

V3.0

CP asymmetries in the decays of charm hadrons with
many-body Final States
& short comments about strange hadrons --
Impact of Non-perturbative QCD on CP Violation

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LHCb WS, October 2019



When Gods speak in Riddles

? Tragic Oracles & Tragic Mis-understanding ?

Delphi \longleftrightarrow
(old Delphi detector is still close
to the LHCb experiment)



When `Gods' (= `Symmetries') speak in Riddles

? Tragic Oracles & Tragic Mis-understanding ?

LHCb & Belle II both as a pioneer about non-pert. QCD & weak dynamics - as a team of experimenters and HEP theorists
[as before BaBar & Belle]

experimenters



theorists

On seeing the missile shot by a catapult which had been brought then for the first time from Sicily, the king from Sparta in the fourth century B.C. cried out:
'By Heracles, this is the end of man's valor.'
Analogy of physicists with computers?

Manifestation of a *divine* being through something both simple & striking:
symmetries & their tools !

Fitting the data vs. *Information* inside the data

1st step: models

2nd step: model-independent analyses – indeed, true progress

3rd step: *best fitted analyses* often do *not* give the best
information about the underlying dynamics;
data are the referees - in the end !

crucial: *collaborations* of *experimenters* & *theorists* with
correlations & *judgments* !

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The *goals* for my talk here:

-- *Direct CP asymmetry* in $D^0 \rightarrow K^+K^-/\pi^+\pi^-$ is a wonderful
1st step for a long traveling for fundamental dynamics !

Next one measures *indirect CP* violation in $D^0 \rightarrow K^+K^-$.

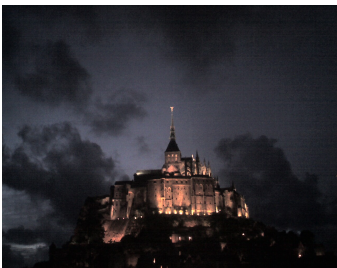
-- *Probes many-body* non-leptonic FS of charm hadrons.

-- Short comments about possible impact of ND on *strange* hadrons.

-- collaboration of HEP & Hadrodynamics from different 'cultures'

- (I) Introdunct: *Wilsonian* OPE, *broken* U- & V-spin symmetries
 - (II) *Consistent* Parameterization of the CKM Matrix
 - (III) *Intermezzo*: *CP asymmetry* in $D^0 \rightarrow K^+K^-/\pi^+\pi^-$
 - (IV) CP asymmetries with $\Delta C \neq 0$ (& lifetimes of charm *baryons*)
 - (V) Direct CP asymmetries for *Strange* Hadrons
- Epilogue for the future: *Collaboration* of HEP & Hadrodynamics
- (VI) Summary: Impact of *non-perturbative* QCD on CP Violation

The slides I think are very important see the symbol



I had produced this picture; later I will explain why it is *not* about bragging rights.

(I) Introduction: *Wilsonian* OPE, *broken* U- & V-spin symmetries

(I.1) *Wilsonian* Operator Product Expansion (OPE)

Almost all invoke OPE -- often *without* using *Wilsonian* prescription!

However: "not all OPE's are created equality!"

Shifman & collaborators had emphasized applying OPE is subtle:

the *Wilsonian* OPE *stops* at ~ 1 GeV, not sizably lower



(I.2) *broken* U- & V-spin symmetries

Does 'Lipkin rule' work for B decays? Hardly.

1st lesson: difference between U- & V-spin is 'fuzzy'
2nd lesson: we have to go *well beyond* 2-body FS



(II) Parameterization of the CKM Matrix

(II.1) Wolfenstein's parameterization

Wolfenstein's parameterization was very smart, easily usable, well-known & used all the time. The SM with 3 families of quarks describes the CKM matrix with 4 parameters: λ , A , ρ , η ;

expansion of $\lambda = 0.223$, while A , ρ , η are $O(1)$.

*Fitted values give $A \approx 0.82$ -- but $\eta \approx 0.35$, $\rho \approx 0.14$ not close to unity; -- thus not real control over *systematic* uncertainties.*

(II.2) Consistent parameterization

Consistent parameterization of CKM matrix with more precision [Y.H. Ahn, H-Y. Cheng, S. Oh (2011)] *through* $O(\lambda^6)$!

