

Understanding the EW Phase Transition @ LHC and Beyond

Jose Miguel No
IFT-UAM/CSIC, Madrid



Opportunities at Future Colliders
Madrid, 11/06/19

Understanding the EW Phase Transition @ LHC and Beyond *Future Colliders*

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Understanding the EW Epoch

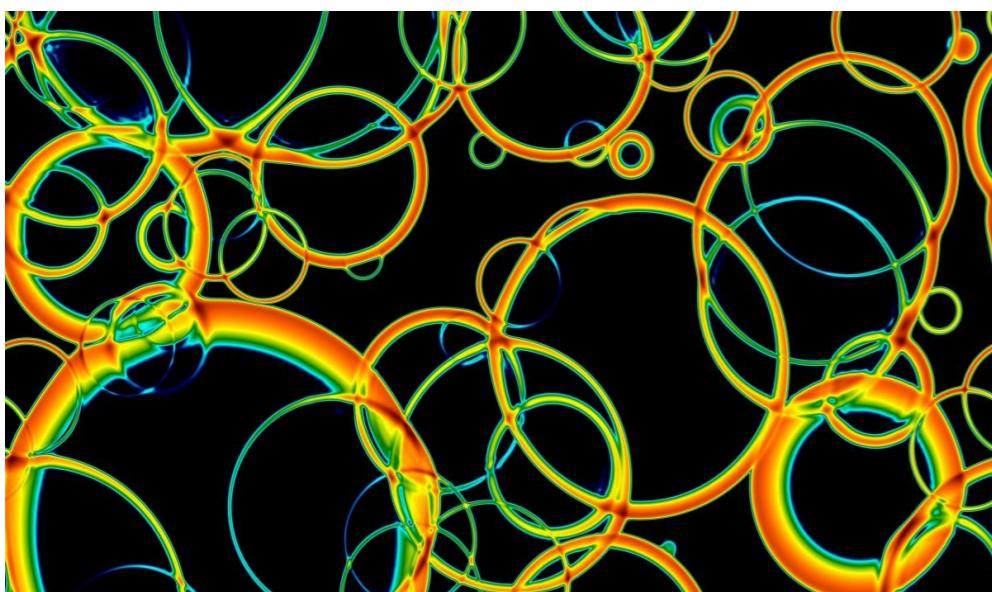
Why?

- Yield Precise knowledge of EWSB in Early Universe
- (Possible) Cosmological Relics from the EW Epoch

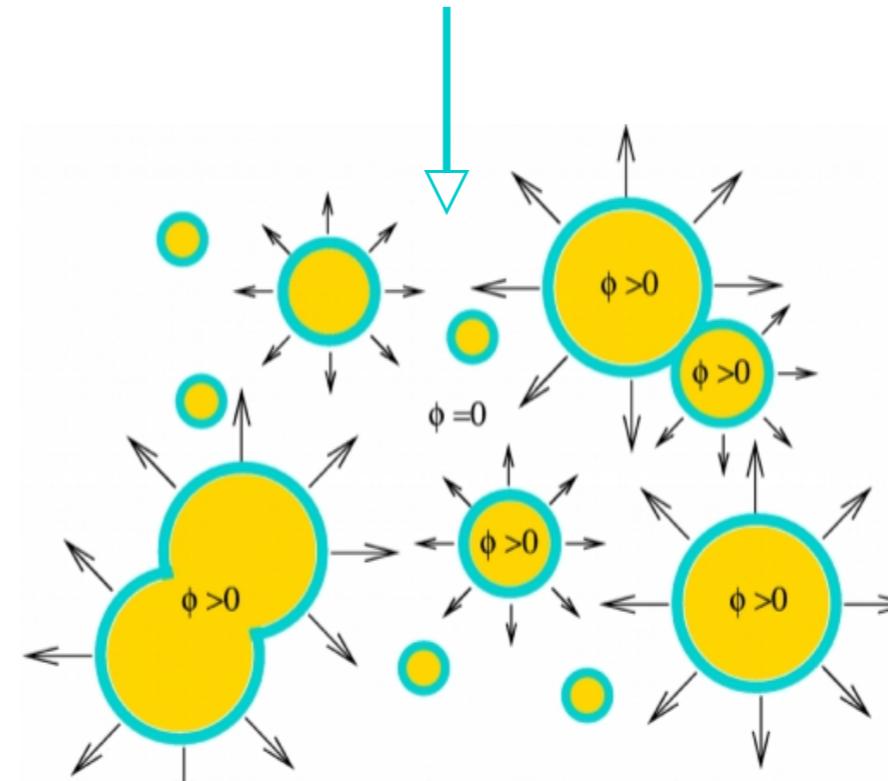
Understanding the EW Epoch

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Gravitational Wave Signal



RECALL
Talk by
David Weir

[courtesy of David Weir]

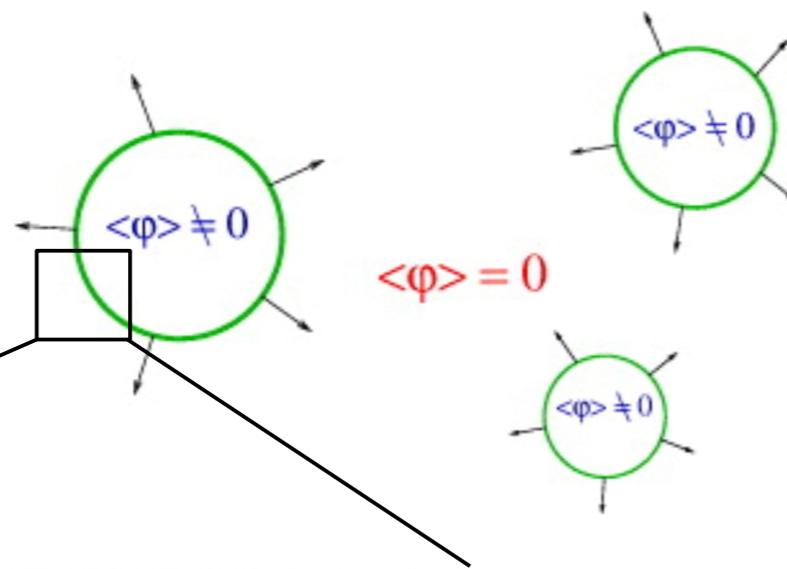
Hindmarsh, Huber, Rummukainen, Weir, PRD **96** (2017) 103520

Sourced by bubble Collisions &
subsequent plasma motions

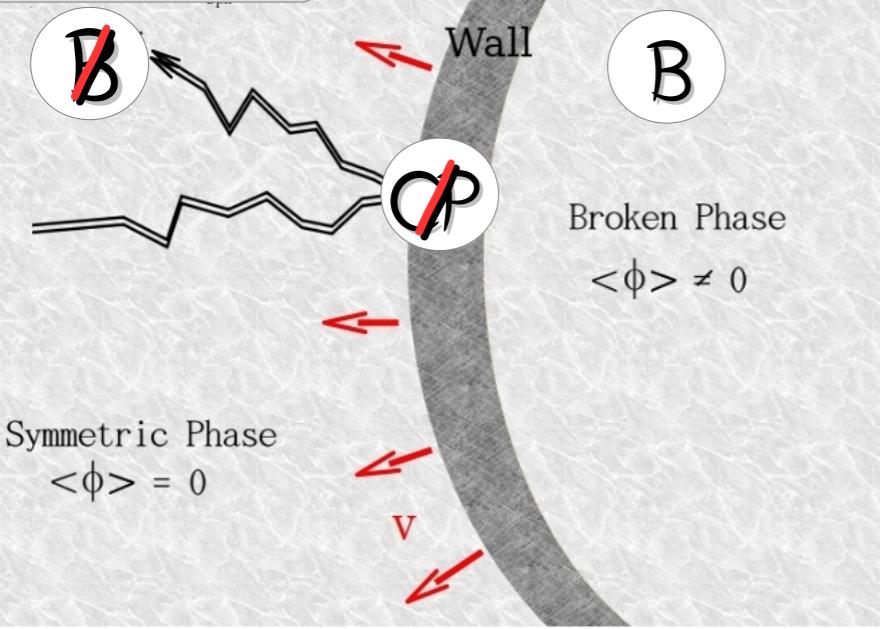
Understanding the EW Epoch

Why?

- Yield Precise knowledge of EWSB in Early Universe
- (Possible) Cosmological Relics from the EW Epoch
- (Possible) Answer to Open Mysteries at Interface Particle Physics
Cosmology



Sphalerons



Matter-Antimatter Asymmetry
► **Baryogenesis**

SAKHAROV CONDITIONS (for dynamical generation of baryon asymmetry)

B Violation Sphalerons

C/CP Violation

Departure from Thermal Equilibrium

EW Phase Transition

Higgs Evolution
in Early Universe



FINITE-TEMPERATURE EFFECTIVE POTENTIAL

$$V_{\text{eff}}(h, T) = V_0(h) + V_0^{\text{loop}}(h) + V_T(h, T)$$

Tree-level
potential

Loop
corrections

Thermal
corrections

(Perturbative) Nature of EWPT

Higgs Evolution in Early Universe



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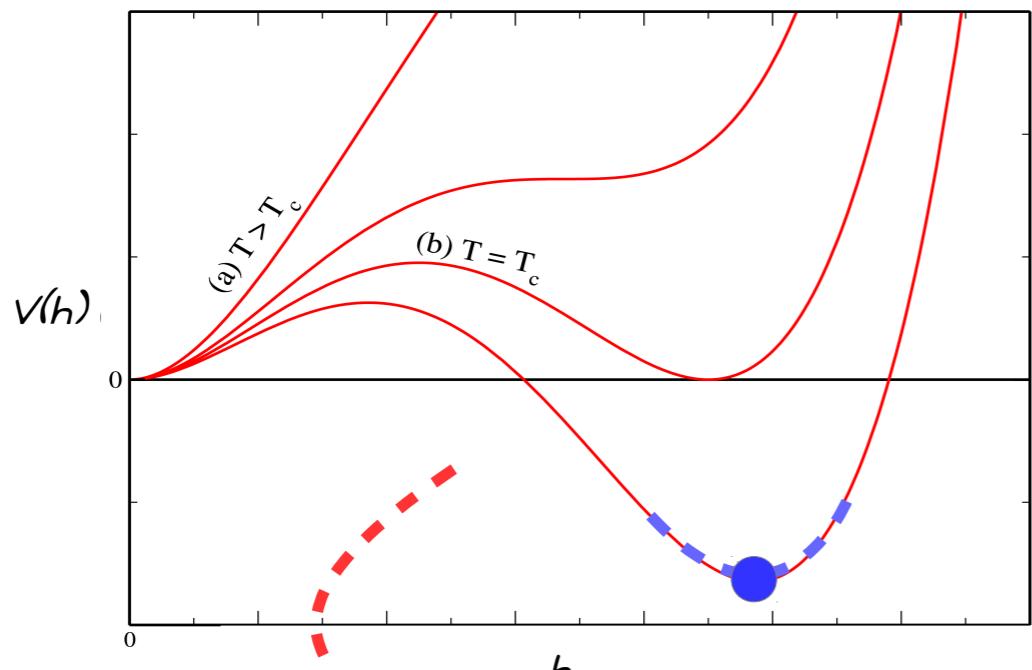
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(Perturbative) Nature of EWPT

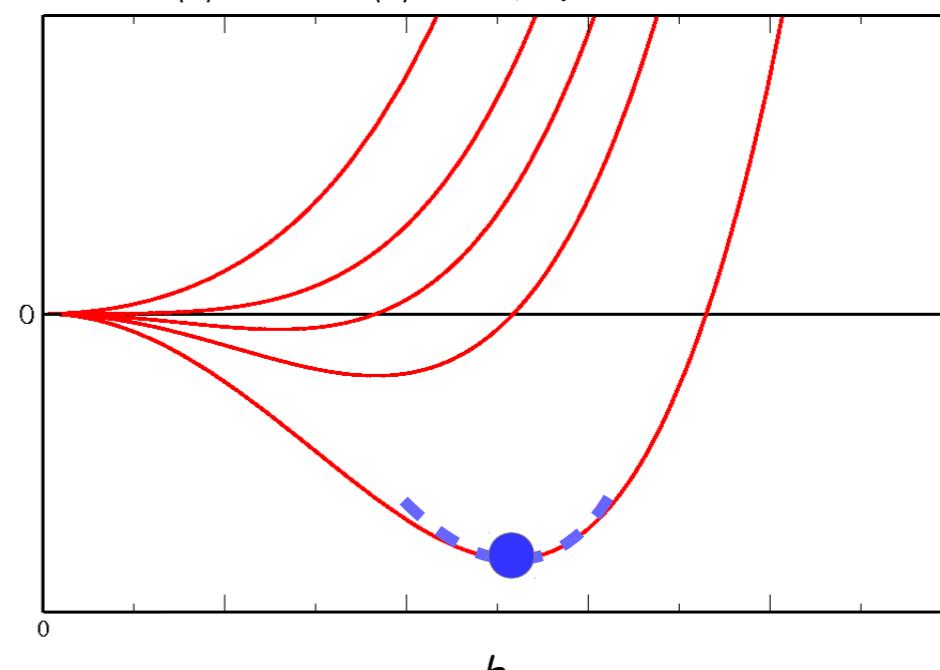
1st Order:

$\langle h \rangle = 0 \rightarrow \langle h \rangle = h(T)$ Discontinuous



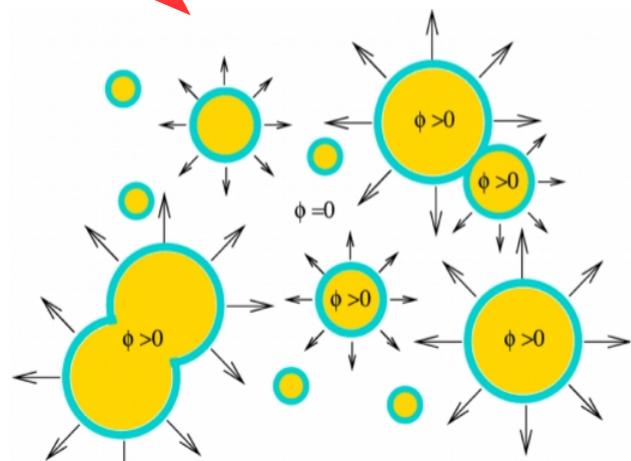
2nd Order:

$\langle h \rangle = 0 \rightarrow \langle h \rangle = h(T)$ Continuous



$v = 246 \text{ GeV}$

$m_h = 125 \text{ GeV}$



Higgs Evolution in Early Universe



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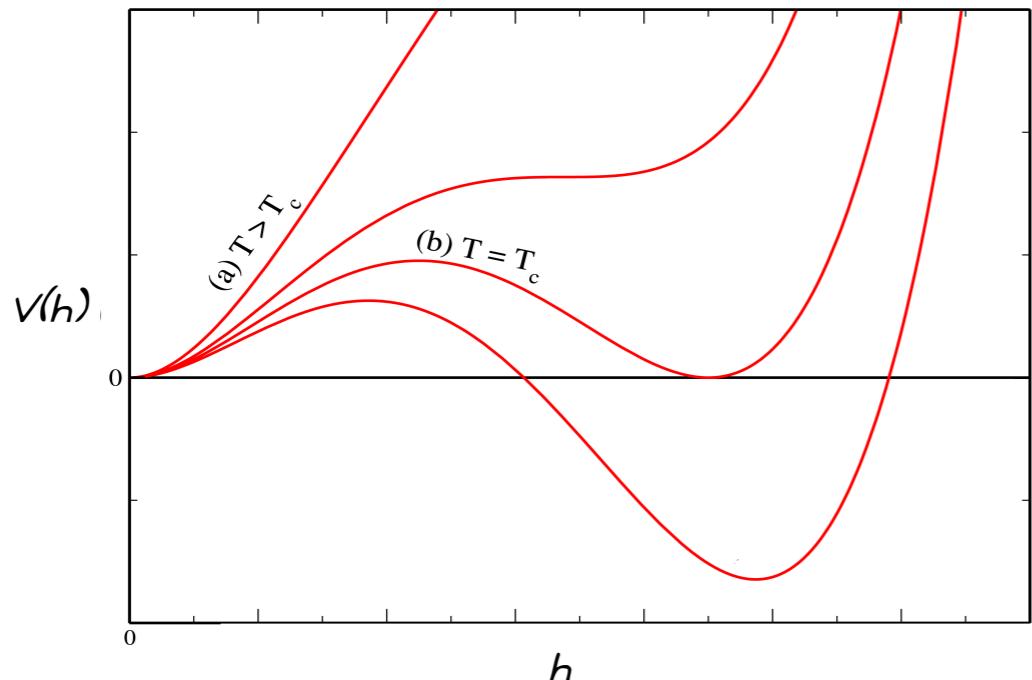
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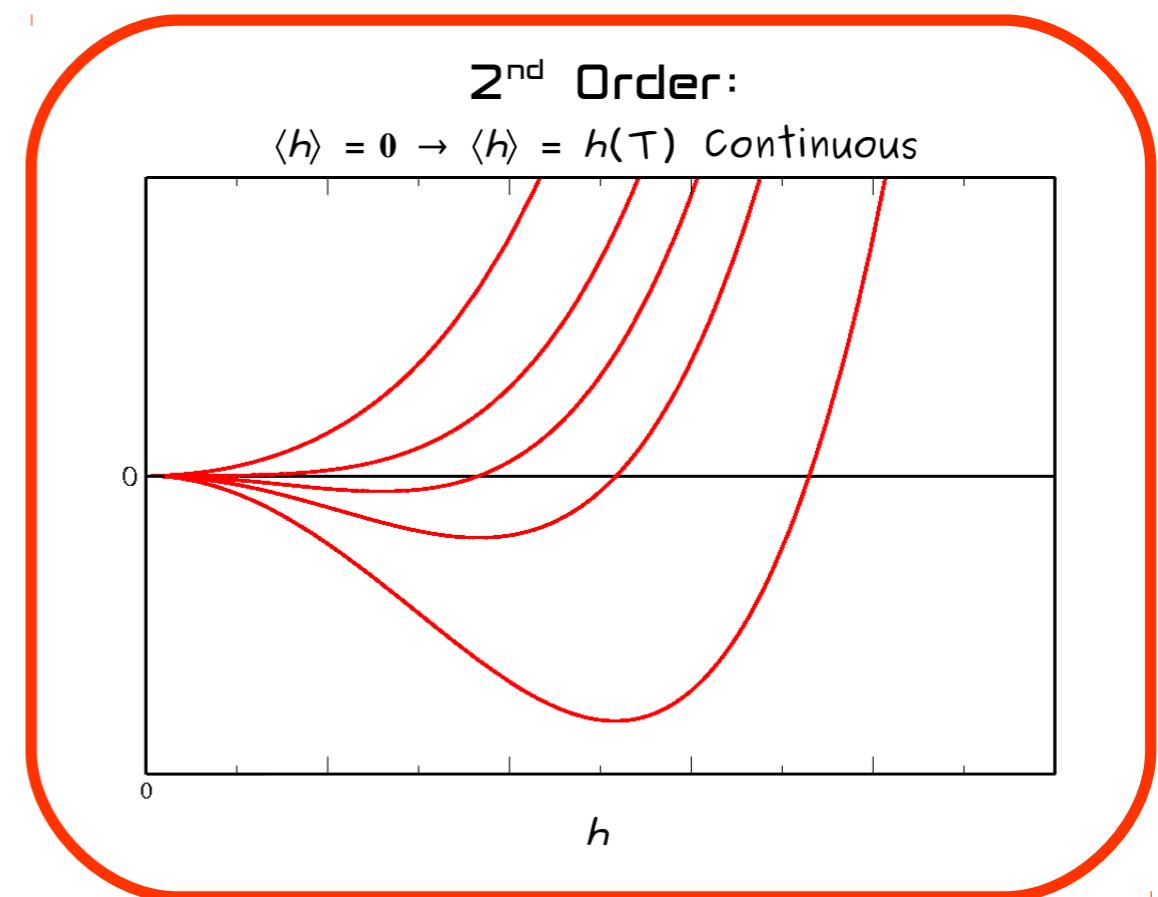
1st Order:

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2nd Order:

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SM : EWPT (non-perturbatively) is Smooth Cross-Over

Kajantie, Laine, Rummukainen, Shaposhnikov, Phys. Rev. Lett. **77** (1996) 2887

Higgs Evolution in Early Universe



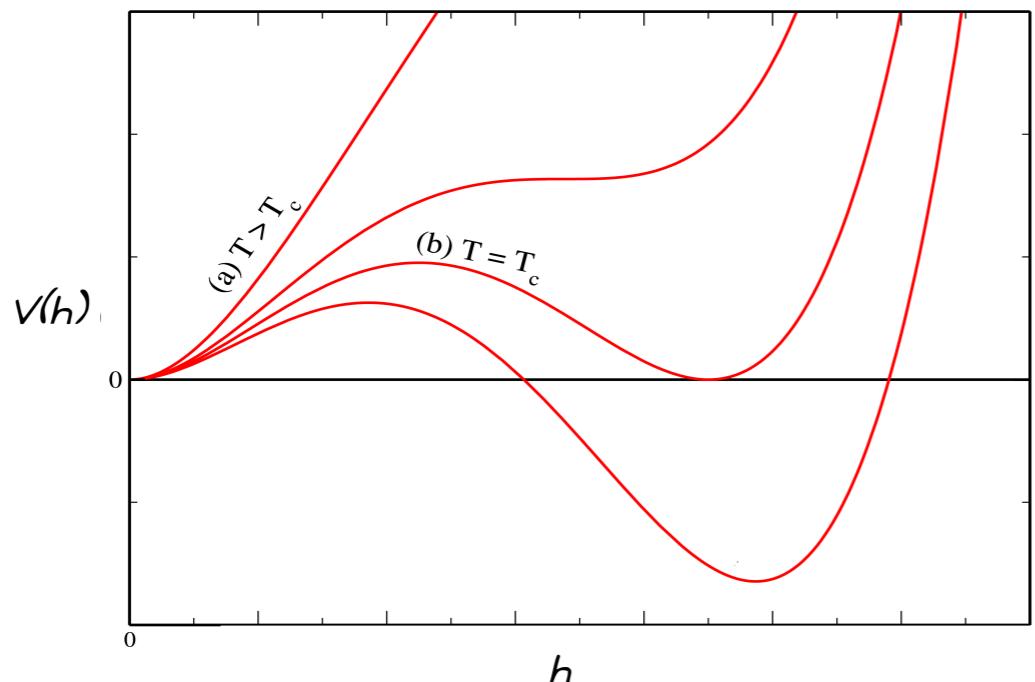
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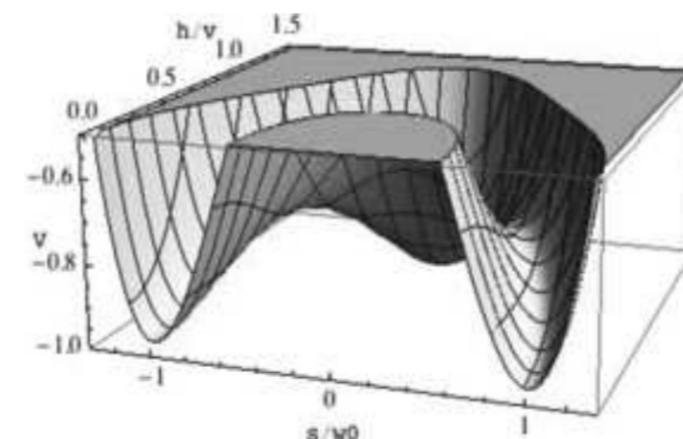
Tree-level
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Non-analytic term $(m^2)^{3/2}$ in $V(h, T)$
from Matsubara Zero-modes
(only present for bosons)

Multiple fields involved in the EWPT
may allow for tree-level potential barrier



BSM: New Physics sizeably coupled to Higgs can
drastically change the EWPT nature

Higgs Evolution in Early Universe



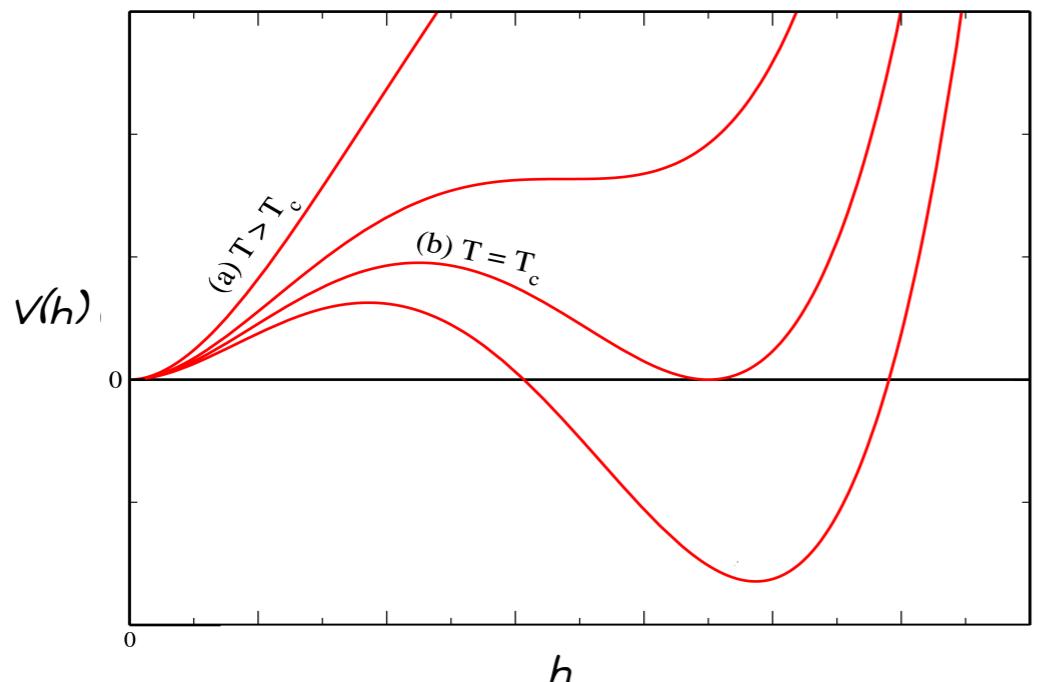
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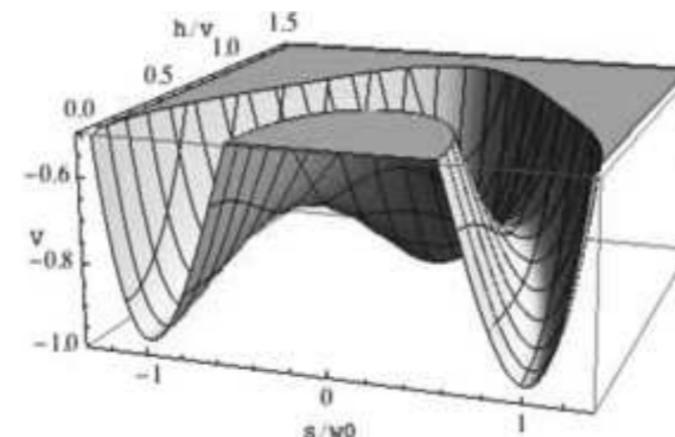
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Multiple fields involved in the EWPT
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BSM: New Physics sizeably coupled to Higgs can
drastically change the EWPT nature

- ▶ New Physics will induce deviations in Higgs couplings
- ▶ New Physics needed close to EW scale

What BSM Scenarios?

Chung, Long, Wang, PRD **87** (2013) 023509

NO Systematic approach for BSM
yielding 1st Order EW Phase Transition



Collider Phenomenology

- ① EFT not possible in general
 - New Particles Present in Thermal plasma → EW Scale
 - New Particles get mass from EWSB

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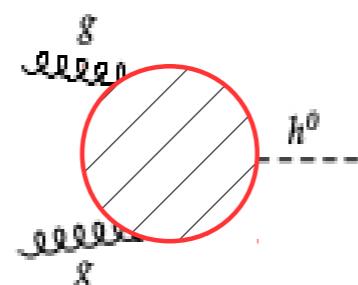
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Collider Phenomenology

- ① EFT not possible in general
 - New Particles Present in Thermal plasma → EW Scale
 - New Particles get mass from EWSB
- ② Models with same EWPT Dynamics & Very Different Collider Phenomenology

e.g. Colored vs Uncolored BSM



What BSM Scenarios?

SM + Scalar Singlet

Espinosa, Quiros 93, Benson 93, Choi, Volkas 93, Vergara 96, Branco, Delepine, Emmanuel-Costa, Gonzalez 98, Ham, Jeong, Oh 04, Ahriche 07, Espinosa, Quiros 07, Profumo, Ramsey-Musolf, Shaughnessy 07, Noble, Perelstein 07, Espinosa, Konstandin, No, Quiros 08, Barger, Langacker, McCaskey, Ramsey-Musolf, Shaughnessy 09, Ashoorioon, Konstandin 09, Das, Fox, Kumar, Weiner 09, Espinosa, Konstandin, Riva 11, Chung, Long 11, Barger, Chung, Long, Wang 12, Huang, Shu, Zhang 12, Fairbairn, Hogan 13, Katz, Perelstein 14, Profumo, Ramsey-Musolf, Wainwright, Winslow 14, Jiang, Bian, Huang, Shu 15, Kozaczuk 15, Cline, Kainulainen, Tucker-Smith 17, Kurup, Perelstein 17, Chen, Kozaczuk, Lewis 17, Gould, Kozaczuk, Niemi, Ramsey-Musolf, Tenkanen, Weir 19...

SM + Scalar Doublet
(2HDM)

Turok, Zadrozny 92, Davies, Froggatt, Jenkins, Moorhouse 94, Cline, Lemieux 97, Huber 06, Froome, Huber, Seniuch 06, Cline, Kainulainen, Trott 11, Dorsch, Huber, No 13, Dorsch, Huber, Mimasu, No 14, Basler, Krause, Muhlleitner, Wittbrodt, Wlotzka 16, Dorsch, Huber, Mimasu, No 17, Bernon, Bian, Jiang 17, Andersen, Gorda, Helset, Niemi, Tenkanen, Tranberg, Vuorinen, Weir 18...

SM + Scalar Triplet

Patel, Ramsey-Musolf 12, Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir 18 ...

MSSM

Carena, Quiros, Wagner 96, Delepine, Gerard, Gonzalez Felipe, Weyers 96, Cline, Kainulainen 96, Laine, Rummukainen 98, Carena, Nardini, Quiros, Wagner 09, Cohen, Morrissey, Pierce 12, Curtin, Jaiswal, Meade 12, Carena, Nardini, Quiros, Wagner 13, Katz, Perelstein, Ramsey-Musolf, Winslow 14...

NMSSM...

