

# NLO EW/QCD corrections for $W^+Z$ scattering at the LHC

$pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X @ \mathcal{O}(\alpha_s \alpha^6)$  and  $\mathcal{O}(\alpha^7)$  for  $\sqrt{s} = 13 \text{ TeV}$

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# Outline

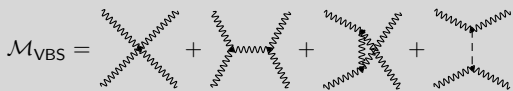
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- 2 Leading orders
- 3 Next-to-leading orders
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## Vector-boson scattering in a nutshell

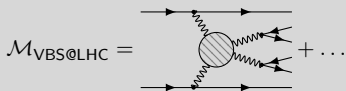
→ Scattering of two (massive) vector-bosons, e.g.:

- $W^\pm W^\pm \rightarrow W^\pm W^\pm$  (“like-sign W scattering”) → focus of WG1 so far: [A. Ballestrero et al.]
- $W^\pm Z \rightarrow W^\pm Z$

$$W^+ Z \rightarrow W^+ Z$$



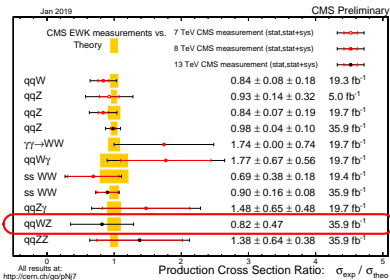
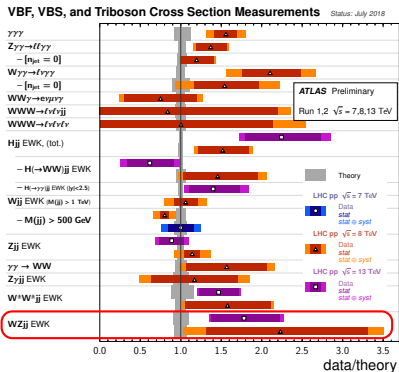
$$pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$$



Vector-boson scattering (VBS) physics program:

- Constrain anomalous quartic gauge couplings (with triple-gauge boson prod.)
  - Measure Higgs-vector-vector couplings, complementary to on-shell Higgs decay measurements
  - Probe EW symmetry breaking: interplay between triple and quartic gauge couplings and the Higgs boson(s); large cancellations for longitudinal VBS: ensures **tree-level unitarity**
- Precise prediction of the SM cross section needed

# Experiment: $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$

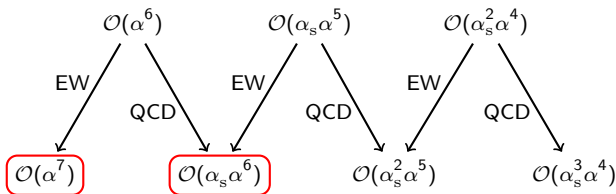


- ATLAS 8 TeV: [CERN-EP-2016-017]
- ATLAS 13 TeV: Observ. with  $5.6 \sigma$  sig. ( $\mathcal{L} = 36.1 \text{ fb}^{-1}$ ) [ATLAS-CONF-2018-033]
- ATLAS 13 TeV: Observ. with  $5.3 \sigma$  sig. ( $\mathcal{L} = 36.1 \text{ fb}^{-1}$ ) [CERN-EP-2018-286]

→ talk by Narei Lorenzo Martinez

- CMS 13 TeV: Meas. with  $1.9 \sigma$  sig. ( $\mathcal{L} = 35.9 \text{ fb}^{-1}$ ) [CMS-PAS-SMP-18-001]
- CMS 13 TeV: Meas. with  $2.2 \sigma$  sig. ( $\mathcal{L} = 35.9 \text{ fb}^{-1}$ ) [CMS-SMP-18-001]

Theory:  $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$



- All LOs presented in Sec. V.3 of the SM Les Houches 2017 report [Bendavid et al.]: QCD (~80%) dominates over EW
  - Approx.  $\mathcal{O}(\alpha_s \alpha^6)$ : +4% [Bozzi, Jäger, Oleari, Zeppenfeld]
  - $\mathcal{O}(\alpha_s^3 \alpha^4)$  calculation available [Campanario, Kerner, Ninh, Zeppenfeld]
  - Parton-shower effects of the EW production [Jäger, Karlberg, Scheller]
- $\mathcal{O}(\alpha^7)$  EW corrections desirable, because like-sign case shows large corrections (-16%)
- calculate full  $\mathcal{O}(\alpha_s \alpha^6)$  for an updated setup, check validity of approximations

## Fiducial phase space volume and parameters

Cuts are exactly the “Loose Fiducial” cuts defined by CMS<sup>1</sup>[CMS-PAS-SMP-18-001]:

- At least two  $R = 0.4$  anti- $k_t$  jets with  $p_T > 30$  GeV,  $|\eta| < 4.7$ , and  $\Delta R_{j\ell} > 0.4$
- $M_{j_1 j_2} > 500$  GeV,  $\Delta\eta_{j_1 j_2} > 2.5$
- $p_{T,\ell} > 20$  GeV and  $|y_\ell| < 2.5$
- $|M_{\mu\bar{\mu}} - M_Z| < 15$  GeV
- $M_{\ell\ell} > 4.0$  GeV and  $M_{3\ell} > 100.0$  GeV

Other:

- Photons recombined with charged particles using anti- $k_t$  algorithm with  $R = 0.1$
- PDFs: NNPDF31\_nlo\_as\_0118\_luxqed
- $\sqrt{s} = 13$  TeV

Complex mass scheme [Denner, Dittmaier, Roth, Wackerroth][Denner, Dittmaier, Roth, Wieders], input parameters:

- $G_\mu = 1.6638 \times 10^{-5} \text{ GeV}^{-2}$
- $M_W = 80.3530$  GeV,  $\Gamma_W = 2.0843$  GeV
- $M_Z = 91.1535$  GeV,  $\Gamma_Z = 2.4943$  GeV
- $M_H = 125.0$  GeV,  $\Gamma_H = 4.07 \times 10^{-3}$  GeV

with EW coupling calculated as:

$$\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left( 1 - \frac{M_W^2}{M_Z^2} \right)$$

Scale choice:

- $\mu = \sqrt{p_{T,j_1} \cdot p_{T,j_2}}$  [Denner, Hošeková, Kallweit]
- 7-point scale variation to estimate pert. uncertainty

<sup>1</sup>Results for an ATLAS-like setup in backup-slides

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- 1 Introduction
- 2 Leading orders**
  - Overview
  - Integrated cross sections
  - Distributions
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- 4 Next-to-leading order results
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## Overview: leading orders

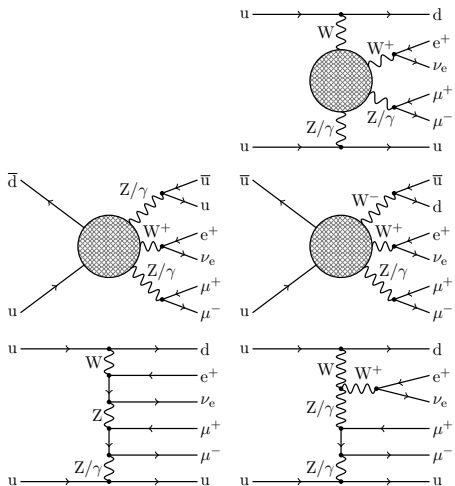
For  $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$  two different leading orders (LO):  $\mathcal{O}(g_s^2 e^4)$  and  $\mathcal{O}(e^6)$ .

