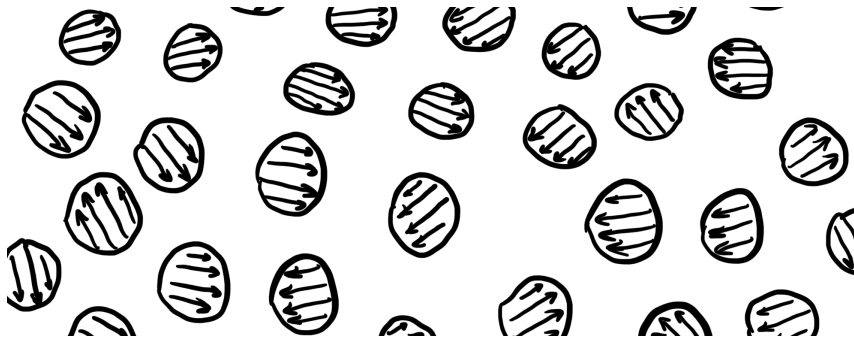


# Clumpy Polarized Vector Dark Matter and the end of inflation



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ZPW2019 Workshop - A New Look at Dark Matter

University of Zurich, January 9, 2019

Mar Bastero-Gil, Jose Santiago, Lorenzo Ubaldi, RVM: 1810.07208 + ongoing

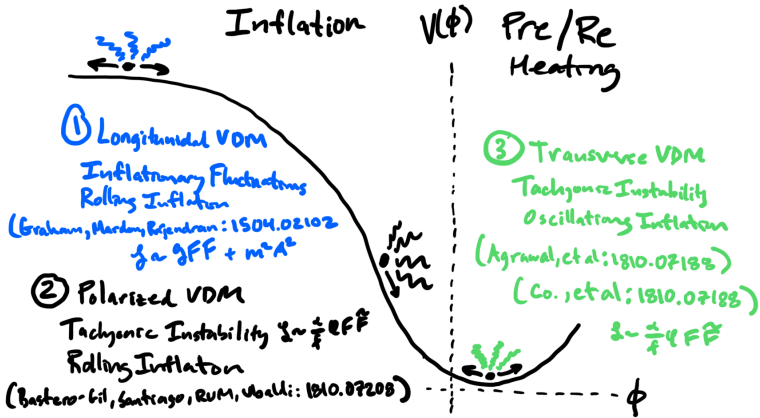
# Overview

- ▶ Context and motivation
- ▶ Polarized VDM production
- ▶ Energy density spectrum
- ▶ Ongoing/Future directions
- ▶ Summary and Conclusions

# Vector Dark Matter (VDM) Models & Pheno

- ▶ VDM an exciting topic due to **recent progress**
- ▶ **Interesting for pheno reasons**: dark photon experiments, indirect/direct detection, lensing, GWs, super radiance, etc.
- ▶ **Can appear in many models**: pseudo scalar inflation, QCD axion mechanisms, dark Gauge/Higgs sectors, relaxions
- ▶ (So far) generically five **VDM production mechanisms**:
  - ▶ freeze-in: [0811.0326](#)
  - ▶ mis-alignment: [1105.2812](#), [1201.5902](#)
  - ▶ parametric enhancement: [1810.07195](#)
  - ▶ inflationary fluctuations: [1504.02102](#)
  - ▶ **tachyonic instability**: [1810.07196](#), [1810.07195](#), [1810.07208](#)
- ▶ Tachyonic instability well **studied in many contexts**  
(axion inflation, dissipation in inflation and relaxion mechanisms, primordial magnetic fields, baryo/lepto genesis, chiral gravitational waves during inflation, preheating, decreasing abundance of QCD axion DM)

# Recent VDM Production Mechanisms

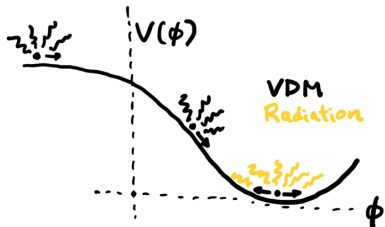


\* Misalignment,  
 Freeze-In



④ Longitudinal VDM  
 Parametric Enhancement  
 Dark Higgs Mechanism  
 (Dror, Harigaya, Narayan: 1810.07195)  
 $\xi \sim \frac{1}{4} \frac{H^2}{M^2} - V(\psi)$

