Characterization of matter in the Megabar regime using laser shock compression: applications to planetology

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International HighRadMat workshop CERN, 10-12 July 2019



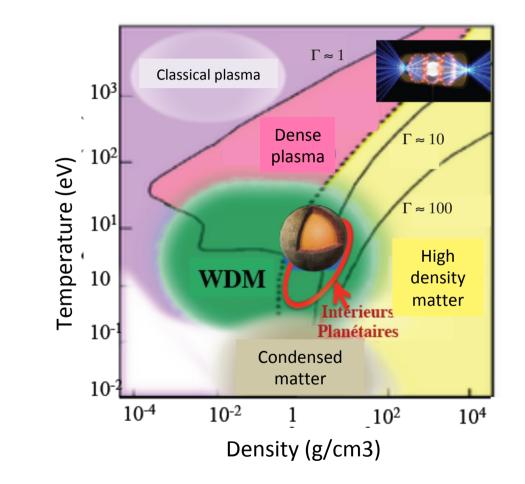
Introduction: The Warm Dense Matter Why its characterization is important ? What is planetology in laboratory? How to do it? What is a laser shock? How to measure the equation of state?

✓ Recent developments: some examples on silicates

✓ Conclusions

The Warm Dense Matter





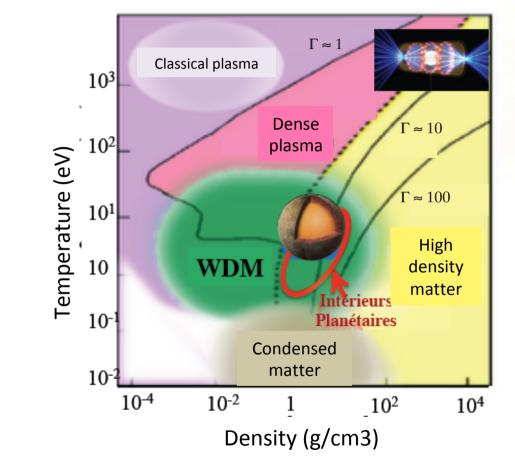


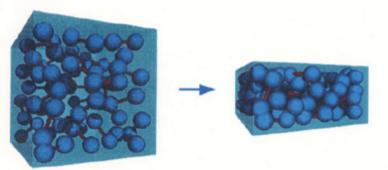
0. 1 eV < T < 100 eV

P > Mbar

The Warm Dense Matter







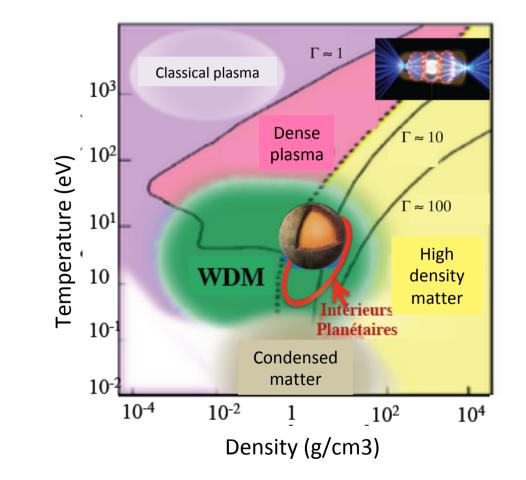
WDM is the state at the intersection between plasma physics and condensed matter physics.

WDM is correlated and degenerate Correlated $\Gamma = E_c / E_{th} > 1$ Coulomb energy E_c Thermal energy E_{th} Degenerate $T_F > T$

Difficult to simulate theoretically -> Quantum Molecular Dynamics calculations -> need of experimental data to validate them

The Warm Dense Matter





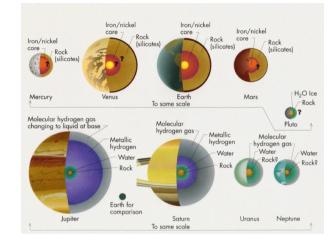
Conditions found in inertial confinement fusion path compression and inside planets

In the last tens years -> new topic "planetology in laboratory"

An important motivation to study WDM : planetary science

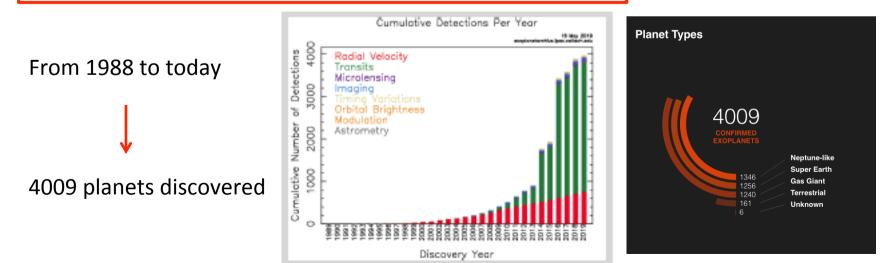


 \diamond Study of Formation and evolution of planets

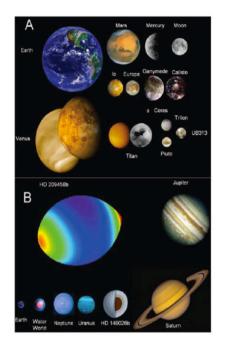


♦ Study of planet interiors





Key questions about planets inside and outside the Solar System



What is the nature of the iron core at the center of Earth and other terrestrial planets? -> Dynamo effect
What is the interior structure of Jupiter and the other giant planets? Why is Saturn luminosity not compatible with its age?

The internal structure is inferred indirecity from their global properties: M mass, the radius and gravitationnal moments (few observables) For exoplanets -> only mass and radius

To progress in the planetology:

We have to know the equation of state, the conductivity, structural properties etc...of the matter existing in the planet interiors.

How create this planetary matter in a laboratory?



Static way

Diamond cell Isothermal Compression

 $P \approx 0$ - a few Mbar



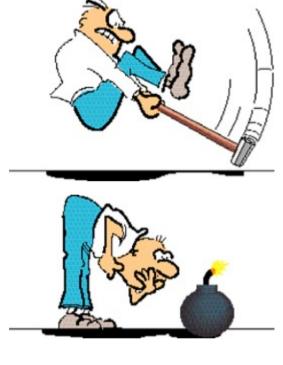
Chemical explosions, gas guns, ions beams

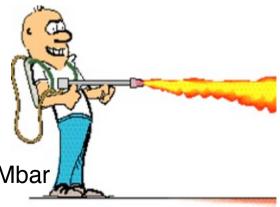
High power lasers



Shock Compression

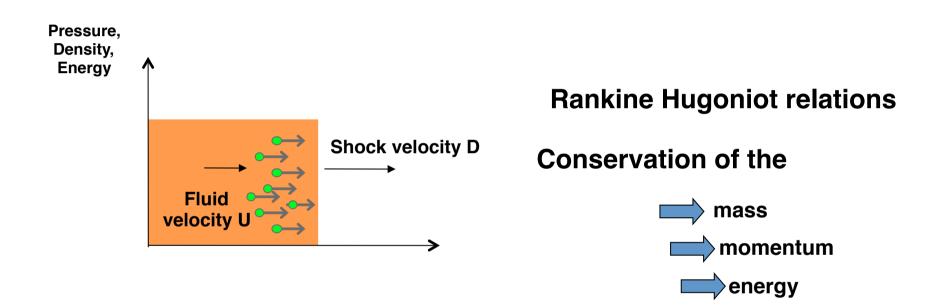
 $P \approx 0$ – several tens of Mbar





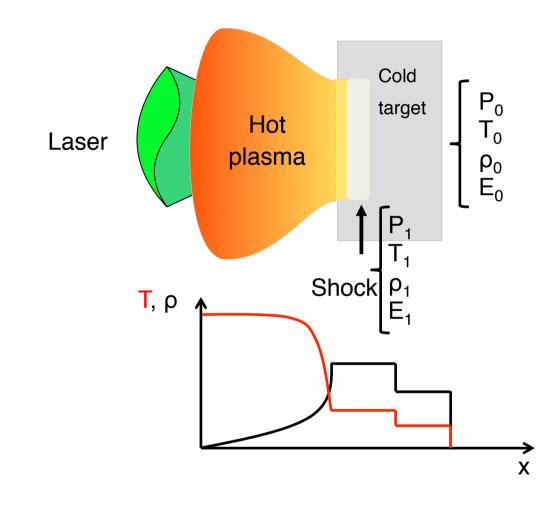
What is a shock ?





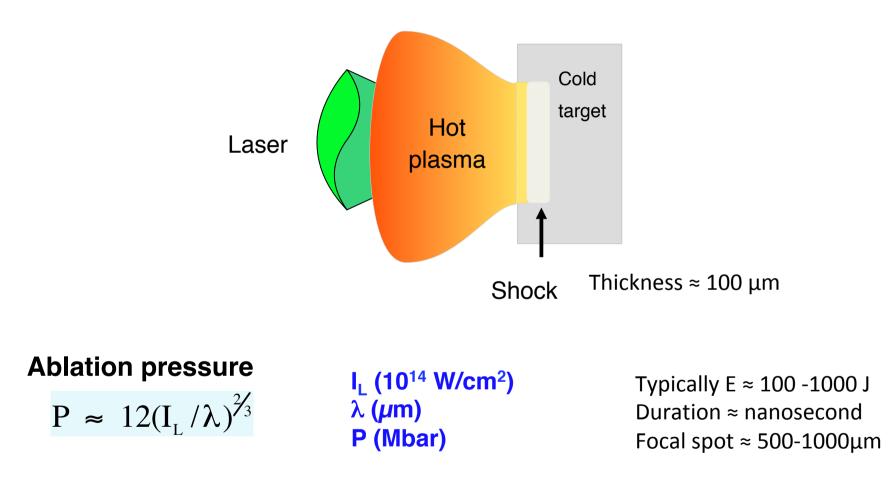


Laser driven shock



Laser driven shock





Today ---> Pressures of several tens of Mbar

EOS measurements using a shock



Rankine-Hugoniot

 $\left\{ \begin{array}{ll} \rho_0 D = \rho \; (D\text{-}U) & \text{mass} \\ \\ \rho_0 DU = P\text{-}P_0 & \text{momentum} \\ \\ \rho_0 D(\text{E-}E_0 + U^2/2) = PU & \text{energy} \end{array} \right.$

5 unknown parameters (D,U,P,E,ρ)

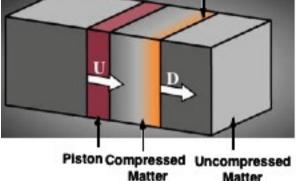
To have a point on $f(P, E, \rho) = 0$

✓2 parameters - *absolute measurement* 2 velocities D and U \rightarrow time and distance

✓1 parameter - *relative measurement* shock velocity D in 2 different materials (one used as reference)

Shock front

Pn Pn En



P, p, E

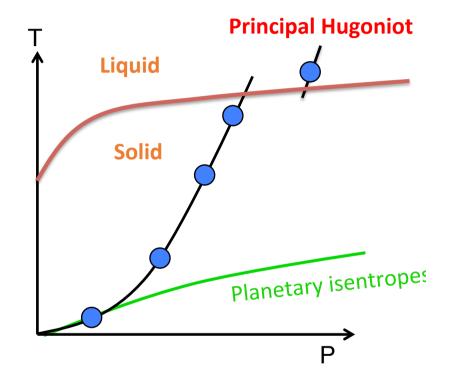


Rankine-Hugoniot

 $\begin{cases} \rho_0 D = \rho (D-U) & mass \\ \rho_0 DU = P-P_0 & momentum \\ \rho_0 D(E-E_0+U^2/2)=PU & energy \end{cases}$

5 unknown parameters (D,U,P,E, ρ)

To have a point on $f(P, E, \rho) = 0$

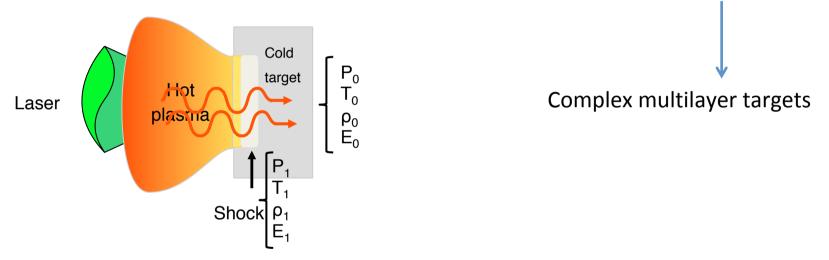


✓2 parameters - *absolute measurement*2 velocities D and U → time and distance

 ✓1 parameter - relative measurement shock velocity D in 2 different materials (one used as reference)



The shock must be uniform, well controlled -> without preheating



To measure parameters with required precision ($\frac{2}{2} \frac{qq}{8}$) for a target < <u>1 mm</u> within $\approx 10^{-9} \text{ s}$



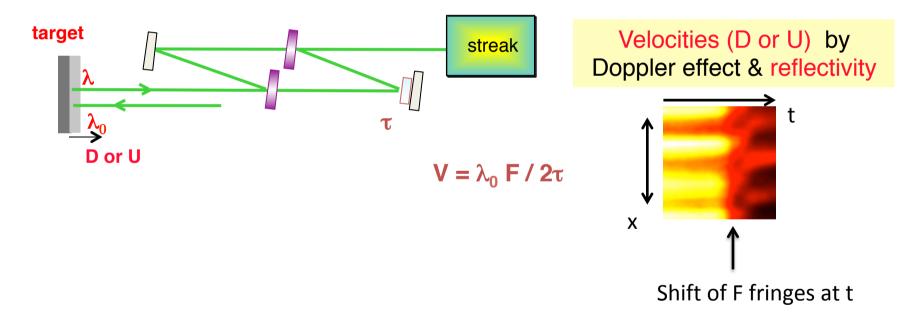
High resolution for the detectors $< 10 \ \mu m$ et $\approx 10^{-12} \ s$

How do we measure shock parameters?