Pattern is not so obvious as before:

correlations between 4 triangles, not focus 'golden one'

-- maximal SM value for $S(B^0 \rightarrow \psi K_S) \sim 0.74$ for indirect CPV

-- SM value $S(B_s^0 \rightarrow \psi \phi) \sim 0.03 - 0.05$

-- basically zero CPV for *double Cabibbo suppressed (DCS)* decays

- *hunting region for ND!*

(III) *Intermezzo* – *Direct CP asymmetry* in $D^0 \rightarrow K^+K^-/\pi^+\pi^-$!

Now we are just entering a new era:

for the first time CP violation has been established in $\Delta C \neq 0$!
LHCb collaboration has shown its data from the run-1 & run-2 --
but an achievement:

$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+K^-) - A_{CP}(D^0 \rightarrow \pi^+\pi^-) = (-1.54 \pm 0.29) \times 10^{-3}$$

indirect CPV was found first in $\Delta S \neq 0 \neq \Delta B$, but not yet for $\Delta C \neq 0$;

SM 'paints' the 'landscape' for indirect CPV $\sim 10^{-4} - 10^{-3}$.

Here talk about SCS rates [below will discuss DCS ones]:

- $BR(D^0 \rightarrow K^+K^-) \sim 4 \times 10^{-3}$ vs. $BR(D^0 \rightarrow \pi^+\pi^-) \sim 1.4 \times 10^{-3}$;
- $BR(D^+ \rightarrow K^+K_S) \sim 2.8 \times 10^{-3}$ vs. $BR(D^+ \rightarrow \pi^+\pi^0/\eta/\eta') \sim (1.2/3.8/5.0) \times 10^{-3}$;
- $BR(D_S^+ \rightarrow \pi^+K_S) \sim 1.2 \times 10^{-3}$ vs. $BR(D_S^0 \rightarrow K^+\pi^0/\eta/\eta') \sim (0.6/1.8/1.8) \times 10^{-3}$.

three comments:

- first one probes direct CP asymmetries in 2-body FS ;
- present data show the impact of FSI ;
- it is crucial to probe 3- & 4-body FS; I will discuss next. *

[Suggestion: LHCb \rightarrow LHCbc]

(IV) CP asymmetries with $\Delta C \neq 0$

March 2019: LHCb Collaboration has established *direct CP asymmetry*

Next steps:

-- Indirect CP violation

-- *SCS* decays direct CP asymmetries:

$D^0 \rightarrow 2\pi^+2\pi^- / K^+K^-\pi^+\pi^-$; $D^+ \rightarrow \pi^+\pi^+\pi^- / \pi^+K^+K^-$; $D_s^+ \rightarrow K^+\pi^+\pi^- / K^+K^+K^-$

- Averaged CPV: SM ~ 0.001

- Regional CPV: large impact of re-scattering like ~ 0.01 or more

-- *DCS* decays direct CP asymmetries:

$D^0 \rightarrow K^+\pi^-\pi^+\pi^- / 2K^+K^-\pi^-$; $D^+ \rightarrow K^+\pi^+\pi^- / K^+K^+K^-$; $D_s^+ \rightarrow K^+K^+\pi^-$

- Averaged CPV: basically zero for the SM

- Regional CPV: hunting region for ND with no SM background when one has large data plus refined tools plus novel lessons about non-perturb. QCD

- Maybe the main challenge: confused by true CF transitions

(IV.1) CP asymmetries with singly Cabibbo suppressed (SCS) ones

$$\text{BR}(D^+ \rightarrow \pi^+\pi^+\pi^-) = (3.27 \pm 0.18) \times 10^{-3}, \quad \text{BR}(D^+ \rightarrow \pi^+K^+K^-) = (9.93 \pm 0.24) \times 10^{-3};$$

$$\text{BR}(D_s^+ \rightarrow K^+\pi^+\pi^-) = (6.6 \pm 0.4) \times 10^{-3}, \quad \text{BR}(D_s^+ \rightarrow K^+K^+K^-) = (0.218 \pm 0.021) \times 10^{-3};$$

$$\text{BR}(D^0 \rightarrow 2\pi^+2\pi^-) = (7.56 \pm 0.20) \times 10^{-3}, \quad \text{BR}(D^0 \rightarrow K^+K^-\pi^+\pi^-) = (2.47 \pm 0.11) \times 10^{-3};$$

