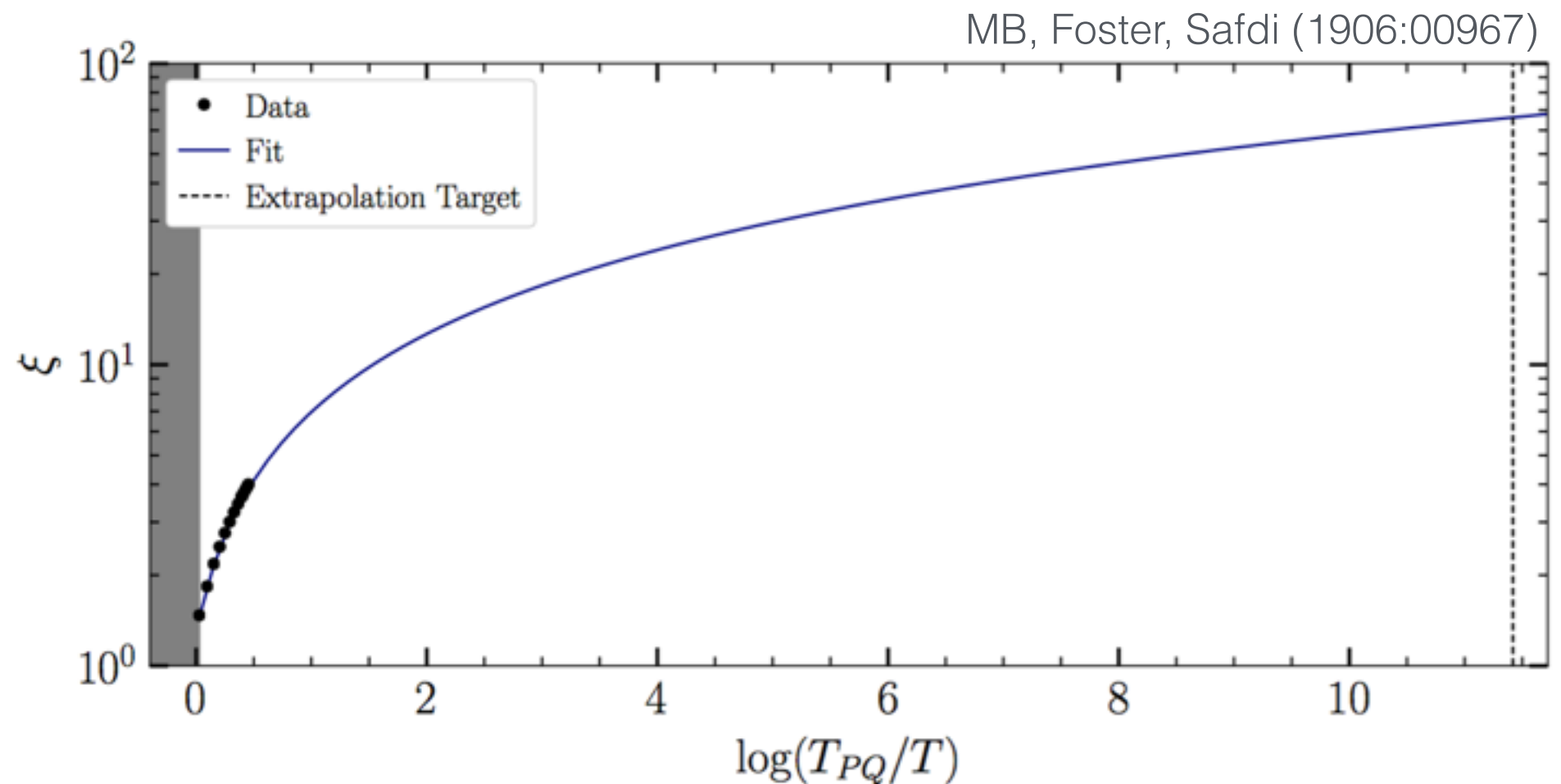
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scaling regime?



**Scaling regime:** 1 string per Hubble volume

We see logarithmic deviations from this assumption similar to *M. Gorghetto & G. Villadoro 2018!*

**More on this later!**

Inflation

thermal spec.

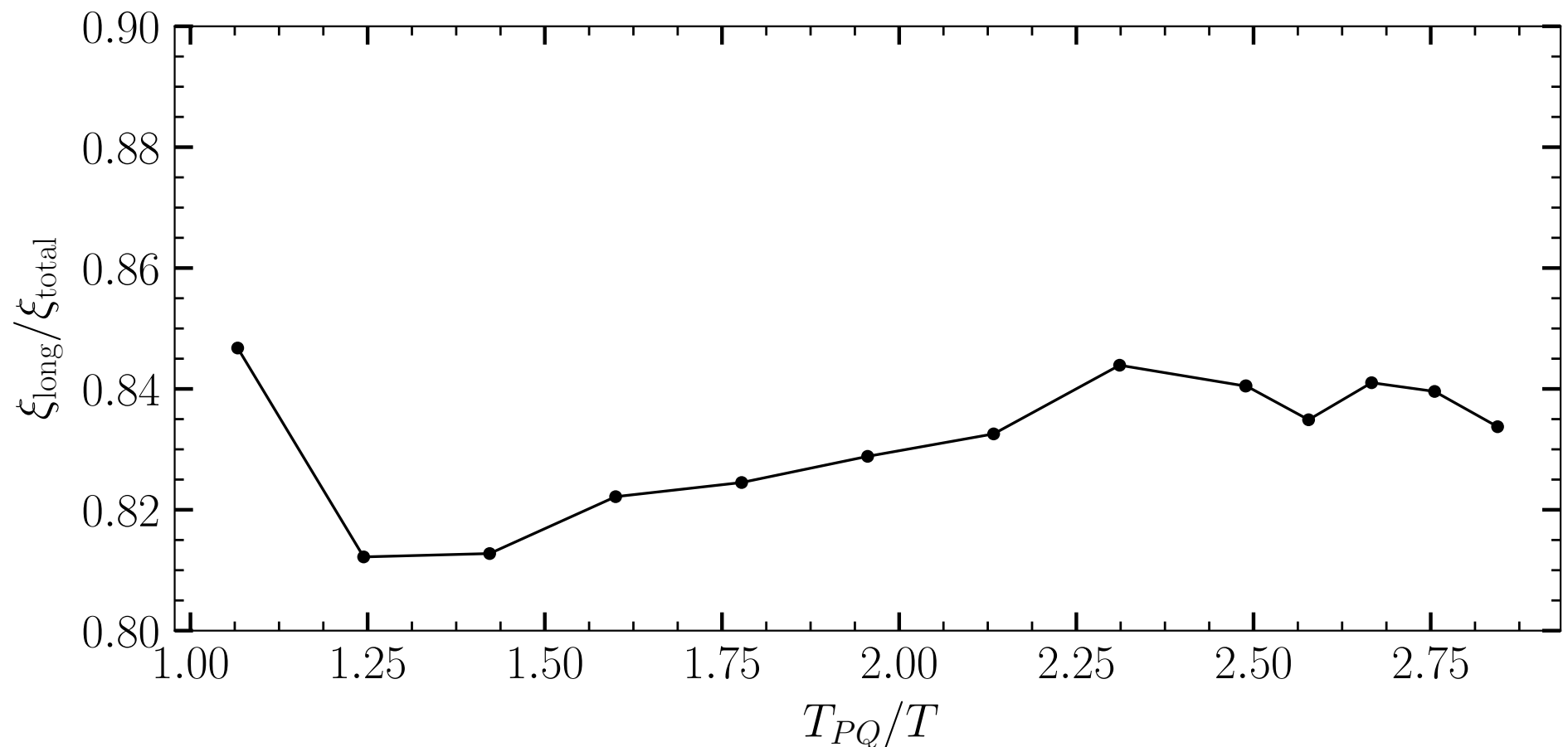
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analytic

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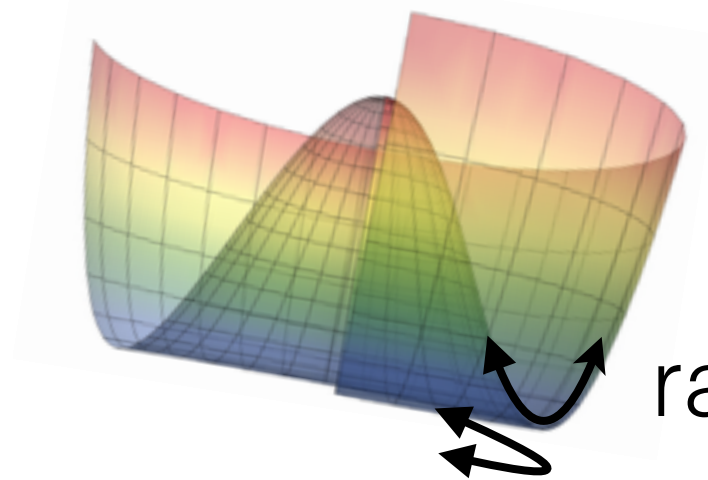
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scaling regime?

QCD transition

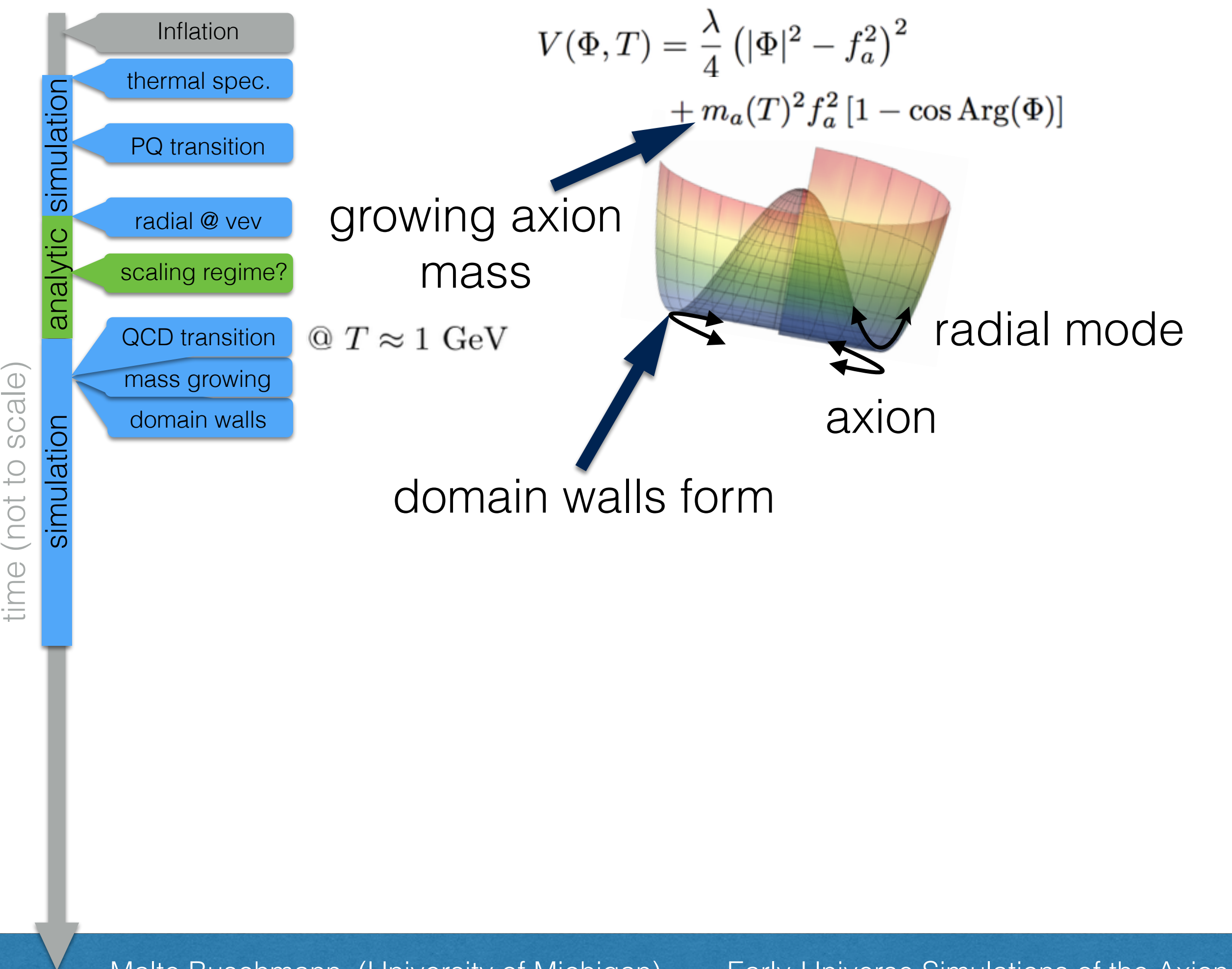
@  $T \approx 1$  GeV

$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2 + m_a(T)^2 f_a^2 [1 - \cos \text{Arg}(\Phi)]$$



radial mode

axion





time (not to scale)

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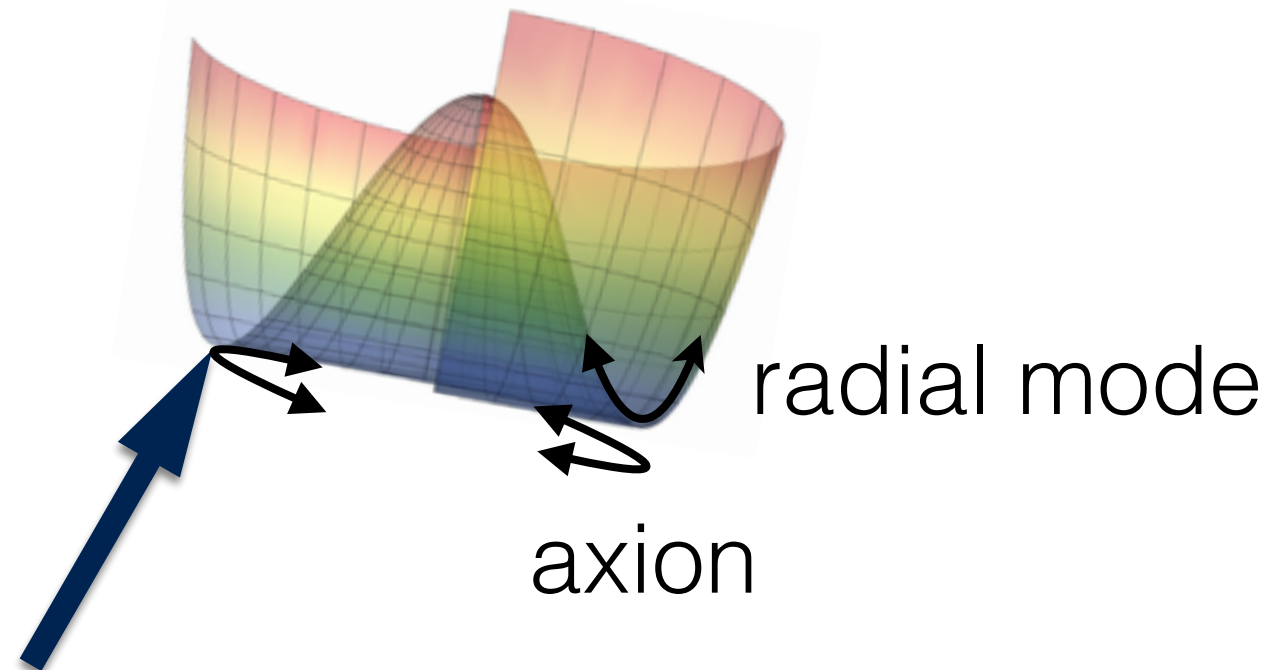
mass growing

domain walls

network collapse

@  $T \approx 1 \text{ GeV}$

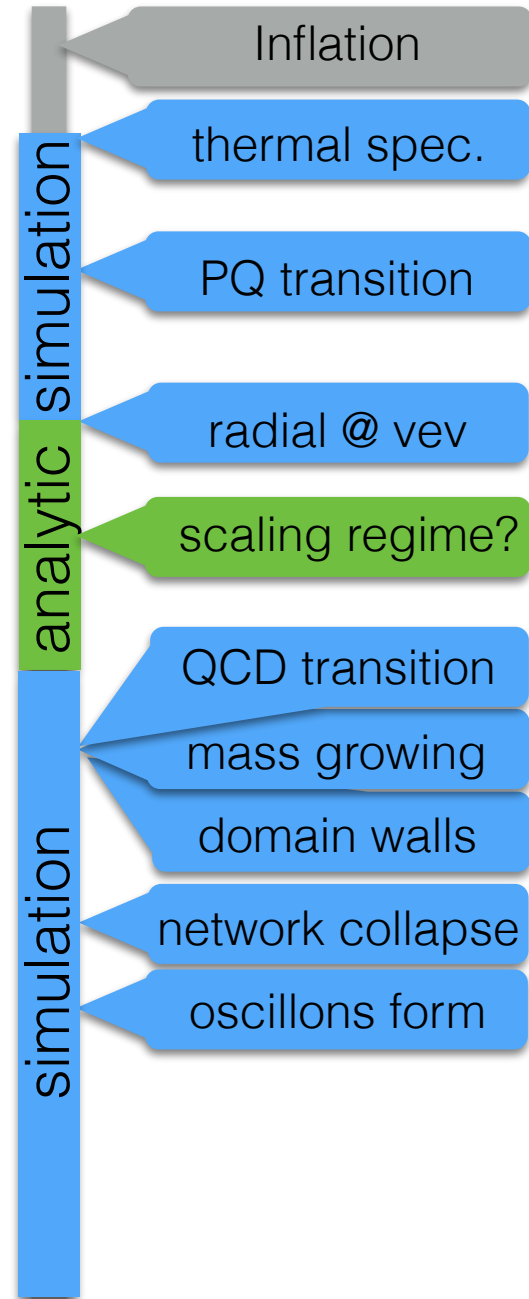
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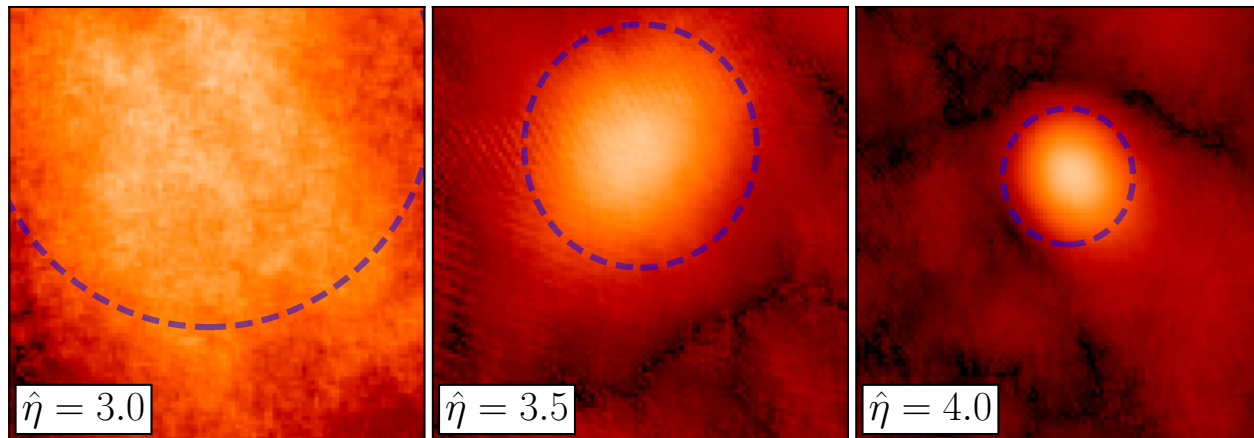
tension in domain walls  
causes string-domain wall network  
to collapse

