

# Introduction to Silicon Detectors

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First School for Particle Detectors and Applications  
SPDAK 2019

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# Outline

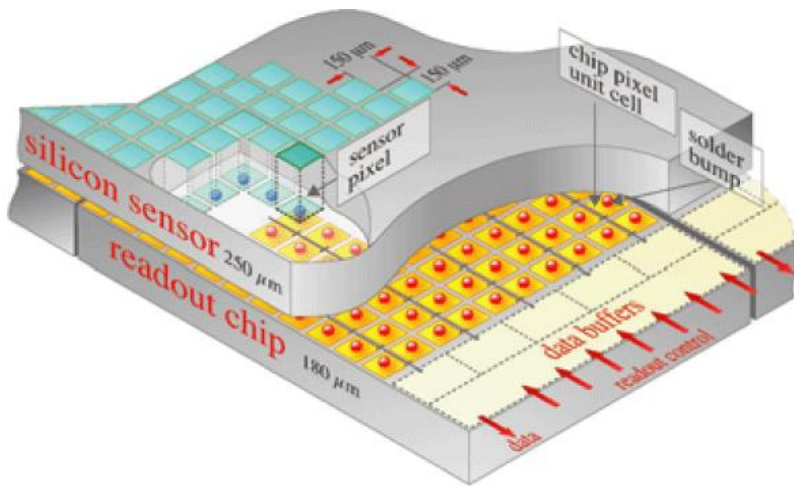
1. Introduction
  - Types of silicon detectors
  - Interaction of particles with silicon
2. Properties of silicon
3. Silicon detectors for charged particle detection
4. Silicon detectors for photon detection
5. Summary

# 1. Introduction

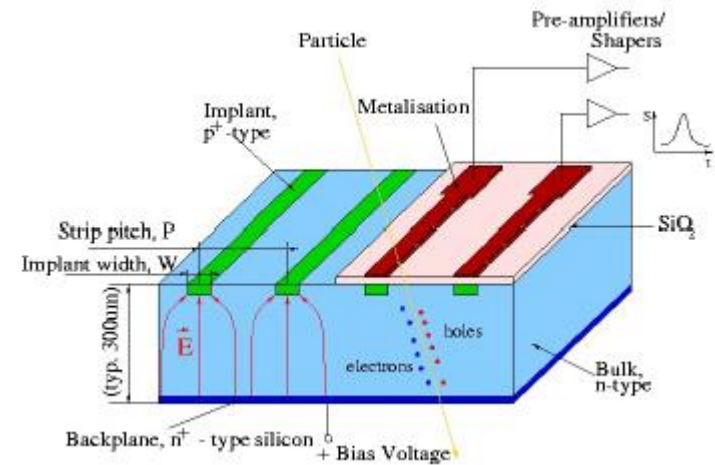
# Types of Silicon Detectors

[http://hep.fi.infn.it/CMS/sensors/Silicon\\_Detector.gif](http://hep.fi.infn.it/CMS/sensors/Silicon_Detector.gif)

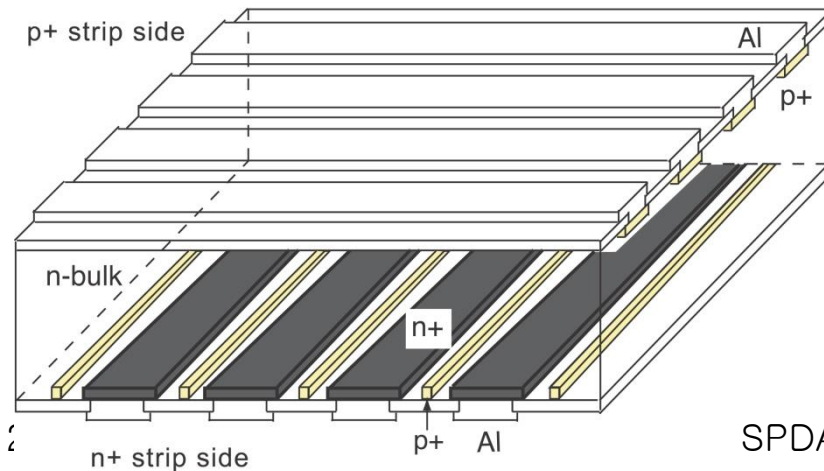
## Pixel sensor for CMS



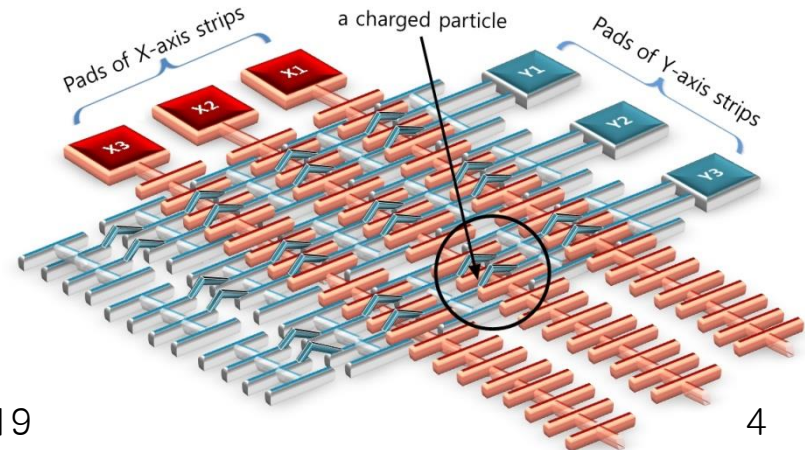
## Single-side strip sensor



## Double-side strip sensor

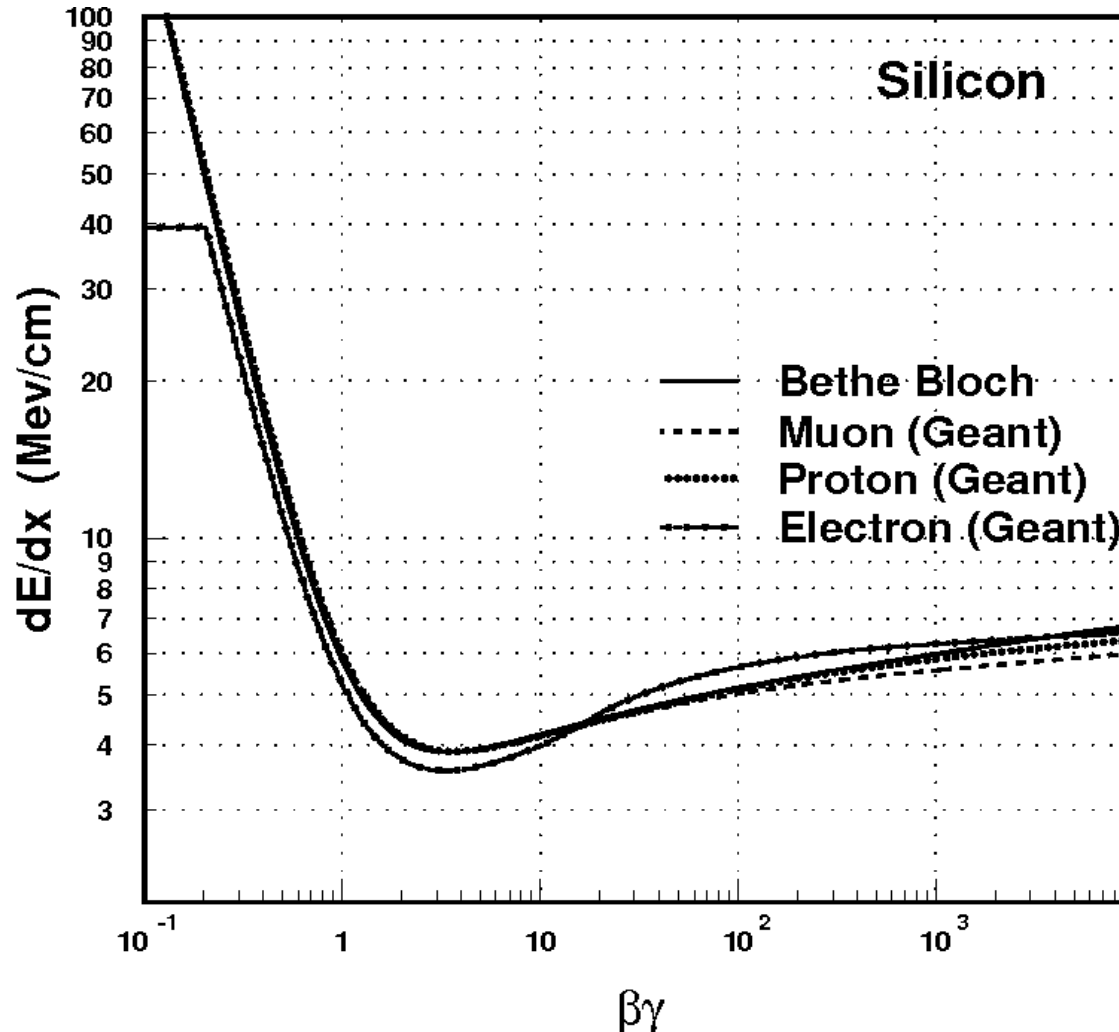


## Strip-pixel sensor



# Interaction of charged particles with silicon

By S. Banerjee & A. Caner



# Energy loss by ionization

$z$ : charge of incident particle

Bethe equation

$$\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

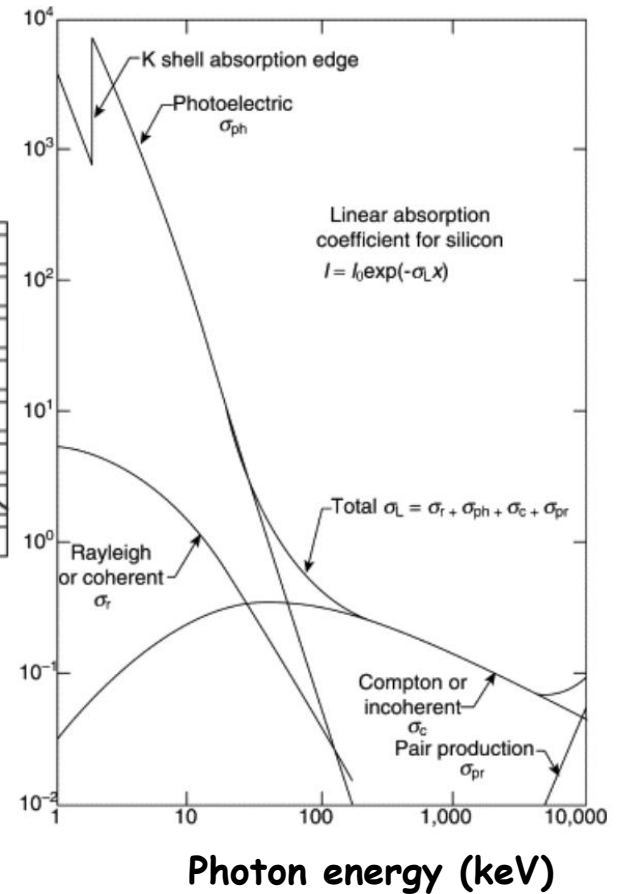
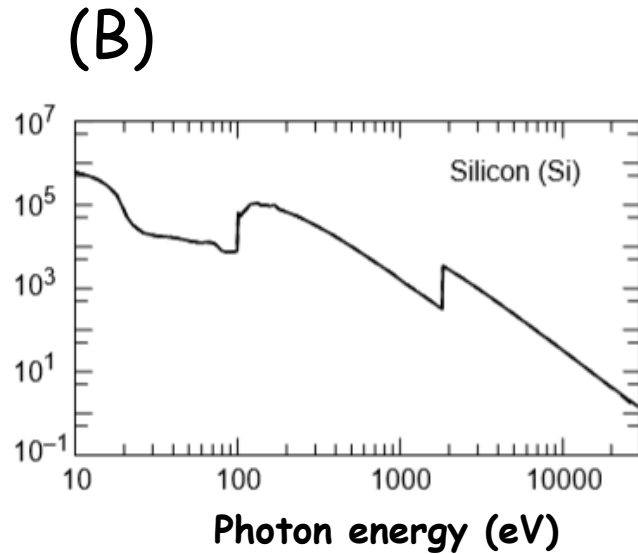
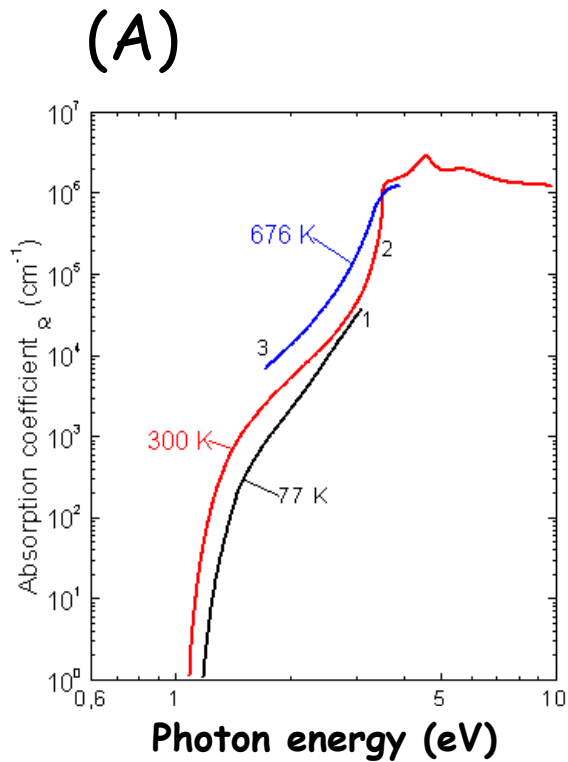
$$\left\langle \frac{dE}{dx} \right\rangle \propto z^2$$

$\left\langle \frac{dE}{dx} \right\rangle \approx 40 \text{ keV} / 100 \text{ } \mu\text{m}$  in Si for minimum ionizing particles

3.6 eV required for producing a pair of e-h in Si  
 $\approx 10,000$  e-h pairs / 100  $\mu\text{m}$  expected in Si

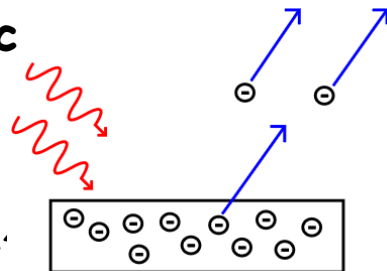
# Interaction of photons with silicon

(C)



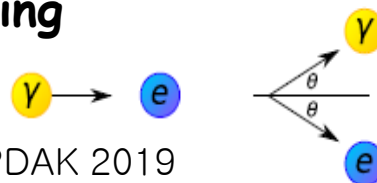
Photoelectric effect

2019-01-1

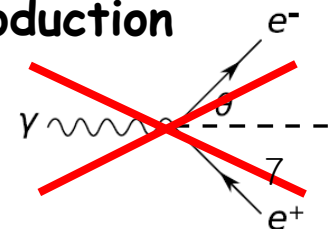


Compton scattering

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Pair production



# References for the plots in Page 6

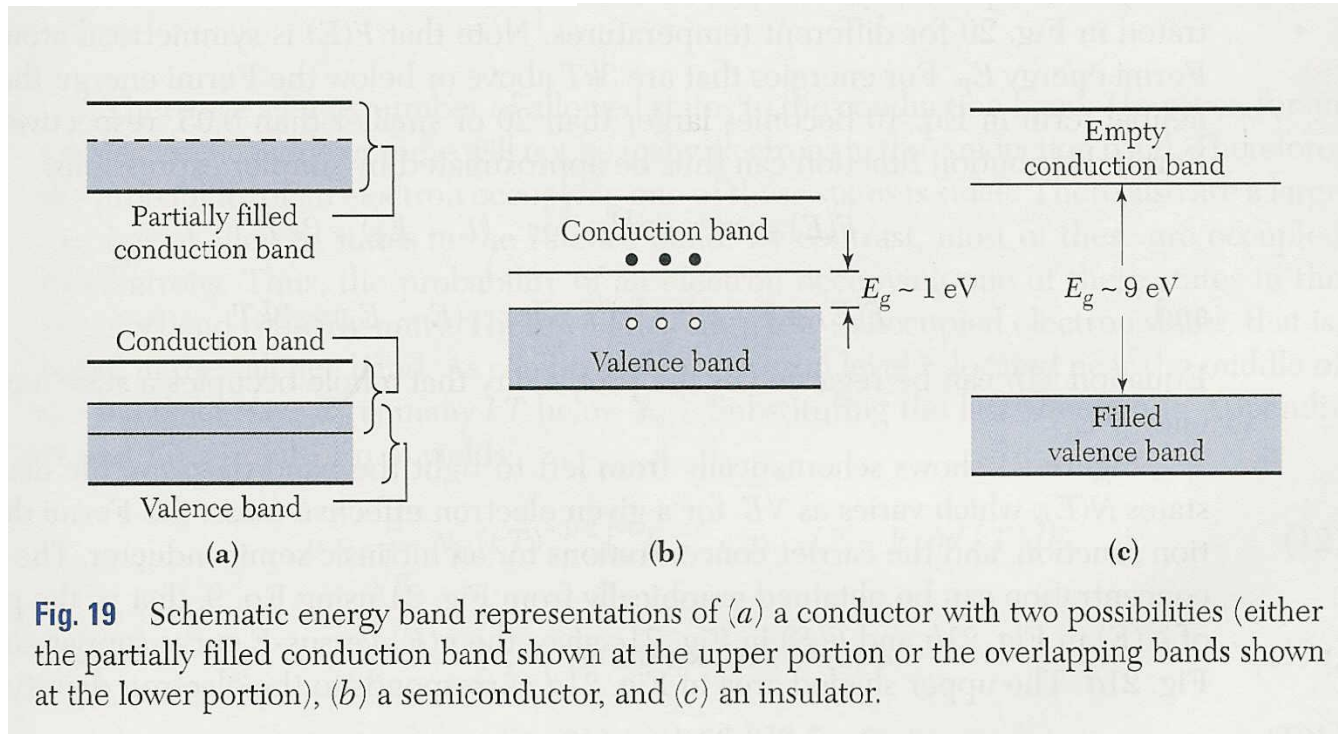
- A. Sze, S. M., *Physics of Semiconductor Devices*, John Wiley and Sons, N.Y., 1981. Jellison, Jr., G. E. and F. A. Modine, *Appl. Phys. Lett*- 41, 2 (1982) 180-182.
- B. X-RAY DATA BOOKLET, Lawrence Berkeley National Laboratory
- C. Durini (Editor), "High Performance Silicon Imaging: Fundamentals and Applications of CMOS and CCD Sensors", Woodhead Publishing, 2014 Particularly: Chapter 10 (p286) by R. Turchetta, STFC, UK



## **2. Properties of silicon**

# Band & bandgap

Isolated atoms brought together to form lattice  $\rightarrow$  discrete atomic levels shift to form energy bands



**Fig. 19** Schematic energy band representations of (a) a conductor with two possibilities (either the partially filled conduction band shown at the upper portion or the overlapping bands shown at the lower portion), (b) a semiconductor, and (c) an insulator.

From 'Semiconductor Devices  
Physics and Technology Second Edition'  
by S.M. Sze

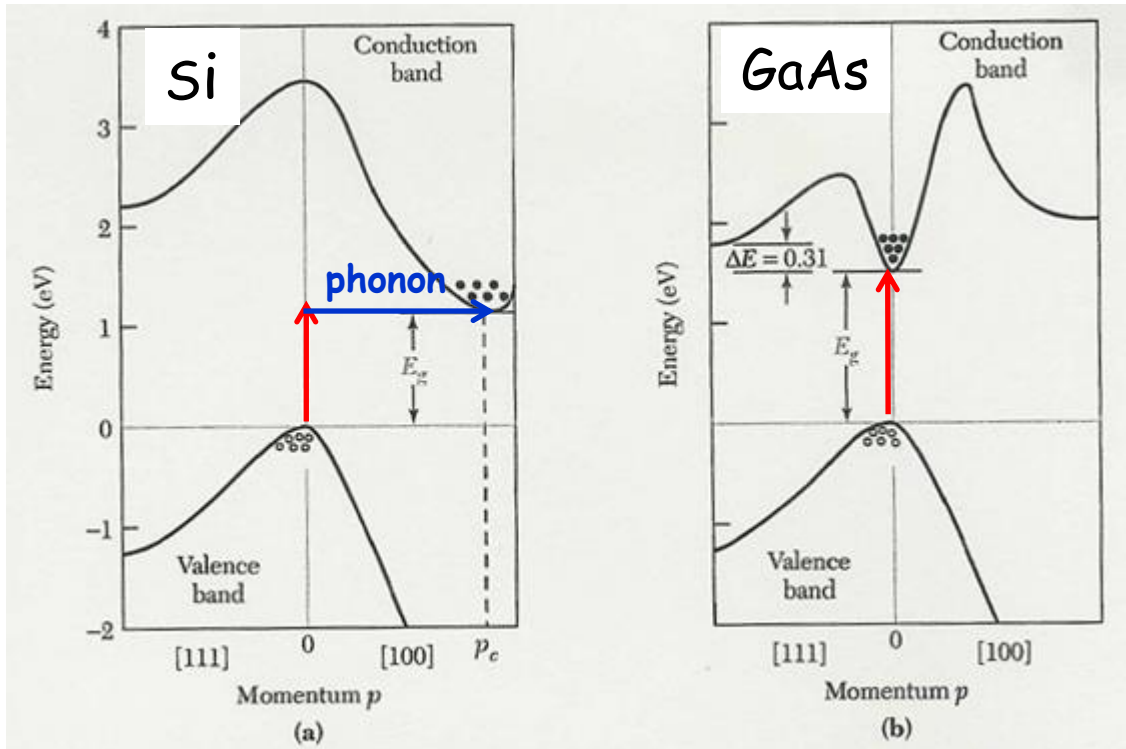
$E_g$ : band gap (1.12 eV for Si)  
Note:  $kT \sim 0.026 \text{ eV}$  at room temp.