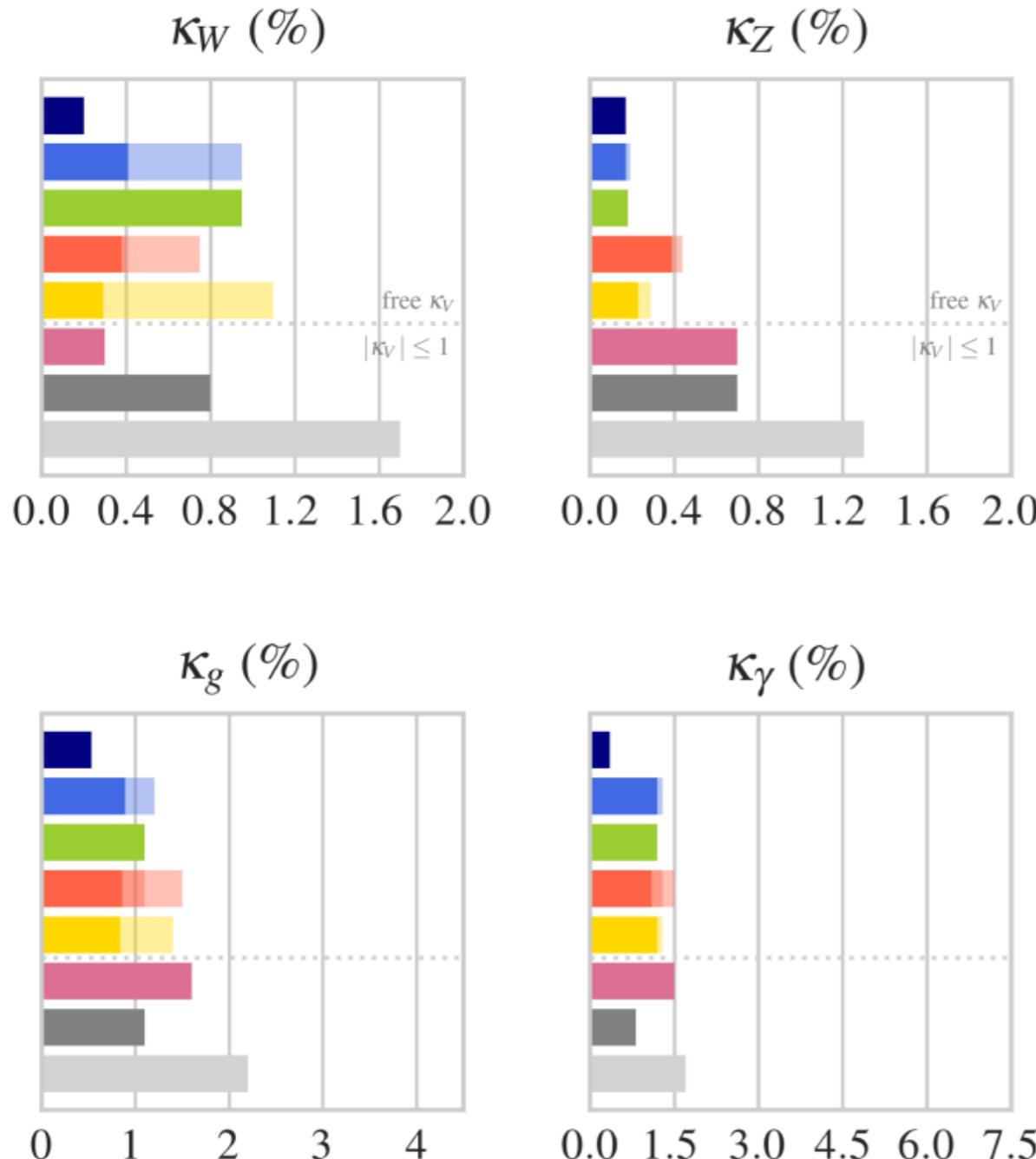
Pietroni 93, Davies, Froggatt, Moorhouse 95, Huber, Schmidt 01, Ham, Oh, Kim, Yoo, Son 04, Menon, Morrissey, Wagner 04, Funakubo, Tao, Yokoda 05, Huber, Konstandin, Prokopec, Schmidt 07, Chung, Long 10, Kozaczuk, Profumo, Stephenson Haskins, Wainwright 15...

EFT Approach (H^6)

Grojean, Servant, Wells 05, Bodeker, Froome, Huber, Seniuch 05, Huang, Joglekar, Li, Wagner 15...

What BSM Signatures?

Indirect Probes (Higgs couplings)



ECFA Higgs Study Group, 2019
(for the ESPP Update)

Higgs@FC WG

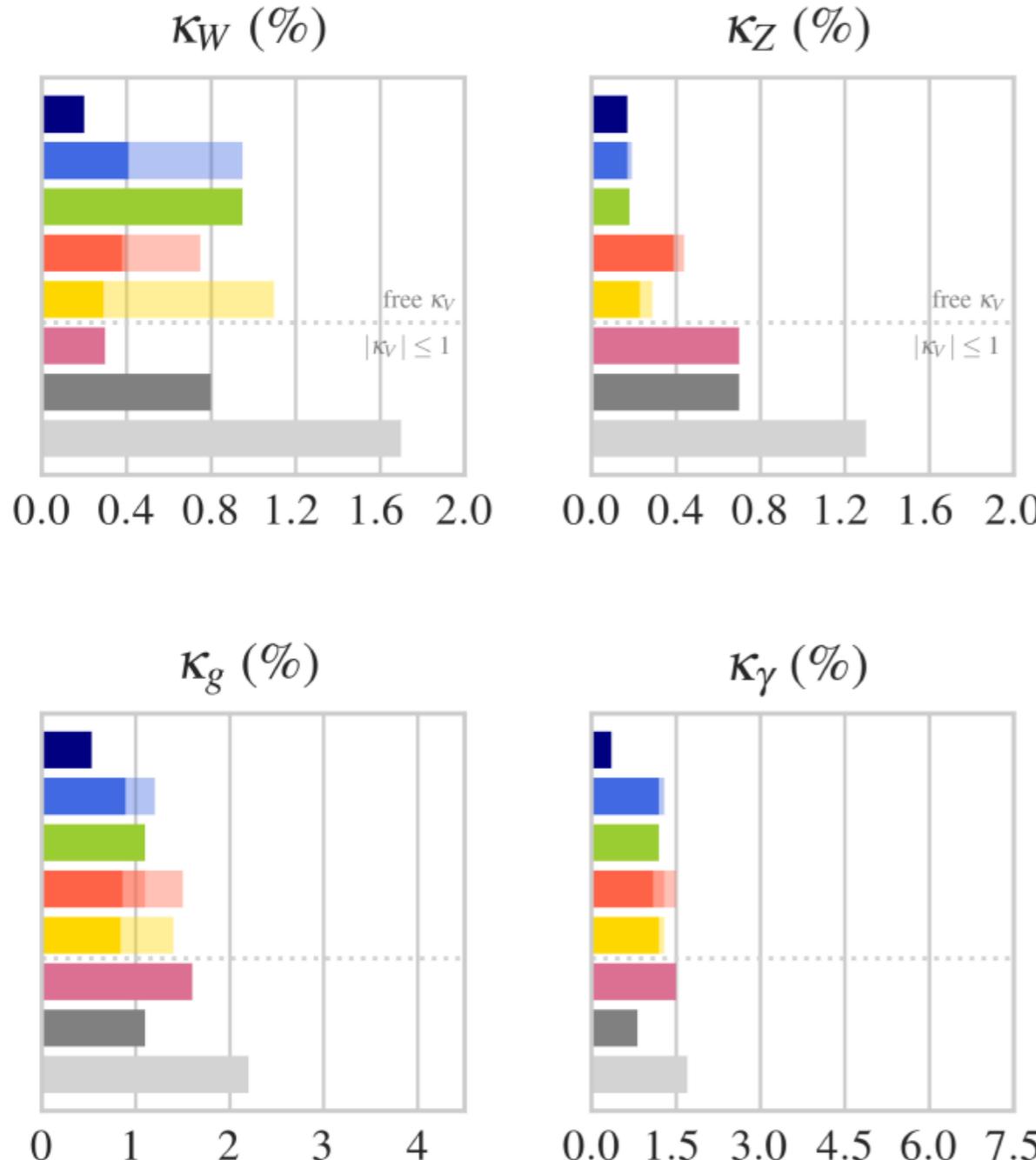
Kappa-3, May 2019

FCC-ee+FHCC-eh+FCC-hh	CLIC ₃₈₀
FCC-ee ₃₆₅ +FCC-ee ₂₄₀	ILC ₅₀₀ +ILC ₃₅₀ +ILC ₂₅₀
FCC-ee ₂₄₀	ILC ₂₅₀
CEPC	LHeC ($ \kappa_V \leq 1$)
CLIC ₃₀₀₀ +CLIC ₁₅₀₀ +CLIC ₃₈₀	HE-LHC ($ \kappa_V \leq 1$)
CLIC ₁₅₀₀ +CLIC ₃₈₀	HL-LHC ($ \kappa_V \leq 1$)

[courtesy of Christophe Grojean]

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Kappa-3, May 2019	
FCC-ee+eh+hh	CLIC ₃₈₀
FCC-ee ₃₆₅ +ee ₂₄₀	ILC ₅₀₀ +ILC ₃₅₀ +ILC ₂₅₀
FCC-ee ₂₄₀	ILC ₂₅₀
CEPC	LHeC ($ \kappa_V \leq 1$)
CLIC ₃₀₀₀ +CLIC ₁₅₀₀ +CLIC ₃₈₀	HE-LHC ($ \kappa_V \leq 1$)
CLIC ₁₅₀₀ +CLIC ₃₈₀	HL-LHC ($ \kappa_V \leq 1$)

[courtesy of Christophe Grojean]

Scenario	BR_{inv}	BR_{unt}	include HL-LHC
kappa-3	measured	measured	yes

What BSM Signatures?

Indirect Probes (Higgs couplings)



ECFA Higgs Study Group, 2019
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Higgs@FC WG

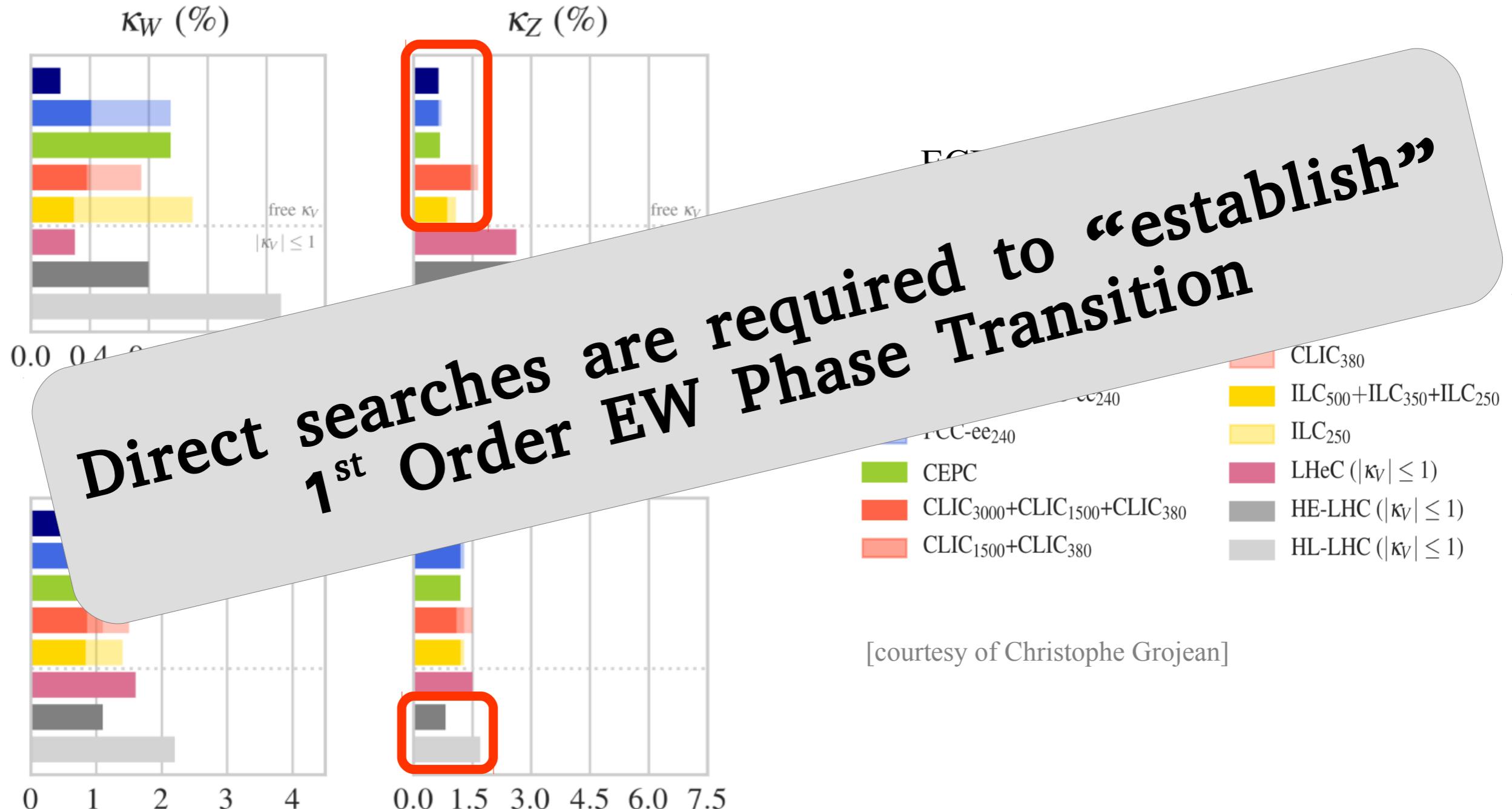
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FCC-ee+FCC-eh+FCC-hh	CLIC ₃₈₀
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[courtesy of Christophe Grojean]

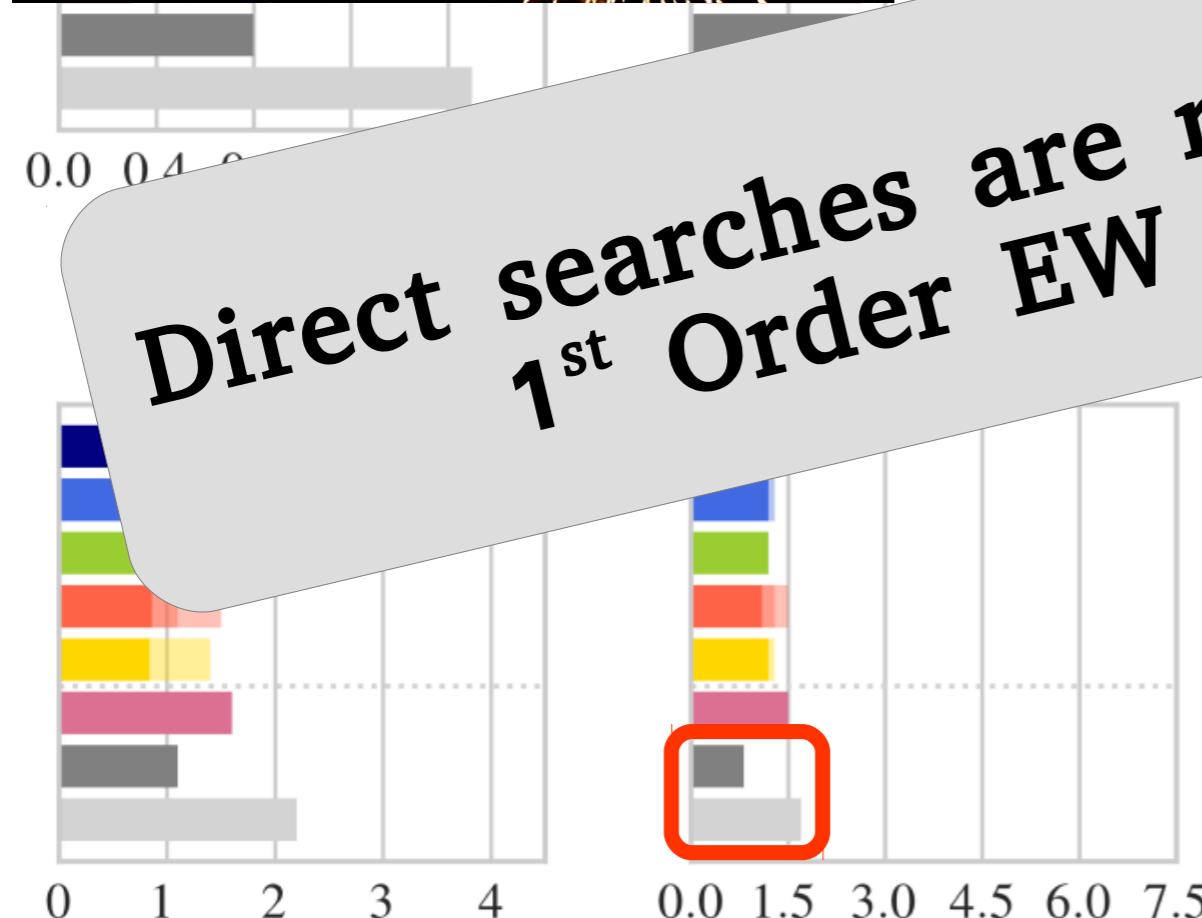
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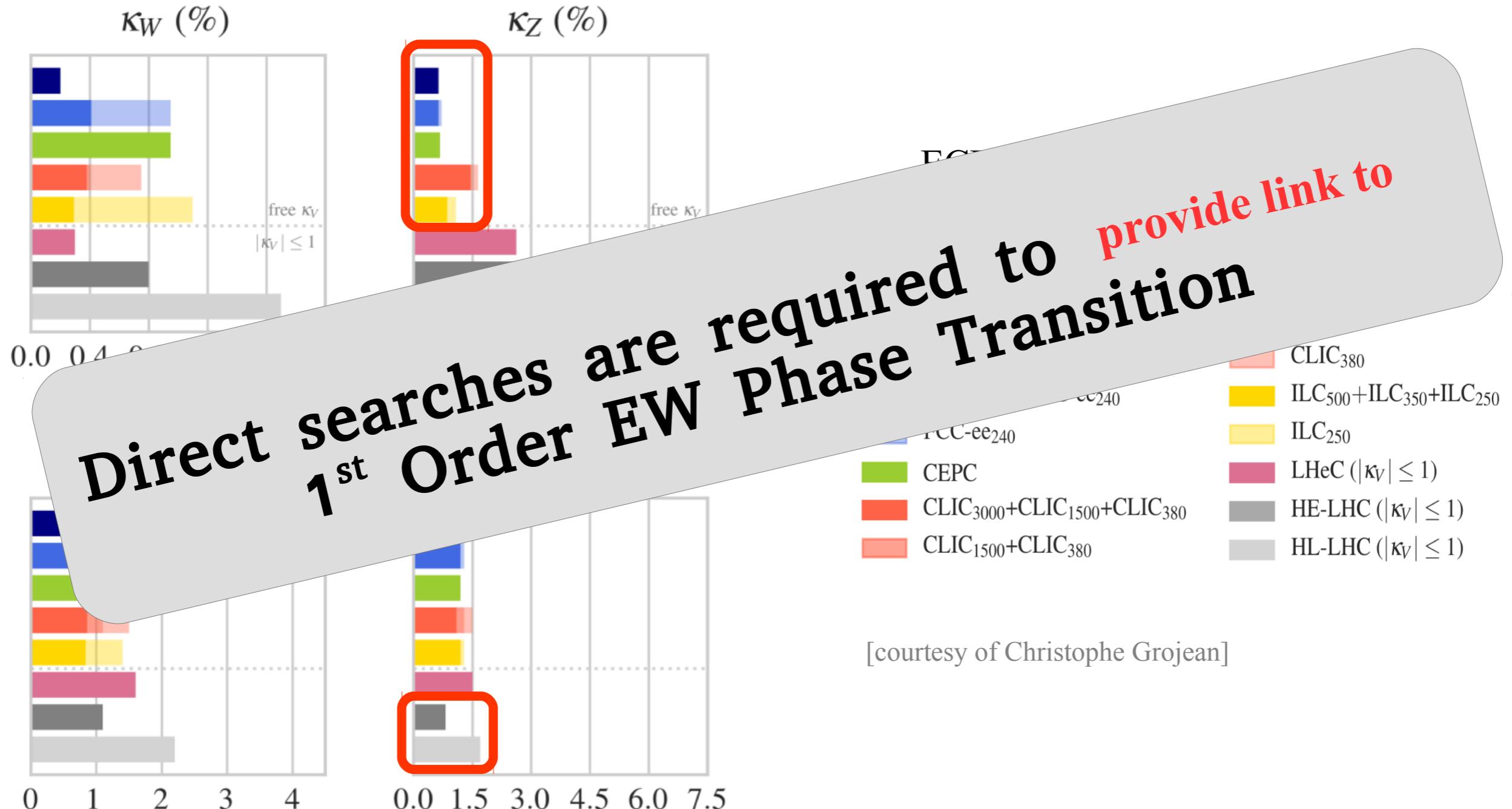


Direct searches are required to “establish”
1st Order EW Phase Transition



What BSM Signatures?

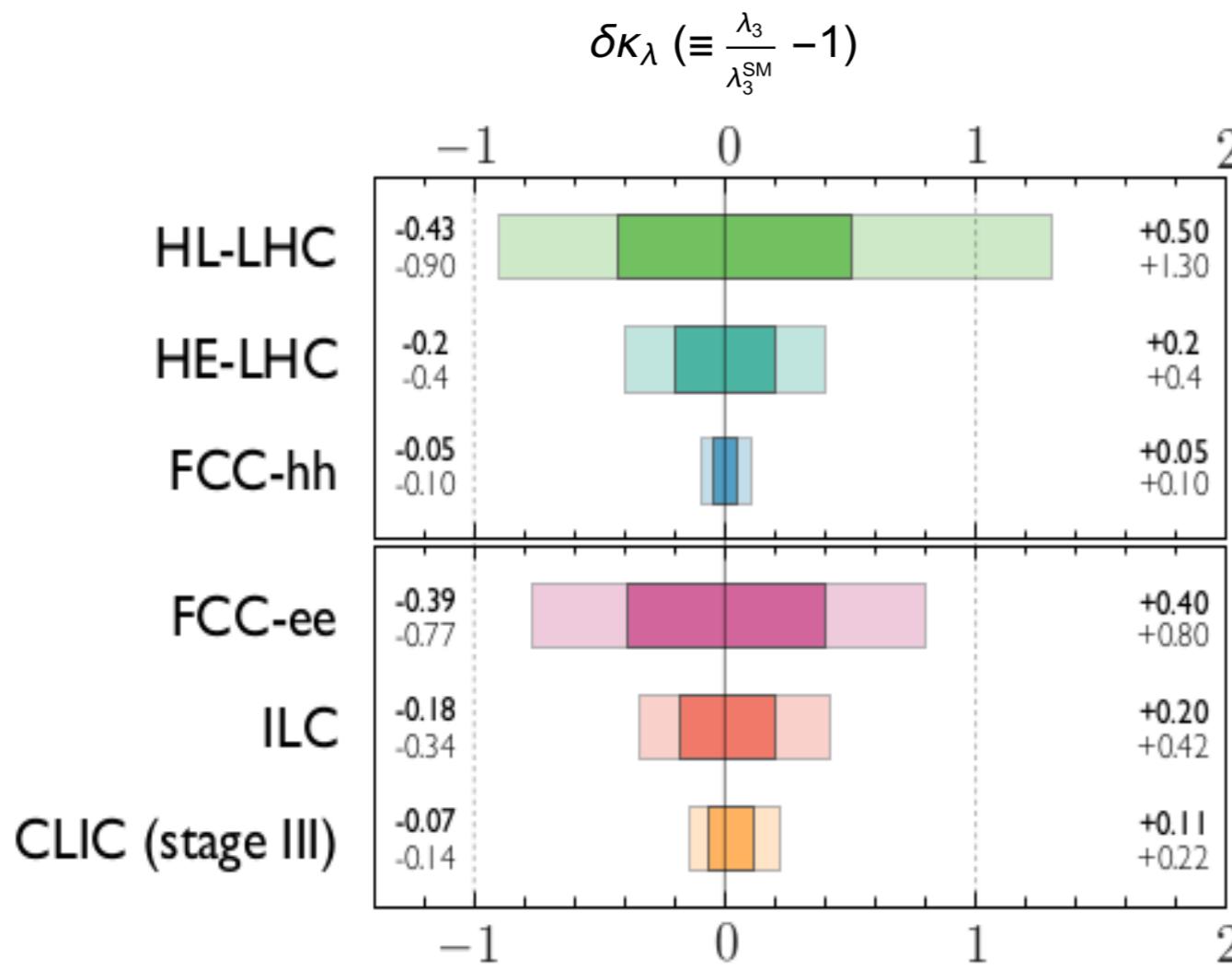
Indirect Probes (Higgs couplings)



What BSM Signatures?

“Indirect” Probe: **Higgs self-coupling**

ECFA Higgs Study Group, 2019
(for the ESPP Update)

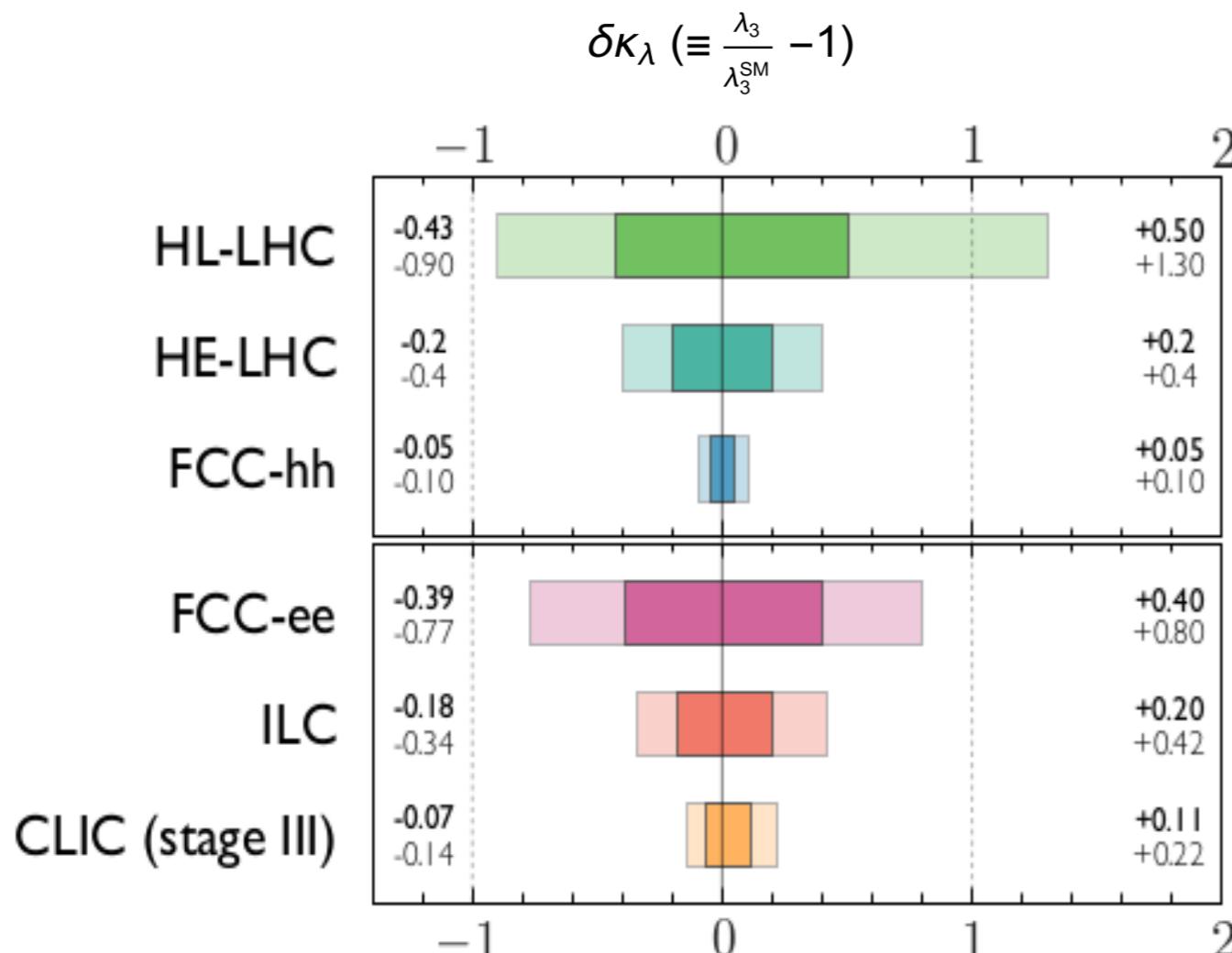


Dark: 68%CL, Light: 95%CL

What BSM Signatures?

“Indirect” Probe: **Higgs self-coupling**

ECFA Higgs Study Group, 2019
(for the ESPP Update)



Also in this case, NP may manifest itself via direct signatures!

