

Recent results from OKA setup @ U-70 synchrotron

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On behalf of «OKA» collaboration (IHEP-INR-JINR)

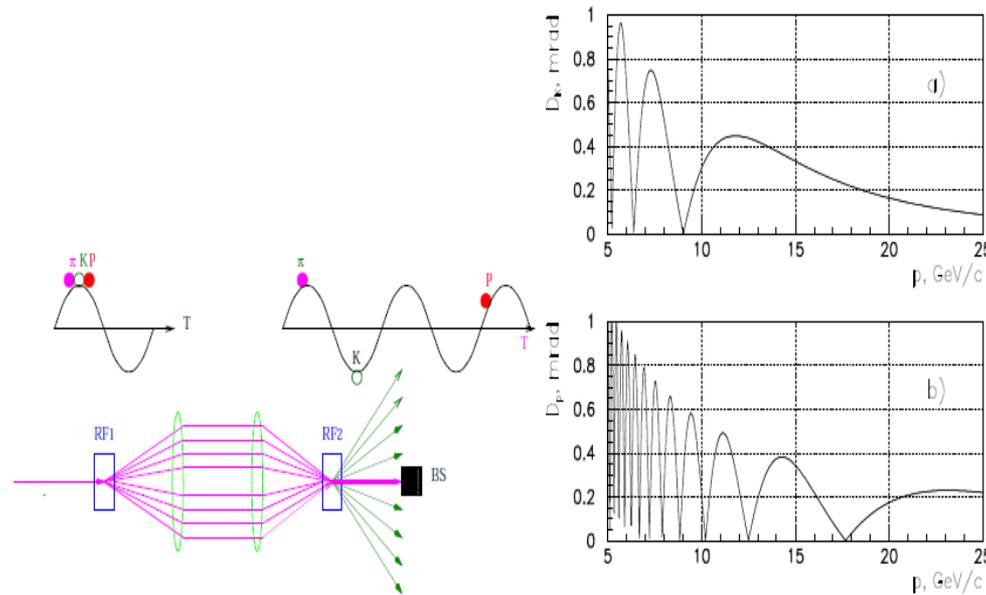
“International Conference on Kaon Physics”, Perugia,
10-13 September 2019

The talk layout

- OKA beam, detector, data
- $K\mu 2\gamma$ decay study, measurement of $F_V - F_A$
- $K3\pi\gamma$ decay rediscovery and study

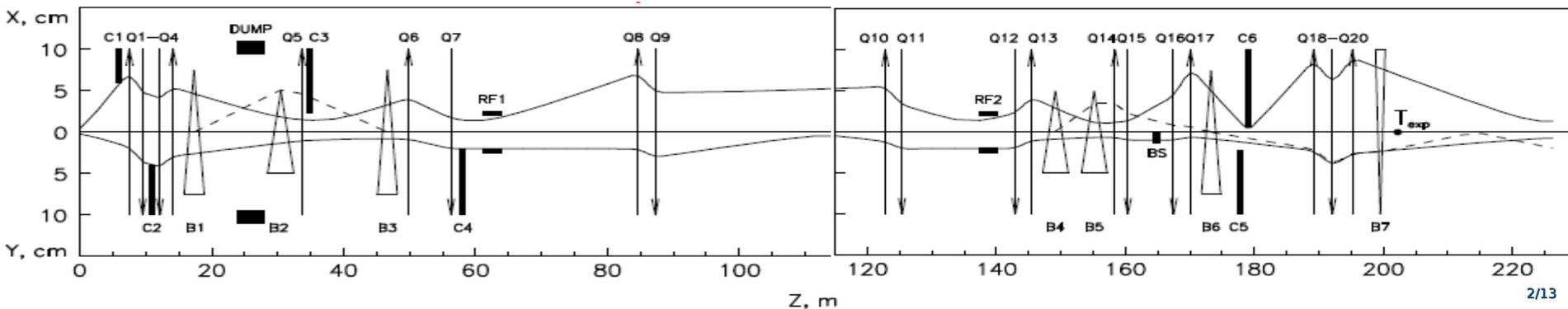
OKA: The experiment with RF-separated high energy K^\pm beam @U-70

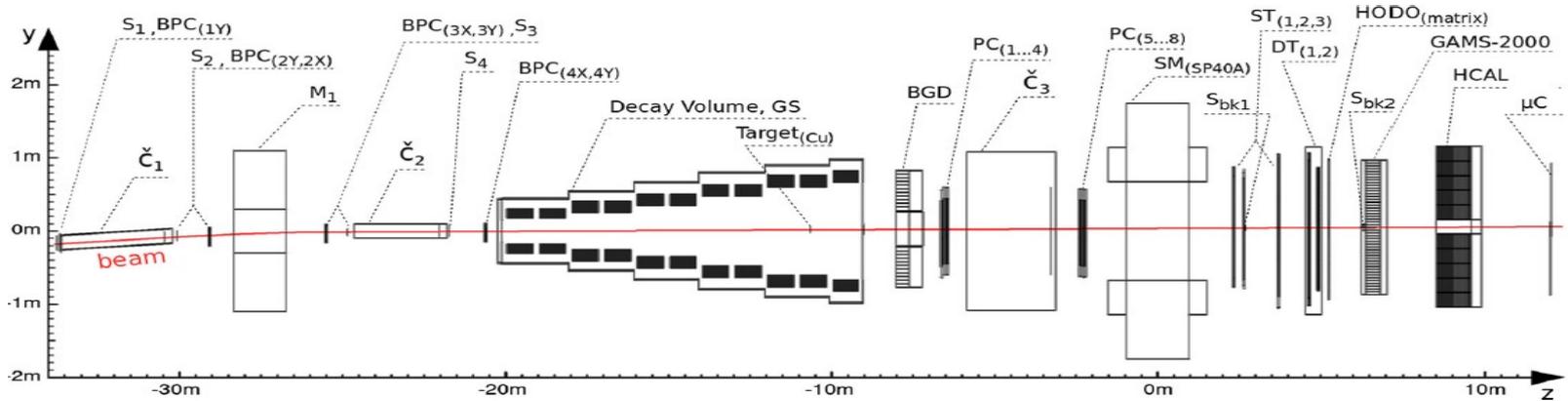
RF separation with Panofsky scheme is realised. It uses two Karlsruhe-CERN SC RF deflectors. Sophisticated cryogenic system, built at IHEP provides superfluid He for cavities cooling.