Usual diagnostics

Velocity Interferometer System for Any Reflector (VISAR)

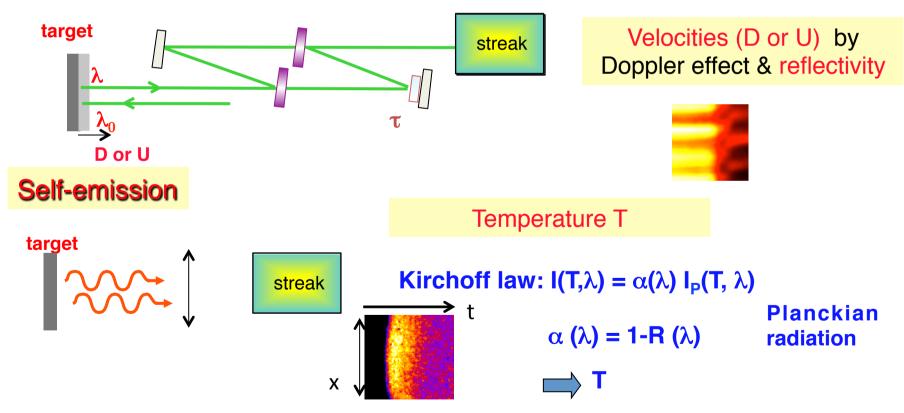


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Usual diagnostics

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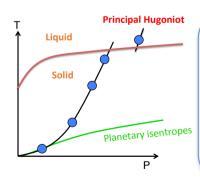
We obtained reliable EOS data (method tested on standard materials) Koenig et al. PRL 94



 \circ Three main challenges

To perform microscopic study to progress in the knowledge of phase diagrams of the main planetary components

✓ Coupling X-ray diagnostics (X-ray diffraction, X-ray absorption near edge spectroscopy ...) with a laser shock



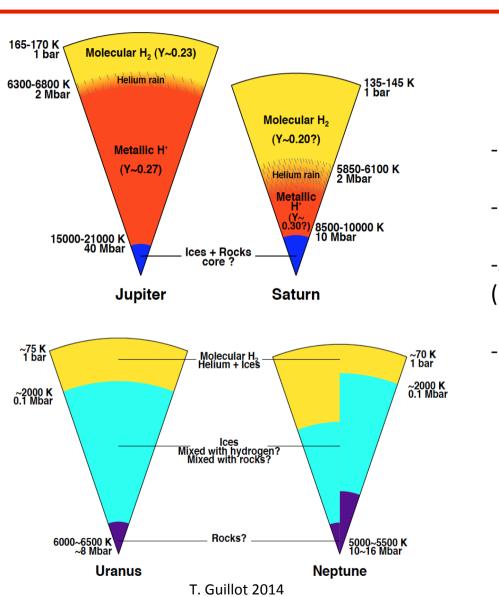
To achieve planetary conditions (dense and cold < 1eV) Shock Too bot

Shock——> Too hot

 Alternative compression techniques (quasiisentropic compression, double choc, DAC+ shock)

To investigate complex compounds typical of planetary interiors

Main planetary compounds



-hydrogen and helium

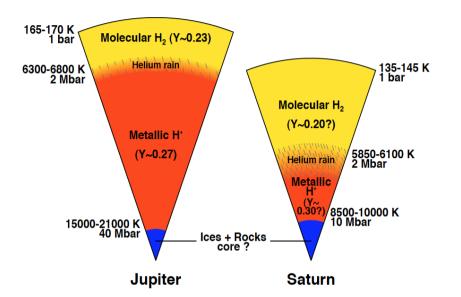
-mixtures of H_2O , NH_3 , CH_4

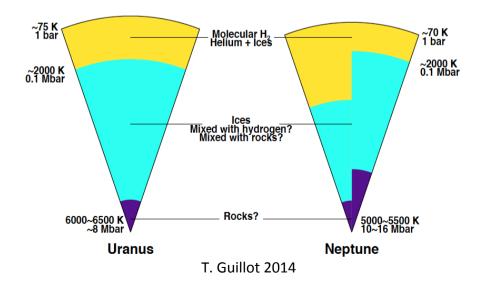
-Silicates and oxides: (Mg,Fe)2SiO₄, (Mg,Fe)SiO₃, (Mg,Fe)O

-Iron and iron alloys

Main planetary compounds







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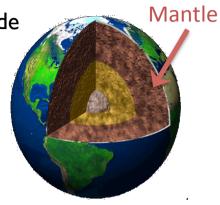
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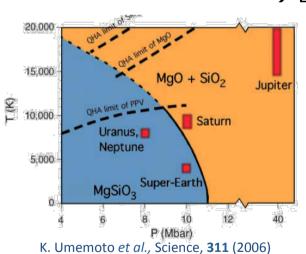


Silicates (MgSiO₃, Mg₂SiO₄, ...) are expected to be inside

- cores of giant planets
- deep mantles of terrestrial ones

How do these compounds melt, dissociate or turn metallic?





 \rightarrow Evolution and characteristics of these planets

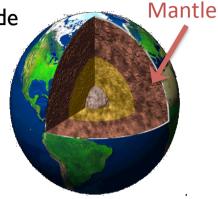
Ab initio calculations predict the dissociation of MgSiO₃ \rightarrow (SiO₂ + MgO)

We need experimental data in high pressure regime to validate theory



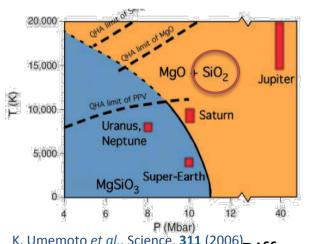
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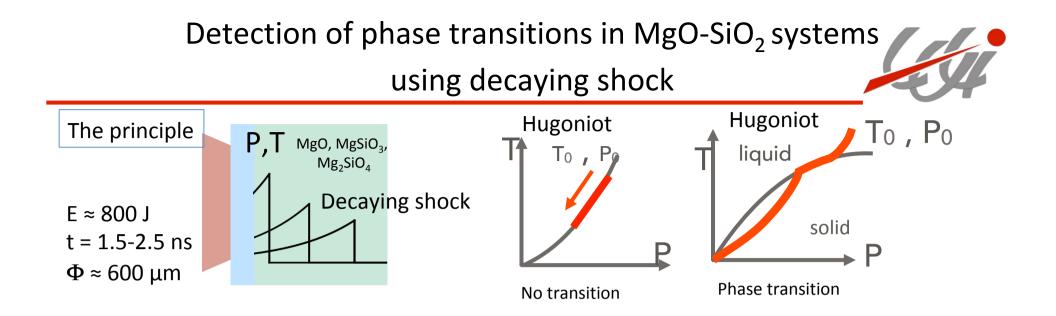


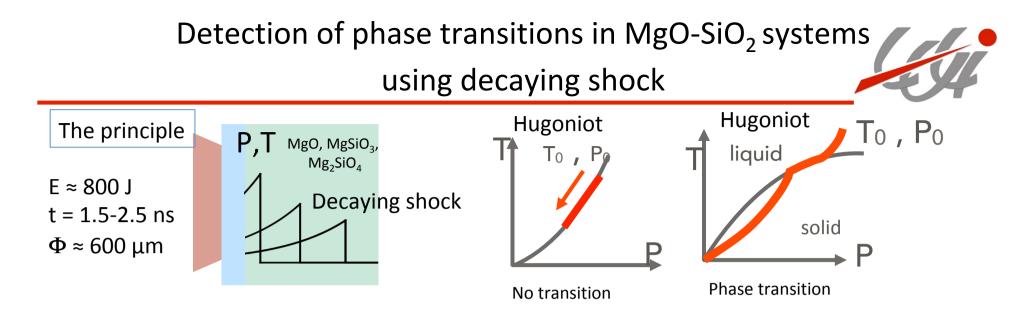
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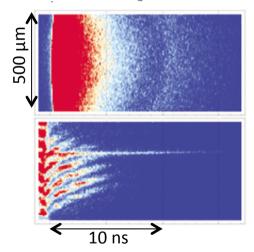
K. Umemoto *et al.*, Science, **311** (2006) Different experimental campaigns:

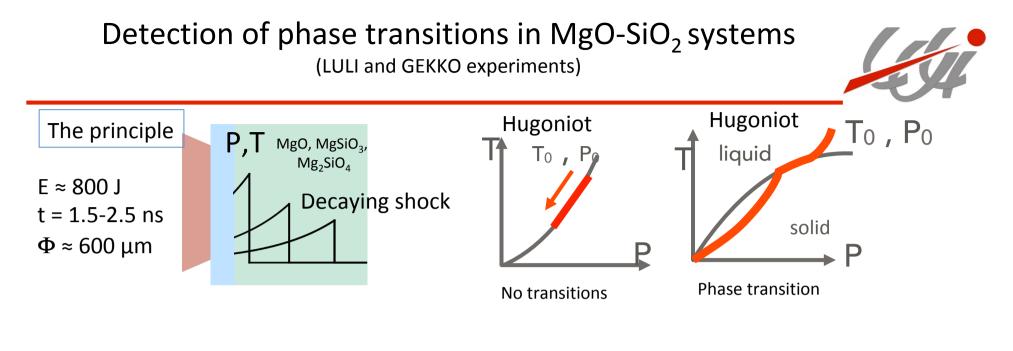
- Detection of phase transitions using decaying shock (LULI and GEKKO)
- Electronic and ionic structural changes using XANES (LULI)
- Phases transitions using X-ray diffraction (recent experiment at LCLS)

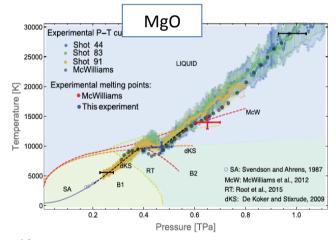




MgO







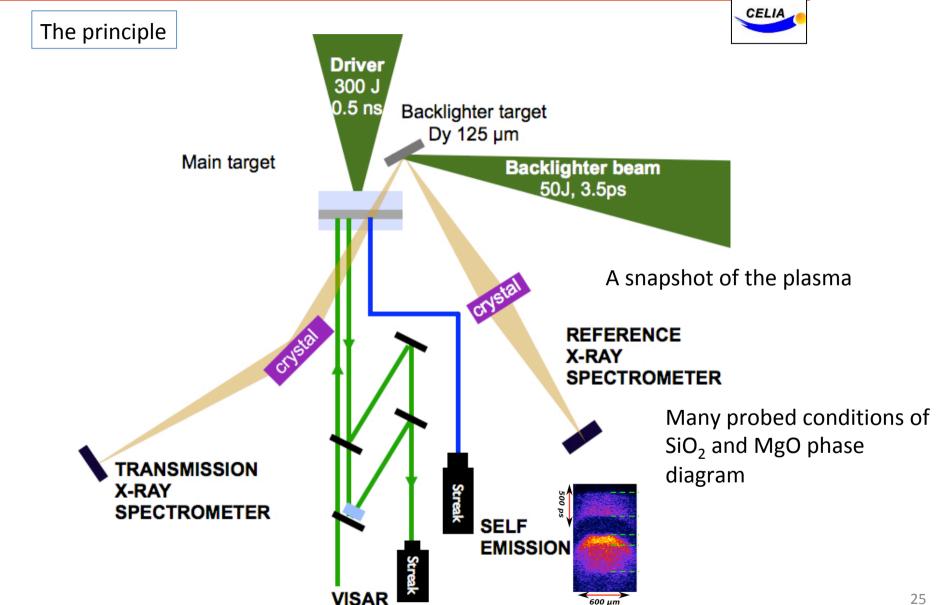
Melting feature at 4.7 Mbar

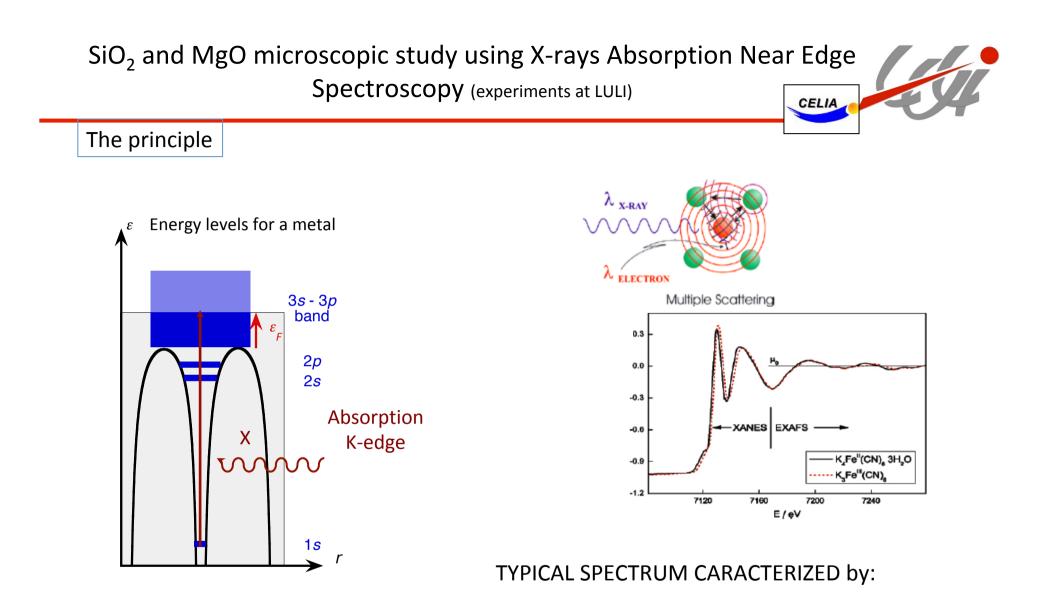
- No other phase transitions
- Existence of a low conducting liquid layer at the mantle