Dark: 68%CL, Light: 95%CL

EWPT Scenarios within LHC Reach



EWPT Scenarios within LHC Reach

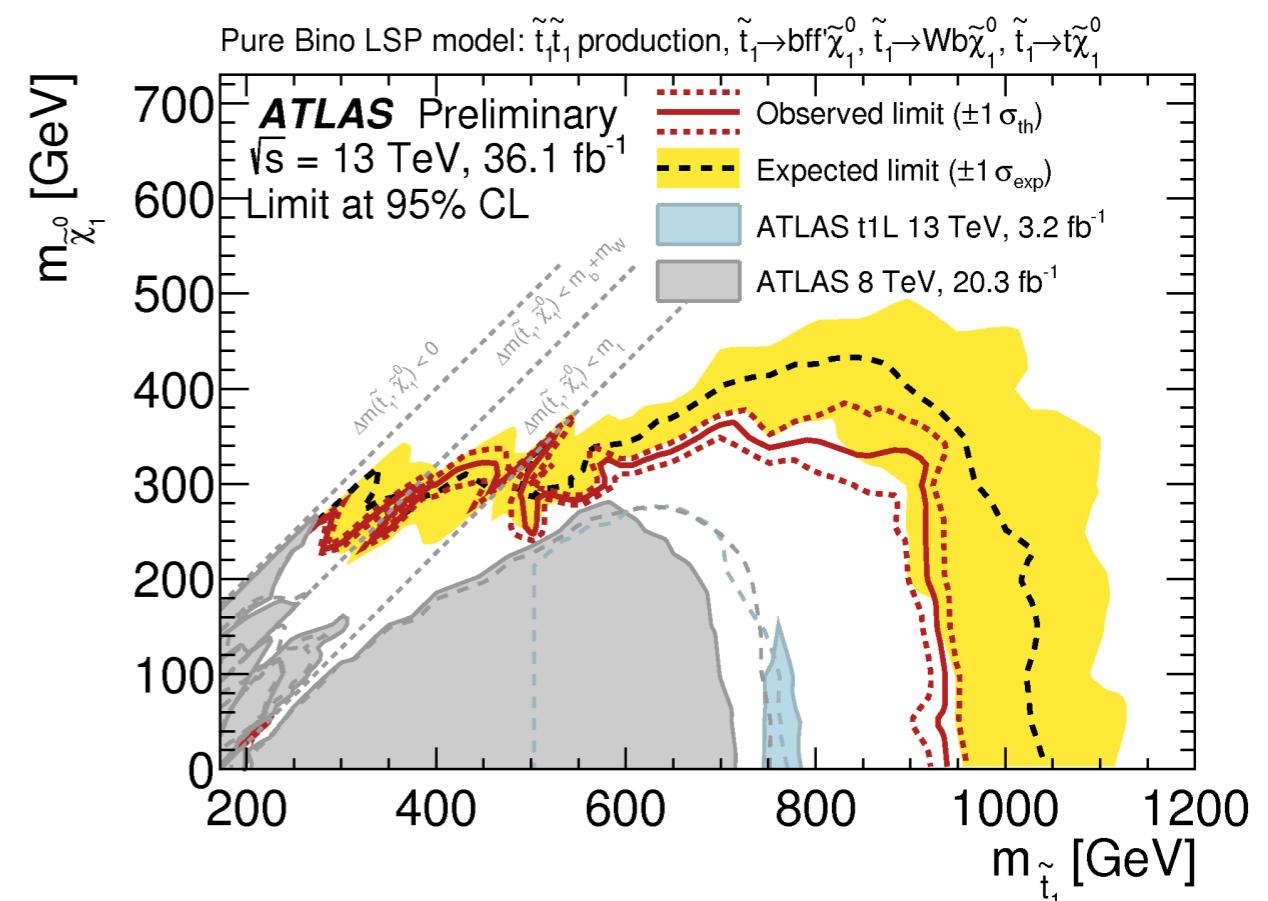
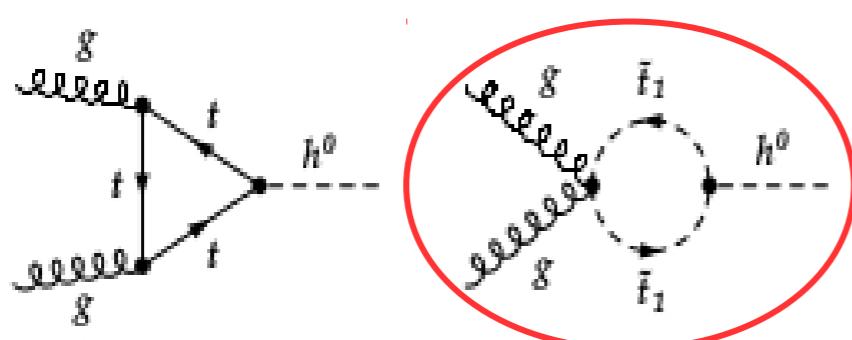


▷ MSSM (light stop scenario)



[courtesy of Kimmo Kainulainen]

Large Deviations from SM Higgs Signal Strengths **due to light stops**



EWPT Scenarios within LHC Reach



▷ NON-MINIMAL HIGGS SECTOR

e.g. **2HDM**

$$\begin{aligned} V(H_1, H_2) = & \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 - \mu^2 [H_1^\dagger H_2 + \text{h.c.}] \\ & + \frac{\lambda_1}{2} |H_1|^4 + \frac{\lambda_2}{2} |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 \\ & + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} \left[(H_1^\dagger H_2)^2 + \text{h.c.} \right] \end{aligned}$$

EWPT Scenarios within LHC Reach



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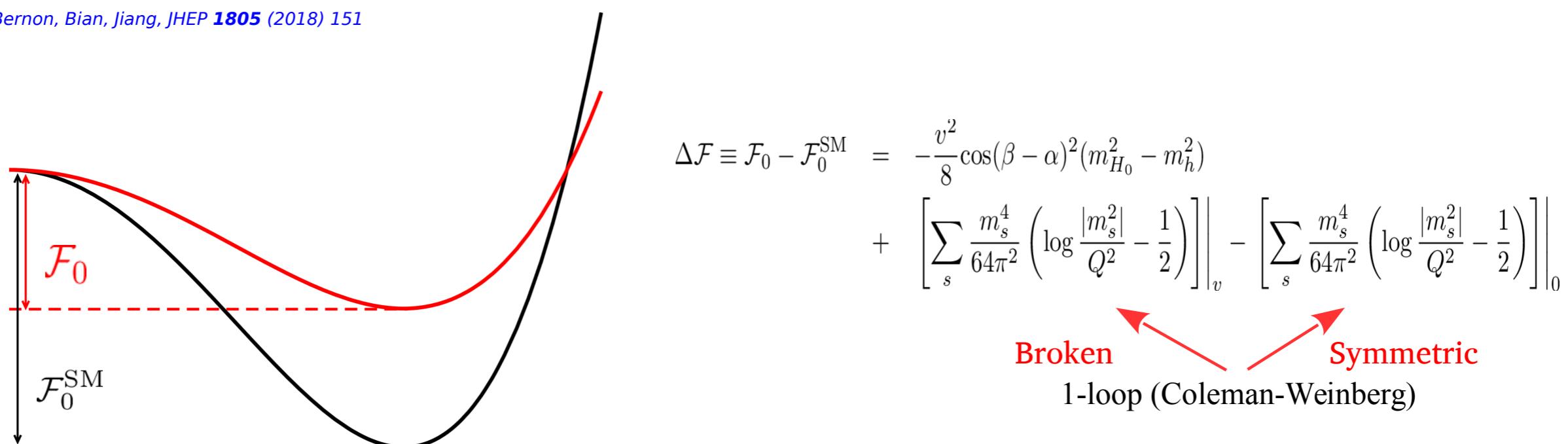
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 \end{aligned}$$

Nature of EWPT dominantly controlled by
T=0 Vacuum energy difference

*Dorsch, Huber, Mimasu, JMN, JHEP **1712** (2017) 086*

*Bernon, Bian, Jiang, JHEP **1805** (2018) 151*



EWPT Scenarios within LHC Reach



▷ NON-MINIMAL HIGGS SECTOR

e.g. **2HDM**

$$m_{H_0, A_0, H^\pm}^2 = \mu^2 + \lambda_i v^2$$

Difference between Symmetric - Broken phase in CW piece guaranteed for large BSM mass splitting!

$$m_{A_0} - m_{H_0}$$

$$\begin{aligned} \Delta \mathcal{F} \equiv \mathcal{F}_0 - \mathcal{F}_0^{\text{SM}} &= -\frac{v^2}{8} \cos(\beta - \alpha)^2 (m_{H_0}^2 - m_h^2) \\ &+ \left[\sum_s \frac{m_s^4}{64\pi^2} \left(\log \frac{|m_s^2|}{Q^2} - \frac{1}{2} \right) \right]_v - \left[\sum_s \frac{m_s^4}{64\pi^2} \left(\log \frac{|m_s^2|}{Q^2} - \frac{1}{2} \right) \right]_0 \end{aligned}$$

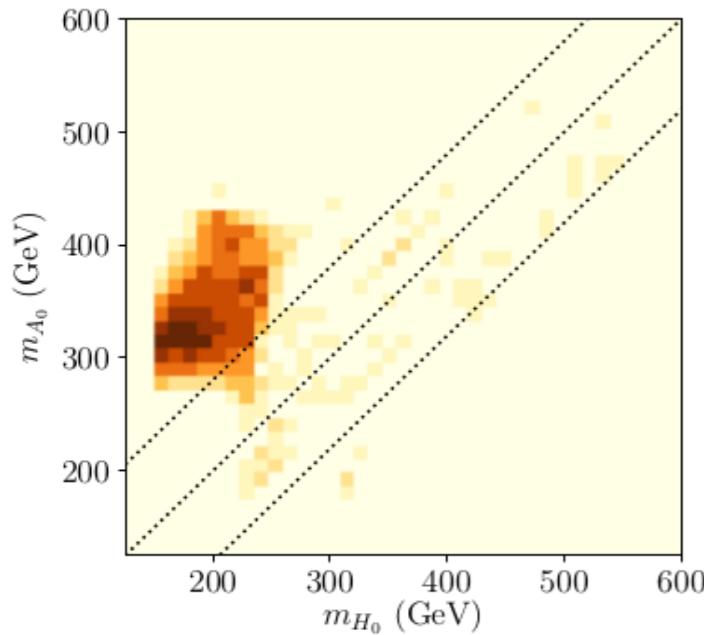
Broken Symmetric
1-loop (Coleman-Weinberg)

EWPT Scenarios within LHC Reach

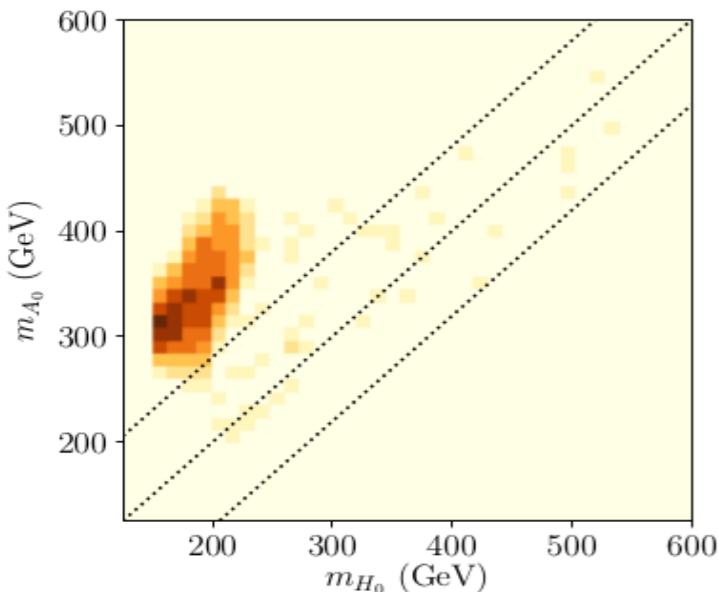


► NON-MINIMAL HIGGS SECTOR

e.g. **2HDM**



(b) $\tan(\beta) = 2.0$



(c) $\tan(\beta) = 2.5$

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EWPT Scenarios within LHC Reach



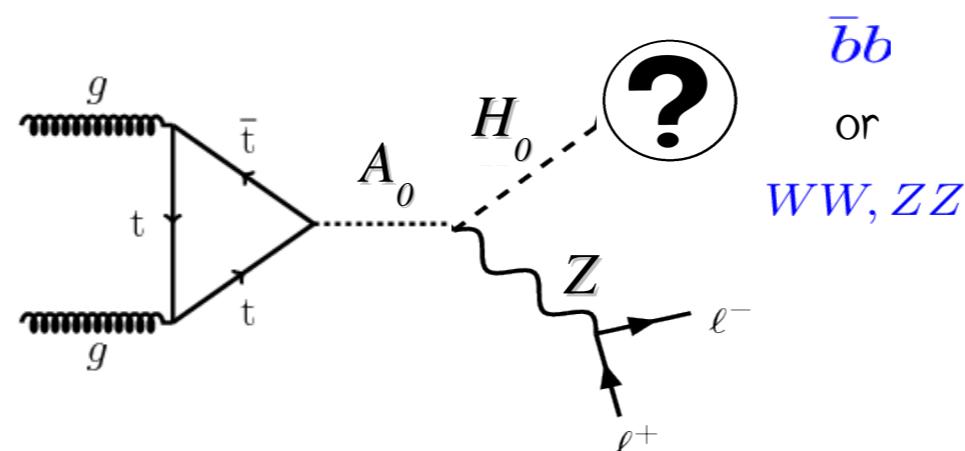
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$$m_{A_0} - m_{H_0} \sim v$$

Search for 2HDM 1st Order EWPT region via $A_0 \rightarrow H_0 Z$

Dorsch, Huber, Mimasu, JMN, Phys. Rev. Lett. 113 (2014) 211802



EWPT Scenarios within LHC Reach



▷ NON-MINIMAL HIGGS SECTOR

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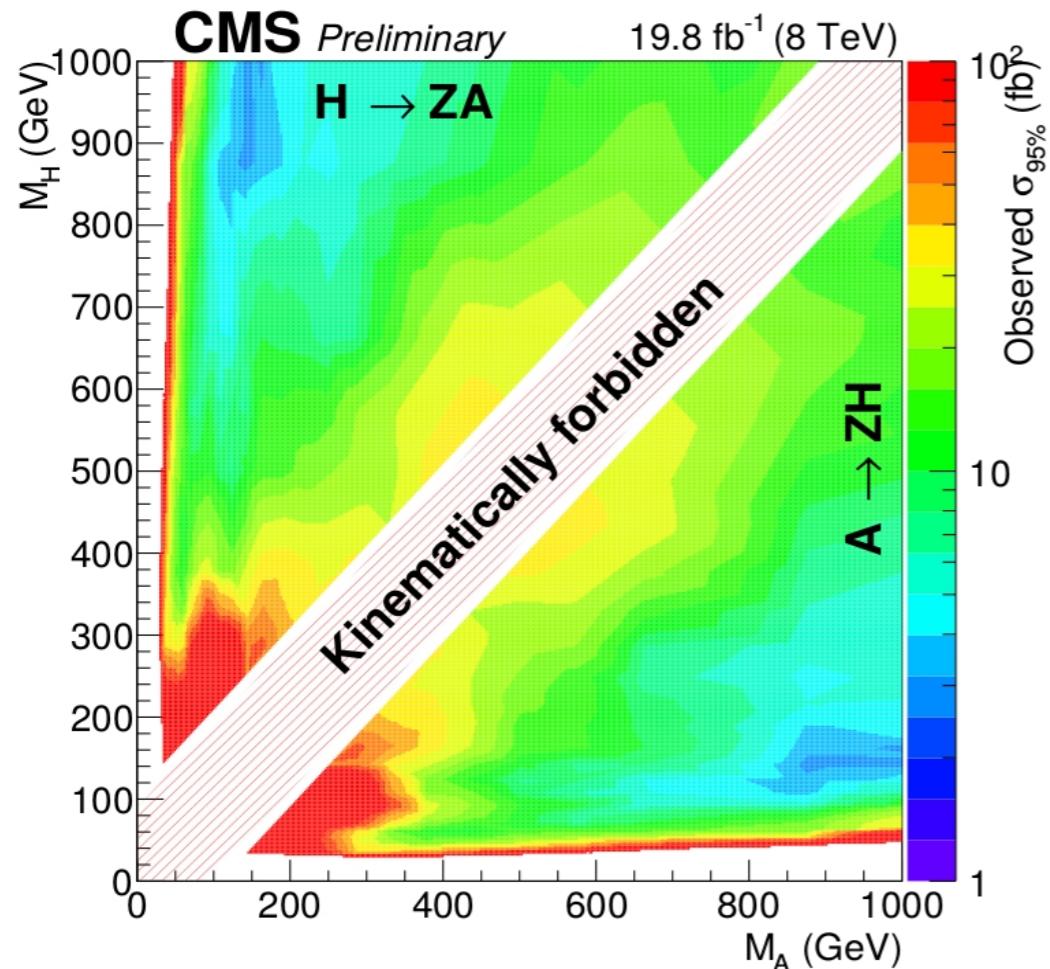
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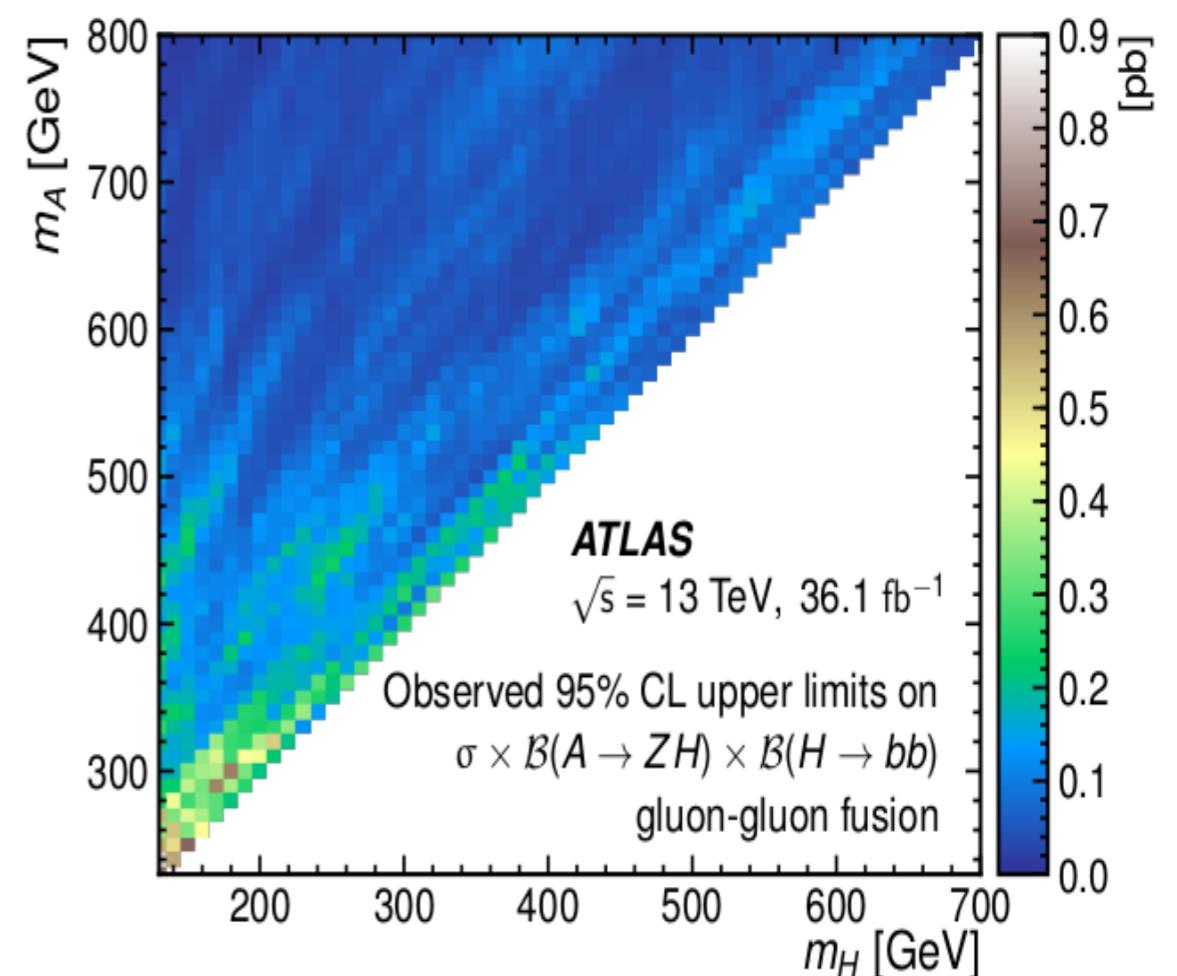
Dorsch, Huber, Mimasu, JMN, Phys. Rev. Lett. **113** (2014) 211802

CMS-PAS-HIG-15-001 ([1603.02991](#))

Search for H/A decaying into Z and A/H, with $Z \rightarrow \ell\ell$ and
 $A/H \rightarrow bb$ or $A/H \rightarrow \tau\tau$



ATLAS-PHYS-EXO-16-034 ([1804.01126](#))



EWPT Scenarios within LHC Reach



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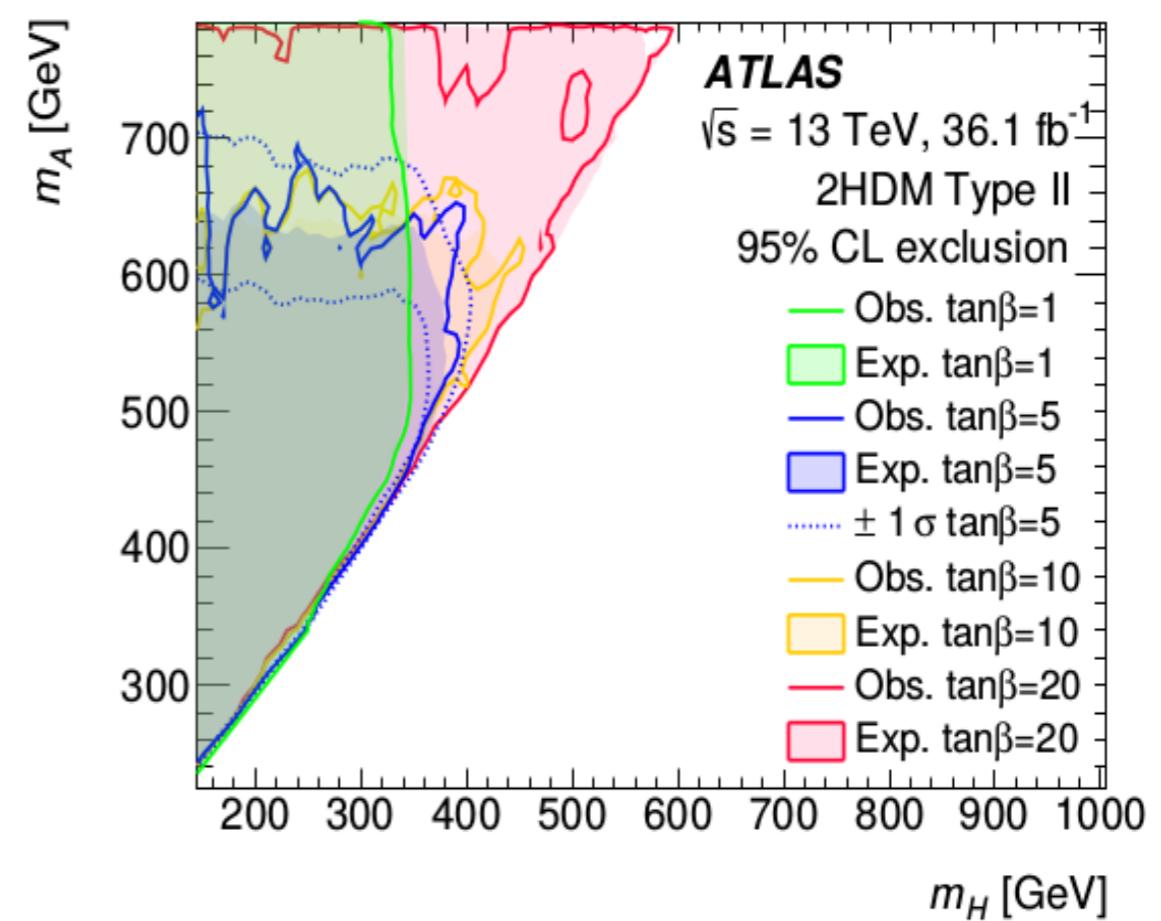
Search for 2HDM 1st Order EWPT region via $A_O \rightarrow H_O Z$

Dorsch, Huber, Mimasu, JMN, Phys. Rev. Lett. **113** (2014) 211802

Very strong LHC 13 TeV limits on 2HDM EWPT!



[courtesy of Kimmo Kainulainen]



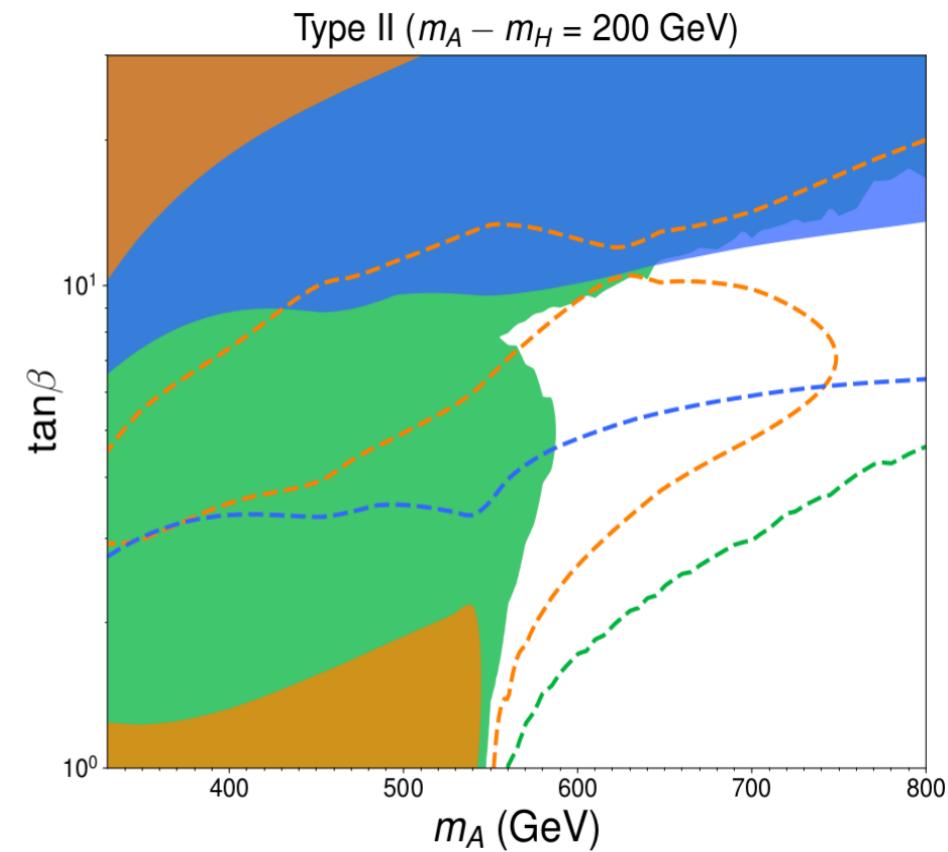
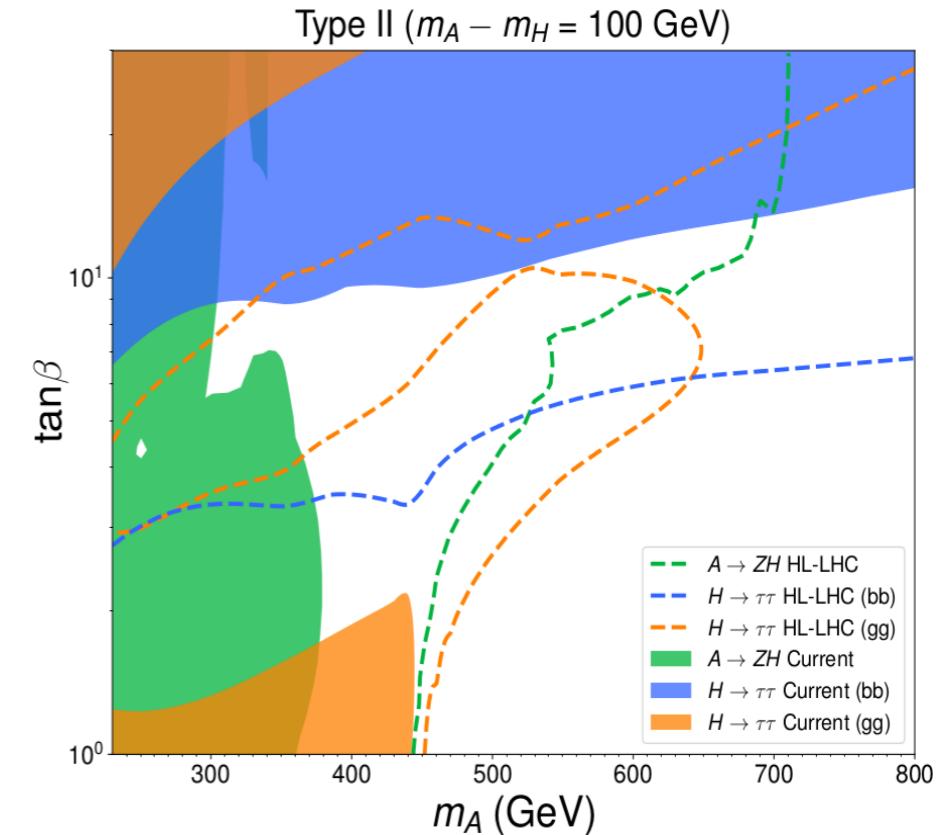
EWPT Scenarios within LHC Reach

for *Higgs Physics at HL-LHC & HE-LHC*
Report, 2019 (by K.Mimasu, JMN)

▷ NON-MINIMAL HIGGS SECTOR

e.g. **2HDM**

**HL-LHC will fully explore
2HDM EWPT**



EWPT Scenarios within LHC Reach?

▷ SM + SCALAR EW MULTIPLET

e.g. **EW Triplet**

*Fileviez Perez, Patel, Ramsey-Musolf, Wang, PRD **79** (2009) 055024*

*Patel, Ramsey-Musolf, PRD **88** (2013) 035013*

$$V_{H\Sigma} = \frac{a_1}{2} H^\dagger \Sigma H + \frac{a_2}{2} H^\dagger H \text{ Tr } \Sigma^2$$

EWPT Scenarios within LHC Reach?

▷ SM + SCALAR EW MULTIPLET

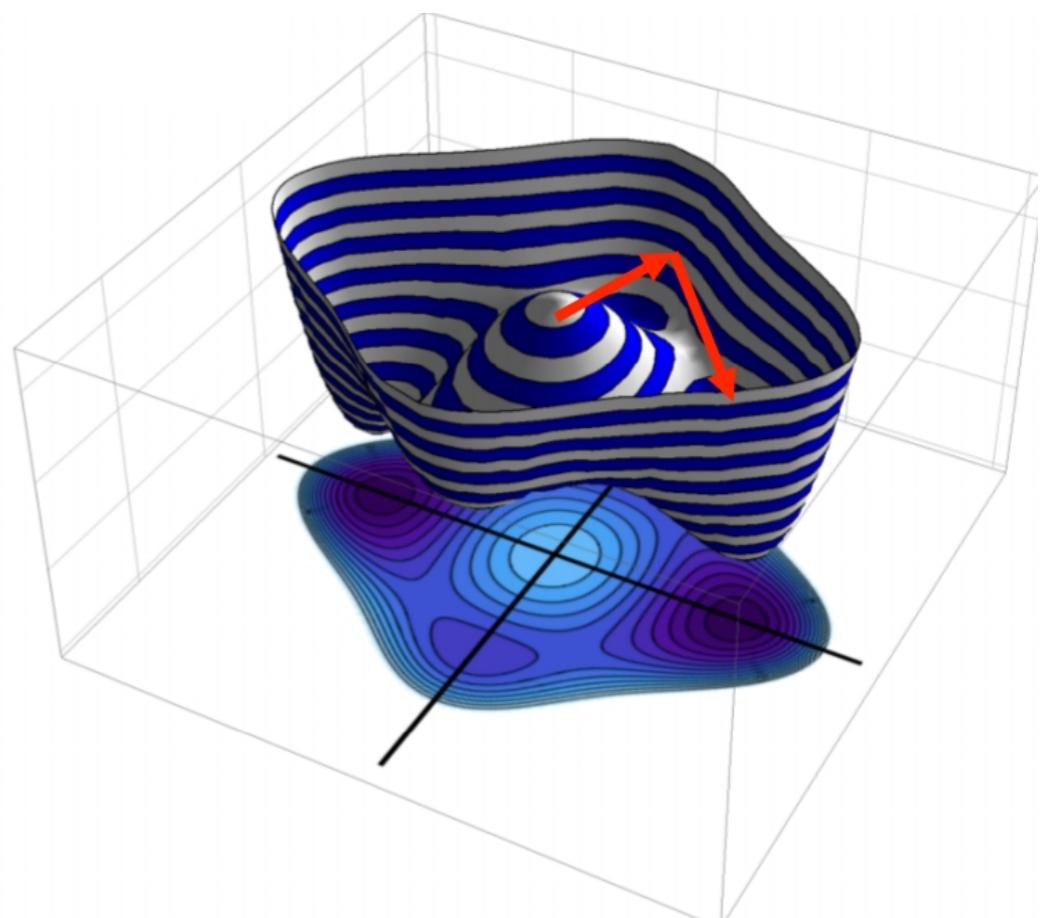
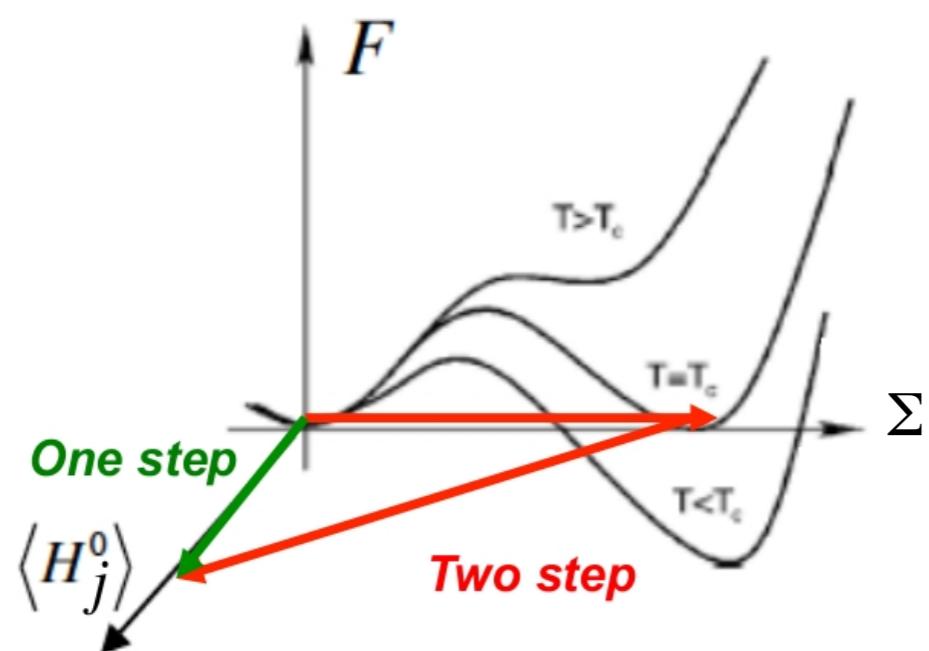
e.g. **EW Triplet**

Fileviez Perez, Patel, Ramsey-Musolf, Wang, PRD **79** (2009) 055024

Patel, Ramsey-Musolf, PRD **88** (2013) 035013

$$V_{H\Sigma} = \frac{a_1}{2} H^\dagger \Sigma H + \frac{a_2}{2} H^\dagger H \text{Tr } \Sigma^2$$

Possible multi-step EWPT



[courtesy of Michael Ramsey-Musolf]

EWPT Scenarios within LHC Reach?

