

Introduction to Silicon Detectors

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Outline

1. Introduction
 - Types of silicon detectors
 - Interaction of particles with silicon
2. Properties of silicon
3. Silicon detectors for charged particle detection
4. Silicon detectors for photon detection
5. Summary

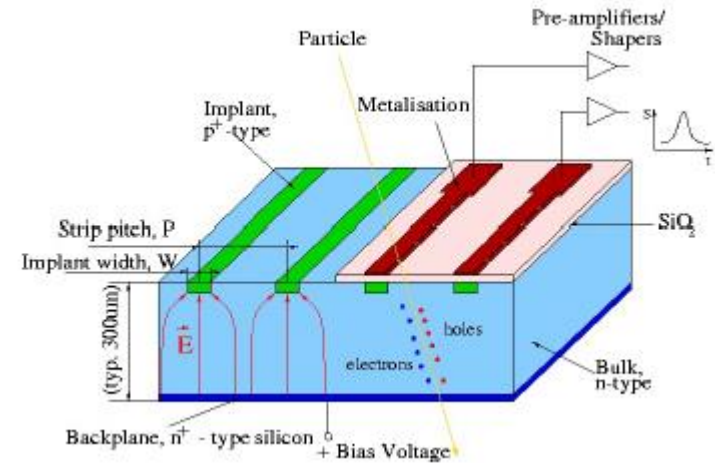
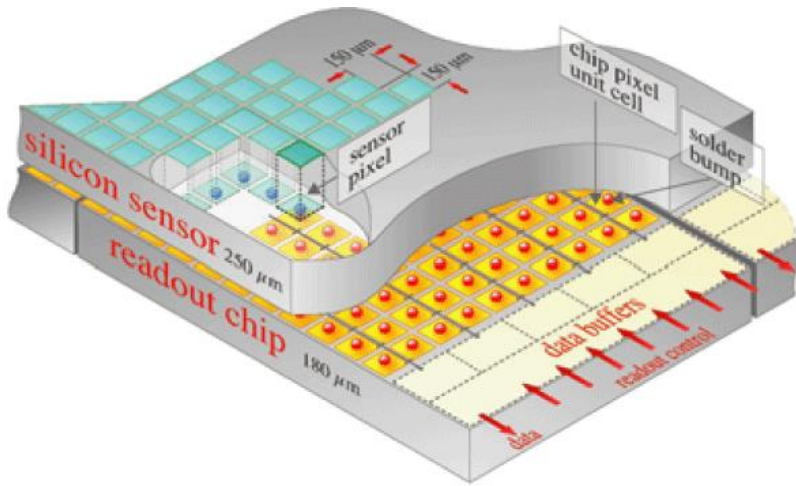
1. Introduction

Types of Silicon Detectors

Pixel sensor for CMS

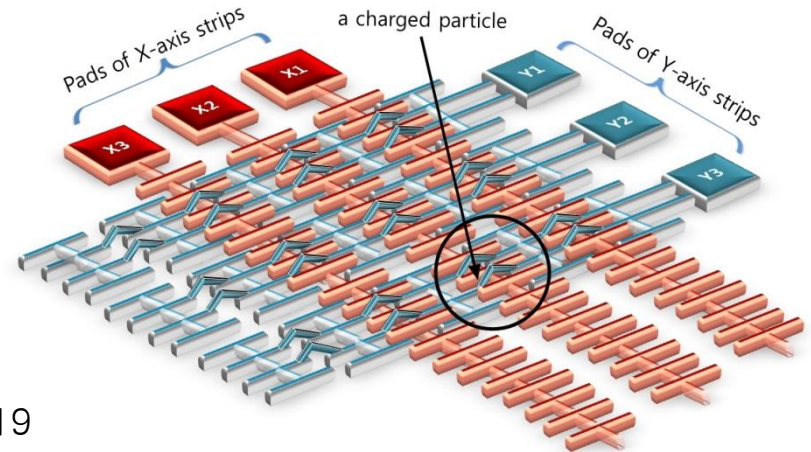
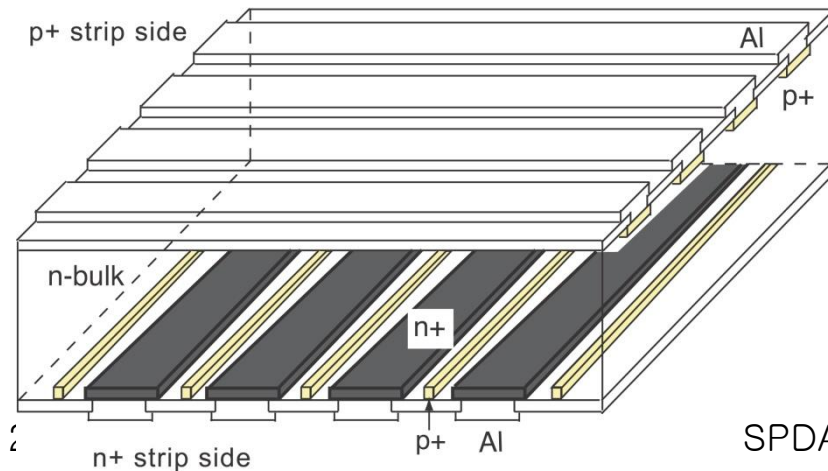
http://hep.fi.infn.it/CMS/sensors/Silicon_Detector.gif

Single-side strip sensor



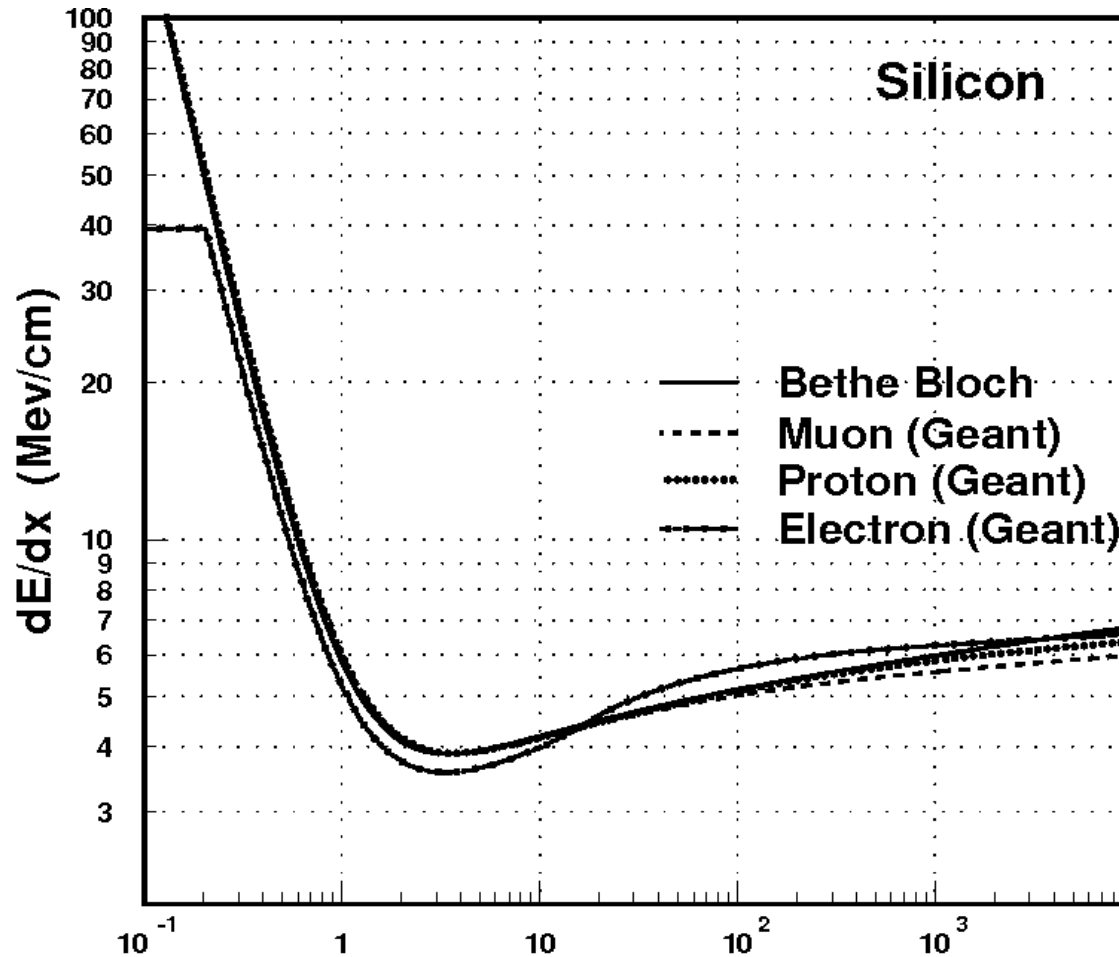
Double-side strip sensor

Strip-pixel sensor



Interaction of charged particles with silicon

By S. Banerjee & A. Caner



Energy loss by ionization

z : charge of incident particle

Bethe equation

$$\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

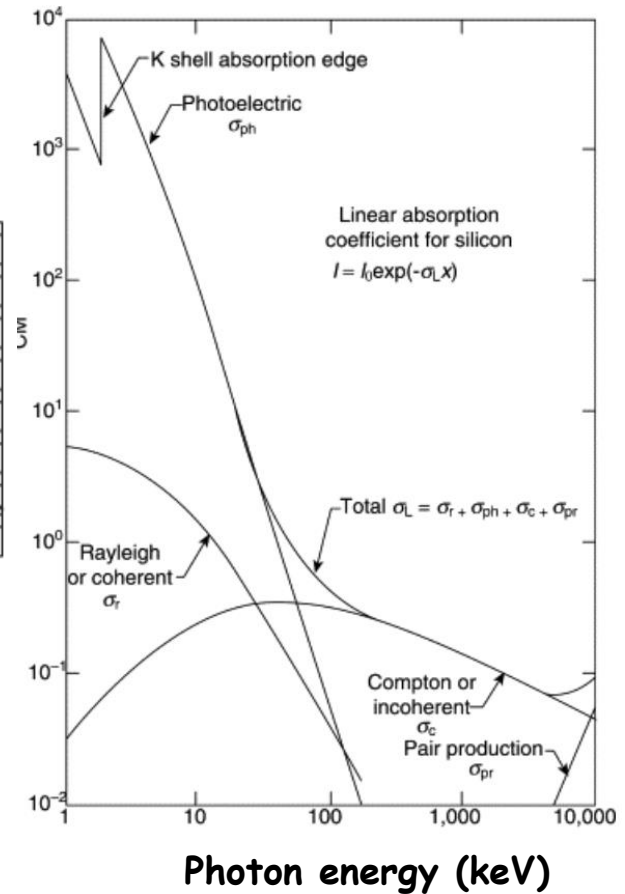
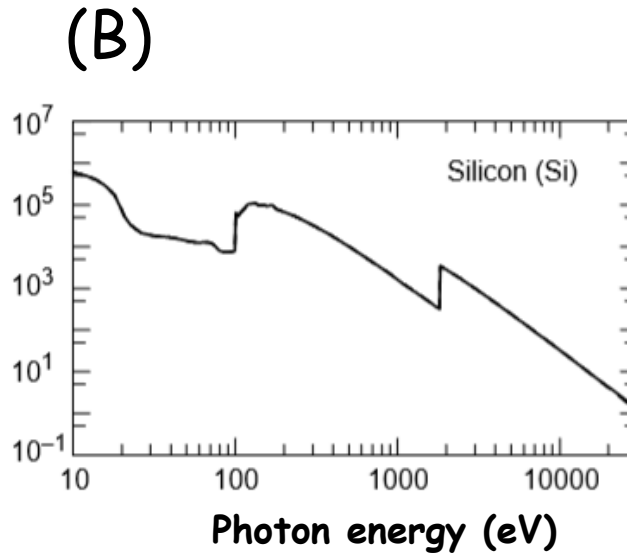
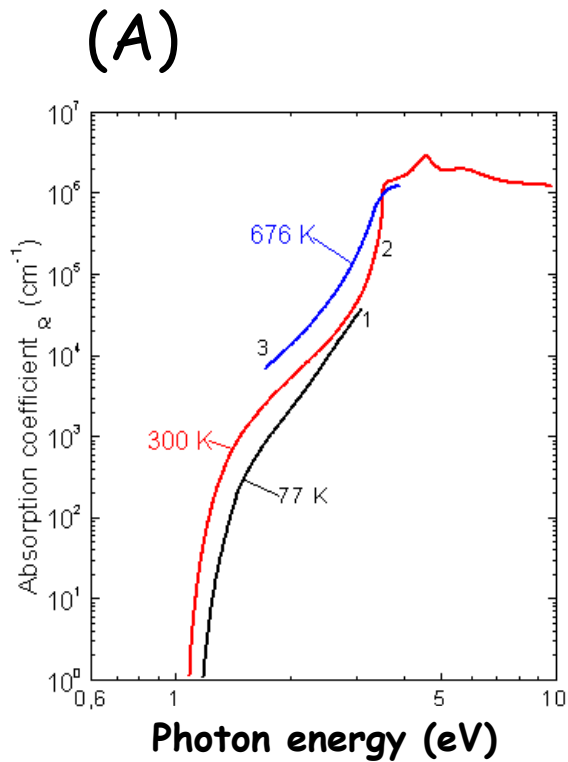
$$\left\langle \frac{dE}{dx} \right\rangle \propto z^2$$

$\left\langle \frac{dE}{dx} \right\rangle \approx 40 \text{ keV} / 100 \text{ } \mu\text{m}$ in Si for minimum ionizing particles

3.6 eV required for producing a pair of e-h in Si
 $\approx 10,000$ e-h pairs / 100 μm expected in Si

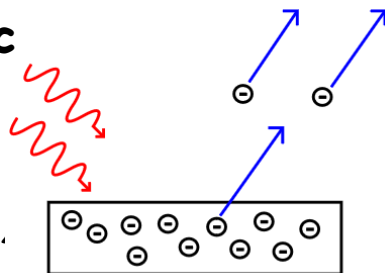
Interaction of photons with silicon

(C)



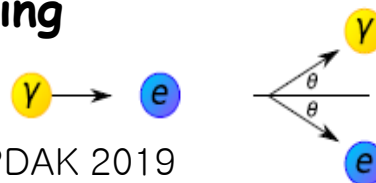
Photoelectric effect

2019-01-1

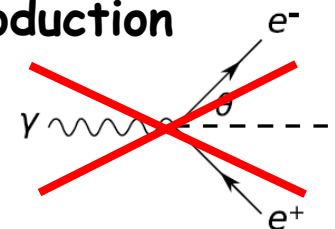


Compton scattering

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Pair production



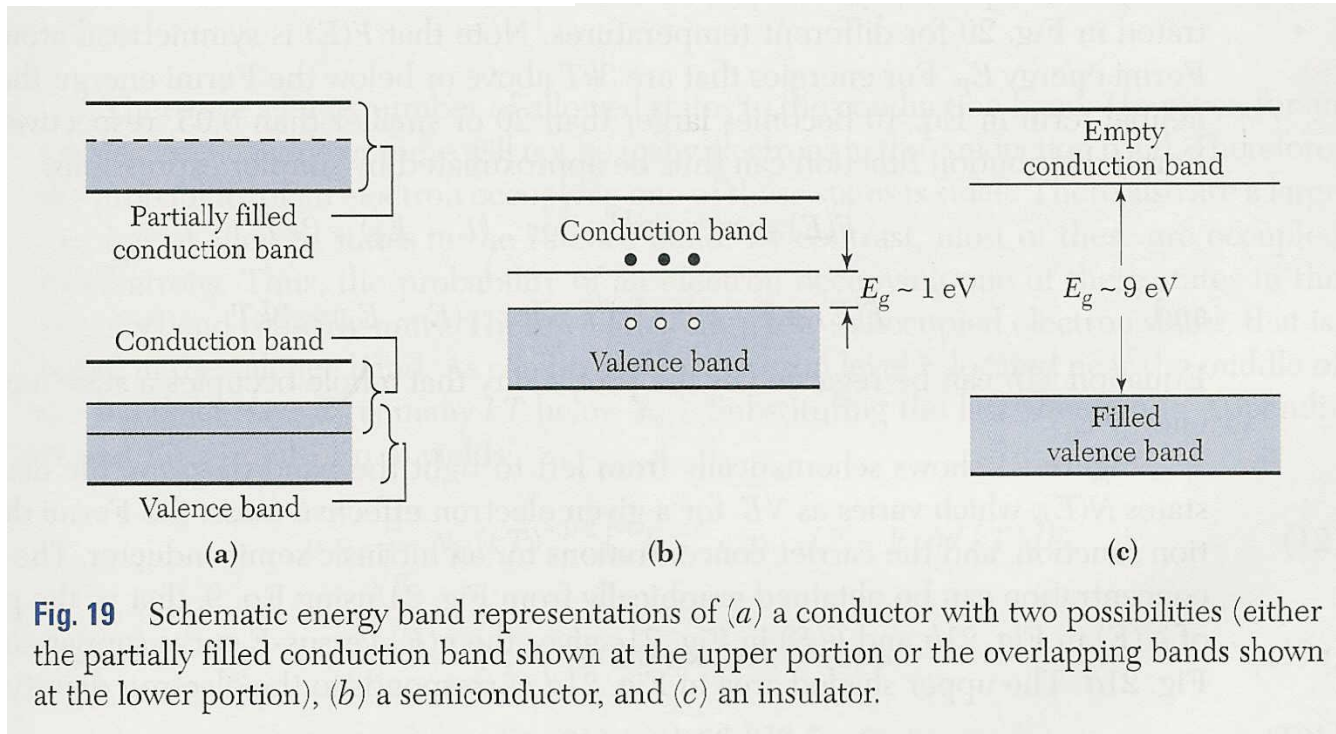
References for the plots in Page 6

- A. Sze, S. M., *Physics of Semiconductor Devices*, John Wiley and Sons, N.Y., 1981. Jellison, Jr., G. E. and F. A. Modine, *Appl. Phys. Lett*- 41, 2 (1982) 180-182.
- B. X-RAY DATA BOOKLET, Lawrence Berkeley National Laboratory
- C. Durini (Editor), "High Performance Silicon Imaging: Fundamentals and Applications of CMOS and CCD Sensors", Woodhead Publishing, 2014 Particularly: Chapter 10 (p286) by R. Turchetta, STFC, UK

2. Properties of silicon

Band & bandgap

Isolated atoms brought together to form lattice \rightarrow discrete atomic levels shift to form energy bands



From 'Semiconductor Devices
Physics and Technology Second Edition'
by S.M. Sze

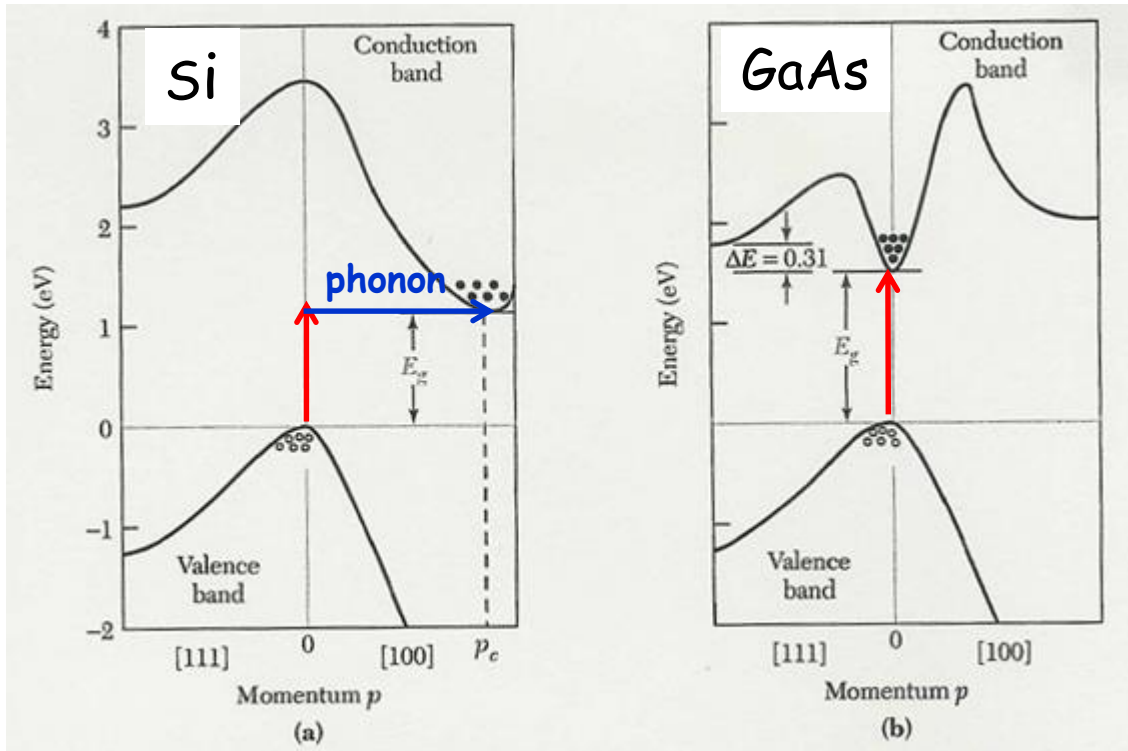
E_g : band gap (1.12 eV for Si)
Note: $kT \sim 0.026 \text{ eV}$ at room temp.