Operating frequency, (S-band)	2865 MHz
Wavelength, λ	~ 10.5 cm
Effective deflector length	2.74 m
Number of cells/deflector	104
Mean deflecting field	$\sim 1(0.6)$ MV/m
Working temperature	1.8 K

Main beam parameters :	
Primary proton beam energy	50 GeV
Primary proton beam intensity	7×10^{12} ppp
Secondary beam momentum	17.7 GeV
Length of the beam line	~ 200 m
K^+ intensity at the end	$\sim 10^6$
K^+ in the beam	up to 20%





- **Beam spectrometer:** 1mm pitch BPC ~1500 channels; Sc and Č counters
- **Decay volume with Veto system:** L=11m; Veto: 670 Lead-Scintillator sandwiches 20* (5mm Sc+1.5 mmPb), WLS
- **PC's, ST's and DT's for magnetic spectrometer:** ~5000 ch. PC (2 mm pitch) + 1300 DT (1 and 3 cm)
- **Pad(Matrix) Hodoscope** ~300 ch. WLS+SiPM readout
- **Magnet:** aperture 200*140 cm²
- **Gamma detectors:** GAMS2000, BGD EM cal. ~ 4000 LG.
- **Muon identification:** GDA-100 HCAL + 4 muon counters (μC) behind
- **For some runs Cu target inside decay volume was used:** Ø=8 cm, t=2mm and C3 big Cerenkov counter

Main Triggers

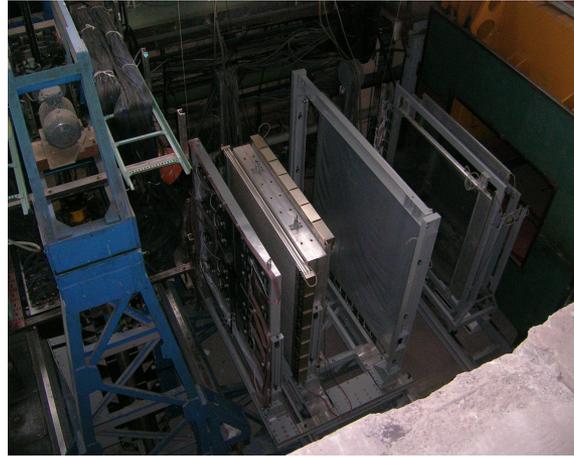
$$S_1 \cdot S_2 \cdot S_3 \cdot \overline{C_1} \cdot C_2 \cdot \overline{S_{bk}} \cdot (\sum_{GAMS} > 2.5 GeV) \cup (2 \leq MH \leq 4)$$

Prescaled Triggers

$$S_1 \cdot S_2 \cdot S_3 \cdot \overline{C_1} \cdot C_2 \cdot \overline{S_{bk}} / 10 \quad S_1 \cdot S_2 \cdot S_3 \cdot \overline{C_1} \cdot C_2 \cdot \overline{S_{bk}} \cdot \mu C / 4$$



General view of the OKA setup



ST, DT chambers, Matrix Hodoscope, ECAL



Decay volume Veto System



RF deflector in the beamline



Liquid He lines

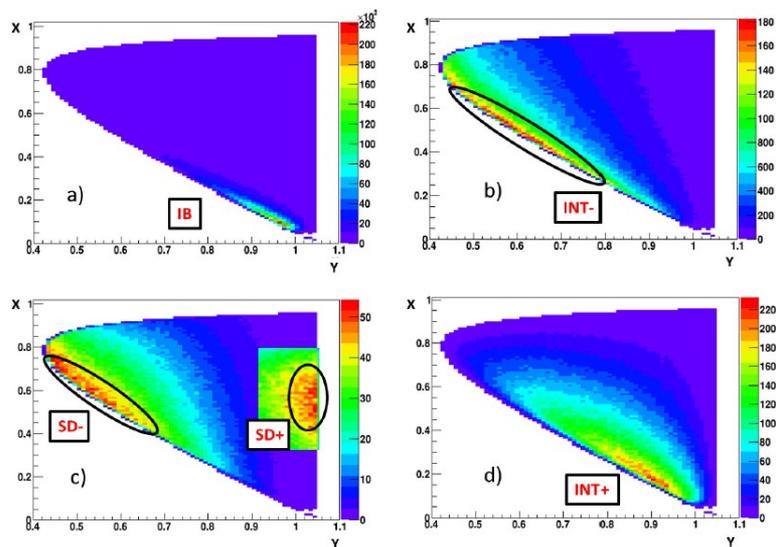


Tail of the beam line

Run's in 2010-2013, 2018 $N_K \sim 5 \times 10^{10}$

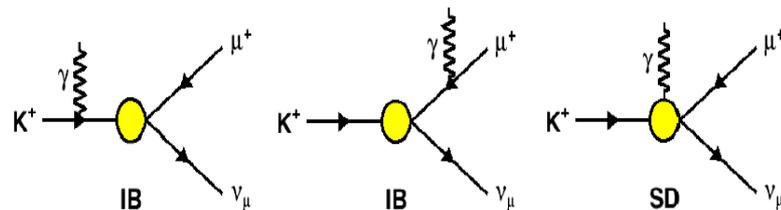
Main directions of the data analysis:

Decays: $Ke3$, $K\mu3$, $K^+ \rightarrow \mu^+ \nu_s$, $Ke3\gamma$, $K\mu3\gamma$, $K^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma$, $K^+ \rightarrow \mu^+ \nu \gamma$, $K^+ A \rightarrow K^+ \pi^0 A$



$$x = \frac{2E_\gamma^{cm}}{m_K}; \quad y = \frac{2E_\mu^{cm}}{m_K}$$

$$A_{IB} = \frac{\alpha}{2\pi} \Gamma_{K\mu^2} \frac{1}{(1-r)^2}; \quad A_{SD} = \frac{\alpha}{2\pi} \Gamma_{K\mu^2} \frac{1}{4r(1-r)^2} \left(\frac{m_K}{f_K}\right)^2; \quad A_{INT} = \frac{\alpha}{2\pi} \Gamma_{K\mu^2} \frac{1}{(1-r)^2} \frac{m_K}{f_K}; \quad r = \frac{m_\mu}{m_K}$$



$$\frac{d\Gamma}{dx dy} = A_{IB} f_{IB}(x, y) + A_{SD} [(F_V + F_A)^2 f_{SD^+}(x, y) + (F_V - F_A)^2 f_{SD^-}(x, y)] - A_{INT} [(F_V + F_A) f_{INT^+}(x, y) + (F_V - F_A) f_{INT^-}(x, y)]$$

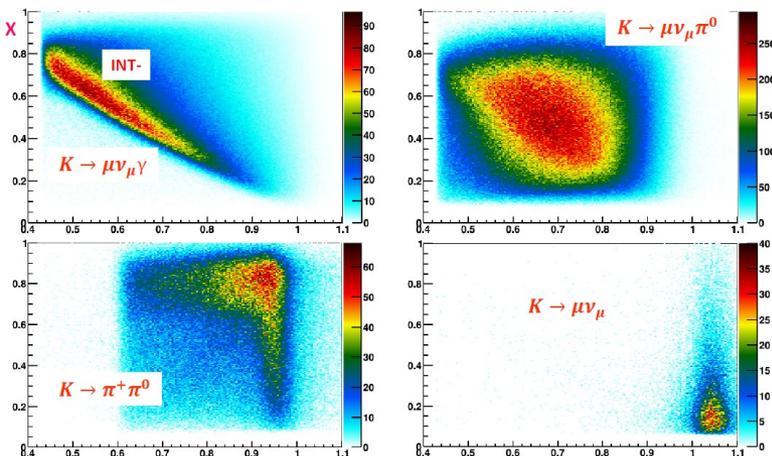
$$f_{IB}(x, y) = \left[\frac{1-y+r}{x^2(x+y-1-r)} \right] \times \left[x^2 + 2(1-x)(1-r) - \frac{2xr(1-r)}{x+y-1-r} \right]$$

$$f_{SD^+}(x, y) = [x+y-1-r][(1-x)(1-y)+r]$$

$$f_{SD^-}(x, y) = [1-y+r][(x+y-1)(1-x)-r]$$

$$f_{INT^+}(x, y) = \left[\frac{1-y+r}{x(x+y-1-r)} \right] \times [(1-x)(1-x-y)+r]$$

$$f_{INT^-}(x, y) = \left[\frac{1-y+r}{x(x+y-1-r)} \right] \times [x^2 - (1-x)(1-x-y) - r]$$



Main background sources

$$\chi_{PTO}(p^4): \quad F_V = \frac{\sqrt{2}M_K}{8\pi^2 F_\pi} = 0.096; \quad F_A = \frac{4\sqrt{2}M_K}{F_\pi} (L'_9 + L'_{10}) = 0.042; \quad F_V - F_A = 0.054$$

$$\chi_{PTO}(p^6): \quad F_V = F_V(0)(1 + \lambda(1-x)); \quad F_V(0) = 0.082; \quad \lambda = 0.4; \quad F_A = 0.034$$

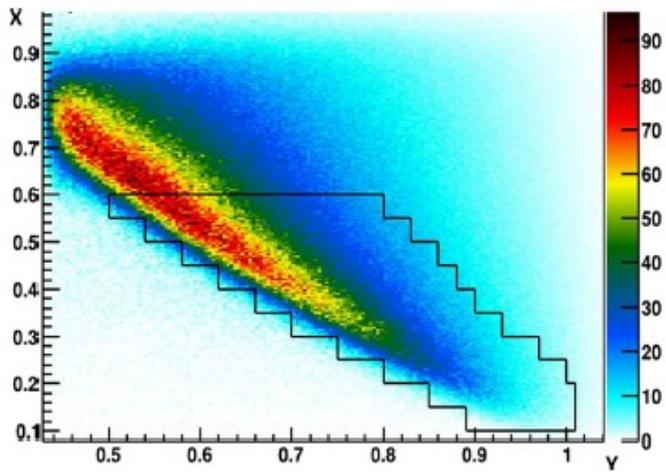
VALUE	CL%	EVTS	DOCUMENT ID	TECN
-0.21 ± 0.06		22K	DUK 2011	ISTR
... We do not use the following data for averages, fits, limits, etc. ...				
-0.24 to 0.04	90	2588	ADLER 2000B	B787
-2.2 to 0.6	90		DEMIDOV 1990	XEBC
-2.5 to 0.3	90		AKIBA 1985	SPEC



