

*String fusion approach for MC modelling of  
pp, pA and AA collisions and possible  
application in Geant4 FTF and QGS*

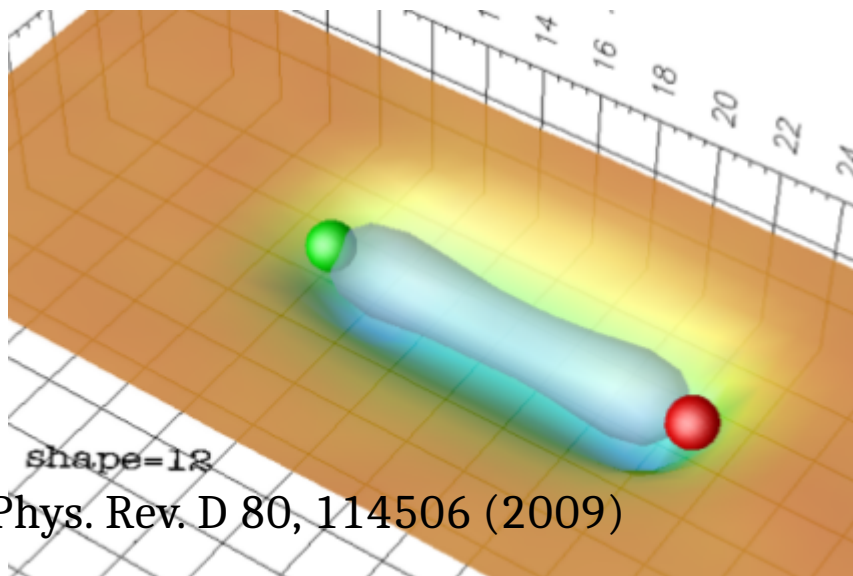
**Vladimir Kovalenko**

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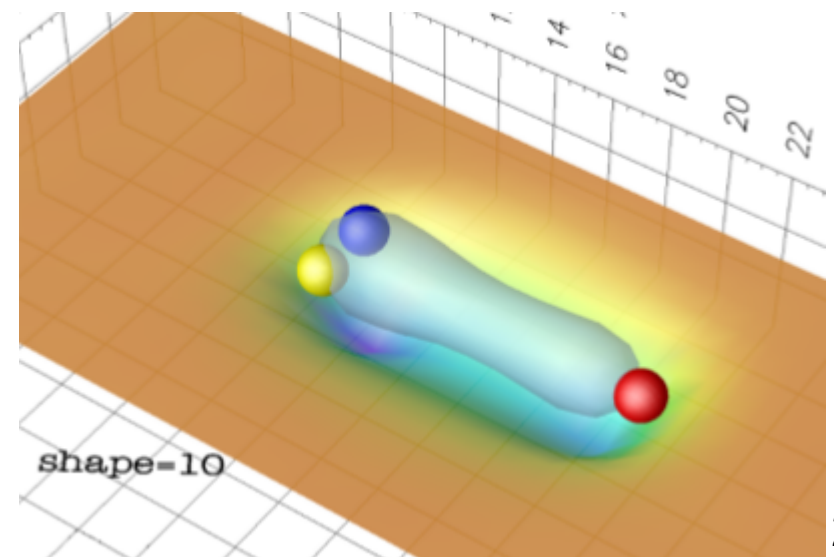
Geant4 Hadronic Working Group Meeting  
**Wednesday 14 Nov 2018, 17:00**

## Strings

- Strings are one-dimensional extended objects
- Strings first were introduced during the late 1960s and early 1970s as a theory of hadrons
- It was able to describe such phenomena as Regge trajectories: the mesons families were discovered with masses related to spins in a way that one can be expected from rotating strings.
- Strings as colour tubes, stretched between pair quark-antiquark are found also in the lattice QCD calculations



[6.1] Phys. Rev. D 80, 114506 (2009)