Indirect vs Direct Bandgap Semiconductors

From 'Semiconductor Devices
Physics and Technology
Second Edition'
by S.M. Sze

Indirect bandgap

Direct bandgap



$$\text{Excitation/De-excitation} = E_g + E_{\text{phonon}}$$

$$\text{Excitation/De-excitation} = E_g$$

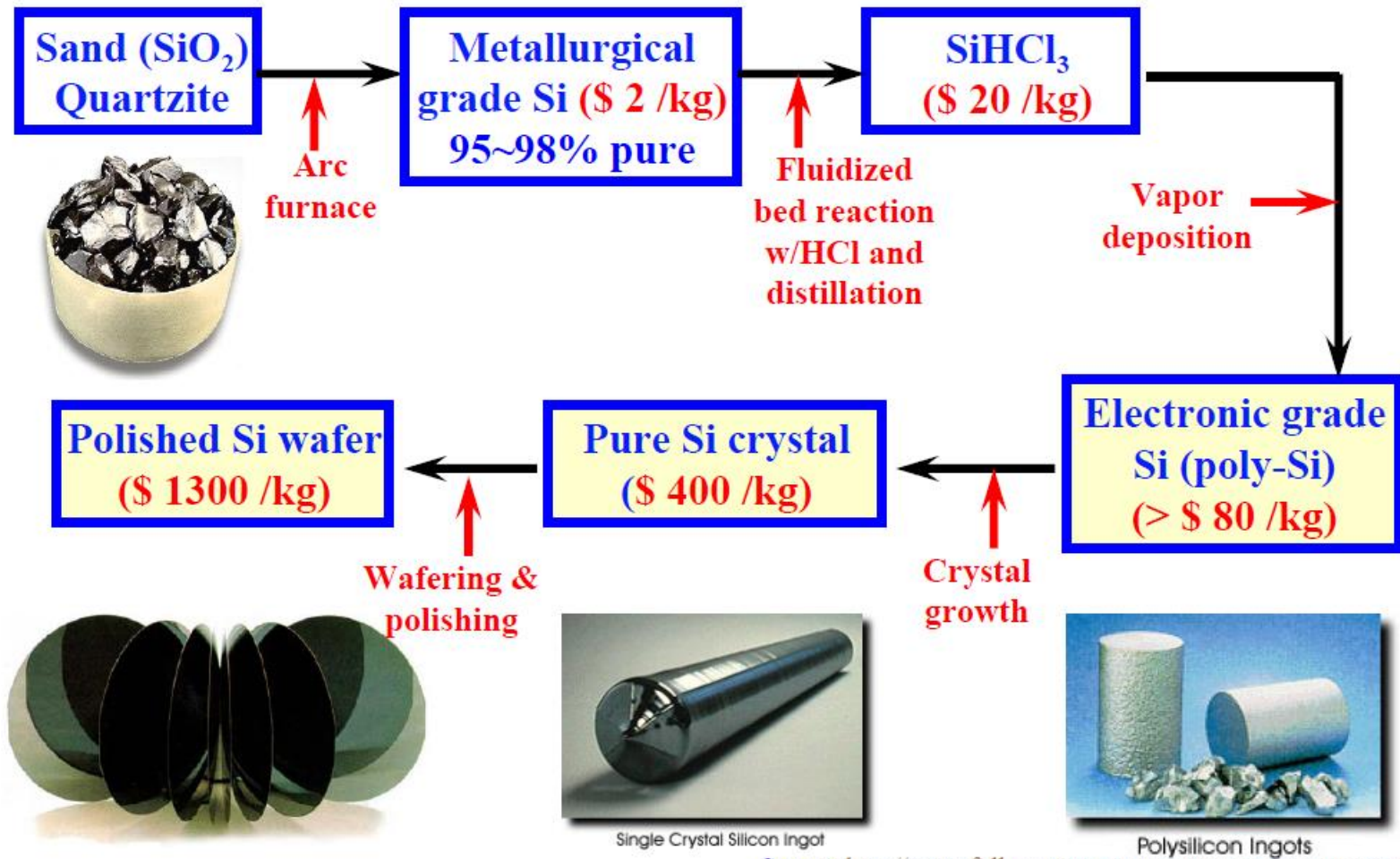
Why Silicon?

- abundant --> cheap
- Lighter
- SiO₂ layer
 - Naturally or inexpensively formed
 - chemically and mechanically very stable
 - effectively passivates the surface states of the underlying silicon
 - forms an effective diffusion barrier for the commonly used dopant species
 - easily preferentially etched from the silicon, and vice versa, with high selectivity
 - By contrast, GeO₂ is a chemically unstable, poor electrical insulator that is 33 times more soluble in water than SiO₂, making it less suited to the photolithographic and wet chemical processes used to fabricate integrated circuits.

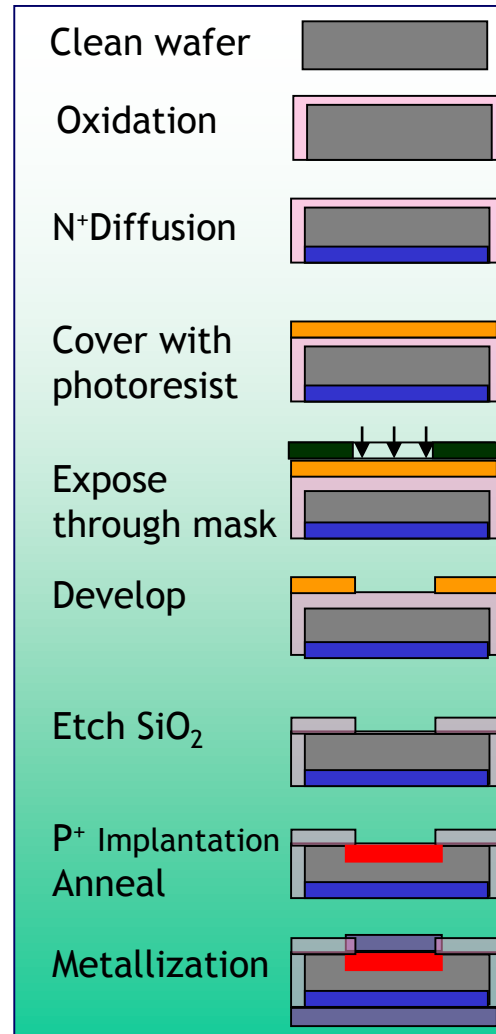
III	IV	V
5 B	6 C	
13 Al	14 Si	15 P
31 Ga	32 Ge	33 As
49 In	50 Sn	51 Sb

Acceptors Semiconductors Donors

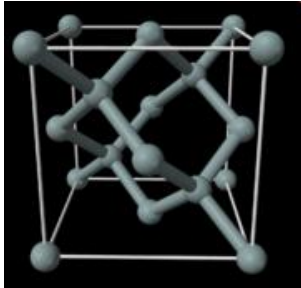
Sand to silicon wafer



Recipe for fabrication process

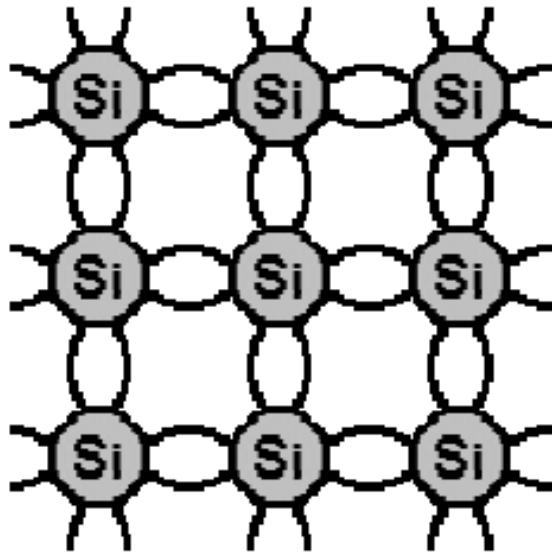


Intrinsic Si semiconductor

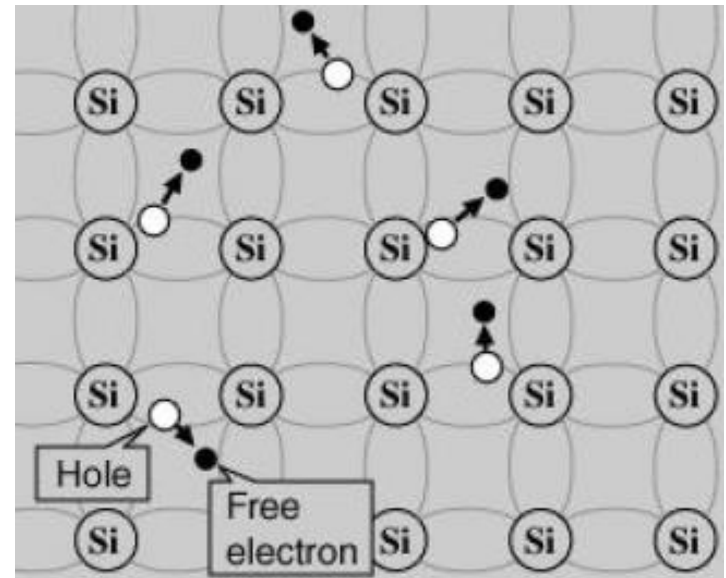


The crystalline structure is *Diamond Cubic* (FCC). Bare wafers of $\langle 100 \rangle$ or $\langle 111 \rangle$ crystals are popular ones used for silicon detector fabrications.

low T : electrons bound in lattice



higher T : free electrons & holes



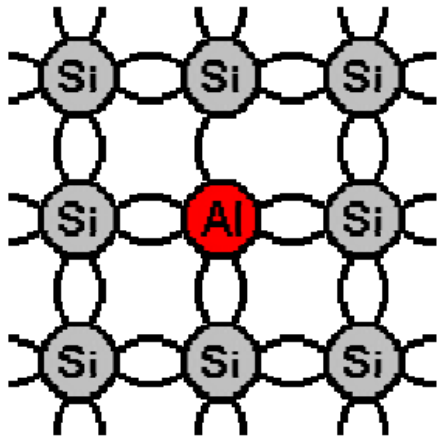
Impurities

- Intrinsic semiconductor = pure, no impurities.
- Extrinsic semiconductor = impurities added.
- Some impurities always present.
- Turns out to be extremely useful to add impurities to control the properties of the semiconductor.

Jargons

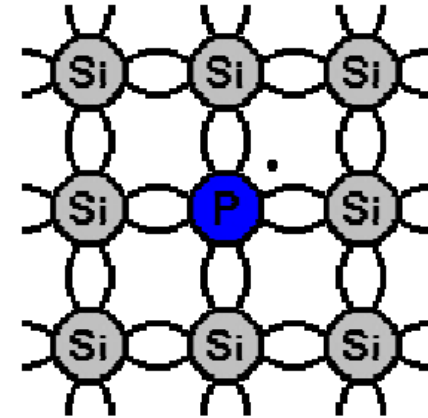
- The heavily-doped pieces are called n^+ -type or p^+ -type; the lightly-doped pieces, simply n-type or p-type.

Doping: acceptors & donors



III	IV	V
5 B	6 C	
13 Al	14 Si	15 P
31 Ga	32 Ge	33 As
49 In	50 Sn	51 Sb

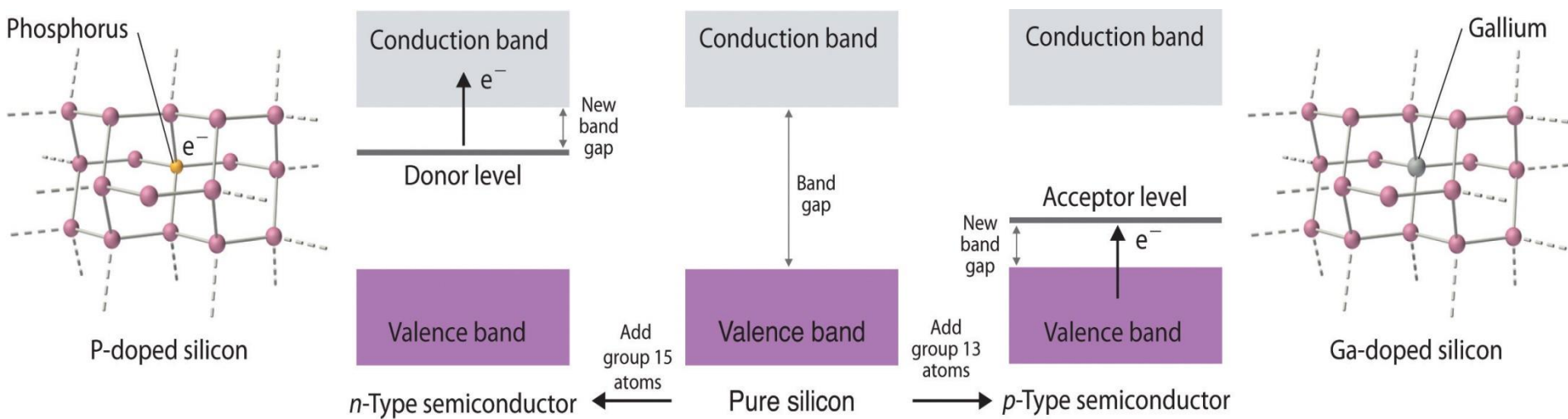
Acceptors Semiconductors Donors



- Al or B impurities.
- 3 e^- in outer shell
- 3 e^- for bonds, one hole left-over (free)
- Acceptor impurity
- P-type silicon

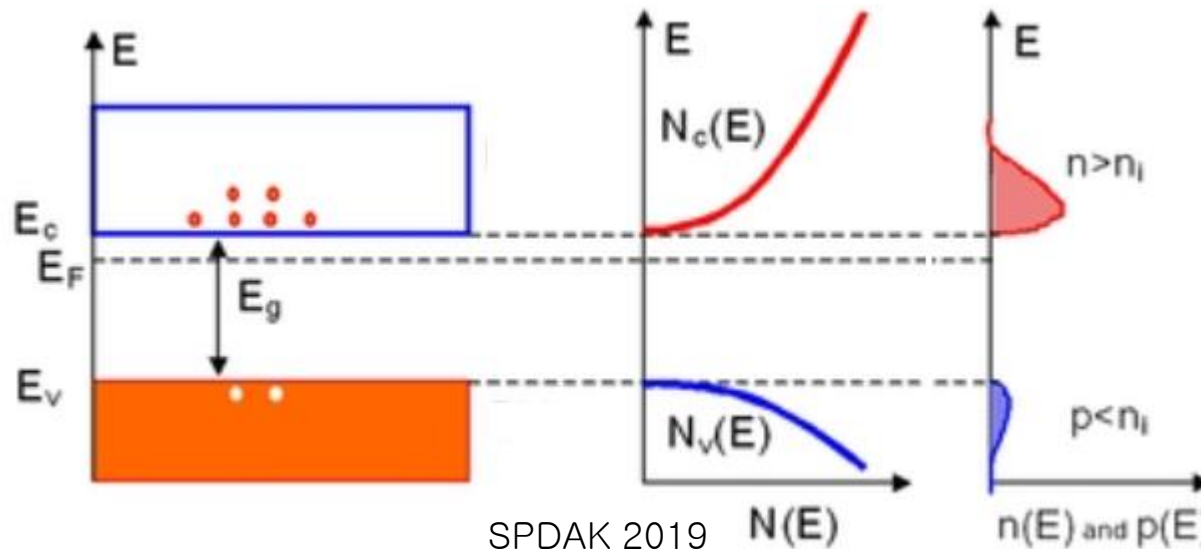
- P or As impurities.
- 5 e^- in outer shell.
- 4 e^- for bonds, one e^- left-over (free).
- Donor impurity
 - (donates e^-)
- N-type silicon

Effect of doping



(a) Doping with a group 15 element

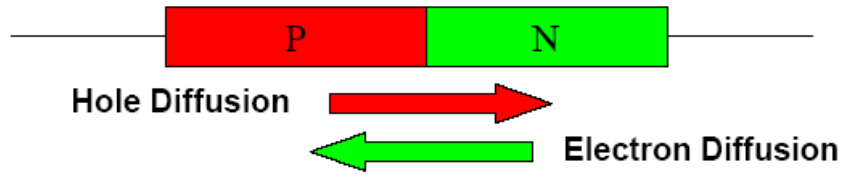
(b) Doping with a group 13 element



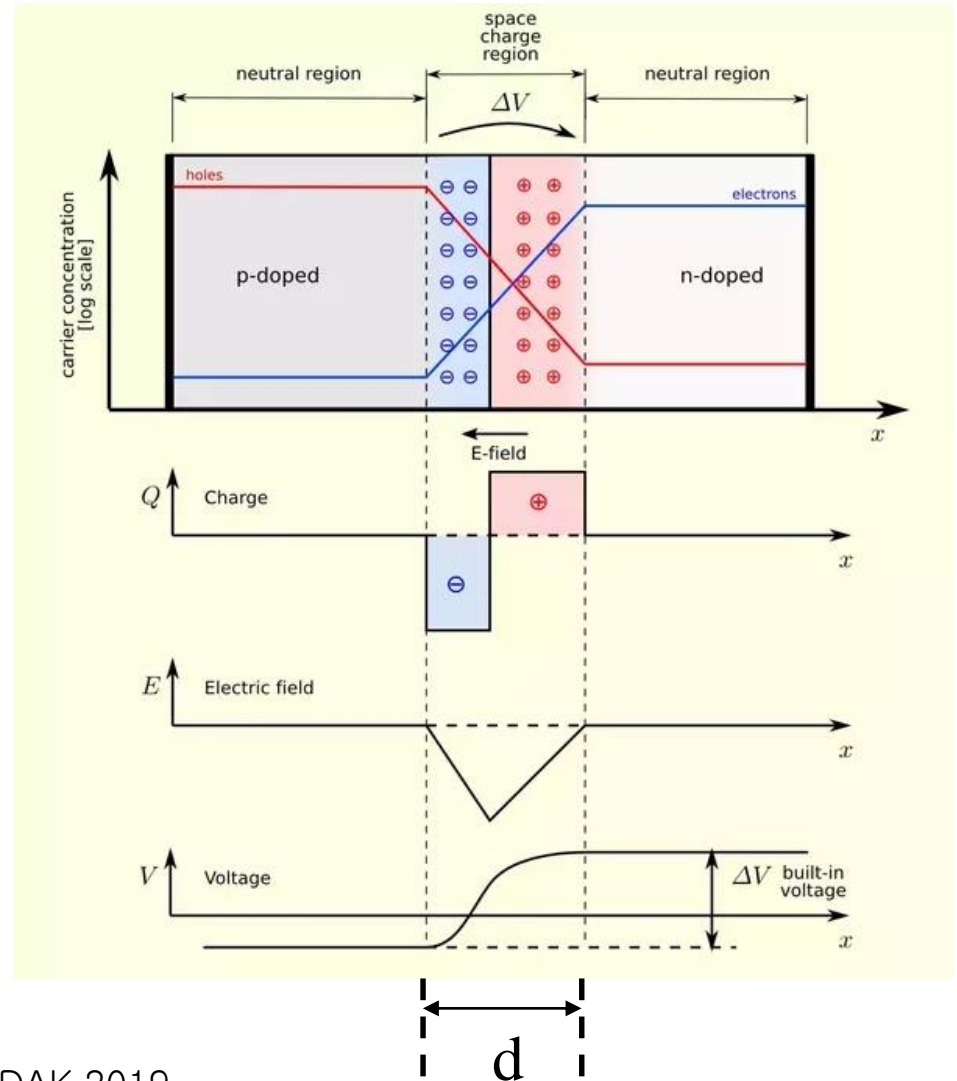
3. Silicon detectors for charged particle detection

p-n junction (fundamental structure)

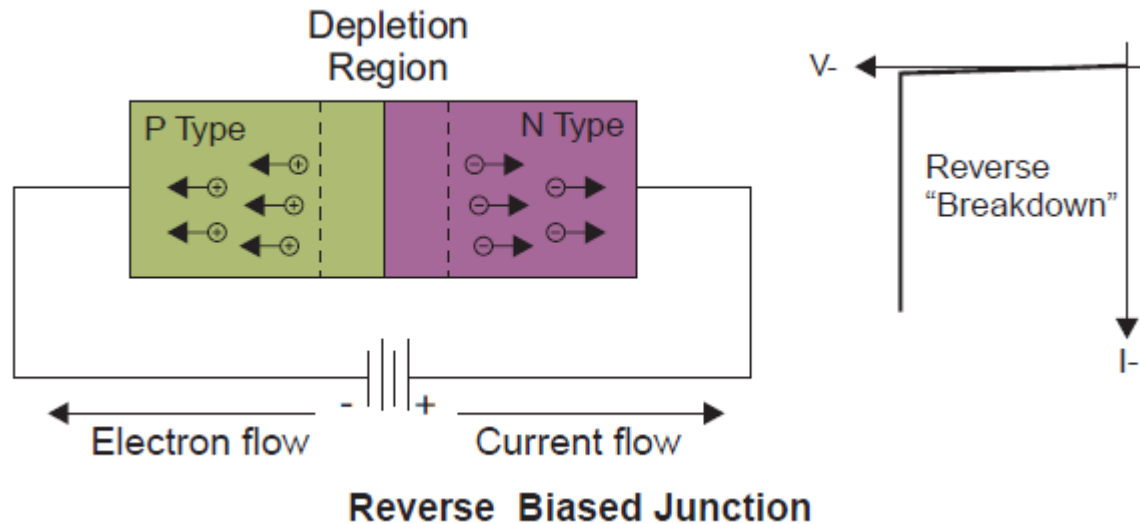
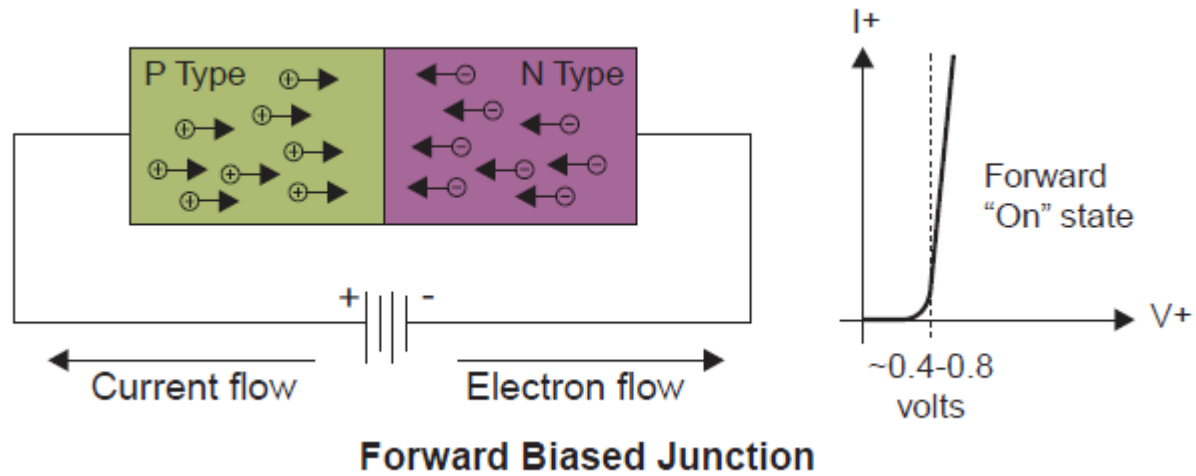
Bring p-type and n-type into contact:



The depletion region d is a region with no charge carriers (with no free charges).



p-n junction



Depletion depth

$$d = \sqrt{\frac{2\epsilon}{e} \frac{N_A + N_D}{N_A N_D} (V_{bi} + V)}$$

V_{bi} : potential difference due to barrier field

$$d = \sqrt{\frac{2\epsilon(V_{bi} + V)}{eN_B}}$$

In many cases, $N_A \gg N_D$ or $N_D \gg N_A$
 N_B is the smallest of N_D and N_A

$$d = \sqrt{2\epsilon\mu\rho(V_{bi} + V)}$$

An exercise :
intrinsic Si at 300K
 $\rho = 3.3 \times 10^5 \Omega \text{ cm}$
 $V \sim 110 \text{ V}$
 $d \sim 300 \mu\text{m}$

$$d = 0.5 \mu\text{m} \sqrt{\rho(V_{bi} + V)} \quad (\text{n-type})$$

$$d = 0.3 \mu\text{m} \sqrt{\rho(V_{bi} + V)} \quad (\text{p-type})$$

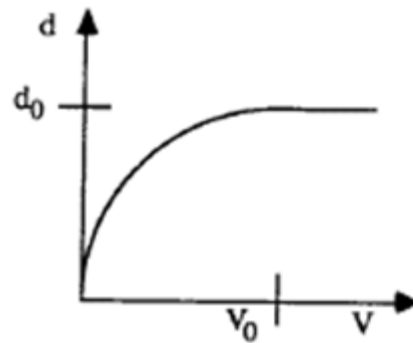
(V in Volts and ρ in Ωcm) for Si

p-n junction reverse bias characteristics

d = depletion layer depth

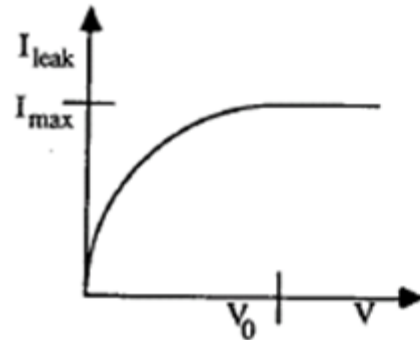
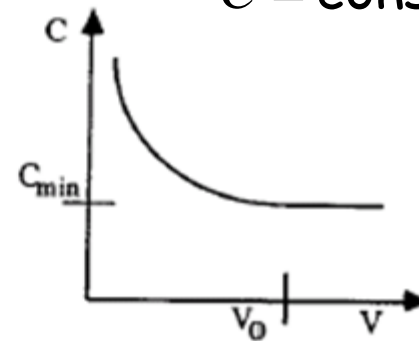
$$d \propto \sqrt{V} \text{ for } V < V_0$$

$$d = d_0 \text{ for } V > V_0$$



$$C \propto 1/\sqrt{V} \text{ for } V < V_0$$

$$C = \text{const. for } V > V_0$$



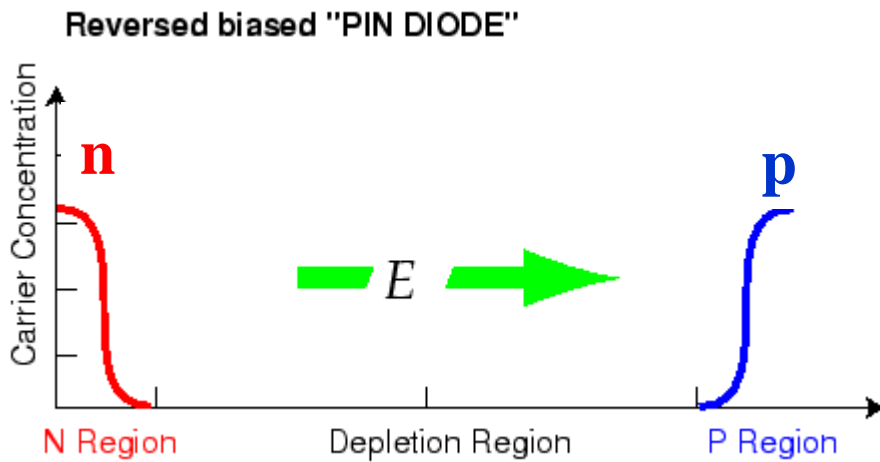
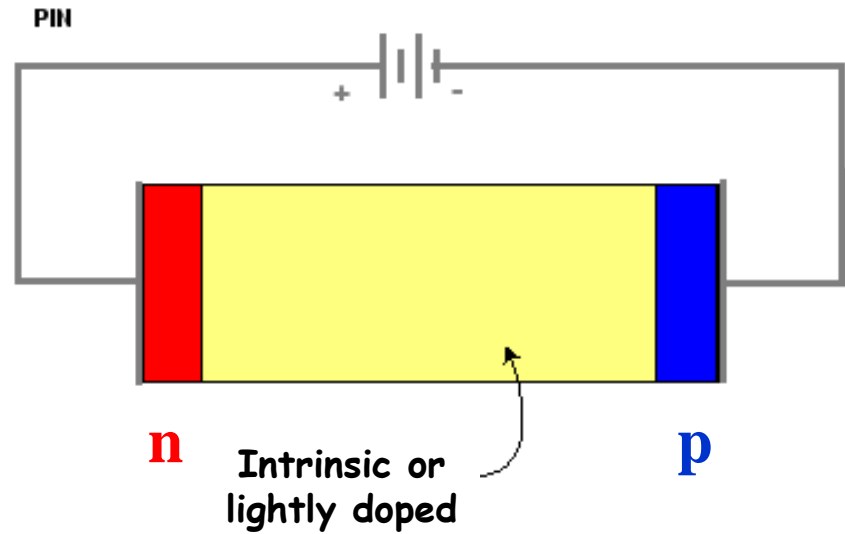
$$i \propto d \propto \sqrt{V} \text{ for } V < V_0$$

$$i = \text{const. for } V > V_0$$

V_0 = full depletion voltage

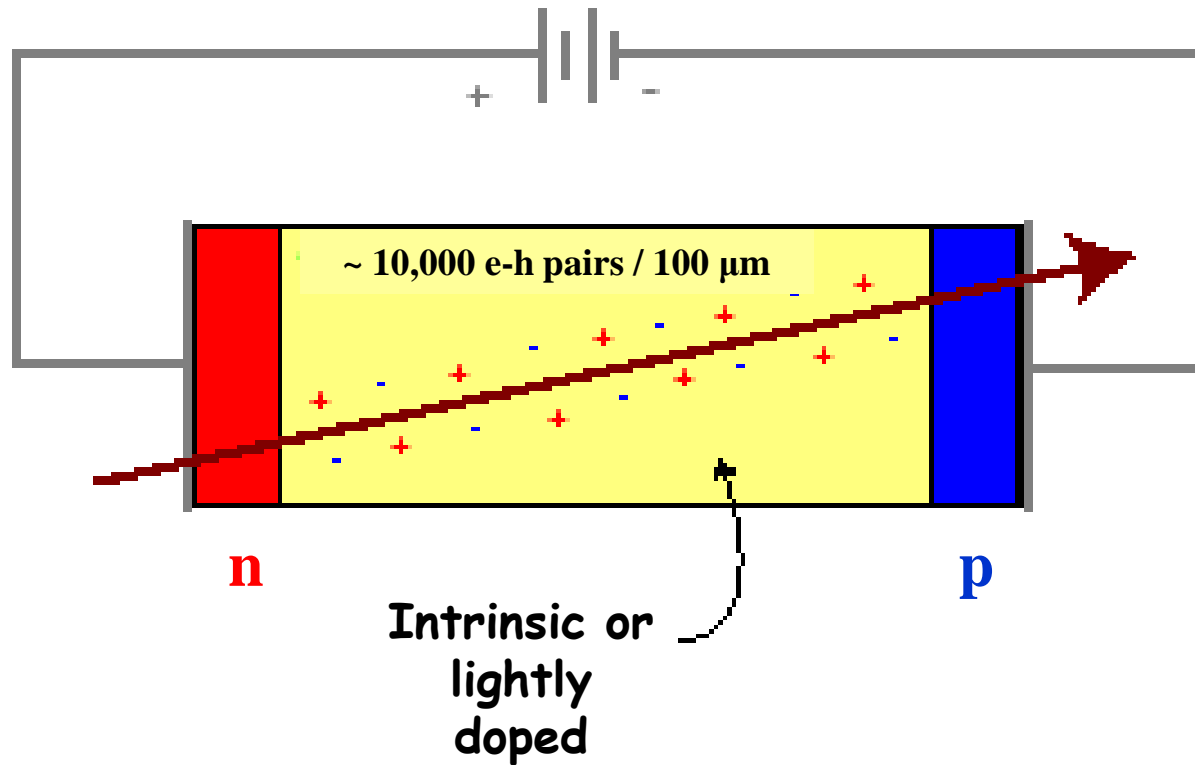
d_0 = junction thickness

PIN Diode



When a charged particle traverses the depletion zone

Simple detector

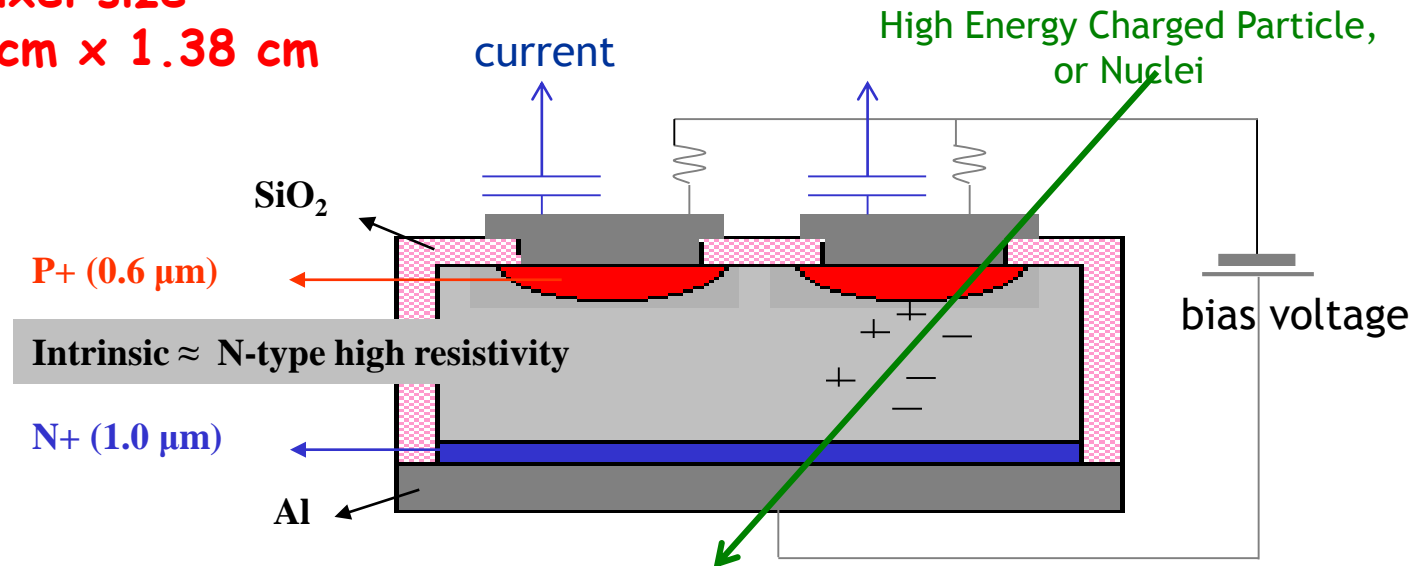


Silicon pixel sensor

- PIN diode, DC type
- Wafer: 5 inch, 525 μm in thickness, double polished side, N-type high resistivity ($>5 \text{ k}\Omega\text{-cm}$), (111) orientation

pixel size

= 1.55 cm \times 1.38 cm

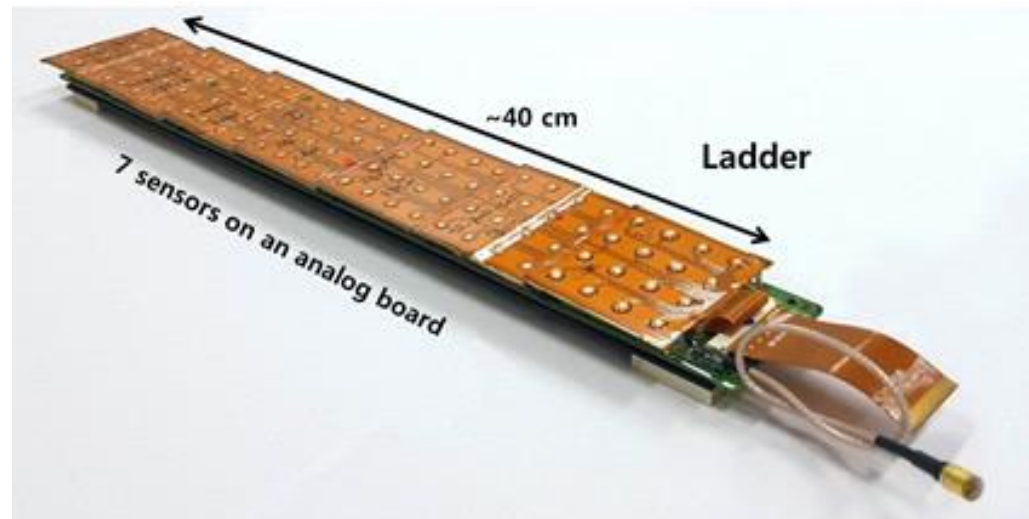
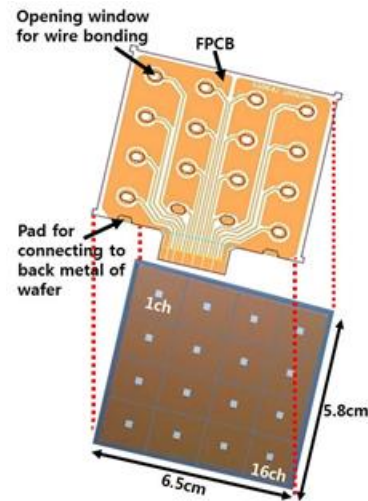


$$\left\langle \frac{dE}{dx} \right\rangle \propto z^2$$

Measure the ionization energy loss in silicon sensor
-> Determine the charge of the incident particle

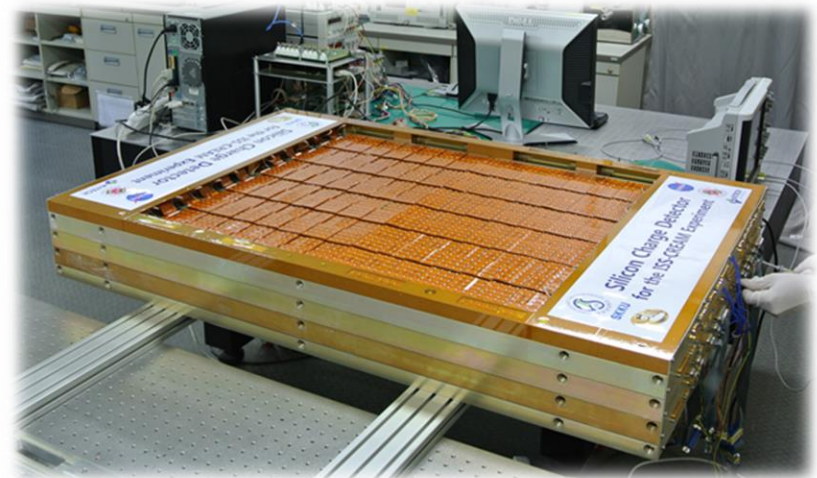
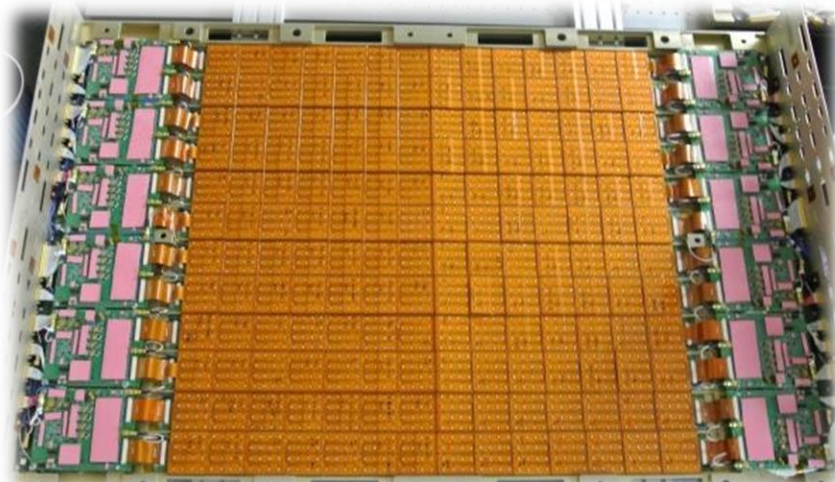
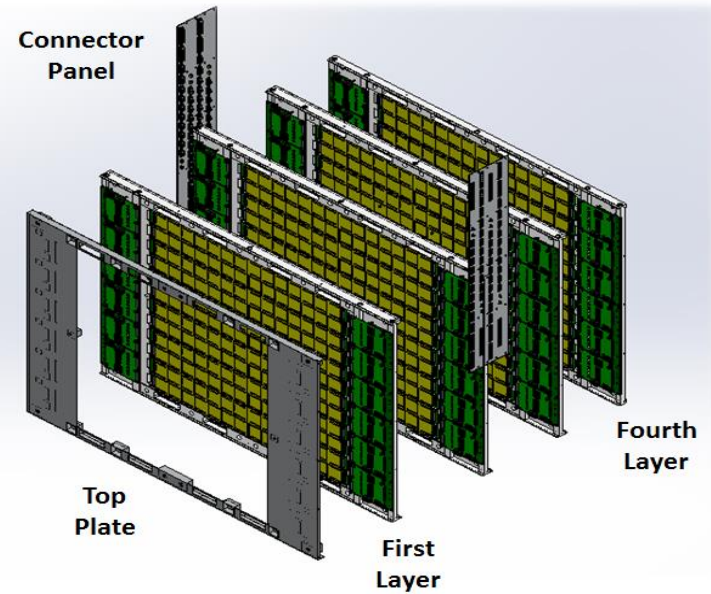
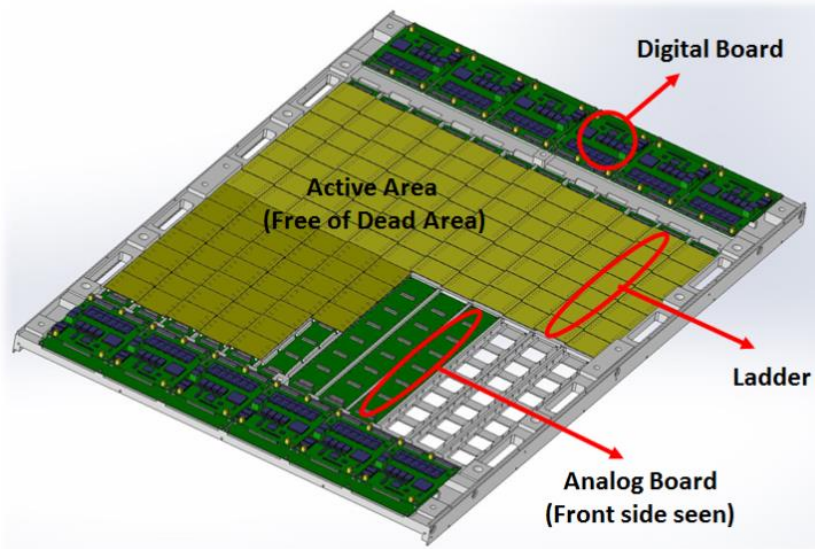
Silicon Pixel Sensor & Ladder for SCD