# Clumpy Polarized Vector DM Production



Can **account for observed DM**  
for masses  $\sim 10^{-15} - 10^6$  GeV

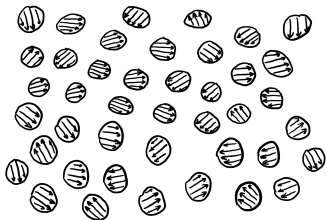
This mechanism naturally leads  
to **various novel features**:

- ▶ Energy density spectrum contains **information on inflaton potential**
- ▶ Typical scale at which VDM 'clumps' directly tied to scale at end of inflation  $\Rightarrow$  **peak in energy density spectrum**
- ▶ Only one polarization produced tachyonically during slow roll of inflaton  $\Rightarrow$  **VDM is polarized**

The coupling  $\phi F\tilde{F}$  leads to a **tachyonic instability** and **exponential production** of one transverse polarization

Reaches its maximum near the **end of inflation**

Inflaton decays perturbatively into radiation  $\Rightarrow$  reheating



# Action and Equations of Motion

Starting point is the **action** for a (massive or massless) vector boson coupled to the inflaton via a **pseudo scalar coupling**:

$$S = - \int d^4x \sqrt{-g} \left[ \frac{1}{2} \partial_\mu \phi \partial^\mu \phi + V(\phi) \right. \\ \left. + \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} m^2 A_\mu A^\mu + \frac{\alpha}{4f} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} \right]$$

(Mass can be Stuckelberg OR Higgsed. Neglect possible  $U(1)$  kinetic mixing with hypercharge)

Inflaton **potential is generic** & defines the Hubble scale:  $H = \frac{\sqrt{V(\phi)}}{\sqrt{3}M_{\text{Pl}}}$

Gives **EOM** for inflaton, longitudinal, & transverse VDM modes:

$$\ddot{\phi} + 3H\dot{\phi} + V' = \frac{\alpha}{f} F\tilde{F} \approx 0, \\ \ddot{A}_\pm + H\dot{A}_\pm + \left( \frac{k^2}{a^2} \pm \frac{k}{a} \frac{\alpha\dot{\phi}}{f} + m^2 \right) A_\pm = 0, \\ \ddot{A}_L + \frac{3k^2 + a^2 m^2}{k^2 + a^2 m^2} H\dot{A}_L + \left( \frac{k^2}{a^2} + m^2 \right) A_L = 0$$

(P. W. Graham, J. Mardon, S. Rajendran: 1504.02102)

# Tachyonic instability during slow roll

Customary to define the tachyonic enhancement parameter:

$$\xi \equiv \frac{\alpha \dot{\phi}}{2Hf} = \sqrt{\frac{\epsilon}{2}} \frac{\alpha}{f} M_{\text{Pl}}, \quad \delta\xi = \mathcal{O}(10) \text{ over } 60 \text{ e-folds}$$

(Increases with increasing  $\dot{\phi}$  and decreasing  $H$  until end of inflation)

**Controls exponential enhancement** and related to potential via

$$\epsilon \equiv -\dot{H}/H^2, \quad |\dot{\phi}| \approx V'/3H, \quad \epsilon = \frac{\dot{\phi}^2}{2H^2 M_{\text{Pl}}^2}$$

Defining  $\bar{m} \equiv m/H$  and using  $\tau < 0$ ,  $\tau \simeq -\frac{1}{aH}$  during inflation, obtain **transverse mode EOM in conformal time** ( $ad\tau = dt$ ):

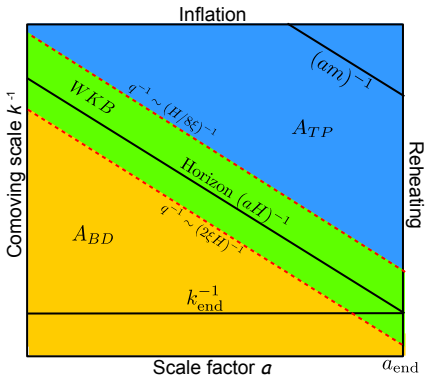
$$\left[ \frac{\partial^2}{\partial \tau^2} + k^2 \pm 2k \frac{\xi}{\tau} + \frac{\bar{m}^2}{\tau^2} \right] A_{\pm}(k, \tau) = A''_{\pm} + \omega^2(k, \tau) A_{\pm} = 0$$

