# Phenomenology of light sterile neutrinos



Yu-Feng Li

liyufeng@ihep.ac.cn

**Institute of High Energy Physics, Beijing** 

XVIII International Workshop on Neutrino Telescopes
18-22 March 2019, Venice, Italy

# **Three Neutrino Paradigm**

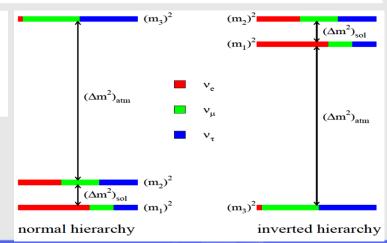
### Standard Parameterization of Mixing Matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{13}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

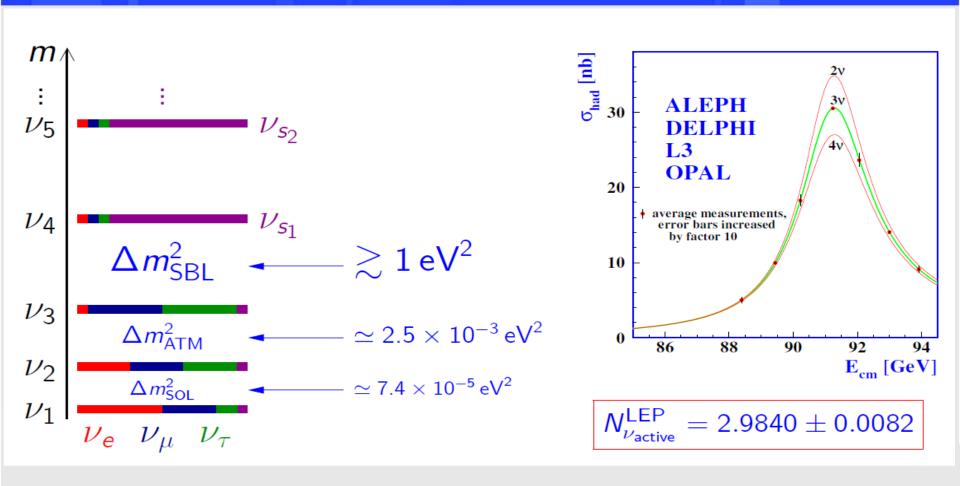
$$= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

$$c_{ab} \equiv \cos \vartheta_{ab}$$
  $s_{ab} \equiv \sin \vartheta_{ab}$   $0 \le \vartheta_{ab} \le \frac{\pi}{2}$   $0 \le \delta_{13}, \lambda_{21}, \lambda_{31} < 2\pi$ 

- 3 Mixing Angles:  $\vartheta_{12}$ ,  $\vartheta_{23}$ ,  $\vartheta_{13}$
- 1 CPV Dirac Phase:  $\delta_{13}$
- 2 independent  $\Delta m_{kj}^2 \equiv m_k^2 m_j^2$ :  $\Delta m_{21}^2$ ,  $\Delta m_{31}^2$
- Absolute Neutrino Masses
- > Two CPV Majorana Phases



### Beyond 3-v oscillations: sterile neutrinos



**Explanation of short baseline oscillations:** 

eV-scale sterile neutrinos (which have mixing with active mass eigenstates)

Status of short baseline oscillations in nue(bar) disappearance channels

# **Gallium anomaly**

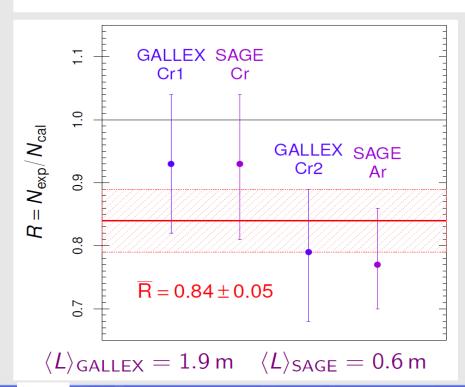
SAGE, PRC (2006); PRC (2009); Laveder et al. (2007), etc.

### **Gallium Radioactive Source Experiments: GALLEX and SAGE**

### **Test of Solar Neutrino Detection**

Detection Process: 
$$\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$$

$$\nu_e$$
 Sources:  $e^- + {}^{51}\mathrm{Cr} \rightarrow {}^{51}\mathrm{V} + \nu_e$   $e^- + {}^{37}\mathrm{Ar} \rightarrow {}^{37}\mathrm{Cl} + \nu_e$ 



~2.9σ deficit

Neutrino energies: ~0.8 MeV

$$\Delta m_{\mathsf{SBL}}^2 \gtrsim 1\,\mathrm{eV}^2 \gg \Delta m_{\mathsf{ATM}}^2 \gg \Delta m_{\mathsf{SOL}}^2$$

Anomaly supported by the new cross section measurement

$$^{3}\text{He} + ^{71}\text{Ga} \rightarrow ^{71}\text{Ge} + ^{3}\text{H}$$

Frekers et al., PLB 706 (2011) 134

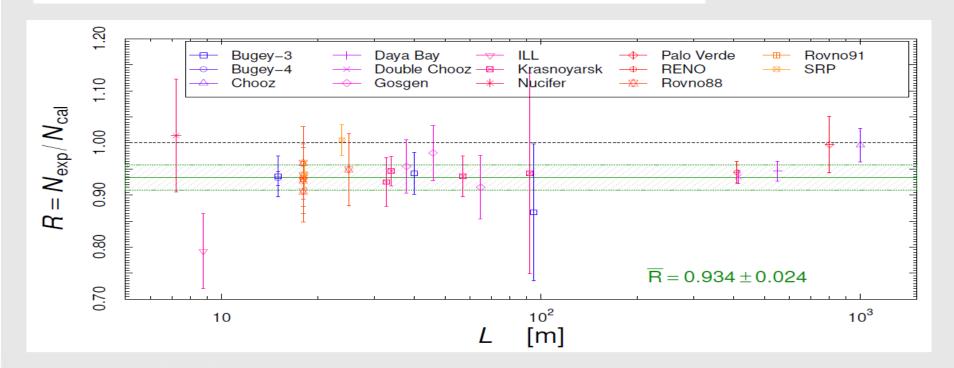
Contributions from excited states verified Giunti et. al. 1210.5715

### **Reactor Antineutrino Anomaly**

[Mention et al, PRD 83 (2011) 073006]