# Indirect vs Direct Bandgap Semiconductors

From 'Semiconductor Devices  
Physics and Technology  
Second Edition'  
by S.M. Sze

Indirect bandgap

Direct bandgap



Excitation/De-excitation =  $E_g + E_{\text{phonon}}$

Excitation/De-excitation =  $E_g$

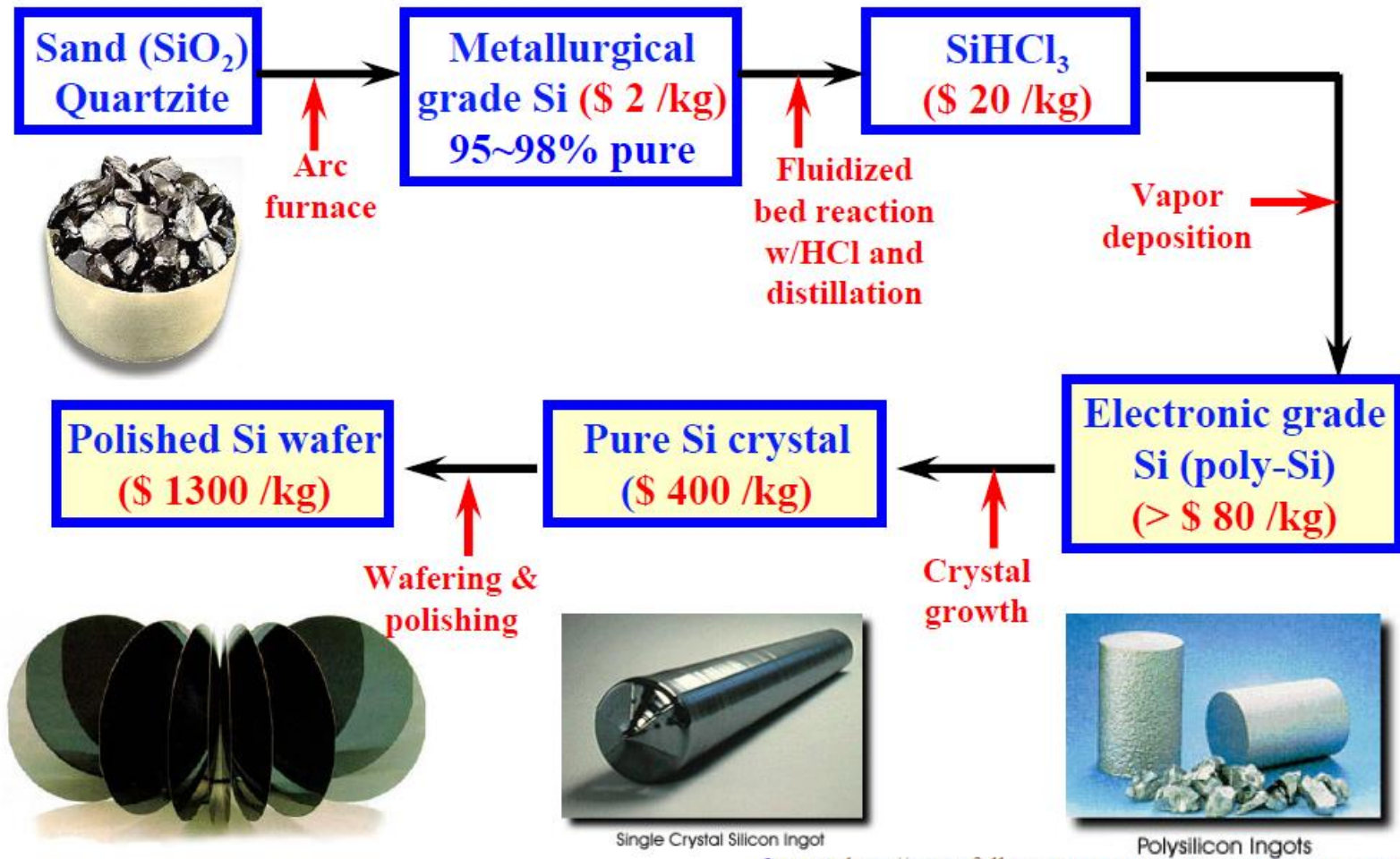
# Why Silicon?

- abundant --> cheap
- Lighter
- $\text{SiO}_2$  layer
  - Naturally or inexpensively formed
  - chemically and mechanically very stable
  - effectively passivates the surface states of the underlying silicon
  - forms an effective diffusion barrier for the commonly used dopant species
  - easily preferentially etched from the silicon, and vice versa, with high selectivity
  - By contrast,  $\text{GeO}_2$  is a chemically unstable, poor electrical insulator that is 33 times more soluble in water than  $\text{SiO}_2$ , making it less suited to the photolithographic and wet chemical processes used to fabricate integrated circuits.

III	IV	V
5 B	6 C	
13 Al	14 Si	15 P
31 Ga	32 Ge	33 As
49 In	50 Sn	51 Sb

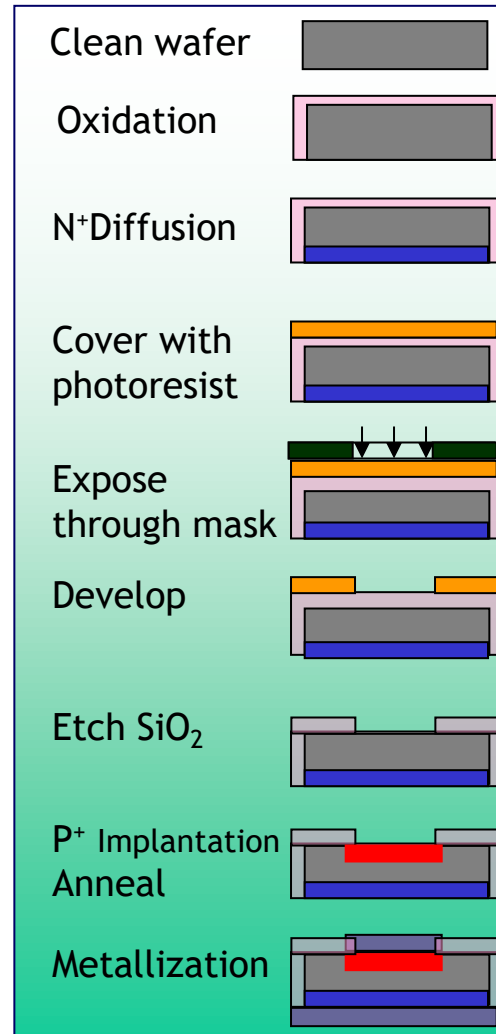
Acceptors      Semiconductors      Donors

# Sand to silicon wafer

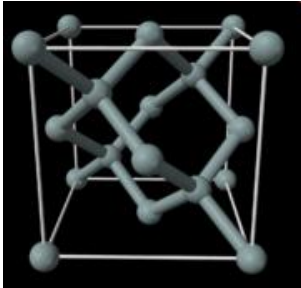


Source: <http://www.fullman.com/semiconductors/semiconductors.html>

# Recipe for fabrication process

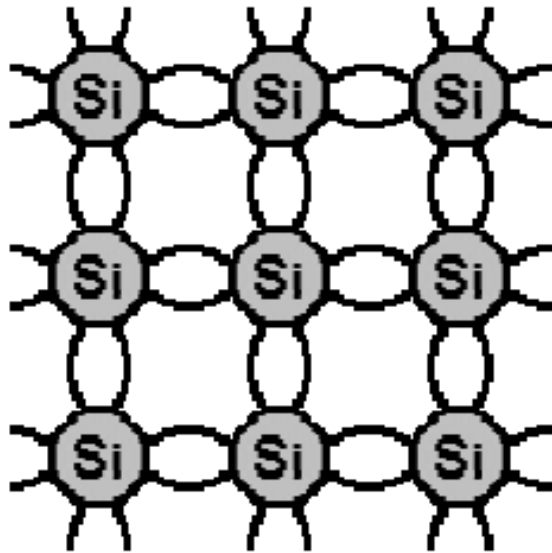


# Intrinsic Si semiconductor

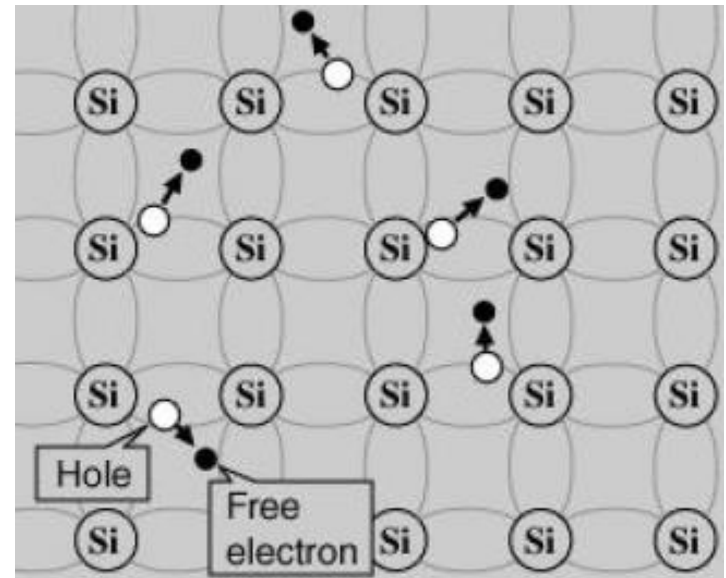


The crystalline structure is *Diamond Cubic* (FCC). Bare wafers of  $\langle 100 \rangle$  or  $\langle 111 \rangle$  crystals are popular ones used for silicon detector fabrications.

low T : electrons bound in lattice



higher T : free electrons & holes



# Impurities

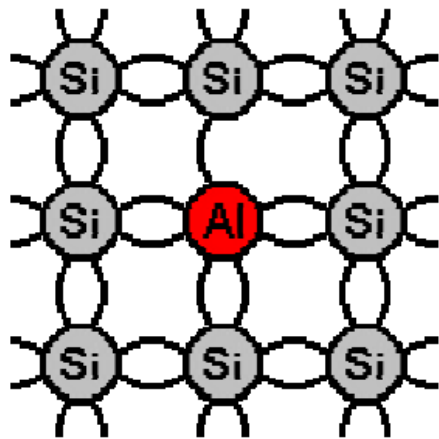
- Intrinsic semiconductor = pure, no impurities.
- Extrinsic semiconductor = impurities added.
- Some impurities always present.
- Turns out to be extremely useful to add impurities to control the properties of the semiconductor.

## Jargons

- The heavily-doped pieces are called  $n^+$ -type or  $p^+$ -type; the lightly-doped pieces, simply n-type or p-type.

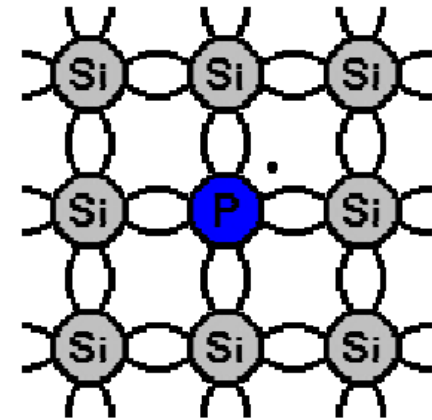


# Doping: acceptors & donors



III	IV	V
5 B	6 C	
13 Al	14 Si	15 P
31 Ga	32 Ge	33 As
49 In	50 Sn	51 Sb

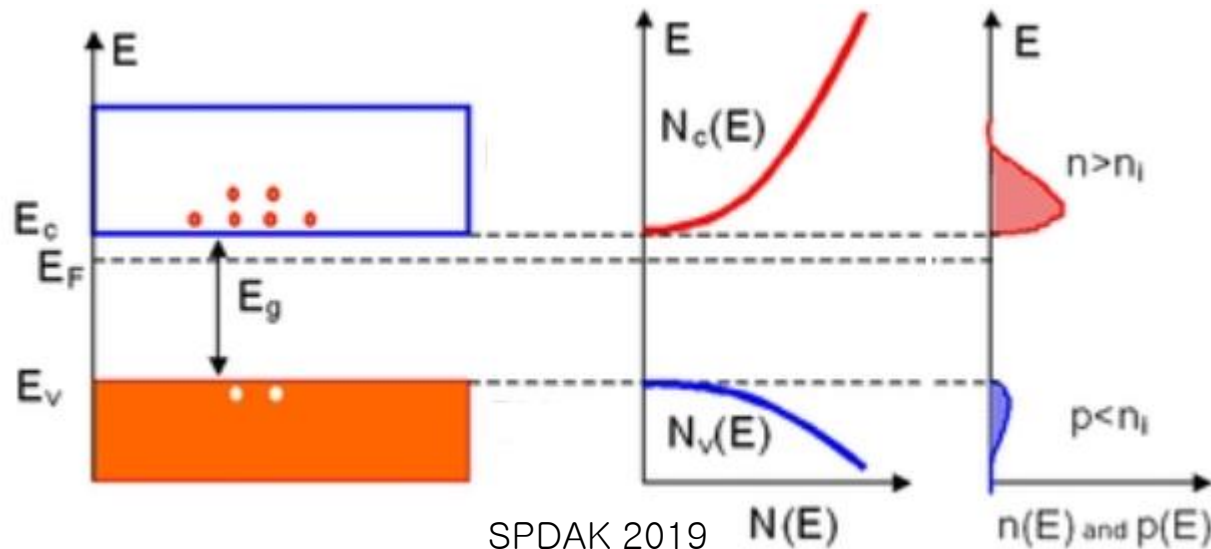
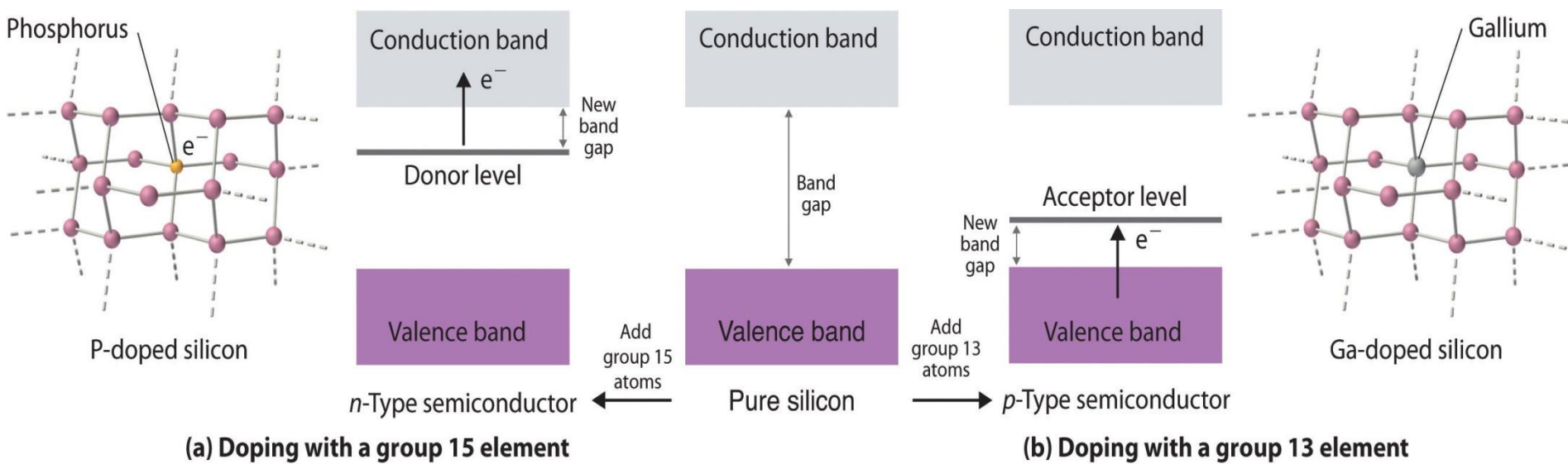
Acceptors                      Semiconductors                      Donors



- Al or B impurities.
- 3  $e^-$  in outer shell
- 3  $e^-$  for bonds, one hole left-over (free)
- Acceptor impurity
- P-type silicon

- P or As impurities.
- 5  $e^-$  in outer shell.
- 4  $e^-$  for bonds, one  $e^-$  left-over (free).
- Donor impurity
  - (donates  $e^-$ )
- N-type silicon

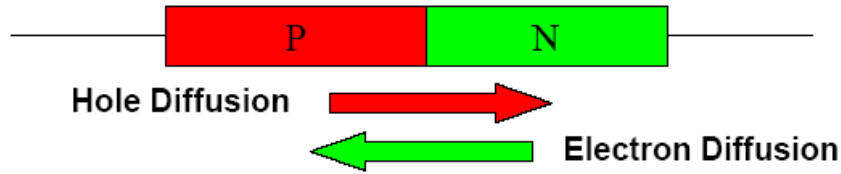
# Effect of doping



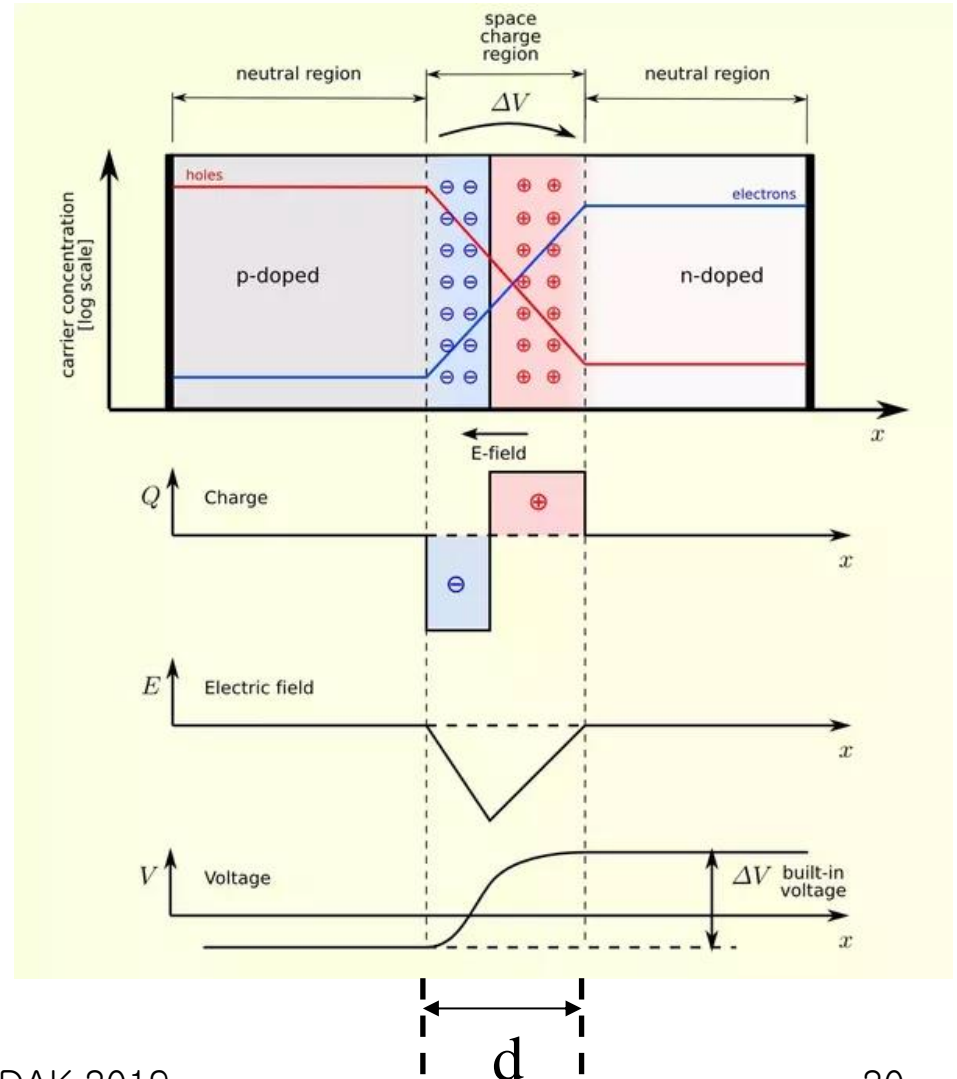
### **3. Silicon detectors for charged particle detection**

# p-n junction (fundamental structure)

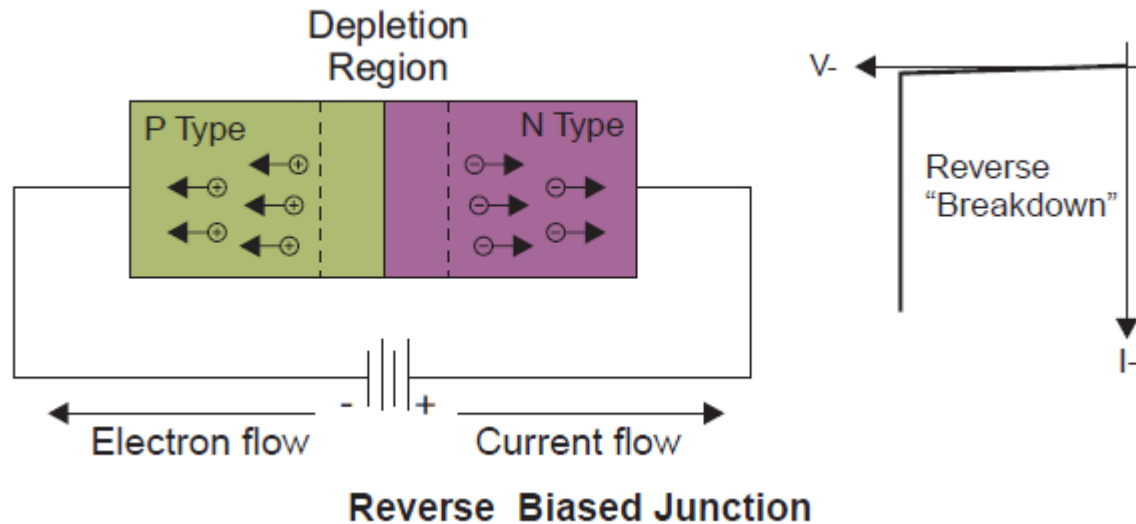
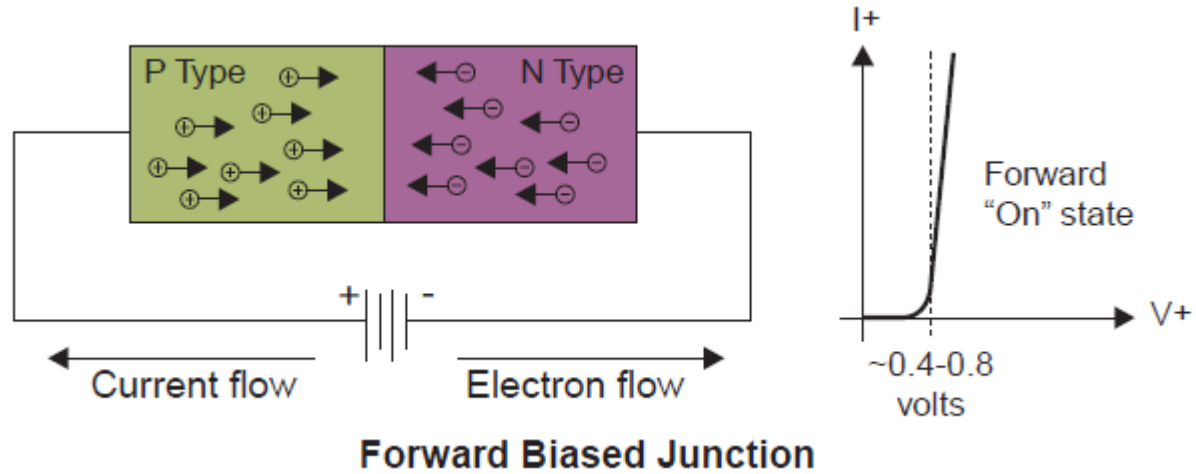
Bring p-type and n-type into contact:



The depletion region  $d$  is a region with no charge carriers (with no free charges).