With convention  $\dot{\phi} > 0$  we have  $\xi > 0 \Rightarrow$  **ONLY the  $A_+$  mode experiences tachyonic enhancement** when frequency satisfies:

$$\Omega^2(k, \tau) = -\omega^2(k, \tau) = -(k^2 + 2k \frac{\xi}{\tau} + \frac{\bar{m}^2}{\tau^2}) > 0 \quad (\text{note: } -\infty < \tau < 0)$$

# Exponentially Enhanced Tachyonic Mode ( $\bar{m} \ll 1$ )

**Tachyonic instability** ( $\Omega^2 > 0$ ) triggered when physical momenta satisfy  $q = k/a < 2\xi H \Rightarrow$  **wavelength of order horizon**  $q^{-1} \sim H^{-1}$



**Conformal diagram** gives intuition on amplitudes:

$$\lim_{-k\tau \rightarrow \infty} A_{\pm}(k, \tau) = \frac{e^{-ik\tau}}{\sqrt{2k}} \equiv A_{BD}$$

$$A_{+}(k, \tau) \simeq \sqrt{\frac{-2\tau}{\pi}} e^{\pi\xi} K_1 \left[ 2\sqrt{-2\xi k\tau} \right]$$

( $-k\tau < 2\xi$ ,  $K_1 \equiv$  modified Bessel 2nd kind)

$$\lim_{-k\tau \rightarrow 0} A_{+}(k, \tau) = \frac{e^{\pi\xi}}{2\sqrt{2\pi k\xi}} \equiv A_{TP}$$

[Well known solutions (constant  $\xi$ ) from gauge field production mechanisms: **Anber & Sorbo: 0606534**]

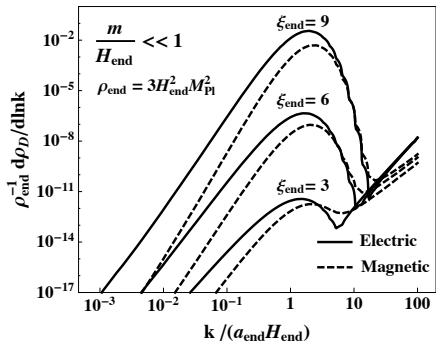
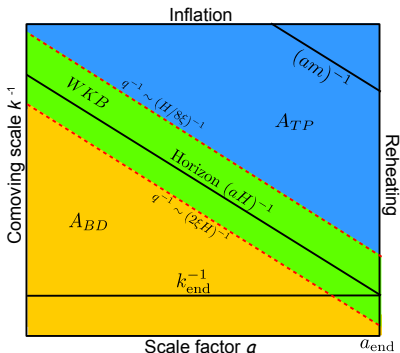
The amplitude at horizon crossing (where **most of the power** is) is well **approximated by WKB** in the range  $H/8\xi < q < 2\xi H$

$$A_{+}(k, \tau)_{\text{WKB}} \simeq \frac{1}{\sqrt{2k}} \left( \frac{-k\tau}{2\xi} \right)^{1/4} e^{\pi\xi - 2\sqrt{-2\xi k\tau}}$$



# Input energy spectrum at end of inflation

While WKB is useful for intuition, since  $\xi$  is time dependent, need to numerically solve EOM to obtain accurate spectrum



VDM has dark 'magnetic' & 'electric' energy density contribution

$$\frac{d\rho}{d \ln k} = \frac{1}{2a^4} \left( \frac{k^3}{2\pi^2} \right) \left( |\partial_\tau A(k, \tau)|^2 + (k^2 + a^2 m^2) |A(k, \tau)|^2 \right) = \frac{d\rho_E}{d \ln k} + \frac{d\rho_B}{d \ln k}$$

Peak at  $k^{-1} \sim k_{\text{end}}^{-1} \ll k_{\text{CMB}}^{-1} \Rightarrow$  power suppressed at CMB scales

# Estimating the VDM Relic Abundance

**Inflaton energy** converted to VDM and radiation:

$$\rho_I = V(\phi) = 3H^2 M_{\text{Pl}}^2$$

Energy stored in **radiation**:

$$\begin{aligned}\rho_R(T_{\text{RH}}) &= \frac{\pi^2}{30} g_*(T_{\text{RH}}) T_{\text{RH}}^4 \\ &= \epsilon_R^4 3H^2 M_{\text{Pl}}^2 = \epsilon_R^4 \rho_I\end{aligned}$$

Defines **reheat temperature**:

$$T_{\text{RH}} = \epsilon_R \left( \frac{90}{\pi^2 g_*(T_{\text{RH}})} \right)^{1/4} \sqrt{HM_{\text{Pl}}}$$