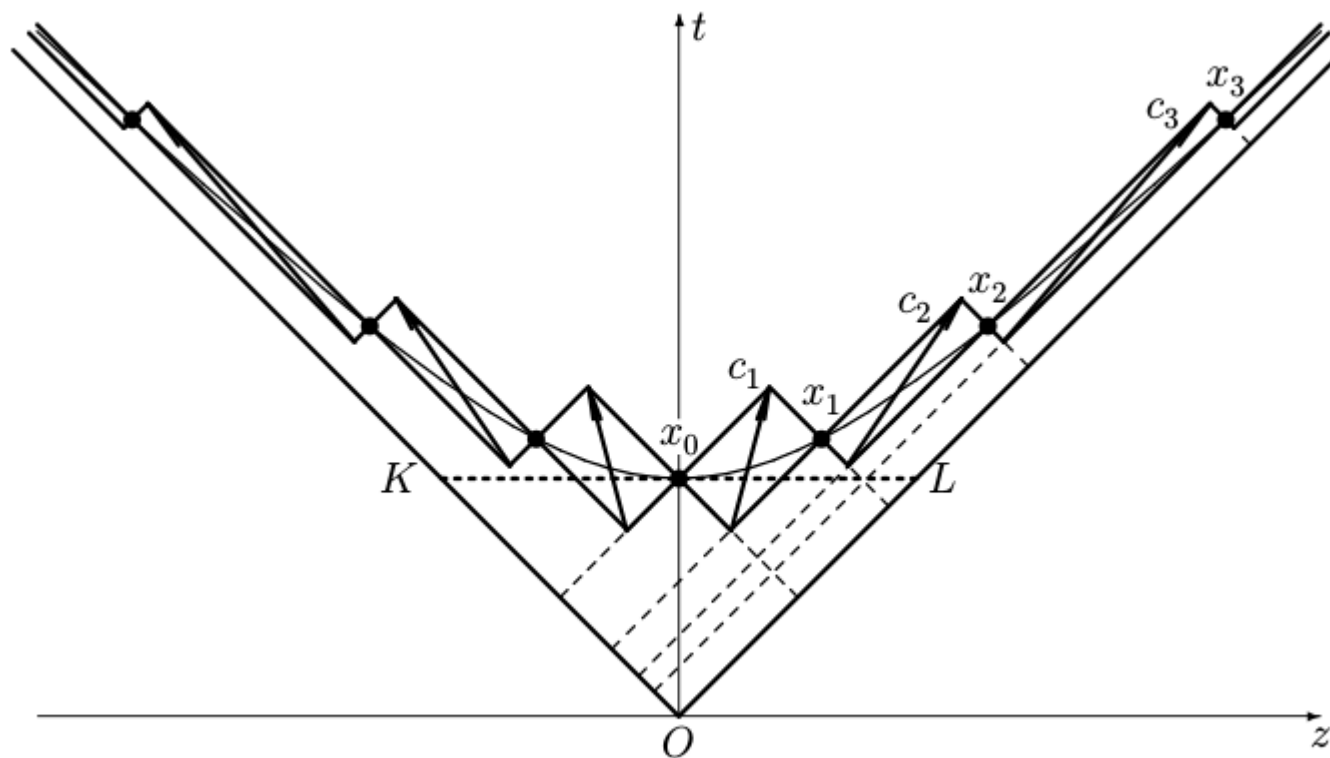


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# String fragmentaion

$$dP(x) = S_0^{-1} \exp(-S_x/S_0) dS_x$$

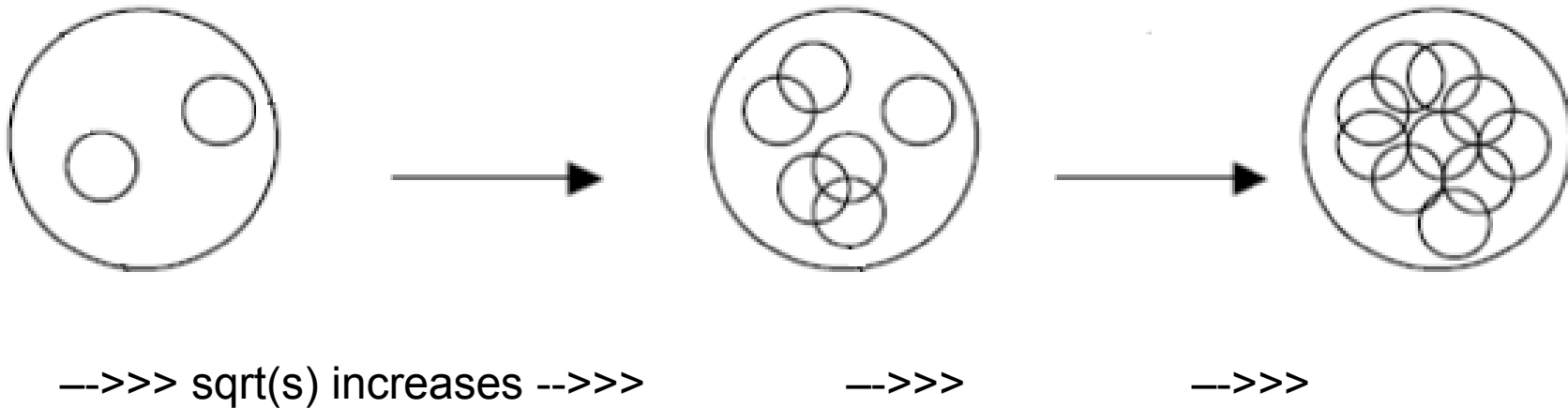
- Dominant string decay



The dominant string decay.

## Application to pp and AA collisions...

- A contains valence quark-diquark pair and a several sea quark-antiquark pairs
- Due to MPI it is possible to produce several strings at the same time-> they will overlap in transverse plane!
- Effect is more crucial in AA collisions



## String fusion

$$Q^2(n) = \left( \sum_{i=1}^n \bar{Q}_i(1) \right)^2 = \sum_{i=1}^n Q_i^2(1) + \sum_{i \neq j} \bar{Q}_i(1) \cdot \bar{Q}_j(1)$$

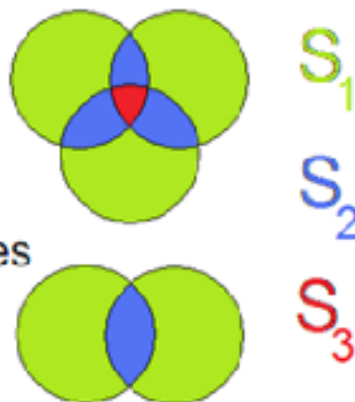
$$\langle Q^2(n) \rangle = nQ^2(1)$$

overlaps

SFM

$$C = \{S_1, S_2, \dots\}$$

$S_k$  – area covered k-times



$$\langle \mu \rangle_k = \mu_0 \sqrt{k} \frac{S_k}{\sigma_0}$$

$$\langle p_t^2 \rangle_k = p_0^2 \sqrt{k}$$

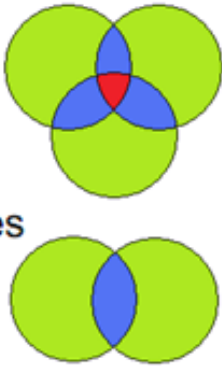
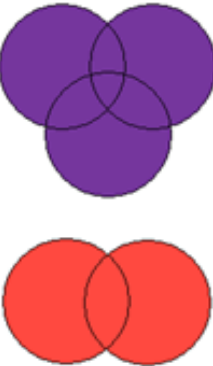
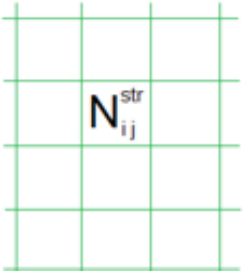
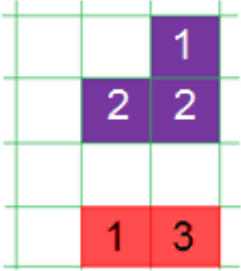
$$\langle p_t \rangle_k = p_0 \sqrt[4]{k}$$

$S_k$  – area, where k strings are overlapping,  $\sigma_0$  single string transverse area,  $\mu_0$  and  $p_0$  – mean multiplicity and transverse momentum from one string

M. A. Braun, C. Pajares, Nucl. Phys. B 390 (1993) 542.

M. A. Braun, R. S. Kolevator, C. Pajares, V. V. Vechernin, Eur. Phys. J. C 32 (2004) 535.

# String fusion: mechanism versions

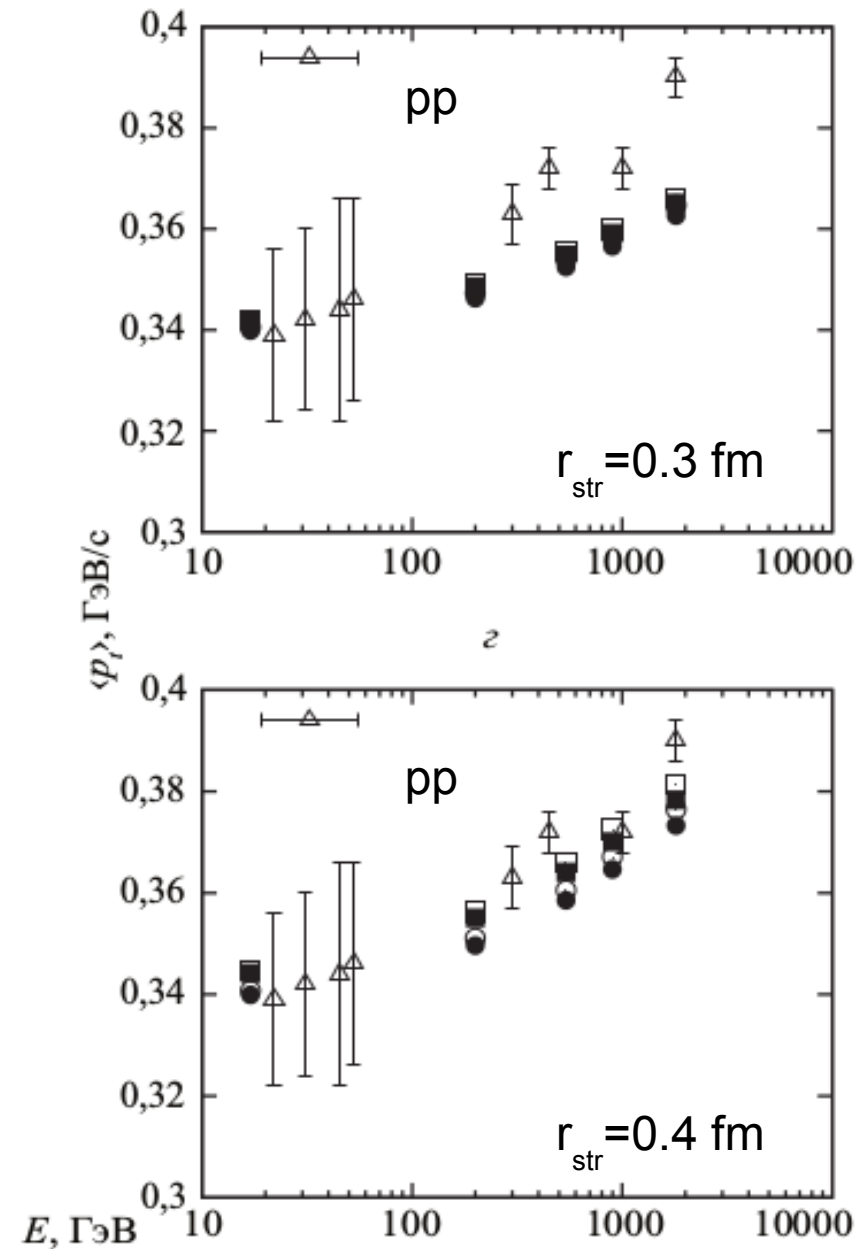
	"overlaps" (local fusion)	"clusters" (global fusion)
<b>SFM</b>	<div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <math>C = \{S_1, S_2, \dots\}</math>  <math>S_k</math> – area covered k-times                 </div> <div style="text-align: center;">  </div> <div style="margin-left: 20px;"> <math>S_1</math>  <math>S_2</math>  <math>S_3</math> </div> </div>	<div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <math>C = \left\{ \begin{matrix} S_1^{cl}, S_2^{cl}, \dots \\ N_1^{str}, N_2^{str}, \dots \end{matrix} \right\}</math>  <math>k_i^{cl} = \frac{N_i^{str} \cdot \sigma_0}{S_i^{cl}}</math> </div> <div style="text-align: center;">  </div> <div style="margin-left: 20px;"> <math>N_1^{str} = 3</math>  <math>S_1^{cl}</math>  <math>N_2^{str} = 2</math>  <math>S_2^{cl}</math> </div> </div>
<b>cellular analog of SFM</b>	<div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <math>C = \{N_{ij}^{str}\}</math>  <math>k_{ij} = N_{ij}^{str}</math> – "occupation" numbers                 </div> <div style="text-align: center;">  </div> </div>	<div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <math>C = \left\{ \begin{matrix} S_1^{cl}, S_2^{cl}, \dots \\ N_1^{str}, N_2^{str}, \dots \end{matrix} \right\}</math>  <math>k_i^{cl} = \frac{N_i^{str} \cdot \sigma_0}{S_i^{cl}}</math> </div> <div style="text-align: center;">  </div> <div style="margin-left: 20px;"> <math>S_1^{cl} = 3\sigma_0; N_1^{str} = 5; k_1^{cl} = 5/3</math>  <math>S_2^{cl} = 2\sigma_0; N_2^{str} = 4; k_2^{cl} = 2</math> </div> </div>

