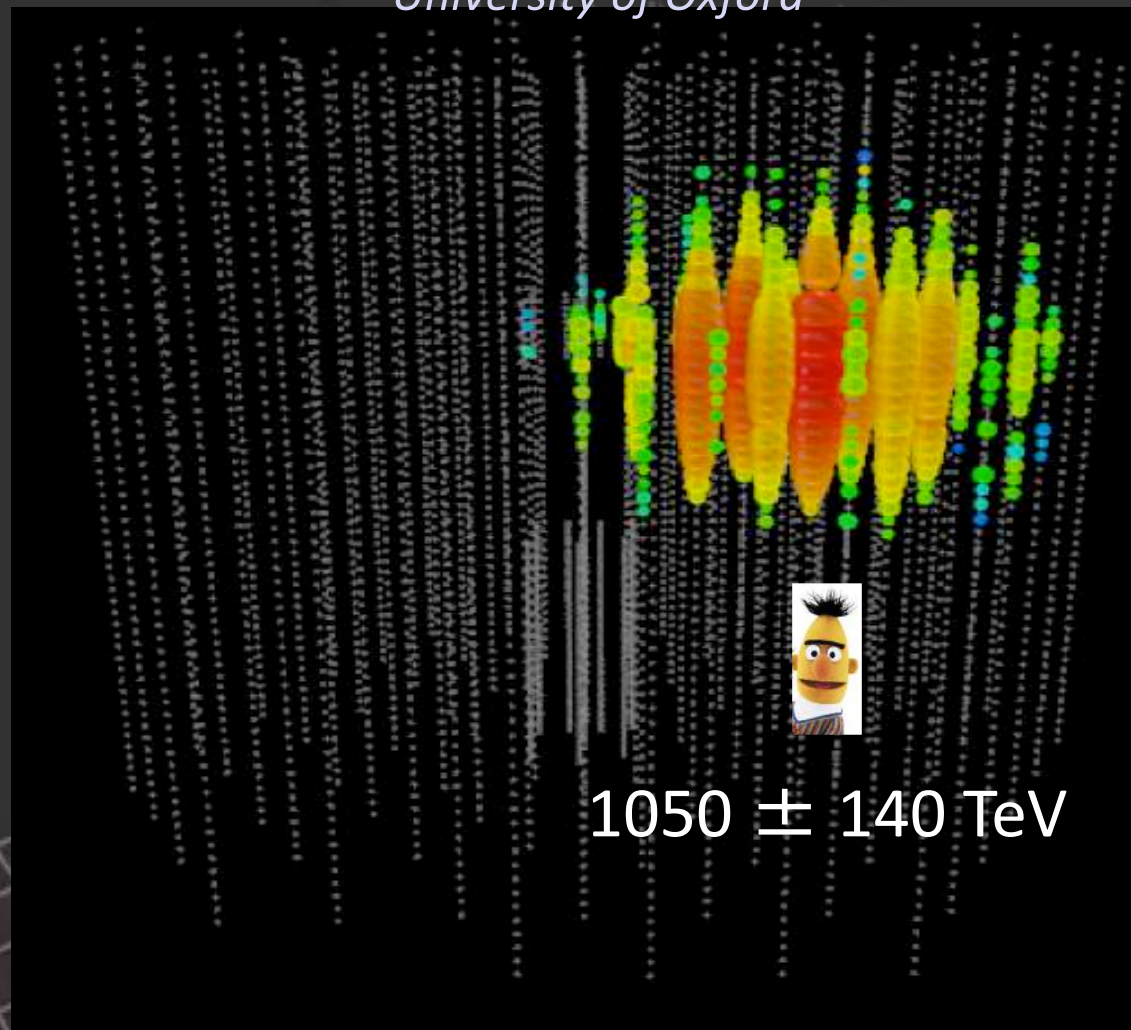


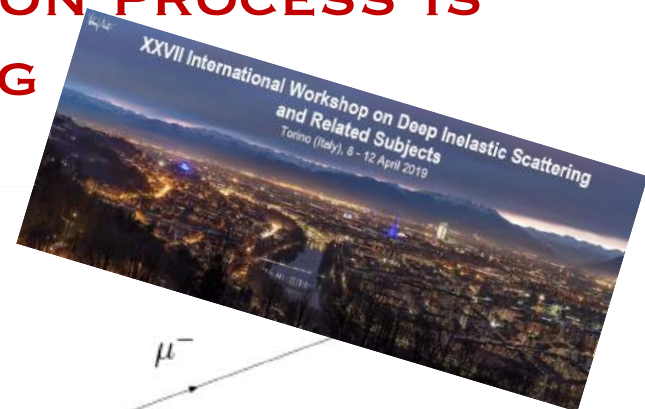
High energy neutrino cross-sections

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University of Oxford



ABOVE A FEW GEV THE DOMINANT INTERACTION PROCESS IS ν - N DEEP INELASTIC SCATTERING



$$\frac{\partial^2 \sigma_{\nu, \bar{\nu}}^{CC, NC}}{\partial x \partial y} = \frac{G_F^2 M E}{\pi} \left(\frac{M_i^2}{Q^2 + M_i^2} \right)$$

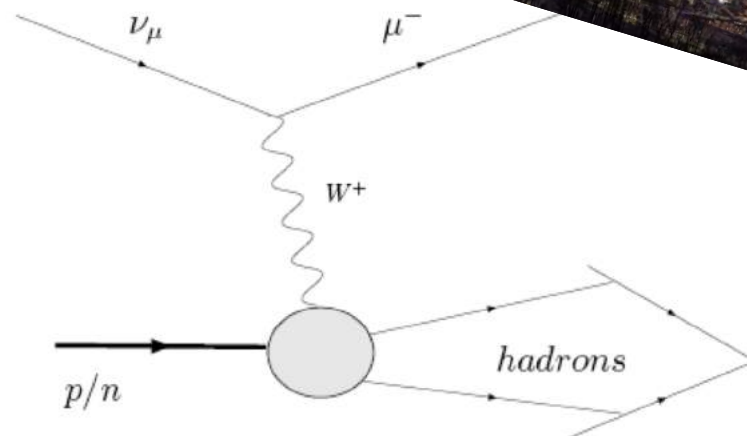
$Q^2 \uparrow \Rightarrow$ propagator \downarrow

$$\left[\frac{1 + (1 - y)^2}{2} F_2^{CC, NC}(x, Q^2) - \frac{y^2}{2} F_L^{CC, NC}(x, Q^2) \right]$$

$$\pm y \left(1 - \frac{y}{2} \right) x F_3^{CC, NC}(x, Q^2)]$$

$Q^2 \uparrow \Rightarrow$ parton distribution functions \uparrow

$$F_i(x, Q^2) = \sum_{a=g, q} \int_x^1 \frac{dz}{z} C_{i,a} \left(\frac{x}{z}, Q^2 \right) f_a(z, Q^2)$$

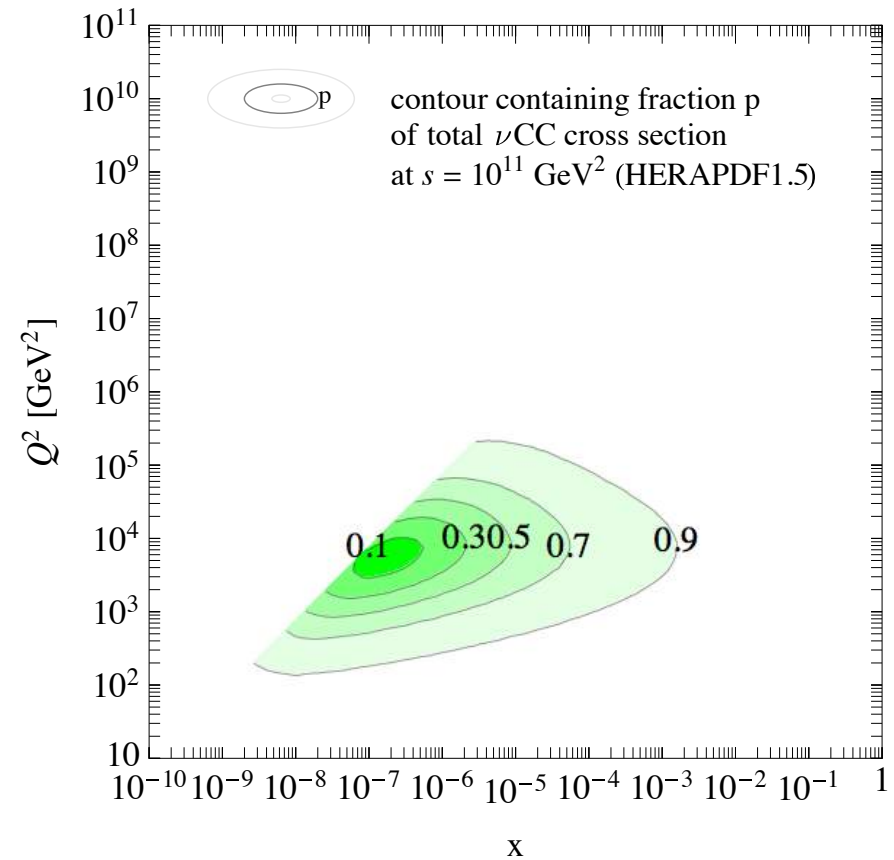
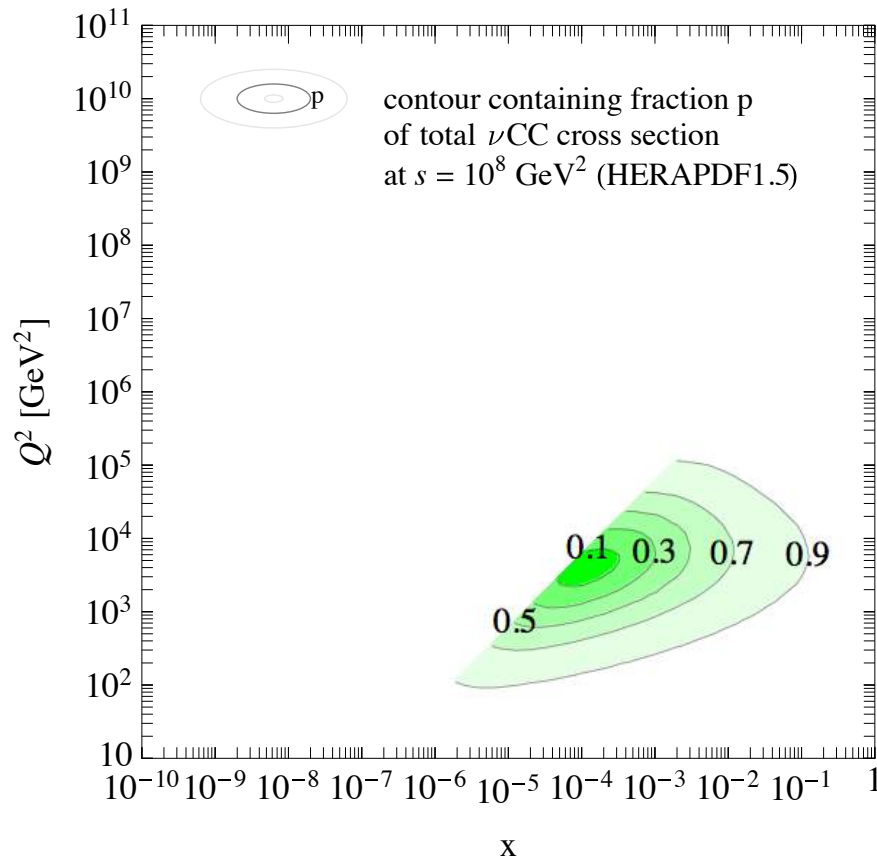