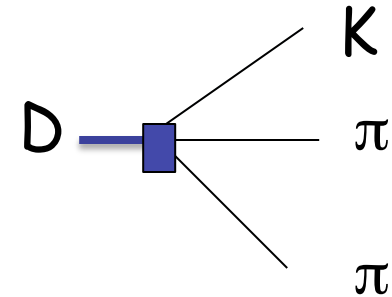
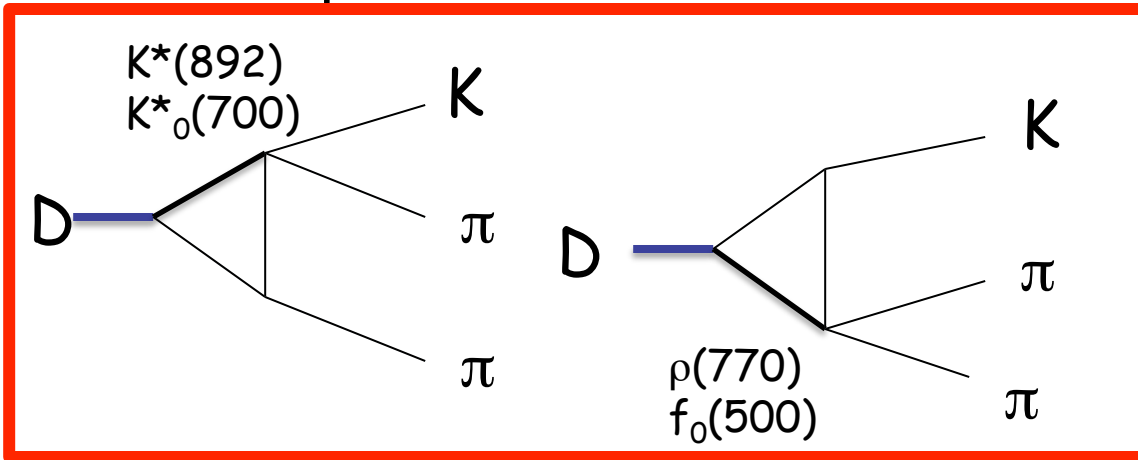
LHCb collaboration is probing CPV in many-body FS 'now' !

Remember:

do *not* ignore the impact of broad (scalar) resonances like $f_0(500)/\sigma$, $K^*_0(700)/\kappa$ etc. etc.

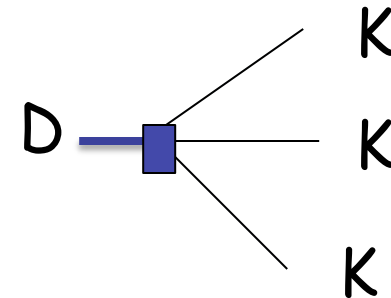
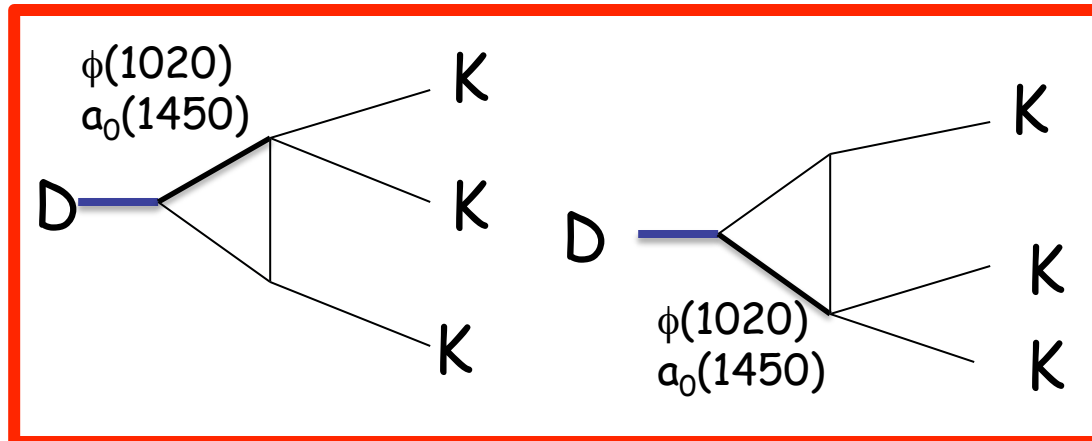
Furthermore, broad resonances in the region $\sim 0.5 - 1.5$ GeV cannot be described with Breit-Wigner parameterization.

The landscapes of hadrons



`effective' (?!) operator

Re-scattering is crucial to understand the underlying dynamics !



`effective' (?!) operator

need `judgment' about applying resonances, *threshold enhancements* etc. with tools like *dispersion relations*

(IV.1) CP asymmetries with singly Cabibbo suppressed (SCS) ones

Analyses with *dispersion relations*!

The idea came from theorists.