# p-n junction



# Depletion depth

$$d = \sqrt{\frac{2\epsilon}{e} \frac{N_A + N_D}{N_A N_D} (V_{bi} + V)}$$

$V_{bi}$  : potential difference due to barrier field

$$d = \sqrt{\frac{2\epsilon(V_{bi} + V)}{eN_B}}$$

In many cases,  $N_A \gg N_D$  or  $N_D \gg N_A$   
 $N_B$  is the smallest of  $N_D$  and  $N_A$

$$d = \sqrt{2\epsilon\mu\rho(V_{bi} + V)}$$

An exercise :

intrinsic Si at 300K

$$\rho = 3.3 \times 10^5 \Omega \text{ cm}$$

$$V \sim 110 \text{ V}$$

$$d \sim 300 \mu\text{m}$$

$$d = 0.5 \mu\text{m} \sqrt{\rho(V_{bi} + V)} \quad (\text{n-type})$$

$$d = 0.3 \mu\text{m} \sqrt{\rho(V_{bi} + V)} \quad (\text{p-type})$$

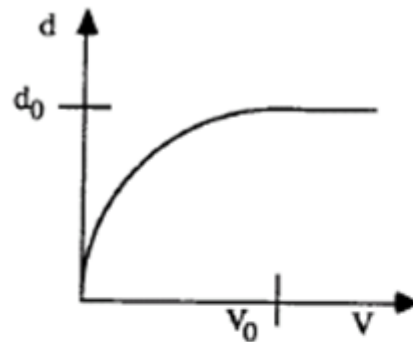
(V in Volts and  $\rho$  in  $\Omega\text{cm}$ ) for Si

# p-n junction reverse bias characteristics

$d$  = depletion layer depth

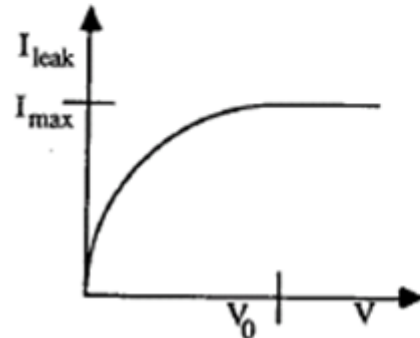
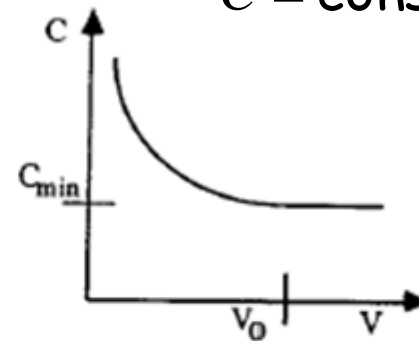
$$d \propto \sqrt{V} \text{ for } V < V_0$$

$$d = d_0 \text{ for } V > V_0$$



$$C \propto 1/\sqrt{V} \text{ for } V < V_0$$

$$C = \text{const. for } V > V_0$$



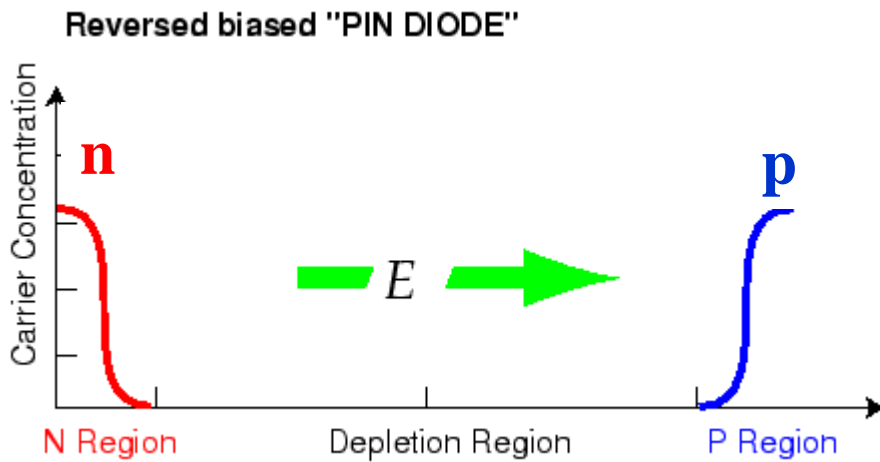
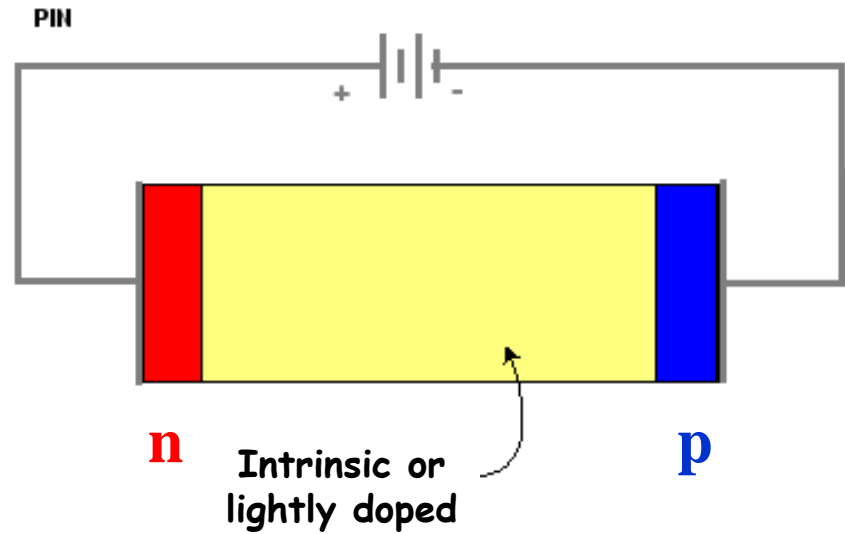
$$i \propto d \propto \sqrt{V} \text{ for } V < V_0$$

$$i = \text{const. for } V > V_0$$

$V_0$  = full depletion voltage

$d_0$  = junction thickness

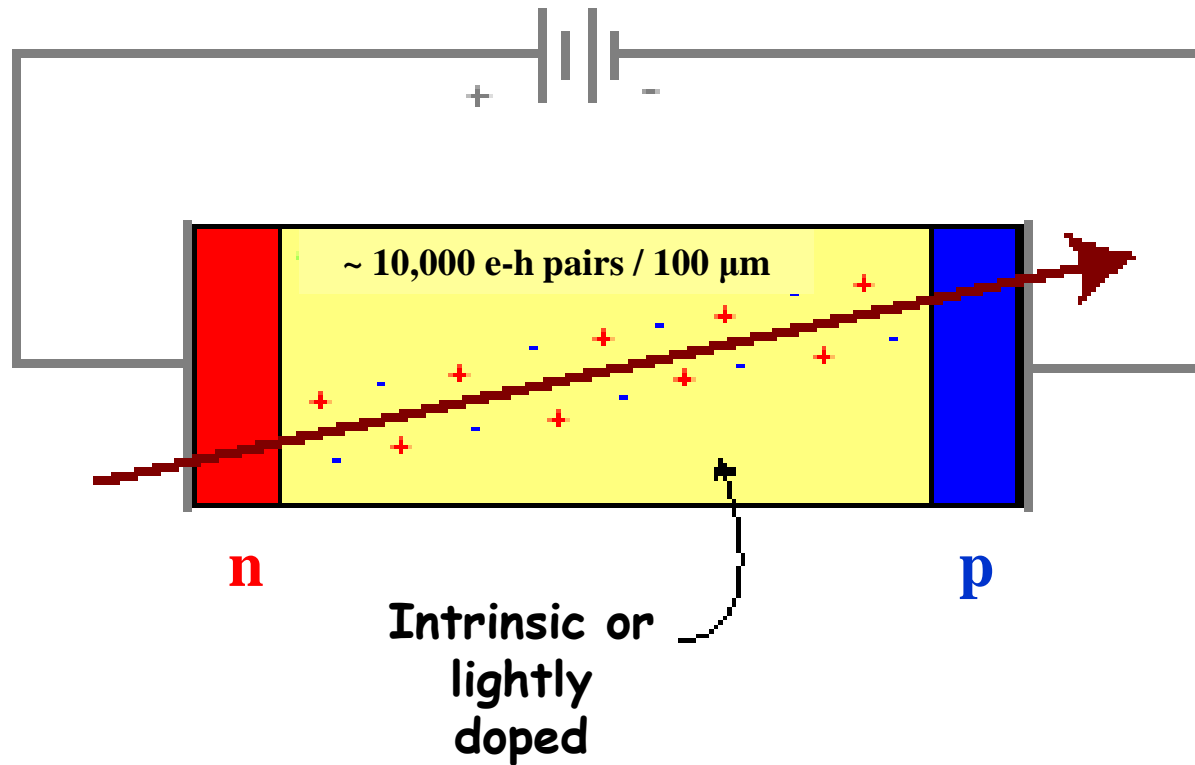
# PIN Diode





# When a charged particle traverses the depletion zone

Simple detector

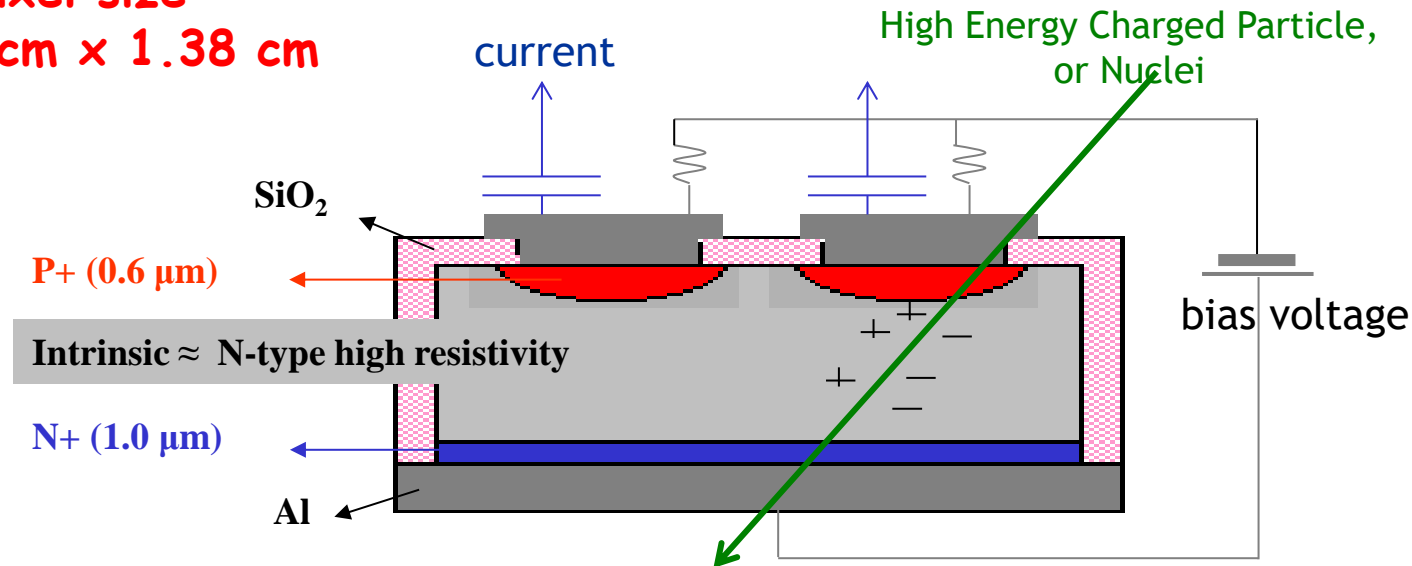


# Silicon pixel sensor

- PIN diode, DC type
- Wafer: 5 inch, 525  $\mu\text{m}$  in thickness, double polished side, N-type high resistivity ( $>5 \text{ k}\Omega\text{-cm}$ ), (111) orientation

pixel size

= 1.55 cm  $\times$  1.38 cm

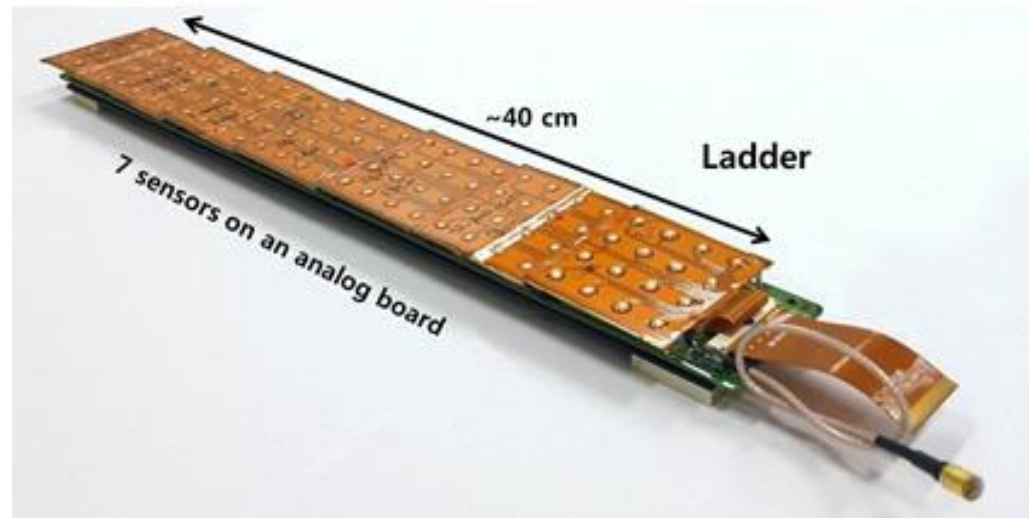
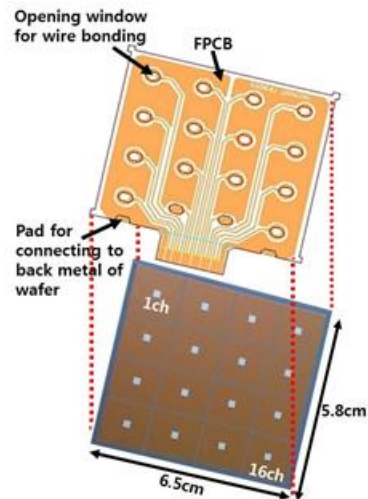


$$\left\langle \frac{dE}{dx} \right\rangle \propto z^2$$

Measure the ionization energy loss in silicon sensor  
-> Determine the charge of the incident particle

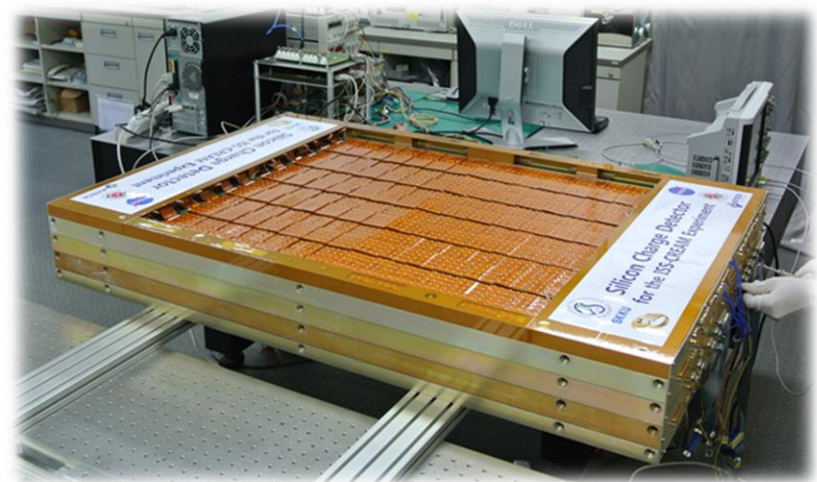
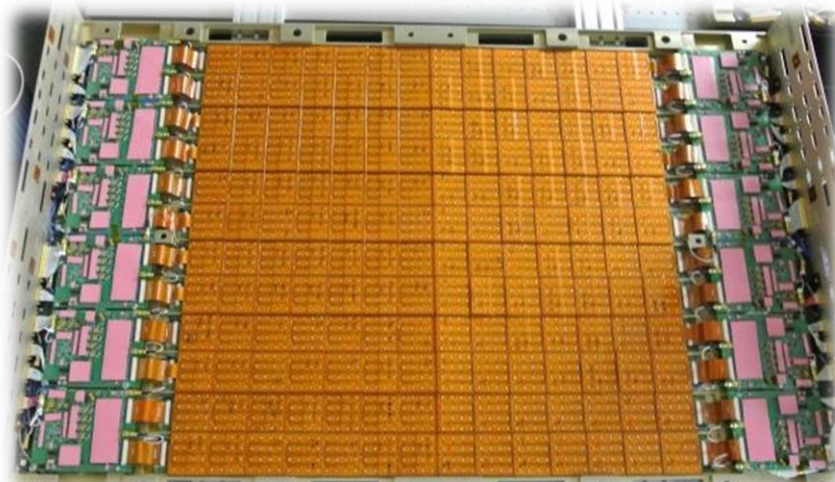
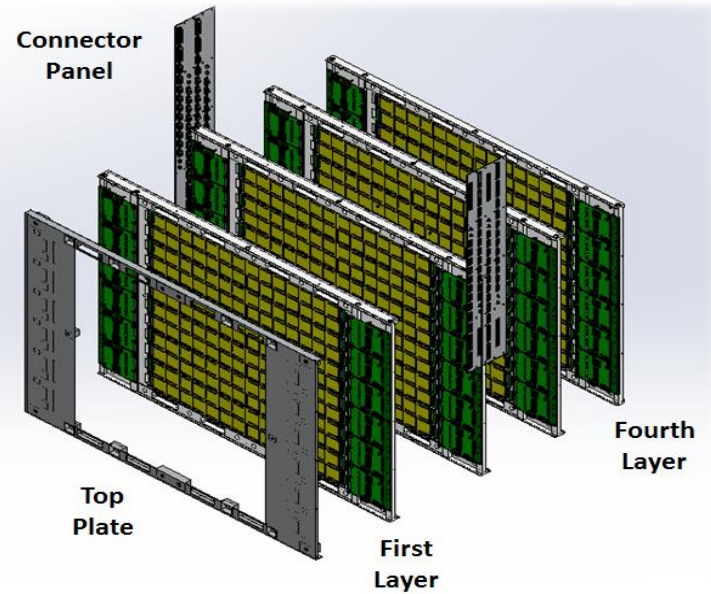
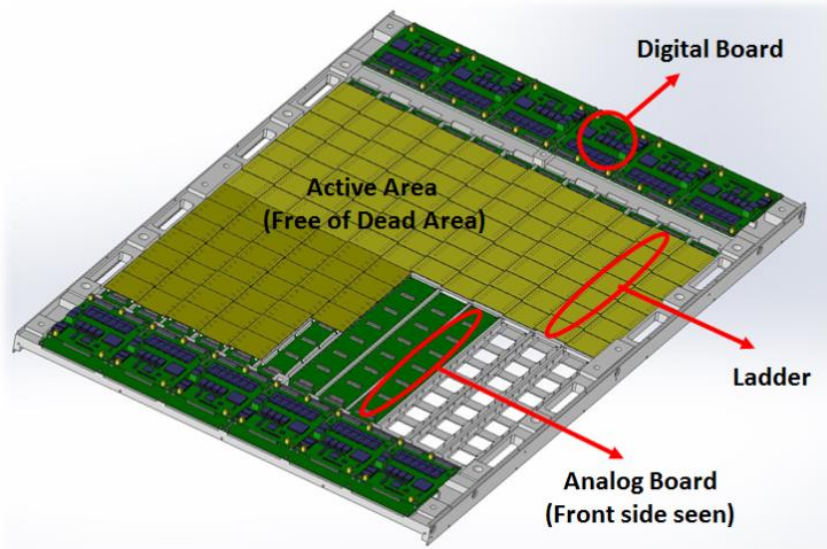
# Silicon Pixel Sensor & Ladder for SCD