Repercussions for super earth B field

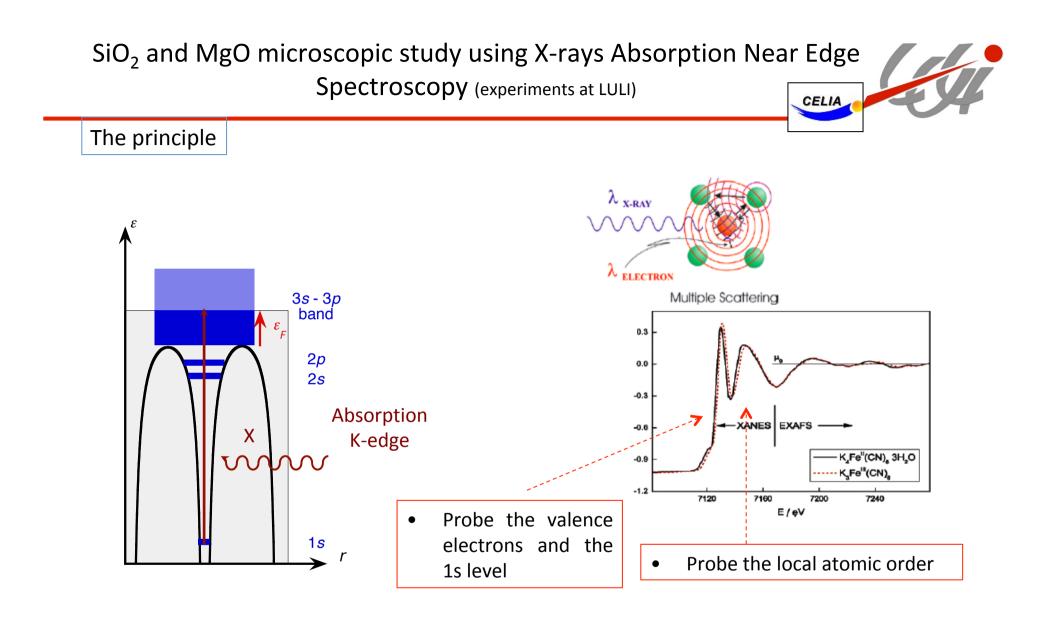
R. Bolis et al. GRL 2016

SiO₂ and MgO microscopic study using X-rays Absorption Near Edge Spectroscopy (experiments at LULI)

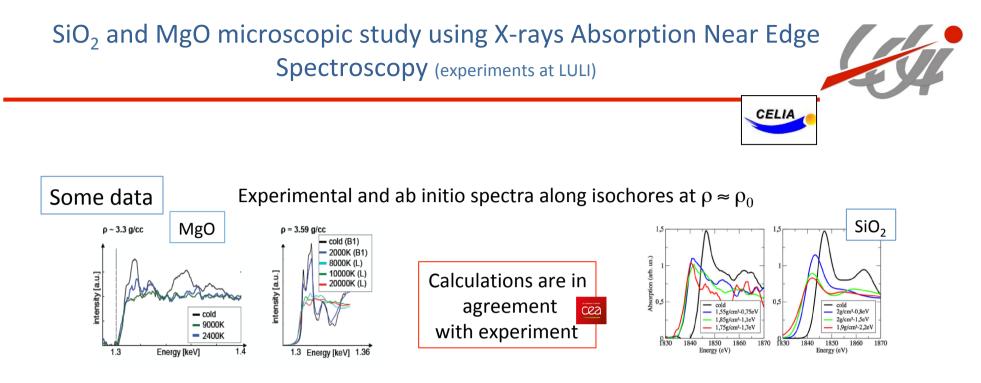




- Absorption edge corresponds to the transition of the photoelectron from the 1s level to the first unoccupied level above the Fermi energy
- Oscillations due to the scattering of the phtoelectron on the neighbouring atoms

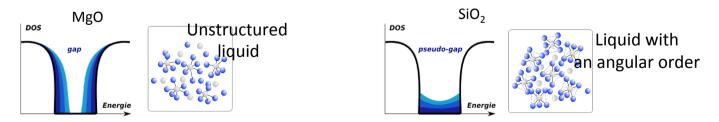


Powerful diagnostic to study both electronic and ionic structure changes, phase transitions and to test directly approximations used in theories



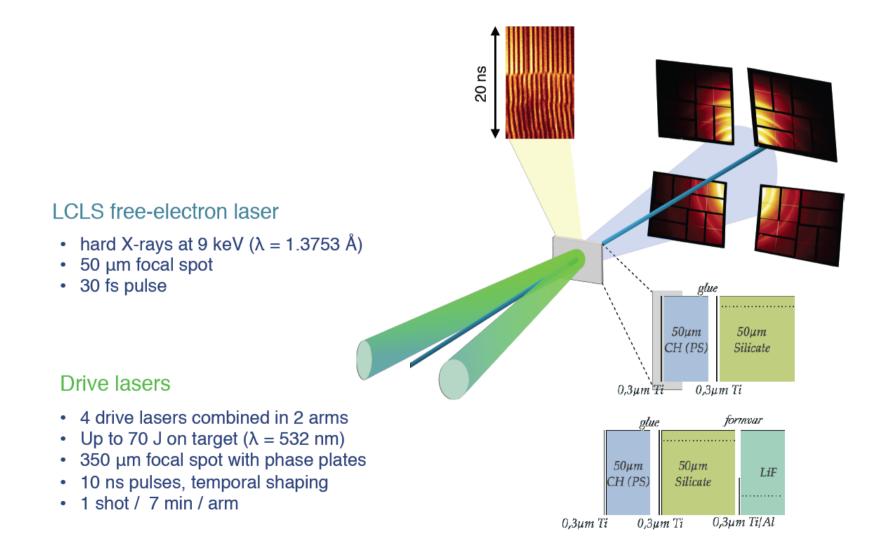
A. Denoeud et al PRL 2014, A. Denoeud et al. PRE 2016, Bolis et al submitted

✓ We were able to get information on the gap closure mechanism and on liquid structures



X-ray diffraction at Linac Coherent Light Source

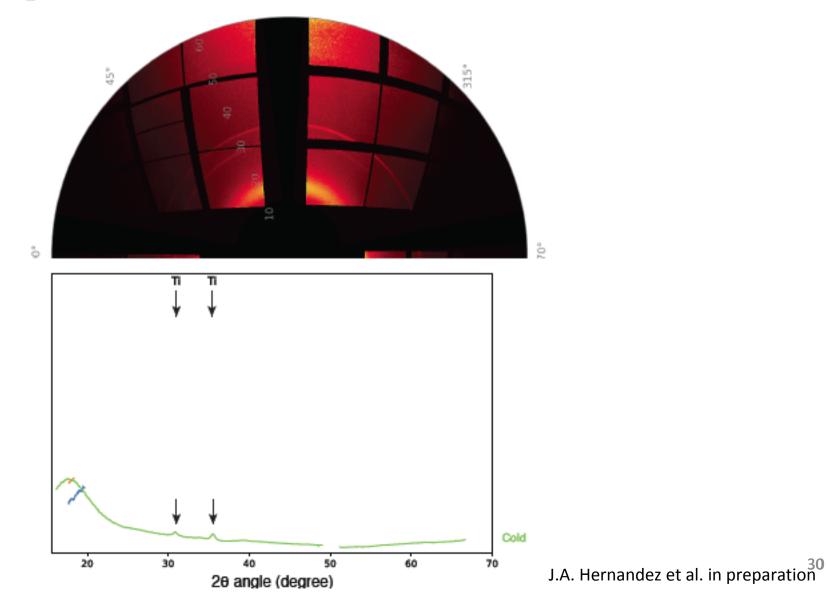




Results on fused silica SiO₂



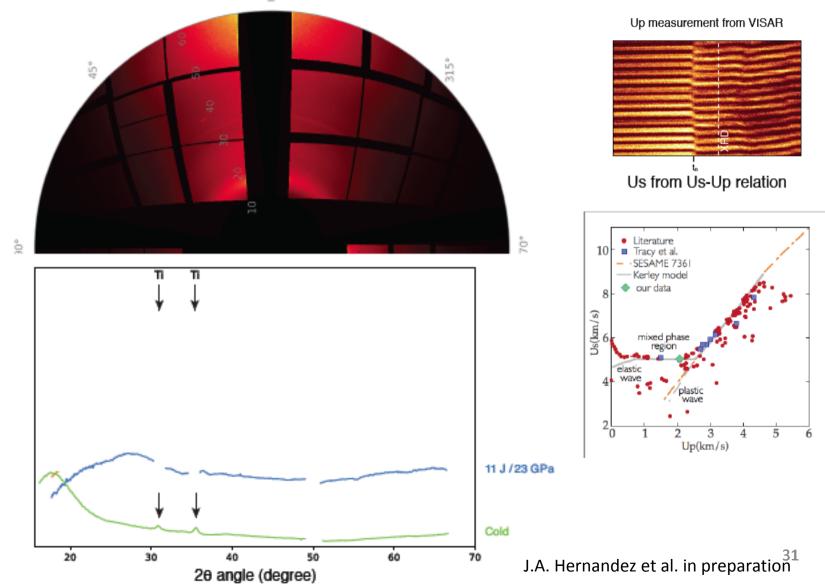
Fused-SiO₂ initially in 4-fold Si-O coordination



Results on fused SiO₂



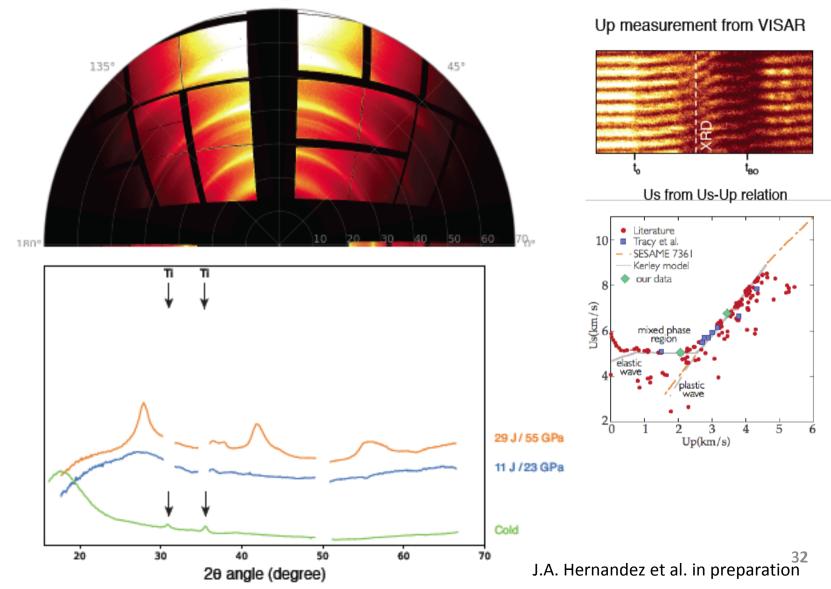
Formation of amorphous phase with 6-fold coordination - 23 GPa - 3.3 ns



Results on fused SiO₂

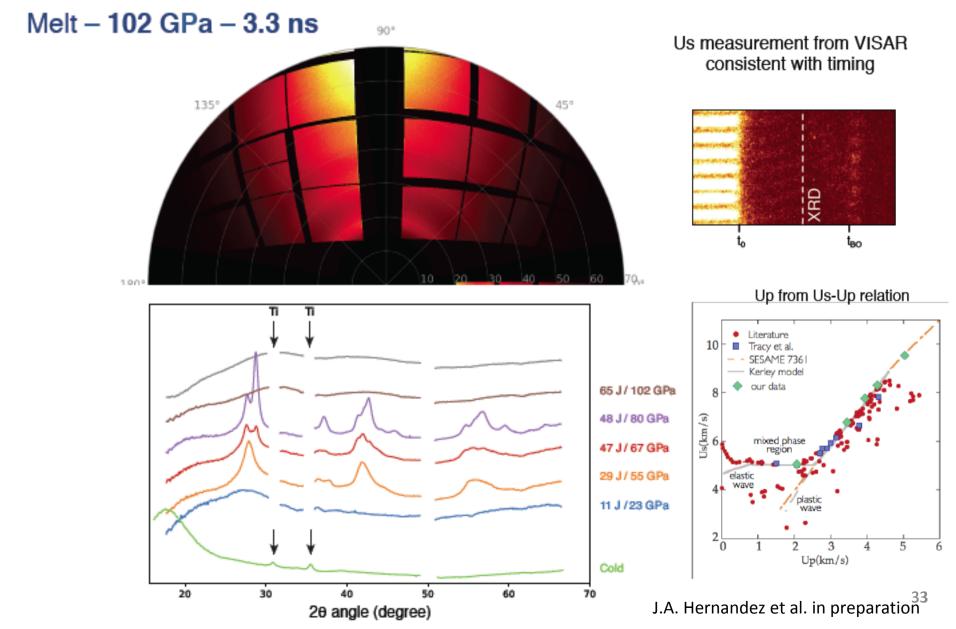


Crystallization of stishovite (TiO2-type structure) - 55 GPa - 4.6 ns



Results on fused SiO₂







Reliable equation of state measurements using a laser shock

Studying phase transition is mandatory : Coupling with X-ray diagnostics -> complex, but very interesting results

