

# Lattice results on exotics with hidden charm and bottom

Sasa Prelovsek

Faculty of Mathematics and Physics, University of Ljubljana

Department of Theoretical Physics, Jozef Stefan Institute, Ljubljana

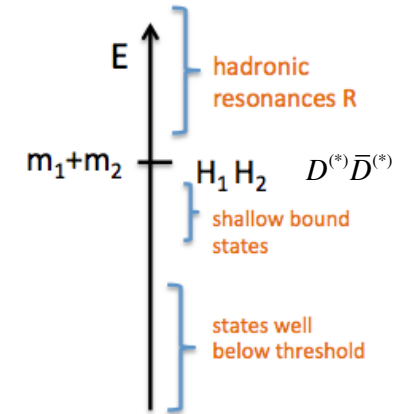
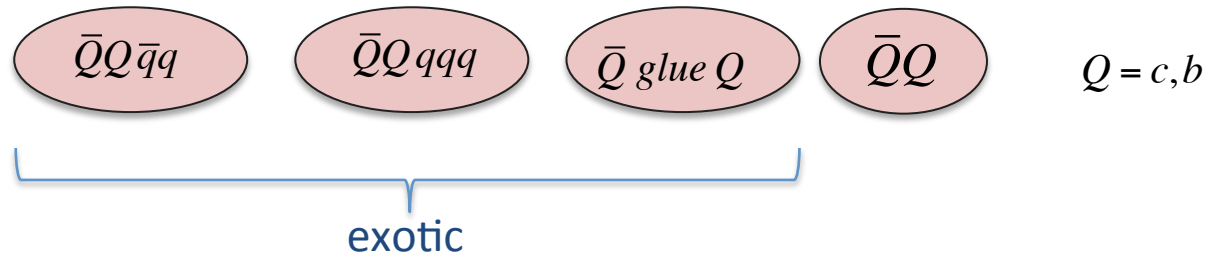
University of Regensburg



Implications of LHCb measurements and future prospects

16.10.2019

# Outline



Hadrons with hidden charm and bottom; focus on exotic and lattice results:

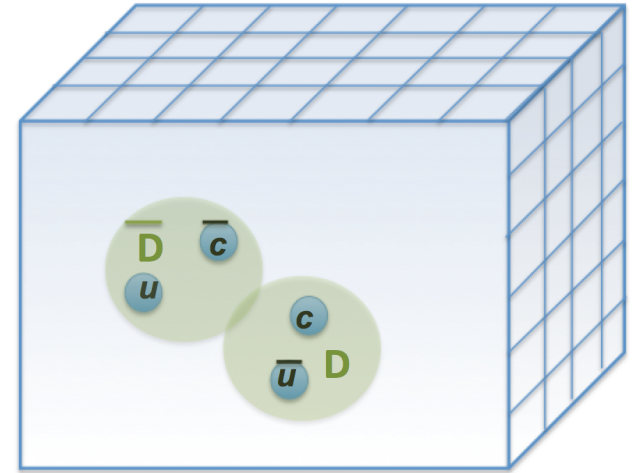
- states well below strong decay threshold or treated as strongly stable “doable”
- states above or just below one threshold “more difficult, but doable”
- state above several threshold ( $Z_c, Z_b, P_c, \dots$ ) “challenging”
- lattice predictions of yet undiscovered exotic hadrons (but with different flavor than indicated above)

# Lattice QCD

$$L_{QCD} = -\frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu} + \sum_{q=u,d,s,c,b,t} \bar{q} i \gamma_\mu (\partial^\mu + i g_s G_a^\mu T^a) q - m_q \bar{q} q$$

$$\langle C \rangle = \int DG Dq D\bar{q} C e^{-S_{QCD}/\hbar}$$

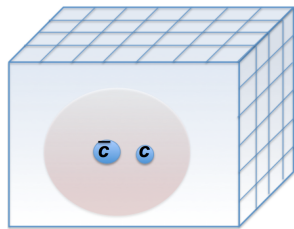
discretized finite Euclidian  
space-time



## Determine energies of eigenstates $E_n$ and overlaps

charmonium:  $J^{PC} : \bar{c} \Gamma c, (\bar{c} \Gamma_1 u)(\bar{u} \Gamma_2 c) = D \bar{D}, [\bar{c} \Gamma_3 \bar{u}][c \Gamma_4 u]$

$$C_{ij}(t) = \langle 0 | \mathcal{O}_i(t) \mathcal{O}_j^\dagger(0) | 0 \rangle = \sum_n \underbrace{\langle 0 | \mathcal{O}_i | n \rangle}_{\text{overlap}} e^{-E_n t} \underbrace{\langle n | \mathcal{O}_j^\dagger | 0 \rangle}_{\text{energy of eigenstate } |n\rangle}$$



$$J^{PC} = 1^{--} : E_1(\vec{p} = 0) = m_{J/\psi}$$

$\bar{c}c$  and  $\bar{b}b$  annihilation omitted for all result in this talk.  
Then hadrons below  $\underline{D}D$  or  $\underline{B}B$  are strongly stable

$$E_n(\vec{p} = 0) = m_n$$

**States well below thresholds  
or  
treated as strongly stable  
“doable”**

# Excited bottomonia, bottomonium hybrids

$\bar{b} b$



$\bar{b} \text{ glue } b$



$m_{\text{hybrid}} \geq 10.9 \text{ GeV}$

S. Ryan & D. Wilson,  
Hadron Spectrum Coll,  
private communication  
details in Lattice2019 talk  
(to appear)

lattice QCD:  $m_{\pi} \approx 400 \text{ MeV}$   
relativistic b-quark:  
main challenge a  $m_b$  errors

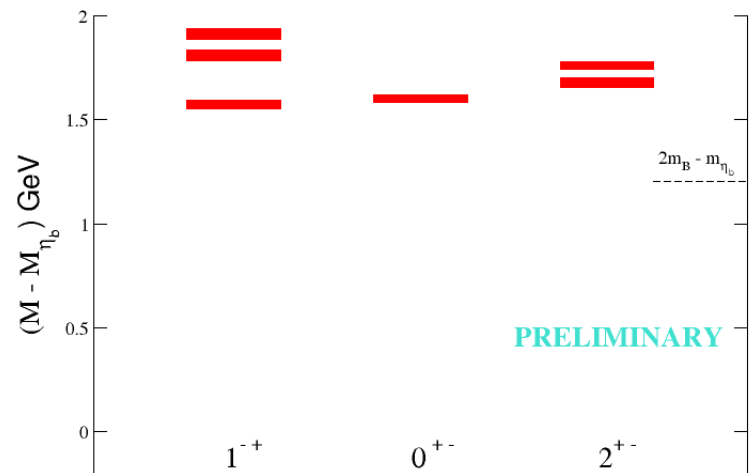
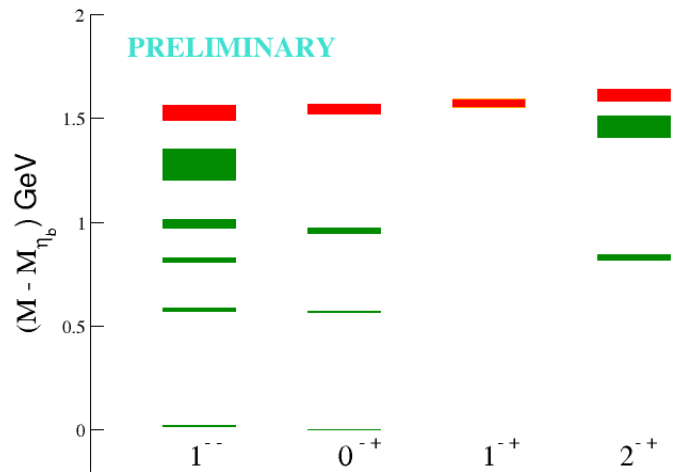
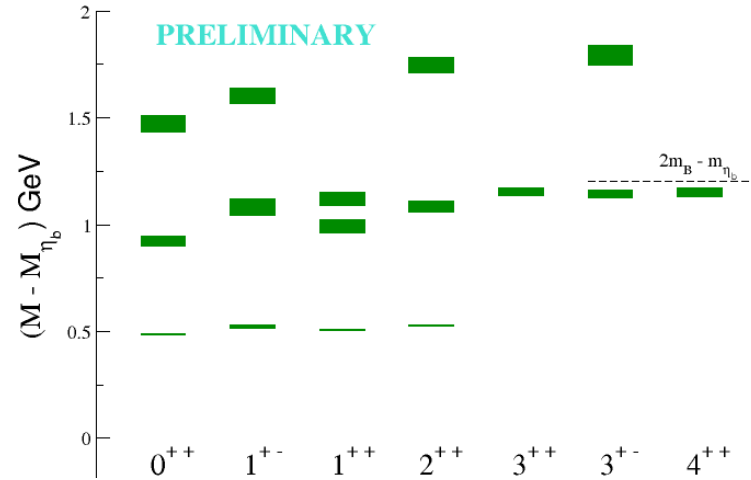
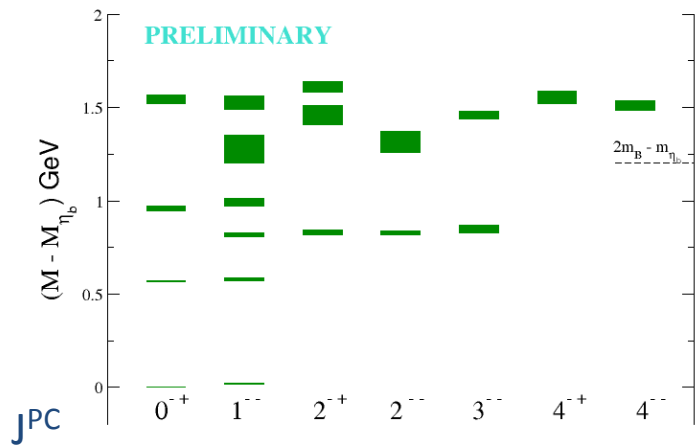
states above  $B\bar{B}$  threshold  
treated as strongly stable

most of states below  $B\bar{B}$   
experimentally discovered

previous lattice results on  
excited  $b\bar{b}$  spectrum  
[Wurtz, Lewis, Woloshyn,  
1505.04410, PRD]