Built by SKKU group



pixel size = $1.55 \times 1.38 \text{ cm}^2$

Silicon Charge Detector (design, fabrication & assembly) Built by SKKU group



2019-01-14

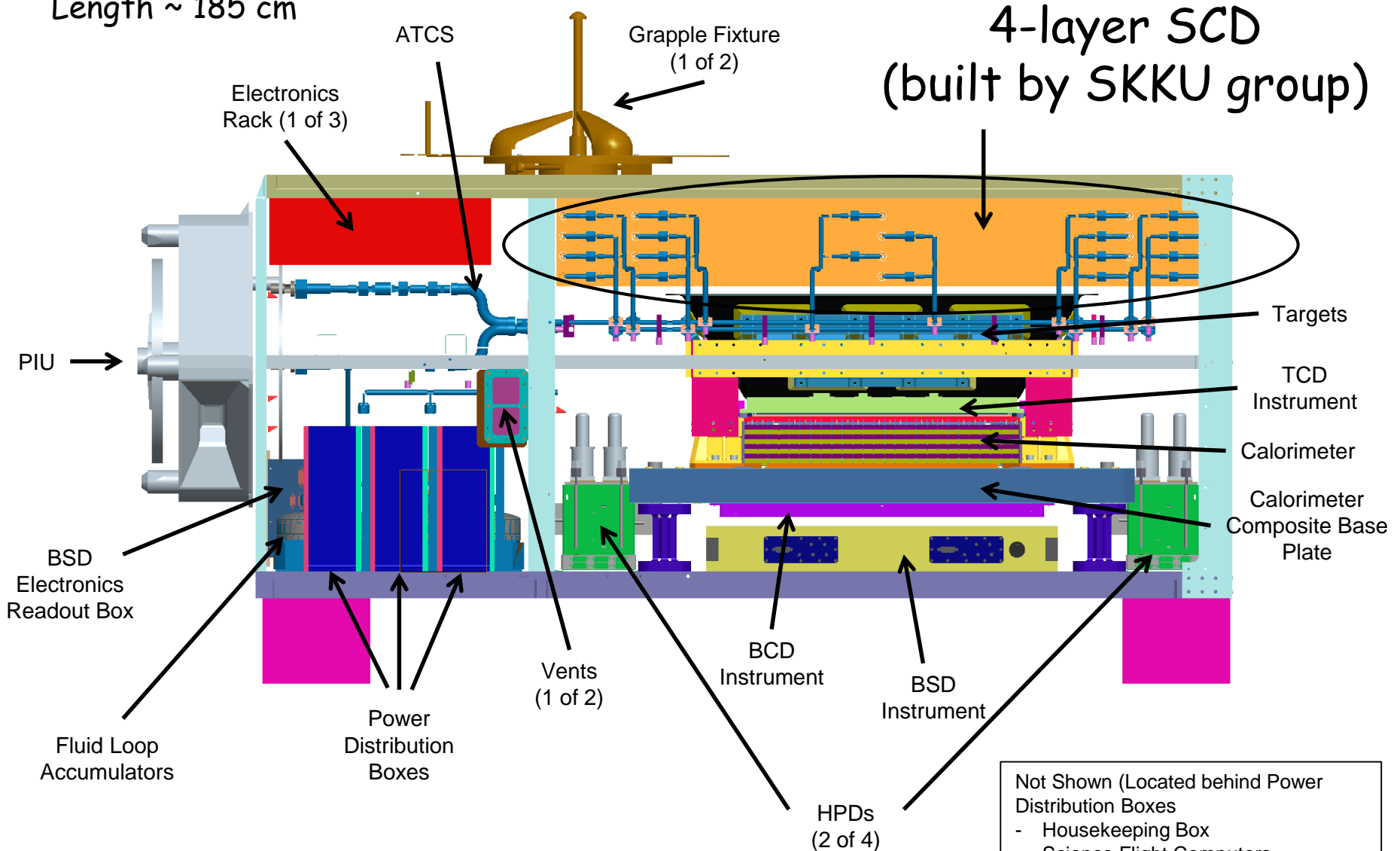
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Silicon Charge Detector (specification)

Mass (kg)	143
Overall Dimension (cm ³)	127.7 (L) x 81.7 (W) x 16.6 (H)
Active Area (cm ²)	78.2 x 73.6
# Layers	4
# Channels	total 10752 (2688 per layer)
Power Consumption (W)	182.5

Mass ~ 1258 kg
Power ~ 415 W
Length ~ 185 cm

ISS-CREAM payload



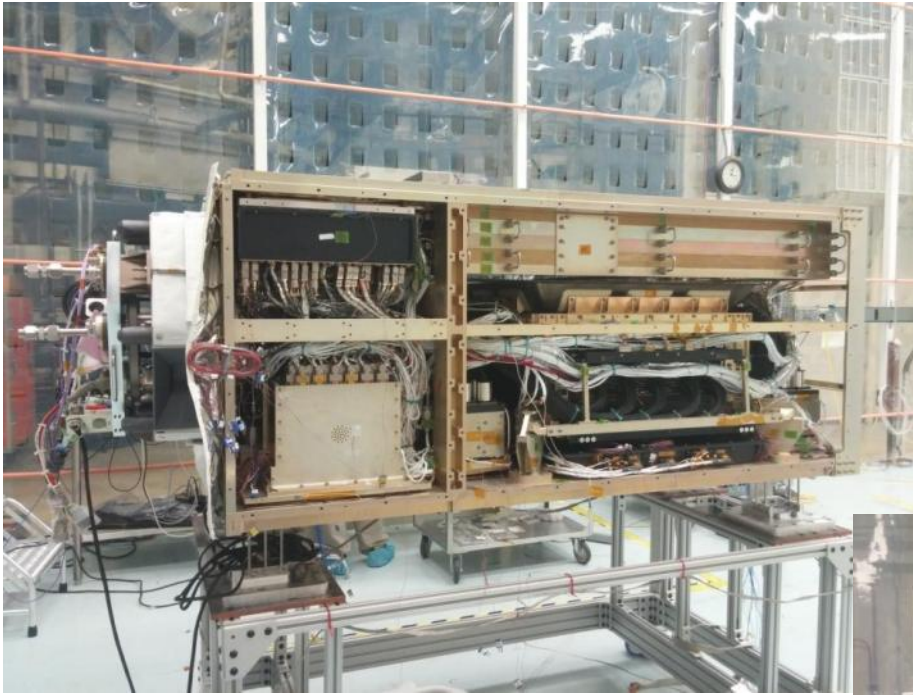
2019-01-14

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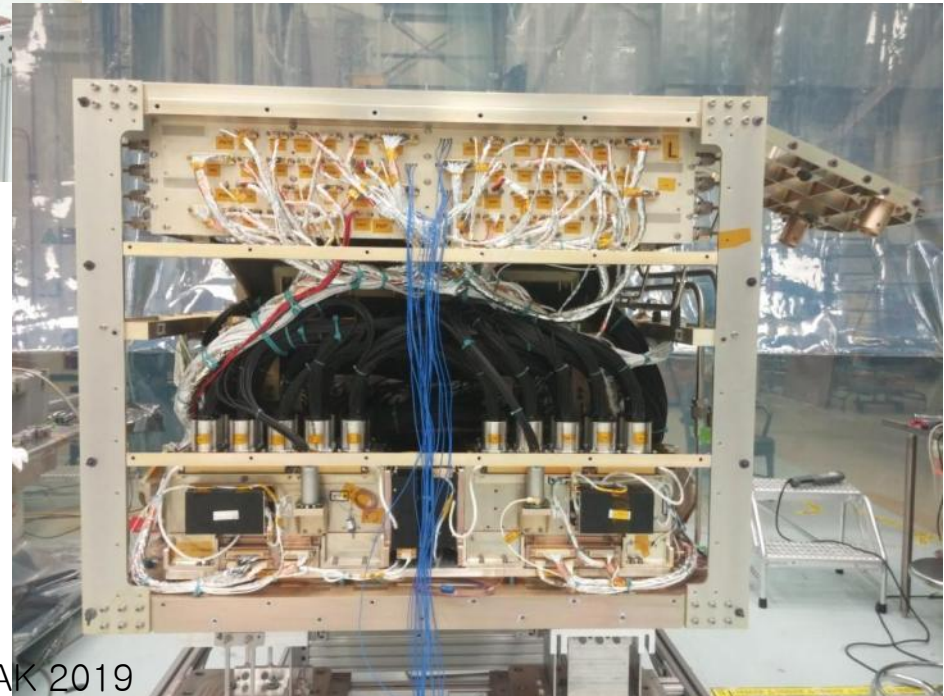
Not Shown (Located behind Power Distribution Boxes)

- Housekeeping Box
- Science Flight Computers

ISS-CREAM @ GSFC before TVAC test (July 22-25, 2015)

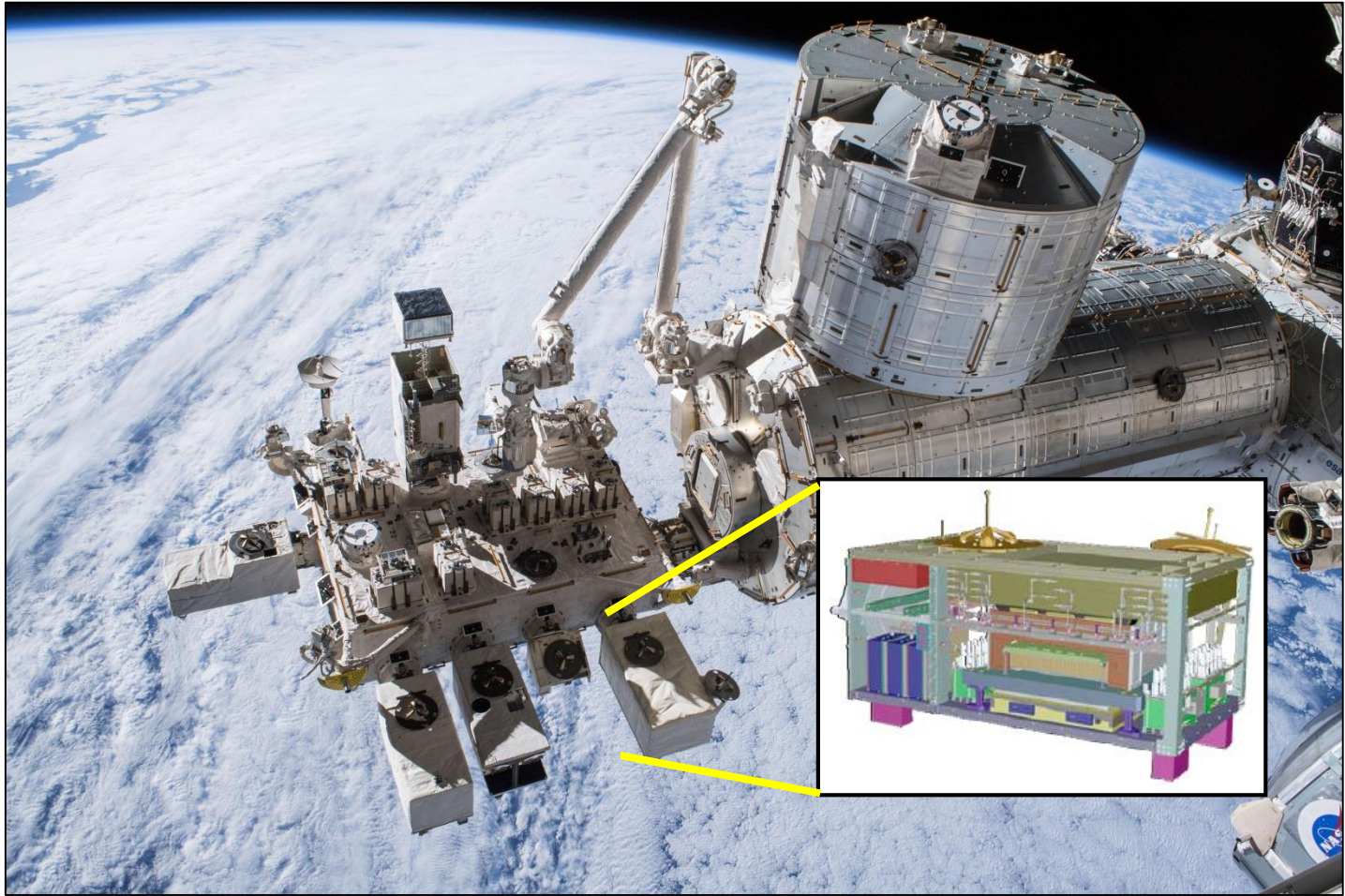


2019-01-14



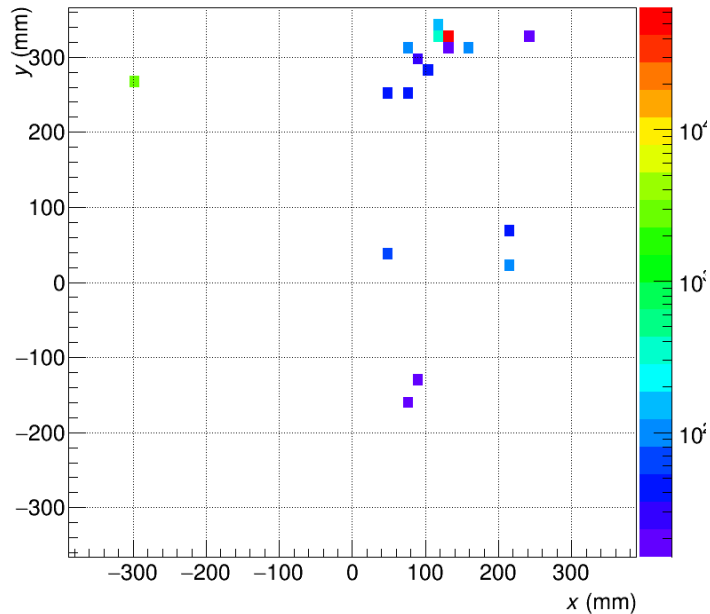
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ISS-CREAM in space operation



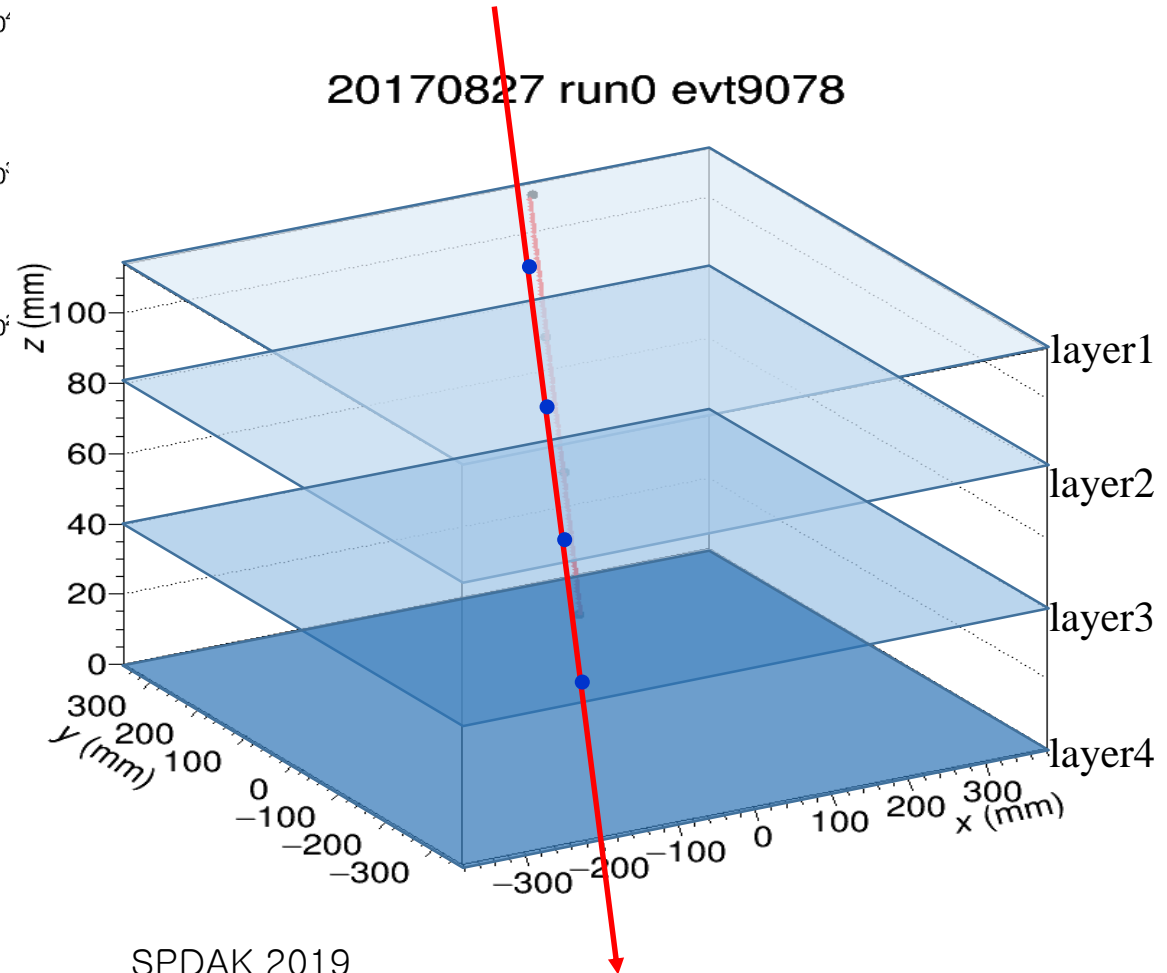
SCD performance: standalone tracking

20170827 run0 evt9078 layer1



A 4-layer track!

