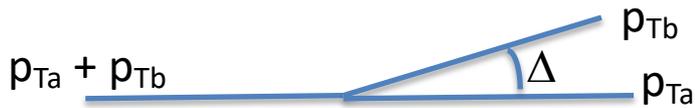




# LUND PLANE AND APPLICATIONS

# Jet Lund diagram

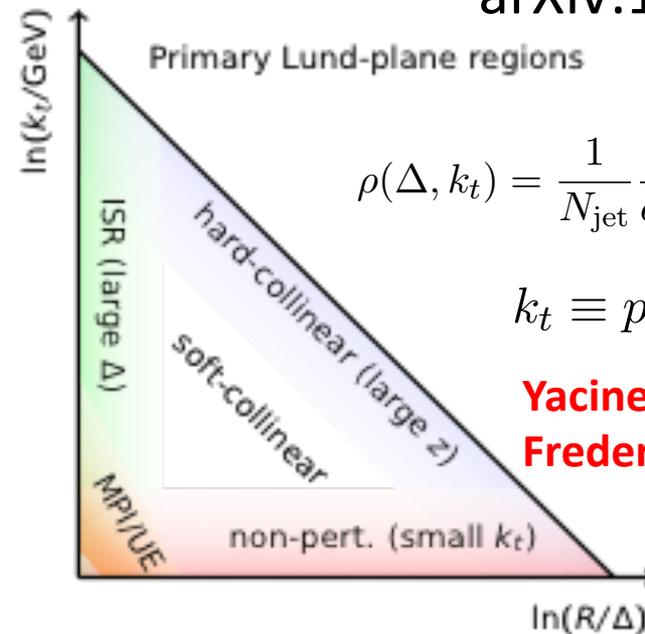
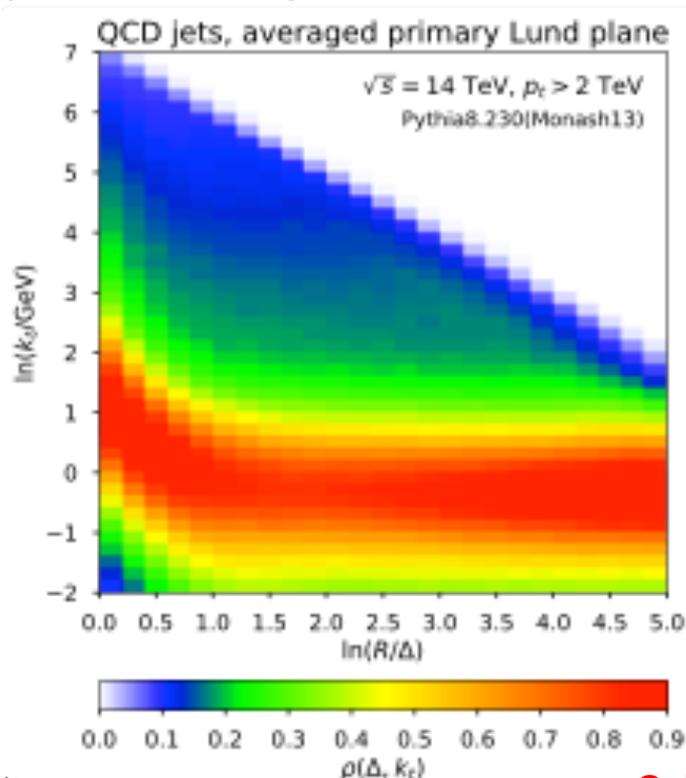


$$p_{T,a} > p_{T,b}, \quad \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^2$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

Lund diagrams, a theoretical representation of the phase space within jets, have long been used in discussing parton showers and resummations. We point out that they can be created for individual jets through repeated Cambridge/Aachen declustering, providing a powerful visual representation of the radiation within any given jet.

arXiv:1807.04758



$$\rho(\Delta, k_t) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln k_t d \ln 1/\Delta}$$

$$k_t \equiv p_{tb} \Delta_{ab},$$

**Yacine on Monday...**  
**Frederic yesterday...**

To leading order in perturbative QCD and for  $\Delta \ll 1$ , one expects for a quark initiated jet

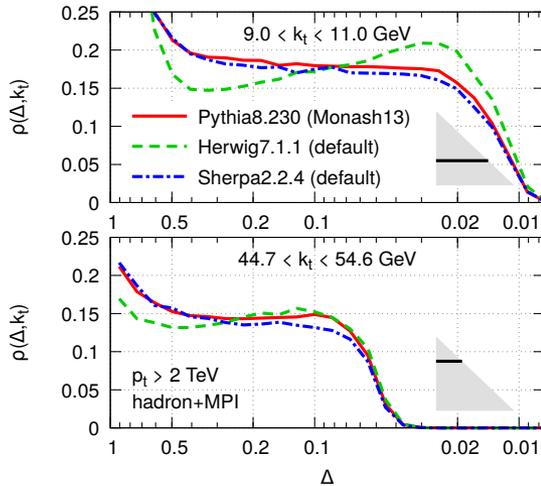
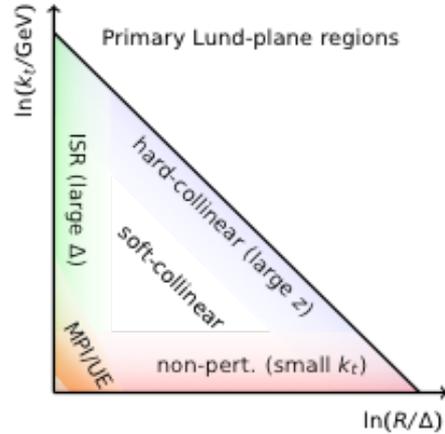
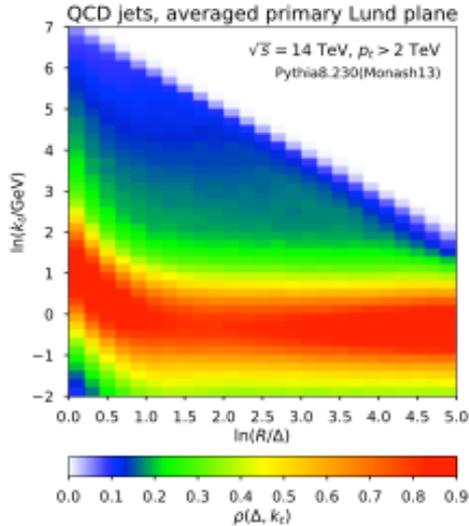
$$\rho \simeq \frac{\alpha_s(k_t) C_F}{\pi} \bar{z} (p_{gq}(\bar{z}) + p_{gq}(1 - \bar{z})), \quad \bar{z} = \frac{k_t}{p_{t,\text{jet}} \Delta}$$

# Jet Lund diagram

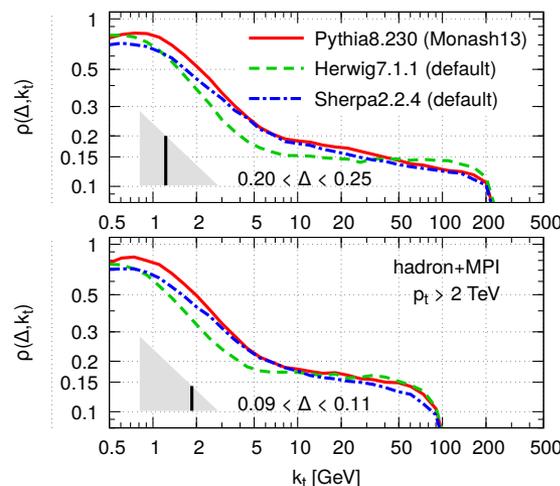
$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^3$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

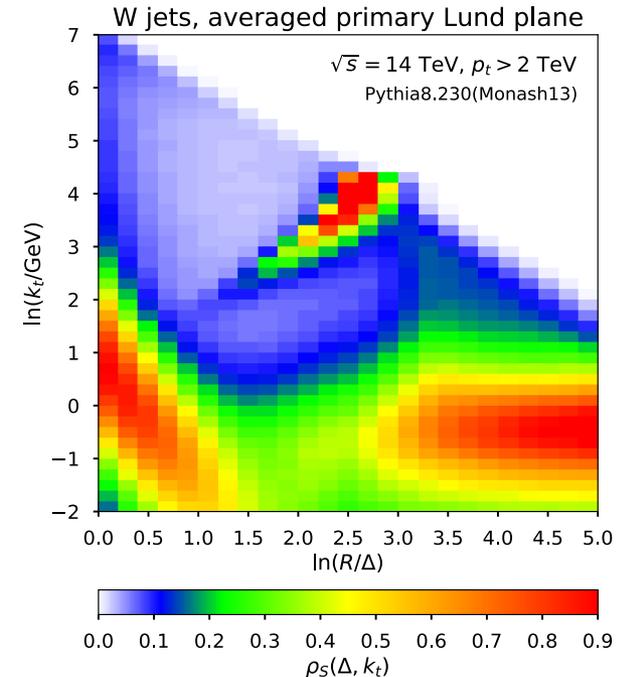
- Comparison of event generators
- Use for ML – jet ID (RHS below: boosted electroweak boson tagging at high momenta)



(a)

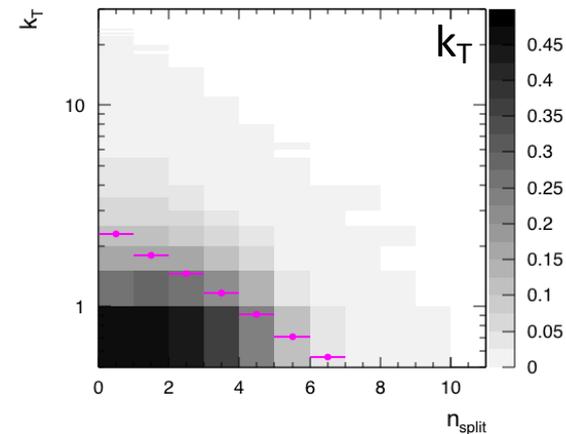
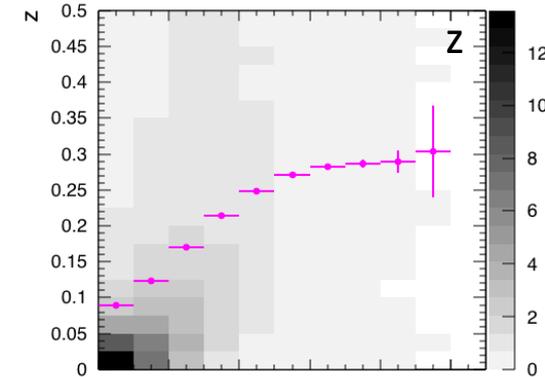
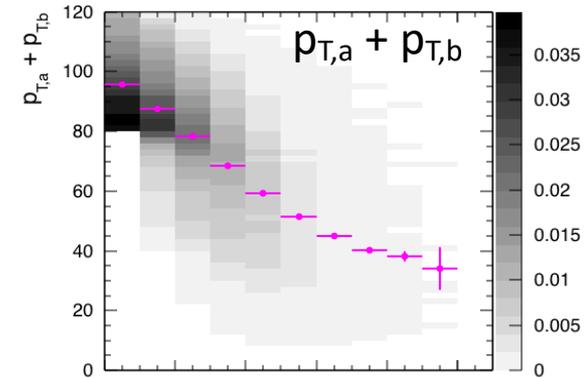
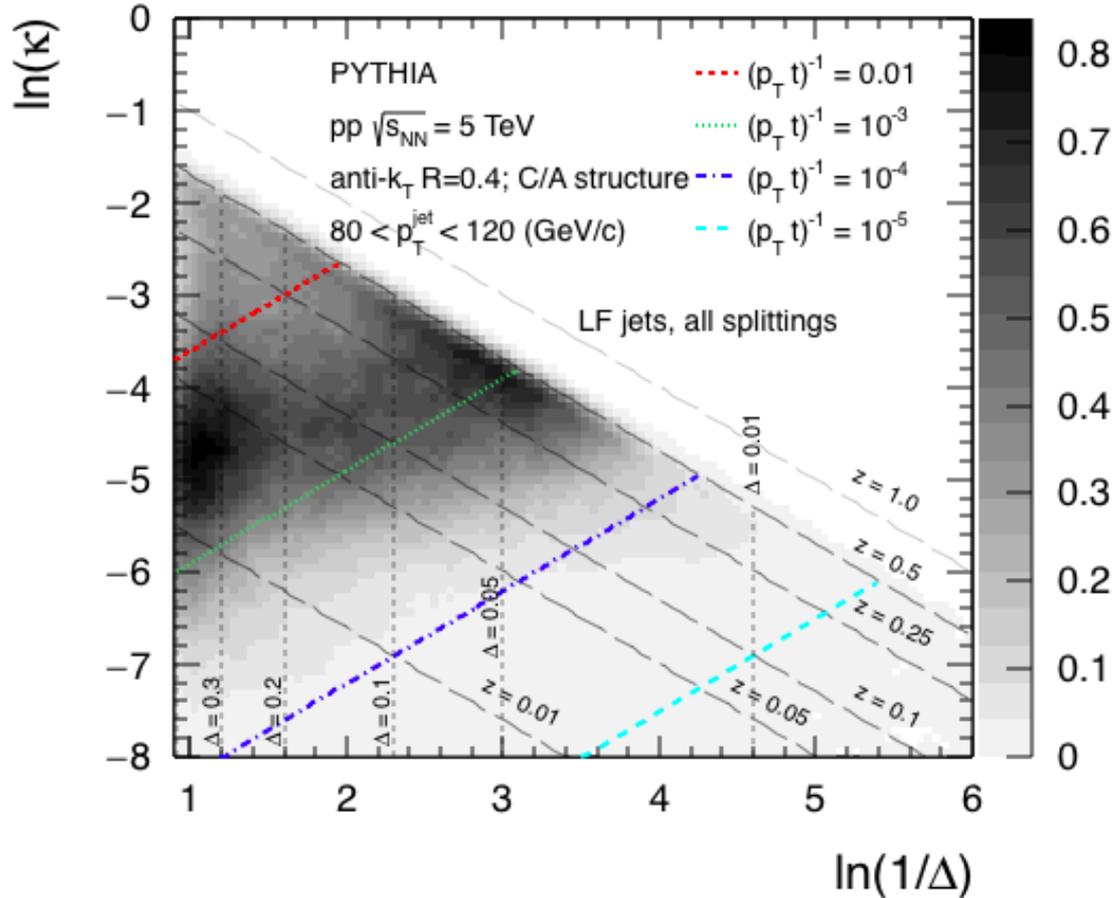


(b)

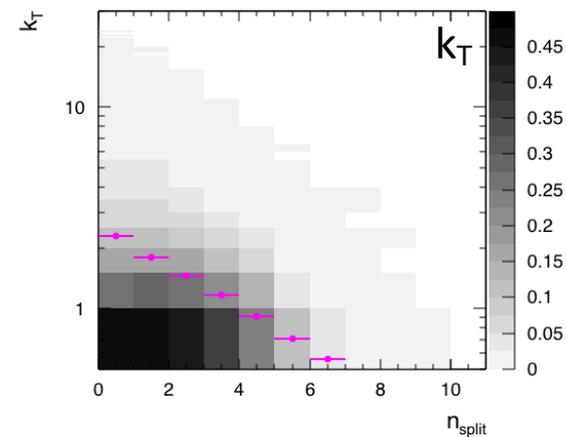
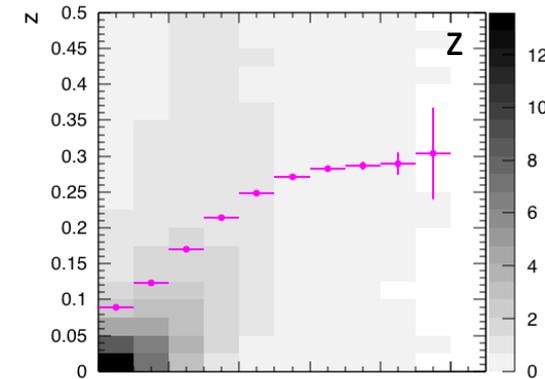
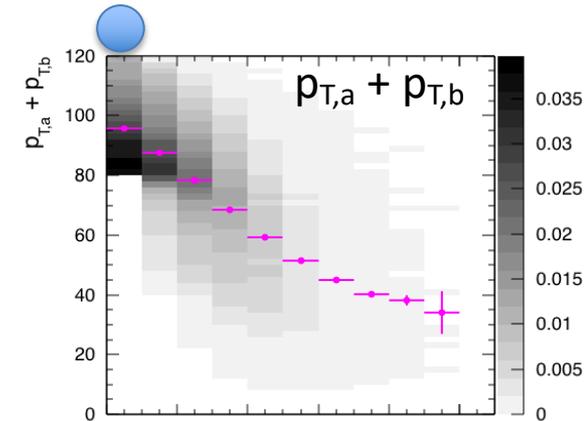
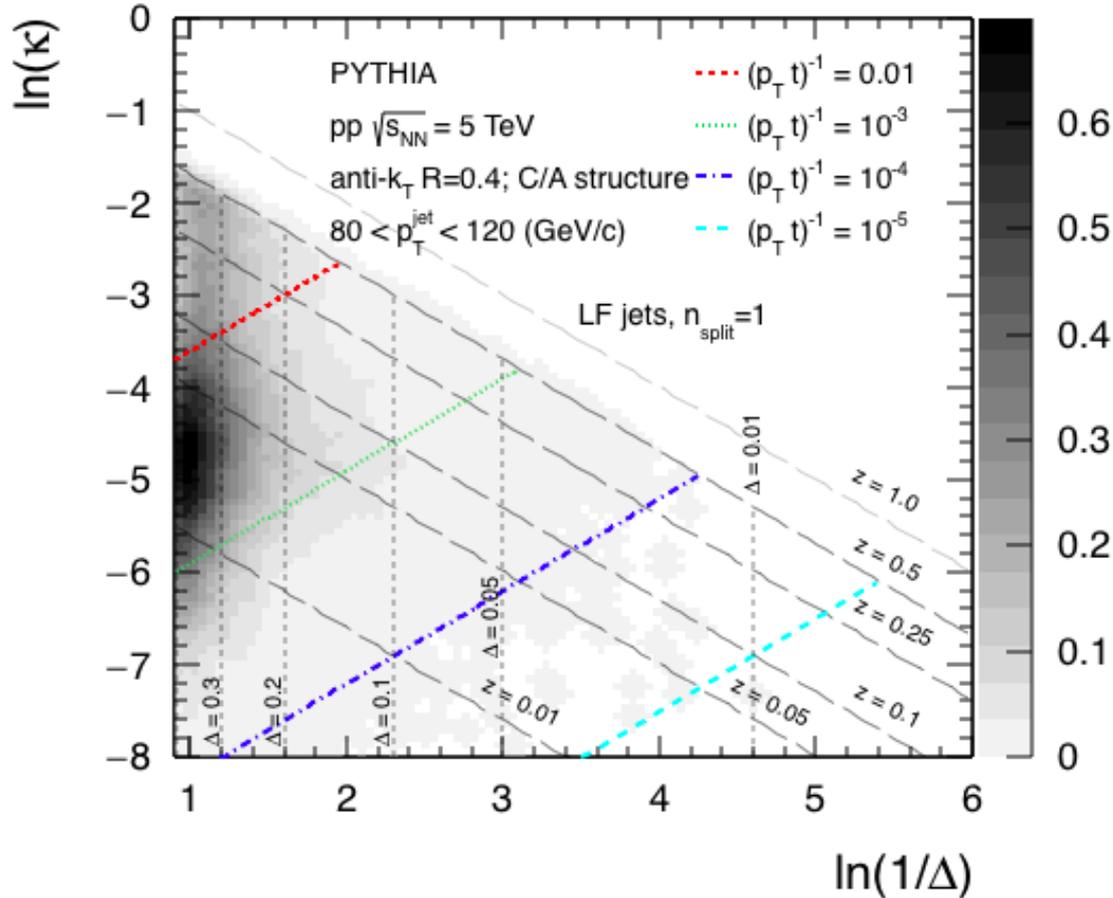


**Figure 3:** Emission density along slices of the Lund plane, at fixed  $k_t$  (top) and  $\Delta$  (bottom), comparing three event generators.

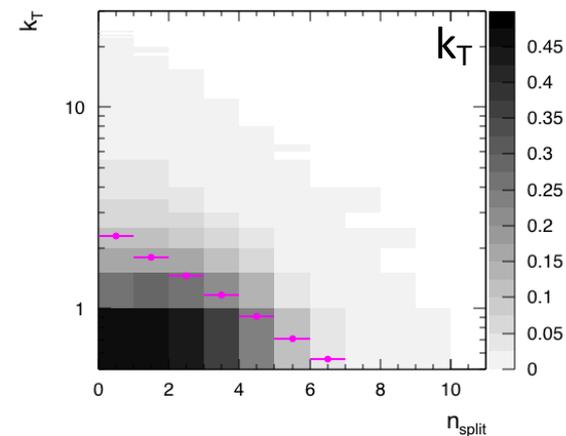
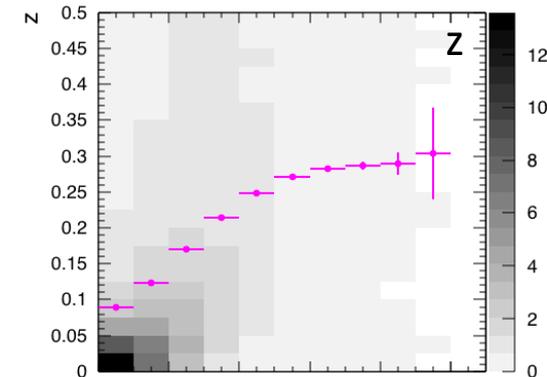
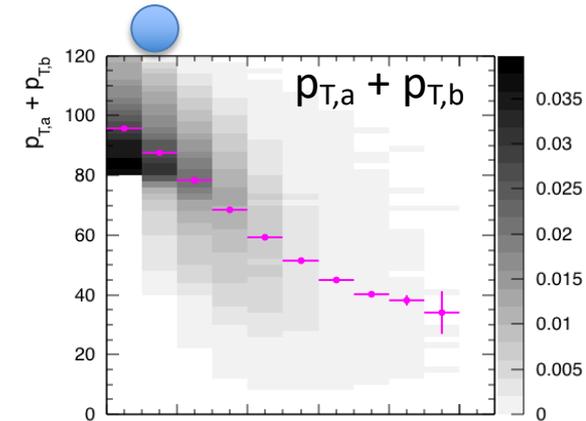
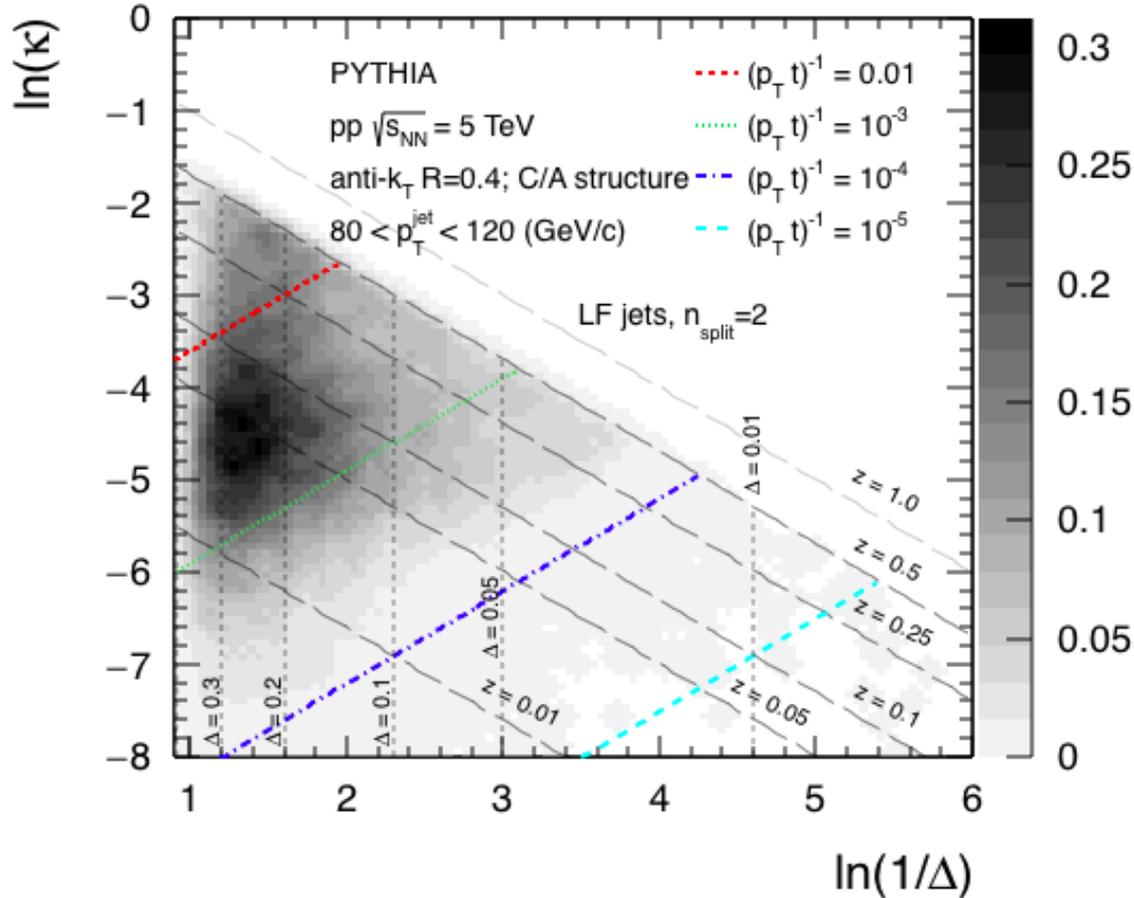
# Declusterization