We divided them into five (mutually exclusive) classes:

- ①  $\mathcal{O}(\alpha^6)$  **electroweak production** with quark-quark initial state (but without bottom-quarks)
- ②  $\mathcal{O}(\alpha_s^2 \alpha^4)$  **strong production** (without bottom-quarks)
- ③  $\mathcal{O}(\alpha_s \alpha^5)$  quark-quark **interference**
- ④  $\mathcal{O}(\alpha^6)$  double-**photon** initiated and  $\mathcal{O}(\alpha_s \alpha^6)$  single-**photon** initiated
- ⑤  $\mathcal{O}(\alpha^6)$  and  $\mathcal{O}(\alpha_s^2 \alpha^4)$  with **bottom-quarks**

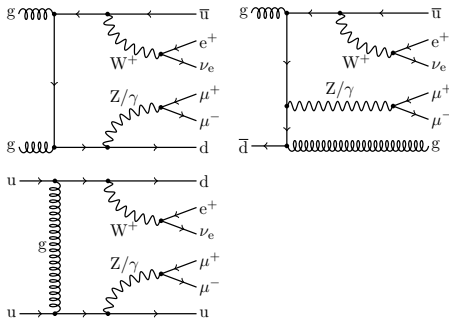


## Electroweak production LOs



- 40 different partonic channels at  $\mathcal{O}(\alpha^6)$
- contain the **vector-boson scattering** subdiagrams,
- and “semi-leptonic triple-gauge-boson production” processes ( $W^\pm ZZ$  and  $W^+W^-Z$ ),
- and other double-, single, non-resonant diagrams

## Strong production LOs

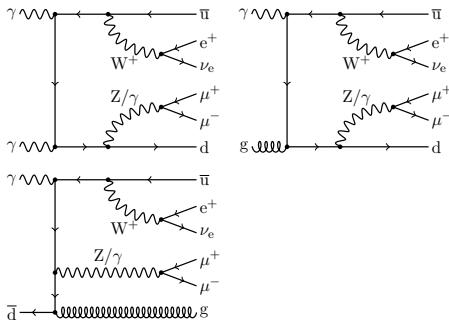


→ In comparison to like-sign W-scattering gluons are possible at LO (charge)

- 8 additional diagrams with **two gluons**, making up 66 % of the cross section

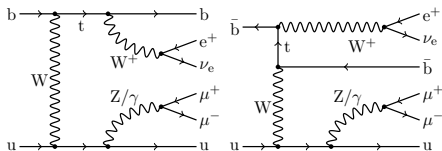
→ in total the  $\mathcal{O}(\alpha_s^2 \alpha^4)$  is **4.3 times larger** than the electroweak LOs

## Photon-initiated LOs



- 2 **double photon** MEs at  $\mathcal{O}(\alpha^6)$  (tiny contribution)
- 12 **photon-gluon** MEs at  $\mathcal{O}(\alpha_s \alpha^5)$  (very small contribution)
- remember: no final state photons at LO because of  $n_j \geq 2$

## Bottom-quark LOs



- 12 MEs with **bottom-quarks**
- “top-Z-jet production” for the  $bu/bc \rightarrow e^+ \nu_e \mu^+ \mu^- bu/c$
- only resonant tops, **no** resonant anti-tops because of  $W^+ \rightarrow$  up-bottom contribution dominates over all others (90%)
- contribution comparable in size with the EW LOs
- separable with b-tagging

## LO integrated cross sections

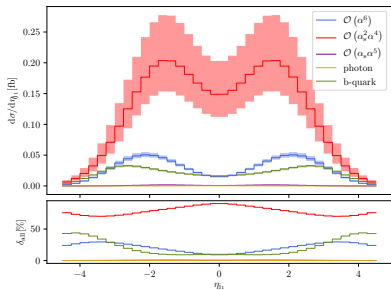
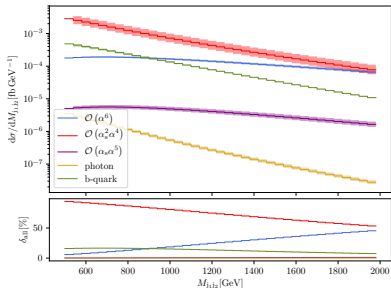
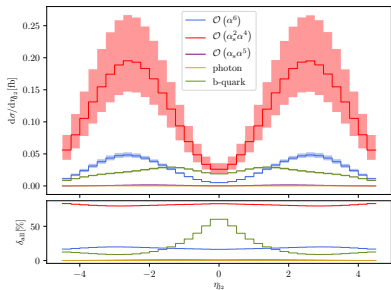
Integrated xs for  $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj$  @  $\sqrt{s} = 13$  TeV:

| Sum [fb] | EW [fb]                     | QCD [fb]                   | Int. [fb]                     |
|----------|-----------------------------|----------------------------|-------------------------------|
| 1.55     | $0.255^{+9.03\%}_{-7.75\%}$ | $1.10^{+37.0\%}_{-24.9\%}$ | $0.00682^{+18.4\%}_{-14.4\%}$ |
| 100 %    | 16.4 %                      | 70.6 %                     | 0.439 %                       |

| Photons [fb]                   | Bottom-quarks [fb]          |
|--------------------------------|-----------------------------|
| $0.000988^{+11.5\%}_{-9.47\%}$ | $0.195^{+3.59\%}_{-7.22\%}$ |
| 0.0636 %                       | 12.5 %                      |