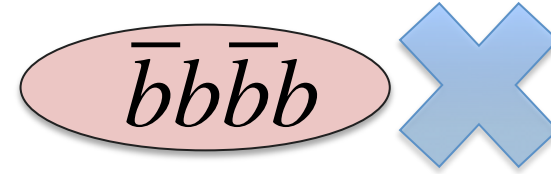
EFT+lattice prediction of  
hybrids [Brambilla, Lai,  
Segovia, Castella, Vario,  
1805.07713, PRD 2019]

charmonium hybrids:  
backup slides



exotic  $J^{PC}$

# Non-existence of strongly stable fully beautiful tetraquark



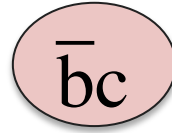
Lattice QCD: No indication for strongly stable state (below threshold) with

$$J^{PC} = 0^{++}, 1^{+-}, 2^{++}$$

threshold  $\eta_b\eta_b$   $\eta_b\Upsilon$   $\Upsilon\Upsilon$

[Hughes, Eichten, Davies, HPQCD, 1710.03236, PRD 2018]

# Discovery of $B_c^*(2S)$ & confirmation of $B_c(2S)$



$m[B_c(2S)]:$  6872.1(1.3)(0.1)(0.8) MeV

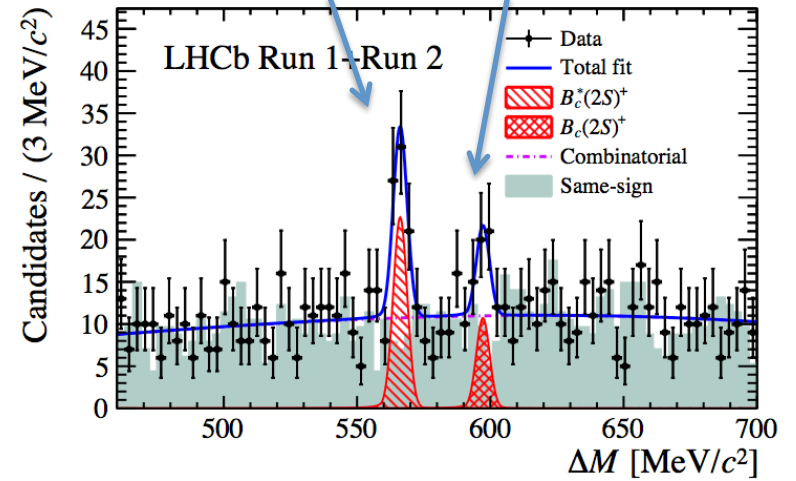
$B_c^*(2S)$  peak at  $M=m[B_c(2S)] - \Delta M$  6841.2(0.6)(0.1)(0.8) MeV

agrees with [CMS, 1902.00571, PRL]

$B_c^*(2S) \rightarrow B_c^* \pi^+ \pi^-$ ,  $B_c^* \rightarrow B_c \gamma$  photon undetected

[LHCb, 1904.00081, PRL]

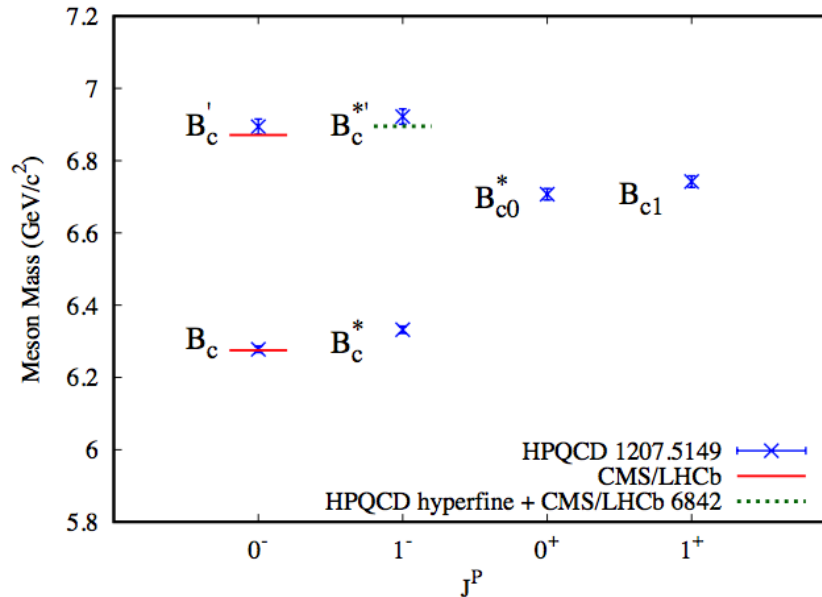
$B_c^*(2S)$  peak  $m[B_c(2S)]$



## Lattice QCD:

[HPQCD, 1207.5149, Lytle, talk at QWG19]

c: relativistic  
b: NRQCD



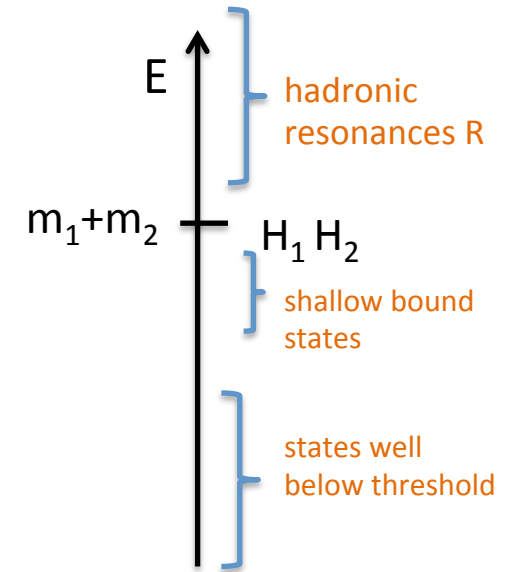
$$\Delta M = \{m[B_c^*] - m[B_c]\} - \{m[B_c^*(2S)] - m[B_c(2S)]\}$$

-----  
 $m[B_c^*(2S)]$  determined using  $\Delta M$  from experiment and  $m(B_c^*) - m(B_c)$  from lattice (HPQCD)

$c\bar{c}$  and  $b\bar{b}$  annihilation omitted for all result in this talk.  
Then hadrons below  $\underline{D}\underline{D}$  or  $\underline{B}\underline{B}$  are strongly stable

strong decay threshold:

$$D^{(*)}\bar{D}^{(*)}, \quad B^{(*)}\bar{B}^{(*)}$$



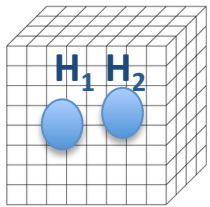
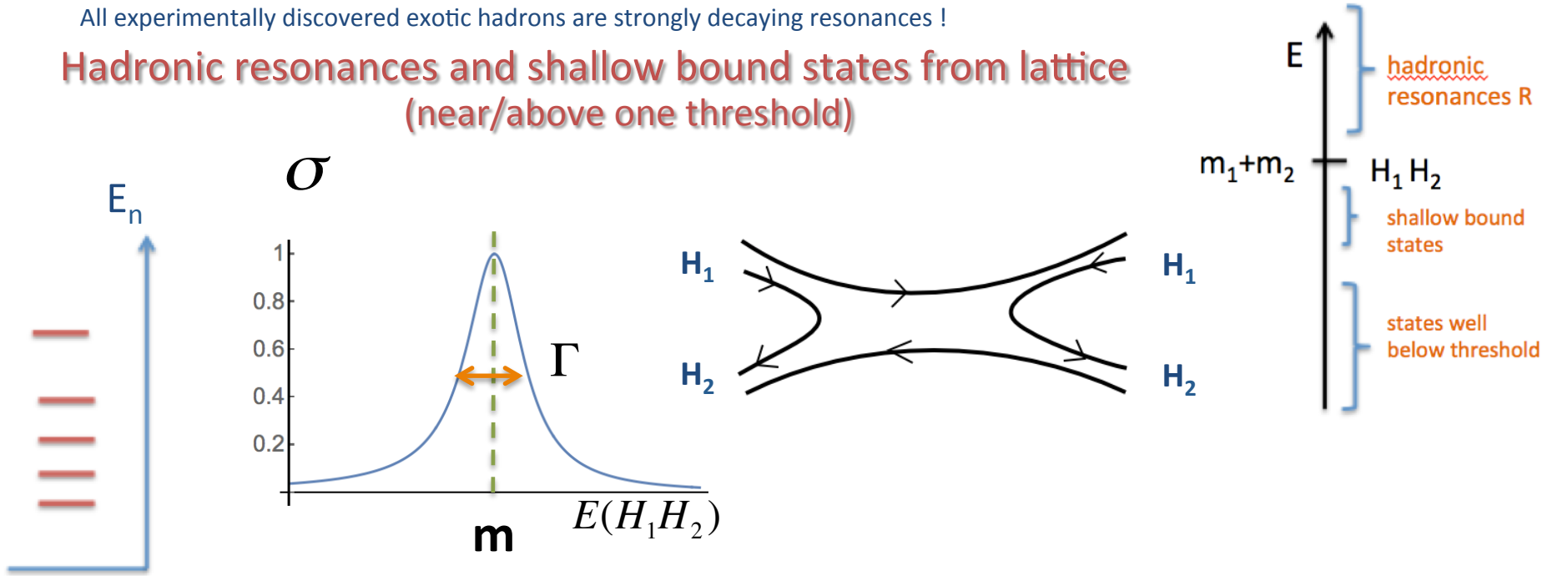
## States above or slightly below one threshold