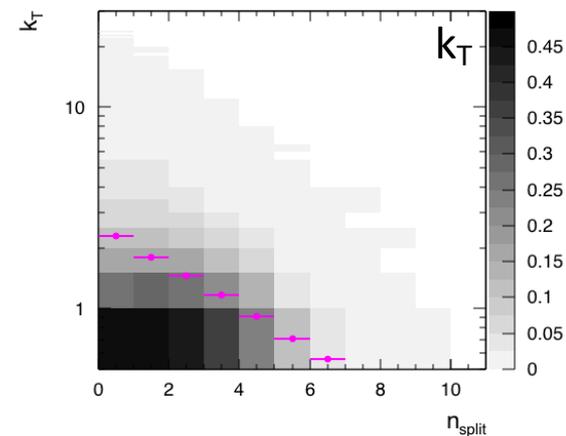
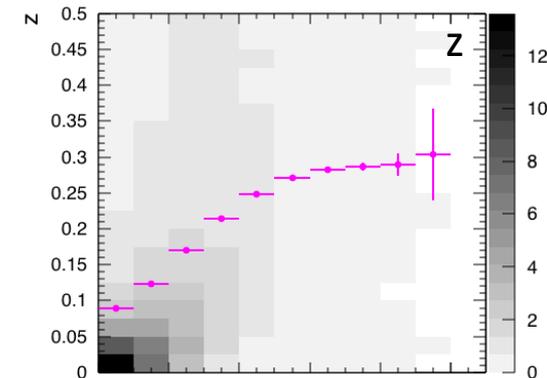
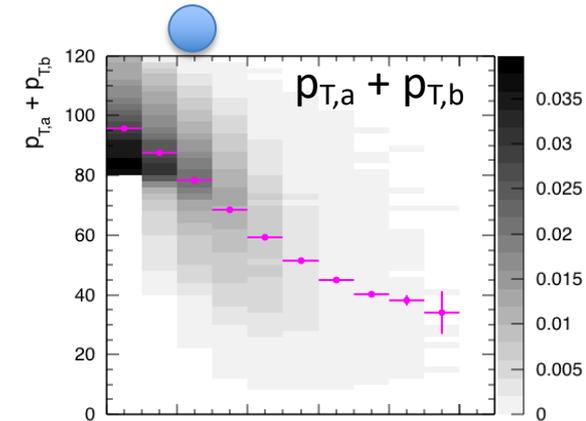
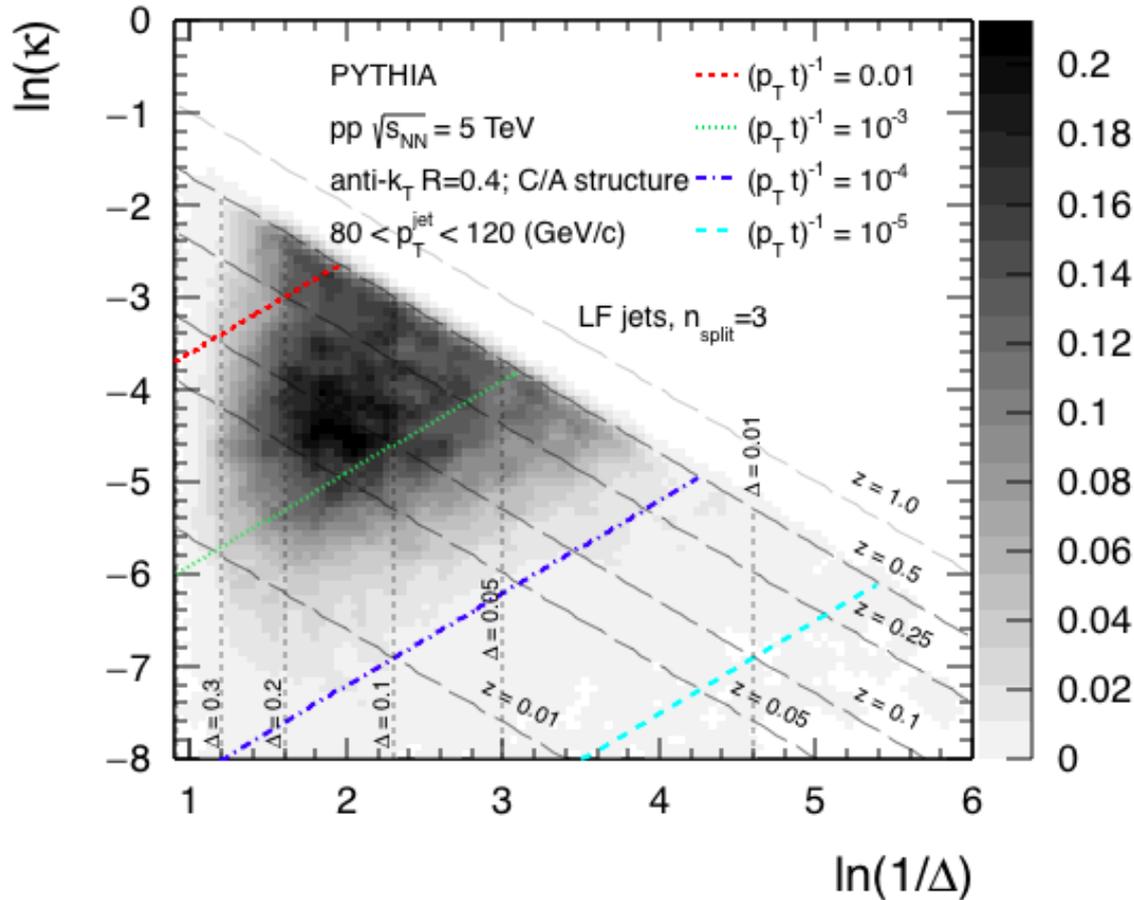
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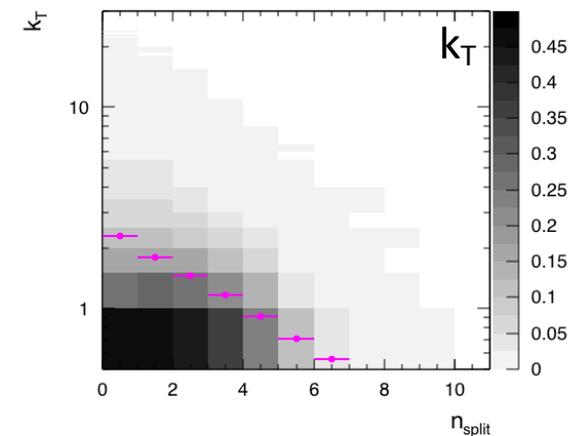
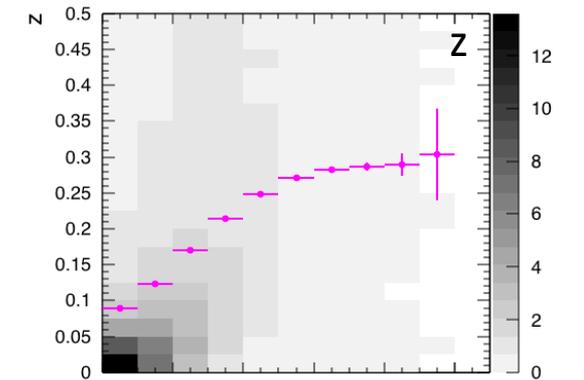
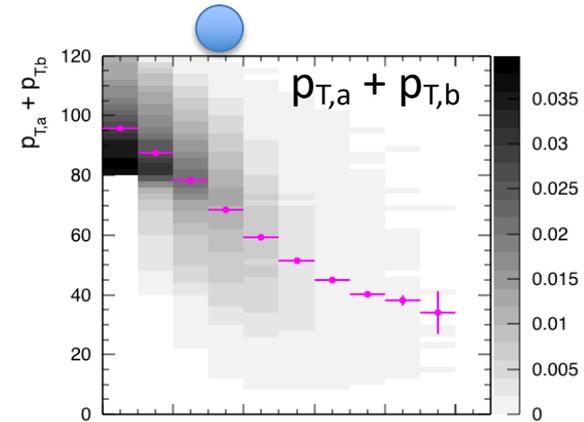
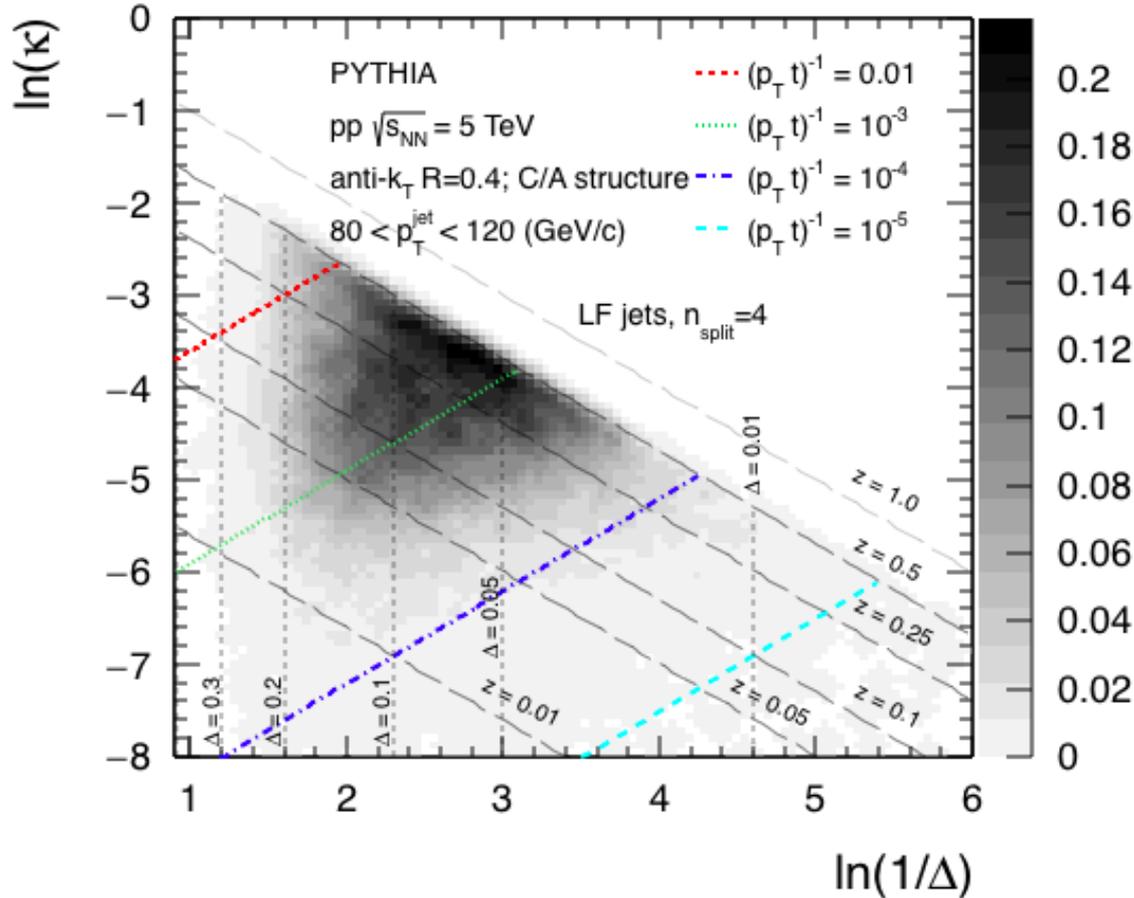
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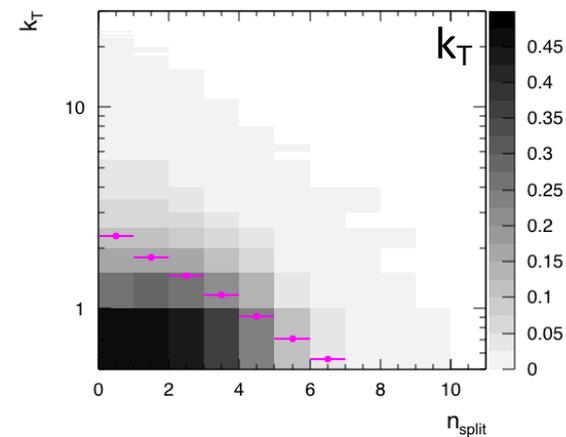
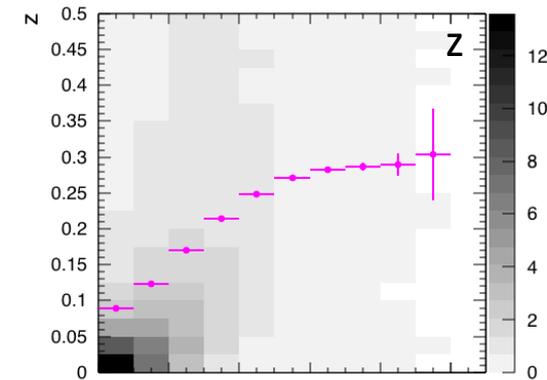
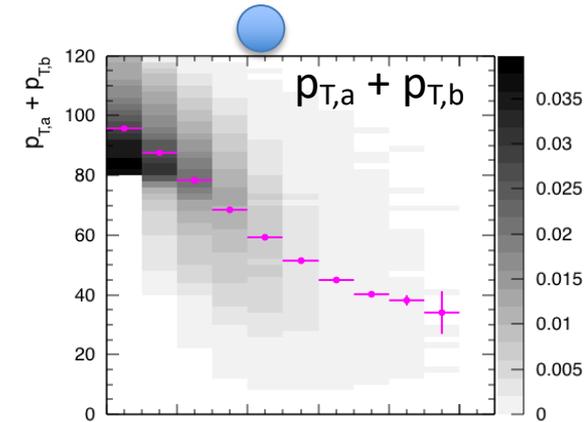
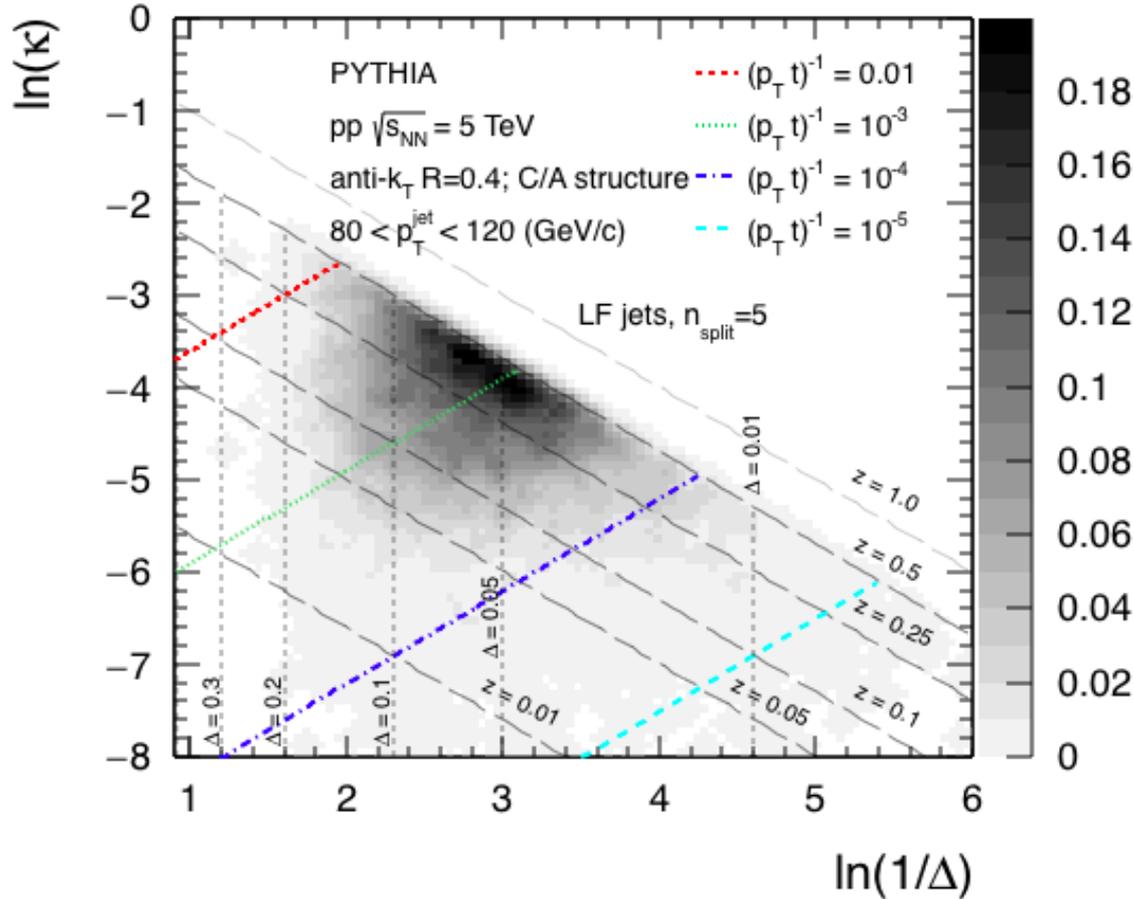
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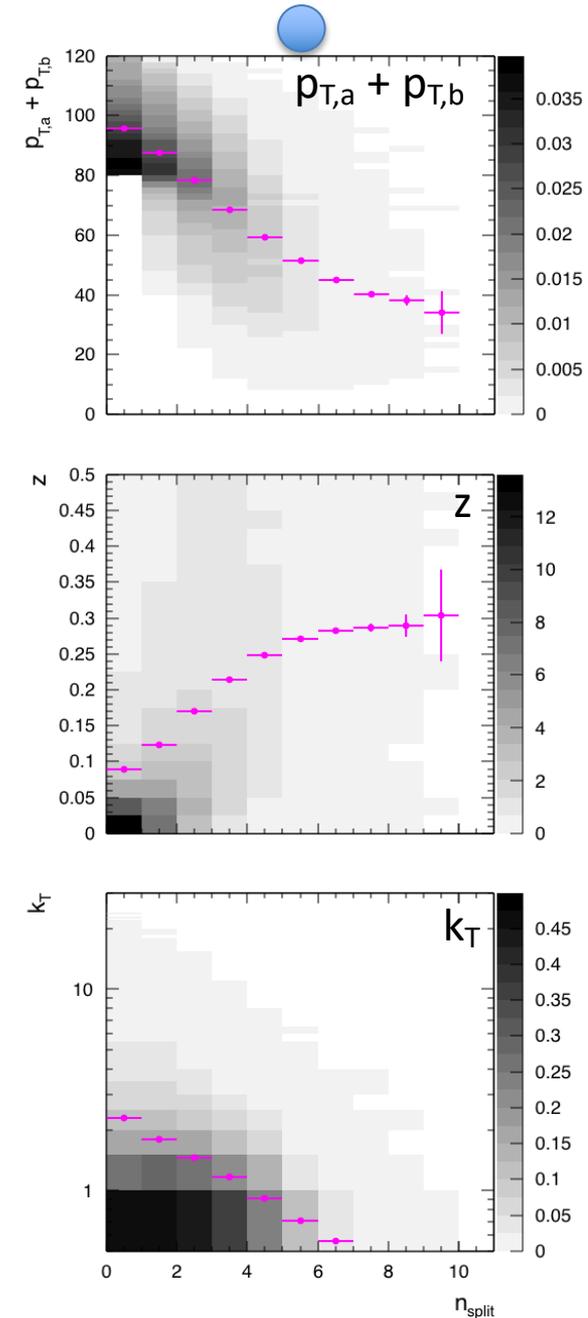
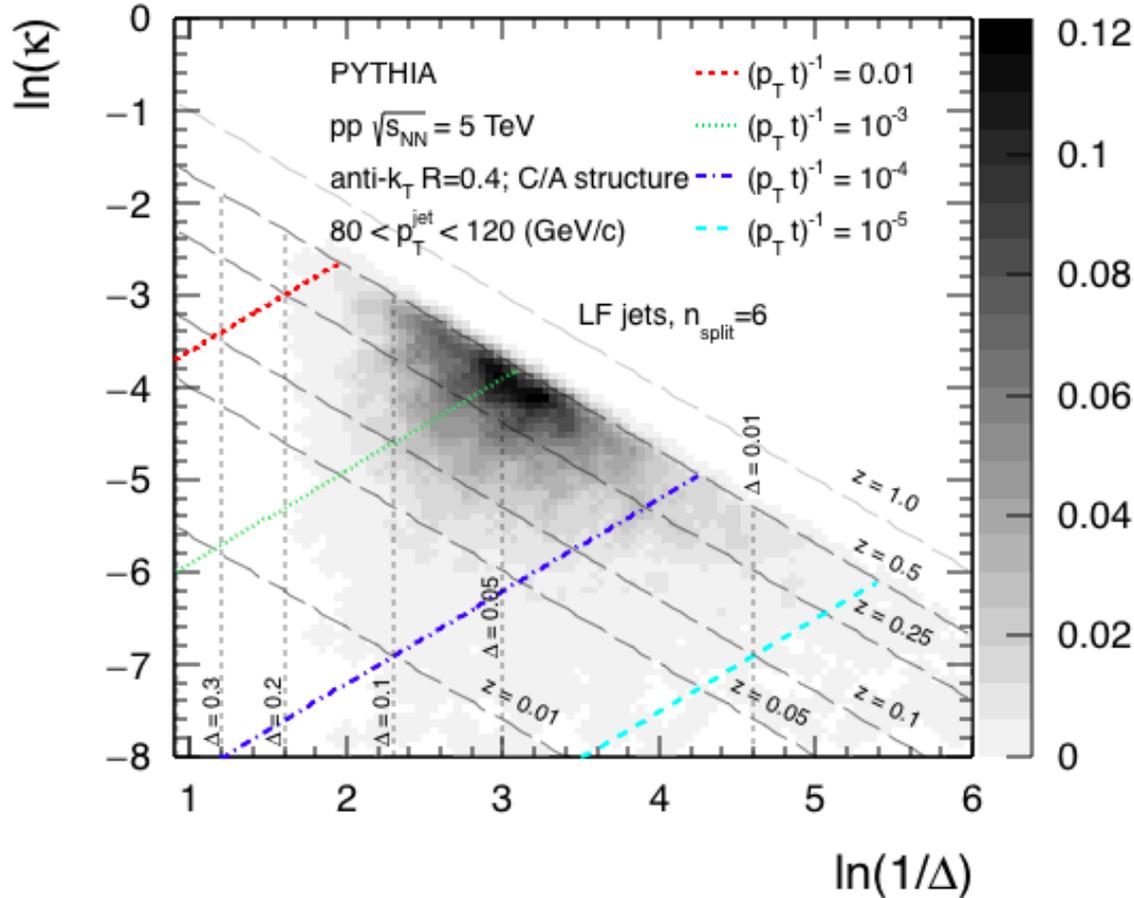
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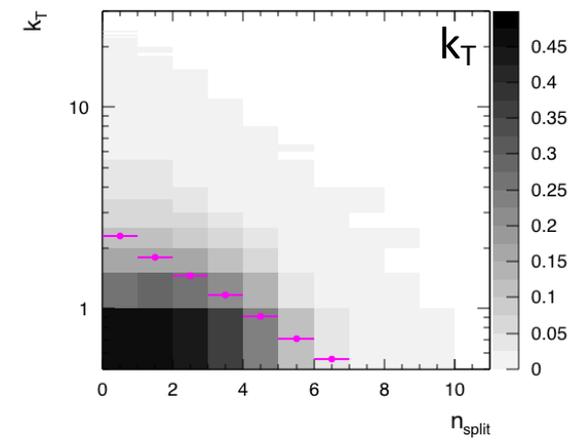
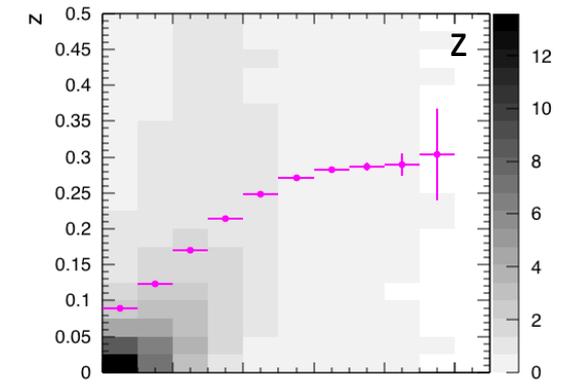
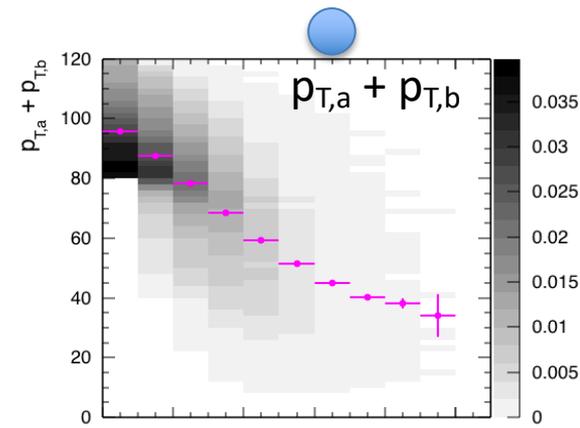
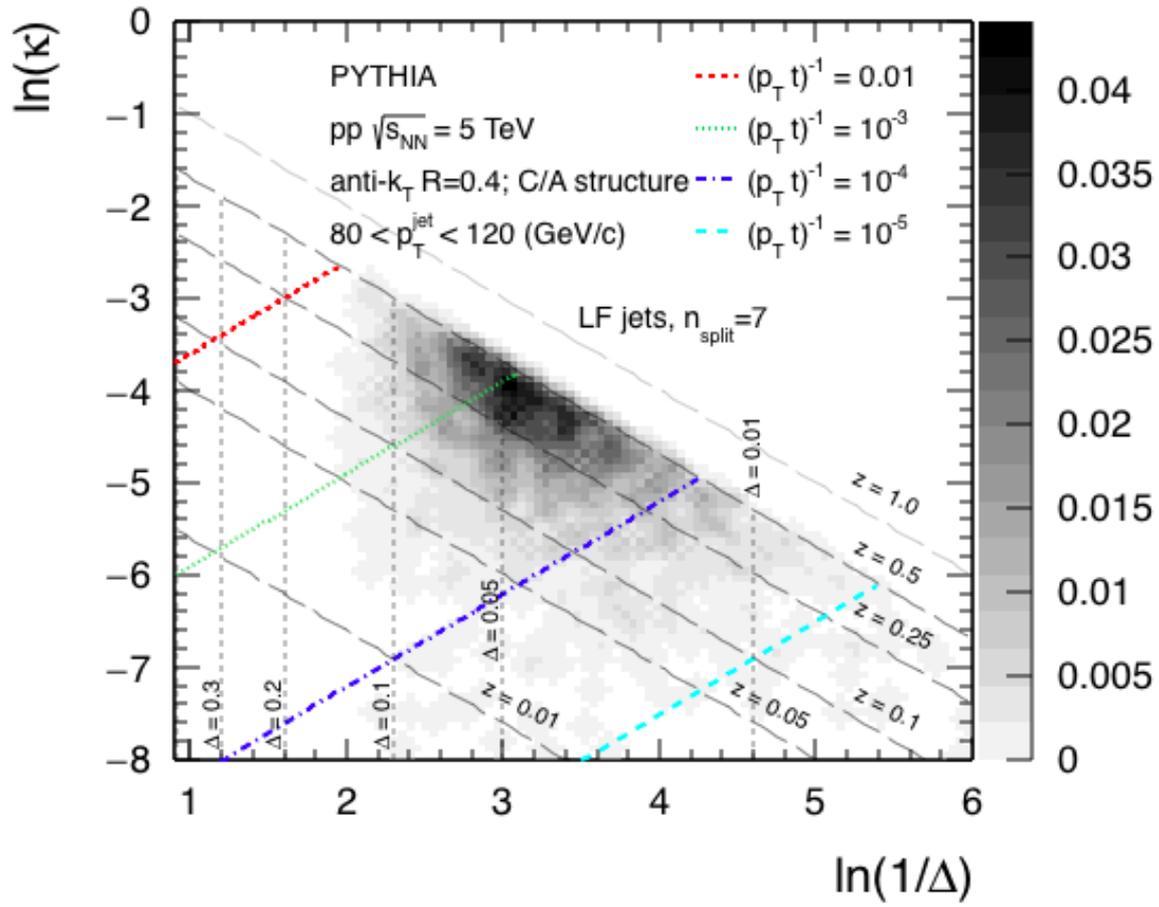
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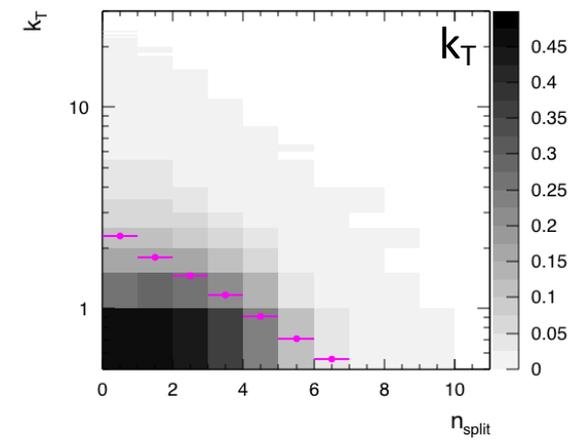
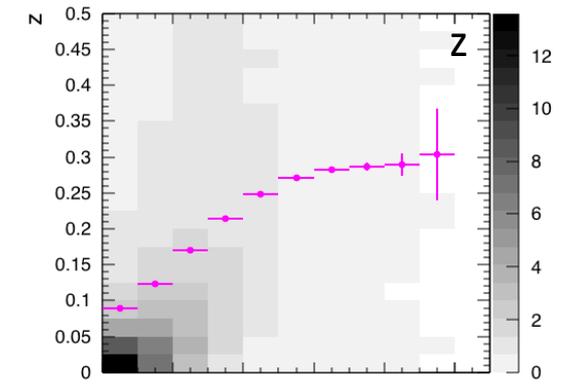
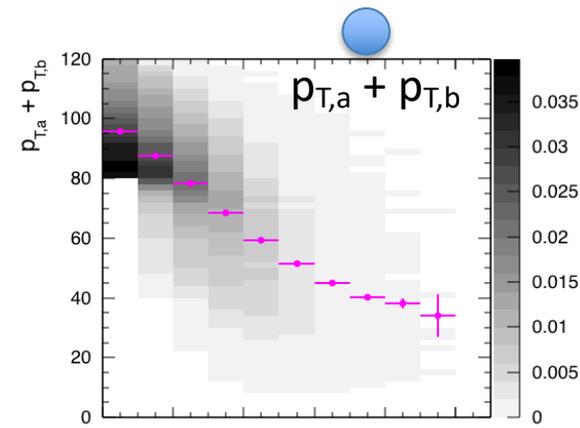
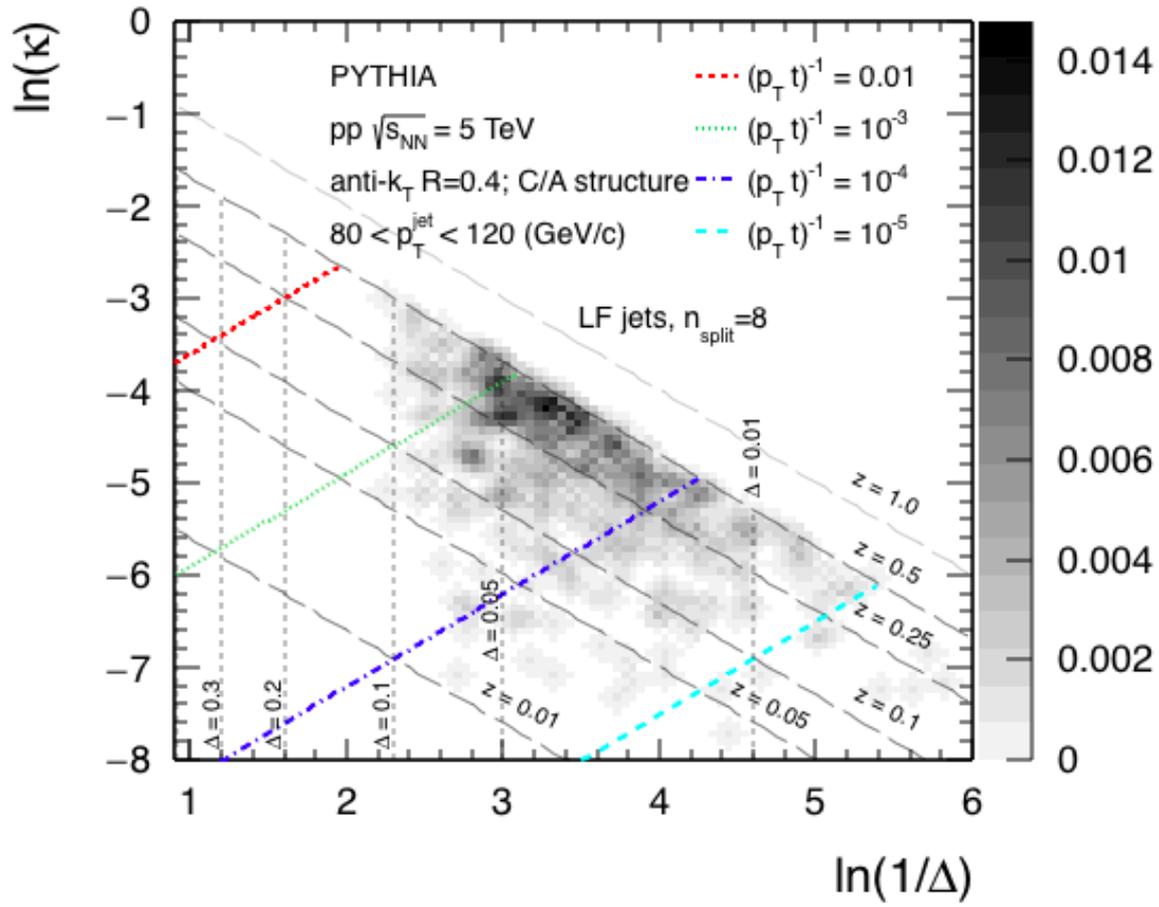
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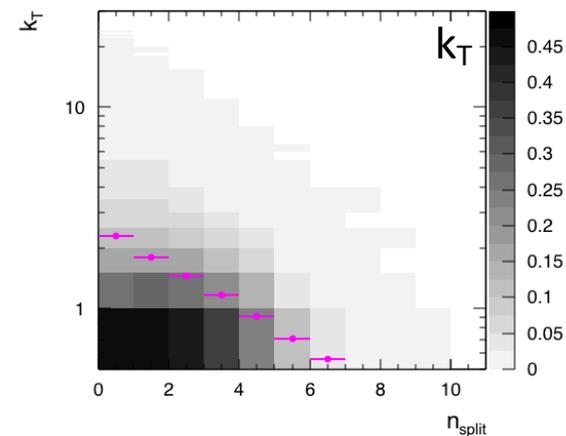
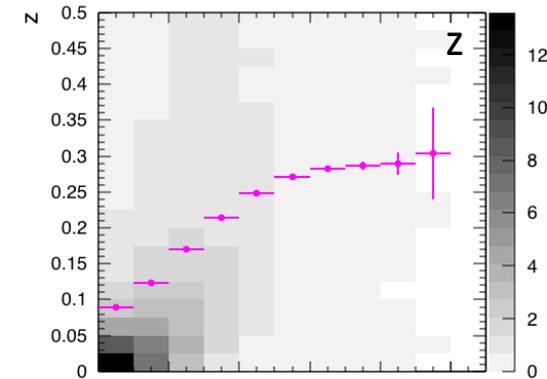
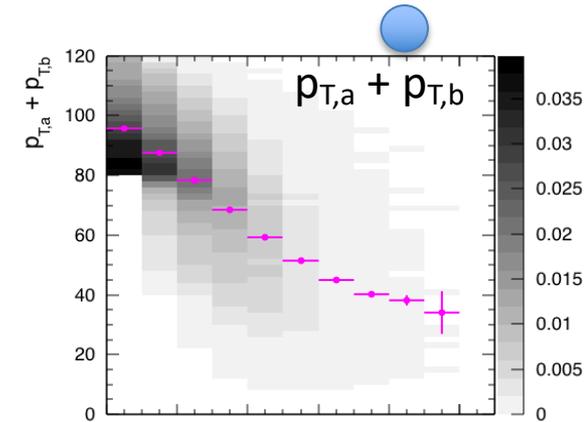
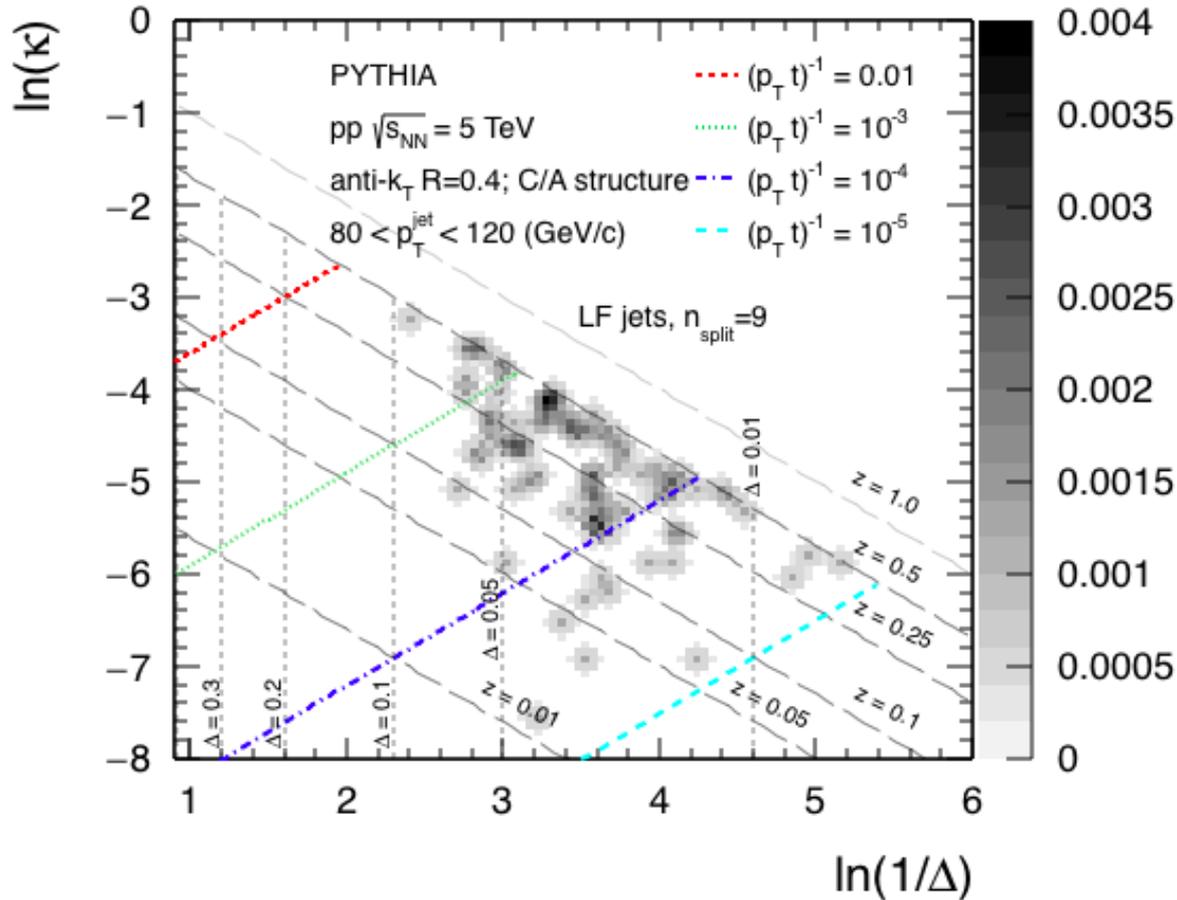
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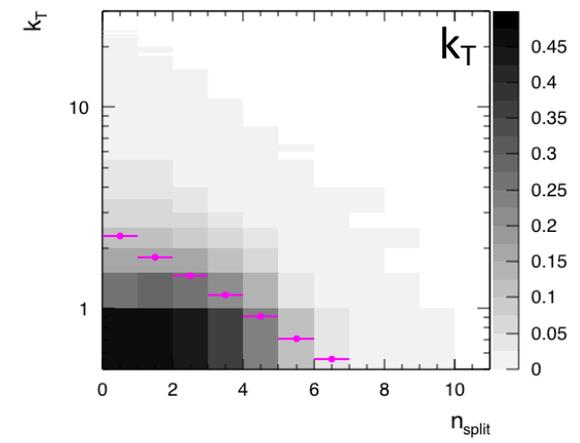
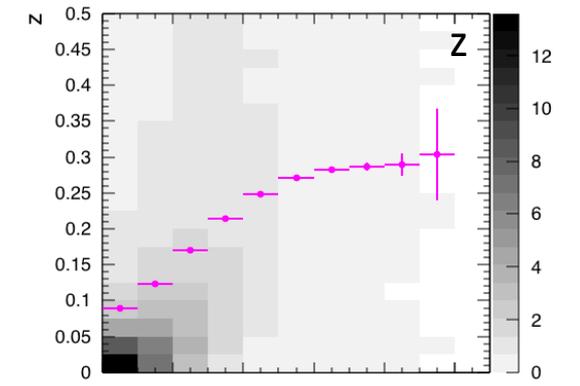
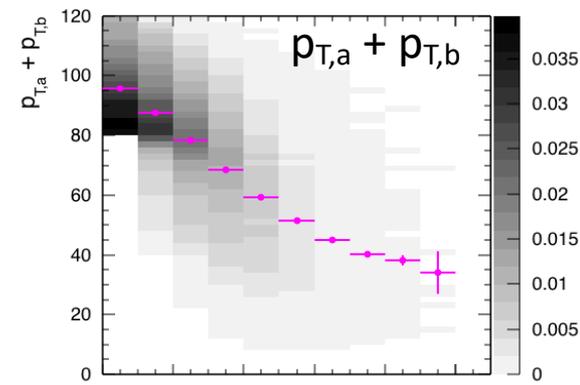
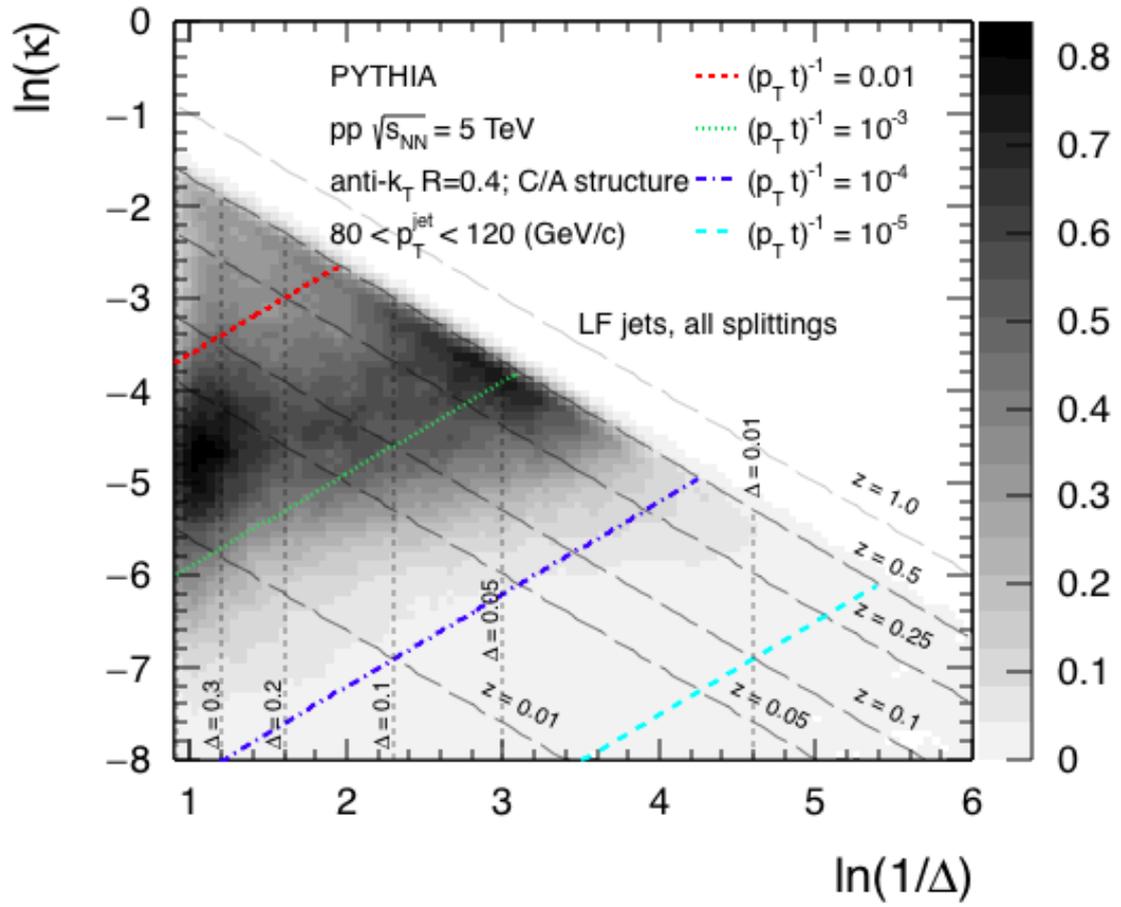
# Declusterization