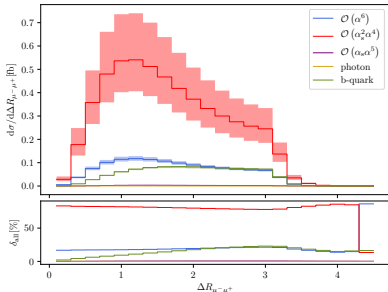
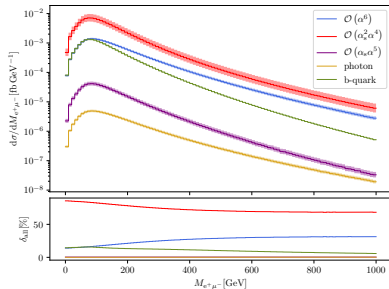
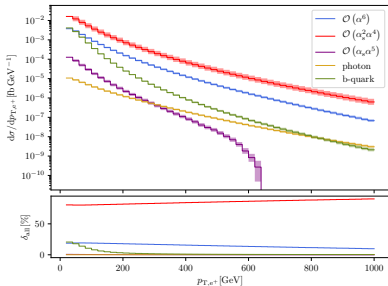
- very large **QCD** contributions mainly due to gluon-PDF
- small **interference** (known from like-sign VBS)
- smaller **EW** contribution compared to like-sign VBS ( $\rightarrow$  Z-boson)
- **photon** contributions completely irrelevant  $\rightarrow$  leave out photon-initiated at NLO
- important: **bottom-quark** contributions

## Jet observables



- $\delta_{all}$ : percentage of each contr. to the sum
- Crossover between EW/bottom-quarks at  $M_{j_1j_2} \approx 900$  GeV and EW/QCD at  $M_{j_1j_2} \approx 2100$  GeV
- interesting behavior of the subleading jet for bottom-quark contributions for the central region
- large QCD uncertainty band due to  $\alpha_S^2$  vs.  $\alpha_S^0$  in the EW

# Leptonic observables



- Cuts  $M_{\mu^-\mu^+} < M_Z + 15 \text{ GeV}$  and  $p_{T,\ell} > 20 \text{ GeV}$  limit  $\Delta\eta_{\mu^-\mu^+} < 3.4$ , so that  $\Delta R < 4.6$

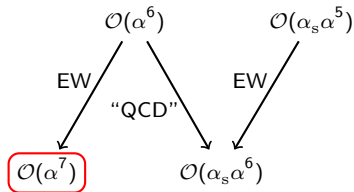
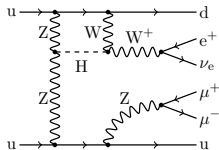
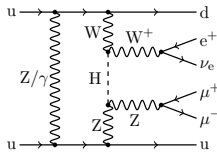
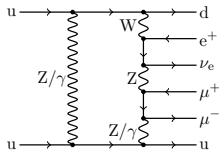
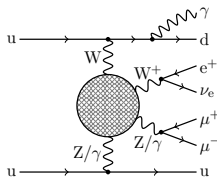
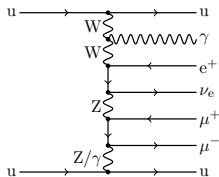
$$\cosh \Delta\eta_{\ell_1\ell_2} = \frac{M_{\ell_1\ell_2}}{2p_{T,\ell_1}p_{T,\ell_2}} + \cos \phi_{\ell_1\ell_2}$$

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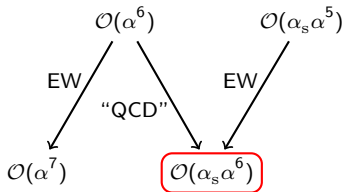
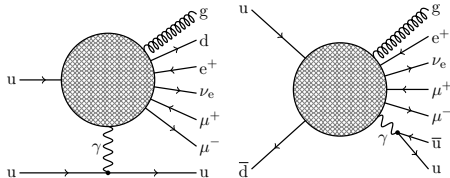
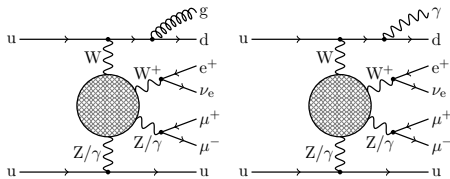
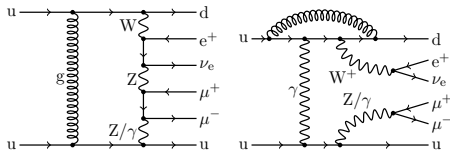


# $\mathcal{O}(\alpha^7)$ real and virtual correction diagrams



- Real radiation  $\rightarrow$  add **photon**
- Neglect real MEs with initial state photons
- Loops with 8-point functions, different complex masses
- More diagrams with Higgs bosons!
- Up to **83,000 diagrams** per initial state

# $\mathcal{O}(\alpha_s \alpha^6)$ mixed corrections: "QCD"



→ Correction is neither purely QCD/EW, it is mixed

- photon initial-state singularities: cancelled with collinear counterterm (PDFs)
- photon final-state singularities: require photon-to-jet transition functions (strictly speaking)
- **many** partonic channels and contributions: 40 virtuals, 16 EW reals, 40+28 QCD reals, 16 EW int. dipoles, 40 QCD int. dipoles, ...

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## Integrated cross section

Integrated xs for  $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$  @  $\sqrt{s} = 13$  TeV:

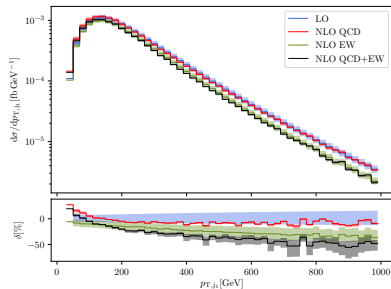
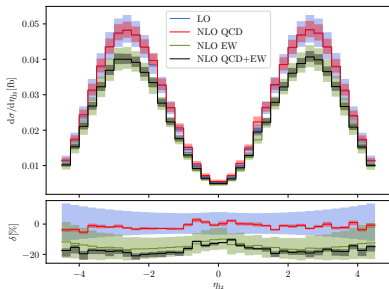
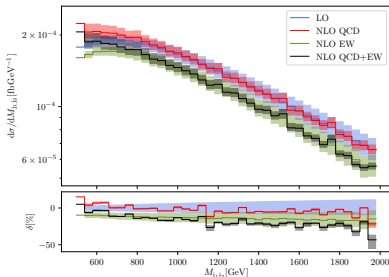
| LO <sup>2</sup> [fb]                      | NLO EW [fb]   | NLO QCD [fb]  | NLO EW+QCD [fb]                                      |
|---|---|---|--|
| 0.255 <sup>+9.03%</sup> <sub>-7.75%</sub> | 0.214 <sup>+8.62%</sup> <sub>-7.43%</sub><br>-16.0% | 0.250 <sup>+0.970%</sup> <sub>-0.960%</sub><br>-1.93% | 0.209 <sup>+0.750%</sup> <sub>-1.08%</sub><br>-17.9% |