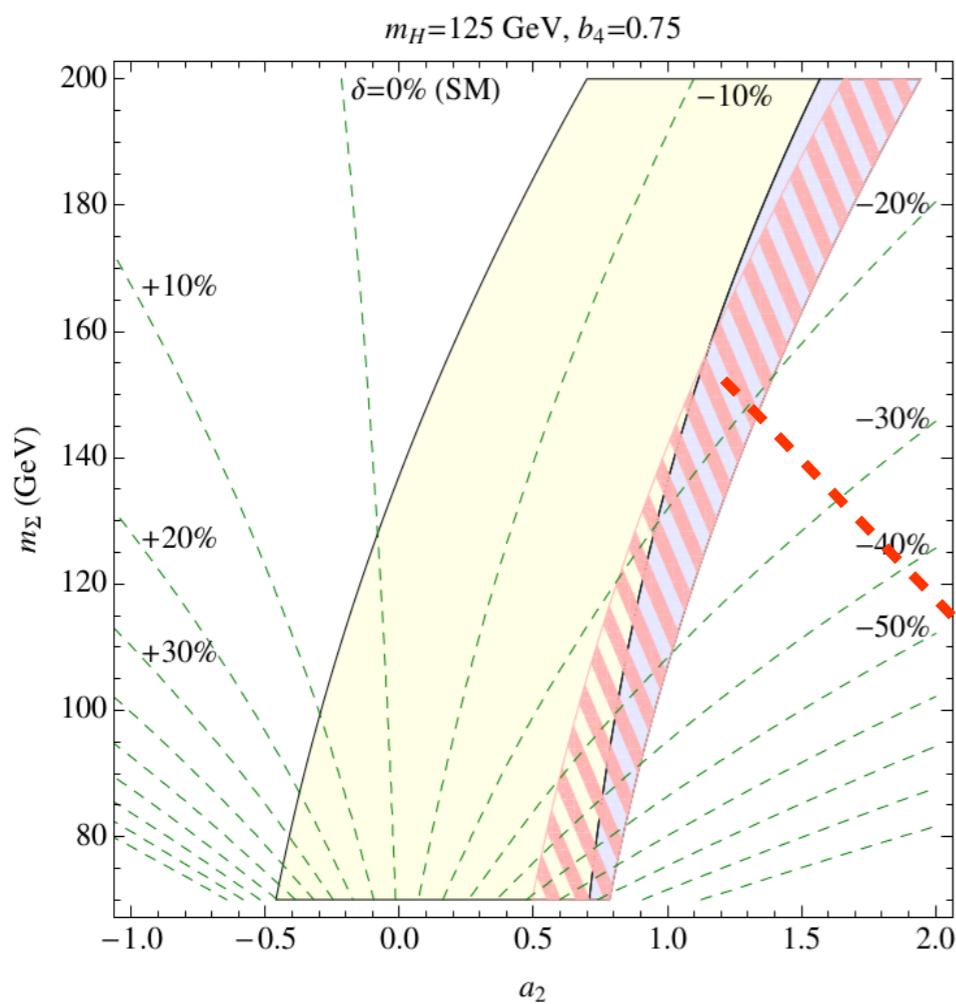
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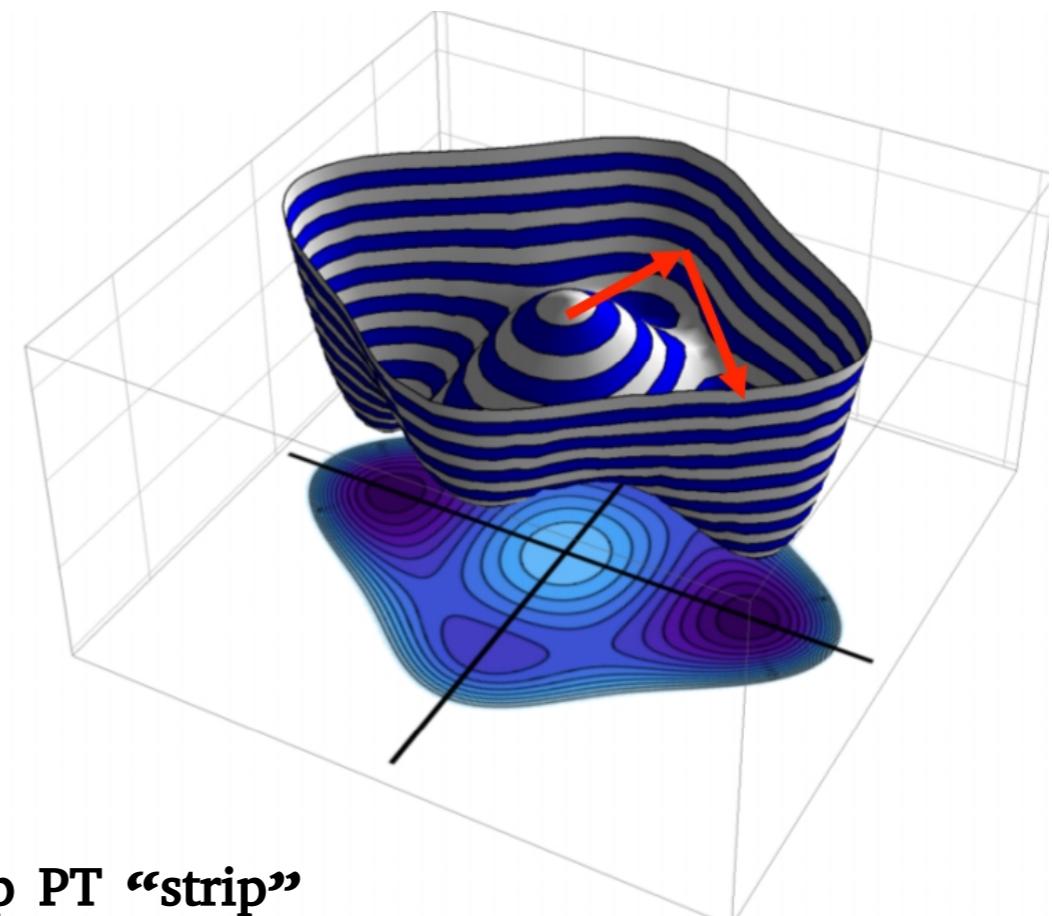
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Possible multi-step EWPT



Two-step PT “strip”
 $(a_2 \text{ vs } m_\Sigma \text{ relation})$



EWPT Scenarios within LHC Reach?

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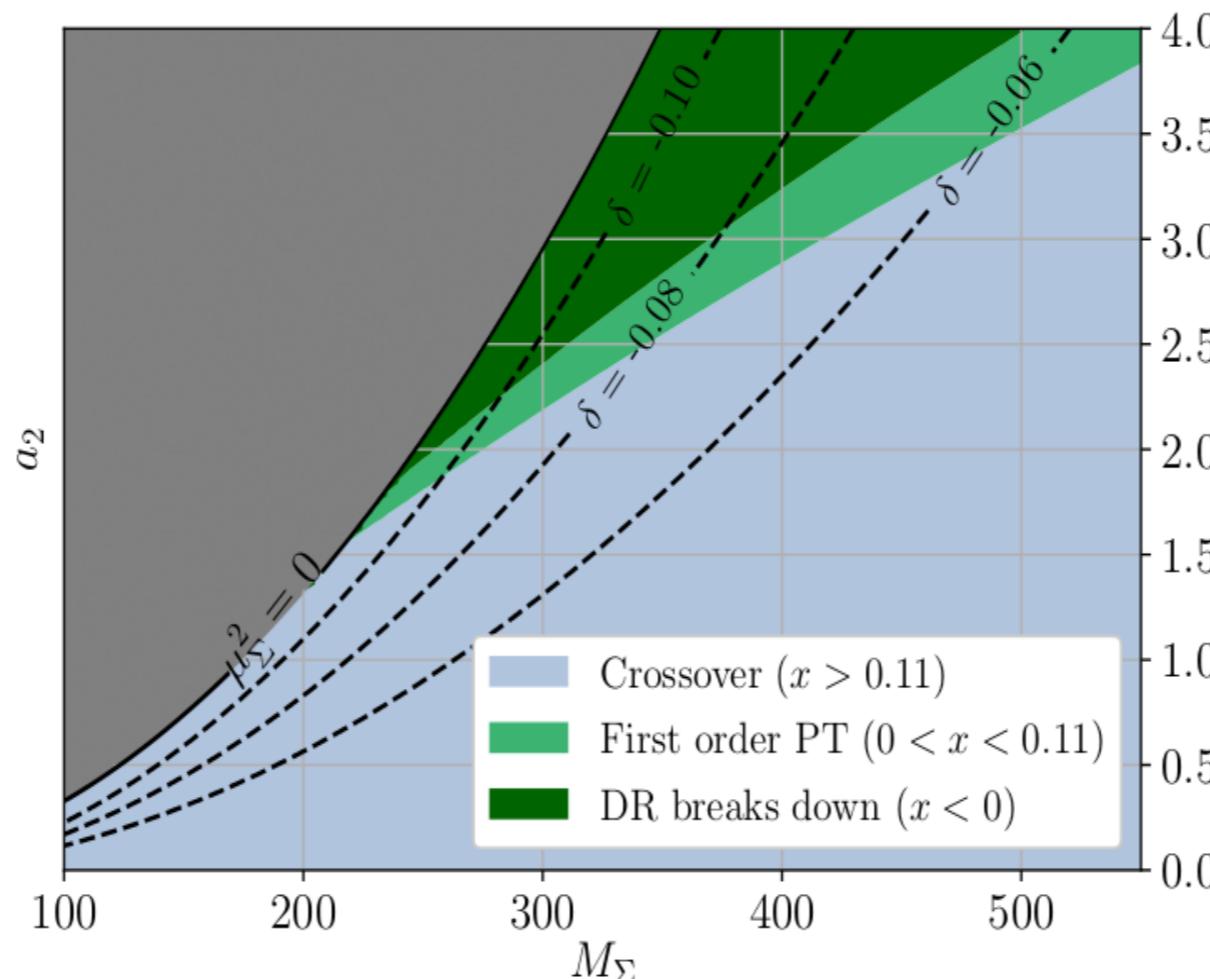
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Non-Perturbative EWPT Study

Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir, arXiv:1802.10500



Dim. Reduction
(3D Eff. Theory)

$$\bar{V}_3(H) = \bar{\mu}_3^2 H^\dagger H + \bar{\lambda}_3 (H^\dagger H)^2$$

$$x = \frac{\bar{\lambda}_3}{\bar{g}_3^2}, \quad y = \frac{\bar{\mu}_3^2}{\bar{g}_3^4}$$

EWPT Scenarios within LHC Reach?

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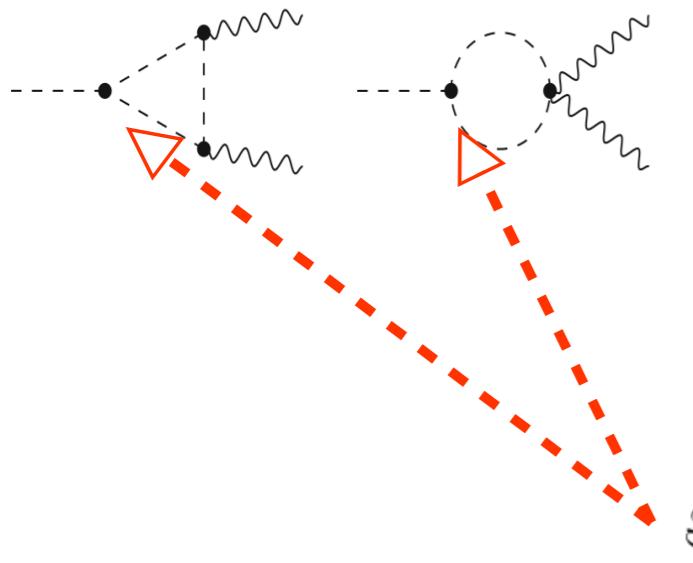
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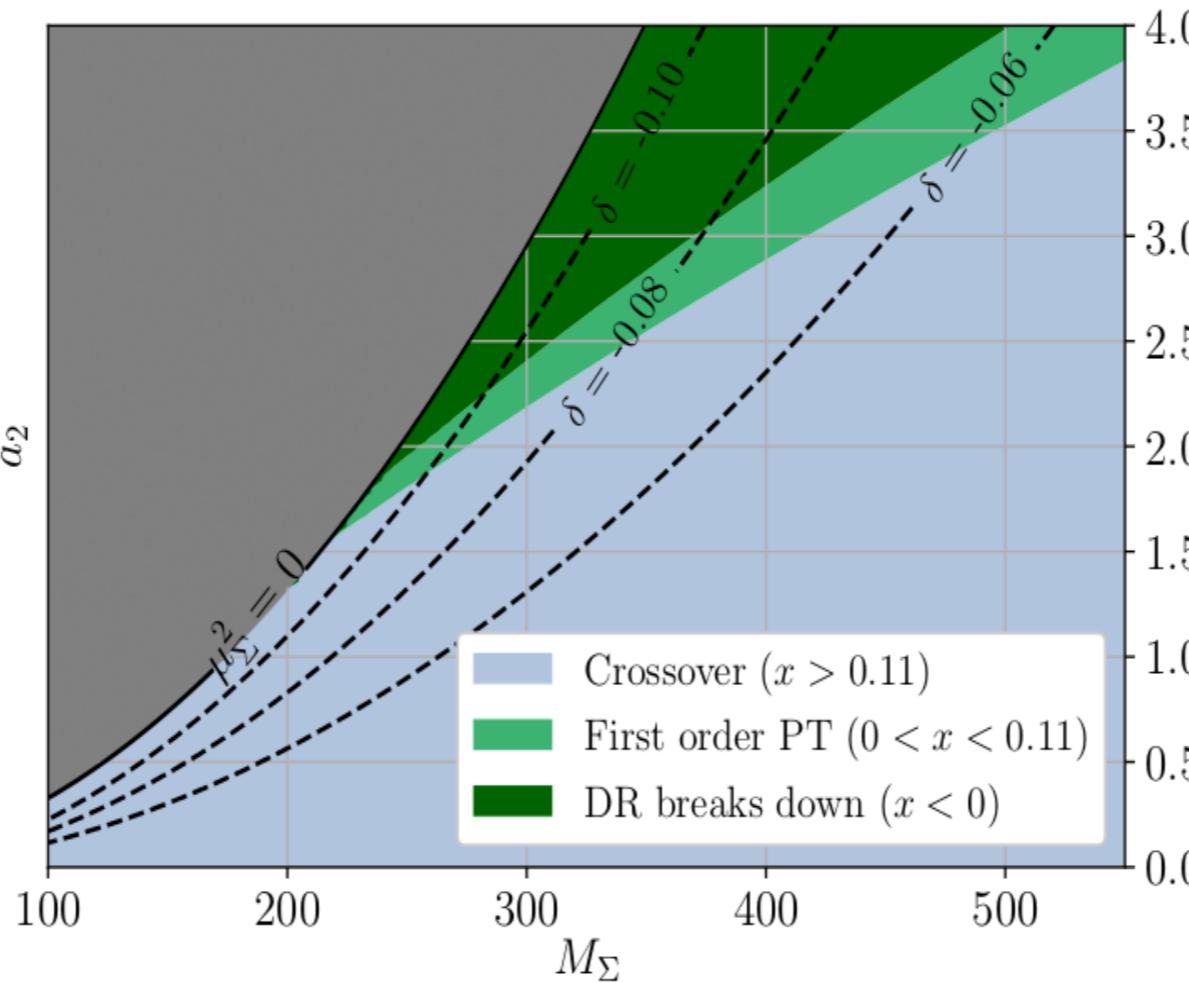
Non-Perturbative EWPT Study

Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir, arXiv:1802.10500



Charged component of triplet modifies $h \rightarrow \gamma\gamma$

$$\delta = \frac{\Gamma^{\Sigma\text{SM}}(h \rightarrow \gamma\gamma) - \Gamma^{\text{SM}}(h \rightarrow \gamma\gamma)}{\Gamma^{\text{SM}}(h \rightarrow \gamma\gamma)}$$



EWPT Scenarios within LHC Reach?

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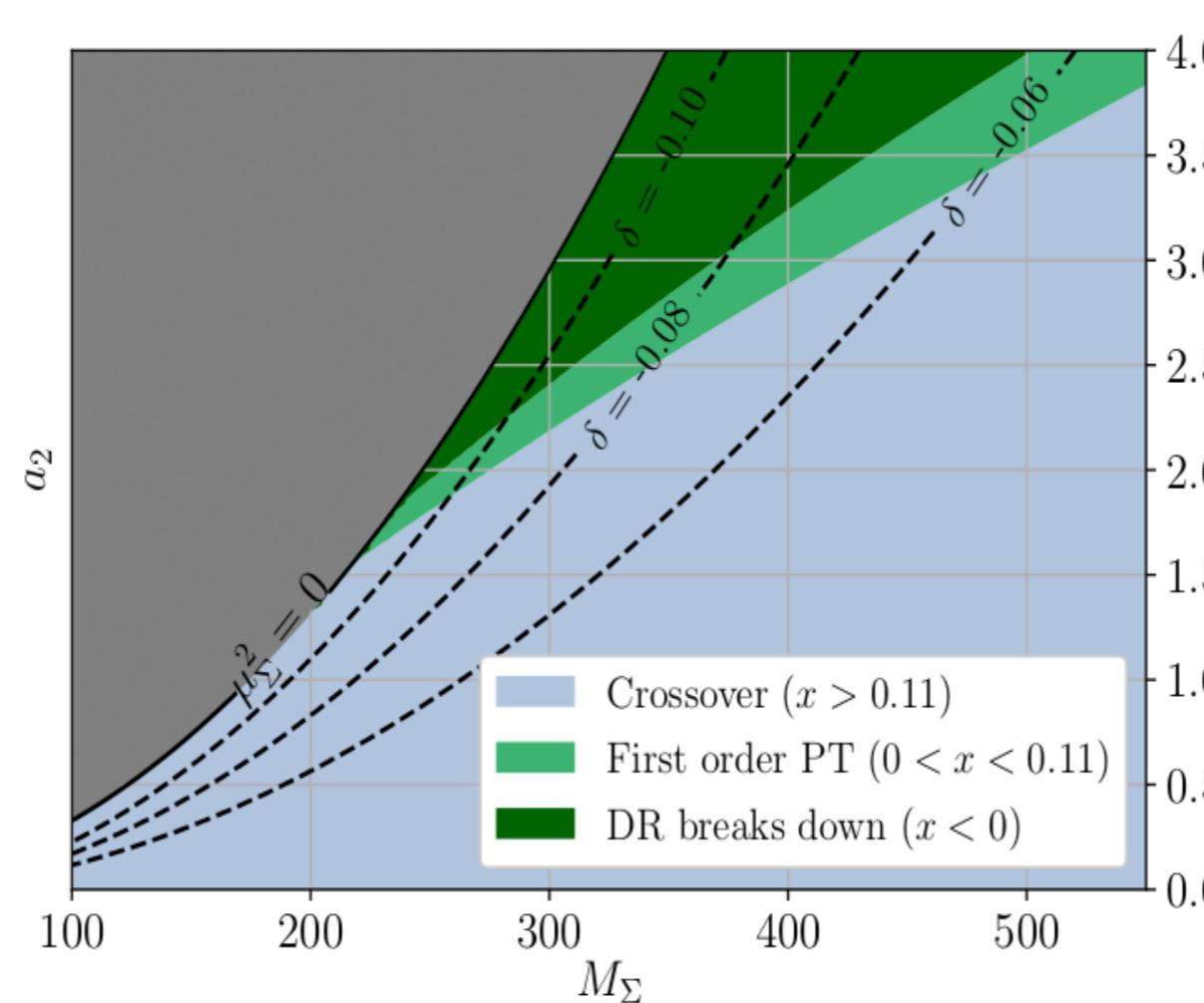
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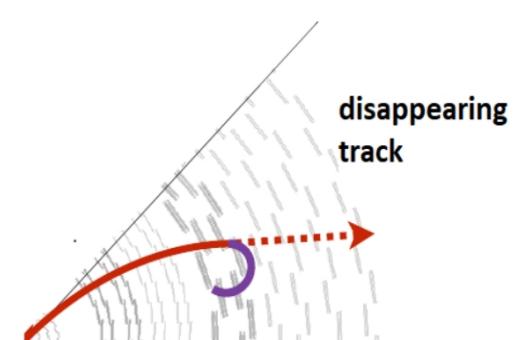
Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir, arXiv:1802.10500



very small (radiative) mass splitting between charged-neutral triplet states

$\delta M_\Sigma \sim 100 - 300 \text{ MeV}$

Disappearing Track Signature!



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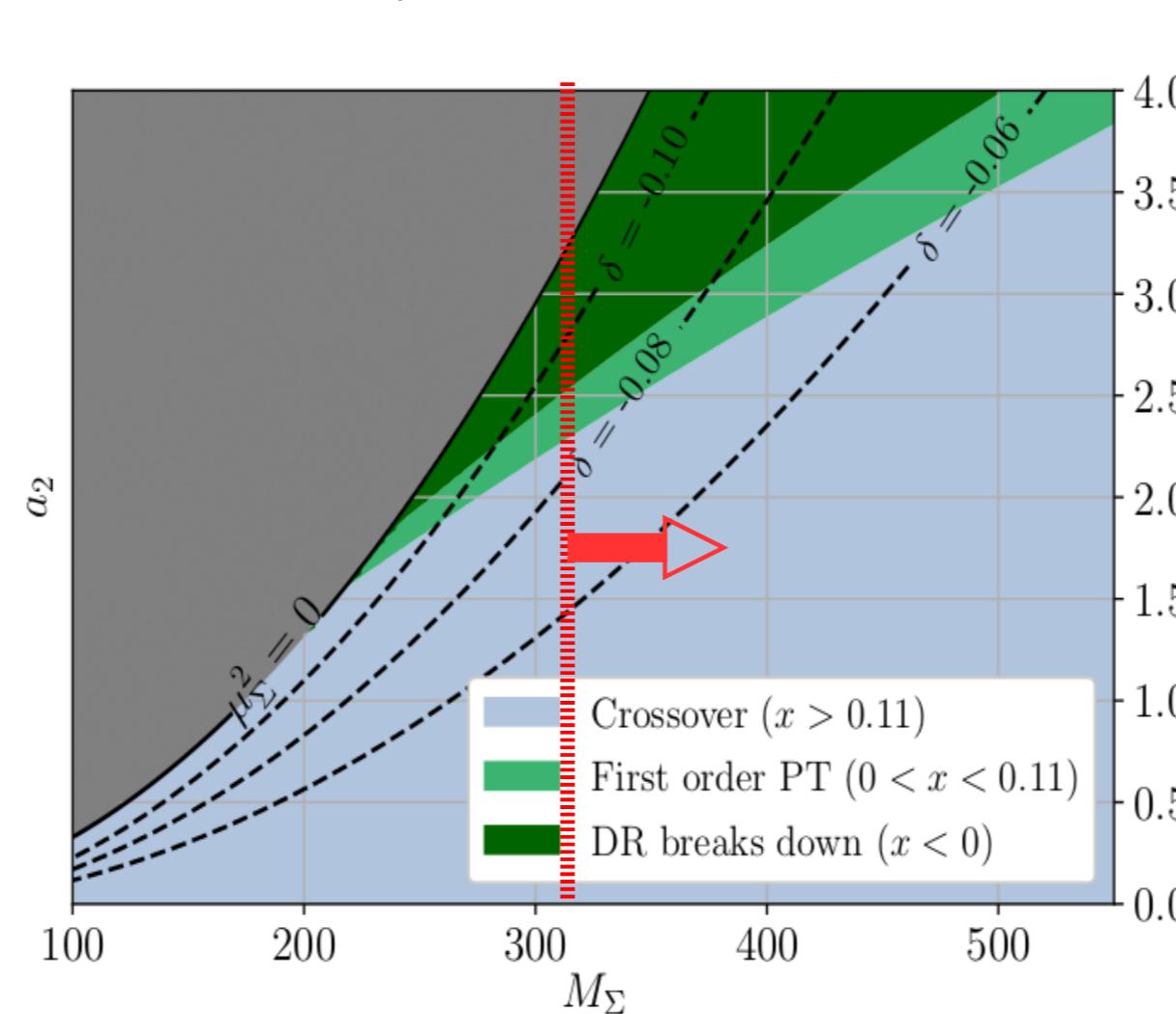
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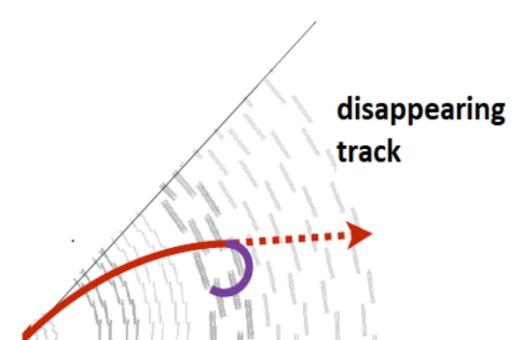
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EWPT Scenarios for Future Colliders!

Singlet
Driven EW Phase Transition

(lots of) Motivation

- ⇒ Neutral Naturalness
- ⇒ Higgs Portal (Dark Sectors)
- ⇒ Non-minimal SUSY (e.g. NMSSM)
- ⇒ Warped Extra Dim (dilaton...)
- ...

EWPT Scenarios for Future Colliders!

Singlet
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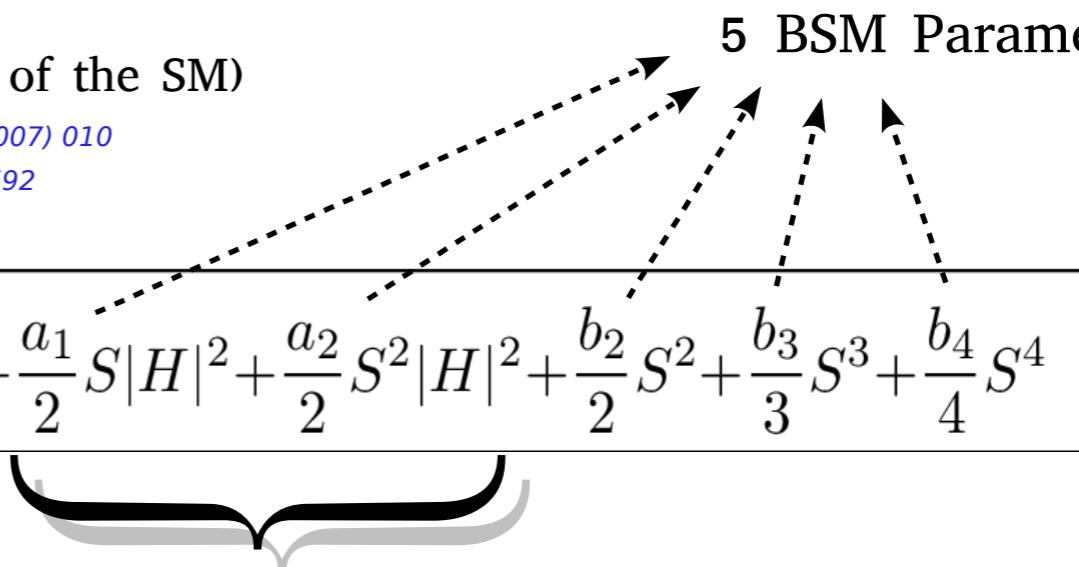
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- ...

