#### A Sedrakian

miroducii

Dense OC

Constructin EoS

Sequentia phase transitions

Low-mass twin and GW

# The fourth family of comapct stars

Armen Sedrakian
Frankfurt Institute for Advanced Studies
Institute for Theoretical Physics, Wroclaw University
In collaboration with Jia-Jie Li and Mark Alford
MPCS 2019, September 21, 2019



FIAS Frankfurt Institute for Advanced Studies



### A Sedrakian

Introduct

Dense QC

Constructin EoS

phase transitions

Low-mass twin and GW

### Outline

- Introduction to compact star equilibria
- Dense QCD and the construction of EoS
- New equilibria via sequential phase transitions within QCD
- Low-mass twins and GW
- Remarks on cooling
- Conclusions

### A Sedrakian

Introduction

Dense OCD

Constructin EoS

Sequentia phase transitions

Low-mass twin and GW

### **Equilibria of compact objects**

150



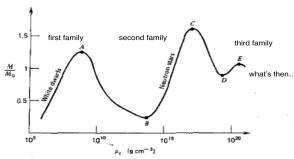


Figure 6.2 Schematic diagram showing the turning points in the mass versus central density diagram for equilibrium configurations of cold matter.

S. Shapiro, S. Teukolsky, "Black holes, White dwarfs and Neutron Stars"

- -White dwarfs -first family,  $M \le 1.5 M_{\odot}$ , [S. Chandrasekhar, L. Landau (1930-32)]
- -Neutron Stars second family,  $M \le 2M_{\odot}$ , [Oppenhimer-Volkoff (1939)]
- -Hybrid Stars third family,  $M \le 2M_{\odot}$ , [Gerlach (1968), Glendenning-Kettner (2000)]
- Fourth Family? M. Alford and A. Sedrakian, Phys. Rev. Lett. 119, 161104 (2017).

### A Sedrakian

#### Introduction

miroduction

Constructing EoS

phase transitions

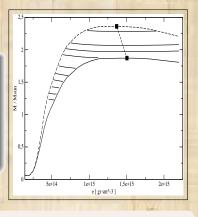
Low-mass twin and GW

• Einstein's field equations:

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = -8\pi T_{\mu\nu},$$

• Energy-momentum tensor:

$$T_{\mu\nu} = -P(r)g_{\mu\nu} + [P(r) + \epsilon(r)] u_{\mu}u_{\nu}$$



TOV equations:

$$\begin{array}{lcl} \frac{dP(r)}{dr} & = & -\frac{G\epsilon(r)M(r)}{c^2r^2}\left(1+\frac{P(r)}{\epsilon(r)}\right)\left(1+\frac{4\pi r^3P(r)}{M(r)c^2}\right)\left(1-\frac{2GM(r)}{c^2r}\right)^{-1}.\\ \\ M(r) & = & 4\pi\int\limits_0^r r^2\epsilon(r)dr. \end{array}$$

A Sedrakian

miroduciic

Dense QCD

EoS

Sequential phase transitions

Low-mass twin and GW

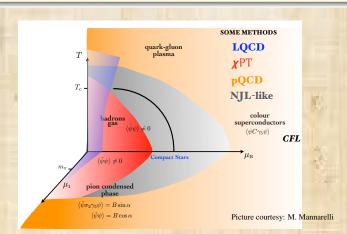
The Lagrangian of QCD is written for  $\psi_q = (\psi_{qR}, \psi_{qG}, \psi_{qB})^T$  as

$$\mathcal{L}_{QCD} = \underbrace{\bar{\psi}_q^i(i\gamma^\mu)(D_\mu)_{ij}\psi_q^j - \textit{m}_q\bar{\psi}_q^i\psi_{qi}}_{quarks} - \underbrace{\frac{1}{4}F_{\mu\nu}^aF^{a\mu\nu}}_{gluons(Yang-Mills)} \; ,$$

where 
$$(D_{\mu})_{ij} = \delta_{ij}\partial_{\mu} - ig_s t^a_{ij}A^a_{\mu}$$
, and  $F^{\mu\nu} = \partial^{\mu}A^{\nu} - \partial^{\nu}A^{\mu} - 2q(A^{\mu} \times A^{\nu})$ 