Please note: NLO QCD (and NLO EW+QCD) are preliminary

- No dep. on  $\mu_R$  → No reduction of the pert. uncertainty for the NLO EW
- **Large corrections** on the integrated cross section, comparable to like-sign scattering
- Corrections are larger in specific regions of  $p_T$  distributions
- QCD corrections rather small

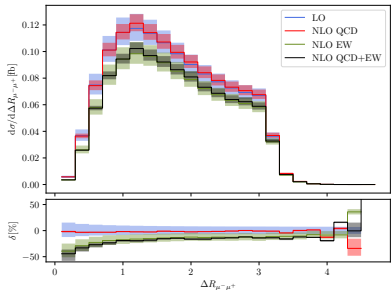
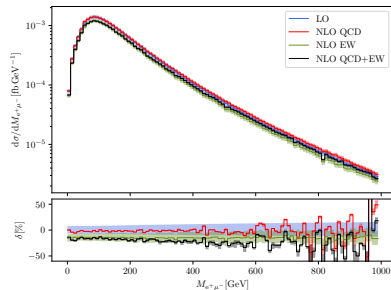
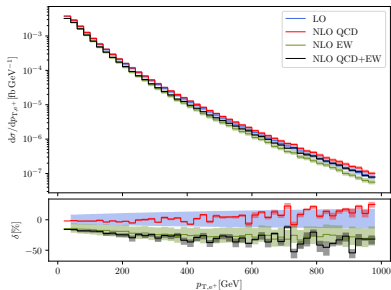
<sup>2</sup>only  $\mathcal{O}(\alpha^6)$

## Jet observables



- Please note: NLO QCD (and NLO EW+QCD) are preliminary
- EW/QCD corrections basically flat for  $M_{j_1j_2}$
- $M_{e^+\mu^-}$  very flat conc. EW and QCD corrections
- EW corrections become more negative for large  $p_{T,j_1}$

## Leptonic observables



- Please note: NLO QCD (and NLO EW+QCD) are preliminary
- EW corrections “remove” events where the muons are close

## Summary

- After  $W^+W^+$ ,  $W^+Z$  scattering is the next important channel for VBS
- **Large EW corrections** for a realistic setup:  $-16\%$
- Even larger corrections for some  $p_T$  observables
- First preliminary results for the complete  $\mathcal{O}(\alpha_s\alpha^6)$ : small corrections,  $-2\%$
- Confirms that  $\mu = \sqrt{p_{T,j_1} \cdot p_{T,j_2}}$  is (still) a good scale choice

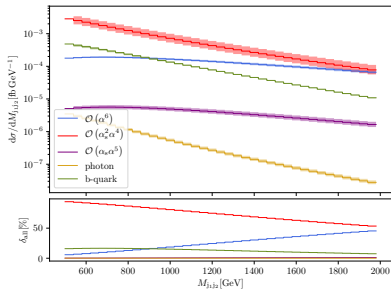
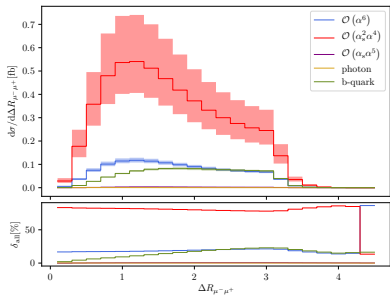
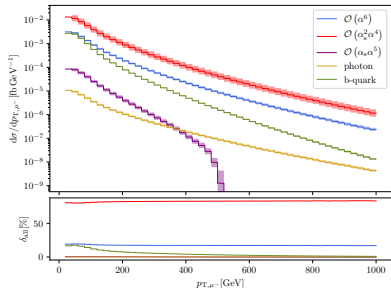
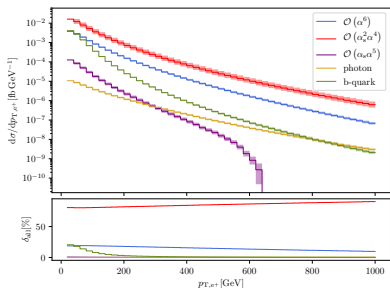
## Acknowledgments

# Thank you!

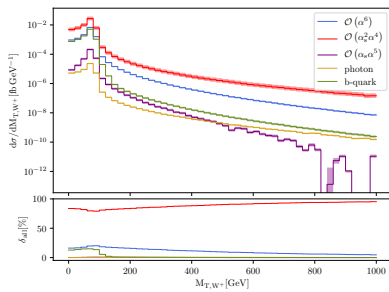
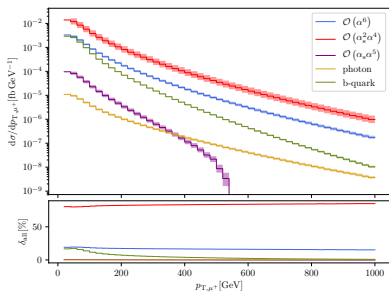
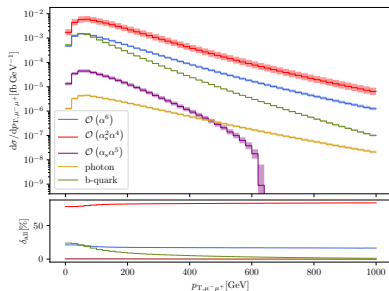
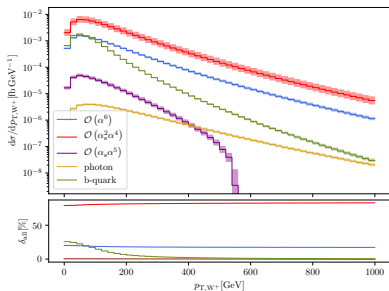
- We acknowledge support by the state of Baden-Württemberg through bwHPC and the German Research Foundation (DFG) through grant no INST 39/963-1 FUGG and grant DI 784/3.
- This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 740006.



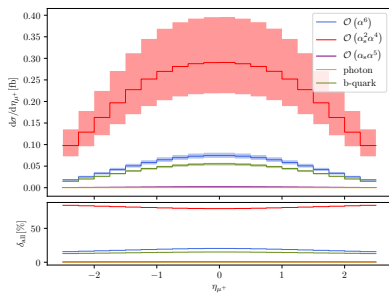
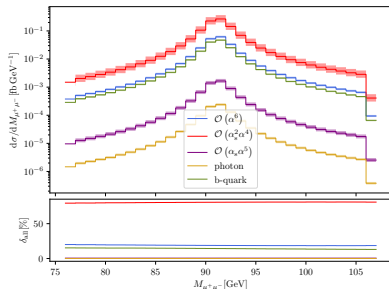
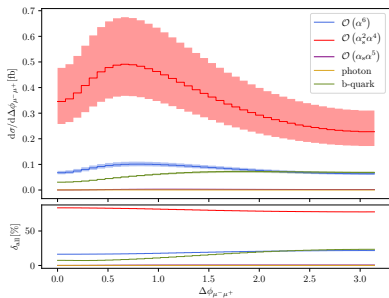
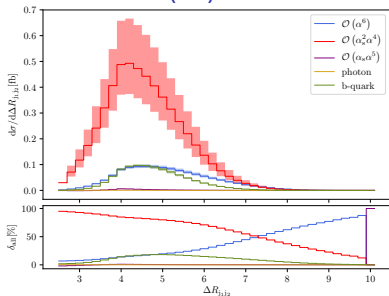
## LO distributions (I)



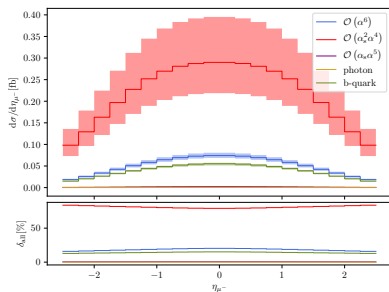
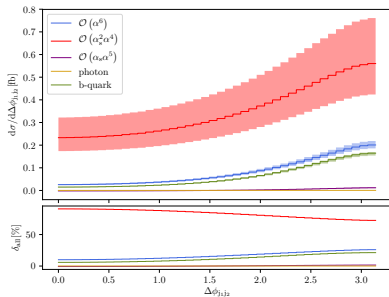
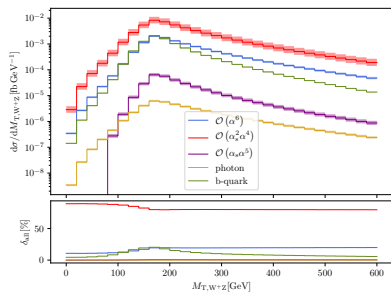
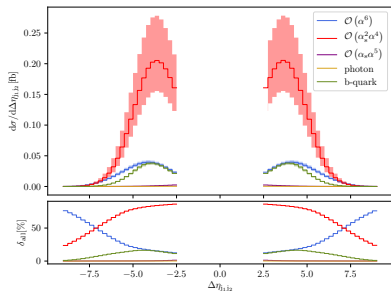
## LO distributions (II)



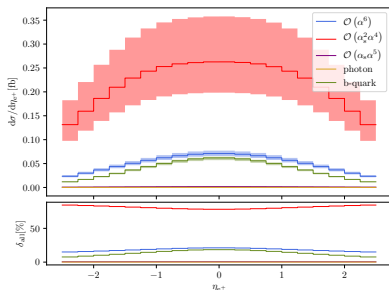
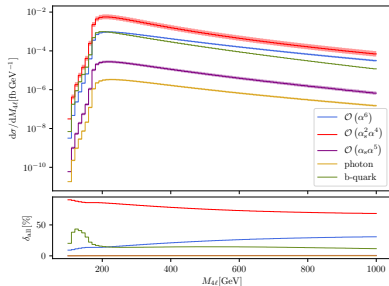
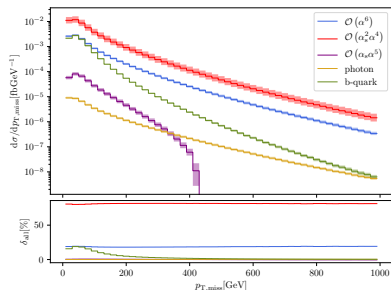
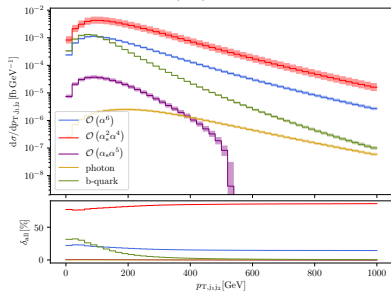
## LO distributions (III)



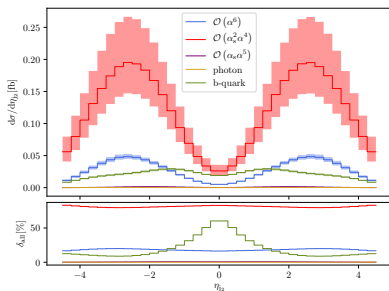
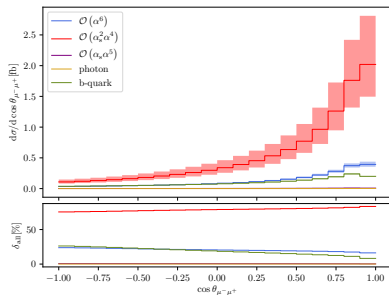
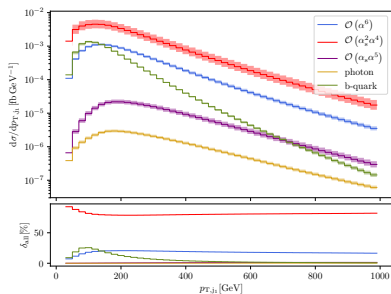
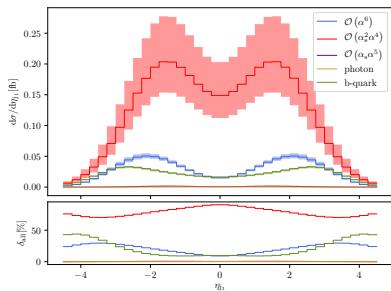
## LO distributions (IV)



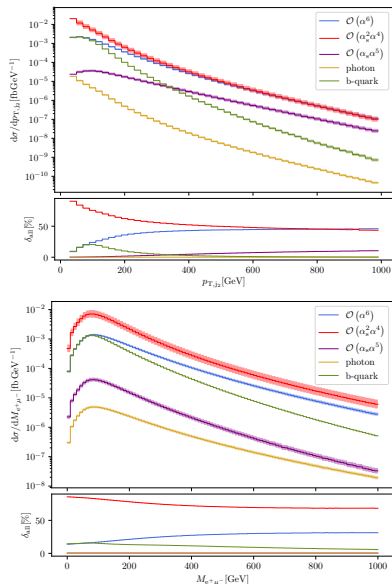
## LO distributions (V)