“more difficult, but doable”



All experimentally discovered exotic hadrons are strongly decaying resonances !

## Hadronic resonances and shallow bound states from lattice (near/above one threshold)



energy of eigenstate

scattering matrix for real E

$E \rightarrow$

$T(E)$

$$\sigma(E) \propto |T(E)|^2$$

continuation to complex E

analytic relation:

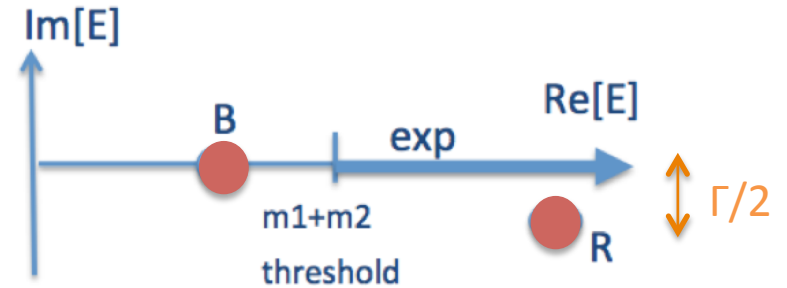
Luscher 1991

Sasa Prelovsek

$$T_B(E) \propto \frac{1}{E^2 - m_B^2}$$

$$T_B(E = m_B) = \infty$$

$$T_R(E) = \frac{-m_R \Gamma}{E^2 - m_R^2 + i m_R \Gamma}$$



location of poles in complex E plane

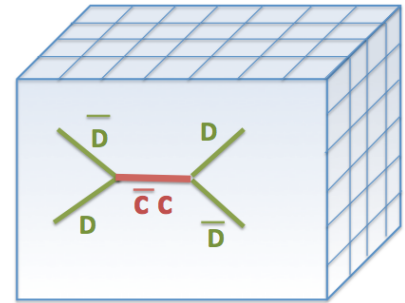
$E = E_{cm}$

Lattice results on exotics with hidden bottom and charm

# Charmonia with $J^{PC}=3^-$ and $1^{--}$

$\bar{c}c$  conventional  
 $n^{2s+1}l_J = 1^3D_3, 1^3D_1$

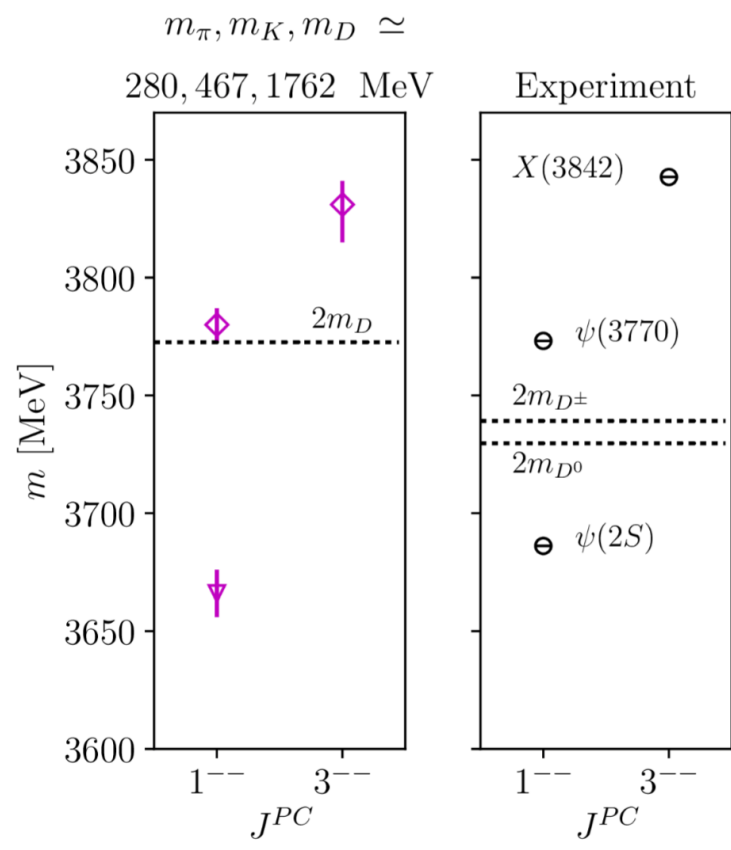
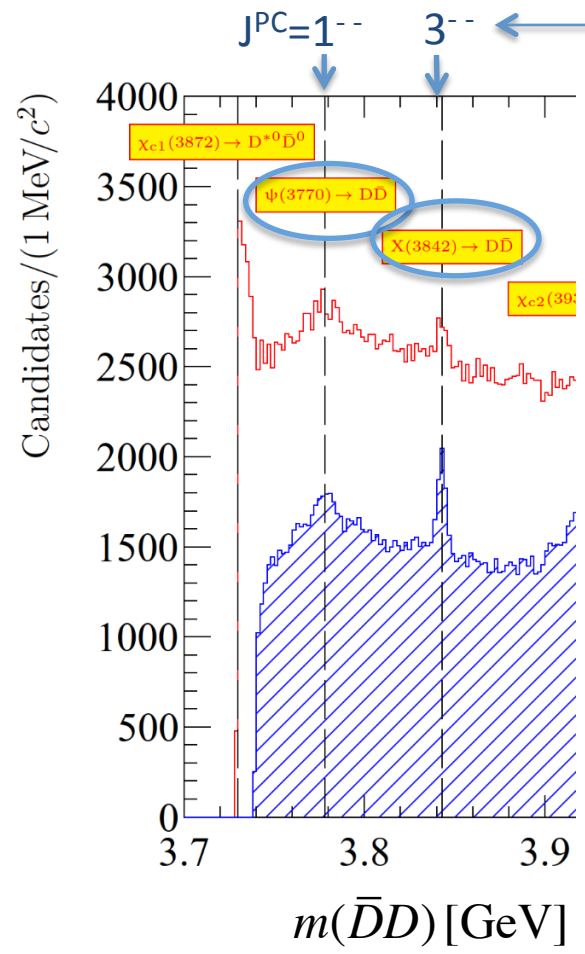
first discovery of charmonium with  $J=3$



partial waves  $L=3$  and  $L=1$

LHCb 2019, 1903.12240, JHEP 2019

Lattice QCD: Piemonte, Collins, Padmanath, Mohler, S.P. : 1905.03506, PRD 2019



widths of resonances:

- $\psi(3770)$

$$\Gamma = \frac{g^2 p^3}{6\pi s}$$

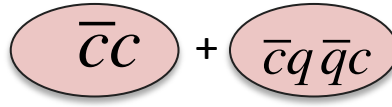
	$g$
lat	$16.0^{+2.1}_{-0.2}$
exp	$18.7 \pm 0.9$

- $X(3842)$

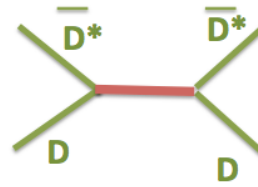
to narrow to resolve in this lat. sim.