EWPT Scenarios for Future Colliders

The **xSM** (singlet scalar extension of the SM)

*Profumo, Ramsey-Musolf, Shaughnessy, JHEP **0708** (2007) 010*

*Espinosa, Konstandin, Riva, Nucl. Phys. **B854** (2012) 592*

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$


Higgs Portal (Higgs - Singlet Mixing)

EWPT Scenarios for Future Colliders

Simplest case

The xSM with Z_2

3 BSM Parameters

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

Higgs Portal

EWPT Scenarios for Future Colliders

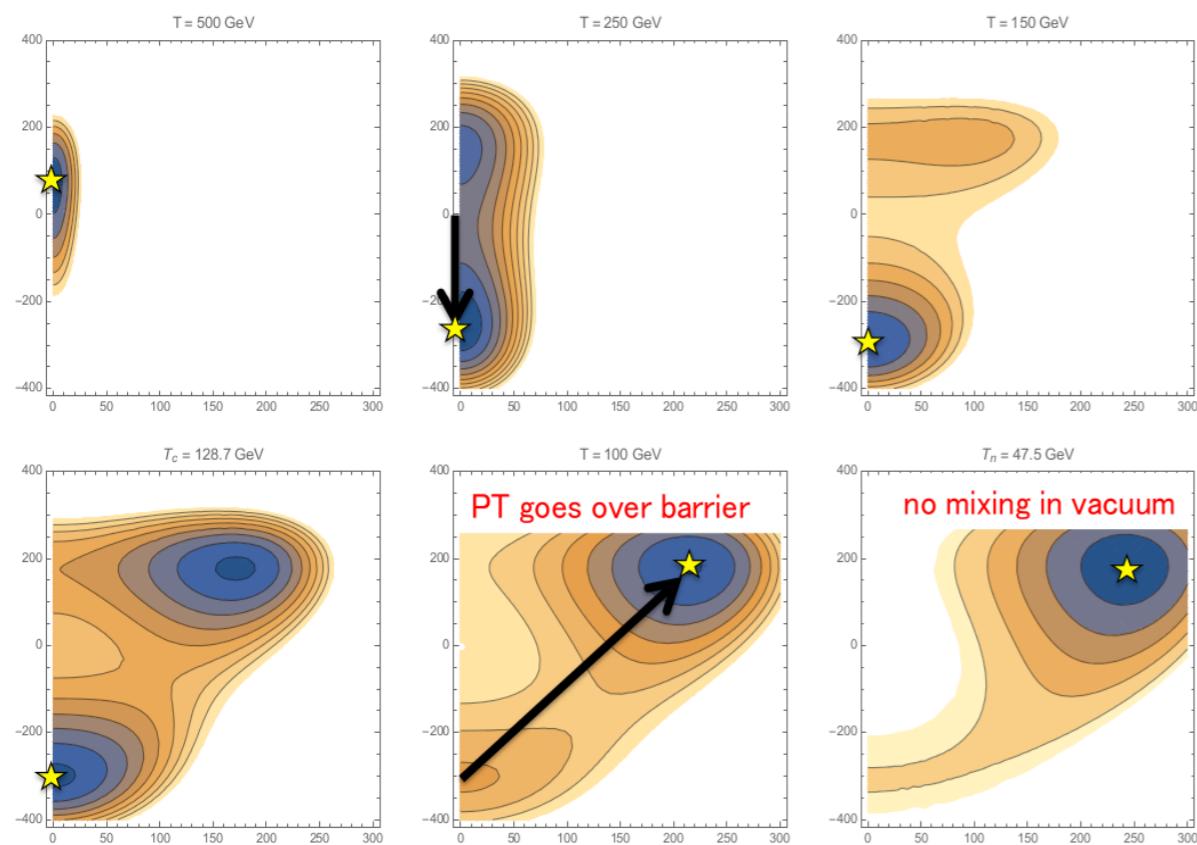
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Higgs Portal

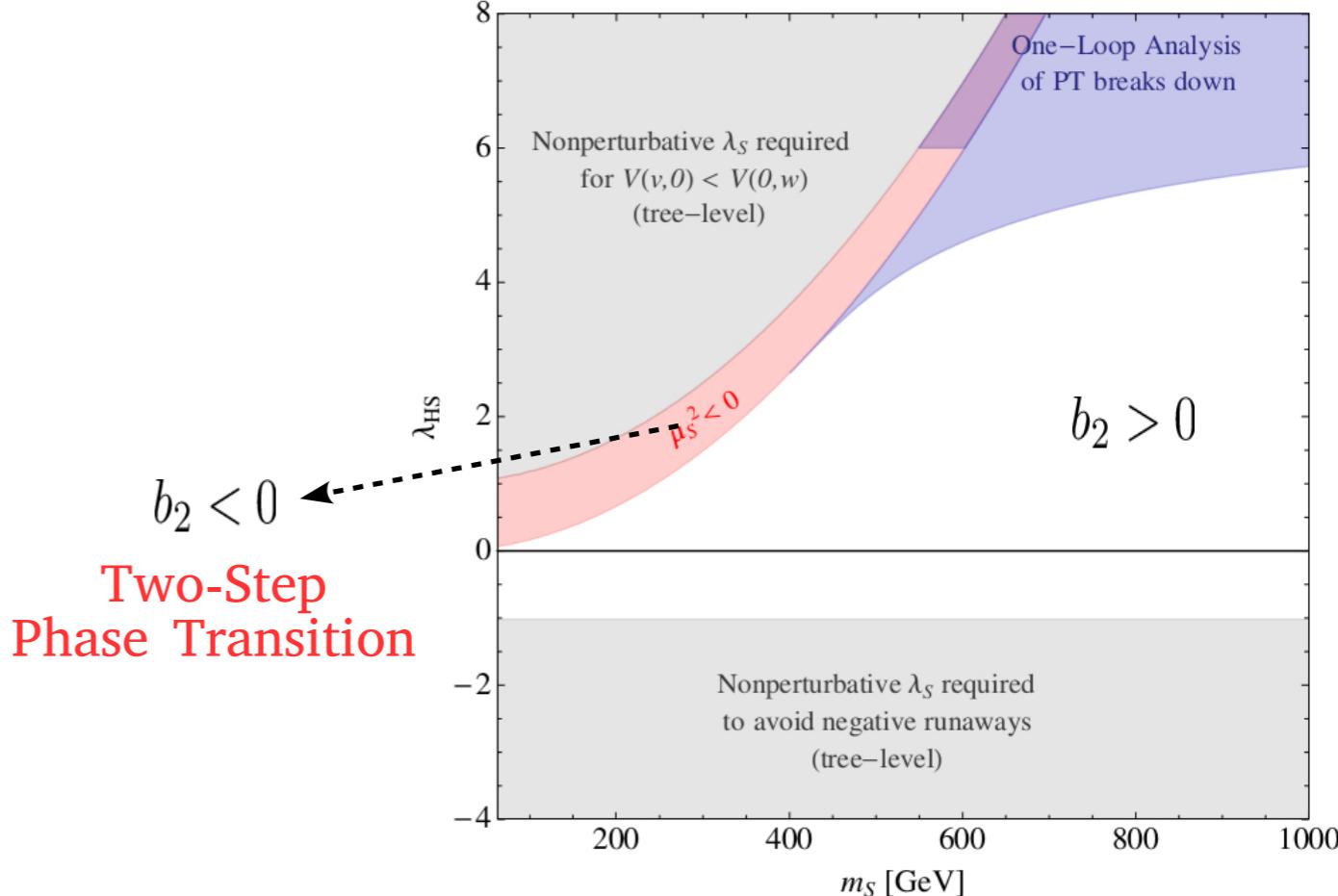
3 BSM Parameters



[courtesy of Andrew Long]

$b_2 < 0$
Two-Step
Phase Transition

$b_2 > 0$



EWPT Scenarios for Future Colliders

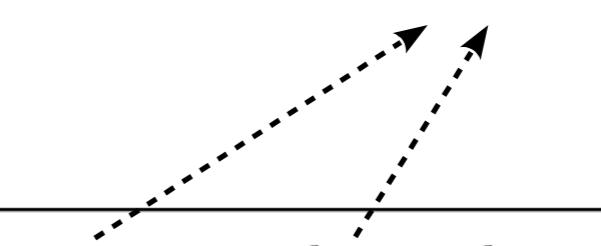
(FCC-ee, hh, CLIC)

Simplest case

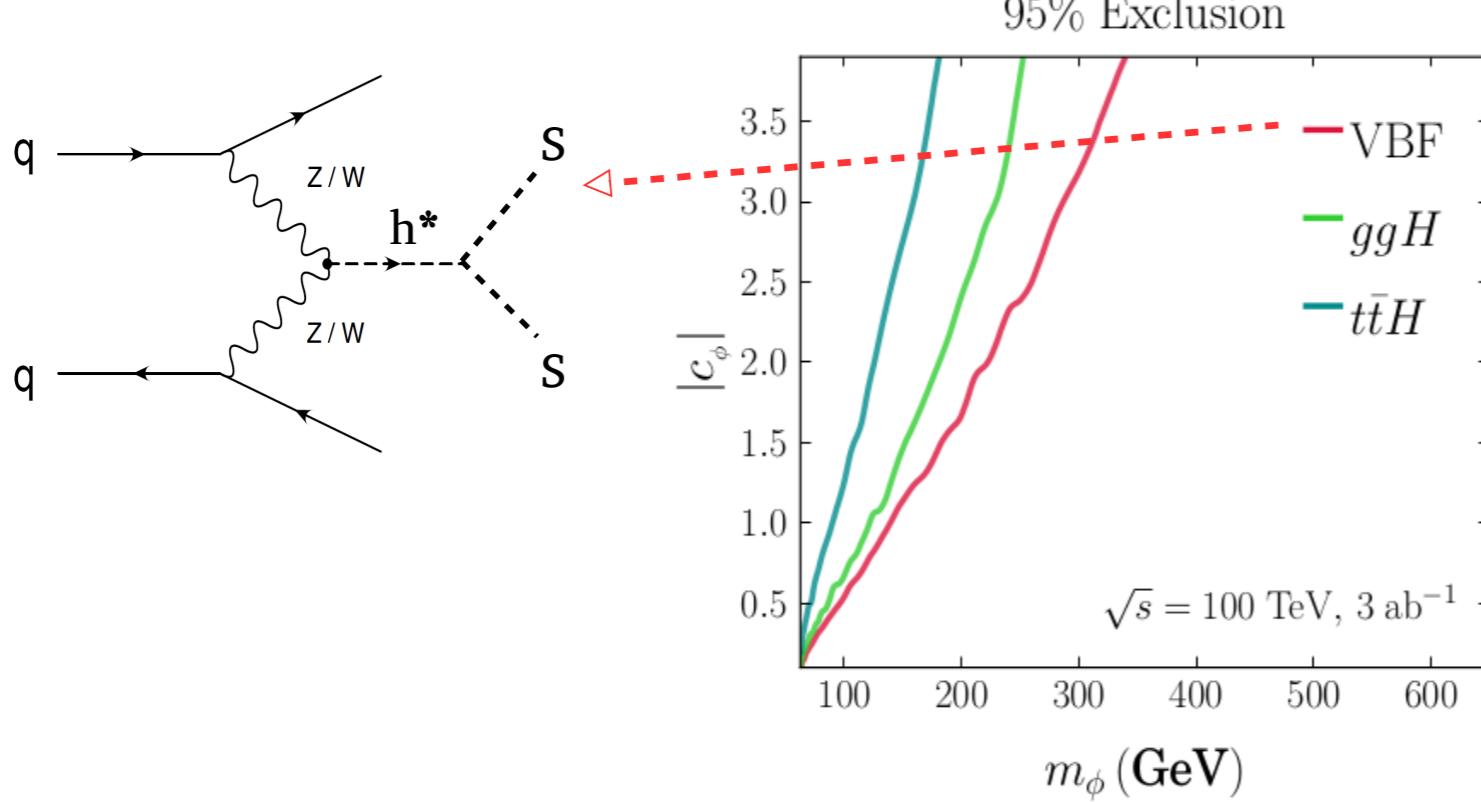
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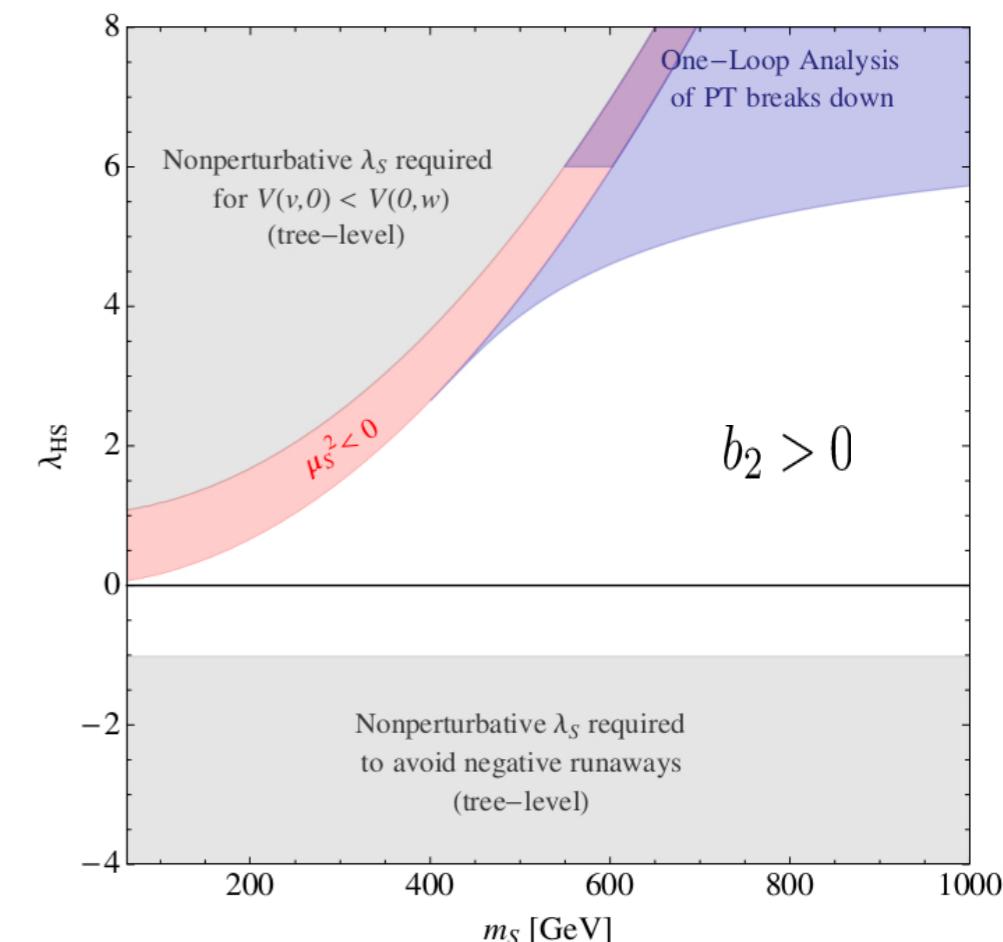
3 BSM Parameters



Direct Searches (“Higgs portal above threshold”)



Craig, Lou, McCullough Thalapillil JHEP **1602** (2016) 127



Curtin, Meade, Yu, JHEP **1411** (2014) 127

EWPT Scenarios for Future Colliders

(FCC-ee, hh, CLIC)

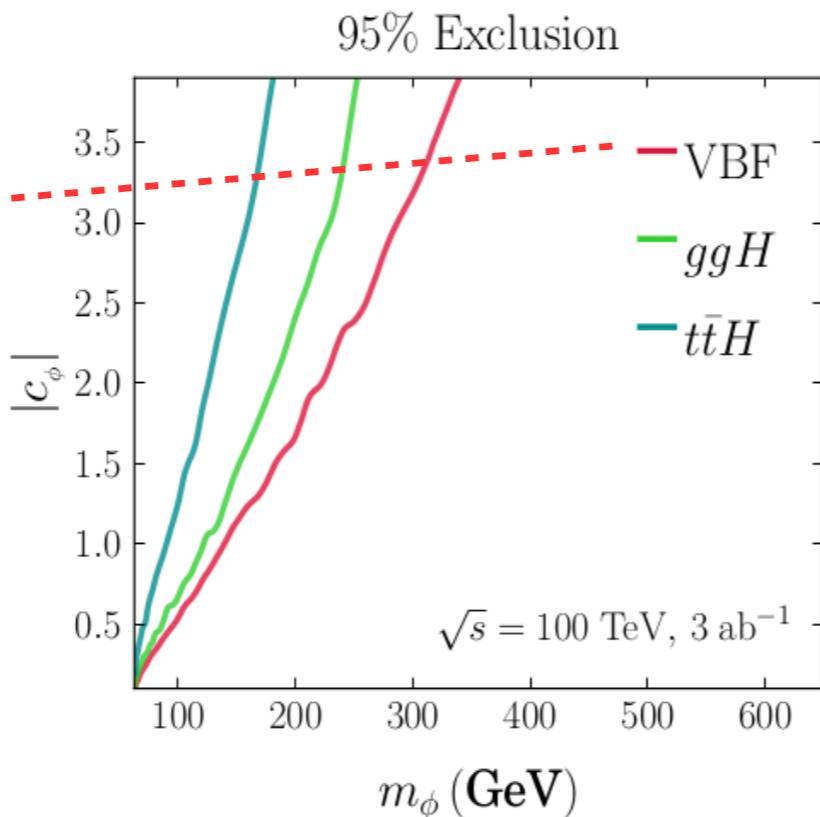
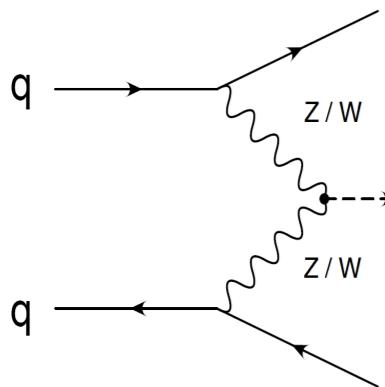
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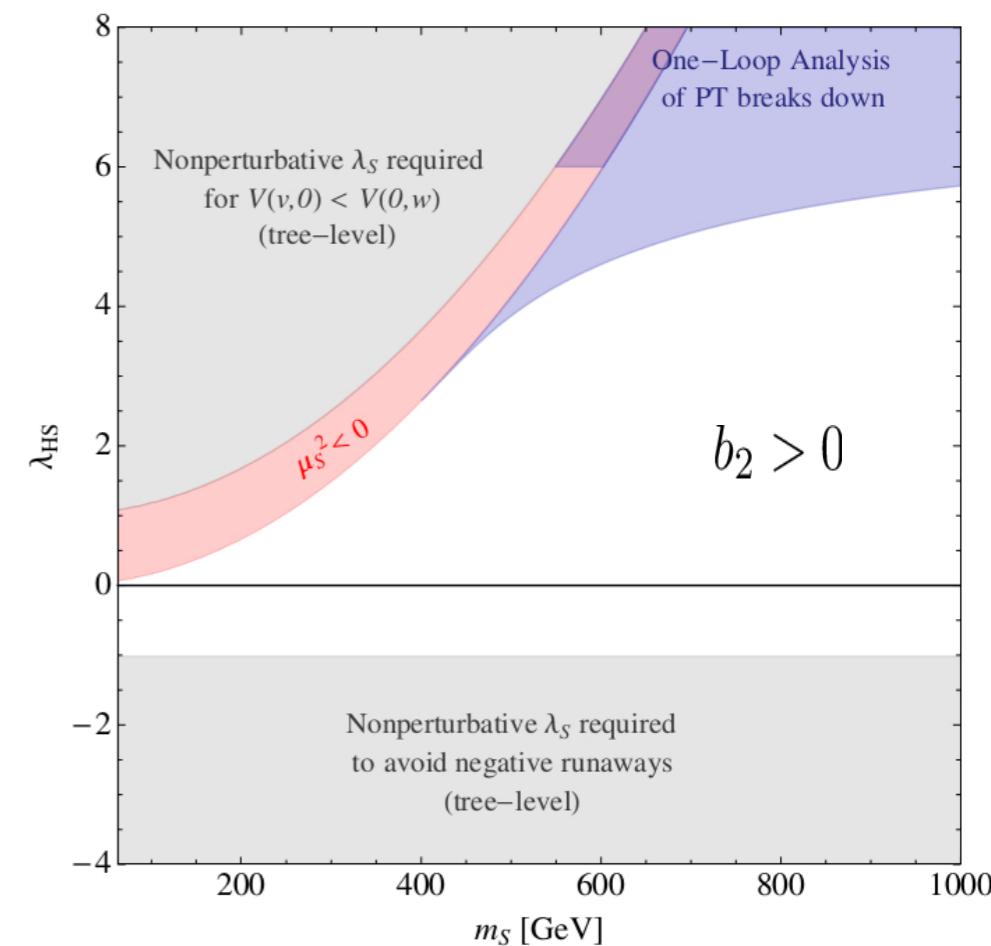


direct searches very tough!
(with a caveat... ask me!)

Garcia-Abenza, JMN, To Appear



Craig, Lou, McCullough Thalapillil JHEP **1602** (2016) 127



Curtin, Meade, Yu, JHEP **1411** (2014) 127

EWPT Scenarios for Future Colliders

(FCC-ee, hh, CLIC)

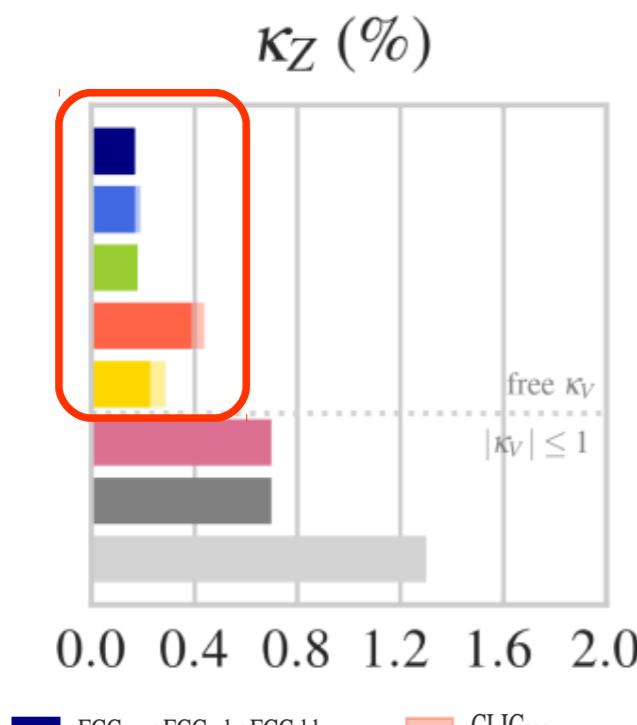
Simplest case

The xSM with Z_2

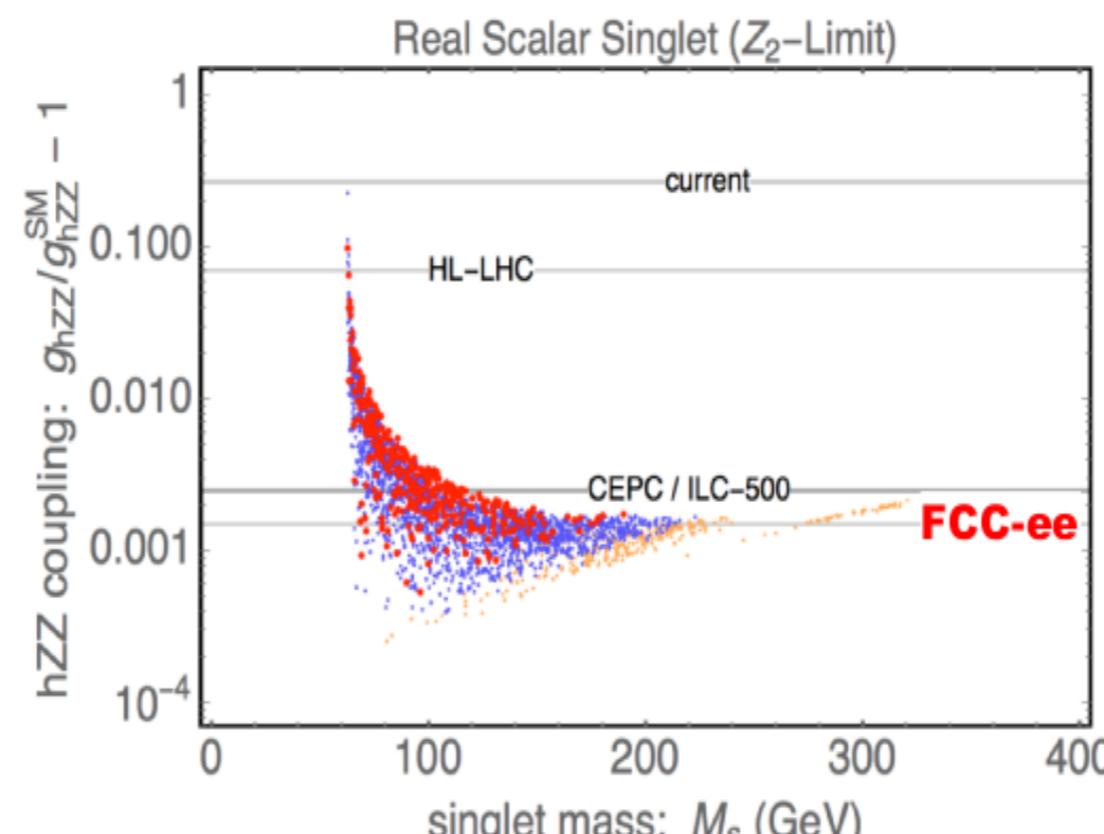
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3 BSM Parameters

Indirect Searches

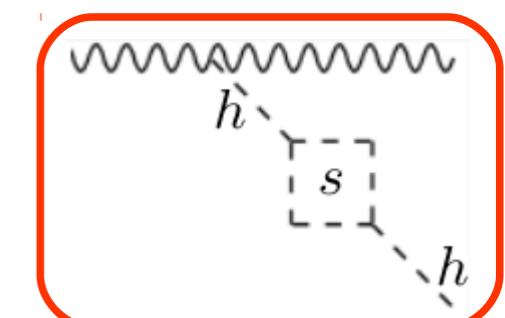


- FCC-ee+CLIC380+CLIC1500
- FCC-ee+CLIC380
- FCC-ee+CLIC1500
- FCC-ee+CLIC240
- FCC-ee+ILC500+ILC350+ILC250
- FCC-ee+ILC500
- FCC-ee+ILC250
- CEPC
- HE-LHC ($|\kappa_V| \leq 1$)
- HL-LHC ($|\kappa_V| \leq 1$)



Huang, Long, Wang PRD **94** (2016) 075008

Precision to probe loop corrections!



EWPT Scenarios for Future Colliders

The General xSM Case

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

$$H = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v_0 + h + iG^0) \end{pmatrix}, \quad S = x_0 + s$$

h_2 inherits its couplings
to SM via Higgs Mixing

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ s \end{pmatrix} \quad \sin 2\theta = \frac{(a_1 + 2a_2 x_0)v_0}{(m_1^2 - m_2^2)} \quad m_{h1} = 125 \text{ GeV}$$

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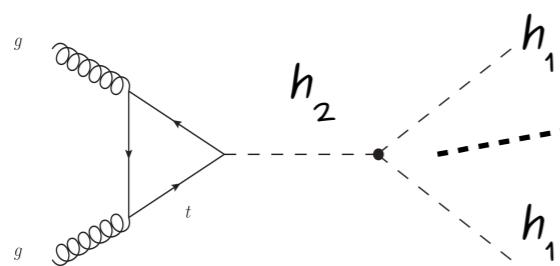
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$m_2 > 250 \text{ GeV}$ Resonant Higgs Pair Production

Dolan, Englert, Spannowsky, Phys. Rev. **D87** (2013) 5, 055002

JMN, Ramsey-Musolf, Phys. Rev. **D89** (2014) 095031

Chen, Dawson, Lewis, Phys. Rev. **D91** (2015) 035015



$$\lambda_{211} = \frac{s_\theta}{2} [c_\theta^4(m_2^2 - m_1^2)/v_0 + 2v_0(a_2 - 3\lambda)c_\theta^2 - (a_1 + 2a_2 x_0 - 2b_3 - 6b_4 x_0)c_\theta s_\theta - a_2 v_0 s_\theta^2]$$

EWPT Scenarios for Future Colliders

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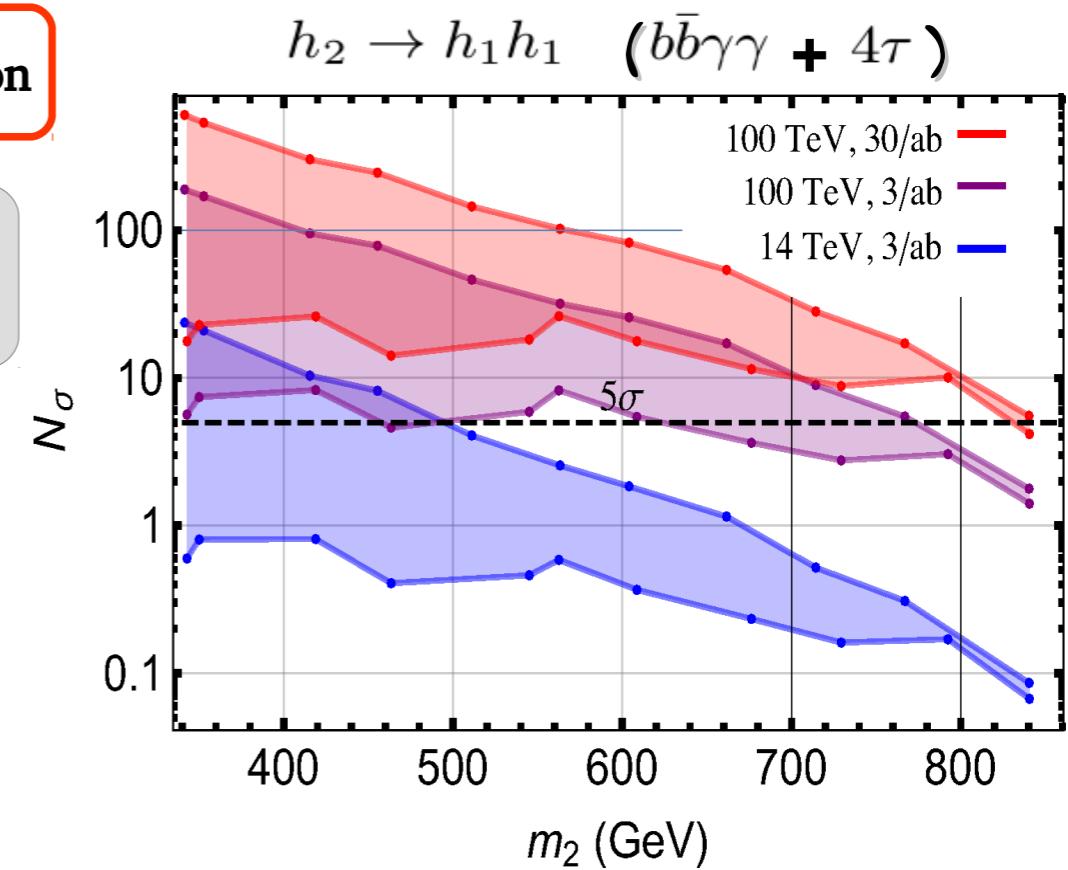
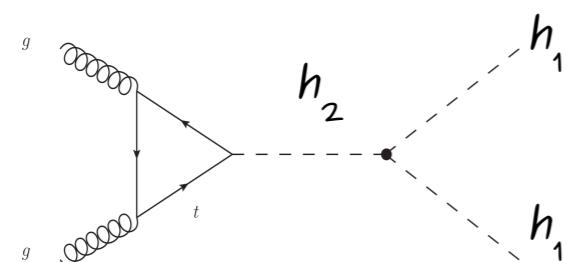
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$$\sin 2\theta = \frac{(a_1 + 2a_2 x_0)v_0}{(m_1^2 - m_2^2)}$$

$m_{h_1} = 125$ GeV

$m_2 > 250$ GeV Resonant Higgs Pair Production

FCC-hh largely probes 1st Order EW Phase Transition parameter space via $h_2 \rightarrow h_1 h_1$



EWPT Scenarios for Future Colliders

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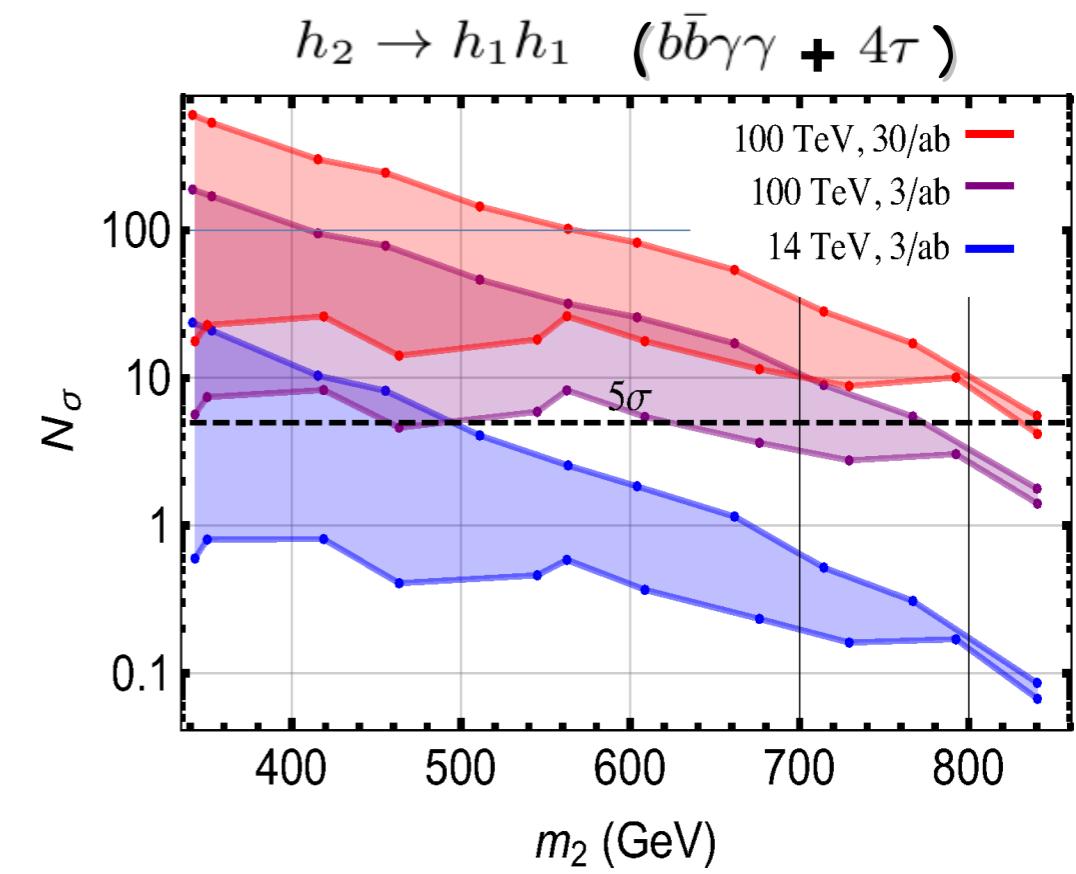
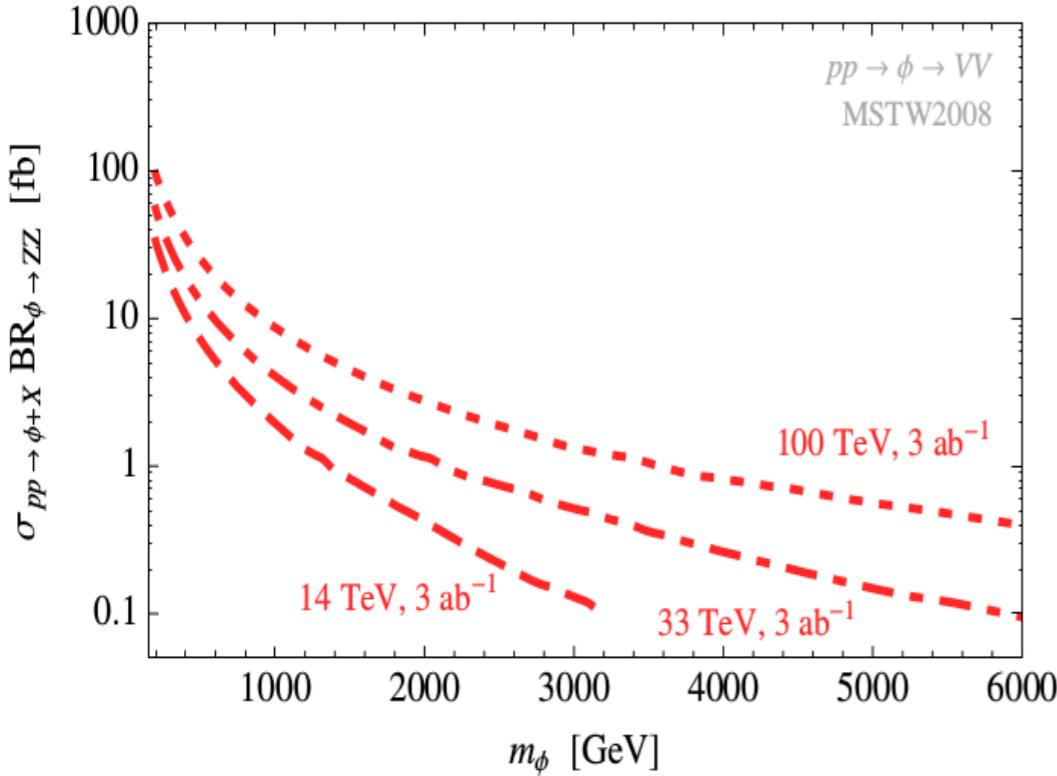
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$m_{h_1} = 125$ GeV