Built by SKKU group



pixel size =  $1.55 \times 1.38 \text{ cm}^2$

# Silicon Charge Detector (design, fabrication & assembly) Built by SKKU group

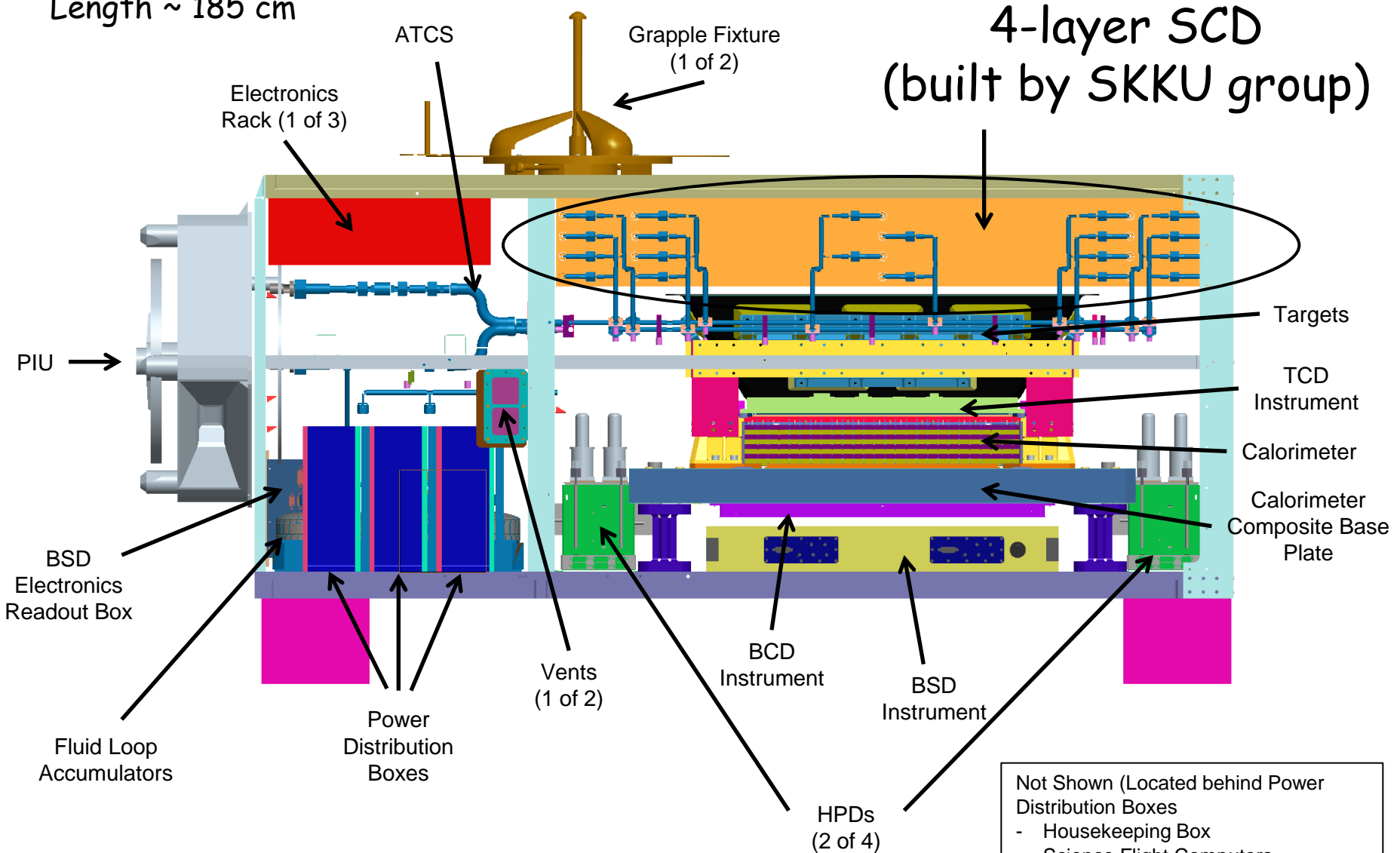


# Silicon Charge Detector (specification)

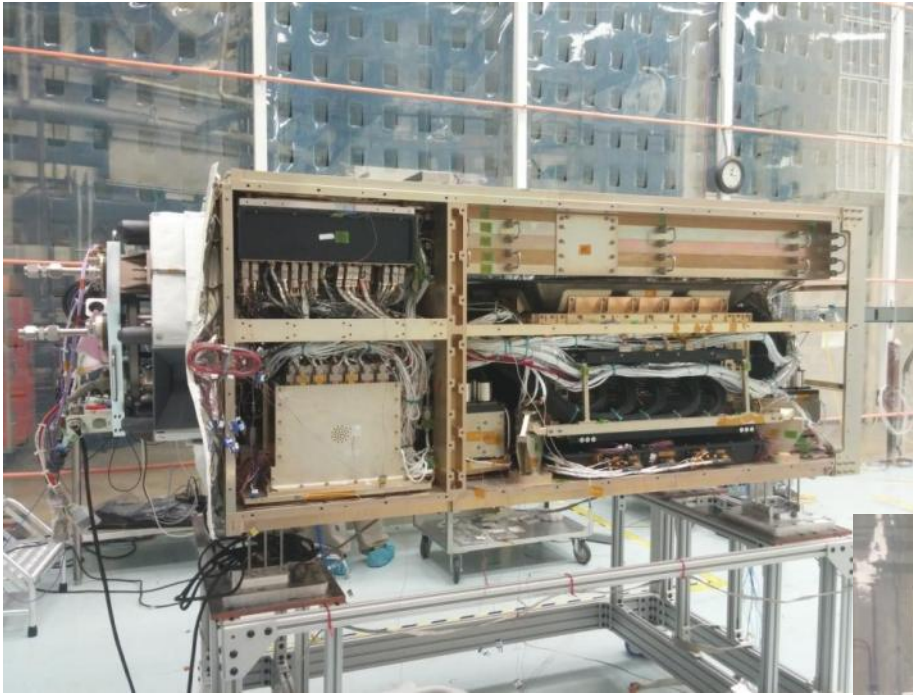
Mass (kg)	143
Overall Dimension (cm <sup>3</sup> )	127.7 (L) x 81.7 (W) x 16.6 (H)
Active Area (cm <sup>2</sup> )	78.2 x 73.6
# Layers	4
# Channels	total 10752 (2688 per layer)
Power Consumption (W)	182.5

Mass ~ 1258 kg  
 Power ~ 415 W  
 Length ~ 185 cm

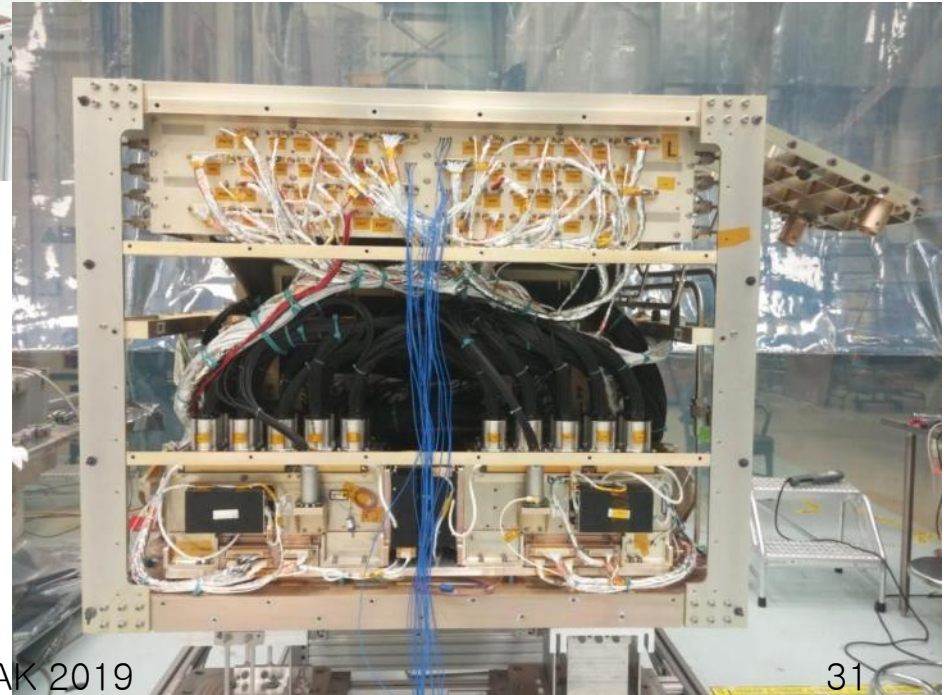
# ISS-CREAM payload



# ISS-CREAM @ GSFC before TVAC test (July 22-25, 2015)



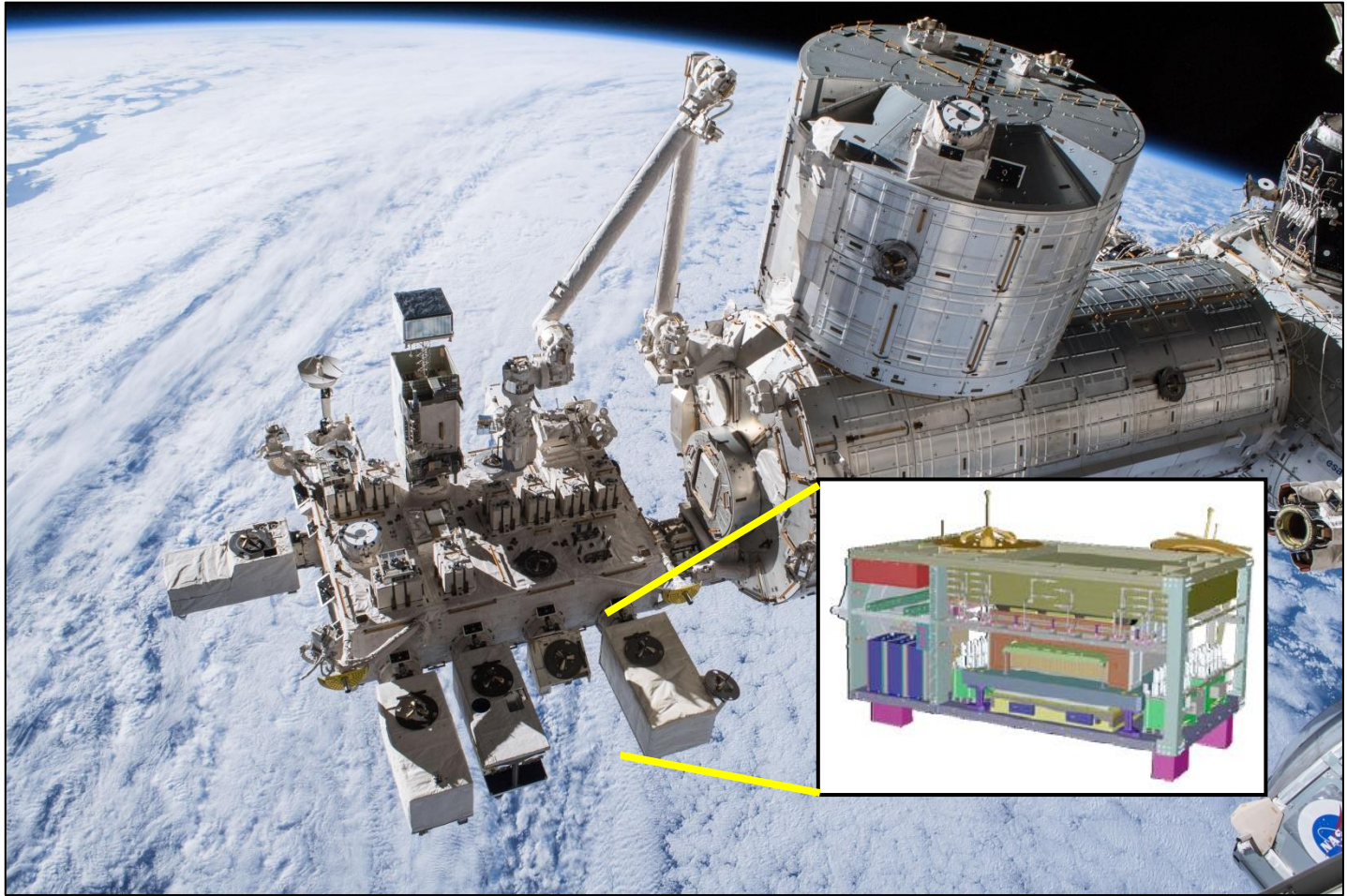
2019-01-14



SPDAK 2019

31

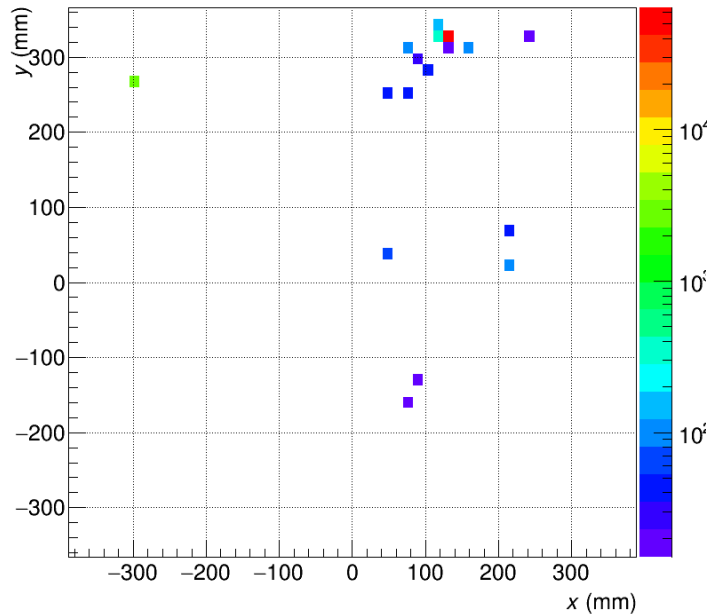
# ISS-CREAM in space operation





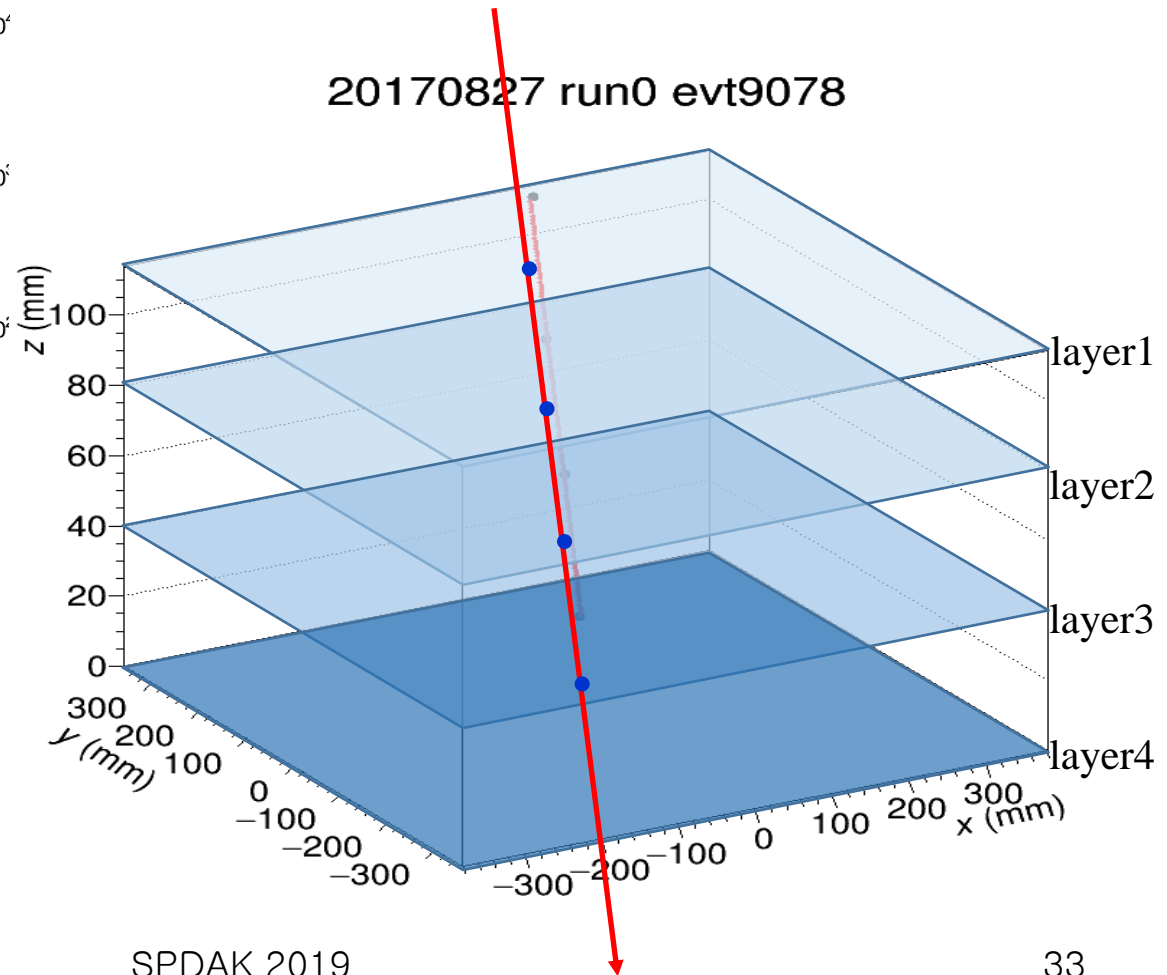
# SCD performance: standalone tracking

20170827 run0 evt9078 layer1



## A 4-layer track!

20170827 run0 evt9078

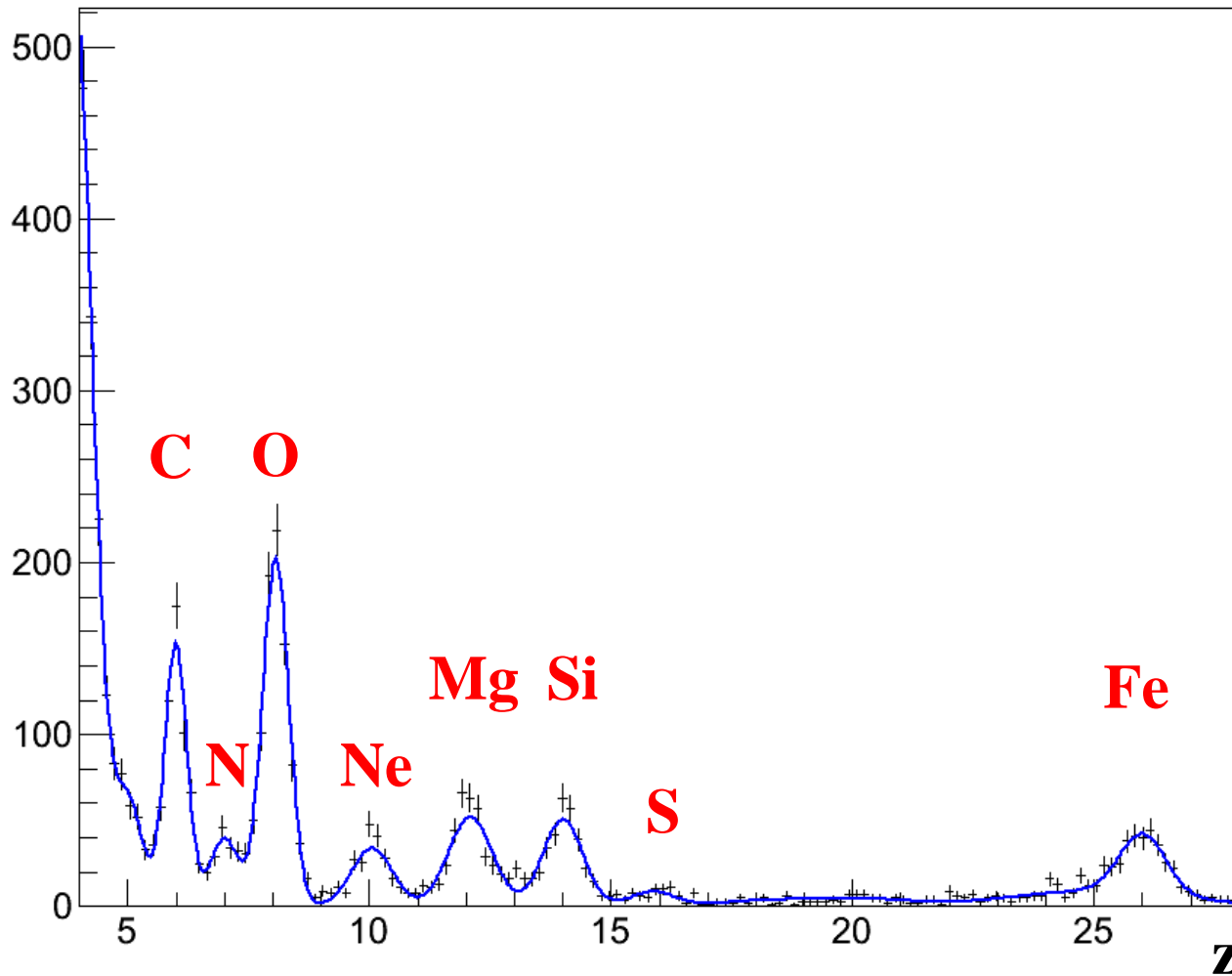


$$\theta = 34.19 +1.91 -0.59^\circ$$

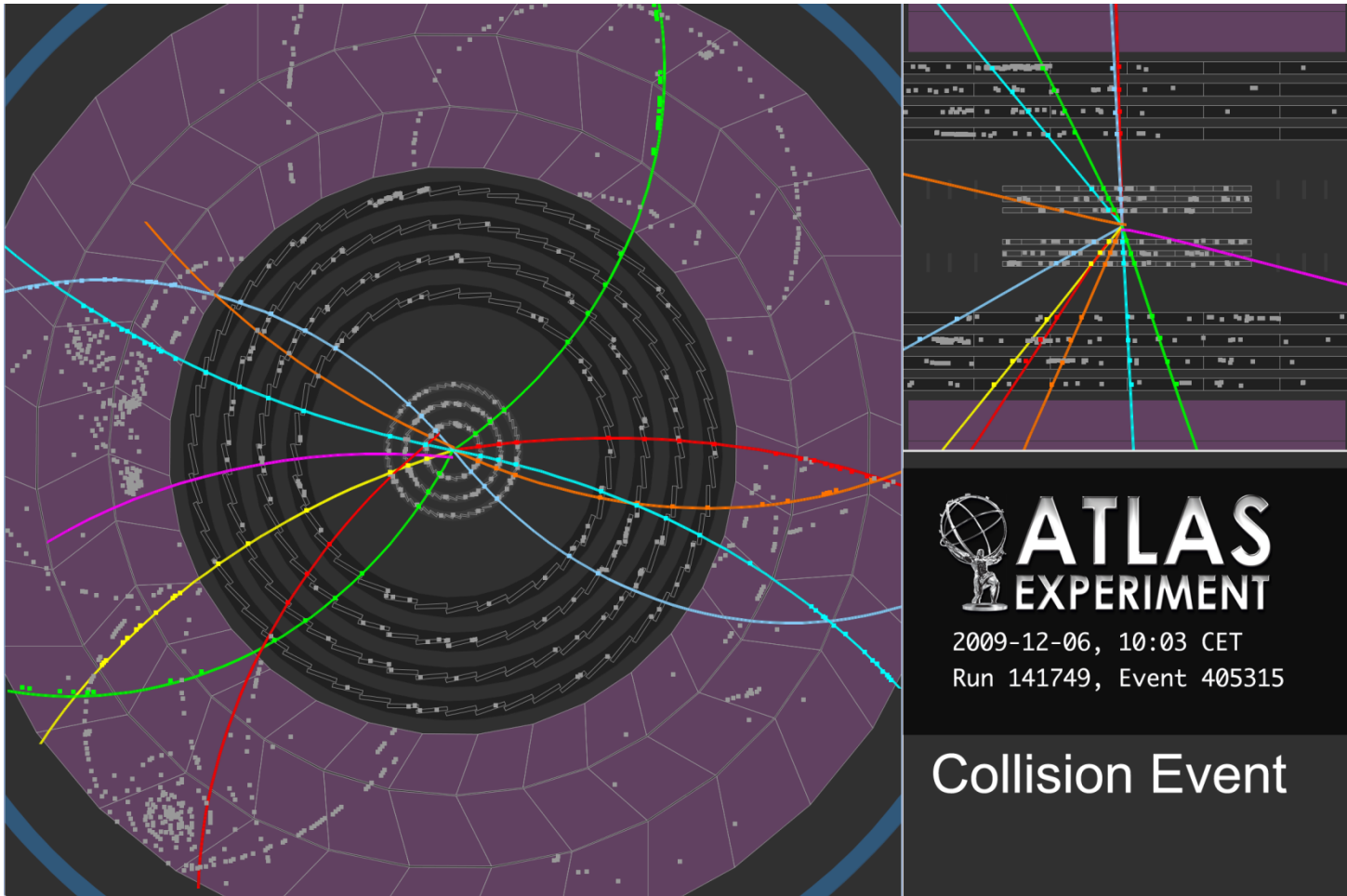
$$\varphi = 105.5 +5.9 -2.9^\circ$$

# SCD performance: charge measurement

*Preliminary!*



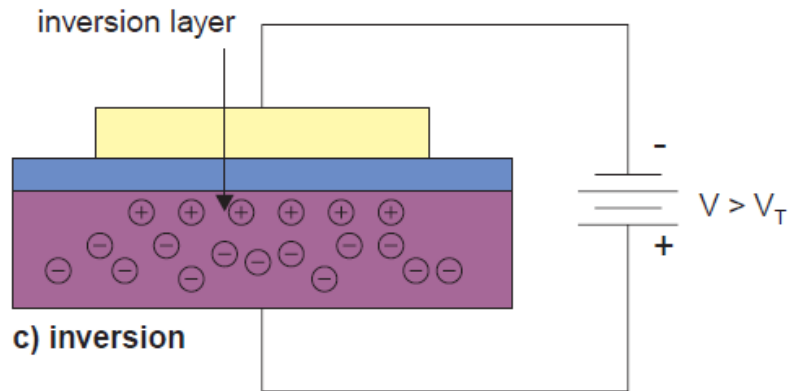
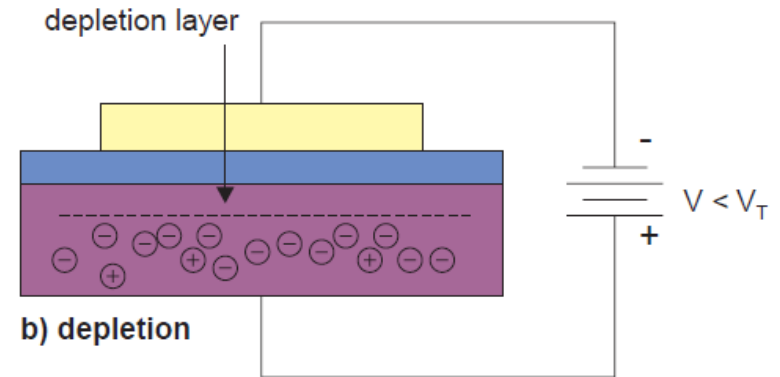
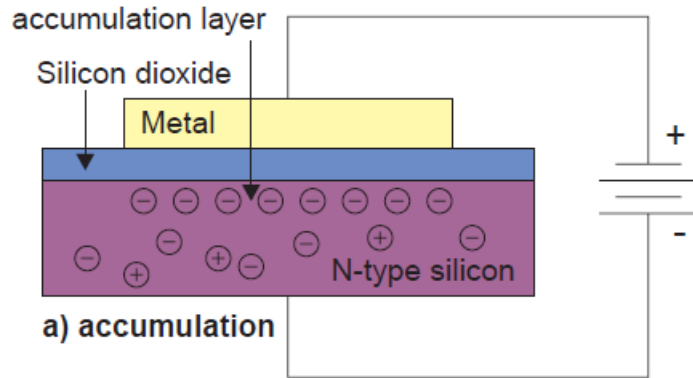
# ATLAS Silicon Trackers