# $\chi_{c1}(2P)$ aka $X(3872)$

[Belle, 2003]



Aim: look for poles in  $D\bar{D}^*$  scattering matrix



- Lattice QCD
- first evidence [S.P., Leskovec, 1307.5172, PRL 2013] ➔
- Fock components: [Padmanath, Lang, S.P., 1503.03257, PRD 2015]

crucial:  $D\bar{D}^*$ ,  $\bar{c}c$ , less important:  $(\bar{c}q)(cq)$

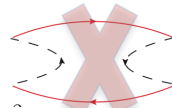
no charged partner found up to  $m=4.2$  GeV (in agreement with exp)  
 unfortunately, no other published lattice paper on  $X(3872)$  till now

- Dyson-Schwinger / Bethe-Salpeter approach ➔

[Wallbott, Eichmann, Fischer, 1905.02615, PRD 2019]

location of pole in the scattering matrix

- pole for X found although  $\bar{c}c$  Fock component omitted,  $q\bar{q}$  annihilation omitted  
 (in contrary: lattice studies find that  $\bar{c}c$  is crucial for getting pole related to X)



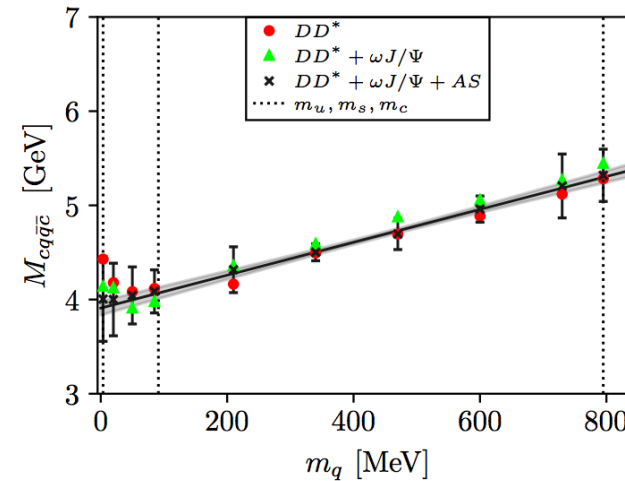
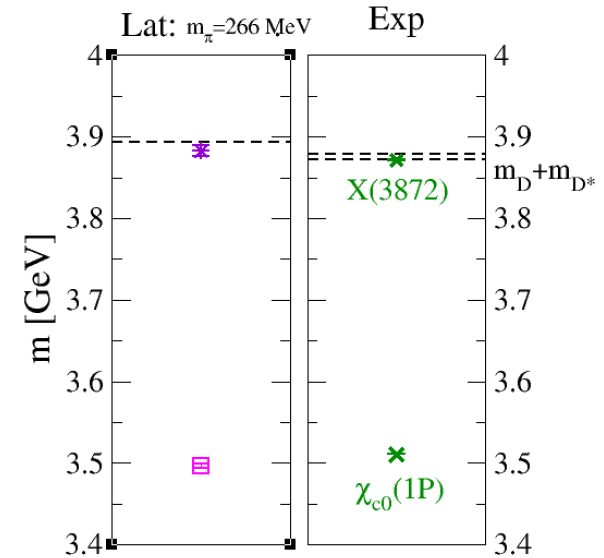
- exp evidence that X is not completely molecular:

ideal combination of  $I=0,1$  (molecule) would lead to completely dominant rate to  $J/\psi \rho$   
 (since  $J/\psi$   $\omega$  is 7 MeV above and  $\omega$  is very narrow), while exp rates are comparable

$\bar{c}c : (I=0)$

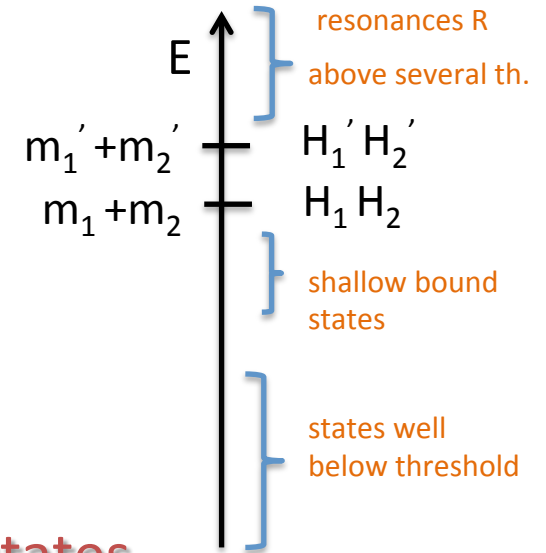
molecule:  $(I=0) + (I=1)$

$X \rightarrow J/\psi \omega, J/\psi \rho$



$$M_{1^{++}}^{cq\bar{q}c} = 3916(74) \text{ MeV}$$

mass not accurate enough to determine whether below or above  $D\bar{D}^*$  threshold



## Hadrons that strongly decay to several final states

### Scattering in two or more channels

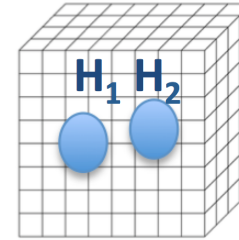
“challenging”

examples: all experimentally discovered  $Z_c$ ,  $Z_b$ ,  $P_c$

Extracting scattering matrix from lattice

## Resonance above one threshold

$$R \rightarrow H_1 H_2 \quad T(E) \xleftarrow{E_n} \text{Luscher's method}$$



Lattice simulation of one-channel scattering via Luscher's method: doable

## Resonance above two or more thresholds

most of exotic hadrons are above more than one threshold, for example  $Z_c(4430)$

$$R \rightarrow H_1 H_2, H_1' H_2'$$

$$\text{channel } a: H_1 H_2$$

$$\text{channel } b: H_1' H_2'$$

$$T(E) = \begin{bmatrix} \begin{matrix} a \rightarrow a \\ T_{aa}(E) \end{matrix} & \begin{matrix} a \rightarrow b \\ T_{ab}(E) \end{matrix} \\ \begin{matrix} T_{ab}(E) \\ b \rightarrow a \end{matrix} & \begin{matrix} T_{bb}(E) \\ b \rightarrow b \end{matrix} \end{bmatrix} \xleftarrow{E_n} \text{Luscher's method}$$

Lattice simulation of coupled-channel scattering via Luscher's method: challenging

- several coupled channels studied in the light-quark sector (Hadron Spectrum collaboration)
- only simulations for hadrons with heavy quarks  
excited D mesons [Moir, Peardon, Ryan, Thomas, Wilson, 1607.07093, JHEP 2016]  
 $Z_c$  channel [Chen et al., CLQCD, 1907.03371]
- final conclusions on many interesting states therefore not available (yet)

# $P_c$ pentaquarks



$P_c = uud\bar{c}c \rightarrow (uud) (\bar{c}c): p J/\psi, \dots$

$\rightarrow (udc) (\bar{c}u): \Sigma_c^+ \bar{D}^0, \dots$

[LHCb 2019, 1904.03947, PRL]

Indications that  $\Sigma_c^+ \underline{D}^{(*)}$  molecular component is important:

- **experiment** finds them slightly below those thresholds
- supported by **phenomenological models** with  $\rho/\omega$  exchange predicted 2010-2012 [Wu, Molina, Oset, Zou, 1007.0573, PRL; Wu et al., 1202.1036, PRC, Yang et al, 1105.2901, Wang et al, 1101.0453, PRC]

- **Lattice QCD** addressed simplified question:

Do  $P_c$  resonances appear in one-channel

$p J/\psi \rightarrow P_c \rightarrow p J/\psi$

scattering if it is decoupled from other channels ?

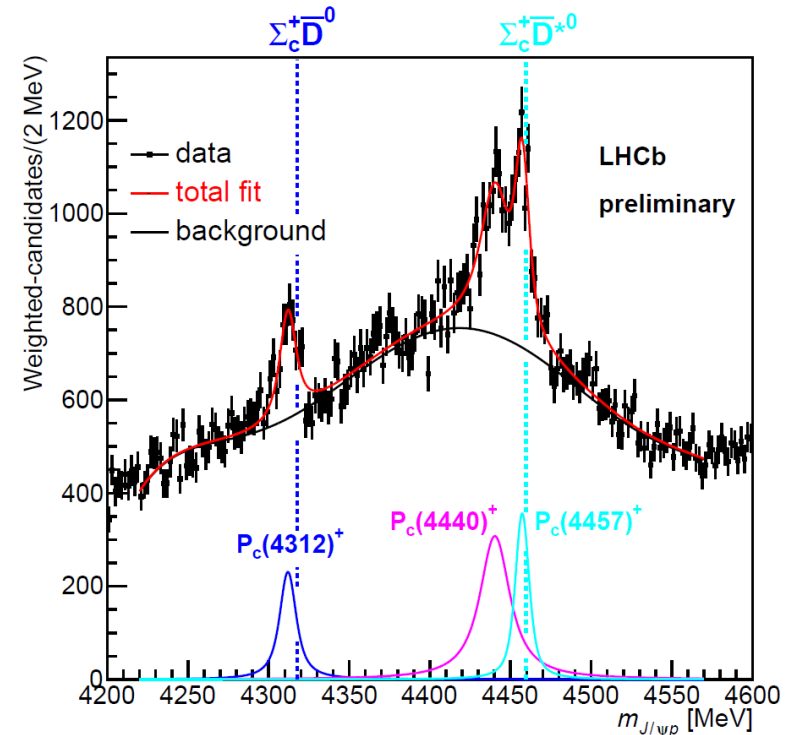
Answer: No [Skerbis, S. P., 1811.02285, PRD 2019]

$T(E) \approx 0$  within large errors, small interaction, no resonance

$J^P$  not determined from exp.