# Declusterization



# Declusterization

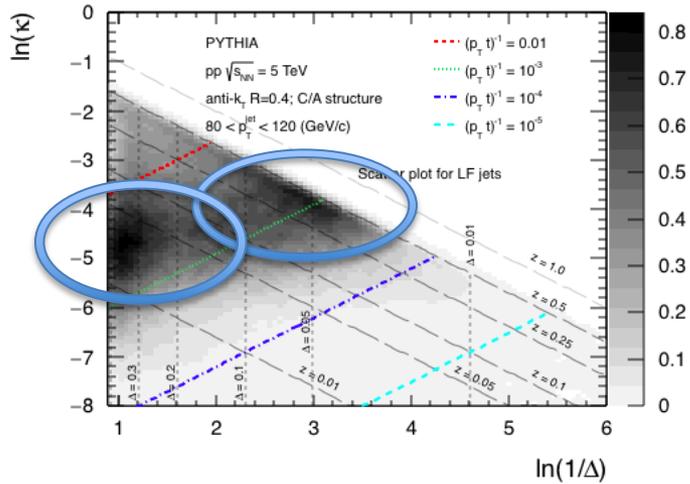


# Jet Lund diagram

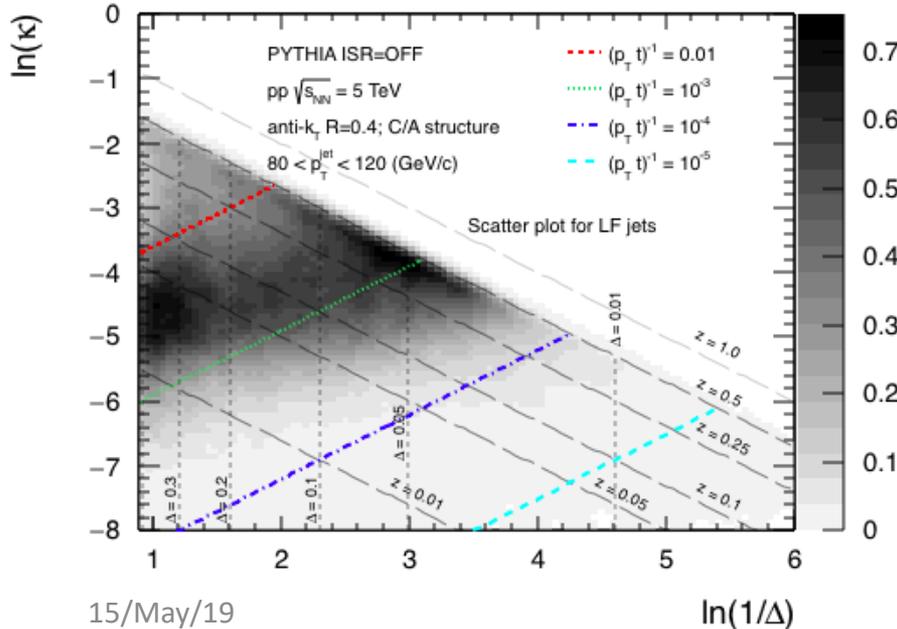
$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{15}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

Expectation: for every  $R$  and  $p_T$ , the phase space should be filled rather uniformly => the local max. at the max. angle is not expected.. The uniform distribution should be a feature of FSR...  
=> Structures to some degree a feature of UE (IR/MPIs)

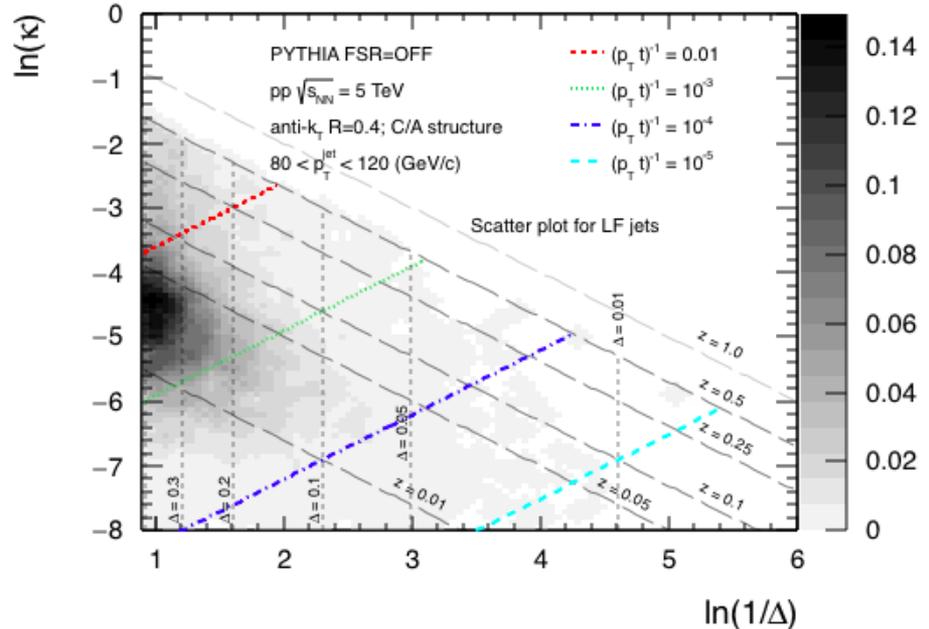


Initial State Radiation OFF



15/May/19

Final State Radiation OFF



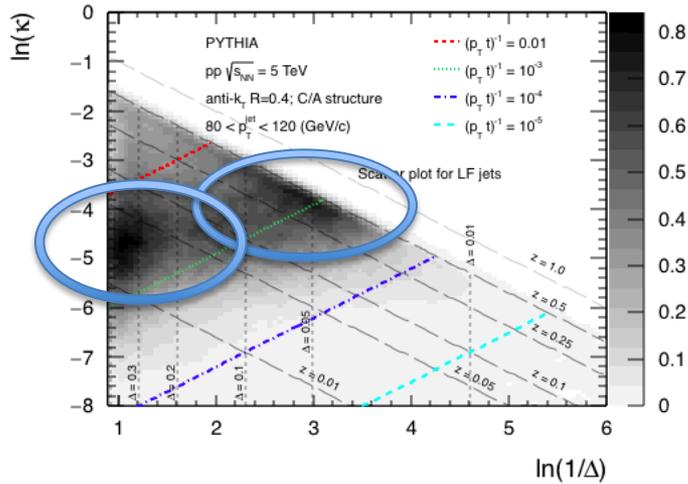
Tue 23/10/2018 09:32:16 CEST

# Jet Lund diagram

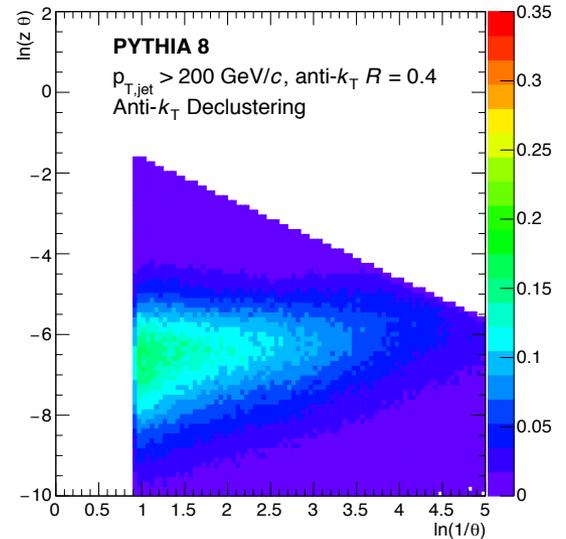
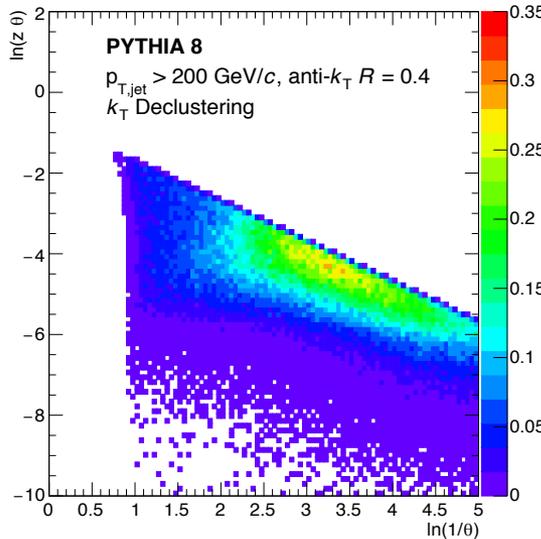
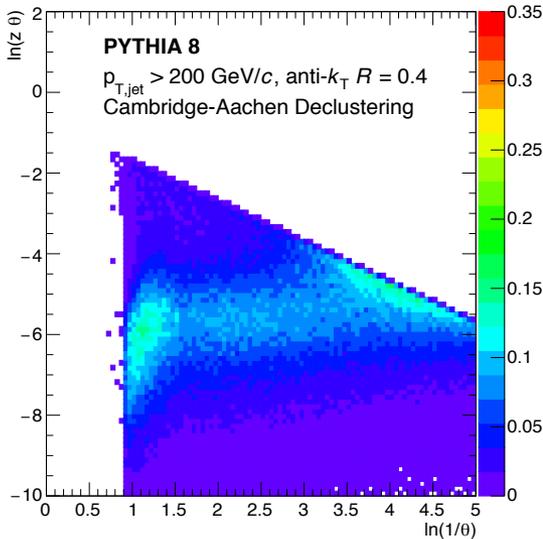
$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{16}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

Structures vary with the algorithm used – last year exercise – remember Frederic yesterday...



Tue 23/10/2018 09:35:11 CEST



<https://arxiv.org/pdf/1808.03689.pdf>

Figure 3: Lund diagrams reconstructed from a sample anti- $k_T$   $R = 0.4$  jets generated by PYTHIA8. Three reclustering strategies were considered: C/A (left),  $k_T$  (middle), and anti- $k_T$  (right).

15/May/19

# Jet

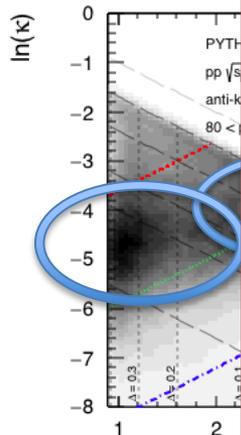
## Declustering other jet-algorithm sequences

F. Dreyer

- ▶ Choice of C/A algorithm to create clustering sequence related to physical properties and associated to higher-order perturbative structures
- ▶ anti- $k_t$  or  $k_t$  algorithms result in double logarithmic enhancements

$$\bar{\rho}_2^{(\text{anti-}k_t)}(\Delta, \kappa) \simeq +8C_F C_A \ln^2 \frac{\Delta}{\kappa}$$

$$\bar{\rho}_2^{(k_t)}(\Delta, \kappa) \simeq -4C_F^2 \ln^2 \frac{\Delta}{\kappa}$$



$$\frac{d^2\sigma_{T,b}}{d\ln 1/\Delta} \Delta_{ab}^{17}$$

eric

Tue 23/10/2018 09:35:11 CEST

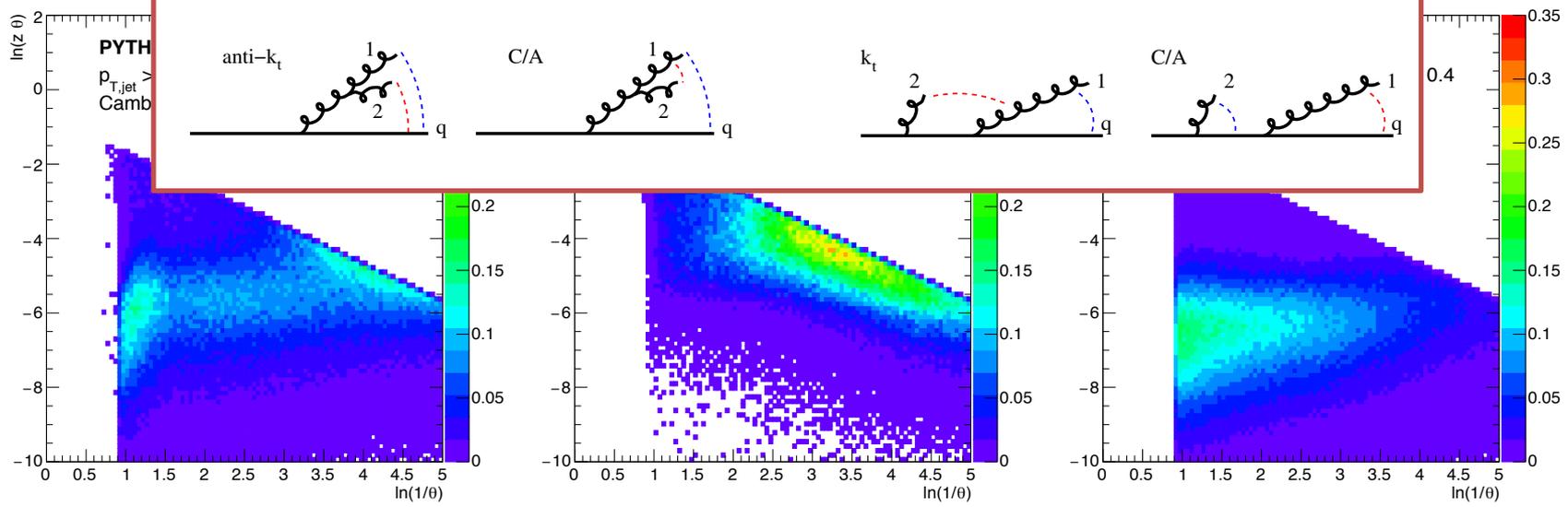


Figure 3: Lund diagrams reconstructed from a sample anti- $k_T$   $R = 0.4$  jets generated by PYTHIA8. Three reclustering strategies were considered: C/A (left),  $k_T$  (middle), and anti- $k_T$  (right).

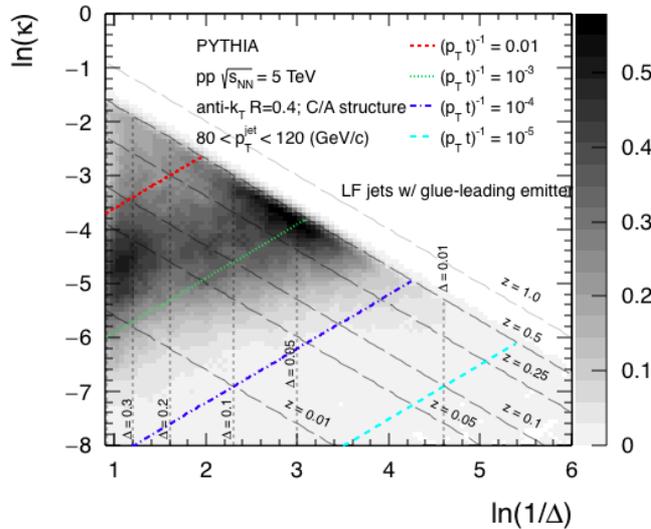
15/May/19

# Notes on heavy-quarks

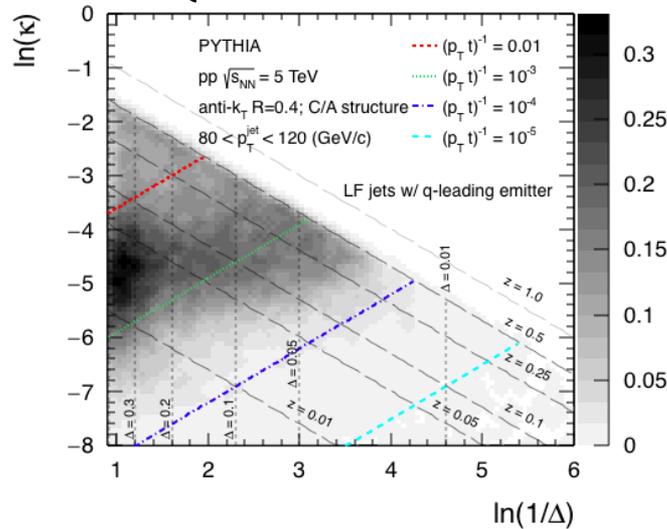
$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}^{18}}{d \ln \kappa d \ln 1/\Delta}$$

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}$$

## Gluon



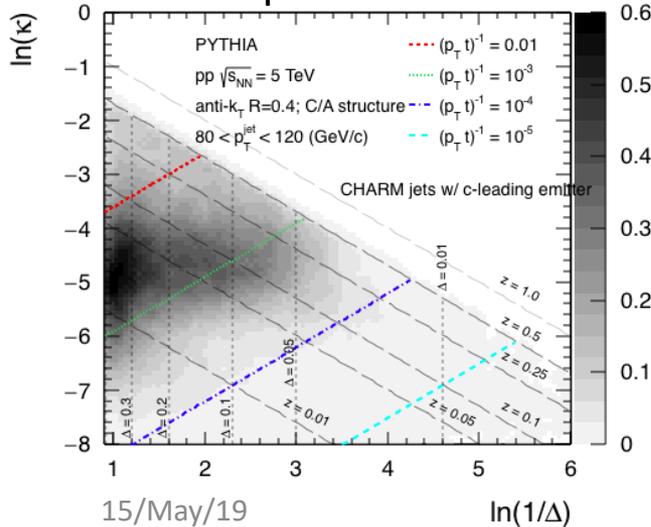
## LF Quark



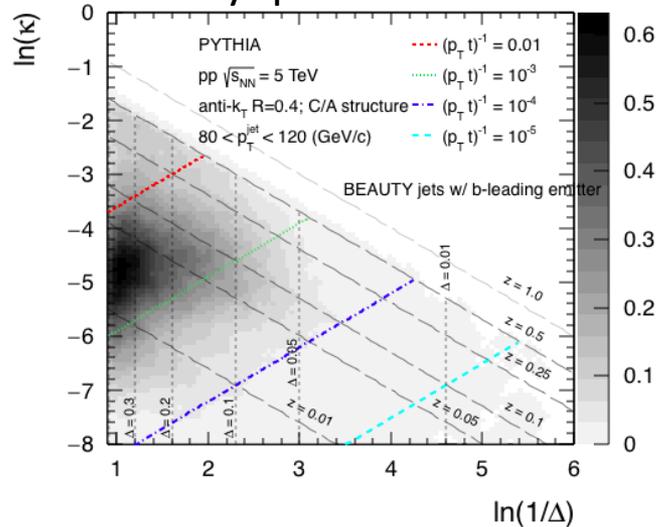
Purely MC exercise – compare LF to HF jets

An approximation:  
- use the leading parton within the emitter (follow Q)

## Charm quark



## Beauty quark



Opportunity? – explore with Machine Learning

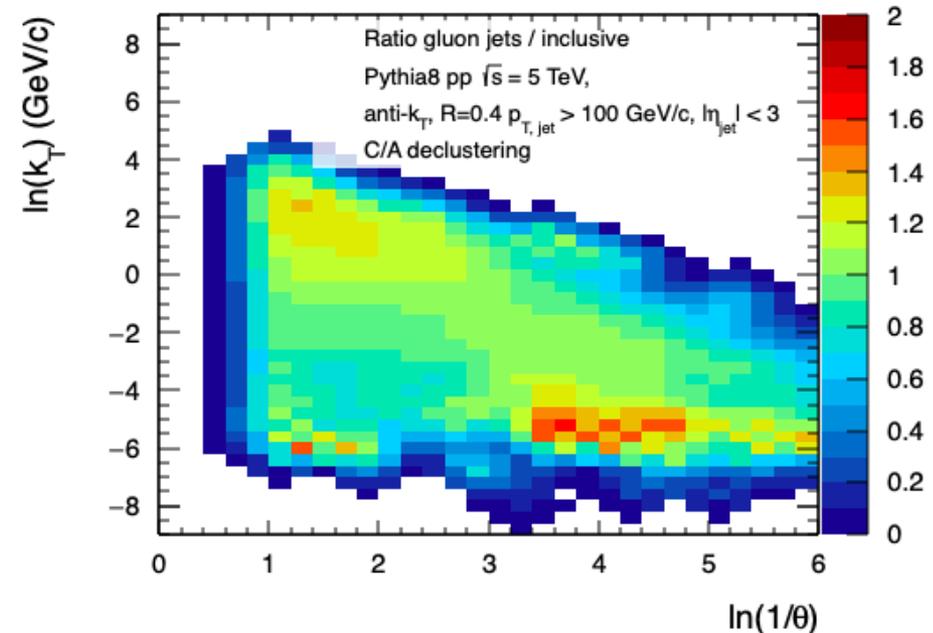
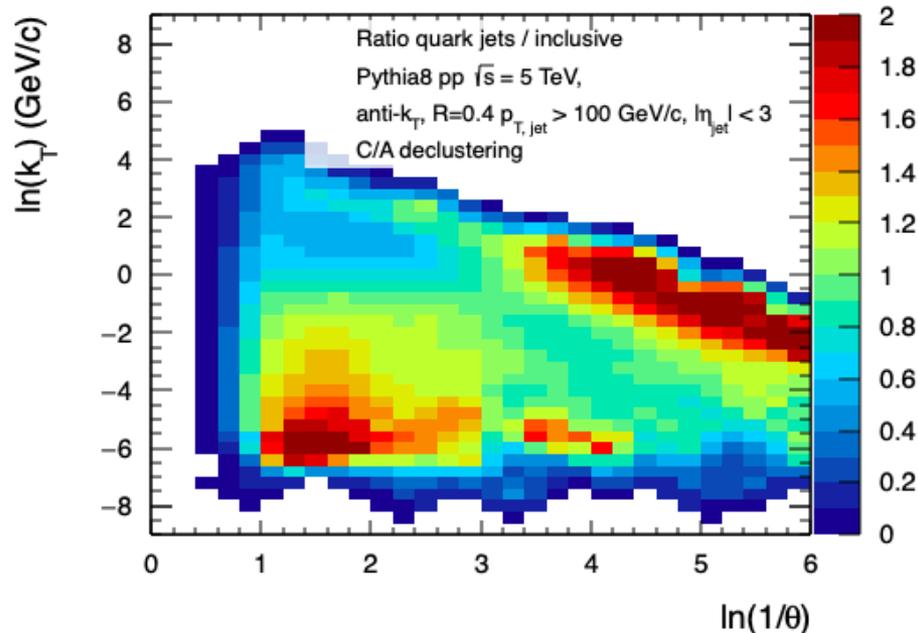
Jet quenching – detail studies of mass dependence of energy loss?

