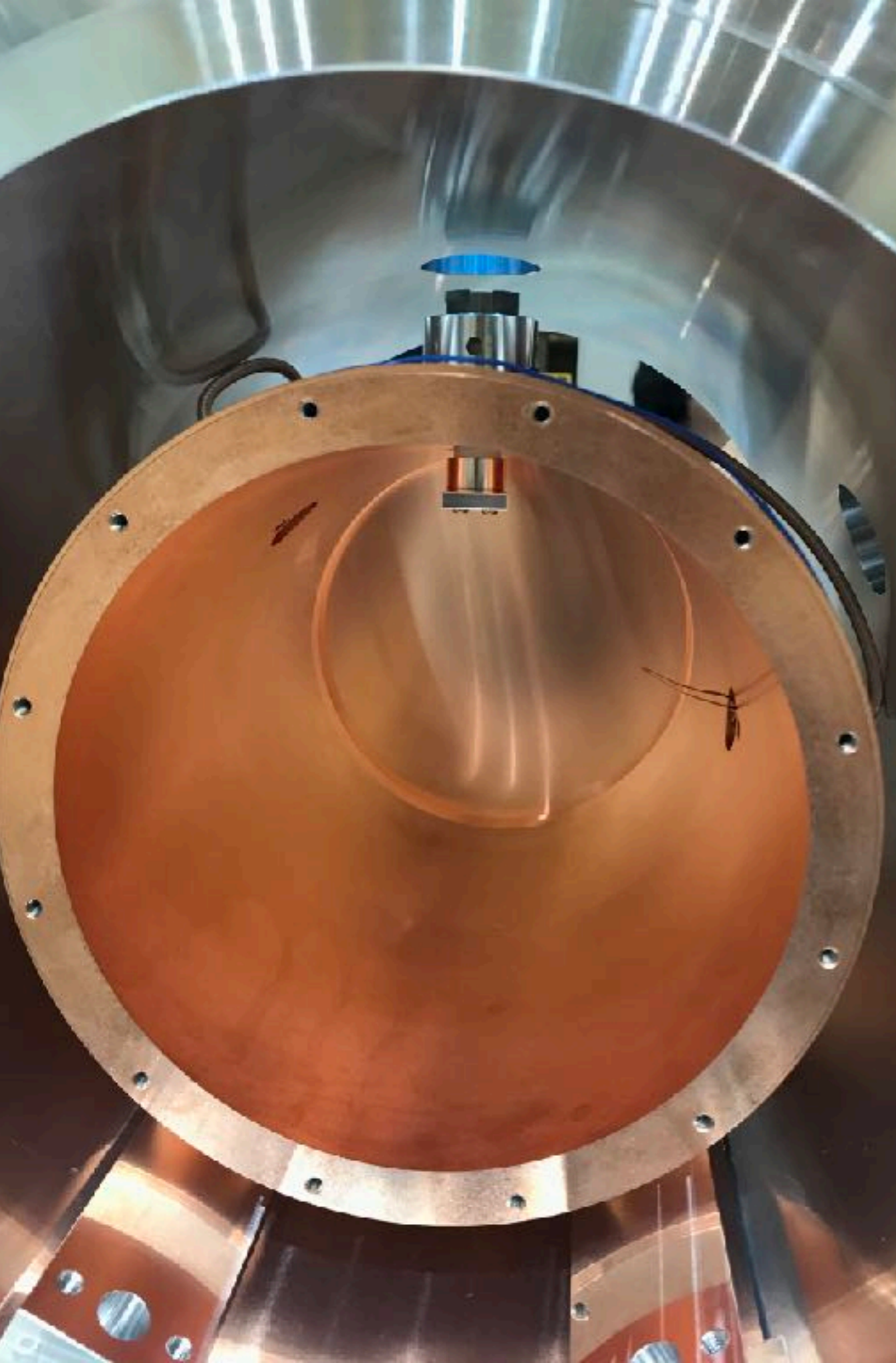


Spectroscopy of Muonium Hyperfine Structure at J-PARC

Yasuhiro UENO, from RIKEN, for MuSEUM collaboration





Agenda

➤ **Introduction**

- Motivation
- Procedure
- Apparatus

➤ **Recent Measurements at low B field**

- Result with lower gas pressure

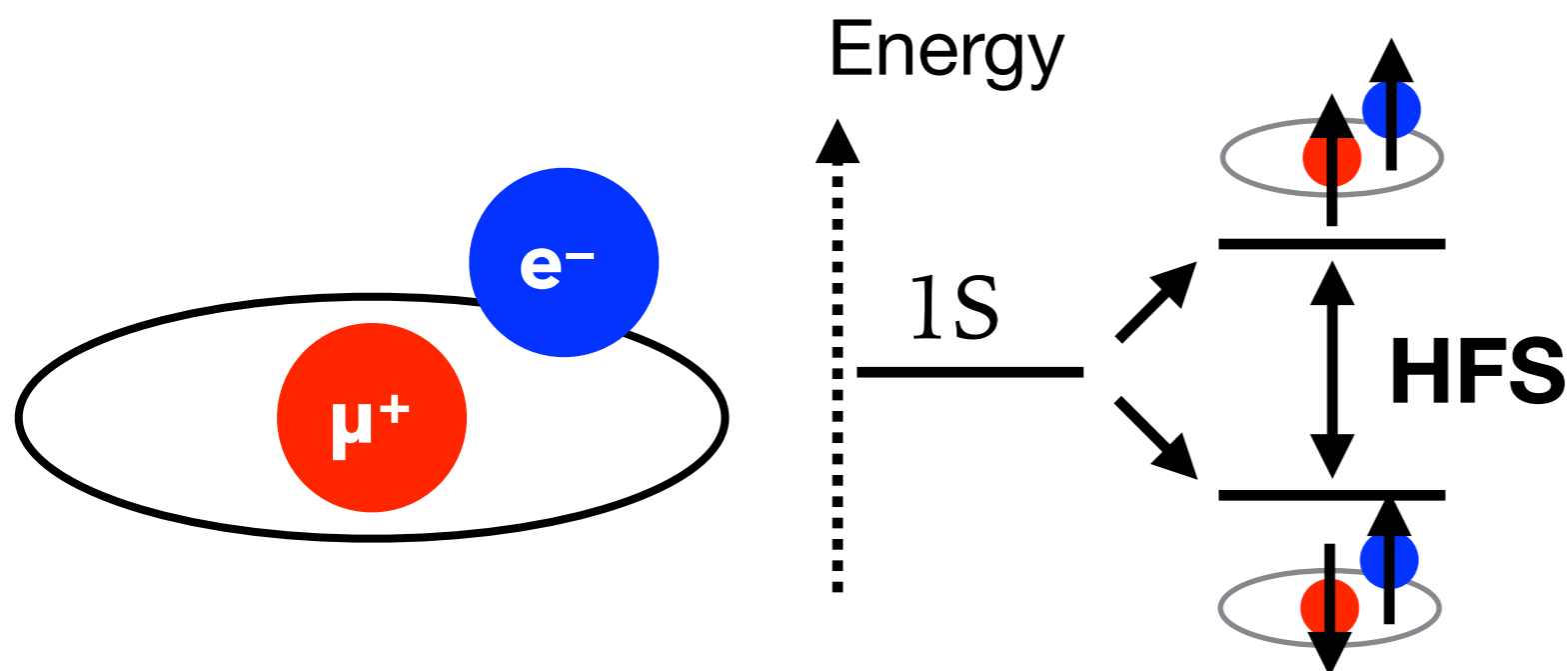
➤ **R&D for future**

- Mixture gas
- magnet for high field measurement
- Time differential method

Experiment: MuSEUM

3

- **Muonium Spectroscopy Experiment Using Microwave**
- Muonium: μ^+e^- , no nuclear structure, calculation with high precision
- Two major motivations
 - **Test of the bound-state QED**
 - **Most precise determination of the muon magnetic moment** (synergy with the muon $g-2$ experiment)

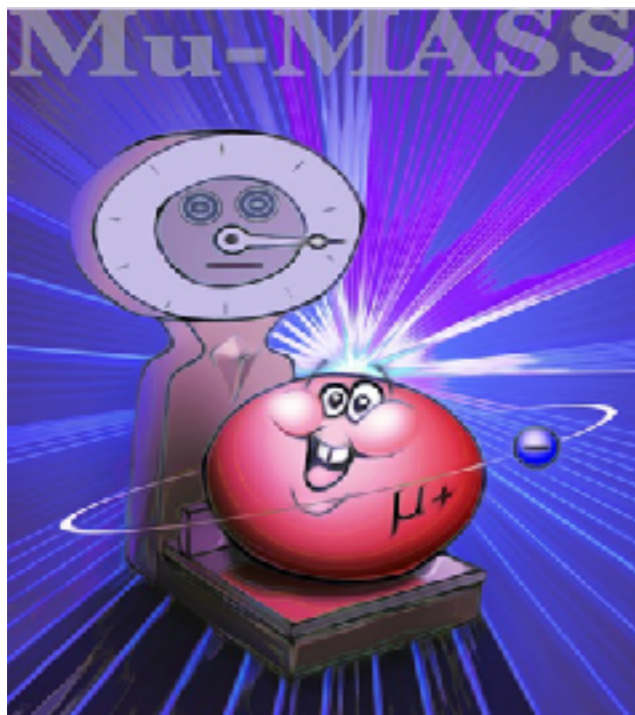


HFS	H	Mu
relative uncertainty of theory	560 ppb	115 ppb

Test of the Bound-State QED

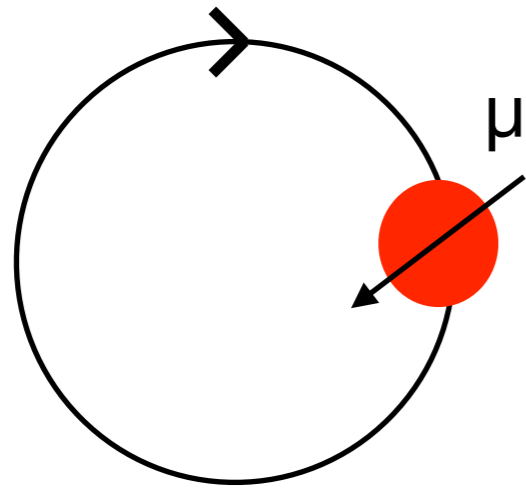
4

- $\nu_{\text{exp}} = 4\,463\,302\,765\,(53)\text{ Hz}$ Experiment at LAMPF (1999)
- $\nu_{\text{th}} = 4\,463\,302\,891\,(511)(70)(2)\text{ Hz}$ (m_{μ}/m_e)(QED)(α) By Eides
- Effort in QED calculation for $<10\text{ Hz}$ precision is in progress by Eides et al.
- Combined with independent muon mass determination
→ test of the bound-state QED



- **Muonium Laser Spectroscopy** planned at PSI (Paul Scherrer Institute)
- Improve Muonium 1s-2s by a factor of 1000
- Determine the muon mass with 1 ppb (more than a factor of 100 improvement)

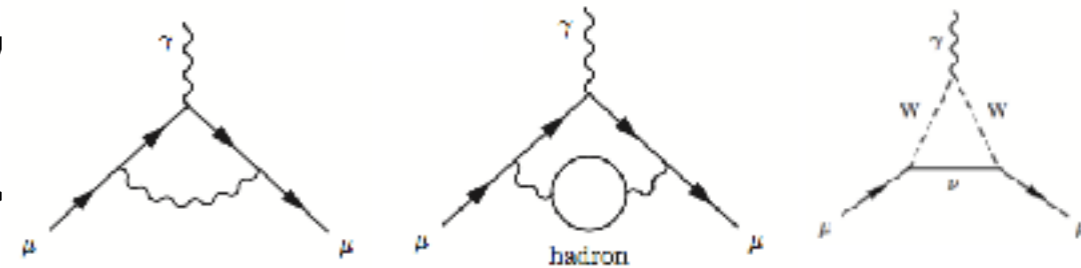
Muon Magnetic Moment and Muon $g-2$ 5



3.7 σ discrepancy



A. Keshavarzi, *et al.*, Phys. Rev. D. (2018)



SM Theory including QED,

Weak, Hadronic contributions

Talk by D. Nomura

Muon Ring **Experiment** at BNL

GW Bennett *et al.*, PRD 73 072003 (2006)

$$a_\mu = \frac{R}{\frac{\mu_\mu}{\mu_p} - R}$$

a_μ : muon $g-2$

(anomalous magnetic moment)

R determined
by muon ring Experiment:

Current: 540 ppb

Future: <140 ppb

new experiments by
Fermilab and J-PARC

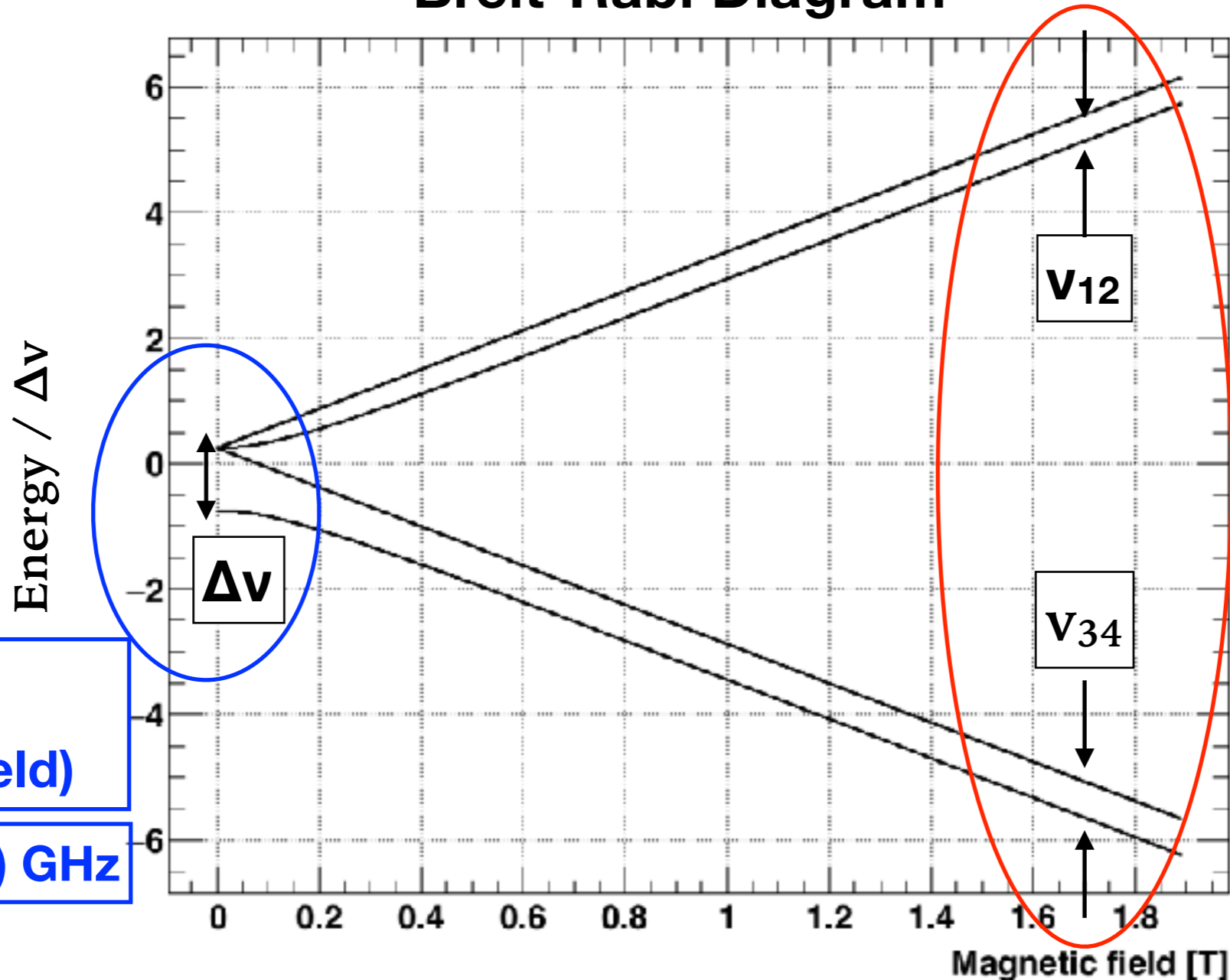
26 ppb (QED assumed) or
120 ppb (direct determination)
MuSEUM aim: 10 ppb (direct)

Talks by S. Corrodi,
and S. Lee

MuSEUM: Zeeman Splitting

6

Breit-Rabi Diagram



“Zero” Field
(very low B field)
4.463 3022 (14) GHz

High Field
(at 1.7 T)
 $V_{12} + V_{34} = \Delta v$
 $V_{12} - V_{34} \propto \mu_{\mu} / \mu_p$
4.463 302 765 (53) GHz

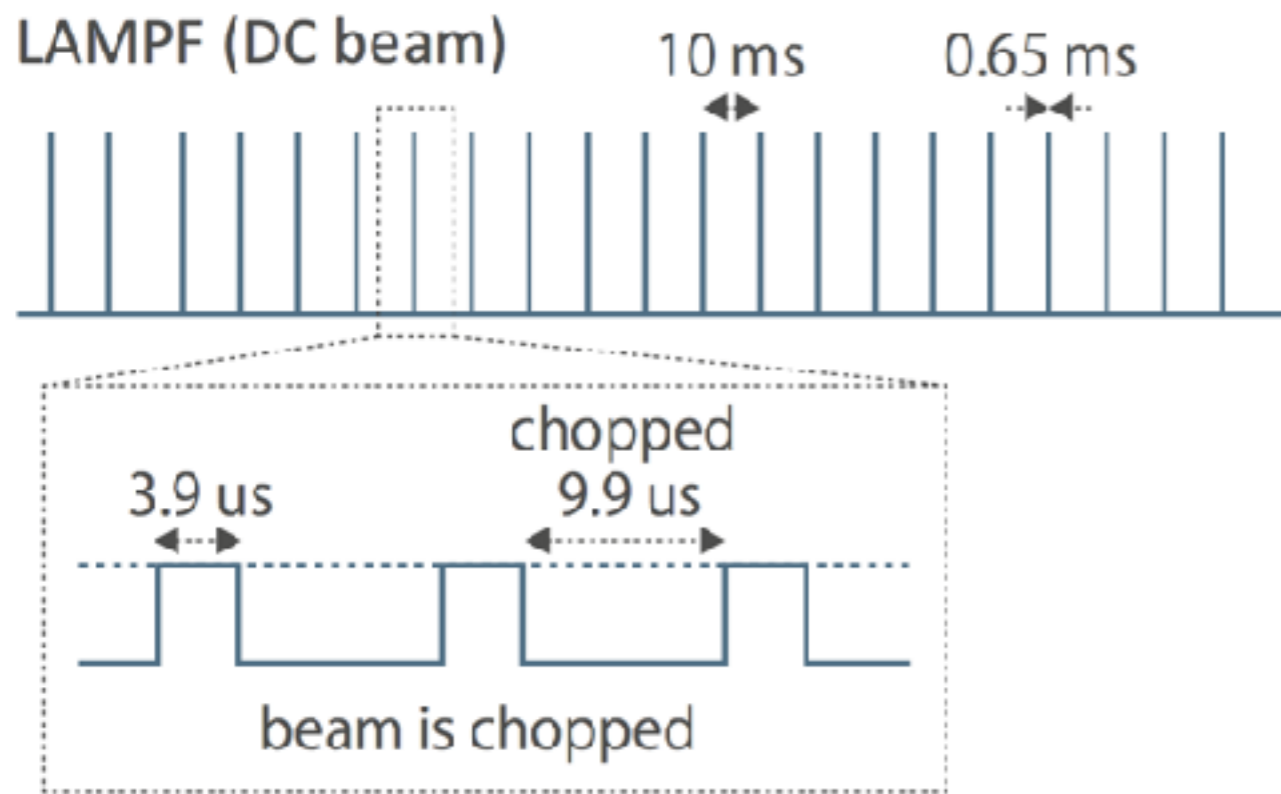
Both world records at **Los Alamos Meson Physics Facility (LAMPF)**