Most of the contribution to DIS cross-section comes from: $Q^2 \sim M_W^2$ and $x \sim \frac{M_W^2}{M_N E_\nu}$

At leading order (LO) : $F_L = 0$, $F_2 = x(u_\nu + d_\nu + 2s + 2b + \bar{u} + \bar{d} + 2\bar{c})$,
 $x F_3 = x(u_\nu + d_\nu + 2s + 2b - \bar{u} - \bar{d} - 2\bar{c}) = x(u_\nu + d_\nu + 2s + 2b - 2\bar{c})$

Can calculate numerically at Next-to-Leading-Order (NLO) ... no significant further change at NNLO

As the neutrino energy increases, *low* values of Bjorken- x are being probed

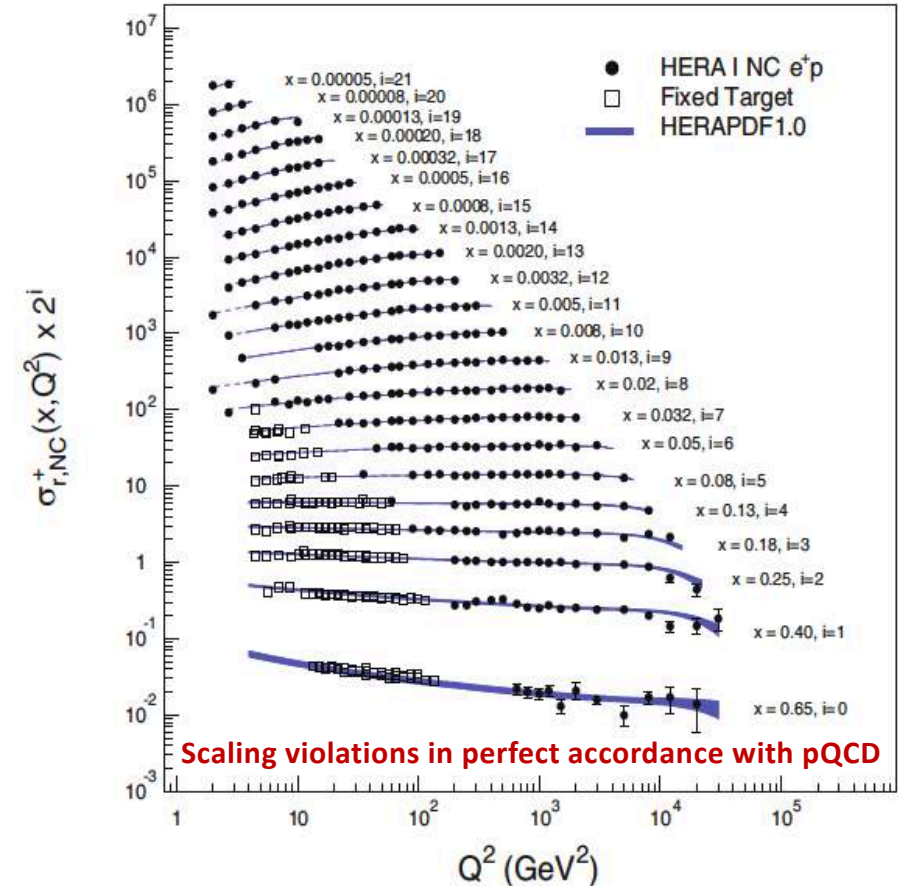
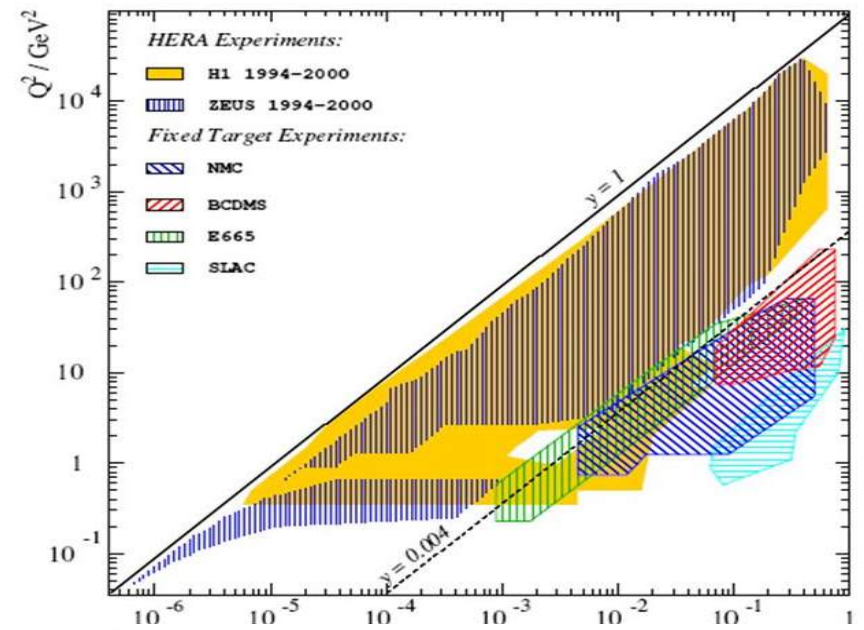
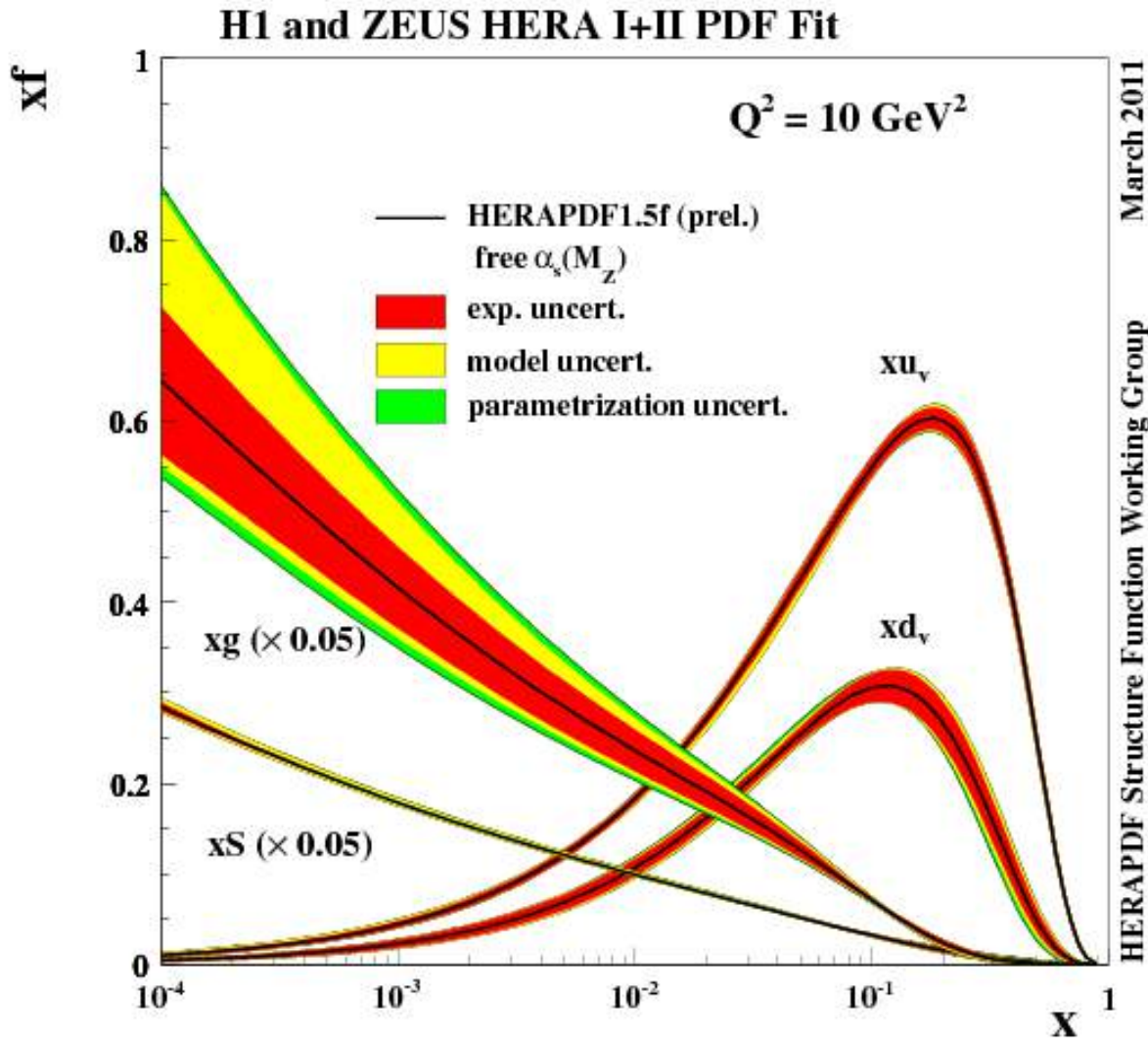