# Evolution of Oscillons

time (not to scale)



MB, Foster, Safdi (1906:00967)



## Facts about Oscillons:

1. They are regions with large field values/large energy density
2. Their size is given by the axion wavelength  $\sim$  inverse  $m_a(T)$
3. They remain stable as long as  $m_a(T)$  is increasing
4. Start to dilute once the axion reaches its zero-temperature mass



# Evolution of Oscillons

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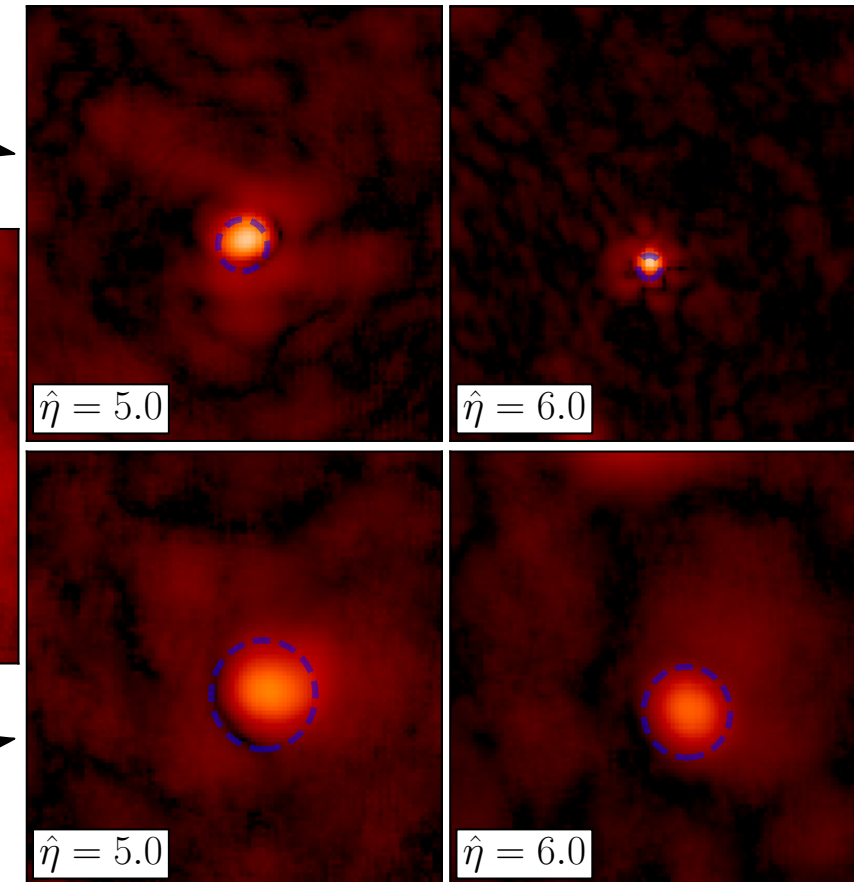
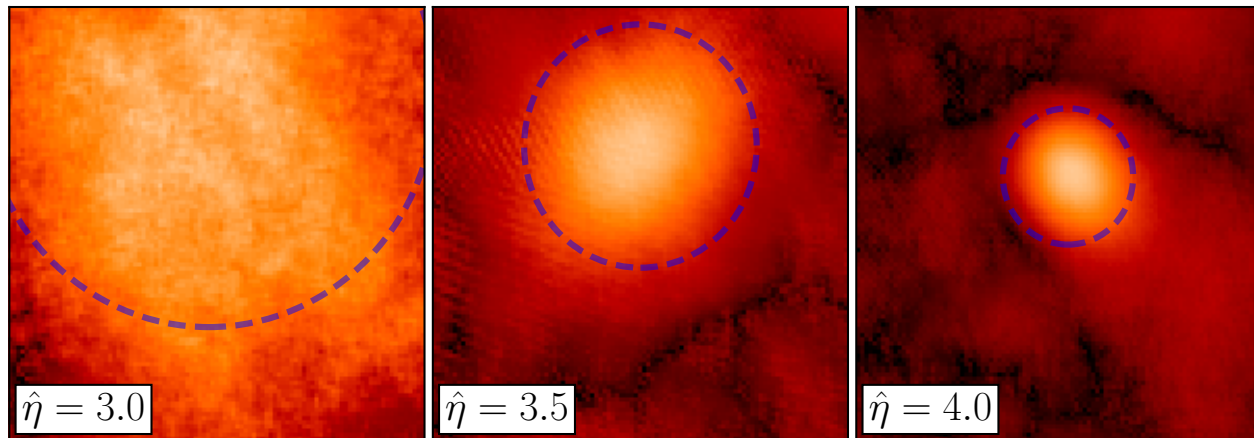
network collapse

oscillons form

mass constant

oscillons decay

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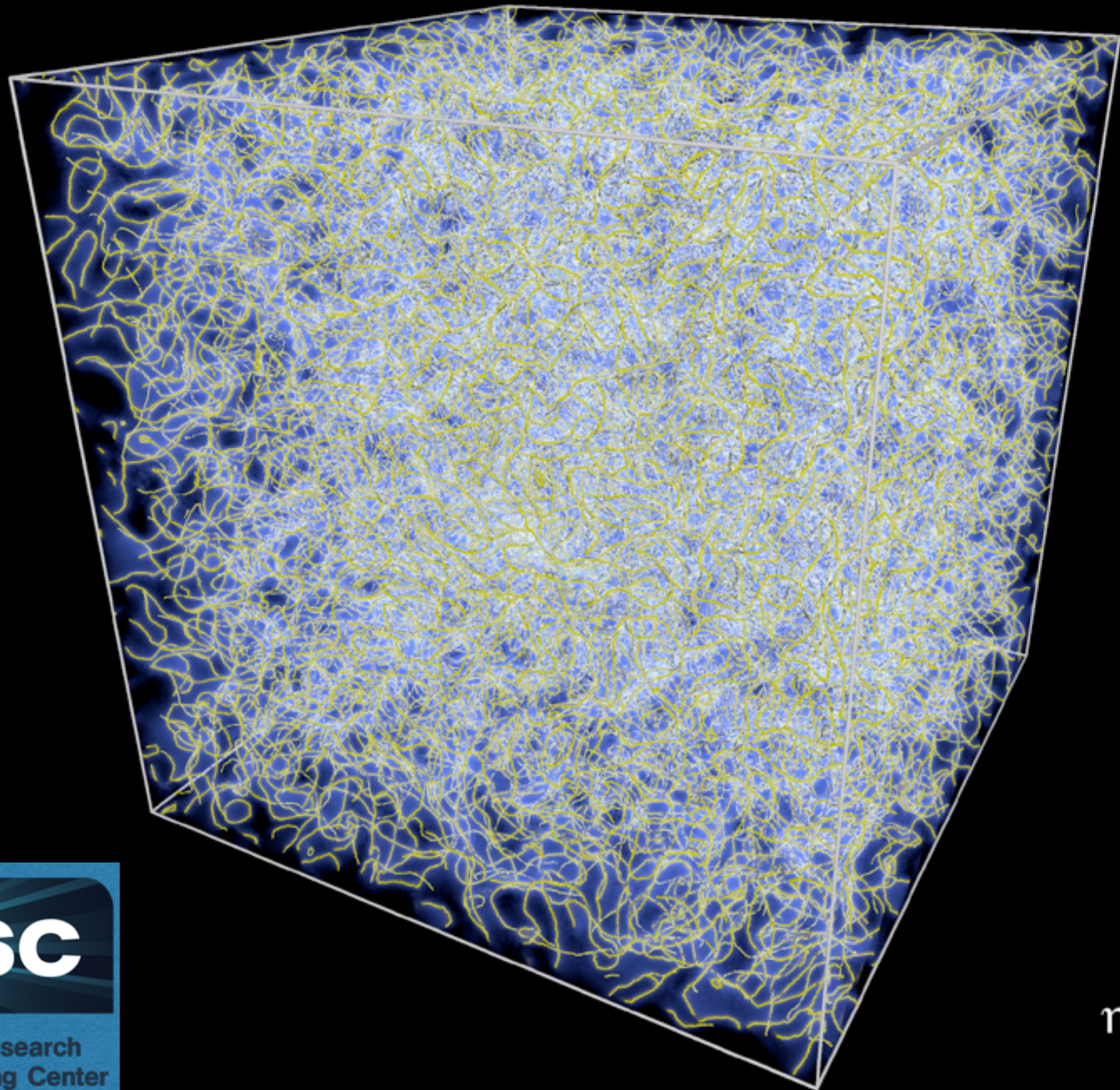
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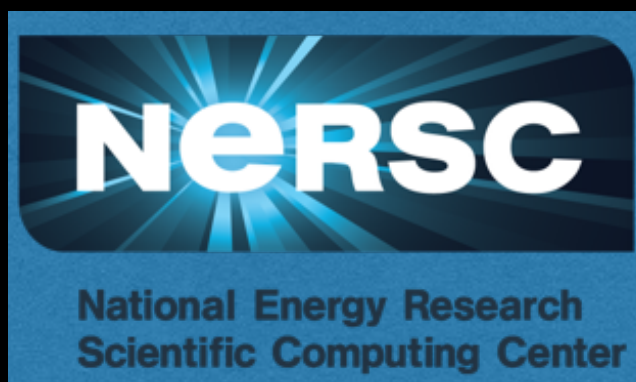
mass constant