M. A. Braun, C. Pajares, Nucl. Phys. B 390 (1993) 542.

M. A. Braun, R. S. Kolevator, C. Pajares, V. V. Vechernin, Eur. Phys. J. C 32 (2004) 535.

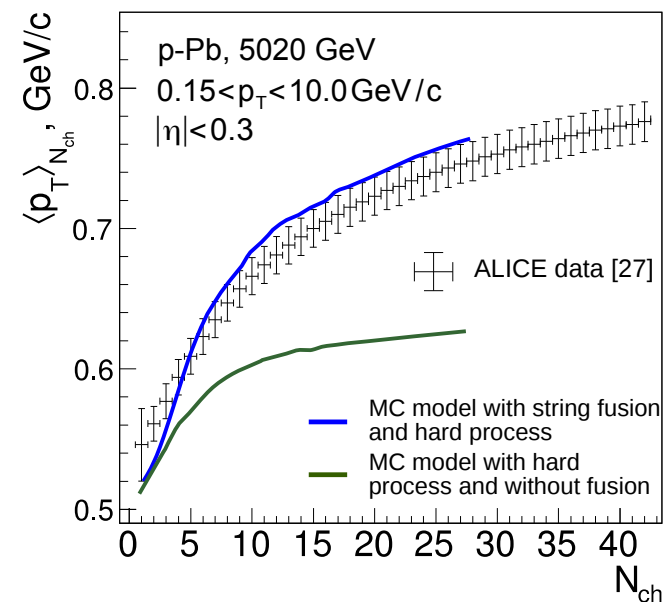
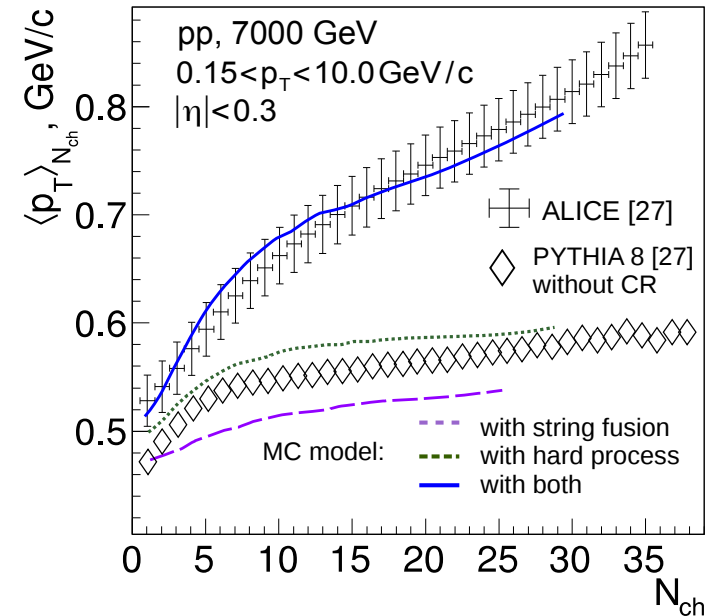
## Effects of string fusion: Increase of mean $p_t$ with energy

- Number of sea pairs growth with  $\sqrt{s}$
- More strings are formed  $\rightarrow$  more overlaps
- $\rightarrow$  more fusion,  $p_t$  grows



V. V. Vechernin, I. A. Lakomov, A. M. Puchkov, Vestn. SPb. Univ., Ser. 4: Fiz. Khim., No. 3, 3 (2010)

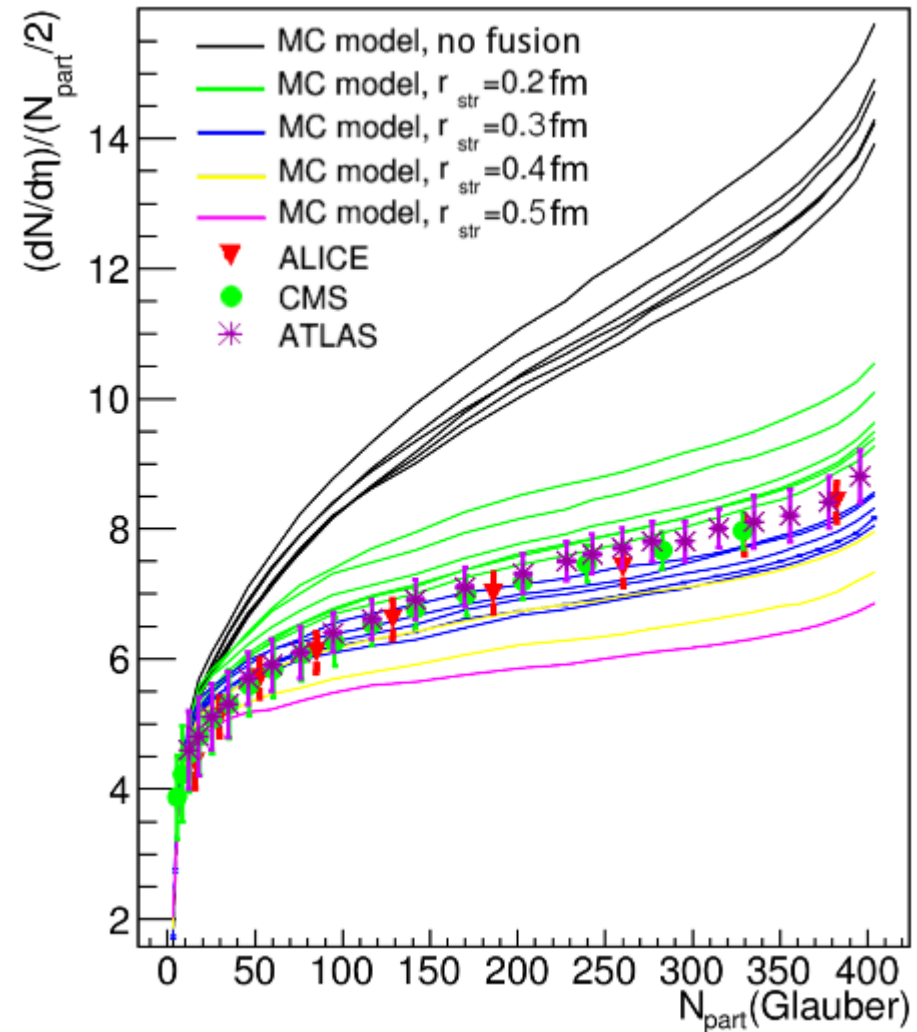
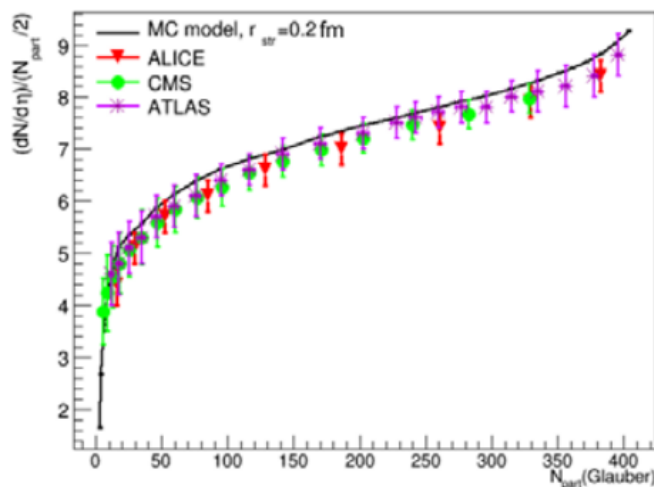
Effects of string fusion:  
 Increase of mean  $p_t$   
 with multiplicity:  
 In pp and p-A collisions