Free electron lasers or synchrotron facilities coupled with a nanosecond laser open an opportunity

Collaborators



LULI team: A. Ravasio, J. A. Hernandez, M. Guarguaglini, M. Koenig, A. Denoeud

Laser shock compression community laboratories



Geophysics and astrophysics community





THANK YOU FOR ATTENTION



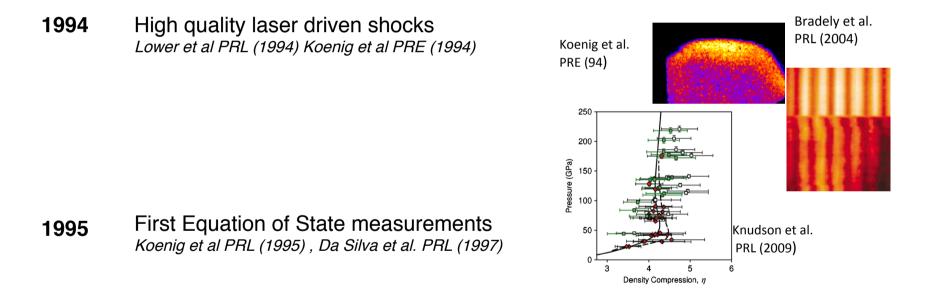
ADDITIONAL SLIDES

High energy density physics definition HEDP P > 1 Mbar (i.e $\rho/\rho_0 > 1$) Extreme matter states log N(H) [m⁻³] 35 20 25 40 SHORT PUL GRB 10 6 Supernova A wide range of physics area progenitors ICF 4 8 log kT [eV] log T [°K] BROWN DWARF SUN P(total)=1Mbar 60 MO 2 Ionized 0 Unionized ACCESSIBLE by NIF & LMJ ACCESSIBLE by LULI2000 -5 0 +5 +10log p [g/cm³] Energy density input \approx energy density at room T **HEDP** Typically: 10⁹ - 10¹¹ J/m³ volume involved in laser target $\approx 10^{-9} \, \text{m}^3$ Easily accessible with a high laser power of a few hundreds J

Experimental state of the art

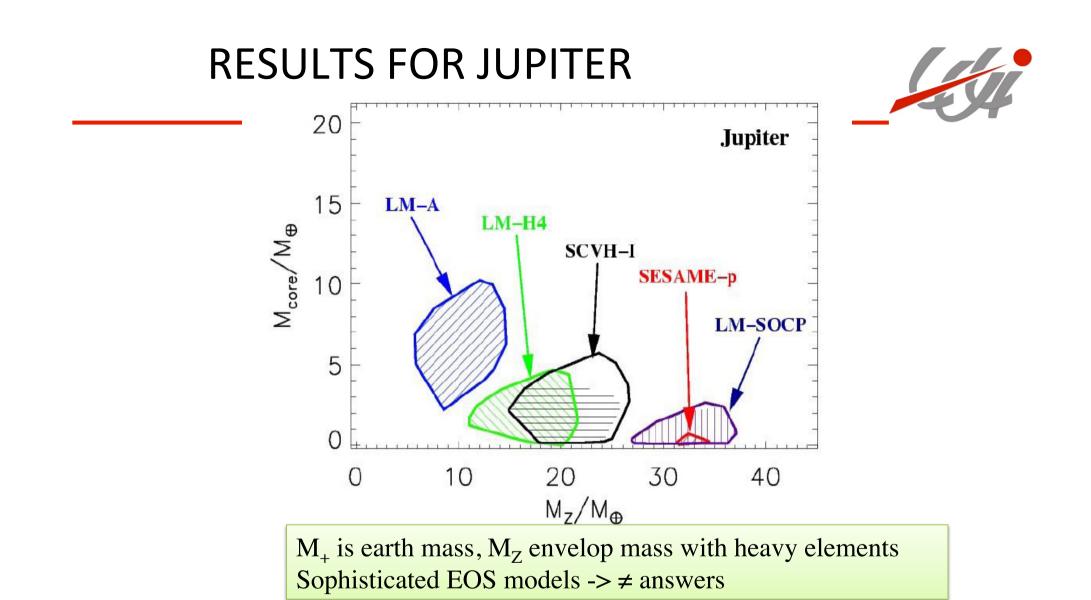


1993 The pressure record of 0.75 Gbar *Cauble et al PRL (1993)*



1996 \rightarrow **today** - Reliable Hugoniot data of interest for planetology

- Macroscopic characterization of WDM (EOS, reflectivity, conductivity, etc...)



•Accretion around solid mass

Core

No core

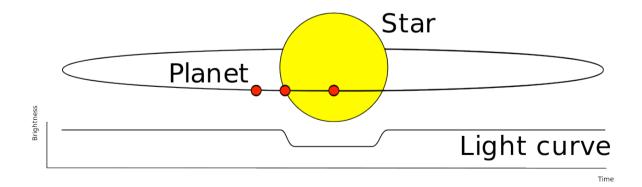
•gravitationnal collapse due to condensation

DETECTION OF EXOPLANETS



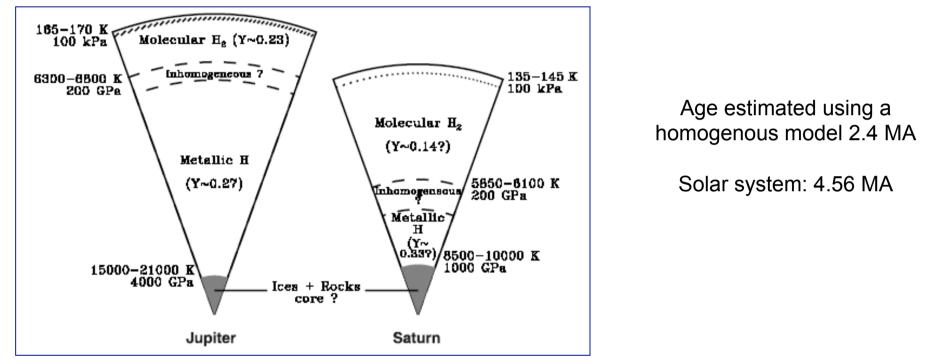
1/ Radial velocity A star with a planet will move in its own small orbit in response to the planet's gravity. The radial velocity can be deduced from the displacement in the parent star's spectral lines due to the Doppler effect.

2/ Transit photometry Radius





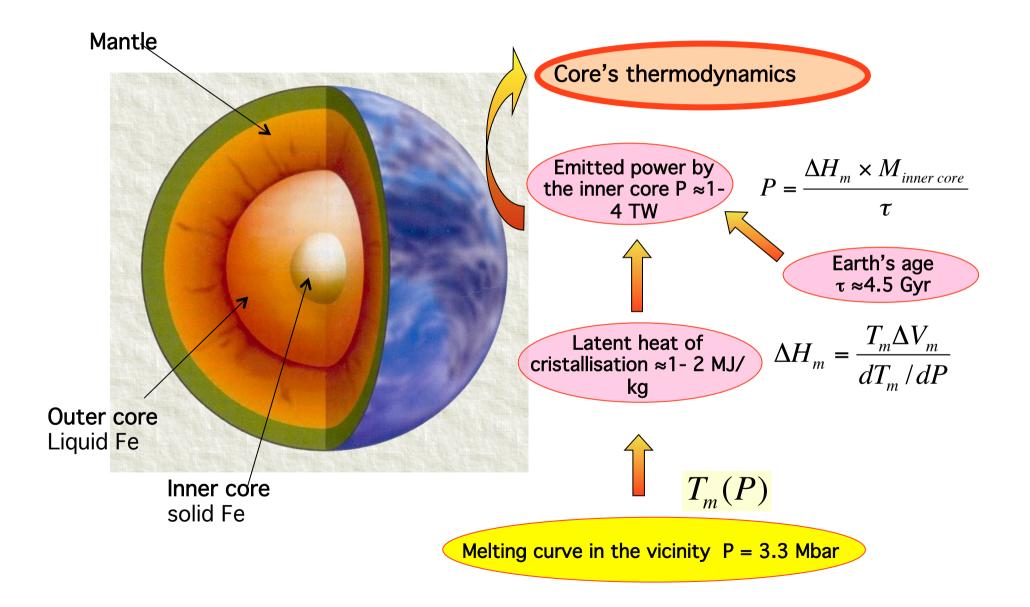
Saturn is too bright

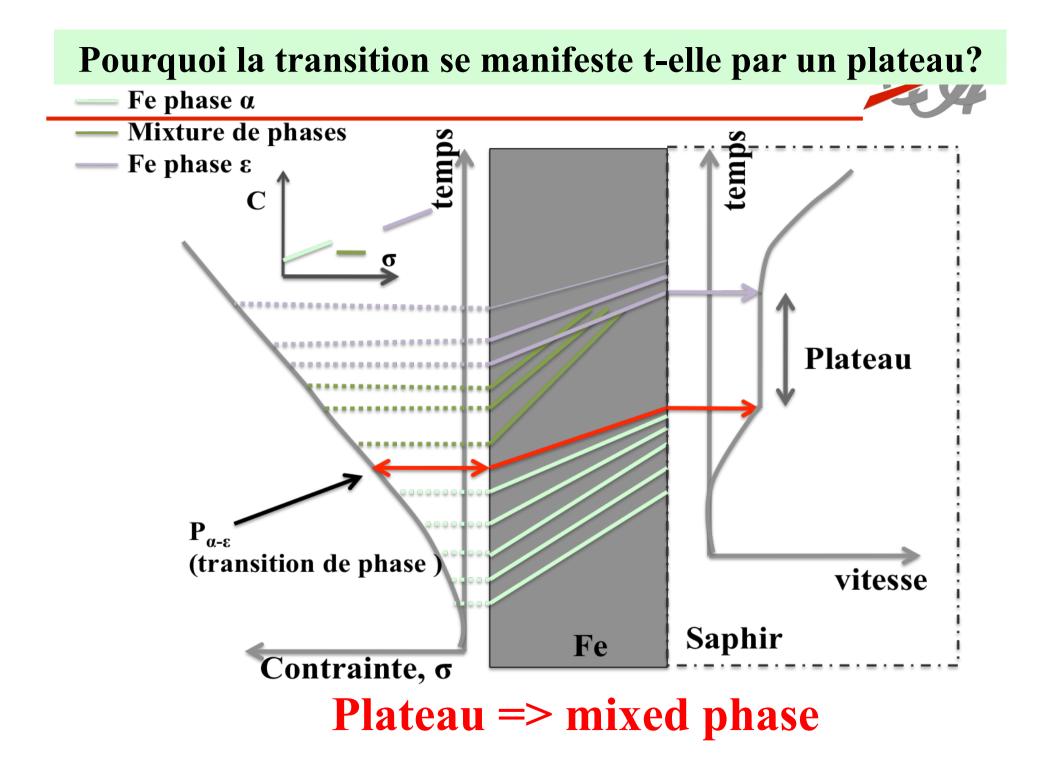


•Problem of miscibility of He-H?

Saturn could generate some of its heat through the "raining out" of droplets of helium deep in its interior. As the droplets descend through the lower-density hydrogen, the process releases heat.

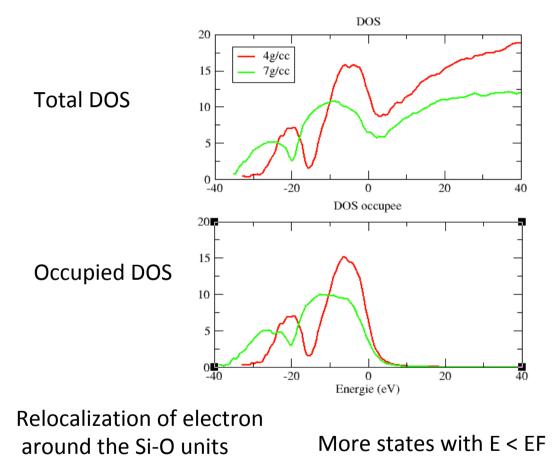
Our comprehension of the Earth's interior depends upon the EOS of iron





MODIFICATION OF THE DENSITY of STATES for the LIQUID

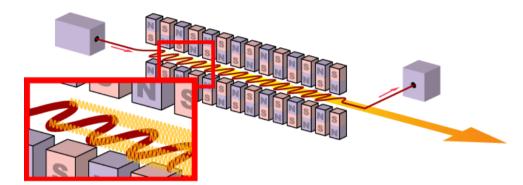
SiO2 along the isotherm at 1 eV



Less free electrons \rightarrow conductivity \succ

XFEL principle

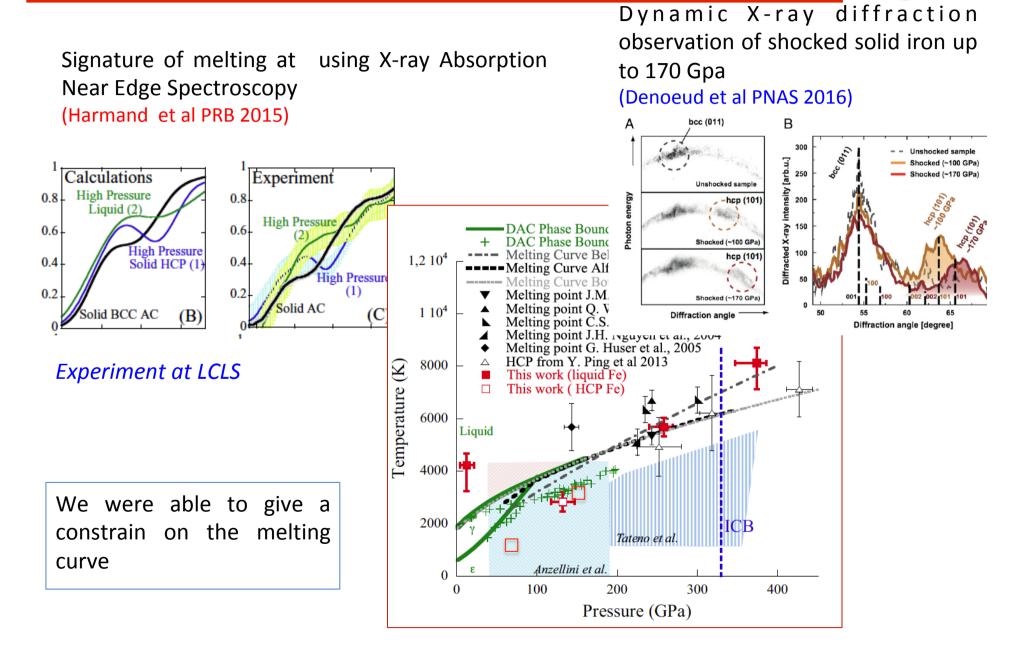




To create an FEL, a beam of electrons is accelerated to almost the speed of light. The beam passes through an undulator, a side to side magnetic field produced by a periodic arrangement of magnets with alternating poles across the beam path.