oscillons decay

field linear

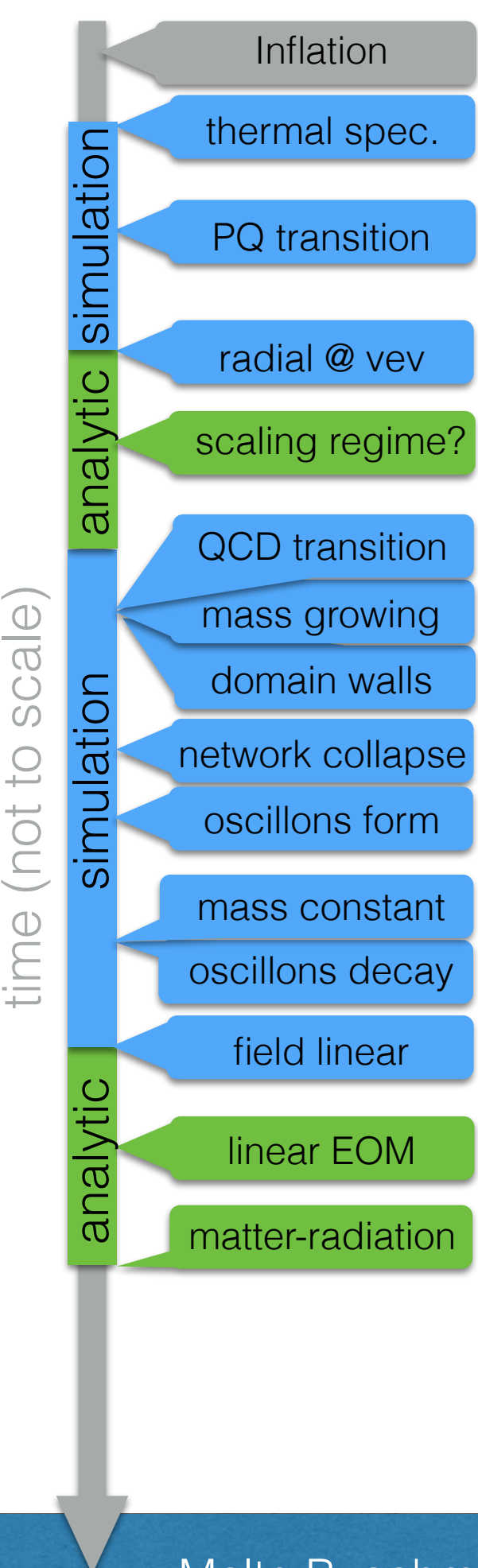


$\eta=0.40$



<https://youtu.be/1By1DMq1Epl>

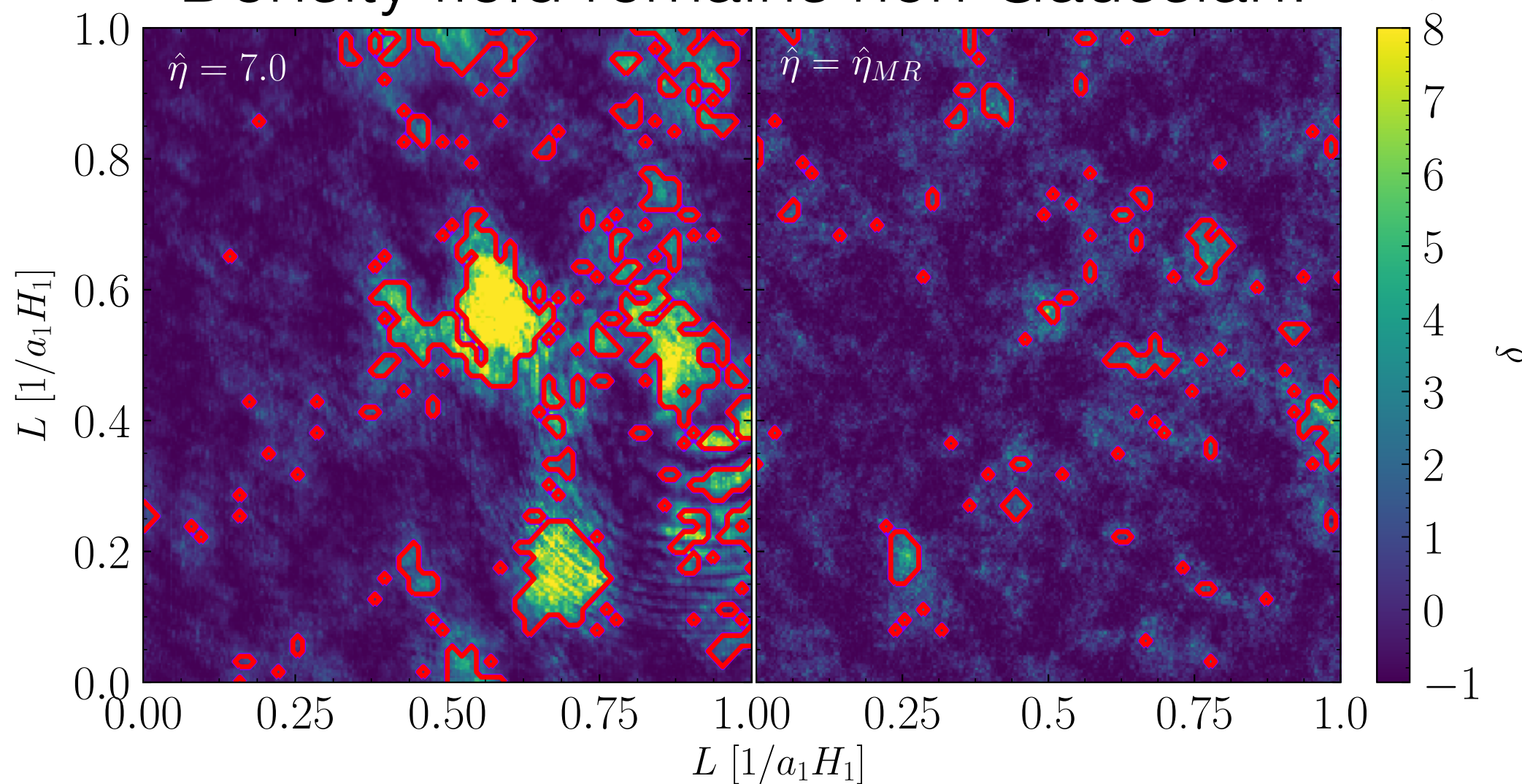




## After the simulation ends:

1. Analytic evolution to matter-radiation equality
2. Identify over-dense regions  $\delta = (\rho - \bar{\rho})/\rho$

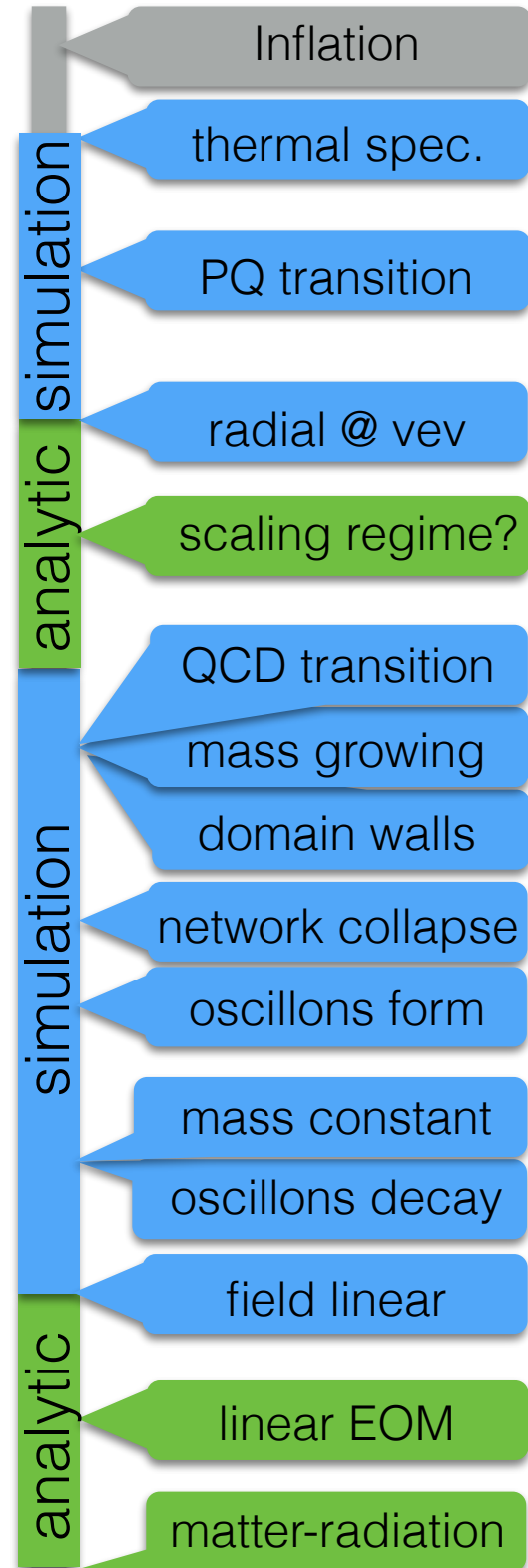
Density field remains non-Gaussian!



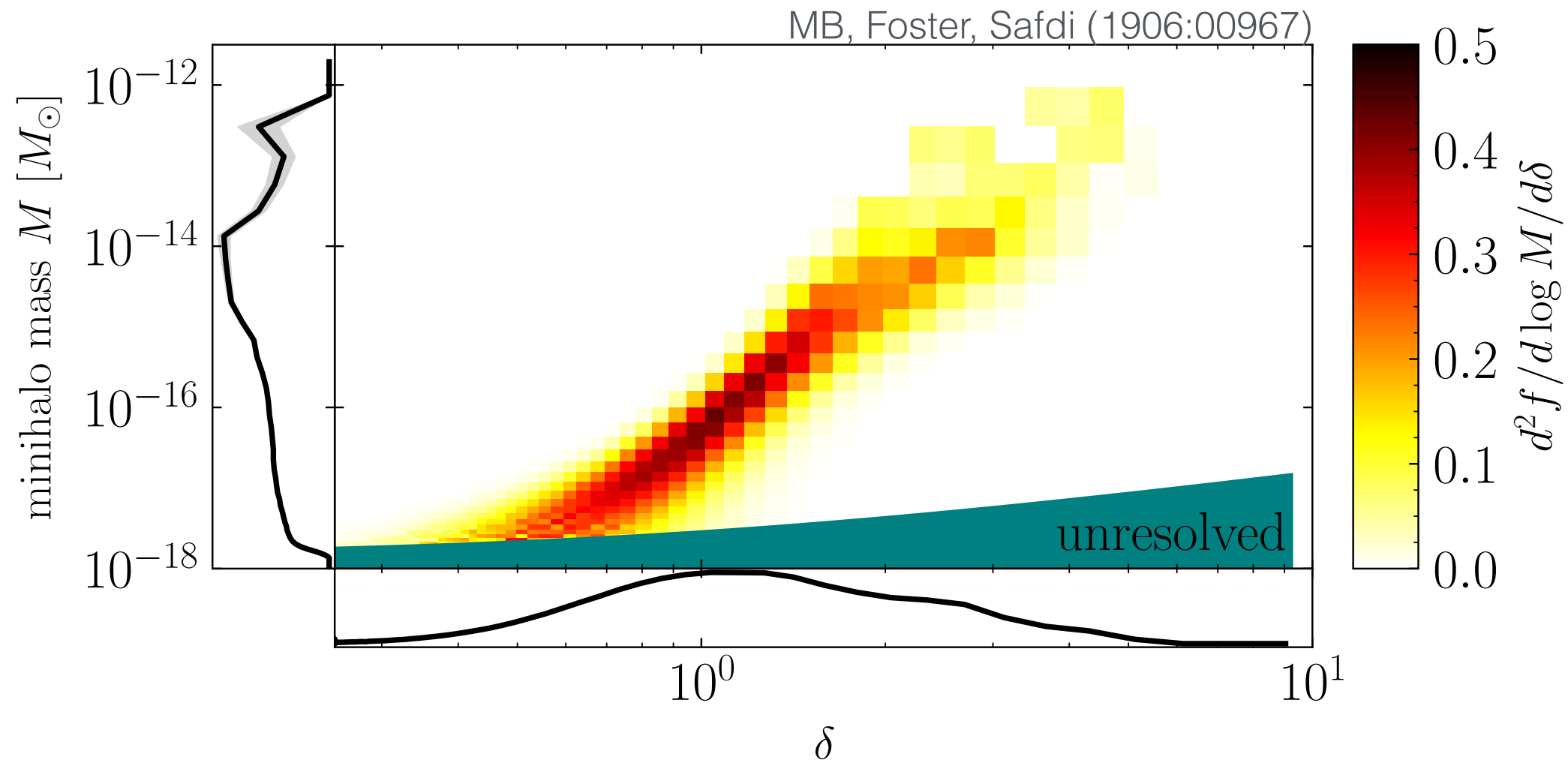
Assign each over-density a mass and a concentration parameter  $\delta$



time (not to scale)



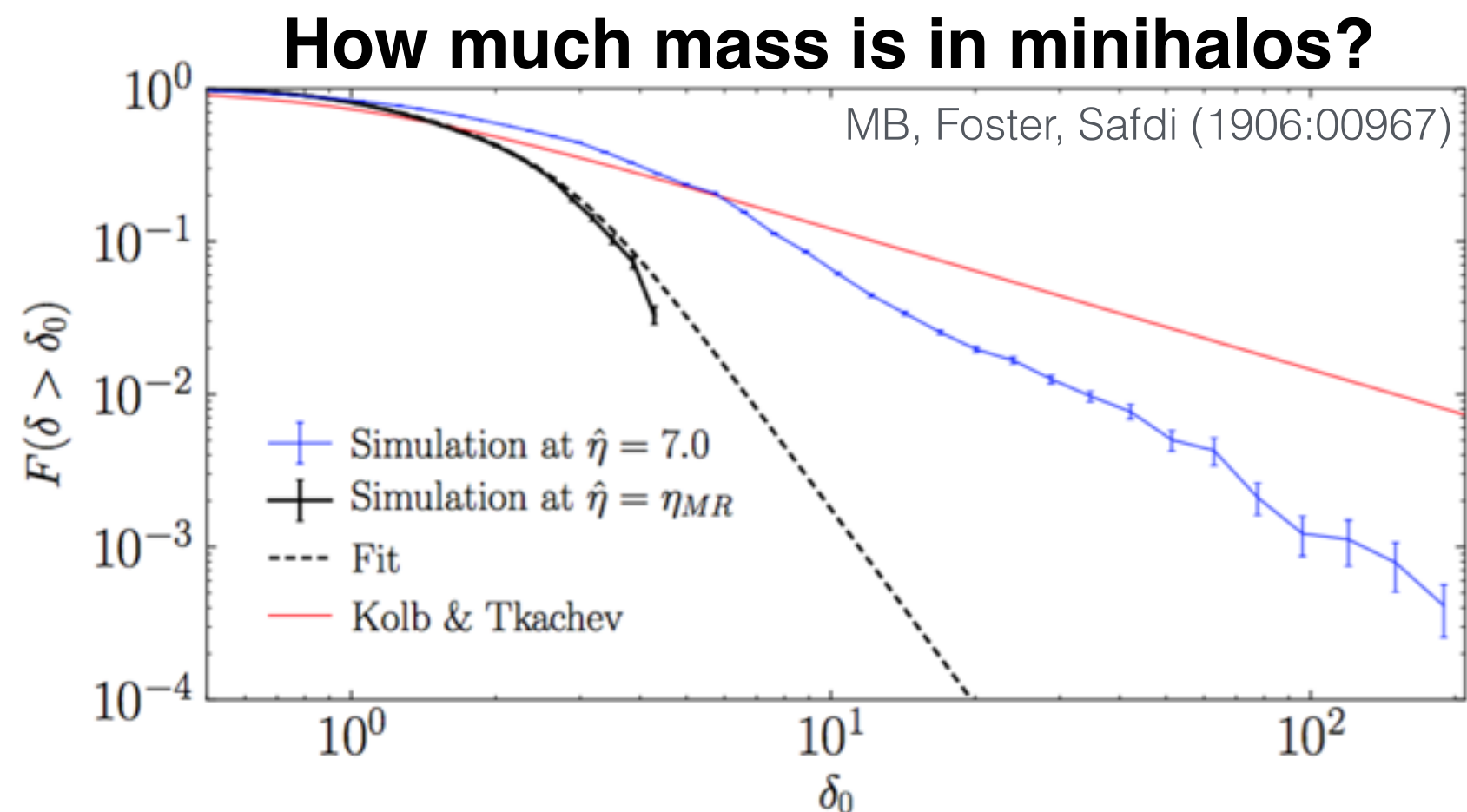
# Characterising the minihalo spectrum



**Typical minihalo mass:**  $10^{-14}$  solar masses

Important information for:  
microlensing, pulsar timing surveys, (in)direct detection, ...

# Characterising the minihalo spectrum



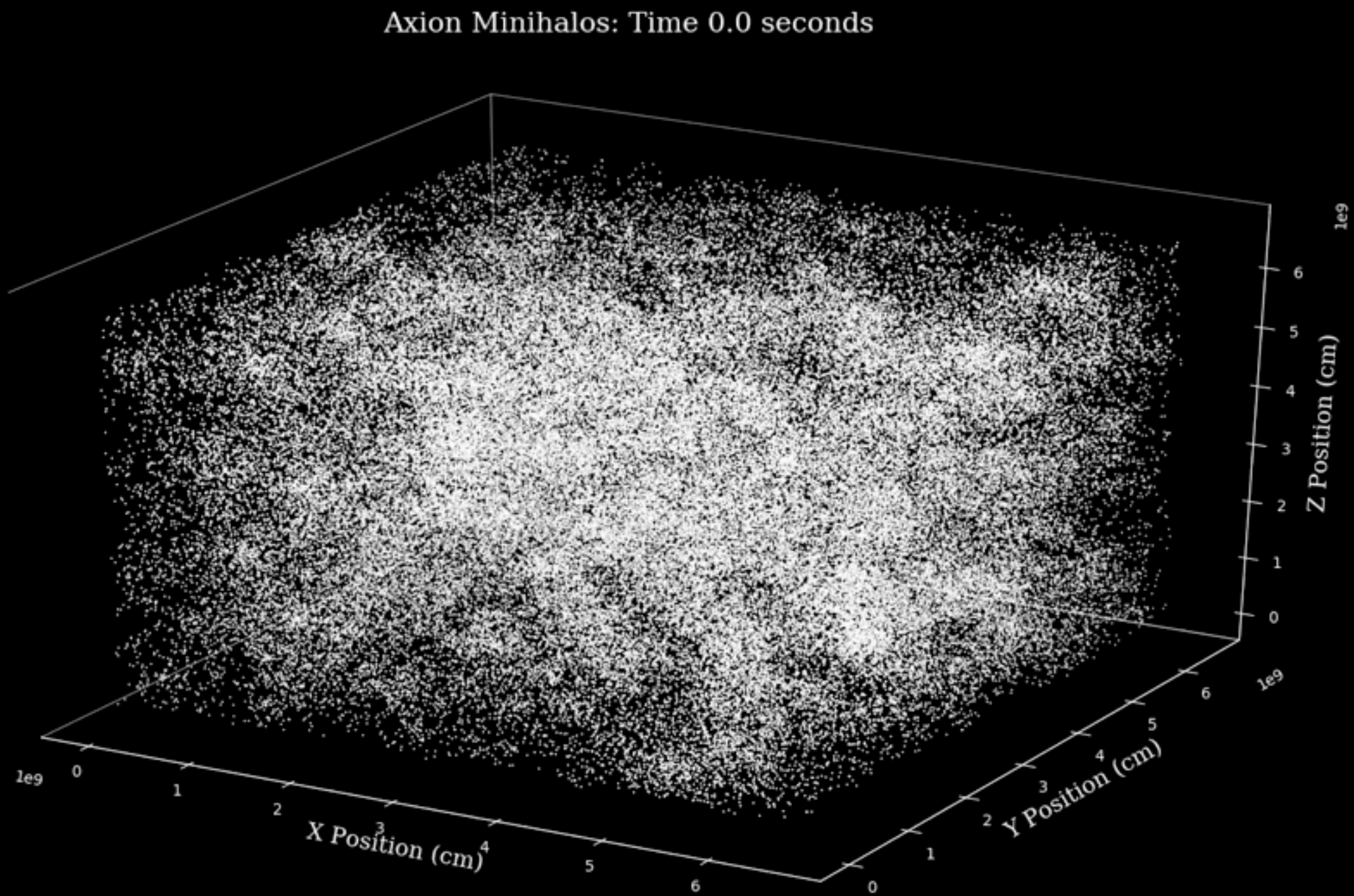
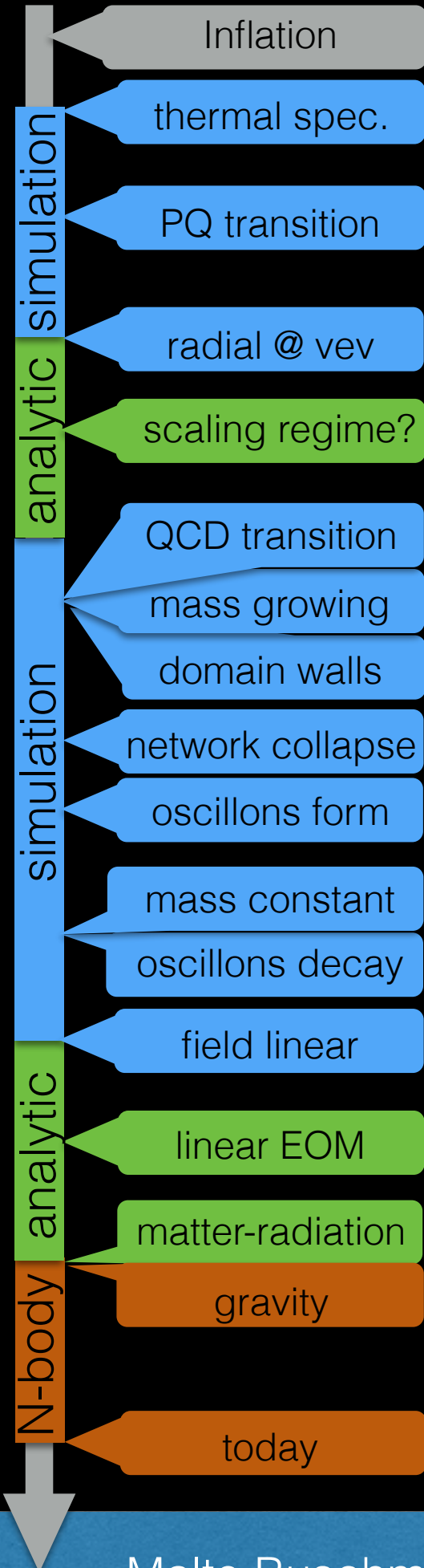
**Kolb & Tkachev in 1994:** 100 x 100 x 100 grid  
According to Moore's law that corresponds to a  
1800 x 1800 x 1800 grid in 2018

**This work:** 2048 x 2048 x 2048 grid

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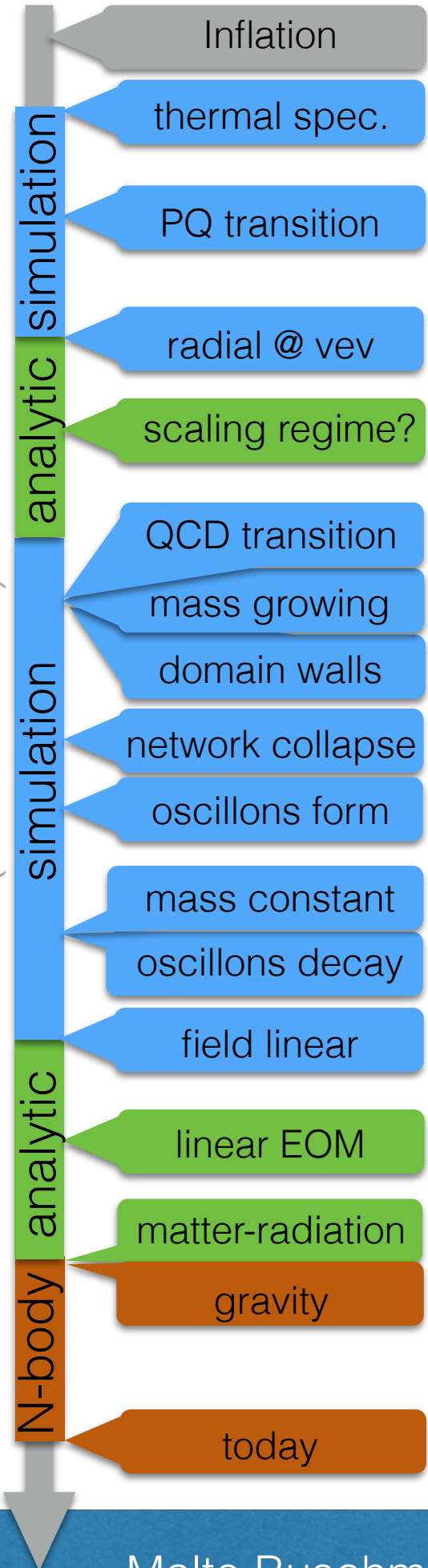
time (not to scale)



MB, Foster, Safdi, Wentzel (work in progress!)