K⁺ → μ⁺ν γ selection and analysis

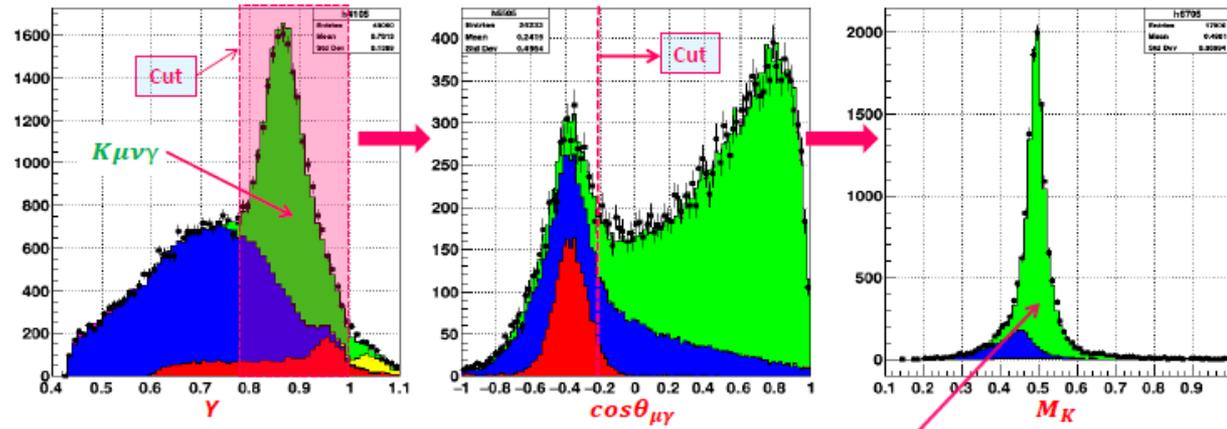
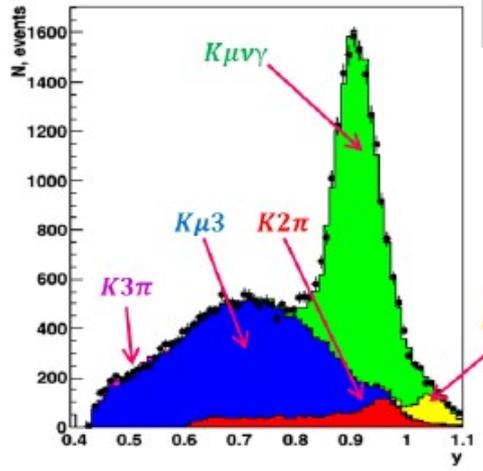
Based on half of the statistics of 2012 run, N_K ~ 1.2 x 10¹⁰

- 1 beam K⁺ track
- 1 secondary track identified as μ in GAMS, GDA-100 and MC
- Decay vertex inside DV
- 1 e.m. shower in GAMS with E > 1 GeV not associated with charged track
- E_{GS} < 10 MeV ; E_{BGD} < 100 MeV



- ISTRA+ procedure
- x,y region is divided into strips Δx=0.05 (~12 MeV)
- plot y-distribution; select cuts {y_{min}, y_{max}} ; plot cos θ_{μγ}* ; select cos_{min} cut; Plot M_K
- Simultaneous fit of the 3 histograms, parameters- N_{sig}, N_{bkg}, both signal(IB) and bkg shapes are from MC
- to correctly estimate errors, fit only M_K – plot with initial parameters of the simultaneous fit

From the fits, in total 95428±309 signal events 25 < E*_γ < 150 MeV (ISTRA+ 22K)



Geant3 MC: 22M sig., 624M bkg.
only IB term in signal

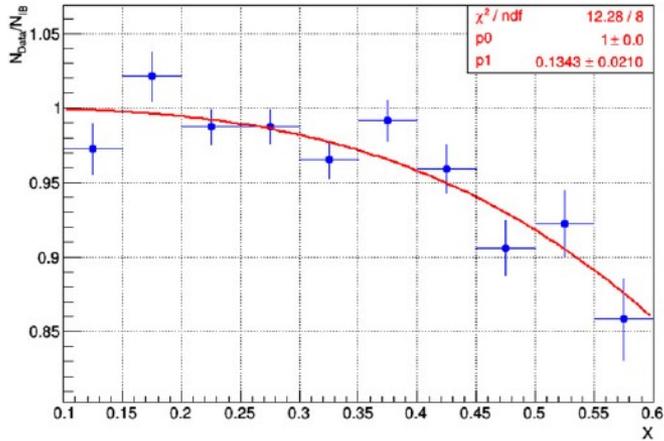
Strip #3 (0.2 < x < 0.25)

$$M_K^2 = (p_\mu + p_\nu + p_\gamma)^2$$

$$\vec{p}_\nu = \vec{p}_K - \vec{p}_\mu - \vec{p}_\gamma ; E_\nu = |\vec{p}_\nu|$$