covarinat derivative

gluonic field (Yang-Mills) field tensor



#### A Sedrakian

Introducti

#### Dense QCD

Constructin EoS

Sequential phase transitions

Low-mass twin and GW

### Color-superconductivity within the NJL model

$$\mathcal{L}_{NJL} = \underbrace{\bar{\psi}(i\gamma^{\mu}\partial_{\mu} - \hat{m})\psi}_{\text{quarks}} + \underbrace{G_{V}(\bar{\psi}i\gamma^{\mu}\psi)^{2}}_{\text{vector}} + \underbrace{G_{S}\sum_{a=0}^{8}[(\bar{\psi}\lambda_{a}\psi)^{2} + (\bar{\psi}i\gamma_{5}\lambda_{a}\psi)^{2}]}_{\text{scalar-pseudoscalar}}$$

$$+ \underbrace{G_{D}\sum_{\gamma,c}[\bar{\psi}_{\alpha}^{a}i\gamma_{5}\epsilon^{\alpha\beta\gamma}\epsilon_{abc}(\psi_{C})_{\beta}^{b}][(\bar{\psi}_{C})_{\rho}^{r}i\gamma_{5}\epsilon^{\rho\sigma\gamma}\epsilon_{rsc}\psi_{\sigma}^{s}]}_{\text{pairing}}$$

$$- \underbrace{K\left\{\det_{f}[\bar{\psi}(1+\gamma_{5})\psi] + \det_{f}[\bar{\psi}(1-\gamma_{5})\psi]\right\},}_{t'\text{Hooft interaction}}$$

- quarks:  $\psi_{\alpha}^{a}$ , color a = r, g, b, flavor  $(\alpha = u, d, s)$ ; mass matrix:  $\hat{m} = \text{diag}_{f}(m_{u}, m_{d}, m_{s})$ ;
- other notations:  $\lambda_a$ , a=1,...,8,  $\psi_C=C\bar{\psi}^T$  and  $\bar{\psi}_C=\psi^T C$ ,  $C=i\gamma^2\gamma^0$ .

### Parameters of the model:

- $G_S$  the scalar coupling and cut-off  $\Lambda$  are fixed from vacuum physics
- $G_D$  is the di-quark coupling  $\simeq 0.75G_S$  (via Fierz) but free to change
- $G_V$  and  $ho_{
  m tr}$  are treated as free parameters

### A Sedrakian

mtroducti

Dense QCD

Constructin EoS

Sequential phase transitions

Low-mass twin and GW

# QCD interactions pairing interactions and gaps

$$\Delta \propto \langle 0 | \psi^a_{\alpha\sigma} \psi^b_{\beta\tau} | 0 \rangle$$

- Symmetric in space wave function (isotropic interaction)
- Antisymmetry in colors *a*, *b* for attraction
- Antisymmetry in spins  $\sigma$ ,  $\tau$  (Cooper pairs as spin-0 objects)
- Antisymmetry in flavors  $\alpha, \beta$

### 2SC phase:

Low densities, large  $m_s$  (strange quark decoupled)

$$\Delta(2SCs) \propto \Delta \epsilon^{ab3} \epsilon_{\alpha\beta} \qquad \delta\mu \ll \Delta,$$

Crystalline or gapless phases:

Intermediate densities, large  $m_s$  (strange quark decoupled)

$$\Delta$$
(cryst.)  $\propto \epsilon_{\alpha\beta}\Delta_0 e^{i\vec{Q}\cdot\vec{r}}$   $\delta\mu > \Delta$ ,

CFL phase:

High densities nearly massless u, d, s quarks

$$\Delta(CFL) \propto \langle 0|\psi_{\alpha L}^{a}\psi_{\beta L}^{b}|0\rangle = -\langle 0|\psi_{\alpha R}^{a}\psi_{\beta R}^{b}|0\rangle = \Delta\epsilon^{abC}\Delta\epsilon_{\alpha\beta C}.$$

### A Sedrakian

Introduction

Dense OCT

Constructing EoS

Sequentia phase transitions

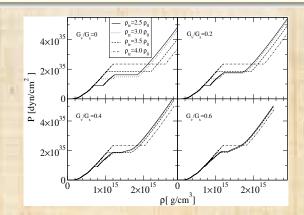
Low-mass twin

# EOS including (hyper)nuclear, 2SC and CFL phases of matter

Choose Maxwell (large surface tension) or Glendenning (low surface tension) constructions. Matching condition for Maxwell is simply