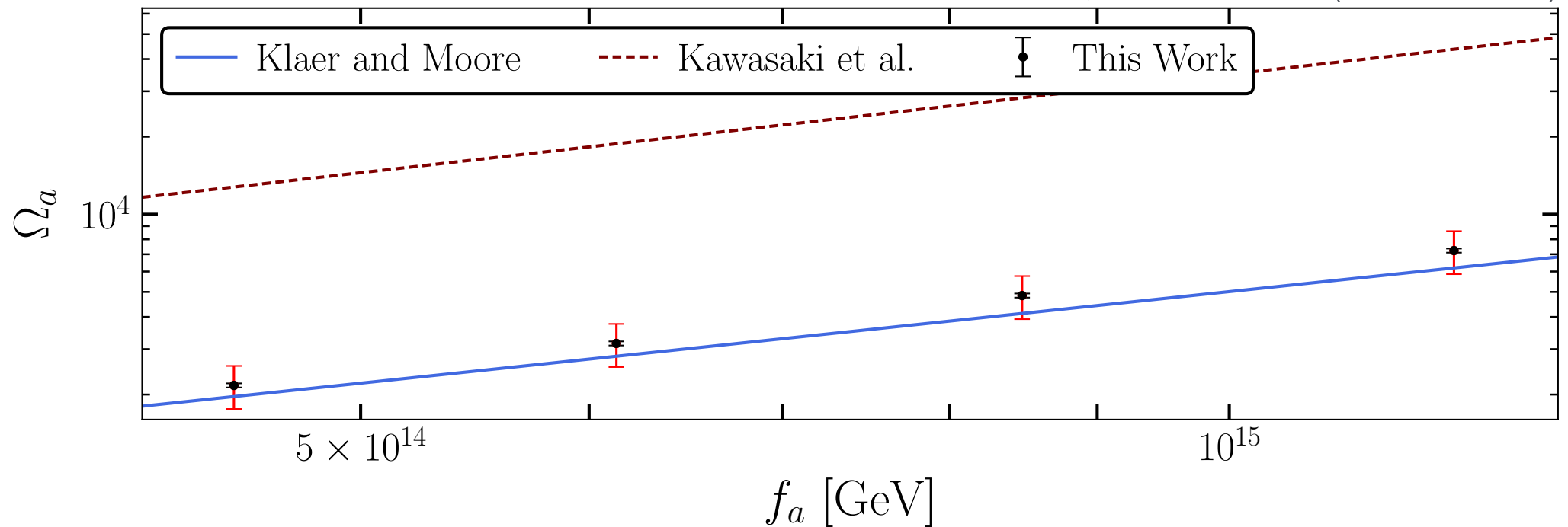


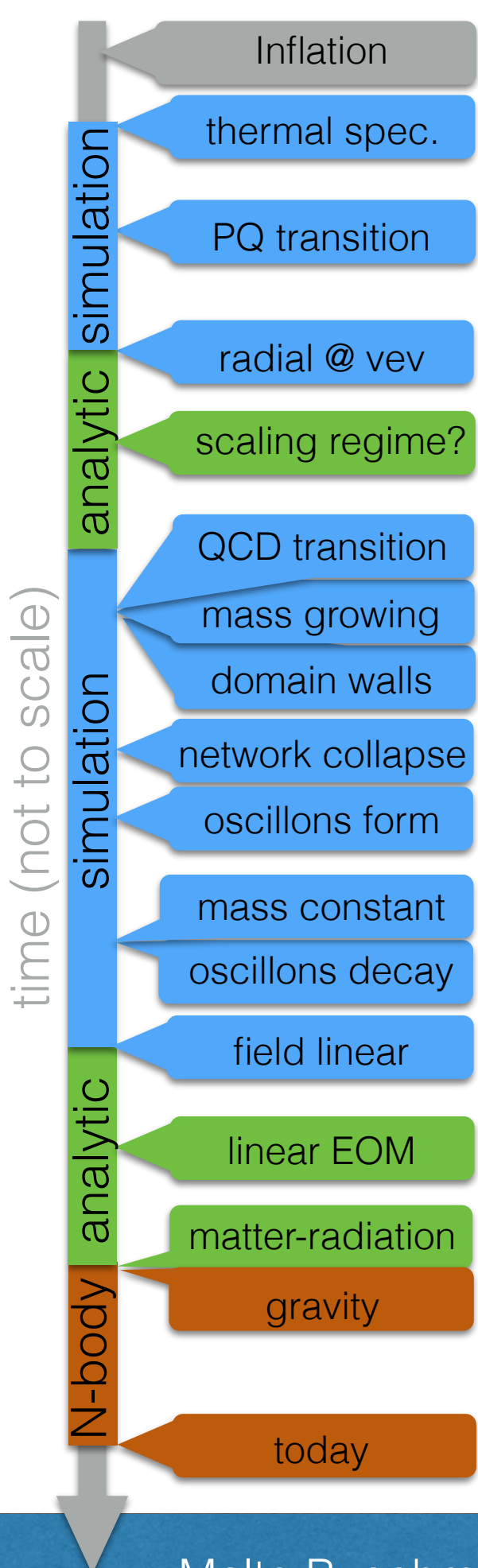
time (not to scale)



# Obtaining the relic abundance

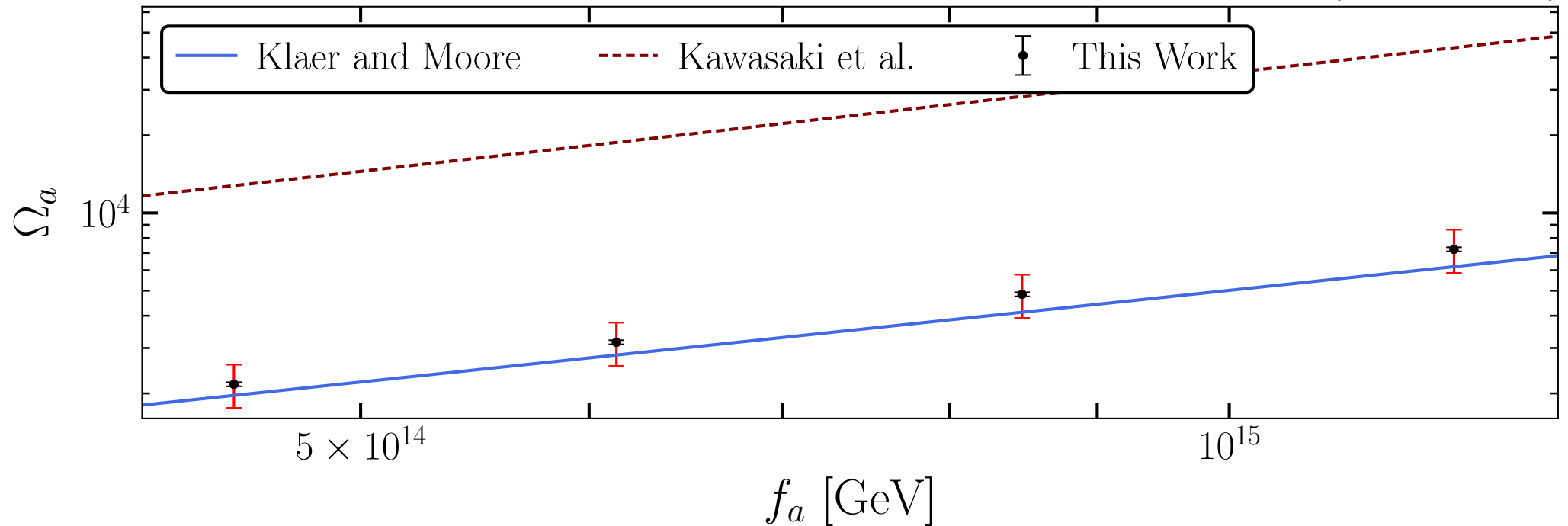
MB, Foster, Safdi (1906:00967)





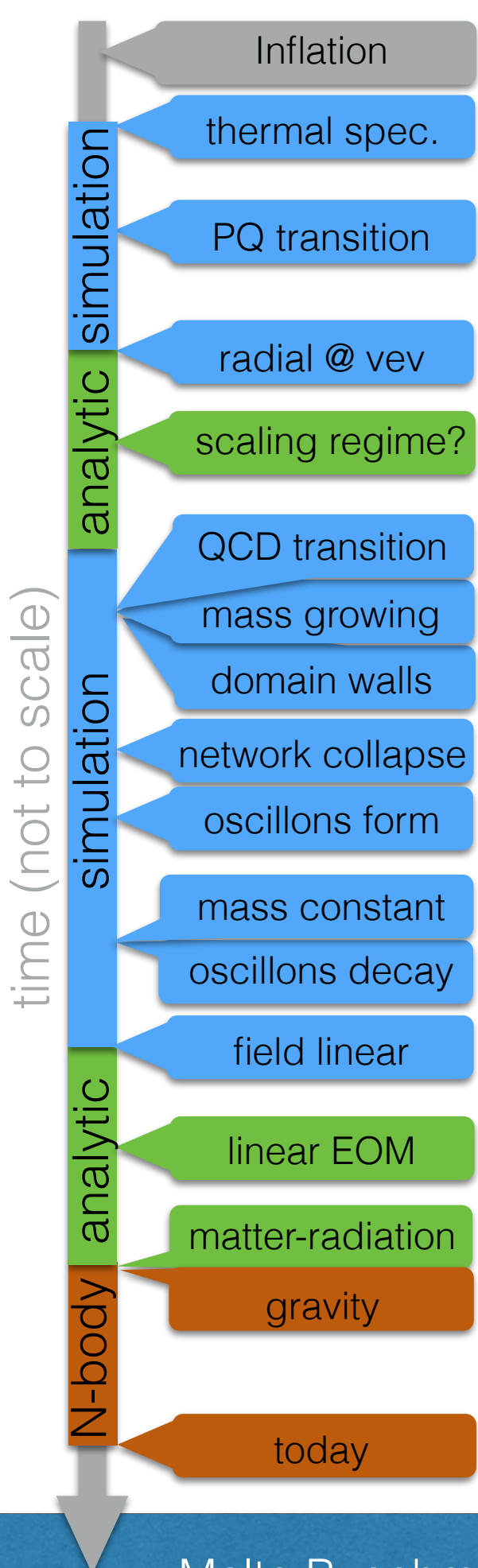
# Obtaining the relic abundance

MB, Foster, Safdi (1906:00967)



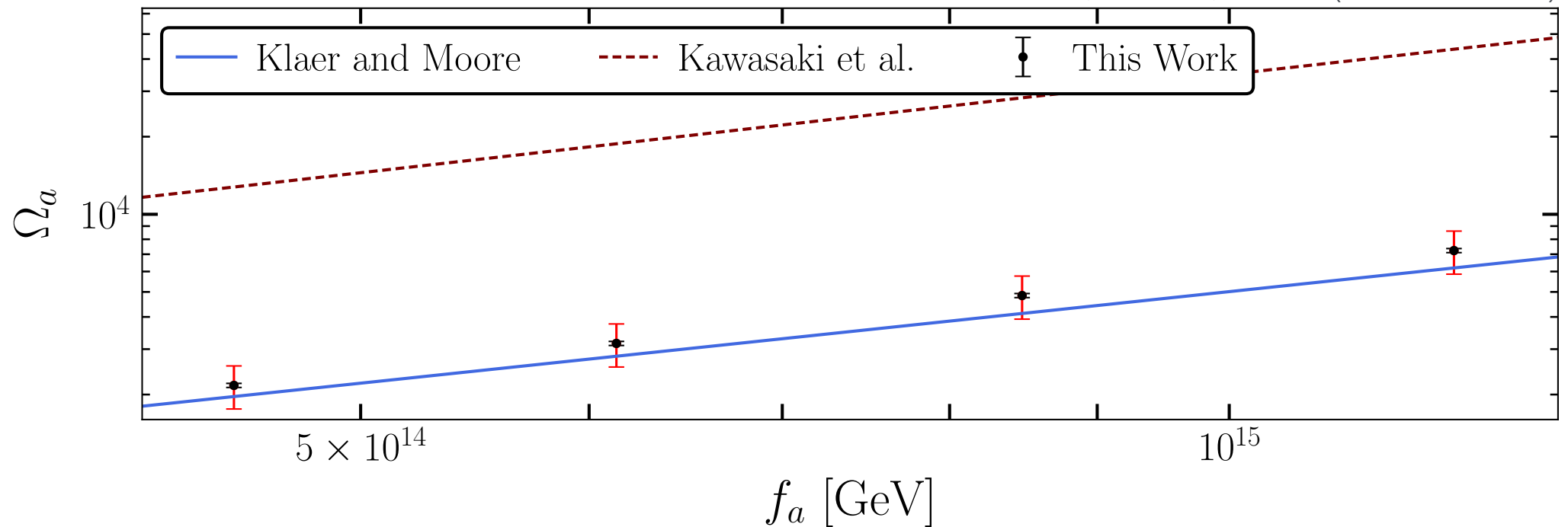
Correct relic abundance reached for:

$$m_a = 25.2 \pm 11.0 \mu\text{eV}$$



# Obtaining the relic abundance

MB, Foster, Safdi (1906:00967)



Correct relic abundance reached for:

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## Uncertainties coming from:

31% uncertainty on the relation between abundance and  $f_a$

27% uncertainty from mass growth  $m_a(T)$

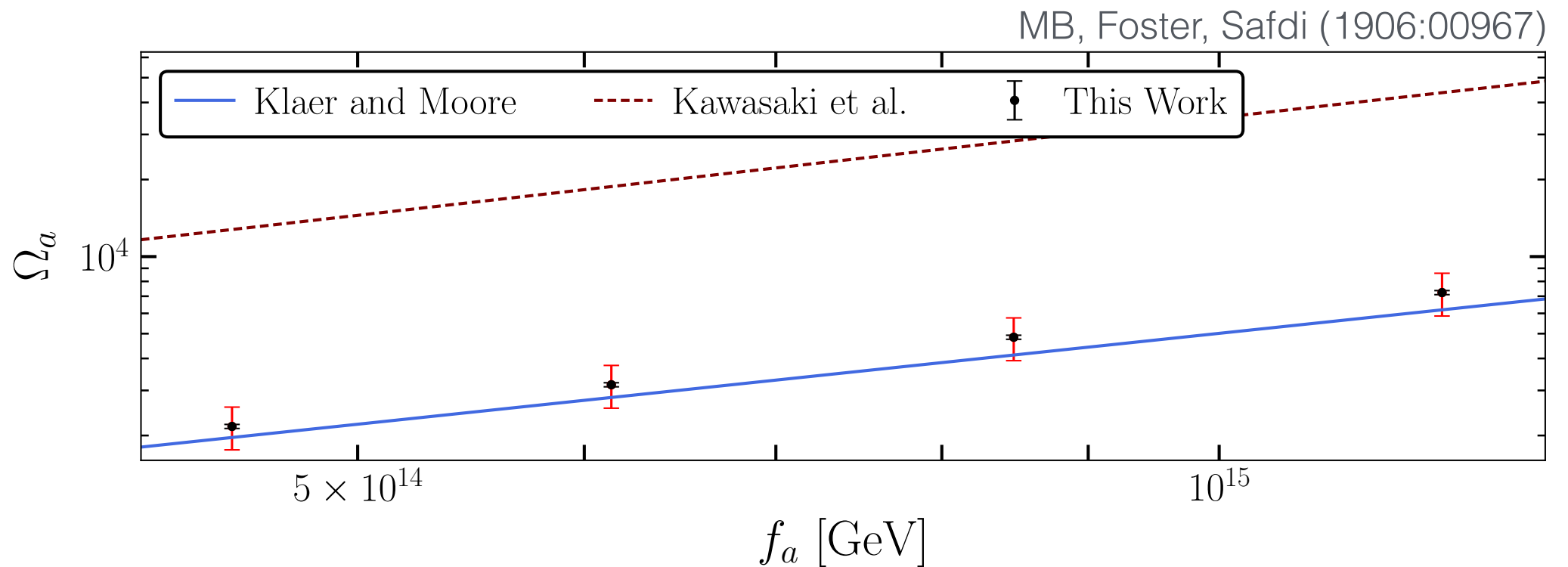
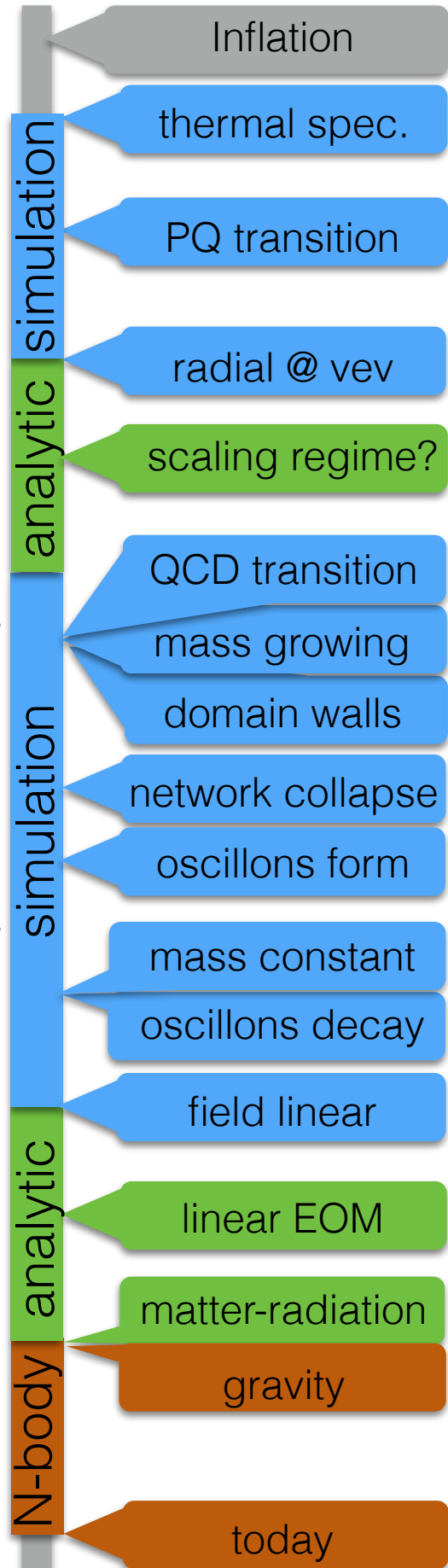
15% from violation of scaling regime

~10% others: statistical, fixed degrees of freedom,...



# Sources of Uncertainties on the Axion Mass

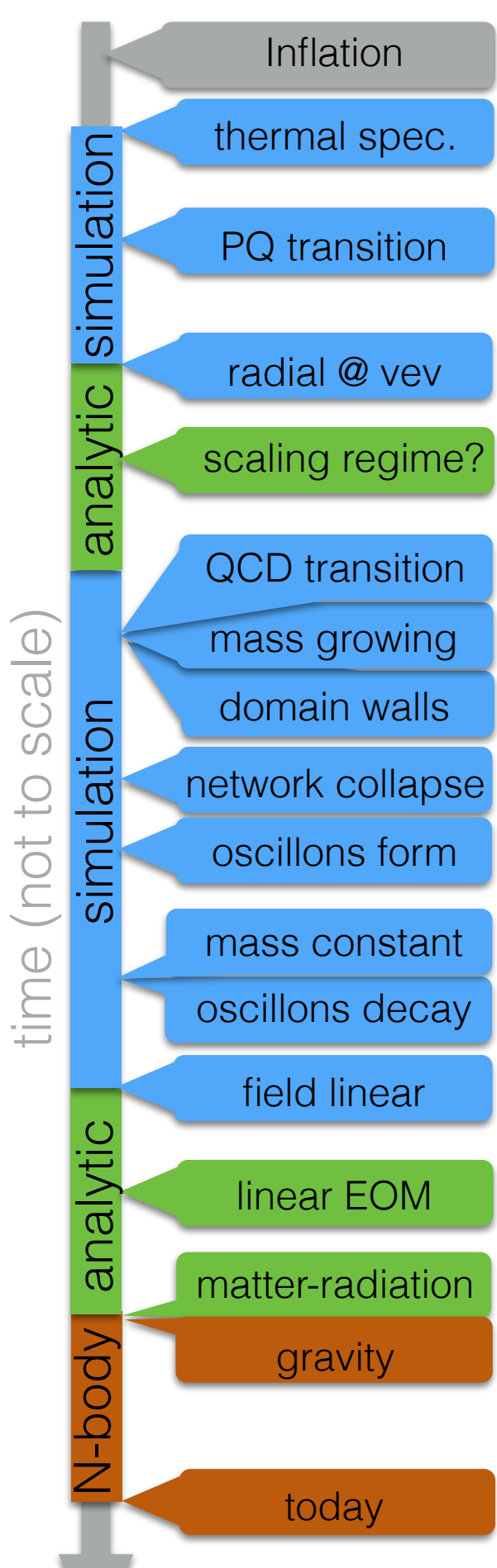
time (not to scale)



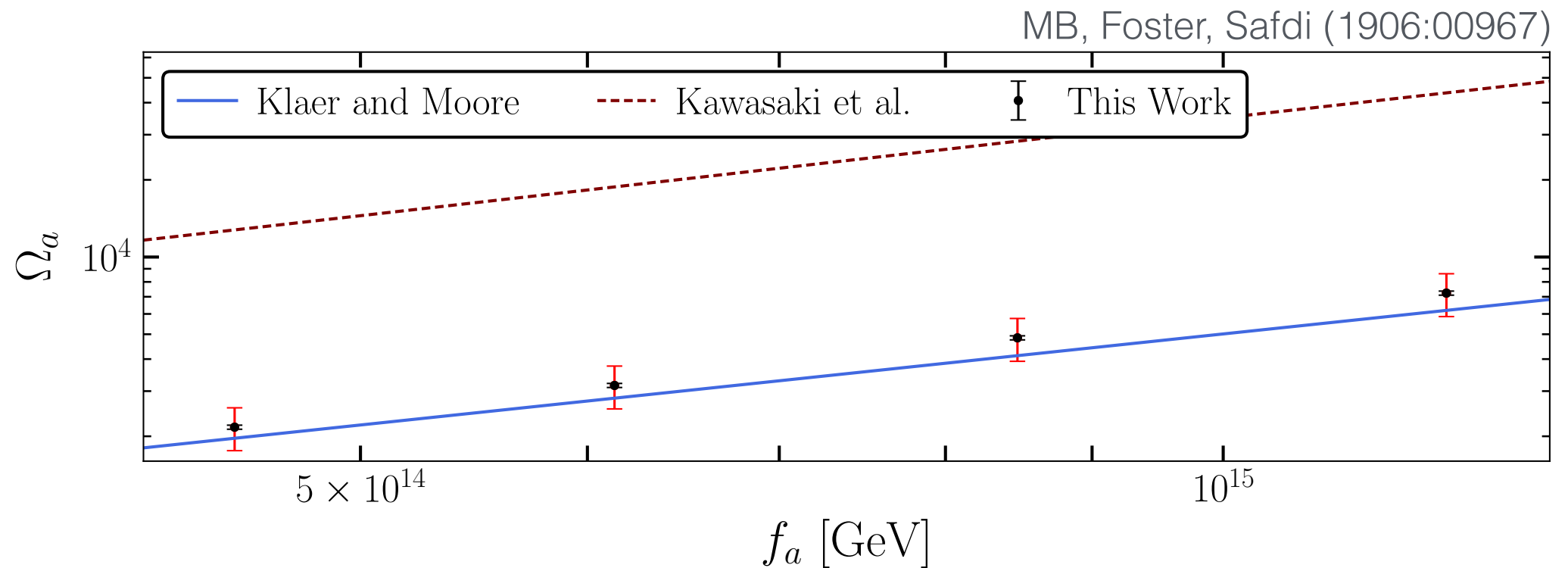
In particular oscillons make it impossible to simulate at low breaking scales. Extrapolations needed:

$$\rho_a \propto f_a^{(6+n)/(4+n)}$$

with  $n=6.68$  from lattice simulations



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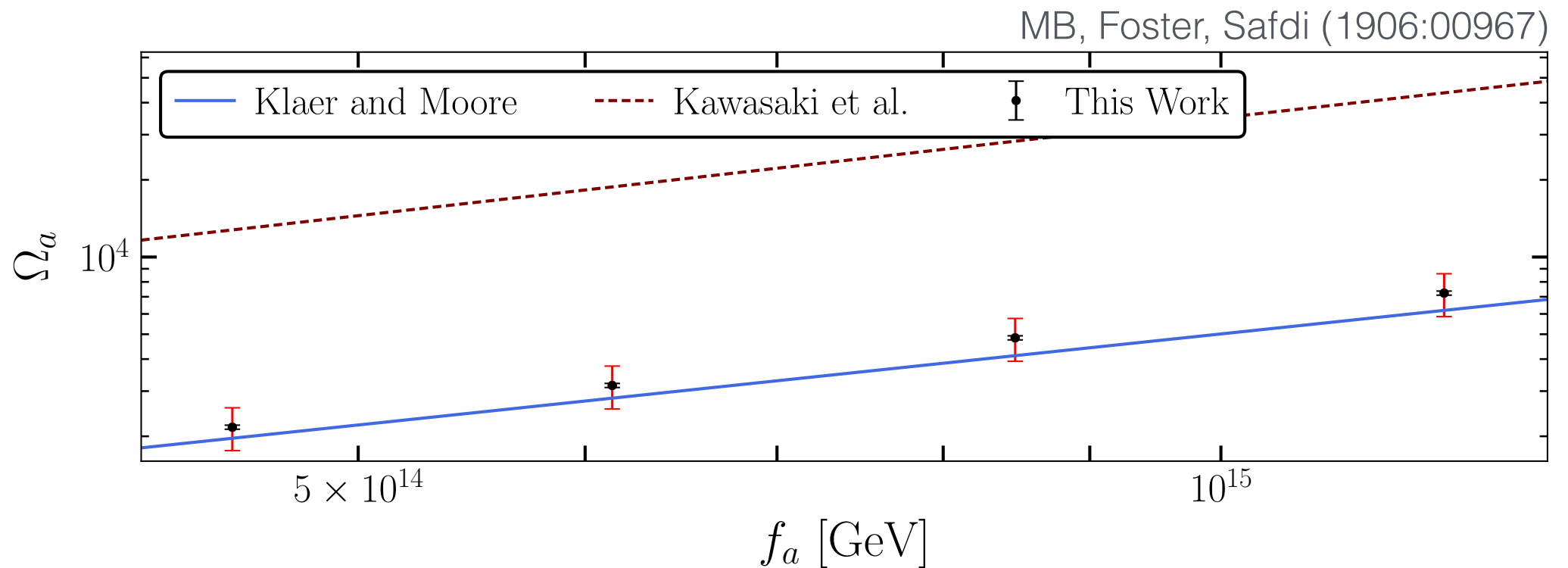
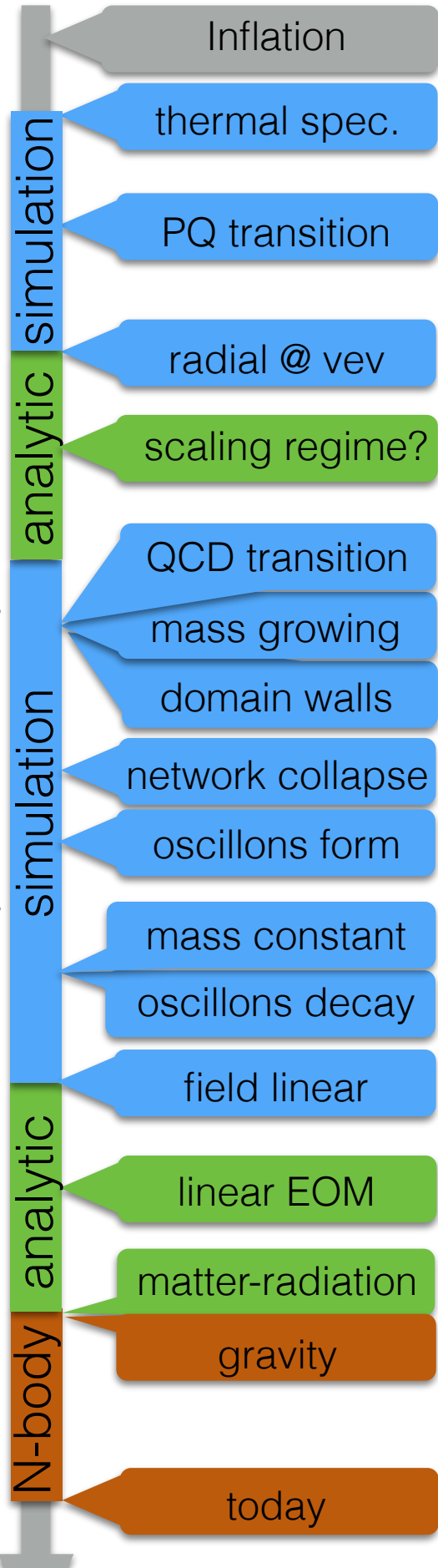
**Expected:**  $\alpha = (n + 6)/(n + 4) \approx 1.187$ .

**Simulation:**  $\alpha = 1.24 \pm 0.04$ .

**Leads to 31% uncertainty on axion mass**

# Sources of Uncertainties on the Axion Mass

time (not to scale)