Mertsch, Cooper-Sarkar & Sarkar, JHEP 08:042,2011

So to determine the DIS cross-section accurately it is essential to have measurements of PDFs down to as *low* x as is possible ... for E_ν higher than $\sim 10^3 \text{ TeV}$ we have to evolve these further (using the DGLAP formalism)

(Warning: Off-the-shelf PDFs, e.g. on <http://lhapdf.hepforge.org>, often ‘freeze’ below some low value of Bjorken- x (i.e. values are set to zero), so care must be taken at very high E_ν to avoid errors!)

The H1 & ZEUS experiments at HERA were the first to measure DIS at high Q^2 and low Bjorken- x ... an unexpected finding was the very *steep* rise of the **gluon PDF** at low x which has significance for high energy neutrino interactions

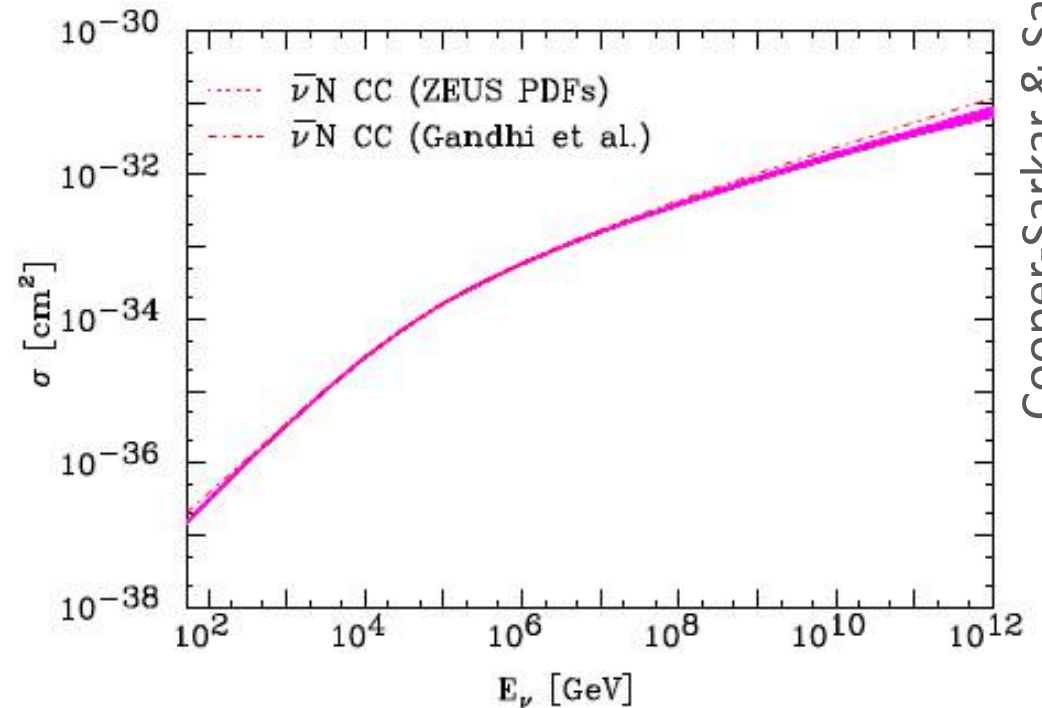
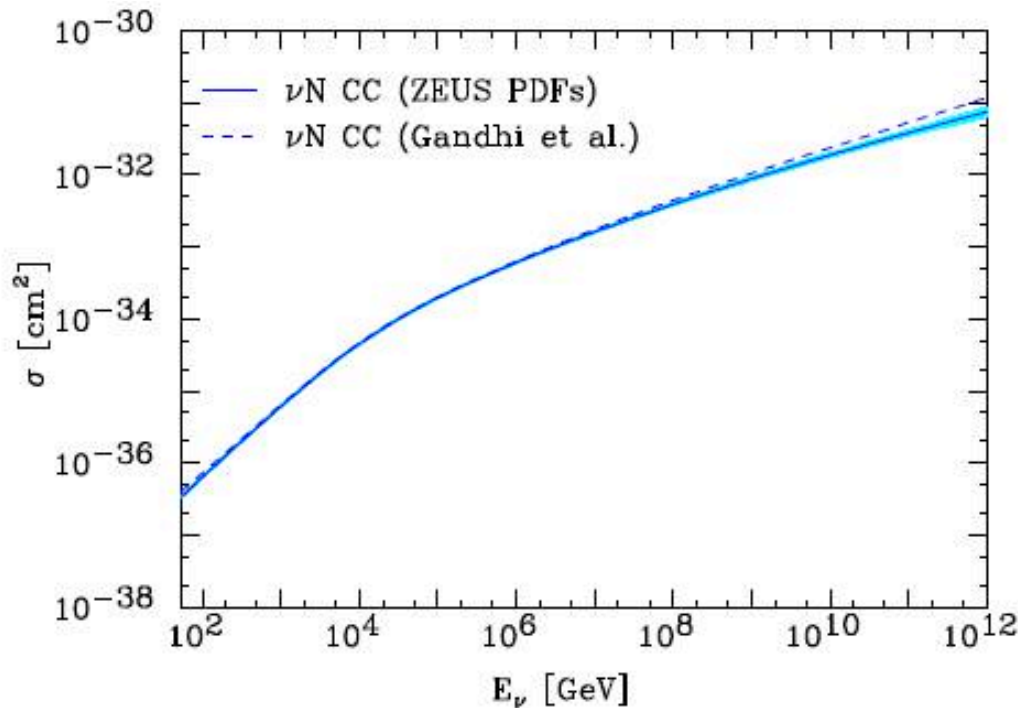
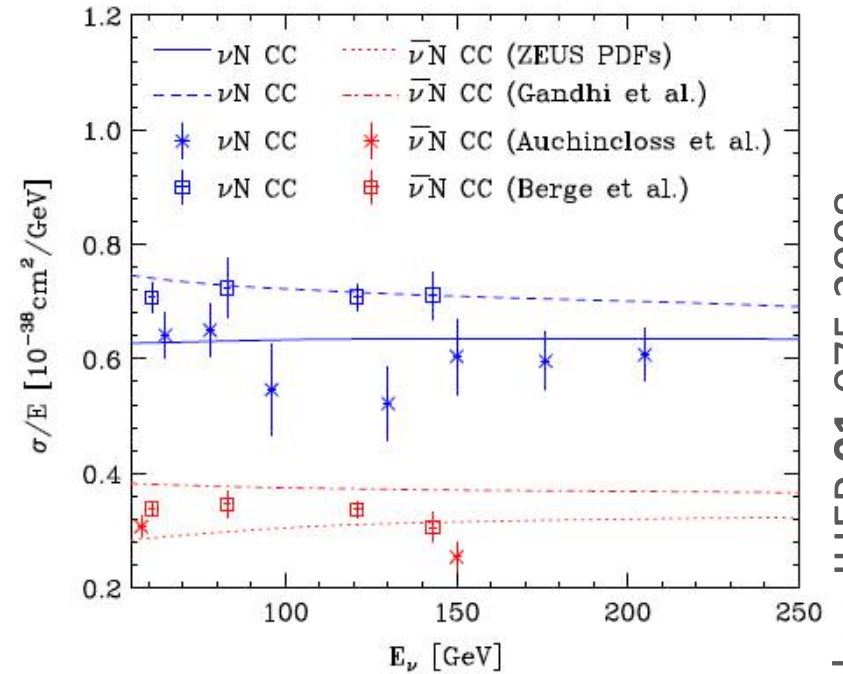


The cross-section using modern PDFs is up to $\sim 40\%$ *below* the previous 'standard' calculation of Gandhi *et al* (1998)

We also quantified the *uncertainty* to be $< 5-10\%$ even at the highest energies ... in the framework of pQCD

At very high energies where very low- x is being probed, recombination/saturation effects may reduce the cross-section by a factor of up to ~ 2 ... However DGLAP evolution appears to fit well *all* experimental data – so no imperative for this yet! (although fit does improve with BFKL resummation)