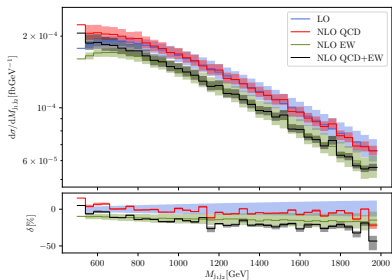
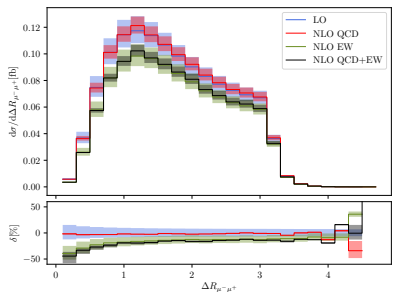
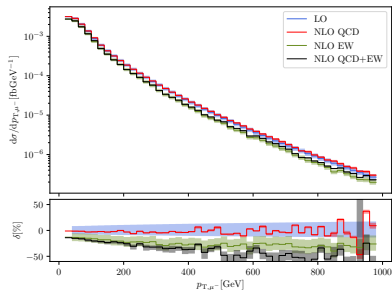
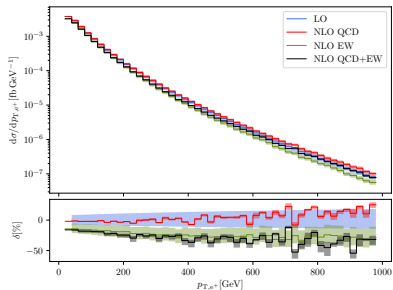
## LO distributions (VI)



## LO distributions (VII)

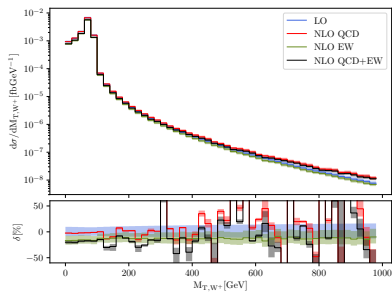
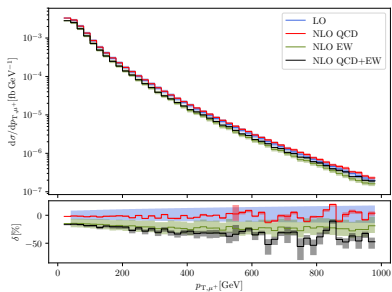
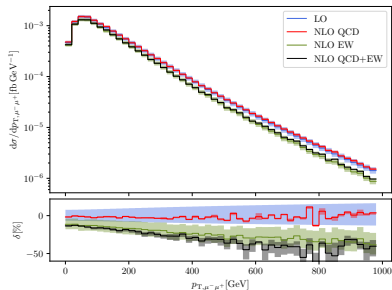
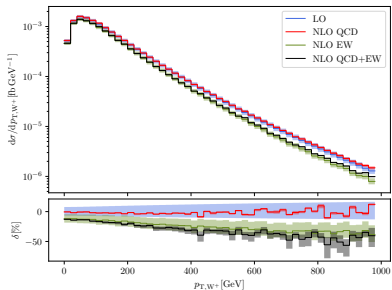


## NLO distributions (I)

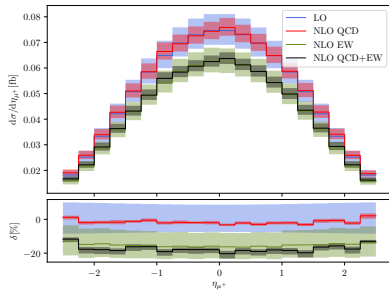
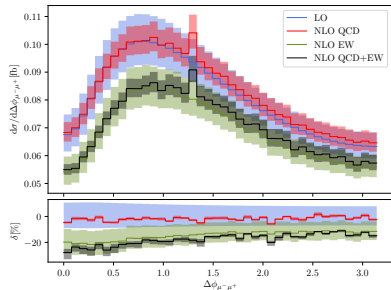
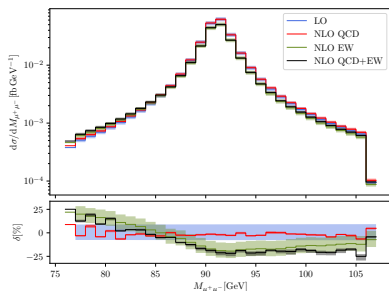
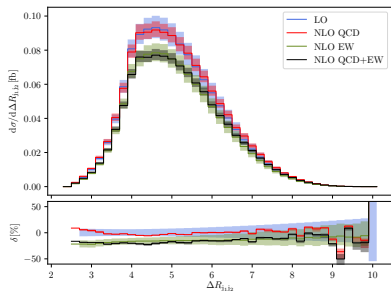




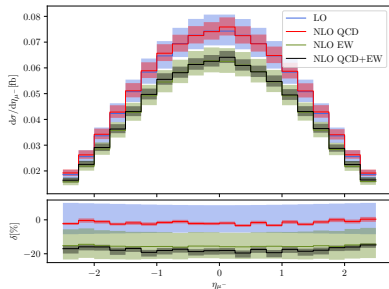
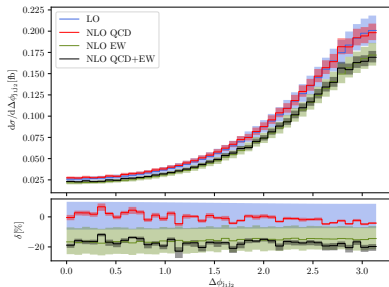
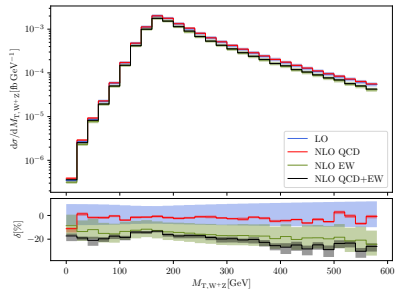
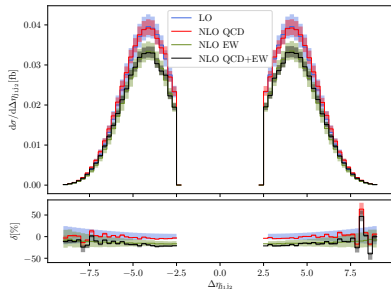
## NLO distributions (II)