Their precision are **statistically limited, we need more muons!**

Intense Pulsed Muon Beam: J-PARC MLF 7

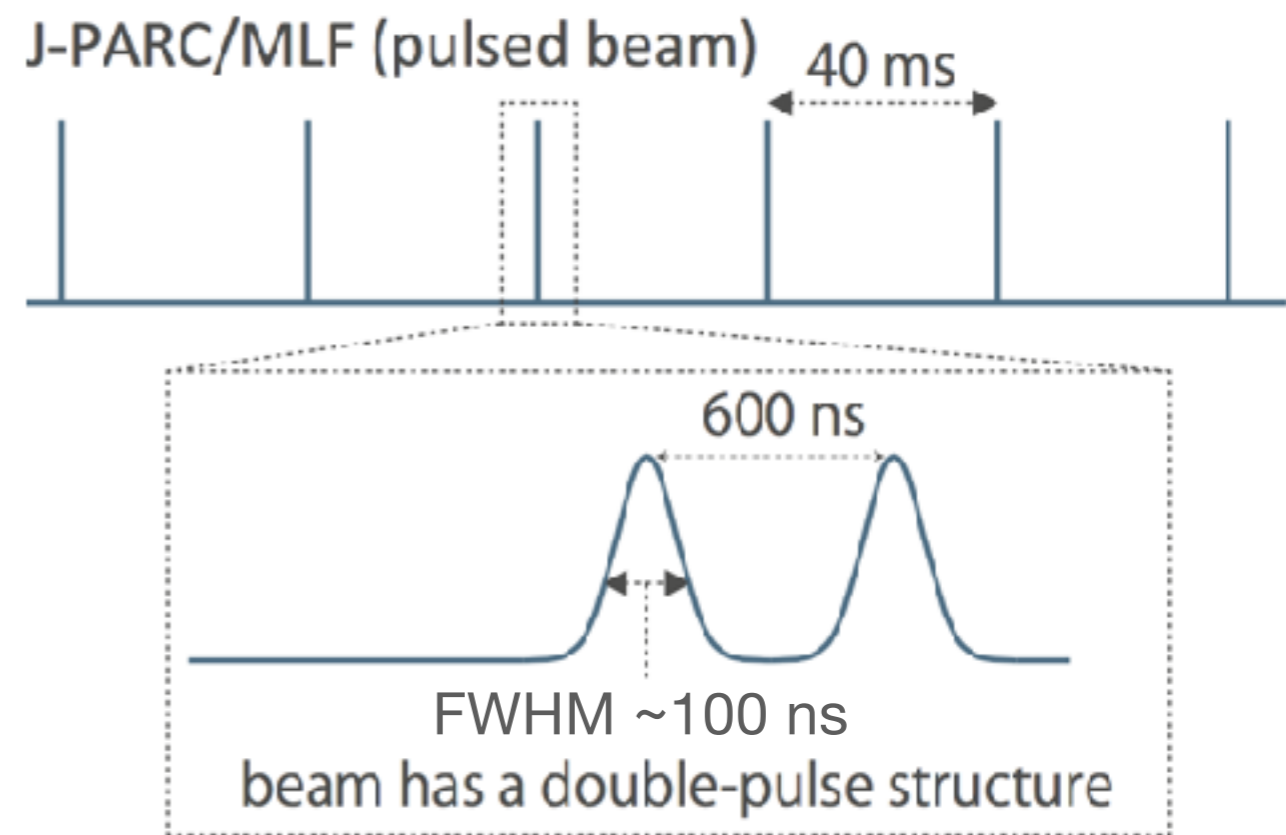
- The precision of the precursor experiments were limited by statistics
- We use the most intense pulsed muon beam at J-PARC MLF

Precursor Measurement at LAMPF



after chop: $2 \times 10^6 \mu^+/\text{sec}$

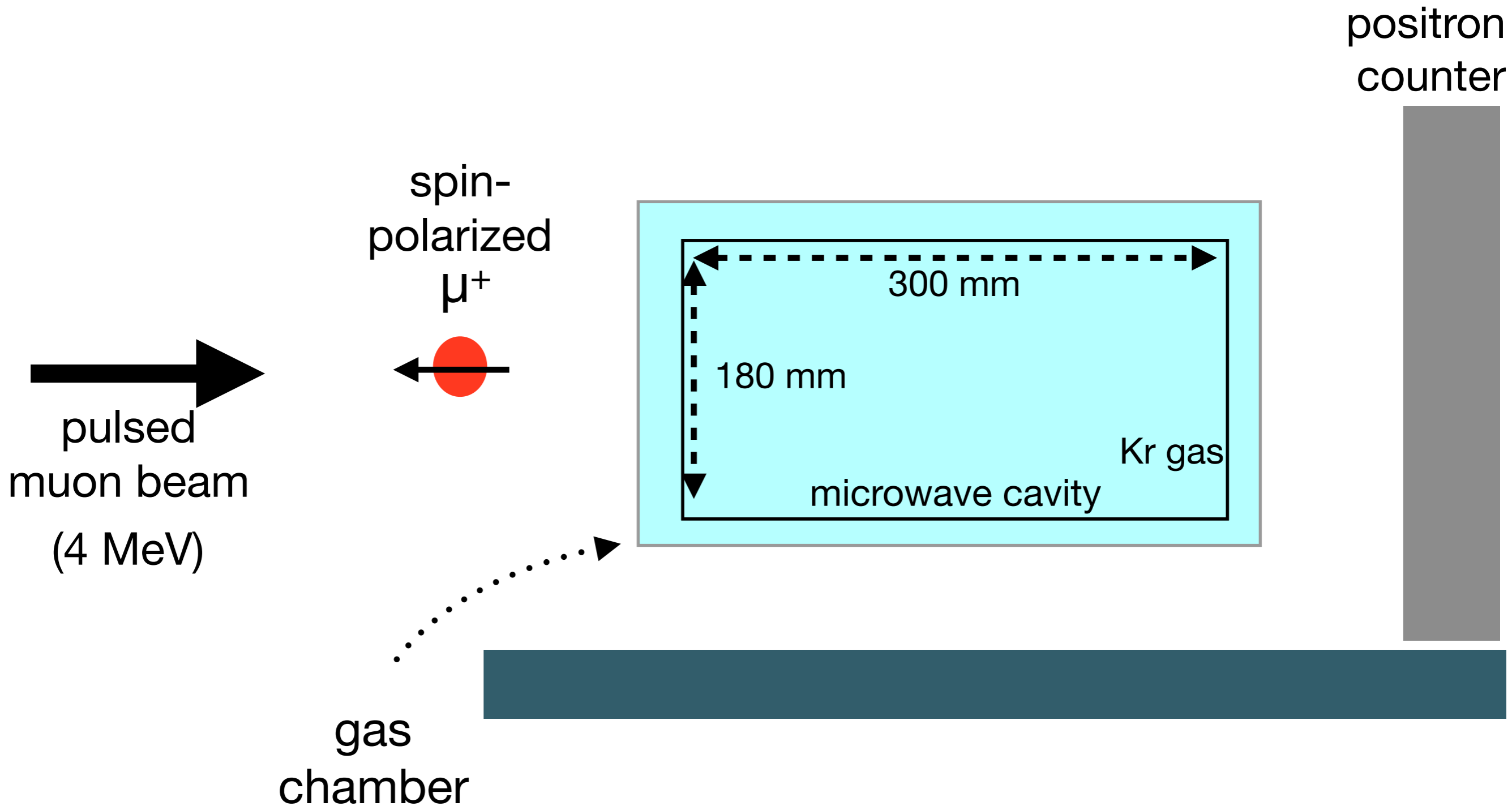
Our Measurement at J-PARC MLF



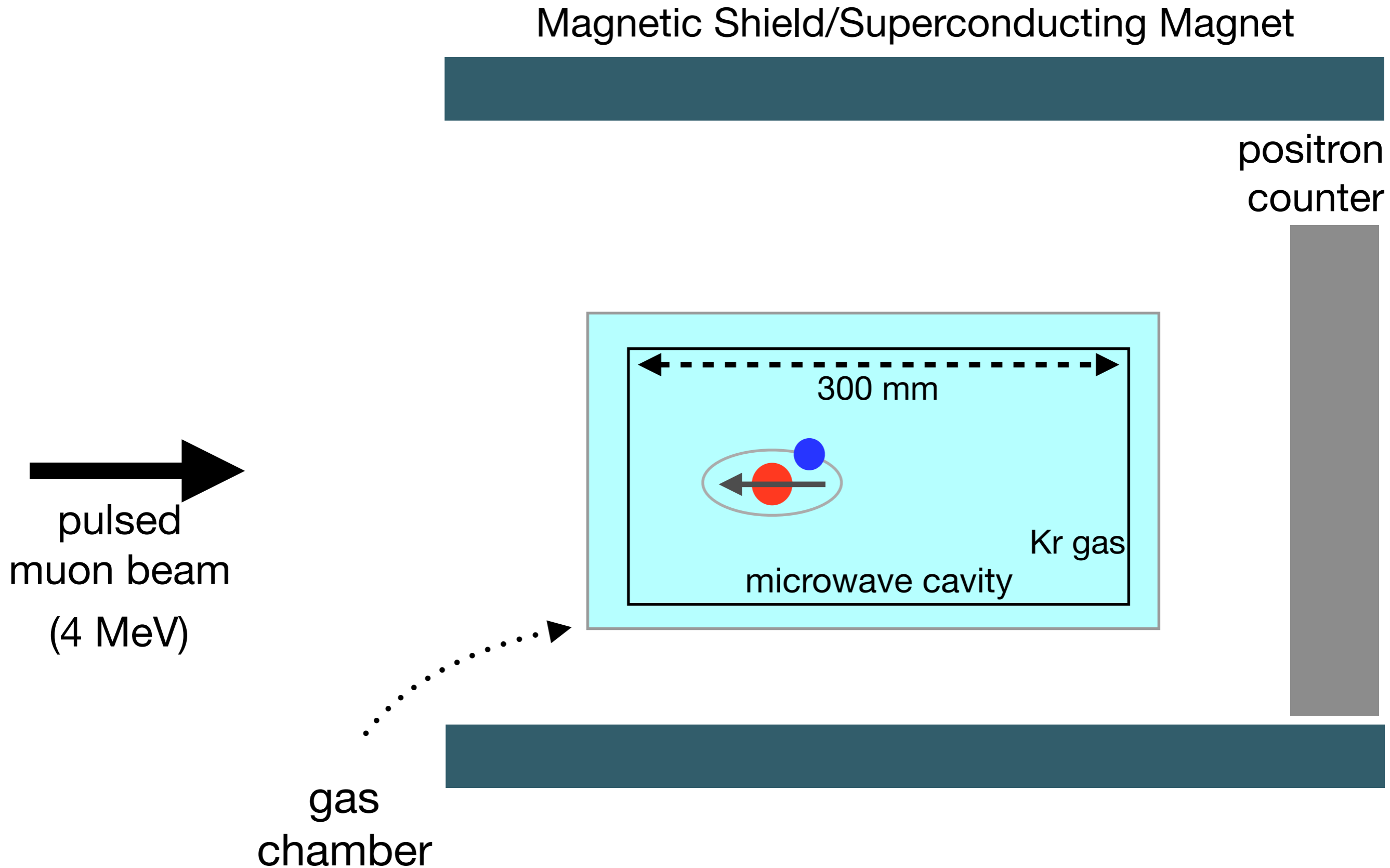
$> 10^8 \mu^+/\text{sec}$ (H-Line 1 MW)

Procedure of Measurement

Magnetic Shield/Superconducting Magnet



Procedure of Measurement




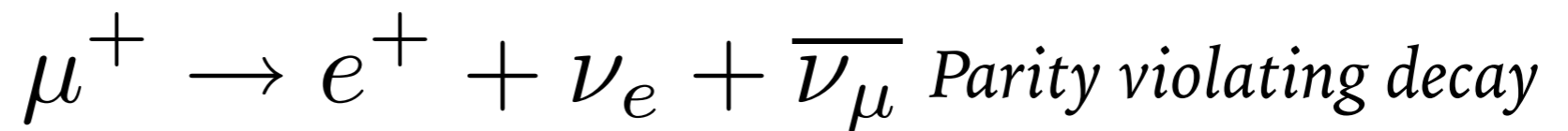
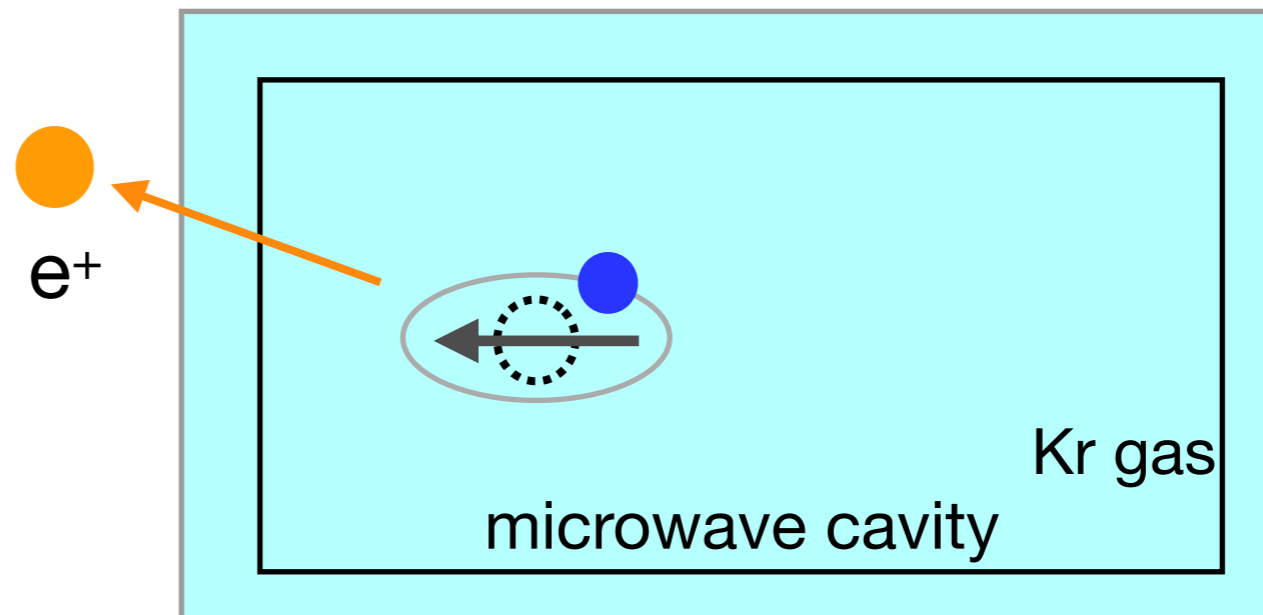
Procedure of Measurement

Magnetic Shield/Superconducting Magnet

positron
counter

Microwave OFF resonance


pulsed
muon beam
(4 MeV)



Procedure of Measurement

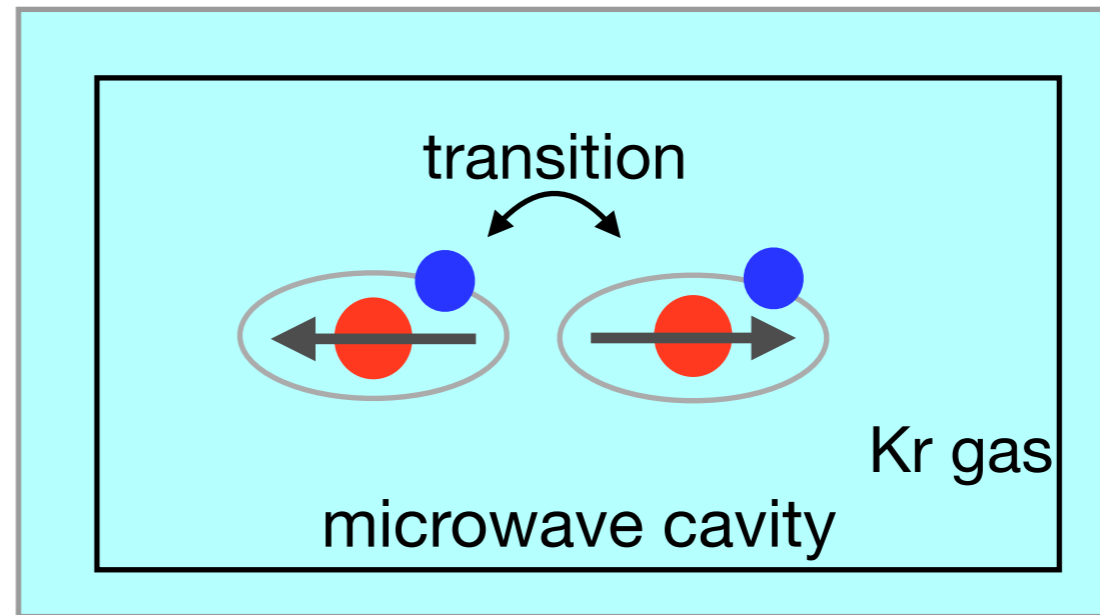
Magnetic Shield/Superconducting Magnet




positron
counter



Microwave ON resonance

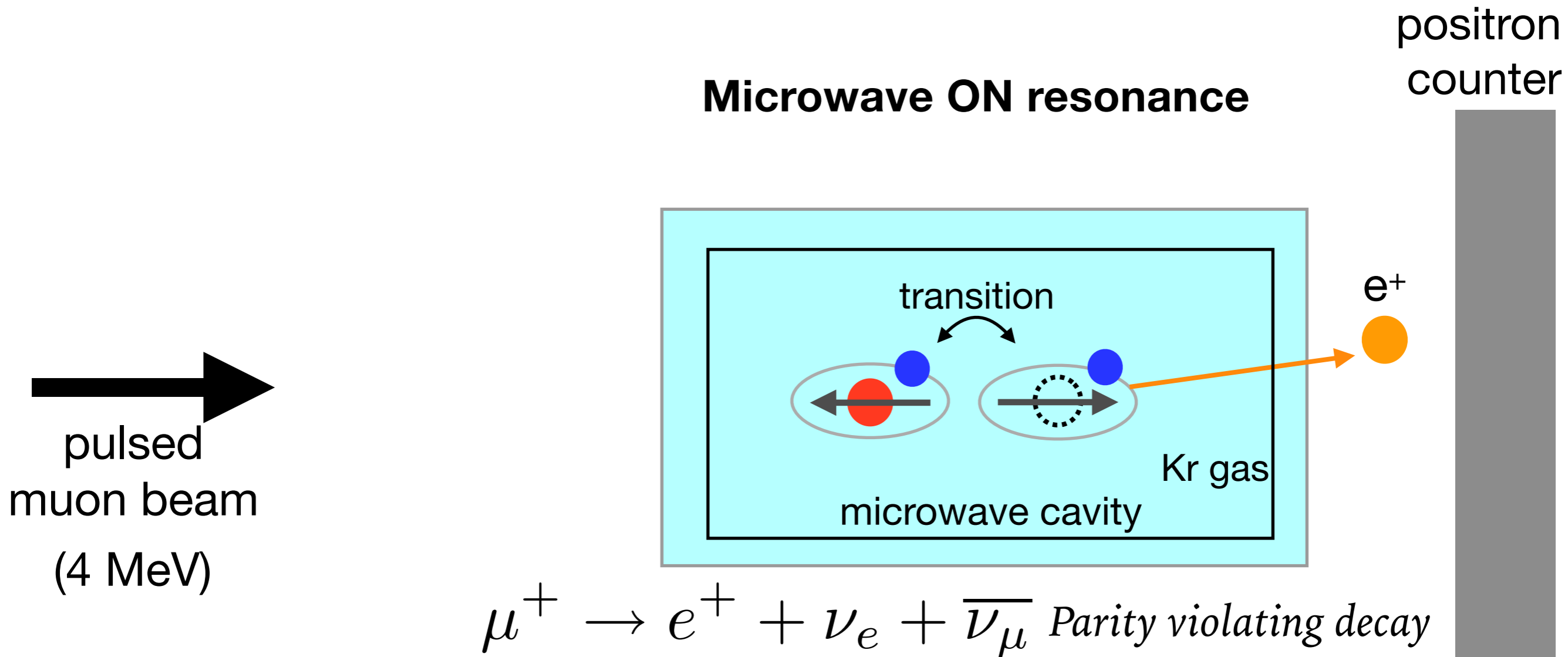



pulsed
muon beam
(4 MeV)