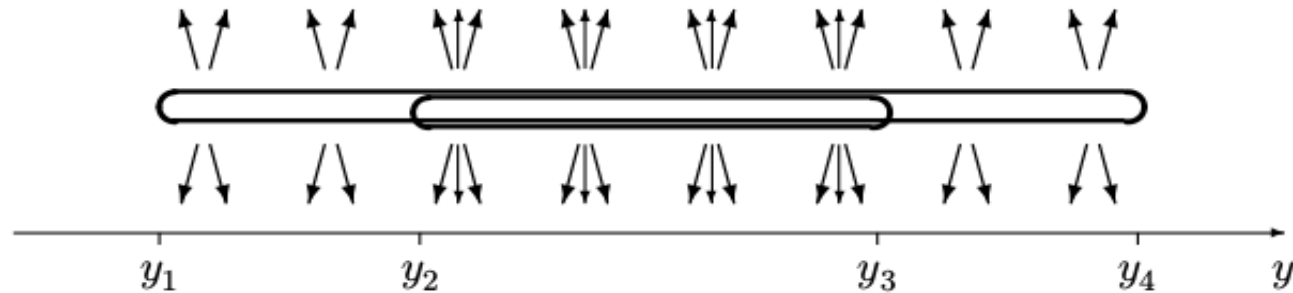
## Decrease of multiplicity

- Decrease of multiplicity, which is pronounced especially in PbPb collisions (compared to non-fusion case)
- Cluster of  $n$  fused strings emits  $\sqrt{n}$  times less particles, than  $n$  independent strings

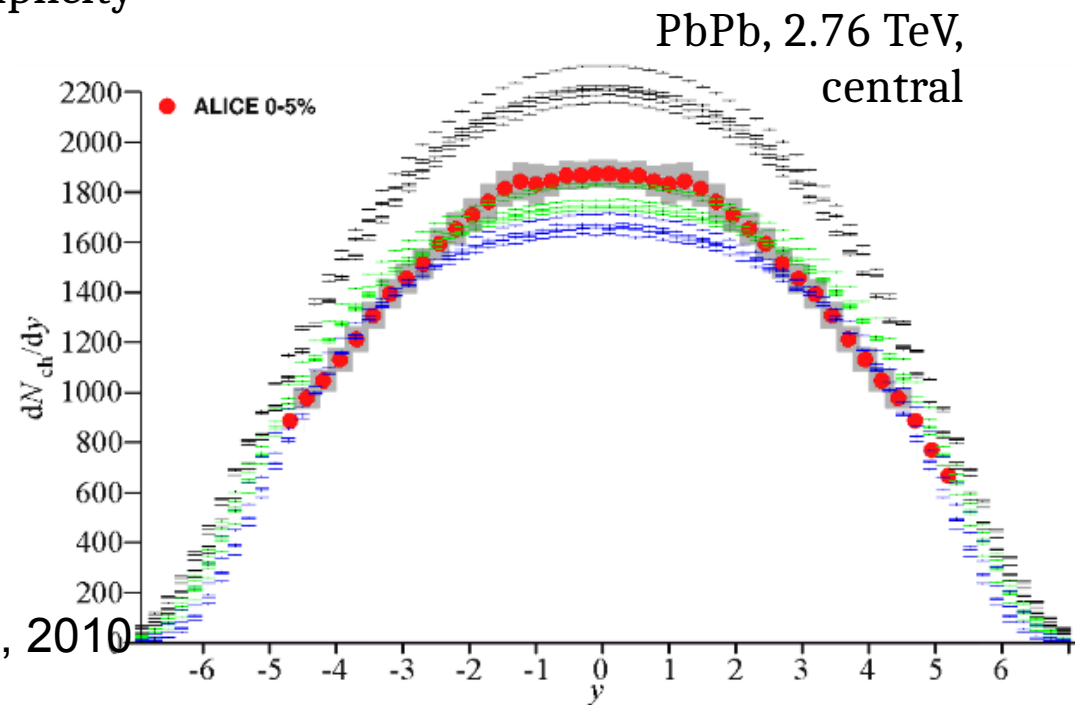
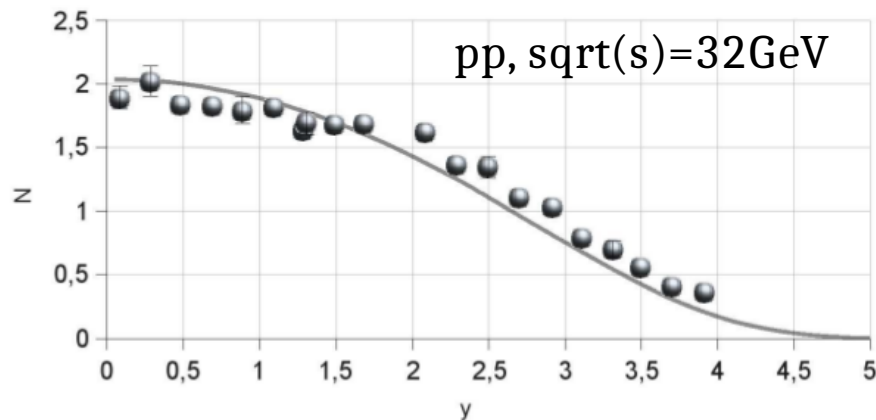


V. Kovalenko. PoS (QFTHEP 2013) 052, 2013

## Rapidity distribution of multiplicity



- Accounting the finite rapidity width of the strings, together with string fusion, allows to calculate rapidity distribution of the multiplicity