However, it pointed out one needs `good' data to analyze with a team of experimenters & theorists;

$$\text{amplitude } f(s) = (1/\pi) \int ds' \text{Im } f(s') / (s' - s - i\varepsilon)$$

$$\text{amplitude } f(s) = f(0) + (s/\pi) \int ds' \text{Im } f(s') / s'(s' - s - i\varepsilon)$$

Dispersion relations are above models, but below QFT;
both experimenters & theorists need judgments to apply –
i.e. dispersion relations are `Protestant', not `Catholic'.

(IV.2) CP asymmetries with doubly Cabibbo suppressed ones

PDG2018 for *DCS* decays:

$$\text{BR}(D^+ \rightarrow K^+K^+K^-)/\text{BR}(D^+ \rightarrow K^-\pi^+\pi^+) = (0.95 \pm 0.22) \times 10^{-3}$$

$$\text{BR}(D^+ \rightarrow K^+\pi^+\pi^-)/\text{BR}(D^+ \rightarrow K^-\pi^+\pi^+) = (5.77 \pm 0.22) \times 10^{-3}$$

$$\text{BR}(D_s^+ \rightarrow K^+\pi^-K^+)/\text{BR}(D_s^+ \rightarrow K^-K^+\pi^+) = (2.33 \pm 0.23) \times 10^{-3}$$

LHCb for *DCS* decays, [arXiv:1810.03138 \[hep-ex\]](https://arxiv.org/abs/1810.03138) about 8 TeV (not run-2)
published in JHEP 03 (2019) 176

$$\text{BR}(D^+ \rightarrow K^+K^+K^-)/\text{BR}(D^+ \rightarrow K^-\pi^+\pi^+) = (0.6541 \pm 0.0025 \pm 0.0042) \times 10^{-3}$$

$$\text{BR}(D^+ \rightarrow K^+\pi^+\pi^-)/\text{BR}(D^+ \rightarrow K^-\pi^+\pi^+) = (5.231 \pm 0.009 \pm 0.023) \times 10^{-3}$$

$$\text{BR}(D_s^+ \rightarrow K^+\pi^-K^+)/\text{BR}(D_s^+ \rightarrow K^-K^+\pi^+) = (2.372 \pm 0.024 \pm 0.025) \times 10^{-3}$$

what a progress in this experiment !

(IV.2) CP asymmetries with doubly Cabibbo suppressed ones

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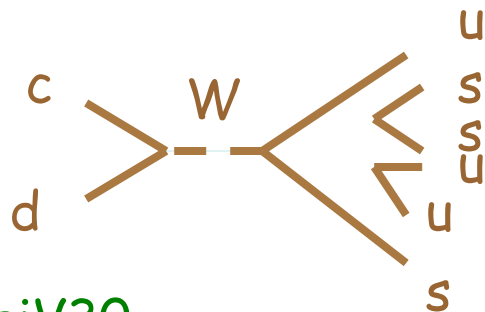
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what a progress in this experiment!

However, look at Feynman diagrams in Figs. 1(a), 1(b) & 1(c) on page 1 of this article:

-- Figs. 1(b) & 1(c) are okay, but incomplete.

-- however, my main problem comes from Fig. 1(a):

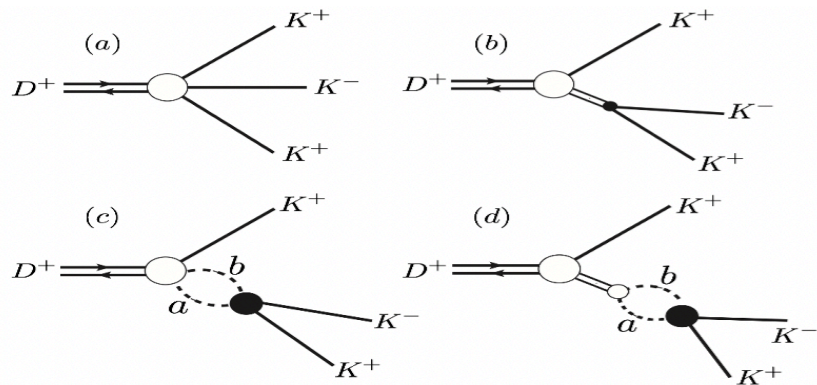


-- `WA' no chance to be the leading source !
-- `WA' \leftrightarrow re-scattering (FSI) is *misleading* !