Procedure of Measurement

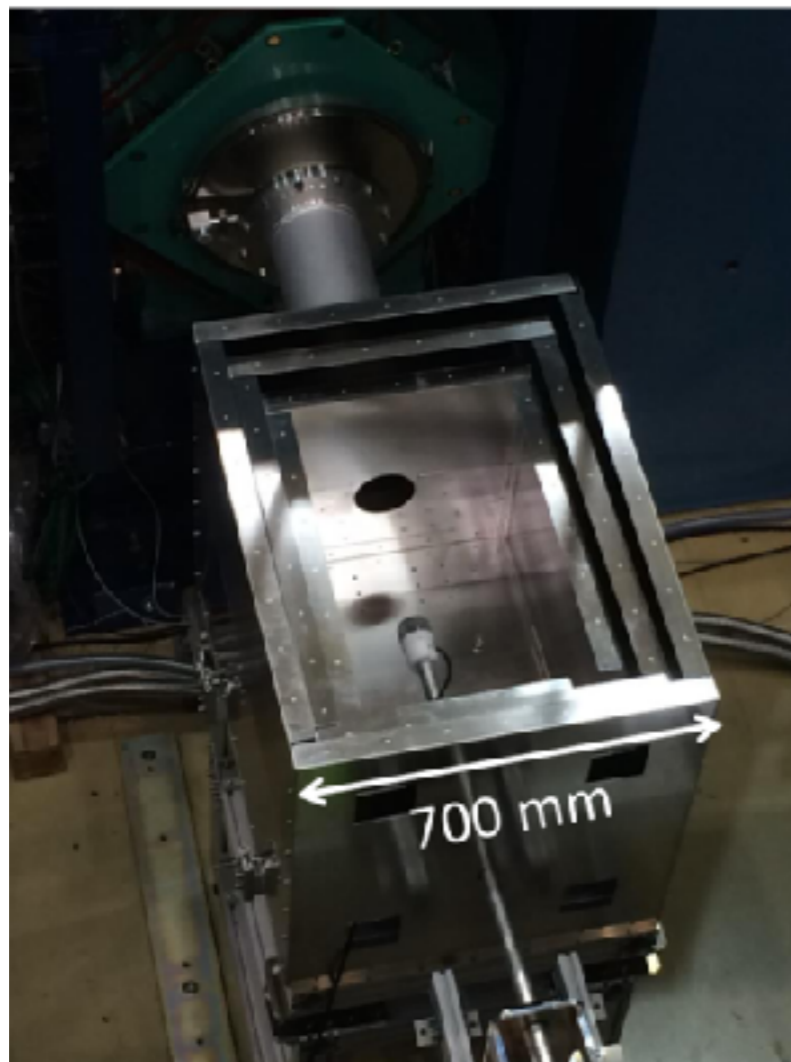
Magnetic Shield/Superconducting Magnet



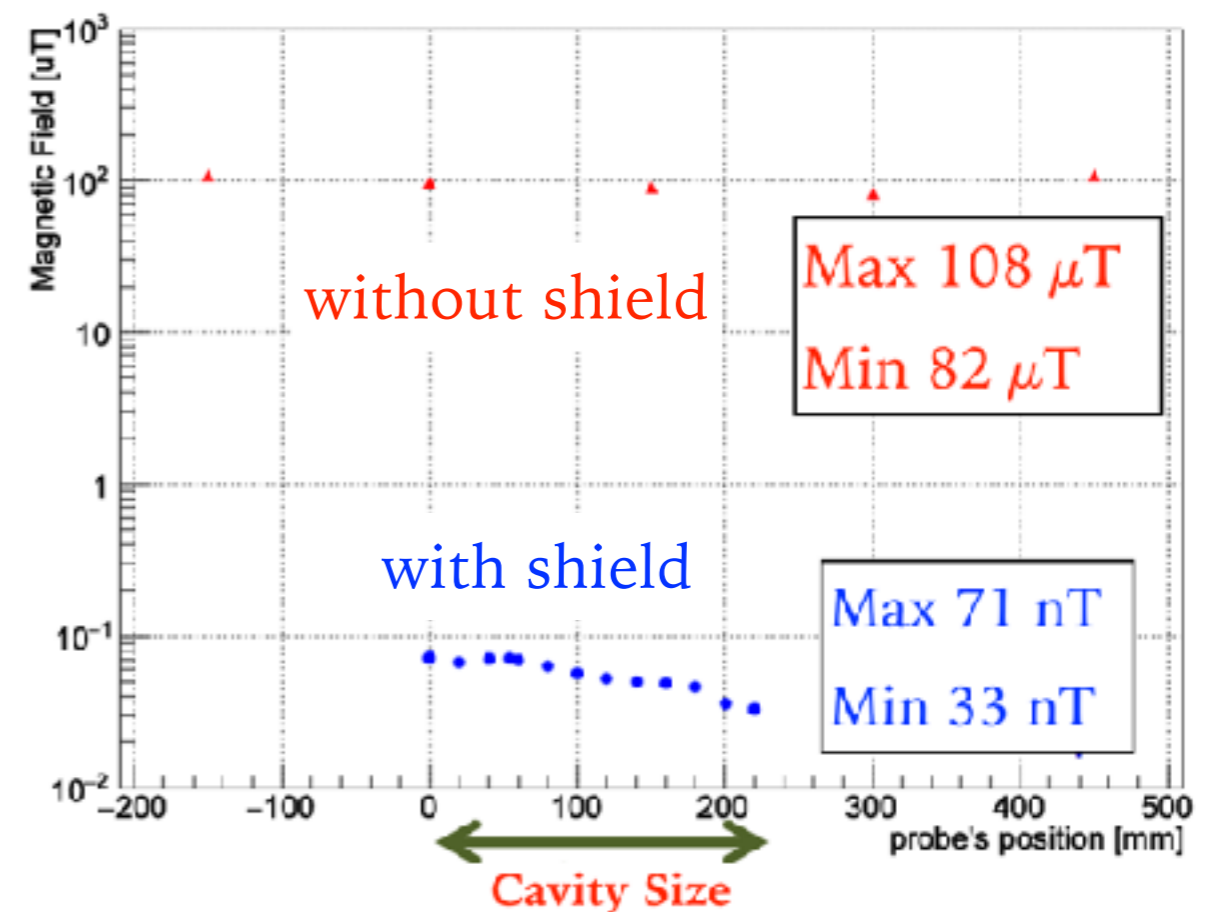
Shield for Magnetic Field

13

- Geomagnetic field and stray field from the beam line magnets
- **Three-layer permalloy shields** suppress the magnetic field (1/1000 suppression)
- Field measurement by flux-gate probe

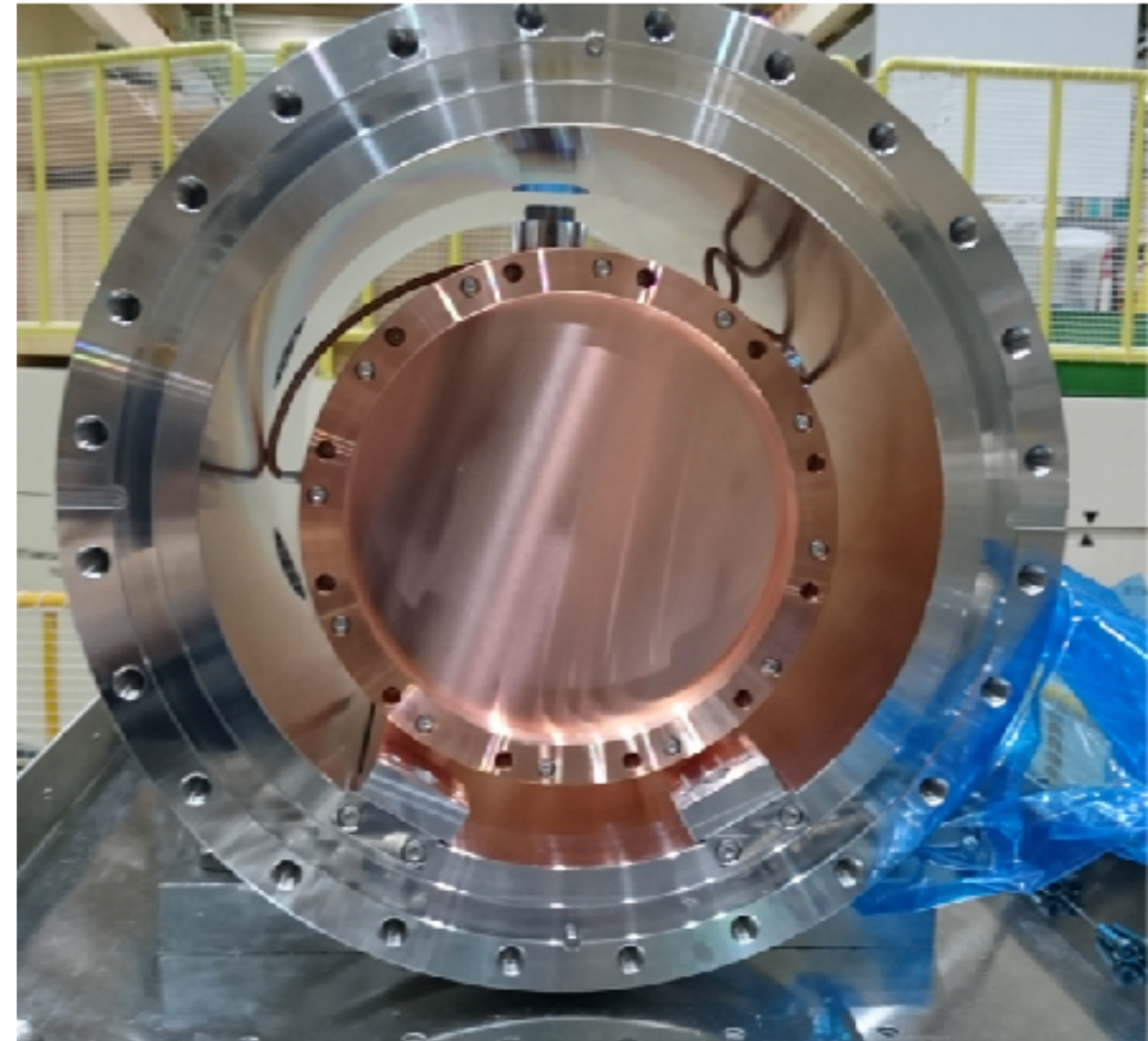
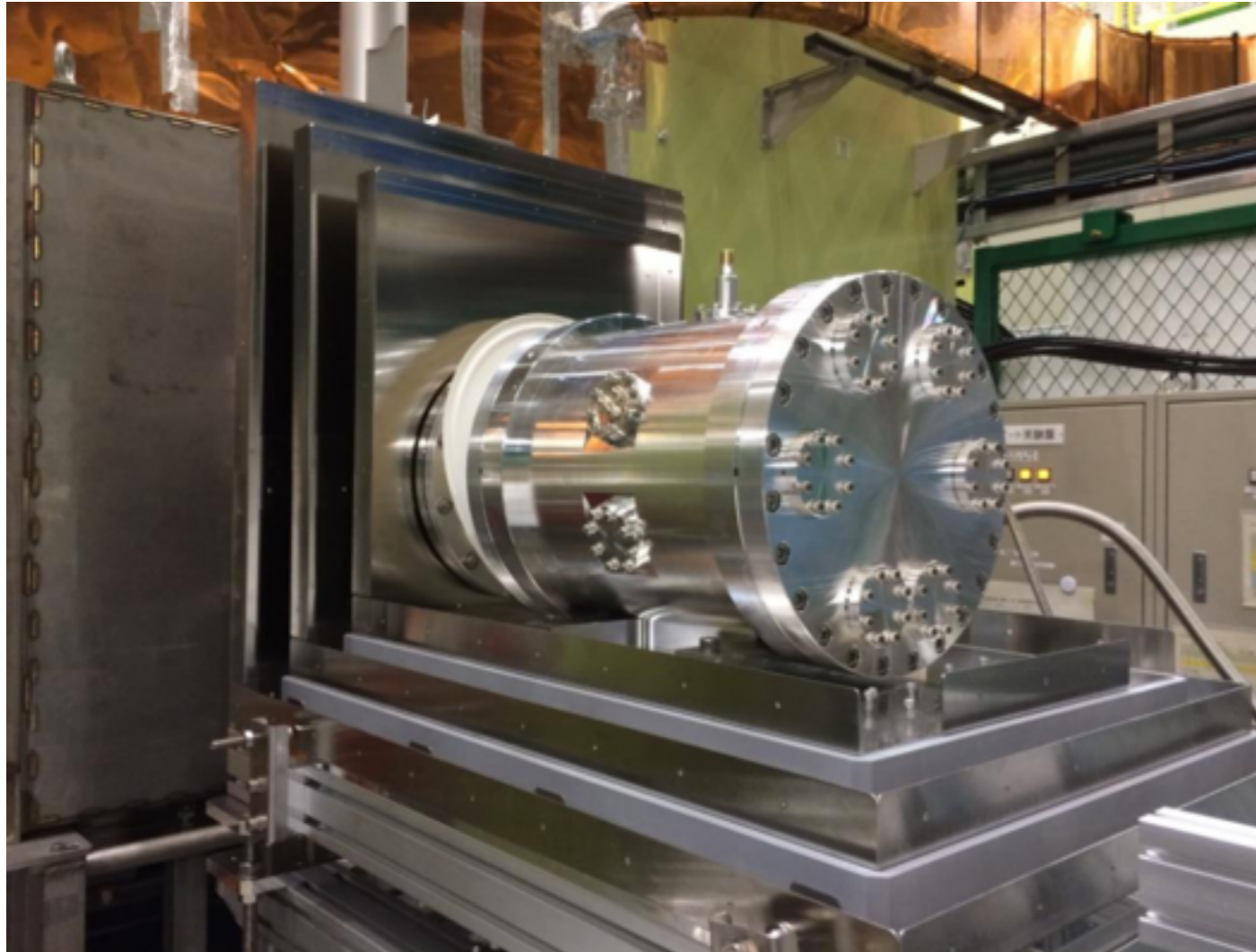


Comparison of field with and without the shield



Gas Chamber and Microwave Cavity

14

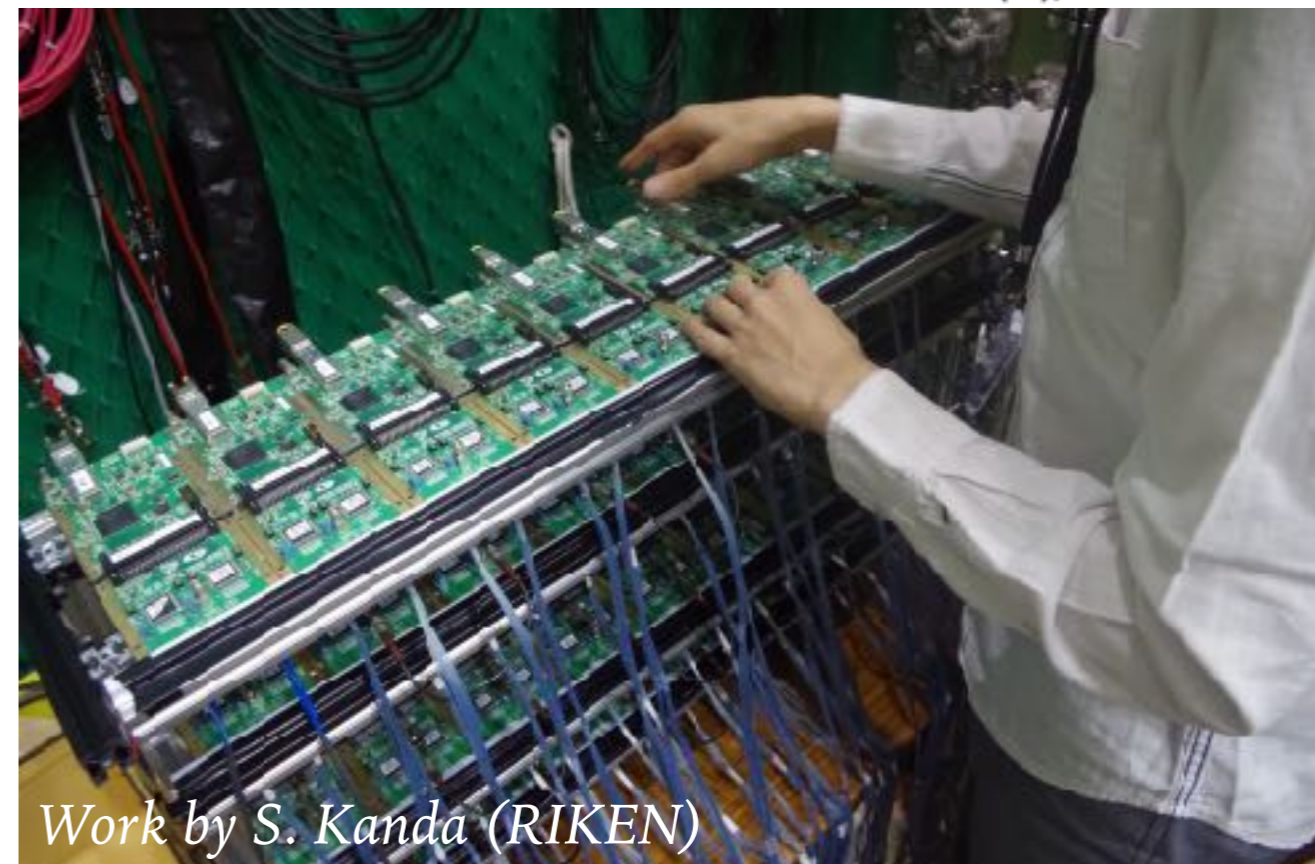
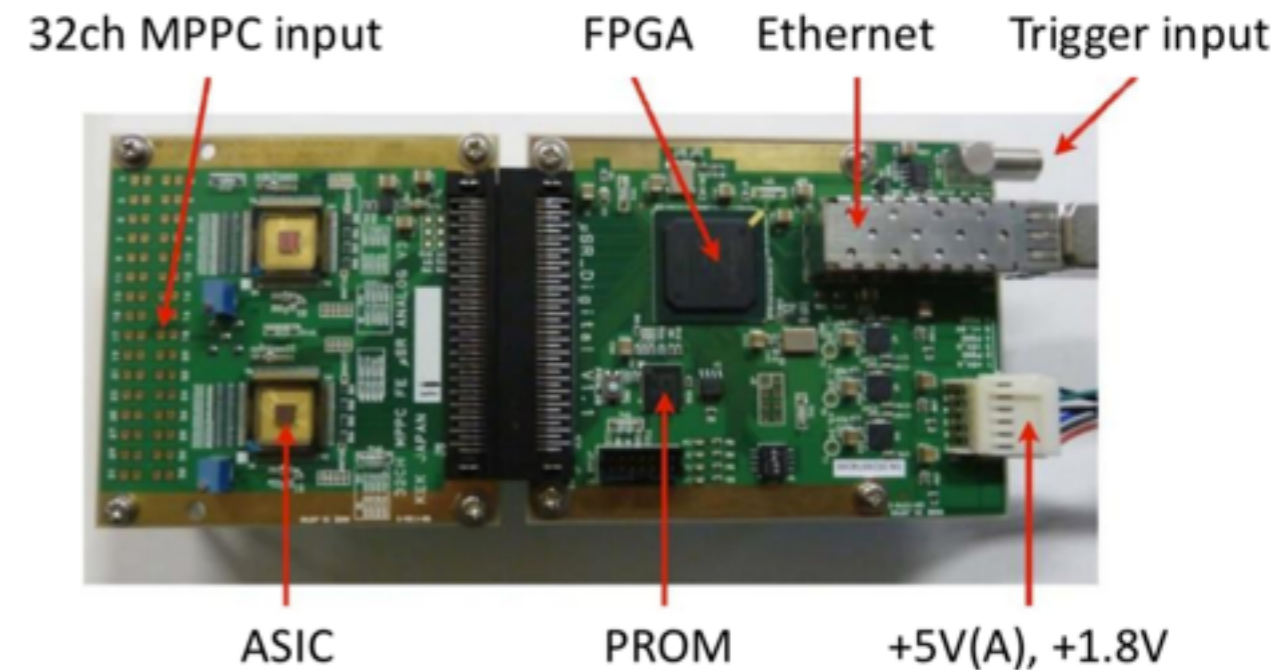
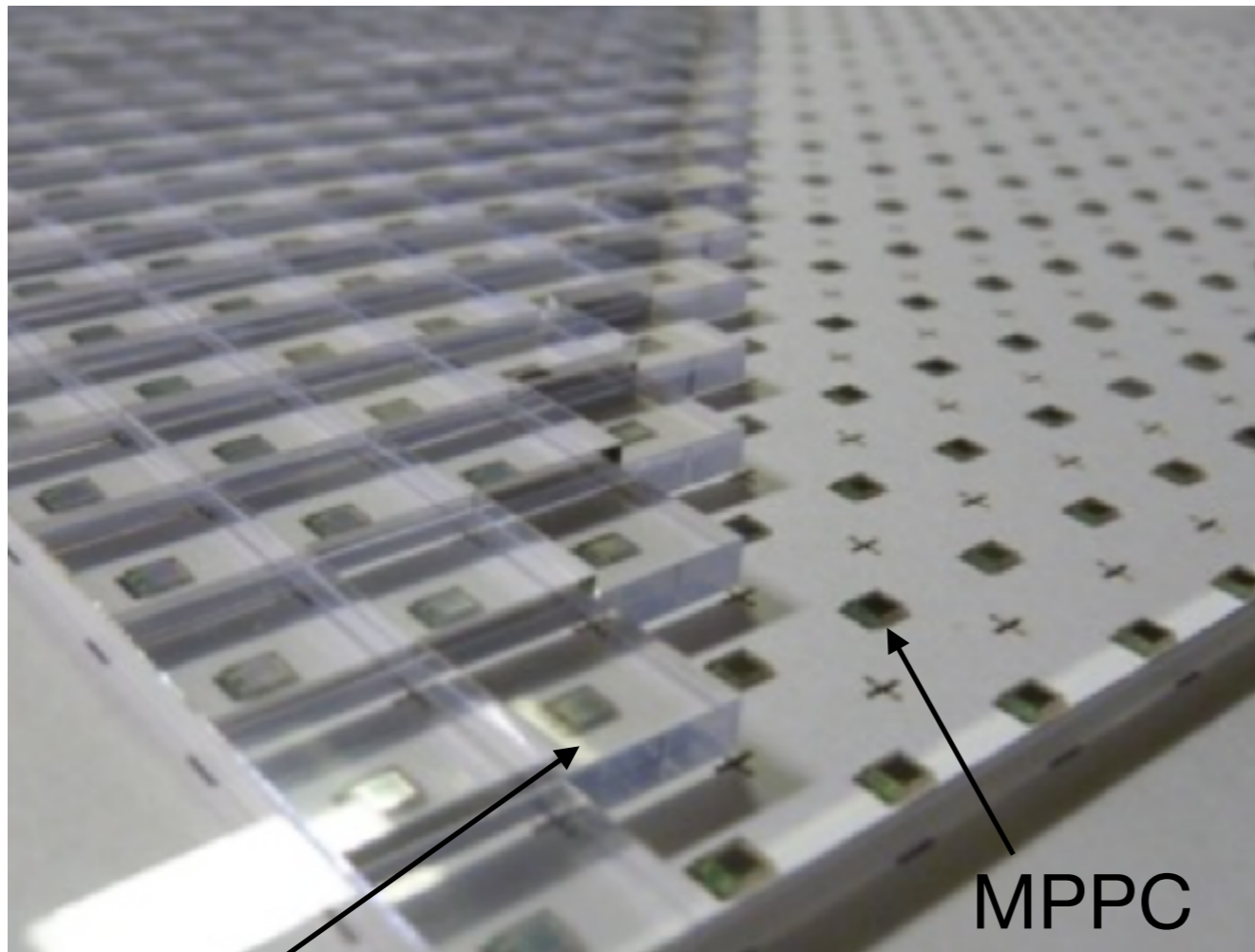