$$P_N(\mu_B) = P_O(\mu_B),$$

i.e., with low-density nuclear and high-density quark phases



#### A Sedrakian

minoductio

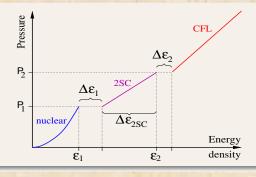
Dense QCI

### Constructing EoS

phase transition

Low-mass twin and GW

# Synthetic equations of state with constant speed of sound



- Instead of full NJL-model EoS with 2SC-CFL transition use synthetic EoS
- Realistic DD-ME2 EoS below the deconfinement (Colucci-Sedrakian EoS)
- Parametrize synthetic EoS via Constant Speed of Sound (CSS) parameterization (Alford-Han-Prakash 2013), also Haensel-Zdunik (2012).

### A Sedrakian

Introducti

Dense QC.

### Constructing EoS

Sequential phase transitions

Low-mass twins and GW

### Relativistic DFT theory

$$\mathcal{L} = \sum_{B} \bar{\psi}_{B} \left[ \gamma^{\mu} \left( i \partial_{\mu} - g_{\omega BB} \omega_{\mu} - \frac{1}{2} g_{\rho BB} \boldsymbol{\tau} \cdot \boldsymbol{\rho}_{\mu} \right) - (m_{B} - g_{\sigma BB} \boldsymbol{\sigma}) \right] \psi_{B}$$

baryonic contribution

$$+ \underbrace{\frac{1}{2}\partial^{\mu}\sigma\partial_{\mu}\sigma - \frac{1}{2}m_{\sigma}^{2}\sigma^{2}}_{}$$

scalar mesons

$$\underbrace{\frac{1}{4}\omega^{\mu\nu}\omega_{\mu\nu} + \frac{1}{2}m_{\omega}^{2}\omega^{\mu}\omega_{\mu} - \frac{1}{4}\rho^{\mu\nu}\rho_{\mu\nu} + \frac{1}{2}m_{\rho}^{2}\rho^{\mu}\cdot\rho_{\mu}}_{}$$

vector mesons

$$+ \sum_{\lambda} \bar{\psi}_{\lambda} (i\gamma^{\mu}\partial_{\mu} - m_{\lambda})\psi_{\lambda} - \frac{1}{4}F^{\mu\nu}F_{\mu\nu},$$

leptons

- B-sum is over the baryonic octet  $B \equiv p, n, \Lambda, \Sigma^{\pm,0}, \Xi^{-,0}$
- Meson fields include  $\sigma$  meson,  $\rho_{\mu}$ -meson and  $\omega_{\mu}$ -meson
- Leptons include electrons, muons and neutrinos for  $T \neq 0$

### A Sedrakian

Introductio

Dense QC

Constructing EoS

Sequential phase transitions

Low-mass twir and GW

### Fixing the couplings: nucleonic sector

$$g_{iN}(\rho_B) = g_{iN}(\rho_0)h_i(x), \qquad i = \sigma, \omega, \qquad h_i(x) = a_i \frac{1 + b_i(x + d_i)^2}{1 + c_i(x + d_i)^2}$$
  
 $g_{\rho N}(\rho_B) = g_{\rho N}(\rho_0) \exp[-a_{\rho}(x - 1)].$ 

DD-ME2 parametrization of D. Vretenar, P. Ring et al. Phys. Rev. C 71, 024312 (2005).

	$\sigma$	$\omega$	ρ
$m_i$ [MeV]	550.1238	783.0000	763.0000
$g_{Ni}(\rho_0)$	10.5396	13.0189	3.6836
$a_i$	1.3881	1.3892	0.5647
$b_i$	1.0943	0.9240	_
$c_i$	1.7057	1.4620	_
$d_i$	0.4421	0.4775	_

Total number of parameters 8: boundary conditions on h(x) at x = 1.

### A Sedrakian

Introduction

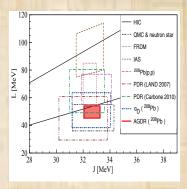
Dense QCI

Constructing EoS

phase transitions

Low-mass twin and GW

- saturation density  $\rho_0 = 0.152 \text{ fm}^{-3}$
- binding energy per nucleon E/A = -16.14 MeV,
- incompressibility  $K_0 = 250.90 \text{ MeV}$ ,
- symmetry energy J = 32.30 MeV.
- symmetry energy slope L = 51.24 MeV,
- symmetry incompressibility  $K_{sym} = -87.19 \text{ MeV}$



$$\begin{split} K_0 &= k_F^2 \frac{\partial E/A}{\partial k^2}|_{k=k_F} = 9\rho_0^2 \frac{\partial^2 E/A}{\partial \rho^2}|_{\rho=\rho_0}, \qquad S(\rho) = \frac{1}{2} \frac{\partial^2 \epsilon/\rho}{\partial \delta^2}|_{\delta=0}. \\ S(\rho) &= J + L\left(\frac{\rho-\rho_0}{3\rho_0}\right) + \frac{1}{2} K_{\text{sym}} \left(\frac{\rho-\rho_0}{3\rho_0}\right)^2. \end{split}$$