Connections of HEP & Hadrodynamics

One example in [arXiv:1902.05884v3 \[hep-ex\]](https://arxiv.org/abs/1902.05884v3) published in JHEP 04 (2019) 063

The world of hadrons



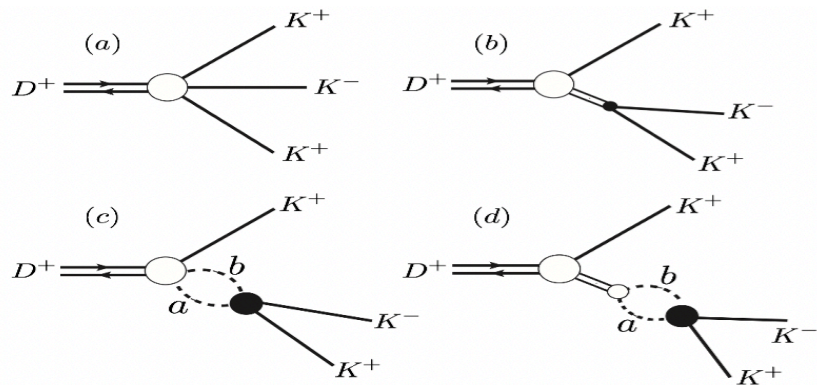
Nice 'painting' !

Figure 10. Diagrams contributing to the amplitude T for the decay $D^+ \rightarrow K^- K^+ K^+$: (a) the final state kaons are produced directly from the weak vertex; (b) a bare resonance is produced directly from the weak vertex; (c) particles produced at the weak vertex undergo final state interactions; (d) final state interactions endow finite widths to the resonances. The full circle represents the unitary $ab \rightarrow K^+ K^-$ scattering amplitude with angular momentum J and isospin I , and $ab = KK, \pi\pi, \eta\pi$ and $\eta\eta$.

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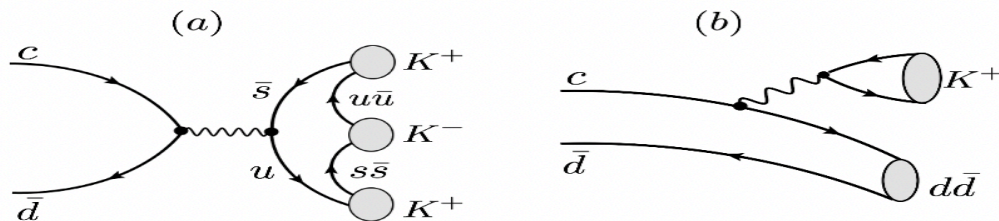
The world of hadrons



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The world of quarks & gluons



'WA' \leftrightarrow re-scattering (FSI)
is *misleading*!

Figure 9. Diagrams representing the two quark-level topologies for the $D^+ \rightarrow K^- K^+ K^+$ decay. In the Triple-M [3], diagram (a) is assumed to be the dominant mechanism of the decay, whereas diagram (b) is suppressed since the production of a $K^+ K^-$ pair from a $d\bar{d}$ pair requires rescattering.

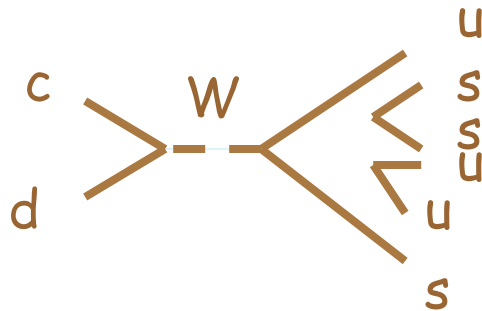
(IV.2) $\Delta C \neq 0$ with 3-body FS

LHCb for DCS decays, [arXiv:1902.05884v3\[hep-ex\]](https://arxiv.org/abs/1902.05884v3) about 8 TeV (not run-2)
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`Dalitz plot analysis of the $D^+ \rightarrow K^- K^+ K^+$ decay'

p. 12, `Figure 9 (a) is assumed to be the dominant mechanism ...'

again



- `WA' no chance to be the leading source !
- `WA' \leftrightarrow re-scattering (FSI) is *misleading* !
- *cannot ignore $D^+ \rightarrow K^+ \pi^+ \pi^-$!*

(IV.2) $\Delta C \neq 0$ with 3-body FS

LHCb for DCS decays, [arXiv:1810.03138 \[hep-ex\]](https://arxiv.org/abs/1810.03138) from 8 TeV;