- Gas pressure monitored by a capacitance gauge
Impurity measured by Q-MASS spectrometer
- Cavity Q factor ~ 10000 , Input power ~ 1 W
Cavity resonance frequency is tunable: 4463 ± 1 MHz

Positron Detector

15

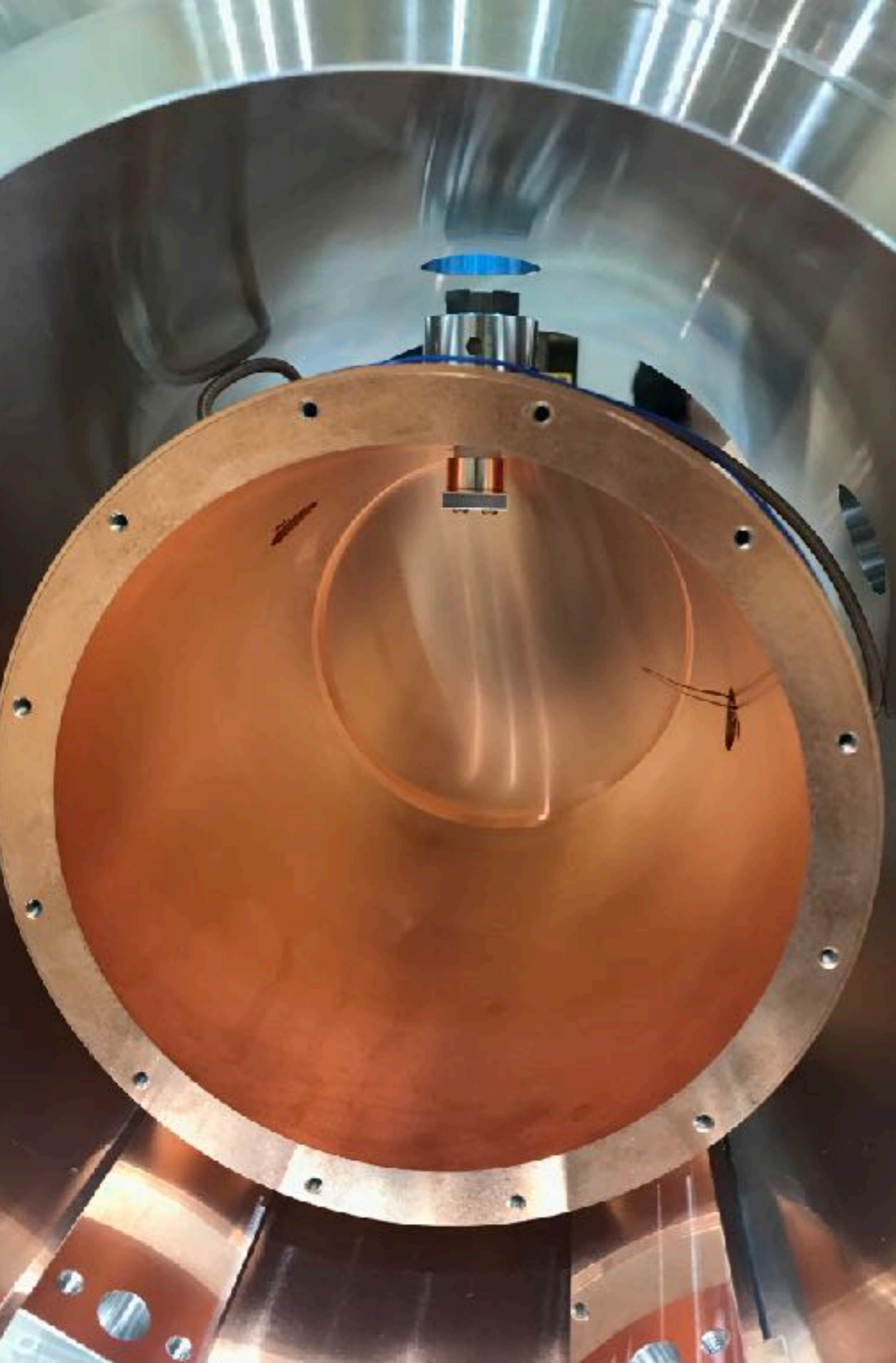
Plastic Scintillator + MPPC(SiPM) + Kalliope read out board



Plastic Scintillator

- Unit cell: 10 mm × 10 mm
- Covers 240 mm × 240 mm
- Two layers, 1152 ch in total

Work by S. Kanda (RIKEN)



Agenda

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- Apparatus

➤ Recent Measurements at low B field

- Result with lower gas pressure

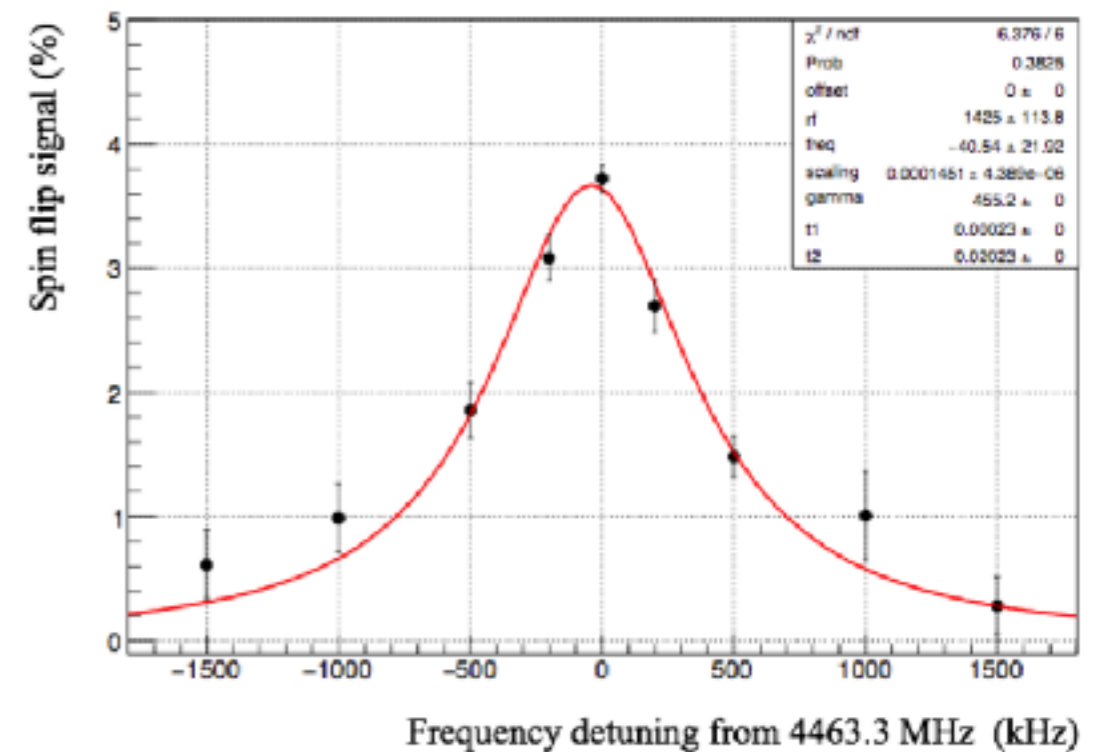
➤ R&D for future

- Mixture gas
- magnet for high field measurement
- Time differential method

First Result in 2016

17

- Measurement in 2016 at zero field at D-Line (Beam Power 200 kW) at Kr pressure = 1.0 atm
- First result: 4.463 292(22) GHz
precision: 22 kHz, statistically limited (world record: 1.4 kHz)
- First measurement of MuHFS using a pulsed muon beam

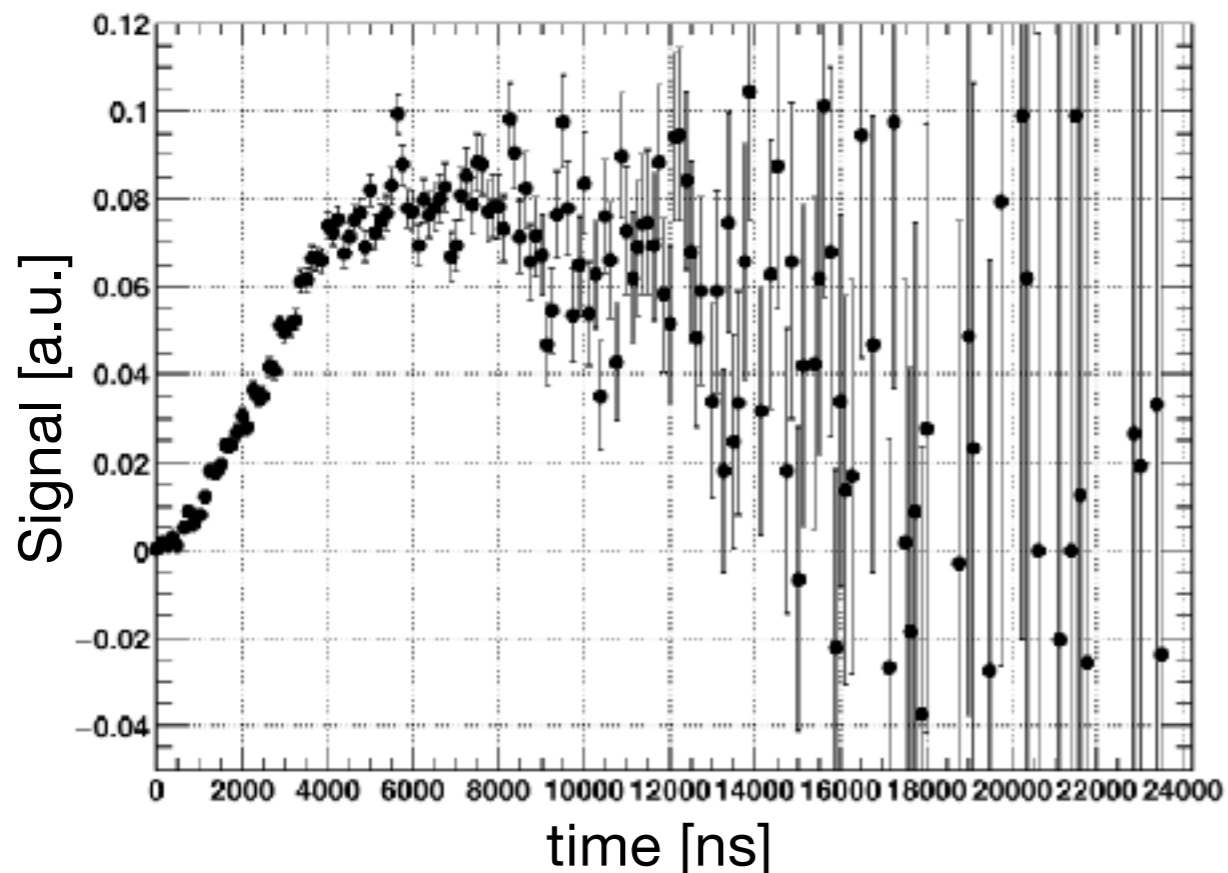


Measurement at Lower Kr Pressure

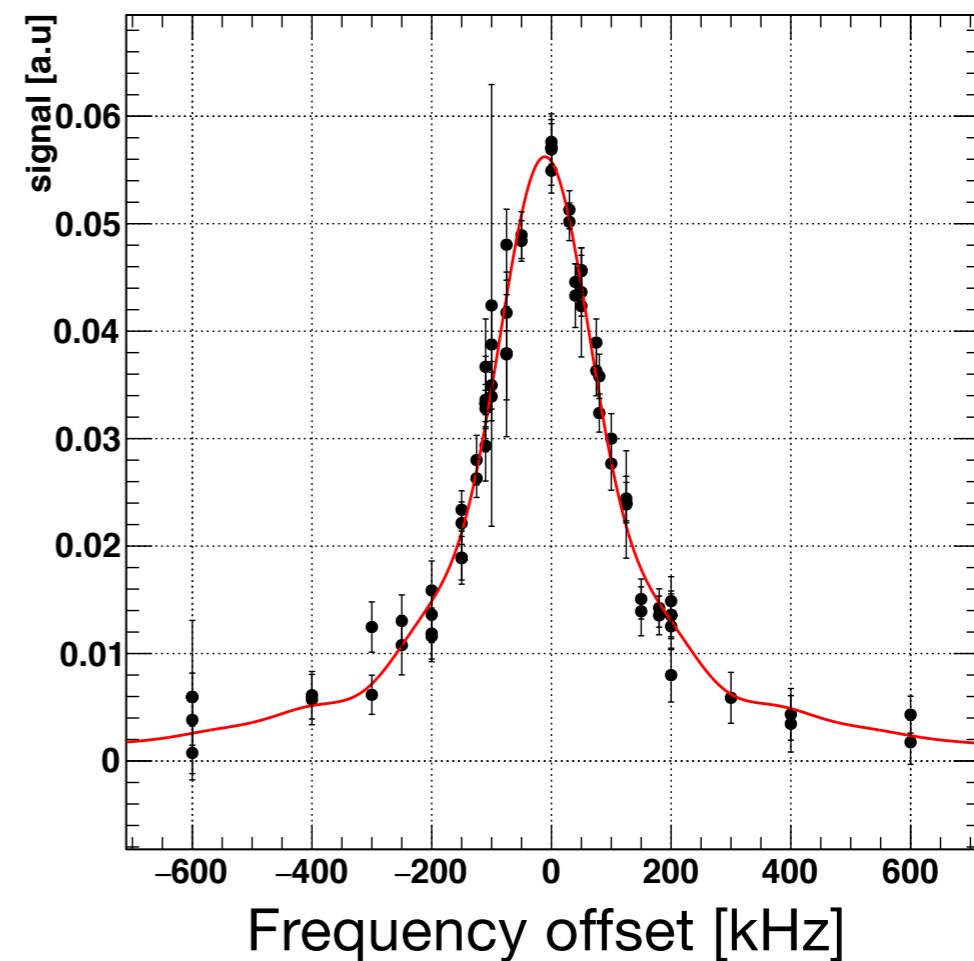
18

- MuHFS shifts in Kr, we need a value in vacuo to compare with theory
- Measurement at lower Kr pressure points (0.3-1.0 atm) in 2018,2019 (D-Line, with improved beam power ~ 500 kW)
- (Measurement at less than 0.8 atm has not been done before)

Kr = 0.7 atm, on resonance



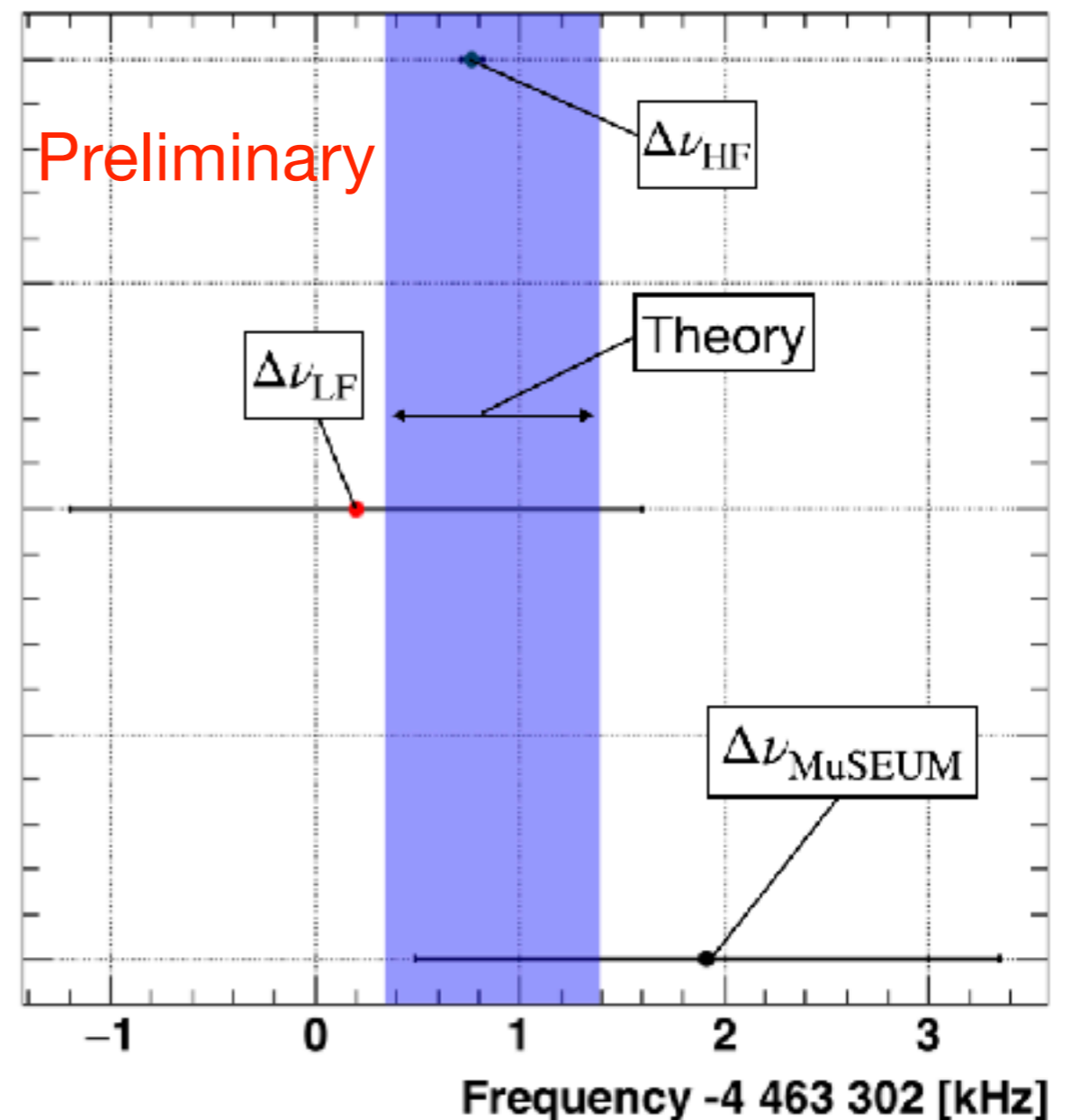
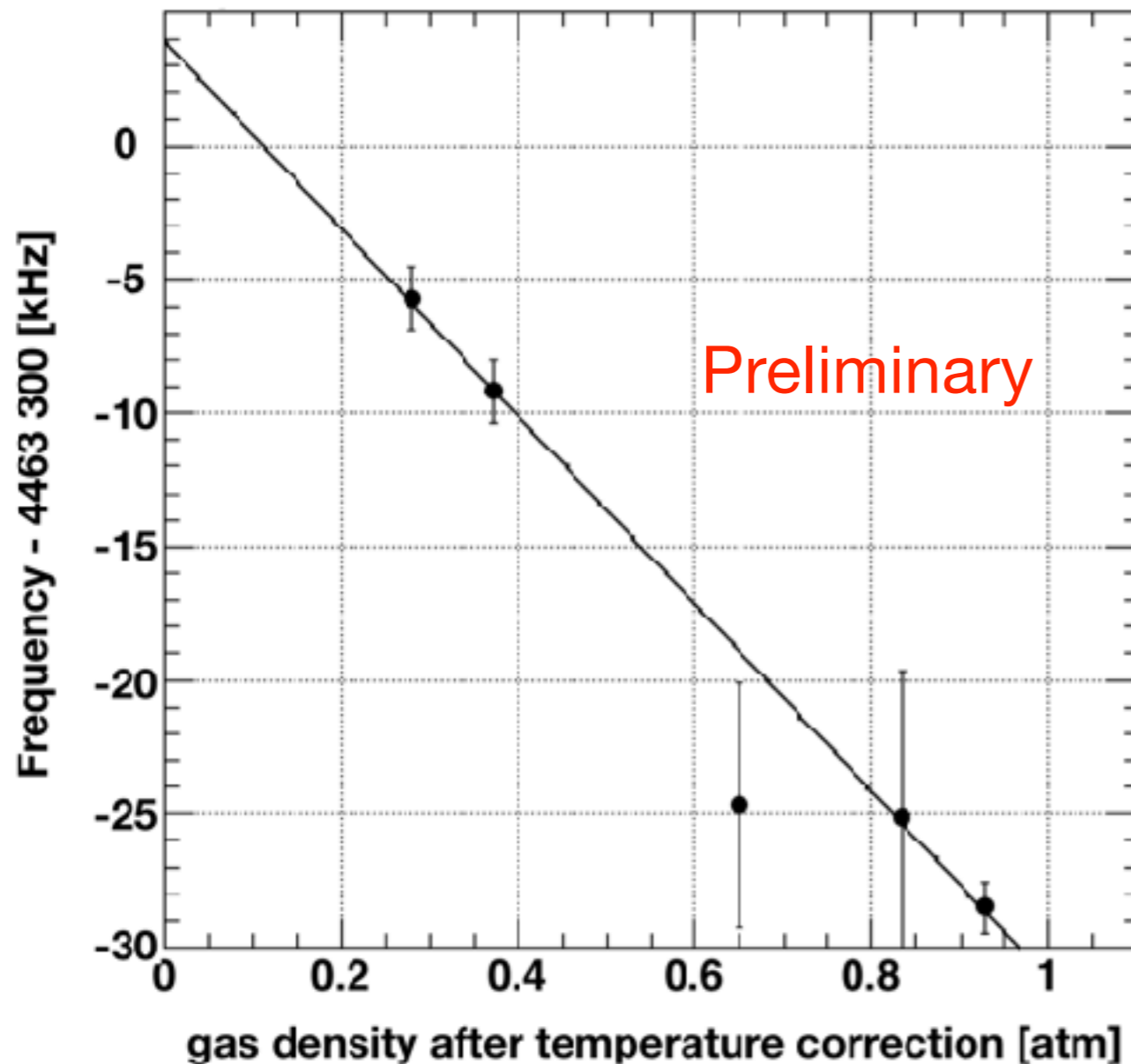
Kr = 0.4 atm