<http://atlas.web.cern.ch/Atlas/public/EVTDISPLAY/events.html>

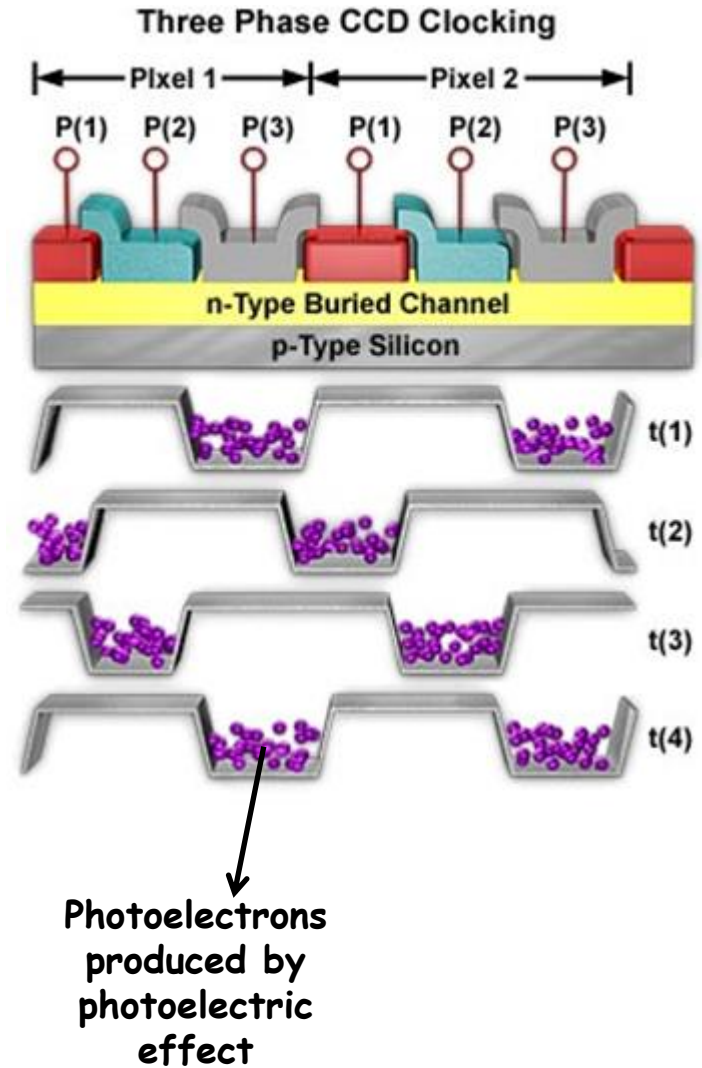
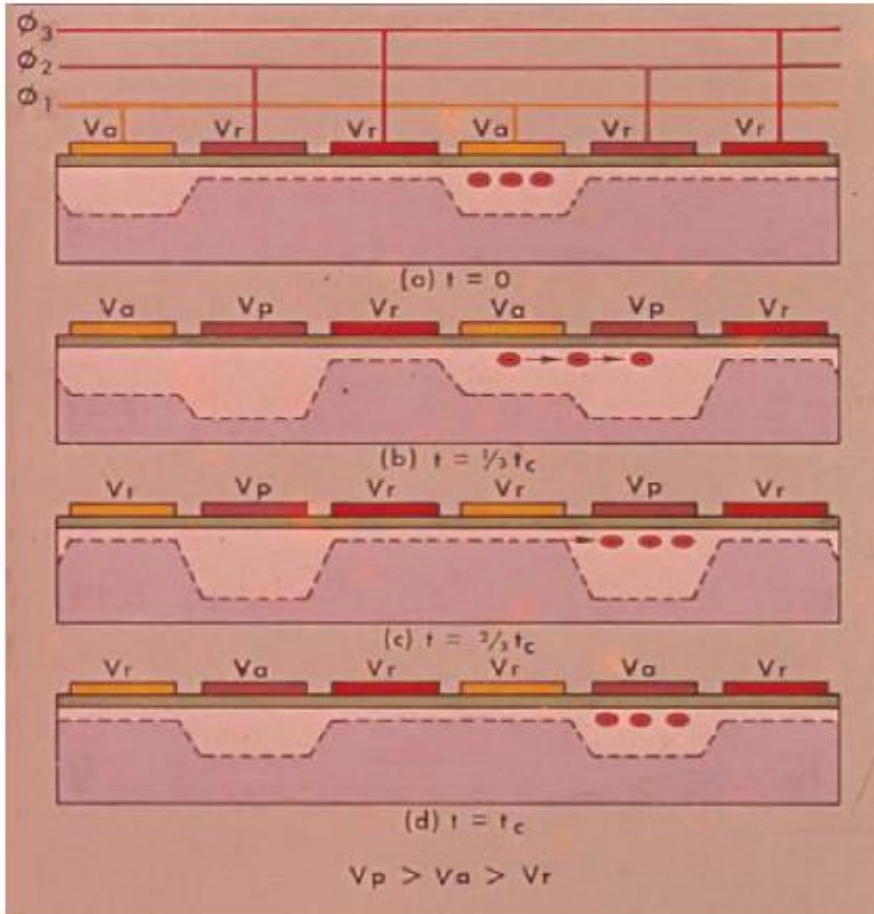
## **4. Silicon detectors for photon detection**

# MOS structure (fundamental structure)

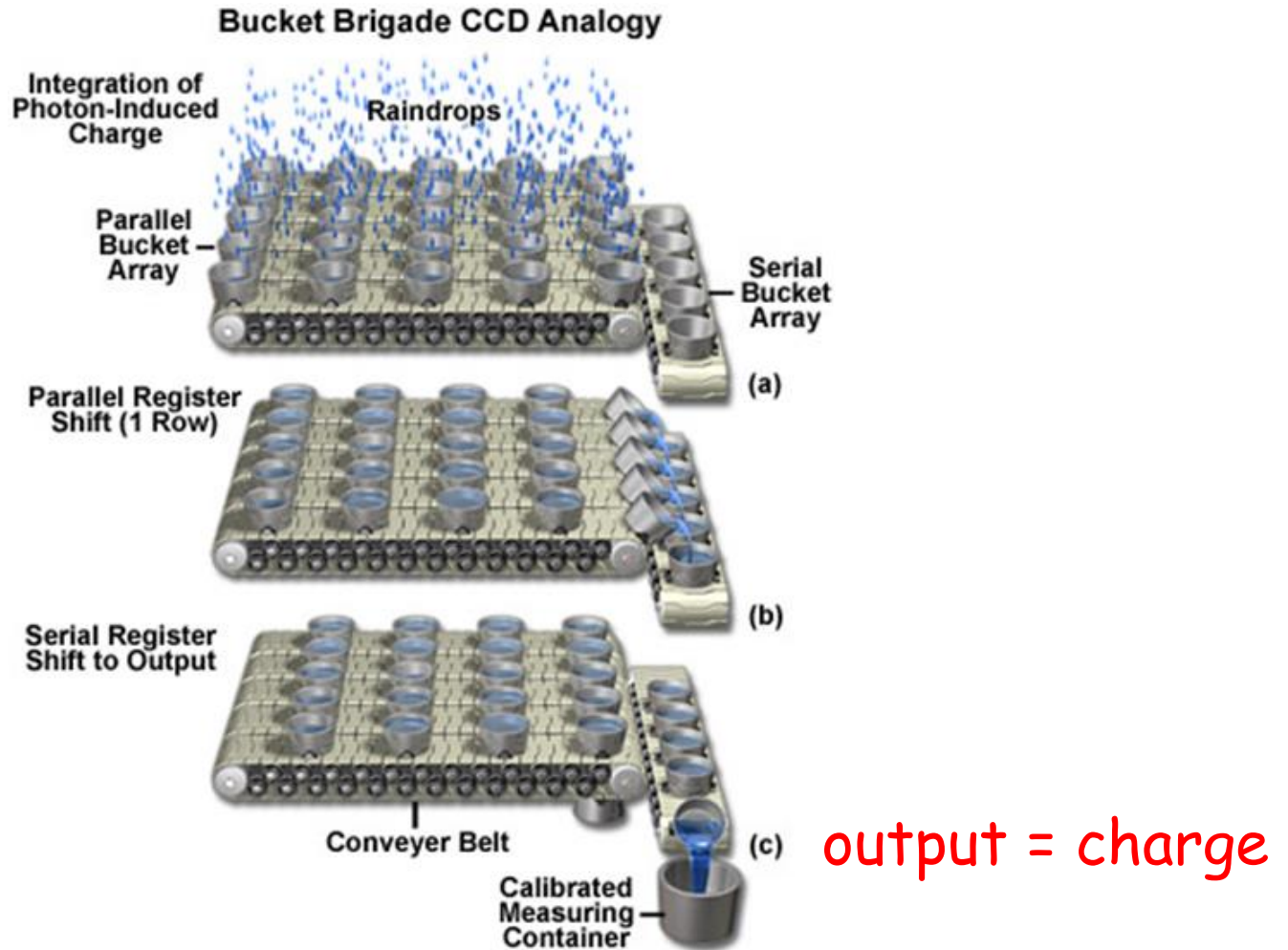


# CCD (Charge Coupled Device) sensor

## Charge Coupled Device



# CCD analogy



# CCD inventors (winners of Nobel prize in physics in 2010)

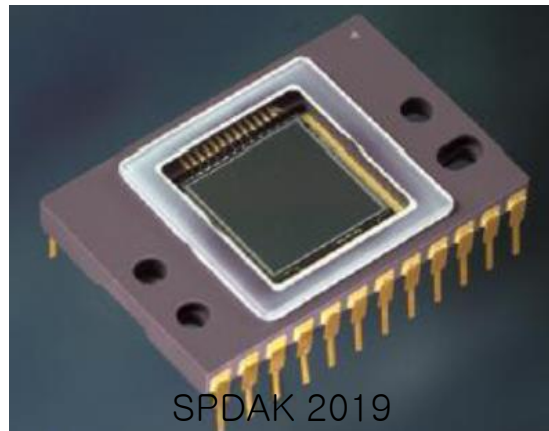
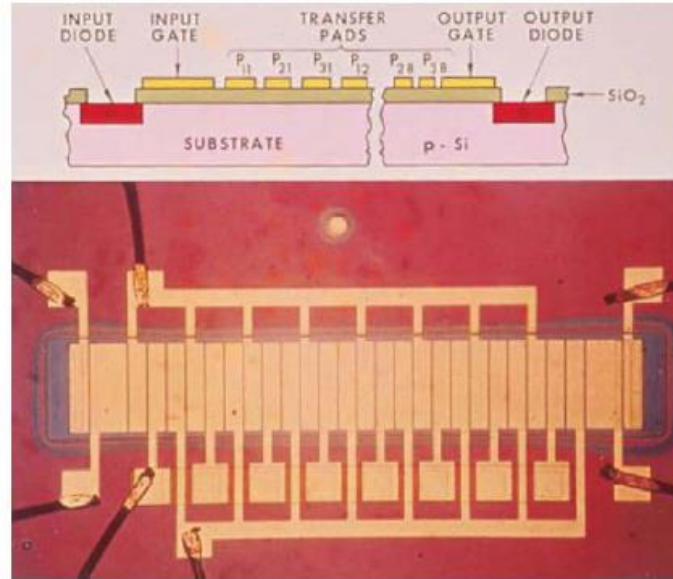
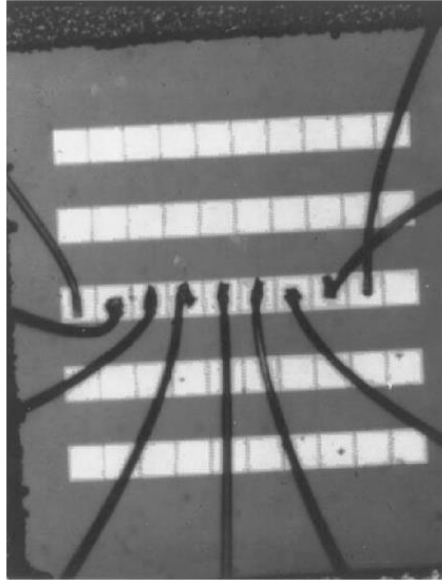
G. E. Smith & W.S. Boyle : invented CCD in 1970



Having Fun @ Bell Lab in 1974 !

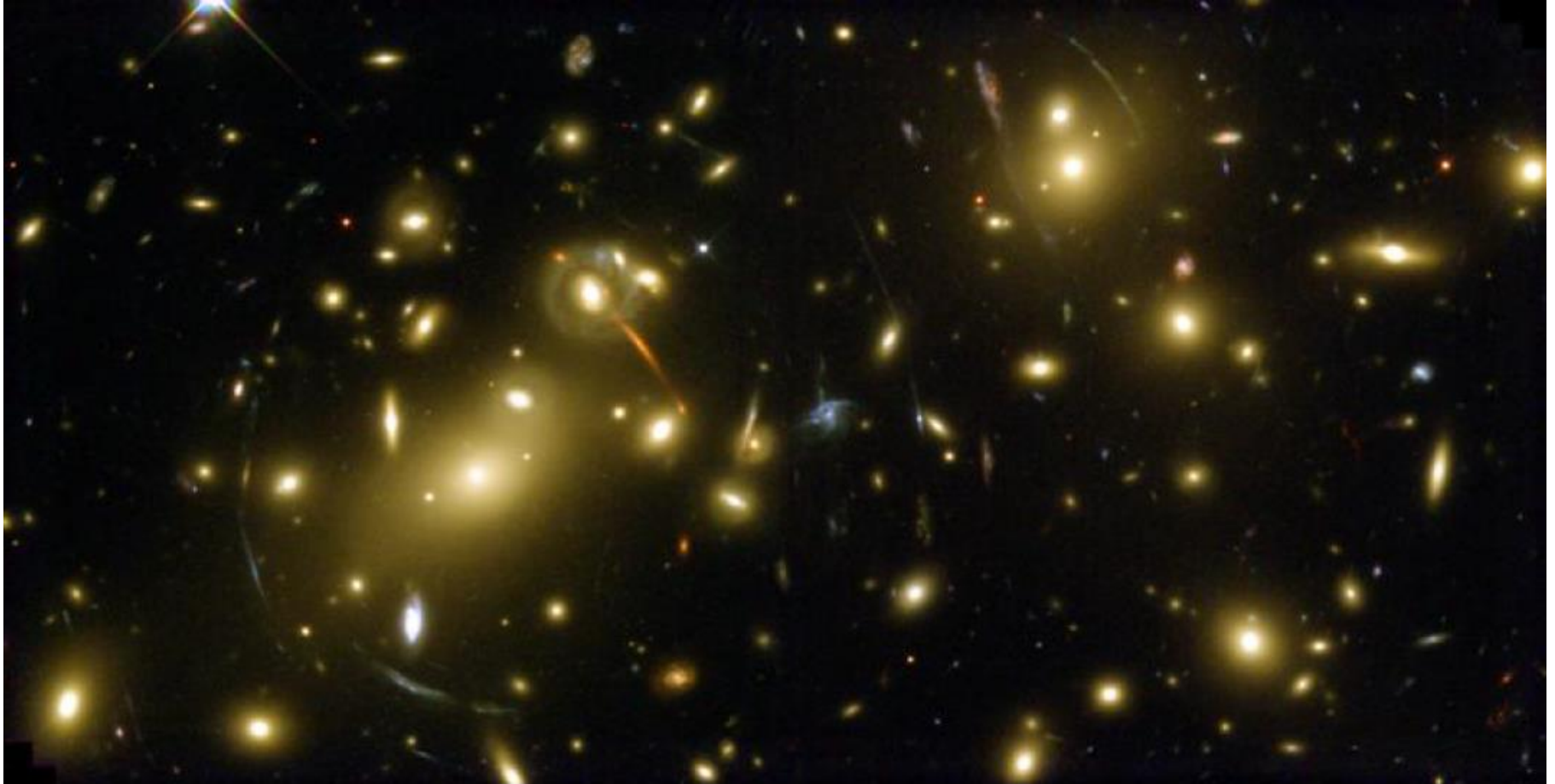


# How much advanced?



Kodak  
Mega pixel CCD  
~ 1cm<sup>2</sup>

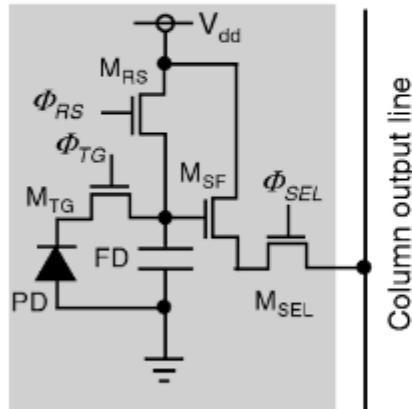
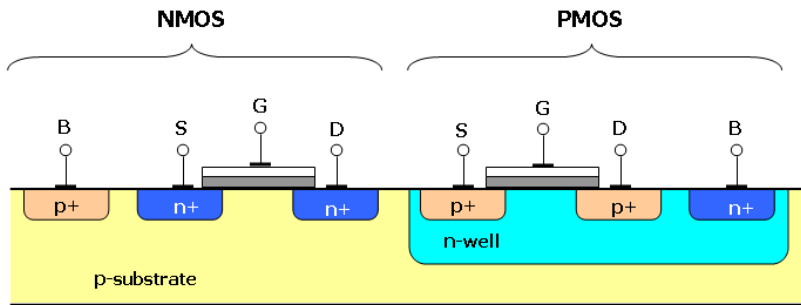
# CCD application in Astronomy/Astrophysics



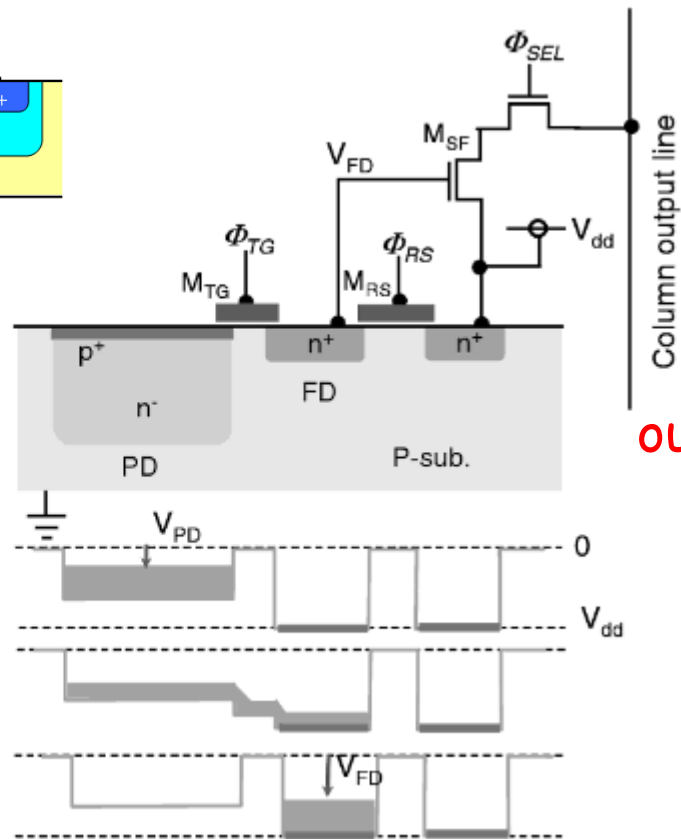
The galaxy cluster Abell 2218. *Image: WFPC2, Hubble Space Telescope, NASA.*