Expected  $J^P$  for molecule in s-wave:

$\Sigma_c(\frac{1}{2}^+) \bar{D}(0^-) \rightarrow J^P = \frac{1}{2}^- \quad \Sigma_c(\frac{1}{2}^+) \bar{D}^*(1^-) \rightarrow J^P = \frac{1}{2}^-, \frac{3}{2}^-$



This indicates that coupling of  $p J/\psi$  channel with other two-hadron channels is likely responsible for  $P_c$  in experiment (in line with LHCb result)

$Z_c^+(3900)$



$Z_c^+ \rightarrow J/\psi \pi^+, \dots$

[BES III, Belle, 2013]

Consensus on the nature of  $Z_c(3900)$  has not been achieved

- ◆ re-analysis of all experimental data is compatible with several scenarios: resonance pole above th., bound state, virtual bound state, kinematical enhancement via triangular diagram

[Pilloni et al, 1612.06490, PLB 2017]

- ◆ Lattice QCD :

extract scattering matrix for coupled channel scattering  $J/\psi \pi, D\bar{D}^*$

- [Ikeda et al., HALQCD, 1602.03465, PRL]

HALQCD method (which was not verified yet on any conventional resonance)

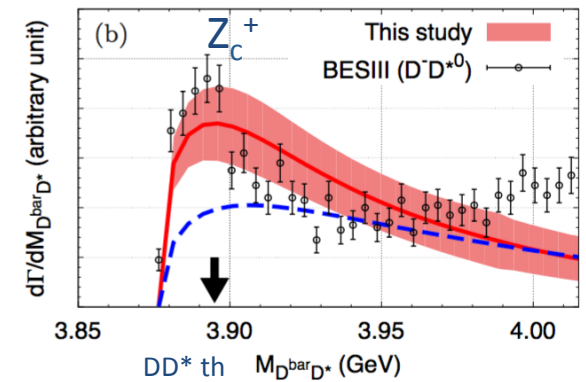
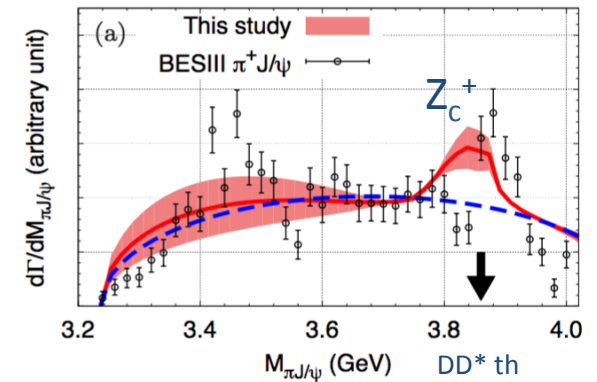
- $Z_c^*(3900)$  coupled-channel effect due to sizable  $J/\psi \pi$  and  $DD^*$  coupling, not genuine resonances (i.e. pole on the unphysical sheet above  $DD^*$  th.)

- [Chen et al., CLQCD, 1907.03371]

- Luscher's method :  $T(E) \approx$  small, small interaction  
no narrow resonance behavior found near  $DD^*$  th.
- in line with previous lattice study that did not extract the scattering matrix

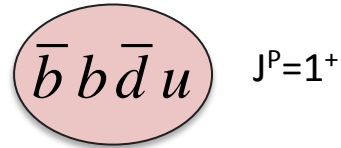
[S.P. et al, 1401.7623, PRD 2015 & HSC, 1709.01417, JHEP 2017]

[Ikeda et al., HALQCD, 1602.03465, PRL]



— differential rate from lattice  
 - - - rate from lattice if coupling between  $J/\psi \pi$  and  $DD^*$  channels set to zero by hand

# $Z_b^+(10610), Z_b^+(10650)$



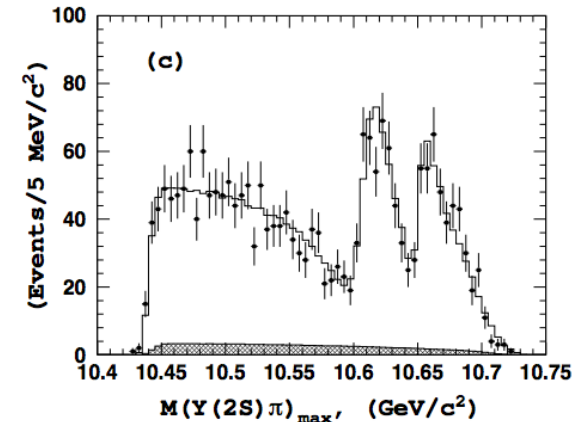
$Z_b^+ \rightarrow \Upsilon(1S, 2S, 3S) \pi^+, h_b(1S, 2S) \pi^+, B^{(*)} \bar{B}^*$

[Belle, 1110.2251, PRL 2012]

Indications that molecular  $B \bar{B}^*$  in  $Z_b^+(10610)$  is crucial:

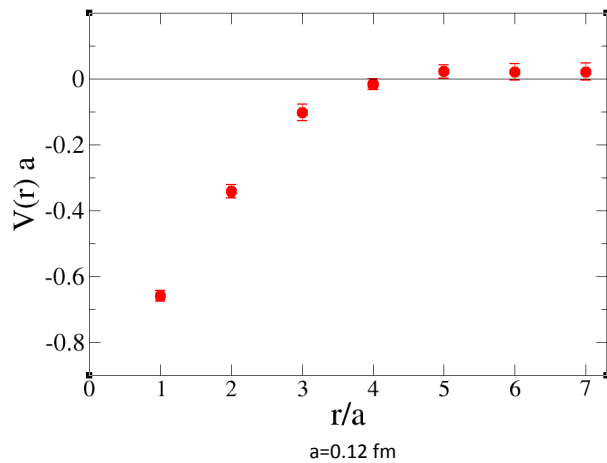
- lies near  $m_B+m_{B^*}$  threshold
- $Br(B \bar{B}^*) \approx 85\%$  although this mode is phase space suppressed
- molecule  $(S_{\bar{b}b} = 1) \otimes (S_{\bar{q}q} = 0) \pm (S_{\bar{b}b} = 0) \otimes (S_{\bar{q}q} = 1)$   
this makes it natural that  $Z_b$  decays comparably to  $\Upsilon (S_{bb}=1)$  and  $h_b (S_{bb}=0)$

- Exploratory (!) lattice study of  $(S_{\bar{b}b} = 1) \otimes (S_{\bar{q}q} = 0)$  component with static b-quarks [S.P., Bahtiyar, Petkovic, 1909.02356], inspired by [Peters, Bicudo, Wagner, 1602.07621]

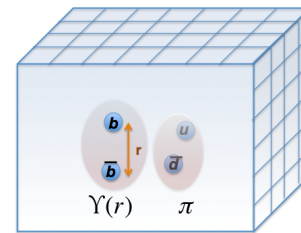
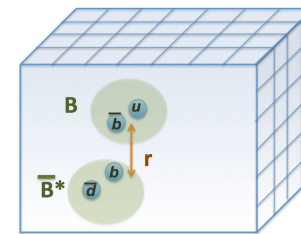


$m_B + m_{B^*}$

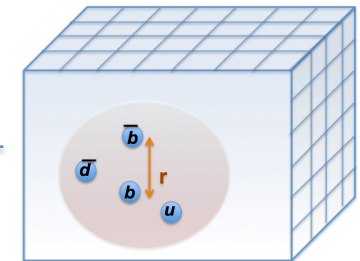
eigen energies  $E_n$  render  
potential between  $B$  and  $\bar{B}^*$



Strong attraction  
between  $B$  and  $\bar{B}^*$   
for  $r=0.1-0.4$  fm.  
Might be responsible  
for existence of  $Z_b$

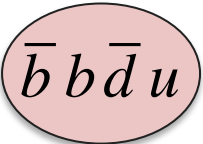


Fock  
components

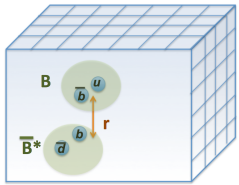




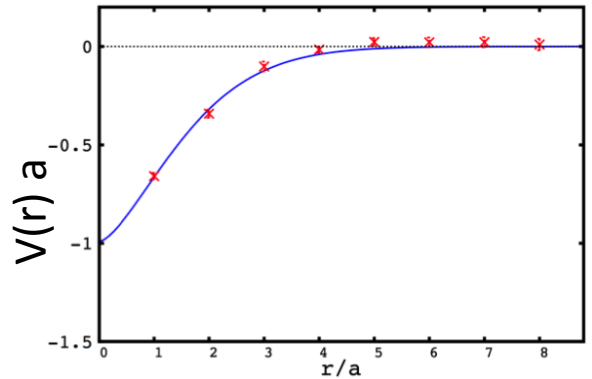
# $Z_b^+(10610), Z_b^+(10650)$



- Lattice study, continued  
[S.P., Bahtiyar, Petkovic, 1909.02356]

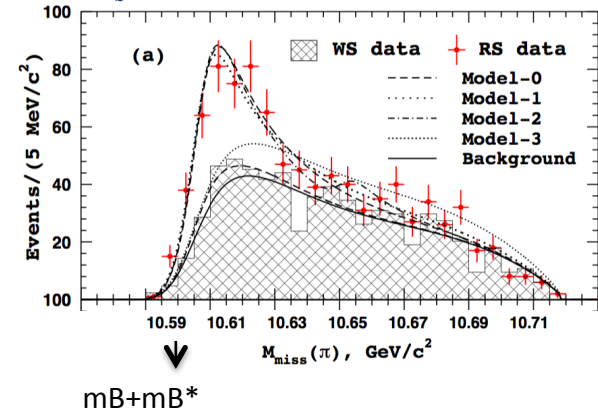


$V(r)$  between B and  $B^*$   
 $a=0.12$  fm  
 $V(r<0.1$  fm) = ?