Measurement at Lower Kr Pressure

19

- Extrapolated the results to obtain the MuHFS in vacuo
- The uncertainty is comparable to the world record (1.4 kHz)
- Our result is consistent with the theory and the precursor experiment

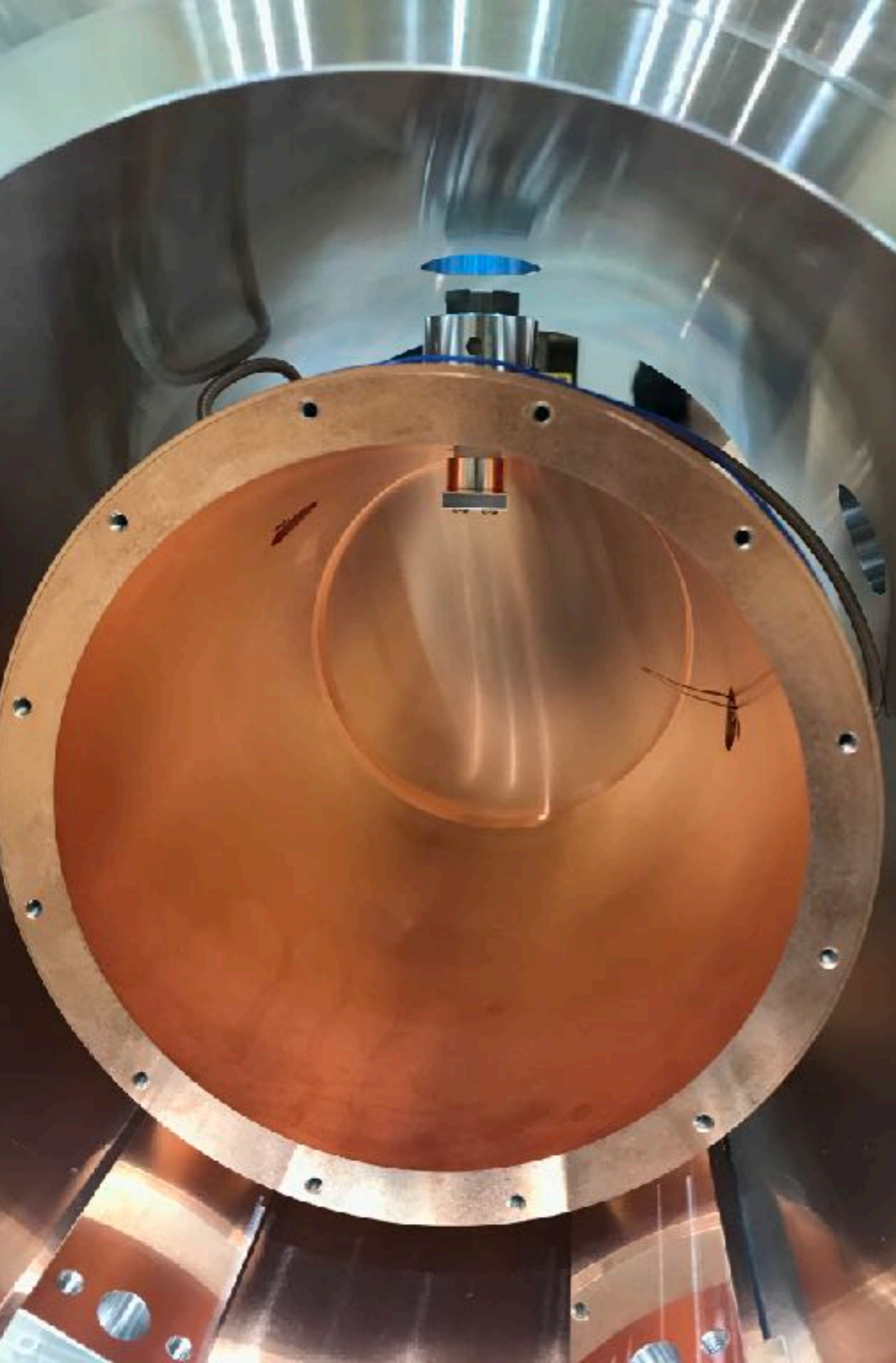


Uncertainty in Weak Field Measurement 20

- Current statistical uncertainty: 1400 Hz in 3 days
With new beamline and 100-days run: **40 Hz** is expected
Further improvement is achievable
- Systematic uncertainty: currently 112 Hz, <10 Hz in future

Systematic uncertainty table

Contribution	Uncertainty [Hz]
Pressure Gauge	79
Pressure Fluctuation	24
Quadratic Term	(2)
Frequency Reference	45
Power Drift	60
Muon Beam	6
Others	< 1
Total	112



Agenda

➤ Introduction

- Motivation
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- Apparatus

➤ Recent Measurements at low B field

- Result with lower gas pressure

➤ R&D for future

- Mixture gas
- magnet for high field measurement
- Time differential method

Systematic Uncertainties for High Field 22

	specification	$\Delta\nu$	μ_μ/μ_p
B field		0	26 ppb
RF stability	0.02%	0.8 ppb	8 ppb
Collision with Kr		1.0 ppb	5 ppb
Kr Temperature	0.2 K	0.4 ppb	4 ppb
Detector pile up		< 0.5 ppb	3 ppb
Others		< 0.8 ppb	7 ppb
Overall		< 1.6 ppb (8 Hz)	29 ppb

Collisional Shift and Gas Species

23

- Systematic uncertainty from the collisional shift is dominant
- There are two major effect from the collision

- Pauli exclusion effect (Short-range)
-> **positive shift**
- Van der Waals interaction effect (Long-range)
-> **negative shift**
dominant for large Z atom

J. Chem. Phys. 32, 972 (1960)

H-HFS pressure dependence in noble gas

B. K. Rao *et al.*, Phys. Rev. A 2(4) 1411(1970).

TABLE V. Values of the fractional pressure shift f_p for all five systems at 273 °K.

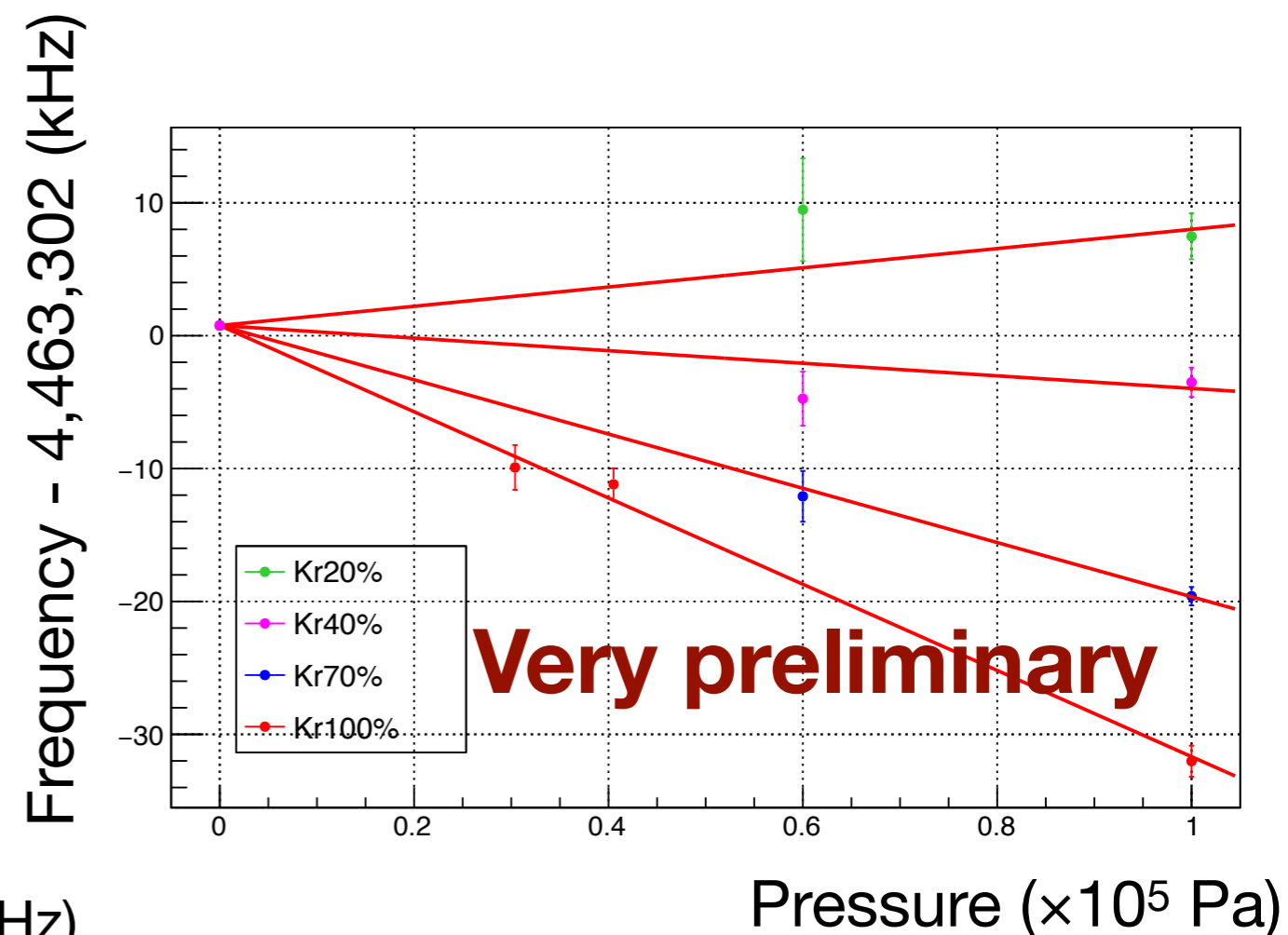
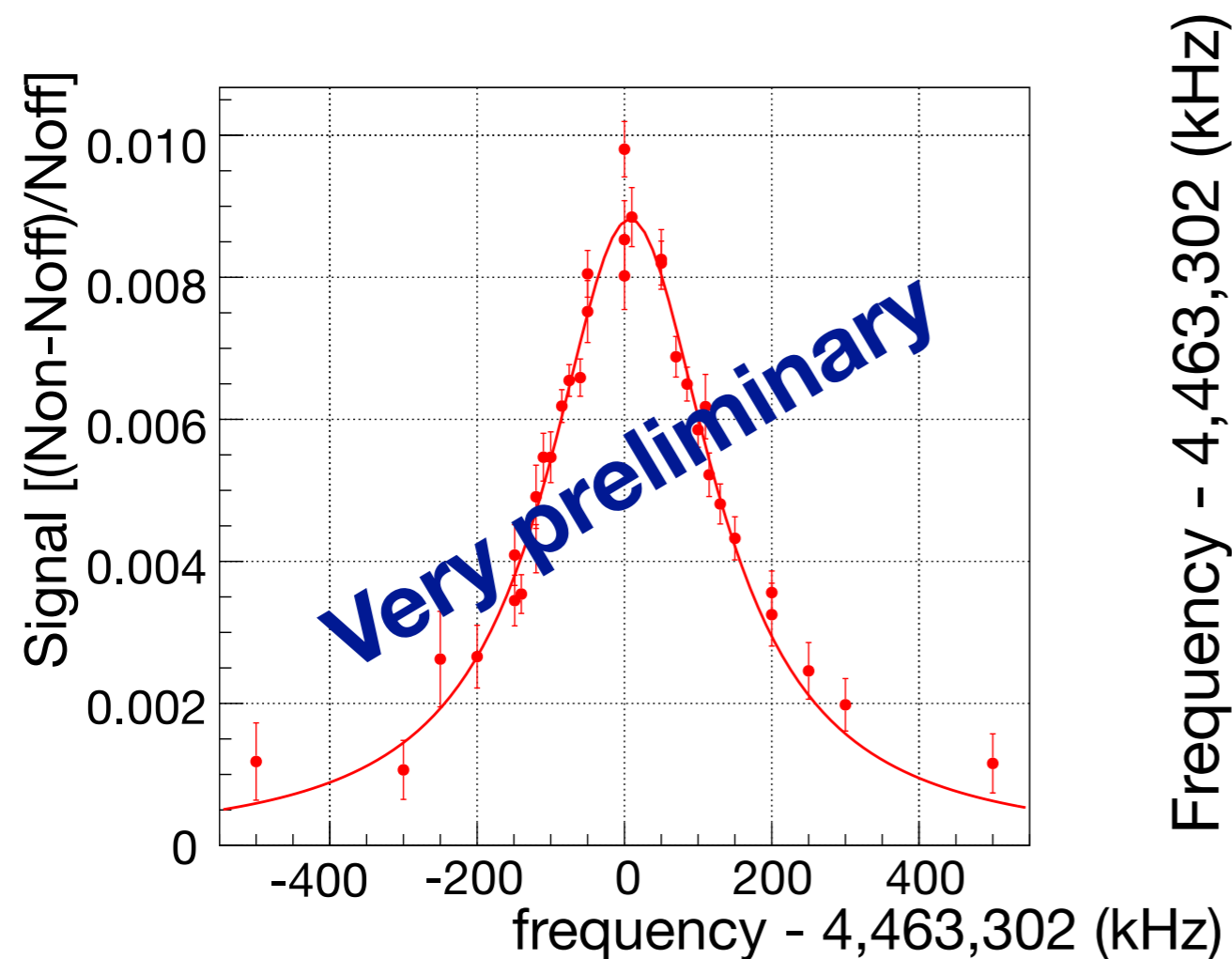
System	f_p (in $10^{-9}/\text{Torr}$)			Experiment
	Short-range	Long-range	Total	
H-He ^a	2.130	- 0.952	1.178	4.80
H-He ^b	2.679	- 0.950	1.729	4.80
H-Ne	2.059	- 1.952	0.107	2.88
H-Ar	4.556	- 7.827	-3.081	-4.77
H-Kr	7.525	-11.842	-4.317	-10.40
H-Xe	10.922	-17.560	-6.638	-20.00

- **He-Kr mixture gas can reduce the collisional shift**
- From Hydrogen HFS, Kr:He=4.8:10.4=Kr32% is ideal

Beam time in Mar & June 2019

24

- ▶ Used mixture gas Kr-He to suppress the extrapolation uncertainty
- ▶ Confirmed Mu formation in Kr-He gas, and observed MuHFS resonance



resonance with Kr 20% gas at 1.0 atm

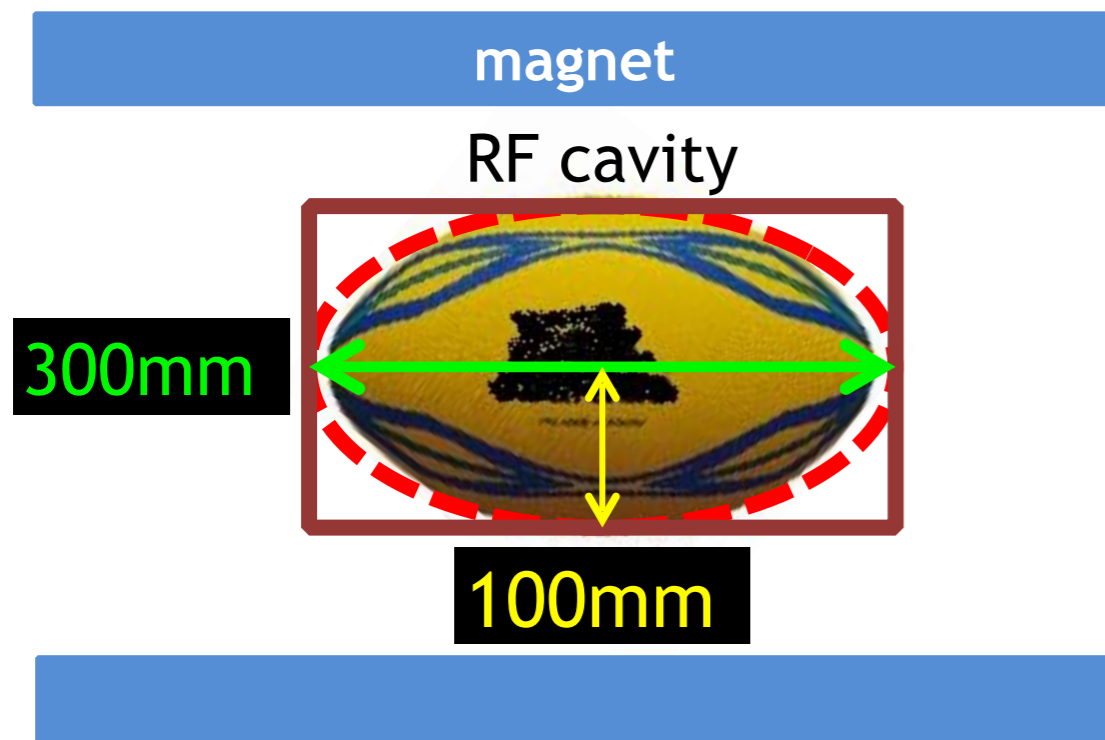
Work by S. Seo (Univ. of Tokyo)

Systematic Uncertainties for High Field 25

	specification	$\Delta\nu$	μ_μ/μ_p
B field		0	26 ppb
RF stability	0.02%	0.8 ppb	8 ppb
Collision with Kr		1.0 ppb	5 ppb
Kr Temperature	0.2 K	0.4 ppb	4 ppb
Detector pile up		< 0.5 ppb	3 ppb
Others		< 0.8 ppb	7 ppb
Overall		< 1.6 ppb (8 Hz)	29 ppb

