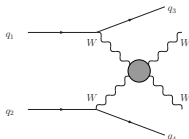


# A MadGraph model for VBS based on a unitarized non-linear EChL analysis

Presented by Rafael L. Delgado

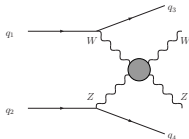
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by  $W^+W^- \rightarrow W^+W^-$  scattering



$$pp \rightarrow WZj_1j_2$$

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VBSCan@Ljubljana, University of Ljubljana, Ljubljana, Slovenia

# Linear vs. non-linear: linear representation

- The  $\omega^a$  and  $h$  fit in a left  $SU(2)$  doublet.
- The Higgs always appears in the combination  $h + v$ .
- Typical situation when  $h$  is a fundamental field.
- Based in a **cutoff  $\Lambda$  expansion**:  $\mathcal{O}(d)/\Lambda^{d-4}$ ,  $d$  and operator of dimension  $d = 4, 6, 8, \dots$
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# Unitarity problem

- VBS amplitude rises with energy, eventually leading to violation of unitarity at some new physics state.
- This leads to an *OVERESTIMATED* number of events in VBS due to an unphysical prediction of EFT. That is, amplitudes *cannot* grow uncontrolled.
- Exception, MSM: Higgs exchange exactly cancels this energy rise in VBS, restoring unitarity event at LO.
- Two options:
  - Set up a low-energy cut-off on the theory, due to the validity limits of the EFT itself. This limit, indeed, comes from the UV completion, whose specification would require to pick up a full (renormali. and unitar.) model from the *theory zoo*.
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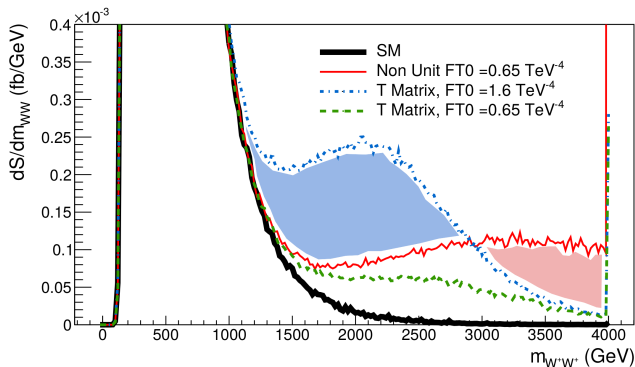
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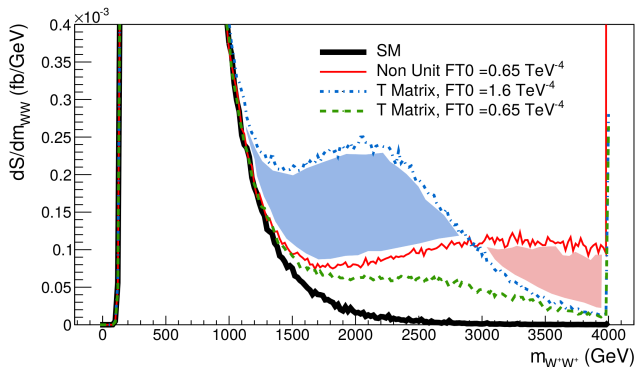
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# Unitarity problem: how bad is the problem?