$K^+ \rightarrow \mu^+ \nu \gamma$ decay, Fv-Fa extraction



χ PT $O(p^4)$ fit : $F_\nu; F_A = \text{const}$

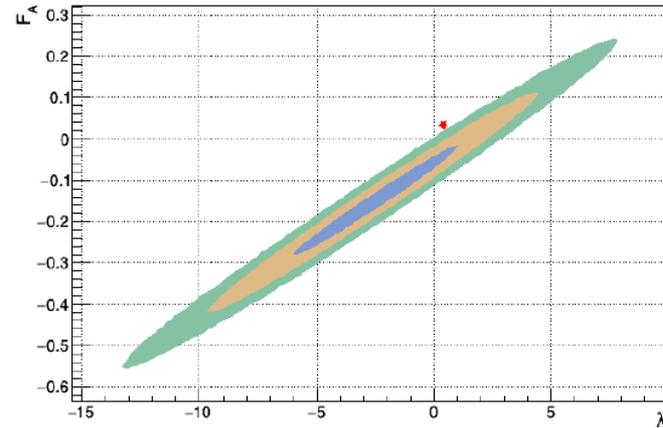
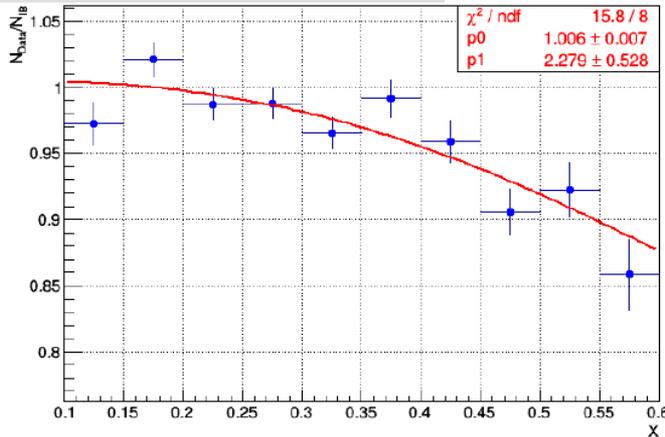
Red line is the result of the fit with $p_{\text{sig}}(x) = p_0(1 + p_1 \cdot \phi_{\text{INT-}}(x)/\phi_{\text{IB}}(x))$;

p_0 is the normalization $p_0 = 1.00 \pm 0.007$; $p_1 = F_\nu - F_A = 0.134 \pm 0.021$

$\phi_{\text{INT-}}(x)$ - x -distribution of reconstructed MC-signal weighted events

$w_{\text{INT-}} = (M_K/F_K) f_{\text{INT-}}(x_{\text{true}}, y_{\text{true}})$; $\phi_{\text{IB}}(x)$ - the same with $w_{\text{IB}} = f_{\text{IB}}(x_{\text{true}}, y_{\text{true}})$

$N_{\text{DATA}} / N_{\text{IB}}$ ratio as a function of x (blue points)



χ PT $O(p^6)$ fit : $F_\nu = F_\nu(0)(1 + \lambda(1-x))$; $F_\nu(0) = 0.082$; $\lambda = 0.4$; $F_A = 0.034$

- Fit with fixed χ PT $O(p^6)$ parameters:

$\chi^2/\text{NDF} = 28.0/9$

- $F_\nu(0)$ and F_A from χ PT $O(p^6)$, λ -free parameter $\rightarrow \lambda = 2.28 \pm 0.53$; $\chi^2/\text{NDF} = 15.8/8$ (see the left figure)

- $F_\nu(0)$ from χ PT $O(p^6)$, λ, F_A -free parameters \rightarrow (see the correlation plot on the right figure)

Systematics

- Non-ideal description of signal and background by MC: $1.3 < \chi^2/\text{NDF} < 1.7$
 Stat. errors in each bin of $N_{\text{DATA}}/N_{\text{IB}}$ -plot scaled with $\sqrt{(\chi^2/\text{NDF})}$. New value $F_V-F_A=0.138\pm 0.026$ (nominal 0.134 ± 0.021)
 $\rightarrow \sigma_{\text{shape}}=0.015$
 - Width of -x- strips: F_V-F_A calculation repeated for 2 different values of width $\Delta x=0.035, \Delta x=0.07$ (nominal 0.05)
 $\rightarrow \sigma_{\Delta x}=0.011$
 - The fit range in x (number of -x- strips): remove one or two bins on the left(right) edge.
 $\rightarrow \sigma_x < 0.006$
 - -y- limit in the strips: instead of maximizing $S/\sqrt{S+B}$ use FWHM from the signal MC
 $\rightarrow \sigma_y=0.008$
 - Effect of INT⁺ : INT⁺ term is added to $N_{\text{DATA}}/N_{\text{IB}}$ fit. The BNL E787 value $|F_V+F_A|=0.165\pm 0.013$ is used (± 0.178)
 $\rightarrow \sigma_{\text{INT}^+}=0.018$
- $\sigma_{\text{SYS}}=0.027$

“OKA” $F_V-F_A = 0.134 \pm 0.021_{\text{stat}} \pm 0.027_{\text{syst}}$

$\chi\text{PT } \mathcal{O}(p^4)$ $F_V = \frac{\sqrt{2} M_K}{8 \pi^2 F_\pi} = 0.096; F_A = \frac{4\sqrt{2} M_K}{F_\pi} (L_9^r + L_{10}^r) = 0.042$

$F_V-F_A = 0.054$ 2.3 σ difference

ExA (gauge non-local effective chiral action) S.Shim et al., Phys.Lett. B795 (2019)438-445

$F_V-F_A = 0.08$ (1.6 σ)

The measured value is in a reasonable agreement with ISTRAP result: $F_V-F_A = 0.21 \pm 0.04_{\text{stat}} \pm 0.04_{\text{syst}}$ (1.15 σ)

And with (model dependent) result of BNL E865 ($K^+ \rightarrow \mu^+ \nu e^+ e^- + e^+ \nu e^+ e^-$) $F_V-F_A = 0.077 \pm 0.026$ (1.13 σ)

Expect tripling of the statistics by the year end

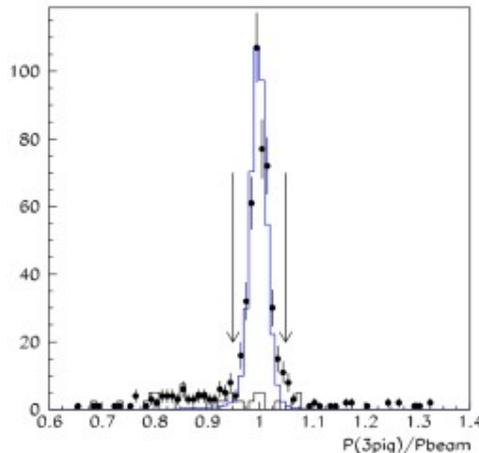
Based on 2 runs: 2012, 2013 analysis $N_K \sim 3.4 \times 10^{10}$