20170827 run0 evt9078

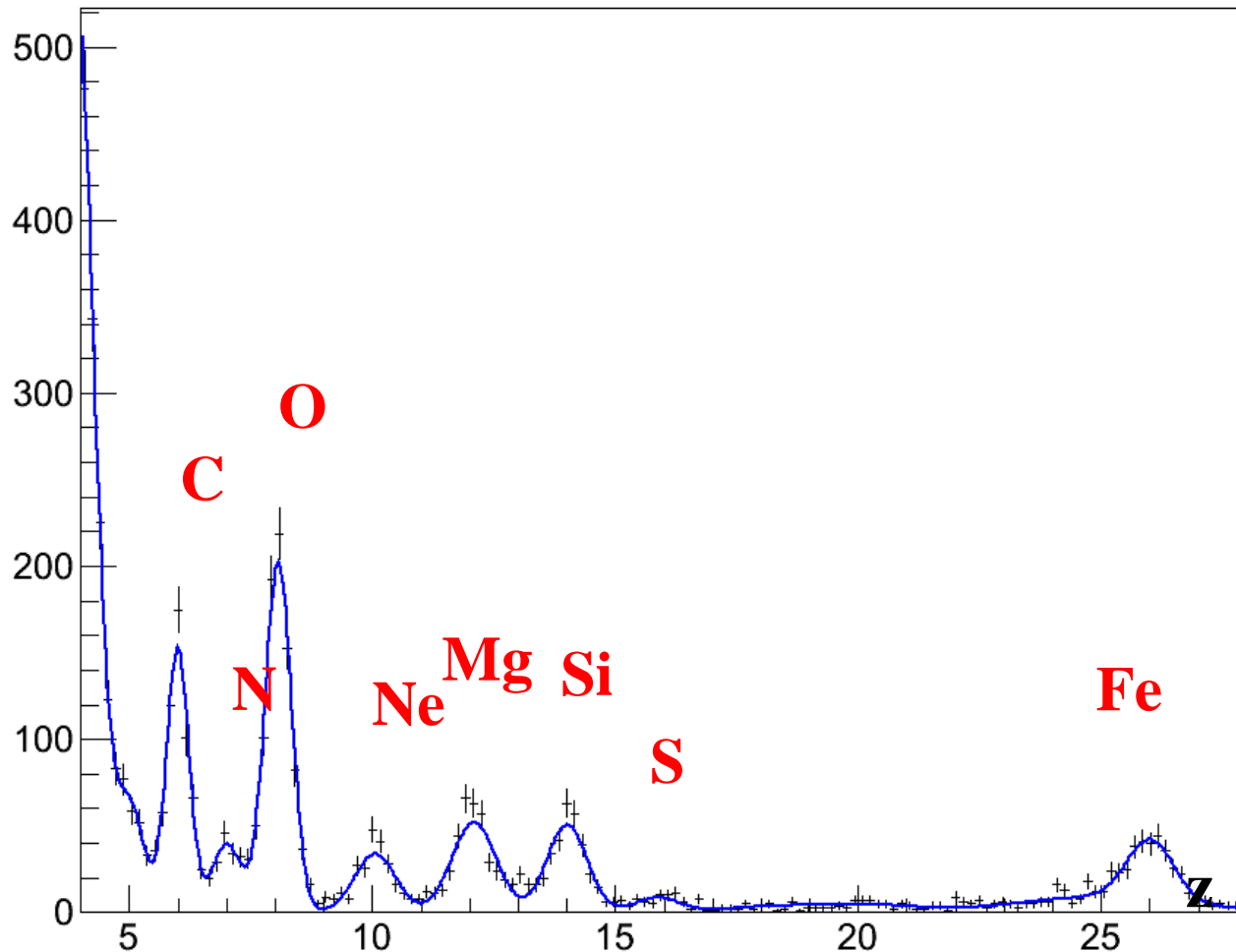


$$\theta = 34.19 +1.91 -0.59^\circ$$

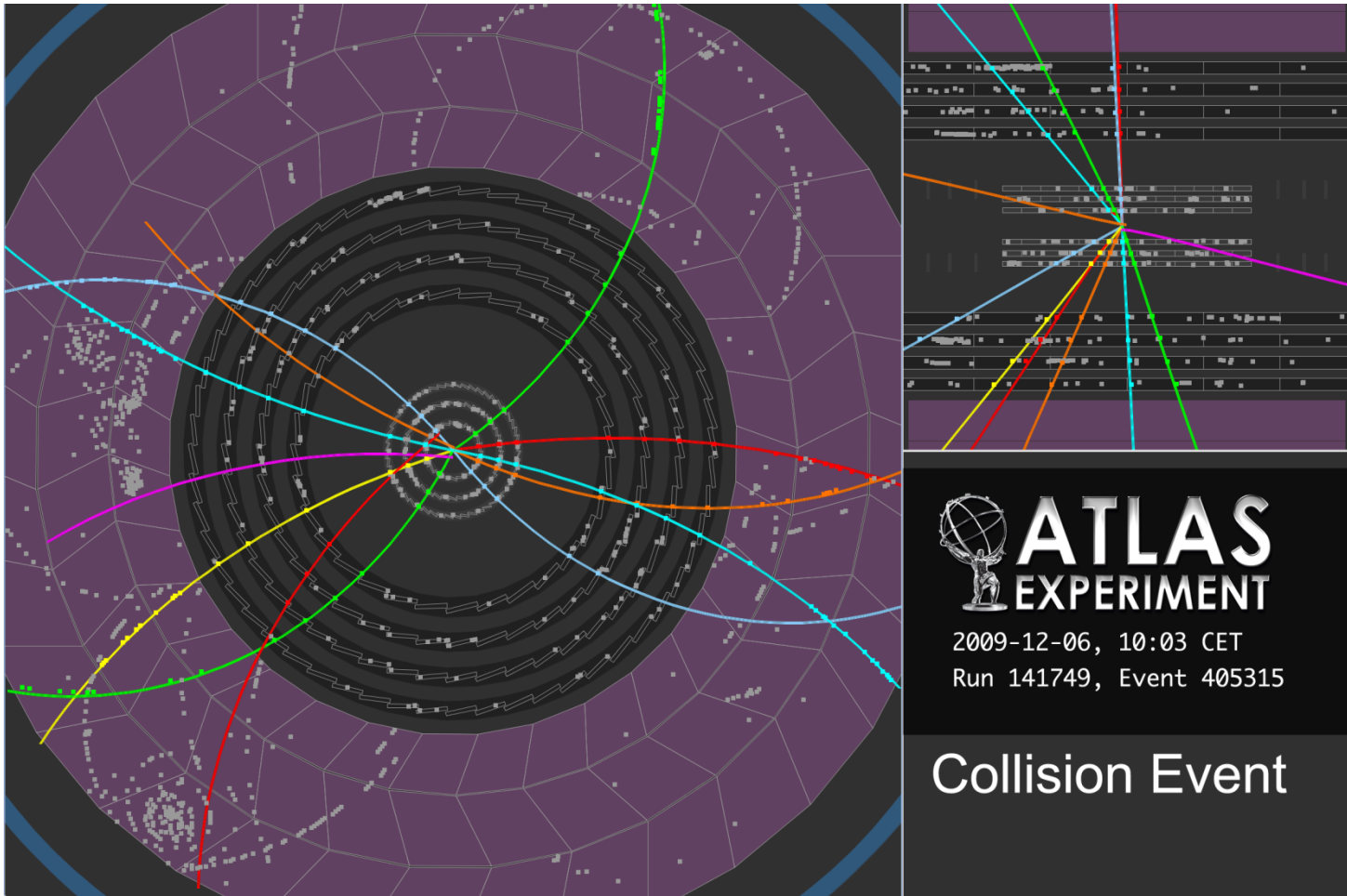
$$\varphi = 105.5 +5.9 -2.9^\circ$$

SCD performance: charge measurement

Preliminary!



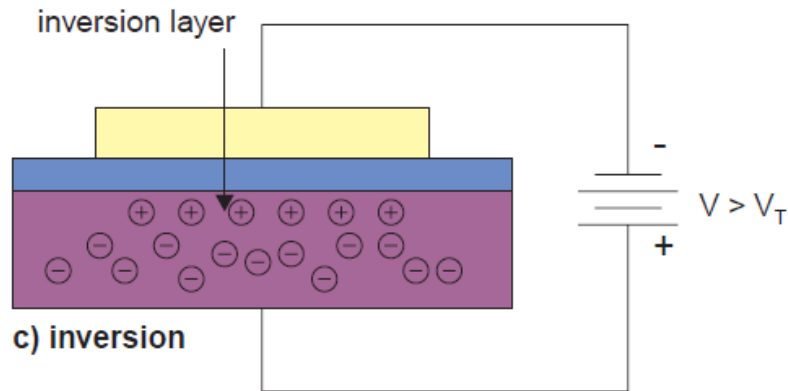
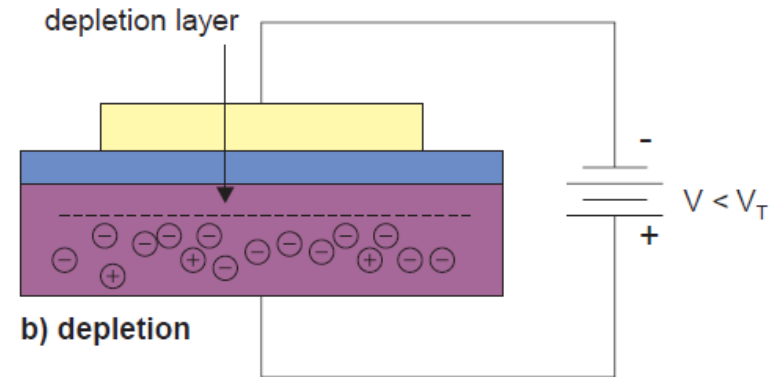
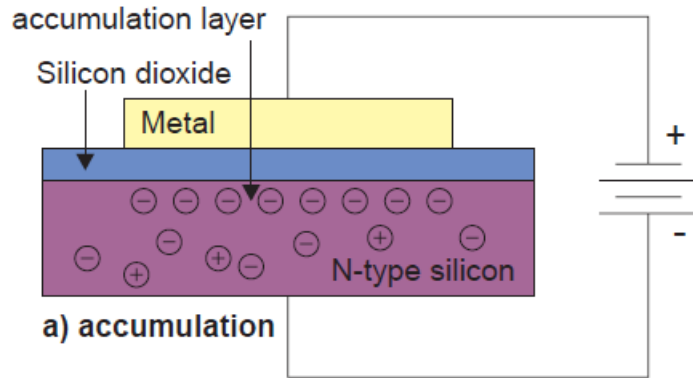
ATLAS Silicon Trackers



<http://atlas.web.cern.ch/Atlas/public/EVTDISPLAY/events.html>

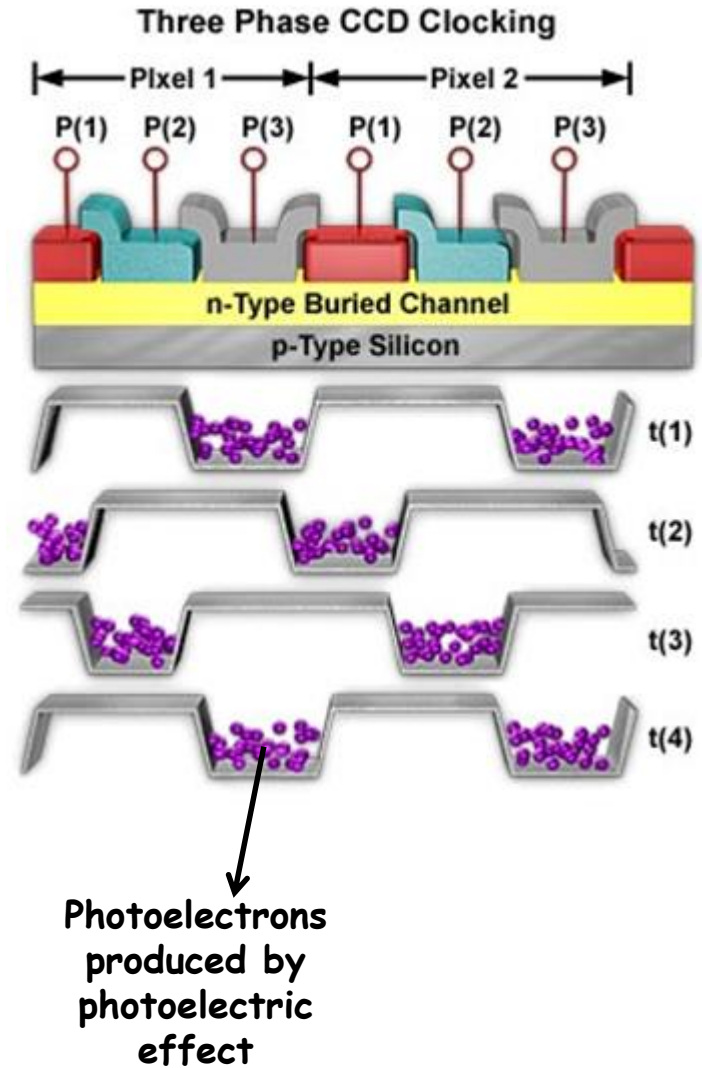
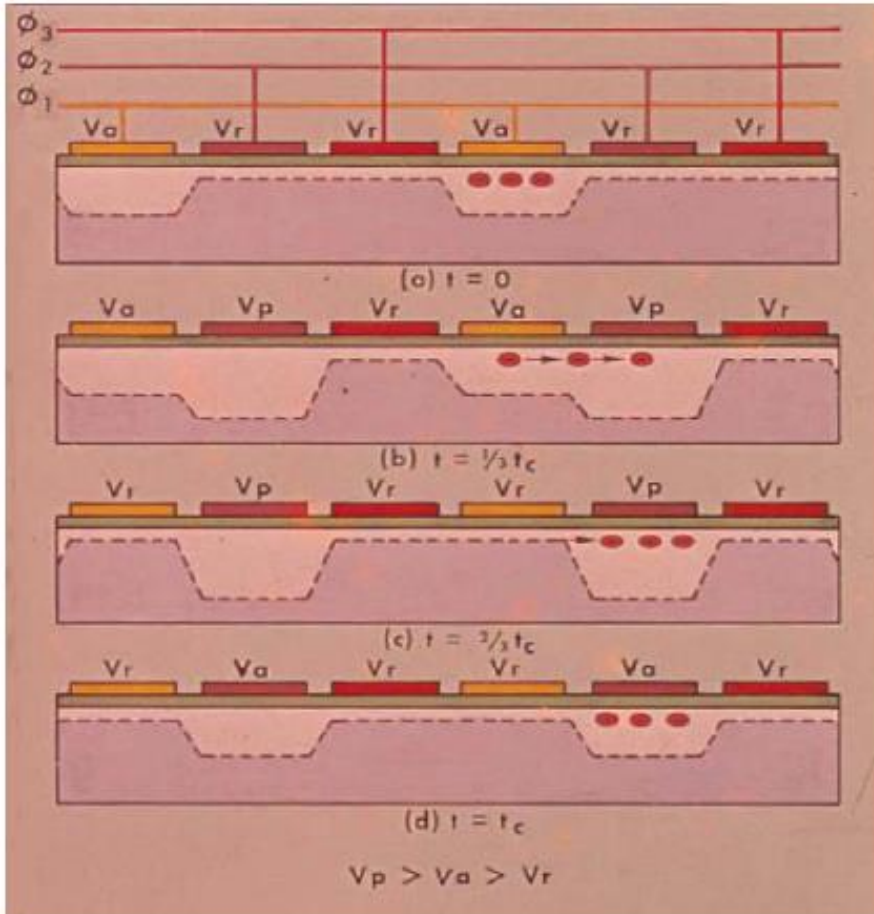
4. Silicon detectors for photon detection

MOS structure (fundamental structure)

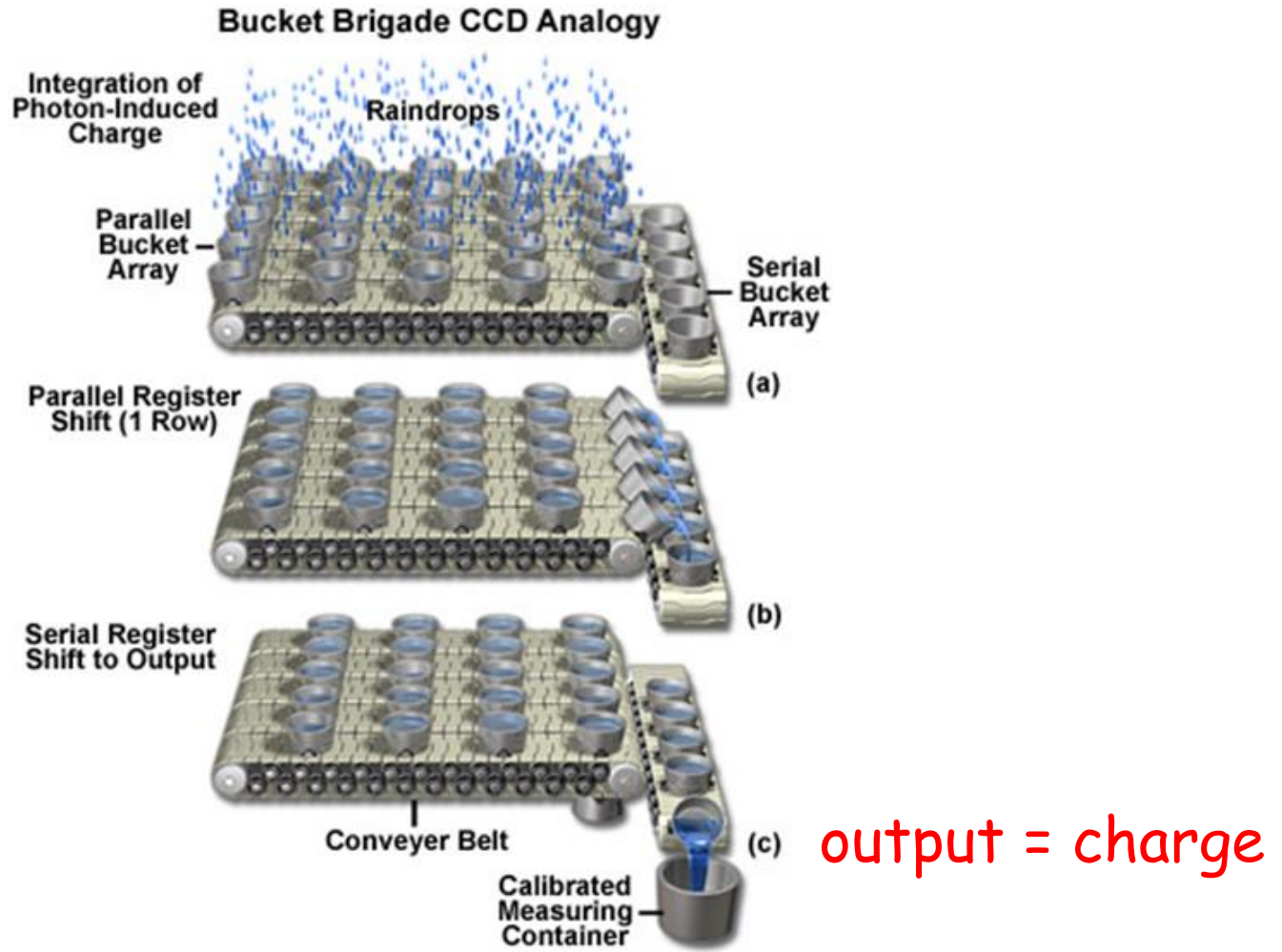


CCD (Charge Coupled Device) sensor

Charge Coupled Device



CCD analogy



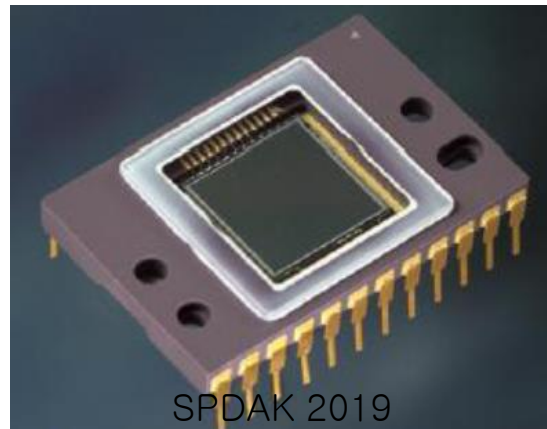
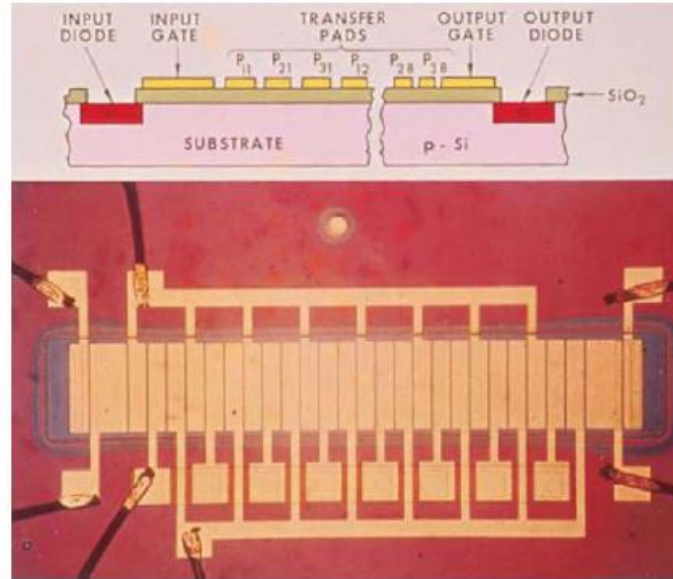
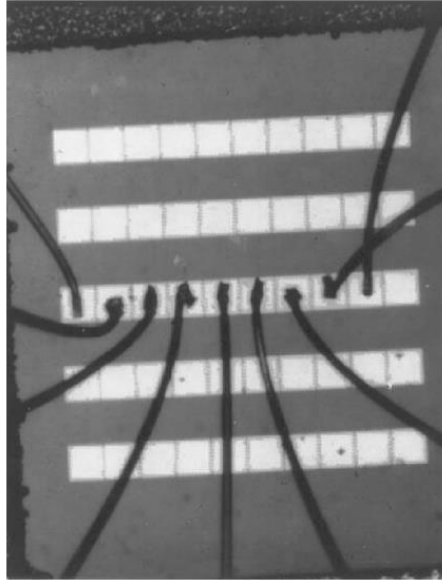
CCD inventors (winners of Nobel prize in physics in 2010)

G. E. Smith & W.S. Boyle : invented CCD in 1970



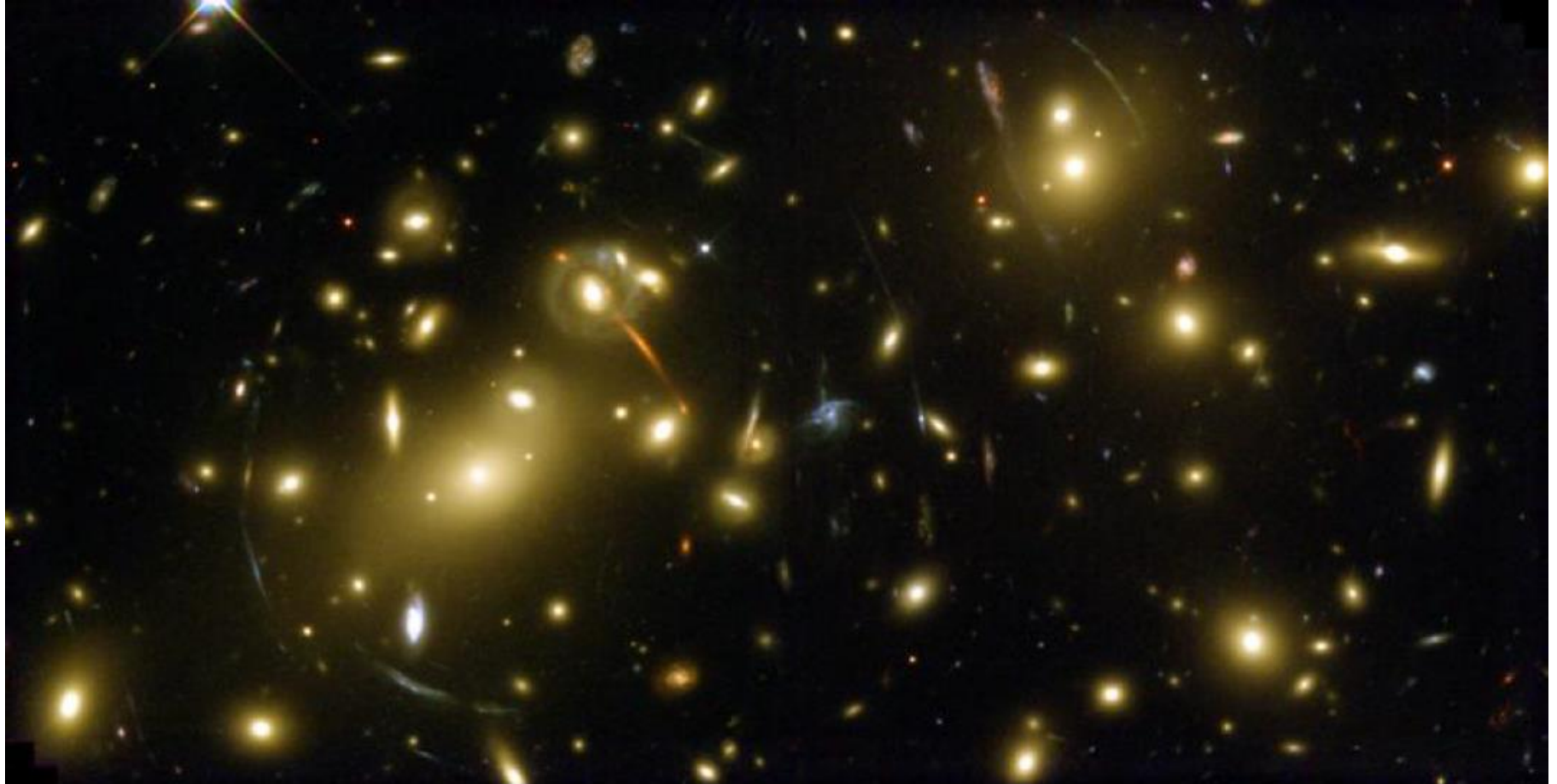
Having Fun @ Bell Lab in 1974 !