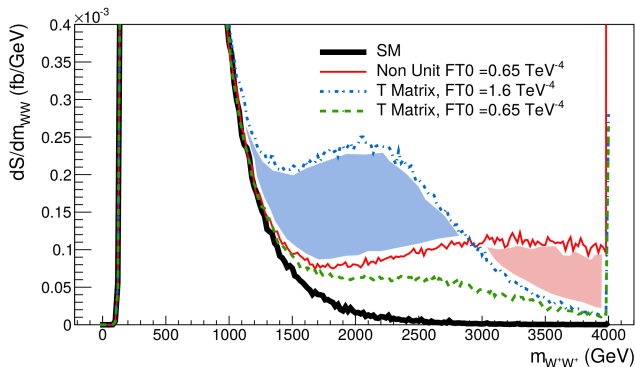
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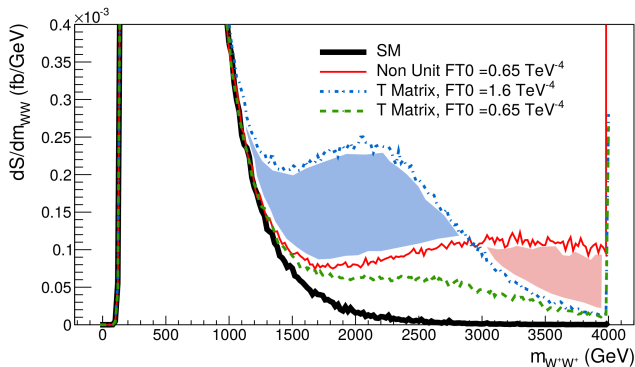
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- Zoo of unitarization procedures: IAM, K-matrix, T-matrix, N/D, large-N,...
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- Depend on analytical continuation (Cauchy's theorem).

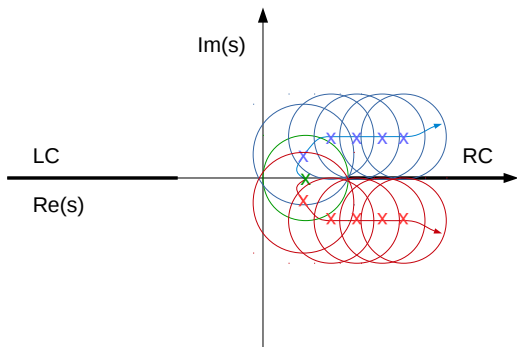
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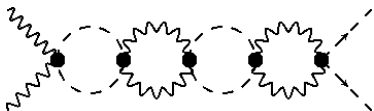
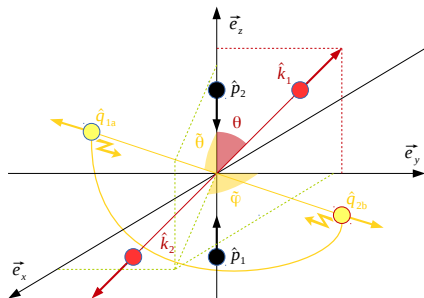
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The screenshot shows a search interface for 'resummation Higgs' on the HEP database. The search results are sorted by 'relevance' and show 431 records. The first five results are listed below:

- 1. BSMPT - Beyond the Standard Model Phase Transitions - A Tool for the Electroweak Phase Transition in Extended Higgs Sectors**  
Philipp Baskler, Margarete Muhlethaler. Mar 7, 2018.  
e-Print: [arXiv:1802.02846 \[hep-ph\]](#) | PDF  
References | BibTeX | LaTeXJUS | LaTeXEUJ | HarvMast | EndNote  
ADS Abstract Service  
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- 2. Double resummation for Higgs production**  
Marco Bonini (INFN, Rome), Simone Marzani (Genoa U. & INFN, Genoa). Feb 21, 2018. 7 pp.  
e-Print: [arXiv:1802.07738 \[hep-ph\]](#) | PDF  
References | BibTeX | LaTeXJUS | LaTeXEUJ | HarvMast | EndNote  
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- 3. Soft Gluon Resummation in Higgs Boson Plus Two Jet Production at the LHC**  
Peng Sun (Nanjing Normal U. & Michigan State U.), C.P. Yuan (Michigan State U.), Feng Yuan (LBNL, MSD). Feb 8, 2018. 8 pp.  
e-Print: [arXiv:1802.02980 \[hep-ph\]](#) | PDF  
References | BibTeX | LaTeXJUS | LaTeXEUJ | HarvMast | EndNote  
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- 4. iHixs 2 - Inclusive Higgs Cross Sections**  
Falko Dulat (SLAC), Achilleas Loutchoukos (Zurich, ETH), Bernhard Mistlberger (CERN). Feb 2, 2018. 46 pp.  
e-Print: [arXiv:1802.06822 \[hep-ph\]](#) | PDF  
References | BibTeX | LaTeXJUS | LaTeXEUJ | HarvMast | EndNote  
CERN Document Server | ADS Abstract Service  
[Registro completo](#)
- 5. Higher order corrections to mixed QCD-EW contributions to Higgs production in gluon fusion**  
Marco Bonini, Kiril Melebrinov (KIT, Karlsruhe), Lorenzo Tancredi (CERN). Jan 31, 2018. 4 pp.  
CERN-TH.2018-011, TT1918-004  
e-Print: [arXiv:1801.10553 \[hep-ph\]](#) | PDF  
References | BibTeX | LaTeXJUS | LaTeXEUJ | HarvMast | EndNote  
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[Registro completo](#) - Creado por 1 registro
- 6. NNLL resummation for the associated production of a top pair with a heavy boson at the LHC**  
Alessandro Bionardi, Alessandro Tesse, S.S. Lee '91. '0018. 8 pp.