# CMOS sensor

CMOS : Complementary Metal Oxide Semiconductor

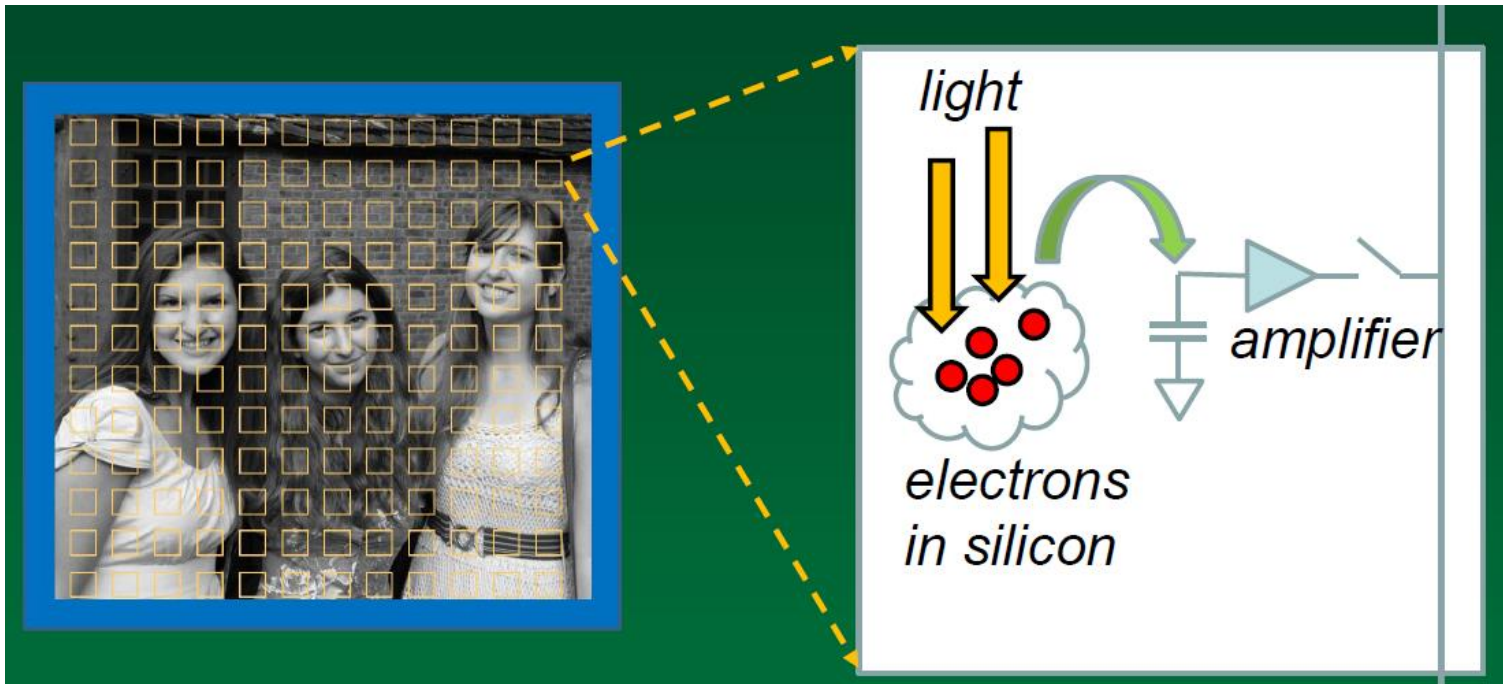


PD = Photo Diode

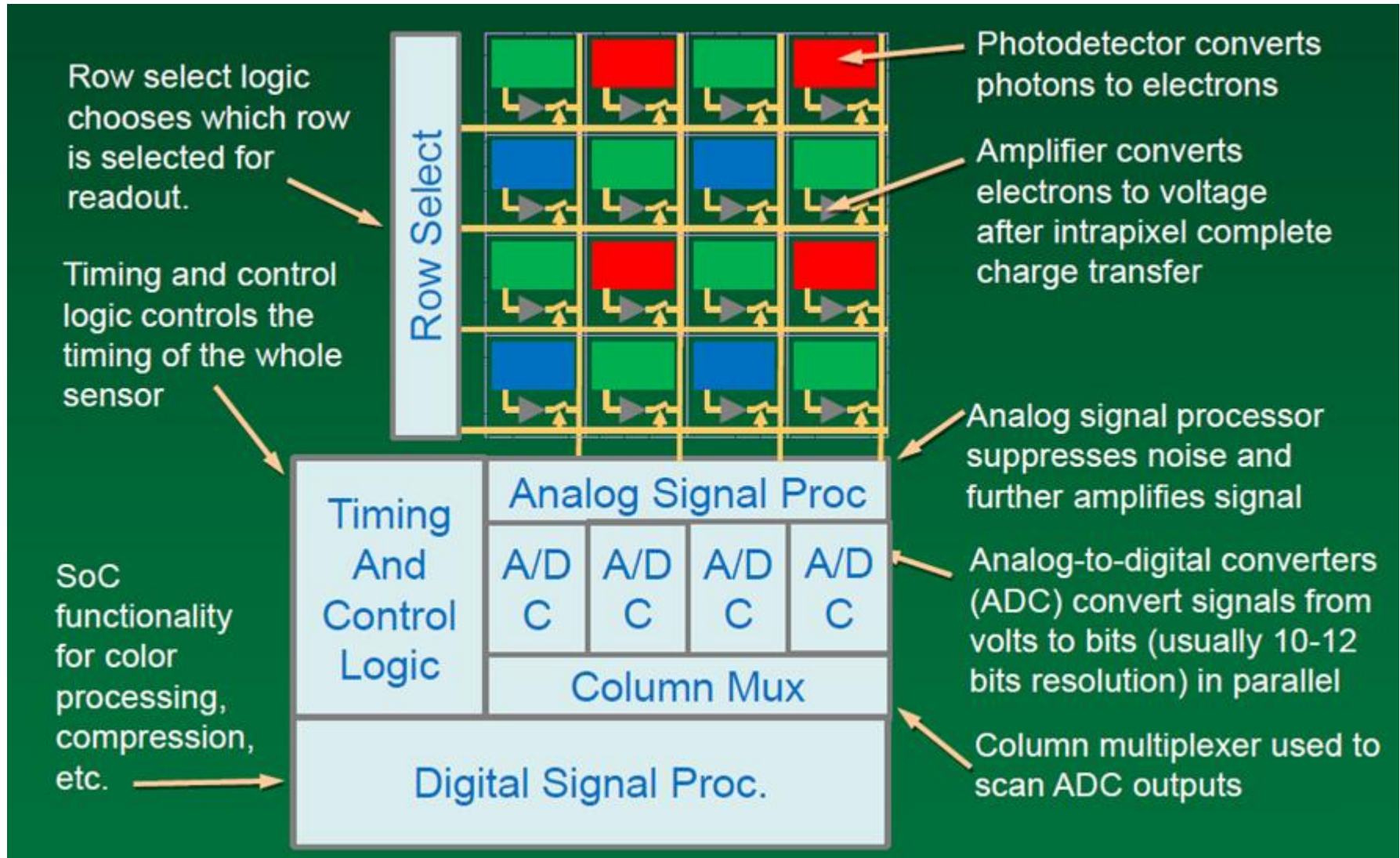


output = voltage

# A pixel in CMOS sensor



# Layout of typical CMOS sensor



# CCD & CMOS summary

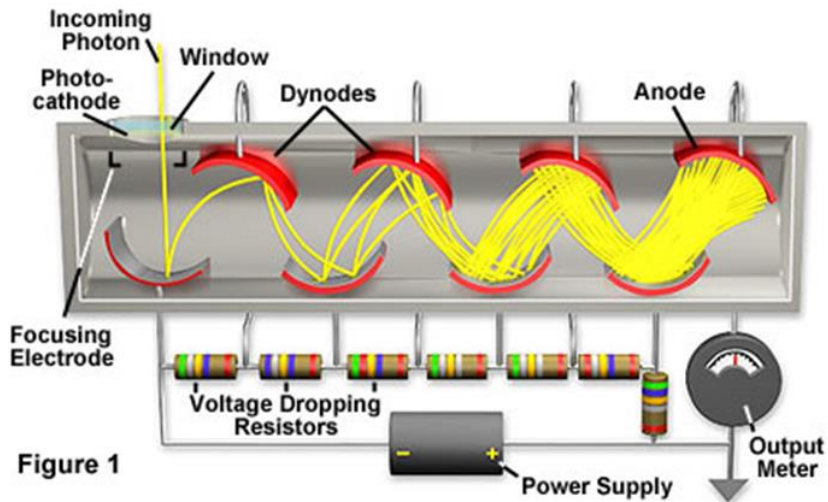
- 원칙적으로는 동일, 즉 포토다이오드 구조로, 광의 세기가 전하량으로 변환되고, 전하를 전압으로 변환 출력
- 변환기가 어디에 위치하는가가 두 센서의 근본적인 차이
  - 픽셀의 정보 이동 방법의 차이, 즉 **CCD**는 전하로 픽셀간 이동 최종 전압으로 변환, **CMOS**는 픽셀 단위에서 전압으로 변환하여 이동
- 잡음이 크고, 동적폭 (**dynamic range**) 및 속도에서 뛰어나지 않음
  - 동적폭 = Full Well Capacity / 잡음
  - Kodak Mega 픽셀 CCD 200,000 전자 / 20전자 = 100,000
- 광량이 적은 환경에서는 고민감도의 센서가 필요하나, **CCD와 CMOS는 증폭형 센서가 아니므로 야간 상황에서 그 성능에 한계**
- 우리의 눈의 민감도는 **CCD** 보다 우수함
  - **CCD** 민감도 ~ 0.03 Lux (냉각 시 0.002 Lux)

# Photomultiplier

- 정확히 말하면 광전자를 다수의 전자로 증폭
- 광음극(photocathode)과 함께 사용하는 PMT(Photomultiplier Tube)와 MCP(Microchannel Plate)가 대표적으로 단일 광자 계수 가능
- 반도체 소자에서는 센서 내부에서 광전자(photoelectron)를 증폭:  
**ICCD(Intensified CCD), EB(Electron Bombardment)CCD, EM(Electron Multiplier)CCD, APD(Avalanche Photodiode), SiPM(Silicon Photomultiplier)**

# Photomultiplier Tubes (PMTs)

- 초민감 초고속 특성을 갖는 광센서로 과거 수십년간 특수목적에 사용
- 그러나 진공관식으로 부피가 매우 크고, 충격에 취약하며 고전압을 필요로 하므로, 야전에서 내구성, 휴대성 및 실용성이 크게 떨어지며, 광량이 많아지면 소자가 파괴되는 문제



PMT의 원리와 Hamamatsu사 제품



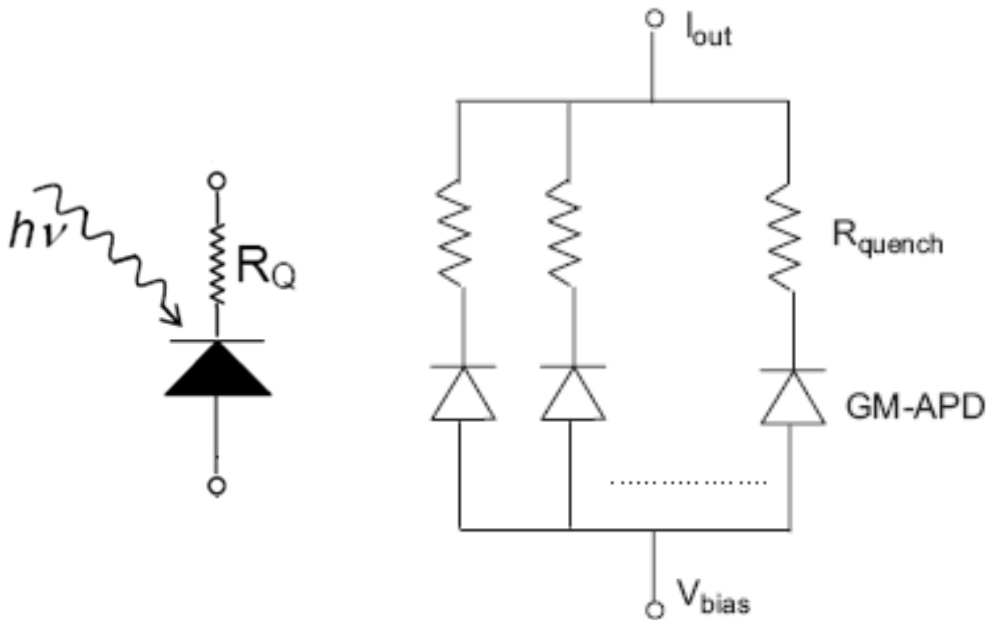
# 20 inch World largest PMT

For Super-K

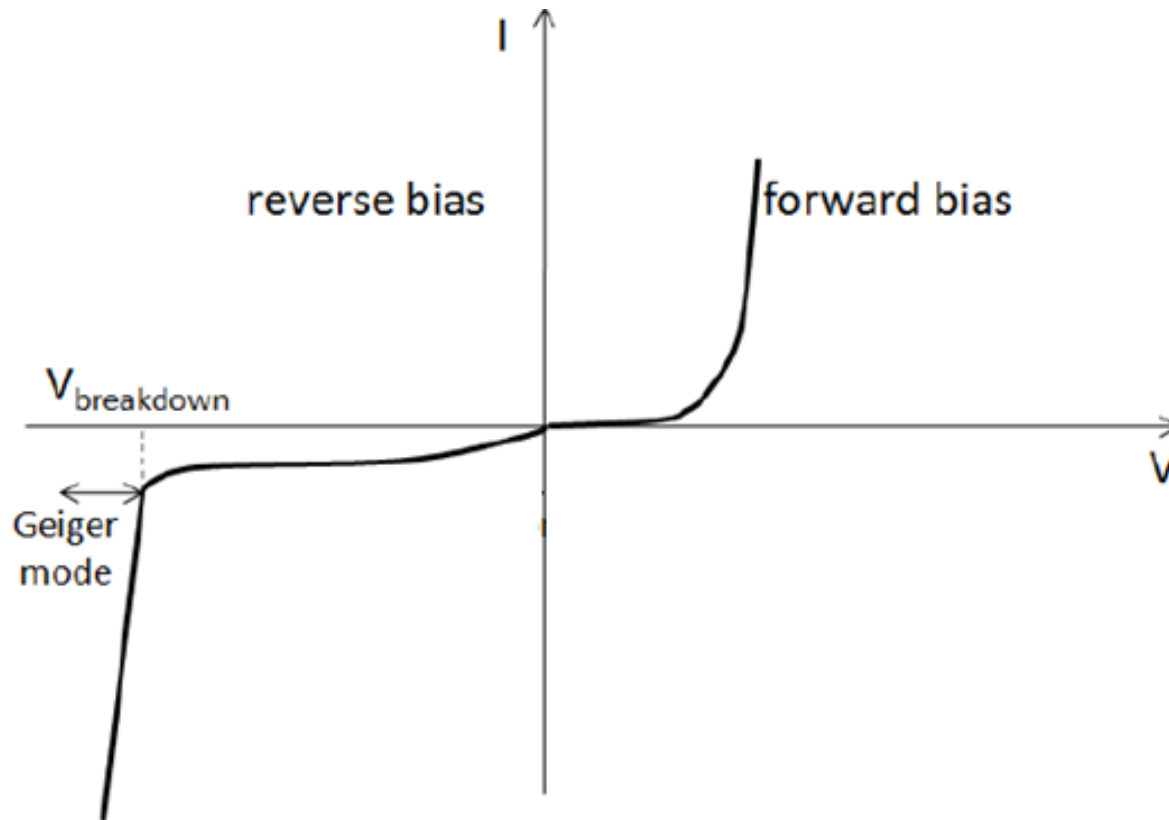


# SiPM (Silicon PhotoMultiplier)

- **Micropixel (Geiger mode APD)** 어레이로 이루어진 반도체 광다이오드
- **Micropixel**의 크기는  $10\sim 100\mu\text{m}$ 로  $1\text{mm}^2$ 의 면적당  $100\sim 1000$ 개 집적
- 각 **Micropixel** 은 공통의 인가전압과 로드 저항으로 작동, 출력신호는 모든 **Micropixel** 신호의 합(**multiplexed output**)
- 즉 **Binary**의 디지털소자로 입사광의 수를 세는 아날로그식의 광센서

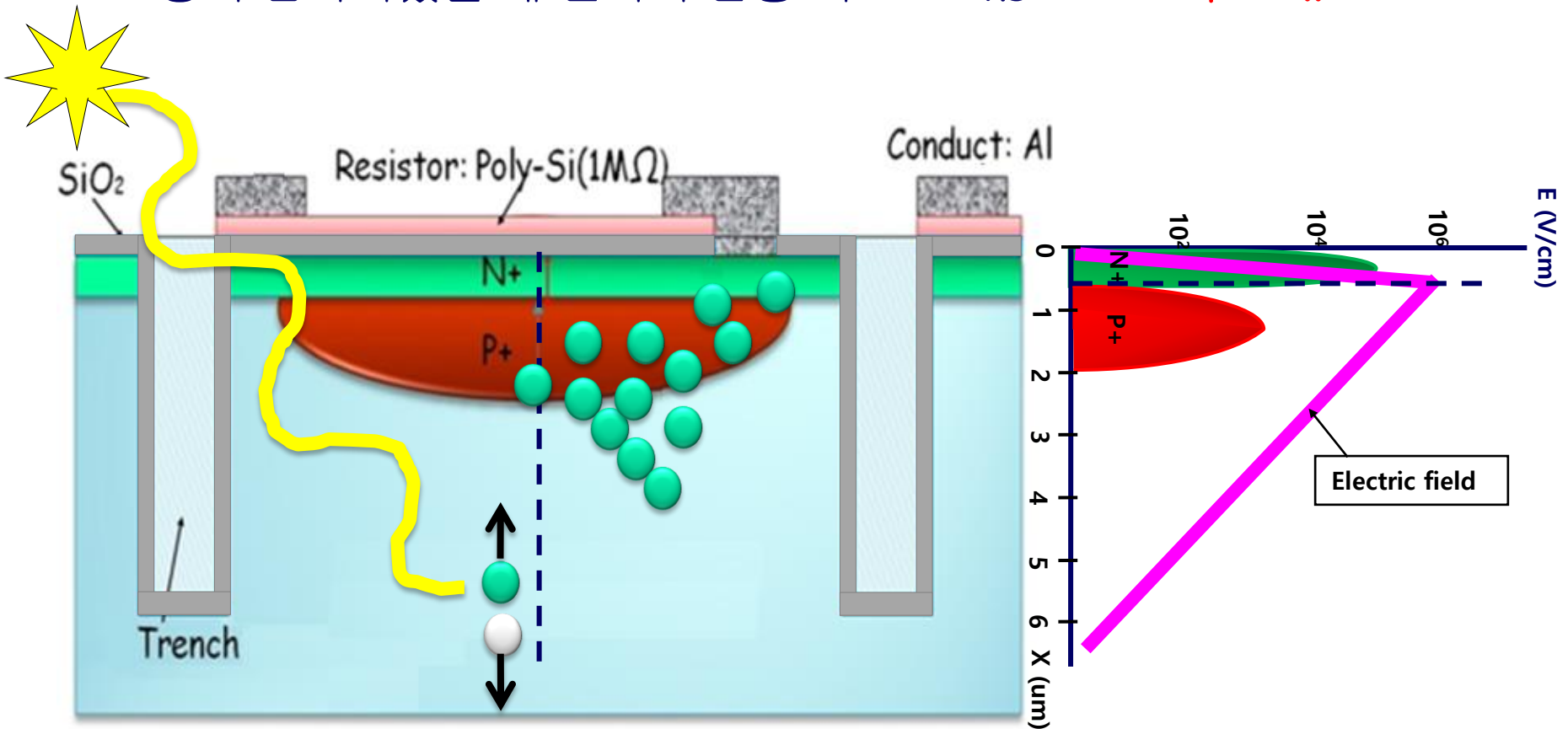


# Geiger Mode

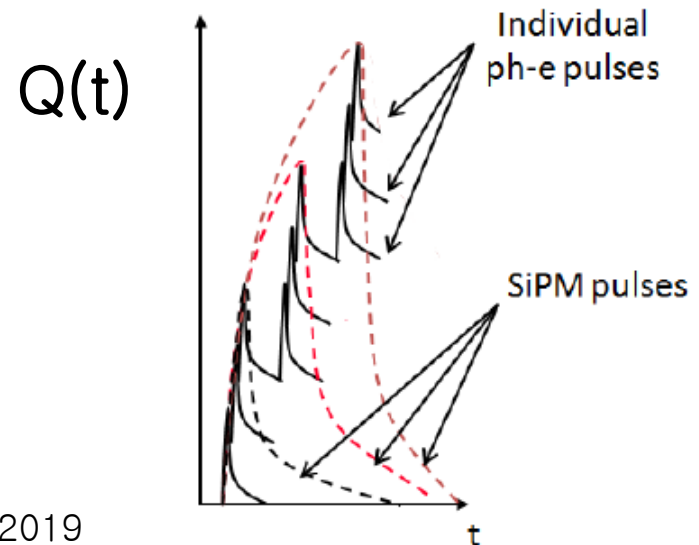
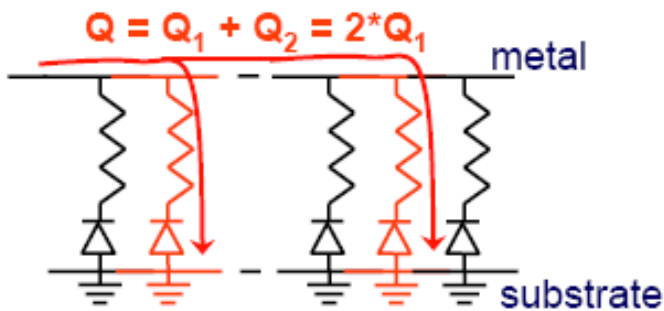
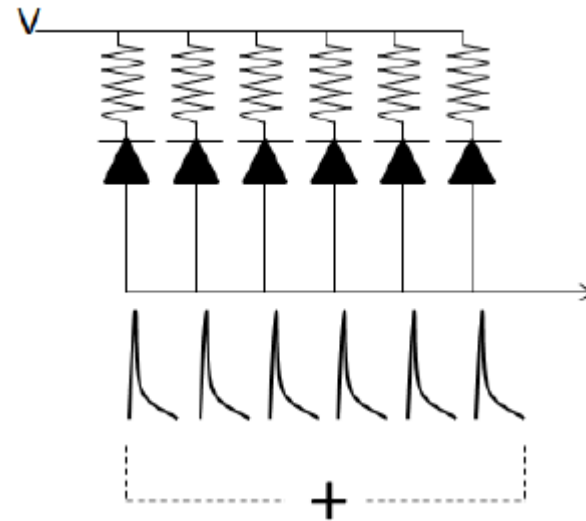
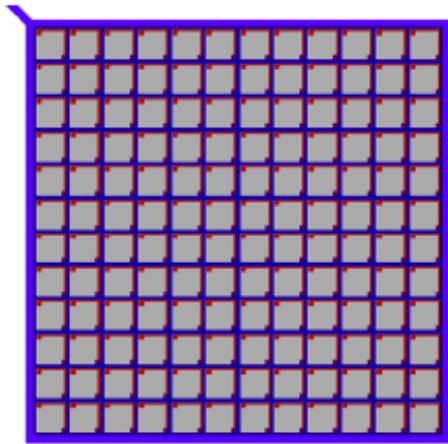