New reactor  $\bar{\nu}_e$  fluxes

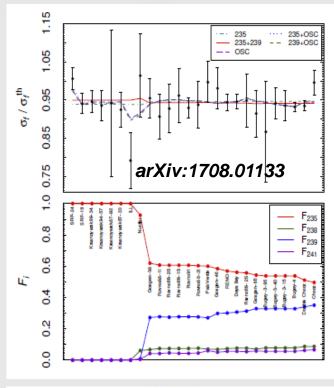
[Mueller et al, PRC 83 (2011) 054615; Huber, PRC 84 (2011) 024617]



- Discrepancy between theory and measurements
- $\sim 2.8 \sigma$  deficit (depending on the theoretical flux uncertainty)
- Nominal theoretical uncertainty from the Mueller+Huber model ~ 2.5%

### A closer look at reactor rates data

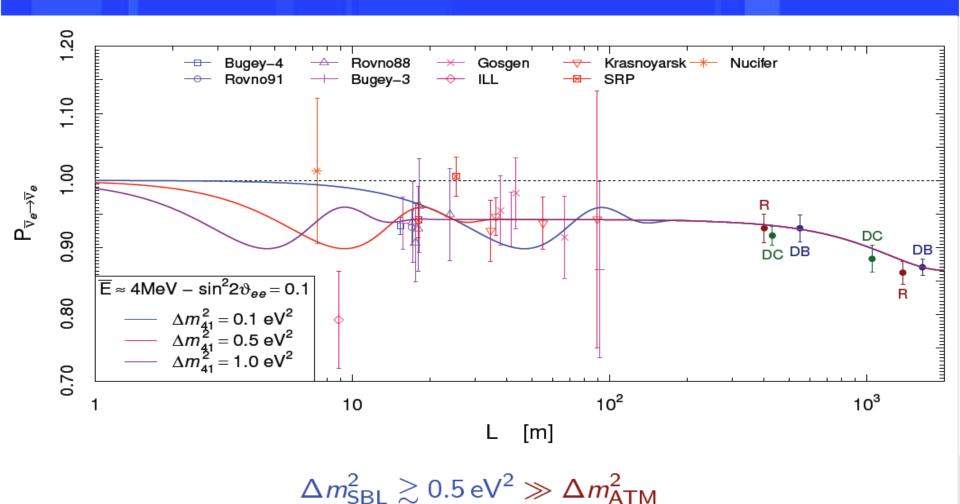
a	Experiment	$f_{235}^a$	$f_{238}^a$	$f_{239}^a$	$f_{241}^a$	$R_a^{\rm exp}$	$\sigma_a^{\rm exp}$ [%]	$\sigma_a^{cor}$ [%]	$\sigma_a^{\mathrm{the}}$ [%]	$L_a$ [m]
1	Bugey-4	0.538	0.078	0.328	0.056	0.932	1.4	}1.4	2.5	15
2	Rovno91	0.606	0.074	0.277	0.043	0.930	2.8	}1.4	2.4	18
3	Rovno88-1I	0.607	0.074	0.277	0.042	0.907	6.4	3.1)	2.4	18
4	Rovno88-2I	0.603	0.076	0.276	0.045	0.938	6.4	53.1	2.4	18
5	Rovno88-1S	0.606	0.074	0.277	0.043	0.962	7.3	2.2	2.4	18
6	Rovno88-2S	0.557	0.076	0.313	0.054	0.949	7.3	3.1	2.5	25
7	Rovno88-2S	0.606	0.074	0.274	0.046	0.928	6.8	) )	2.4	18
8	Bugey-3-15	0.538	0.078	0.328	0.056	0.936	4.2	)	2.5	15
9	Bugey-3-40	0.538	0.078	0.328	0.056	0.942	4.3	4.0	2.5	40
10	Bugey-3-95	0.538	0.078	0.328	0.056	0.867	15.2	J	2.5	95
11	Gosgen-38	0.619	0.067	0.272	0.042	0.955	5.4	) )	2.4	37.9
12	Gosgen-46	0.584	0.068	0.298	0.050	0.981	5.4	2.0	2.4	45.9
13	Gosgen-65	0.543	0.070	0.329	0.058	0.915	6.7	) }	2.4	64.7
14	ILL	1	0	0	0	0.792	9.1		2.4	8.76
15	Krasnoyarsk87-33	1	0	0	0	0.925	5.0	}4.1	2.4	32.8
16	Krasnoyarsk87-92	1	0	0	0	0.942	20.4	J*.1	2.4	92.3
17	Krasnoyarsk94-57	1	0	0	0	0.936	4.2	0	2.4	57
18	Krasnoyarsk99-34	1	0	0	0	0.946	3.0	0	2.4	34
19	SRP-18	1	0	0	0	0.941	2.8	0	2.4	18.2
20	SRP-24	1	0	0	0	1.006	2.9	0	2.4	23.8
21	Nucifer	0.926	0.061	0.008	0.005	1.014	10.7	0	2.3	7.2
22	Chooz	0.496	0.087	0.351	0.066	0.996	3.2	0	2.5	$\approx 1000$
23	Palo Verde	0.600	0.070	0.270	0.060	0.997	5.4	0	2.4	≈ 800
24	Daya Bay	0.561	0.076	0.307	0.056	0.946	2.0	0	2.5	≈ 550
25	RENO	0.569	0.073	0.301	0.056	0.944	2.2	0	2.4	$\approx 411$
26	Double Chooz	0.511	0.087	0.340	0.062	0.935	1.4	0	2.5	$\approx 415$



All Reactors	<sup>235</sup> U	OSC
$\chi^2_{\rm min}$	25.3	23.0
NDF	32	31
GoF	79%	85%

MC:  $^{235}$ U disfavored at  $1.7\sigma$ 

### **RAA:** oscillation-based explanation



SBL oscillations are averaged at the Daya Bay, RENO, and Double Chooz near detectors —> no spectral distortion

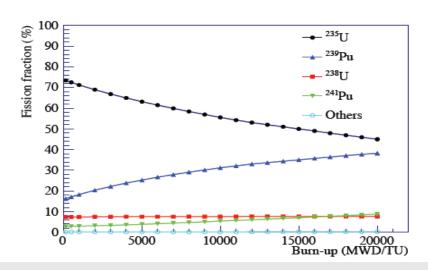
### **Burn-up Feature @ Reactors**

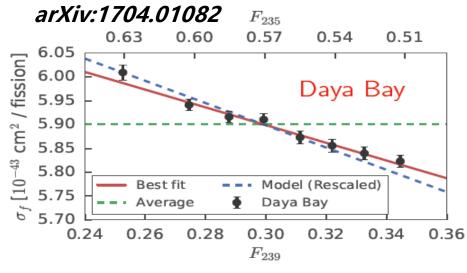
- Produced by the  $\beta$  decays of the fission products of  $^{235}$ U  $^{238}$ U  $^{239}$ Pu  $^{241}$ Pu
- Effective fission fractions:

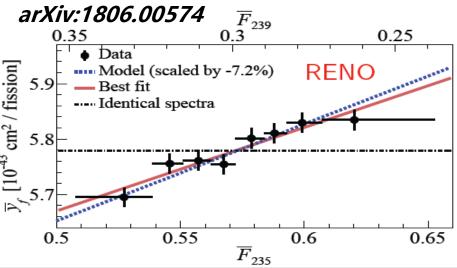
$$F_{235}$$
  $F_{238}$   $F_{239}$   $F_{241}$ 

Cross section per fission:

$$\sigma_f = \sum_{k=235,238,239,241} F_k \, \sigma_{f,k}$$

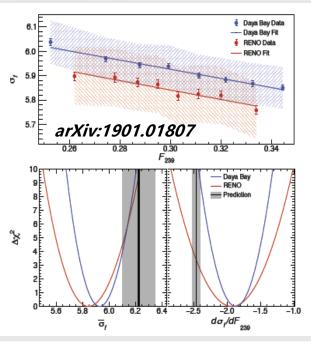


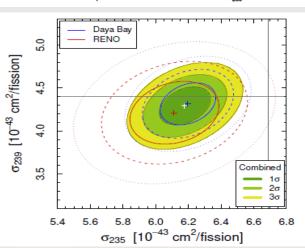




Both experiments disfavor the equal suppression at around 3-sigma!

### A Global Analysis of Reactor Flux Data





	235	239	235+239	235+238+239	235=239=241+238	OSC	235+OSC	239+OSC
$\chi^2_{\rm min}$	34.6	41.6	34.1	29.9	38.6	33.1	29.5	26.9
NDF	39	39	38	37	38	38	37	37
GoF	67%	36%	65%	79%	44%	69%	80%	89%
$r_5$	$0.933 \pm 0.010$	(0.941)	$0.932\pm0.009$	$0.952\pm0.014$	$0.941 \pm 0.013$	(1.014)	$0.984 \pm 0.025$	(1.014)
$r_8$	(0.890)	(0.868)	(0.914)	$0.672\pm0.135$	$0.926 \pm 0.096$	(1.021)	(0.969)	(0.956)
$r_9$	(0.987)	$0.997\pm0.029$	$0.969 \pm 0.030$	$1.042 \pm 0.046$	$0.944 \pm 0.015$	(1.019)	(1.026)	$1.099 \pm 0.040$
$r_1$	(0.989)	(0.938)	(1.003)	(1.001)	$0.942 \pm 0.013$	(1.015)	(1.024)	(1.015)
$\Delta m_{41}^2$						$0.49^{+0.02}_{-0.03}$	$0.48^{+0.05}_{-0.03}$	$0.49 \pm 0.02$
$\sin^2 2\vartheta_{ee}$						$0.15 \pm 0.04$	$0.48^{+0.05}_{-0.03}$ $0.10^{+0.05}_{-0.04}$	$0.16 \pm 0.04$

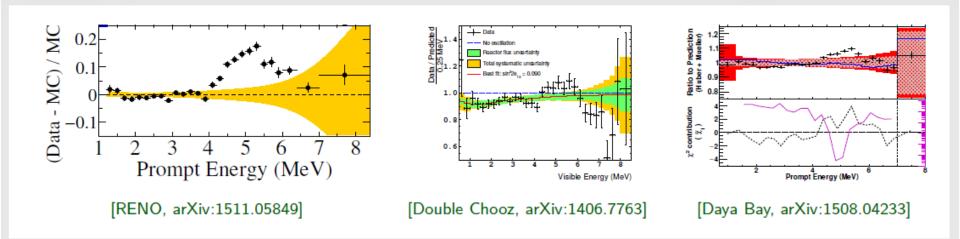
### **DYB+RENO** joint data:

2.9σ preference of U235 over oscillation-only

**Global Flux Data (evolution+rates):** 

- a) A common inaccuracy of all beta conversion predictions: disfavored at 2.9σ
- b) Oscillation-including hypothesis is favored over the oscillation-including one: at 1-2σ

# **New Spectral Feature @ Reactors**

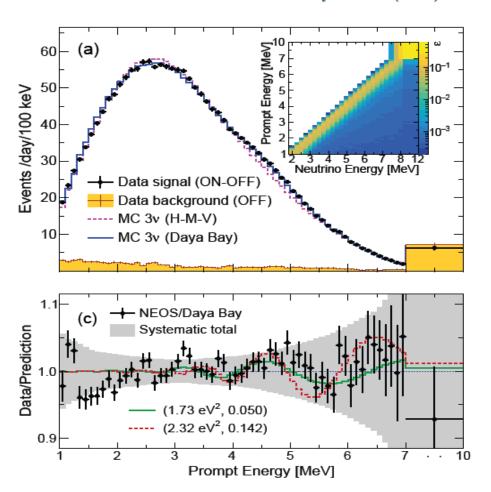


- (1) The "5 MeV bump" cannot be explained by neutrino oscillations (averaged in RENO, Double CHOOZ and Daya Bay)
- (2) Theoretical miscalculation of both the rate and spectrum?
- (3) Detector energy nonlinearity? [Mention et al, PLB 773 (2017) 307] (DYB/DC achieved better than 1% precision → see the talk by Jiajie Ling)
- (4) One may need to increase the uncertainty: e.g. about 4%-5%. [Hayes and Vogel, 2016]

### Spectral ratio result@NEOS

### **NEOS**

[PRL 118 (2017) 121802 (arXiv:1610.05134)]



- Hanbit Nuclear Power Complex in Yeong-gwang, Korea.
- Thermal power of 2.8 GW.
- Detector: a ton of Gd-loaded liquid scintillator in a gallery approximately 24 m from the reactor core.
- ► The measured antineutrino event rate is 1976 per day with a signal to background ratio of about 22.