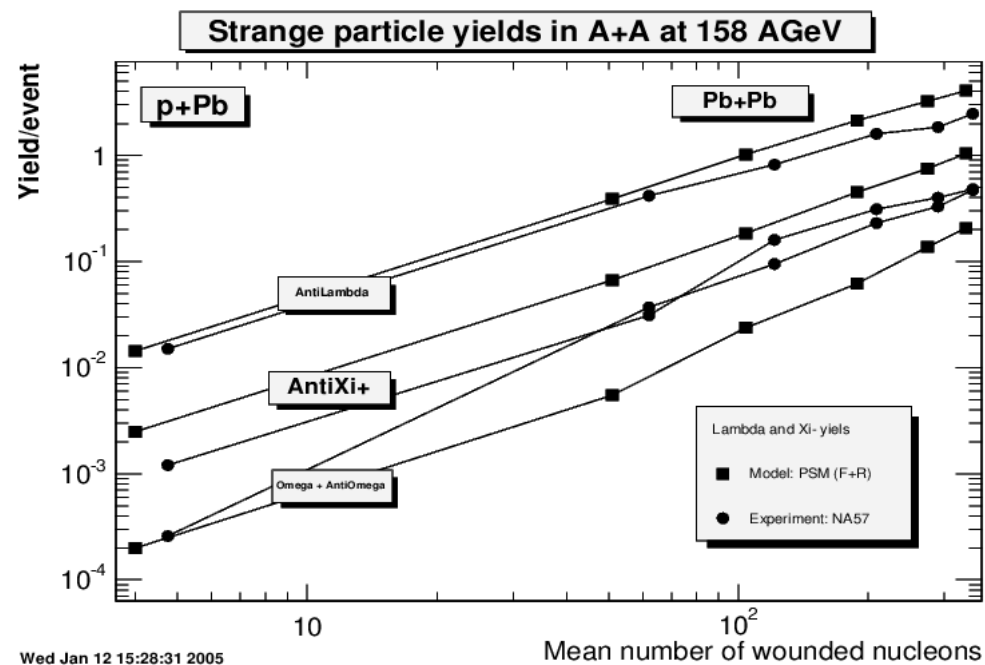
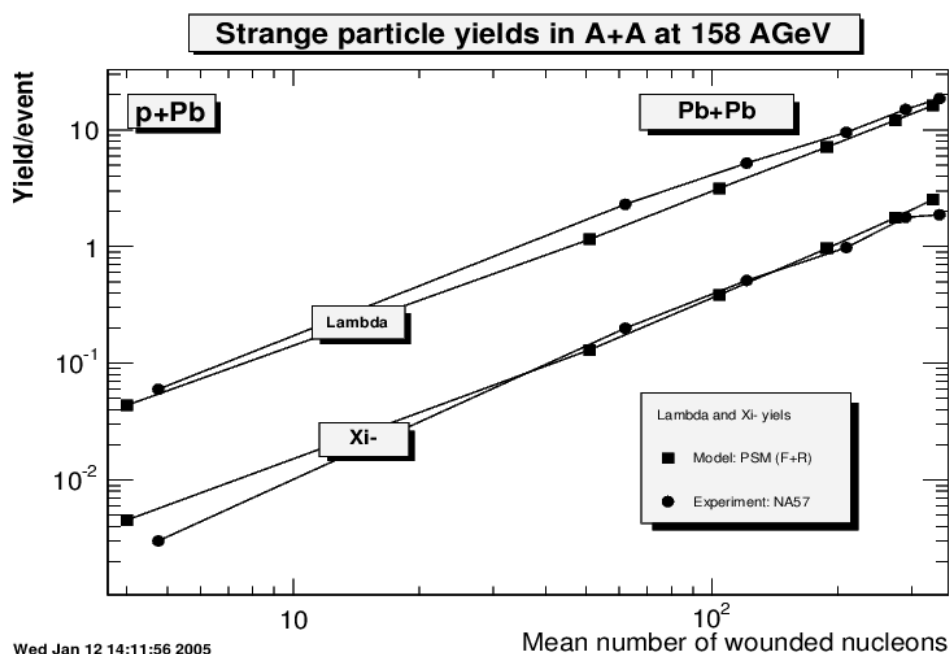


V. Kovalenko. Proc. Science and Progress, SPb, 2010  
 V. Kovalenko. PoS (QFTHEP 2013) 052, 2013

# Centrality dependence of strange particles yields at SPS

- Strings with higher tension  $\rightarrow$  more probability to produce heavier particles

- Schwinger mechanism: 
$$\frac{d^2 N_{ch}}{dp_T^2} \sim \exp\left(\frac{-\pi(p_T^2 + m^2)}{t}\right)$$

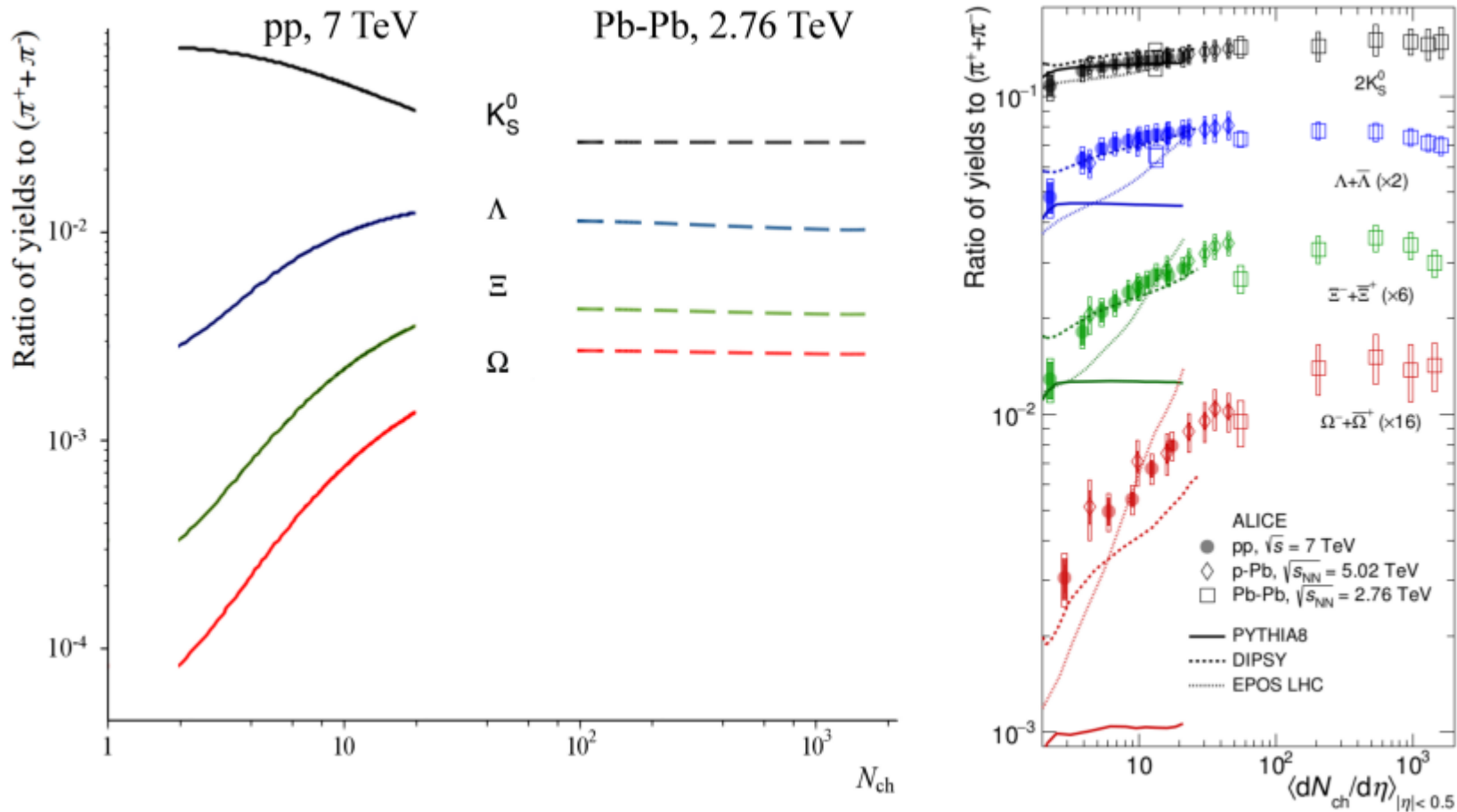


J. Schwinger, Phys. Rev. 82, 664 (1951); T. S. Biro, H. B. Nielsen, and J. Knoll, Nucl. Phys. B 245, 449 (1984).

G. Feofilov, et. al, Proc. QFTHEP 2004 p. 412-418,  
 Physics of Particles and Nuclei 42, 911-962 (2011)

V. P. Kondrat'ev, G. A. Feofilov,

# Multiplicity dependence of strangeness production at LHC



Feofilov G., Kovalenko V., Puchkov A. // arXiv:1710.08895 [hep-ph]. 2017.

Feofilov G., Kovalenko V., Puchkov A. // EPJ Web of Conferences. 2018. Vol. 171, P. 18003, arXiv:1711.00842 [nucl-th].