# SiPM

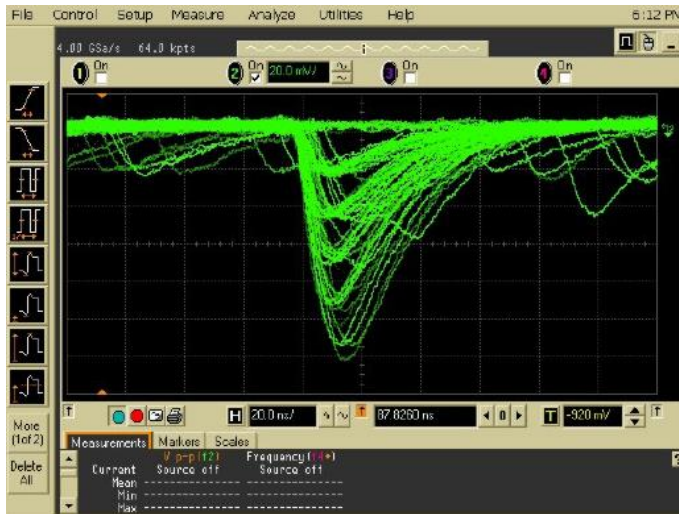
- PN 접합면에 매우 높은 전기장 형성
- 한 개의 광자 입사 -> **100만 배**의 전자증폭 발생 -> **초민감도 !!**
- 광이 입사되었을 때 센서의 반응 속도 -> **1ns 초고속도 !!**



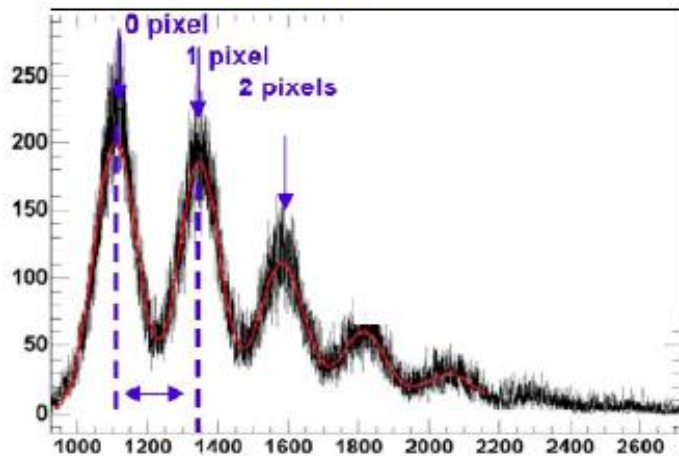
# Analog Signal



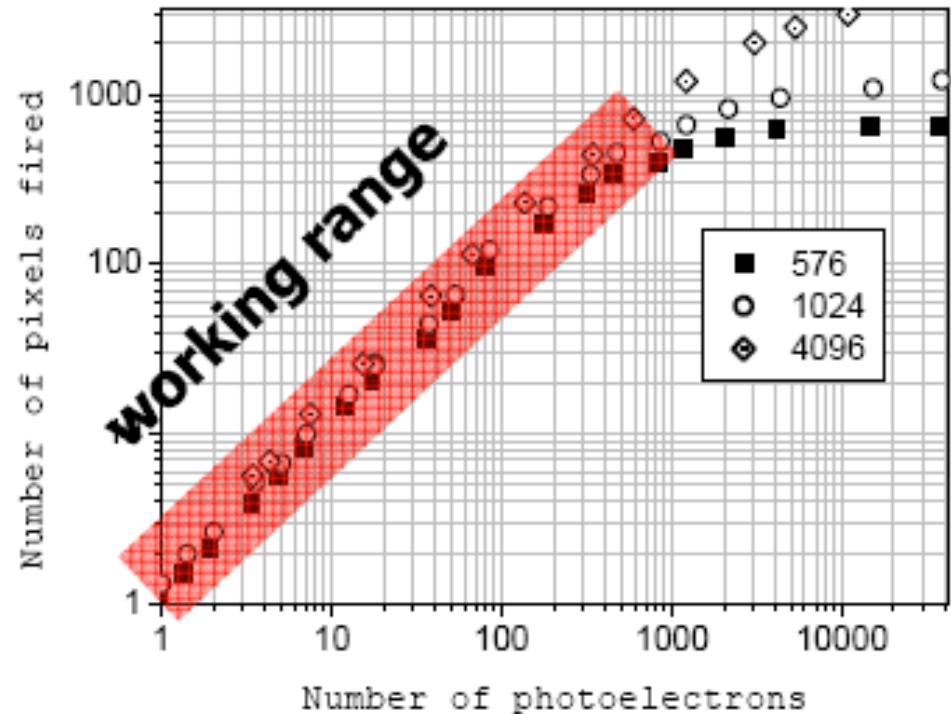
# Analog Signal & Dynamic/Working Range



Gain calibration



IRST of INFN Pisa

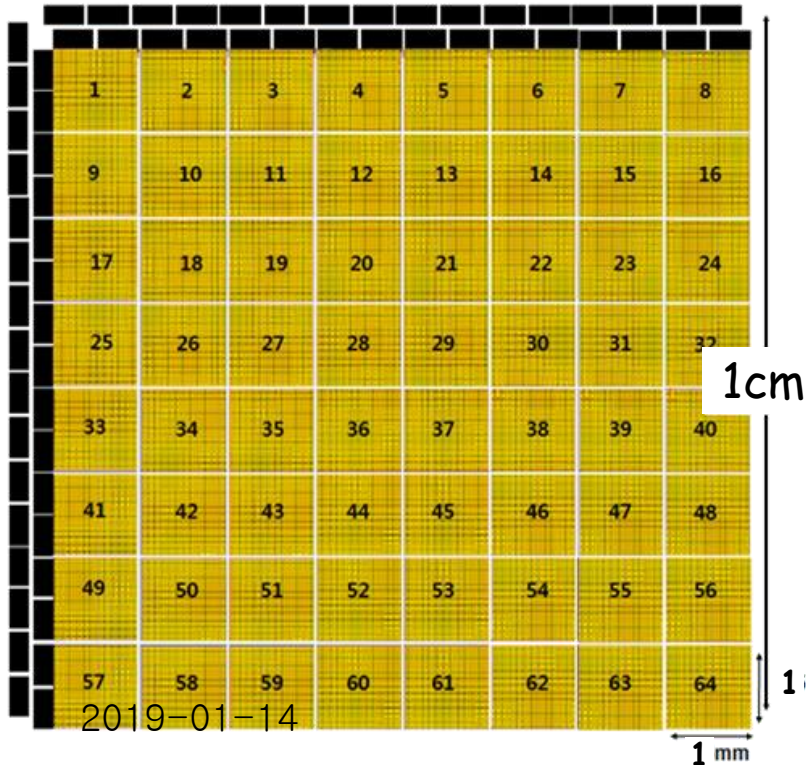


# 다화소용 8 × 8 픽셀 어레이 소자

- ◆ SiPM 픽셀 :  $1 \times 1 \text{ mm}^2$  크기  
( $30 \times 30 \mu\text{m}^2$  크기,  $10^3$ 개의 마이크로 픽셀)

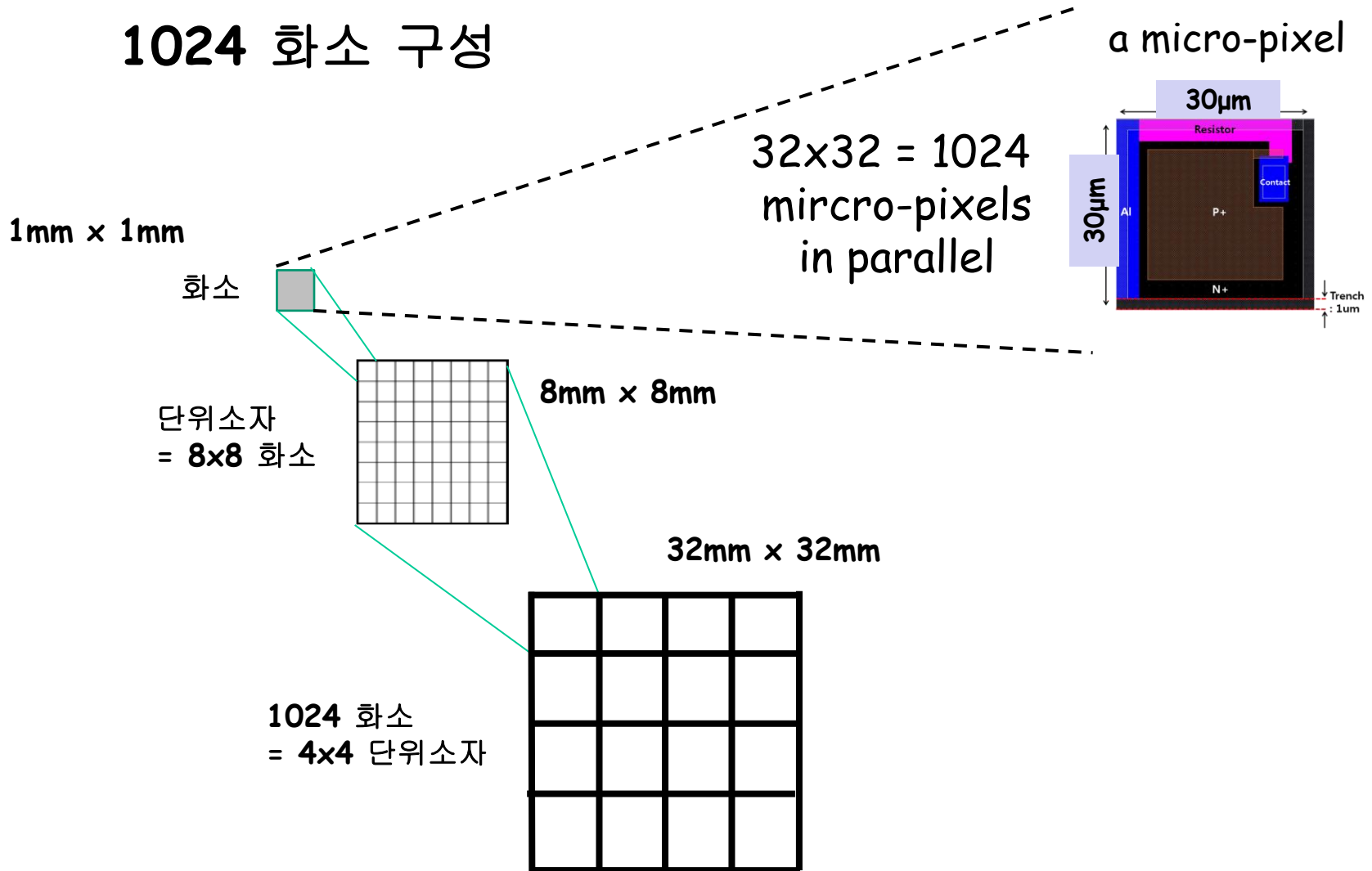
- ◆ 64ch SiPM 소자 :  $1 \times 1 \text{ cm}^2$

64ch 설계도  
1cm



# 1024 화소 배열

## 1024 화소 구성

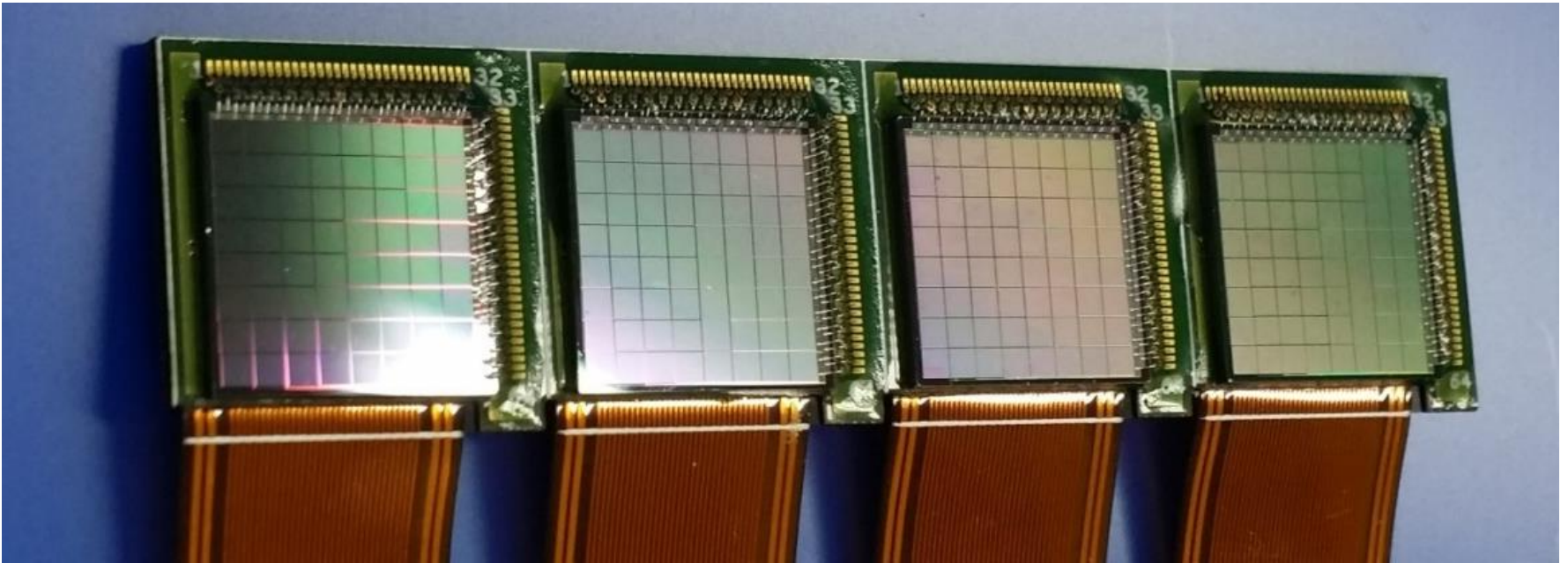




# 단위소자 4개가 wirebonding된 Rigid-FPCB

- ◆ SiPM 픽셀 1024ch 제작:  $1 \times 1 \text{ mm}^2$  크기  
( $30 \times 30 \mu\text{m}^2$  크기,  $10^3$ 개의 마이크로 픽셀)
- ◆ 64ch SiPM 소자 :  $1 \times 1 \text{ cm}^2$

제작된 SiPM 단위 소자들 (각  $1 \text{ cm}^2$ , 64ch의 픽셀로 구성)



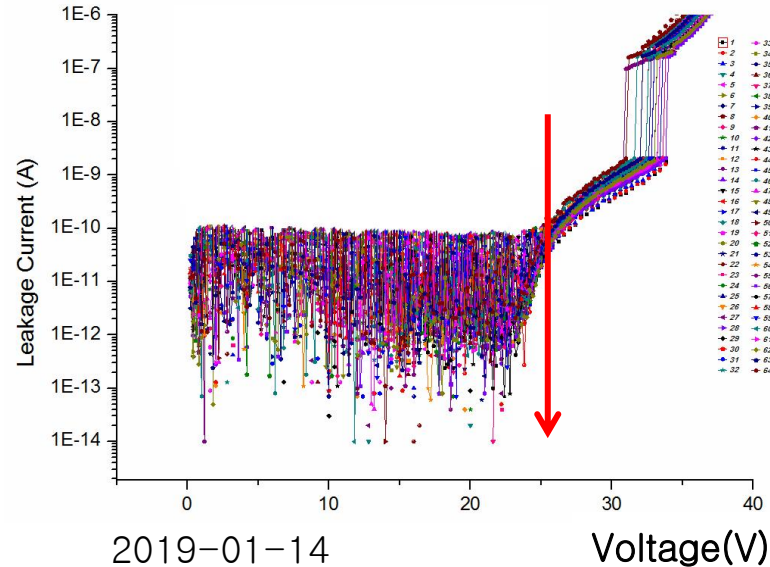
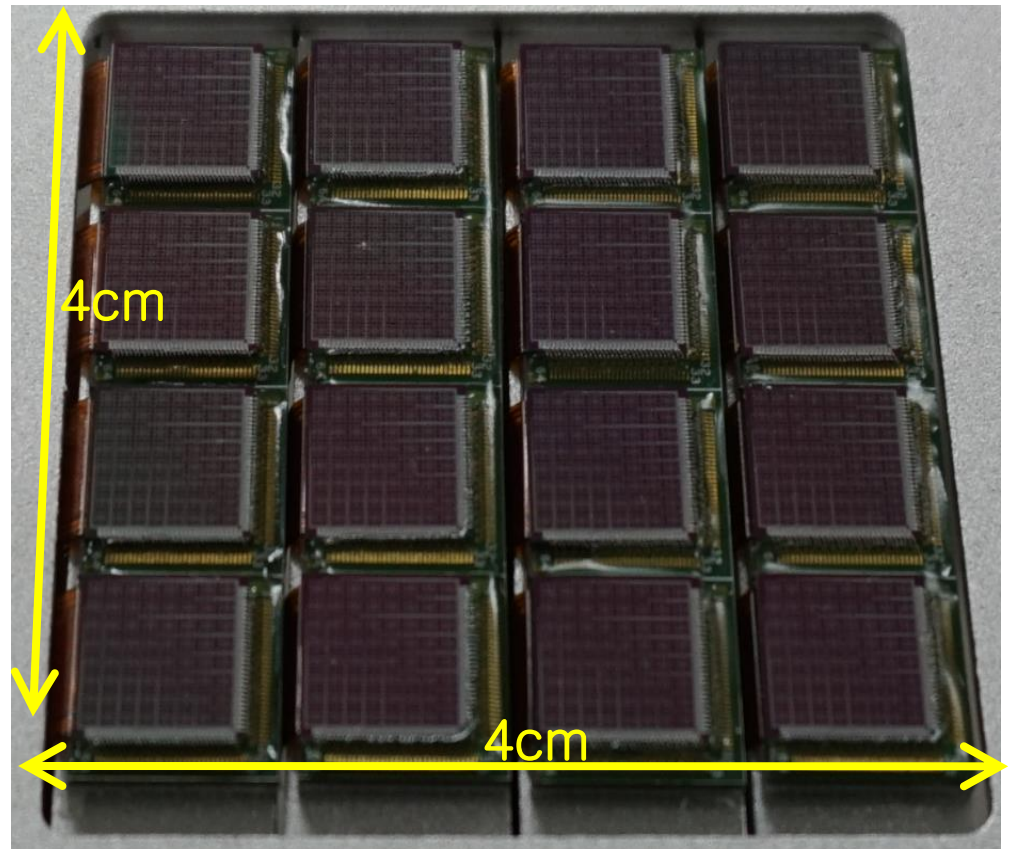
# 16개의 8 x 8 SiPM 픽셀 어레이로 구성된 다화소 (1024-ch)

- ◆ 1단계 SiPM 픽셀 1024ch 제작  
: 1 x 1 mm<sup>2</sup> 크기  
(30x30μm<sup>2</sup> 크기, 10<sup>3</sup>개의 마이크로 픽셀)

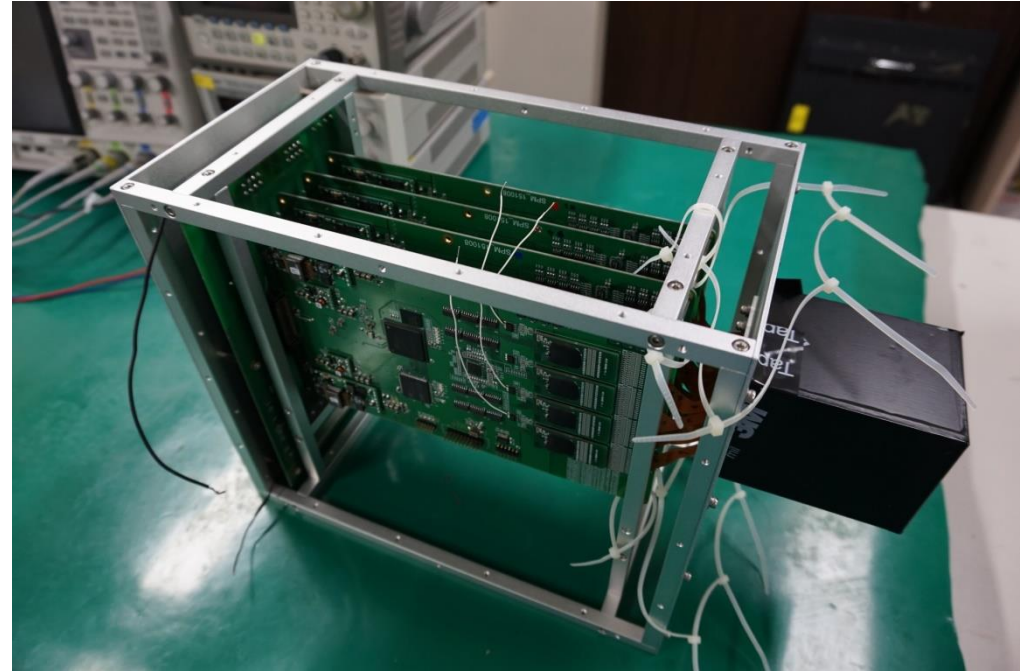
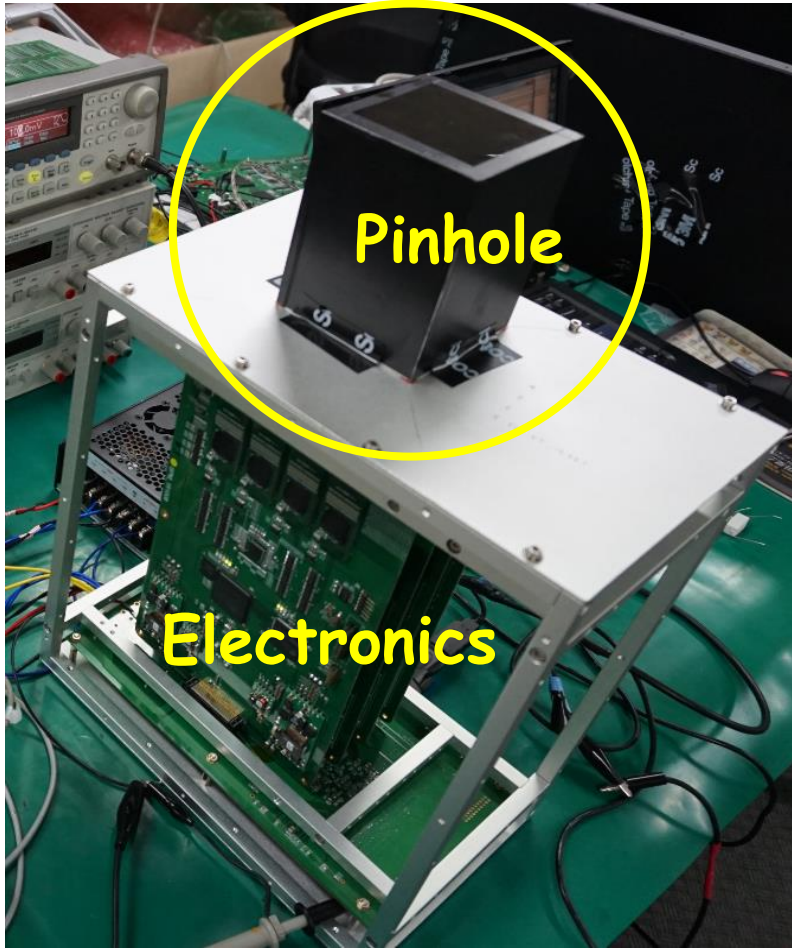
- ◆ 64ch SiPM 소자 : 1 x 1 cm<sup>2</sup>