Self Amplified Spontaneous Emission \rightarrow Stochastic process \rightarrow spectral fluctuations



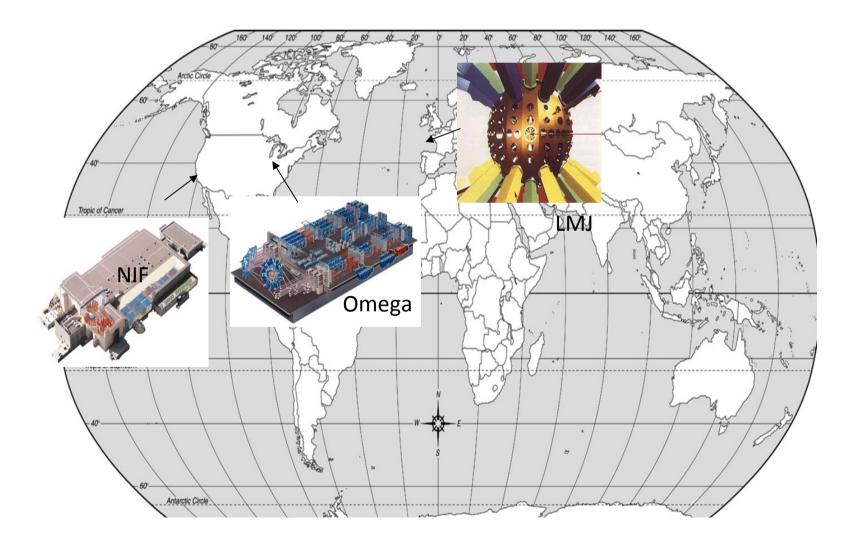


2 ACADEMIC HIGH POWER LASERS E>2 kJ

Nanosecond pulses (10⁻⁹ s) Up to MJ energy

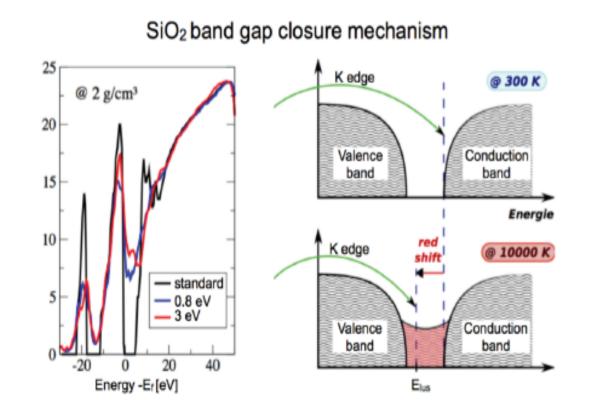


Short Pulse \geq 1 to 4 kJ 1 ps







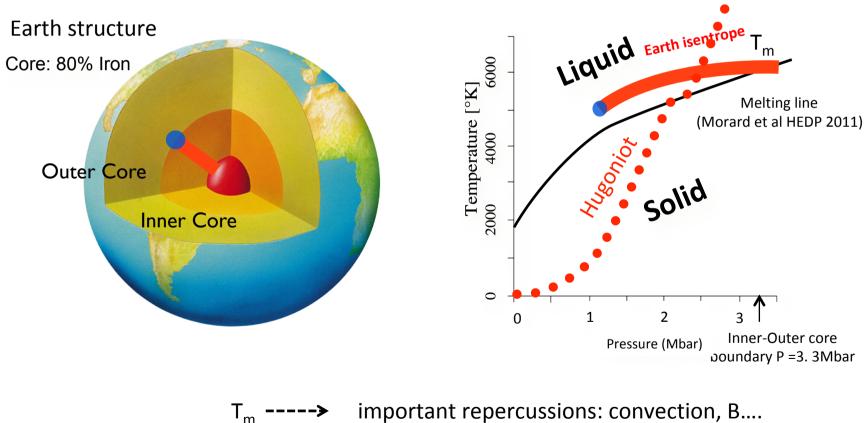


Why do we need to develop quasi-isentropic compression?



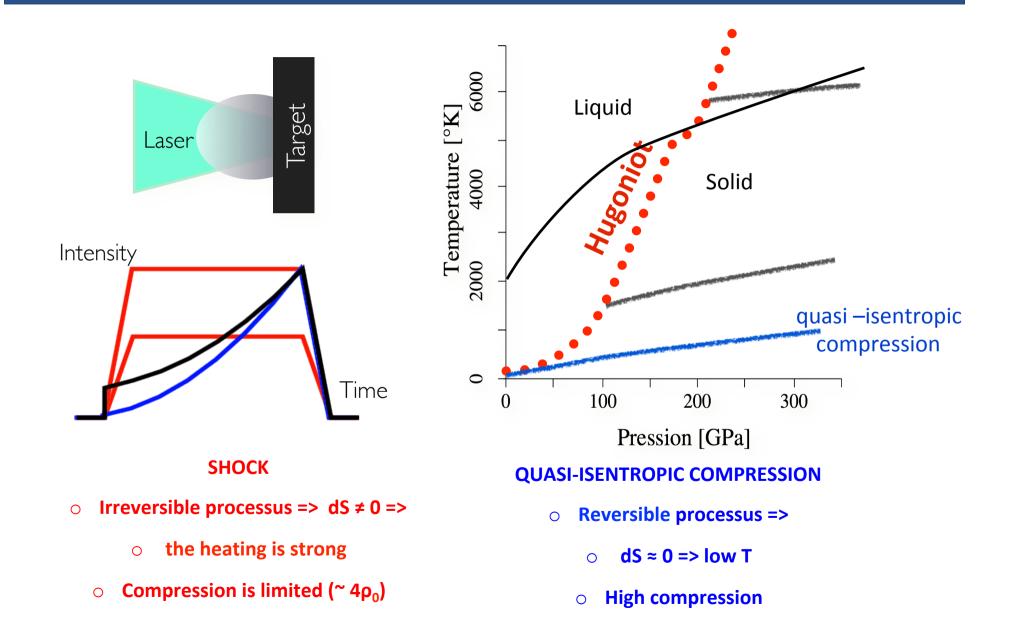
To get closer to planetary isentropes

e.g. : the case of iron



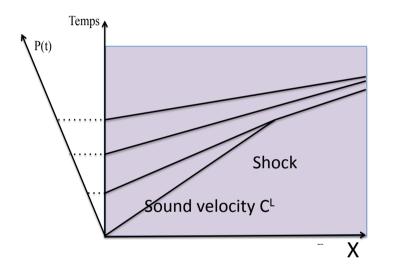
The melting curve $T_m(P)$ has been recently calculated ----> Experimental validation

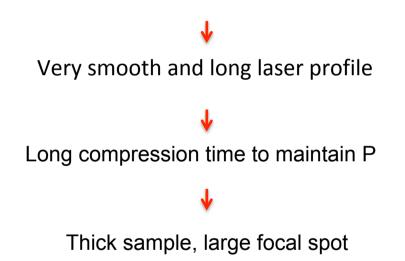
Shock compression versus quasi isentropic compression



The critical points for quasi-isentropic compression

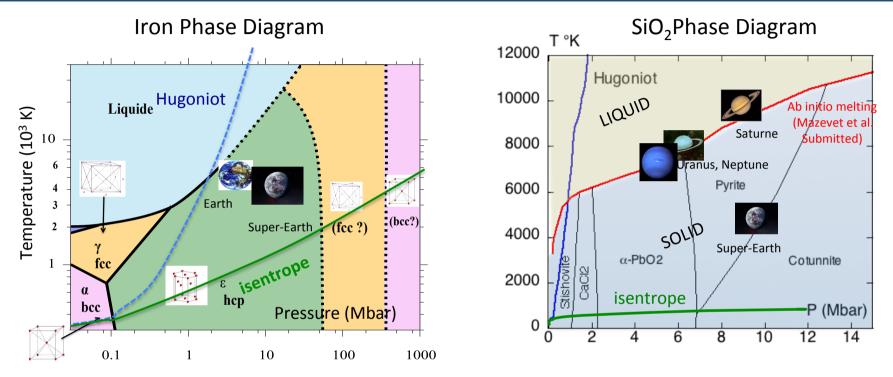
Generation of a sequence of small compressions waves but multi Mbar pressures must be reached





A multi-kJ laser is necessary to achieve P > 10 Mbar

Experiments at LIL in Bordeaux on iron and SiO₂ (the most energetic European laser)



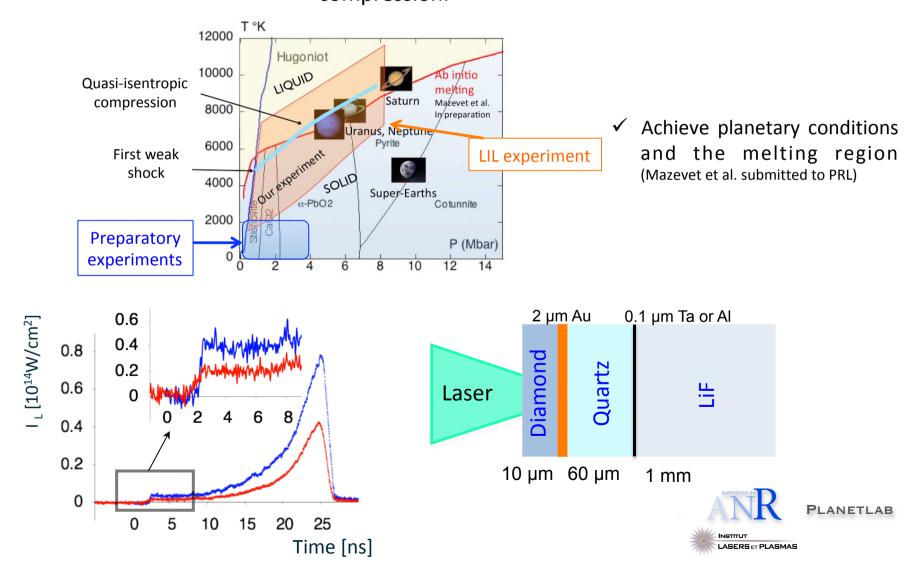
Phase diagrams based on ab initio simulations (Morard 2011, Mazevet submitted, Sitxrude 2012)

The main goal: to reach Super-Earth and giant planets conditions and to investigate region around the melting



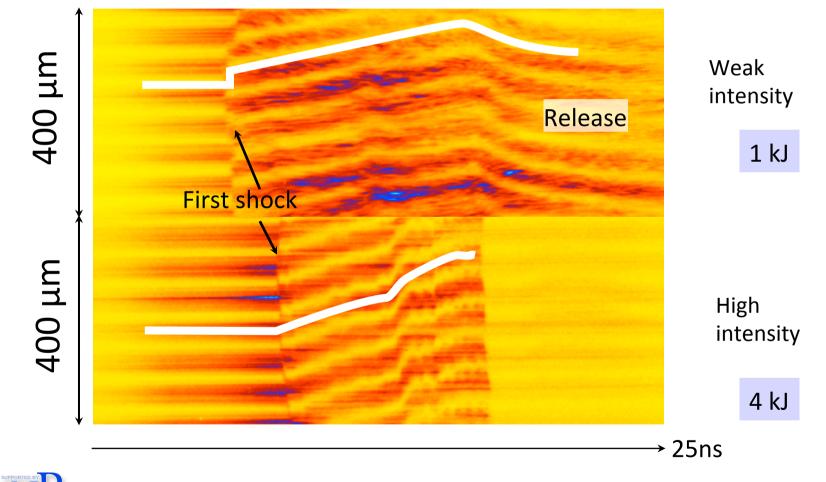
Campaign at LIL: goal and principle

Novel technique coupling a *well-controlled* shock followed by a quasi-isentropic compression.