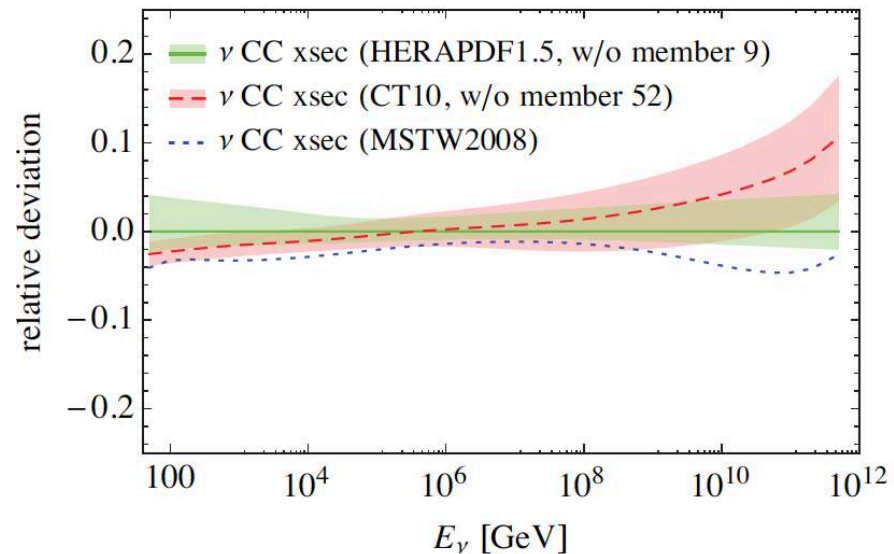
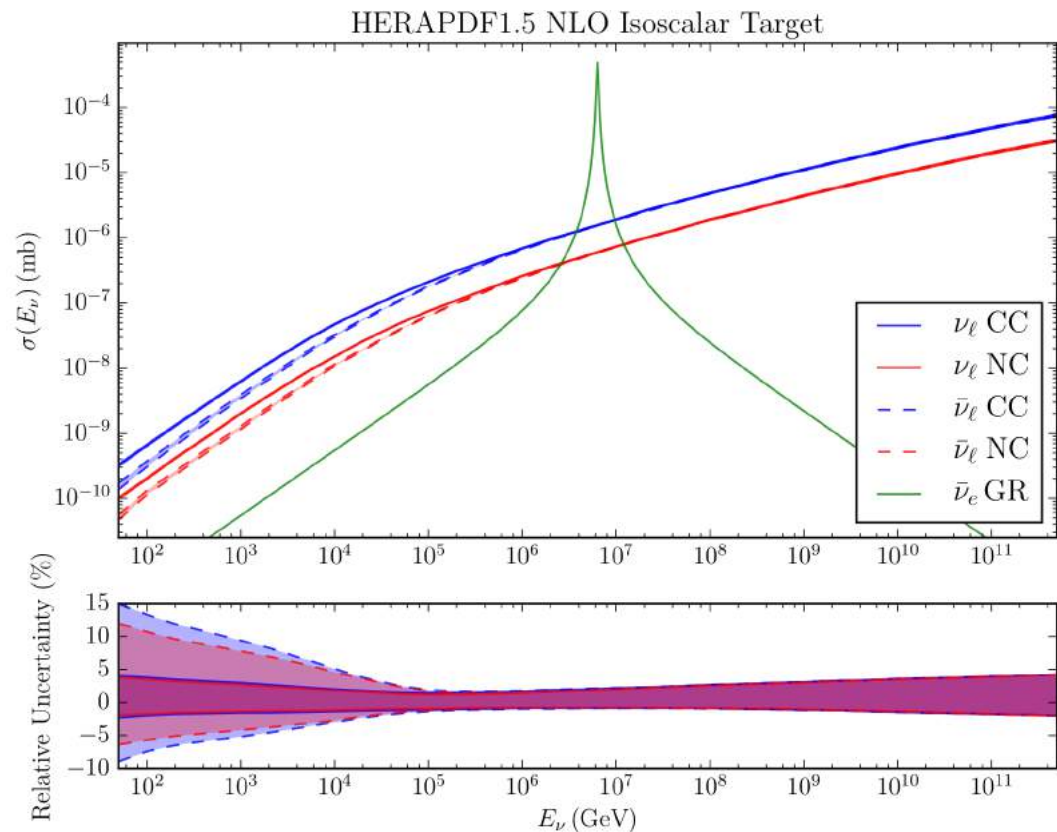
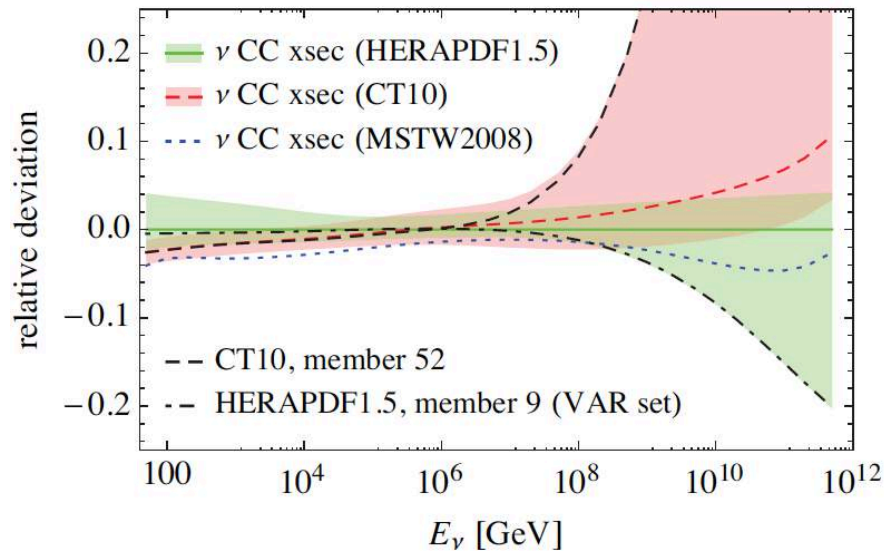
Agrees with low energy (>10 GeV) data



After the full HERA data release we updated the ν -N cross-section @ NLO using HERAPDF1.5, including the effect of heavy quarks on the DGLAP evolution ... the full code is implemented in:

<https://dispred.hepforge.org/>

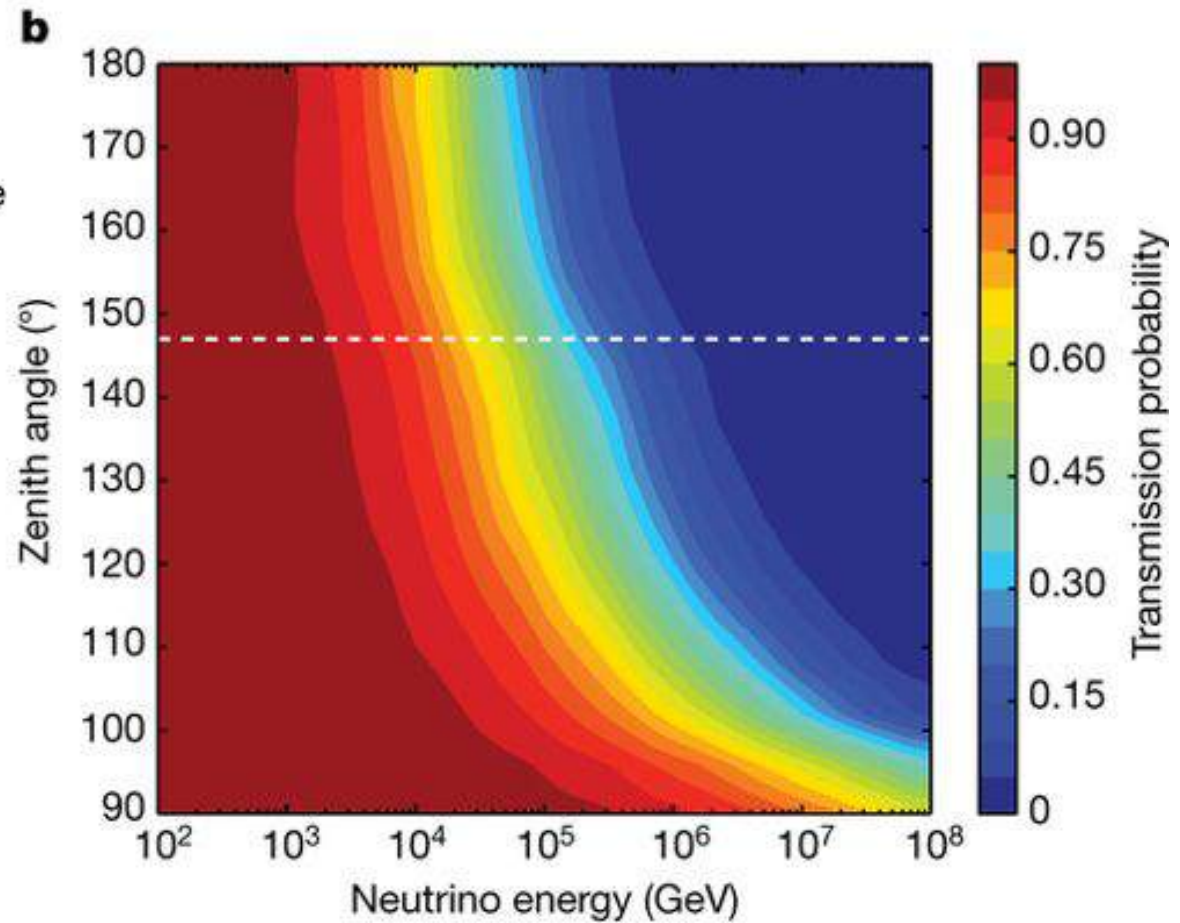
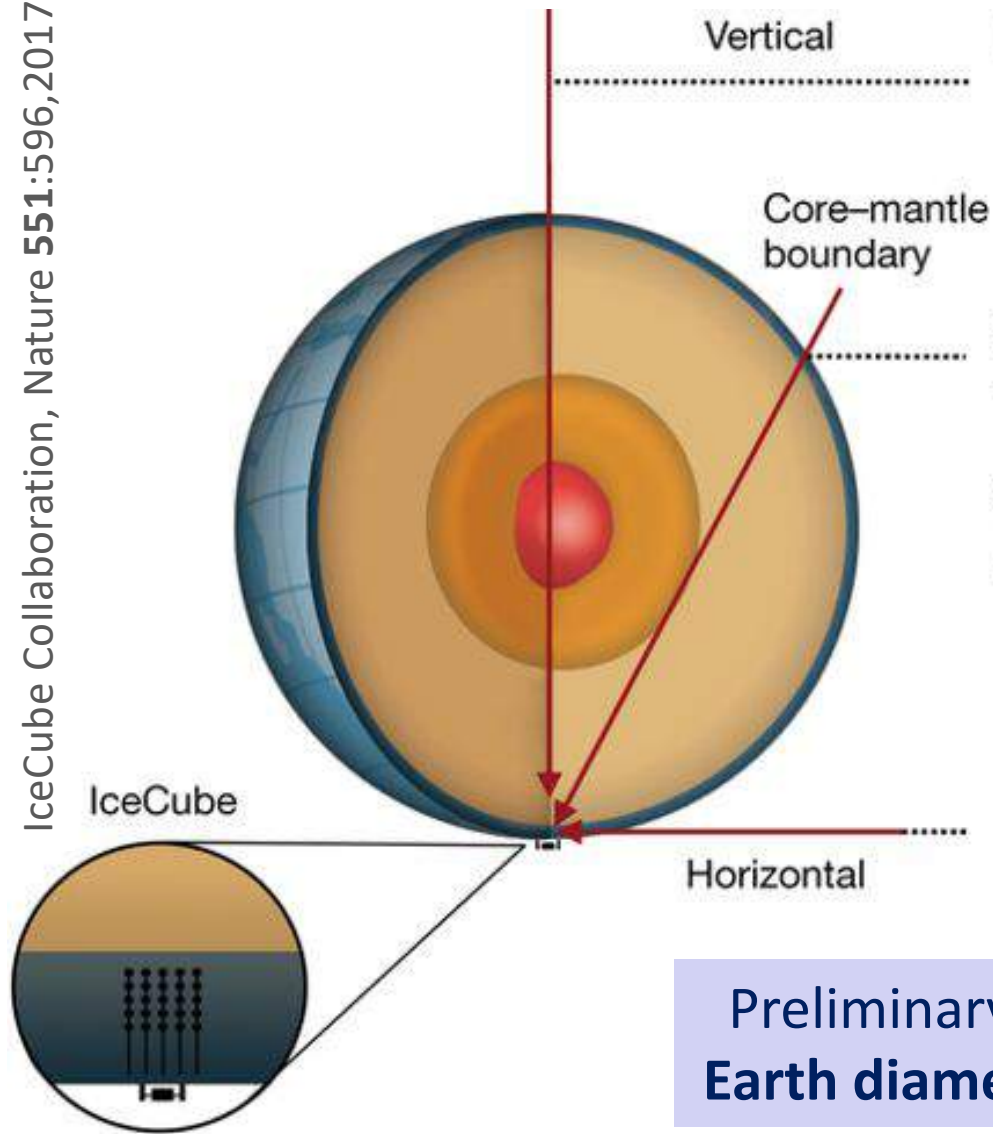
This is the cross-section implemented in NuGen and other event generators