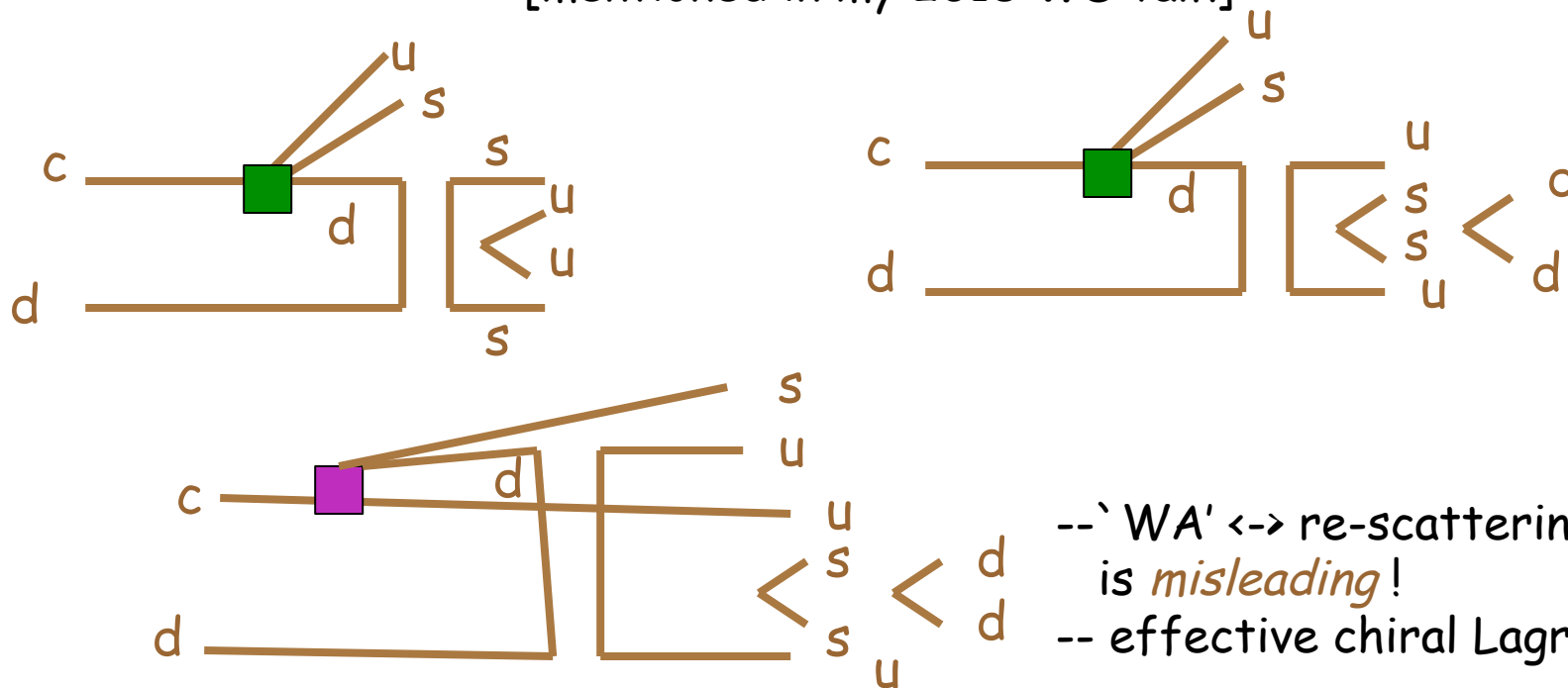
[arXiv:1902.05884v3 \[hep-ex\]](https://arxiv.org/abs/1902.05884v3) from 8 TeV:

$$\text{BR}(D^+ \rightarrow K^+K^+K^-) = (0.587 \pm 0.002 \pm 0.004 \pm 0.018) \times 10^{-4}$$

$$\text{BR}(D^+ \rightarrow K^+\pi^+\pi^-) = (4.70 \pm 0.01 \pm 0.02 \pm 0.15) \times 10^{-4}$$

$$[\text{BR}(D_s^+ \rightarrow K^+\pi^-K^+) = (1.293 \pm 0.013 \pm 0.014 \pm 0.040) \times 10^{-4}]$$

My 'painting' of the amplitudes for $D^+ \rightarrow K^+K^+K^-/K^+\pi^+\pi^-$
[mentioned in my 2018 WS talk]



*

-- 'WA' \leftrightarrow re-scattering (FSI)
is *misleading*!
-- effective chiral Lagrangian! ?