Superconducting Magnet for 1.7 T Field 26

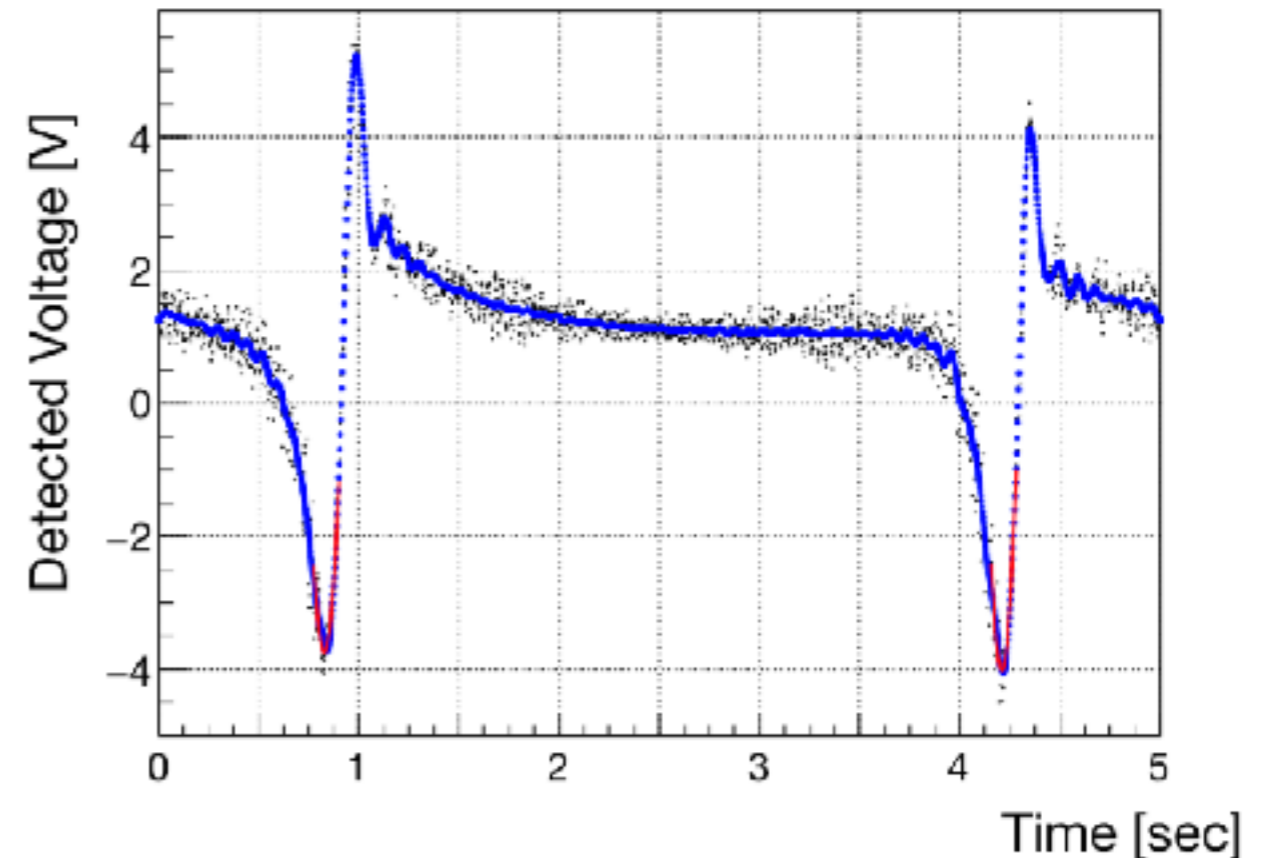
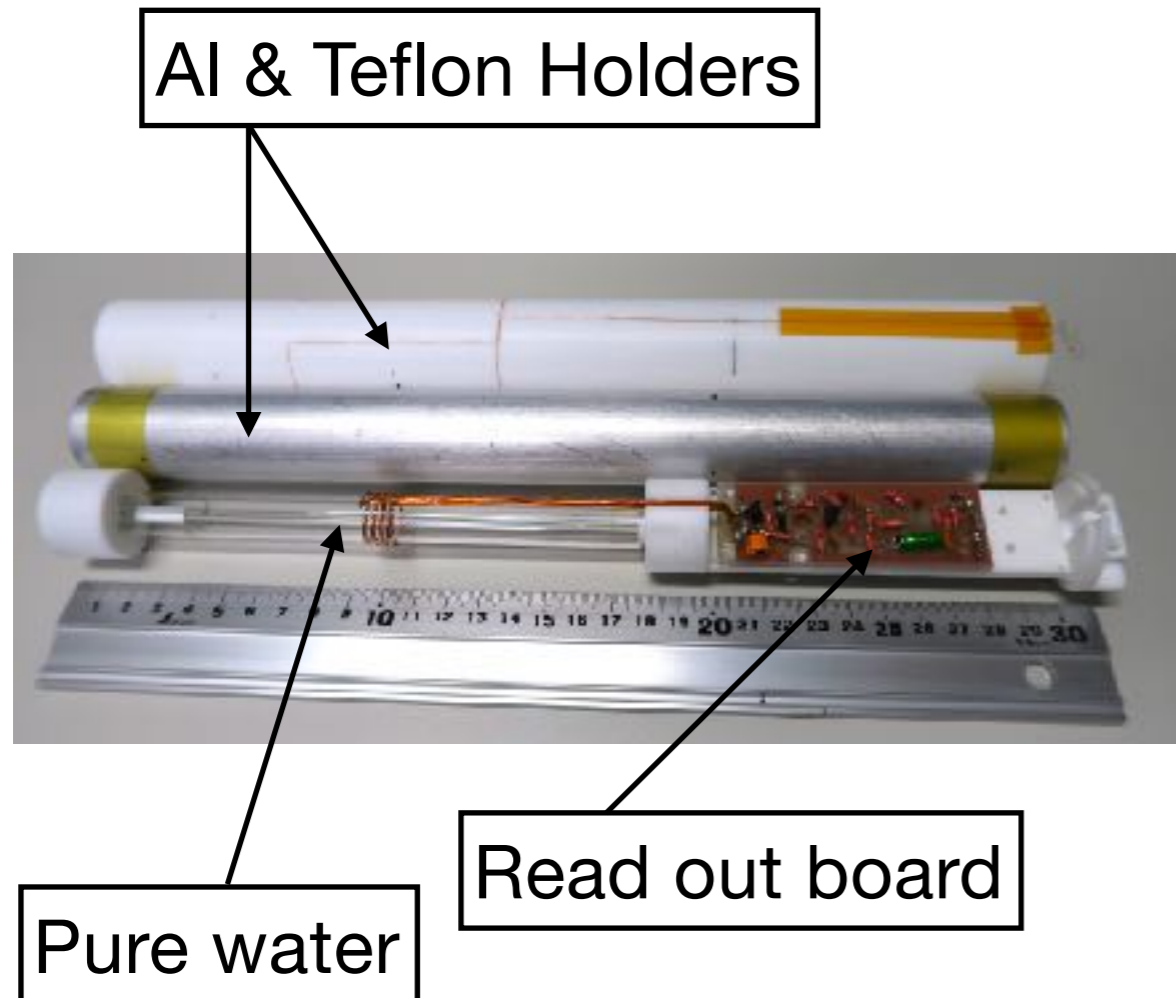
- Time stability: **3 ppb/hour** over 10 days period
(required stability 100 ppb/h) *By K. Sasaki and M. Abe (KEK)*
- Required uniformity is 1 ppm in a rugby-ball sized volume
by shimming we achieved **0.3 ppm**



NMR Magnetometer

27

Work by K. Sasaki, H. Yamaguchi (KEK)
and T. Tanaka (Univ. of Tokyo)

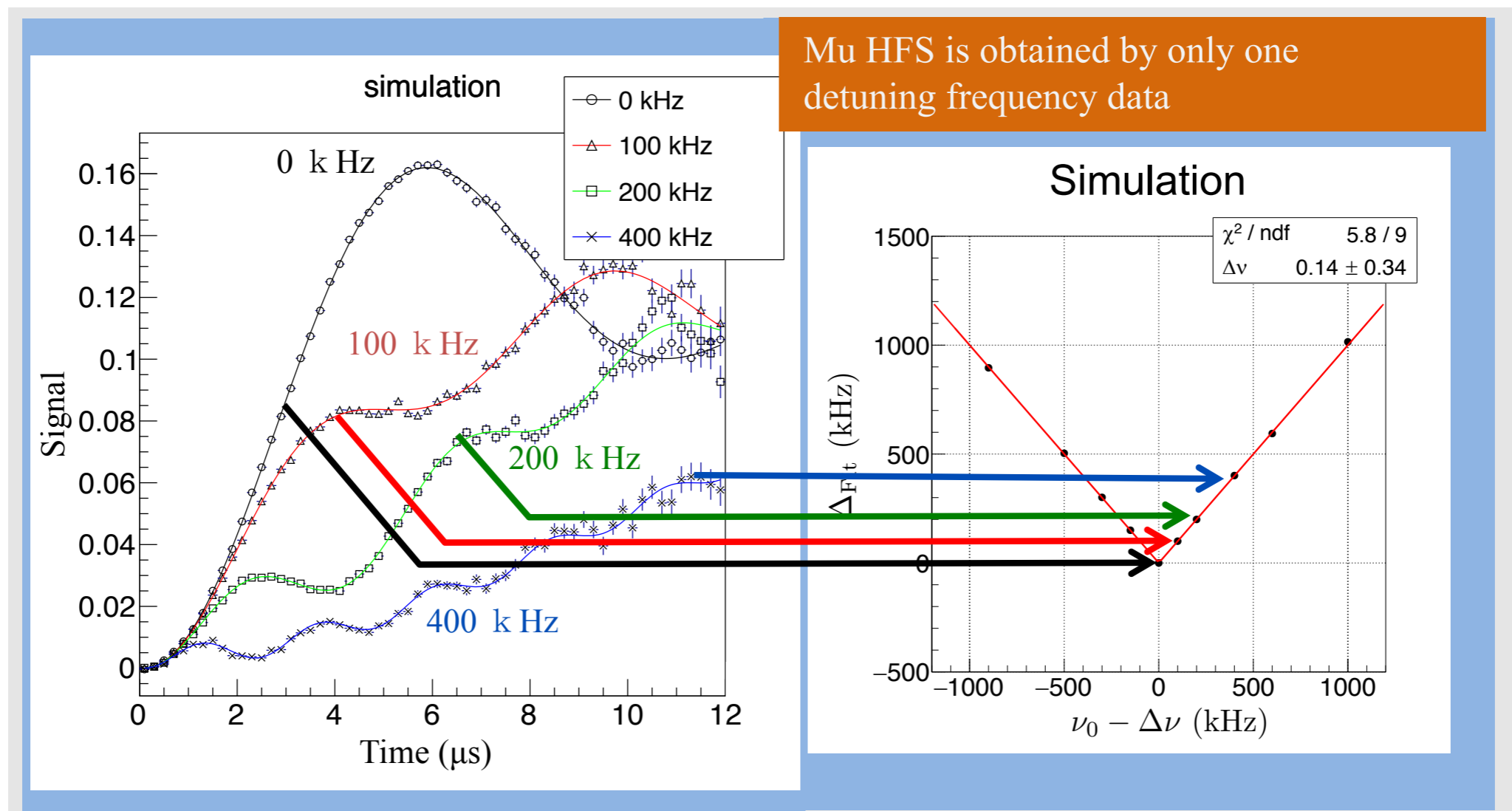


- Proton NMR (Nuclear Magnetic Resonance) in pure water
- Cross-check measurement at 1.45 and 1.7 T with NMR probes used in Fermilab muon $g-2$ experiment
- Progress in the precision: 18 ppb (2017) → **12 ppb** (2019)

Time Differential Method: Simulation

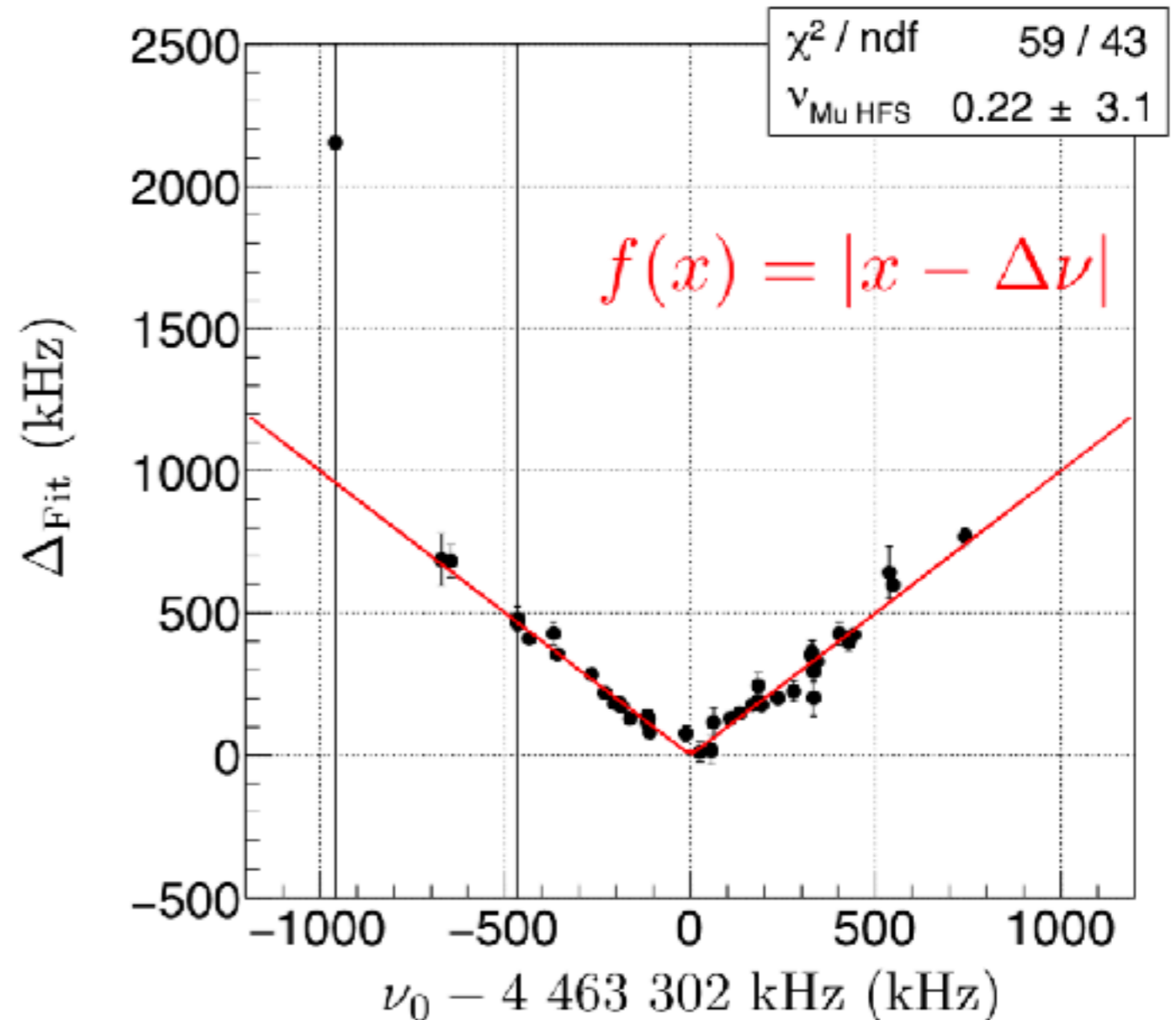
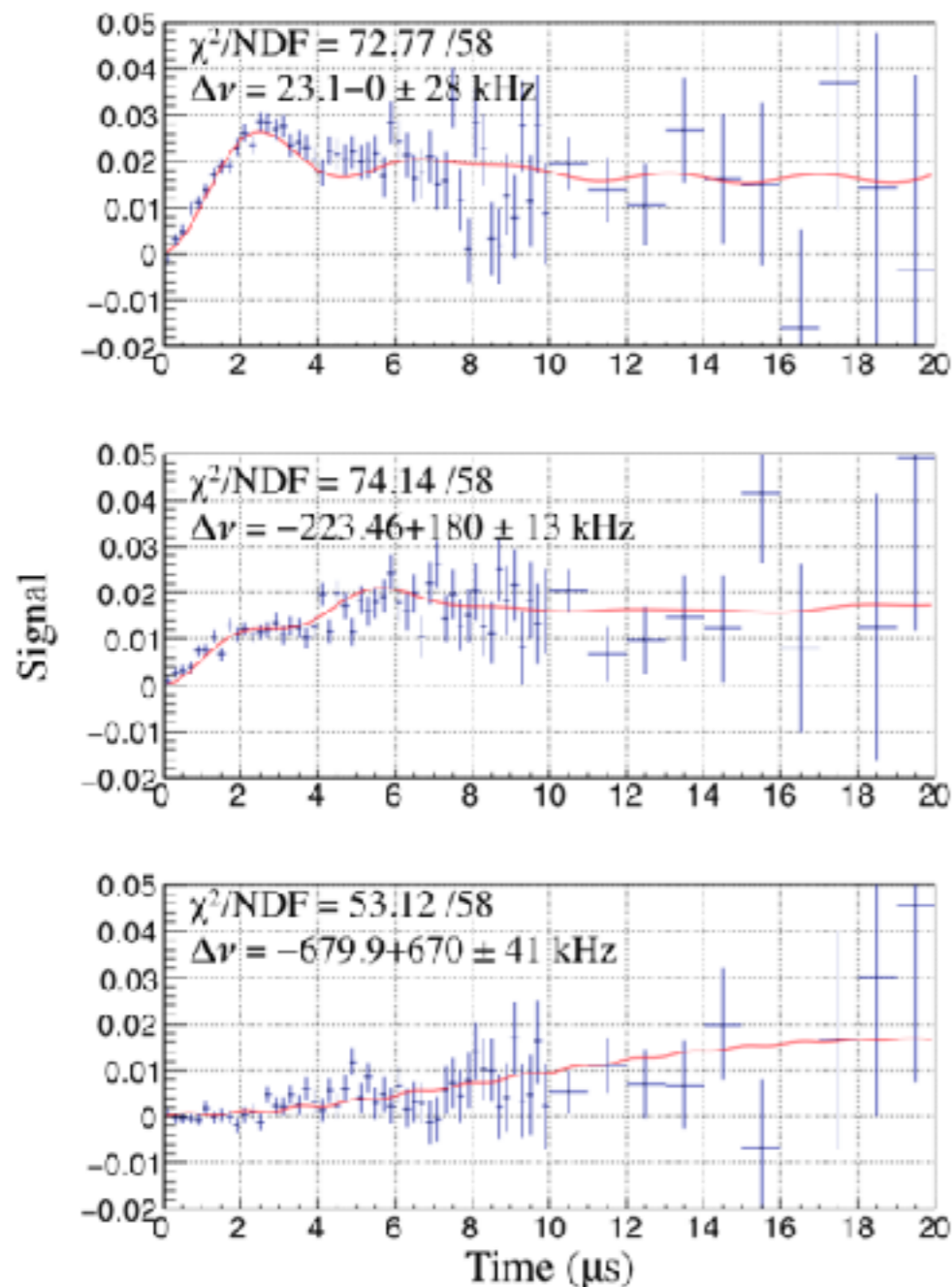
28

- MuHFS determined by fitting the time-dependent signal of muon spin flip (Rabi oscillation)
- No need to take data at many microwave frequency points a method immune to the systematic uncertainty from the microwave power dependence on frequency



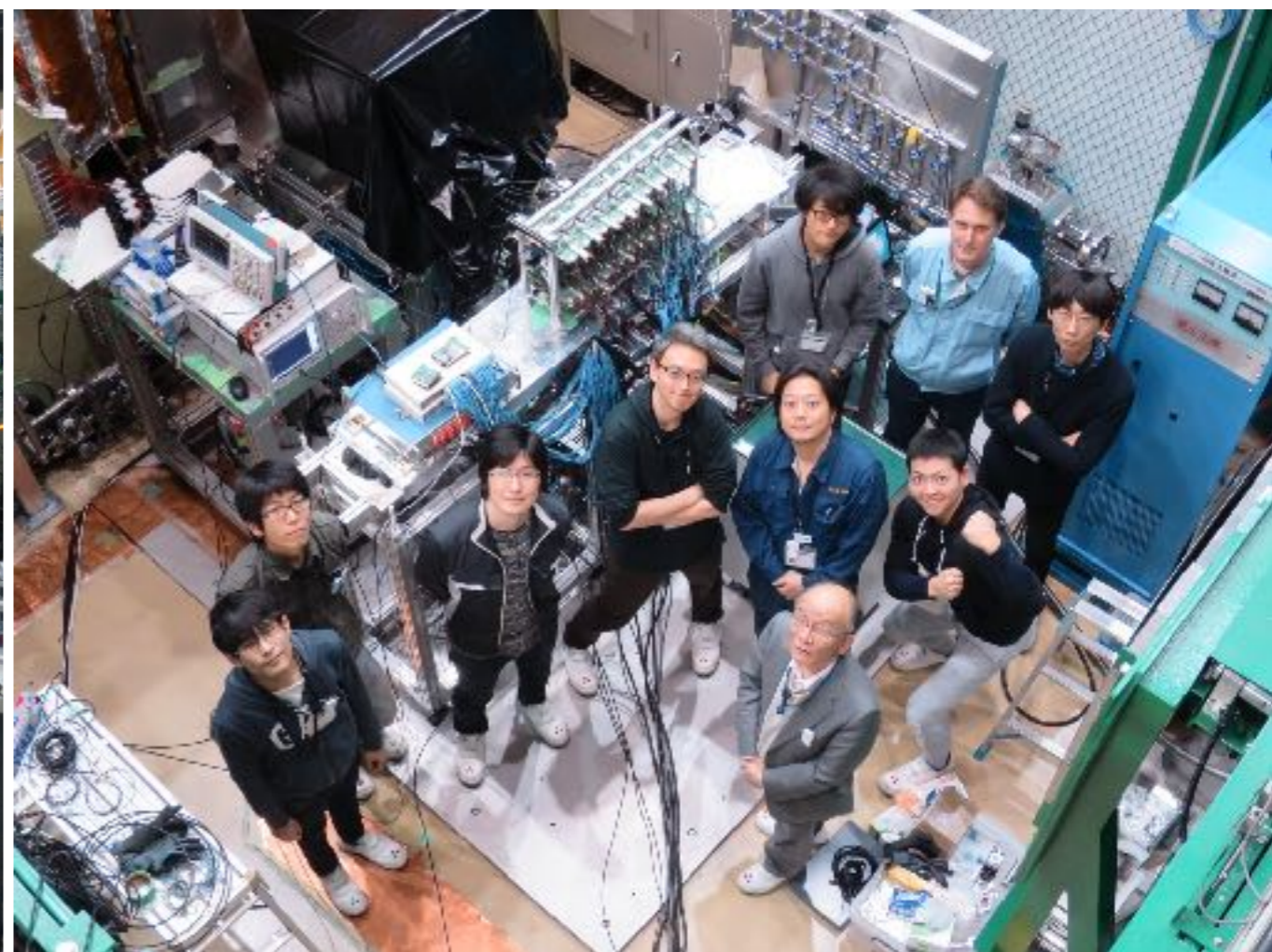
Time Differential Method: data in 2017 29

- First result obtained by time differential method *By S. Nishimura (KEK)*
- Promising method to improve the precision



- MuSEUM
Test of the bound-state QED
Determination of muon magnetic moment
-synergy with muon $g-2$
- Recent measurement with lower Kr gas pressures at low B field
consistent with theory and the precursor experiment
- R&D for future experiment
First measurement using Kr-He mixture gas
Magnet and magnetometer development for high field
measurement
First analysis using time differential method
- MuHFS 2 ppb, μ_μ/μ_p 30 ppb is achievable
(a factor of 10 improvements from the precursor experiment)
Further improvement is in progress