How much advanced?



Kodak
Mega pixel CCD
~ 1cm²

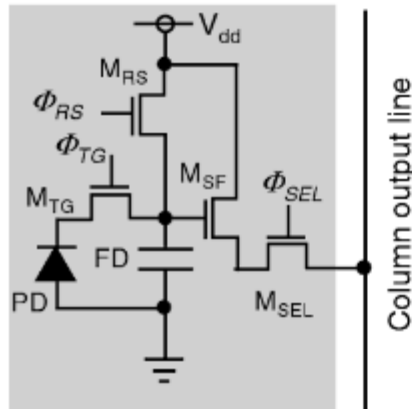
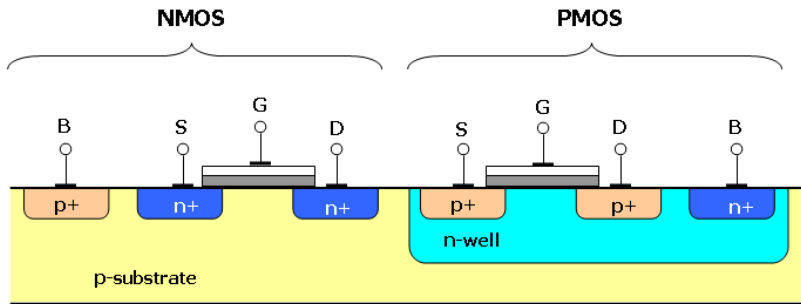
CCD application in Astronomy/Astrophysics



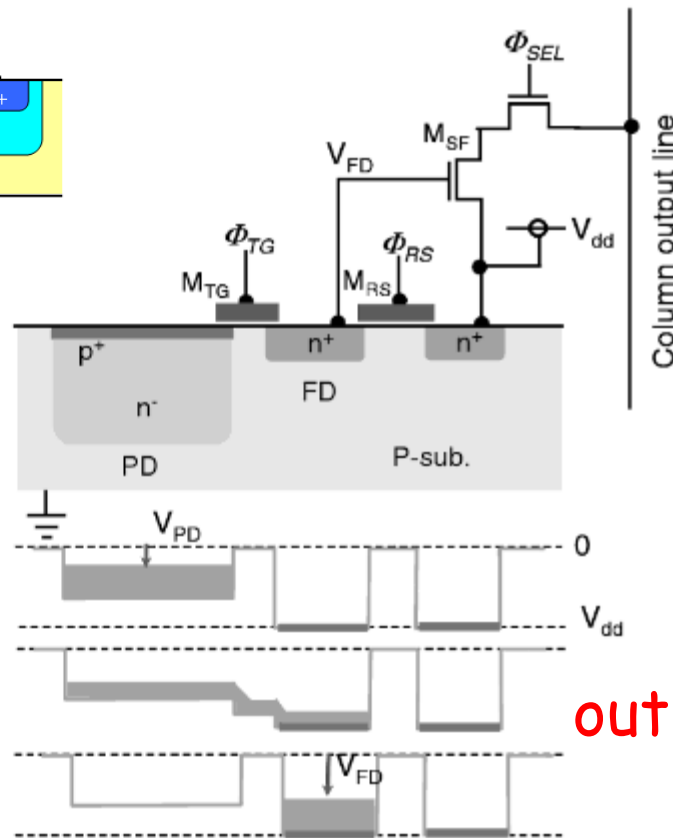
The galaxy cluster Abell 2218. *Image: WFPC2, Hubble Space Telescope, NASA.*

CMOS sensor

CMOS : Complementary Metal Oxide Semiconductor

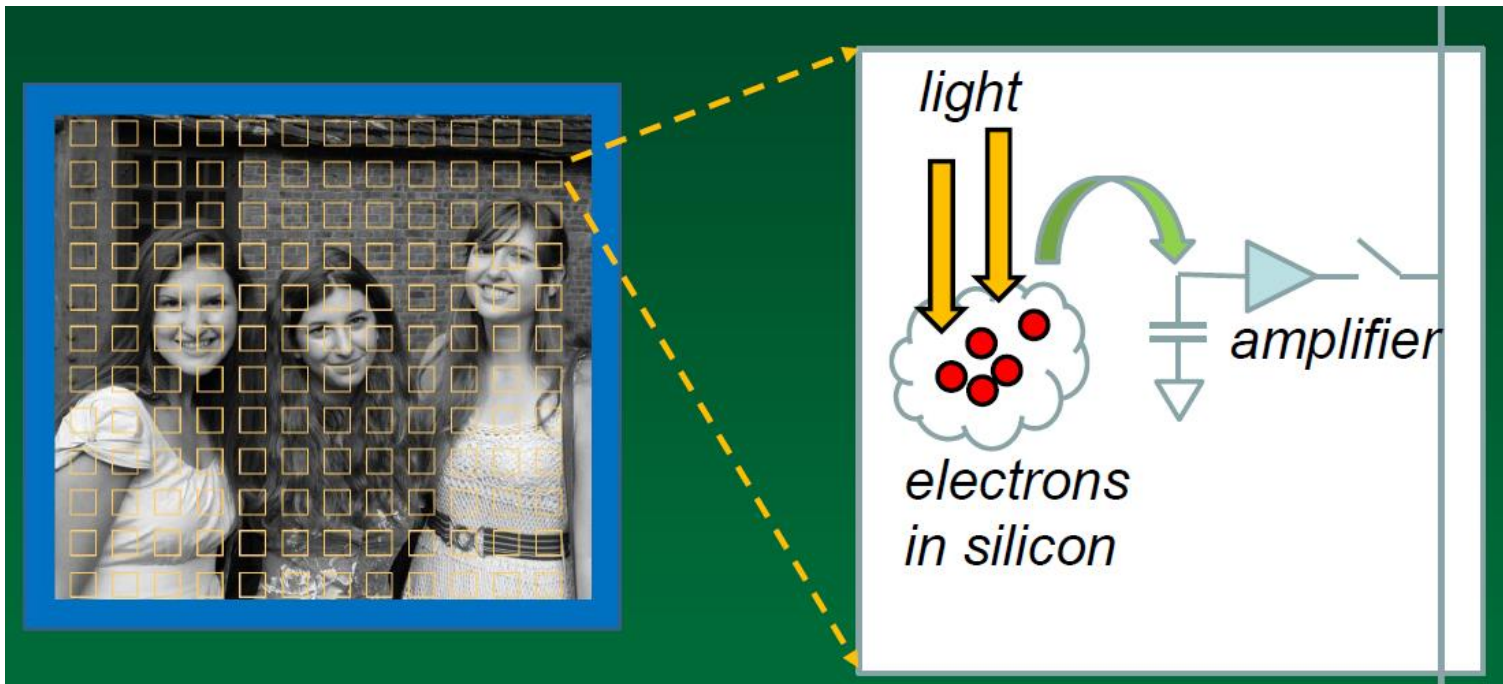


PD = Photo Diode

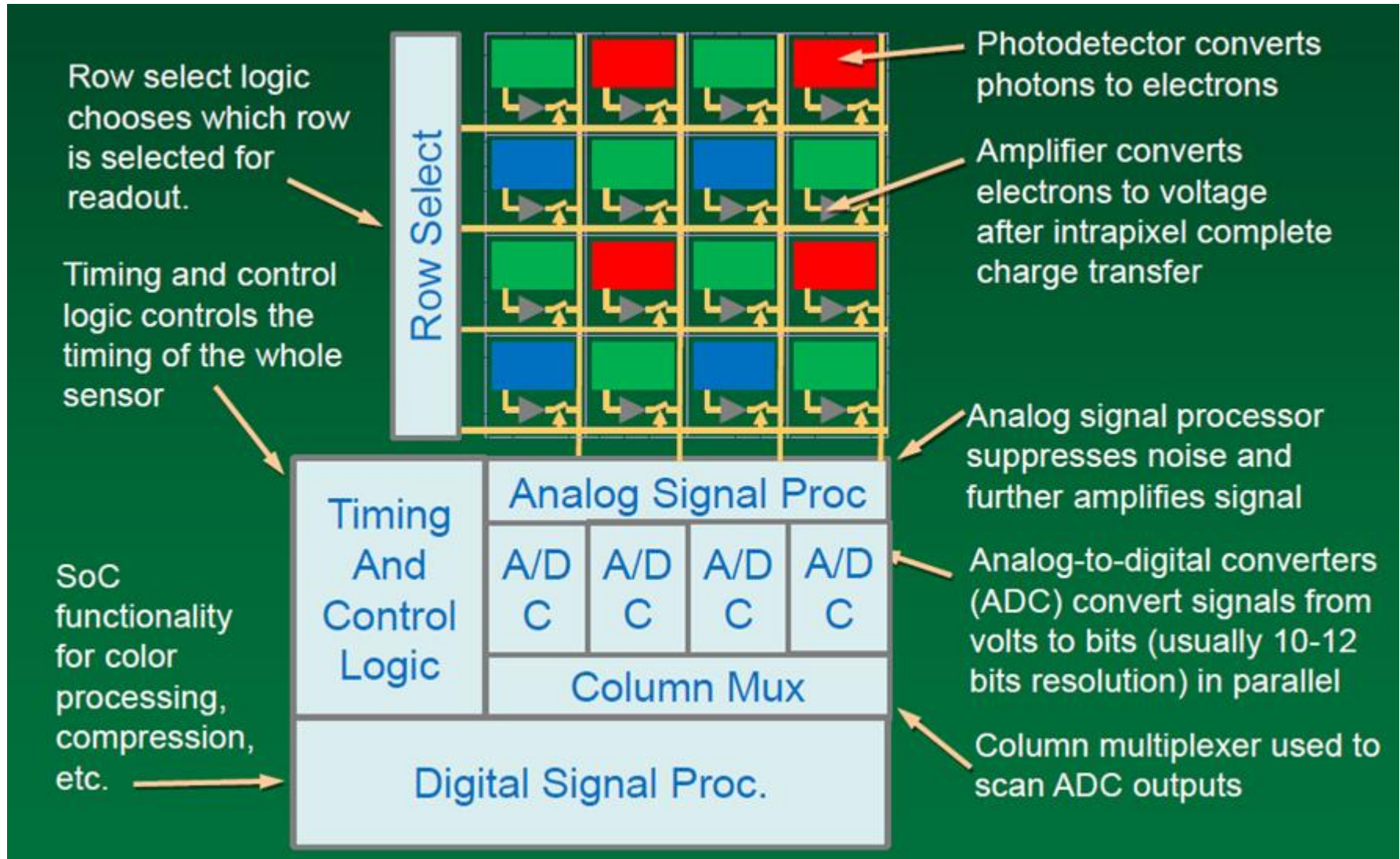


output = voltage

A pixel in CMOS sensor



Layout of typical CMOS sensor



CCD & CMOS summary

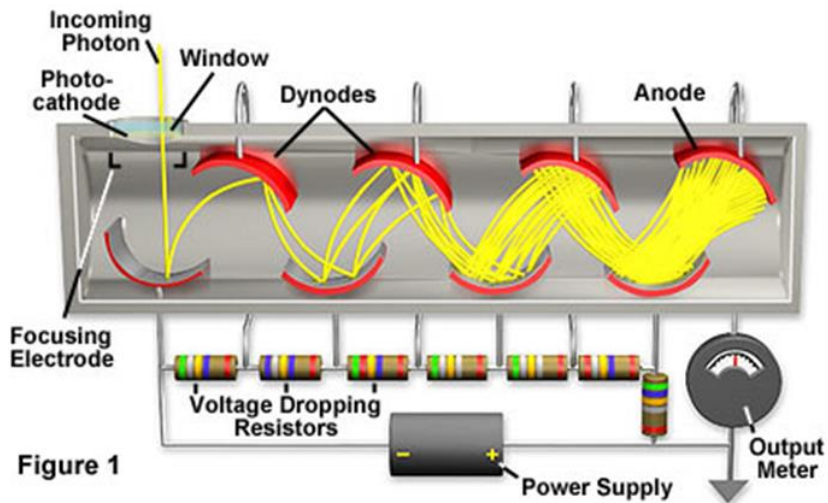
- 원칙적으로는 동일, 즉 포토다이오드 구조로, 광의 세기가 전하량으로 변환되고, 전하를 전압으로 변환 출력
- 변환기가 어디에 위치하는가가 두 센서의 근본적인 차이
 - 픽셀의 정보 이동 방법의 차이, 즉 **CCD**는 전하로 픽셀간 이동 최종 전압으로 변환, **CMOS**는 픽셀 단위에서 전압으로 변환하여 이동
- 잡음이 크고, 동적폭 (**dynamic range**) 및 속도에서 뛰어나지 않음
 - 동적폭 = Full Well Capacity / 잡음
 - Kodak Mega 픽셀 CCD 200,000 전자 / 20전자 = 100,000
- 광량이 적은 환경에서는 고민감도의 센서가 필요하나, **CCD와 CMOS는 증폭형 센서가 아니므로 야간 상황에서 그 성능에 한계**
- 우리의 눈의 민감도는 **CCD** 보다 우수함
 - **CCD** 민감도 ~ 0.03 Lux (냉각 시 0.002 Lux)

Photomultiplier

- 정확히 말하면 광전자를 다수의 전자로 증폭
- 광음극(photocathode)과 함께 사용하는 PMT(Photomultiplier Tube)와 MCP(Microchannel Plate)가 대표적으로 단일 광자 계수 가능
- 반도체 소자에서는 센서 내부에서 광전자(photoelectron)를 증폭:
ICCD(Intensified CCD), EB(Electron Bombardment)CCD, EM(Electron Multiplier)CCD, APD(Avalanche Photodiode), SiPM(Silicon Photomultiplier)

Photomultiplier Tubes (PMTs)

- 초민감 초고속 특성을 갖는 광센서로 과거 수십년간 특수목적에 사용
- 그러나 진공관식으로 부피가 매우 크고, 충격에 취약하며 고전압을 필요로 하므로, 야전에서 내구성, 휴대성 및 실용성이 크게 떨어지며, 광량이 많아지면 소자가 파괴되는 문제



PMT의 원리와 Hamamatsu사 제품

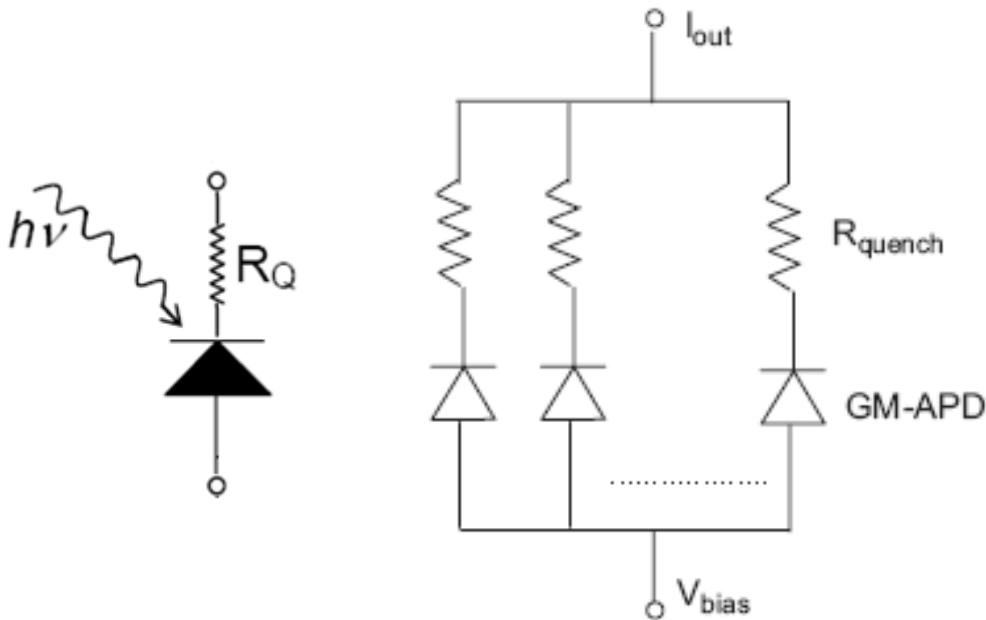
20 inch World largest PMT

For Super-K

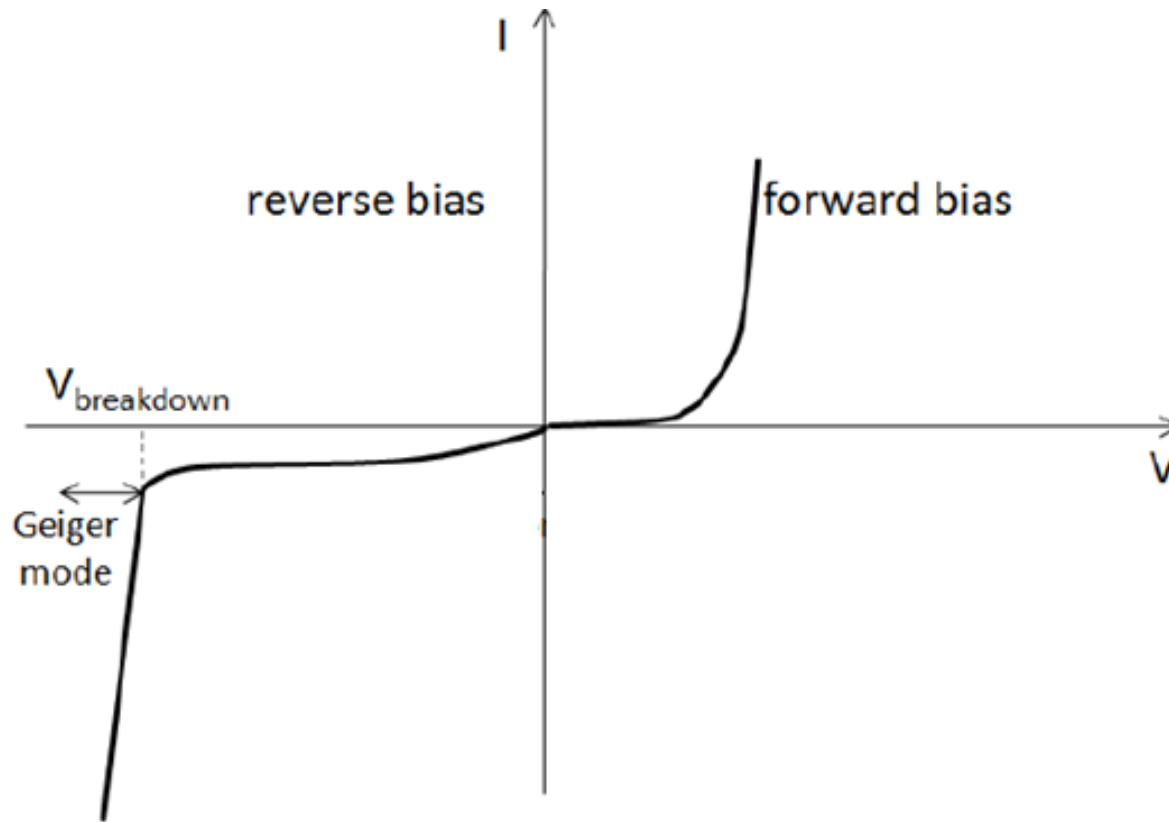


SiPM (Silicon PhotoMultiplier)

- Micropixel (**Geiger mode APD**) 어레이로 이루어진 반도체 광다이오드
- Micropixel의 크기는 $10\sim 100\mu\text{m}$ 로 1mm^2 의 면적당 $100\sim 1000$ 개 집적
- 각 Micropixel 은 공통의 인가전압과 로드 저항으로 작동, 출력신호는 모든 Micropixel 신호의 합(**multiplexed output**)
- 즉 **Binary**의 디지털소자로 입사광의 수를 세는 아날로그식의 광센서