We find *good* agreement between different PDF sets after rejecting unphysical members which would have yielded *negative* values for the structure function F_L (or violated the Froissart bound)

THE ν - N CROSS-SECTION PREDICTION CAN BE TESTED BY EXAMINING THE ZENITH ANGLE DEPENDENCE OF AN *ISOTROPIC* ν FLUX VIEWED THROUGH THE EARTH

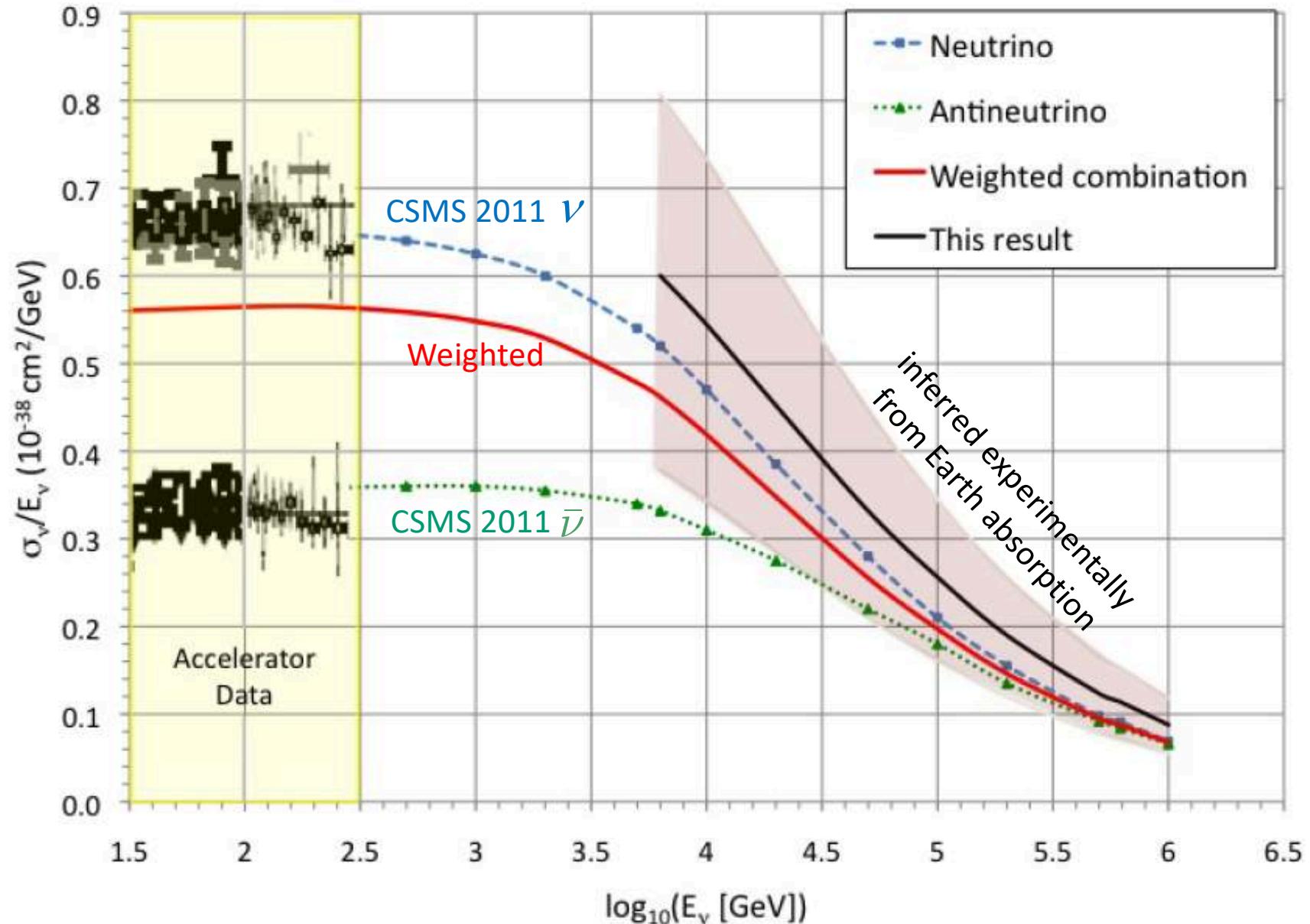
IceCube Collaboration, Nature 551:596,2017



Preliminary Reference Earth Model (PREM), 1981
Earth diameter \Rightarrow interaction length at $E_\nu \sim 40$ TeV

NB: The flux of atmospheric neutrinos (which dominate up to $\sim 10^5$ GeV) is isotropic ... also a good approximation for the extragalactic flux ... galactic component is $< 18\%$