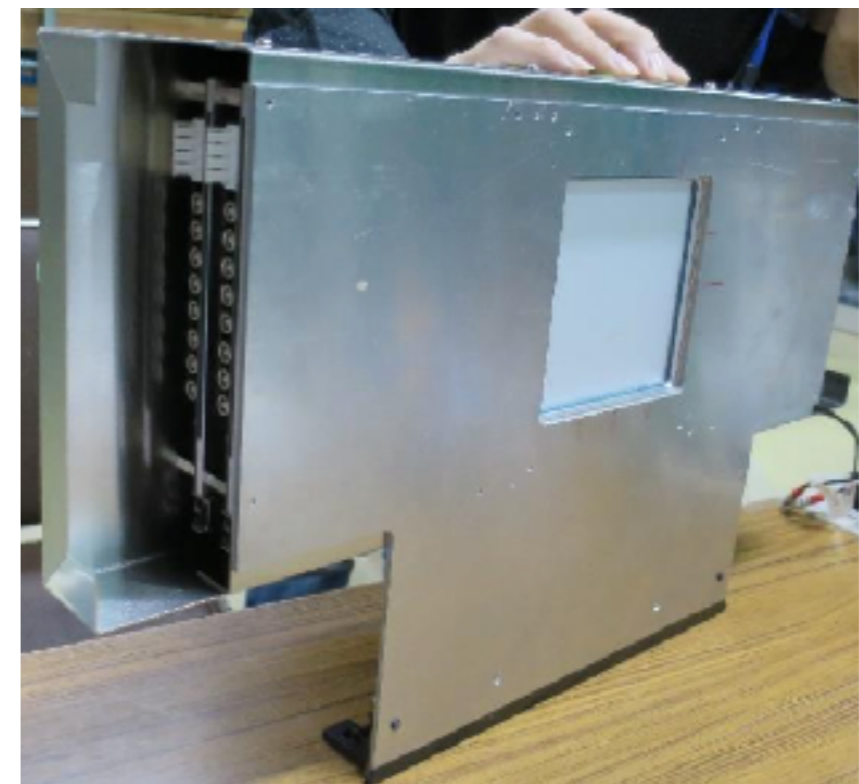
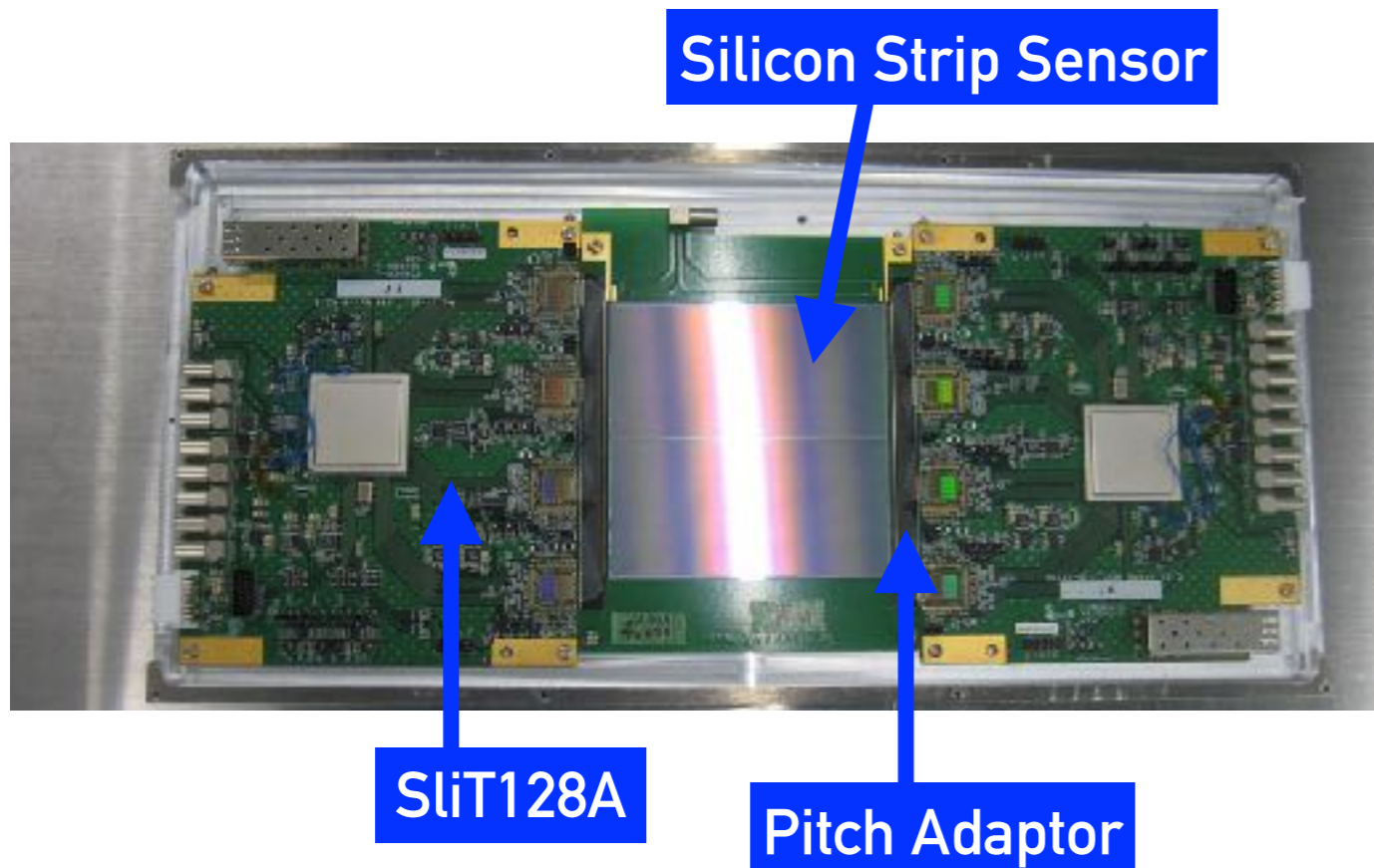
Thank you!



Silicon Strip Sensor

32

- Developed for muon $g-2$ J-PARC experiment
- Capable of high-rate counting; R&D for H-Line measurement in future
- There was stray magnetic field from the detector board; made a permalloy shield for the detector
- Performed satisfactory in beam time on June 2019



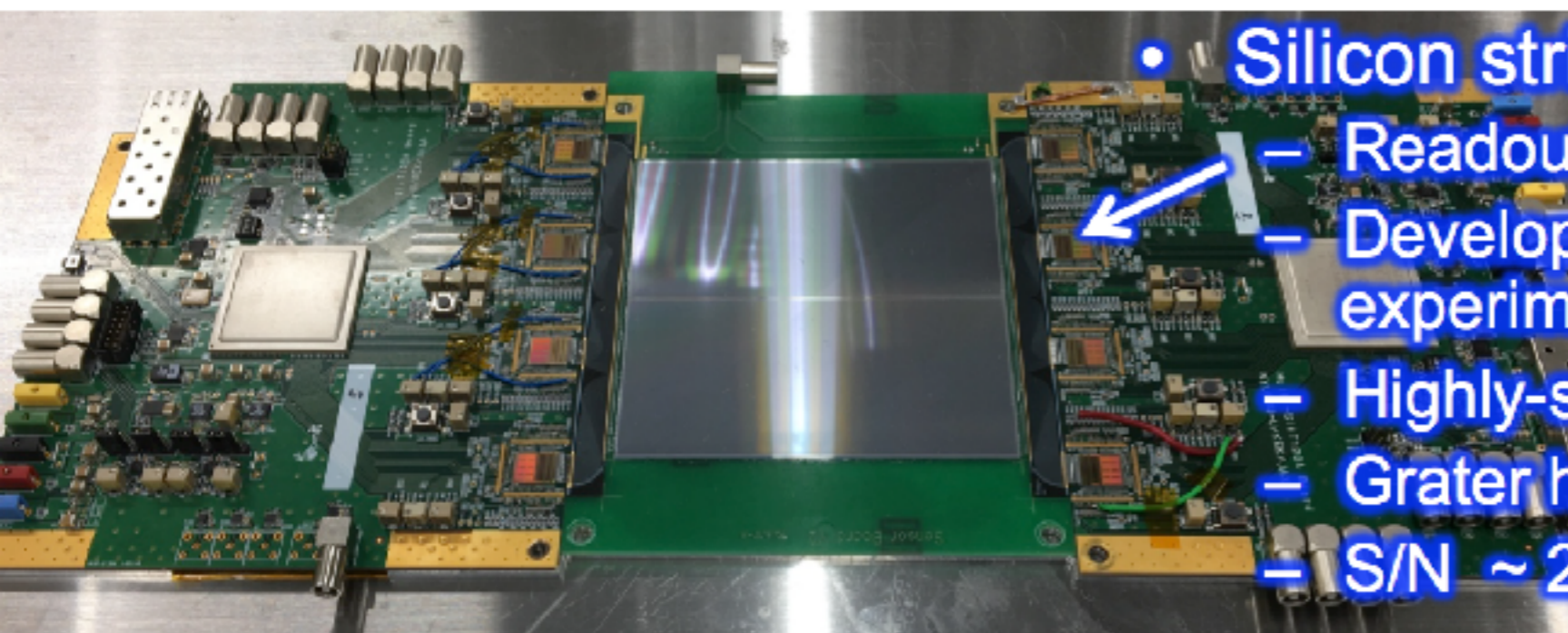
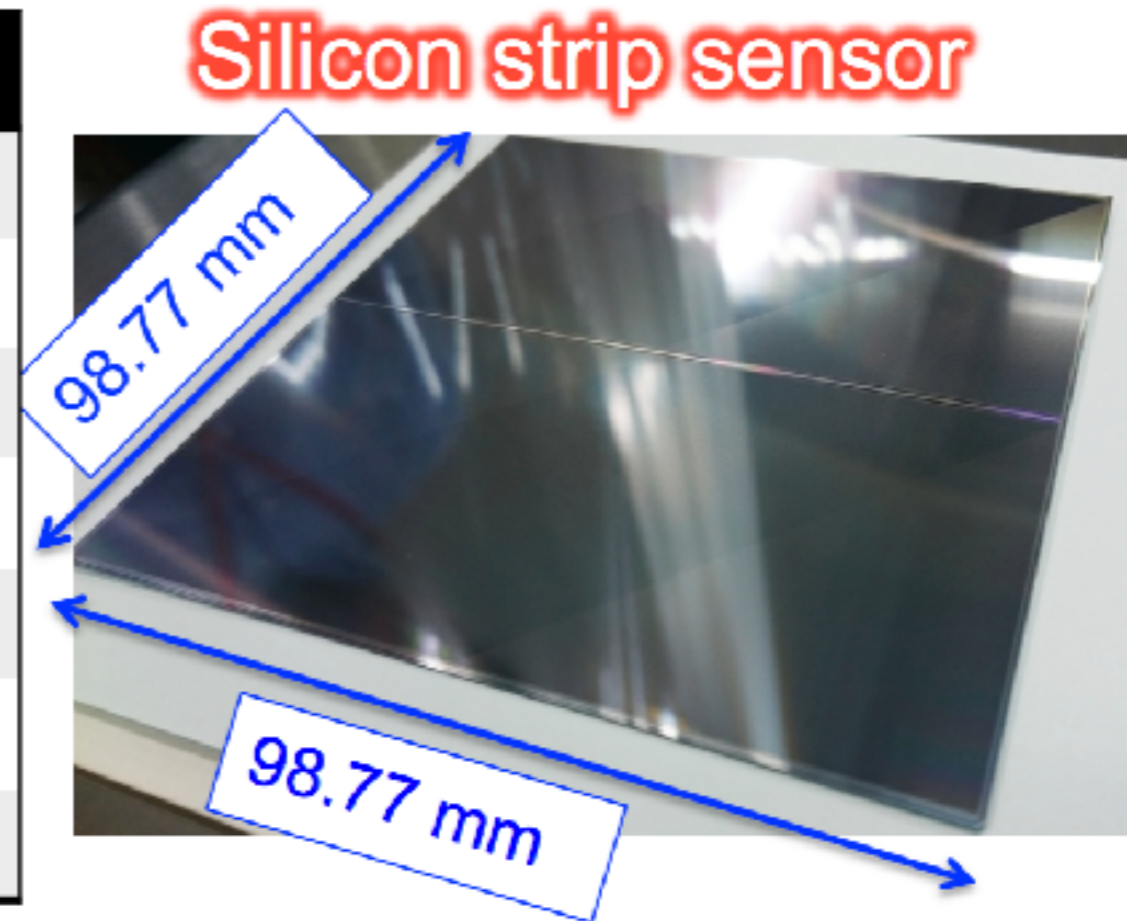
Uncertainty in Weak Field Measurement 33

Contribution	Uncertainty [Hz]		in future [Hz]
Pressure Gauge	79	→	8
Pressure Fluctuation	24	→	2
Quadratic Term	(2)		0
Frequency Reference	45	→	<1
Power Drift	60	→	1
Muon Beam	6		6
Others	< 1		<1
Total	112		10

Silicon Strip Detector

34

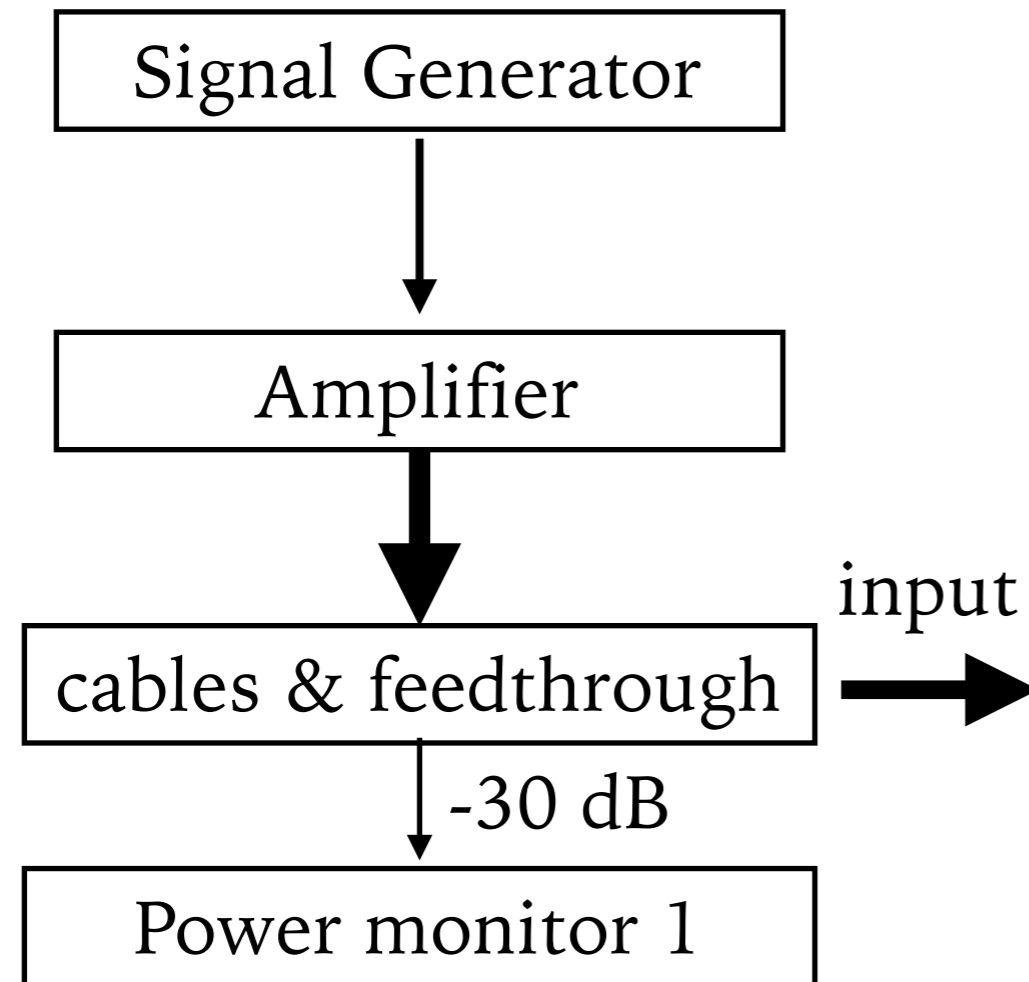
Item	Specification
Sensor type	single-sided, p+ on n
Size	98.77 mm × 98.77 mm
Active area	97.28 mm × 97.28 mm
Strip pitch	0.19 mm
Strip length	48.575 mm
# of strips	512 × 2 blocks
Thickness	0.32 mm



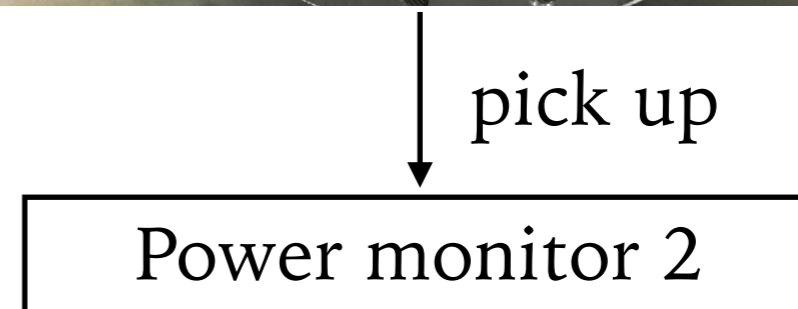
- Silicon strip detector
 - Readout chips (SIT128A, 128 ch/chip)
 - Developed for J-PARC g-2/EDM experiment
 - Highly-segmented
 - Greater high rate capability
 - S/N ~ 21

Microwave Cavity and System

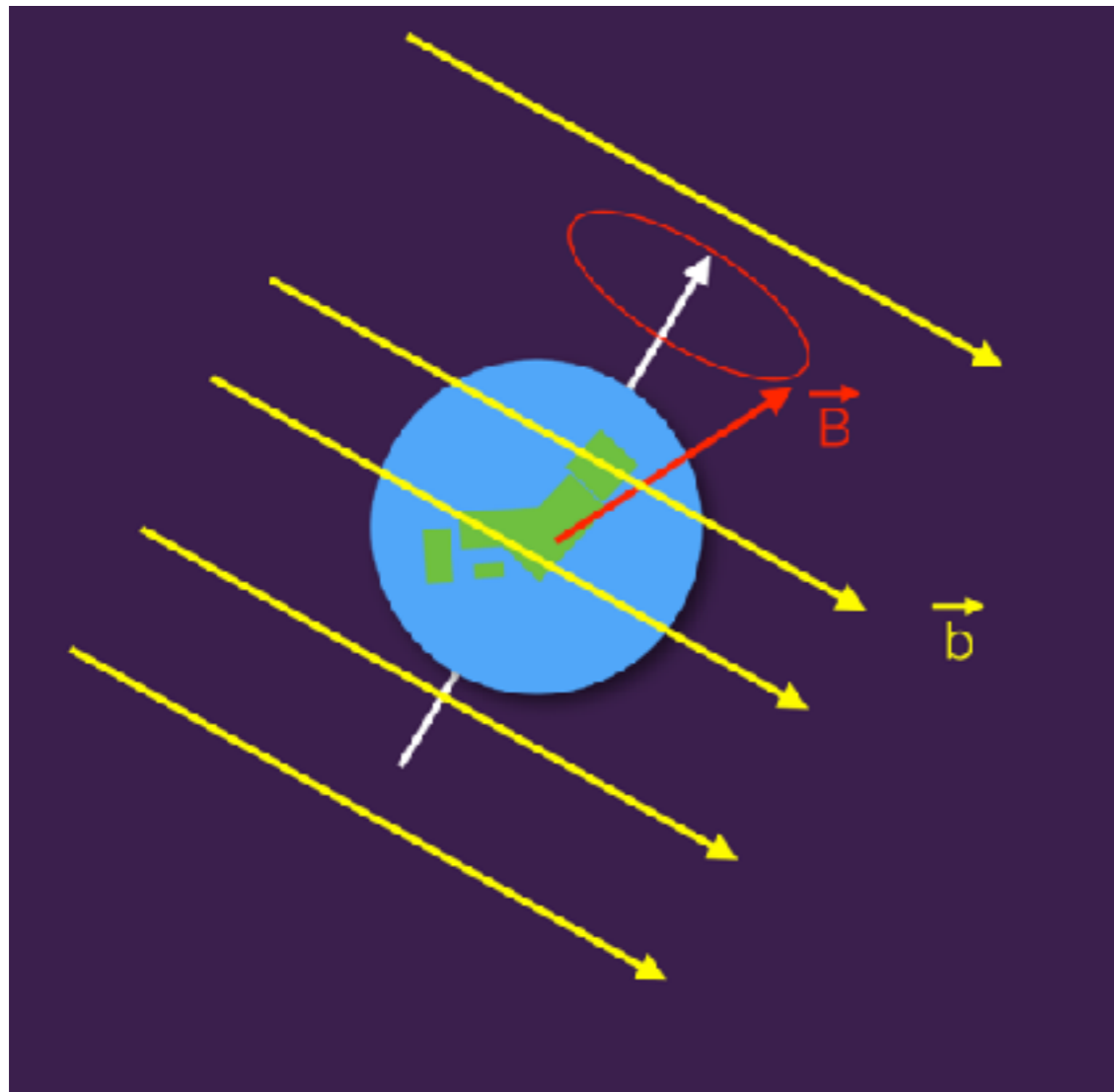
35



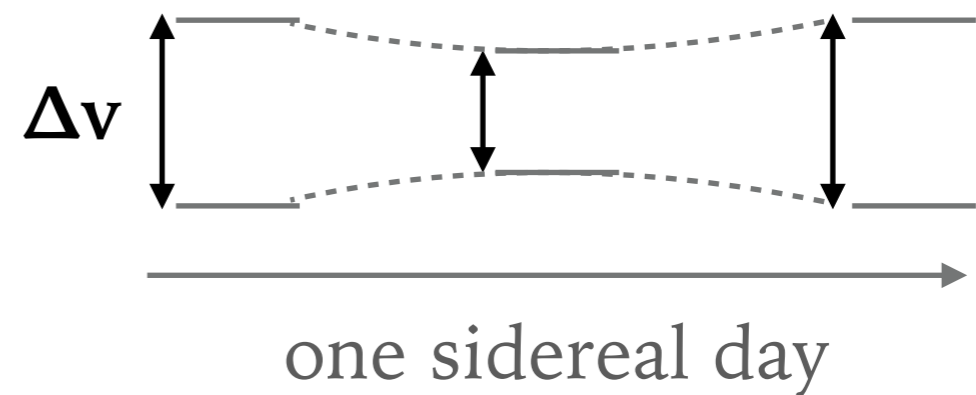
- TM₂₂₀ mode cavity, $Q = 10000$
- Typical input power: 1 W
- Power stability is monitored