Interplay with $h_2 \rightarrow VV$ searches

Crucial for Higgs + Singlet parameter extraction



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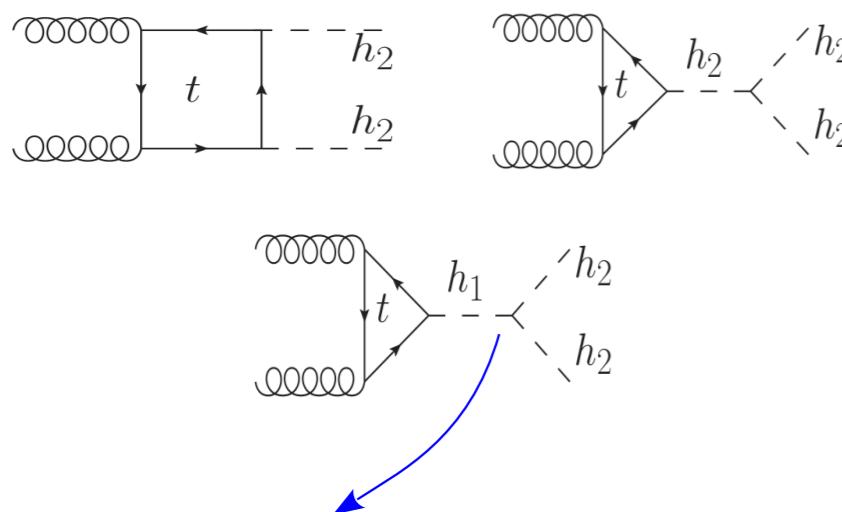
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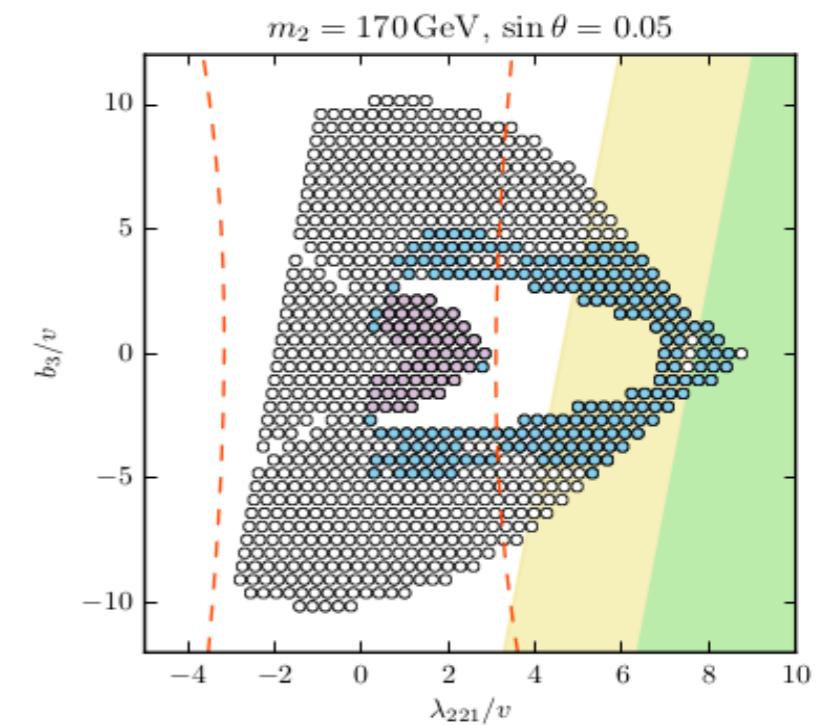
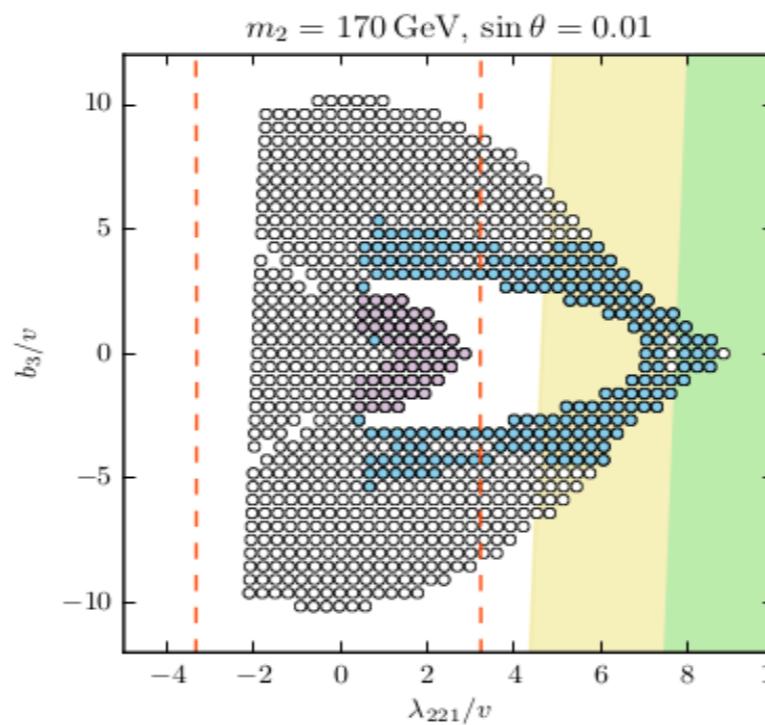
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$m_{h_1} = 125$ GeV

$m_2 < 250$ GeV



$\lambda_{221} \propto a_2$ ($\neq 0$ for $\sin \theta \rightarrow 0$)



Chen, Kozaczuk, Lewis, JHEP **1708** (2017) 096

HL-LHC

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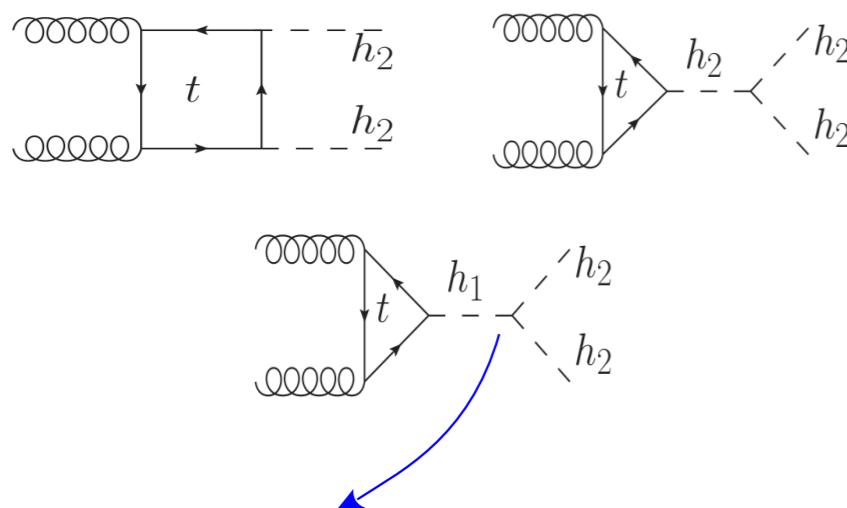
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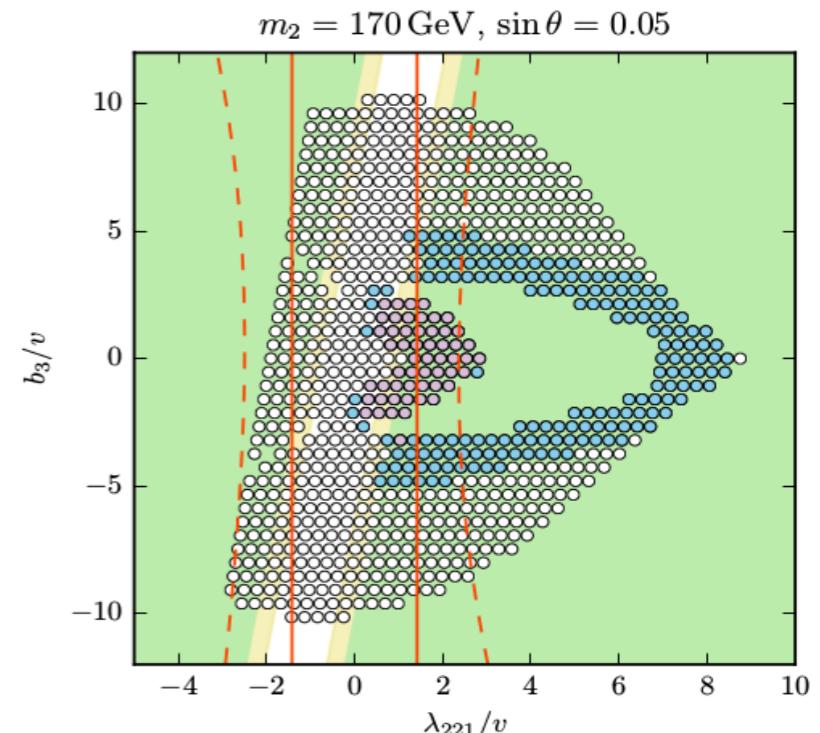
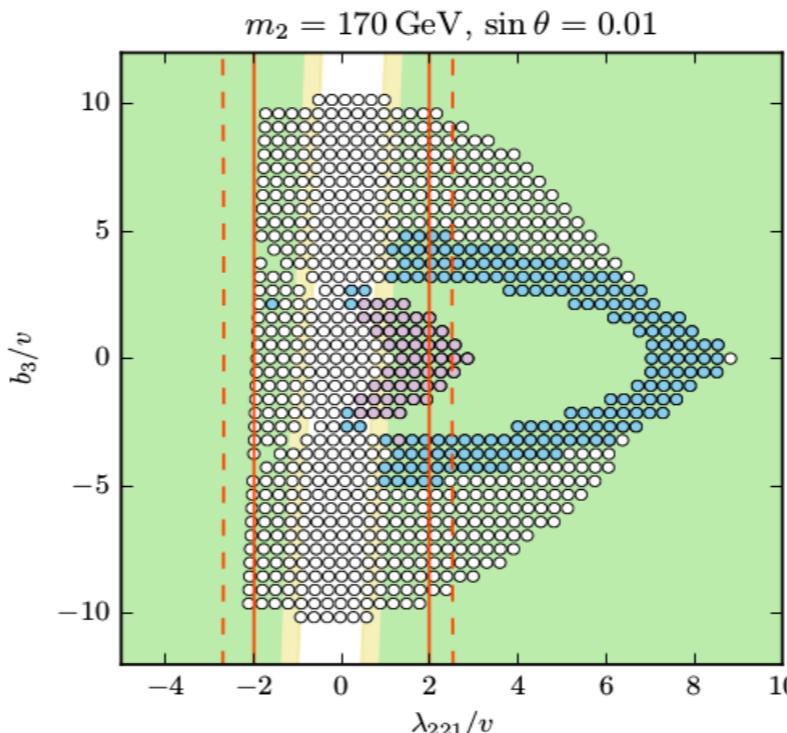
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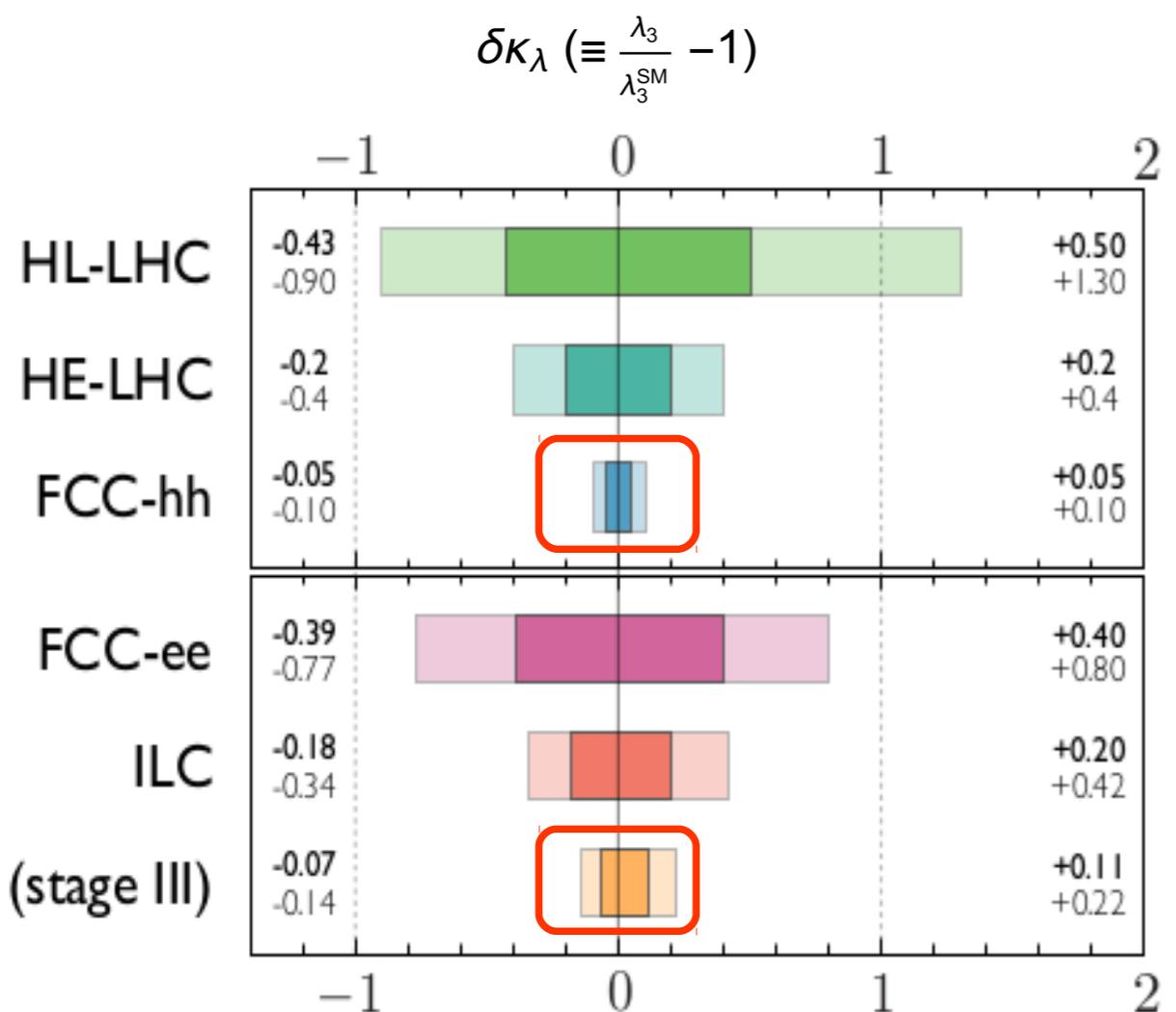
FCC-hh

EWPT Scenarios for Future Colliders

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+ Higgs self-coupling!



FCC-hh

CLIC

Dark: 68%CL, Light: 95%CL

EWPT Scenarios for Future Colliders

CLIC

The General xSM Case

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

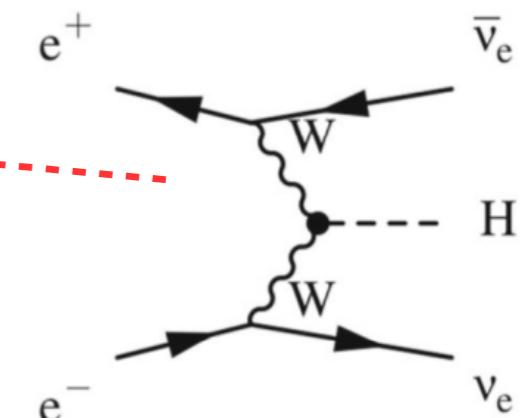
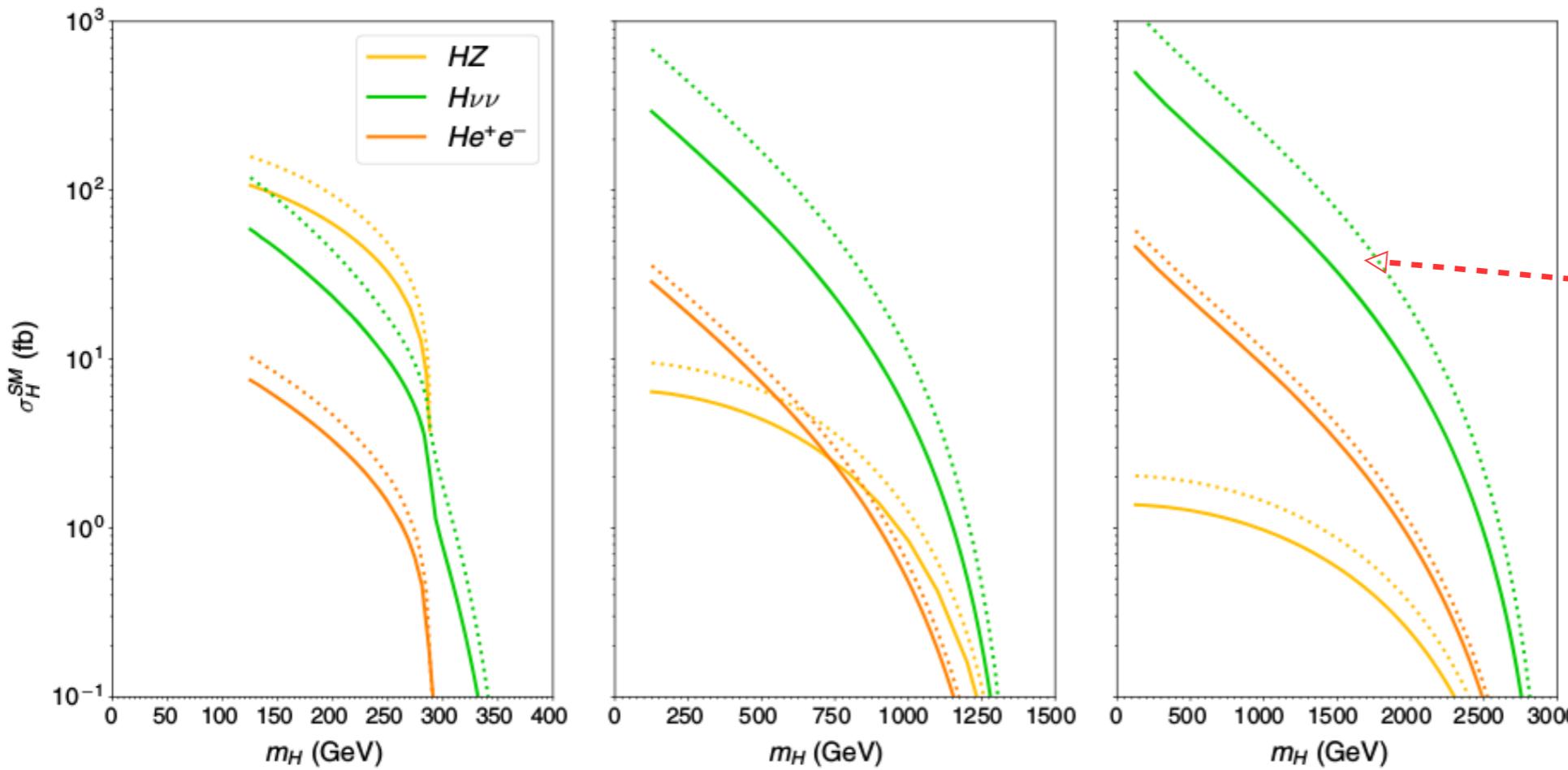
EWPT Scenarios for Future Colliders

CLIC

The General xSM Case

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

Large VBF (heavy) Higgs production XS

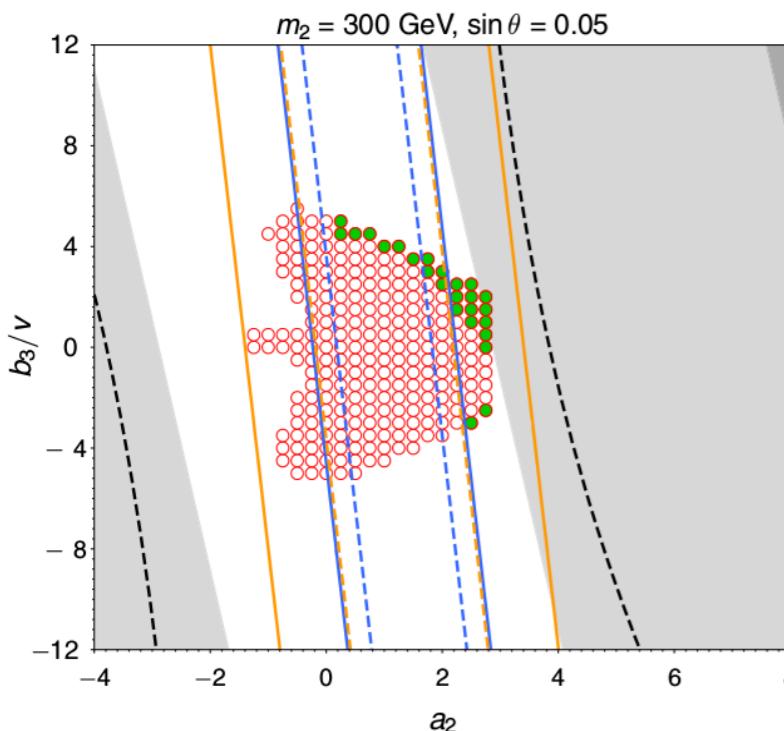
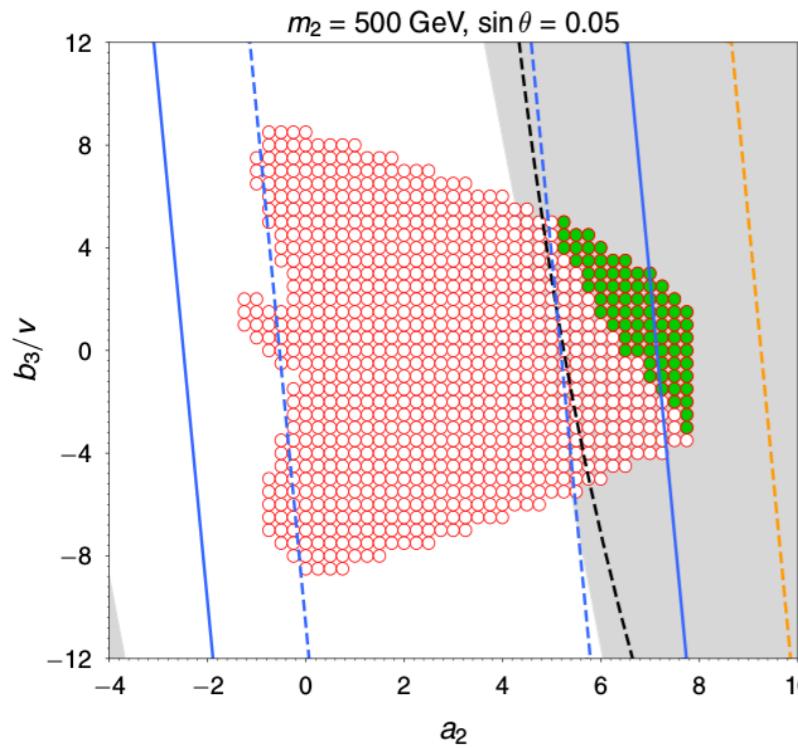


EWPT Scenarios for Future Colliders

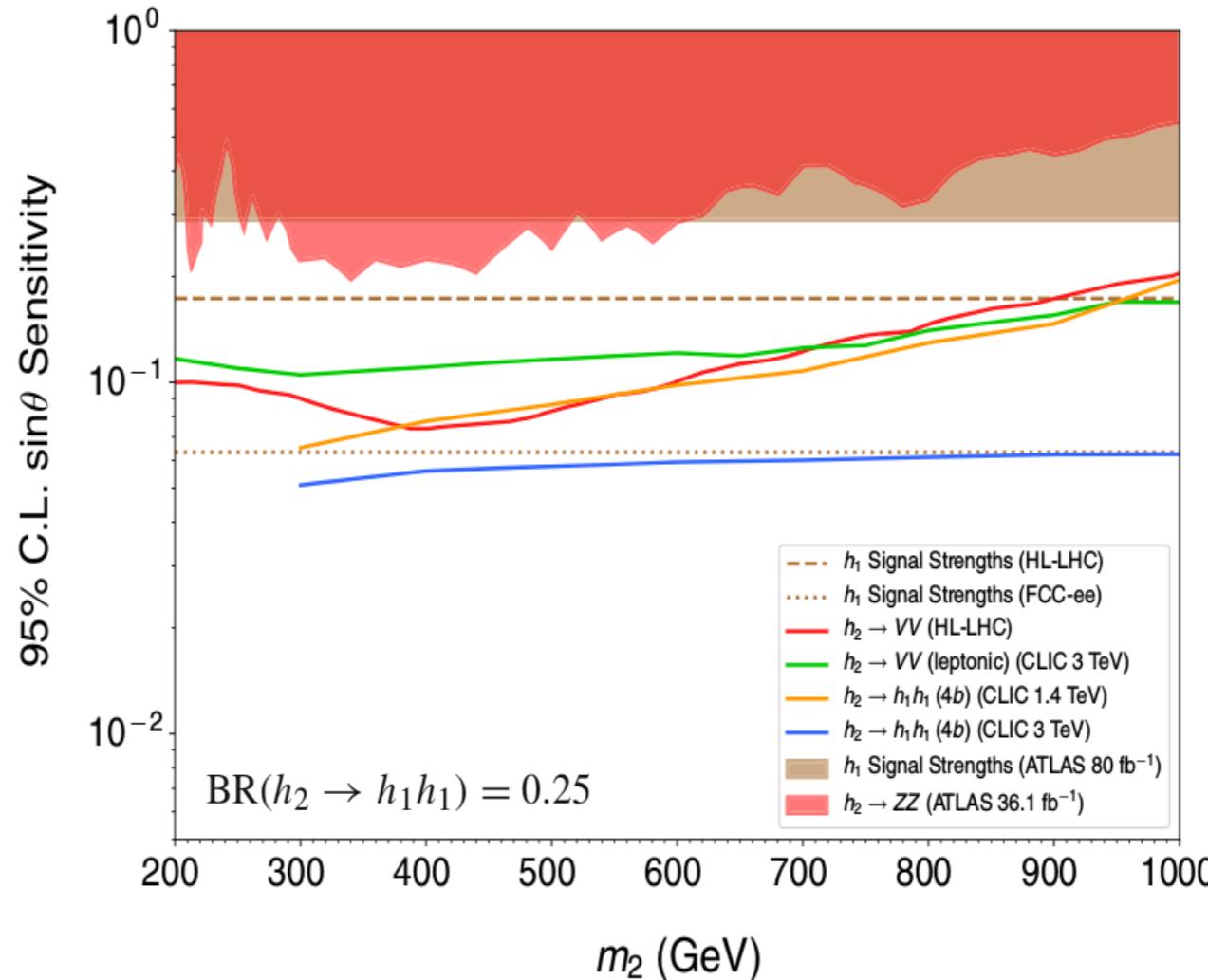
CLIC

The General xSM Case

$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$



$H \rightarrow hh \rightarrow b\bar{b}b\bar{b}$



EWPT Scenarios for Future Colliders

The General xSM Case

CLIC

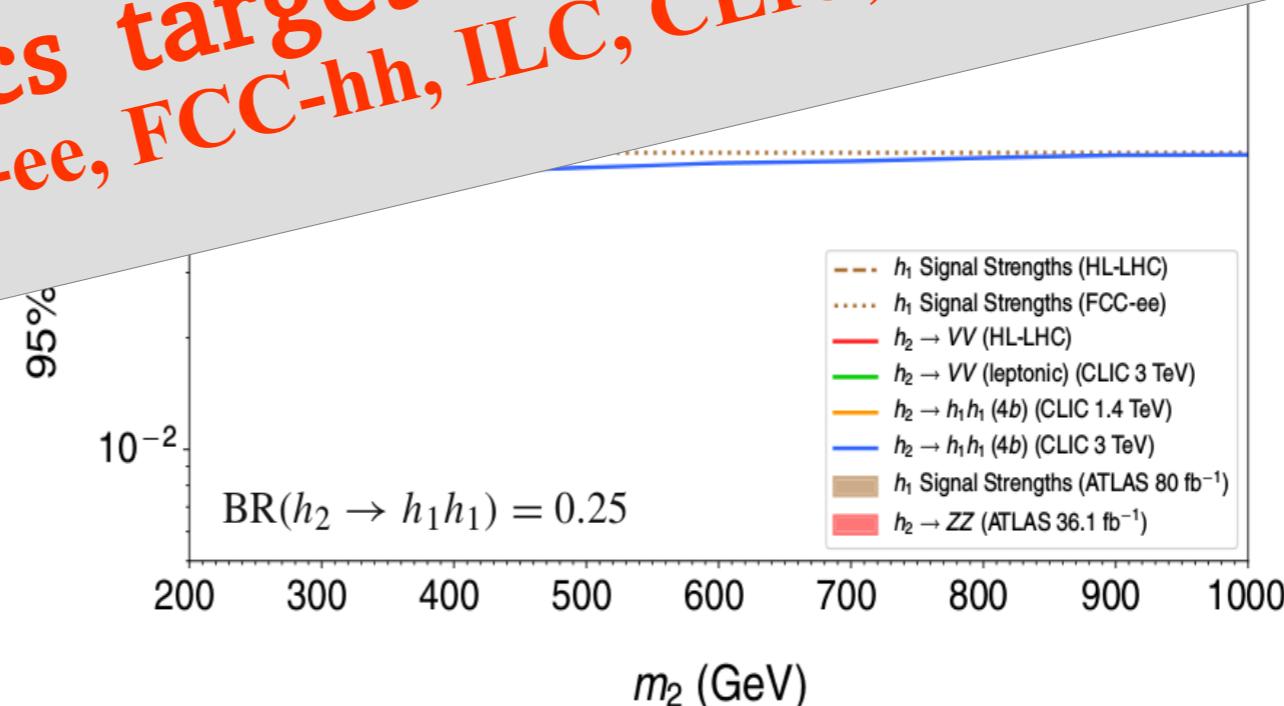
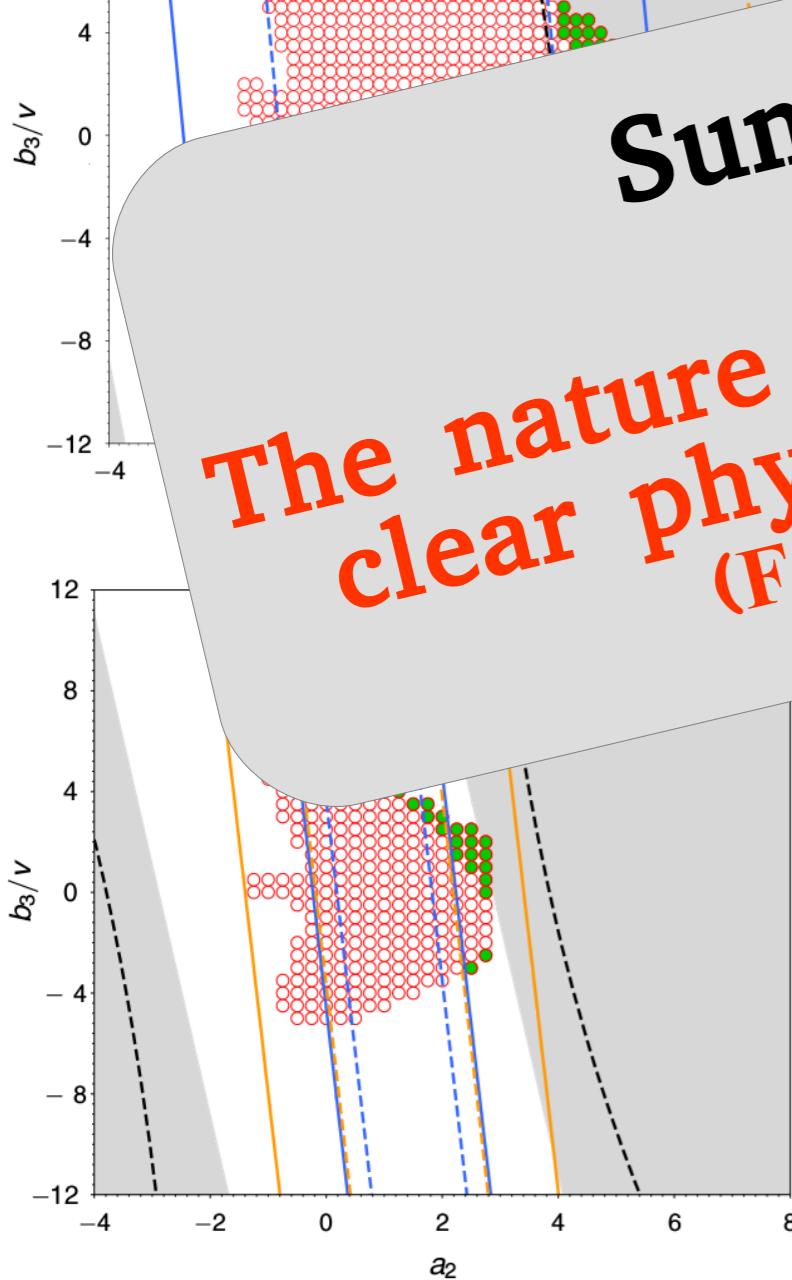
$$V(H, S) = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} S |H|^2 + \frac{a_2}{2} S^2 |H|^2 + \frac{b_2}{2} S^2 + \frac{b_3}{2} S^3 + \frac{b_4}{4} S^4$$