To be learned: gluon splitting contribution...

# Quark and gluon jets...

Quark / inclusive

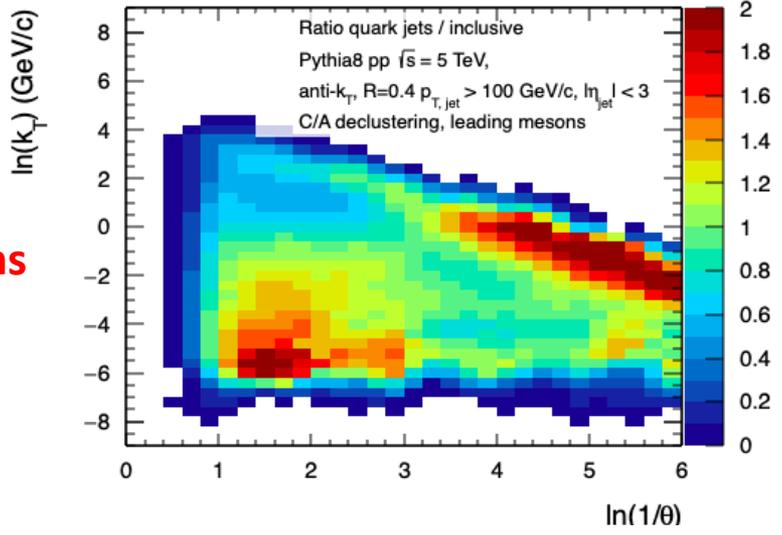
Gluon / inclusive



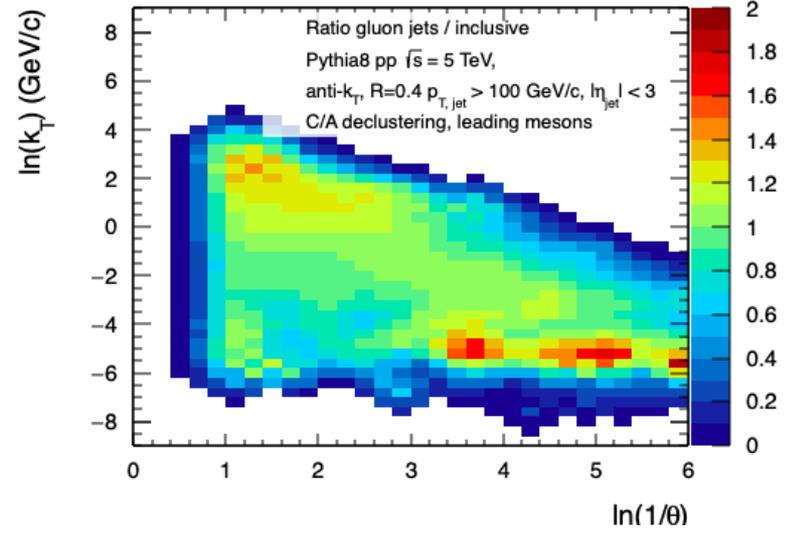
Quark jets as compared to gluons jets: harder fragmentation; more collimated  
 - To explore: what jet quenching does to such these distributions - what effects measurable / what is calculable? -> Felix et al.?

# Leading mesons and baryons – quark and gluon jets... Ratios for leading mesons and baryons

### Quark / inclusive

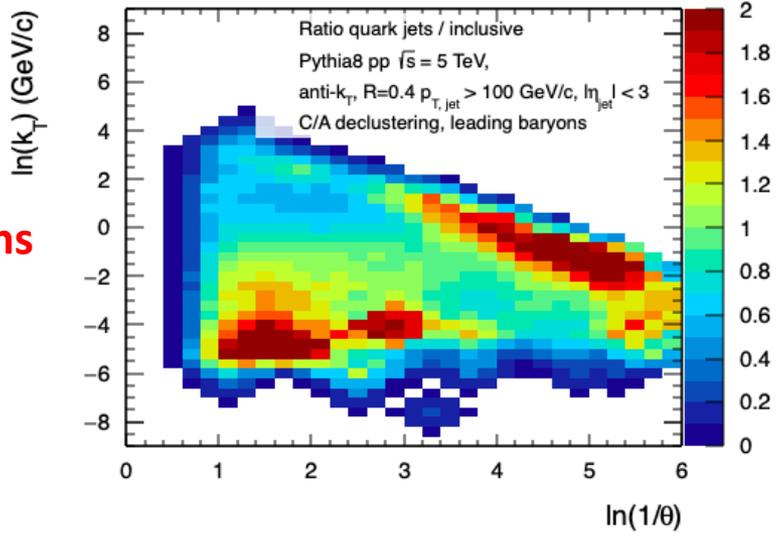


### Gluon / inclusive

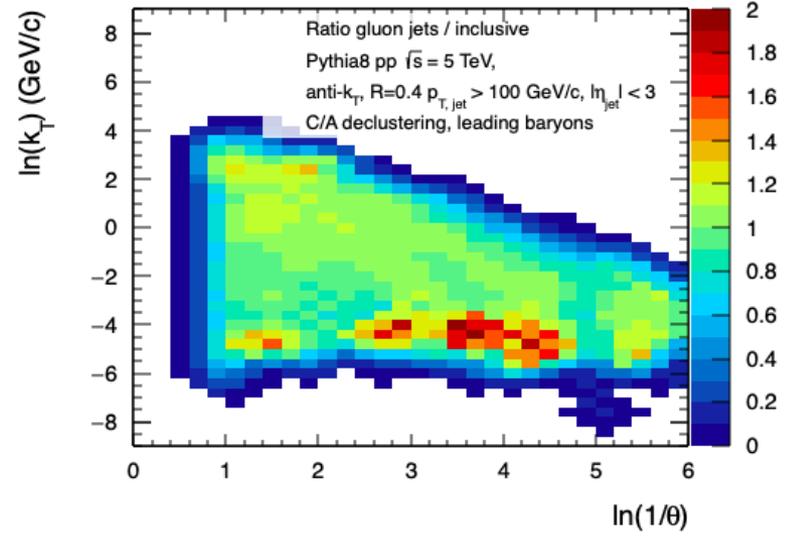


Lead mesons

### Quark / inclusive



### Gluon / inclusive



Lead baryons

# **JET QUENCHING – A QUICK STUDY**

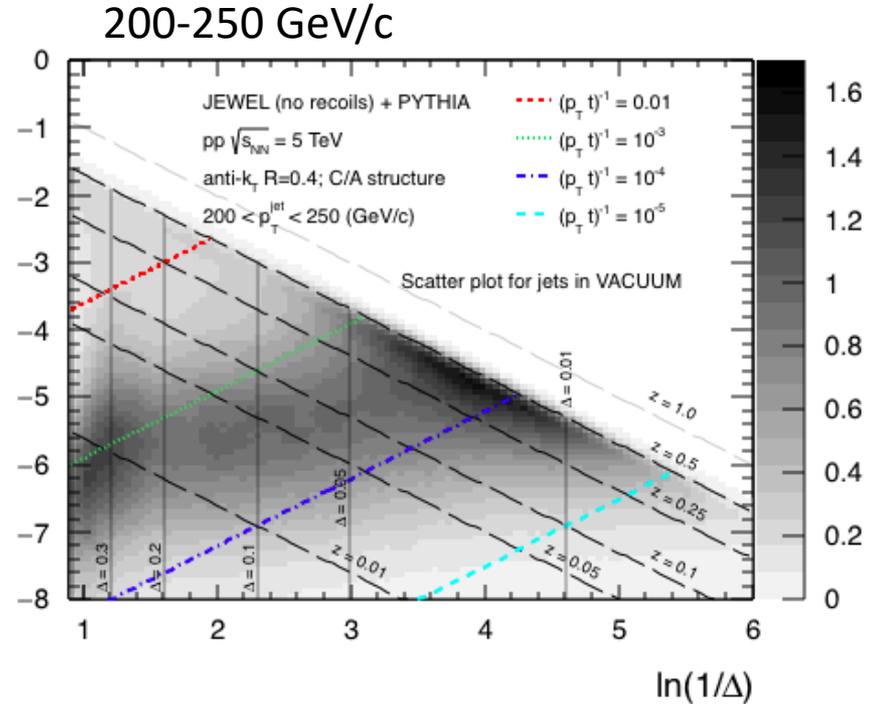
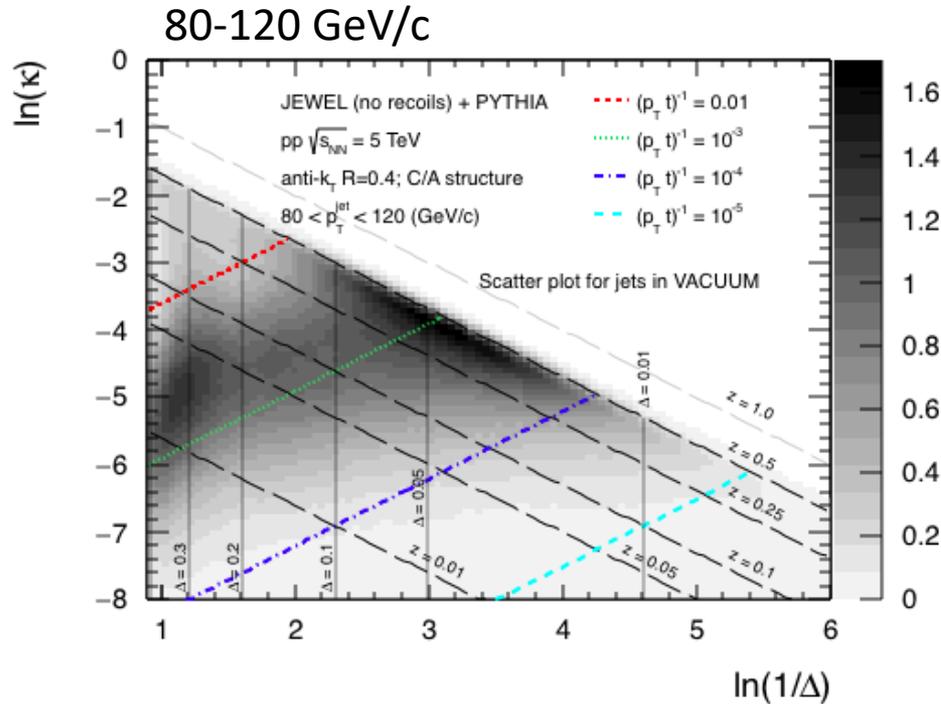
<https://arxiv.org/pdf/1812.06772.pdf>

# Jet Lund diagram

JEWEL + PYTHIA (RECOIL=OFF)  
 10% most central PbPb at 5 TeV  
 VACUUM

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{22}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

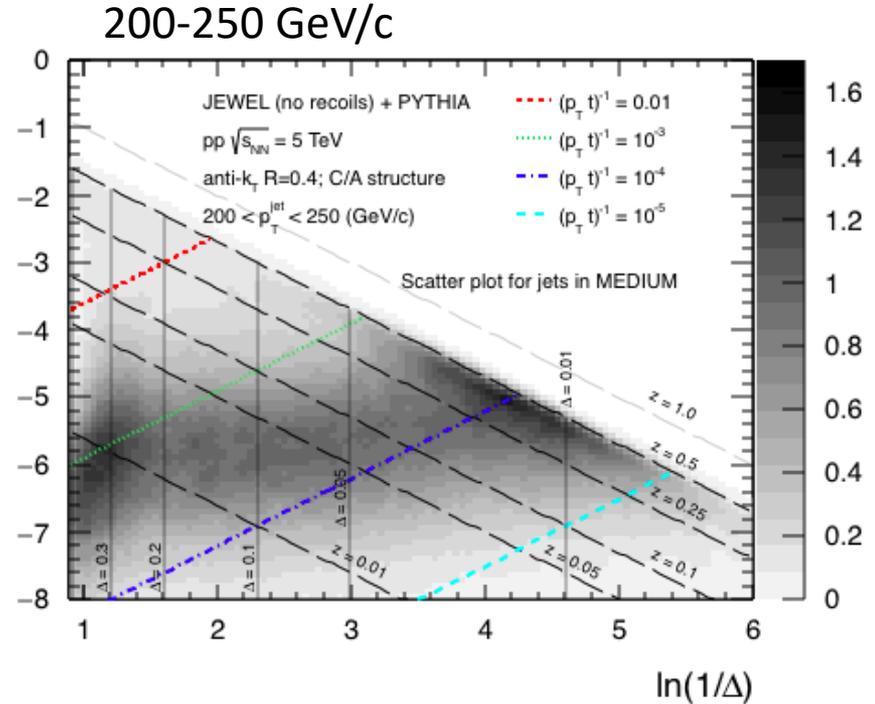
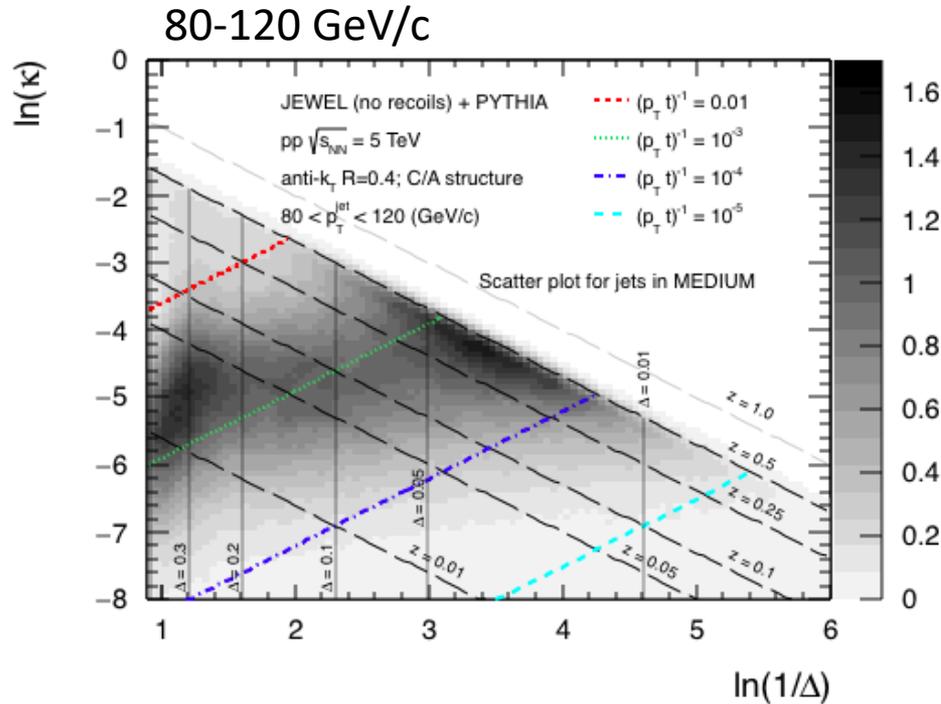


# Jet Lund diagram

JEWEL + PYTHIA (RECOIL=OFF)  
 10% most central PbPb at 5 TeV  
**MEDIUM**

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{23}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

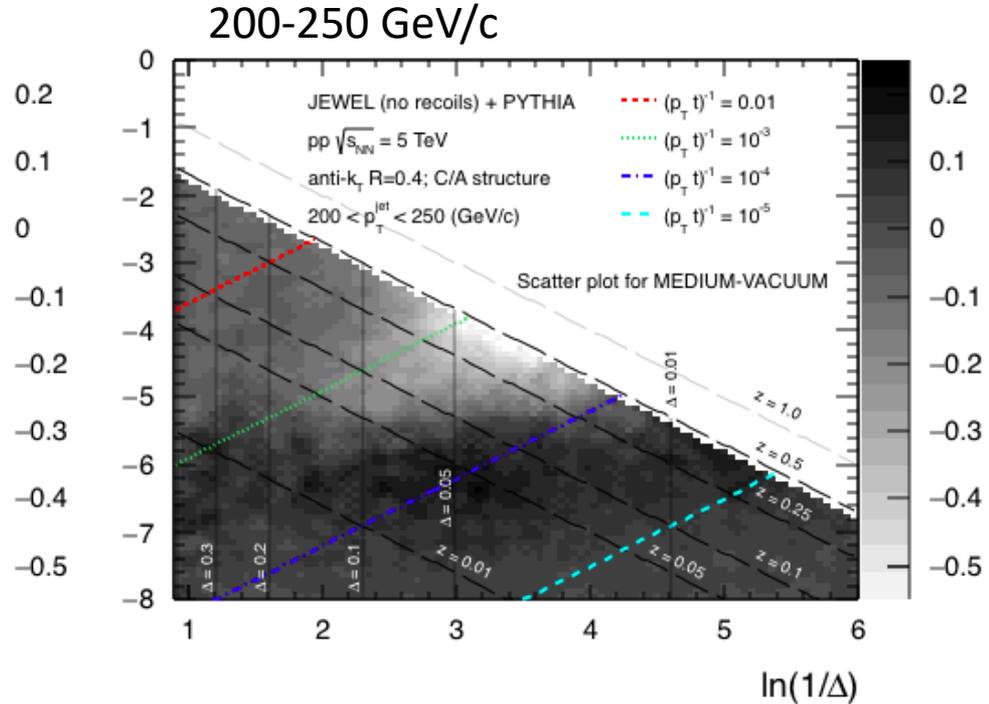
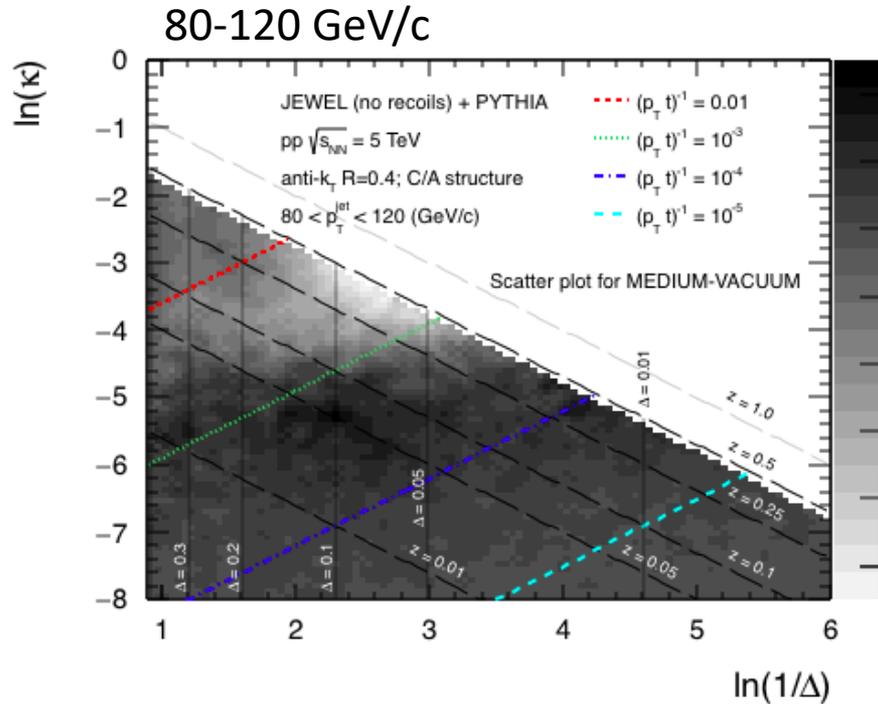


# Jet Lund diagram

JEWEL + PYTHIA (RECOIL=OFF)  
 10% most central PbPb at 5 TeV  
**MEDIUM - VACUUM**

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{24}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$

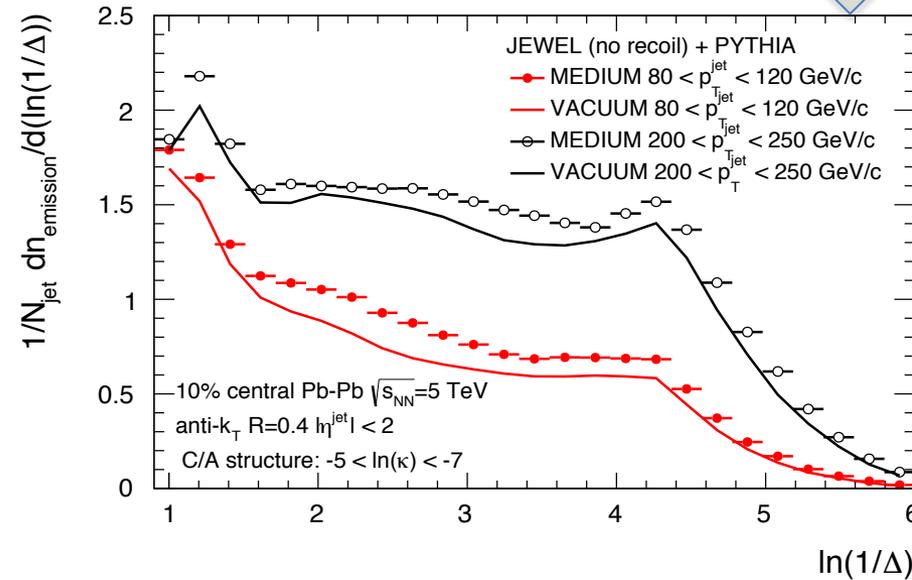
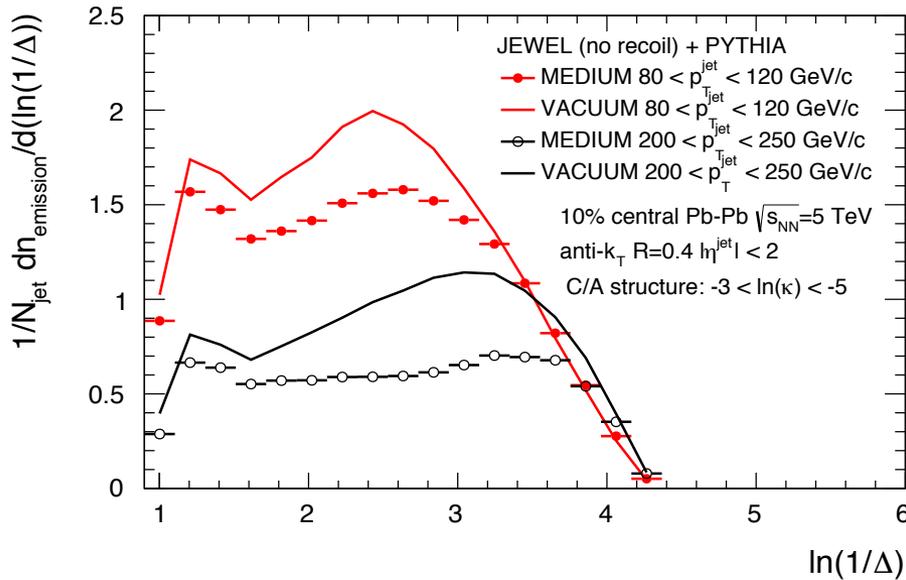
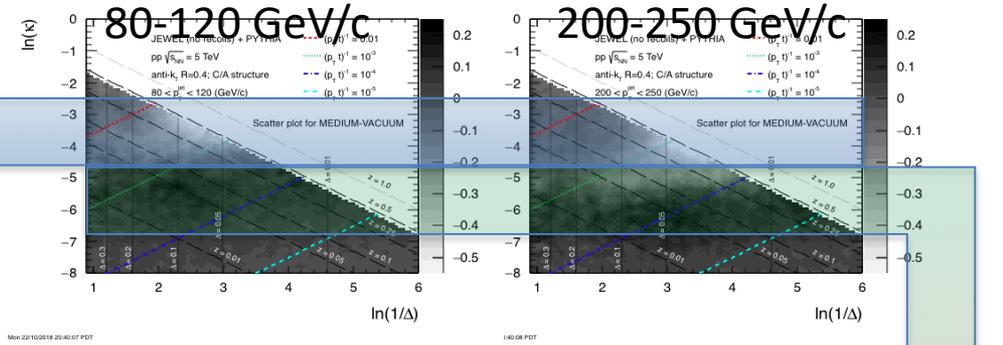


# Jet Lund diagram

JEWEL + PYTHIA (RECOIL=OFF)  
 10% most central PbPb at 5 TeV  
**MEDIUM - VACUUM**

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{25}$$

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$



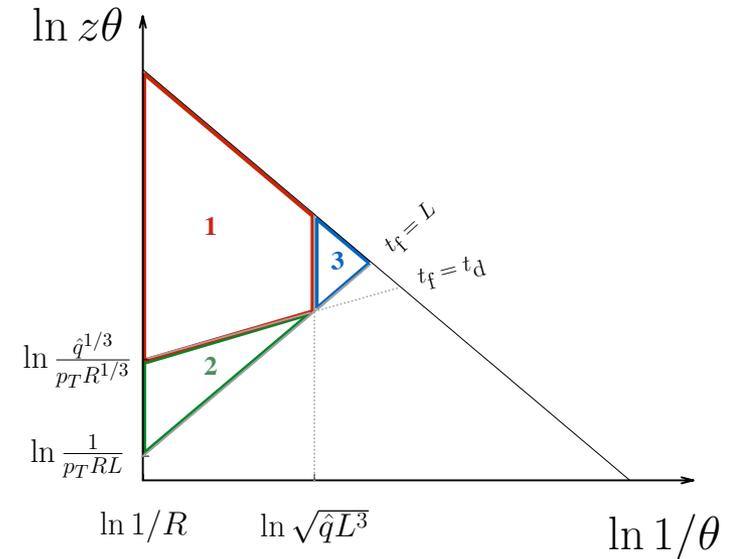
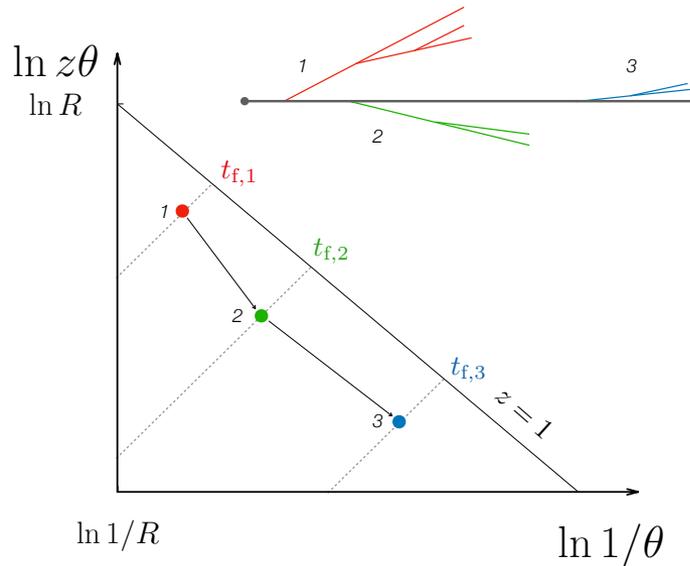
# A reminder from last wshop

the detector. The characteristic time-scale of the splitting is usually referred to as the *formation time*, and is related to the finite energy resolution,  $t_f \sim \Delta E^{-1}$ . It is explicitly given by

$$t_f = \frac{2z(1-z)p_T}{k_T^2} = \frac{2p_T}{M^2}, \quad (2)$$

where  $k_T = z(1-z)p_T\theta$  is the (relative) transverse momentum of the dipole in the small angle limit. This formula can easily be understood as the time-scale for decaying in the rest frame of the parent times its boost factor  $\sim (1/M) \times (p_T/M)$ .