(IV.3) Lifetimes & SL widths of charm baryons

- PDG2018: $\tau(\Omega_c^0) < \tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Xi_c^+)$
in previous century one had expected this pattern based on HQE
in a *simple* qualitative way.
- PDG2019: $\tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Omega_c^0) < \tau(\Xi_c^+)$
the 'landscape' has changed:
while the *pattern* of $\tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Xi_c^+)$ is the same,
it has changed sizably for $\tau(\Omega_c^0)$;
predictions depend on quark *models*, not QFT.
Compare $\Lambda_c^+ = [c(ud)_{j=0}]$ vs. $\Omega_c^0 = [c(ss)_{j=1}]$
- The goal is to measure 'soon' SL widths of $\Xi_c^0, \Xi_c^+, \Omega_c^0$.
They are connected based on *non-perturb.* QCD.

(IV.4) CP asymmetries in weak decays of charm *baryons*

- When one goes for CPV, one cannot stop at 2-body FS: crucial to probe 3- & 4-body FS including regional CPV.
- On first & second steps one goes after SCS ones where the SM predicts small CPV on the order of $O(10^{-3})$.
- For DCS decays the SM predicts basically zero; hunting regions for ND.
- One has to probe CPV in charm baryons with Dalitz plots
 - SCS: $\Lambda_c^+ \rightarrow p \pi^+ \pi^- / p K^+ K^-$
 - DCS: $\Lambda_c^+ \rightarrow p K^+ \pi^-$
 - tiny rates are not the only challenge:
compare DCS $\Lambda_c^+ \rightarrow p K^+ \pi^-$ vs. CF $\Lambda_c^+ \rightarrow p K^- \pi^+$

(V) Present and future lessons of $\Delta S \neq 0$

-- We know that CP asymmetries has been found & established in the transitions of neutral strange mesons:

- *indirect* CPV in $K^0 \rightarrow 2\pi$ with the scale $\sim 2.23 \times 10^{-3}$ data

- *direct* CPV in $K^0 \rightarrow 2\pi$ with $\left\{ \begin{array}{l} \sim 3.6 \times 10^{-6} \text{ data} \\ < 2.2 \times 10^{-6} \text{ SM ?!} \\ \sim 1.1 \times 10^{-6} \text{ "Buras team" ["LQCD"]} \end{array} \right.$



- amazing established data & analyses

- it *might be beyond* the SM: "Buras team" ["LQCD"].

(V) Present and future lessons of $\Delta S \neq 0$

- We know that CP asymmetries has been found & established in the transitions of neutral strange mesons:
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 - amazing established **data & analyses**
 - it *might be beyond* the SM: "Buras team" ["LQCD"].
- Next step for direct CP asymmetry in strange **baryons**
 - $e^+e^- \rightarrow J/\psi \rightarrow \Lambda \Lambda \rightarrow [p \pi^+][p \pi^-]$
 - maybe BESIII could probe CPV by 2019 with below 10^{-3}
 - duality violation enhanced close to thresholds ! ?

It is a novel `road`:

Giovanni Punzi: LHCb can do better with *run-3/4* below 10^{-4} !

$$J/\psi \rightarrow \Lambda \Lambda \rightarrow [p \pi^+][p \pi^-]$$

-- Some details:

$$J/\psi \rightarrow Y \bar{Y} \rightarrow [X \pi] [\bar{X} \pi] \text{ with a } \textit{dedicated trigger}$$

- Measure T-odd moments

$$\alpha_Y^X = \langle \sigma_Y \cdot (\sigma_X \times \pi_X) \rangle, \quad \alpha_{\bar{Y}}^X = \langle \sigma_{\bar{Y}} \cdot (\sigma_X \times \pi_X) \rangle,$$

based on CPT invariance

probe direct CP asymmetry $\langle A_{CP}^X \rangle = (\alpha_Y^X + \alpha_{\bar{Y}}^X) / (\alpha_Y^X - \alpha_{\bar{Y}}^X)$
without polarized Y & \bar{Y} due to very narrow resonance J/ψ !

"Imagination created reality" - Richard Wagner

Epilogue for the future: *Collaboration* of HEP & Hadrodynamics

Need to connect the worlds of quarks & gluons with hadrons !

Back to the history outside



San Francesco, Arezzo (Italy)

Epilogue for the future: *Collaboration* of HEP & Hadrodynamics

Need to connect the worlds of quarks & gluons with hadrons !

Back to the history outside -- & inside



San Francesco, Arezzo (Italy)



'The Dream of Constantine'
by Piero della Francesca,
painter of Early Renaissance,
mathematician/geometer

'dreaming in more dimensions'
Kolya Uraltsev & I had looked at this
painting *in person* & realized that it is
symbol of collaboration.