We assume **instant reheating**:

$$\Rightarrow a_{\text{end}} = a_{\text{RH}}$$

**Initial VDM energy density** produced **at end of inflation** is estimated using WKB

$$\rho_D \approx 10^{-4} \frac{H_{\text{end}}^4}{\xi_{\text{end}}^3} e^{2\pi\xi_{\text{end}}}$$

Hubble parameter decreases (slowly) until inflation ends:

$$H_{\text{end}} = \epsilon_H H$$

To estimate relic abundance today, must **track redshift of VDM energy density**

We **parametrize** ignorance of **potential**  $V(\phi)$  with  $\epsilon_R, \epsilon_H$

## Redshift of energy density

At end of inflation, **energy density peaked** at  $k \sim a_{\text{end}} H_{\text{end}}$

**Modes contributing most** to  $\rho_D(T_{\text{RH}})$  have physical momentum:

$$q(T_{\text{RH}}) \equiv \frac{k}{a_{\text{end}}} \sim H_{\text{end}}$$

At reheating we have  $q(T_{\text{RH}}) \gg m$  and  $q(T)$  then **redshifts** as,

$$q(T) = q(T_{\text{RH}}) \frac{T}{T_{\text{RH}}}$$

VDM becomes **non-relativistic at temperature  $\bar{T}$**  defined by,

$$q(\bar{T}) = m \quad \Rightarrow \quad \bar{T} = m \left( \frac{90}{\pi^2 g_*(T_{\text{RH}})} \right)^{1/4} \frac{\epsilon_R}{\epsilon_H} \left( \frac{M_{\text{Pl}}}{H} \right)^{1/2}$$

Above (below)  $\bar{T}$  **energy density redshifts** like radiation (matter)

# Relic Density of Polarized VDM

**VDM relic density today** normalized to observed amount of CDM:

$$\frac{\Omega_T}{\Omega_{\text{CDM}}} = 7 \times 10^{-6} \left( \frac{m}{\text{GeV}} \right) \left( \frac{H}{10^{11} \text{ GeV}} \right)^{3/2} \left( \frac{\epsilon_H}{\epsilon_R} \right)^3 \left( \frac{e^{2\pi\xi_{\text{end}}}}{\xi_{\text{end}}^3} \right)$$

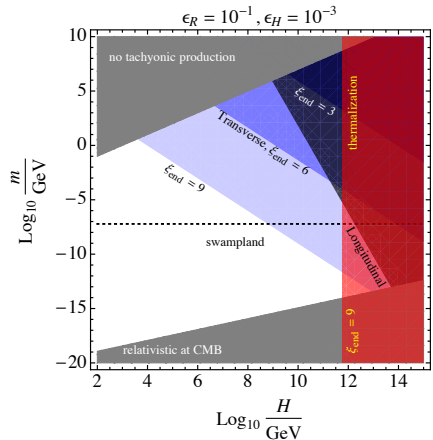
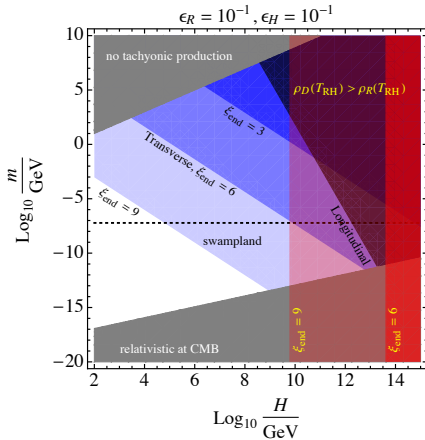
We see  $\Omega_T/\Omega_{\text{CDM}}$  **depends on 5 parameters**:  $m$ ,  $H$ ,  $\xi_{\text{end}}$ ,  $\epsilon_H$ ,  $\epsilon_R$

**Various constraints** must be satisfied for a viable VDM candidate:

- ▶  $m \ll q(T_{\text{RH}})$  for **efficient tachyonic production** at end of inflation
- ▶ VDM becomes (cold) **non-relativistic before MRE**  $\Rightarrow \bar{T} > T_{\text{CMB}}$
- ▶ At RH, **energy in radiation greater than VDM**  $\Rightarrow \rho_R(T_{\text{RH}}) > \rho_D(T_{\text{RH}})$
- ▶ Inflaton & **VDM must not thermalize**  $\Rightarrow$  **upper bound on  $\xi$**  (& kinetic mixing)  
(no other light fields in the dark sector which couple to VDM  $\Rightarrow$  Schwinger effect: [1706.03072](#))
- ▶ Assume **negligible back-reaction** effects on the inflaton dynamics  
(neglect VDM production from inflaton oscillations after inflation: [1810.07188](#), [1810.07188](#))