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Typical Feynman diagram mixing the  $\omega w$  and the  $hh$  channels.  
[PRL114, 221803]

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- Basically, a form-factor to avoid breaking unitarity bound. Not based on analytical continuation.
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- We have theoretical background on comparing different unitarization procedures, and on their motivation: [Phys.Rev.Lett.**114**, 221803], [PRD**91**, 075017], [JHEP**140**, 149],...
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# Our approach: EFTs + Unitarization Procedures

- We are interested in the collider phenomenology of Vector Bosons Scattering ( $WZ \rightarrow WZ$ ), since it is very sensitive to new physics in the EW sector in the LHC.
- Bottom to Top approach: we construct an EFT for the EW sector.  $SU(2)_L \times SU(2)_R$ , EChL copy of ChPT in QCD.
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- 4 considered parameters:  $a$ ,  $b = a^2$ ,  $a_4$ ,  $a_5$ .
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## Effective Lagrangian: considered parameters

$$\mathcal{L}_2 = \frac{v^2}{4} \left[ 1 + 2a \frac{h}{v} + b \left( \frac{h}{v} \right)^2 + \dots \right] \text{Tr}(D_\mu U^\dagger D_\mu U) + \frac{1}{2} \partial_\mu h \partial^\mu h + \dots$$

$$\mathcal{L}_4 = a_4 [\text{Tr}(V_\mu V_\nu)] [\text{Tr}(V^\mu V^\nu)] + a_5 [\text{Tr}(V_\mu V^\mu)] [\text{Tr}(V_\nu V^\nu)] + \dots$$

$$V_\mu = (D_\mu U) U^\dagger, \quad U = \exp\left(\frac{i\omega^a T^a}{v}\right)$$

Bosons  
physics in

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- Degrees of freedom: Gauge Bosons  $W^\pm$ ,  $Z$  + Higgs-like particle ( $h$ ).
- 4 considered parameters:  $a$ ,  $b = a^2$ ,  $a_4$ ,  $a_5$ .
- The NLO-computed EFT grows with the CM energy like  $A \sim s^2$ . Hence, it will eventually reach the unitarity bound, becoming non-perturbative. Options:
  - Limit the validity range of the EFT to the perturbative region. Consider it as a useful parameterization of slight deviations from the SM in the range under the TeV scale.
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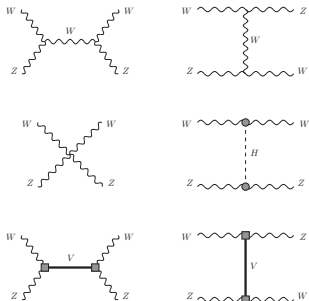


BP	$M_V(\text{GeV})$	$\Gamma_V(\text{GeV})$	$g_V(M_V^2)$	$a$	$a_4 \cdot 10^4$	$a_5 \cdot 10^4$
BP1	1476	14	0.033	1	3.5	-3
BP2	2039	21	0.018	1	1	-1
BP3	2472	27	0.013	1	0.5	-0.5
BP1'	1479	42	0.058	0.9	9.5	-6.5
BP2'	1980	97	0.042	0.9	5.5	-2.5
BP3'	2480	183	0.033	0.9	4	-1

These BPs have been selected for vector resonances emerging at mass and width values that are of phenomenological interest for the LHC.