#### A Sedrakian

miroduciio

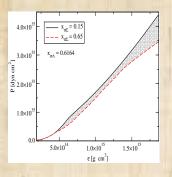
Dense OCI

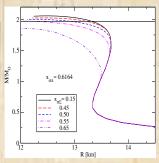
Constructing EoS

Sequentia phase transition

Low-mass twin

### **Equation of state and (hyper)nuclear stars**





Zero temperature equations of state of hypernuclear matter for fixed  $x_{\sigma\Lambda}=0.6164$  and a range of values  $0.15 \le x_{\sigma\Sigma} \le 0.65$ . These values generate the shaded area, which is bound from below by the softest EoS (dashed red line) corresponding to  $x_{\sigma\Sigma}=0.65$  and from above by the hardest EoS (solid line) corresponding to  $x_{\sigma\Sigma}=0.15$ .

### A Sedrakian

miroductio

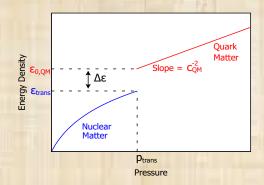
Dense QCI

Constructing EoS

phase transition

Low-mass twins and GW

## **CSS** parameterization



$$\varepsilon(p) = \left\{ \begin{array}{ll} \varepsilon_{\rm NM}(p) & p < p_{\rm trans} \\ \varepsilon_{\rm NM}(p_{\rm trans}) + \Delta \varepsilon + c_{\rm OM}^{-2}(p - p_{\rm trans}) & p > p_{\rm trans} \end{array} \right.$$

M. G. Alford, S. Han, M. Prakash, Phys. Rev. D 88, 083013 (2013).J. Zdunik and P. Haensel A and A 551, A61, (2013).

### A Sedrakian

Introducti

Dense QC

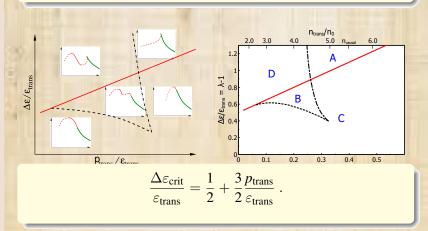
Constructing EoS

Sequential phase transitions

Low-mass twin and GW

### Phase diagram in M-R space

Phase diagram for hybrid star branches in the mass-radius relation of compact stars. The left panel shows schematically the possible topological forms of the mass-radius relation in each region of the diagram.



M. G. Alford, S. Han, M. Prakash, Phys. Rev. D 88, 083013 (2013).

### A Sedrakian

Introductio

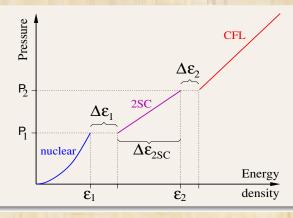
Dense QCI

Constructin EoS

Sequential phase transitions

Low-mass twins and GW

# EoS with sequential phase transitions



Parameters of the models:

$$(\epsilon_1, P_1)$$
  $\Delta \varepsilon_1$ ,  $\Delta \varepsilon_{2SC}$   $(\varepsilon_2, P_2)$   $\Delta \varepsilon_2$ 

Note that there are five independent parameters.