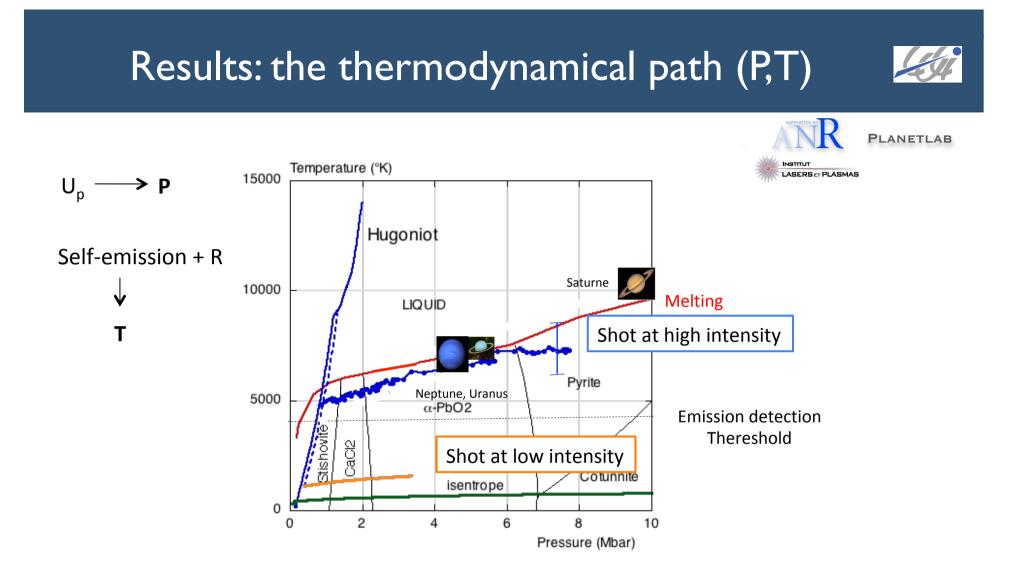


VISAR images



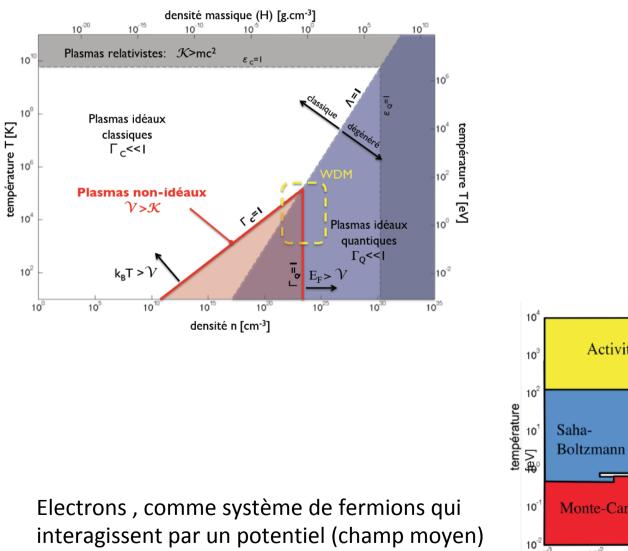


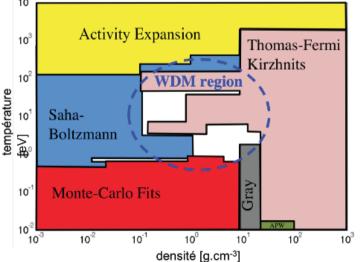




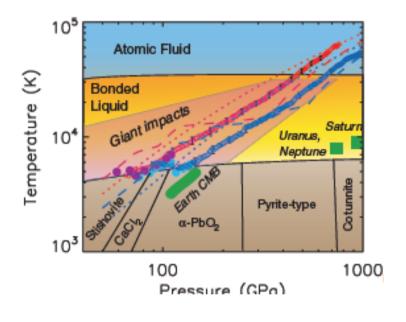
Modèles théoriques











Specific heat capacity deduced by the slope of Hugoniot T

C_v increases above melting

C_v shows a broad peak (yellow region)

Energy required to break all chemical bonds

For higher T (blue region) : bond breaking is essentially complete

Yellow region: « bonded liquid »= liquid containing a mixture of variously sized polymerized structural units

Blue region: « atomic fluid » = no anymore chemical bonds

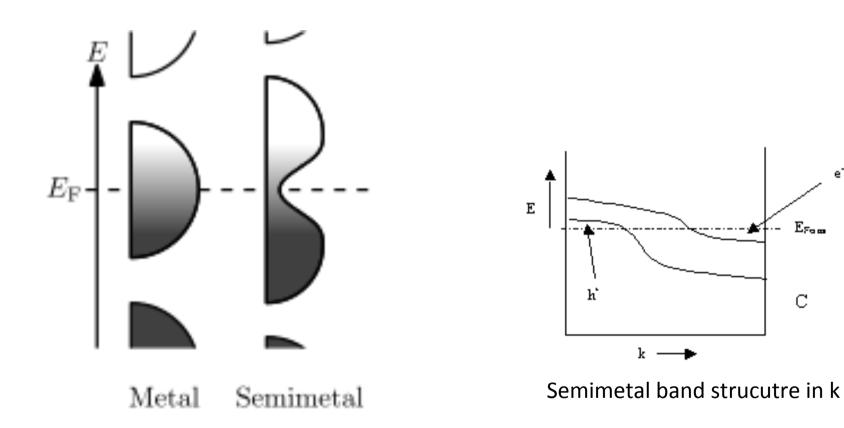


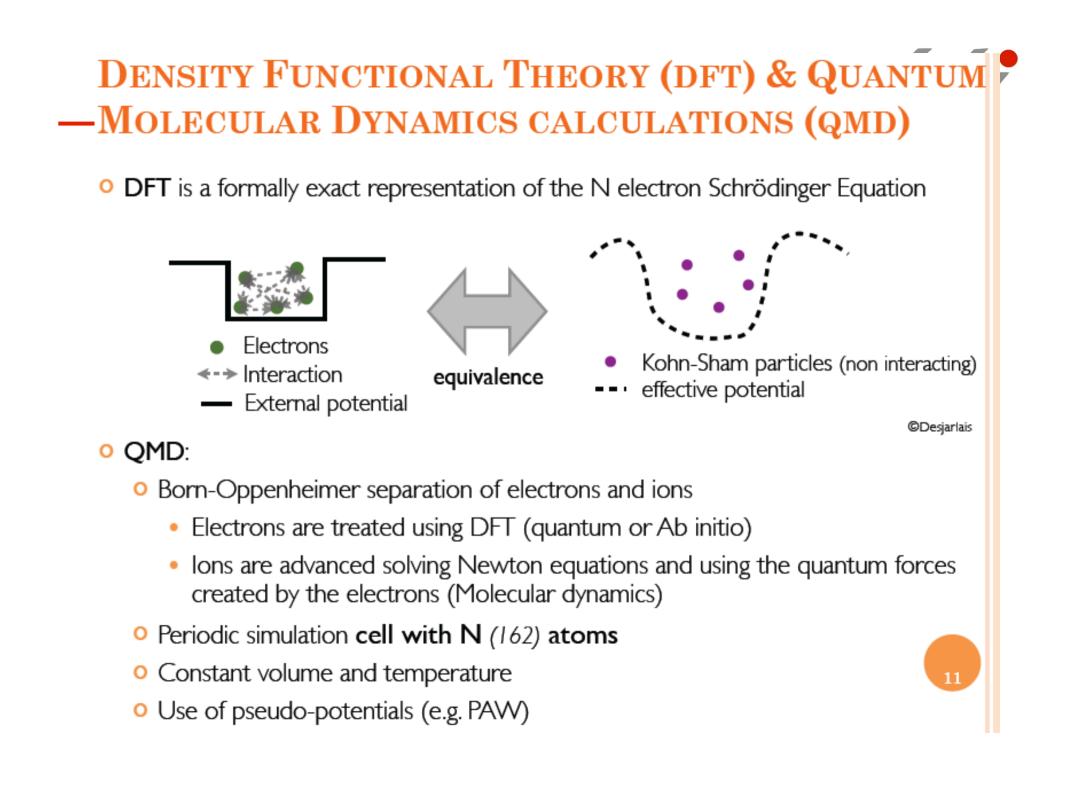
e'

Егаш

С

CONDUCTION BAND STRUCTURE for a METAL and SEMIMETAL







Density Functional Theory

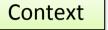
Any property of a system of many interacting particles can be viewed as a functional of the ground state density $n_0(r)$

"Kohn-Sham" theory

It replaces the original many body problem by an auxiliary independent particle problem, which evolves in an external potential

External effectif potential V^{ee} (n(r)) V^{ee} (n(r)) V^{ee} (n(r)) V^{ee} (n(r)) V^{ee} depends on the System state on r V^{ee} (n(r))

XANES as a melting diagnostic for Fe (experiment at LCLS)

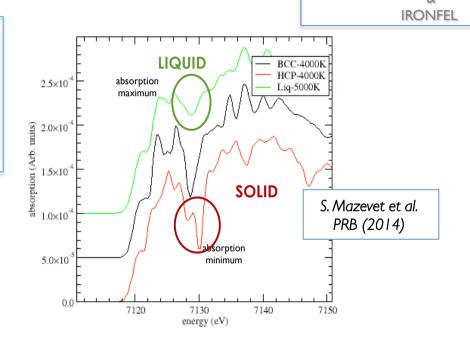


Detection of iron melting at high pressures (geophysics)



PLANETLAB

- Ab initio calculations suggest XANES as a structural diagnostic for iron at planet cores conditions, including melting
- Disappearance of the deep absorption minimum

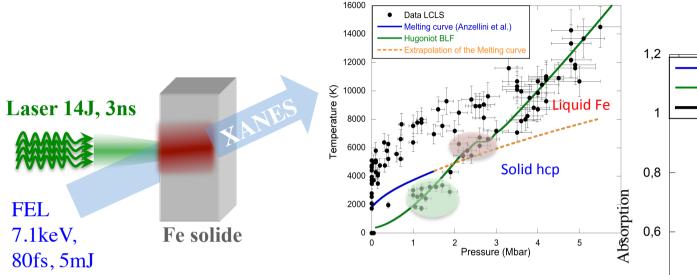


Requirements -> Fe K-edge @ ~ 7.1 keV

- Need a broad band, intense, short source ≈ 7 keV ⇒ not achieved with UHI lasers
- need a huge amount of energy to create the X-ray source (Yaakobi et al. 2003, Ping et al. PRL 2013).
- Alternative approach \Rightarrow XFEL

Some results

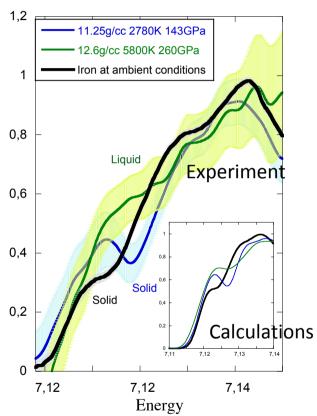


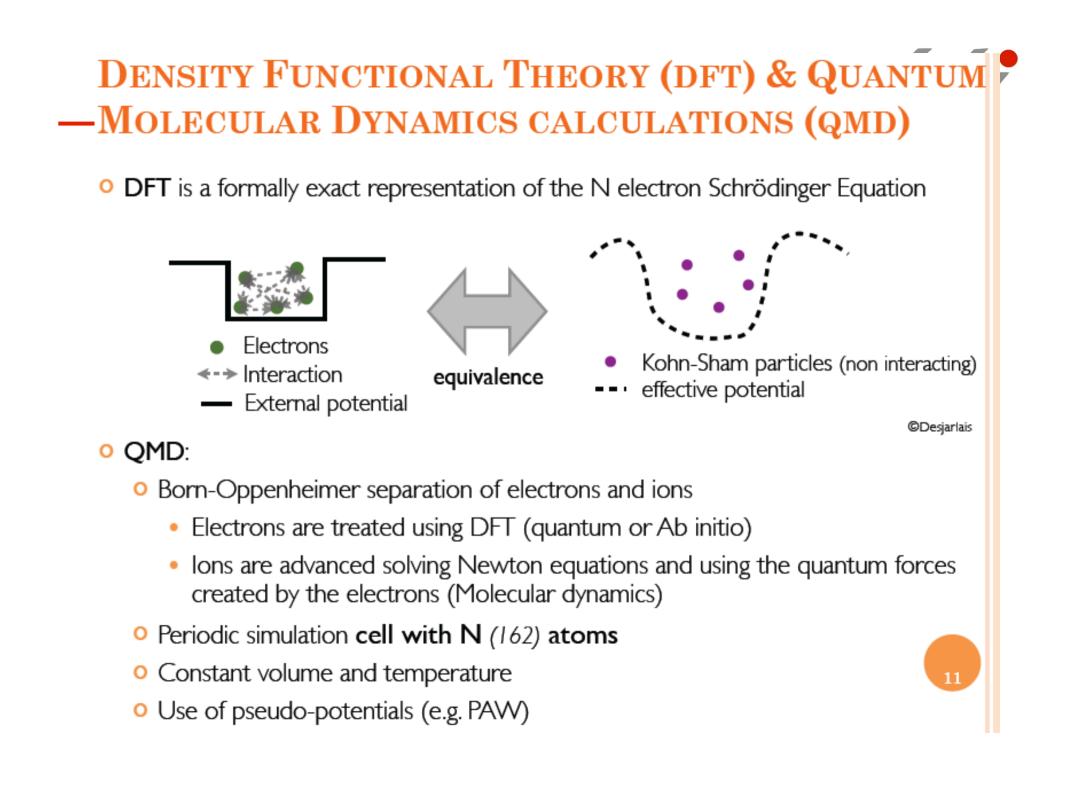


Good agreement between experiments and calculations for the evolution of the spectra (cold bcc/compressed hcp/compressed liquid)

Data confirm that XANES is a good diagnostic to constrain the melting (Harmand & Ravasio et al in preparation)

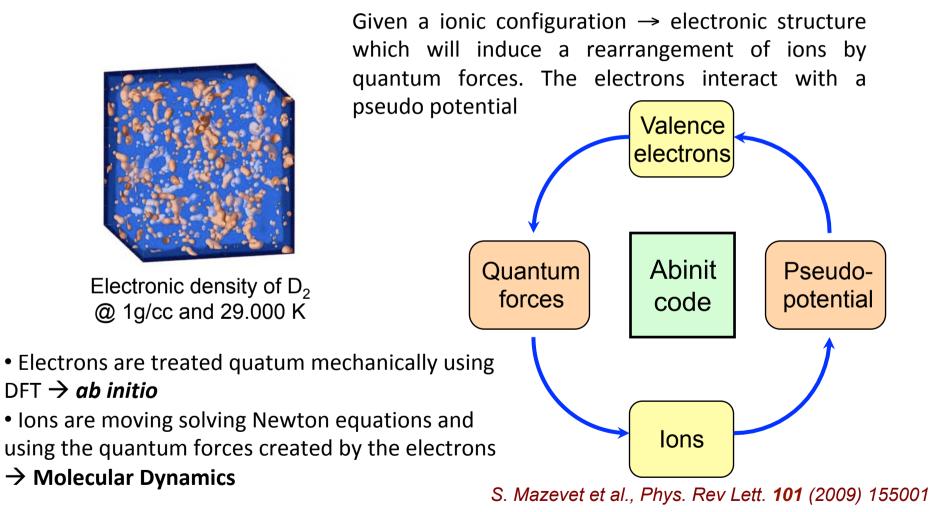
Planetlab & IRONFEL





Quantum Molecular Dynamics calculations

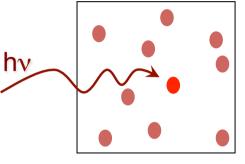
- Principle :
 - atoms are set in a cubic box with periodic limit conditions.