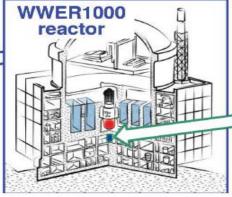
### Spectral ratio result@DANSS

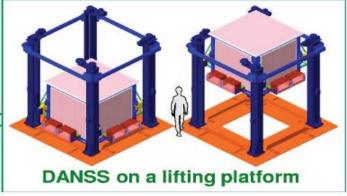
### **DANSS**

[Solvay Workshop, 1 December 2017; La Thuile 2018, 3 March 2018; Neutrino 2018, 8 June 2018]

### Detector of reactor Anti Neutrino based on Solid Scintillator

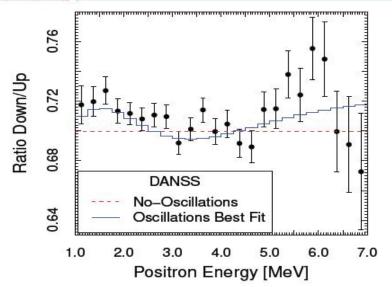






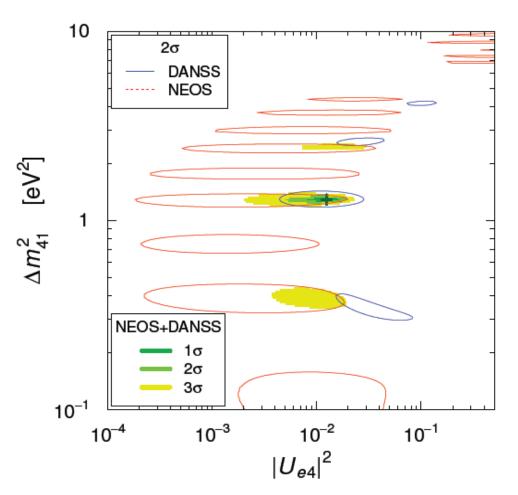
- Installed on a movable platform under a 3 GW reactor.
- Large neutrino flux.
- Reactor shielding of cosmic rays.
- Variable source-detector distance with the same detector!

 $Down = 12.7 \,\mathrm{m}$   $Up = 10.7 \,\mathrm{m}$ 



### Model independent SBL oscillations

Gariazzo et. al., PLB 782 (2018) 13



$$\sim 3.7\sigma$$

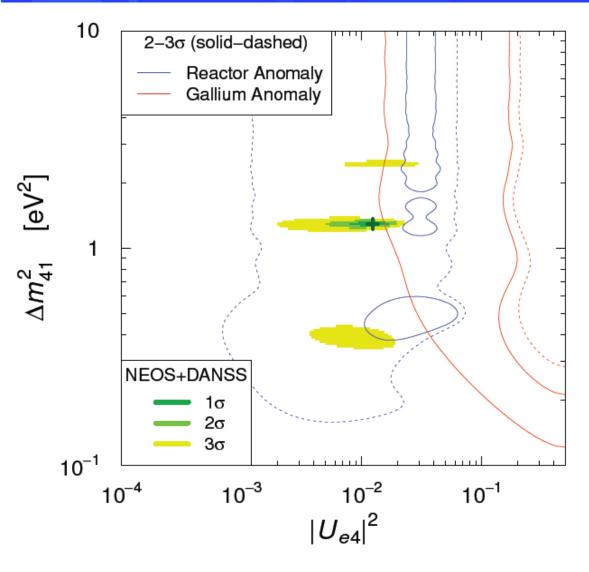
$$\Delta m_{41}^2 = 1.29 \pm 0.03$$

$$|U_{e4}|^2 = 0.012 \pm 0.003$$

$$|U_{e3}|^2 = 0.022 \pm 0.001$$

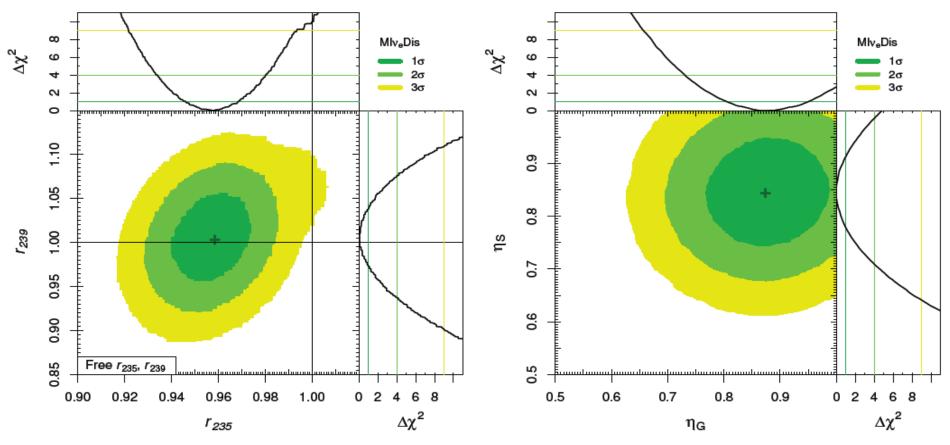
[See also Dentler, Hernandez-Cabezudo, Kopp, Machado, Maltoni, Martinez-Soler, Schwetz, arXiv:1803.10661]

### Implications for Reactor and Gallium anomalies



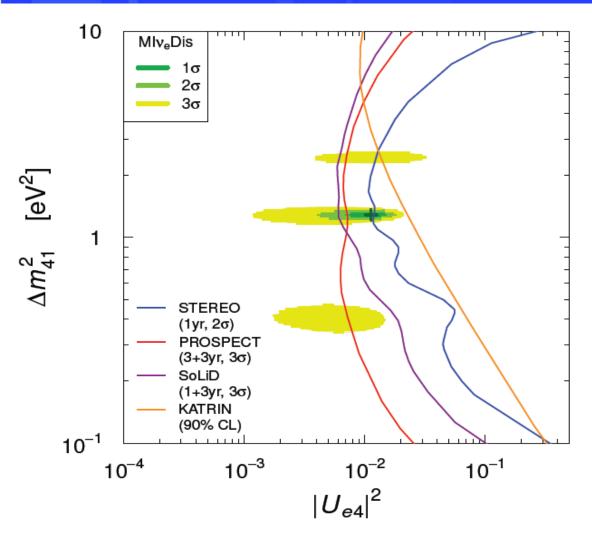
- $ightharpoonup 3\sigma$  agreement.
- $\triangleright$  2 $\sigma$  tension.
- Small overestimate of the reactor fluxes.
- Small overestimate of the GALLEX and SAGE efficiencies.

### Implications for Reactor and Gallium anomalies



- ▶ Indication of  $r_{235} < 1$ .
- Likely small overestimate of the GALLEX and SAGE efficiencies.