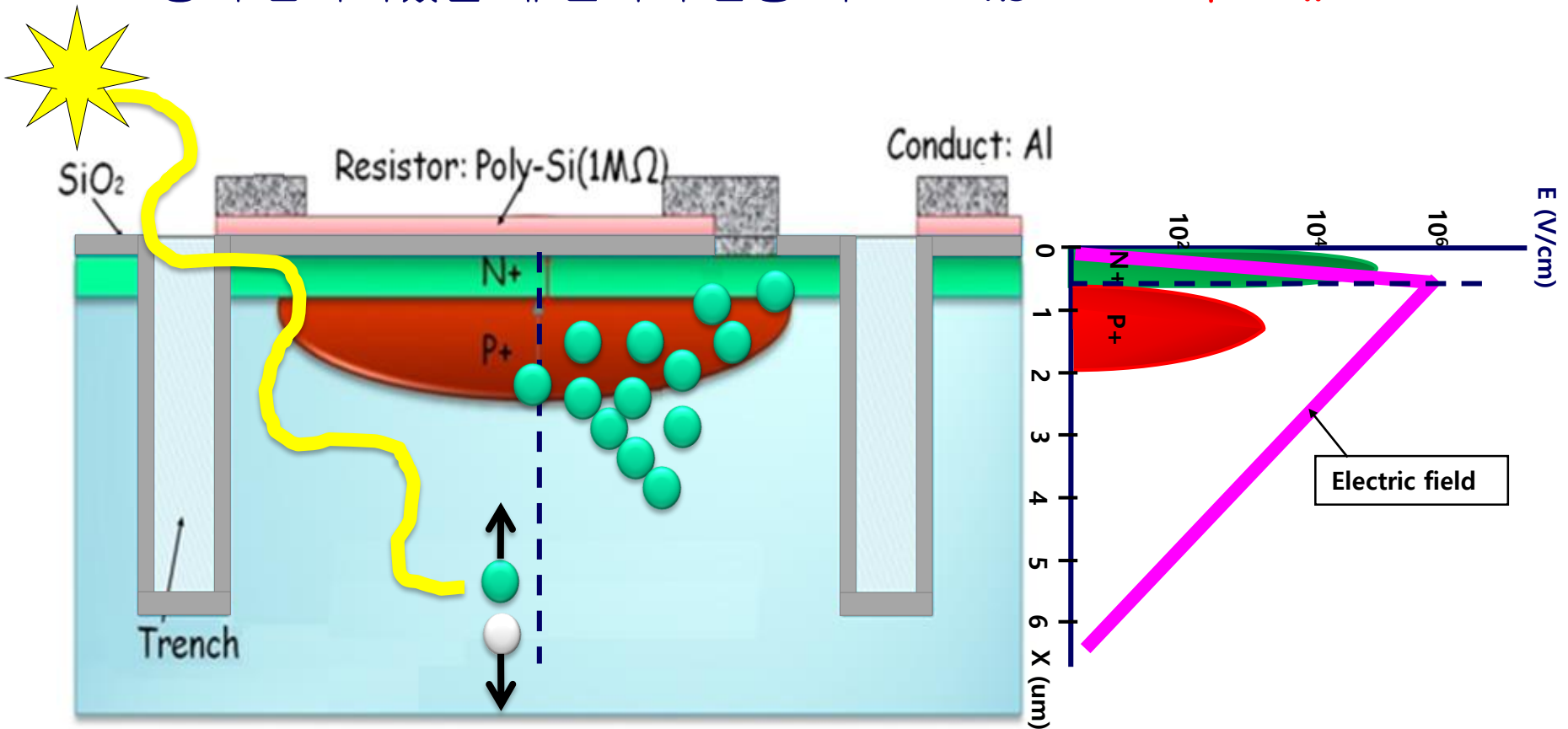


Geiger Mode

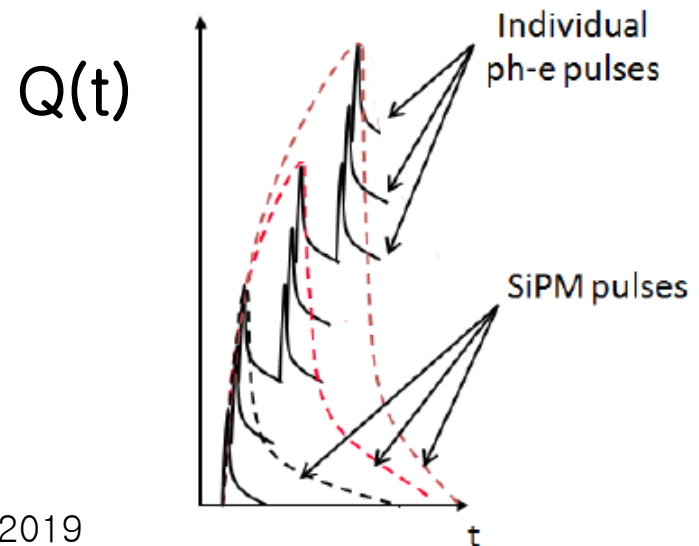
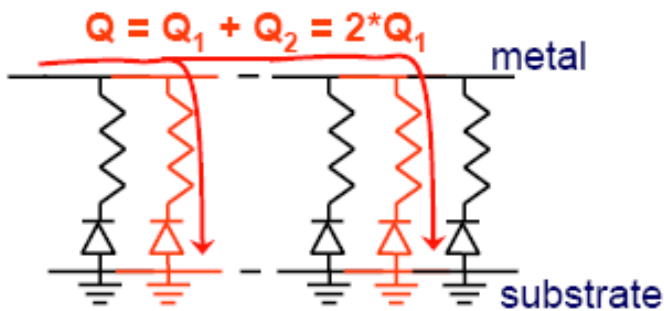
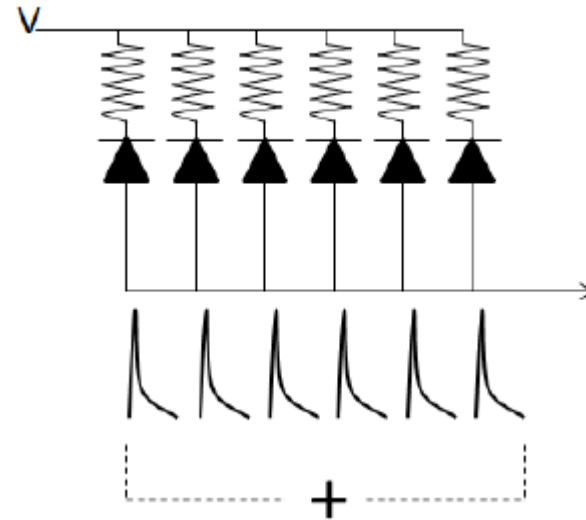
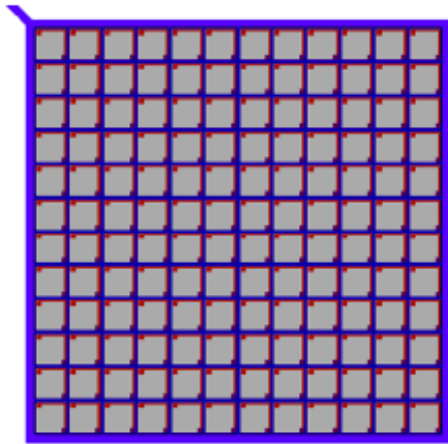


SiPM

- PN 접합면에 매우 높은 전기장 형성
- 한 개의 광자 입사 -> **100만 배**의 전자증폭 발생 -> **초민감도 !!**
- 광이 입사되었을 때 센서의 반응 속도 -> **1ns 초고속도 !!**



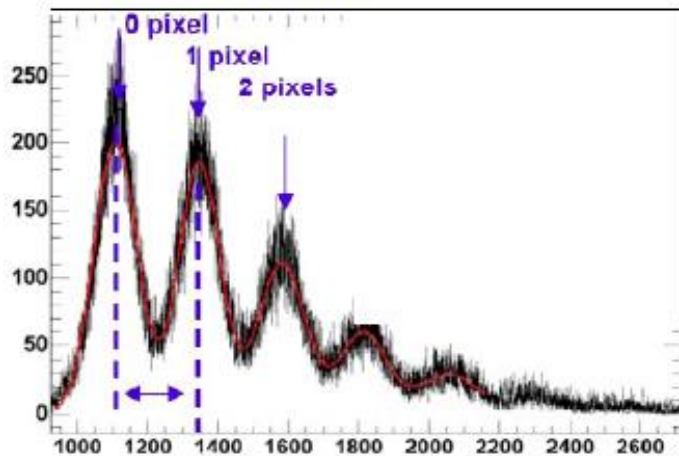
Analog Signal



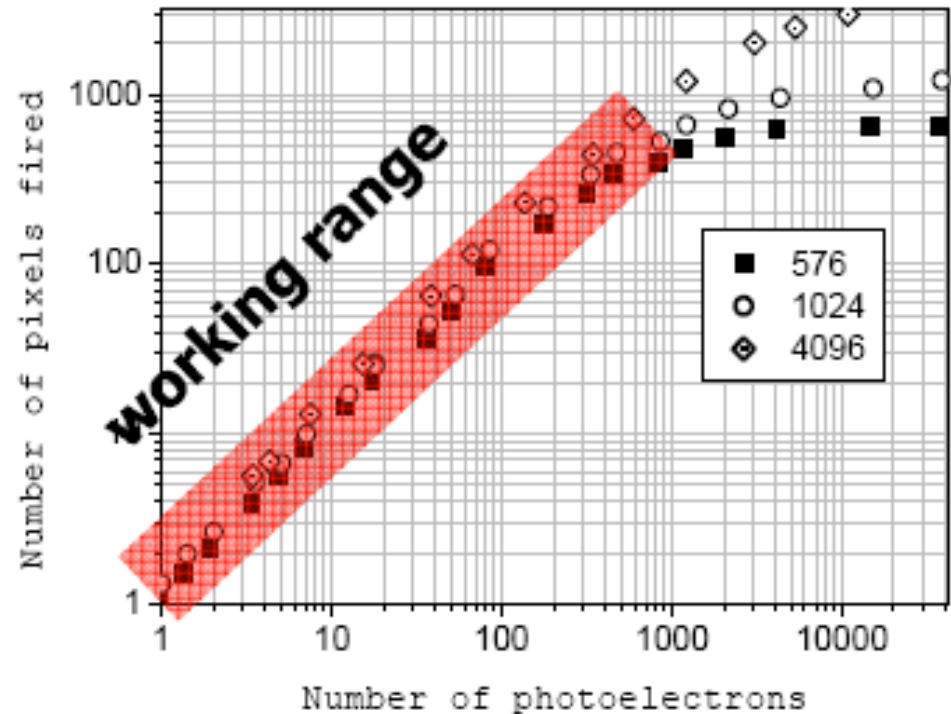
Analog Signal & Dynamic/Working Range



Gain calibration



IRST of INFN Pisa

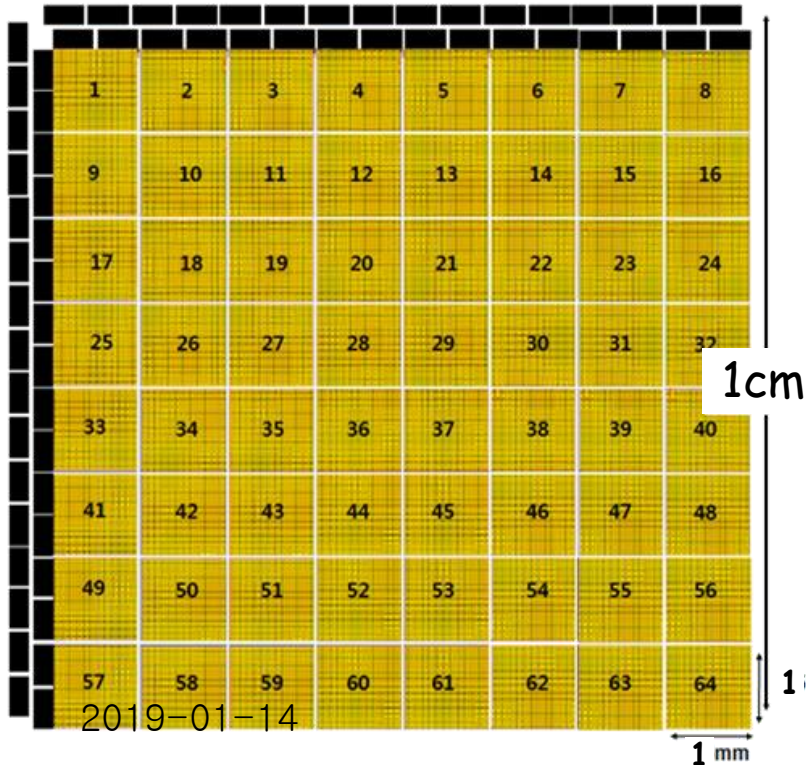


다화소용 8 × 8 픽셀 어레이 소자

- ◆ SiPM 픽셀 : $1 \times 1 \text{ mm}^2$ 크기
($30 \times 30 \mu\text{m}^2$ 크기, 10^3 개의 마이크로 픽셀)

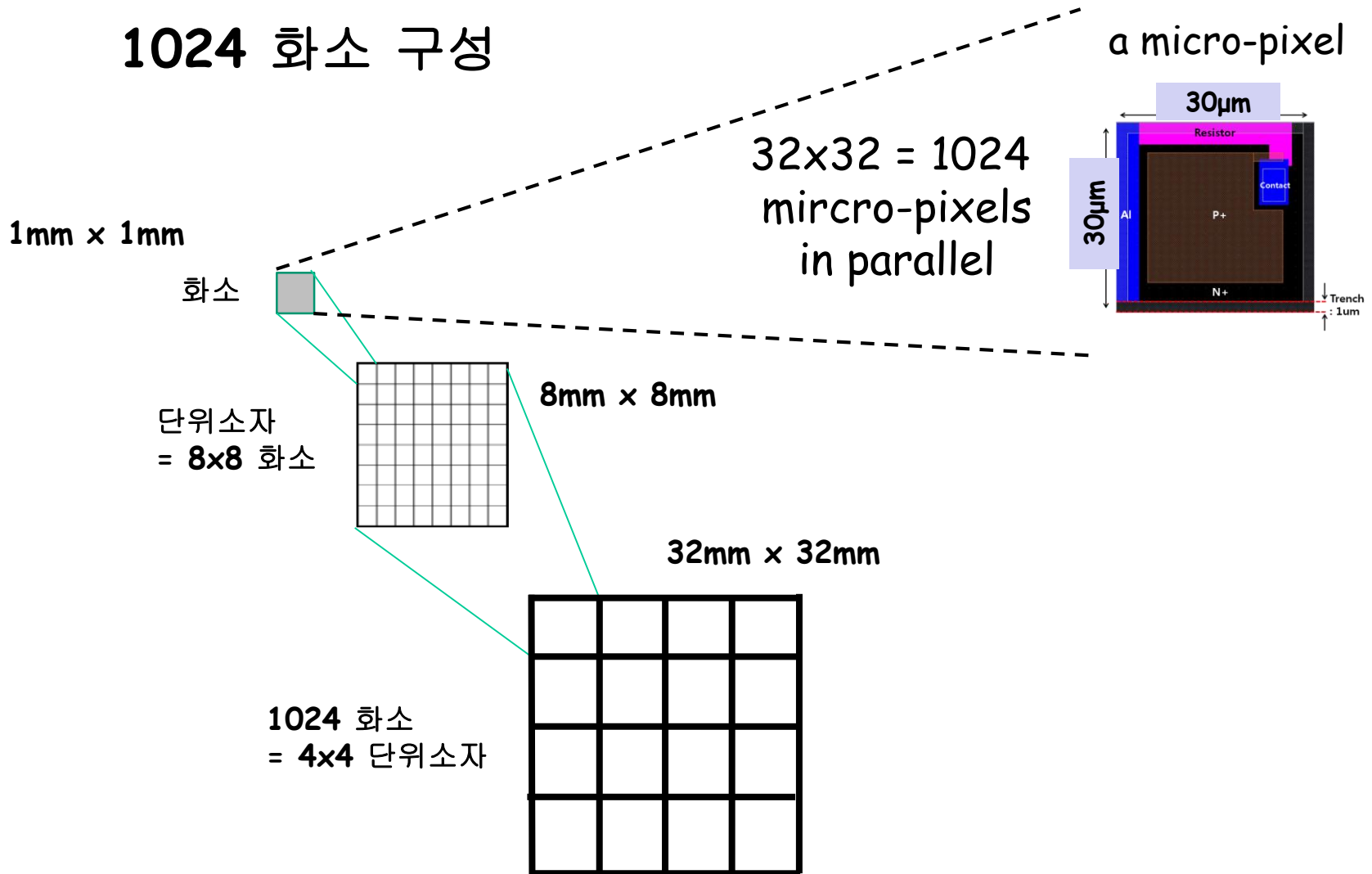
- ◆ 64ch SiPM 소자 : $1 \times 1 \text{ cm}^2$

64ch 설계도
1cm



1024 화소 배열

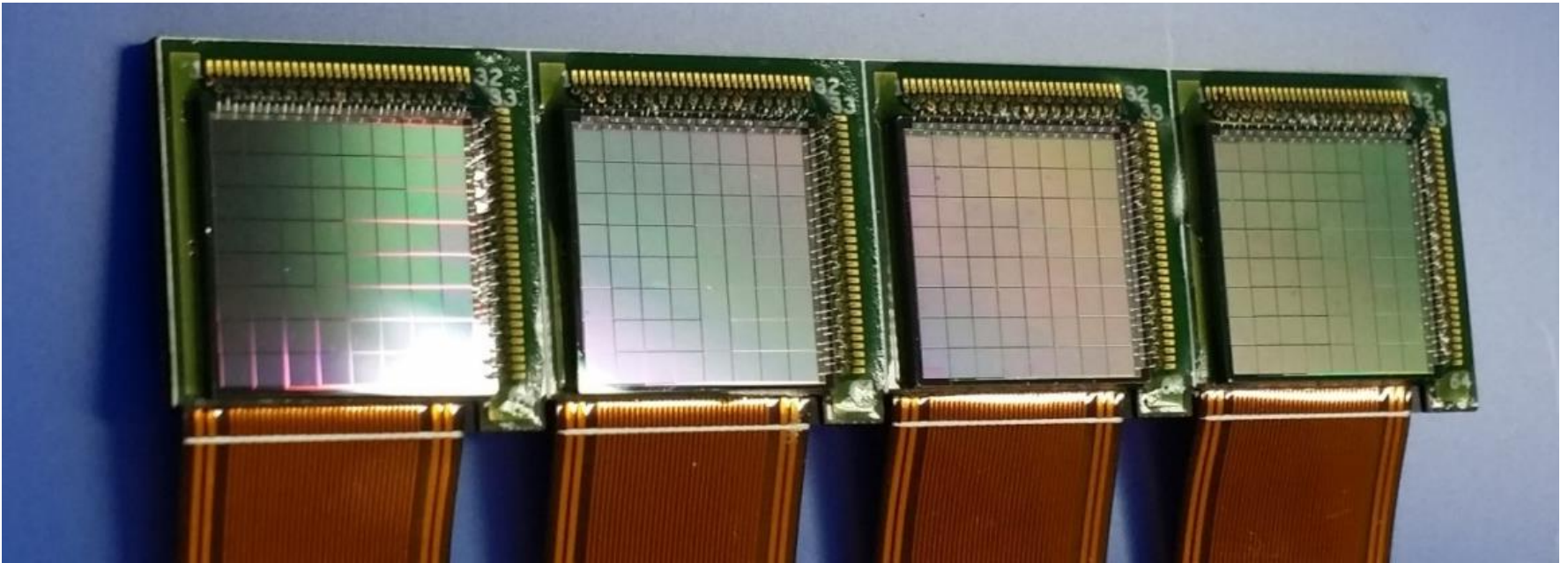
1024 화소 구성



단위소자 4개가 wirebonding된 Rigid-FPCB

- ◆ SiPM 픽셀 1024ch 제작: $1 \times 1 \text{ mm}^2$ 크기
($30 \times 30 \mu\text{m}^2$ 크기, 10^3 개의 마이크로 픽셀)
- ◆ 64ch SiPM 소자 : $1 \times 1 \text{ cm}^2$

제작된 SiPM 단위 소자들 (각 1 cm^2 , 64ch의 픽셀로 구성)



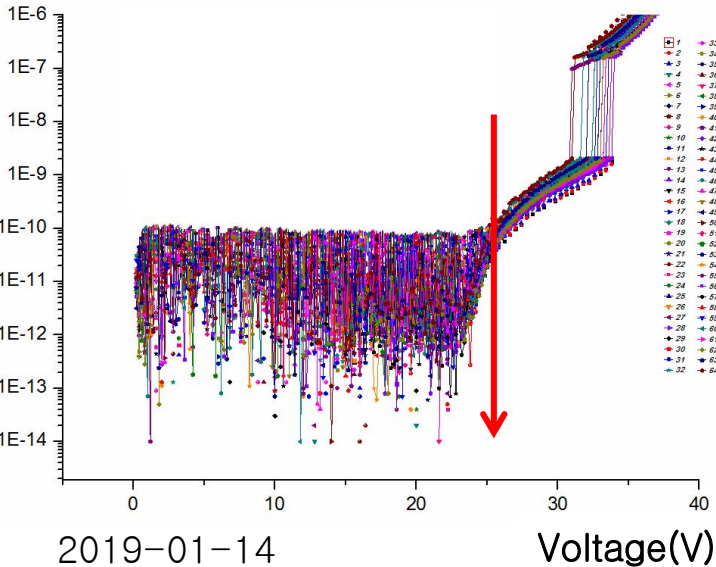
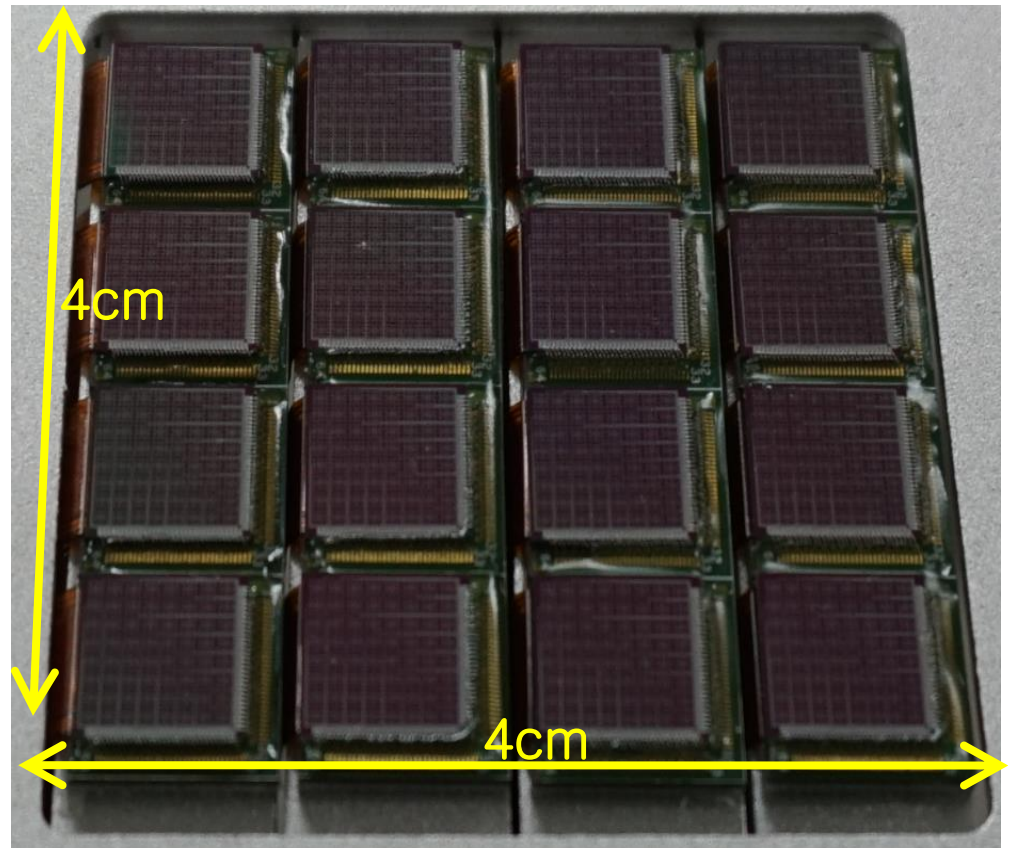
16개의 8 x 8 SiPM 픽셀 어레이로 구성된 다화소 (1024-ch)