### A Sedrakian

Construction

EoS

Sequential phase transitions

Low-mass twir and GW

### The EOS is analytically given

$$P(\varepsilon) = \left\{ \begin{array}{ll} P_1, & \varepsilon_1 < \varepsilon < \varepsilon_1 + \Delta \varepsilon_1 \\ P_1 + s_1 \big[ \varepsilon - (\varepsilon_1 + \Delta \varepsilon_1) \big], & \varepsilon_1 + \Delta \varepsilon_1 < \varepsilon < \varepsilon_2 \\ P_2, & \varepsilon_2 < \varepsilon < \varepsilon_2 + \Delta \varepsilon_2 \\ P_2 + s_2 \big[ \varepsilon - (\varepsilon_2 + \Delta \varepsilon_2) \big], & \varepsilon > \varepsilon_2 + \Delta \varepsilon_2 \end{array} \right.$$

### Need to specify:

- the two speeds of sounds:  $s_1$  and  $s_2$
- the point of transition from NM to QM  $\varepsilon_1$ ,  $P_1$
- the magnitude of the first jump  $\Delta \varepsilon_1$
- the size of the 2SC phase, i.e, the second transition point  $\varepsilon_2$ ,  $P_2$
- the size of the second jump  $\Delta \varepsilon_2$

### A Sedrakian

Introduction

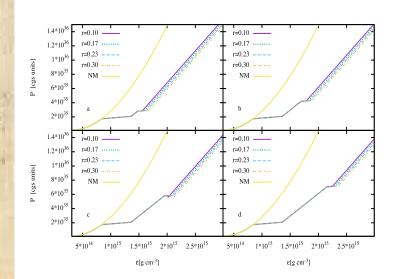
Introductio

Constructin

Sequential phase transitions

Low-mass twin

# Varying parameters of EoS with sequential phase transition



### A Sedrakian

Introduction

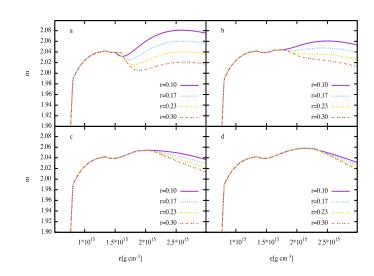
. . . . . . . . . . . . .

Constructin EoS

Sequential phase transitions

Low-mass twin

### .... and resulting topologies of sequences



#### A Sedrakian

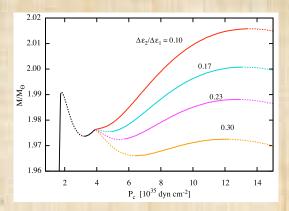
minoduction

Dense QCD

EoS EoS

Sequential phase transitions

Low-mass twin and GW



The stellar mass as a function of the star's central pressure for four different values of  $\Delta \varepsilon_2$ . The other parameters of the EOS are fixed at  $P_1=1.7\times 10^{35}\,\mathrm{dyn\,cm^{-2}}$ ,  $s_1=0.7$ ,  $\Delta \varepsilon_{2\mathrm{SC}}/\varepsilon_1=0.27$ ,  $\Delta \varepsilon_1/\varepsilon_1=0.6$ , and  $s_2=1$ . The vertical dotted lines mark the two phase transitions at  $P_1$  and  $P_2$ . Stable branches are solid lines, unstable branches are dashed lines. We see the emergence of separate 2SC and CFL hybrid branches along with the occurrence of triplets.

### A Sedrakian

Introduction

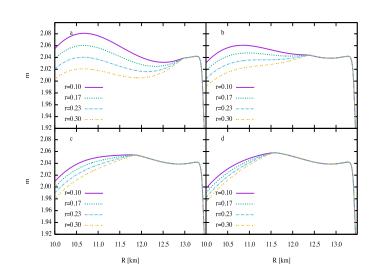
D..... OCD

Constructin EoS

Sequential phase transitions

Low-mass twin

# .... and resulting topologies of mass-radius relations



#### A Sedrakian

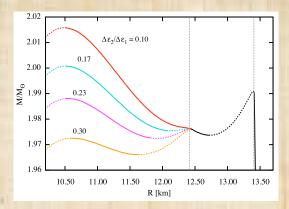
miroductio.

Dense QCI

Constructin EoS

Sequential phase transitions

Low-mass twin



The M-R relations for the parameter values defined above . We have fixed the properties of the nuclear  $\rightarrow$  2SC transition and the speed of sound in 2SC and CFL matter. For the 2SC  $\rightarrow$  CFL transition we have fixed the critical pressure and we vary the energy-density discontinuity  $\Delta\varepsilon_2$ . The separate 2SC and CFL hybrid branches are clearly visible, along with the occurrence of triplets.