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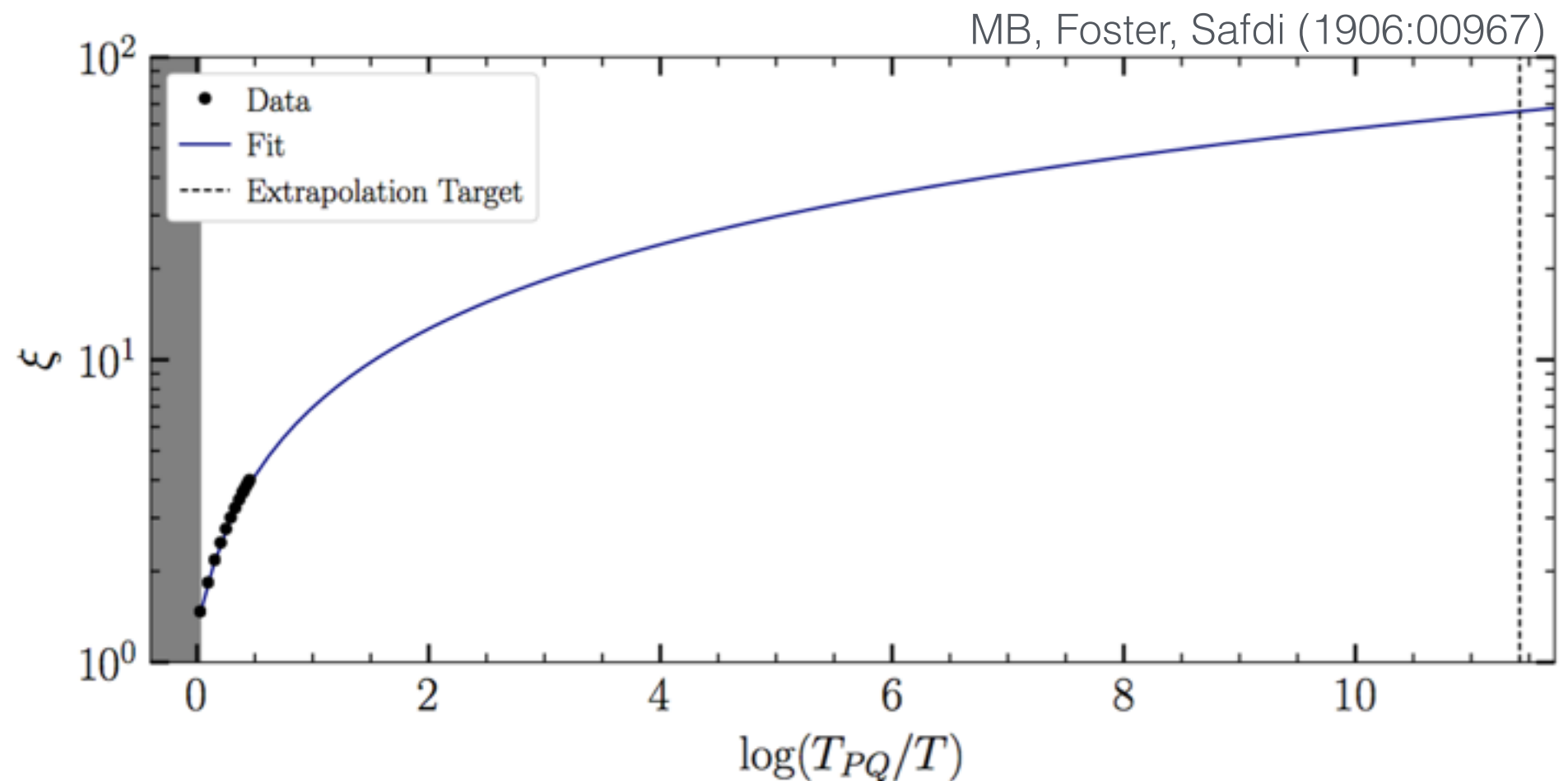
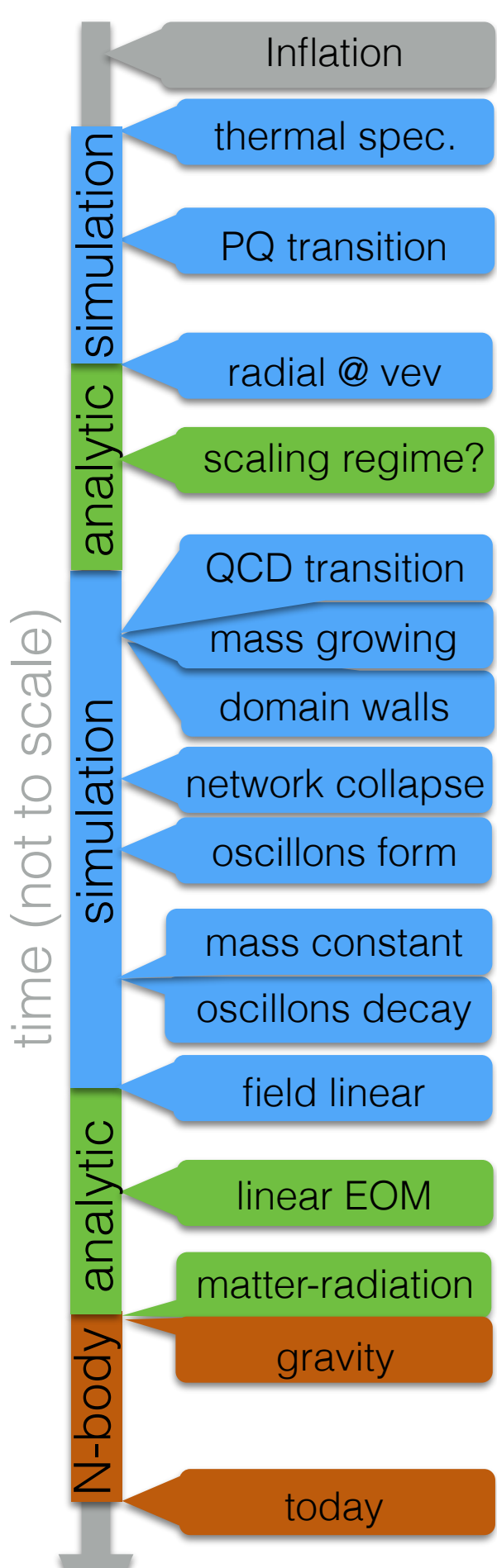
with  $n=6.68$  from lattice simulations

Could be as high as 8.2!

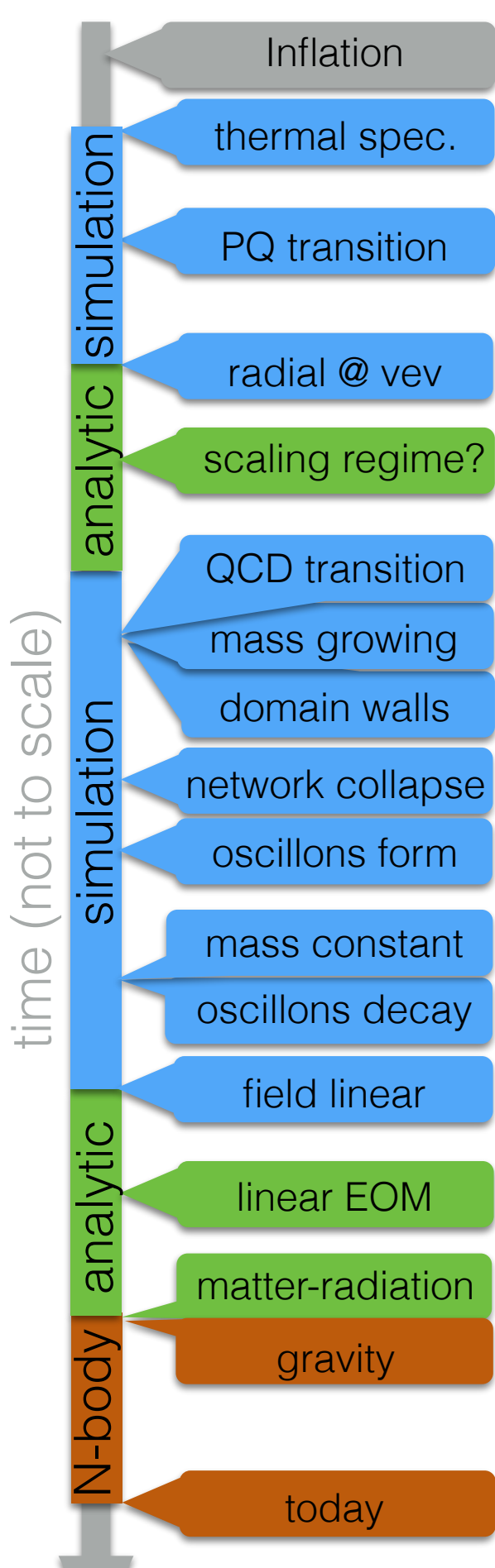
We rerun simulation with 8.2 (in 2D)

**Leads to 27% uncertainty on axion mass**





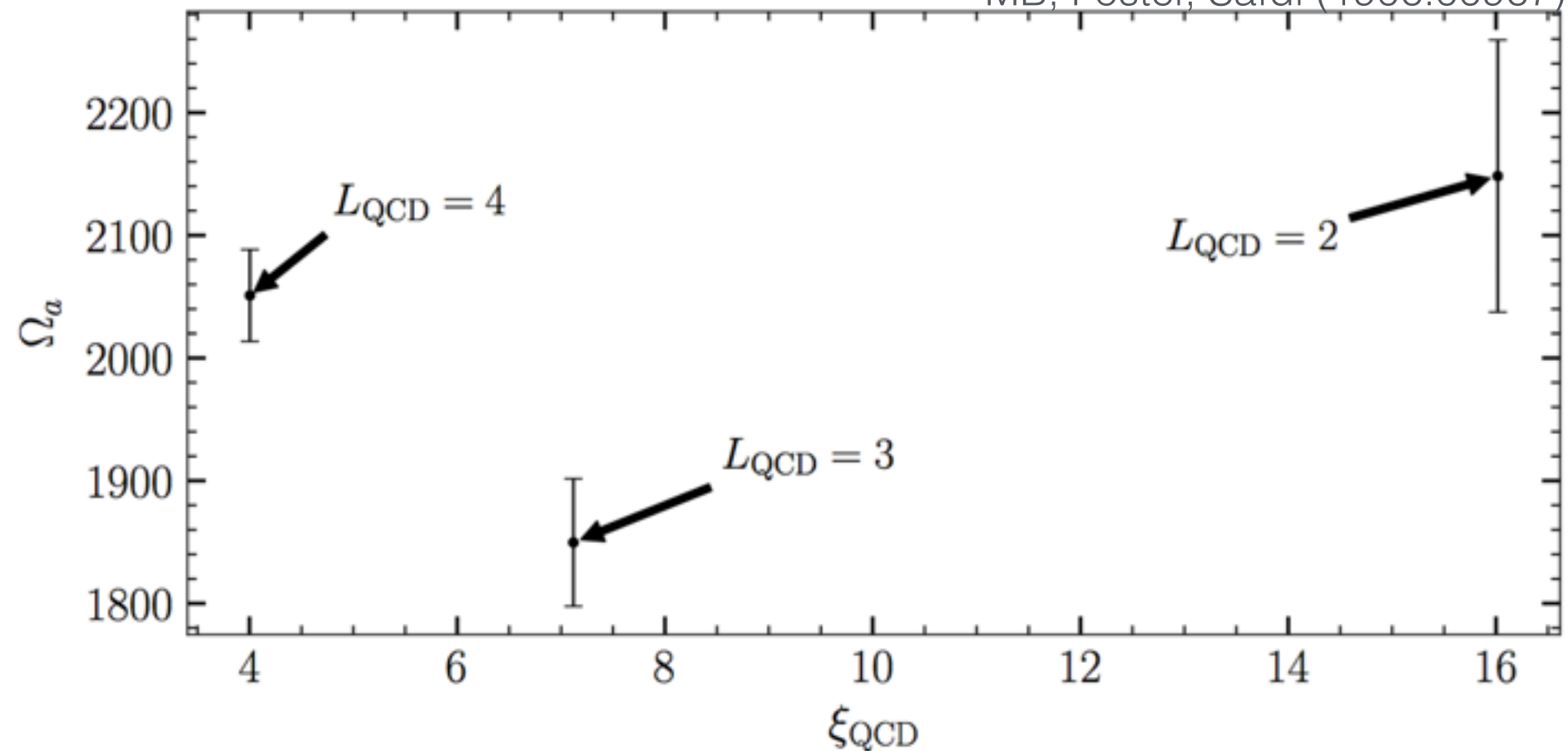
We observe violation of the scaling regime.  
But what affect do about 15 times as many strings have on the relic density?



## Simple estimate:

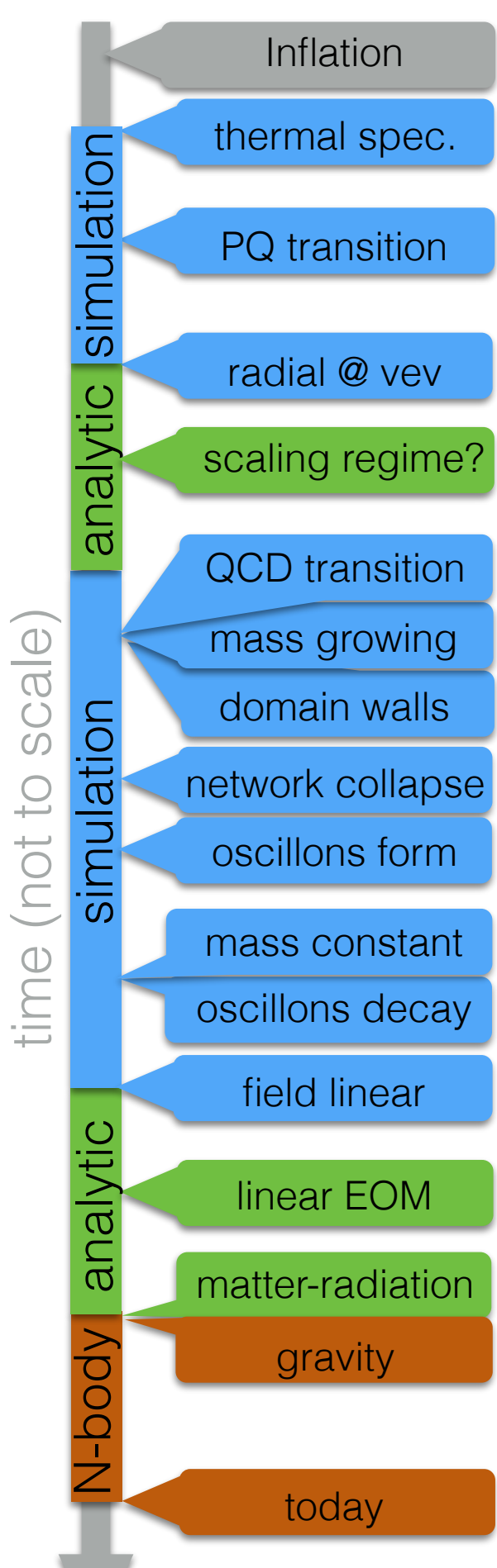
Reinterpretation of the volume of the initial state changes string density

MB, Foster, Safdi (1906:00967)



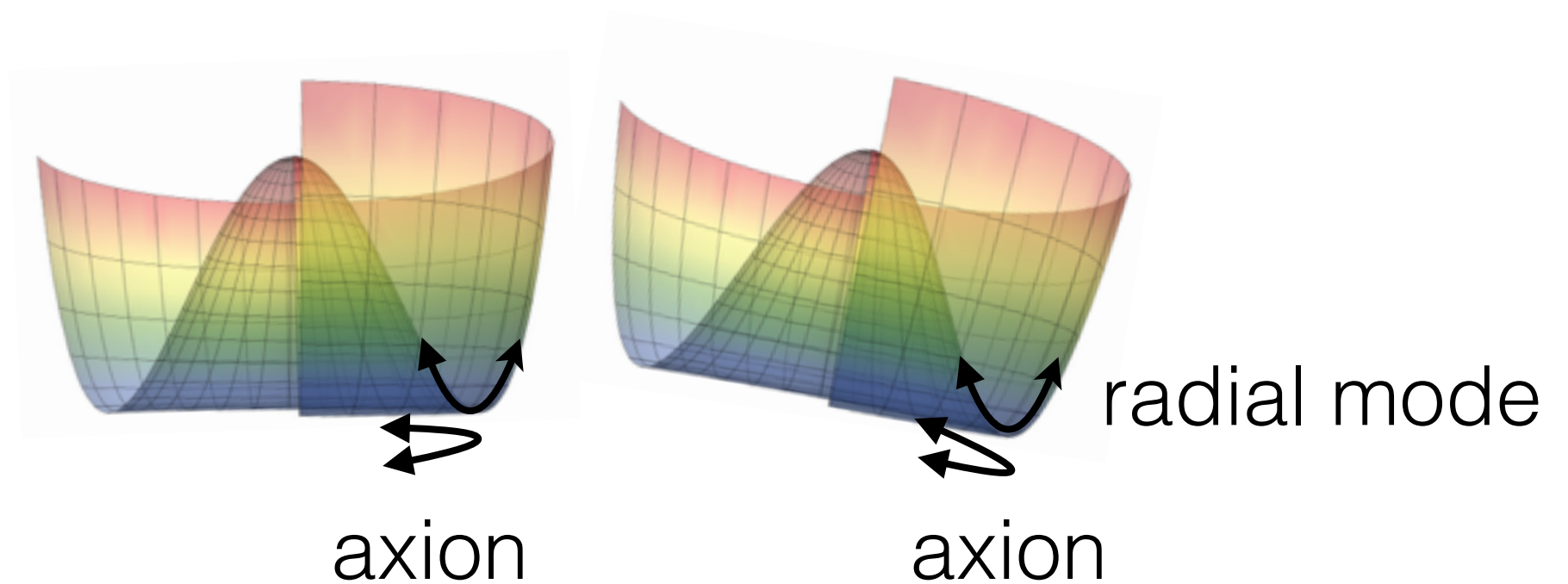
Seems to be a small affect. No trend visible.