[Belle, 1512.07419, PRL 2016]

$Z_b(10610)$  in  $B\bar{B}^*$  decay mode



Solving Schrodinger equation for  $B\bar{B}^*$  system with this  $V(r)$ .

Observed attraction leads to virtual  $B\bar{B}^*$  bound state slightly below threshold

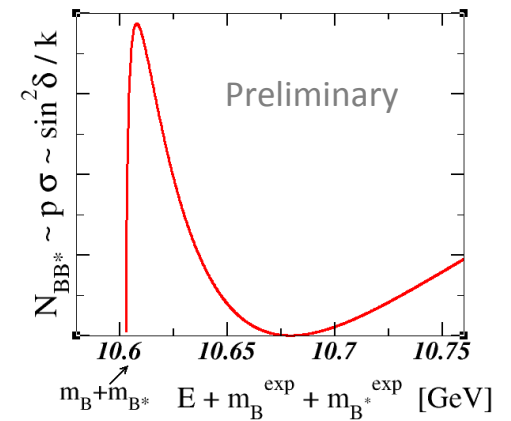
$$\text{Re}[E_{Z_b}] = -32_{-5}^{+29} \text{ MeV}$$

This pole leads to peak in  $N_{B\bar{B}^*}$  above threshold (similar to exp) →

- Virtual bound state consistent with reanalysis of exp data  
[Wang, Baru, Filin, Hanhart, Nefediev, Wynen, 1805.07453, PRD 2018]

So far  $Z_b$  found only by Belle

Could LHCb search for  $Z_b$  in inclusive final state with  $B\bar{B}^*$  ?



pole of  $T(W)$  at  $W_B$

$p = +i|p|$  for bound state

$p = -i|p|$  for virtual bound state

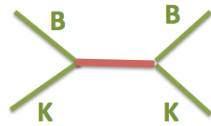
$$W_B = \sqrt{m_B^2 + p^2} + \sqrt{m_{B^*}^2 + p^2} < m_B + m_{B^*}$$

## Lattice predictions of yet unobserved hadrons

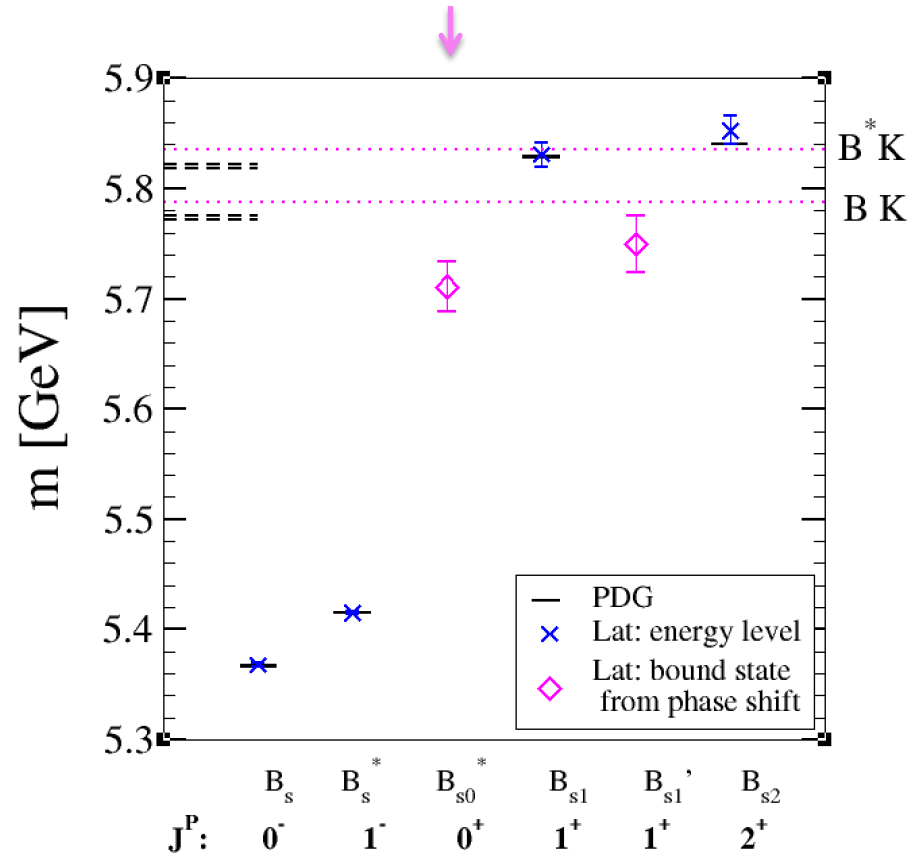
- there are no reliable lattice PRedictions for yet-unobserved  $\bar{Q}Q\bar{q}q$ ,  $\bar{Q}Qqqq$  ( $Q = c, b$ ) since these states likely lie above several thresholds (very challenging)
- Instead, I list predictions of interesting states with different quark content that lie below strong threshold (doable)

# Scalar $B_{s0}$ and axial $B_{s1}$

partner of scalar  $D_{s0}(2317)$



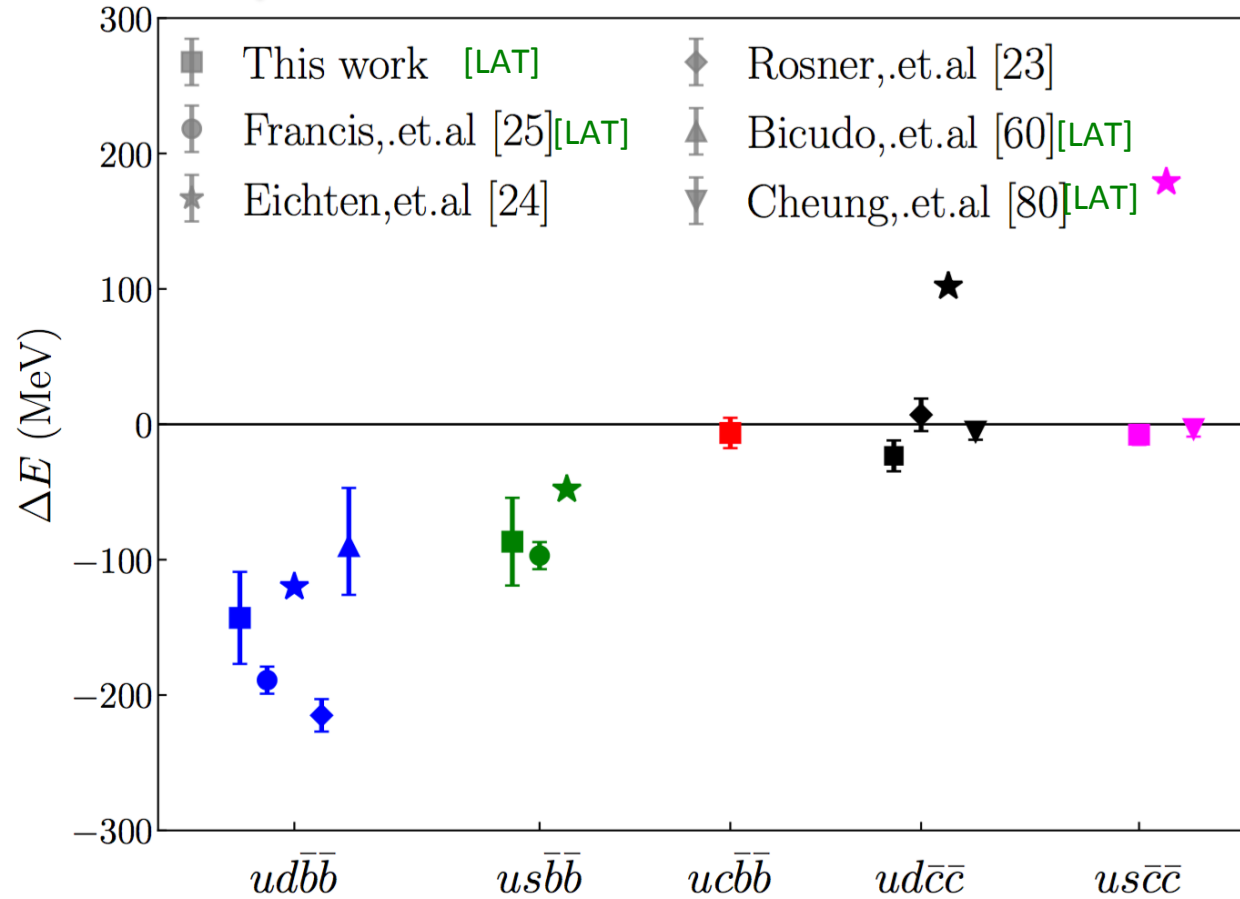
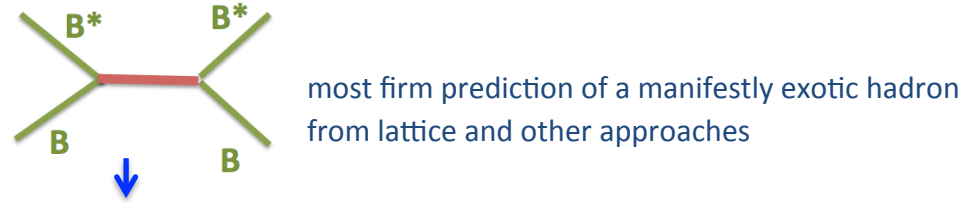
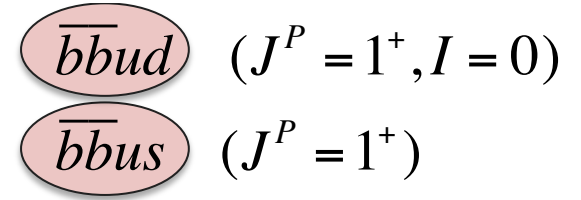
bound state  $B_{s0}^*$  found



lattice QCD, taking into account effects of  $BK^{(*)}$  threshold

[C. Lang, D. Mohler, S.P., R. Woloshyn: 1501.0164, PLB2015]