$m_2 = 500 \text{ GeV}, \sin \theta = 0.05$

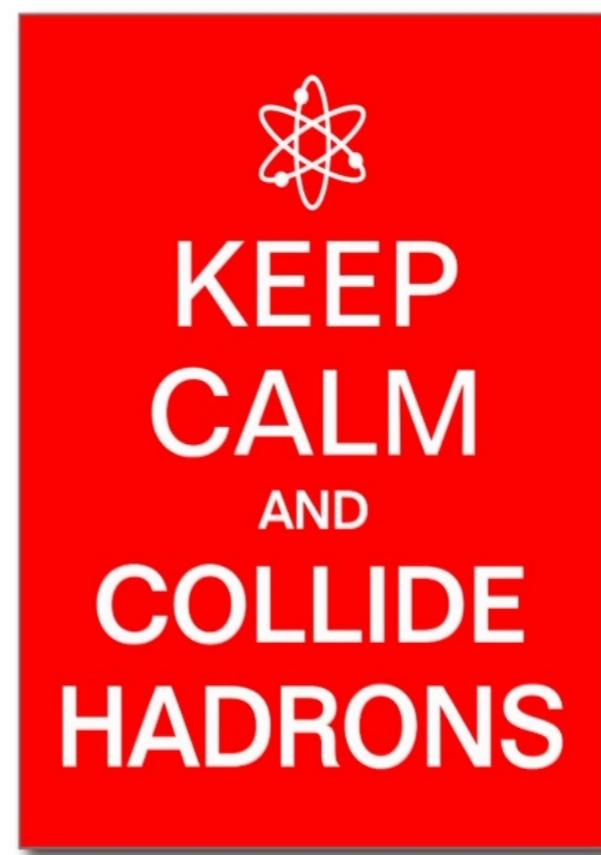
$H \rightarrow h h$

Summary & Conclusions

The nature of the EW Phase Transition is a clear physics target for Future Colliders
(FCC-ee, FCC-hh, ILC, CLIC, CEPC)

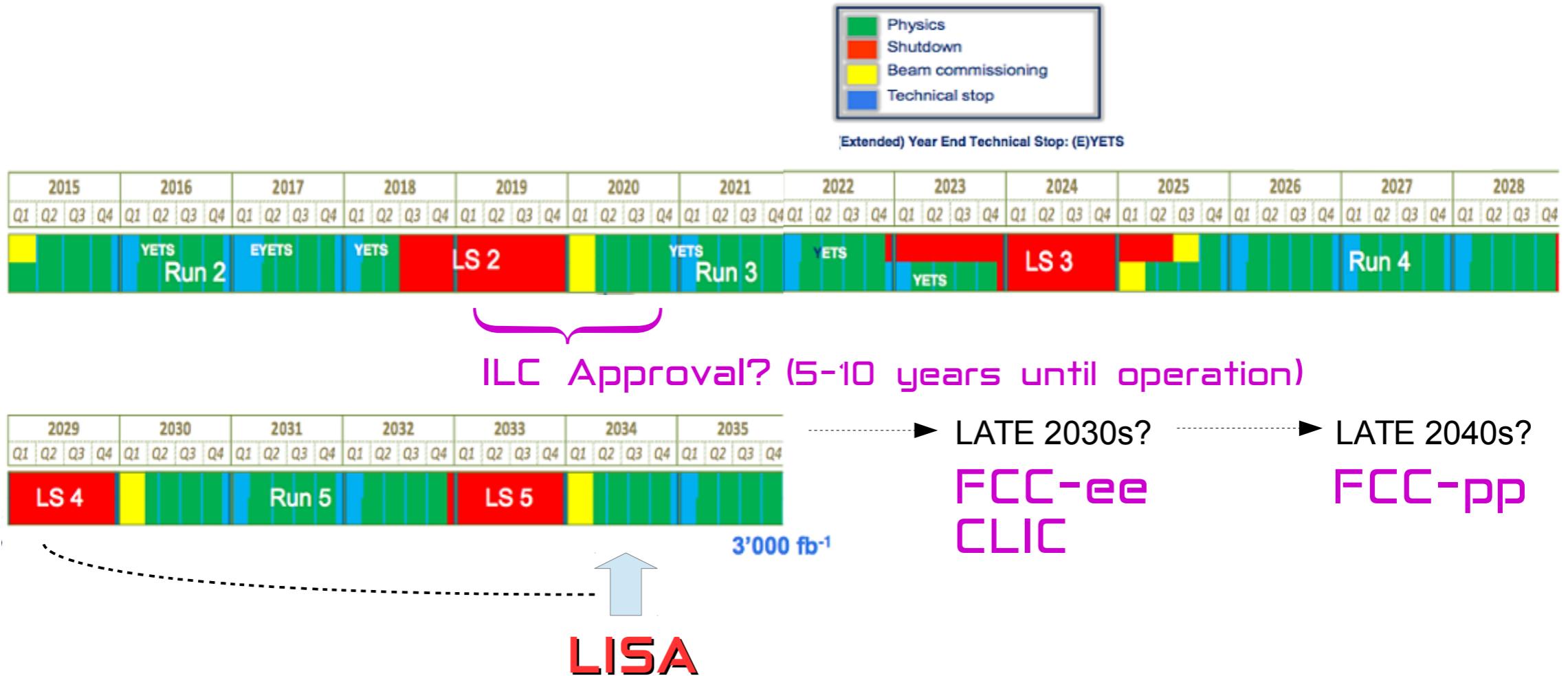


Thank you!





LISA in the Context of High-Energy Colliders Timeline



After LHC, LISA may be Next Step in Exploration
of ElectroWeak Scale Physics

Indirect Probes

	current	HL-LHC	CEPC	ILC	FCC-ee	FCC-hh
hZZ	27%	7%	0.25%	0.25%	0.15%	-
$\Gamma(h \rightarrow \gamma\gamma)$	20%	8%	4%	-	1.5%	-
hhh	-	[-0.8 , 7.7] 95% CL	43%	27%	43%	10%

Assumptions & references:

hZZ current = 5 fb⁻¹ at $\sqrt{s} = 7$ TeV & 20 fb⁻¹ at 8 TeV (1606.02266)

hZZ @ HL-LHC = 3000 fb⁻¹ at $\sqrt{s} = 14$ TeV (1307.7135, CMS)

hZZ @ CEPC = 5000 fb⁻¹ at $\sqrt{s} = 250$ GeV (pre-CDR)

hZZ @ ILC = 2000 fb⁻¹ at $\sqrt{s} = 250$ GeV (1506.05992)

hZZ @ FCC-ee = 2600 fb⁻¹ at $\sqrt{s} = 250$ GeV (1601.0640)

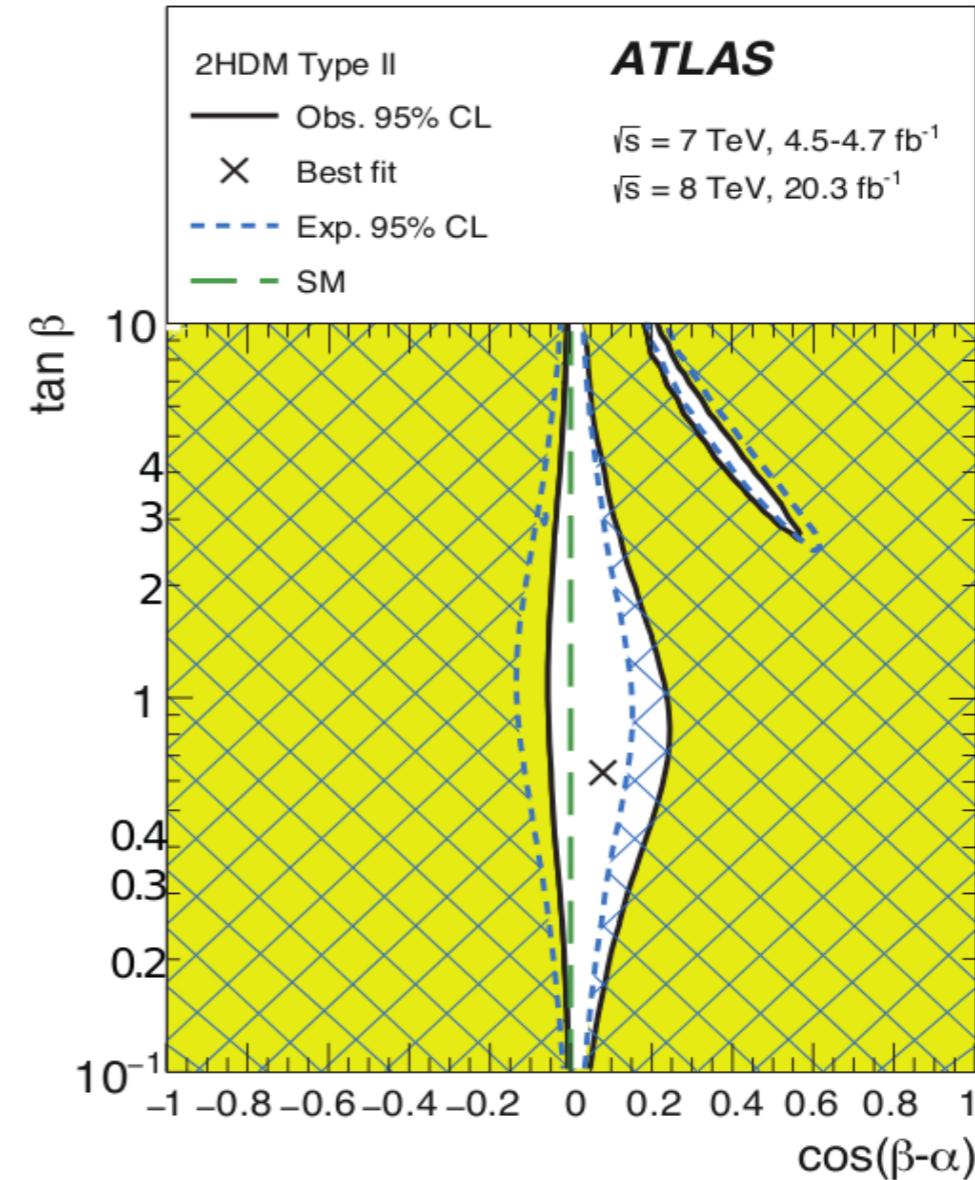
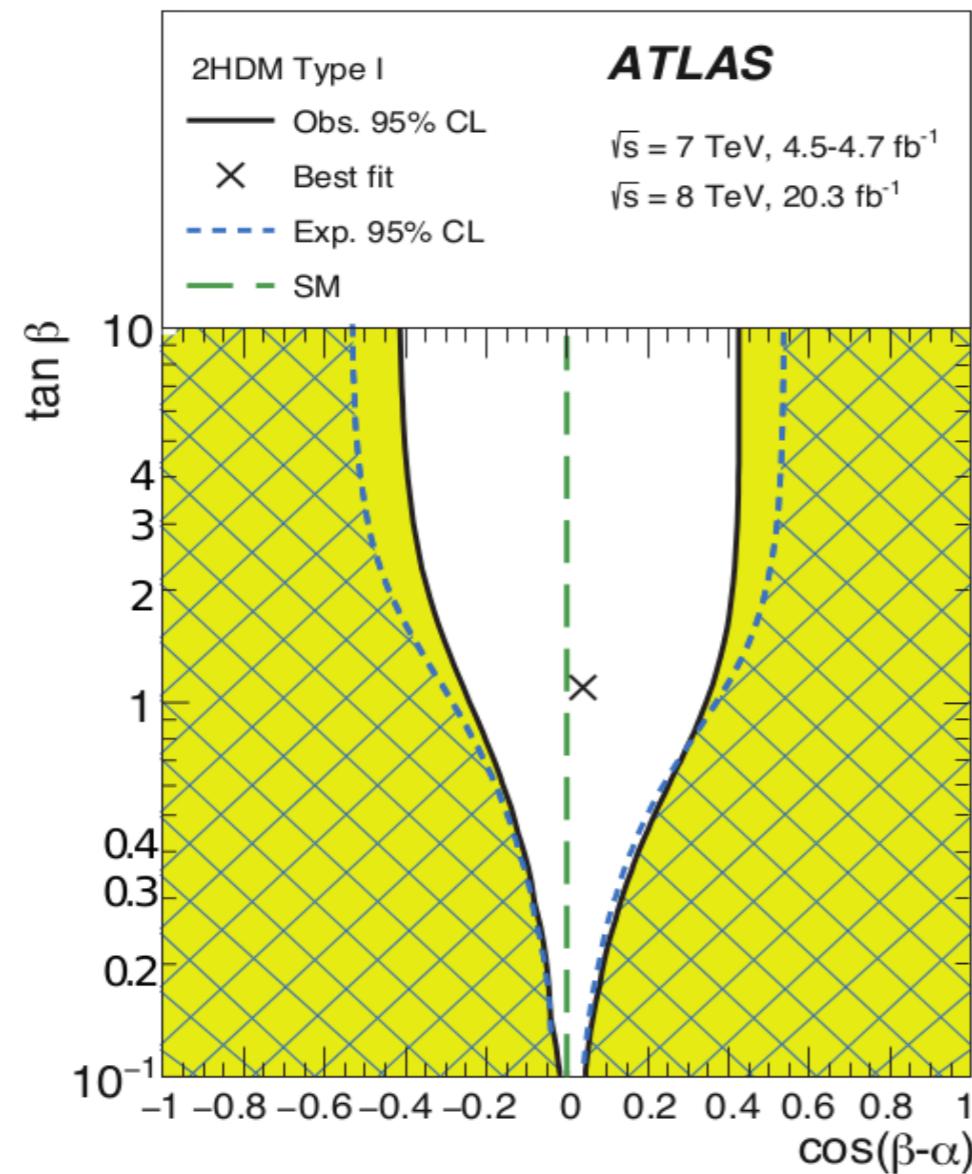
hhh @ HL-LHC = 3000 fb⁻¹ at $\sqrt{s} = 14$ TeV (ATL-PHYS-PUB-2017-001, hh->bb $\gamma\gamma$)

hhh @ ILC = 4000 fb⁻¹ at $\sqrt{s} = 500$ GeV (1506.05992, e⁺e⁻>Zhh, hh->bbbb & bbWW)

hhh @ FCC-hh = 30000 fb⁻¹ at $\sqrt{s} = 100$ TeV (1606.09408)

hhh @ CEPC/FCC-ee = 5000 fb⁻¹ at $\sqrt{s} = 240$ GeV + 1700 fb⁻¹ at $\sqrt{s} = 350$ GeV (1711.03978)

2HDM



2HDM

CMS-PAS-HIG-15-001

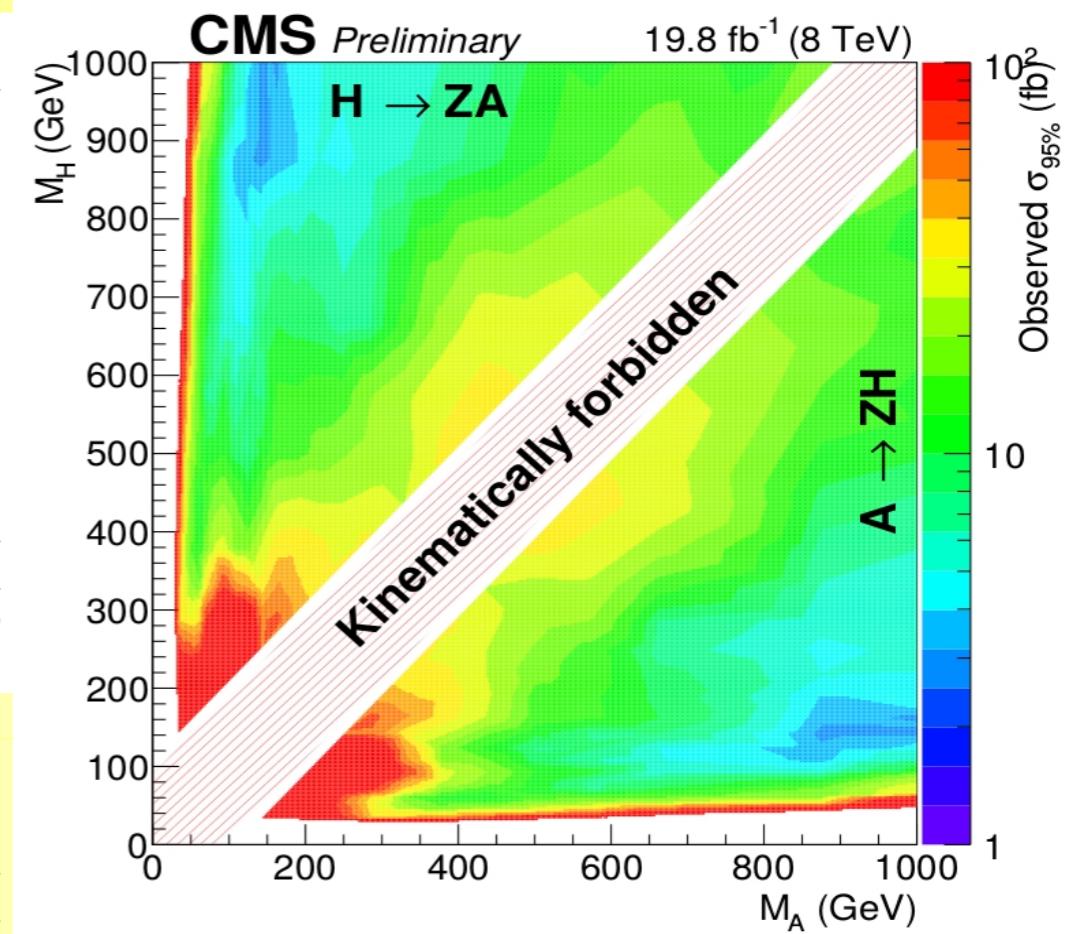
Phys. Lett. B759 (2016) 369 (ArXiv:1603.02991)

Search for H/A decaying into Z and A/H, with $Z \rightarrow \ell\ell$ and
 $A/H \rightarrow b\bar{b}$ or $A/H \rightarrow \tau\tau$

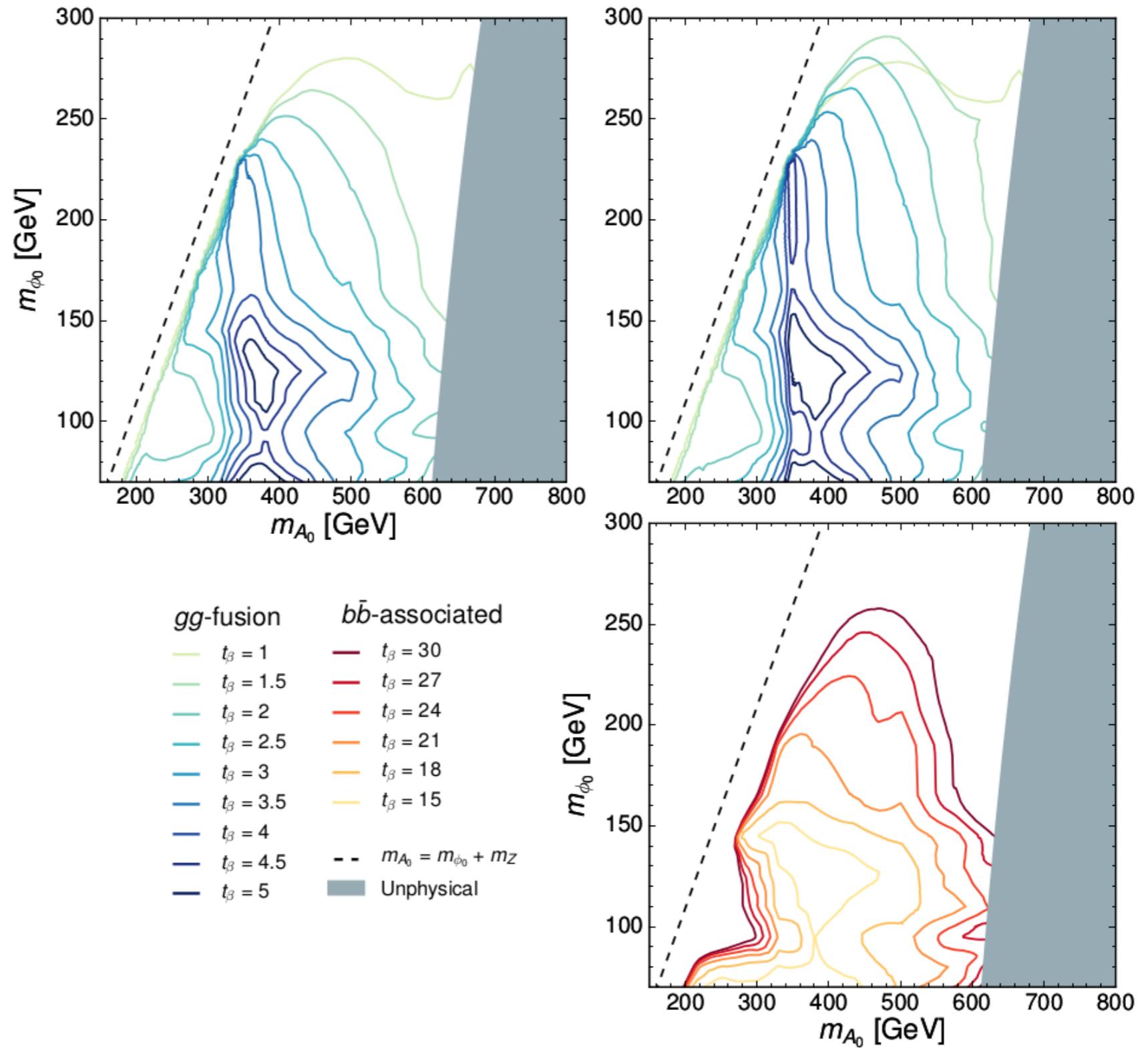
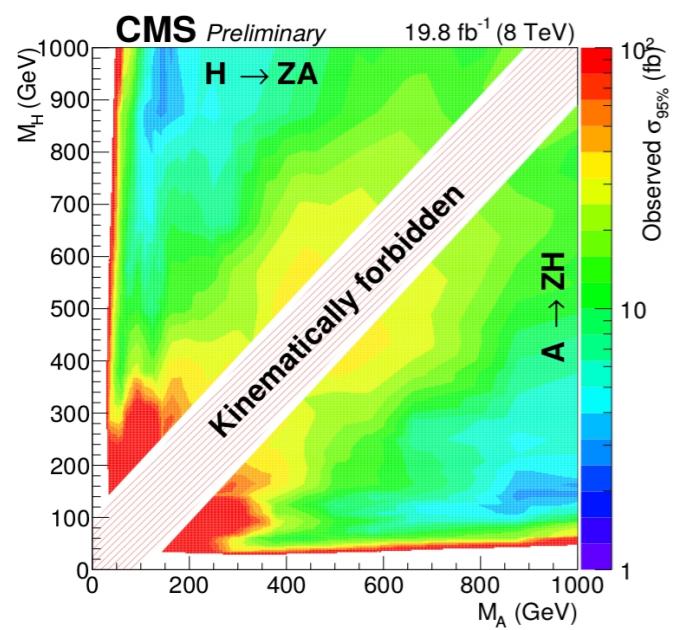
The CMS Collaboration

One important motivation for 2HDMs is that these models provide a way to explain the asymmetry between matter and anti-matter observed in the Universe [4, 5]. Another important motivation is Supersymmetry [6], which is a theory that falls in the broad class of 2HDMs. Axion models [7], which would explain how the strong interaction does not violate the CP symmetry, would give rise to an effective low-energy theory with two Higgs doublets. Finally, it has also been recently noted [8] that certain realizations of 2HDMs can accommodate the muon $g - 2$ anomaly [9] without violating the present theoretical and experimental constraints.

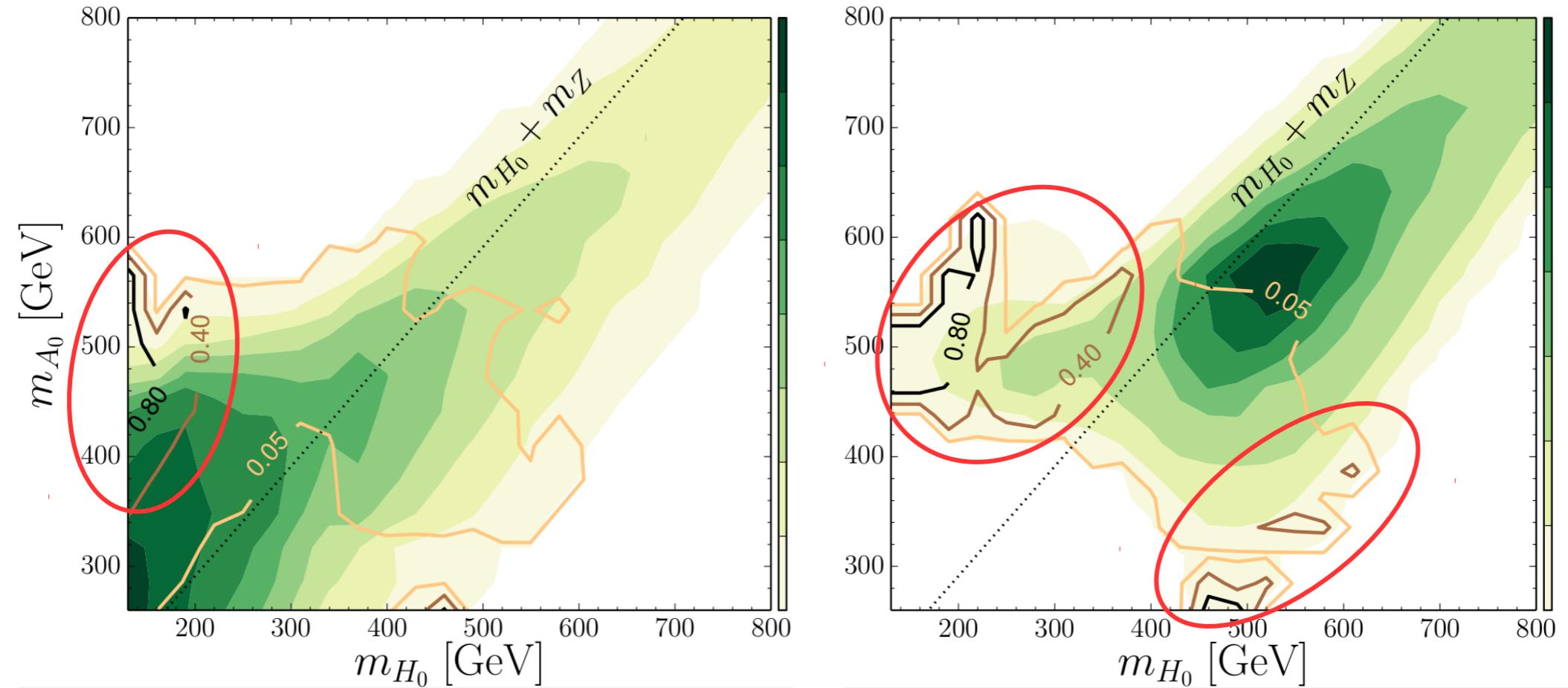
In the most general case 14 parameters are necessary to describe the scalar sector in a 2HDM. However, only 6 free parameters remain once the so-called Z_2 symmetry is imposed to suppress flavor changing neutral currents, in agreement with experimental observations, and the values of the mass of the recently discovered Higgs boson (125 GeV) and the electroweak vacuum expectation value (246 GeV) are assumed. The compatibility of a 125 GeV SM-like Higgs boson with 2HDMs is possible in the so-called alignment limit. In such a limit, one of the CP-even scalars, h or H , is identified with the 125 GeV Higgs boson and the condition $\cos(\beta - \alpha) \approx 0$ or $\sin(\beta - \alpha) \approx 0$ is satisfied, where $\tan \beta$ and α are, respectively, the ratio of the vacuum expectation values, and the mixing angle of the two Higgs doublets. A recent theoretical study [5] has shown that, in this limit, a large mass splitting (>100 GeV) between the A and H bosons would favor the electroweak phase transition that would be at the origin of the baryogenesis process in the early Universe, thus explaining the currently observed matter-antimatter asymmetry in the Universe. In such a scenario, the most frequent decay mode of the pseudoscalar A boson would be $A \rightarrow ZH$.