Considered backgrounds: The pure SM-EW background, of order  $\mathcal{O}(\alpha_{\text{em}}^2)$ .  
The mixed SM-QCDEW background, of order  $\mathcal{O}(\alpha_{\text{em}}\alpha_s)$ .

# Channels: $W^+Z \rightarrow W^+Z$



- Our Proca Lagrangian needs  $g_V = g_V(z, s)$

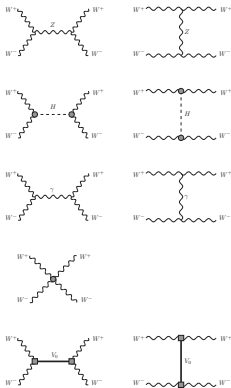
$$g_V^2(z) = g_V^2(M_V^2) \frac{M_V^2}{z} \text{ for } s < M_V^2$$

$$g_V^2(z) = g_V^2(M_V^2) \frac{M_V^4}{z^2} \text{ for } s > M_V^2,$$

$z = s, t, u$  depending on the channel where  $V$  propagates. Fully crossing symmetry leads to a moderate violation of the Froissart bound.

- The parameters of the Proca Lagrangian are adjusted to the IAM results [dynamic  $M_V$ ,  $\Gamma_V$ ,  $g_V(M_V^2)$ ] via a custom piece of software.
- Currently,  $W^+Z \rightarrow W^+Z$  tested.
- Leptonic channel studied:  $pp \rightarrow w^+w^-jj$ ,  $w^\pm \rightarrow l^\pm\nu$

# Channels: $W^+ W^- \rightarrow W^+ W^-$

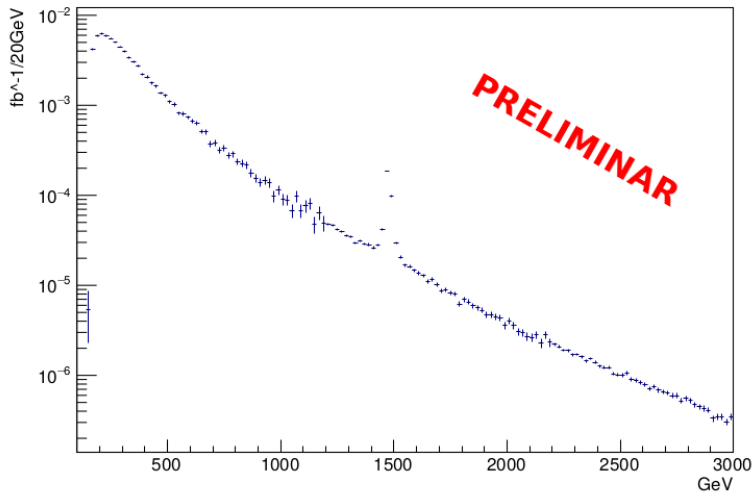


- We are extending our UFO for including  $W^+ W^- \rightarrow W^+ W^-$ .
- We expect to be able to deal with  $WZ \rightarrow WZ$ ,  $WW \rightarrow ZZ$ ,  $ZZ \rightarrow WW$ ,  $W^+ W^- \rightarrow W^+ W^-$ ,  $W^\pm W^\pm \rightarrow W^\pm W^\pm$ .
- On the longer term, we consider completing the EW model for including  $ZZ \rightarrow ZZ$ .
- The UFO model, actually, works.
- We have been granted 150kh of computer time of C2PAP for testing the new UFO.