<https://arxiv.org/pdf/1808.03689.pdf>



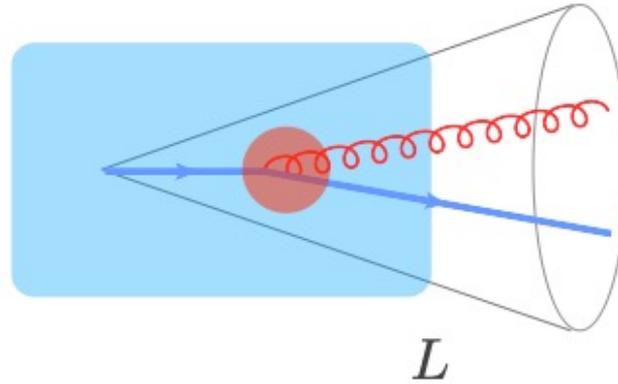
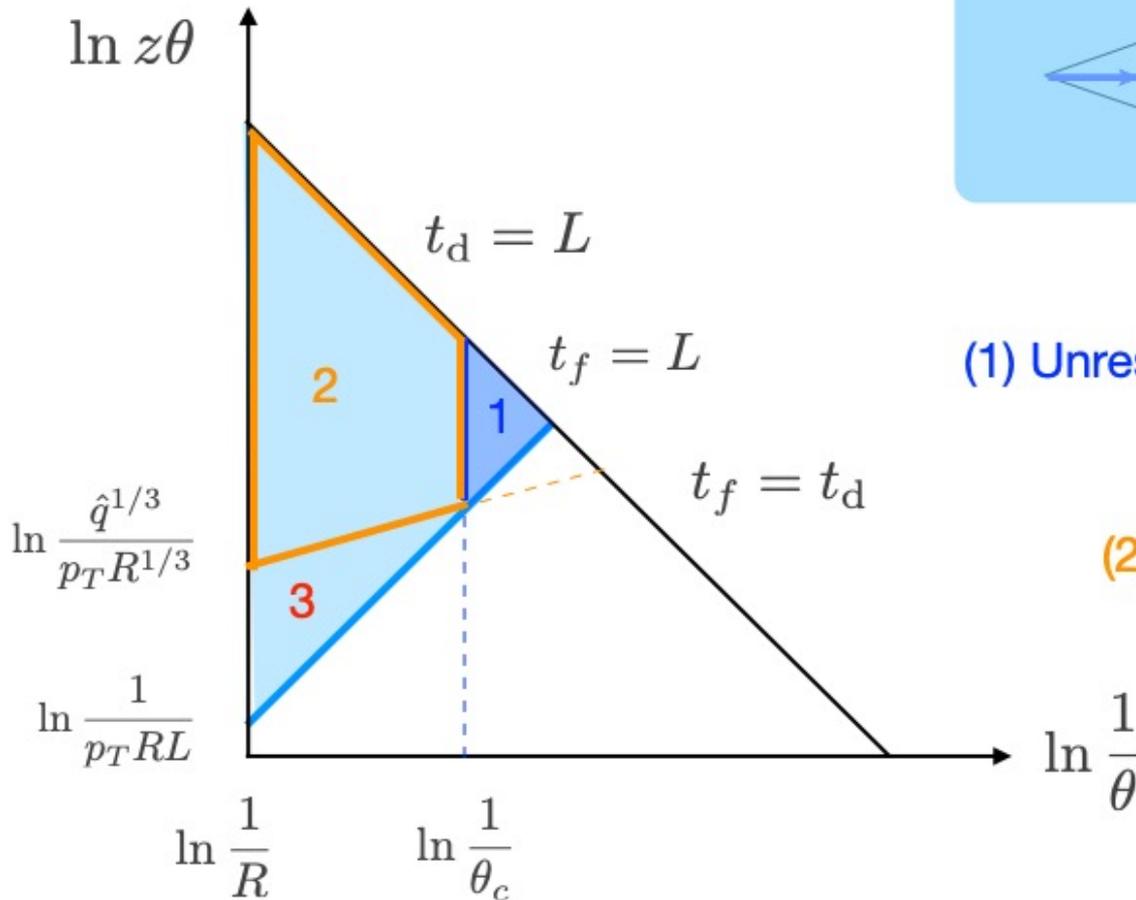
$$\ln z\theta = \ln \frac{1}{\theta} + \ln \frac{1}{p_T t},$$

# Back to the Lund plane

[Andrews et al (2018)]

Monday - Yacine

formation time:  $t_f = (\omega\theta^2)^{-1}$



(1) Unresolved in medium splitting

$$t_d > L$$

(2) Resolved vacuum splitting inside the medium

$$t_f < t_d < L$$

(3) Medium-induced radiation

$$t_d < t_f < L$$

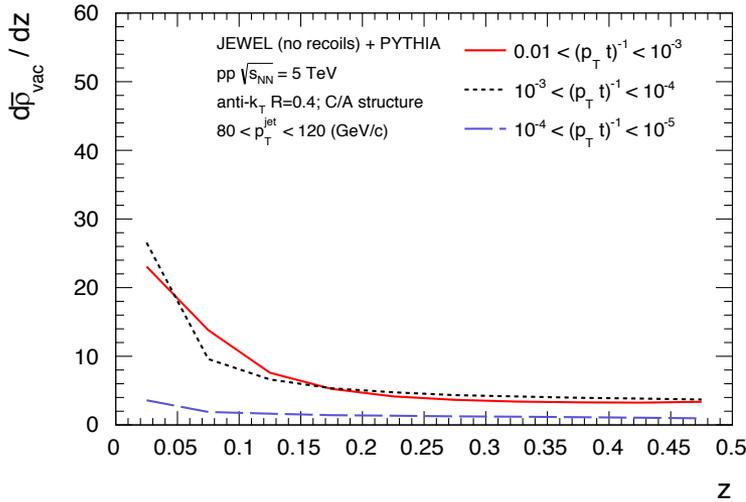
[See talk by P. Caucal for MC implementation]

# Jet Lund diagram

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{28}$$

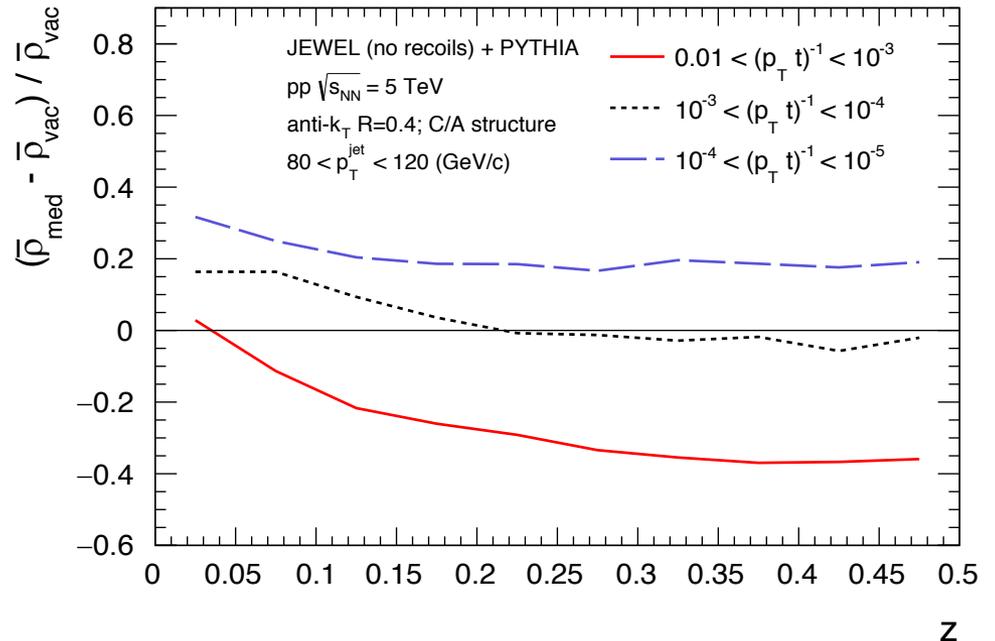
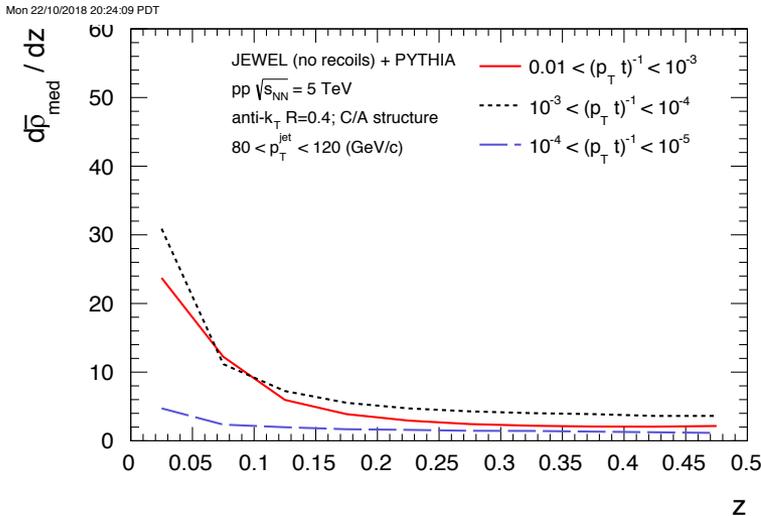
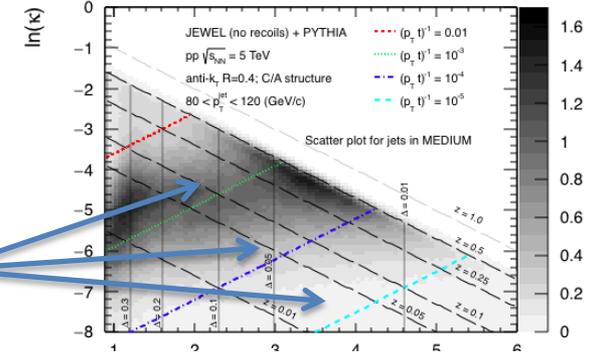
# slicing through time

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$



$$\ln z\theta = \ln \frac{1}{\theta} + \ln \frac{1}{p_T t}$$

Slicing along  $1/(p_T \times t)$   
and projecting along  $z$

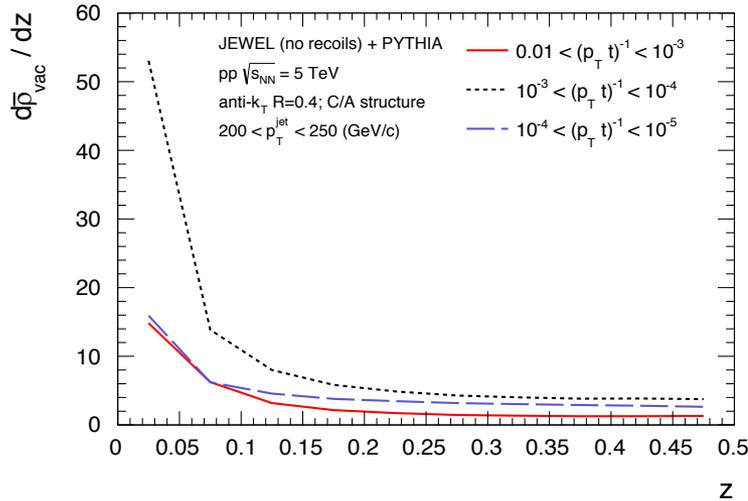


# Jet Lund diagram

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{29}$$

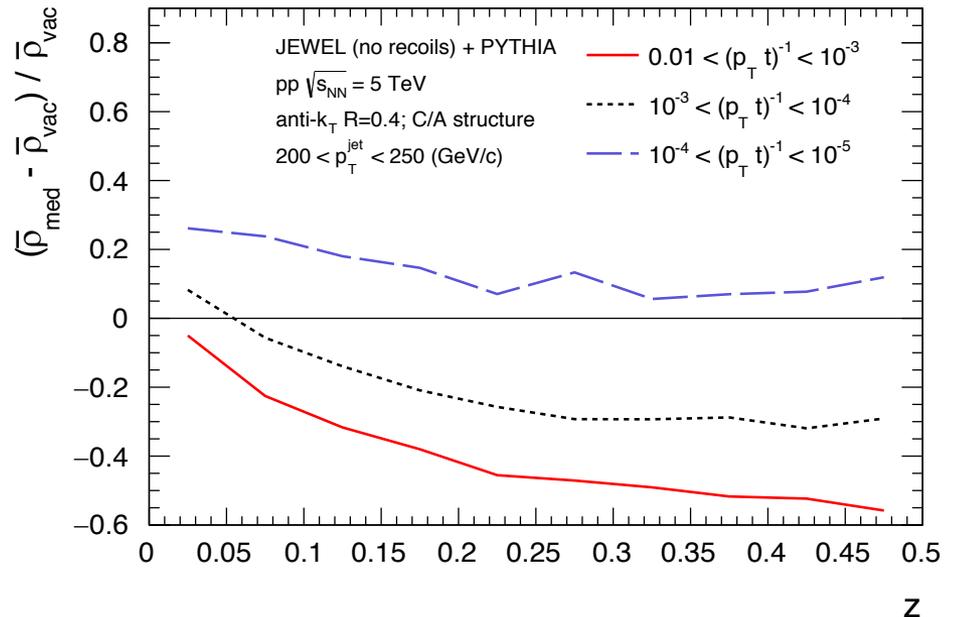
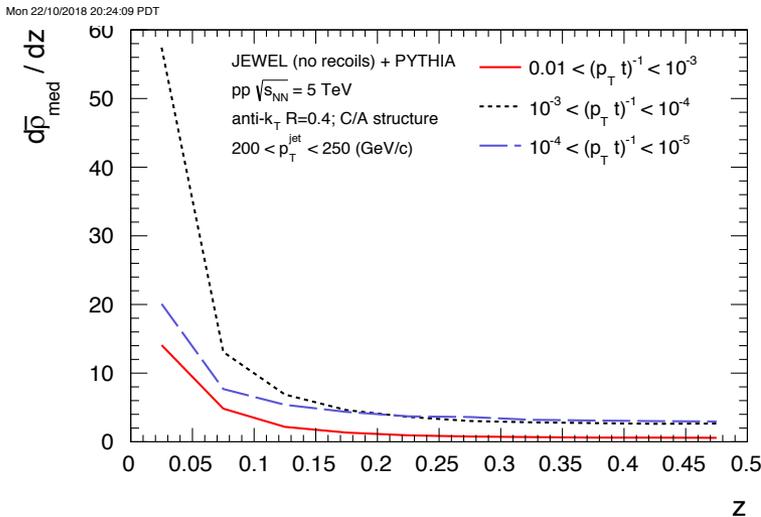
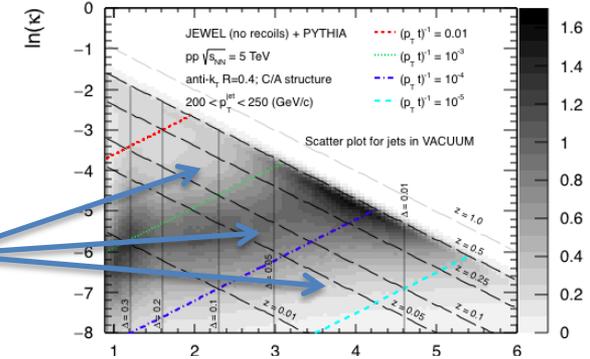
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80 – 120 GeV/c

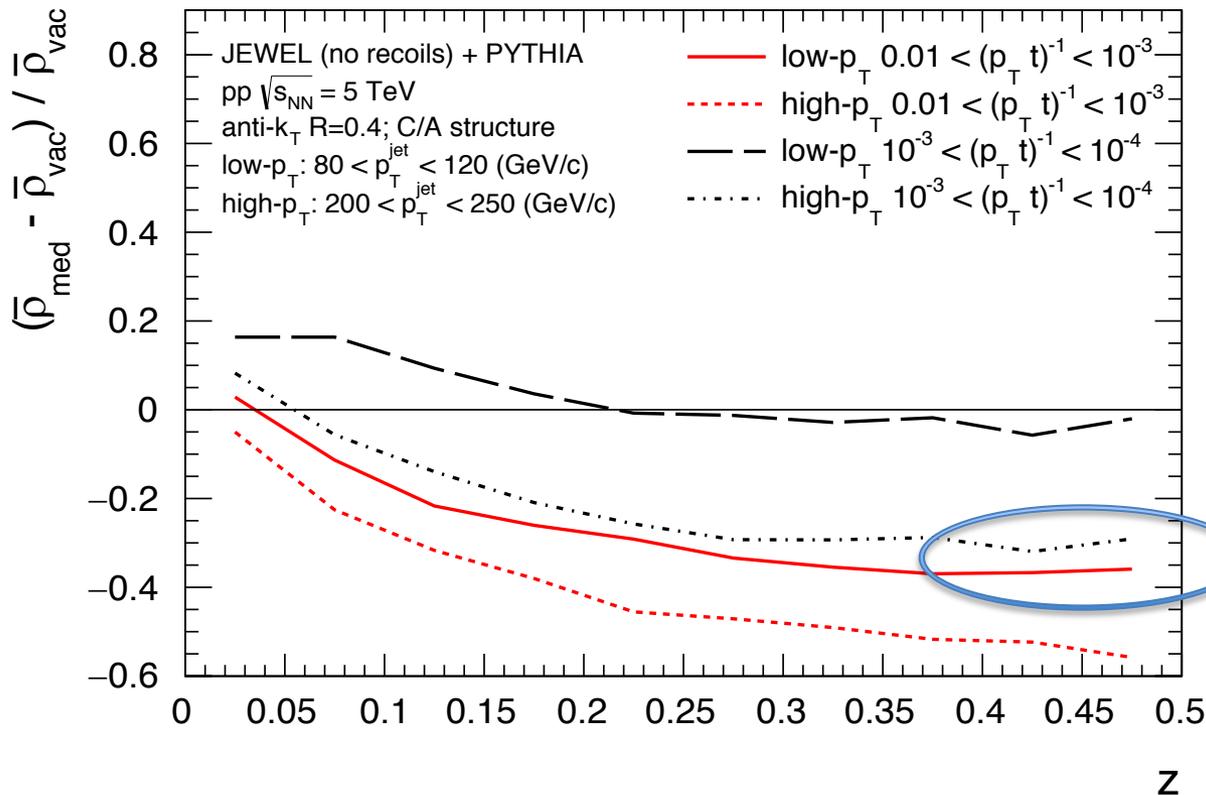
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# Jet Lund diagram slicing through time

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{30}$$

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Low- with high- $p_T$  for  
the similar  $t$



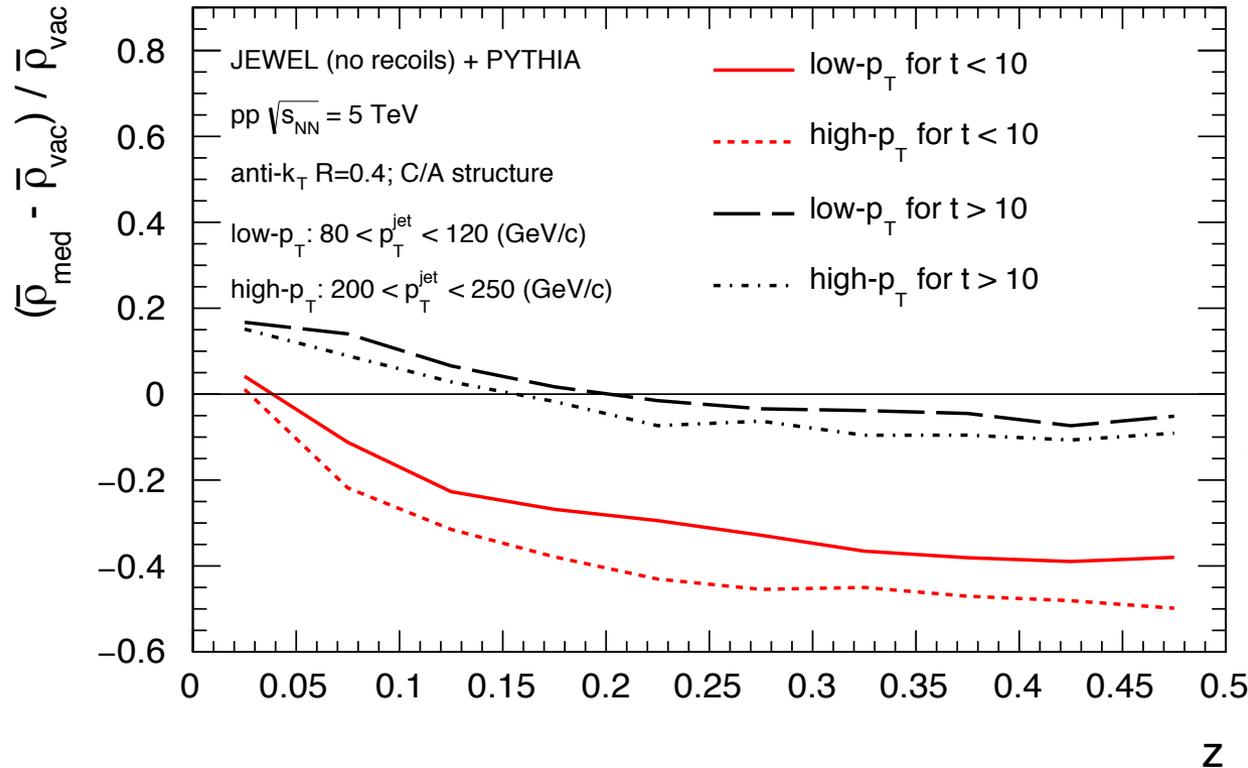
similar suppression  
(scaling factor for  $p_T \times t$   
roughly 80/200)

# Jet Lund diagram

$$p_{T,a} > p_{T,b}, \kappa = \frac{p_{T,b}}{p_{T,a} + p_{T,b}} \Delta_{ab}^{31}$$

slicing through time

$$\bar{\rho}(\Delta, \kappa) = \frac{1}{N_{\text{jet}}} \frac{dn_{\text{emission}}}{d \ln \kappa d \ln 1/\Delta}$$



Low- with high- $p_T$  for the similar  $t$

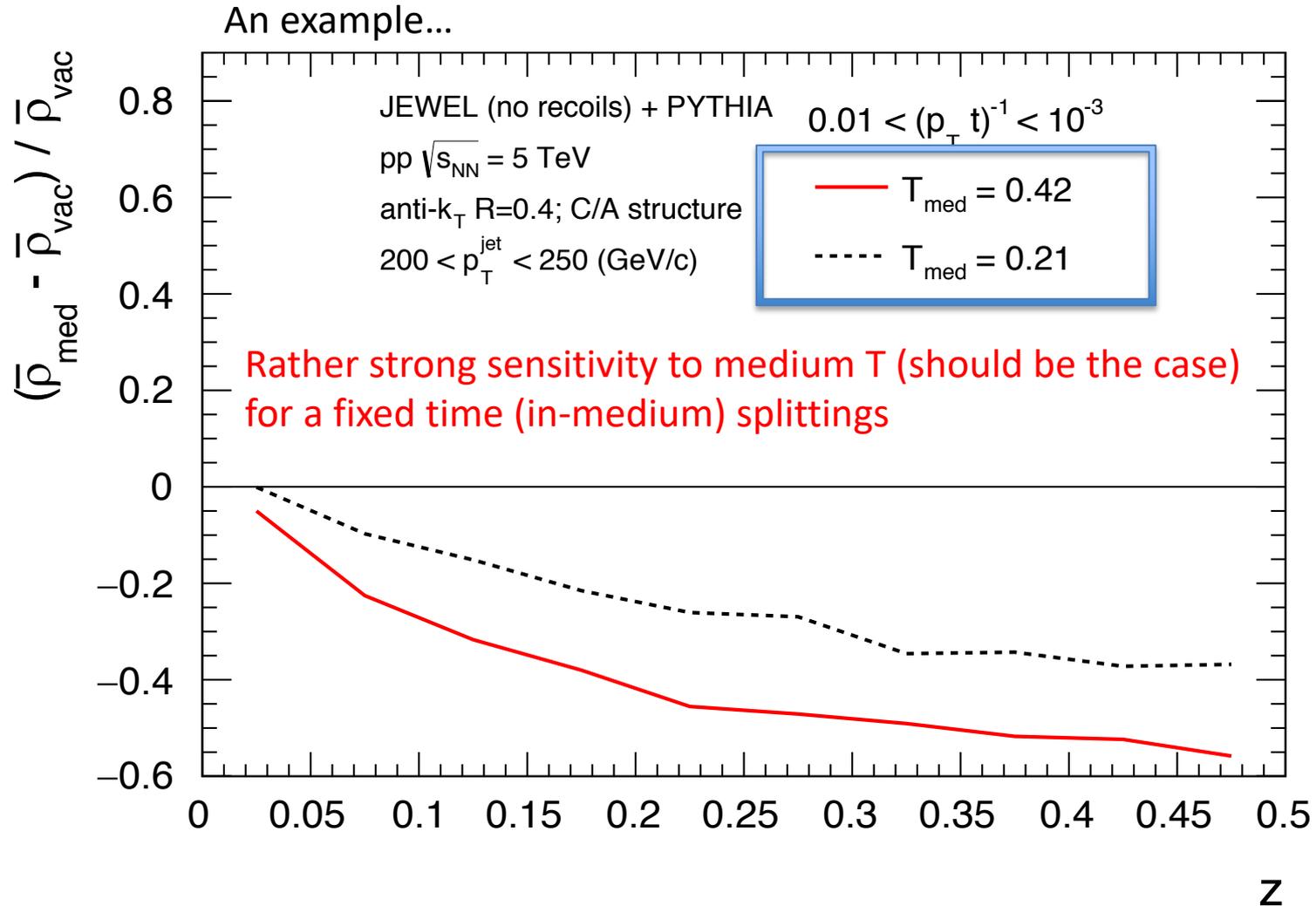


similar suppression  
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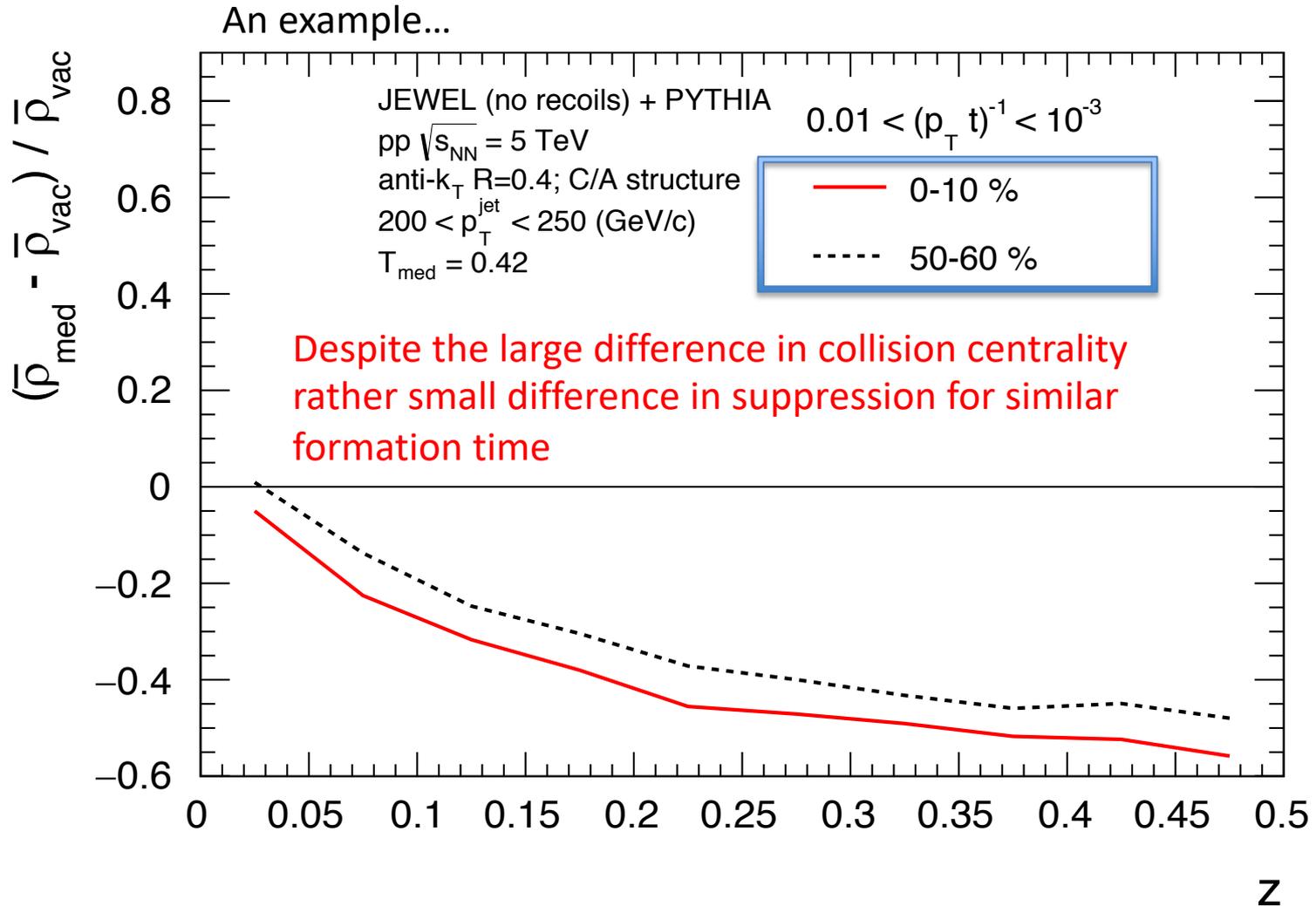
Slicing on formation time => similar suppression for similar  $t$

Explore: Mass ( $z\theta^2$ ) slicing?