***We estimate a 15% uncertainty related to scaling violation.***

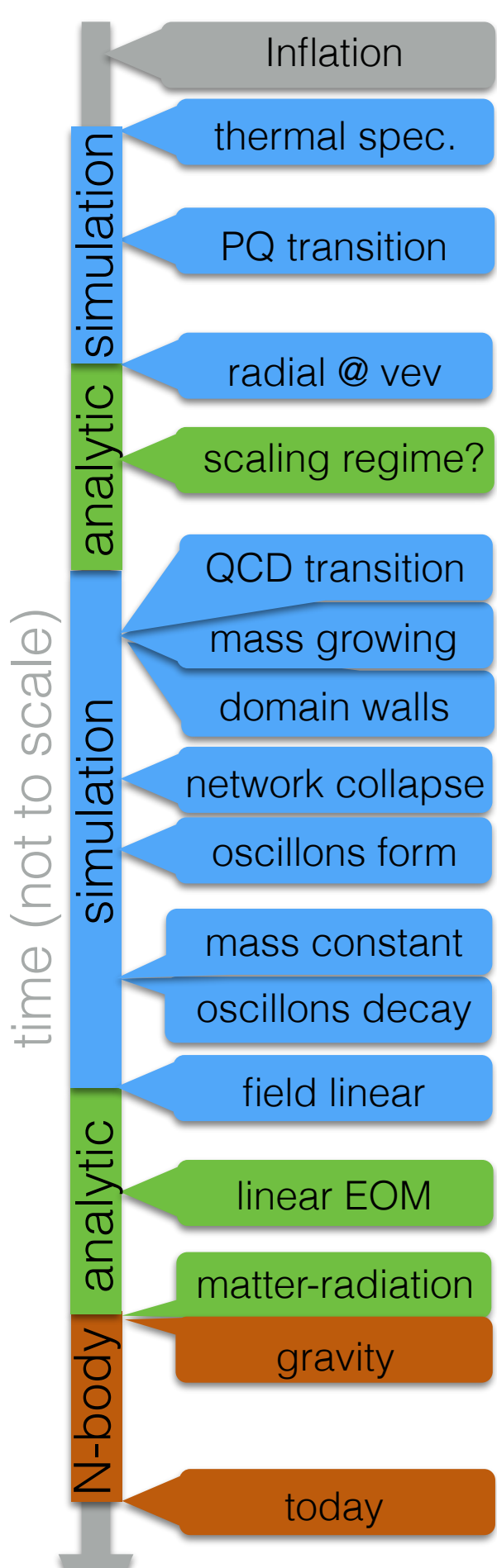


# What is the reason for this?

Number density not conserved  
Axion has to still live on the circle



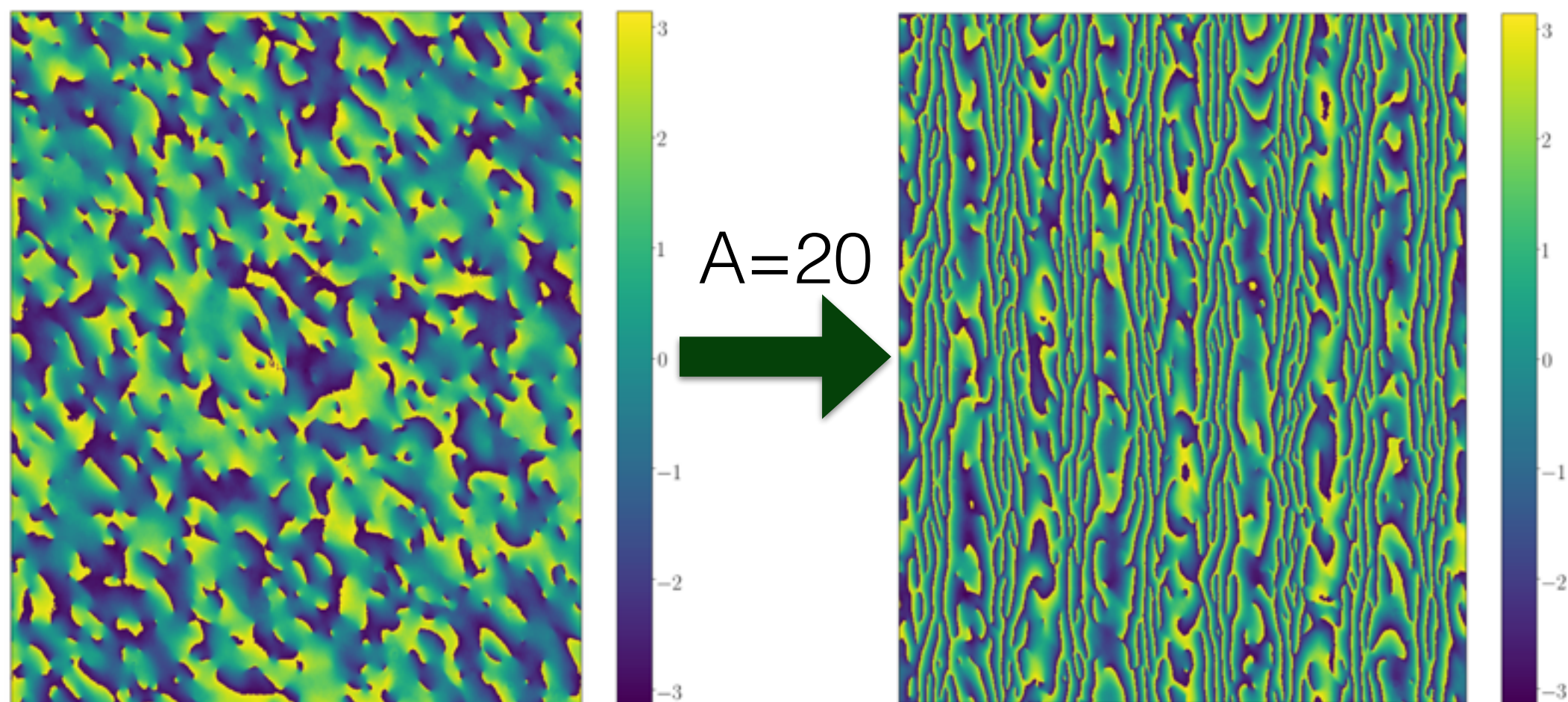




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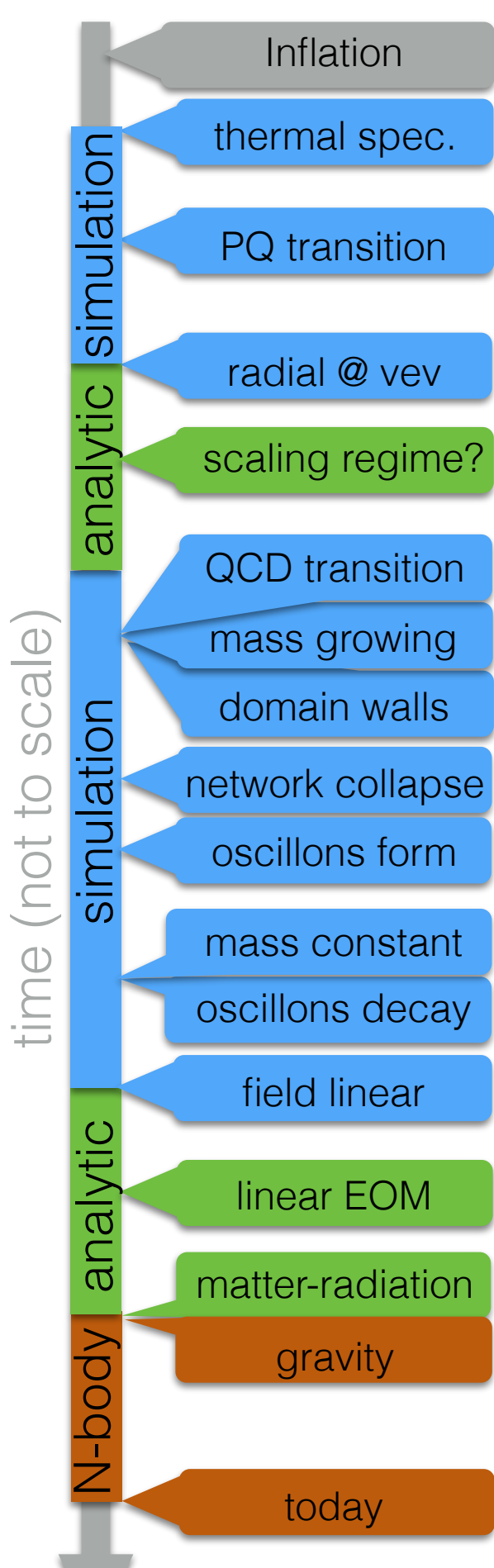
Number density not conserved  
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Inject mode large amplitude mode into field:  
 $\text{PQ field} + A \cos(H x)$



Large amplitude always wraps back.

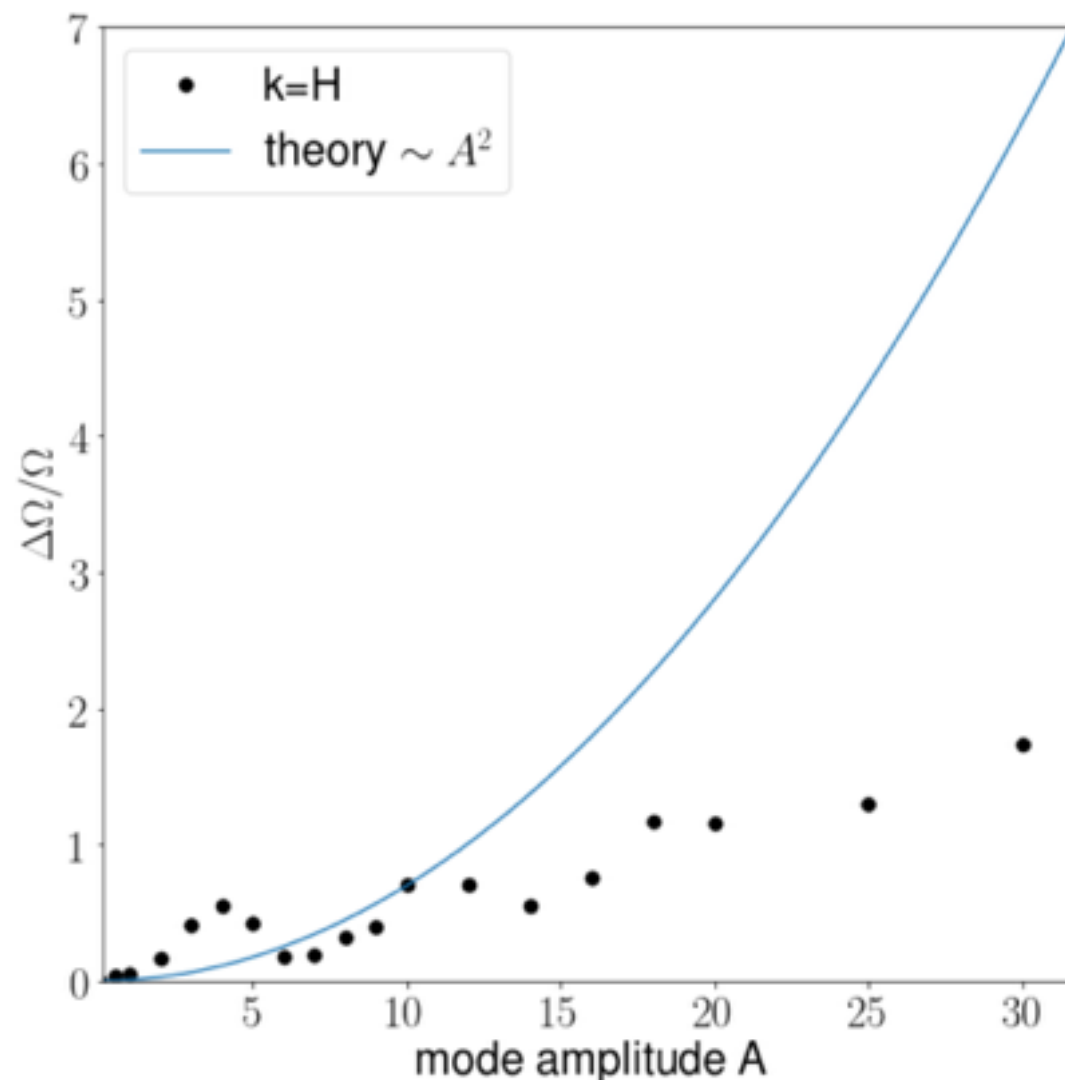




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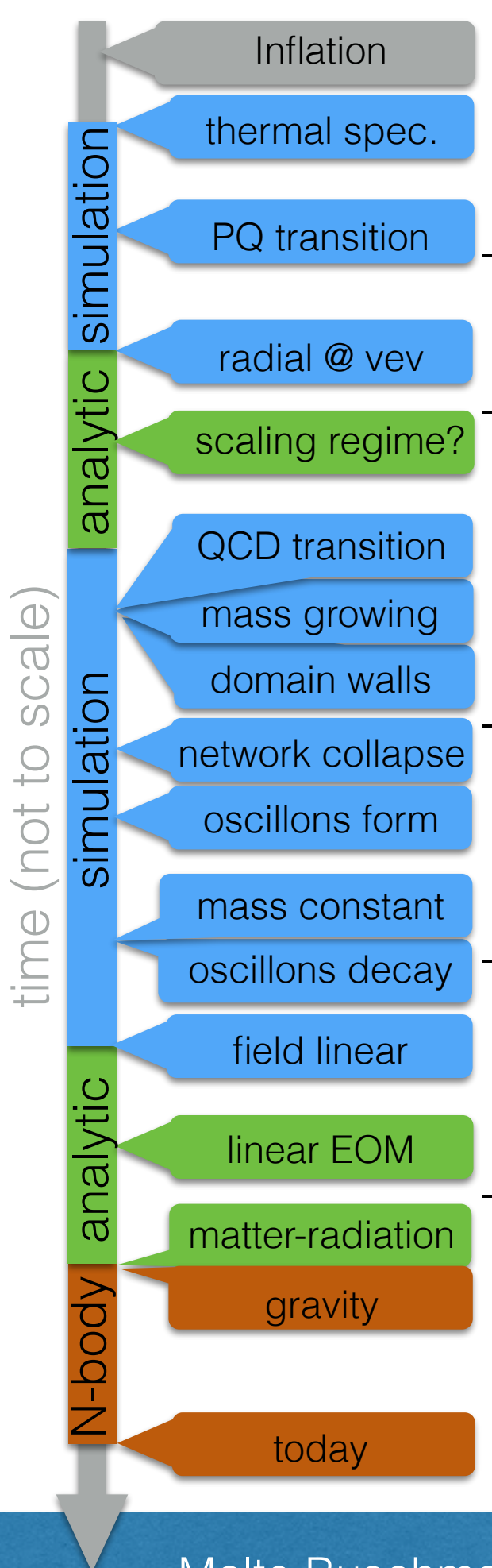