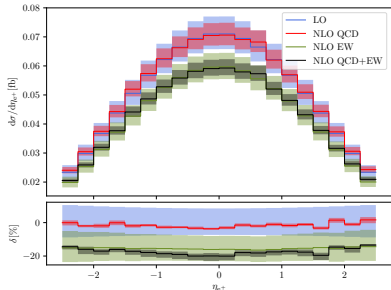
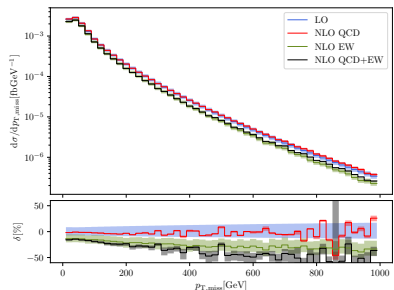
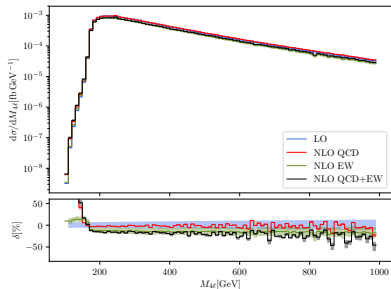
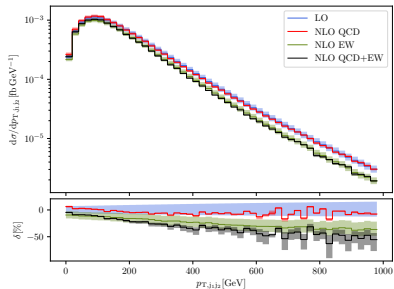
## NLO distributions (III)



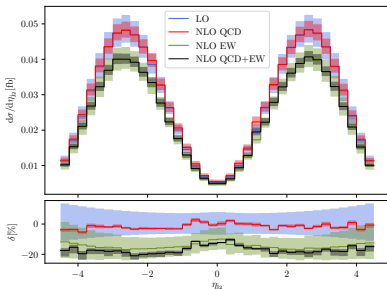
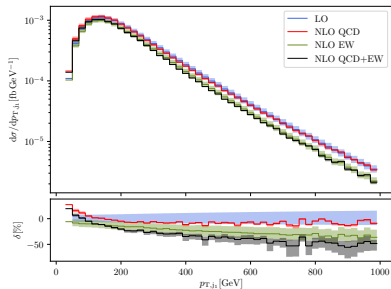
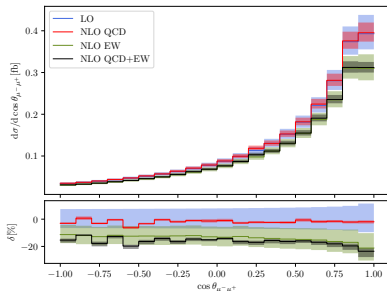
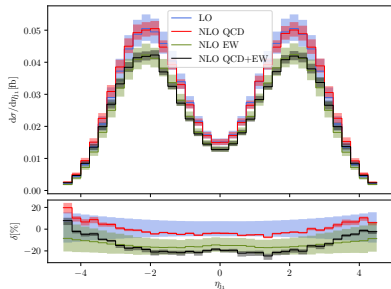
## NLO distributions (IV)



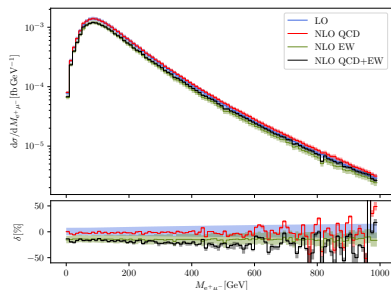
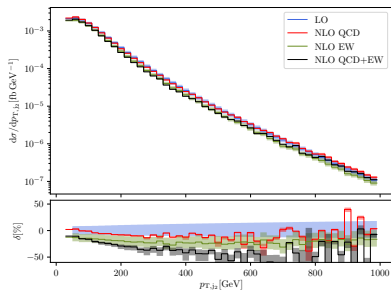
## NLO distributions (V)



## NLO distributions (VI)



## NLO distributions (VII)



## Fiducial phase space volume for the ATLAS-like setup

Cuts chosen similar to the ATLAS

8 TeV-analysis [CERN-EP-2016-017]:

- At least two  $R = 0.4$  anti- $k_t$  jets with  $p_T > 30$  GeV,  $|\eta| < 4.5$ , and  $\Delta R_{j\ell} > 0.3$
- $M_{j_1 j_2} > 500$  GeV, **no  $\Delta\eta_{j_1 j_2}$  cut<sup>2</sup>**
- $p_{T,\ell} > 20$  GeV and  $|y_\ell| < 2.5$
- $p_{T,\text{miss}} > 30$  GeV
- $|M_{\mu\bar{\mu}} - M_Z| < 10$  GeV
- $\Delta R_{\ell\ell} > 0.3$

Other:

- Photons recombined with charged particles using anti- $k_t$  algorithm with  $R = 0.1$
- PDFs: NNPDF30\_nlo\_as\_0118\_qed
- $\sqrt{s} = 13$  TeV

Complex mass scheme [Denner, Dittmaier, Roth, Wackerroth][Denner, Dittmaier, Roth, Wieders], input parameters:

- $G_\mu = 1.663\,787 \times 10^{-5} \text{ GeV}^{-2}$
- $M_W = 80.357\,97 \text{ GeV}$ ,  $\Gamma_W = 2.084\,30 \text{ GeV}$
- $M_Z = 91.153\,48 \text{ GeV}$ ,  $\Gamma_Z = 2.494\,27 \text{ GeV}$
- $M_H = 125.0 \text{ GeV}$ ,  $\Gamma_H = 4.07 \times 10^{-3} \text{ GeV}$

with coupling calculated as:

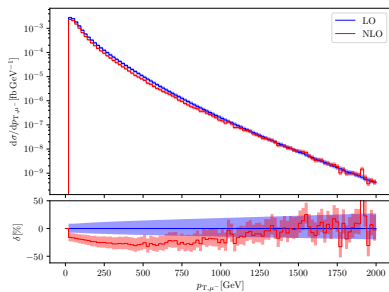
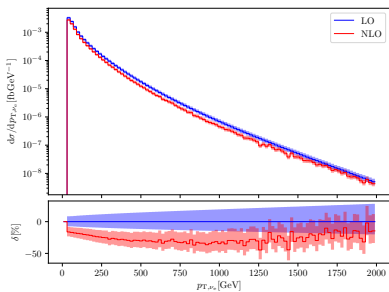
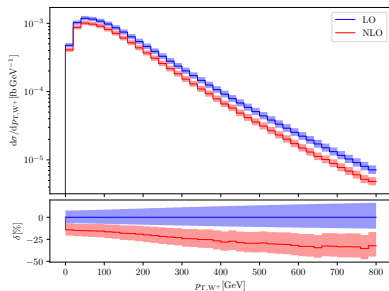
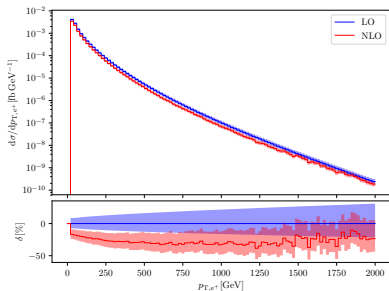
$$\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left( 1 - \frac{M_W^2}{M_Z^2} \right)$$

Scale choice:  $\mu_F = (1/2, 1, 2) \cdot M_W$

→ **No dependence on  $\mu_R$** , since processes do not depend on  $\alpha_s$ !