#### A Sedrakian

miroduction

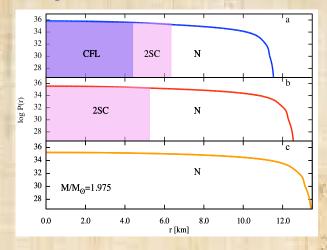
Danca OCT

Constructin EoS

Sequential phase transitions

Low-mass twins and GW

### **Profiles of triplets stars (same mass)**



The profiles (here the log of pressure as a function of the internal radius) of the three members of a triplet with masses  $M=1.975~{\rm M}_{\odot}$ . Here "N" means the nuclear phase. The parameter values are as above, with  $\Delta\varepsilon_2/\Delta\varepsilon_1=0.23$ .

#### A Sedrakian

Introduction

miroductio

Constructin

Sequential phase transitions

Low-mass twin and GW

# Stability conditions for our models

	$\Delta \varepsilon_1/\varepsilon_1$			
$\Delta \varepsilon_2/\Delta \varepsilon_1$	0.4	0.5	0.6	0.7
0.1	s, s	s, s	us, s	u, us
			N-2SC	N-CFL
0.2	s, s	s, s	us, us	u, us
			triplet	N-CFL
0.3	s, s	s, s	us, us	u, us
			N-2SC;N-CFL	N-CFL
0.4	s, s	s, us	us, u	u, u
		2SC-CFL	N-2SC	
0.5	s, s	s, us	us, u	u, u
		2SC-CFL	N-2SC	

In each entry stable/unstable branches are referred by s/u, the 2SC and CFL phases are separated by comma, and the pressure increases from left to right. The presence of twin hybrid configurations or triplet configurations is marked by the underbraces with information about the involved phases ("N" means nuclear).

### A Sedrakian

miroductioi

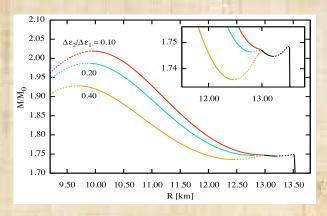
Dense OCD

Constructin EoS

Sequential phase transitions

Low-mass twin and GW

## **Lower mass triplets**



- Low-mass triplets via early transition NM→ QM
- Still 2-solar mass members possible but only with the NM-2SC-CFL composition

### A Sedrakian

Introduction

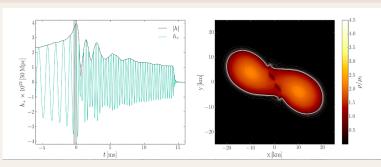
minoductio

Constructin

Sequential phase transitions

Low-mass twin

# GW170817: First gravitational waves from a neutron star merger (Ligo-Virgo-Collaboration)



### The associated EM events observed by over 70 observatories:

- + 2sec gamma ray burst is detected
- +10 h 52 min bright source in optical
- +11 h 36 min infrared emission; +15 h ultraviolet
- +9 days X-rays; +16 days radio

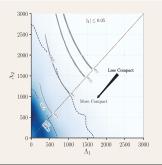
#### A Sedrakian

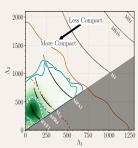
Sequential phase

transitions

TABLE I. Source properties for GW170817: we give ranges encompassing the 90% credible intervals for different assumptions of the waveform model to bound systematic uncertainty. The mass values are quoted in the frame of the source, accounting for uncertainty in the source redshift.

	Low-spin priors $( \chi  \le 0.05)$	High-spin priors $( \chi  \le 0.89)$
Primary mass m <sub>1</sub>	1.36−1.60 M <sub>☉</sub>	1.36-2.26 M <sub>☉</sub>
Secondary mass $m_2$	1.17−1.36 M <sub>☉</sub>	0.86−1.36 M <sub>☉</sub>
Chirp mass M	$1.188^{+0.004}_{-0.002}M_{\odot}$	$1.188^{+0.004}_{-0.002}M_{\odot}$
Mass ratio $m_2/m_1$	0.7–1.0	0.4-1.0
Total mass $m_{tot}$	$2.74^{+0.04}_{-0.01}M_{\odot}$	$2.82^{+0.47}_{-0.09}M_{\odot}$
Radiated energy $E_{rad}$	$> 0.025 M_{\odot} c^2$	$> 0.025 M_{\odot}c^{2}$
Luminosity distance D <sub>L</sub>	40 <sup>+8</sup> <sub>-14</sub> Mpc	40 <sup>+8</sup> <sub>-14</sub> Mpc
Viewing angle Θ	≤ 55°	≤ 56°
Using NGC 4993 location	≤ 28°	≤ 28°
Combined dimensionless tidal deformability $\tilde{\Lambda}$	≤ 800	≤ 700
Dimensionless tidal deformability $\Lambda(1.4M_{\odot})$	≤ 800	≤ 1400