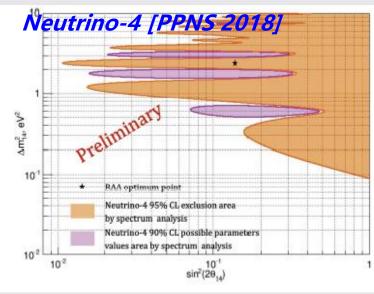
### Model independent fit and the future tests

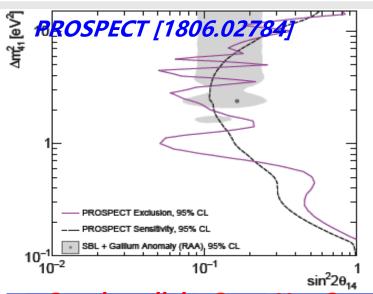


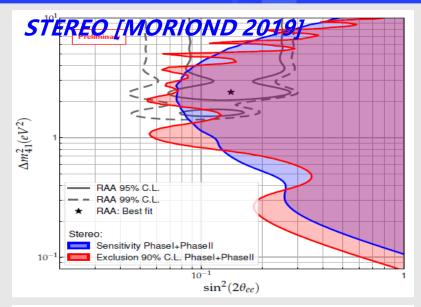
- NEOS and DANSS.
- Reactor rates with free  $^{235}$ U and  $^{239}$ Pu fluxes:  $r_{235}$  and  $r_{239}$ .
- ► Gallium data with free GALLEX and SAGE efficiencies:  $\eta_G$  and  $\eta_S$ .
- New reactor experiments: STEREO, Neutrino-4, SoLiD, PROSPECT
- Kinematic ν<sub>4</sub> mass measurement: KATRIN

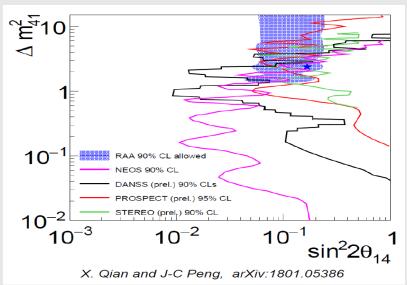
[See also Dentler, Hernandez-Cabezudo, Kopp, Machado, Maltoni, Martinez-Soler, Schwetz, arXiv:1803.10661]

# Latest results from spectral ratios



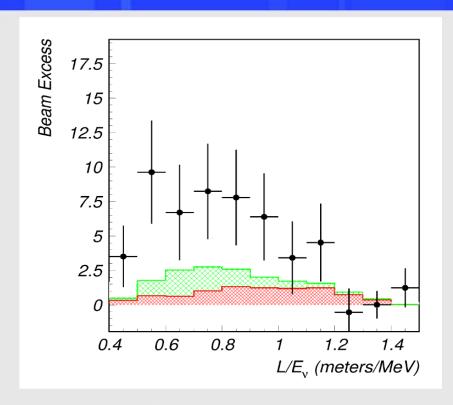


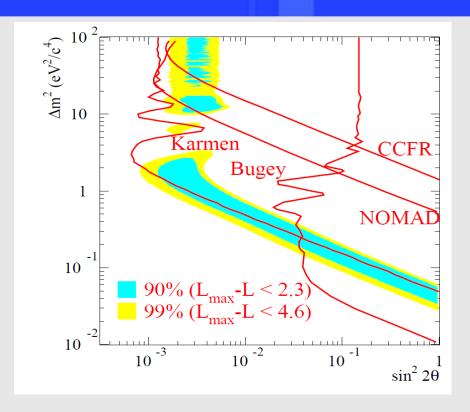




Status of short baseline oscillations in nu-mu(bar)→nu-e(bar) and nu-mu(bar) disappearance channels

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]





### Muon decay-at-rest beam:

$$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{e}$$

 $L \simeq 30 \,\mathrm{m}$ 

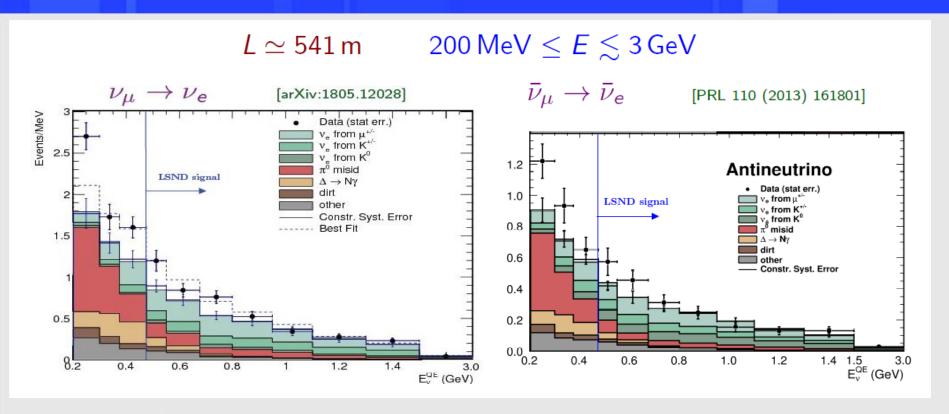
 $20 \,\mathrm{MeV} \leq E \leq 200 \,\mathrm{MeV}$ 

 $3.8\sigma$  excess

$$\Delta m^2 \gtrsim 0.2 \, \mathrm{eV}^2$$

$$\Delta m^2 \gtrsim 0.2 \,\mathrm{eV}^2 \quad (\gg \Delta m_\mathrm{A}^2 \gg \Delta m_\mathrm{S}^2)$$

### **MiniBooNE**

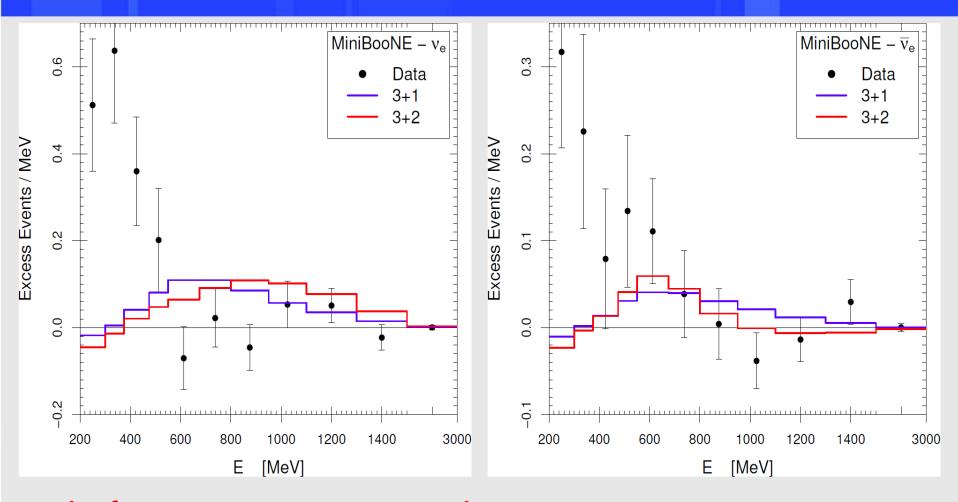


Purpose: check LSND signal with different L&E, but the same L/E (>475 MeV)

~4.5 $\sigma$  (2.8 $\sigma$ ) excess: unidentified backgrounds in low energy ranges?  $\rightarrow$  MicroBooNE.