Final steps need `judgment' about applying resonances, threshold enhancements etc. with dispersion relations

- 1st step: models;
- 2nd step: model-independent
- 3rd step: **best fitted analyses** often do *not* give us the best information about the **underlying dynamics - correlations & judgments**

Future lessons for LHCb/Belle II

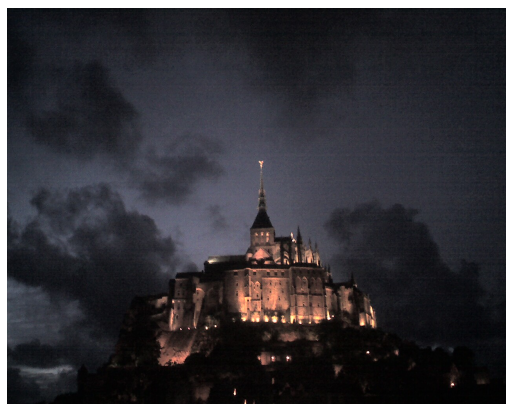
Yes, the data are the referees, but in the end - **theorists** should **not** be the **slaves of the data** !

One example:

IIB&collab.: bragging rights? It goes beyond -- the power of HQE !

$$\tau(\Lambda_b)/\tau(B_d) > 0.9 \quad 1993; \quad \sim 0.94 \quad \& \quad > 0.88 \quad 1996$$

Data: $\tau(\Lambda_b)/\tau(B_d) = 0.77 \pm 0.05$ 1996; 0.81 ± 0.05 2004; 0.94 ± 0.09 2005



I had produced this picture - correlations & judgments are not always obvious!

Short comments in one slide just before the Summary,
namely about $V(qb)$ about exclusive vs. inclusive ones:

$V(cb): \quad B \rightarrow l \nu D/D^* \quad \text{vs.} \quad B \rightarrow l \nu X_c$

- (a) difference $\sim 2 \sigma$

- (b) *data landscape* is not clear about FS: $D, D^*, D^{**}, D^{***}, \dots$

$V(ub): \quad B \rightarrow l \nu \pi/\rho \quad \text{vs.} \quad B \rightarrow l \nu X_u;$

(a) difference $\sim 3 - 4 \sigma;$

(b) *probe* $B \rightarrow l \nu f_0(500)/\sigma \rightarrow l \nu 2\pi$ as a *bridge*
between exclusive & inclusive ones using *dispersion relations*

(c) X_u vs. only π 's ?

(d) *probe* $B^- \rightarrow l^- \nu K^+ K^-$ & $B^0 \rightarrow l^- \nu K^+ K^- \pi^+$ to help to solve this problem

(e) in general "duality" is *not local* close to thresholds

(VI) Summary: Impact of *non*-perturbative QCD on *CP Violation*

about fundamental dynamics:

- (a) *Two-body* FS do not give `royal insights' in general;
- (b) diagrams give no `royal ones';
- (c) Wolfenstein's parameterization of the CKM matrix is well-known & used all the time, but it is *not* `royal ones' for *this* century;
- (d) even more: pole masses give no `royal insights' !

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- (d) even more: pole masses give no `royal insights' !

"Goals for *flavor dynamics* of quarks":

- ☞ Probing *CP* asymmetries in 3- & 4-body FS of charm & beauty hadrons is crucial to find both existence & features of ND.
[At least it shows the impact of non-perturbative QCD.]
- ☞ Theorists do not like waiting: *results from run-2* !
- ☞ Waiting for run-3 & run-4: that is life.
- ☞ Worlds of quarks & gluons and for hadrons are connected, but often they are not obvious (`*duality*' is more subtle than just looking at diagrams)!

Short summary:

-- `We' need more data, but that is not enough -

thinking & judgments about the impact of *long distance* QCD!

[-- HQET [with $\mu = 0$] \neq HQE [$\mu \sim 1 \text{ GeV}$]

HQET: `observables' = perturb. forces + non-perturb. forces

HQE: "observables" = "long-distance" forces + "short-distance" ones]

-- best fitted analyses do not give the best information about the underlying dynamics

-- CP asymmetries in 3- & 4-FS is crucial to make progress about ND

$$\Delta\gamma(a) = |T(P \rightarrow a)|^2 - |\bar{T}(P \rightarrow a)|^2 = 4 \sum_{aj \neq a} T_{aj,a}^{\text{resc}} \text{Im} T_a^* T_{aj}$$

-- `Challenges between Cultures' of HEP vs. Hadrodynamics
like "current quarks" vs. `pole masses of hadrons'

-- My new book will be published in the
Winter 2019/20:

dedicated to L. Okun