항복전압 균일  
->  
Multi channel test

## 1024-ch

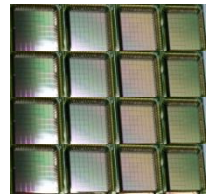
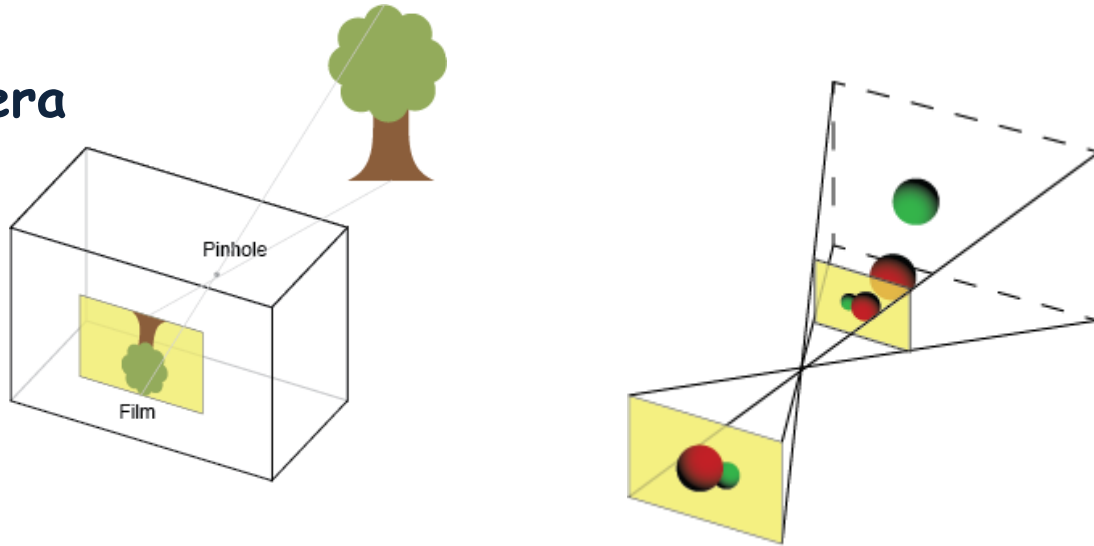


# 1024-ch SiPM + 신호처리장치 + Pinhole



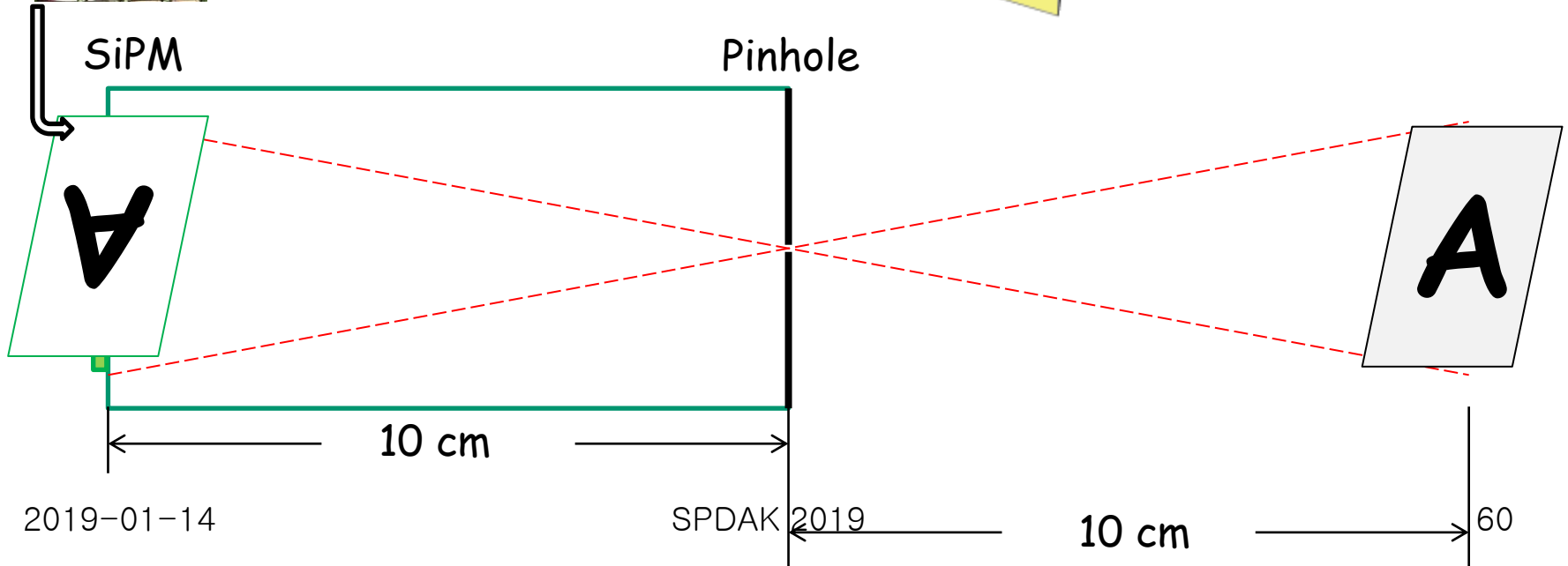
# Image Test

Pinhole Camera



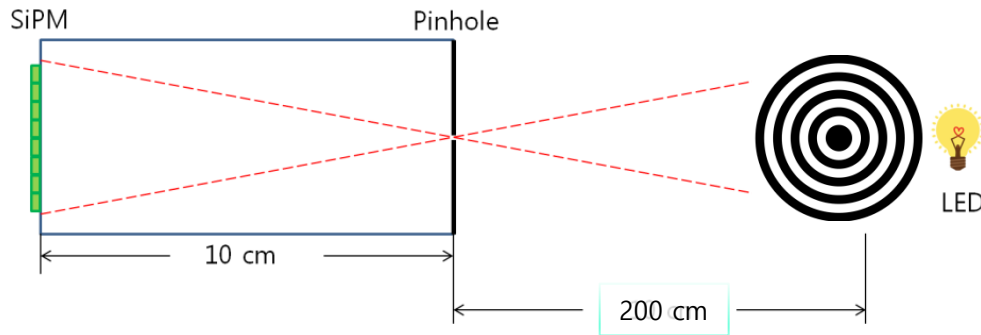
SiPM

Pinhole

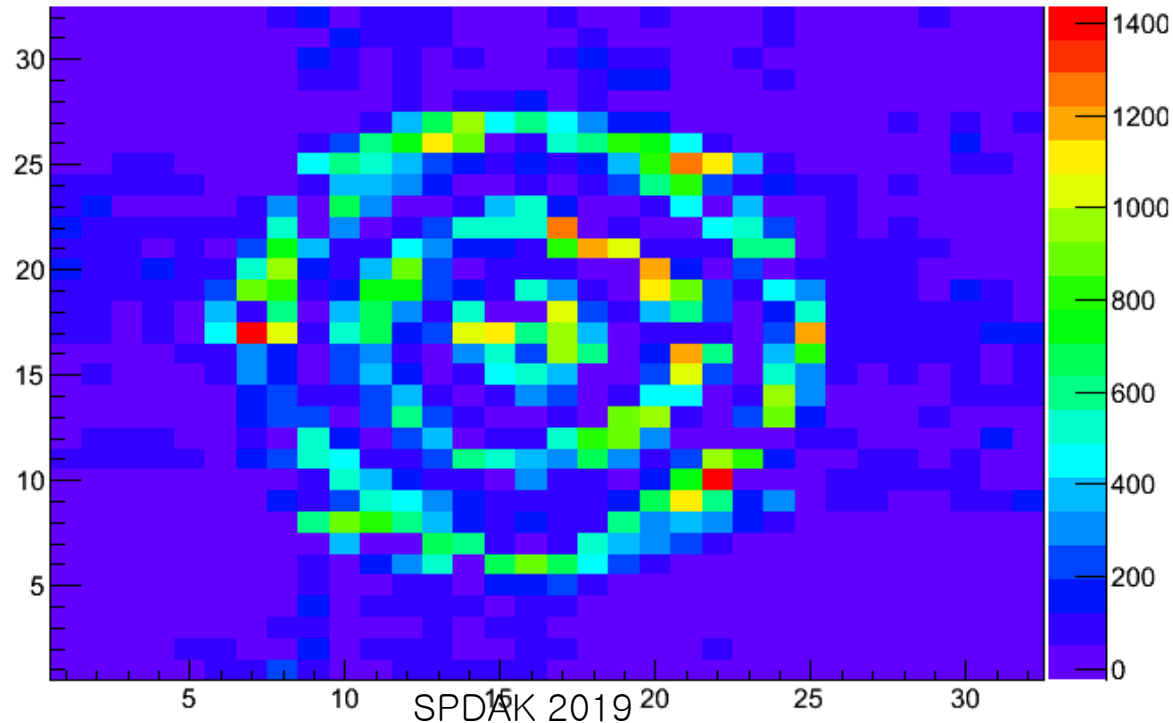


# Image Test

## Pinhole Camera

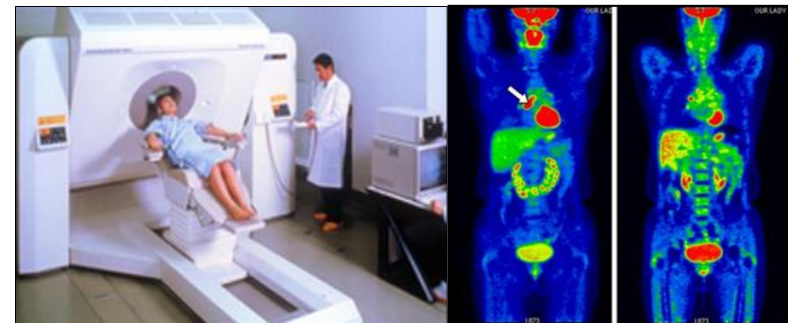
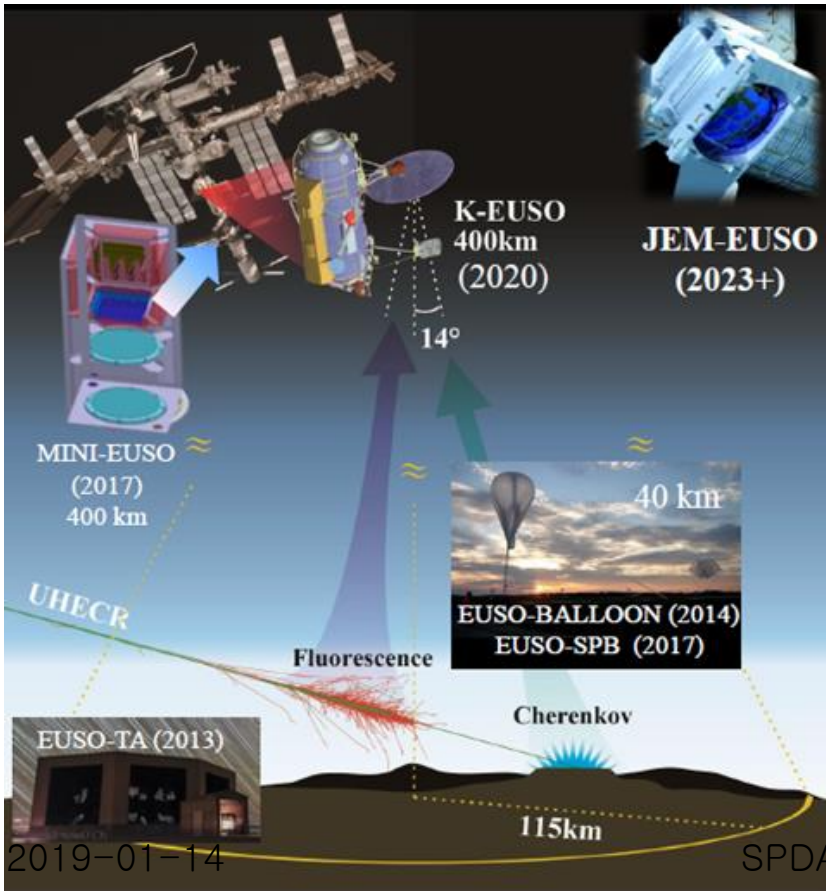


**Absolutely Dark!**  
**CCD or CMOS cameras**  
**can NOT get this image!**



# SiPM Applications

- 천체/천문: 미약한 광신호 측정을 위한 광센서
- 보안 감시 : Homeland Security
- 의료용 : PET Scanners, Medical imaging



## 5. Summary

# Summary

- Silicon is one of most popular material for radiation detection in the fields of Particle physics/Astro-particle physics
  - Charged particle detection
  - Photon detection
- During Lab, try to understand
  - C-V & I-V characteristics of silicon detectors
  - Responses (signals) of silicon detector to radiation sources or cosmic muons
    - Signal as a function of  $V_{\text{bias}}$  ?

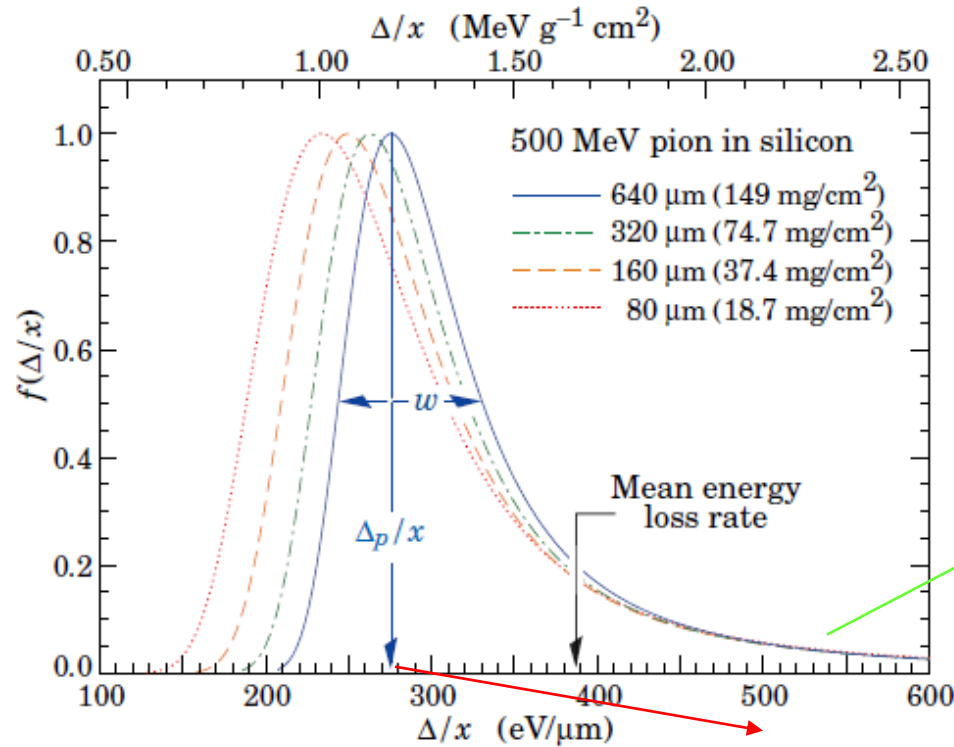


**Back-up slides**

# dE/dx is of random nature

From Review of Particle Physics

Probability density function  $\sim$  Landau Function

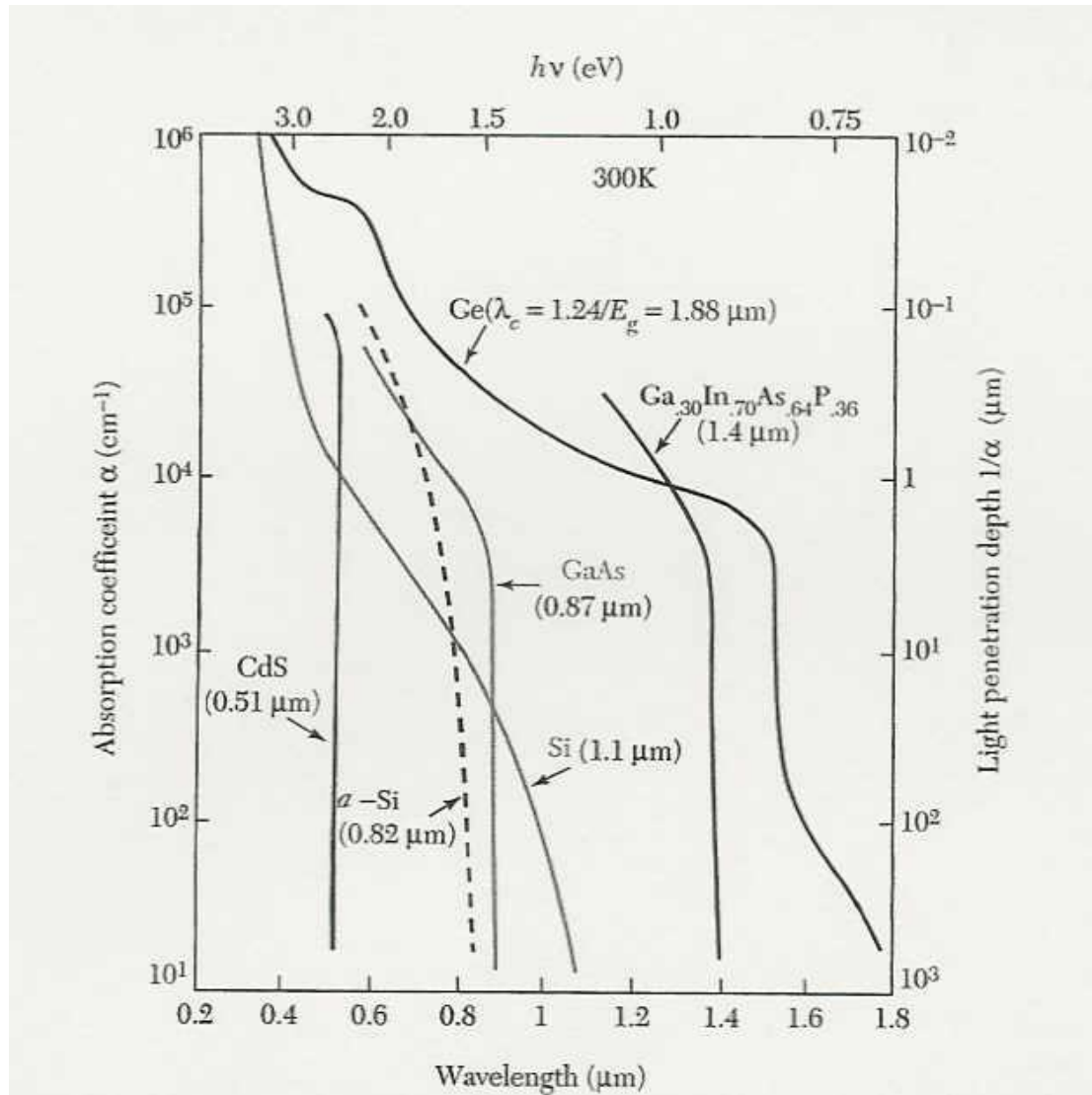


Due to  $\delta$  rays: Knock-on electrons

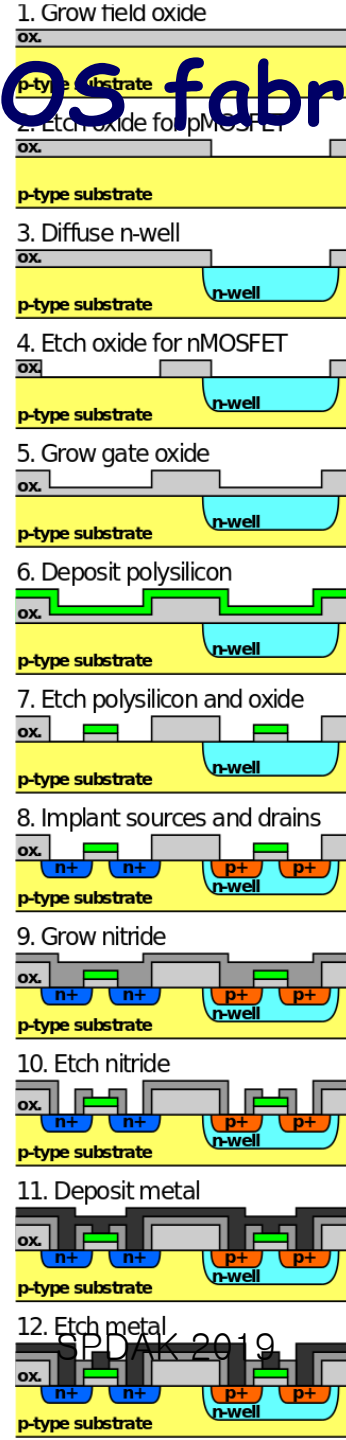
Most probable dE/dx

Landau function  $f_L(\lambda) = 1/\pi \int_0^\infty du \exp[-u(\ln u + \lambda)] \sin \pi u$

# Absorption Coefficient



# Example of CMOS fabrication process



From  
<https://en.wikipedia.org/wiki/CMOS>