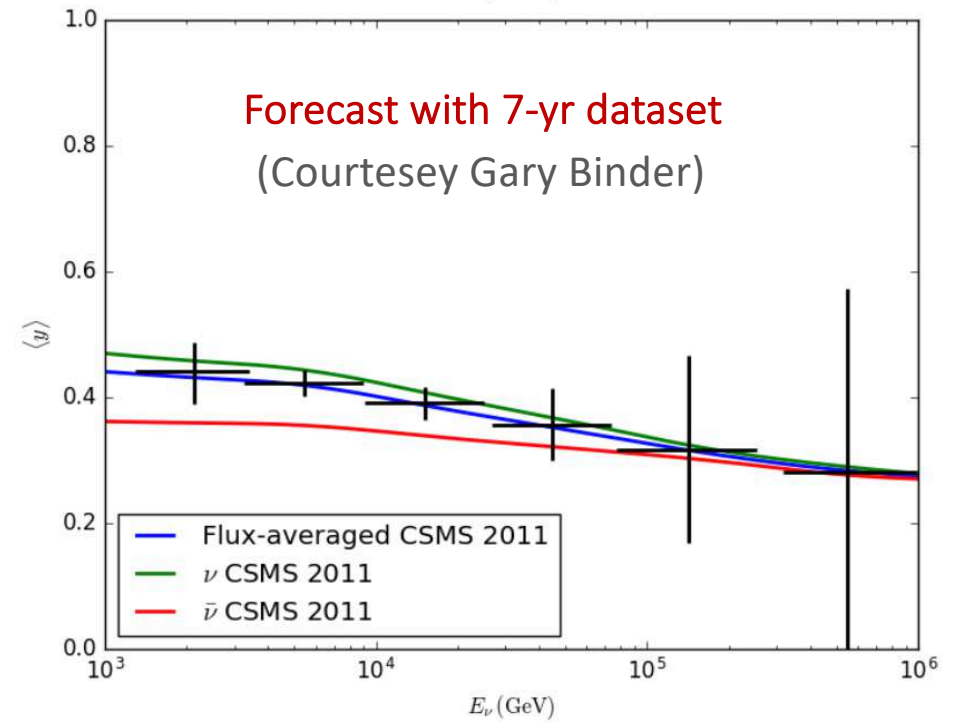
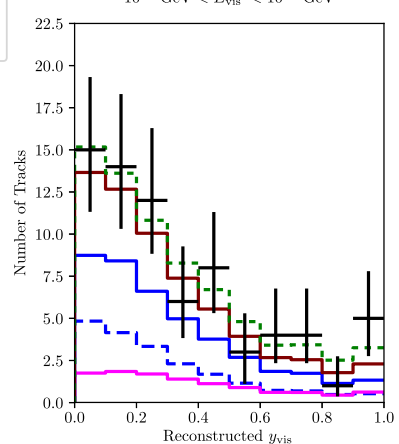
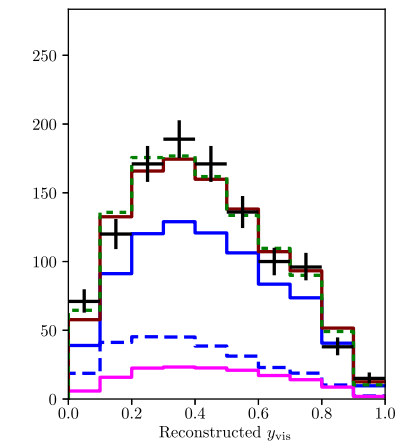
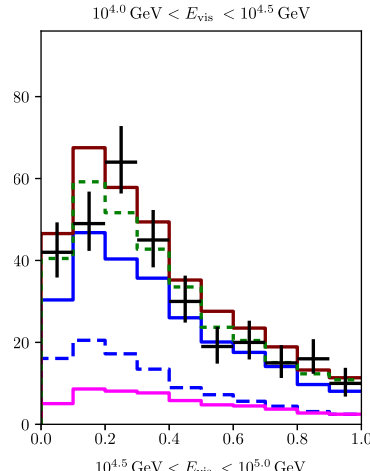
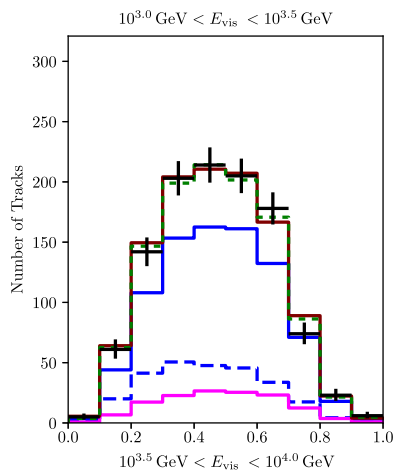
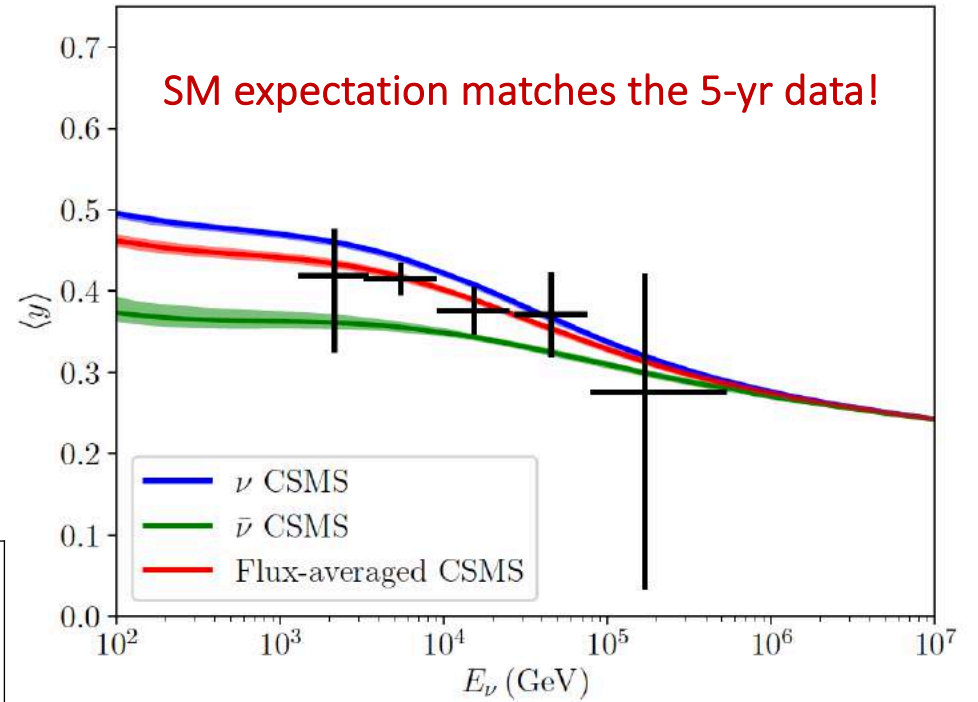
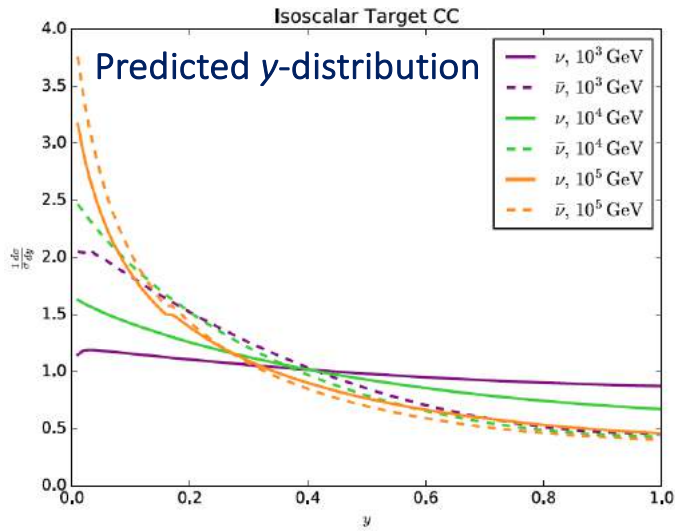
No evidence of deviation from SM up to ~ 980 TeV



IceCube Collaboration, Nature 551:596,2017

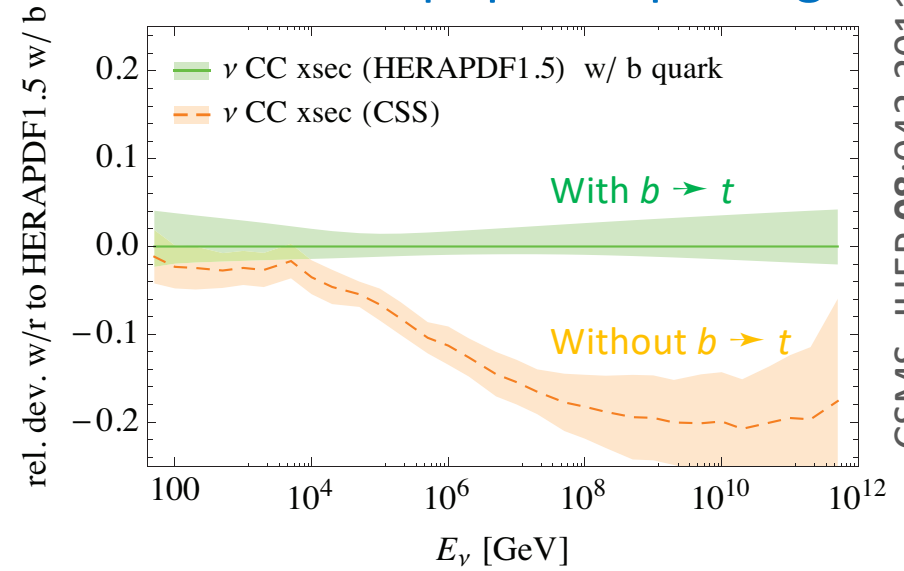
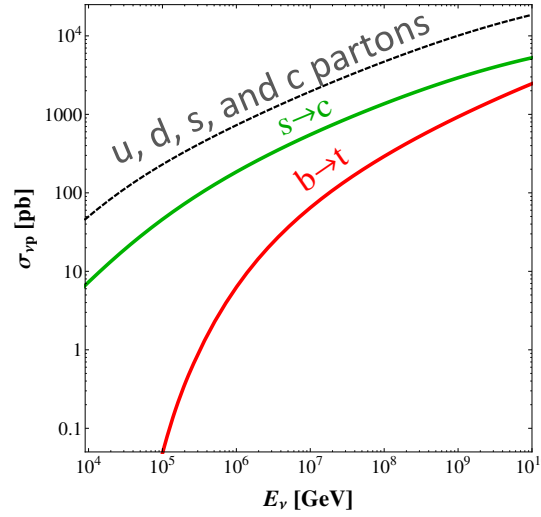
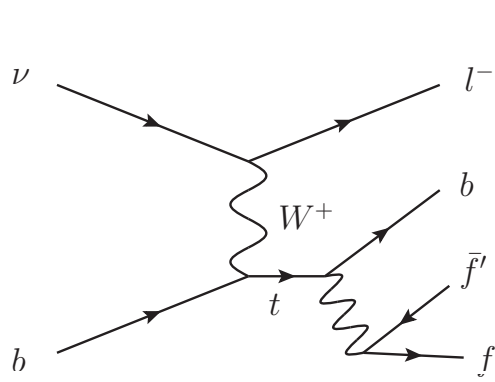
Powerful probe of new physics beyond the SM (e.g. leptoquarks, new dimensions) should be able to probe up to $\sim 10^{10}$ GeV using cosmogenic ν - with **IceCube-Gen2**

ANOTHER TEST OF NEW PHYSICS IS THE INELASTICITY DISTRIBUTION ..