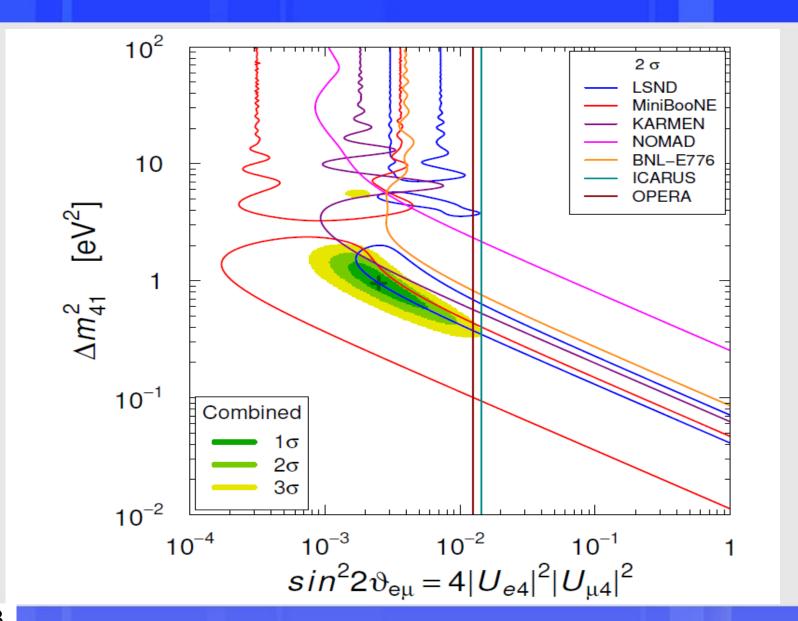
A pragmatic approach: (E>475 MeV) [arXiv: 1308.5288]

# MiniBooNE low energy bins



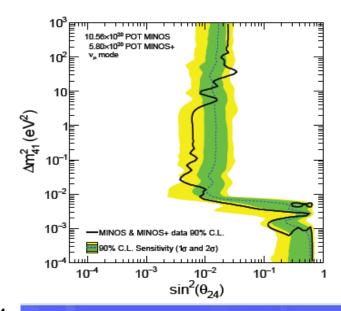
Fit of MB Low-Energy Excess requires small mass splitting and large mixing angle, which are in contradiction with ICARUS/OPERA and the disappearance data.

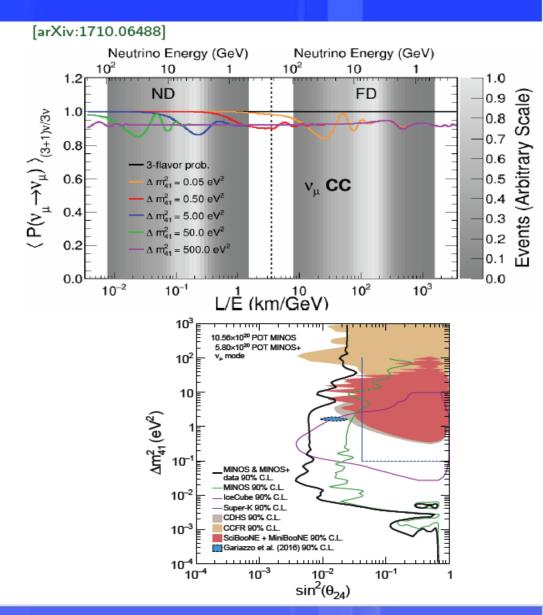
# Appearance data



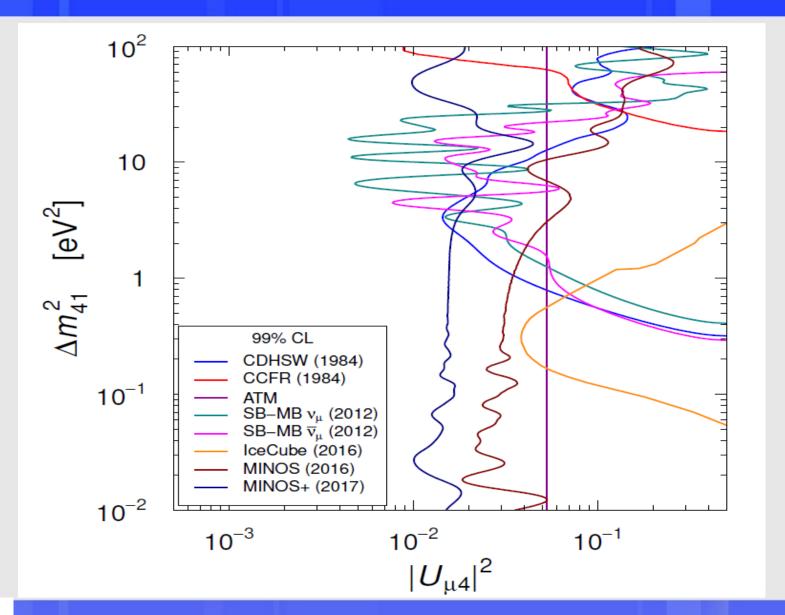
### MINOS+







# All the results in (anti)v<sub>µ</sub> disappearance



Global fit of nu-e(bar) disappearance, nu-mu(bar)→nu-e(bar) and nu-mu(bar) disappearance data

Based on the latest update of Gariazzo, Giunti, Laveder, YFL, arXiv:1703.00860

### SBL oscillations in the 3+1 scheme

In SBL experiments  $\Delta_{21} \ll \Delta_{31} \ll 1$ .

$$P_{\substack{(-) \ \nu_{\alpha} \to \nu_{\beta}}}^{\mathrm{SBL}} \simeq \sin^2 2 \vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

 $\sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha4}|^2|U_{\beta4}|^2$ 

$$P_{\substack{(-) \ \nu_{\alpha} \to \nu_{\alpha}}}^{\mathrm{SBL}} \simeq 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E}\right)$$