# Strongly stable doubly bottom tetraquarks



Taken from Junnarkar, Mathur, Padmanath [1810.12285]

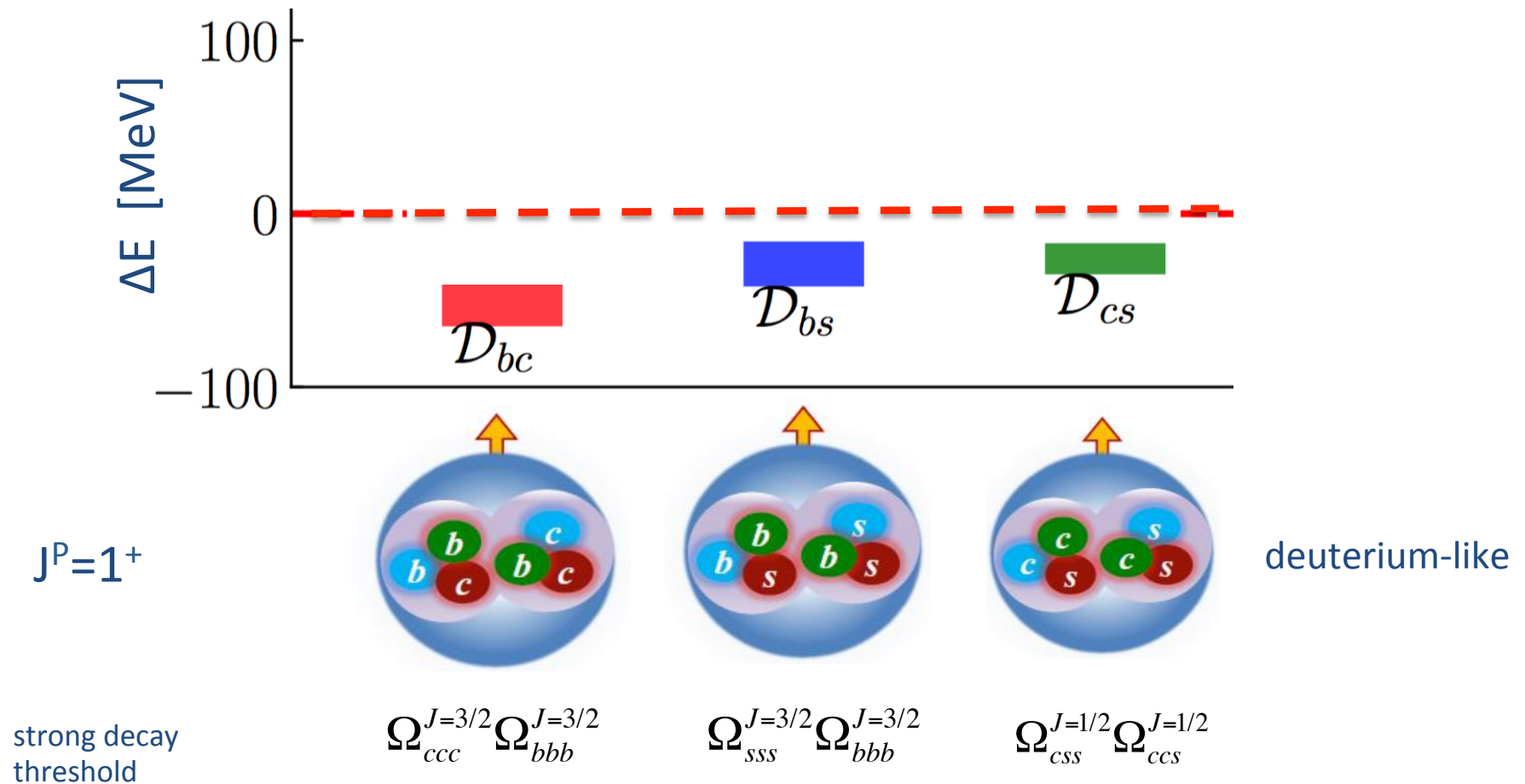
strong decay threshold

$BB^*$

$B_s B^*$

# Strongly and EM stable di-baryons

lattice QCD: Junnarkar, Mathur, [1906.06054, PRL 2019]



# Conclusions

- Compliments to experimental colleagues for discovering a number of conventional and unconventional hadrons !
- Masses of ground and excited hadrons: lattice results and exp agree well
- Lattice QCD can extract scattering matrices for scattering of hadrons: their poles give information on resonances, bound states and virtual bound states
- predictions for many yet undiscovered hadrons
- understanding conventional and exotic states above several thresholds requires extraction of coupled-channel scattering matrices from lattice ...  
Challenging, but hopefully forthcoming

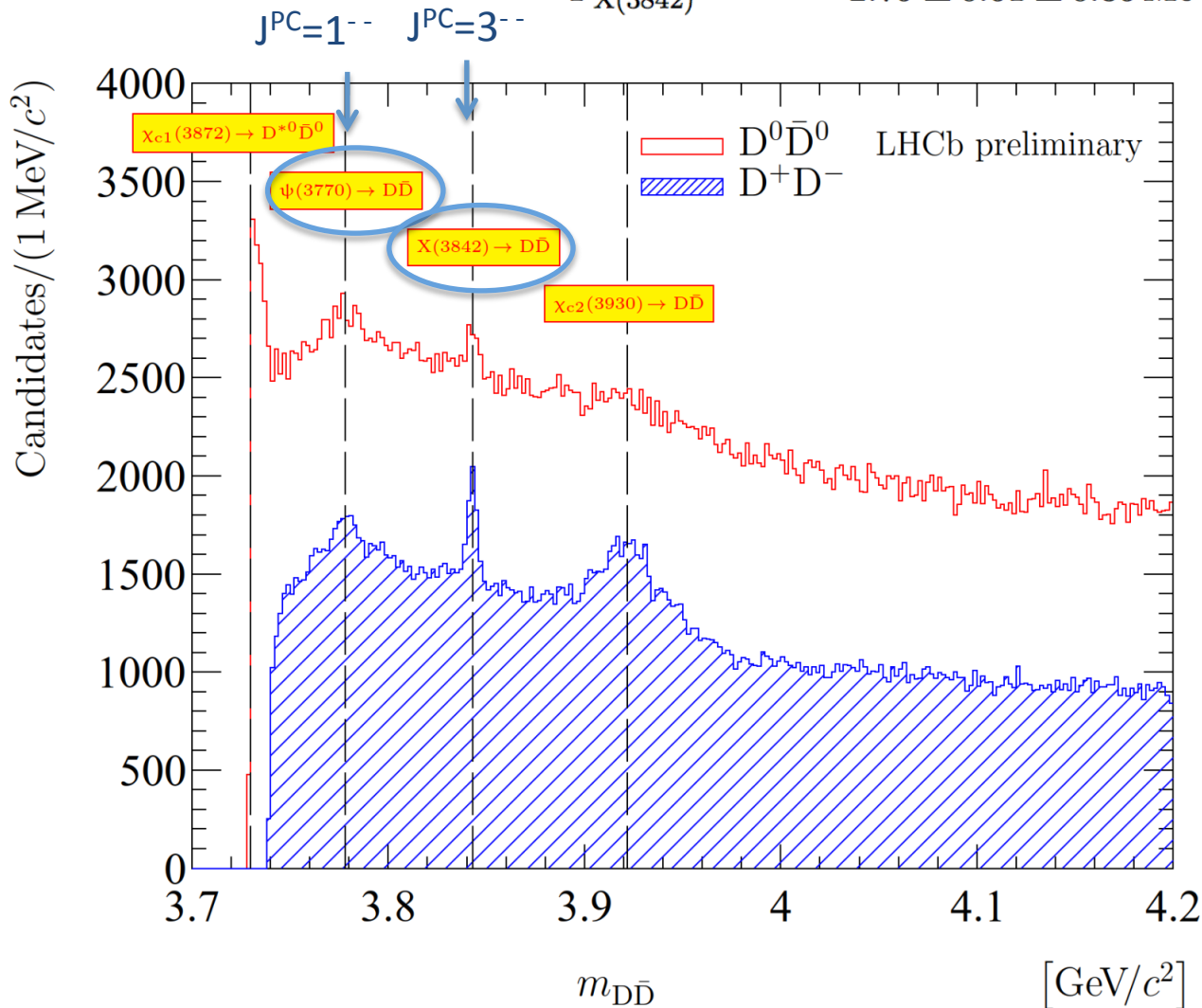
# Backup

# Charmonium resonances in $D\bar{D}$ from LHCb: first discovery of charmonium with $J=3$

$$m_{X(3842)} = 3842.71 \pm 0.16 \pm 0.12 \text{ MeV}/c^2,$$

$$\Gamma_{X(3842)} = 2.79 \pm 0.51 \pm 0.35 \text{ MeV},$$

LHCb 2019  
1903.12240  
JHEP 2019



$J^{PC}$  not experimentally measured

LHCb paper:

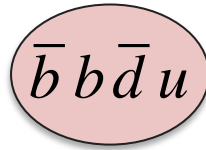
“The narrow natural width and the mass of the X(3842) state suggest the interpretation as charmonium state with  $J^{PC} = 3^{--}$ ”

Quark model quantum numbers:

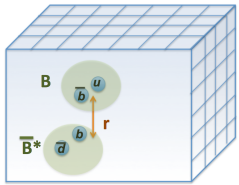
$$n^{2s+1}l_J = 1^3D_3$$



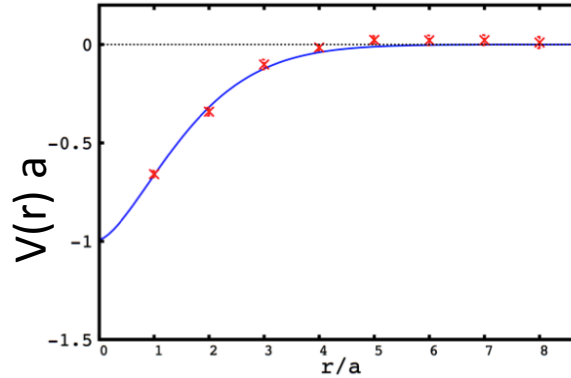
# $Z_b^+(10610), Z_b^+(10650)$



- Lattice study, continued  
[S.P., Bahtiyar, Petkovic, 1909.02356]



$V(r)$  between B and  $\bar{B}^*$   
 $a=0.12$  fm  
 $V(r<0.1$  fm) = ?



Solving Schrodinger equation for  $B\bar{B}^*$  system with this  $V(r)$ .

Observed attraction leads to

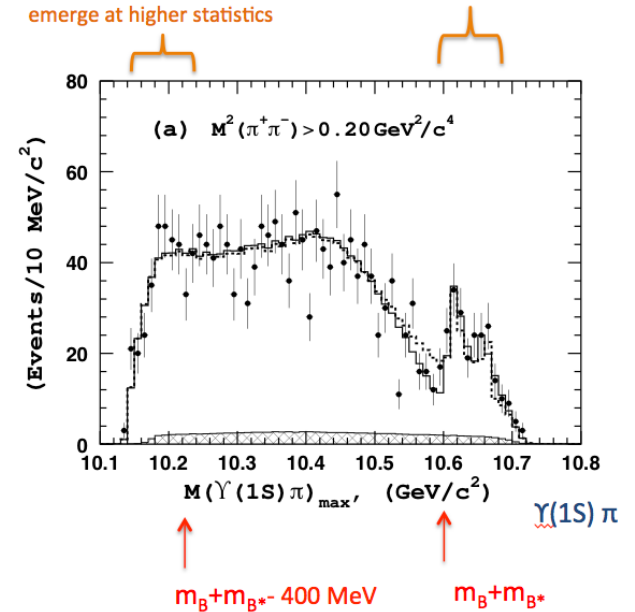
a virtual bound state just below threshold  $\text{Re}[E_{Z_b}] = -32^{+29}_{-5}$  MeV

and also to a deep bound state  $\text{Re}[E_{Z_b}] = -403 \pm 70$  MeV

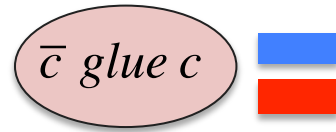
- Could LHCb search for  $Z_b$  in inclusive final state with  $B\bar{B}^*$  ?

Belle PRD 91 (2015) 072003

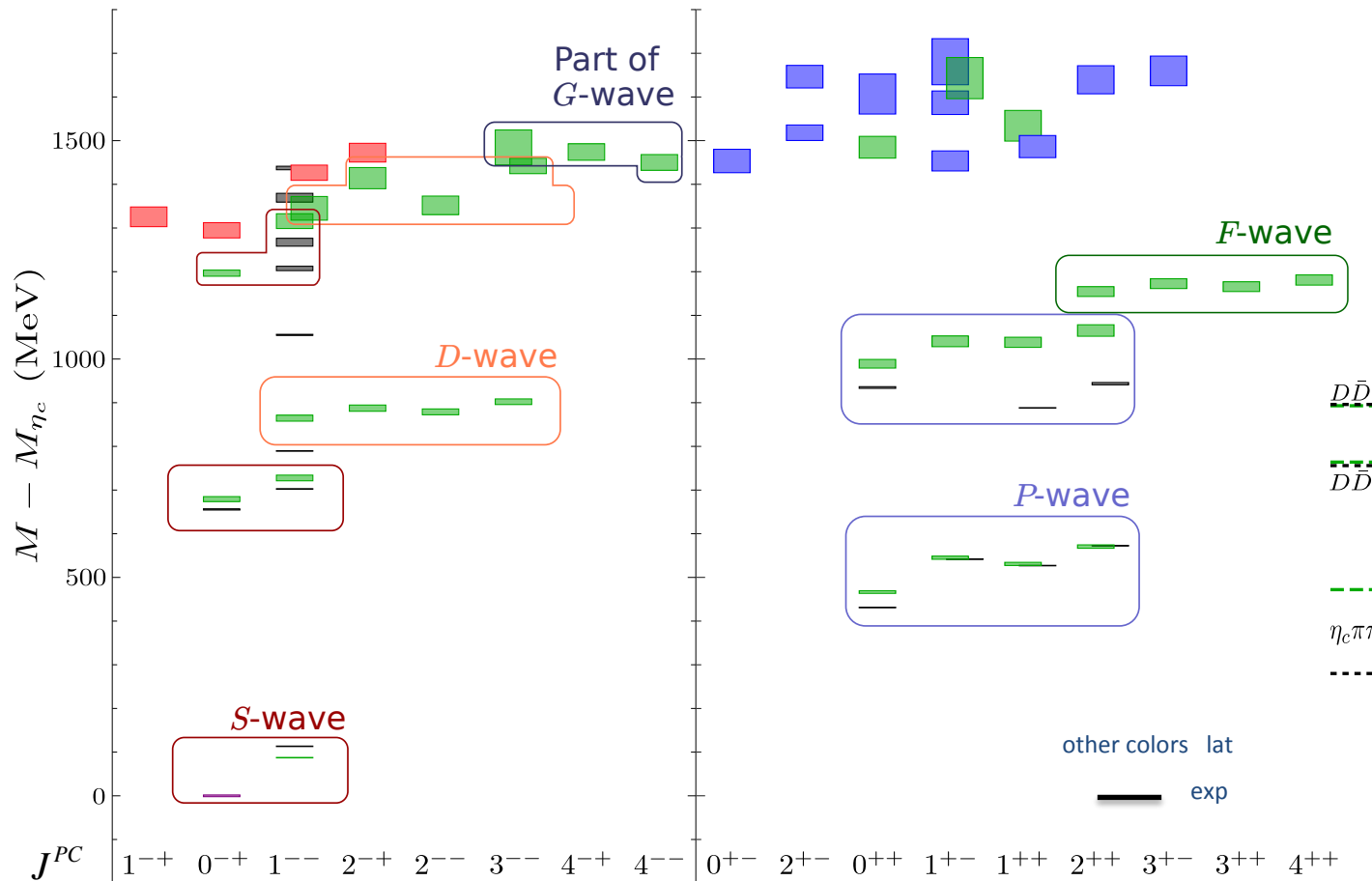
nothing claimed by Belle;  
 significant "bump" could perhaps  
 emerge at higher statistics



# Excited charmonia, charmonium hybrids



[Hadron Spectrum Coll,  
JHEP 2016, 1610.01073]  
lattice QCD:  $m_\pi=240$  MeV



states above  $D\bar{D}$  threshold  
treated as strongly stable;  
effects of thresholds not  
taken into account

red and blue are  
candidates for hybrids  
with excited glue

most of these states  
( $J=3,4$  or exotic  $J^{PC}=1^{-+}, 2^{+}, \dots$ )  
yet to be experimentally  
discovered !!

masses of hybrids in rough  
agreement with EFT+lattice

[Brambilla, Lai, Segovia, Castella, Vario,  
1805.07713, PRD 2019]

prediction also for  $b\bar{b}$  hybrids