Barger et al, PR D95:093002,2017

*** Heavy quark mass effects on DGLAP evolution: bottom to top quark splitting**

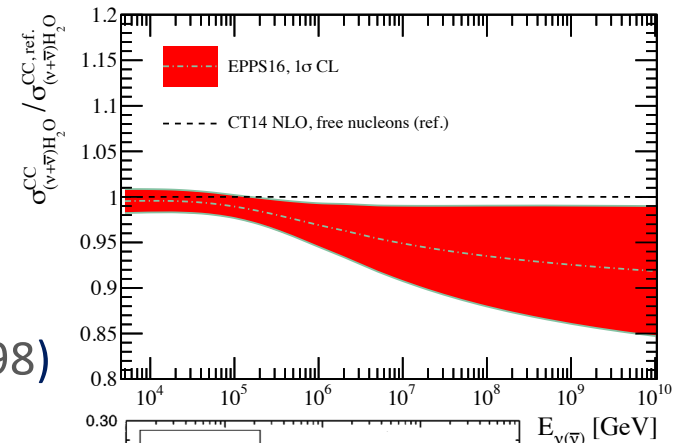


CSMS, JHEP 08:042,2011

However the exact way the $b \rightarrow t$ contribution turns on is under discussion (\Rightarrow ~5% syst. uncertainty)

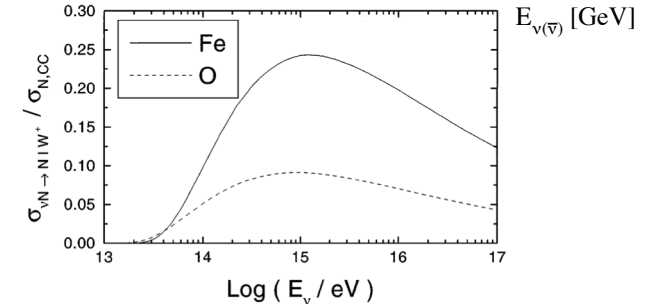
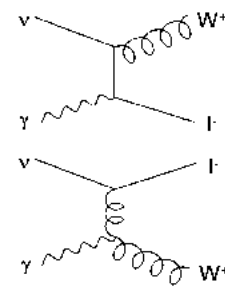
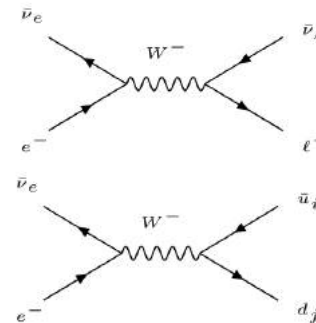
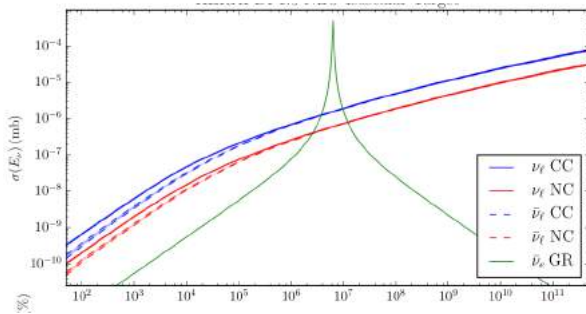
*** Nuclear binding effects ('shadowing'):**

There is *no* experimental evidence for shadowing but it can depress the cross-section by ~5-10% at high energies according to some theoretical estimates (although uncertainties are large)

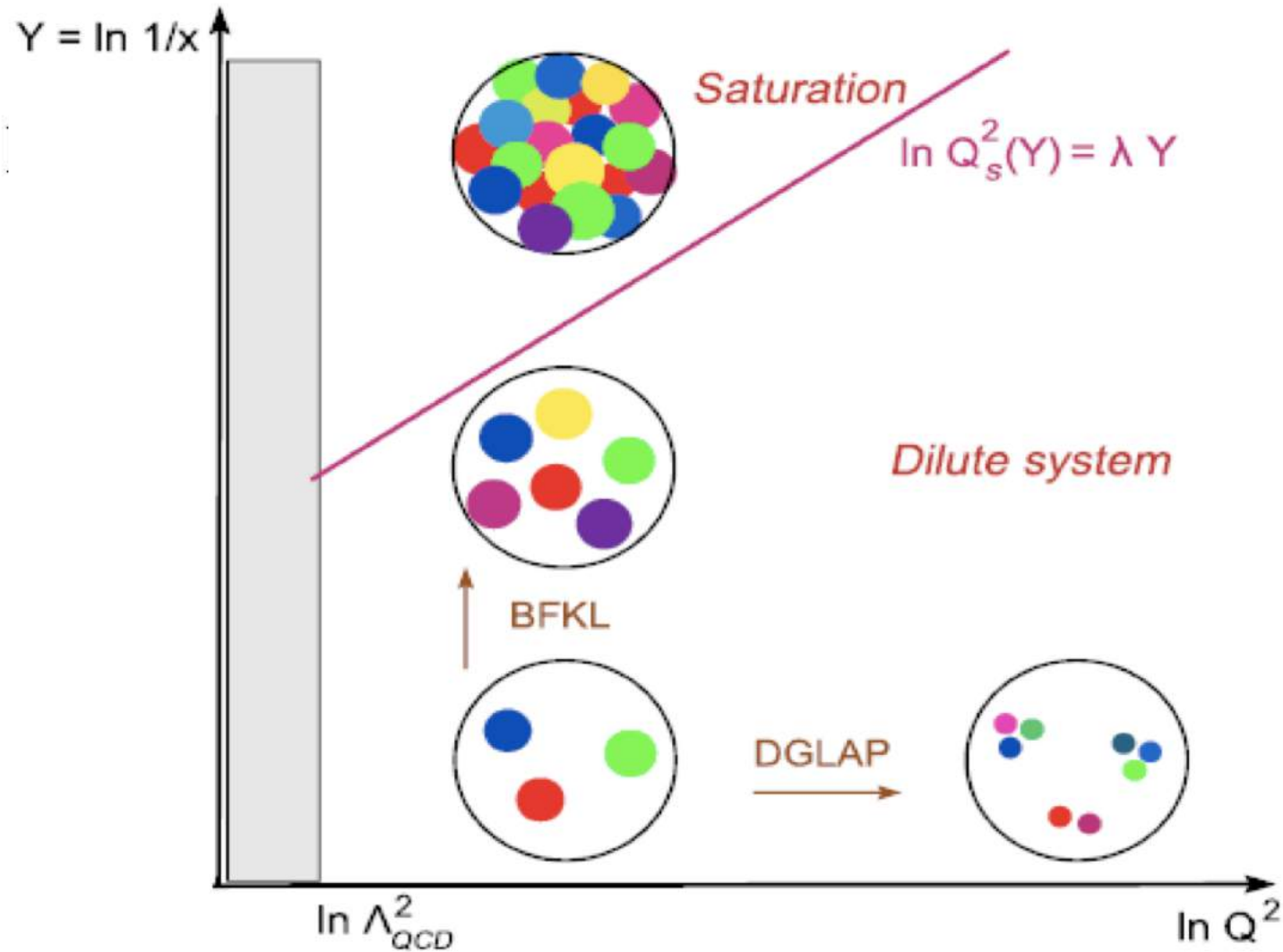


Bertone et al, JHEP 20:217,2019

*** Other contributions:** E.g. Glashow resonance, $\nu\gamma$ (Seckel 1998)



As the gluon density rises at low x , non-perturbative effects *must* become important ... a new phase of QCD - **Colour Glass Condensate** - has been postulated to exist (and has support from RHIC and ALICE data)