- ◆ 1단계 SiPM 픽셀 1024ch 제작
: 1 x 1 mm² 크기
(30x30μm² 크기, 10³개의 마이크로 픽셀)

- ◆ 64ch SiPM 소자 : 1 x 1 cm²

1024-ch

항복전압 균일
->
Multi channel test



1024-ch SiPM + 신호처리장치 + Pinhole

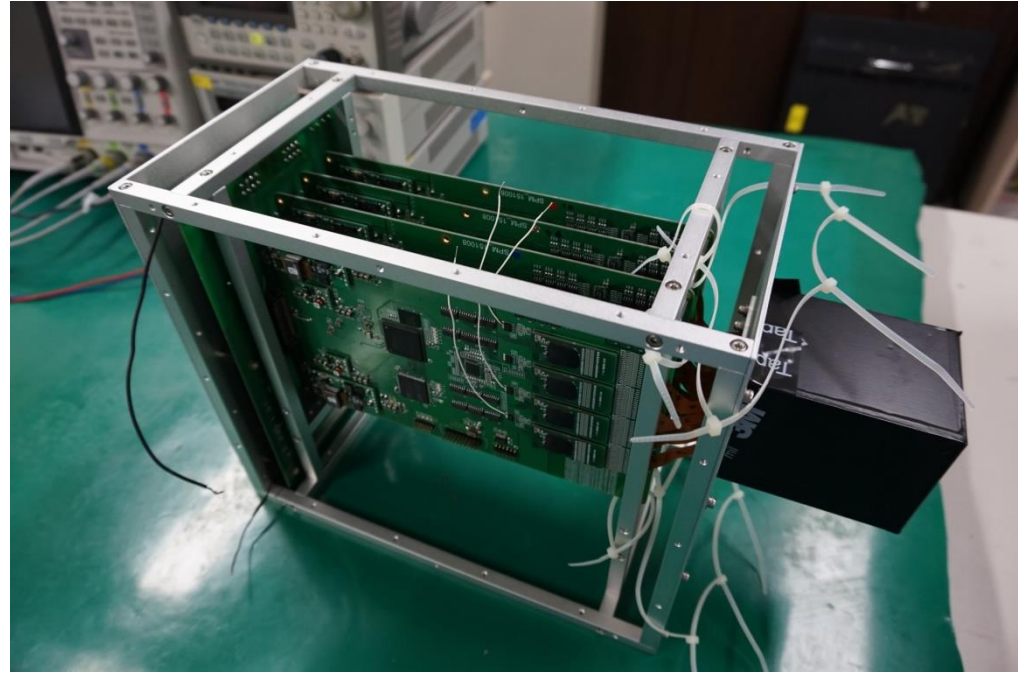
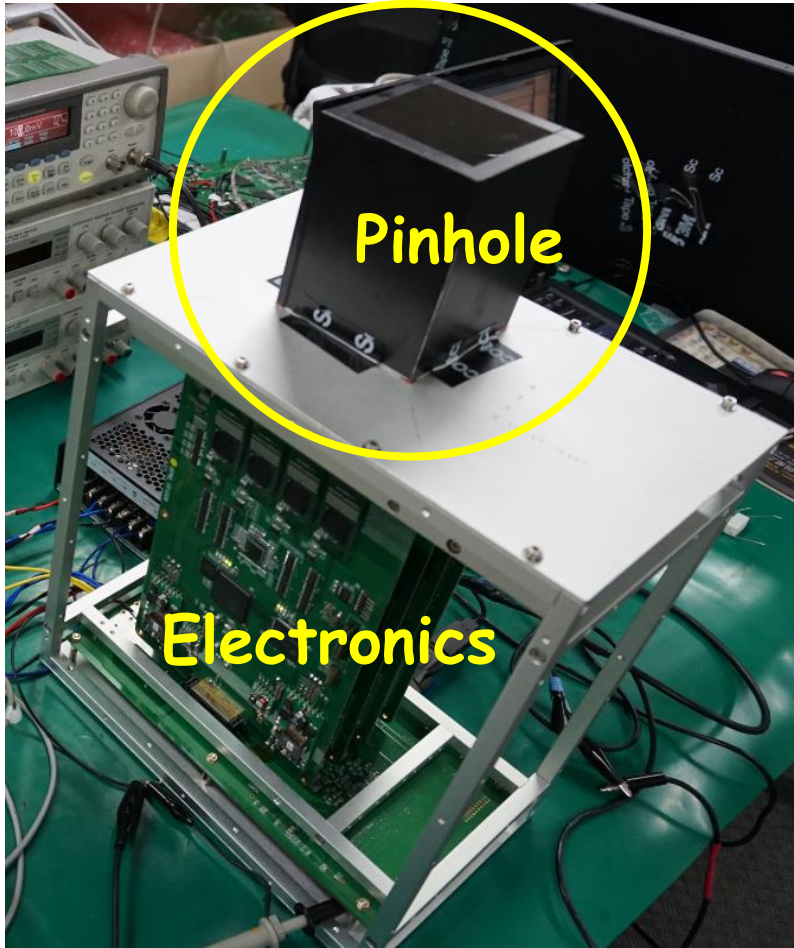
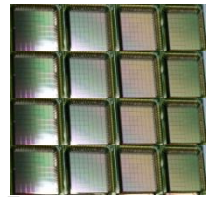
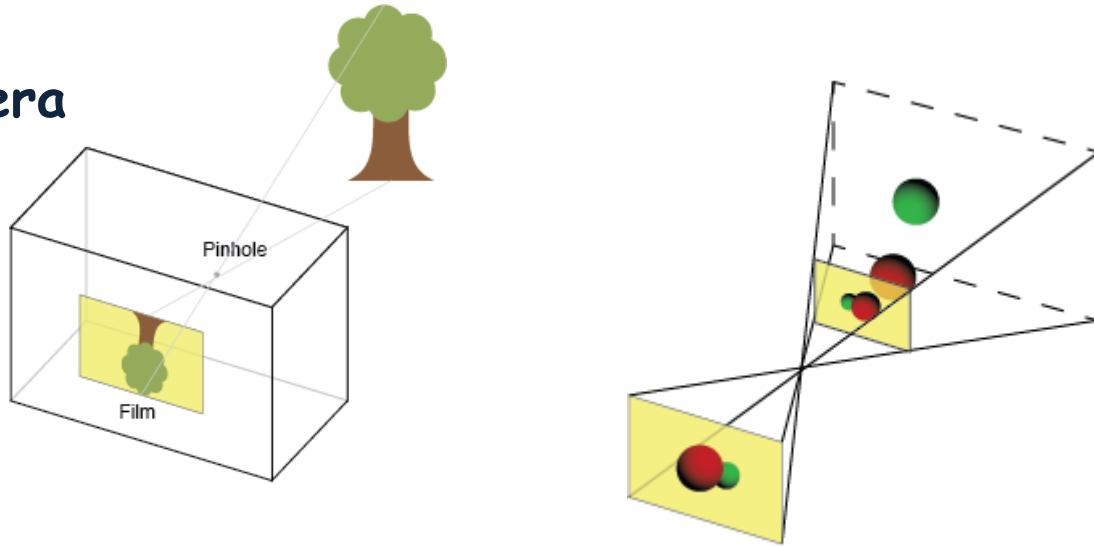


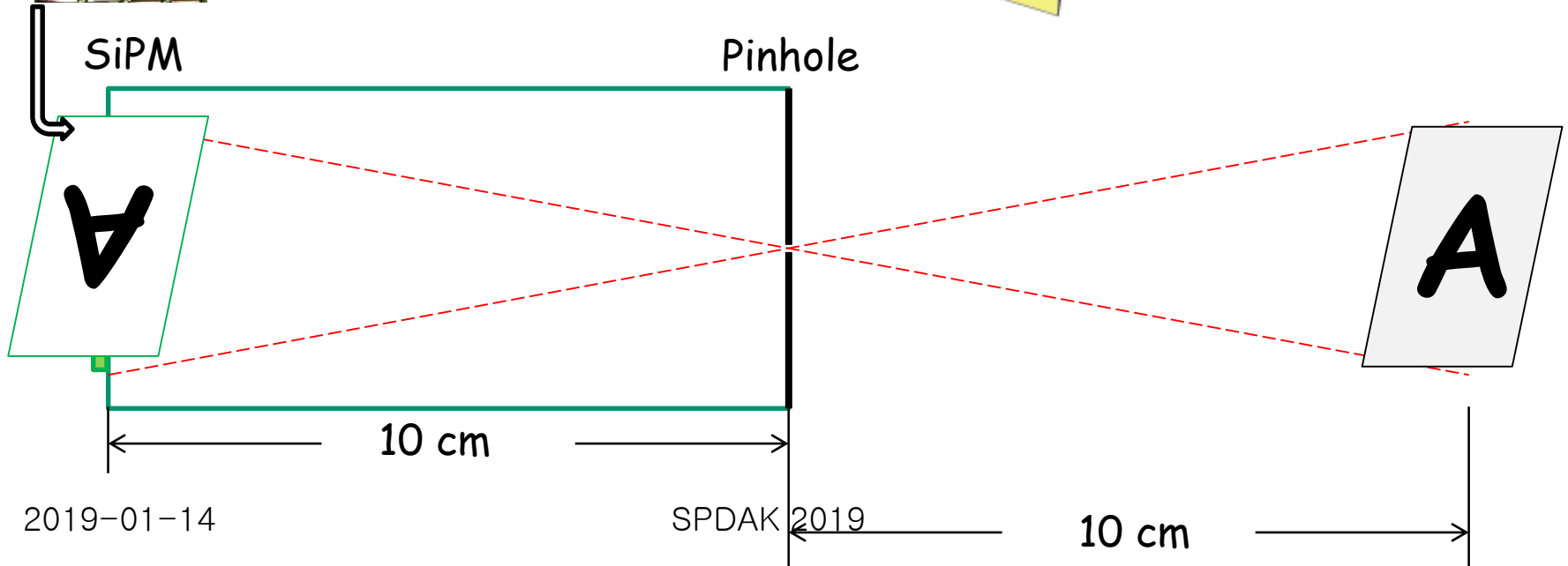
Image Test

Pinhole Camera



SiPM

Pinhole



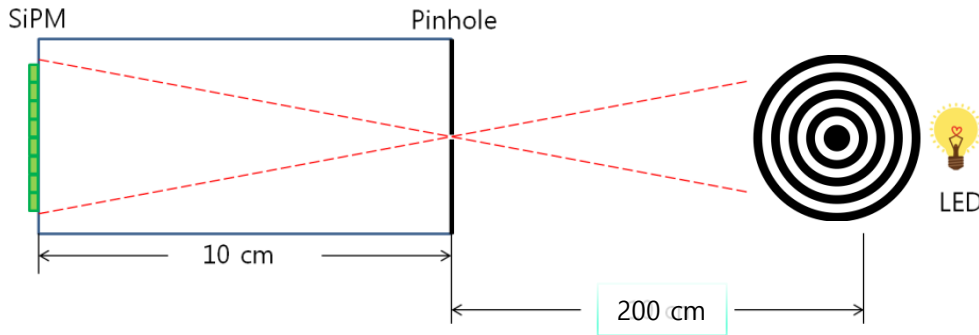
2019-01-14

SPDAK 2019

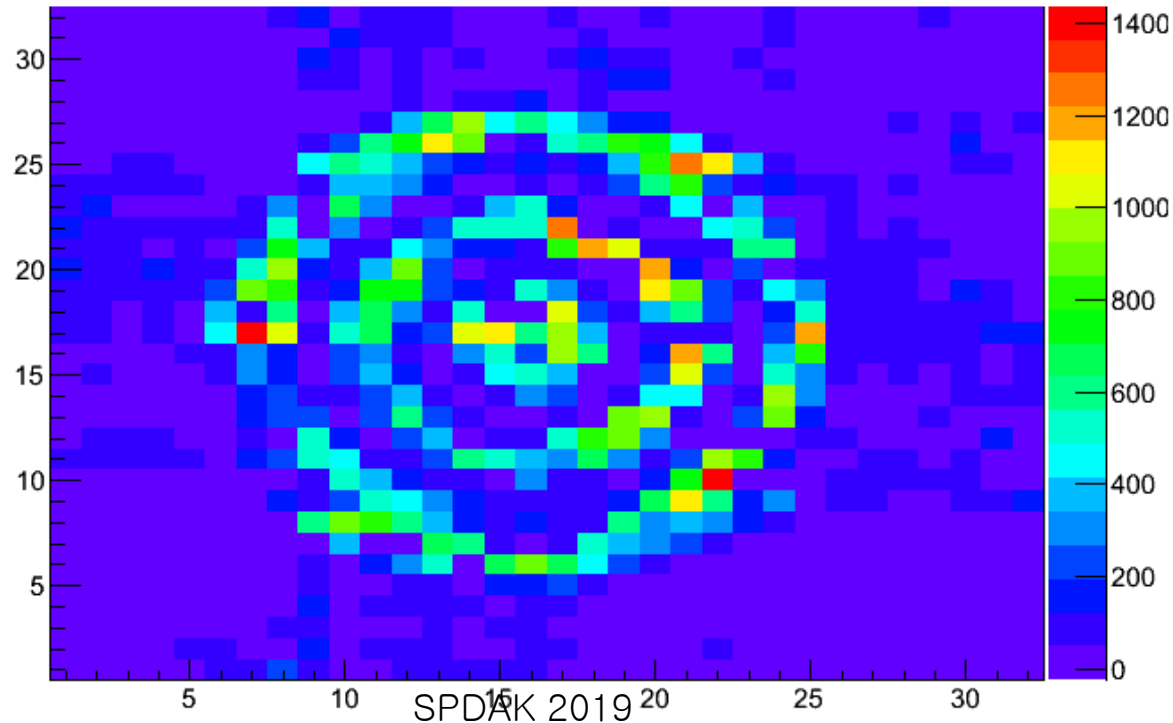
10 cm

Image Test

Pinhole Camera

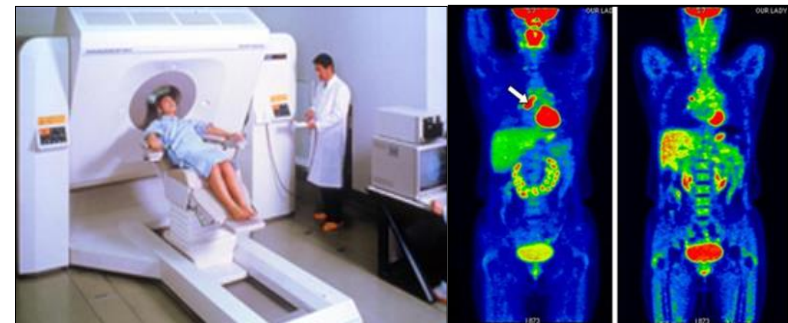
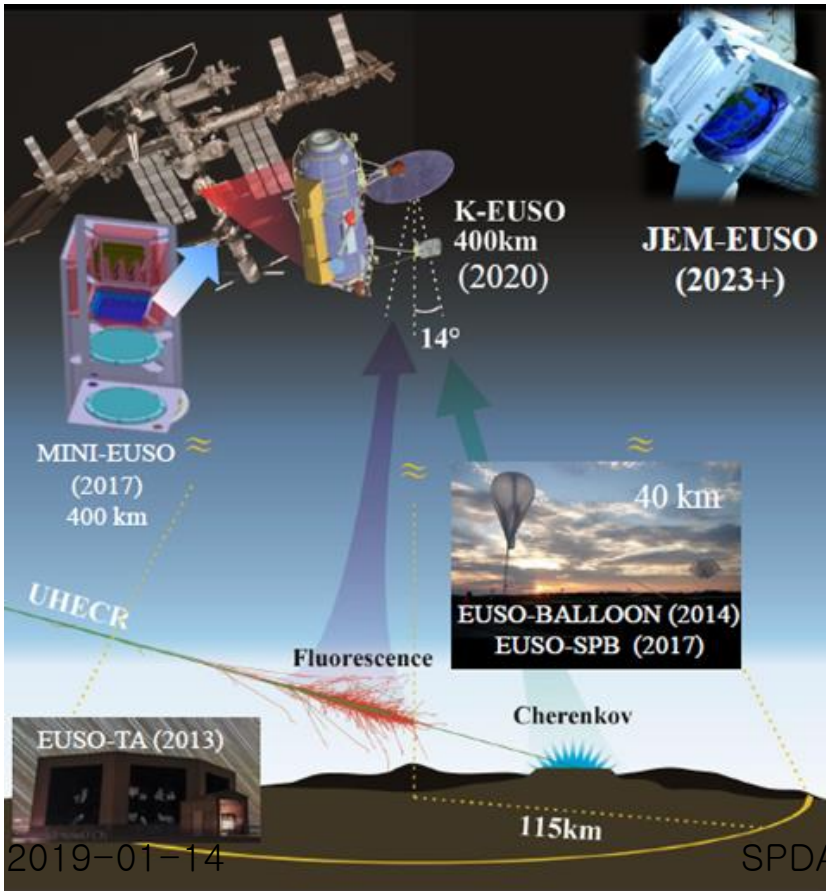


Absolutely Dark!
CCD or CMOS cameras
can NOT get this image!



SiPM Applications

- 천체/천문: 미약한 광신호 측정을 위한 광센서
- 보안 감시 : Homeland Security
- 의료용 : PET Scanners, Medical imaging



5. Summary

Summary

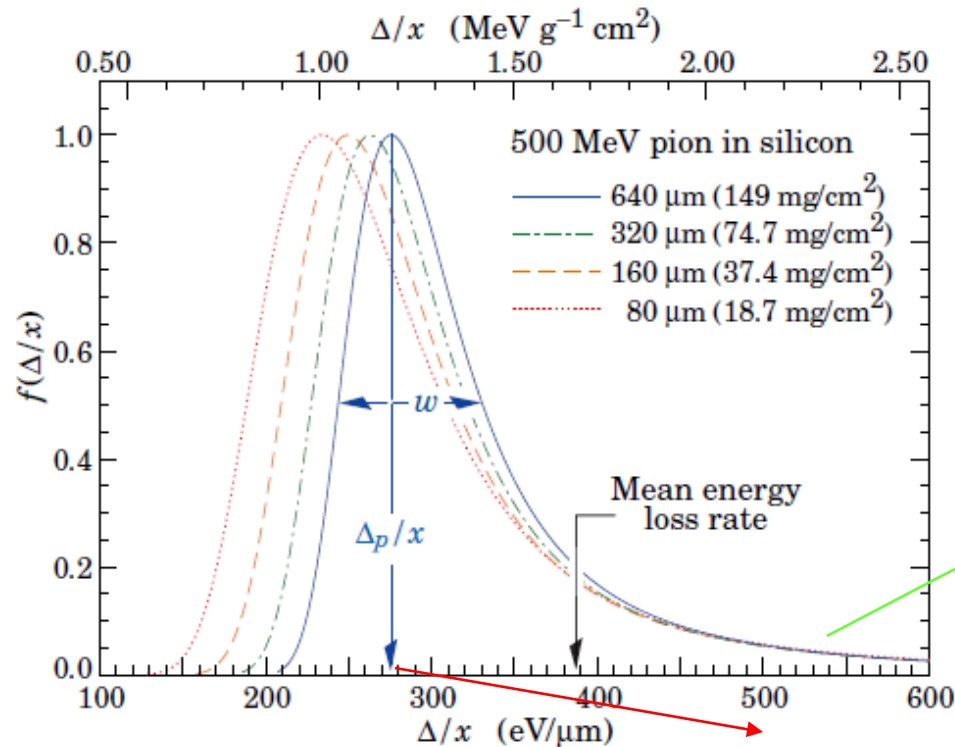
- Silicon is one of most popular material for radiation detection in the fields of Particle physics/Astro-particle physics
 - Charged particle detection
 - Photon detection
- During Lab, try to understand
 - C-V & I-V characteristics of silicon detectors
 - Responses (signals) of silicon detector to radiation sources or cosmic muons)
 - Signal as a function of V_{bias} ?

Back-up slides

dE/dx is of random nature

From Review of Particle Physics

Probability density function ~ Landau Function



Due to δ rays: Knock-on electrons

Most probable dE/dx

Landau function

$$f_L(\lambda) = 1/\pi \int_0^\infty du \exp[-u(\ln u + \lambda)] \sin \pi u$$

Absorption Coefficient