- Lorentz (CPT) violating background field can be detected as **sidereal (or annual) oscillation of the hyperfine frequency**
- Constraint on Standard Model Extension(SME) parameters



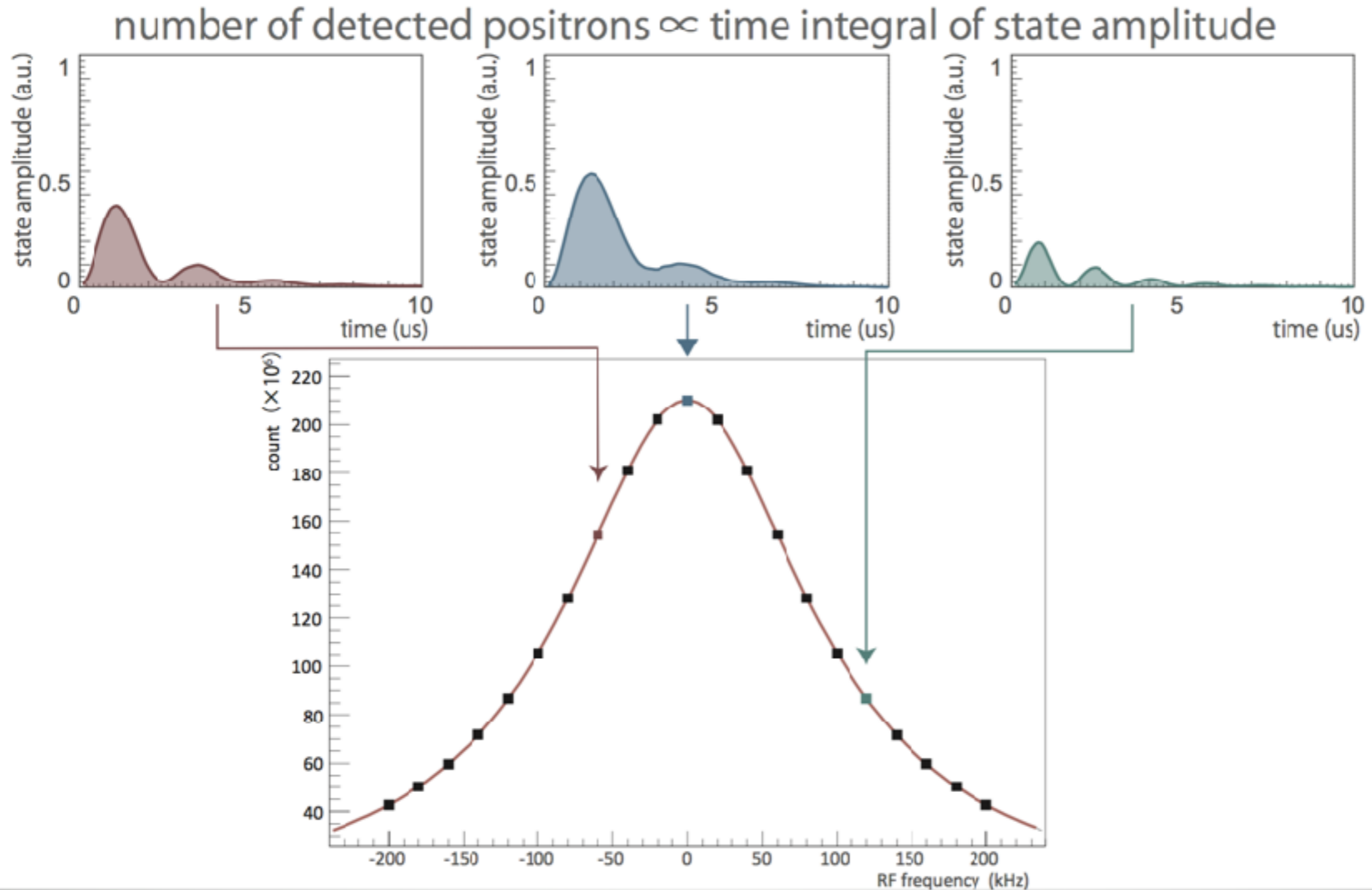
A. H. Gomes, V. A. Kostelecky and A. J. Vargas,
PRD **90** 076009 (2014)



Conventional Method

37

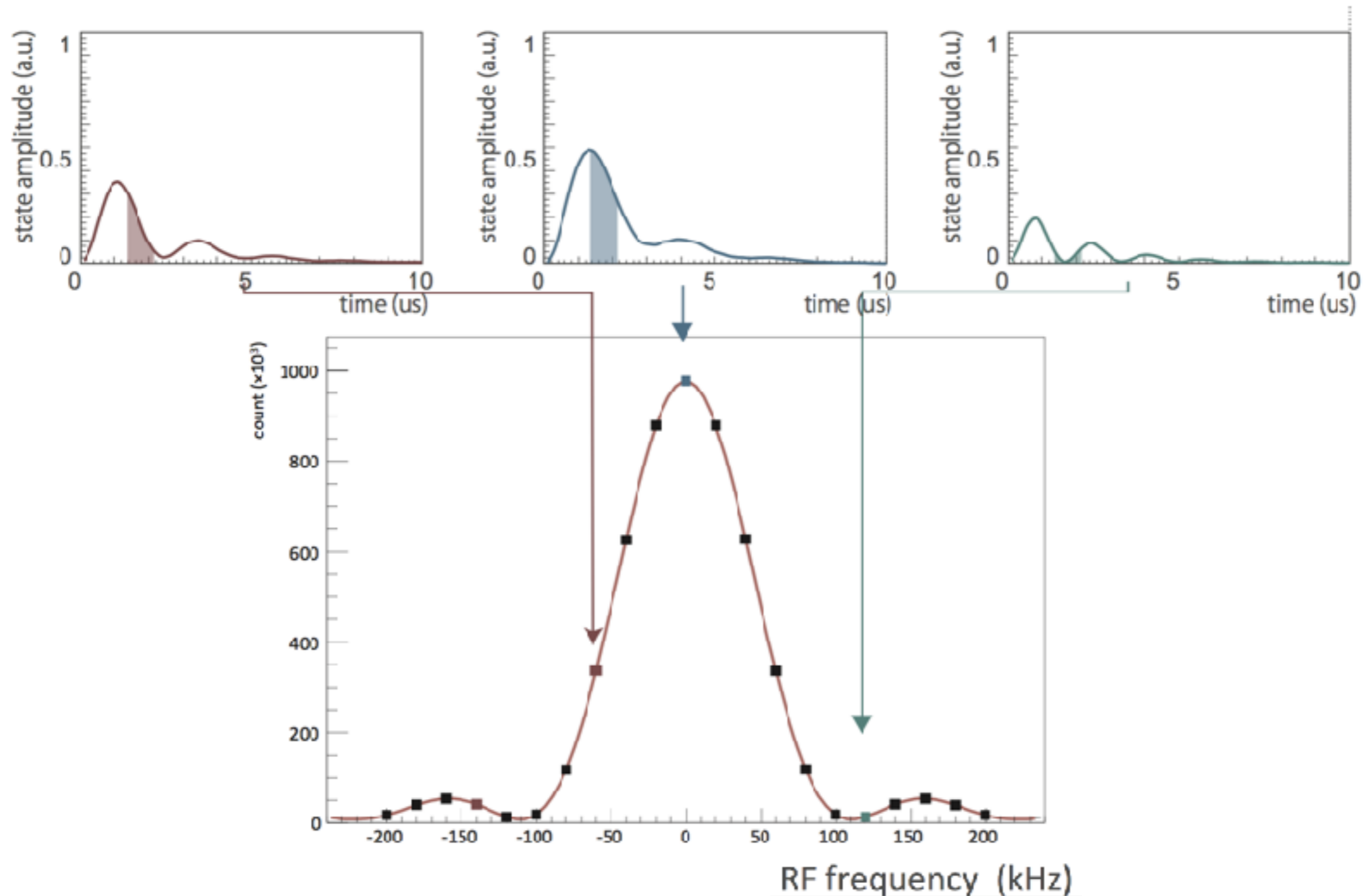
- Integrate all the signal



Old Muonium Method

38

- ▶ Line narrowing technique by the analysis using signals from a delayed time window; Long life time hence narrow natural width.



Passive Shimming Technique

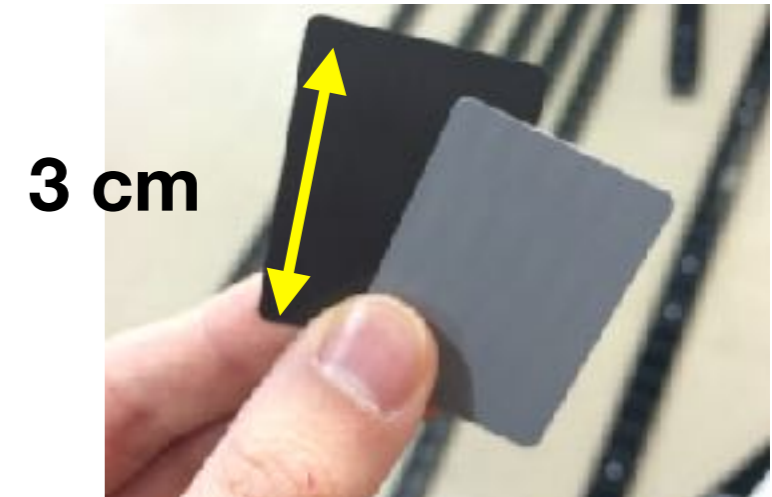
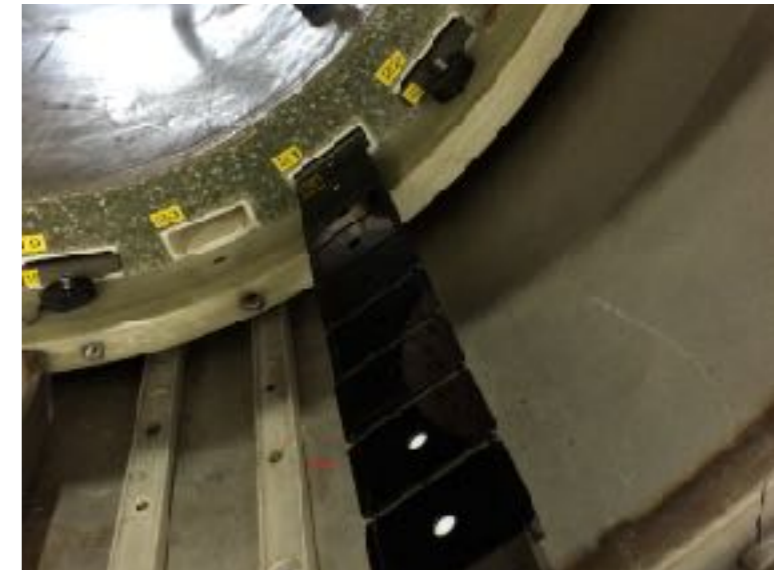
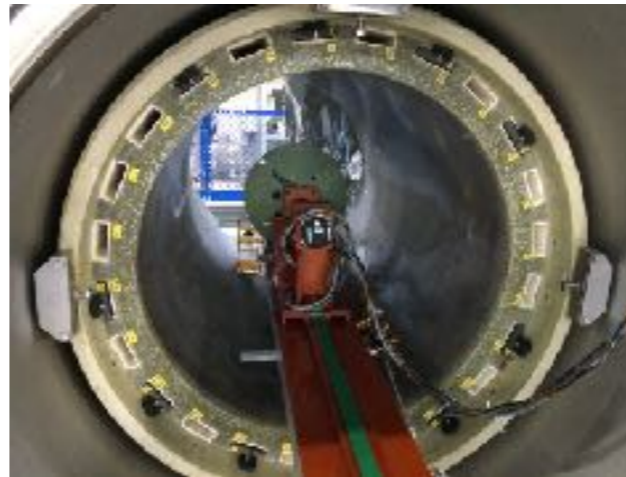
39

- Required field uniformity: 1 ppm
- In addition to shimming coil, shimming by small iron plates is important
- The positions of the iron plates can be calculated by the Singular Value Decomposition Method

Plate Volume:

Thick: 0.325 cc

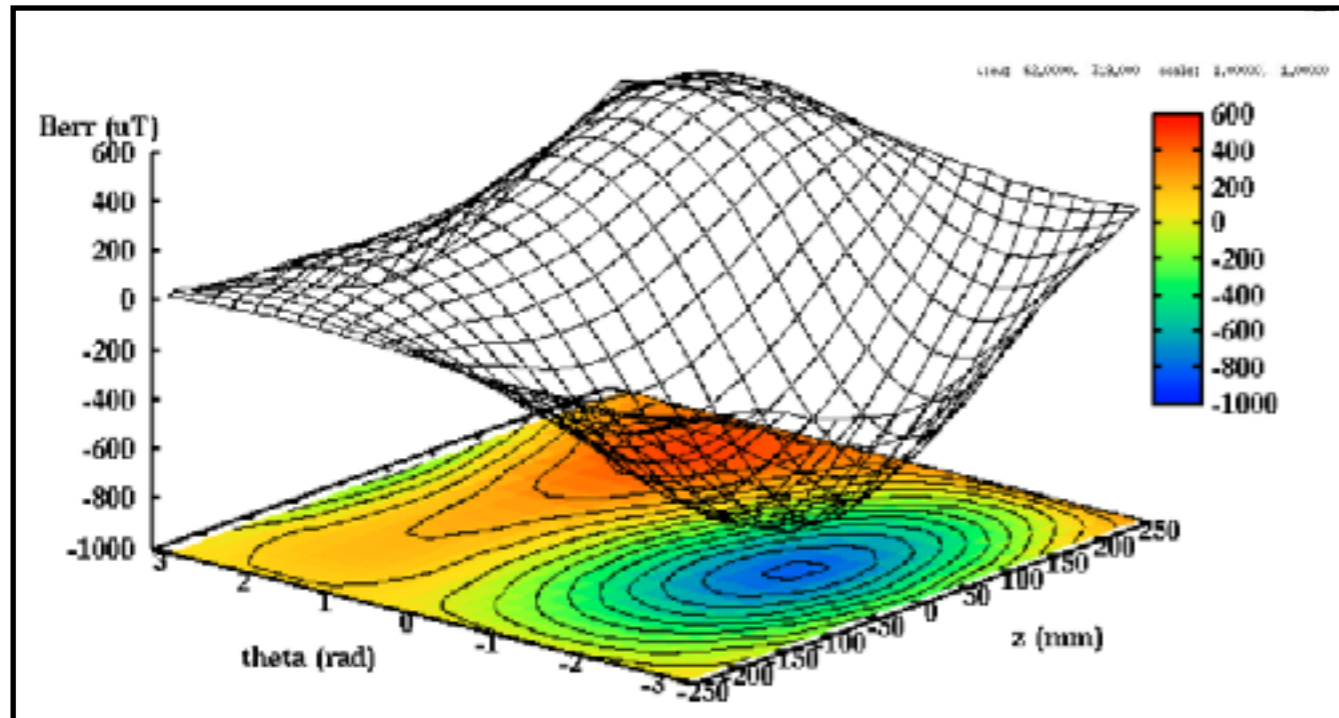
Thin: 0.065 cc



Shimming

40

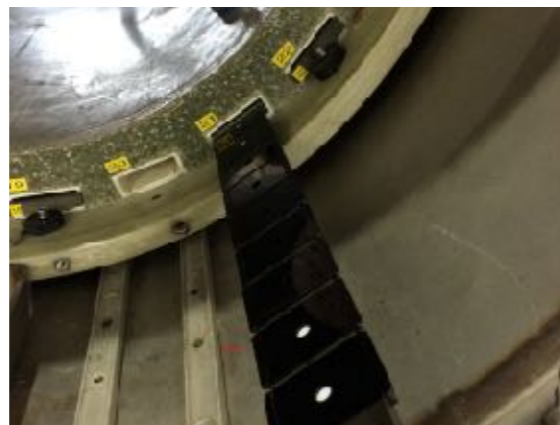
Peak-to-peak: 1000 ppm



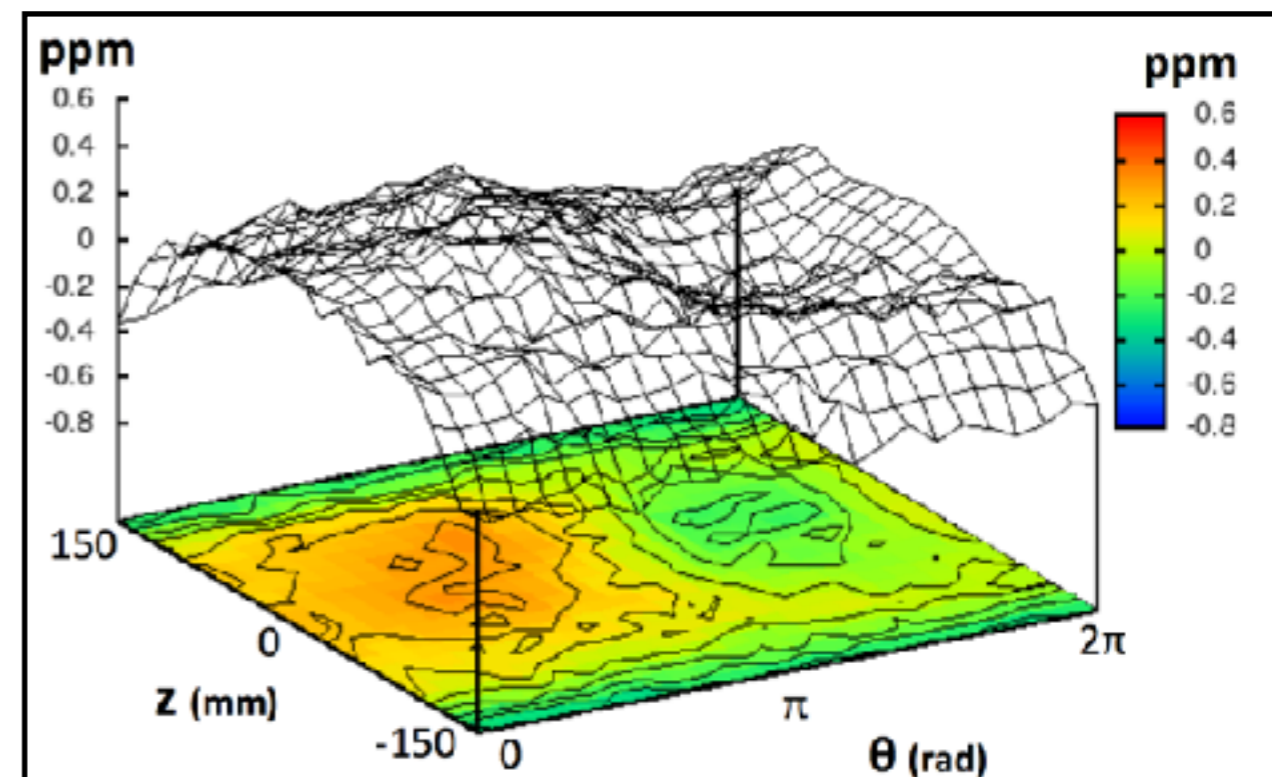
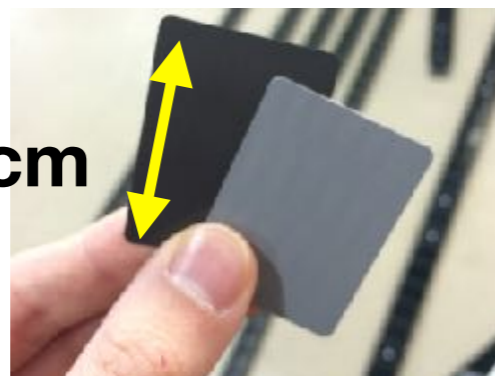
Field uniformity is improved by shimming using iron-plate
We have succeeded in obtaining required uniformity
< 1 ppm



Peak-to-peak: 0.80 ppm



3 cm



Shimming

- By iron-plate shimming, uniformity 1000 ppm \rightarrow 0.8 ppm
(required uniformity: 1 ppm)