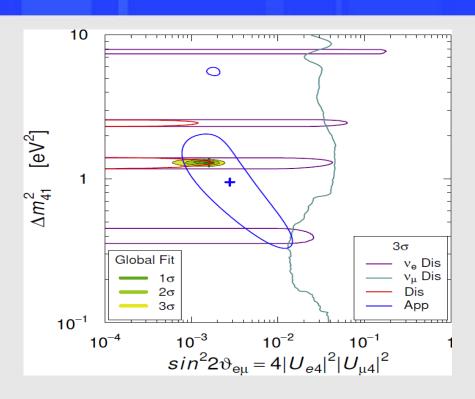
 $\sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha4}|^2 \left(1 - |U_{\alpha4}|^2\right)$ 

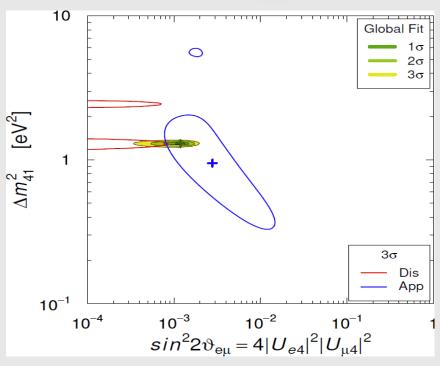
▶ Amplitude of  $\nu_{\mu} \rightarrow \nu_{e}$  transitions:

$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu 4}|^2 \simeq \frac{1}{4}\sin^2 2\vartheta_{ee}\sin^2 2\vartheta_{\mu\mu}$$

- ▶ Upper bounds on  $\nu_e$  and  $\nu_\mu$  disappearance  $\Rightarrow$  strong limit on  $\nu_\mu \rightarrow \nu_e$  [Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, Giunti, Grimus, EPJC 1 (1998) 247]
- Similar constraint in 3+2, 3+3, ...,  $3+N_s!$  [Giunti, Zavanin, MPLA 31 (2015) 1650003]

# **Appearance-Disappearance Tension**



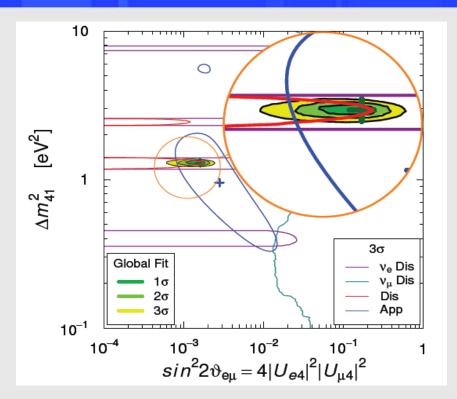


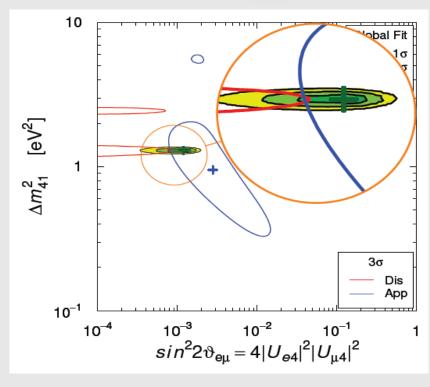
Without (left) and with (right) MINOS+ data (both without the MB low energy bins)

$$\chi^2_{PG}/NDF_{PG} = 7.8/2 \Rightarrow GoF_{PG} = 2\%$$

$$\chi^2_{PG}/NDF_{PG} = 18.3/2 \Rightarrow GoF_{PG} = 0.01\%$$

# **Appearance-Disappearance Tension**





> Without (left) and with (right) MINOS+ data (both without the MB low energy bins)

$$\chi^2_{PG}/NDF_{PG} = 7.8/2 \Rightarrow GoF_{PG} = 2\%$$
  $\chi^2_{PG}/NDF_{PG} = 18.3/2 \Rightarrow GoF_{PG} = 0.01\%$ 

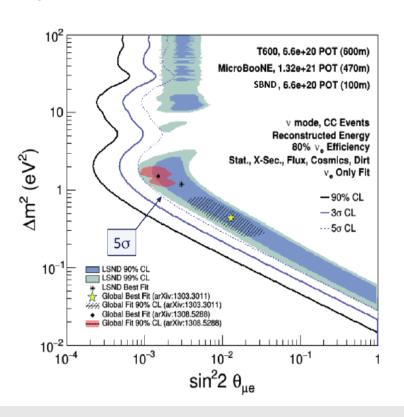
$$\chi^2_{PG}/\mathsf{NDF}_{PG} = 18.3/2 \Rightarrow \mathsf{GoF}_{PG} = 0.01\%$$

From Mild to Strong tension → New physics beyond 3+1 (3+N) vacuum mixing??

# Future test of the appearance channel

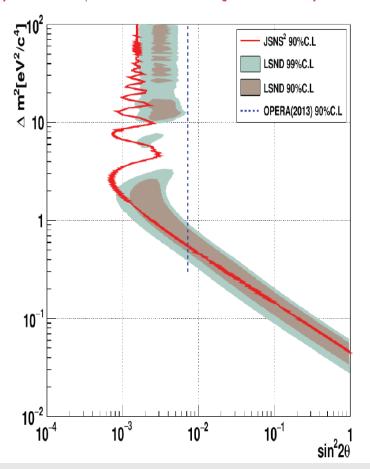
### SBN PROGRAM @ FERMILAB

Definitive program to address LSND/MiniBoone anomalies in next ~5 years.



### JSNS2 @ J-PARK

Sensitivity of the JSNS2 experiment with the latest configuration (1 MW × 3 years × 1 detector).



### Conclusion

- a) Interesting model-independent indications of short baseline oscillations from reactors (DANSS & NEOS)
- b) Reactor and Gallium Anomalies → Need revision of the U235 calculation and small decrease of the GALLEX and SAGE efficiencies. → consistent with the fuel evolution data
- c) Many on-going experiments will check the indication in the next several years:
- DANSS, NEOS, STEREO, Neutrino-4, PROSPECT, SoLid, CHANDLER, ...
- d) The MINOS+ result disfavors the LSND signal in the 3+1 (3+N) vacuum mixing scheme
- → future direct test at SBN@Fermi Lab and JSNS2@J-PARC

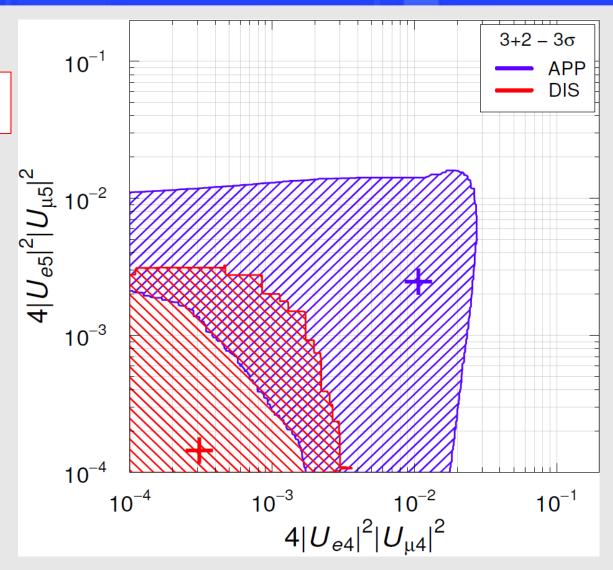
# Thanks!