# Sensitivity to medium's Temperature



# Sensitivity to medium's L (centrality)

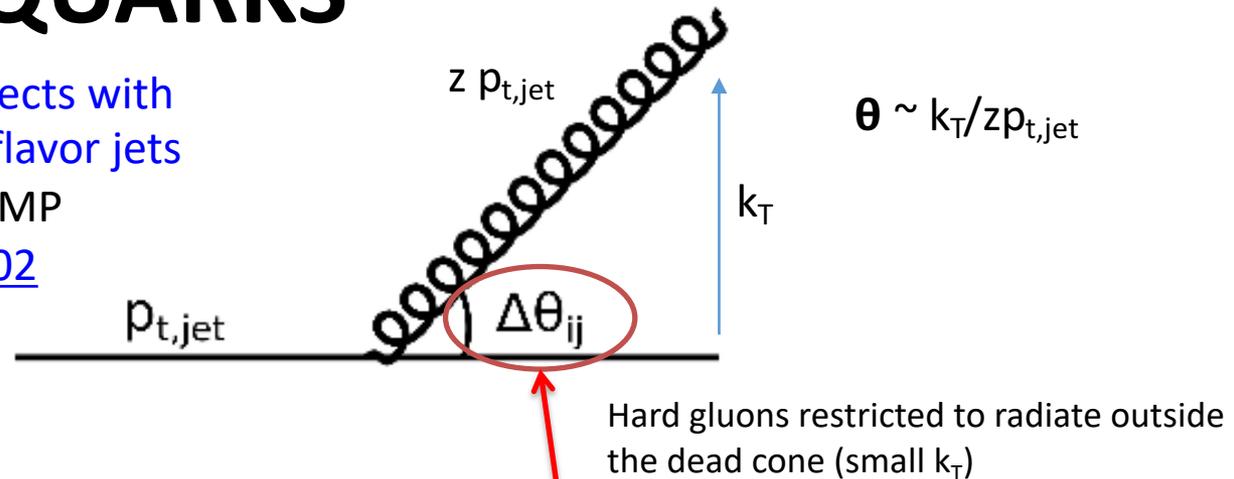


# ONTO HEAVY QUARKS

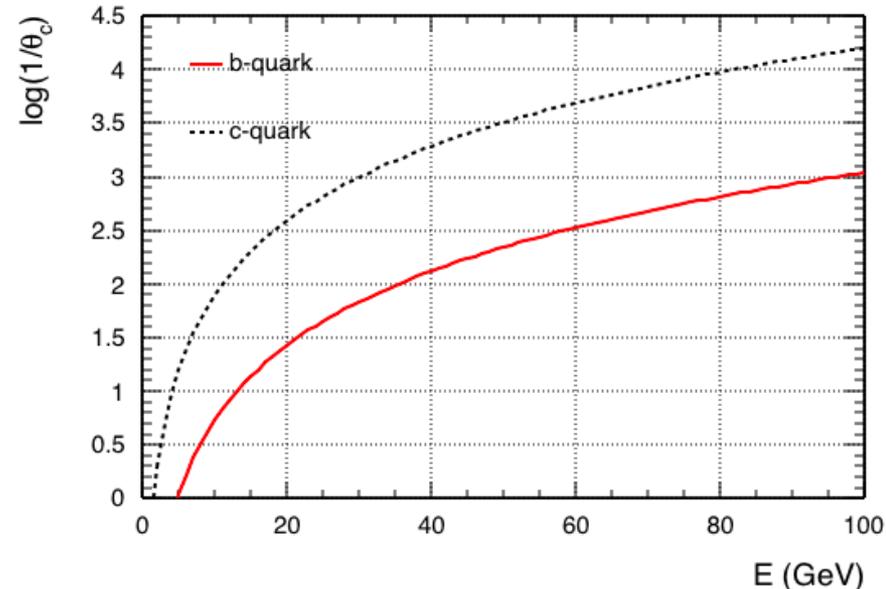
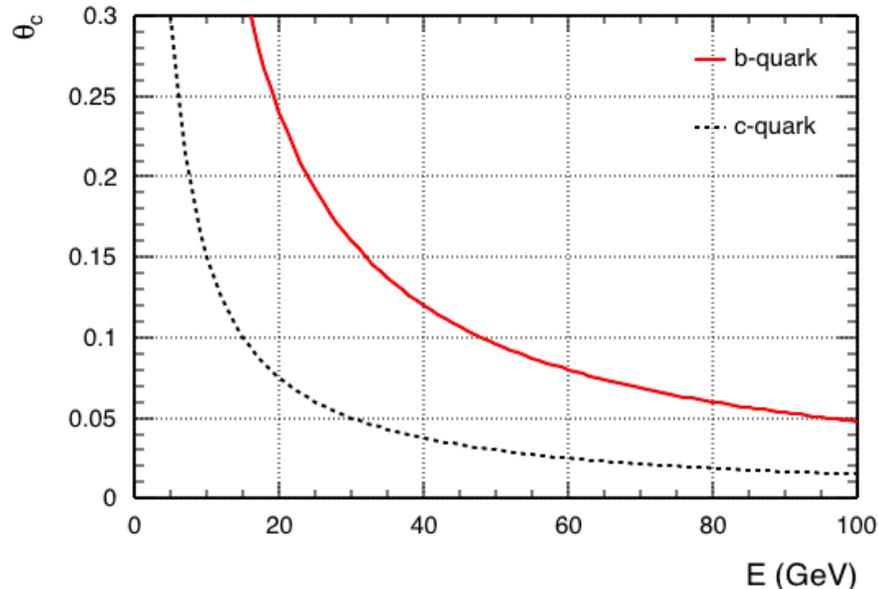
Searching for the dead cone effects with iterative declustering of heavy-flavor jets

Leticia Cunqueiro (ORNL/UTK), MP

<https://arxiv.org/abs/1812.00102>

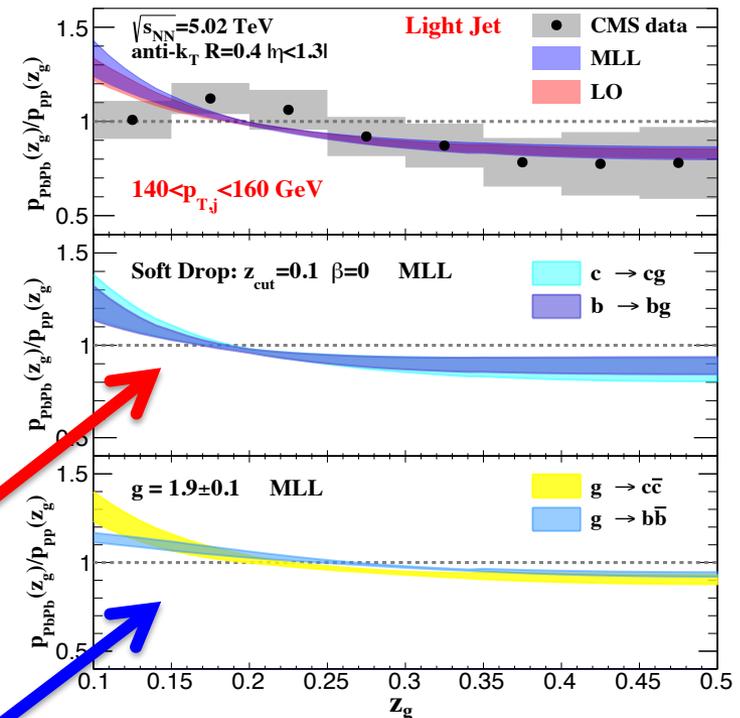


## Dead cone for $\theta < m / E$



# Heavy-flavor and the dead cone...

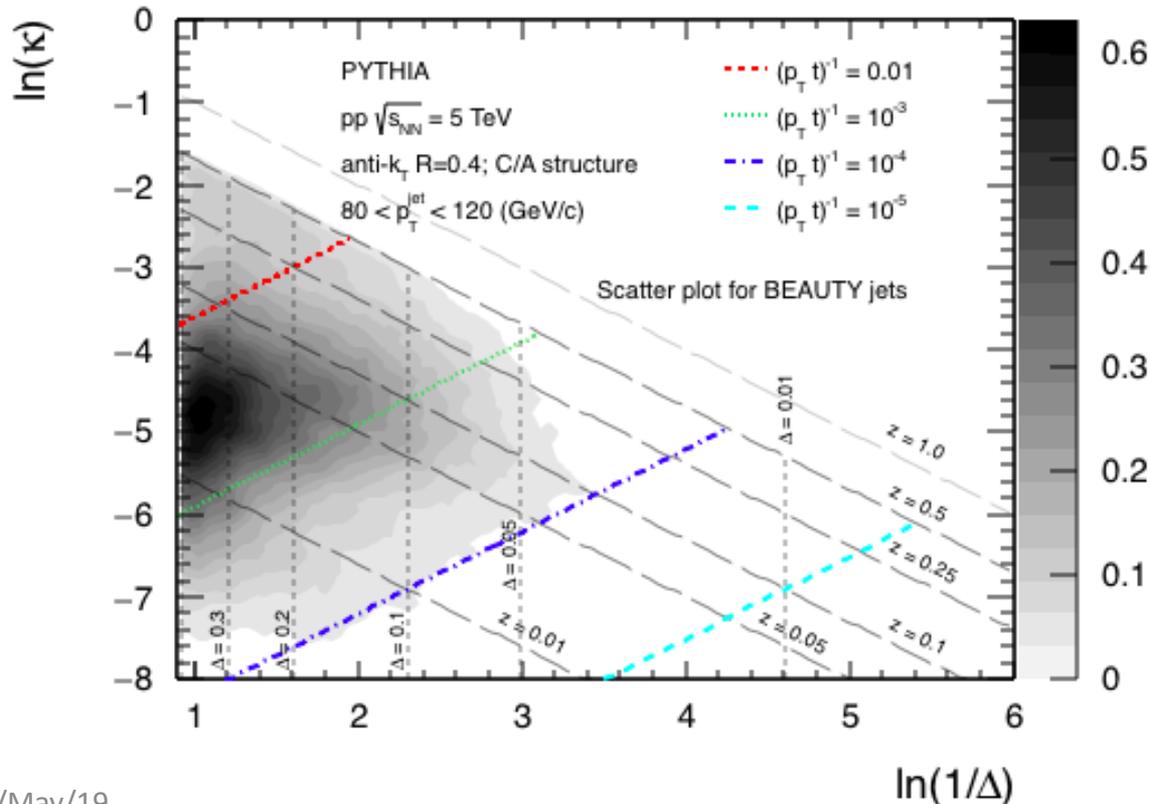
- High-energy HF – little dead-cone effect because of  $m/E$  small – radiative quark (a la LF) e-loss dominant
- I. Vitev et al. study HF-jets with  $z_g$  (standard grooming tech.) => no significant differences as compared to LF jets (high-momentum 140-160 GeV) for HF tagged jet  $Q \rightarrow Qg$
- QQbar splits in parton shower:
  - I. Vitev – little / no in medium modification
  - Novel techniques in pp on Disentangling Heavy Flavor at Colliders [arXiv:1702.02947] – potentially interesting for AA



**Figure 2.** The modification of the jet splitting functions in 0-10% central Pb+Pb collisions at  $\sqrt{s_{NN}} = 5.02$  TeV for the  $p_T$  bin  $140 < p_{T,j} < 160$  GeV. The upper panels compare the LO and MLL predictions to CMS light jet substructure measurements [12]. The middle and lower panels present the MLL modifications for heavy flavor tagged jet - the  $Q \rightarrow Qg$  and  $\rightarrow Q\bar{Q}$ , respectively.

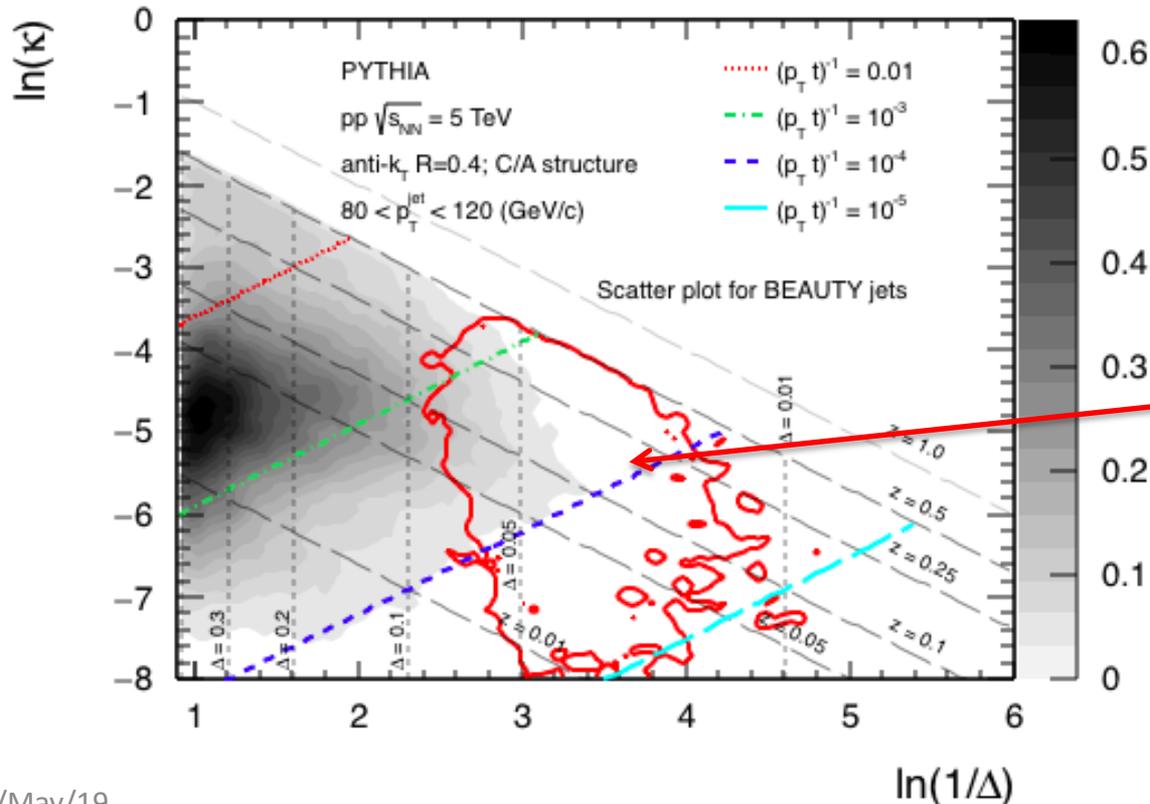
# Heavy-flavor and the dead cone...

- Can we take a look with Lund diagram?
  - Use leading (high- $p_T$ ) HF-hadron (lepton) for the tag & follow declusterization
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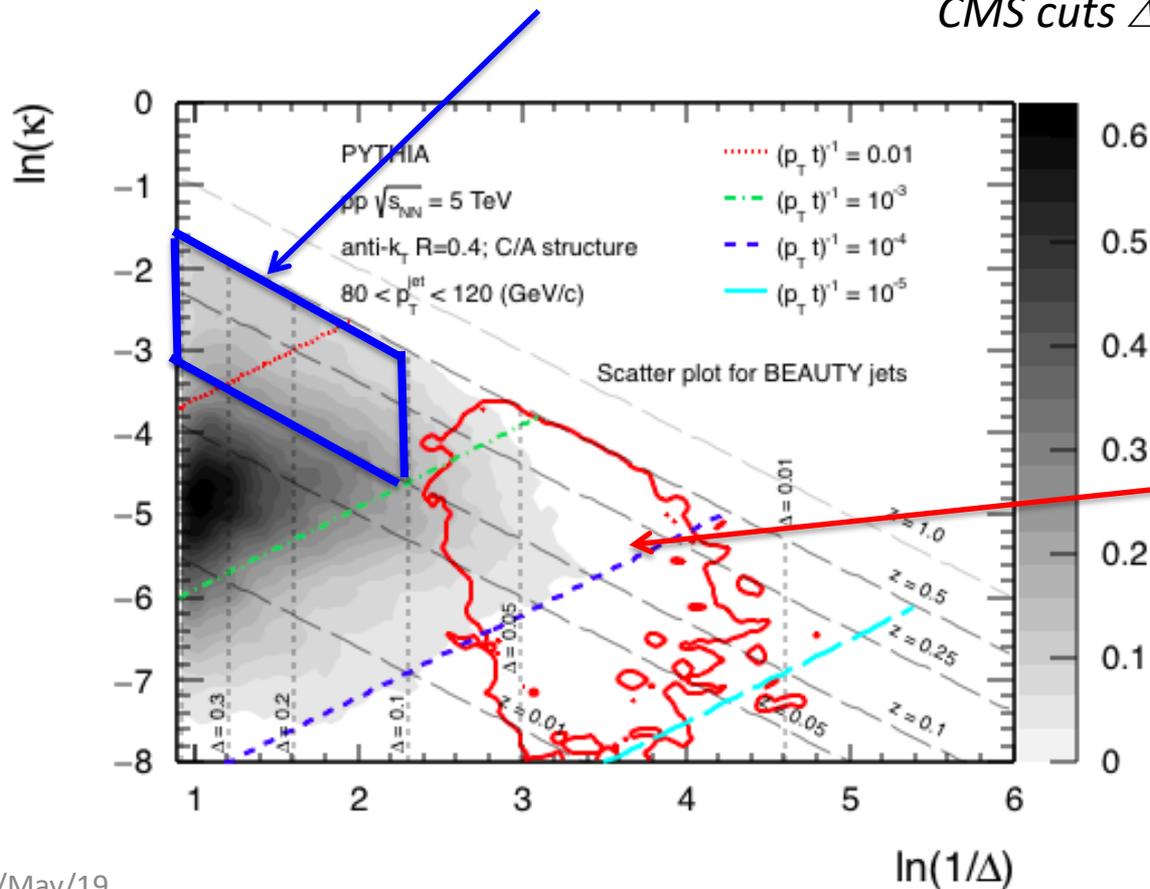
Dead cone

- An approximation
  - $\Delta < m/E$
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*CMS cuts  $\Delta < 0.1$  – ALICE does not*



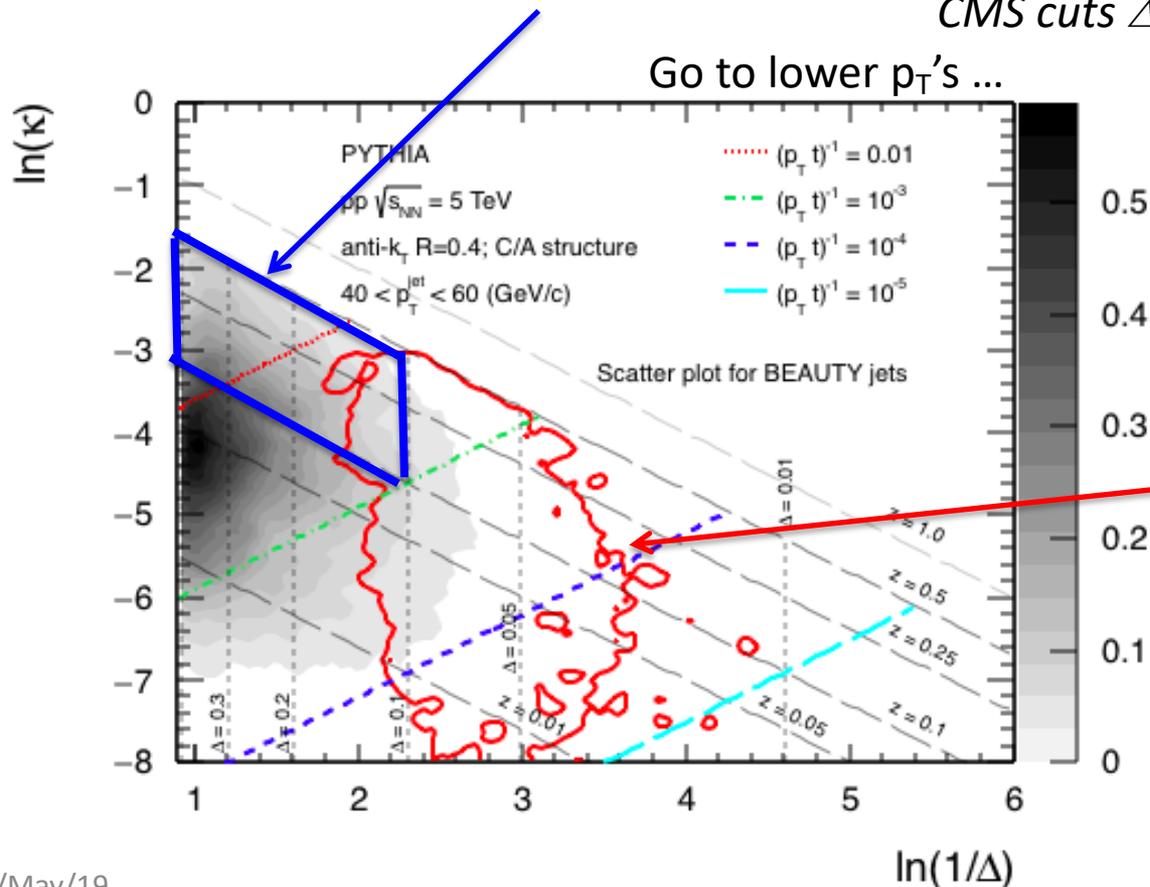
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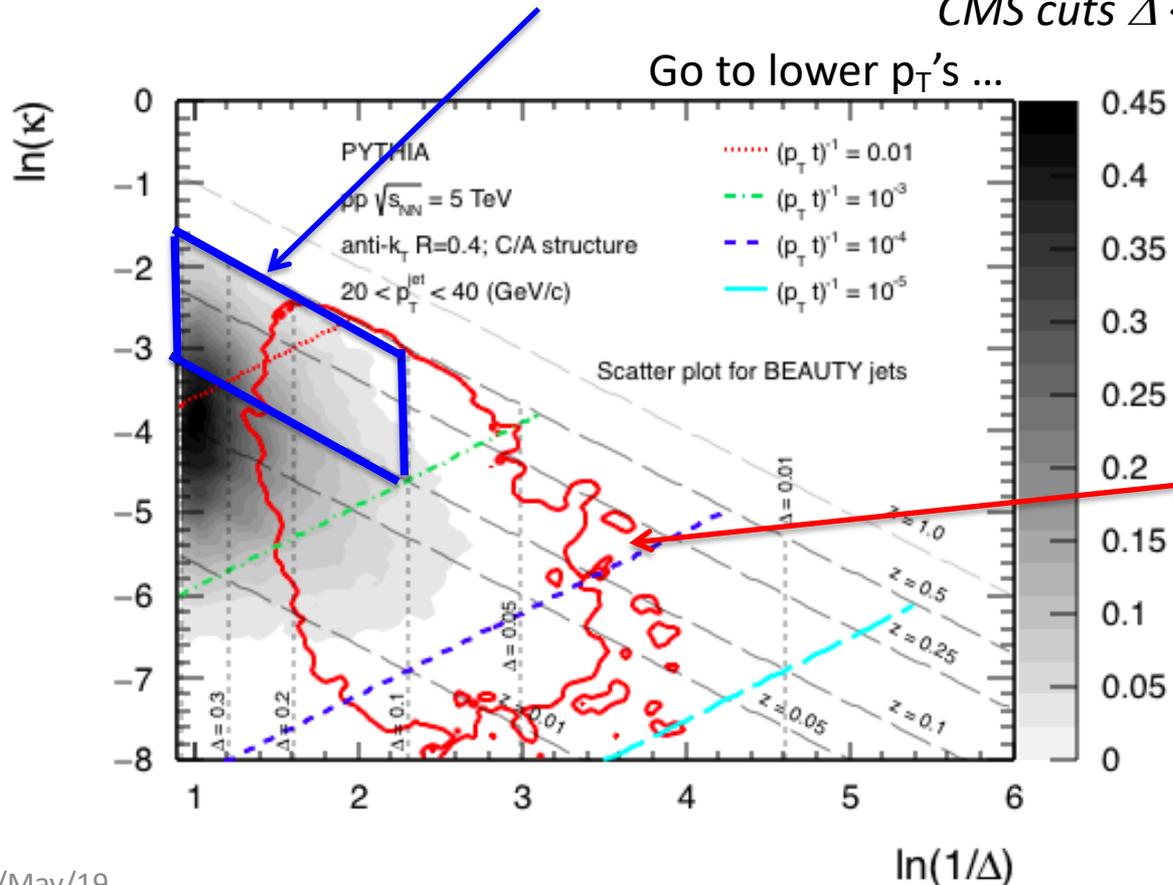
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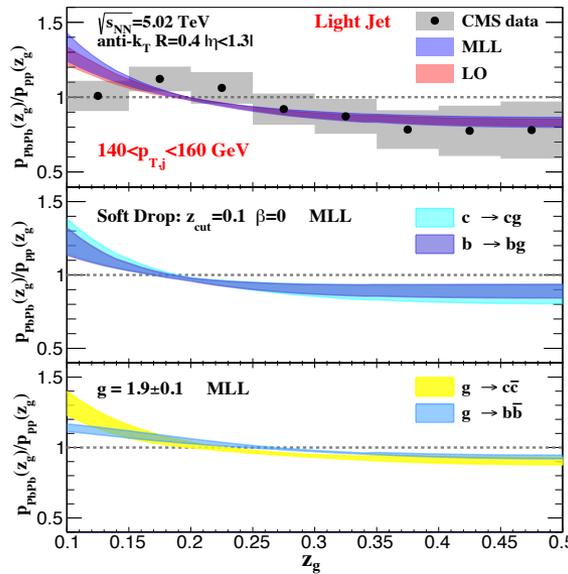


## Dead cone

- An approximation
  - $\Delta < m/E$
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# Lower pT

High- $p_T$

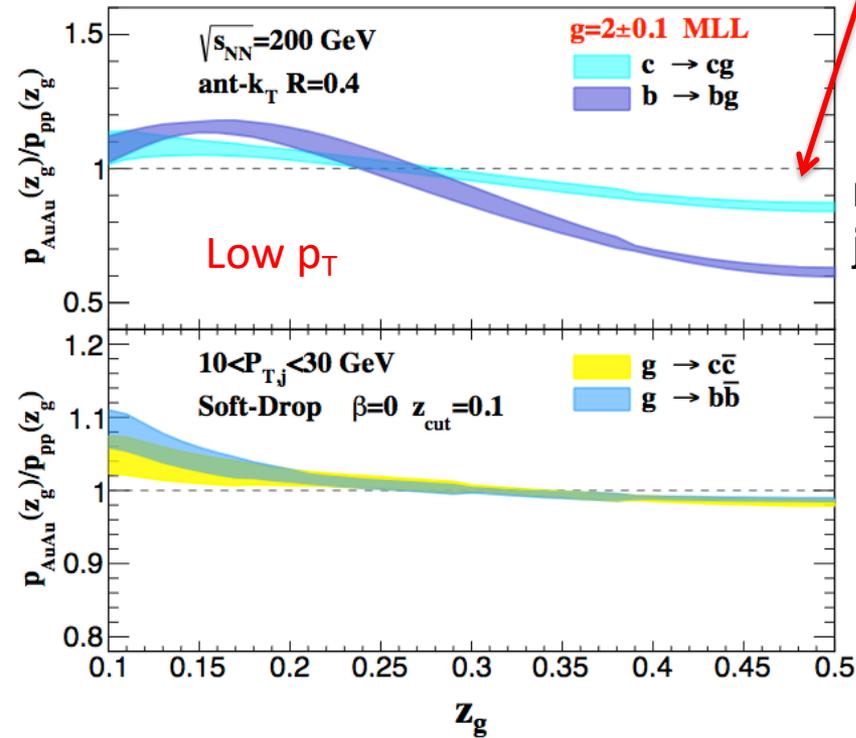


**Figure 2.** The modification of the splitting functions in 0-10% central Pb-collisions at  $\sqrt{s_{NN}} = 5.02$  TeV for the  $p_T$   $140 < p_{T,j} < 160$  GeV. The upper panel compares the LO and MLL predictions to the light jet substructure measurements [12]. The middle and lower panels present the MLL modifications for heavy flavor tagged jet -  $Q \rightarrow Qg$  and  $\rightarrow Q\bar{Q}$ , respectively.

Hai Tao Li  
There it is!  
Normalization?(!)

Modification of fragmentation functions for gluon and quark  
Kang et al 2014

Chien e



modifications of the jet splitting functions

HTL, Vitev 2018

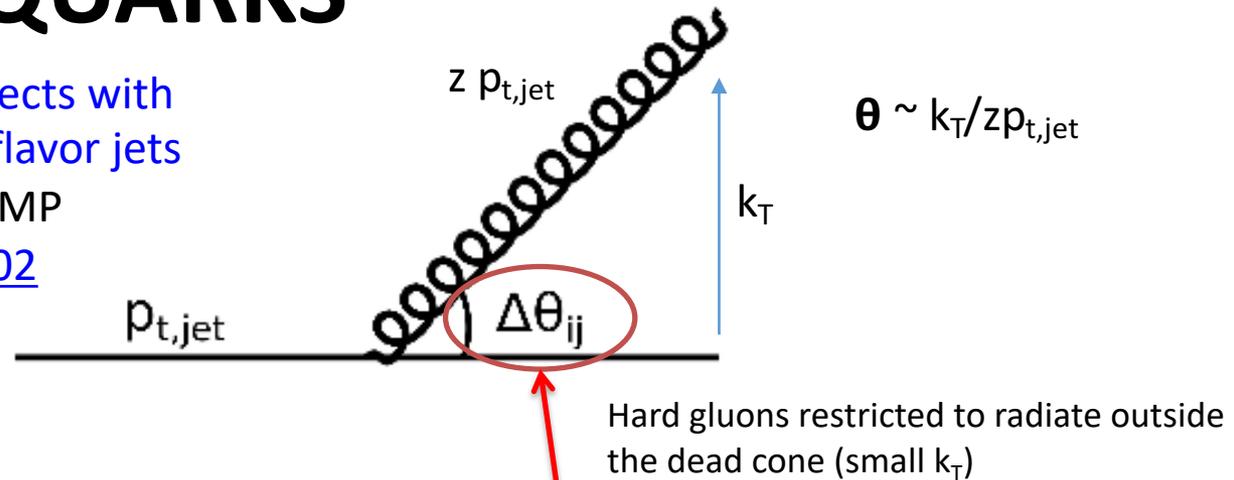
[https://indico.bnl.gov/event/5039/contributions/26256/attachment/s/21619/29615/b\\_jet\\_haitao.pdf](https://indico.bnl.gov/event/5039/contributions/26256/attachment/s/21619/29615/b_jet_haitao.pdf)

# ONTO HEAVY QUARKS

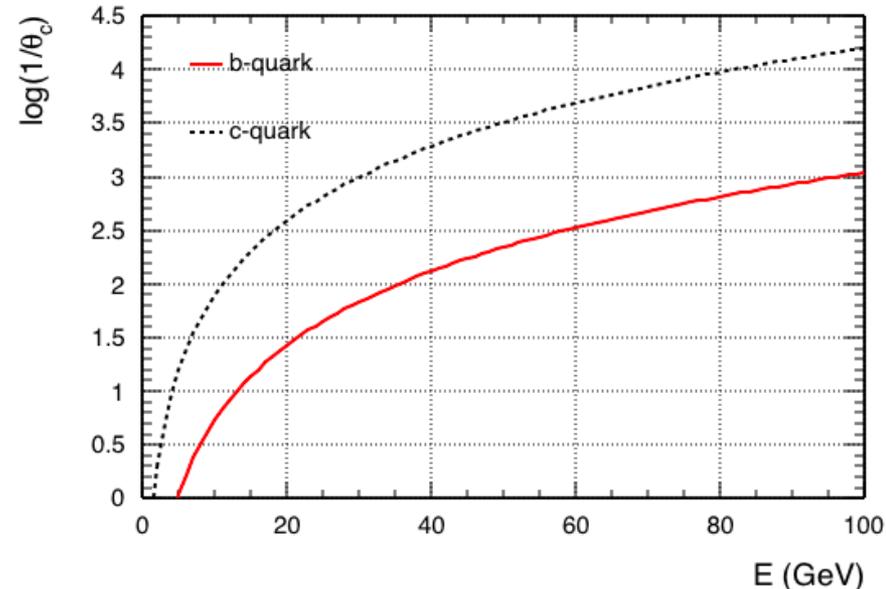
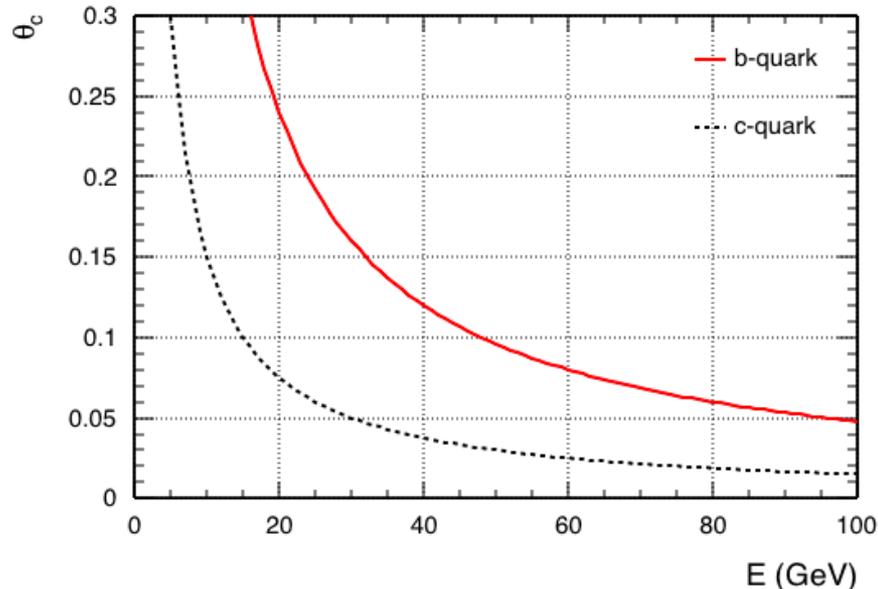
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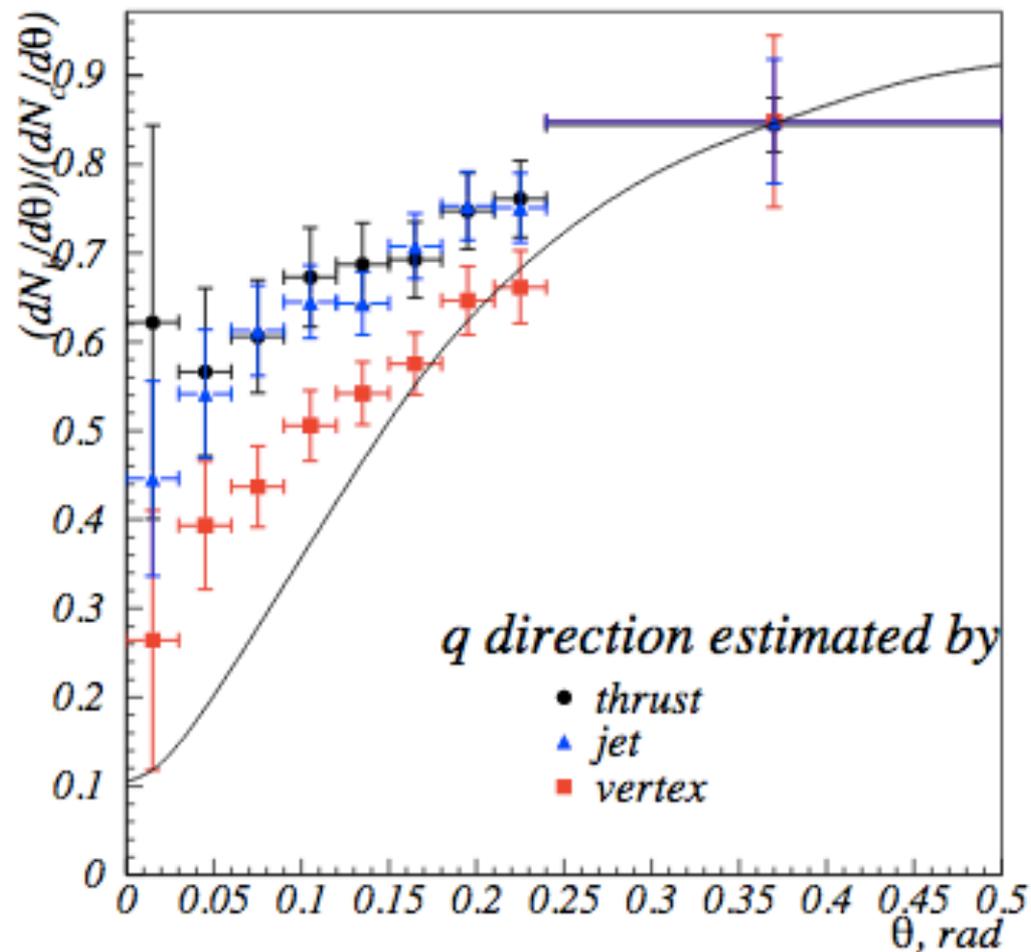
## Dead cone for $\theta < m / E$



# Dead cone measured?

*Battaglia, Orava, Sami "A study of depletion of fragmentation particles at small angles in b-jets with the DELPHI detector at LEP"*

The first and only attempt of direct dead cone measurement



# The recipe... (1/2 – decluster...)

2D map of the jet tree filled via iterative declustering:

- Recluster the jet constituents with CA (a convenient metric for vacuum angular ordered showers)

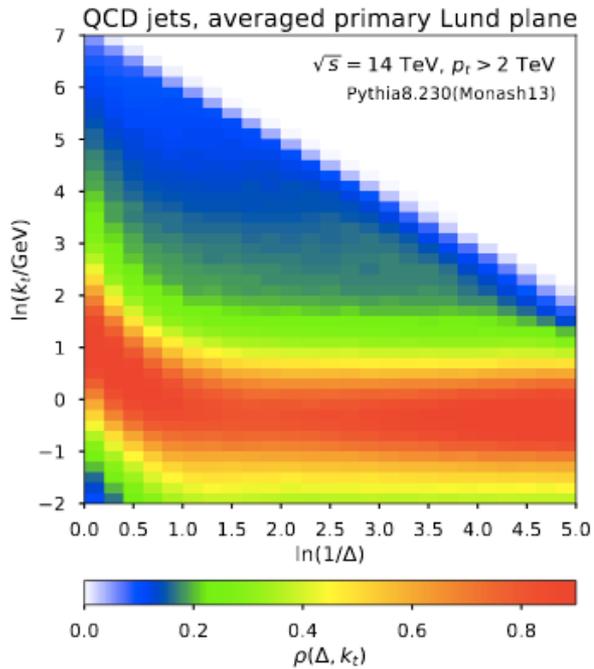
- Uncluster it step by step, from the prongs that were merged last to the prongs that were merged first.