- Assumptions :
 - the number of atoms is fixed.
 - the simulation box size is calculated in order to reproduced the density.
 - the number of energy level calculated is fixed.
 - electrons are treated by quantum mechanics using the Density Functional Theory (DFT).
 - the ions motion is deduced from Newton equations using quantum forces created by electrons.
 - finite temperature DFT : occupations are given by Fermi-Dirac distribution.
 - PAW (Projector Augmented Wave) formalism : interaction between the valence electrons and core electrons + nucleus
 - absorption spectra are calculated applying the linear response theory(Kubo-Grenwhood formulation) and with the impurity model : the absorbing atom is in an excited configuration with 1 hole in the 1s level (the core hole has an infinite life time).

Frozen core approximation: the core electrons are frozen

Quantum Molecular Dynamics calculations (2)









2 types of electrons :

-core electrons \rightarrow the core electronic wavefunctions $\phi_i(r)$ (isolated atomic wavefunction) are obtained using DFT valence electrons \rightarrow the true wavefunctions are replaced by pseudo-wavefunctions for r < R_{PAW} ~

- the pseudo-wavefunction satisfy $\phi_i(r) = \tilde{\phi}_i(r)$ for r > R_{PAW}

The **real valence wavefunction** is **known**, even in the core region, and related to the pseudo-wavefunction by a linear

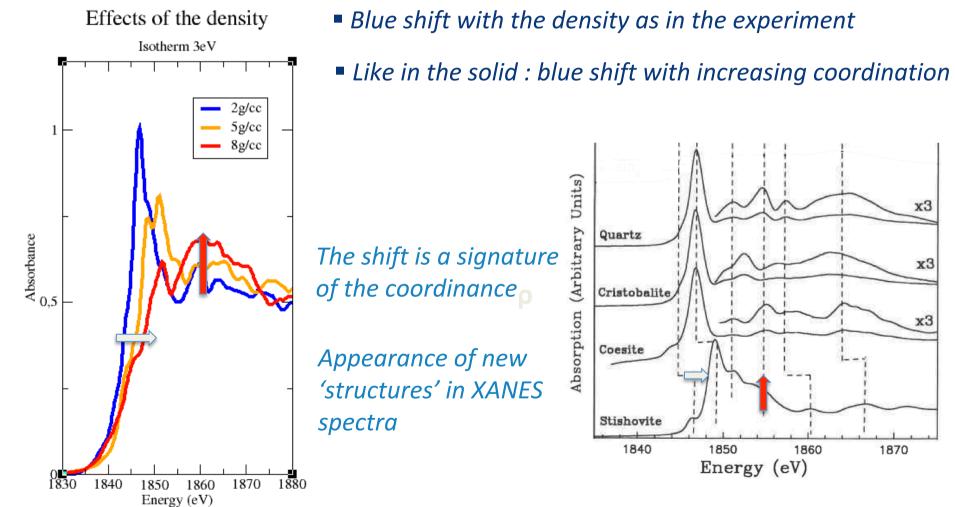
operator

$$\begin{aligned}
\psi_{i,k} = (\tilde{\psi}_{i,k}) + \sum_{R,n} (\phi_{R,n}) - (\tilde{\phi}_{R,n}) \langle \tilde{p}_{R,n} | \tilde{\psi}_{i,k} \rangle \\
\\
\mathsf{R}_{\mathsf{paw}} = (\tilde{\psi}_{i,k}) + (\tilde{\psi}_{i,k}) + (\tilde{\psi}_{i,k}) - (\tilde{\psi}_{i,k}) \rangle \\
\end{aligned}$$

→ PAW calculations are equivalent to all-electrons calculations

Variations in density...



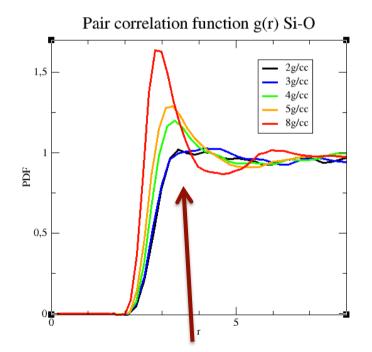


Synchrotron data : Li et al, American Mineralogist 79, 622-632 (1994)

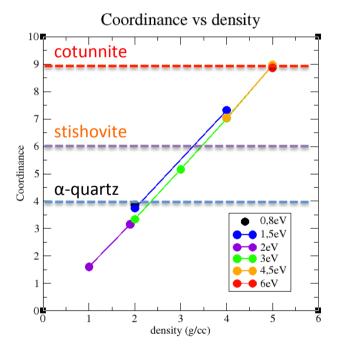
... as a signature of structuring

> An explanation : the structuring of the liquid

Liquid seems to follow the coordinance of the solid phases



• Pair correlation function shows a highly structured liquid for higher densities

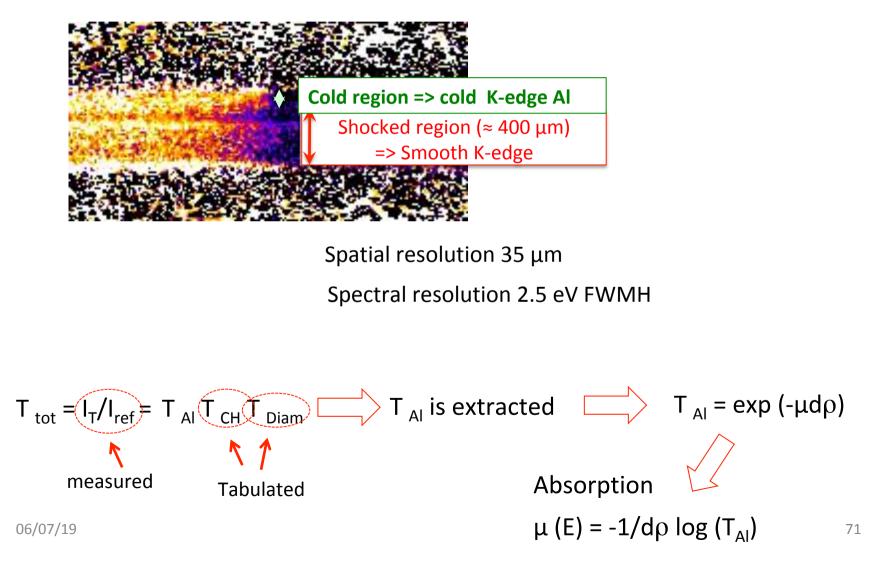


• Coordination increases with density. Up to... highly structured liquid

Typical image and methodology



transmitted/reference spectrum

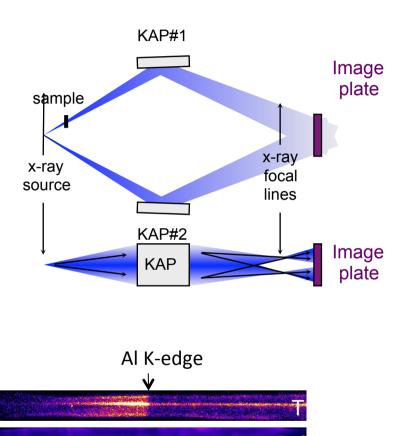


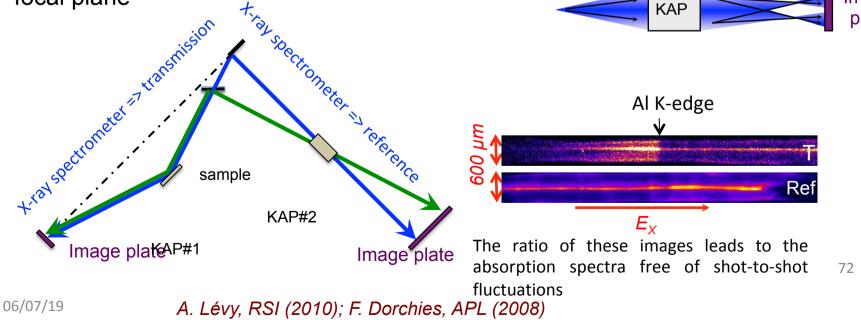
Method for X-ray Absorption Spectroscopy



- Two X-ray spectrometers (KAP conical crystals)
 - Spectral & spatial resolution
 - Free of shot-to-shot X-ray fluctuations
 - Monitoring & correction of the emission from the ablator

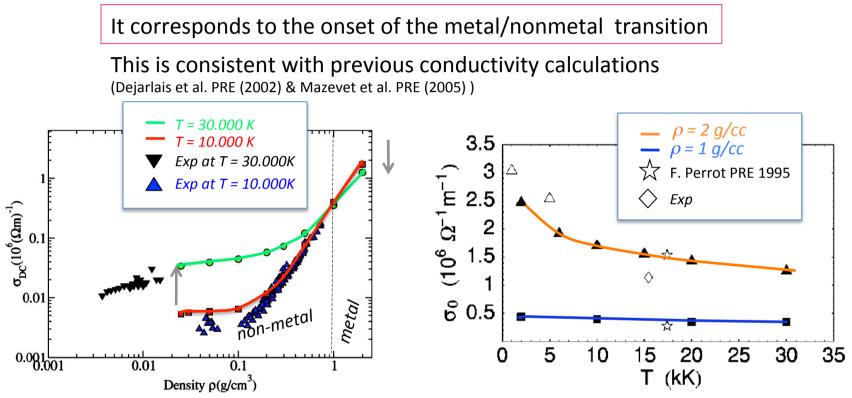
Indeed we had spatial resolution by using a point projection geometry, by putting the Image plate away from the focal plane







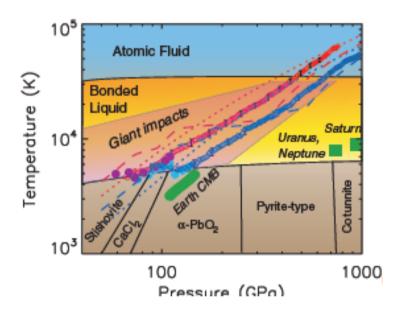
What does this re-localization correspond to?