### A Sedrakian

miroducii

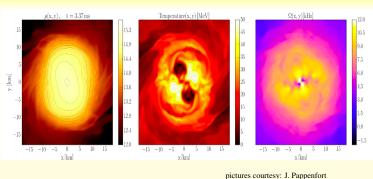
Dense OC

Constructin EoS

Sequential phase transitions

Low-mass twir

### New nuclear physics labora tories



- extreme high temperatures  $\sim 100 \text{ MeV}$
- supra-nuclear densities  $\sim 5 \times n_s$
- high and differential rotation rates

#### A Sedrakian

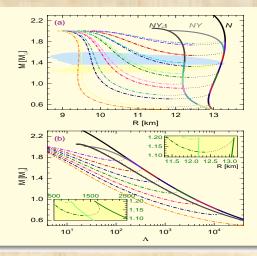
Introduction

Dense OCD

Constructin EoS

Sequentia phase transitions

Low-mass twins and GW



(a) Mass-radius relation for hybrid stars with a single QCD phase translation, with different hadronic envelopes. (b) Mass-deformability relation for stars featuring nucleonic envelopes. The inset shows the results for the case  $M_{\rm max}^{\rm H}/M_{\odot}=1.20$ .

#### A Sedrakian

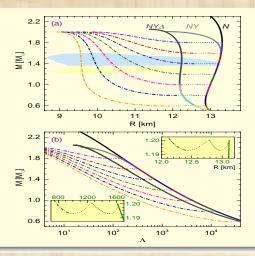
Introduction

Dense OCD

Constructin EoS

Sequentia phase transitions

Low-mass twins and GW



(a) Mass-radius relation for hybrid stars with a single QCD phase translation, with different hadronic envelopes. (b) Mass-deformability relation for stars featuring nucleonic envelopes. The inset shows the results for the case  $M_{\rm max}^{\rm H}/M_{\odot}=1.20$ .

### A Sedrakian

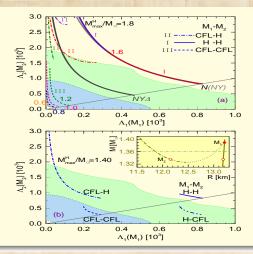
Introduction

Dense QCD

Constructin EoS

Sequential phase transitions

Low-mass twins and GW



a) Tidal deformabilities of compact objects in the binary with chirp mass  $\mathcal{M}=1.186M_{\odot}$  (b) Prediction by an EoS with maximal hadronic mass  $M_{\max}^{H}=1.365M_{\odot}$ . The inset shows the mass-radius relation around the phase transition region. The circles  $M_2$  are two possible companions for circle  $M_1$ , generating two points in the  $\Lambda_1$ - $\Lambda_2$  curves while one point is located below the diagonal line.

#### A Sedrakian

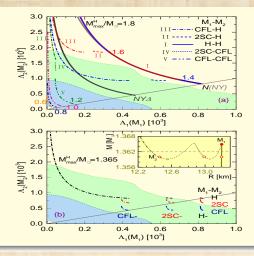
Introduction

Dense QCD

EoS EoS

Sequential phase transitions

Low-mass twins and GW



The case of double phase transition a) Tidal deformabilities of compact objects in the binary with chirp mass  $\mathcal{M}=1.186M_{\odot}$  (b) Prediction by an EoS with maximal hadronic mass  $M_{\rm max}^{\rm H}=1.365M_{\odot}$ . The inset shows the mass-radius relation around the phase transition region. The circles  $M_2$  are two possible companions for circle  $M_1$ , generating two points in the  $\Lambda_1$ - $\Lambda_2$  curves while one point is located below the diagonal line.

### A Sedrakian

miroductic

Dense QC

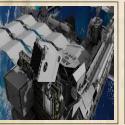
Constructin EoS

phase transition

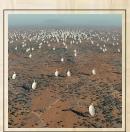
Low-mass twins and GW

### Near future experimental advances:

- NICER (X-ray studies of neutron stars)
- LIGO-VIRGO (Gravitational waves from BNS and pulsars)
- SKA (radio timing of pulsars)







### Theory questions:

- Dense QCD phases: static and dynamic properties
- Astrophysical properties of compact stars with quark phases
- Triplets and twins
- Gravity wave and QCD

Thank you for your attention!