### **Backup**

### The 3+2 scheme and more

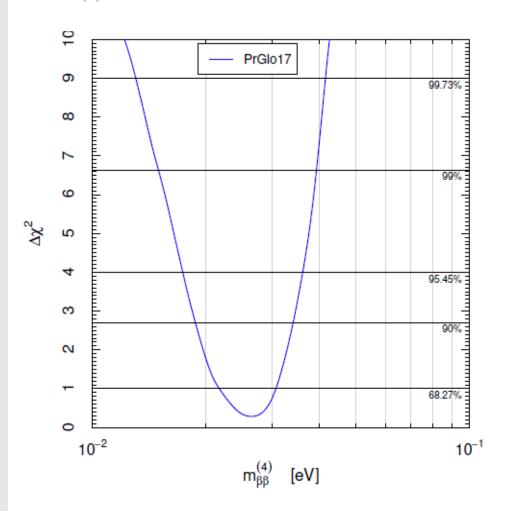
 $\sin^2 2\vartheta_{\alpha\beta}^{(k)} \simeq \frac{1}{4} \sin^2 2\vartheta_{\alpha\alpha}^{(k)} \sin^2 2\vartheta_{\beta\beta}^{(k)},$ 

arXiv:1508.03172



# **Light Sterile Neutrinos@0νββ**

$$m_{\beta\beta} = |U_{e1}|^2 m_1 + |U_{e2}|^2 e^{i\alpha_{21}} m_2 + |U_{e3}|^2 e^{i\alpha_{31}} m_3 + |U_{e4}|^2 e^{i\alpha_{41}} m_4$$



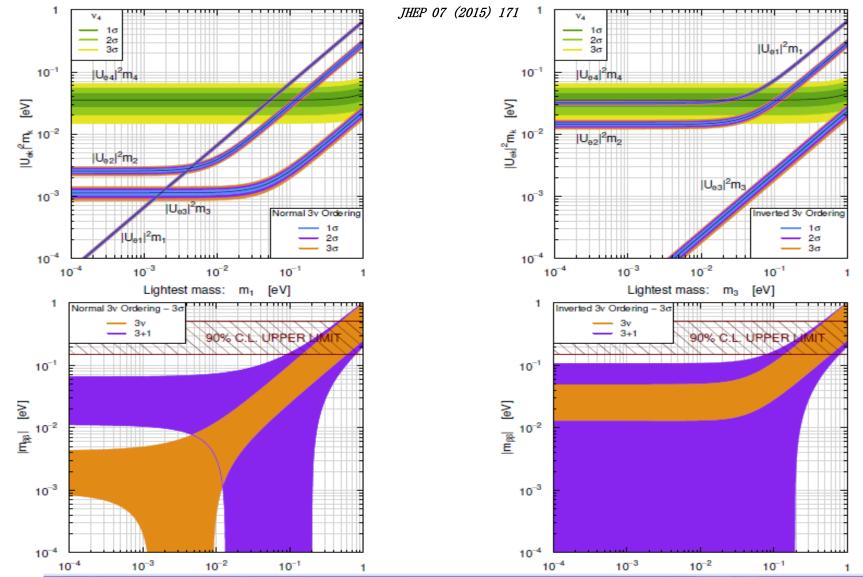
$$m_{\beta\beta}^{(k)} = |U_{ek}|^2 m_k$$

$$m_1 \ll m_4$$
 $\downarrow \downarrow$ 
 $m_{\beta\beta}^{(4)} \simeq |U_{e4}|^2 \sqrt{\Delta m_{41}^2}$ 

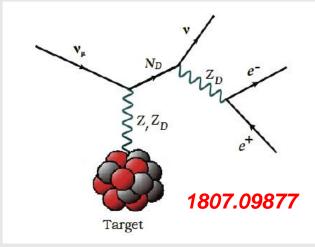
### warning:

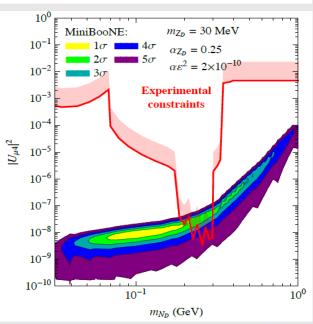
possible cancellation with  $m_{etaeta}^{(3
u)}$ 

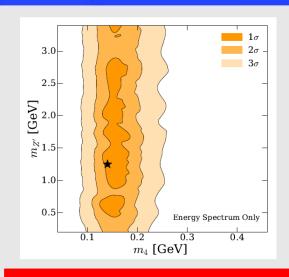
[Barry, Rodejohann, Zhang, JHEP 07 (2011) 091]
 [Li, Liu, PLB 706 (2012) 406]
 [Rodejohann, JPG 39 (2012) 124008]
 [Girardi, Meroni, Petcov, JHEP 1311 (2013) 146]
 [CG, Zavanin, JHEP 07 (2015) 171]

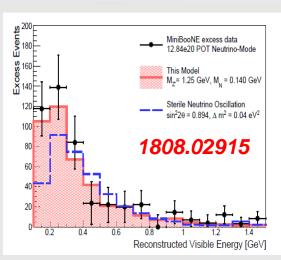


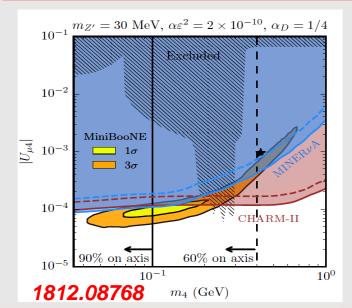
### **Examples of New Physics for the MB Excess**











See also other models and constraints: 1810.07185; 1810.01000; 1808.07460