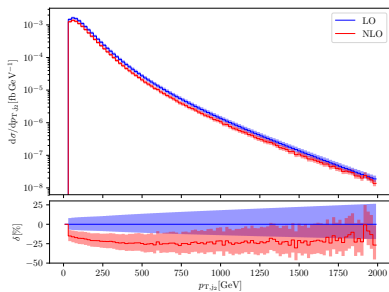
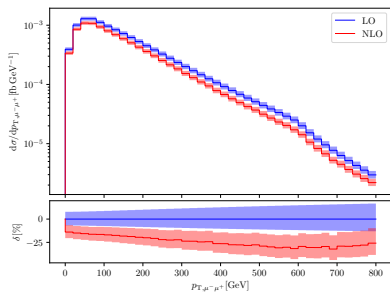
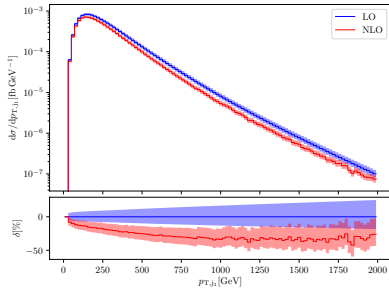
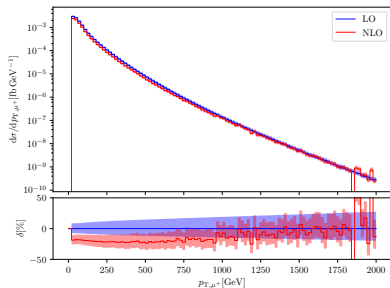
<sup>1</sup>Unused in the ATLAS 8 TeV-analysis, but used both in the ATLAS and CMS 13 TeV analyses

## Distributions (I)

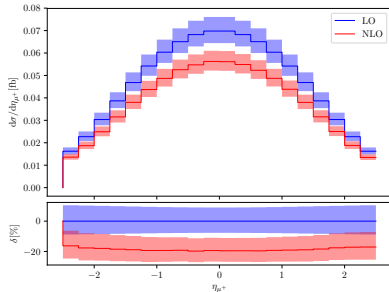
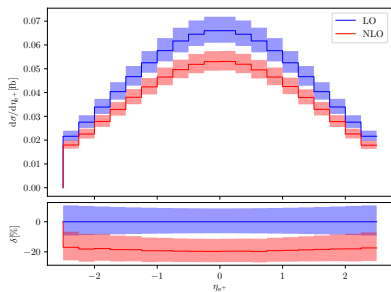
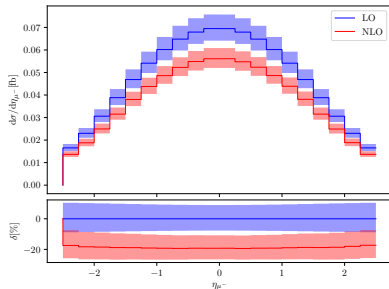
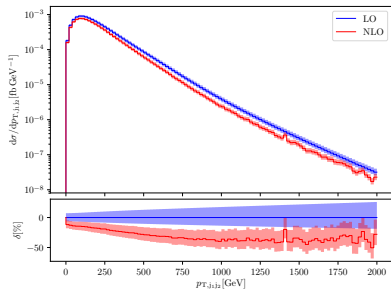




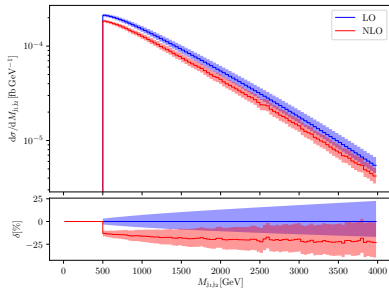
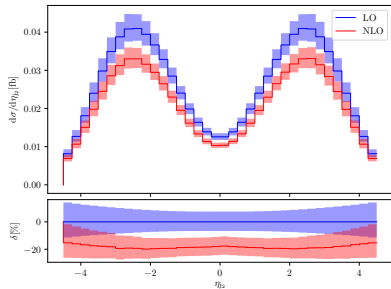
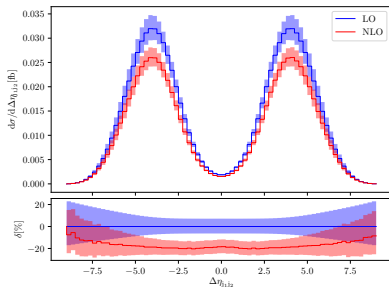
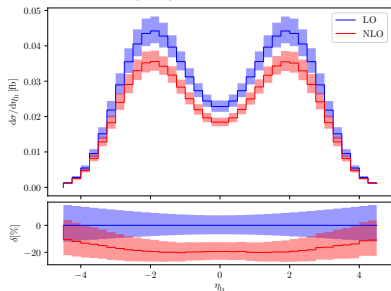
## Distributions (II)



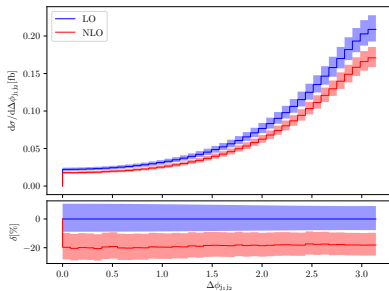
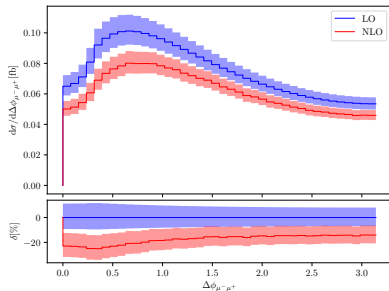
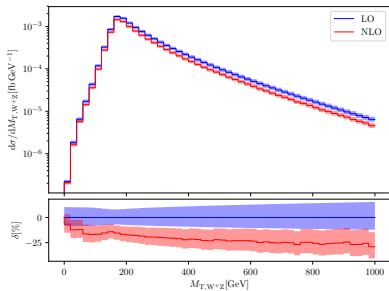
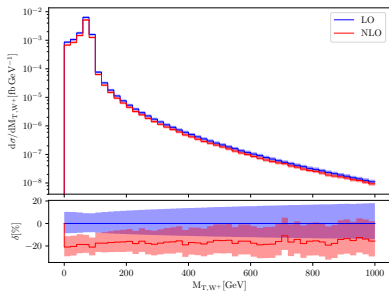
## Distributions (III)



## Distributions (IV)



## Distributions (V)



## Distributions (VI)