- Each time, register the scale  $k_T$  and the opening angle  $\theta$  between the subleading and leading prong

- Always follow the hardest prong

The result is a flat 2D density map (except for the running of the coupling)

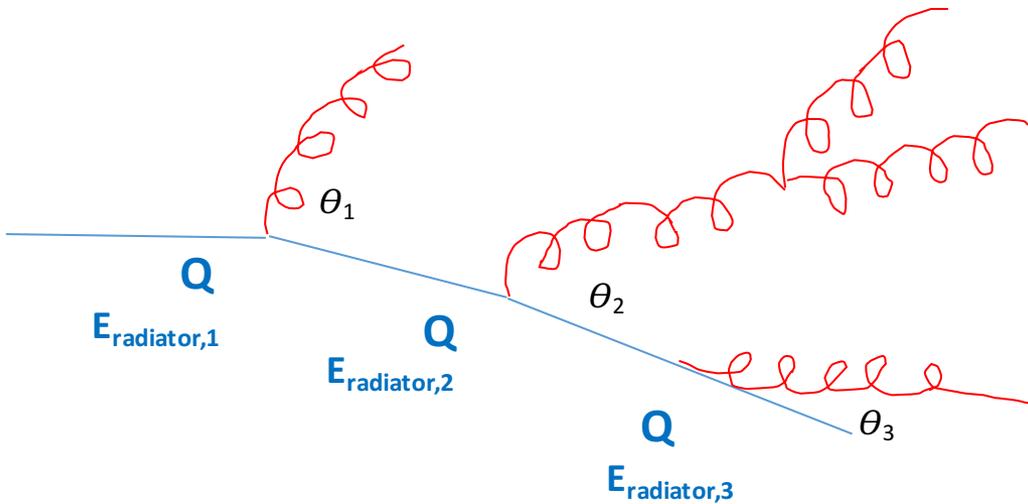
$$d\mathcal{P}_{\text{vac}} = 2 \frac{\alpha_s C_i}{\pi} d \log z \theta d \log \frac{1}{\theta}$$



Dreyer, Soyez, Salam JHEP 1812 (2018) 064

# Recipe... 2/2 – follow HF

## “tag & follow” heavy-flavors (hardest branch)...



We do the standard declustering process

We follow the prong containing the heavy flavor at each step

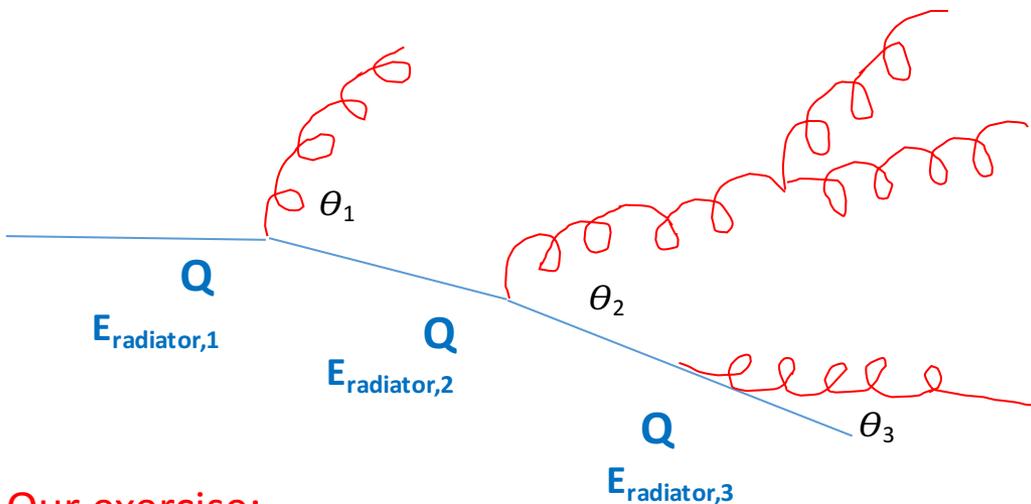
Negligible number of cases where the prong containing the heavy flavor is not the hardest, no ambiguity when comparing to light quarks

At each step of the jet tree we can access the angle of the splitting and the energy of the radiating parent subject,  $E_{\text{radiator}}$ . For  $\theta < m_Q/E_{\text{radiator}}$  we expect to see a suppression of splittings.

For low  $E_{\text{radiator}}$ , which means penetrating the jet to deep levels, the phase space for the dead cone observation grows.

# Recipe... 2/2 – follow HF

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We do the standard declustering process

We follow the prong containing the heavy flavor at each step

Negligible number of cases where the prong containing the heavy flavor is not the hardest, no ambiguity when comparing to light quarks

### Our exercise:

- Pythia8 Tune 4C
- pp collisions at  $\sqrt{s}=13$  TeV
- Select  $c\bar{c}$ ,  $b\bar{b}$  production channels
- At parton level the leading prong at each declustering step is the one containing the heavy parton
- At hadron level, we inhibit the decay of the B and D mesons and the leading prong at each declustering step the one containing the heavy meson.
- Antik<sub>T</sub> jets  $R=0.4$ , CA reclustering algo

# LF vs HQ – parton level – no UE, no ISR

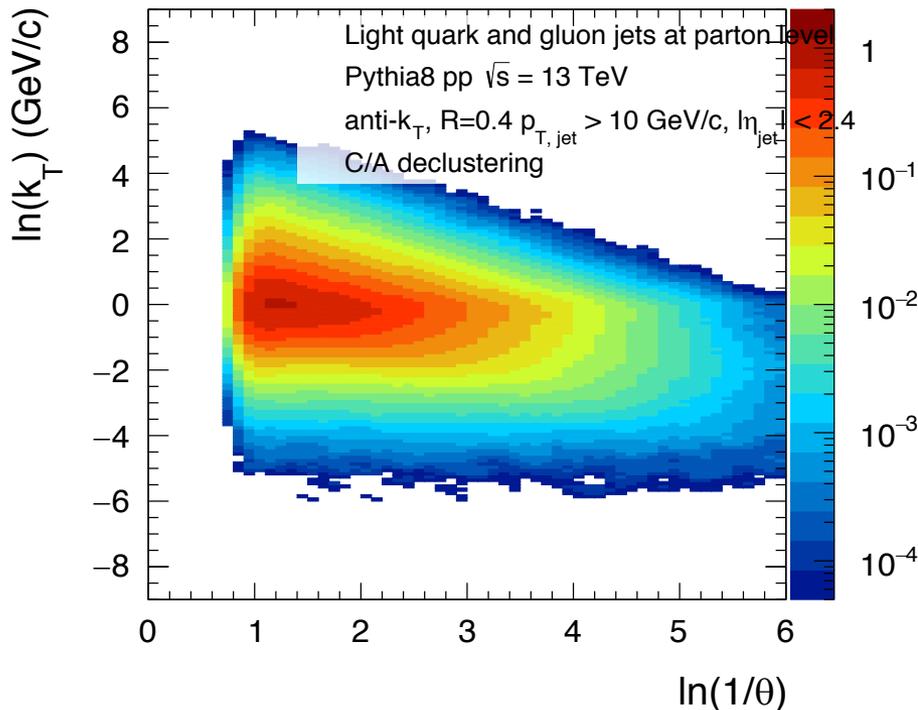
All jets (light quark and gluon)

$\log(kT) = -2 \Leftrightarrow kT = 0.135 \text{ GeV}$

$\log(kT) = 0 \Leftrightarrow kT = 1 \text{ GeV}$

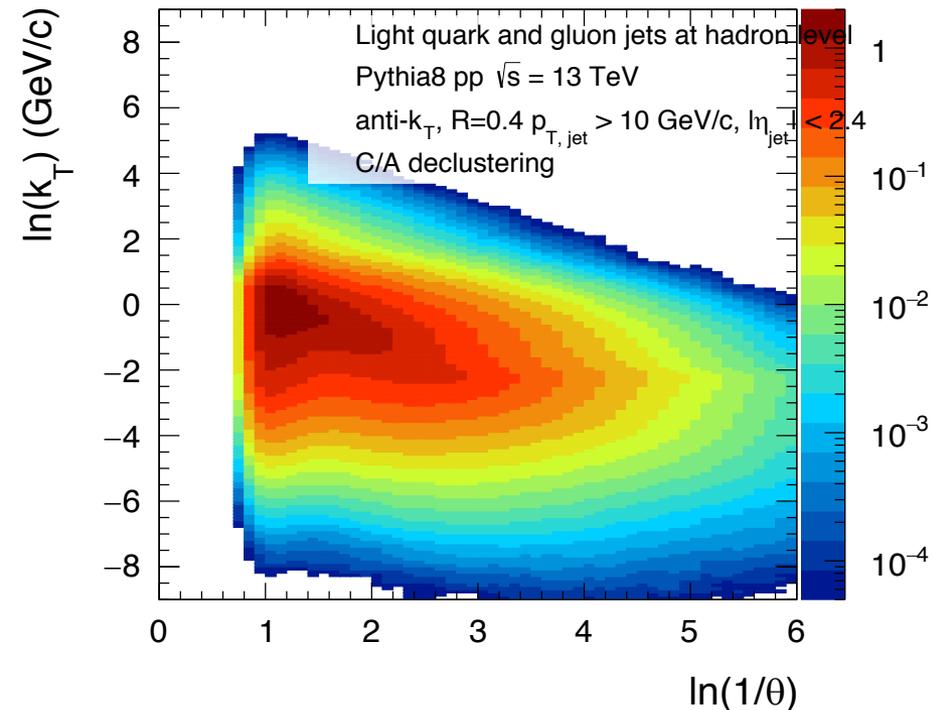
## Parton level

Lund diagram  $\rho(k_T, \theta) = 1/N_{\text{jet}} d^2N / d \ln(k_T) / d \ln(1/\theta) (\text{GeV}/c)^{-1}$



## Hadron level

Lund diagram  $\rho(k_T, \theta) = 1/N_{\text{jet}} d^2N / d \ln(k_T) / d \ln(1/\theta) (\text{GeV}/c)^{-1}$



Tue 29/01/2019 11:48:36 PST

Tue 29/01/2019 11:48:36 PST

Hadron level – ALL processes

# LF vs HQ – parton level – no UE, no ISR

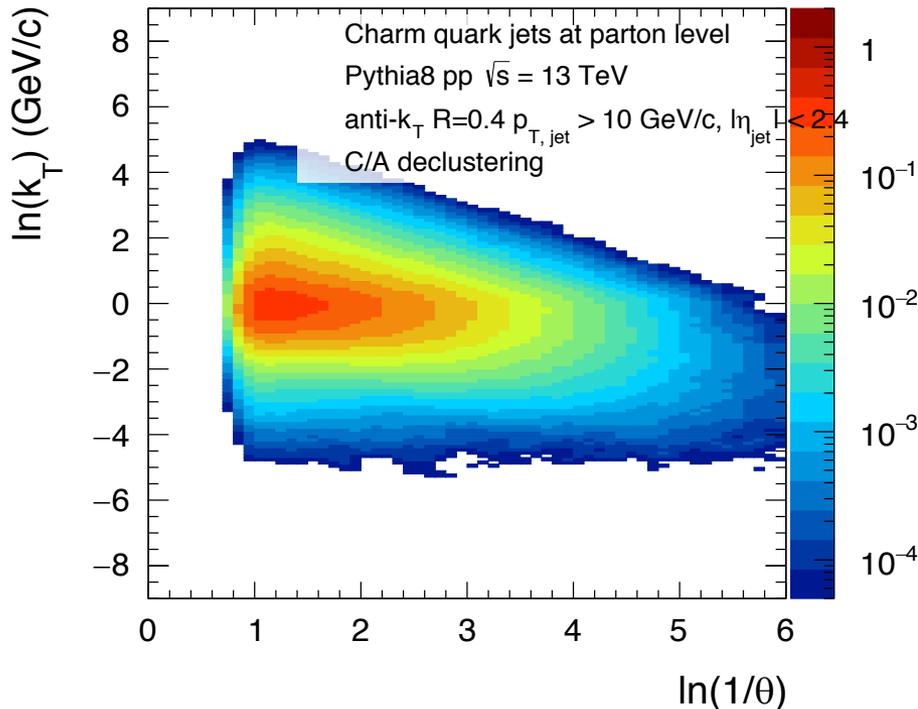
Charm

$$\log(kT) = -2 \Leftrightarrow kT = 0.135 \text{ GeV}$$

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Parton level

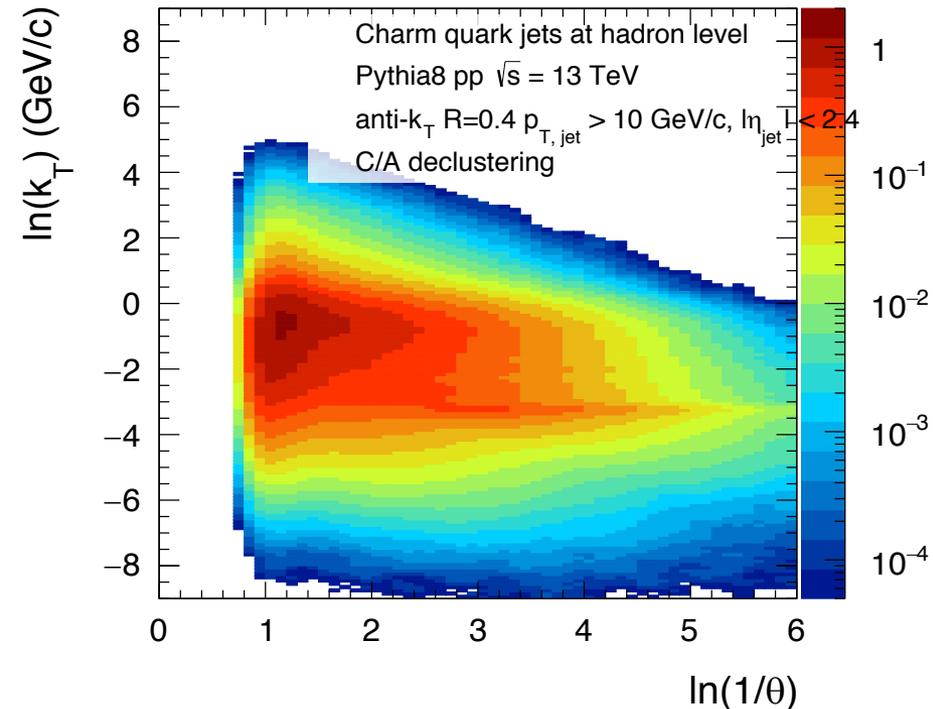
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Hadron level

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Hadron level – ALL processes

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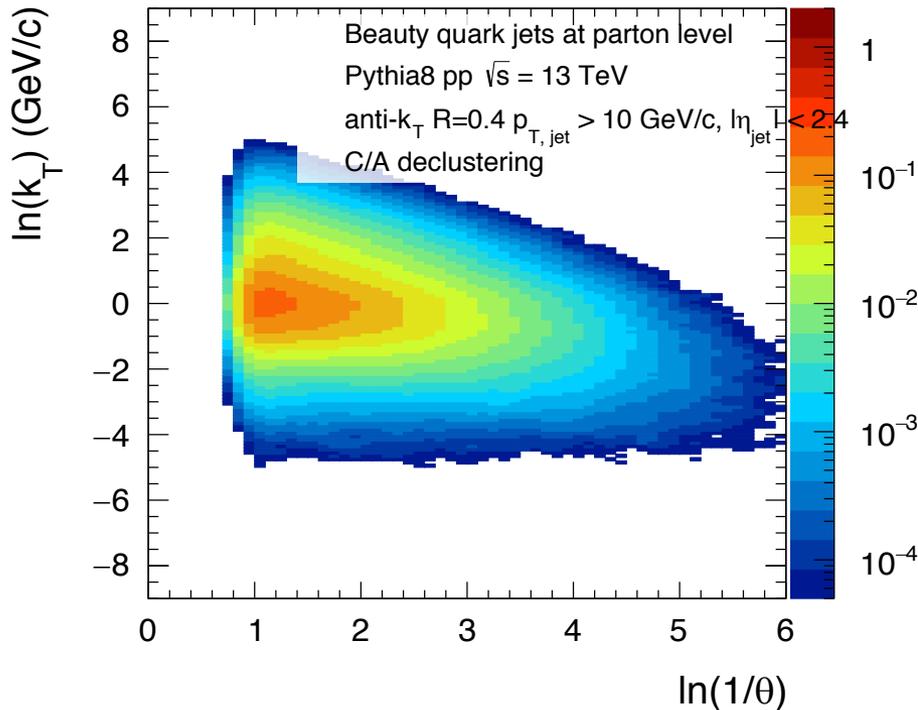
Beauty

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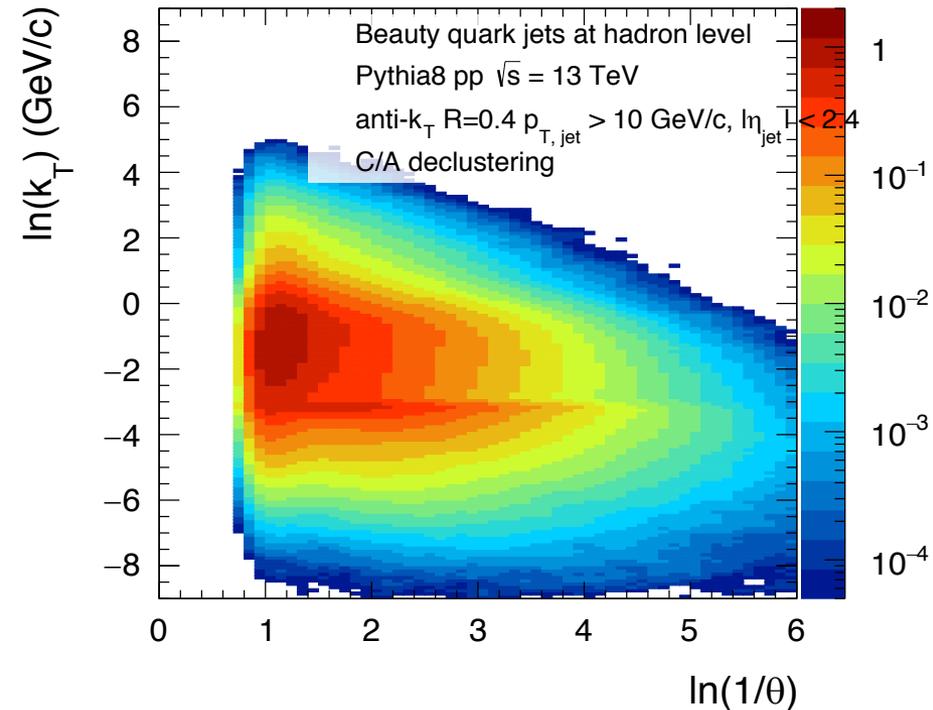
Parton level

Lund diagram  $\rho(k_{\perp}, \theta) = 1/N_{\text{jet}} d^2N / d \ln(k_{\perp}) / d \ln(1/\theta) (\text{GeV}/c)^{-1}$



Hadron level

Lund diagram  $\rho(k_{\perp}, \theta) = 1/N_{\text{jet}} d^2N / d \ln(k_{\perp}) / d \ln(1/\theta) (\text{GeV}/c)^{-1}$



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Hadron level – ALL processes

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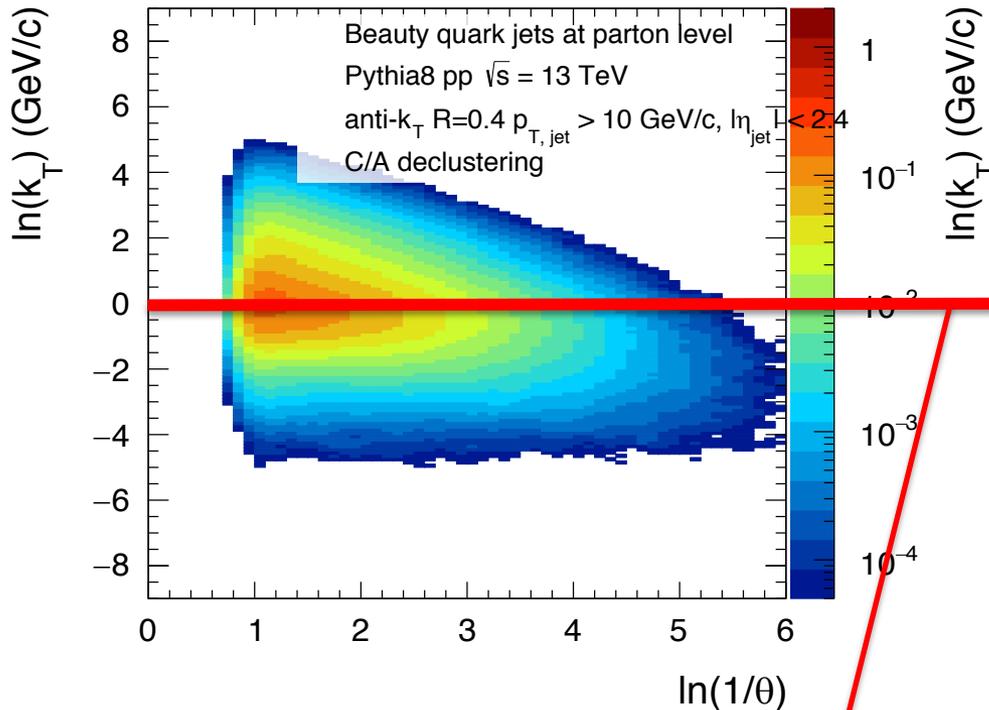
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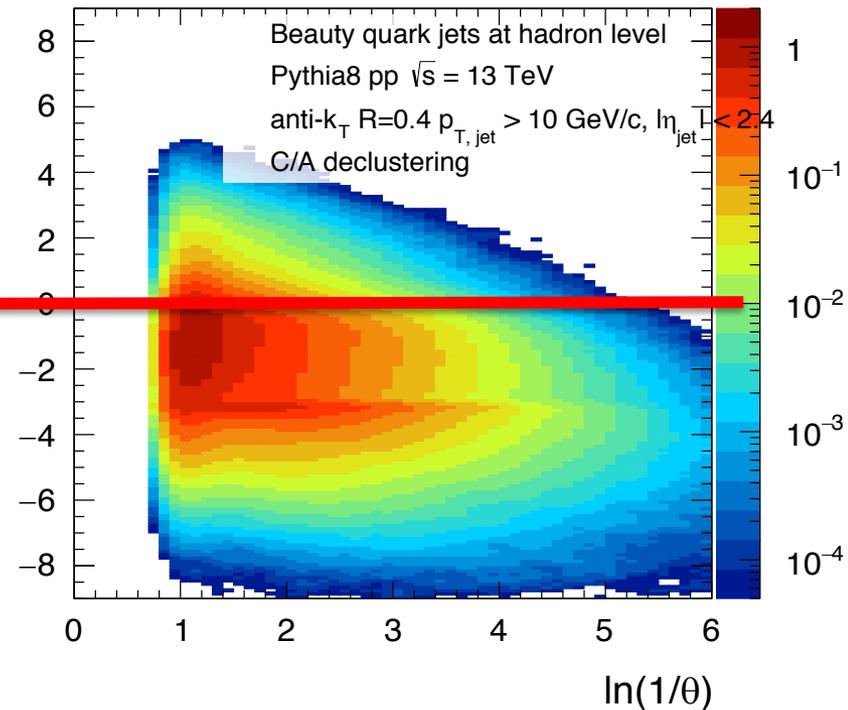
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Hadron level

Lund diagram  $\rho(k_T, \theta) = 1/N_{\text{jet}} d^2N / d \ln(k_T) / d \ln(1/\theta) (\text{GeV}/c)^{-1}$



Hadron level – ALL processes

Non-perturbative effects can be removed/isolated by cutting the region  $\ln(k_T) < 0$

# Dead cone on parton level

Parton level – no UE, no ISR

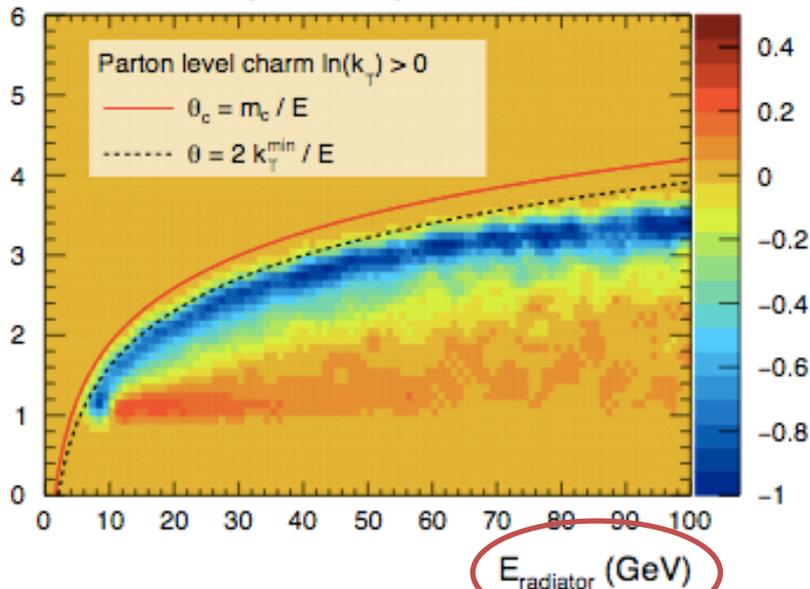
Angle vs. Energy of the radiator

Cut on  $\log(k_T) > 0$

$$E_{\text{radiator}} > 1/(z\theta)$$

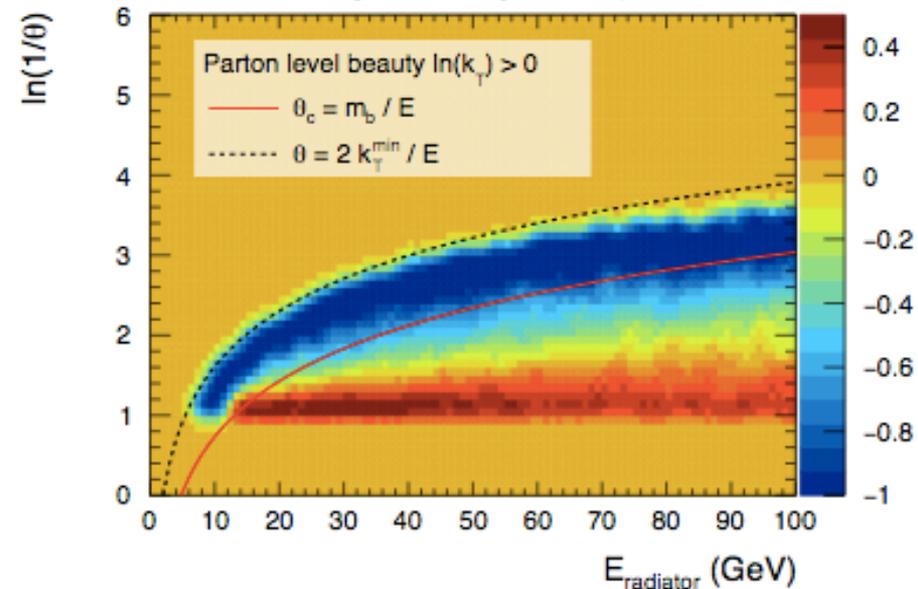
charm

Relative ratio to gluons and light flavor quarks



beauty

Relative ratio to gluons and light flavor quarks



$$Q = \frac{P^Q(\log(1/\theta), E_{\text{radiator}}) - P^{\text{inc}}(\log(1/\theta), E_{\text{radiator}})}{P^{\text{inc}}(\log(1/\theta), E_{\text{radiator}})}$$