2HDM



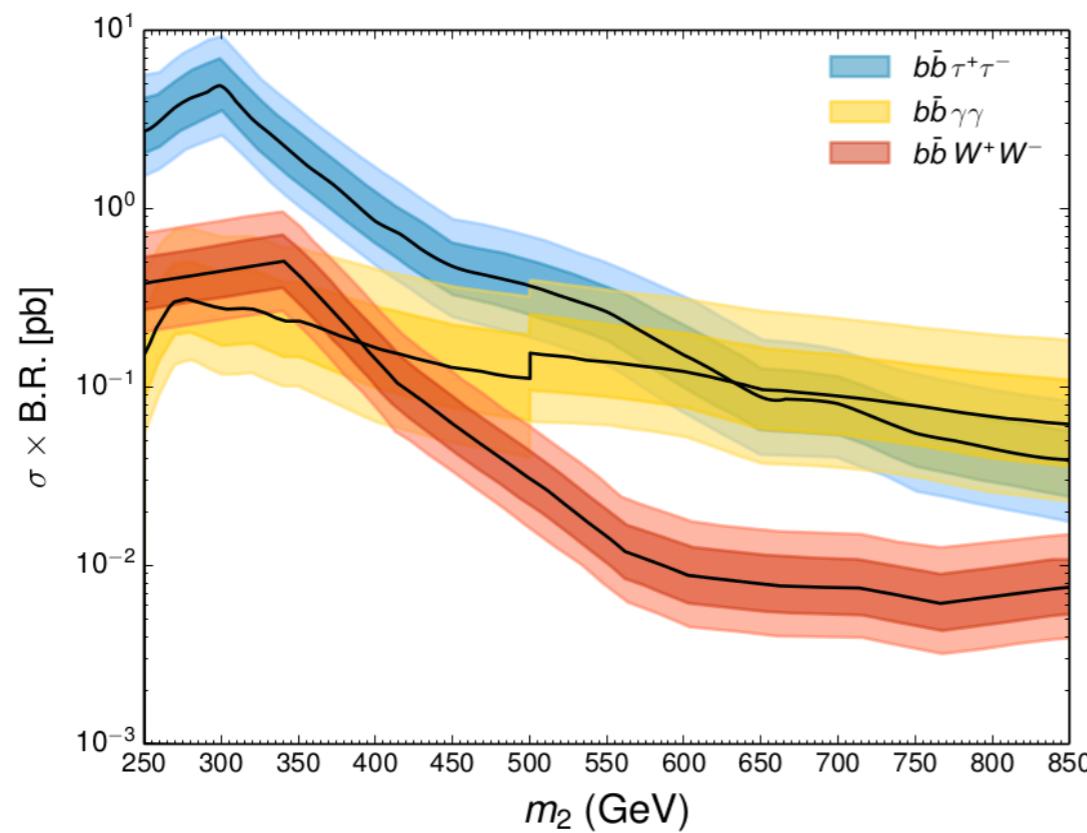
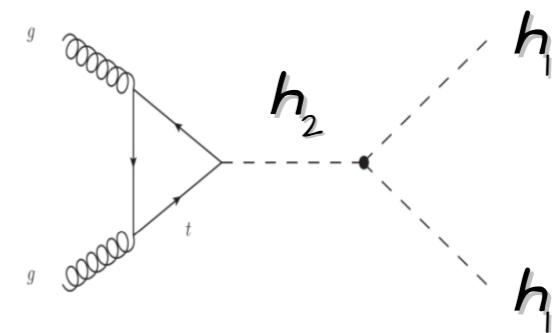
2HDM



Dorsch, Huber, Mimasu, No, JHEP **1712** (2017) 086

Singlet

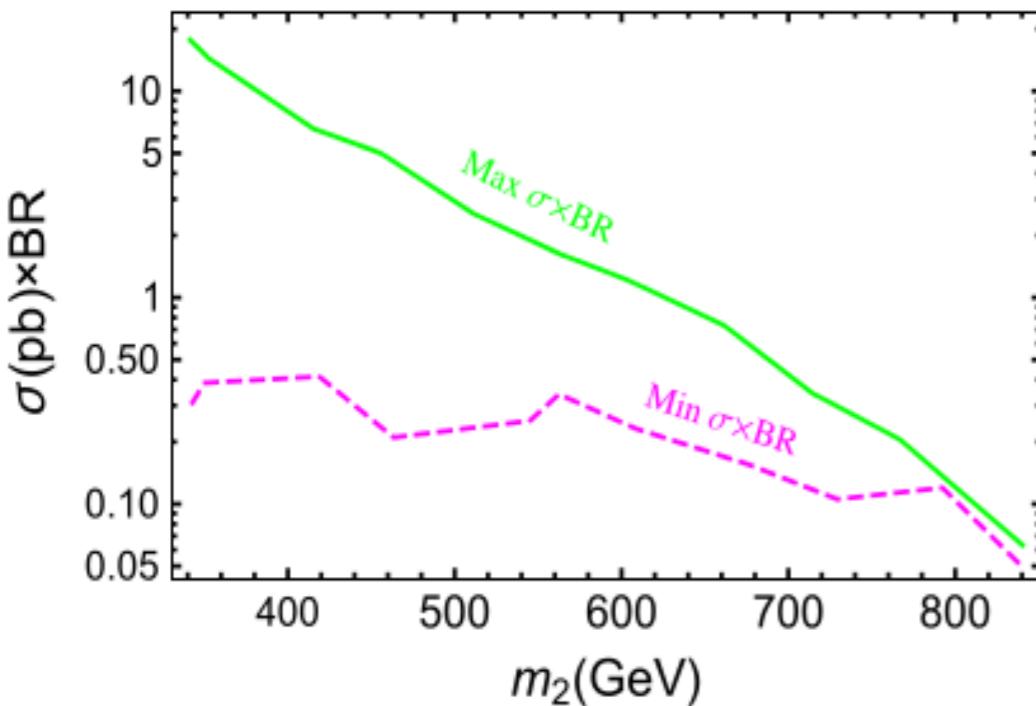
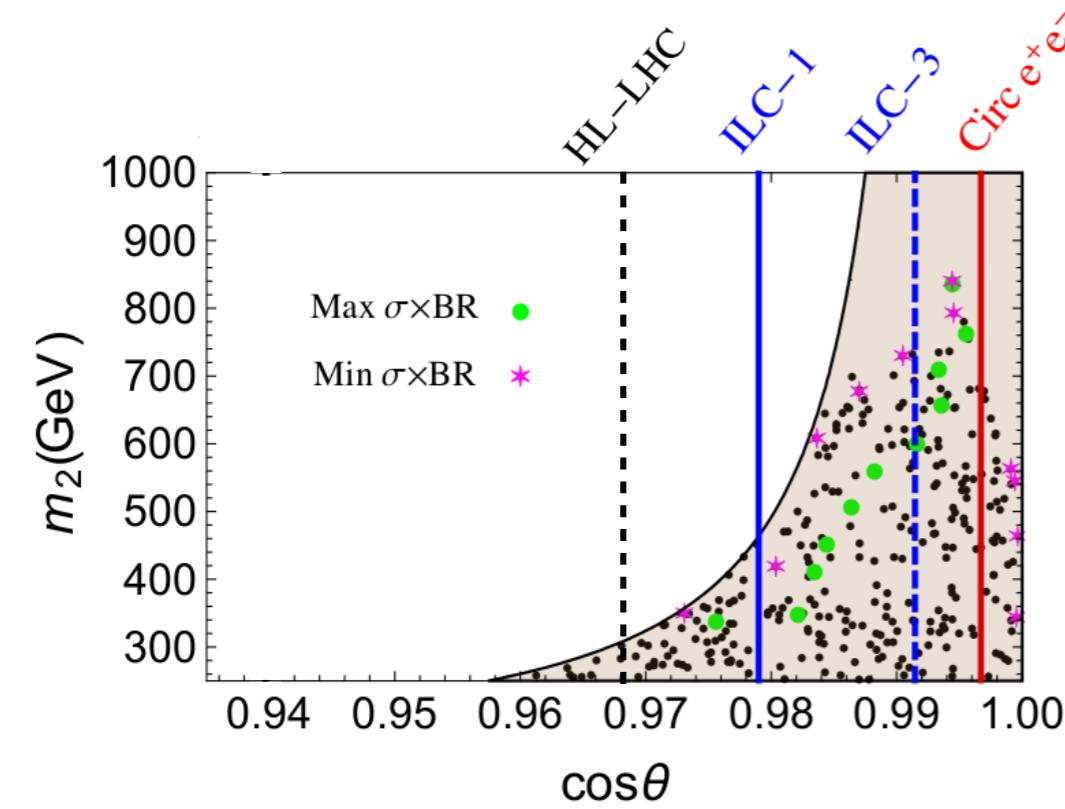
RESONANT HIGGS PAIR PRODUCTION



$$\Gamma_{h_2 \rightarrow h_1 h_1} = \frac{\lambda_{211}^2 \sqrt{1 - 4m_1^2/m_2^2}}{8\pi m_2}$$

- ▶ Scan of 1st Order EWPT Parameter Space
- ▶ Project Scan into m_2 , $\sigma(h_2) \times \text{BR}(h_2 \rightarrow h_1 h_1)$ @ 100 TeV

Kotwal, No, Ramsey-Musolf, Winslow, PRD 94 (2016) 035022



Benchmark	$\cos\theta$	$\sin\theta$	m_2 (GeV)	σ (pb)	BR
B1	0.976	0.220	341	23.9	0.74
B2	0.982	0.188	353	19.0	0.76
B3	0.983	0.181	415	20.1	0.33
B4	0.984	0.176	455	16.3	0.31
B5	0.986	0.164	511	10.8	0.24
B6	0.988	0.153	563	6.96	0.23
B7	0.992	0.129	604	4.01	0.30
B8	0.994	0.113	662	2.23	0.33
B9	0.993	0.115	714	1.73	0.20
B10	0.996	0.094	767	0.918	0.22
B11	0.994	0.105	840	0.802	0.079

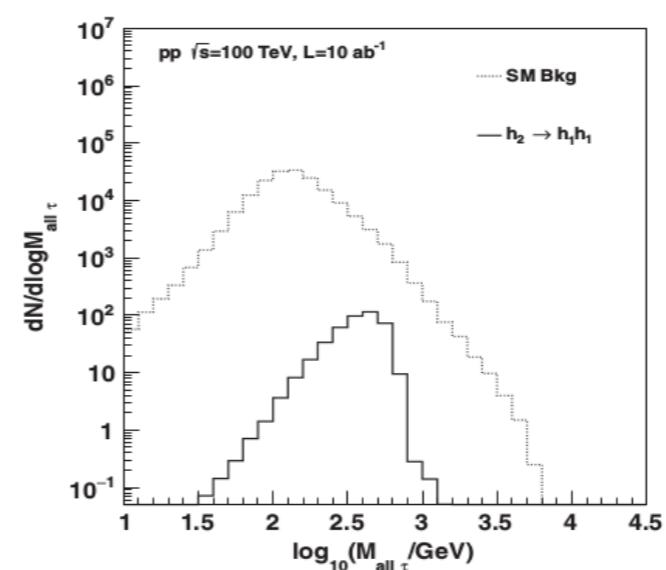
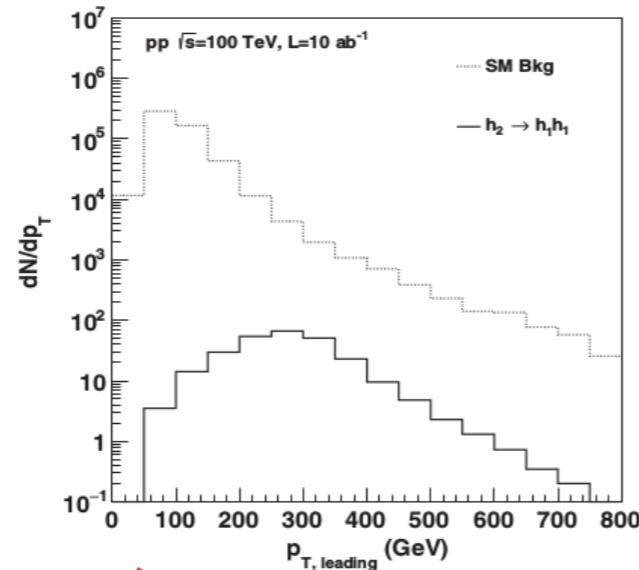
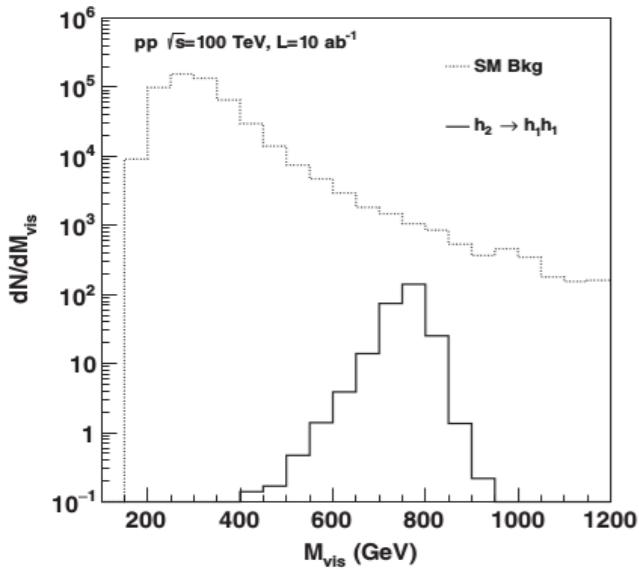
$\sim 17 \text{ pb}$ **BMmax**

Benchmark	$\cos\theta$	$\sin\theta$	m_2 (GeV)	σ (pb)	BR
B1	0.999	0.029	343	0.428	0.72
B2	0.973	0.231	350	27.8	0.014
B3	0.980	0.197	419	23.5	0.018
B4	0.999	0.026	463	0.334	0.63
B5	0.999	0.035	545	0.408	0.62
B6	0.999	0.043	563	0.553	0.62
B7	0.984	0.180	609	7.67	0.030
B8	0.987	0.161	676	4.17	0.037
B9	0.990	0.138	729	2.33	0.045
B10	0.995	0.104	792	0.991	0.12
B11	0.994	0.105	841	0.801	0.062

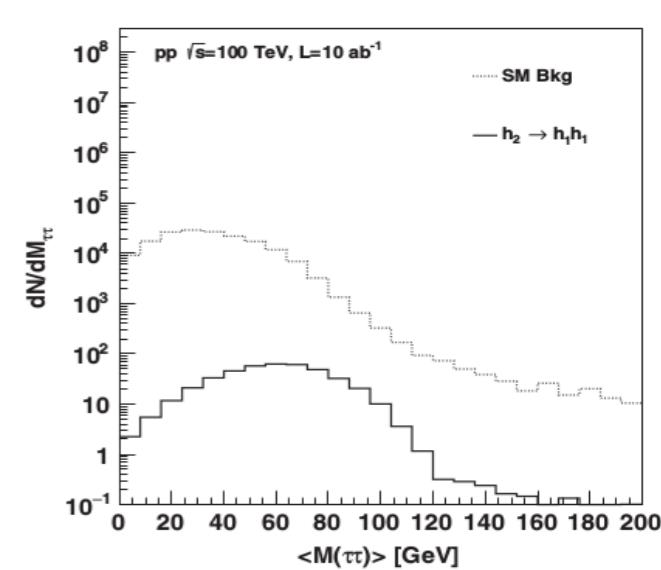
$\sim 50 \text{ fb}$ **BMmin**

Decay channel	Branching ratio
$b\bar{b}b\bar{b}$	3.33×10^{-1}
$\tau\tau b\bar{b}$	7.29×10^{-2}
$W^+(\rightarrow l\nu)W^-(\rightarrow l\nu)b\bar{b}$	1.09×10^{-2}
$\tau\tau\tau\tau$	3.99×10^{-3}
$\gamma\gamma b\bar{b}$	2.63×10^{-3}
$W^+(\rightarrow l\nu)W^-(\rightarrow l\nu)\tau\tau$	1.20×10^{-3}
$\gamma\gamma\tau\tau$	2.88×10^{-4}
$b\bar{b}\mu^+\mu^-$	2.53×10^{-4}
$Z(\rightarrow l^+l^-)Z(\rightarrow l^+l^-)b\bar{b}$	1.41×10^{-4}
$b\bar{b}Z(\rightarrow l^+l^-)\gamma$	1.21×10^{-4}

$b\bar{b}\gamma\gamma$



4τ



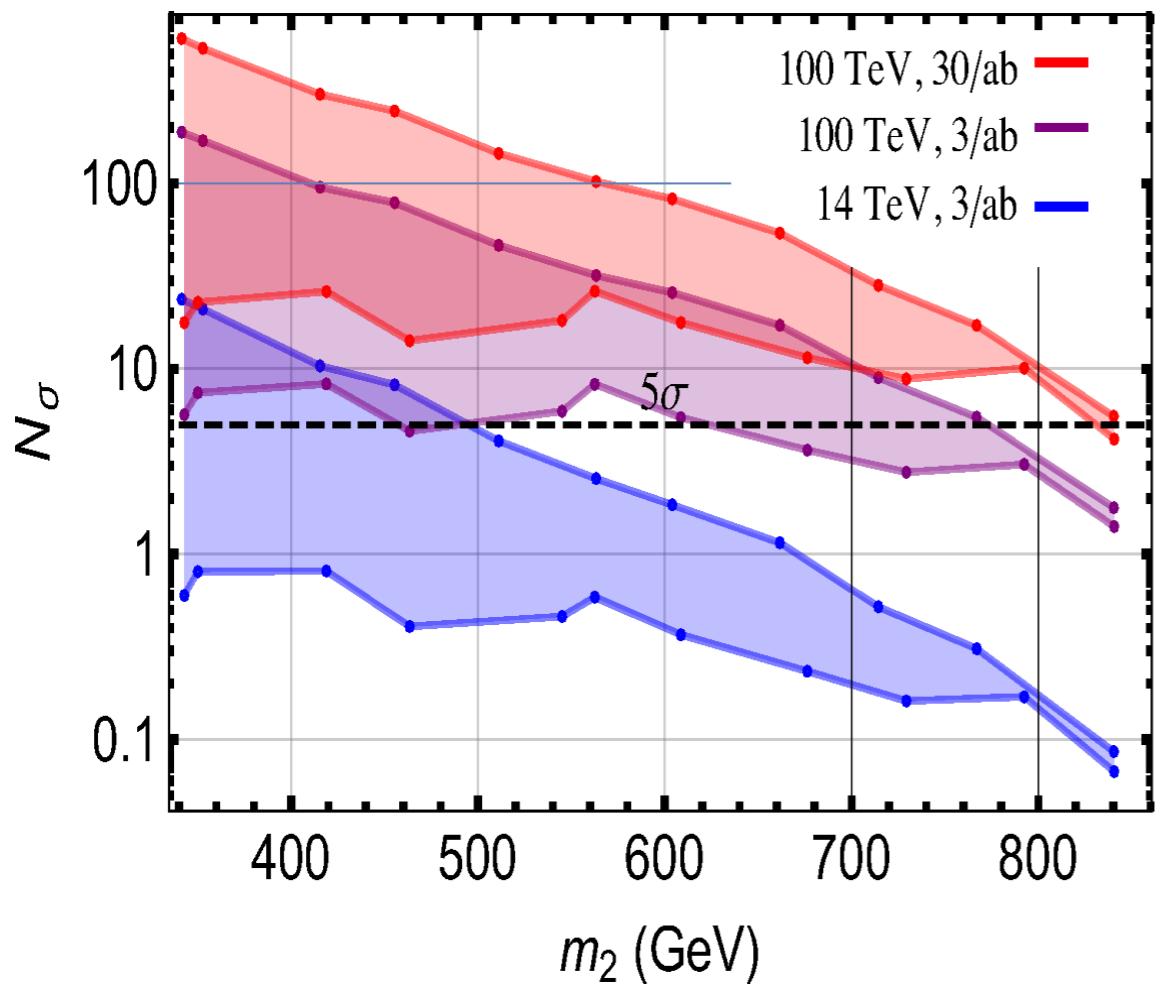
BDT analysis

(e.g. BM10)

$b\bar{b}\gamma\gamma$ and 4τ end-up yielding similar BSM sensitivity

$b\bar{b}\gamma\gamma$ better than 4τ for parameter (m_2) extraction

$h_2 \rightarrow h_1 h_1$ ($b\bar{b}\gamma\gamma + 4\tau$)



► Interplay with $h_2 \rightarrow VV$ searches

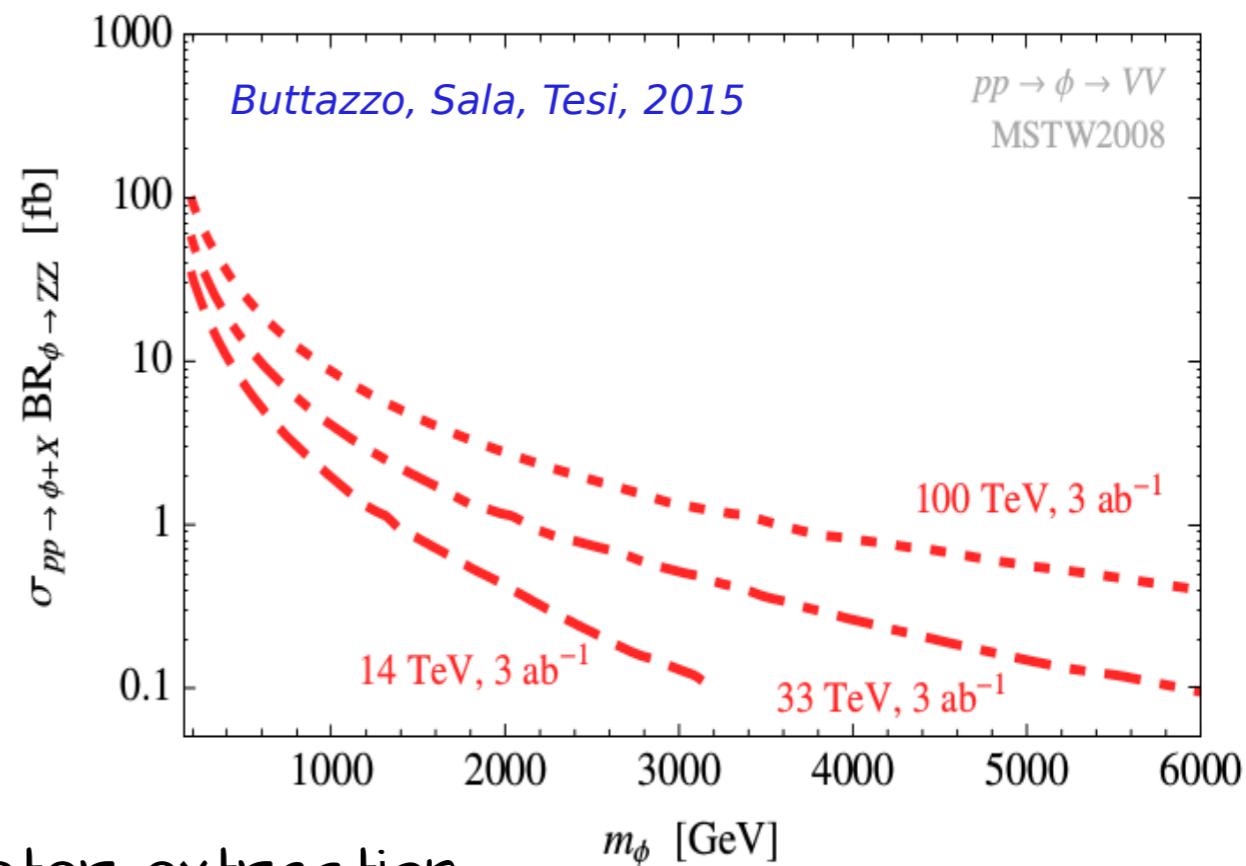
Crucial for Higgs + Singlet parameter extraction

$$\cos\theta \quad \text{vs} \quad \lambda_{211}$$

► Impact of Resonant Di-Higgs on Higgs self-coupling extraction at FCC hh

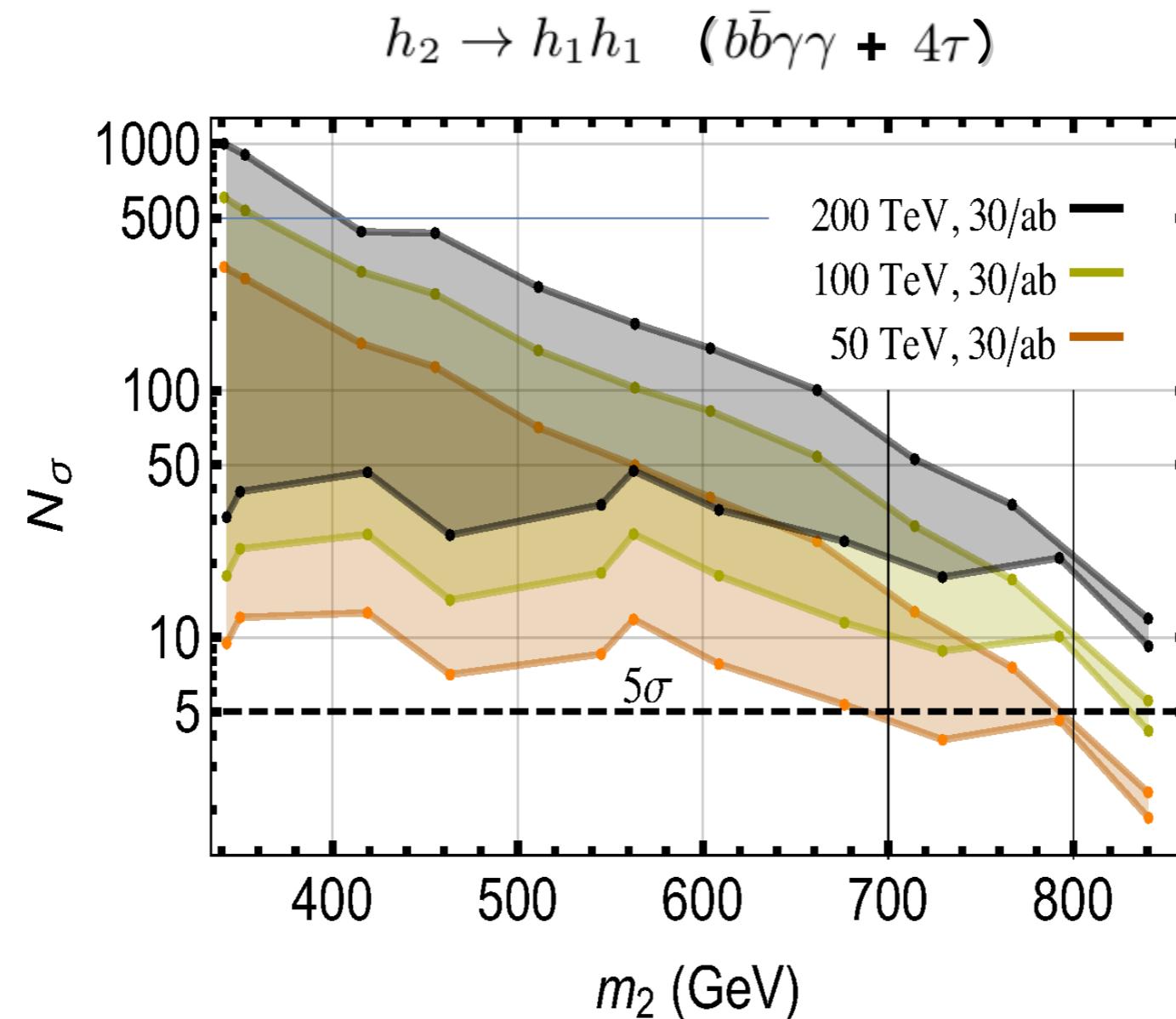
► Go beyond EWPT numerical Scan . . .

FCC hh (30 ab⁻¹) largely probes
1st Order EWPT parameter space
via $h_2 \rightarrow h_1 h_1$



How Sensitivity scales with C.O.M. Energy?

What C.O.M. Energy Needed to Quantitatively Study Singlet-Driven EWPT?



Bubble Dynamics

Laine, Phys. Rev. D49 (1994) 3647

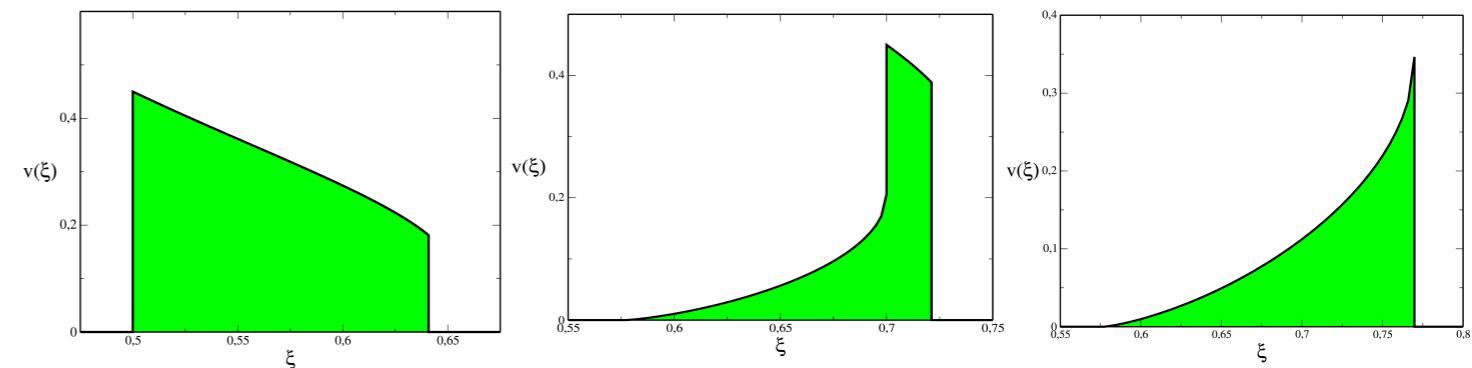
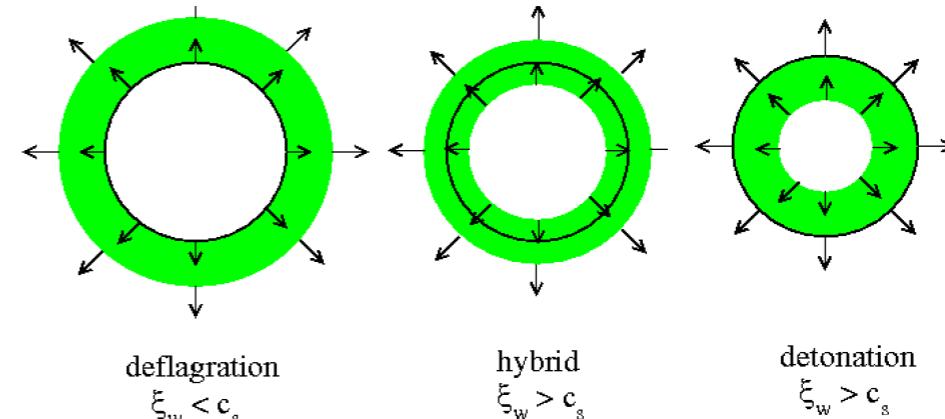
Kurki-Suonio, Laine, Phys. Rev. D51 (1995) 5431

Espinosa, Konstandin, No, Servant, JCAP 1006 (2010) 028

$$\partial_\mu T_{Plasma}^{\mu\nu} = 0 \quad v(r, t) = v(\xi = r/t)$$

$$\frac{1 - \xi v(\xi)}{1 - v^2(\xi)} \left[\frac{\mu^2}{c_s^2} - 1 \right] \partial_\xi v = 2 \frac{v(\xi)}{\xi}$$

$$w(\xi) = w_0 \exp \left[\left(1 + \frac{1}{c_s^2} \right) \int_{v_0}^{v(\xi)} \gamma^2 \mu dv \right]$$



Available PT Energy



Fluid Shells (shock waves)

Kinetic + Thermal E

ENERGY BUDGET

Kamionkowski, Kosowsky, Turner, Phys. Rev. D49 (1994) 2837

Espinosa, Konstandin, No, Servant, ICAP 1006 (2010) 028

$$\int T(r) r^2 dr = \kappa \frac{\epsilon}{3} R_{Bubble}^3$$

$$(\Delta V = \epsilon)$$

GW Source Efficiency

$$\kappa = \frac{3}{\epsilon v_W^3} \int w(\xi) v(\xi)^2 \gamma(\xi)^2 \xi^2 d\xi < 1$$