Inspired by:

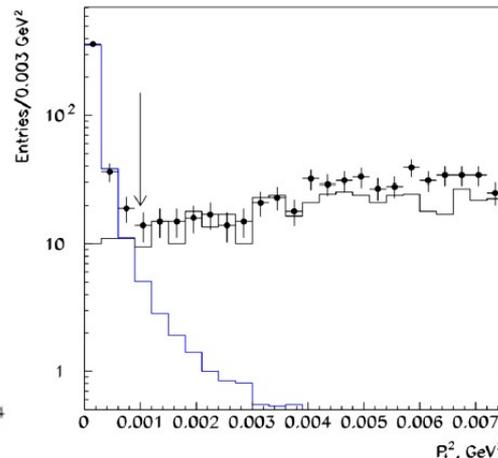
- [1] V.Cirigliano et al., “Kaon Decays in the Standard Model” arXiv:1107.6001 v3 [hep-ph] 14 April 2012
 “The experimental status of $K^+ \rightarrow 3\pi\gamma$ is still rather meager”
- [2] G. D. D’Ambrosio et al., “ $K^+ \rightarrow \pi\pi\pi\gamma$ in Chiral Perturbation Theory” Z. Phys. C76(1997)301-310
 a concept of “generalized bremsstrahlung”

VALUE (10^{-4})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
1.04 ± 0.31	OUR AVERAGE				
1.10 ± 0.48	7	BARMIN	1989	XEBC	$E(\gamma) > 5$ MeV
1.0 ± 0.4		STAMER	1965	EMUL	+
					$E(\gamma) > 11$ MeV

$Br(K^+ \rightarrow \pi^+\pi^+\pi^-\gamma)$ PDGLive screenshot



$|\vec{P}_{3\pi\gamma}|/|\vec{P}_{beam}|$ after cuts



$P_T^2(3\pi\gamma)$ after cuts

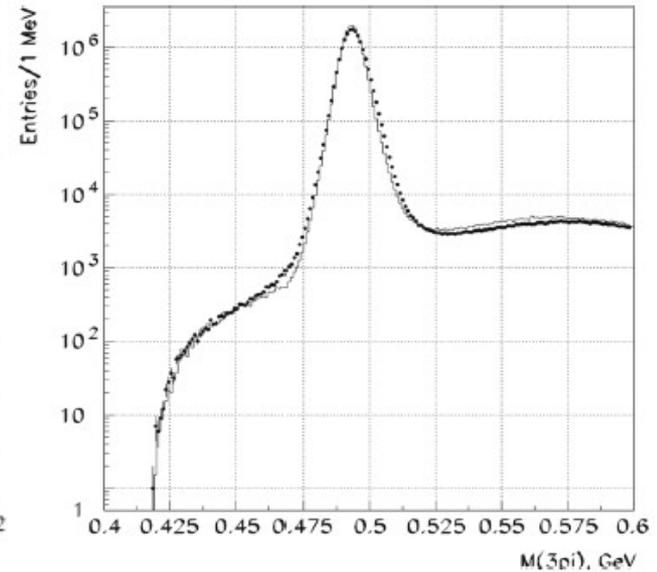
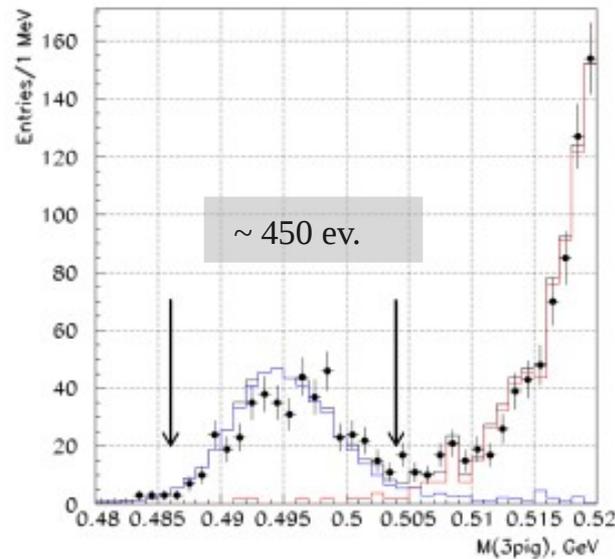
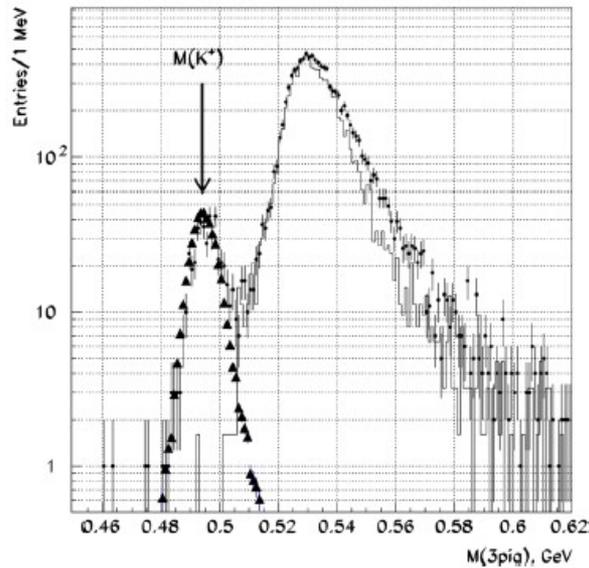
$$S_1 \cdot S_2 \cdot S_3 \cdot \overline{C}_1 \cdot C_2 \cdot \overline{S}_{bk} \cdot (2 \leq MH \leq 4)$$