The cut  $\log(k_T) > k_T^{\text{min}}$  translates into  $E_{\text{radiator}} > k_T^{\text{min}} / z\theta$ . The black dashed line corresponds to the kinematic limit of  $z=0.5$ , above which there are no more entries in the inclusive reference

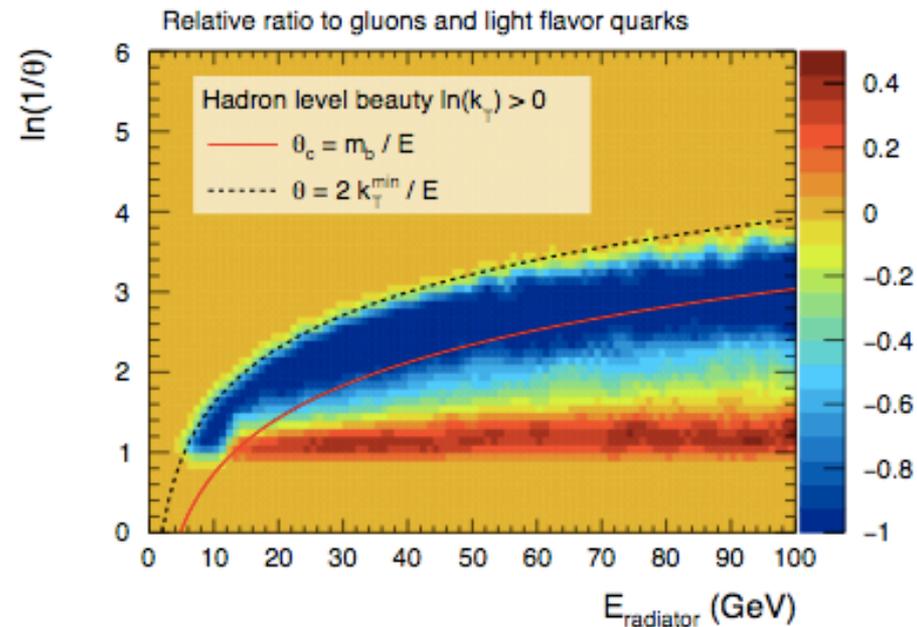
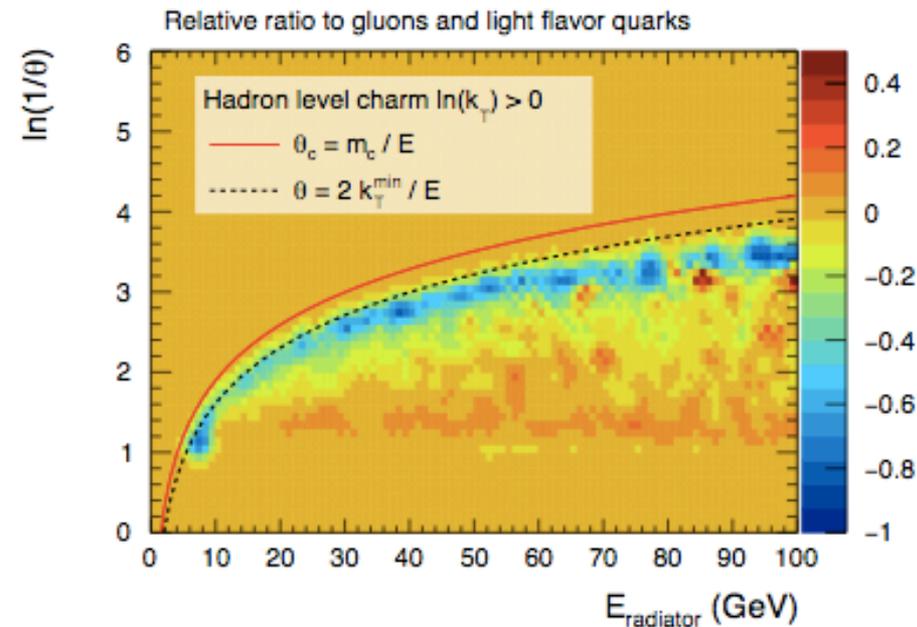
We can identify regions of phase space where  $P^Q = -1$ , meaning no radiation off the heavy quark radiator. **The suppression of large angles couples to the suppression of large  $z$**

# Dead cone at hadron level

Hadron level – ALL processes

**charm**

**beauty**



$$Q = \frac{P^Q(\log(1/\theta), E_{\text{radiator}}) - P^{\text{inc}}(\log(1/\theta), E_{\text{radiator}})}{P^{\text{inc}}(\log(1/\theta), E_{\text{radiator}})}$$

At hadron level the effects are smeared but not washed out

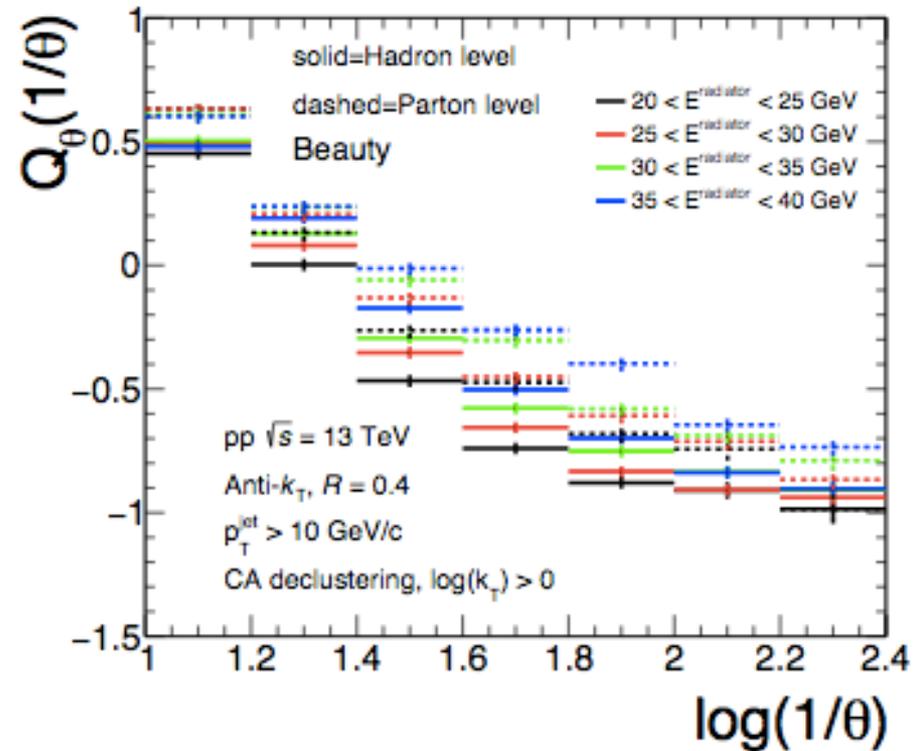
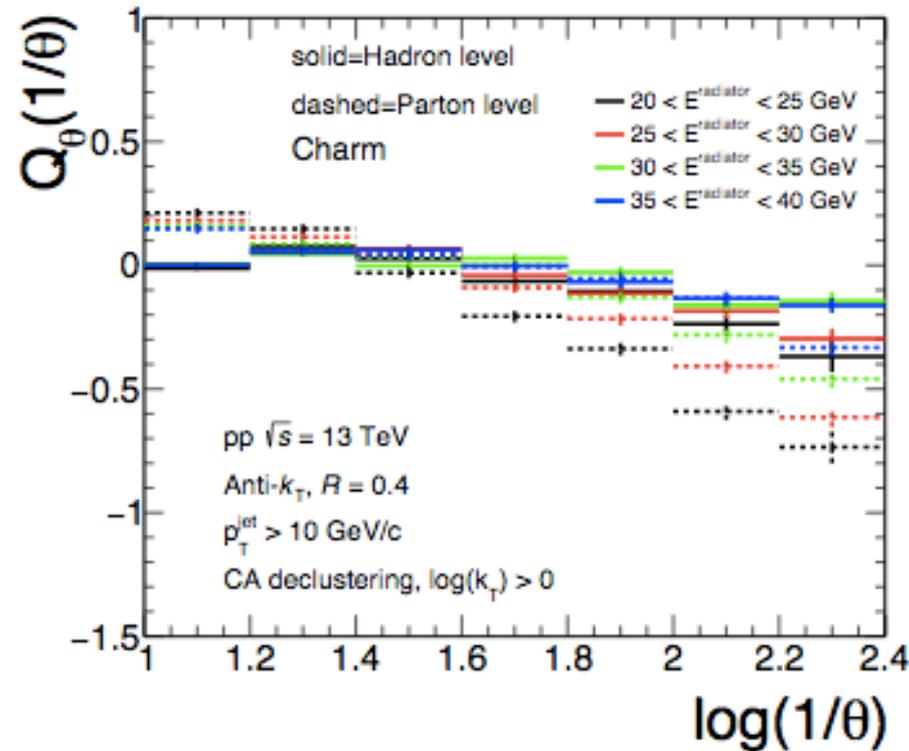
**As expected: the higher  $E_{\text{radiator}}$  is, the dead cone effects appear at smaller angles.**

**For D jets, the effects appear at measurable angles of  $\sim 0.1$  rad for radiator energies of 10-30 GeV**

**For B jets, one can go higher in radiator energy and still have effects at angles of the order of 0.1 rad**

# The observable – projections for E

$$Q_\theta = \frac{P^Q(1/\theta) - P^{inc}(1/\theta)}{P^{inc}(1/\theta)}, E_{\text{radiator}} \in (E_{\text{min}}, E_{\text{max}})$$



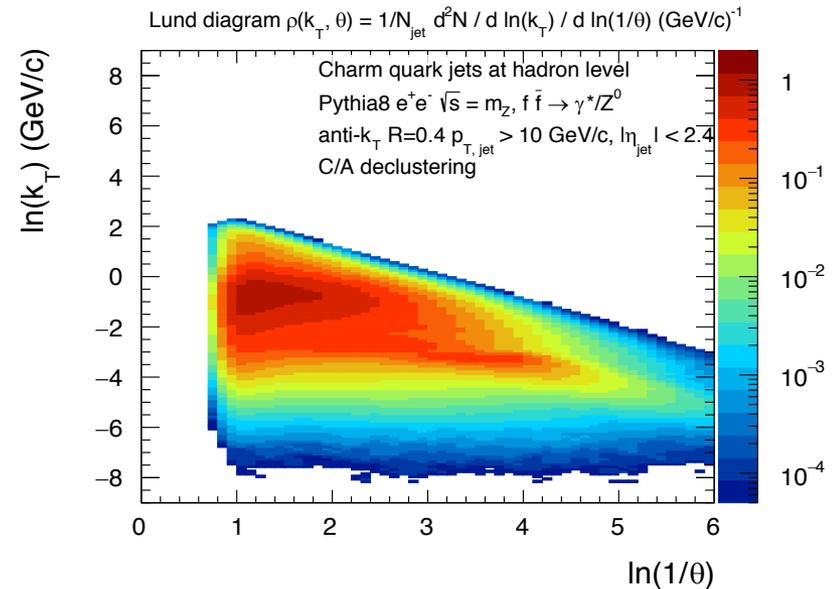
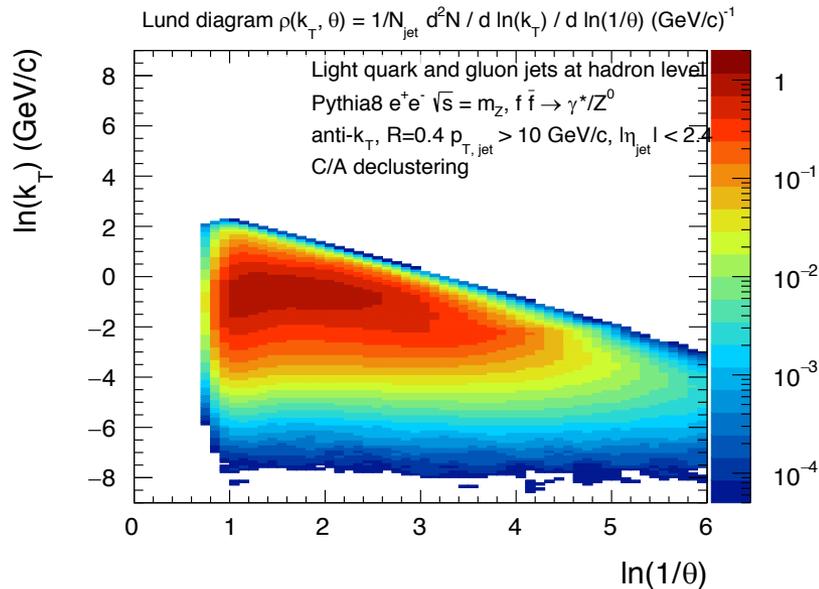
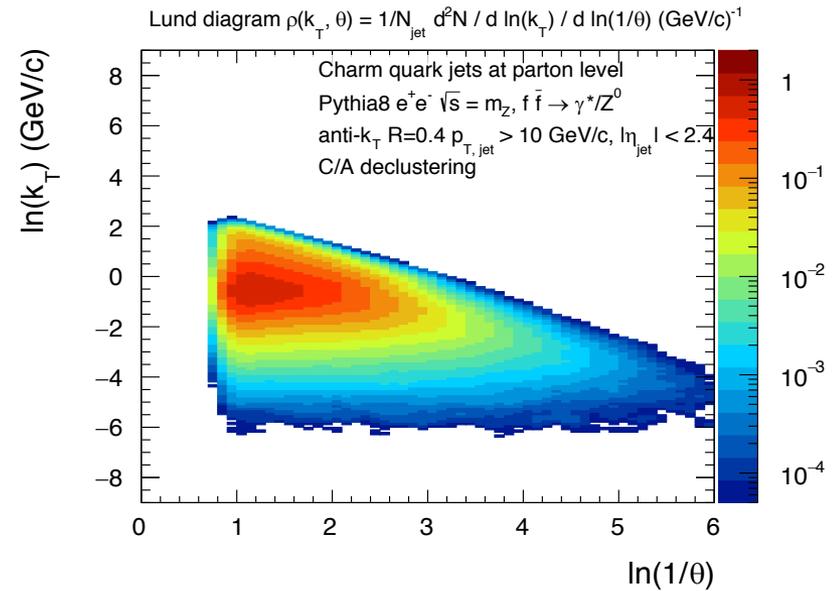
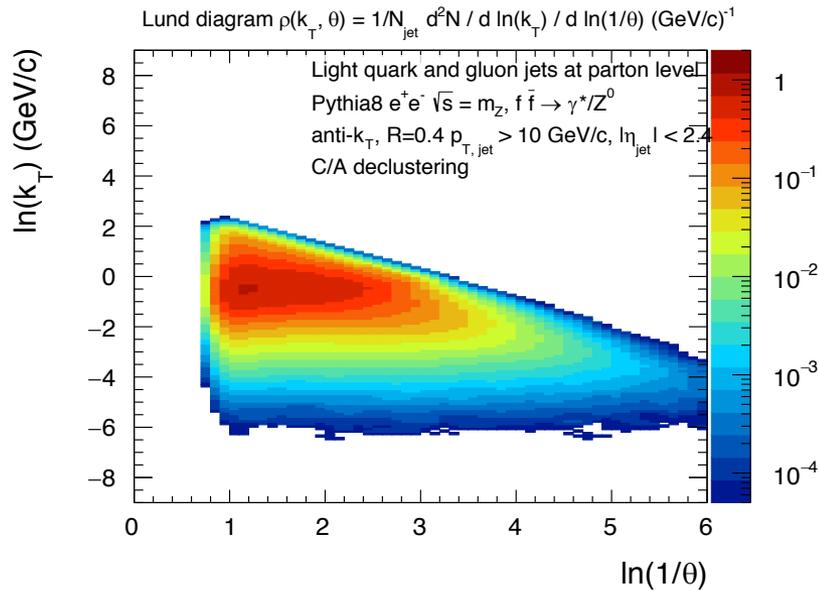
For  $E_{\text{radiator}}=20$  GeV,

D-jets are suppressed by 30% relative to inclusive at  $\theta \sim 0.1$  rad

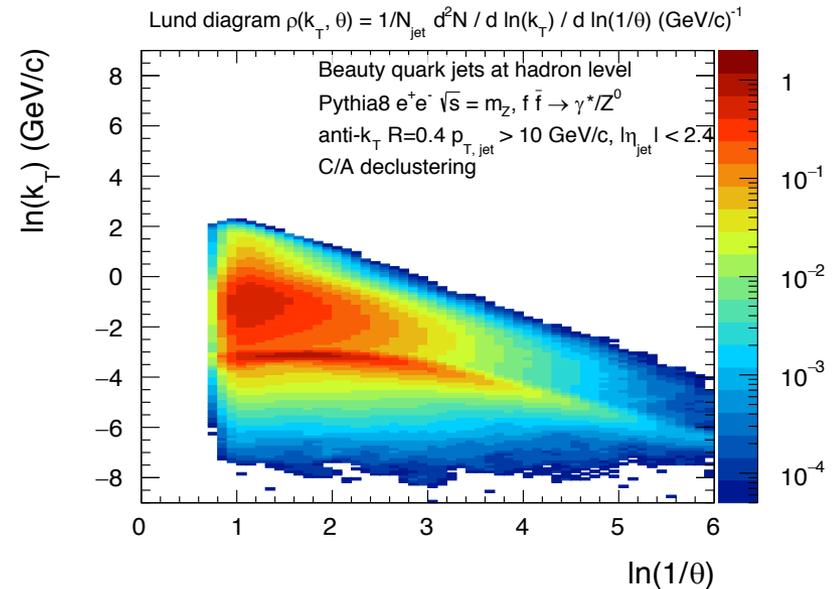
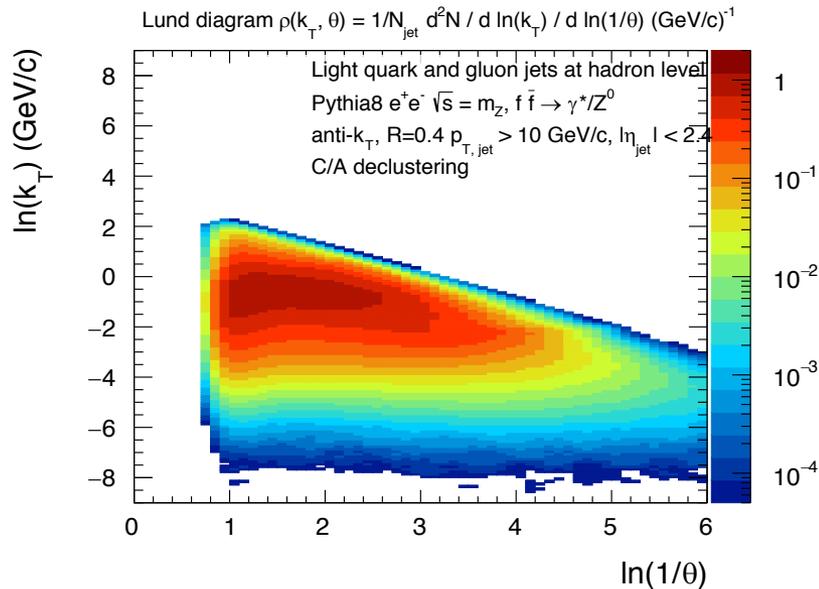
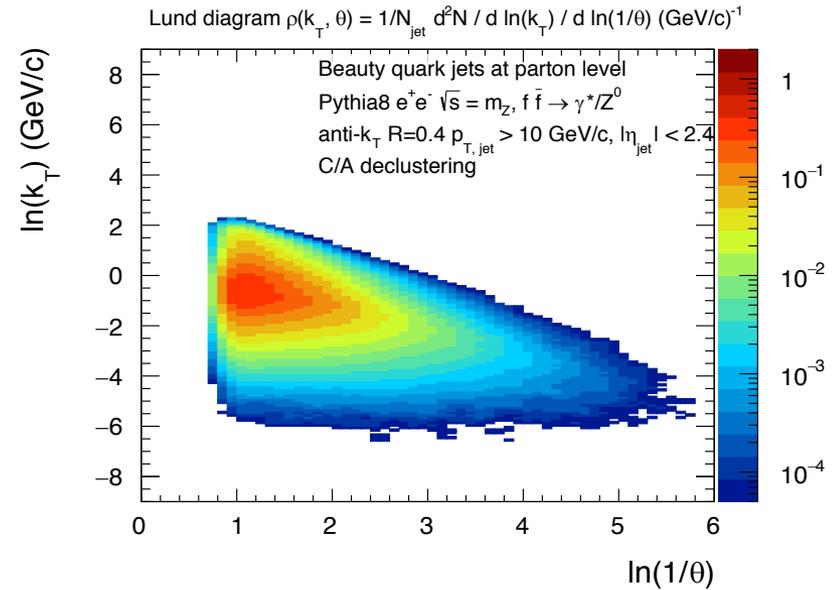
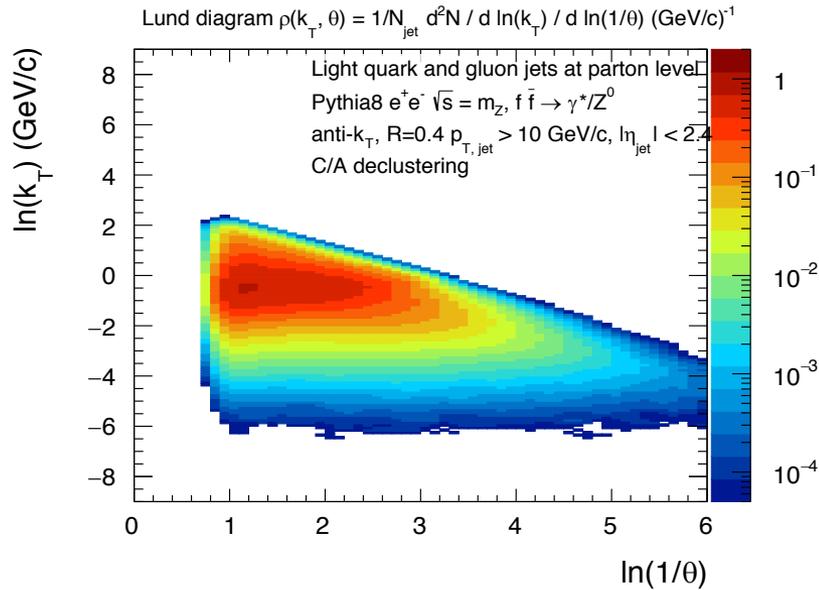
B-jets are suppressed by nearly by 100% relative to inclusive at  $\theta \sim 0.1$  rad

**OUTLOOK: REVISIT LEP, MEASURE AT  
LHC, ... EIC? DETAILED HADRONIZATION  
STUDIES?**

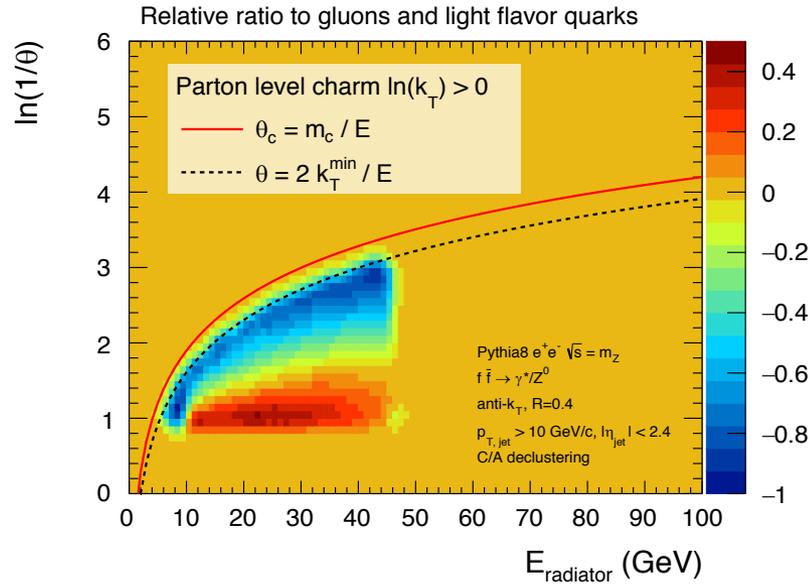
# Outlook : LEP, (eIC...) - charm



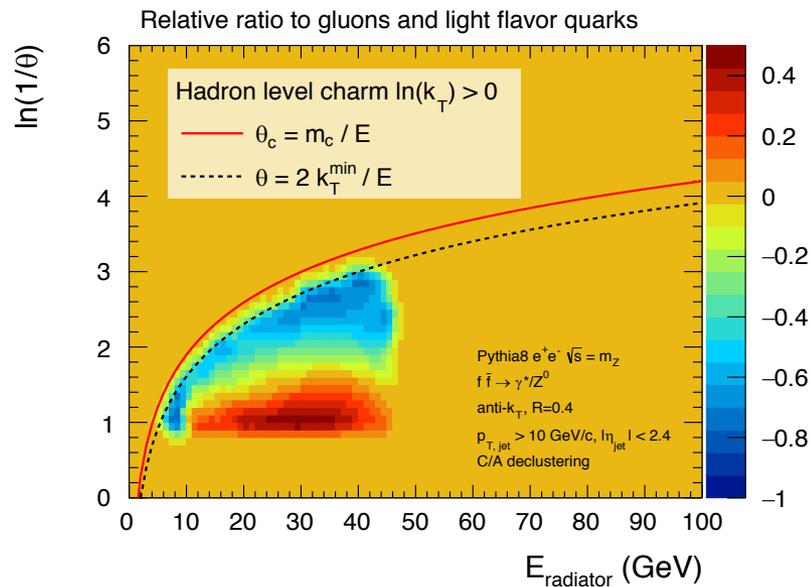
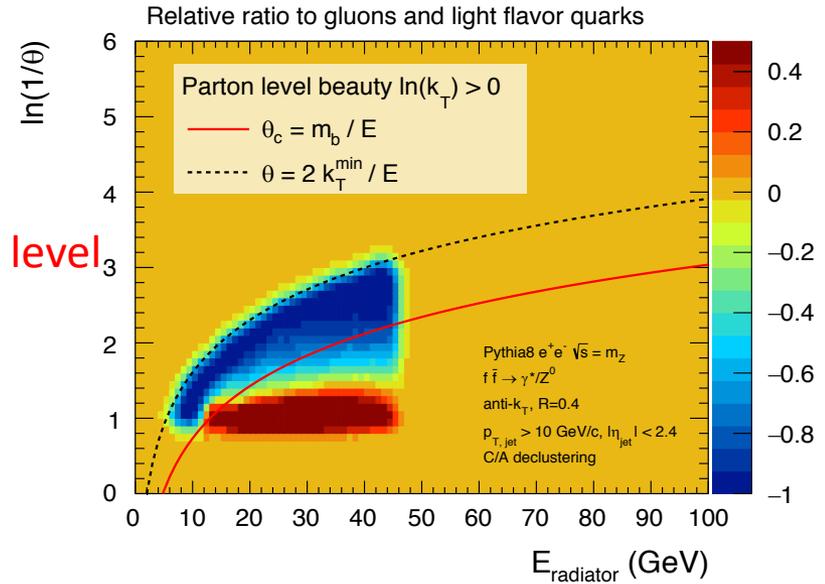
# Outlook : LEP, (eIC...) - beauty



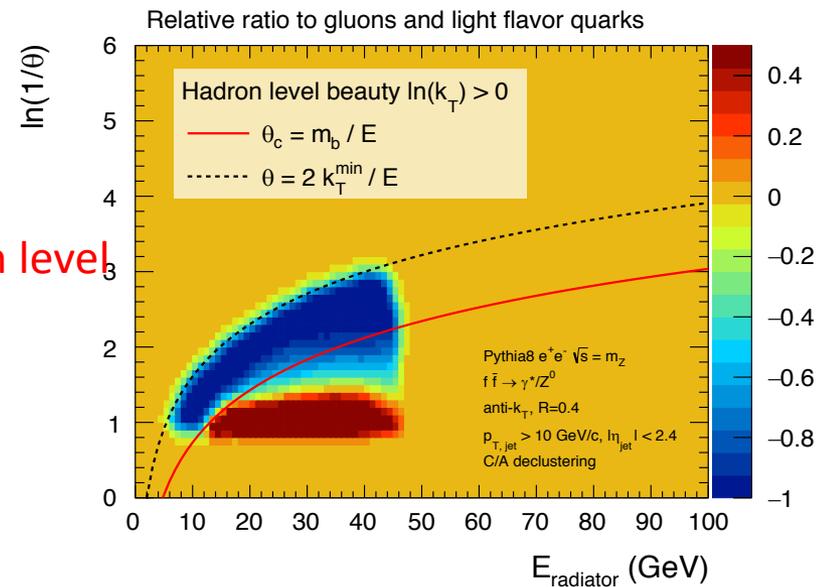
# Outlook : LEP, (eIC...)



Parton level



Hadron level



# A comment: $kT$ cut vs. Soft Drop ?

Soft Drop Condition:

$$\frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} > z_{\text{cut}} \left( \frac{\Delta R_{12}}{R_0} \right)^\beta$$

$$z = \frac{p_{t2}}{p_{t1} + p_{t2}}$$

$$k_T = p_{t2} \cdot \Delta R_{12}$$

$$p_{t2} > k_{T\text{cut}} \quad \text{for } R_0 = 1, \beta = 1$$

# Summary

- Dead cone at the subjet level:
  - rather “simple” conceptually
  - Cut on  $k_T$ : opportunity to study the effect systematically => constraints on hadronization? (LEP, eIC; hadronic collisions more difficult ISR, MPI,...) – other applications (TBStudied)?
- More applications for de-clustering in considerations (jet classification based on Lund plane -  $k_T$ )
  - Role for secondary plane (soft branches)?
  - Azimuthal angle? (hadronization, particle decays?)
- Opportunities for heavy-ion collisions – jet modifications, medium response(?), *different* grooming / selection of splittings... - BUT need to choose the ‘right’ observables (not all equally defined/calculable in theory)