At $\approx 1 \text{ g/cc}$, the *ab initio* conductivity behavior switches from metal to non-metal. For temperatures in the range up to 30.000 K At $\rho < 1 \text{ gr/cc}$ conductivity increases with T At $\rho > 1 \text{ gr/cc}$ conductivity decreases with T



One scenario for SiO₂ (Hicks et al. PRL 2006)



Specific heat capacity deduced by the slope of Hugoniot T

C_v increases above melting

C_v shows a broad peak (yellow region)

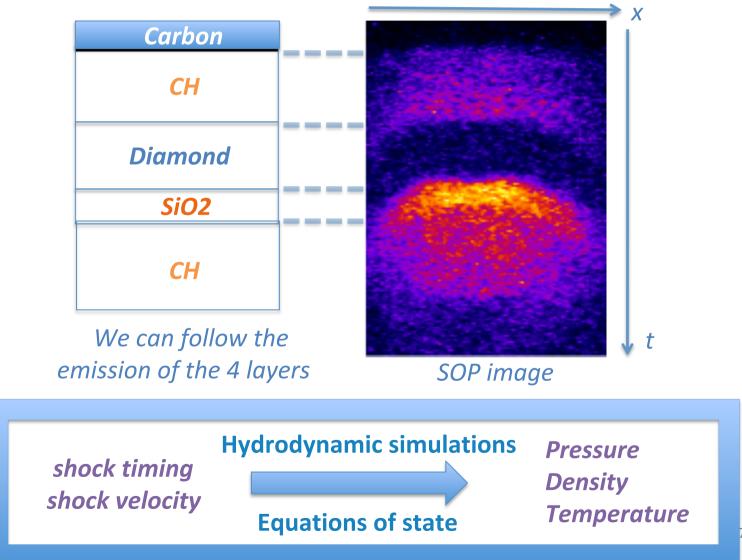
Energy required to break all chemical bonds

For higher T (blue region) : bond breaking is essentially complete

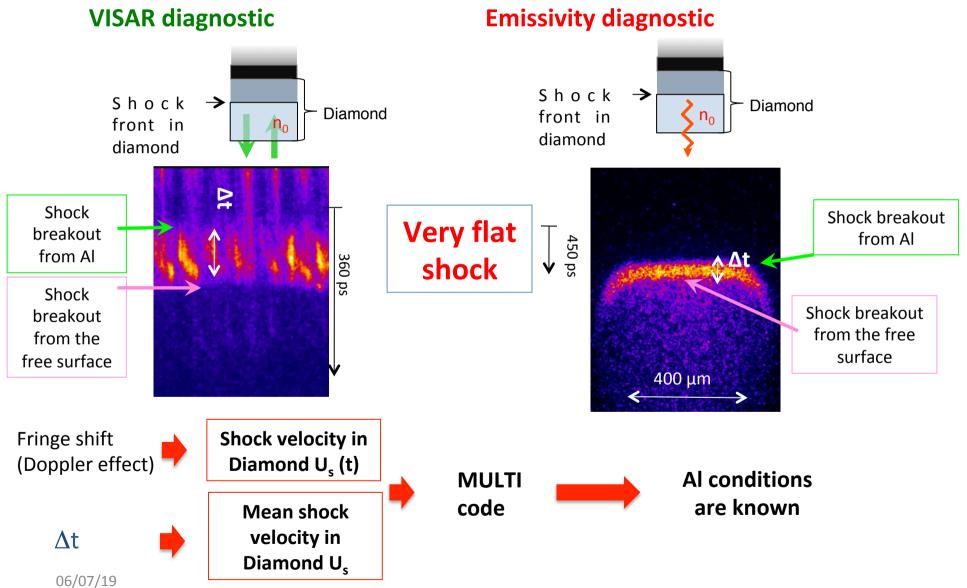
Yellow region: « bonded liquid »= liquid containing a mixture of variously sized polymerized structural units

Blue region: « atomic fluid » = no anymore chemical bonds

Determination of the probed conditions



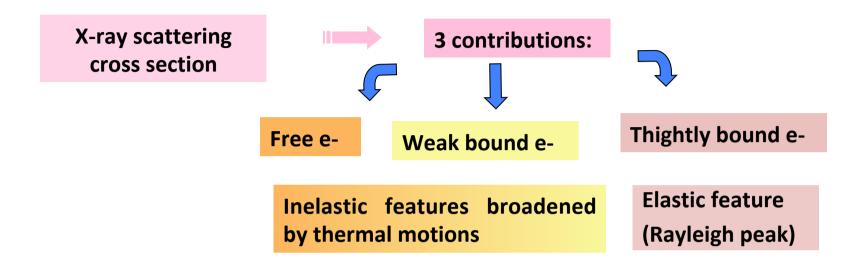
Al plasma parameters deduced from rear side diagnostics



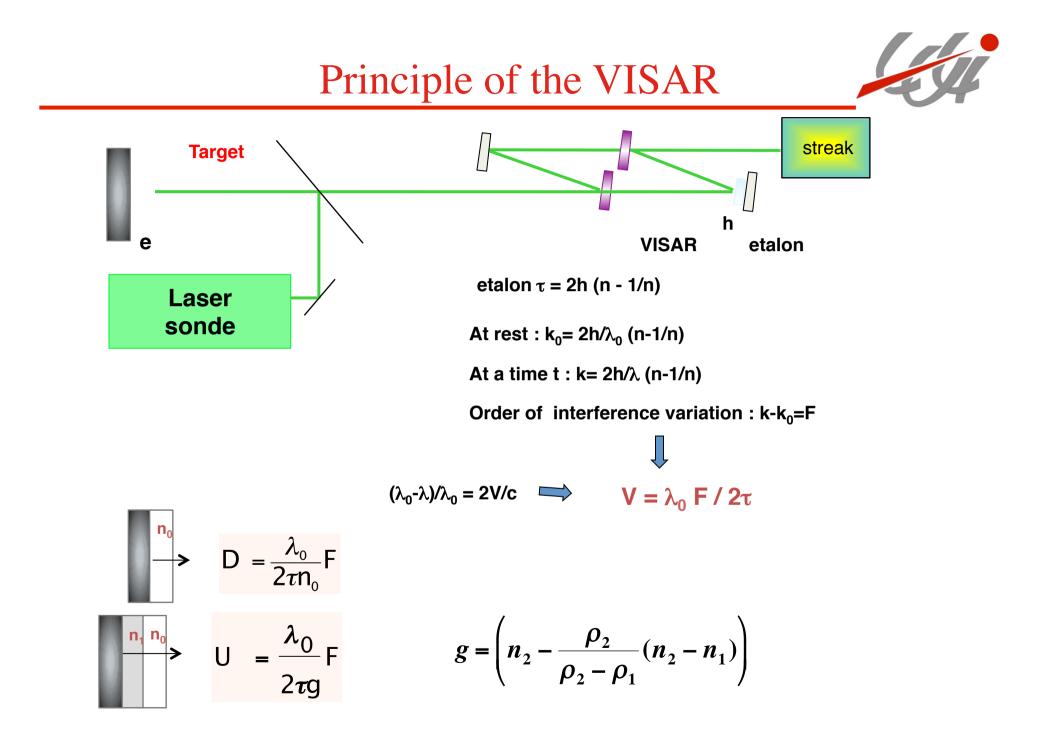
A. Benuzzi-Mounaix, submitted for publication76

Generalities





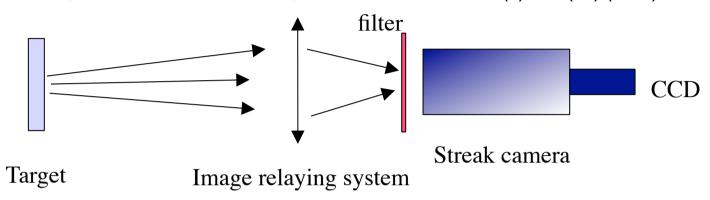
Two regimesScattering parameter $\alpha = \lambda_p / \lambda_s$ $\lambda_p = \lambda_0 / (2 \sin(\theta/2))$ λ_s is screening length
 λ_p is probe wavelengthIf λ_p is < λ_s i.e. $\alpha < 1$ Non Collective regimeScattering on electronsIf λ_p is > λ_s i.e. $\alpha > 1$ Collective regimeAlso scattering on electronic wave



T measurement



Temperature T_b is is corrected to a grey body with the absorption coefficient a = 1 - R, (R measured at 532 nm). a (λ) = a (λ 0) (λ 0/ λ)^{1/2}



$$\Omega$$
 = Solid angle
N=Counts on CCD

$$=\frac{S\Omega\Delta t}{k}\int_{\lambda\lambda}B(\lambda,T_{b})T(\lambda)r(\lambda)d\lambda$$

B = blackbody radiance

T= spectral reponse of the optycal system

r=spectral reponse of the photocatode

K(J/counts) = energy response (streak+CCD)

N

 $\Delta \tau =$ pixell exposure time

We measure r,K and T by using a spectral Lamp (Optics Lab OL5500)

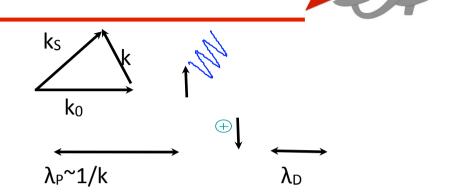
We know $N=f(T_b)$

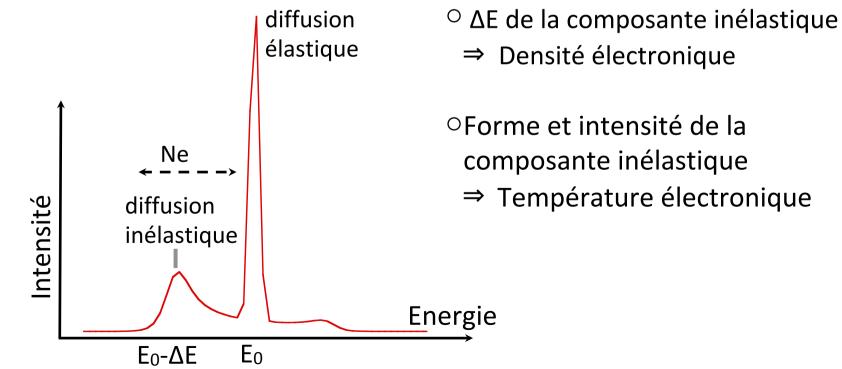
Principe de la mesure

Régime collectif: $\alpha = 1/k\lambda_D \ge 1$

Diffusion a lieu sur les ondes du plasma (plasmon)

spectre diffusé est représentatif des propriétés collectives du plasma



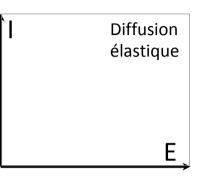


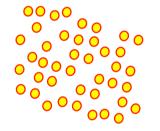
Effets des corrélations

 $n\lambda = 2dsin\theta_{B}$

○ le solide a une structure ionique
 bien définie (réseaux) Гіі→∞

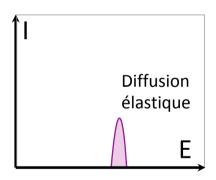
diffusion est déterminée par la loi de Bragg
il n'y a pas de diffusion en dehors de l'angle de Bragg

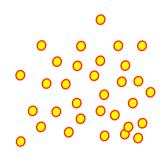




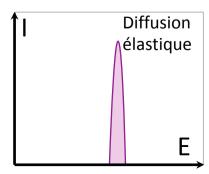
O un ordre à longue portée apparaît dans le plasma Fii>1

- il y a diffusion en dehors de l'angle de Bragg mais moins intense



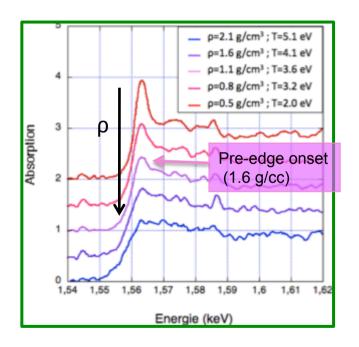


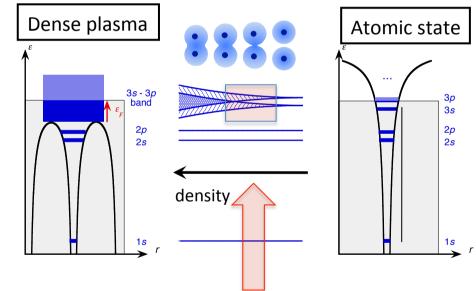
- O plasma non corrélé n'a pas de structure définie Fii<1</p>
- diffusion est possible aussi en dehors de l'angle de Bragg



Study of electronic structure changes in a large WDM

Low compression regime



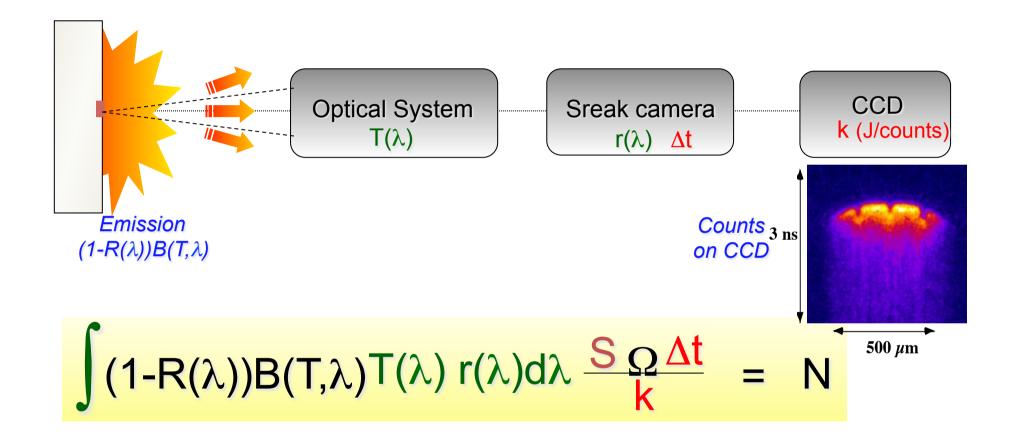


The pre-edge corresponds to the re-localization of the 3p state preceding the formation of the bound atomic states

It corresponds to the onset of the metal/nonmetal transition







Full Calibration of the diagnostic leads to the shock temperature

Internal structure



Internal structure is govern by an equilibrium between pressure and gravity (hydrostatic) (velocities due to matter movements are negligible)

$$\nabla P = \rho \nabla (V + Q)$$

P is pressure and V & Q gravitational & centrifugal potentials For giant planets Q \approx 0.1 V. Rotation of Jupiter is 10 h (very high)

$$V(\vec{r}) = G \int \frac{\rho(\vec{r})}{|\vec{r} - \vec{r}'|} d^3 \vec{r}$$
$$Q(\vec{r}) = \frac{1}{2} \omega^2 r^2 \sin^2 \theta$$

r is the radius with origin at the centre of the planet, θ the angle with respect to the rotation axis, & ω the rotation frequency at point r. if Q=0, we have the simple equation dP/dr=- ρ

Another equation is needed to get the temperature as a function of pressure