Event selection

- Beam track with measured \vec{p}_b
- 3 secondary charged tracs $\Sigma q_i = +$
- Decay vertex should have good χ^2 and to be inside DV
- Charged tracs not identified as electrons in GAMS-200
- One photon with $E_\gamma > 0.5$ GeV
- $M(\pi_1\gamma) > 0.17$ GeV
- $P_T^2(3\pi\gamma) > 0.001$ GeV²
- $0.95 < |\vec{P}_{3\pi\gamma}|/|\vec{P}_{beam}| < 1.05$

Geant3 MC:

- Bkg. $\pi^+\pi^0, \pi^+\pi^0\pi^0, \pi^+\pi^+\pi^-, \mu^+\nu, \pi^0\mu^+\nu, \pi^0e^+\nu \sim 10^9$ ev. mixed with Br, weights for 3 body decays \rightarrow PDG $|M|^2$
- signal weight from the leading order amplitude, derived from $\pi^+\pi^+\pi^-$ [2]



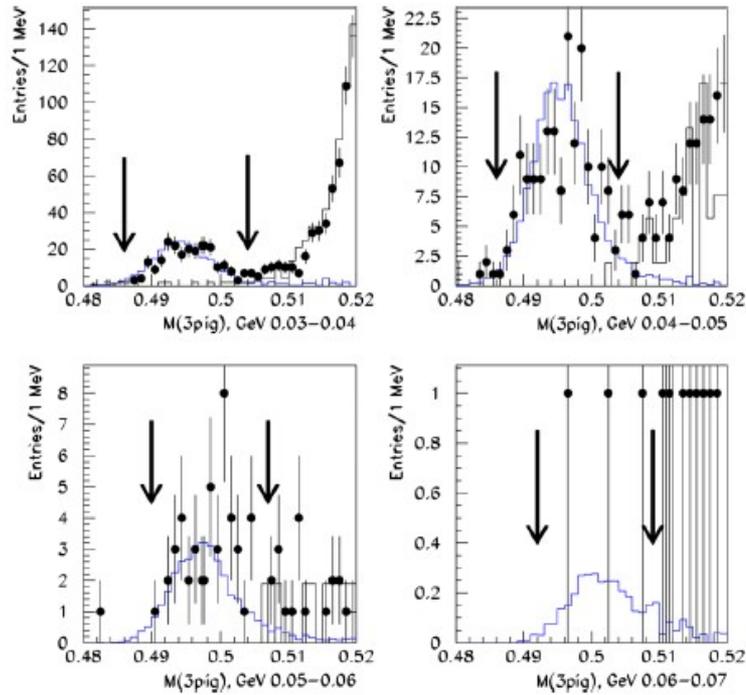
Normalization on $N(K \rightarrow 3\pi) \sim 17 \text{ M}$
 $\text{Br}(K^+ \rightarrow \pi^+\pi^+\pi^- \gamma) = (7.1 \pm 0.4_{\text{stat}}) \cdot 10^{-6} \quad E_\gamma^* > 30 \text{ MeV}$

Systematics

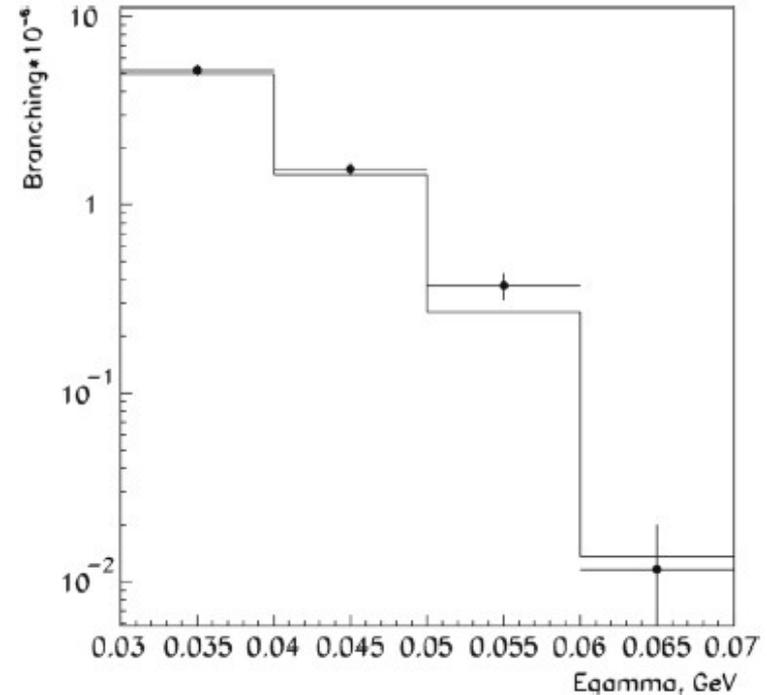
- The main source is uncertainty in the estimate of bkg in the signal region $\rightarrow \sigma_{\text{bkg}} = 0.27 \times 10^{-6}$
 - Cuts variation $\rightarrow \sigma_{\text{cuts}} = 0.1 \times 10^{-6}$
 - Estimate of bkg under $K \rightarrow 3\pi$ $\rightarrow \sigma_{\text{norm}} < 0.04 \times 10^{-6}$
- $\rightarrow \sigma_{\text{SYS}} = 0.3 \times 10^{-6}$

$$\text{Br}(K^+ \rightarrow \pi^+\pi^+\pi^- \gamma) = (7.1 \pm 0.4_{\text{stat}} \pm 0.3_{\text{sys}}) \cdot 10^{-6} \quad E_\gamma^* > 30 \text{ MeV}$$

$$\chi\text{PT } \mathcal{O}(p^4) \quad (6.65 \pm 0.05) \cdot 10^{-6} \quad [2]$$



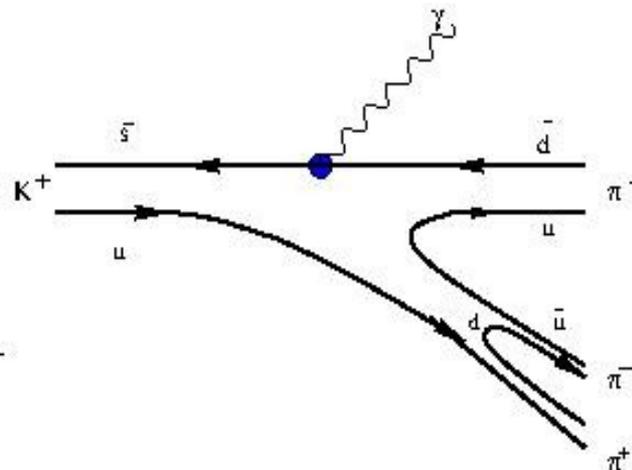
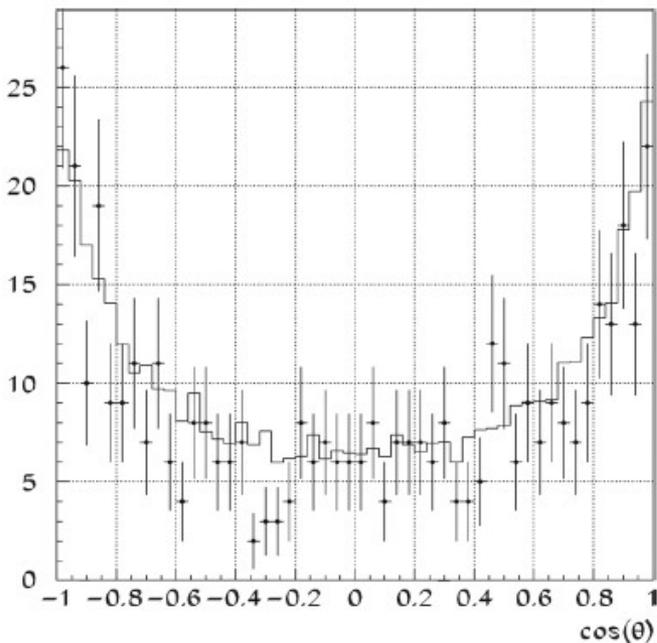
$M_{3\pi\gamma}$ in four 10 MeV bins over E_γ^*



Differential $3\pi\gamma$ branching, compared with theory

Energy interval (GeV)	Branching fraction (data)	Branching fraction (CHPT [8])
0.03–0.04	$(5.17 \pm 0.34) \times 10^{-6}$	$(4.93 \pm 0.05) \times 10^{-6}$
0.04–0.05	$(1.55 \pm 0.12) \times 10^{-6}$	$(1.44 \pm 0.01) \times 10^{-6}$
0.05–0.06	$(0.35 \pm 0.05) \times 10^{-6}$	$(0.269 \pm 0.003) \times 10^{-6}$
0.06–0.07	$(0.11 \pm 0.06) \times 10^{-7}$	$(0.136 \pm 0.002) \times 10^{-7}$

In $B^+ \rightarrow K^+\pi^+\pi^-\gamma$ decay LHCb has found significant ($\sim 5\%$) up-down asymmetry of γ with respect to the hadronic system decay plane. This observable is T-odd. We perform an analogous study for $K^+ \rightarrow \pi^+\pi^-\gamma$.



$$\cos \theta = \frac{\vec{n}_\gamma \cdot [\vec{p}_f(\pi^+) \times \vec{p}_s(\pi^+)]}{\|[\vec{p}_f(\pi^+) \times \vec{p}_s(\pi^+)]\|} \quad \text{An alternative is } \cos \theta = \frac{\vec{n}_\gamma \cdot [\vec{p}_f(\pi^-) \times \vec{p}_s(\pi^-)]}{\|[\vec{p}_f(\pi^-) \times \vec{p}_s(\pi^-)]\|}$$

$$A = (N(\cos\theta > 0) - N(\cos\theta < 0)) / N_{\text{tot}} = -0.04(0.03) \pm 0.05(\text{stat.}) \pm 0.03(\text{syst.})$$

A theoretical support is needed to understand the scale of the effect in the SM and NP

Several radiative decays are under study by “OKA” setup at @ U-70 synchrotron

- The radiative decay $K^+ \rightarrow \mu^+ \nu \gamma$ is studied on statistics of $\sim 95K$ events for $25 \text{ MeV} < E_\gamma^* < 150 \text{ MeV}$. A destructive interference between IB and SD- is clearly seen. The difference of vector and axial constants $F_V - F_A$ is measured:

$$F_V - F_A = 0.134 \pm 0.021_{\text{stat}} \pm 0.027_{\text{syst}} \text{ which is } 2.3 \sigma \text{ from } \chi\text{PT O}(p^4) \text{ and } 1.6 \sigma \text{ from } E\chi A.$$

- The decay $K^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma$ is studied on statistics of ~ 450 events for $30 \text{ MeV} < E_\gamma < 70 \text{ MeV}$ region. Branching fraction and differential branching fractions are measured:

$$\text{Br}(K^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma) = (7.1 \pm 0.4_{\text{stat}} \pm 0.3_{\text{sys}}) \cdot 10^{-6} \text{ To be compared with } \chi\text{PT O}(p^4) \text{ } (6.65 \pm 0.05) \cdot 10^{-6}$$

An upper limit for the photon up-down asymmetry versus pion system decay plane is obtained

$$A = (N(\cos > 0) - N(\cos < 0)) / N_{\text{tot}} = -0.04 \pm 0.05(\text{stat.}) \pm 0.03(\text{syst.})$$