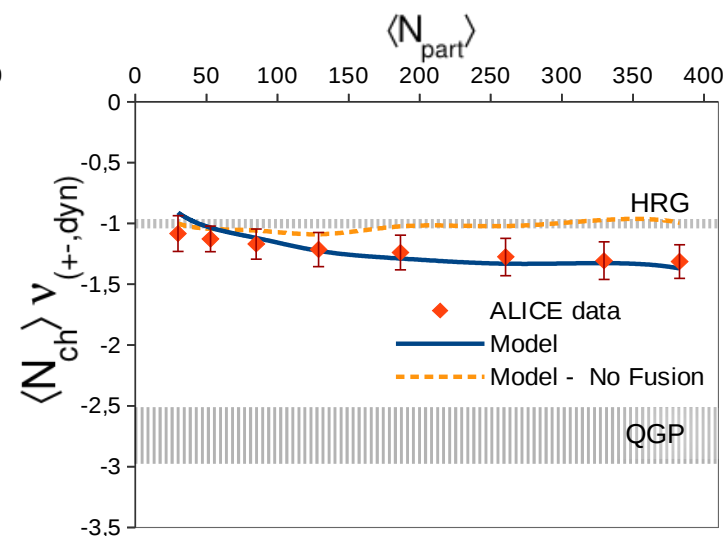
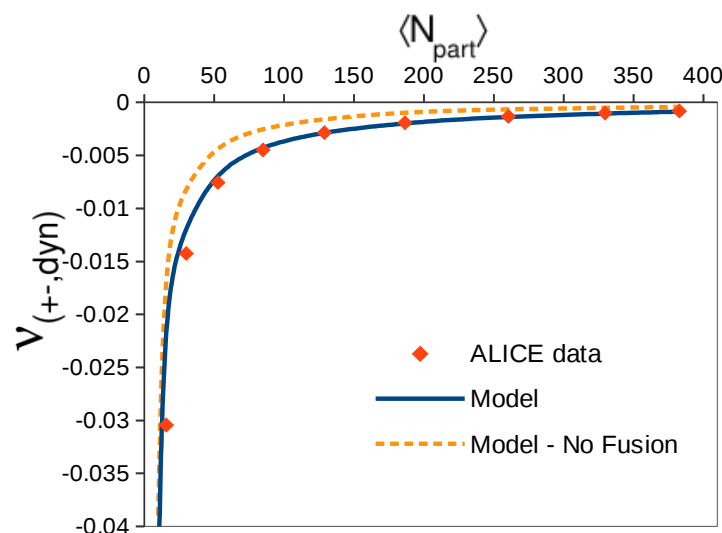
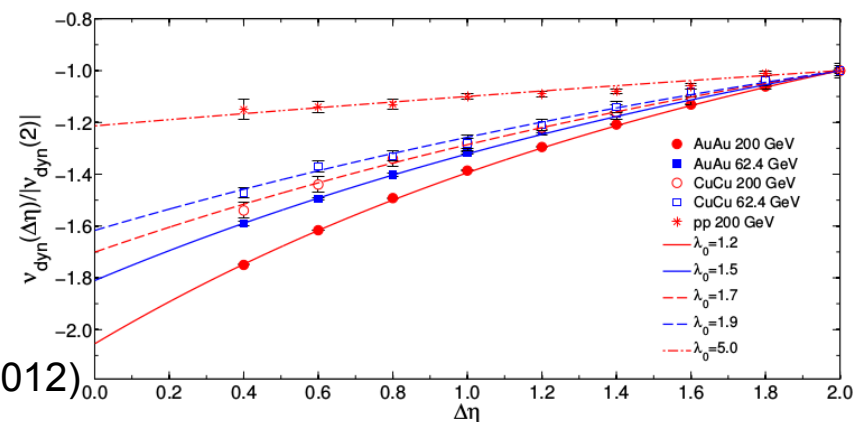
Experiment: J. Adam, et al (ALICE Collaboration) // Nature Physics 13, 535-539 (2017). 12

# Net charge fluctuations

$$v_{\text{dyn}} = \left\langle \left( \frac{N_+}{\langle N_+ \rangle} - \frac{N_-}{\langle N_- \rangle} \right)^2 \right\rangle - \frac{1}{\langle N_+ \rangle} + \frac{1}{\langle N_- \rangle}$$

- String model enables to describe the dependence on the rapidity window width of net charge fluctuations
- The correlation length decreases with increase of sqrt(s), from peripheral to central, from pp to AA -> more fusion, more intensive sources emit particles

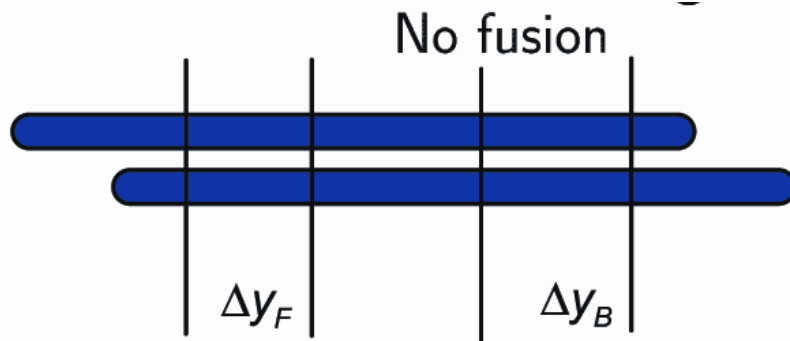
A. Titov, V. Vechernin, PoS (Baldin ISHEPP XXI) 047 (2012)



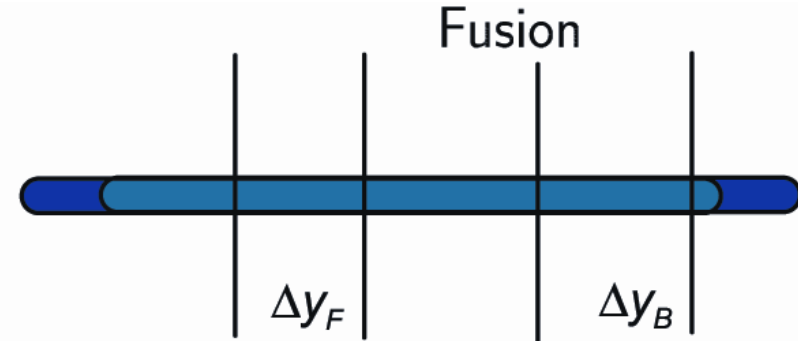
V. Kovalenko,  
PoS(Confinement2018)254  
(2018, in press)

## Long-range (forward-backward) correlations

- Sensitive tool for studying of string fusion phenomena



$$\langle n_F \rangle = 2\mu_0, \quad \langle p_{tB} \rangle = \bar{p}$$



$$\langle n_F \rangle = \sqrt{2}\mu_0, \quad \langle p_{tB} \rangle = \sqrt[4]{2}\bar{p}$$

Positive correlations  $n-n$ ,  $p_t-p_t$ .  
 $p_t-n$  correlations can be negative!