Imposing constraints  $\Rightarrow$  allowed **parameter space** in  $m - H$  plane

# Parameter Space for VDM Relic Abundance



We have also included relic density of longitudinal component:

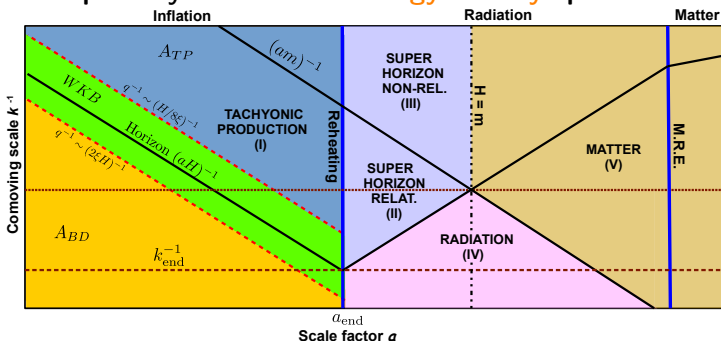
$$\frac{\Omega_L}{\Omega_{\text{CDM}}} = \left( \frac{m}{6 \times 10^{-15} \text{ GeV}} \right)^{1/2} \left( \frac{H}{10^{14} \text{ GeV}} \right)^2$$

(P. W. Graham, J. Mardon, S. Rajendran: 1504.02102)

# Cosmological Evolution of Tachyonic Modes

Energy density spectrum has implications for how **VDM clumps**

Relevant quantity is **late time energy density spectrum**



Can **analytically solve approximate EOMs** in different regions

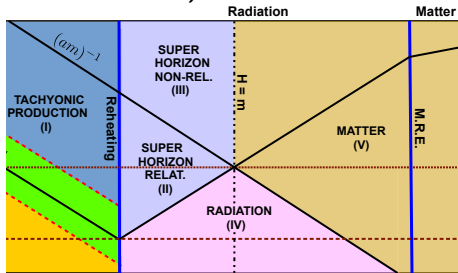
$$\ddot{A}_{\pm} + H\dot{A}_{\pm} + \left(\frac{k^2}{a^2} + m^2\right) A_{\pm} = 0 \quad (\text{after inflation})$$

Must **track evolution of 'electric' and 'magnetic' energy density**

$$\frac{d\rho}{d \ln k} = \left(\frac{k^3}{2\pi^2}\right) \left(\frac{H^2}{2} |\partial_a A(k, a)|^2 + \frac{1}{2a^2} \left(\frac{k^2}{a^2} + m^2\right) |A(k, a)|^2\right) = \frac{d\rho_E}{d \ln k} + \frac{d\rho_B}{d \ln k}$$

# Cosmological Evolution of 'Magnetic' Modes

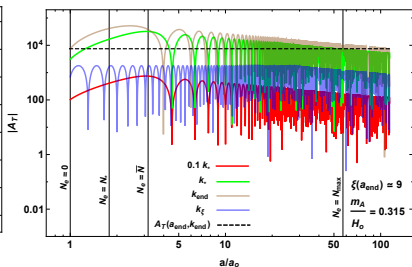
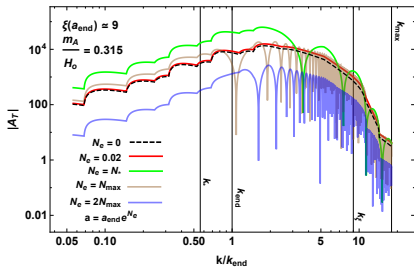
(PRELIMINARY)



'Glue' approx. solutions together at boundaries:

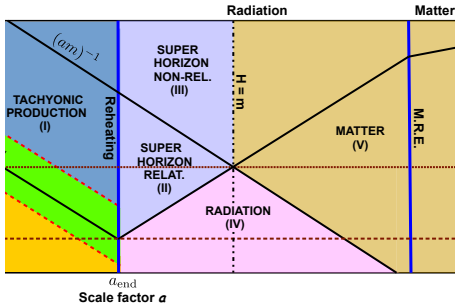
$$\begin{aligned}
 (I) \quad A_+ &= A_{\text{TP}} \\
 (II) \quad A_+ &= c_1 + c_2 a \\
 (III) \quad A_+ &= c_1 + c_2 a \\
 (IV) \quad A_+ &= (a_4 e^{ik\tau} + b_4 e^{-ik\tau}) \\
 (V) \quad A_+ &= \frac{1}{\sqrt{a}} (a_5 e^{imt} + b_5 e^{-imt})
 \end{aligned}$$

Scale factor  $a$



# Cosmological Evolution of 'Electric' Modes

(PRELIMINARY)



'Glue' approx. solutions together at boundaries:

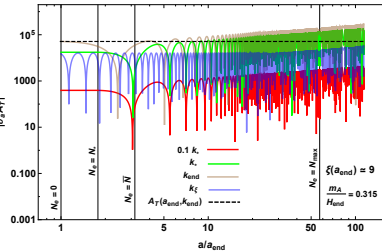
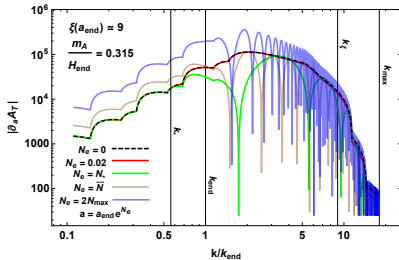
$$(I) \partial_a A_+ = A'_{\text{TP}}$$

$$(II) \partial_a A_+ = c_1$$

$$(III) \partial_a A_+ = c_1$$

$$(IV) \partial_a A_+ = \frac{ik}{a_{\text{end}}^2 H_{\text{end}}} (a_4 e^{ik\tau} - b_4 e^{-ik\tau})$$

$$(V) \partial_a A_+ = \frac{im\sqrt{a}}{a_{\text{end}}^2 H_{\text{end}}} (a_5 e^{imt} - b_5 e^{-imt})$$

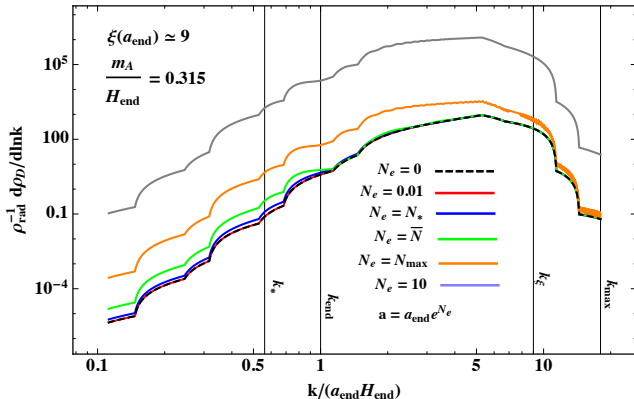




# Late Time Energy Density Spectrum (PRELIMINARY)

$$\frac{d\rho}{d \ln k} = \left(\frac{k^3}{2\pi^2}\right) \left(\frac{H^2}{2} |\partial_a A(k, a)|^2 + \frac{1}{2a^2} \left(\frac{k^2}{a^2} + m^2\right) |A(k, a)|^2\right)$$

Have a **peak at late times**  $\Rightarrow$  implications for structure/clumping



Scale at **end of inflation** connected to scale of VDM clumping  
 Scale of clumping is  $\sqrt{\bar{m}}$  smaller than for longitudinal mode

# Ongoing/Future Work & Summary/Conclusions

- ▶ Ongoing/Future work:
  - ▶ Explore implications of energy density spectrum on VDM **clumping and structure formation**
  - ▶ Examine regions of parameter space where **both longitudinal and transverse** modes give comparable contributions
  - ▶ Study energy density **spectrum for different inflation models**
  - ▶ Explore phenomenology associated with **polarization**
  - ▶ Explore effects of **Stueckelberg vs Higgsed** VDM mass
- ▶ Summary and Conclusions:
  - ▶ We have presented a **new VDM production mechanism**
  - ▶ **Relic abundance** obtained for VDM masses  $10^{-15} - 10^6$  GeV
  - ▶ VDM is **polarized with peak** in energy density spectrum
  - ▶ Clumping scale (peak) **connected to scale at end of inflation**
  - ▶ Mechanism works for **Stueckelberg or Higgsed** VDM mass
  - ▶ Much **phenomenology** yet to explore!

# THANKS!