Excellence Cluster Universe



# M(WZ), MODELS/ww\_IAM-a1 BP1



# Conclusions

- We are developing a UFO model for MadGraph v5.
- We describe the Vector Boson Scattering processes by means of the Electroweak Chiral Lagrangian and the Inverse Amplitude Method.
- We expect to describe the following processes:

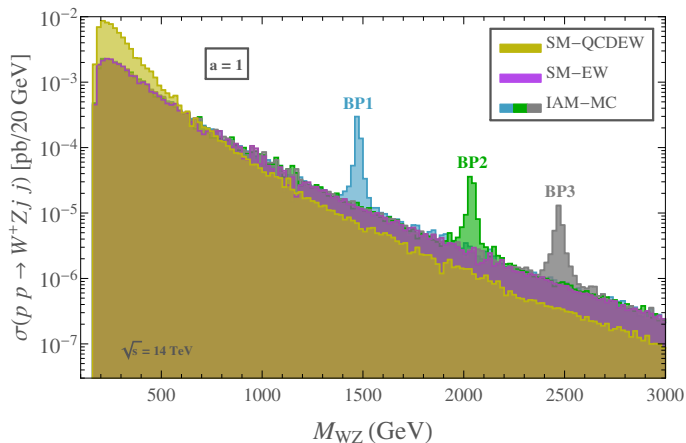
OLD UFO		ON PROGRESS		
$W^\pm Z$	$\rightarrow$	$W^\pm Z$		
$W^\pm W^\mp$	$\rightarrow$	$ZZ$		
$ZZ$	$\rightarrow$	$W^\pm W^\mp$		
		$W^\pm W^\mp$	$\rightarrow$	$W^\pm W^\mp$
		$W^\pm W^\pm$	$\rightarrow$	$W^\pm W^\pm$

- Making a decision about our goal for  $pp \rightarrow w^+ w^- jj \rightarrow w^+ w^- jj$  channel. Suggestions...?
- Several improvements for enhanced usability, so that all parameters of the Proca can be set by standard MadGraph v5 config files.
- LET'S WAIT FOR IT!!

# BACKUP SLIDES

# Isvector Resonance: $WZ$ in final state

JHEP1711, 098

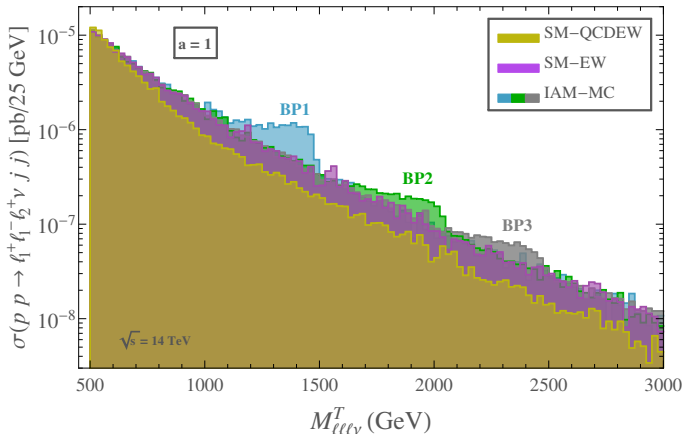


$a = 1$ ;  $a_4 \cdot 10^4 = 3.5$  (BP1), 1 (BP2), 0.5 (BP3);

$-a_5 \cdot 10^4 = 3$  (BP1), 1 (BP2), 0.5 (BP3).

# Isvector Resonance: leptonic final state

JHEP1711, 098



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# Unitarization procedures for elastic processes

$$A^{IAM}(s) = \frac{[A^{(0)}(s)]^2}{A^{(0)}(s) - A^{(1)}(s)},$$

$$A^{N/D}(s) = \frac{A^{(0)}(s) + A_L(s)}{1 - \frac{A_R(s)}{A^{(0)}(s)} + \frac{1}{2}g(s)A_L(-s)},$$

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$$A_0^K(s) = \frac{A_0(s)}{1 - iA_0(s)},$$

$$g(s) = \frac{1}{\pi} \left( \frac{B(\mu)}{D + E} + \log \frac{-s}{\mu^2} \right)$$

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PRD **91** (2015) 075017

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# Usability channel of unitarization procedures

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Method of choice	Any	N/D IK	IAM	Any	N/D IK

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