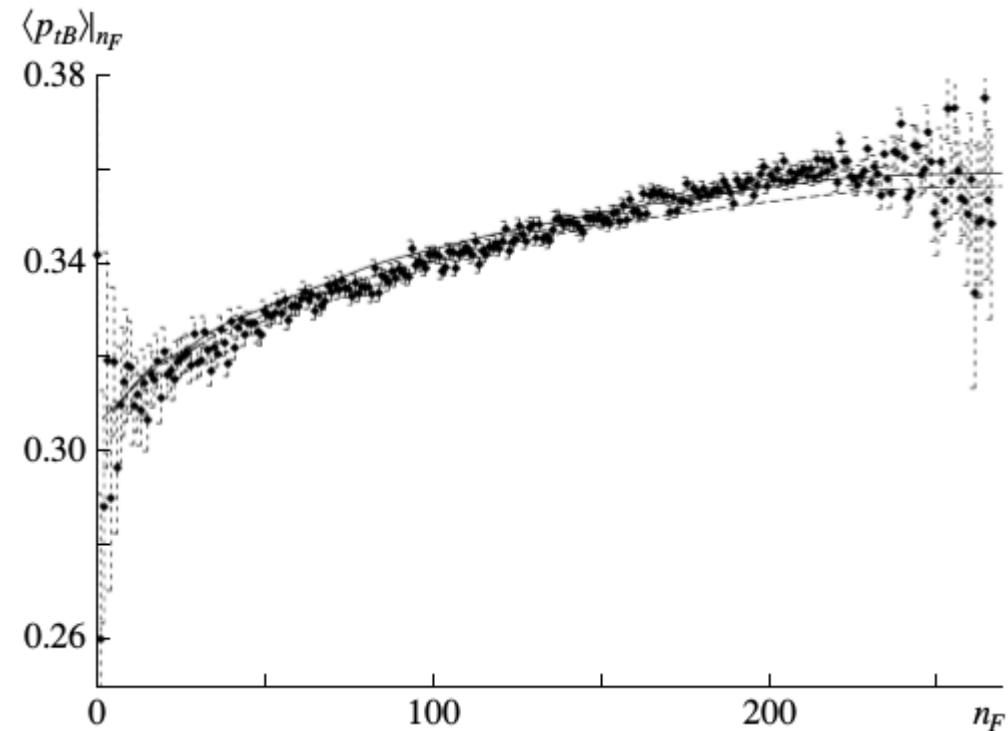
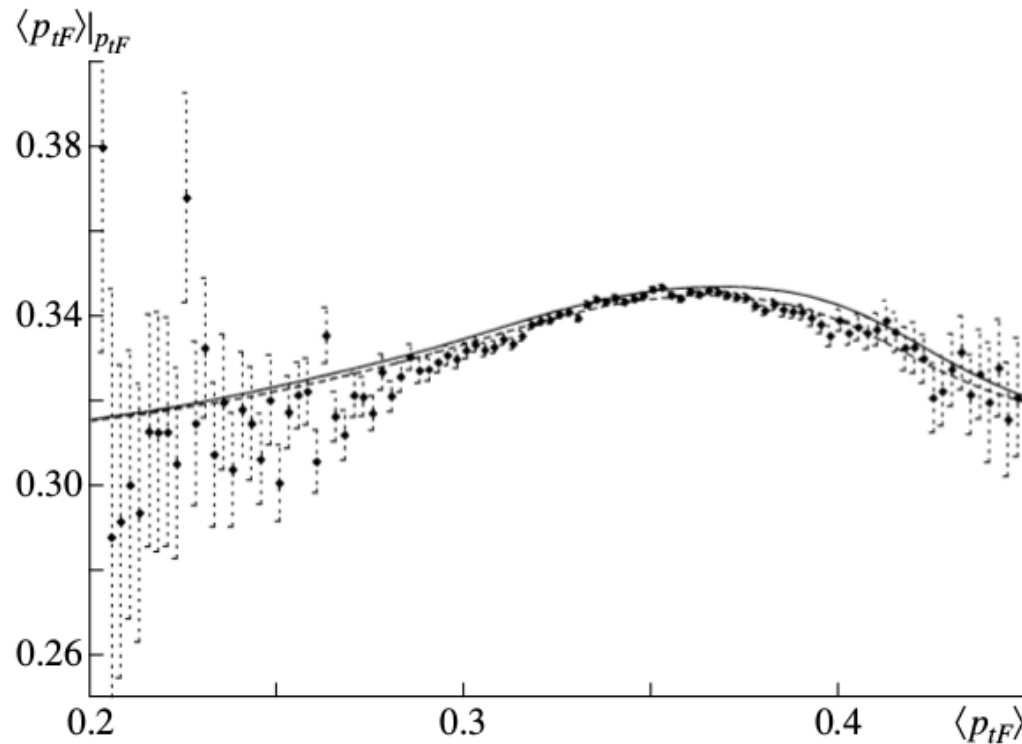
- Important (intensive) observable

event mean transverse momentum  $p_{tF(B)} = \frac{p_{t1} + \dots + p_{tn_{F(B)}}}{n_{F(B)}}$

characterizes whole the event,  
 expected to be robust against centrality determination issues

# Long-range (forward-backward) correlations at SPS energy

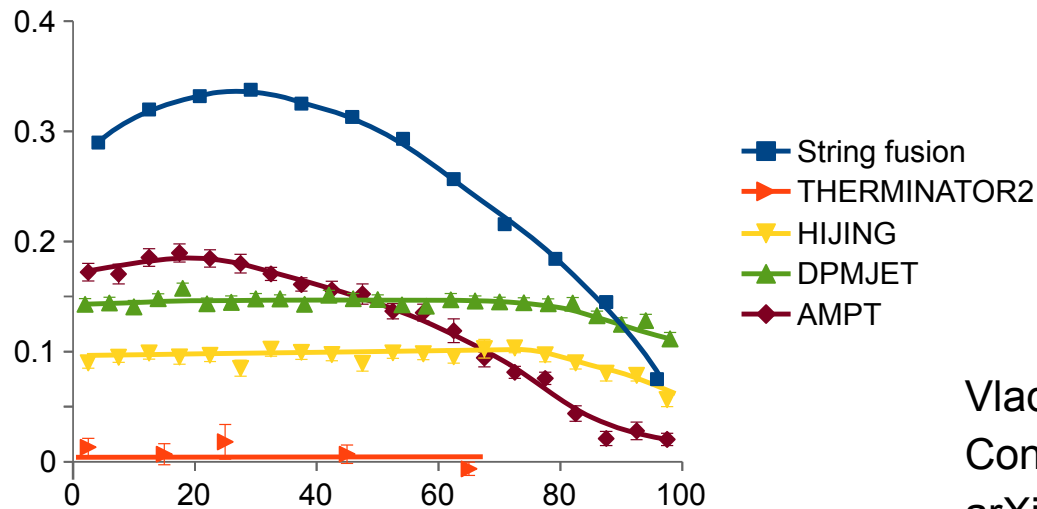
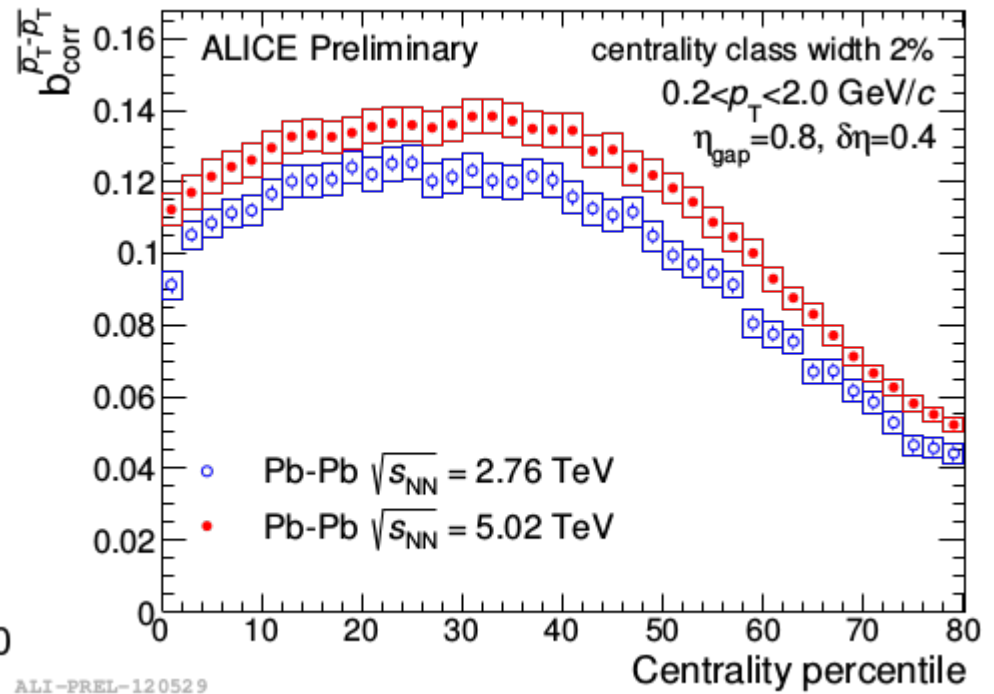
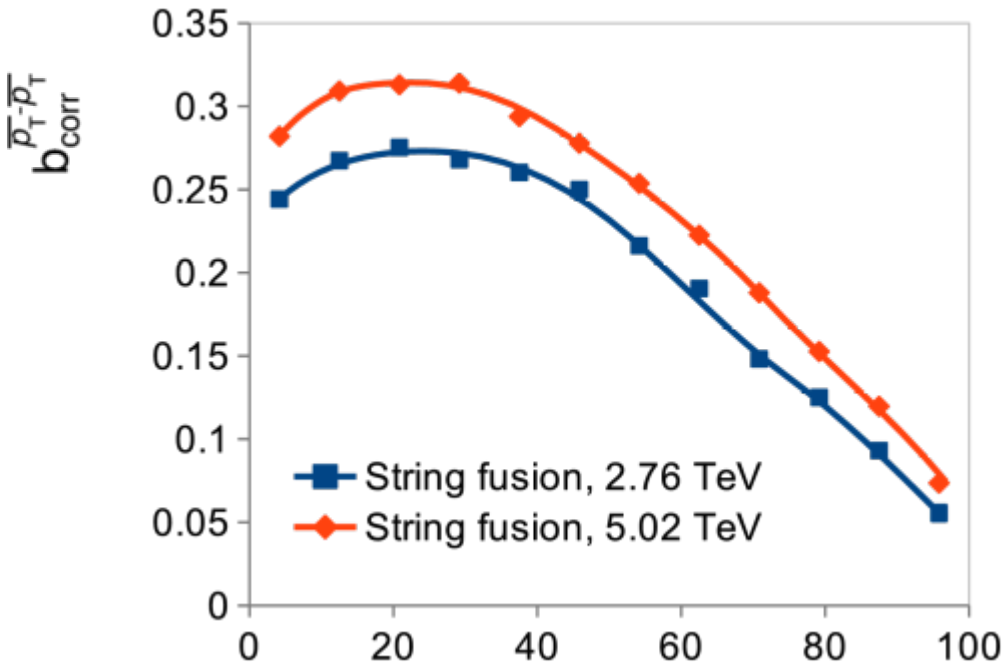
- pt-pt and pt-n correlations in Pb-Pb collisions at the SPS (NA49 data)  
lines – calculations in string fusion model