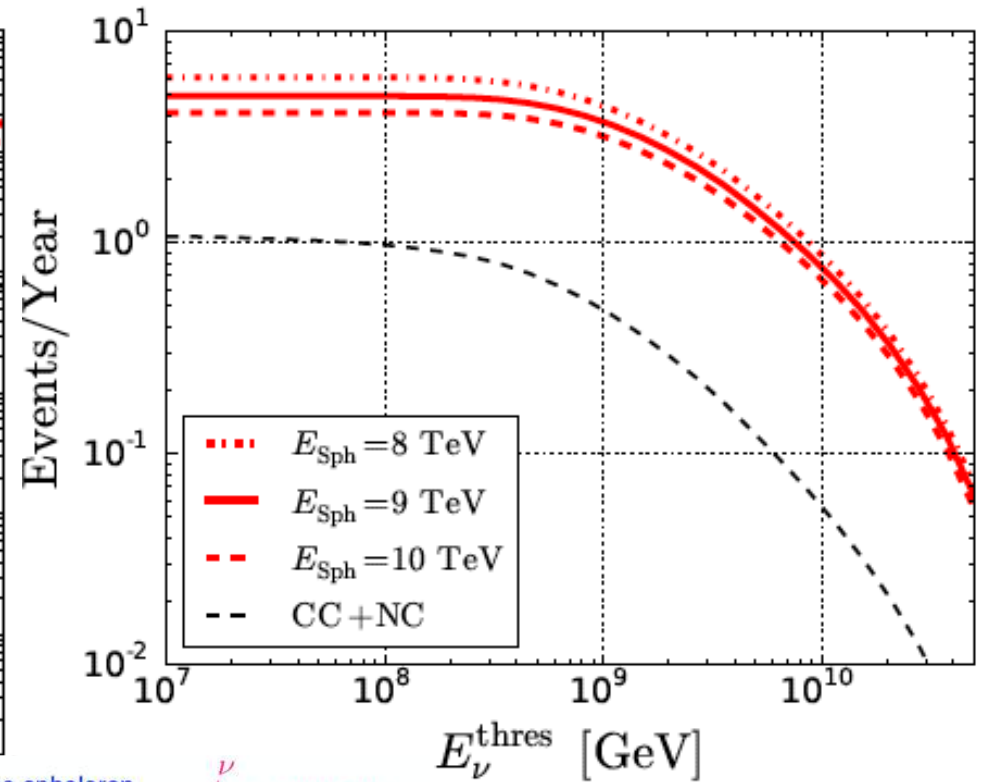
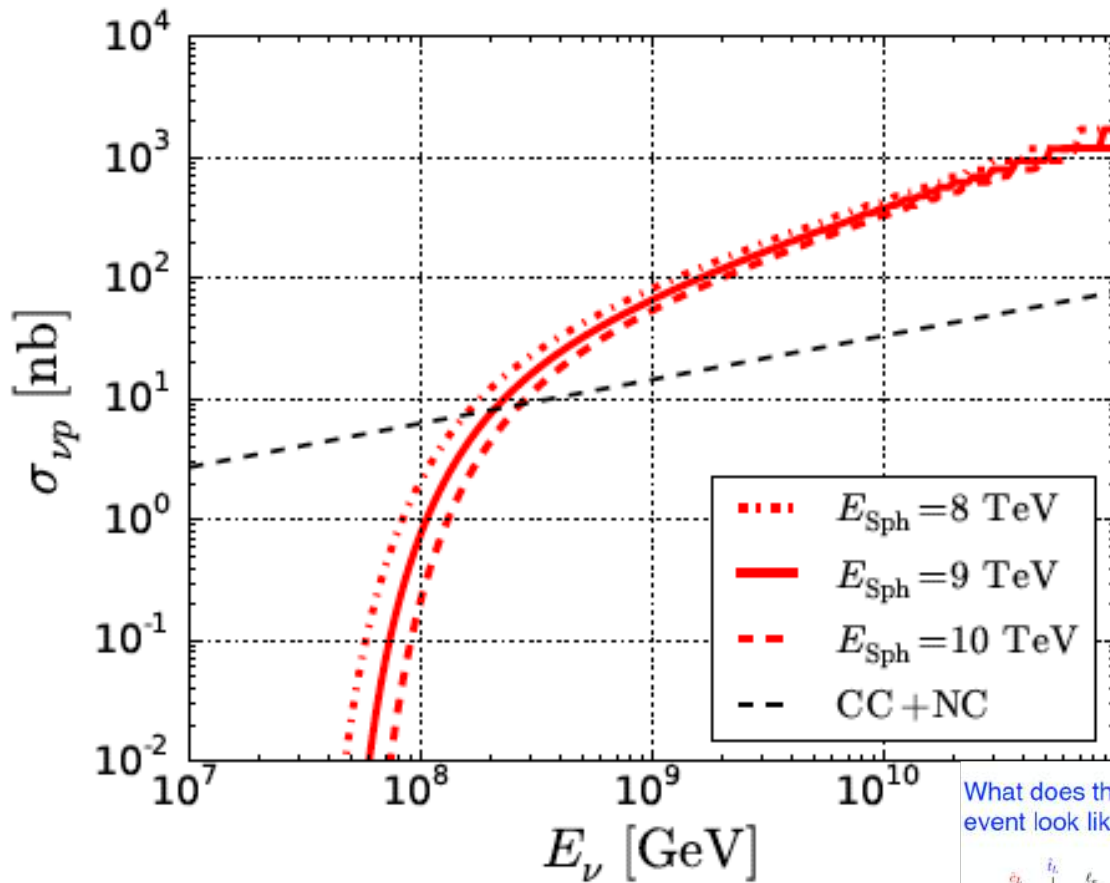
This would strongly suppress the ν - N #-secn below its (unscreened) SM value ... can we test this experimentally with UHE cosmic neutrinos?

... OR THE ν - N CROSS-SECTION MAY BE MUCH *HIGHER* THAN IN THE SM

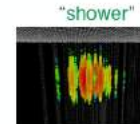
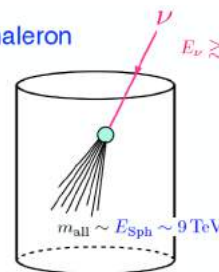
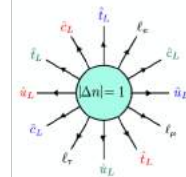
Non-perturbative transitions between degenerate $SU(2)$ vacua (with different $B+L$ #) are exponentially suppressed below the “sphaleron” mass: $\sim M_W/\alpha_W \sim 9$ TeV (update by Tye & Wong, PRD **92**:045005,2015) ... *large* cross-sections are predicted for ν - N scattering at higher cms energies

$$E_\nu \geq E_{\text{sph}}^2 / 2xm_N \simeq 4 \times 10^7 / x \sim 10^{9-11} \text{ GeV}$$

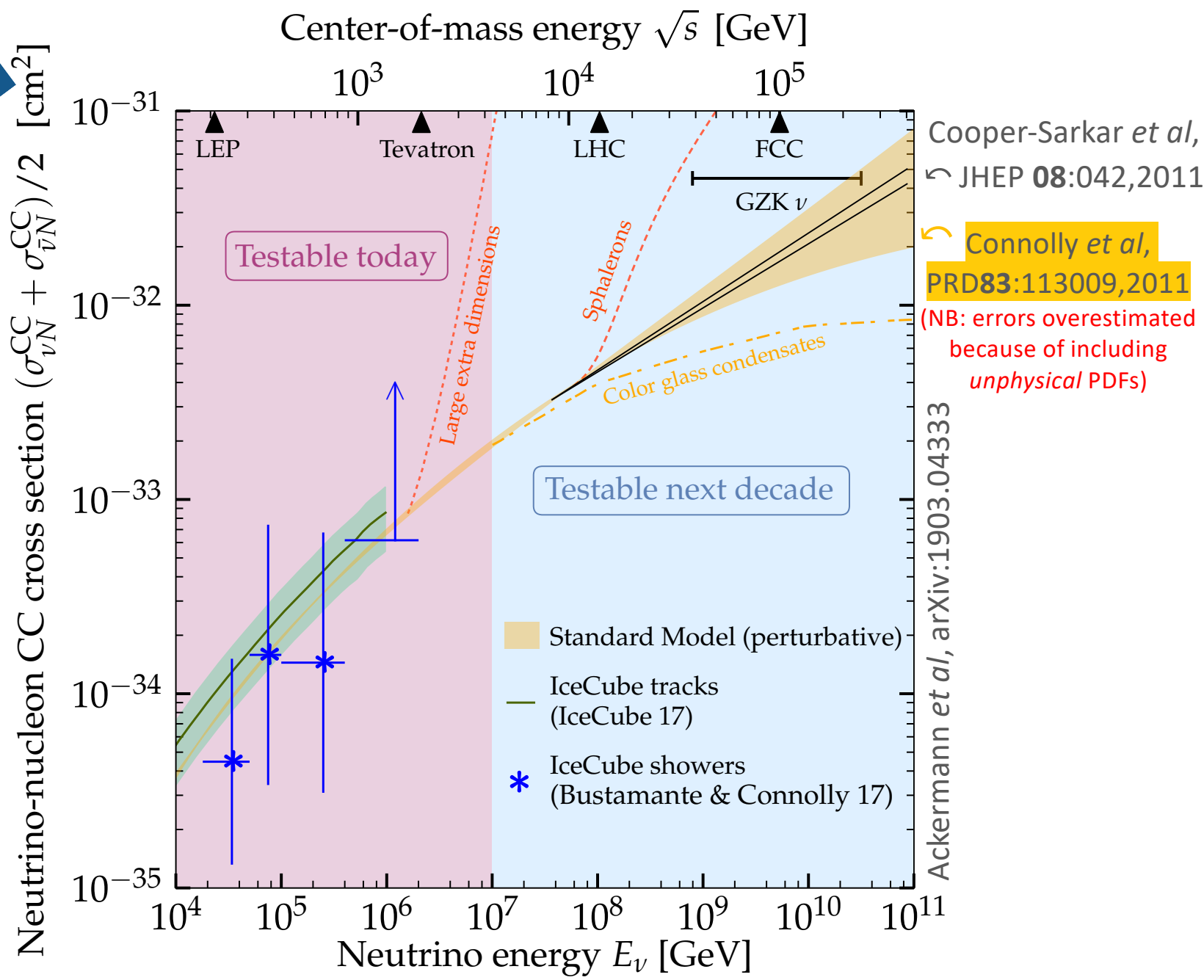
Han & Hooper, PLB **582**:21,2004



What does the sphaleron event look like?



IceCube has sensitivity to electroweak sphalerons comparable to LHC!



The *perturbative* QCD prediction is in fact accurate to $\pm \sim 5\%$ (PDF uncertainties) even at GZK energies ... so new physics (whether non-pert. SM or BSM) would be easy to identify *if* we can detect GZK vs

SUMMARY

- Neutrino telescopes have already measured the ν DIS cross-section up to cms energies ~ 10 times higher than are attainable at the LHC ... finding *no* deviation from the SM
- This sets constraints on new physics that can increase the cross-section e.g. new TeV-scale dimensions, leptoquarks (... admittedly these have been ruled out already in Run II)
- There may be new *non*-perturbative processes *in* the SM which can affect the ν DIS cross-section at still higher energies, e.g. 'electroweak sphalerons' and 'QCD colour glass condensate' - to probe this will require studying the highest energy (GZK) cosmic neutrinos at $\sim 10^{10}$ GeV

To probe the energy frontier we *must* think **BIG** (Gen2, KM3NeT, ...)