# Thank you!



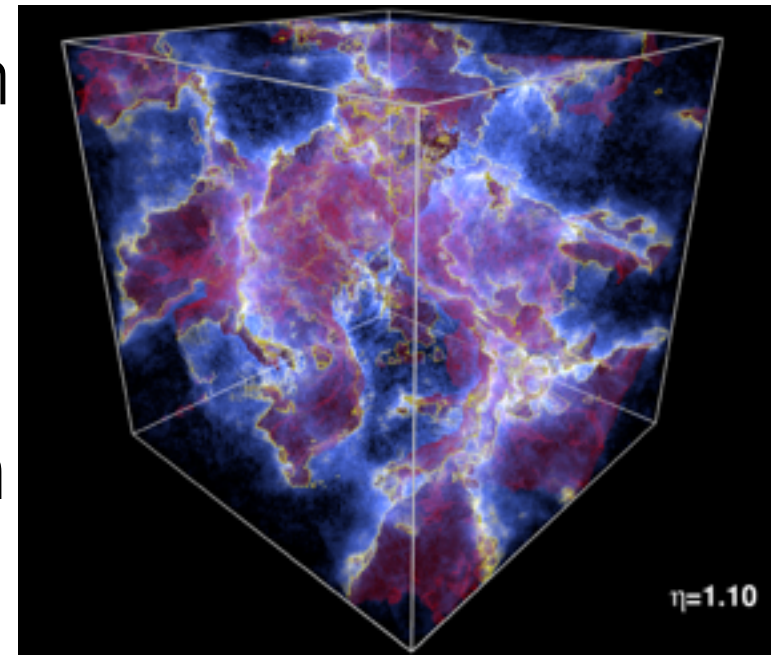
# Summary



Assumption: PQ symmetry broken after inflation

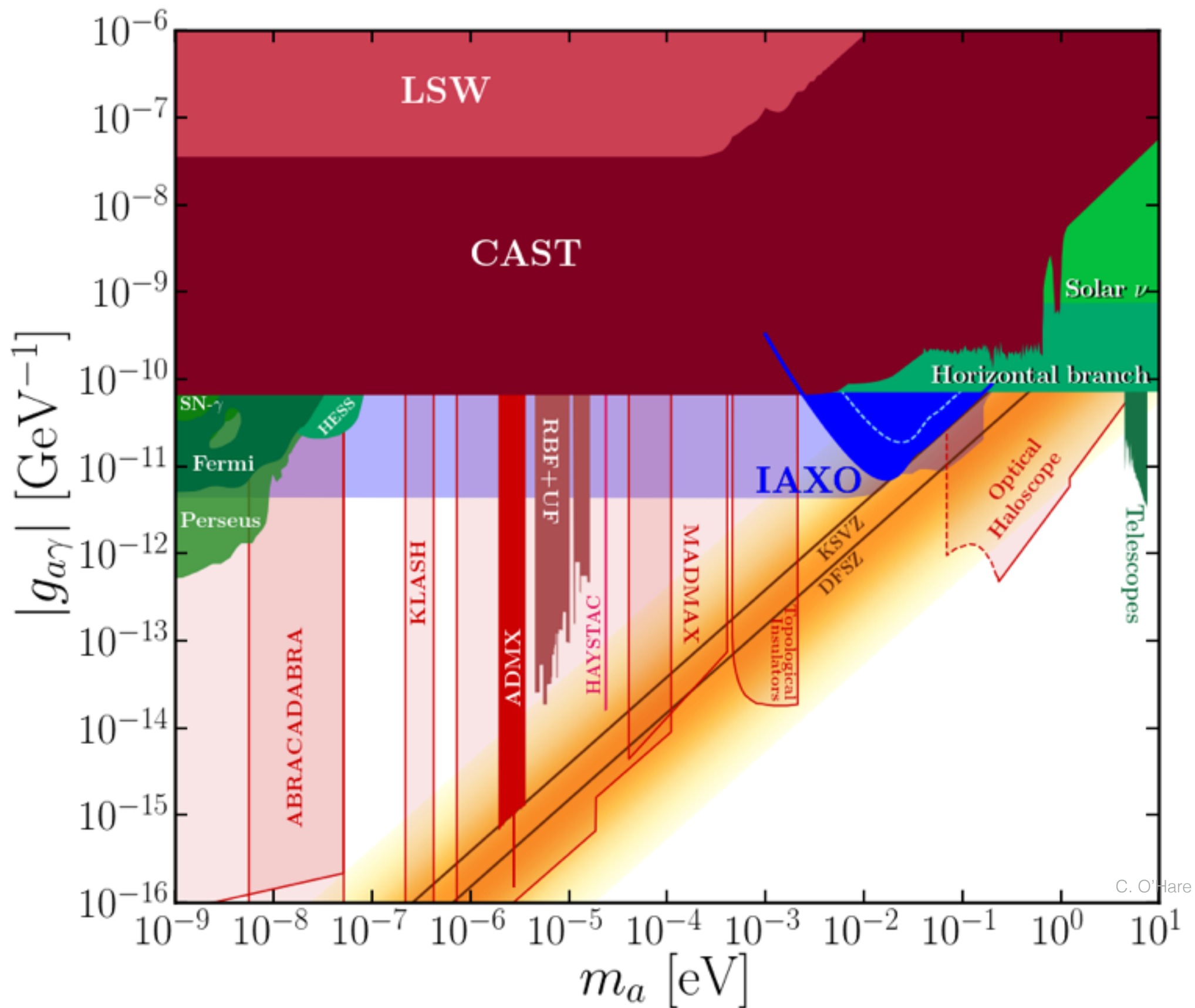
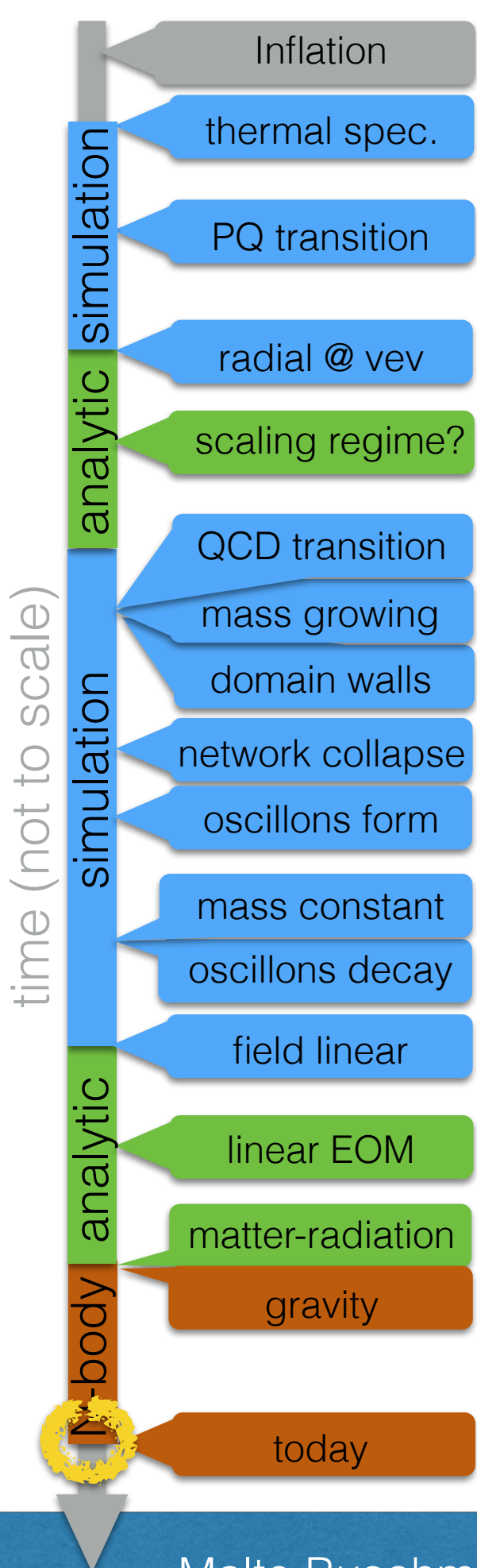
We performed simulations through the PQ and QCD phase transition to matter-radiation equality

Identified minihalo mass spectrum  
Typical mass:  $10^{-14}$  solar masses



Determined the axion mass that reproduces the correct relic abundance:  $m_a = 25.2 \pm 11.0 \mu\text{eV}$

Furthermore: Simulation data publicly available for further studies: <https://zenodo.org/record/2653964> (e.g. gravitational N-body simulations)





# Radio signals from neutron stars

time (not to scale)

Inflation

thermal spec.

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mass growing

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oscillons form

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linear EOM

matter-radiation

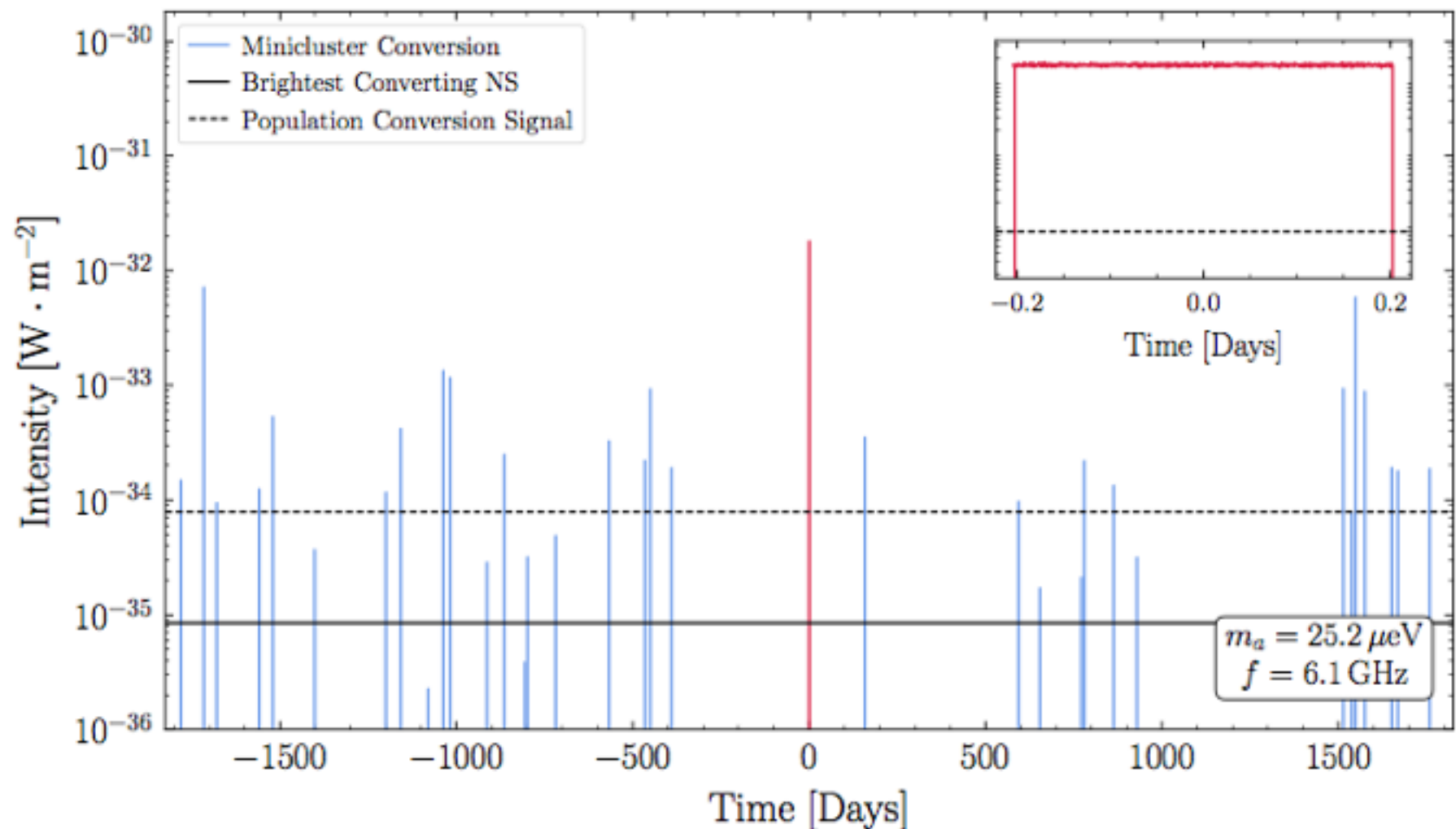
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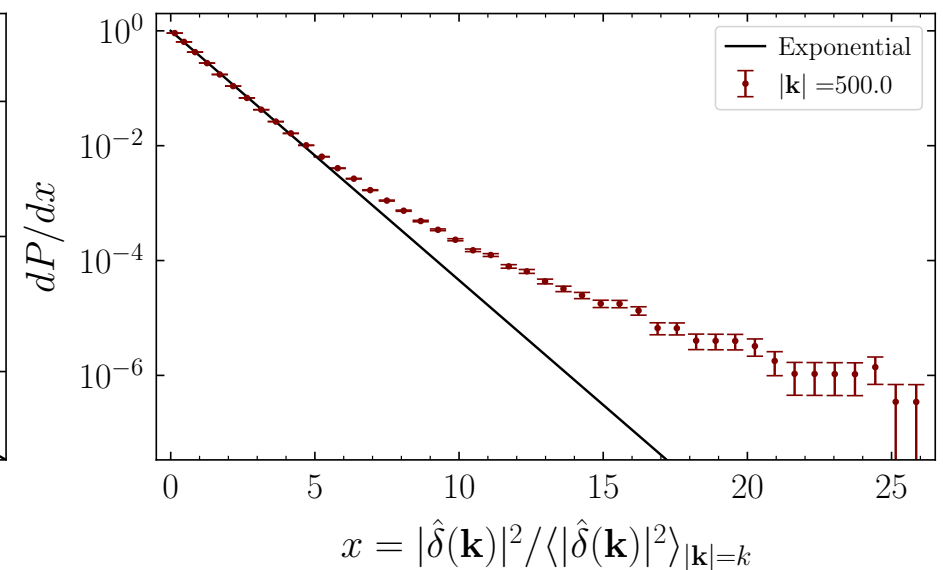
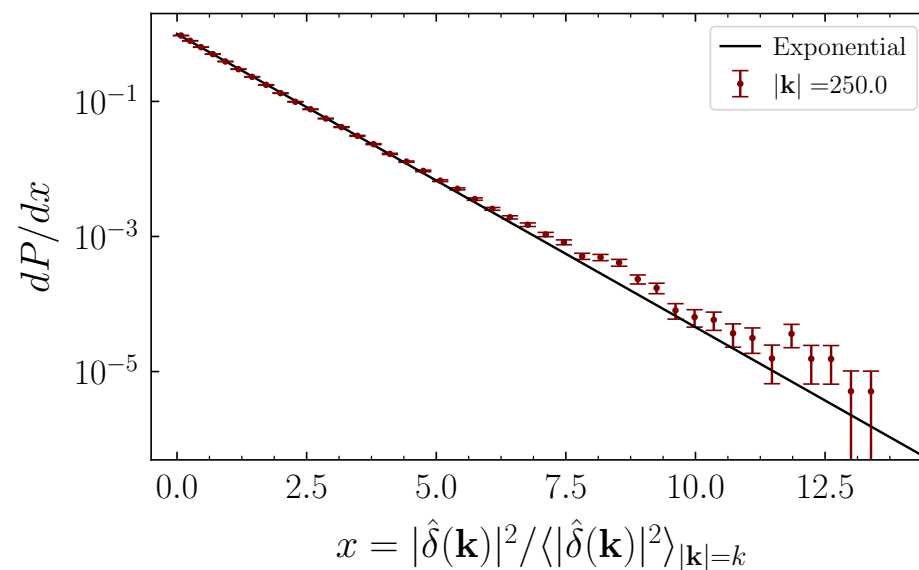
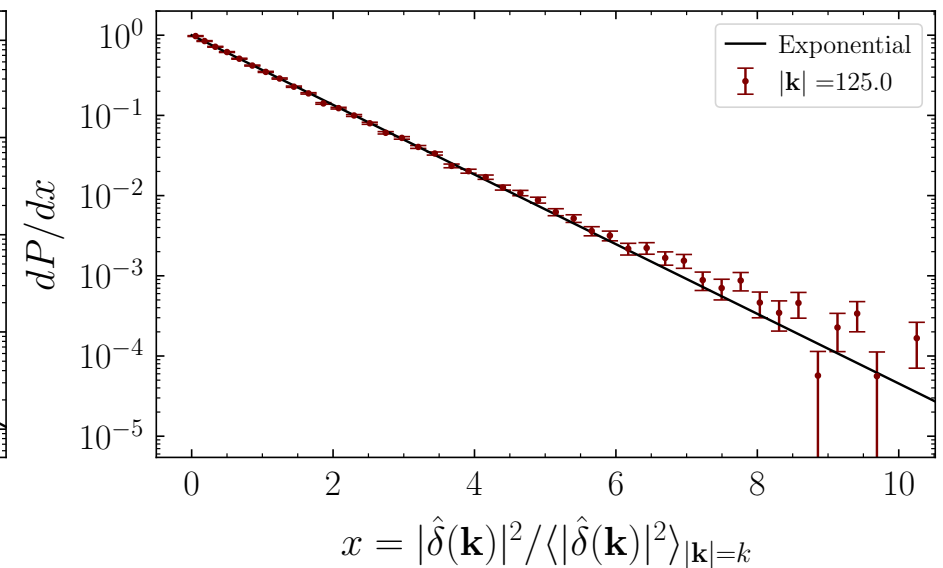
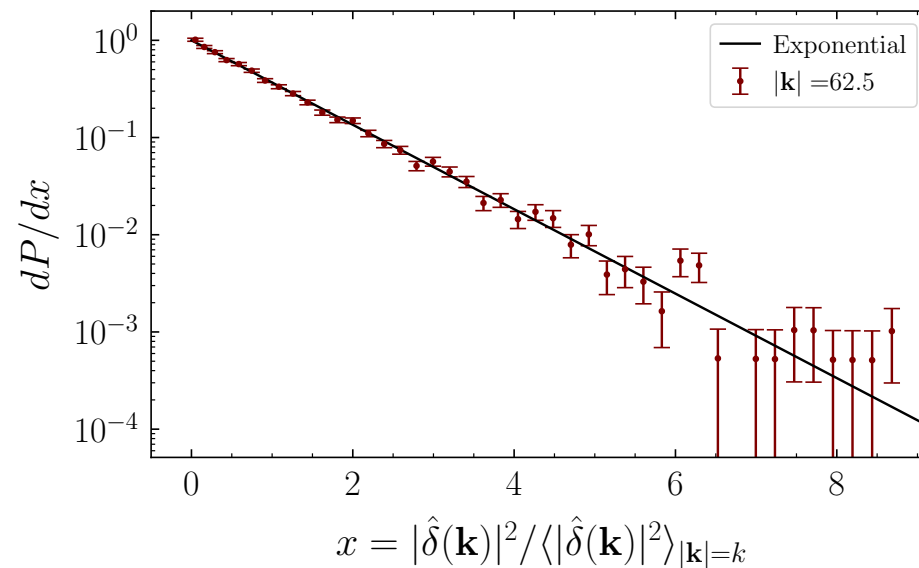
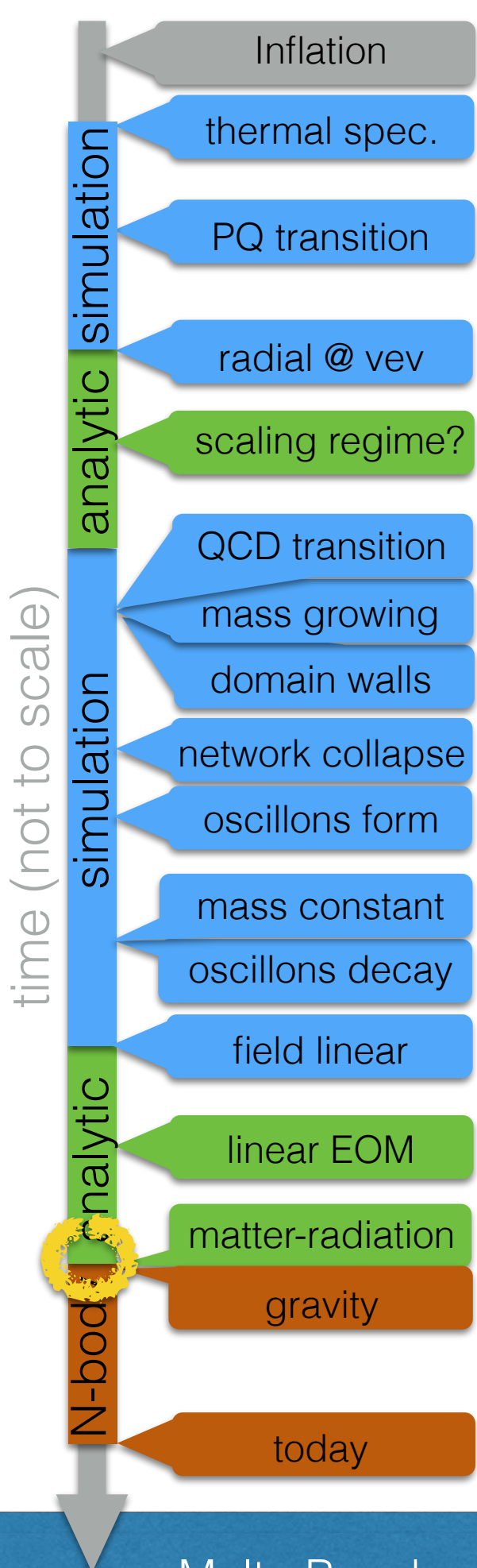
today



Axions convert to radio photons in magnetic field of neutron star

Large peak in flux when neutron star moves to a axion minihalo!





Field is non-Gaussian at small scales!



Power spectrum insufficient to describe the final state

We provide our data at:

<https://zenodo.org/record/2653964>