V. V. Vechernin, R. S. Kolevator, Phys. Atom. Nucl. 70 (2007) 1858

V. V. Vechernin, R. S. Kolevator, Phys. Atom. Nucl. 70 (2007) 1797

# forward-backward pt-pt correlations at LHC energy: PbPb



Preliminary experimental data – I. Altsybeev, “KnE Energy and Physics, pages 304-312, 2018 DOI: 10.18502/ken.v3i1.1759 arXiv:1711.04844 [nucl-ex]

Vladimir Kovalenko, Vladimir Vechernin, J. Phys. Conf. Ser. 798, 012053 (2017), arXiv:1611.07274 [nucl-th]



## Current realisations of string fusion/string tension modification

**PSM (Parton-string model) Monte Carlo generator** (N. Amelin et al.)

Only pairs of strings can be fused :(), Fortran

**Extended Multi-Pomeron Exchange model (EPEM)** N. Armesto, et al Phys. Atom. Nucl. 2008, V. 71, P. 2087.

E. O. Bodnia, V. N. Kovalenko, A. M. Puchkov, G. A. Feofilov // AIP Conf. Proc. 2014, 1606, 273

Semi-analytical calculations, parametrisation. Promising results at qualitative level

**Monte Carlo dipole-based model** V. N. Kovalenko, Phys. Atom. Nucl. 76, 1189 (2013), ] V. Kovalenko, V.

Vechernin, PoS (Baldin ISHEPP XXI) 077 (2012), arXiv:1212.2590 [nucl-th].

Finite Strings in rapidity space, C++/root

**Pythia 8 tune - Thermodynamical String Fragmentation** N. Fischer, T Sjöstrand JHEP 1701 (2017) 140

Very basic way

**Pythia 8 / DIPSY - Rope Hadronization**. C. Bierlich, EPJ Web Conf. 171 (2018) 14003

For pythia needs transverse position of strings. Promising results/under development

**Monte Carlo models by** V. V. Vechernin, R. S. Kolevatov, Phys. Atom. Nucl. 70 (2007) 1858; Phys. Atom. Nucl.

70 (2007) 1797, Vechernin, Lakomov PoS(Baldin ISHEPP XXI)072

Discontinued

## Rough proposals for Geant 4

### QGS model

Fragmentation functions for string decay

->

String fusion can be realized as a parametric dependence of these functions on string density

Parametrisation of string density can be taken from EPEM

### FTF

Realization of Lund string fragmentation. C++. Possible p-A, AA

->

Lund fragmentation parameters can be made dependent on string density,  
In a way similar to what PYTHIA8/DIPSY is doing

In parallel – quick cross-checks with results of Dipole-based Monte Carlo model with string fusion

## Summary

- Modification of string tension is supported by many experimental data
- Strings overlap – string fusion -> source of collectivity in AA, pA and even pp!
- String fusion works as smooth transition from low density up pp to Pb-Pb at LHC

## Ideas for Geant 4

- String fusion effects can be implemented in G4 models FTF and QGS
- Hopefully can help concerning tension at different energies
- This should increase the applicability range of these models up to higher energy and heavy ion collisions

Of course all should be done and validated in a separate branch before going into production

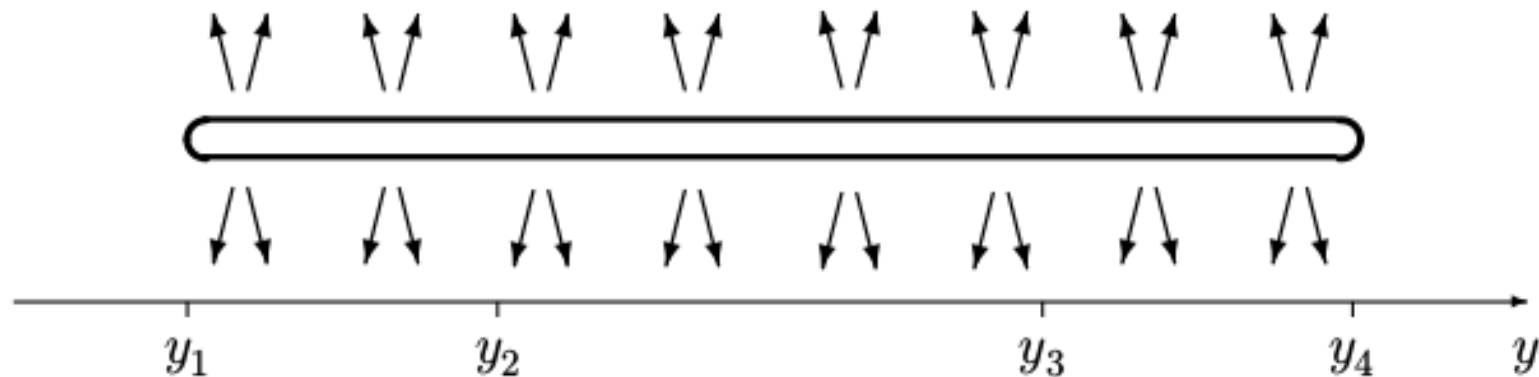
# End Of Presentation

The author acknowledges the support by the grant of the Russian Science Foundation (project 16-12-10176).

# Backup

## String in rapidity space

- Uniform distribution of partocles from  $y_{\min}$  to  $y_{\max}$
- $y_{\min}$  to  $y_{\max}$  are defined as a kinematical condition to decay into at least two particles



- Can study string overlaps:

