



X. Buffat

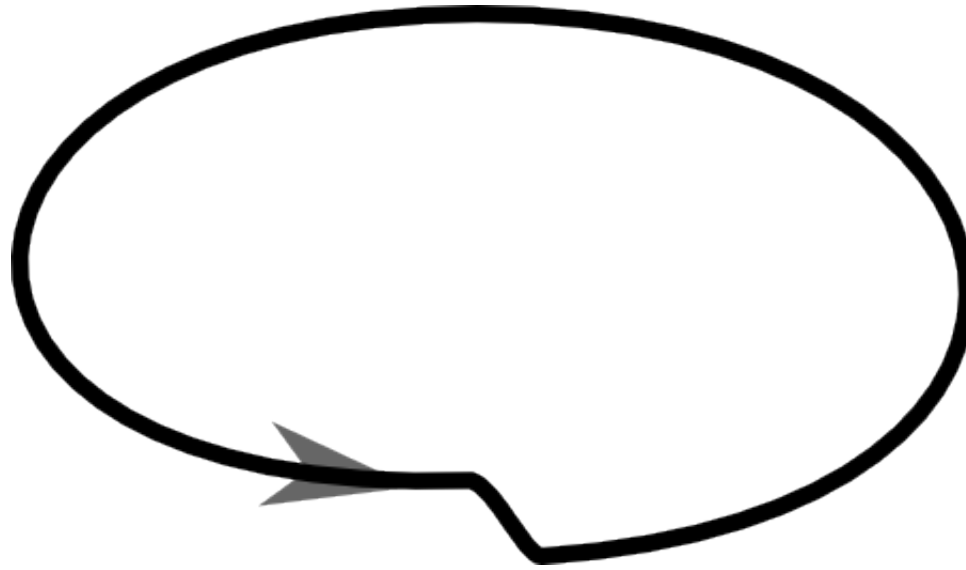
Acknowledgments : L. Barraud, S. Fartoukh, W. Herr, N. Mounet, E. Métral, T. Persson, T. Pieloni\*, A. Ribes Metidieri, B. Salvant, C. Tambasco\*, R. Tomas, S.M. White\*\*



# Content

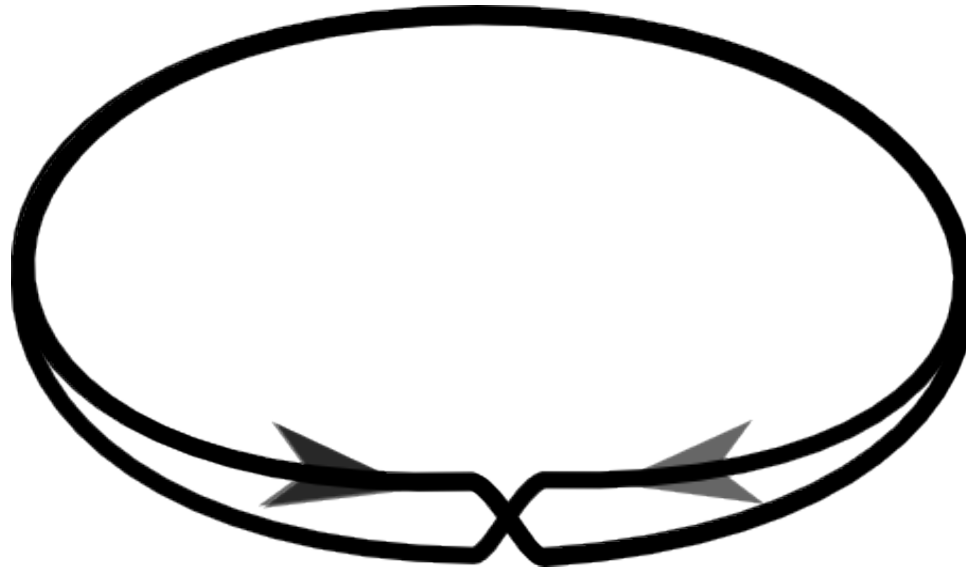
- Coherent beam-beam modes
  - Coherent resonance : The issue with asymmetric machines
  - The mode coupling instability of colliding beams
  - Longitudinal beam-beam mode : The Las Ketchup instability
- Amplitude detuning and Landau damping
  - Long-range
  - Offset and crossing angle : The Shakiri effect
  - Head-on interaction
- PACMAN linear coupling

# Coherent beam-beam mode



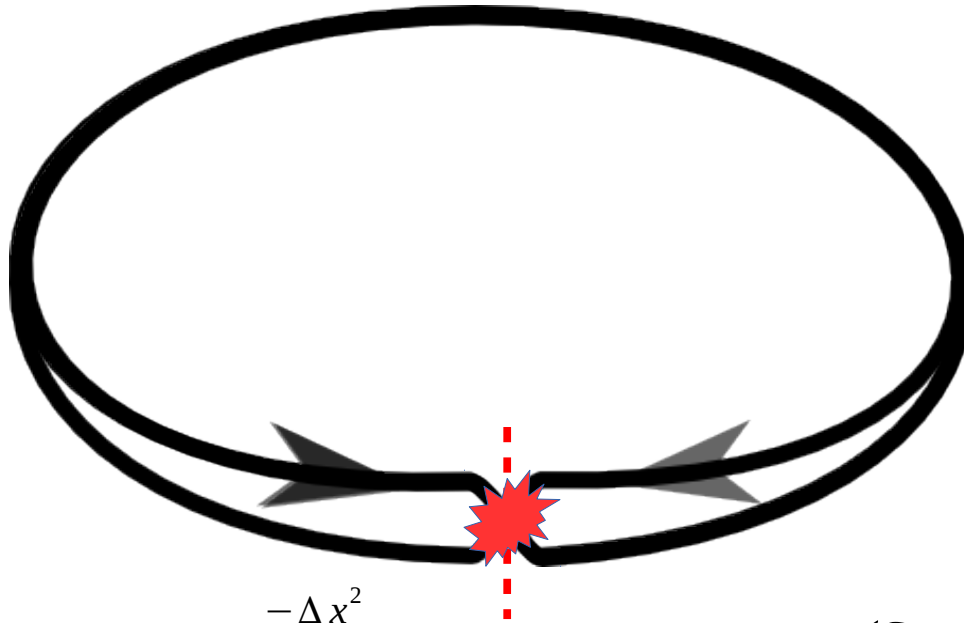
$$\begin{pmatrix} x_1 \\ x_1' \end{pmatrix}_{t+1} = \begin{pmatrix} \cos(2\pi Q) & \sin(2\pi Q) \\ -\sin(2\pi Q) & \cos(2\pi Q) \end{pmatrix} \begin{pmatrix} x_1 \\ x_1' \end{pmatrix}_t$$

# Coherent beam-beam mode



$$\begin{pmatrix} x_{B1} \\ x_{B1}' \\ x_{B2} \\ x_{B2}' \end{pmatrix}_{t+1} = \begin{pmatrix} \cos(2\pi Q) & \sin(2\pi Q) & 0 & 0 \\ -\sin(2\pi Q) & \cos(2\pi Q) & 0 & 0 \\ 0 & 0 & \cos(2\pi Q) & \sin(2\pi Q) \\ 0 & 0 & -\sin(2\pi Q) & \cos(2\pi Q) \end{pmatrix} \begin{pmatrix} x_{B1} \\ x_{B1}' \\ x_{B2} \\ x_{B2}' \end{pmatrix}_t$$

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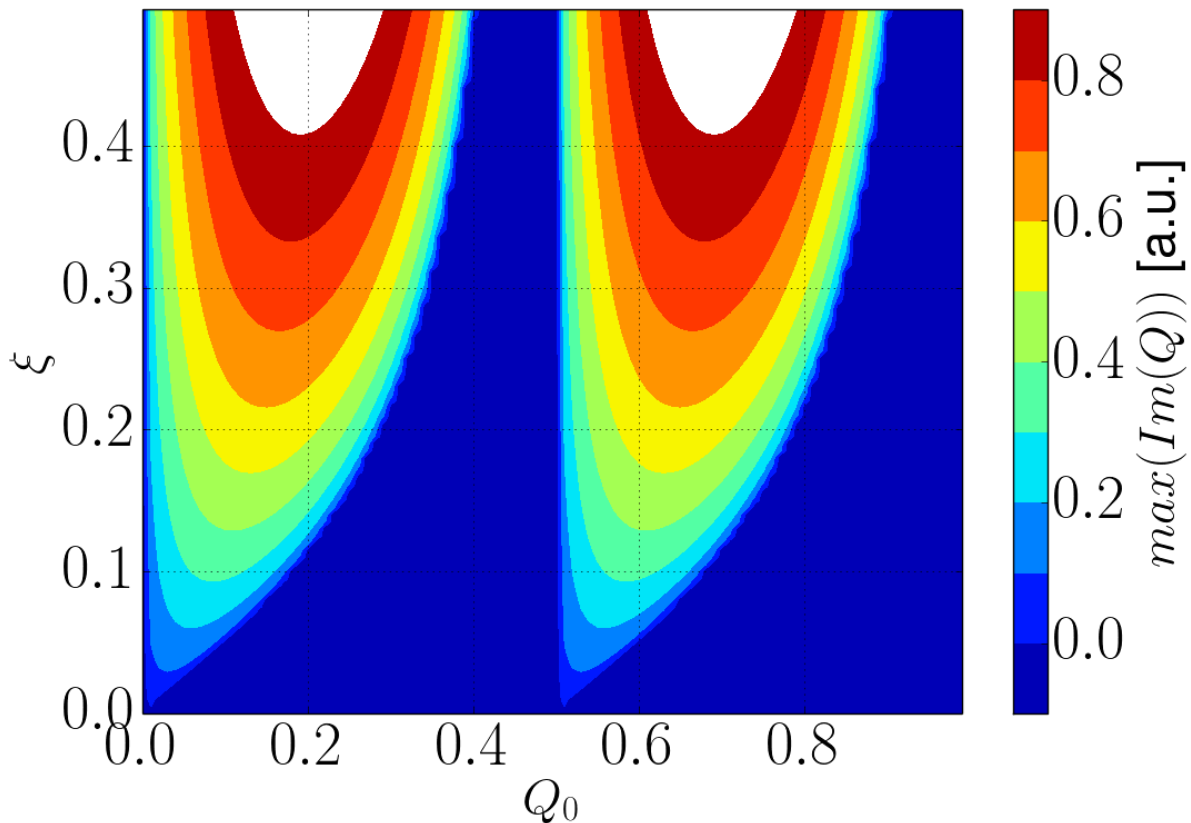
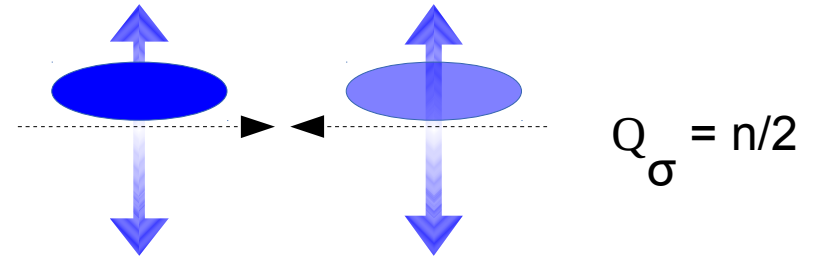


$$\Delta x'_{B1} = \frac{-2r_0 N}{\gamma_r} \frac{1}{\Delta x} \left(1 - e^{\frac{-\Delta x^2}{4\sigma^2}}\right) \approx k(x_{B1} - x_{B2}) \quad (\text{Small amplitude approximation})$$

$$\begin{pmatrix} x_{B1} \\ x_{B1}' \\ x_{B2} \\ x_{B2}' \end{pmatrix}_{t+1} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ +k & 1 & -k & 0 \\ 0 & 0 & 1 & 0 \\ -k & 0 & +k & 1 \end{pmatrix} \cdot M_{\text{lattice}} \begin{pmatrix} x_{B1} \\ x_{B1}' \\ x_{B2} \\ x_{B2}' \end{pmatrix}_t$$

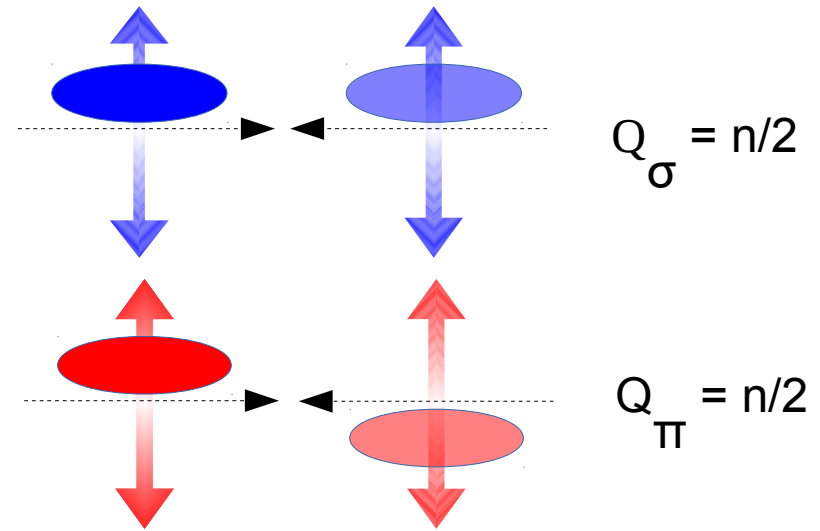
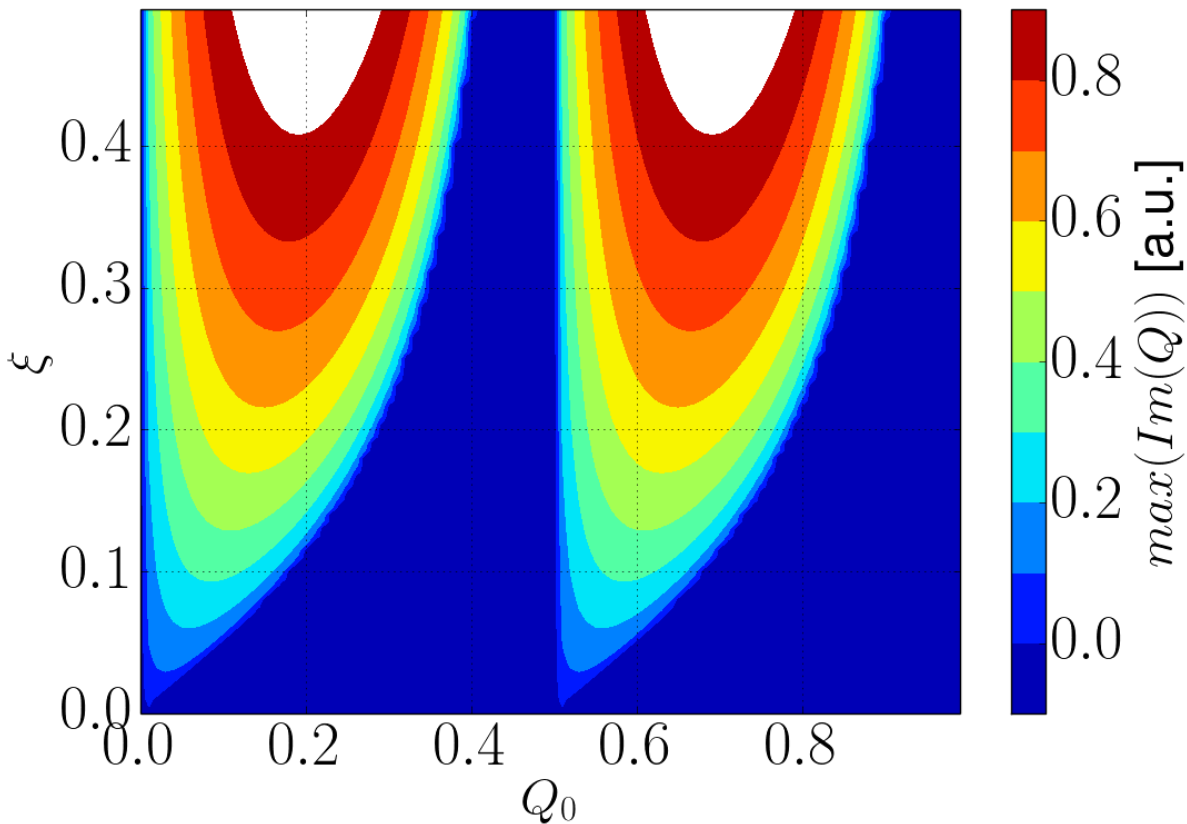
# Coherent beam-beam modes

$$\begin{pmatrix} x_i \\ x_i' \end{pmatrix}_{t+1} = M_{lattice} \cdot M_{BB} \begin{pmatrix} x_i \\ x_i' \end{pmatrix}_t$$



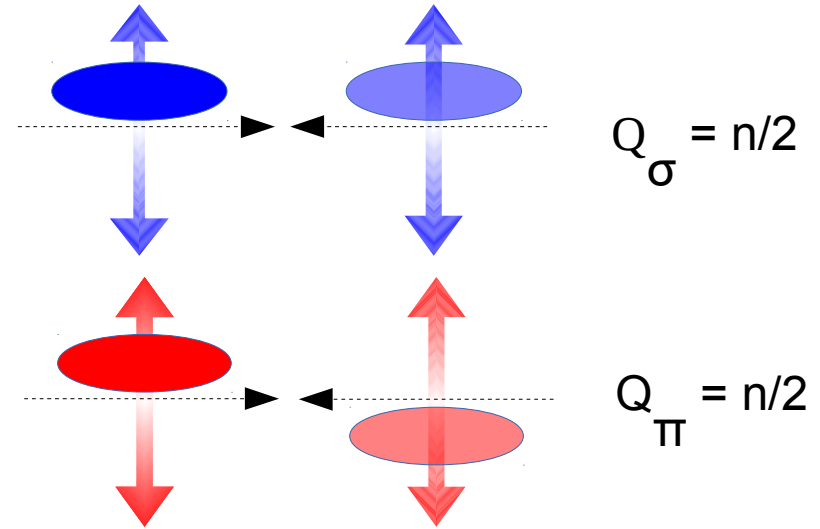
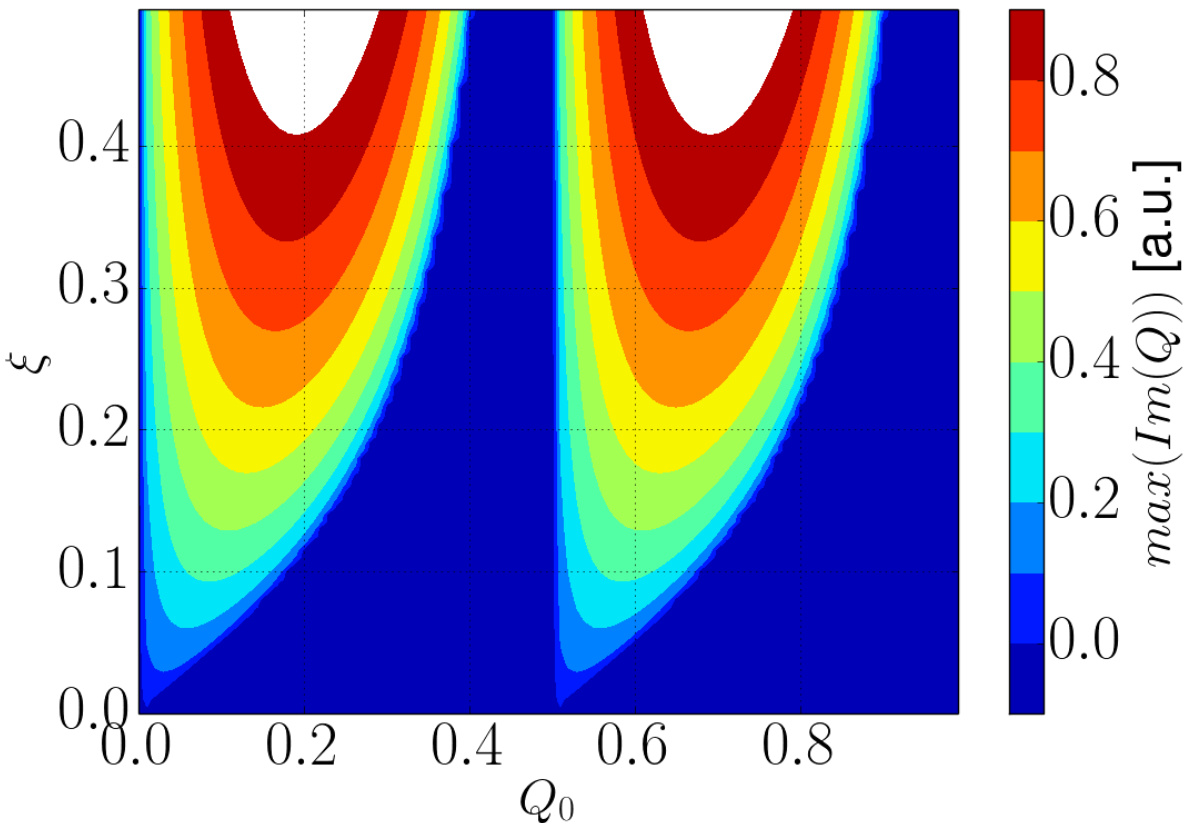
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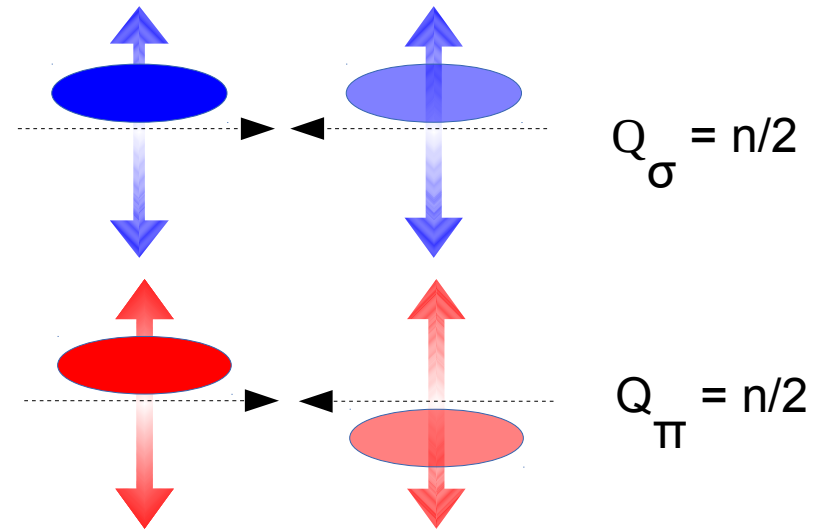
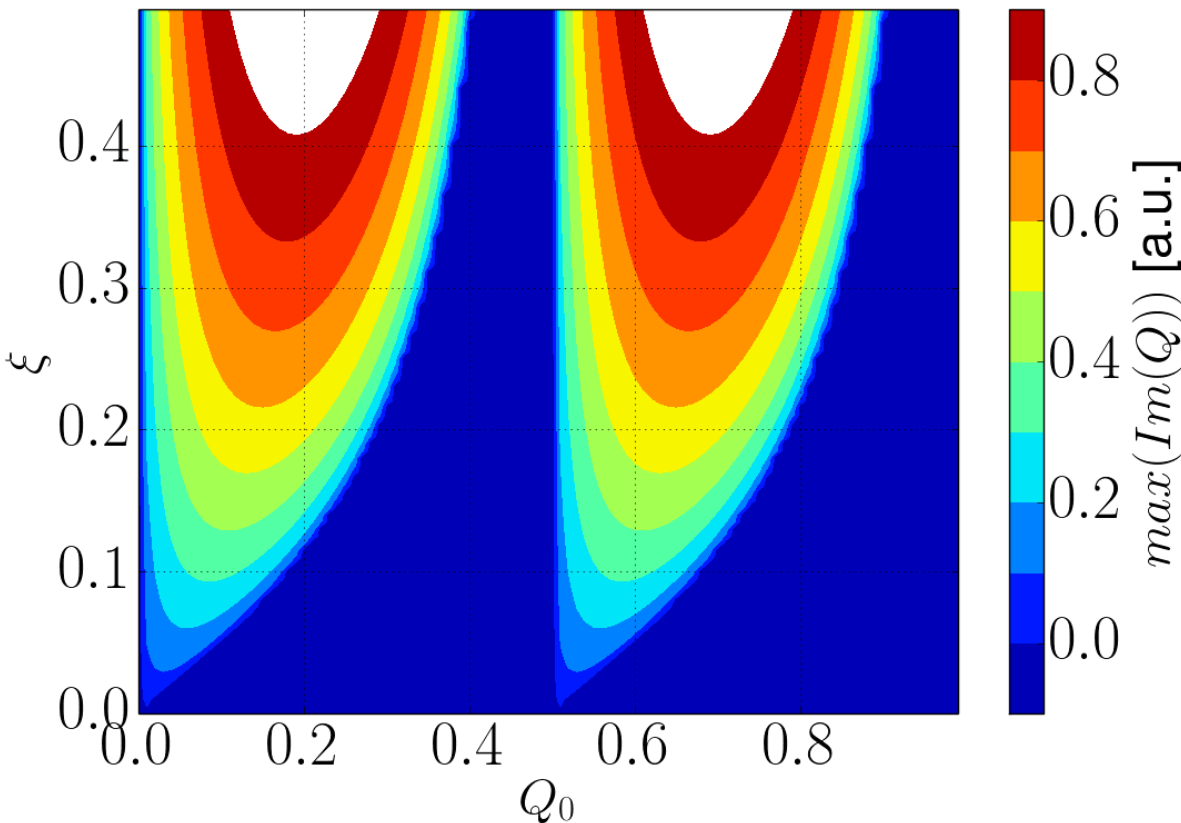


- Under resonant conditions coherent beam-beam modes may be driven unstable
    - Higher orders as well as synchrotron resonances can also lead to such instabilities
- e.g. A. Chao, SSCL-346, 1991*



# Coherent beam-beam modes

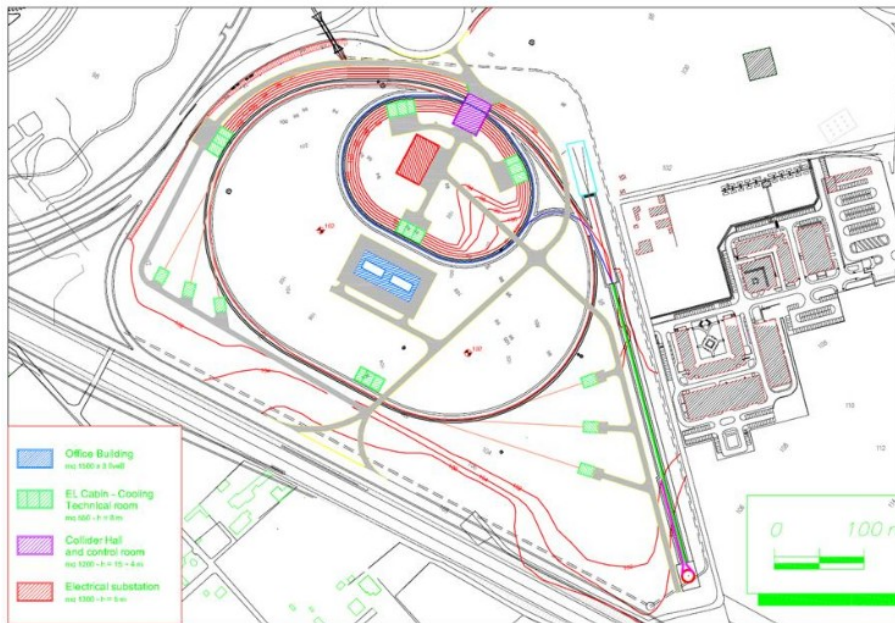
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- Under resonant conditions coherent beam-beam modes may be driven unstable
  - Higher orders as well as synchrotron resonances can also lead to such instabilities  
e.g. A. Chao, SSCL-346, 1991
- The choice of a favourable working point usually matches the constraints also imposed by single particle stability

# Coherent beam-beam mode : Asymmetric machines

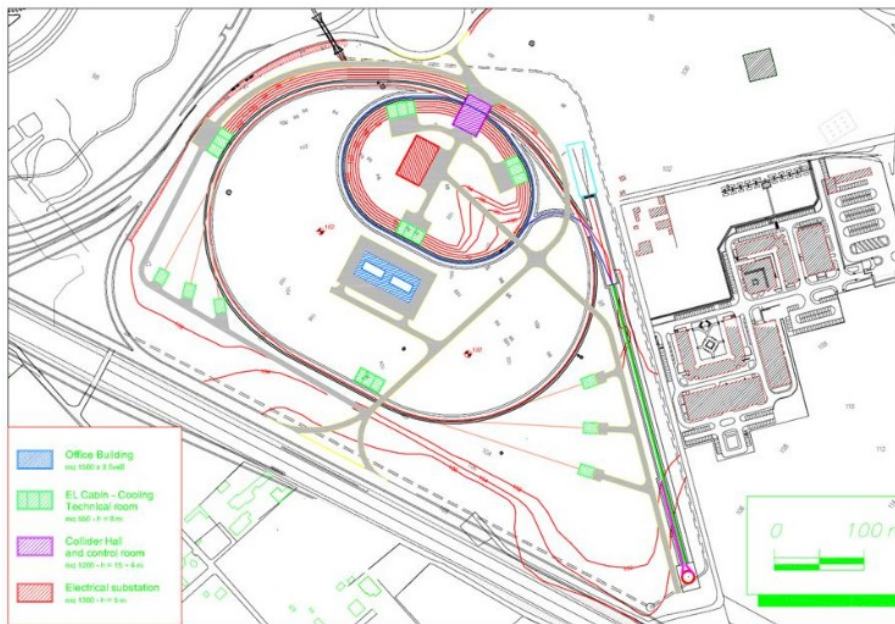
- At the design stage of B factories, colliders with asymmetric ring circumferences were considered



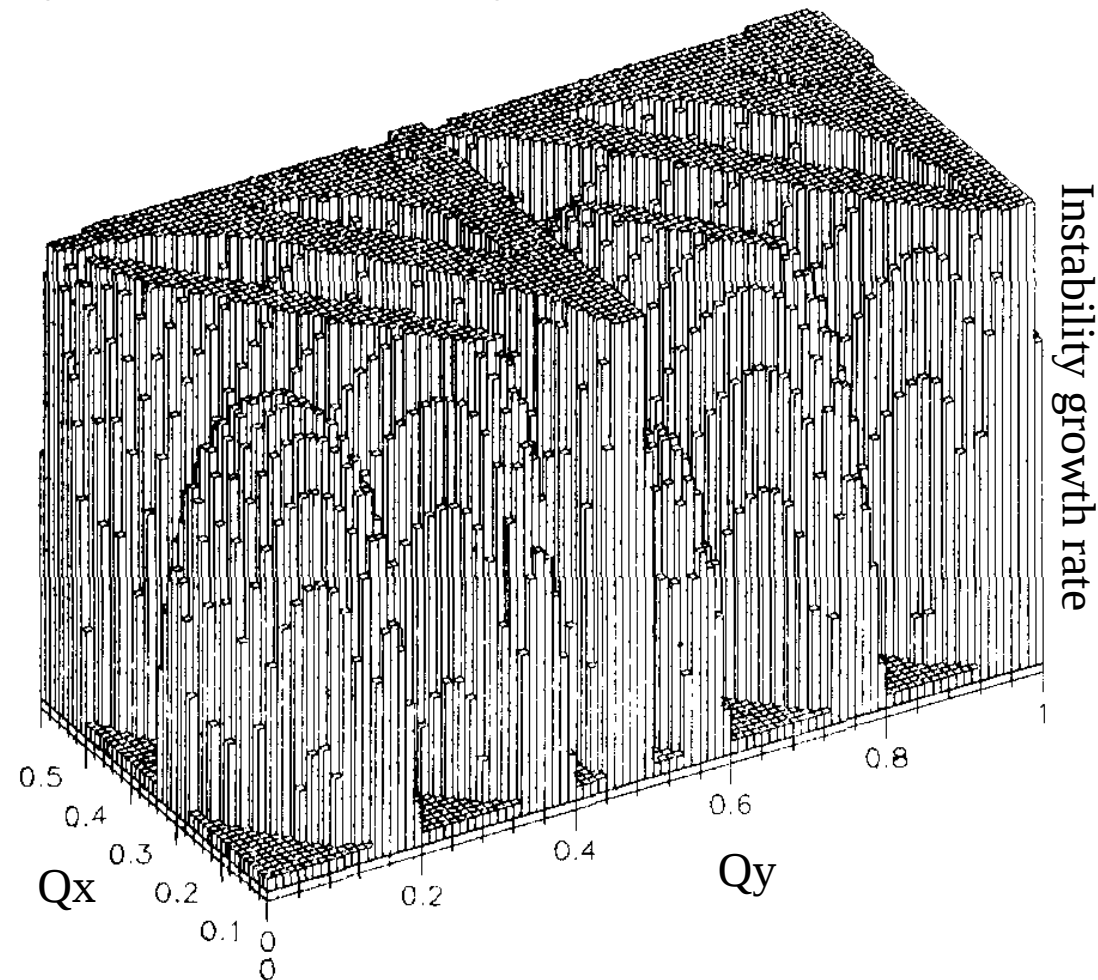
SuperB asymmetric ring layout

# Coherent beam-beam mode : Asymmetric machines

- At the design stage of B factories, colliders with asymmetric ring circumferences were considered
  - The tunes and the super-period are constrained by resonant conditions for the coherent beam-beam modes  
*K. Hirata and E. Keil, Phys. Lett. B 232 3 (1989) / M. Zobov and Y. Zhang, IPAC'11*



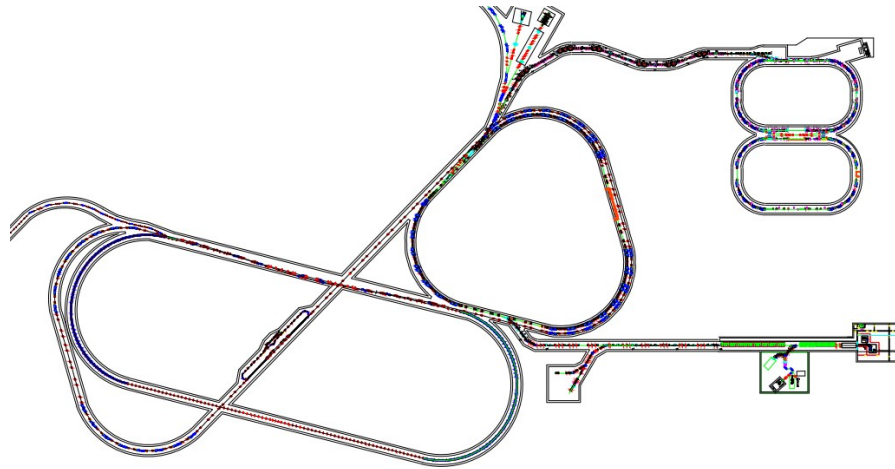
SuperB asymmetric ring layout



# Coherent beam-beam mode : Asymmetric machines

- New 8-shape designs of electron-ion colliders features both asymmetric revolution frequencies and IP locations (→ JLEIC, EicC)

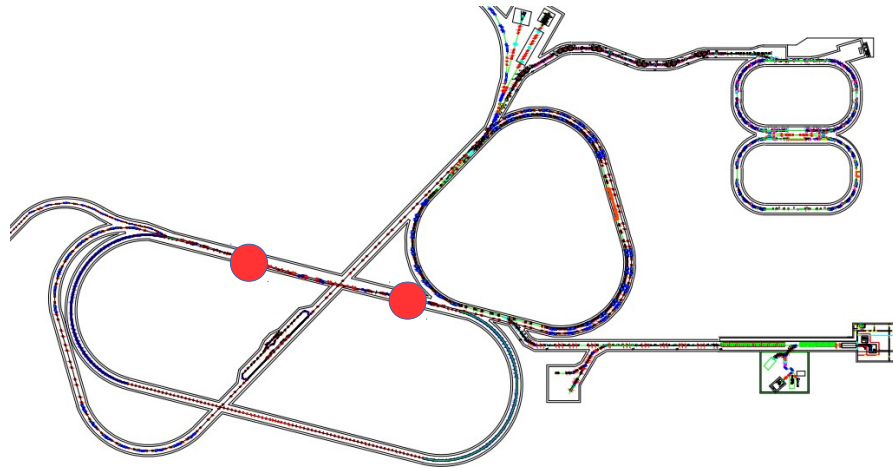
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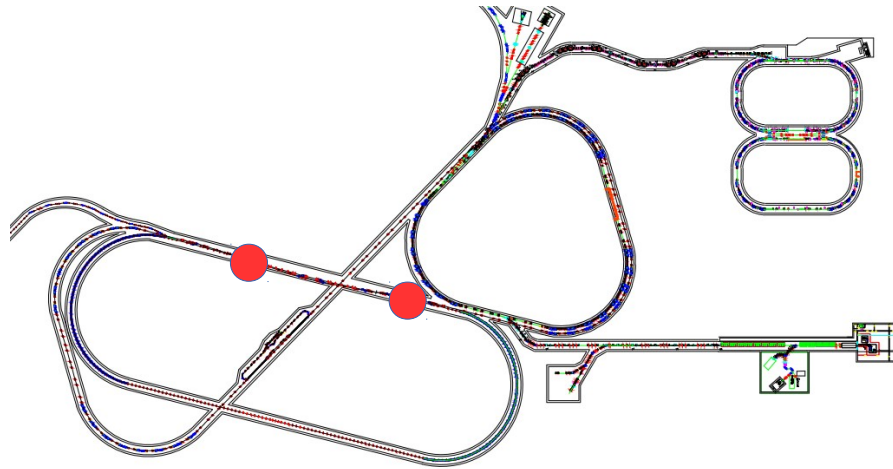
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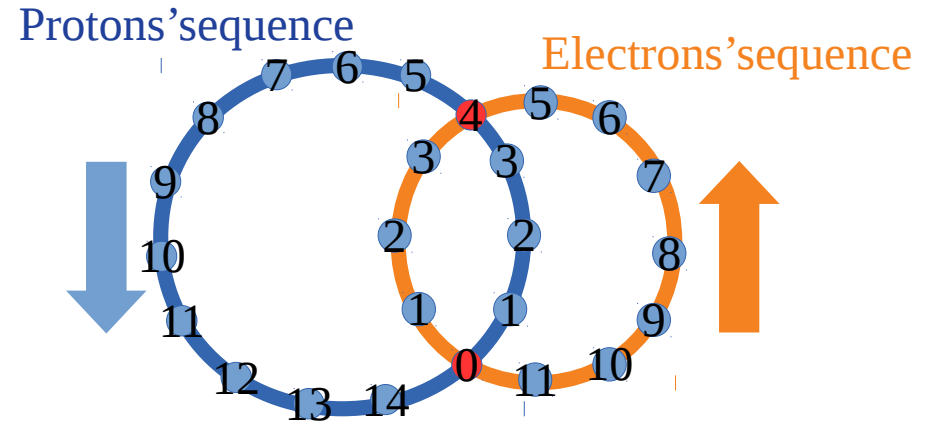
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Model in the BimBim code:

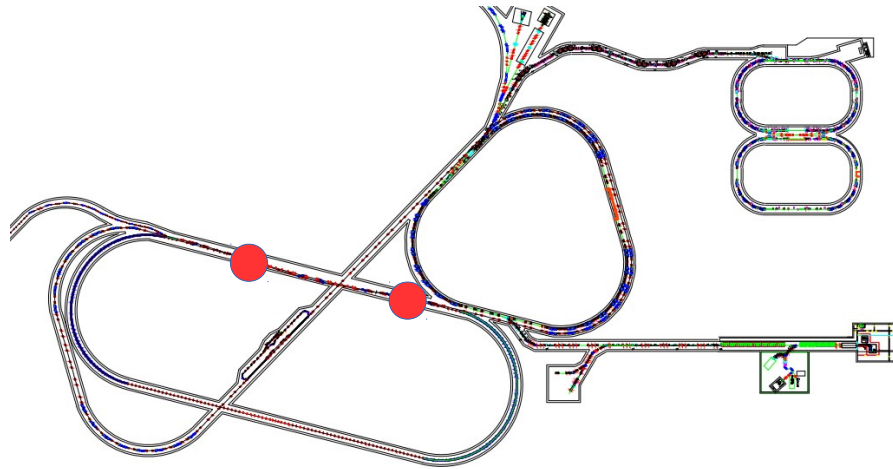




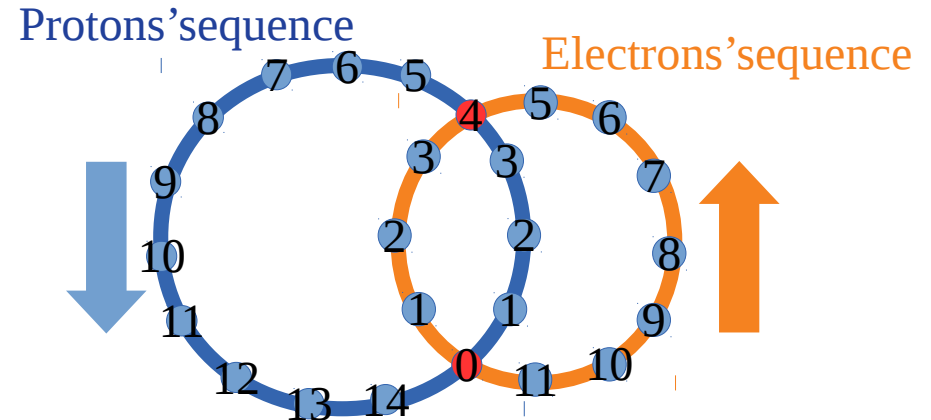
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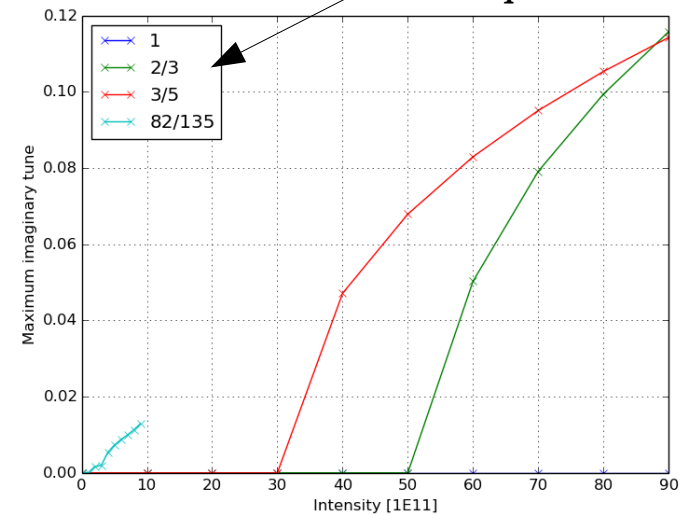
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Ratio of revolution frequencies



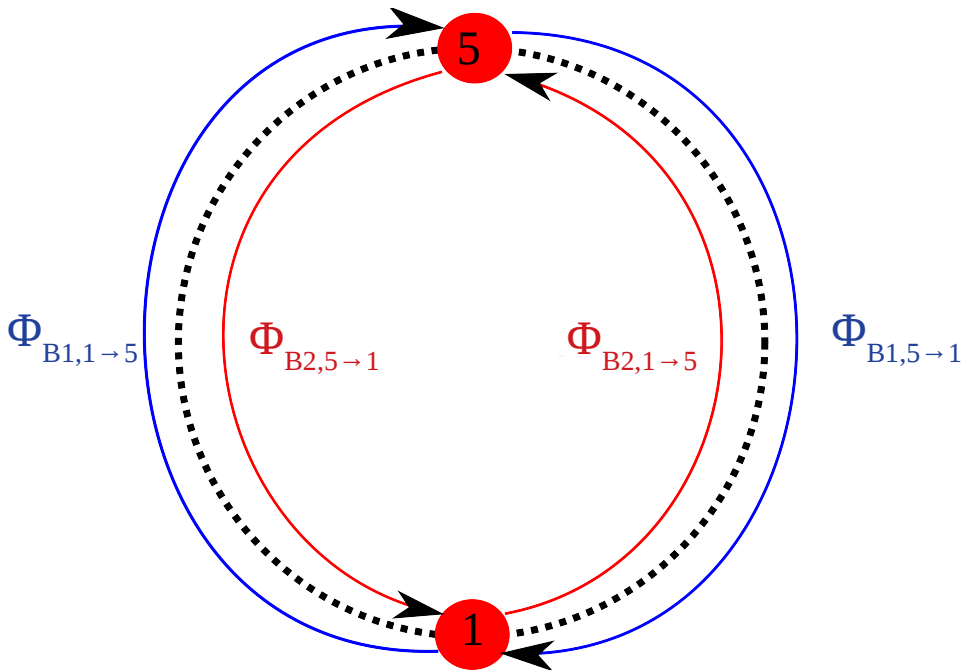
- The results obtained semi-analytically are in agreement with the guidelines of Hirata and Keil :
  - Short super-periods offer a large stable space in the terms of tunes and beam-beam tune shift
  - Long super-periods lead to weak instabilities even with low beam-beam tune shifts

# Mode coupling instability of colliding beams

- The interaction of coherent beam-beam mode with the machine impedance can result in strong mode coupling instabilities *S. White, et al., Phys. Rev. ST Accel. Beams 17 041002 (2014)*
  - This instability is not driven by a resonant condition, it can therefore not be fully mitigated with choices of tunes
  - In some cases, the layout of IPs and phase advance between them can be used to control the beam-beam mode frequencies

→ Act on intrinsic Landau damping

*Y. Alexahin, Nucl. Instrum. Methods Phys. Res. A 480, 253 (2002)*



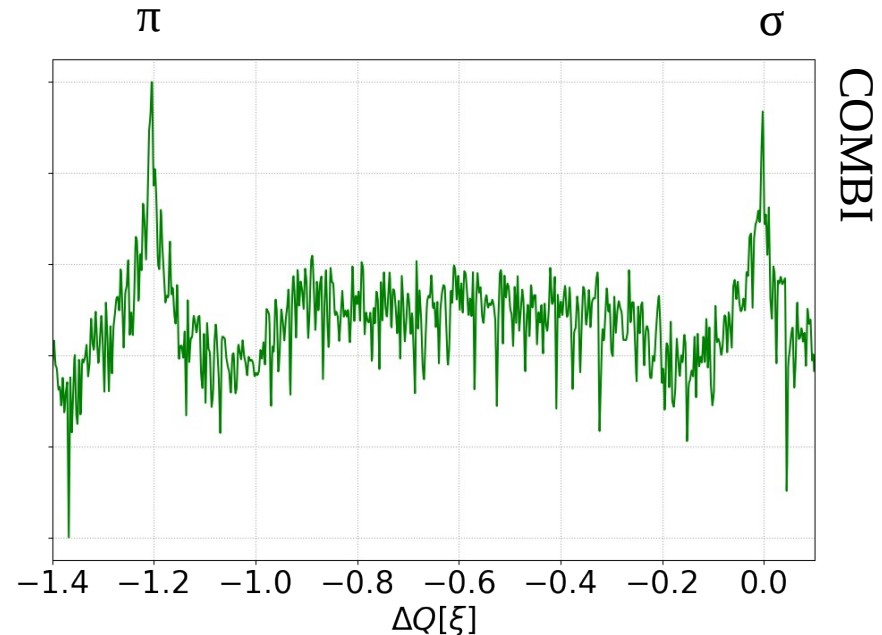
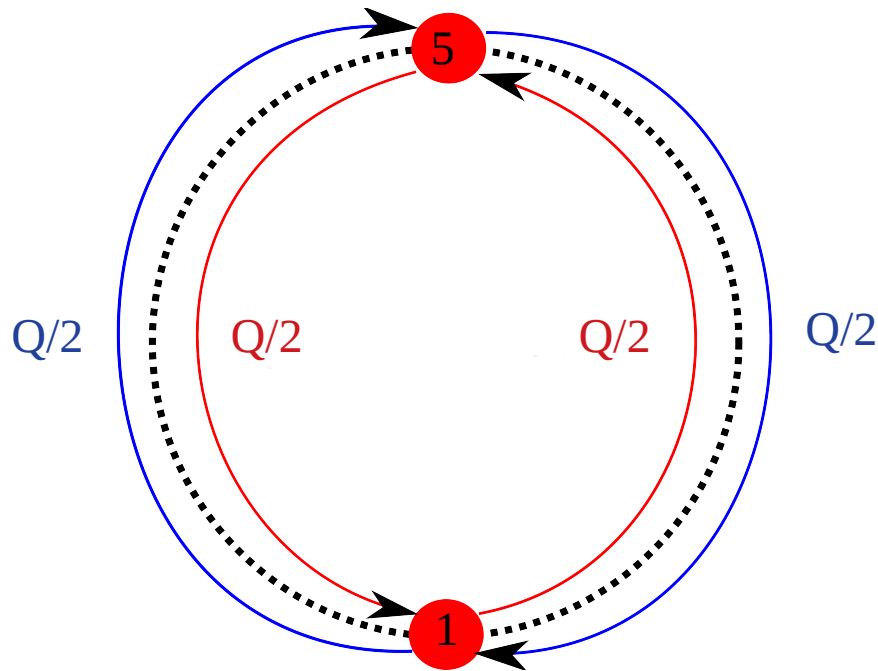


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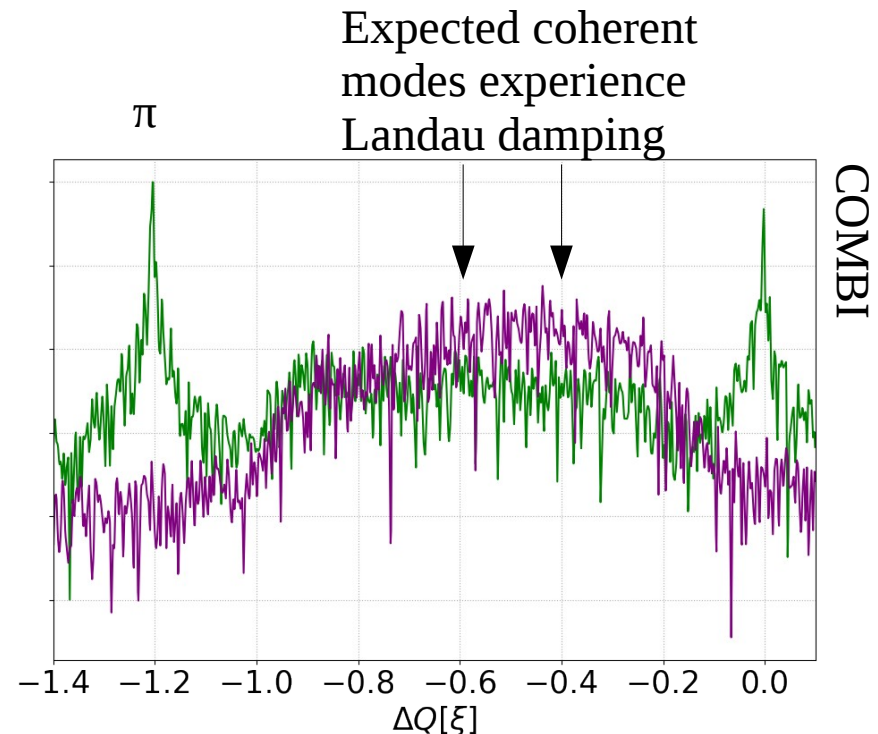
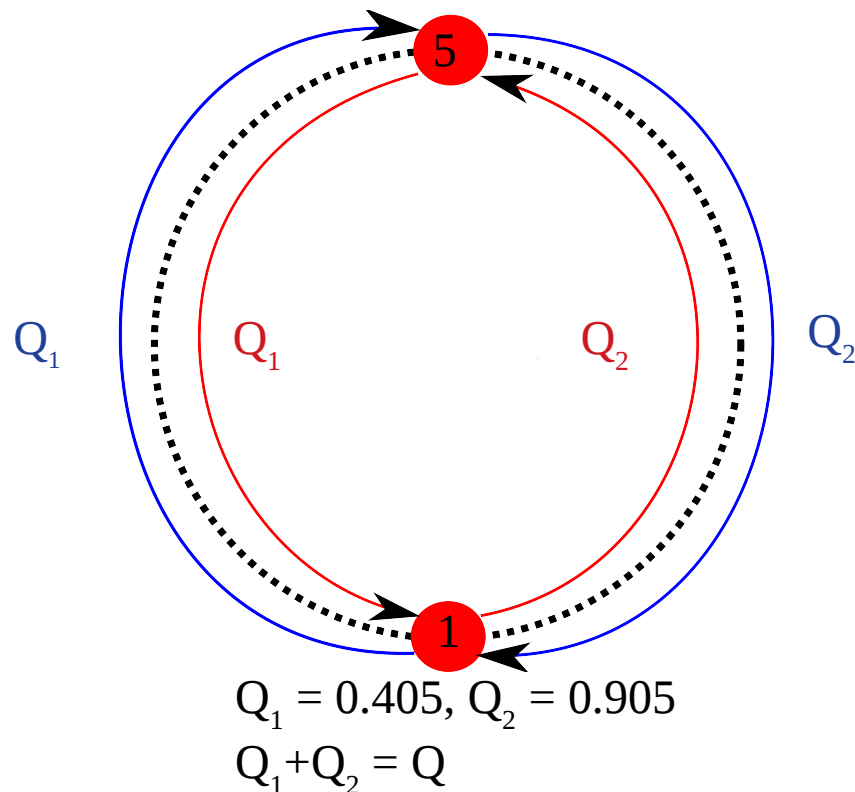


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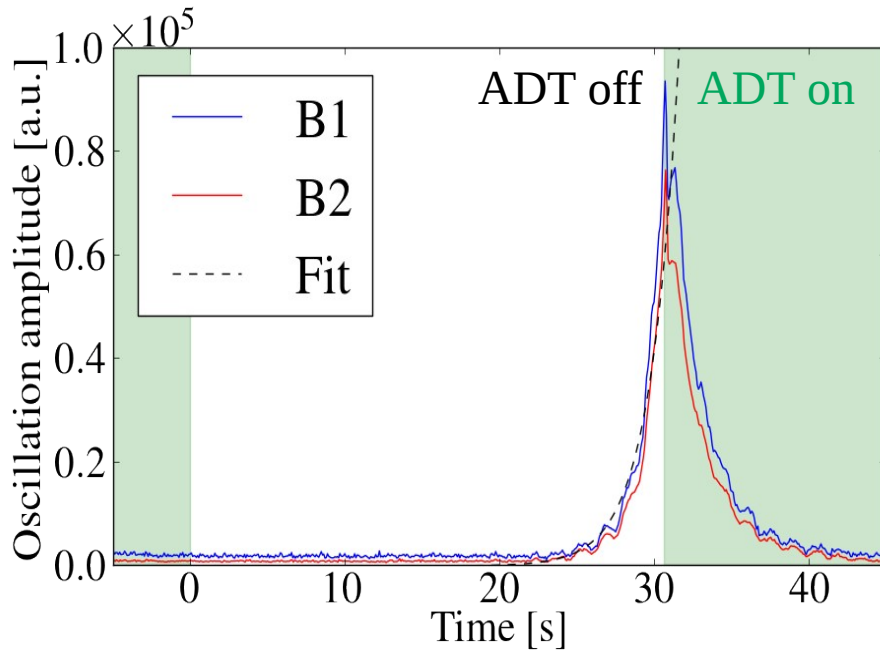
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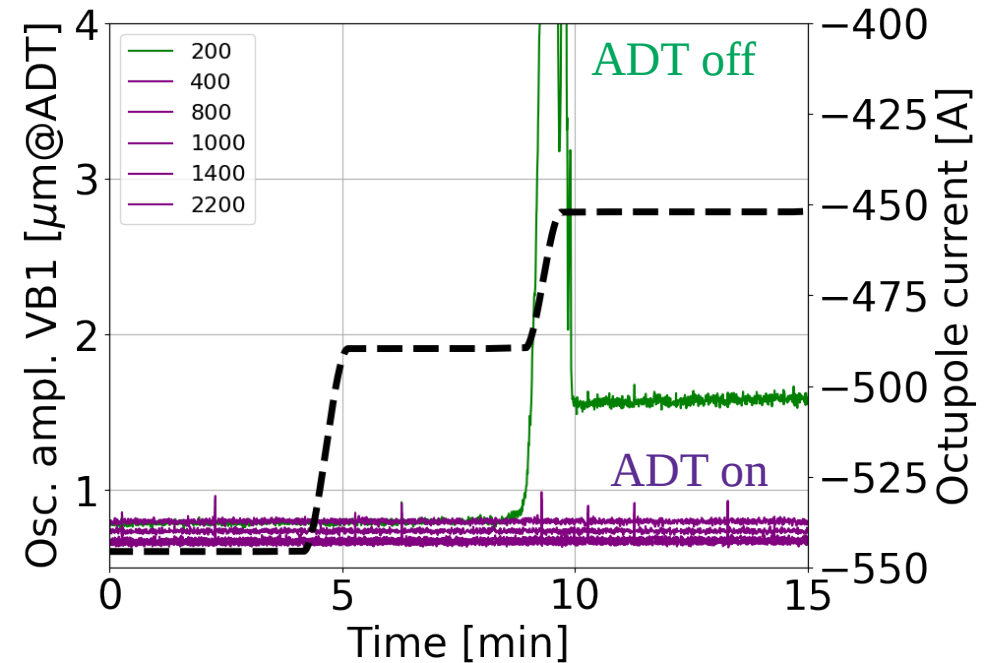
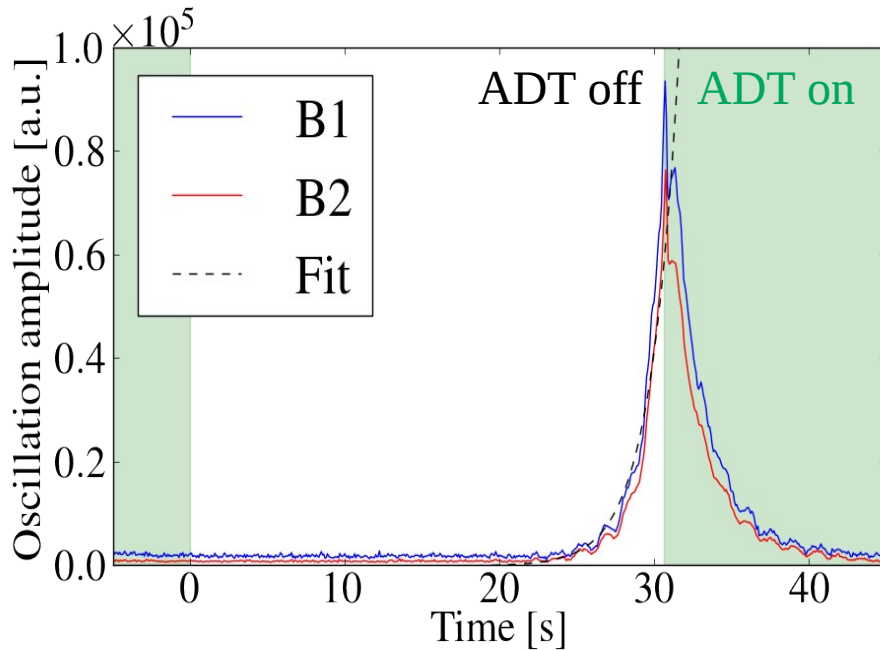


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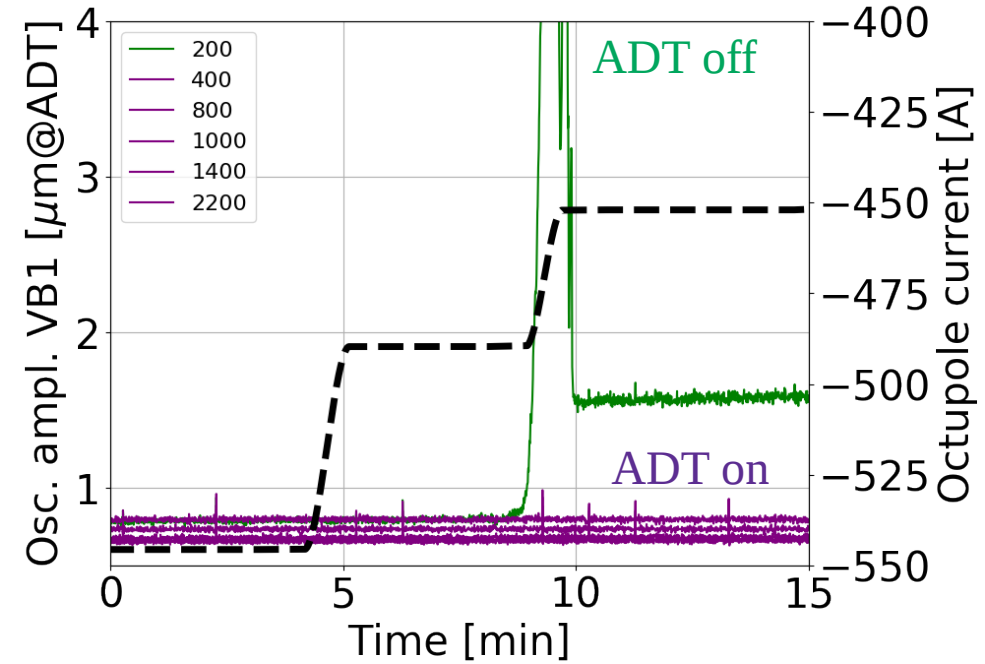
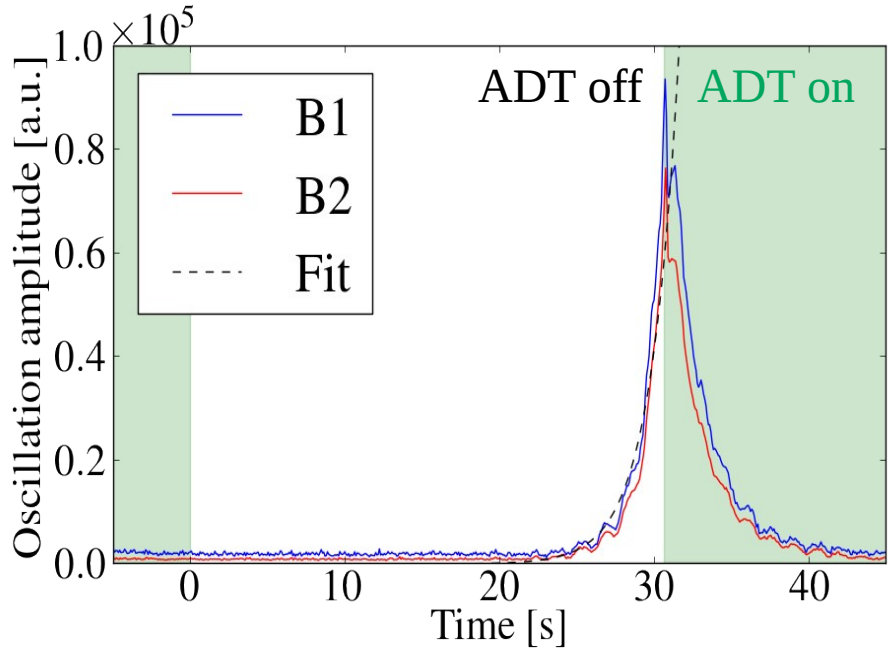
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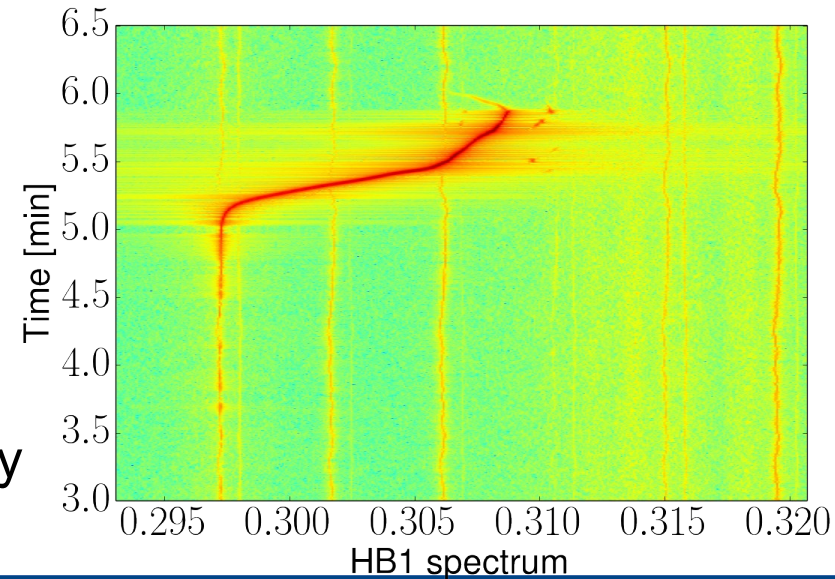


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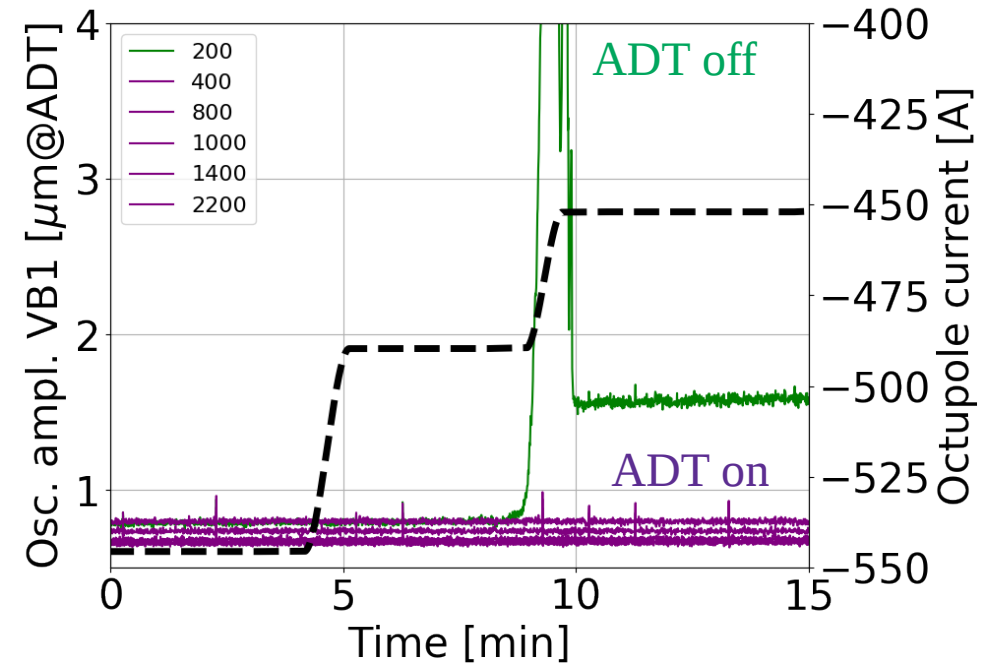
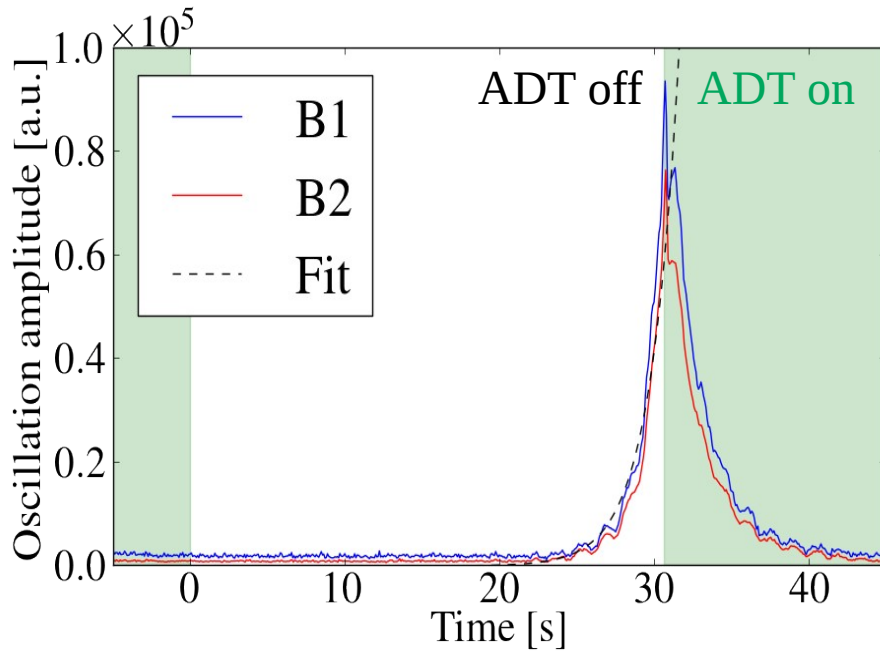


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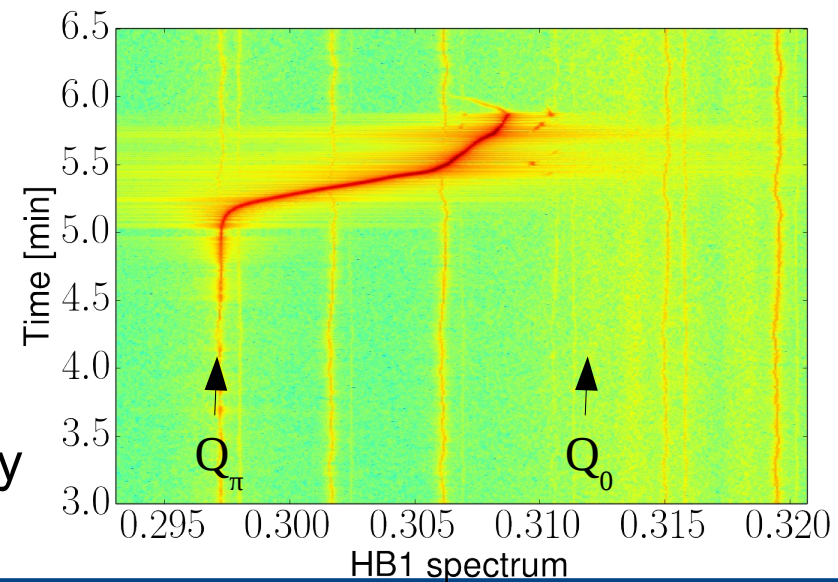




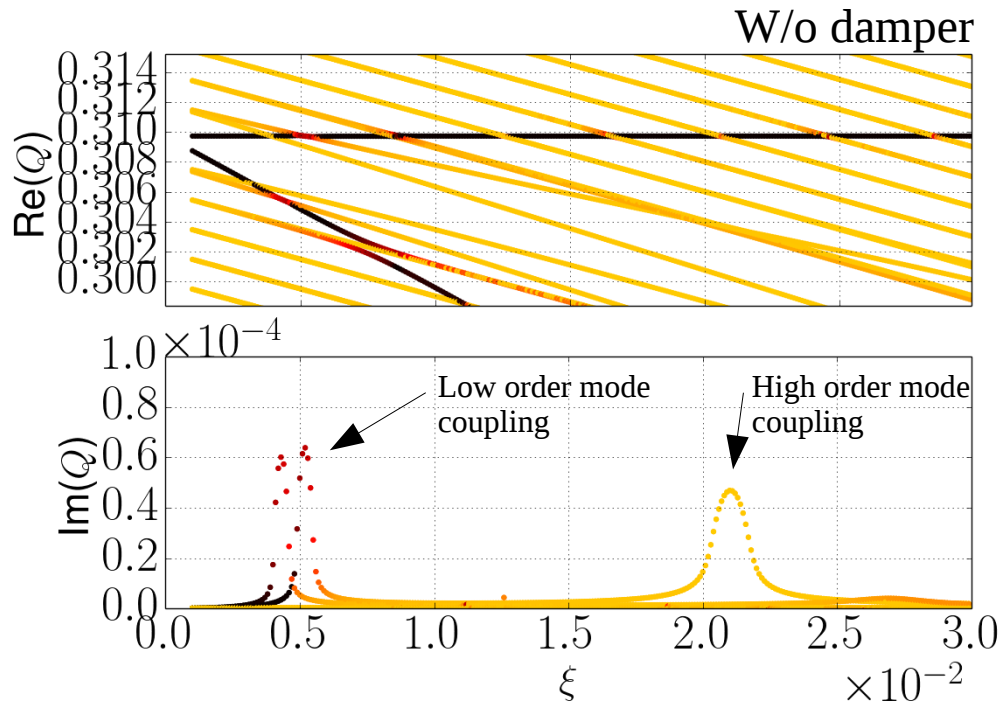
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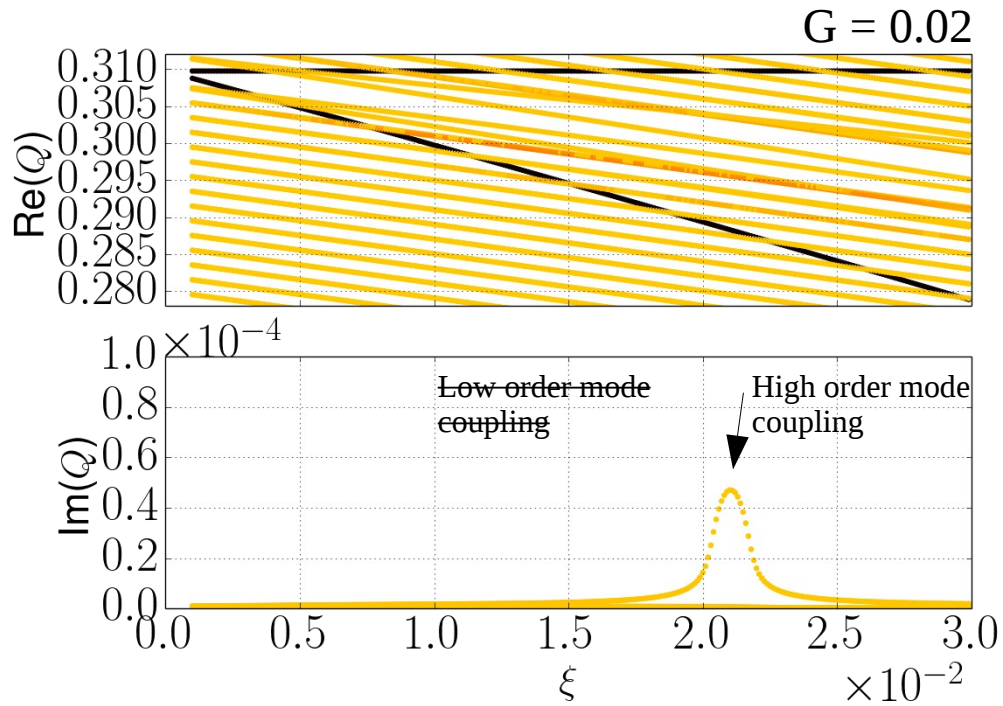


# Mode coupling instability at the HL-LHC



- In the presence of large Piwinski angle or hourglass effect, we may expect mode coupling of higher order head-tail mode which are not efficiently damped by a feedback based on the bunch centroid

# Mode coupling instability at the HL-LHC

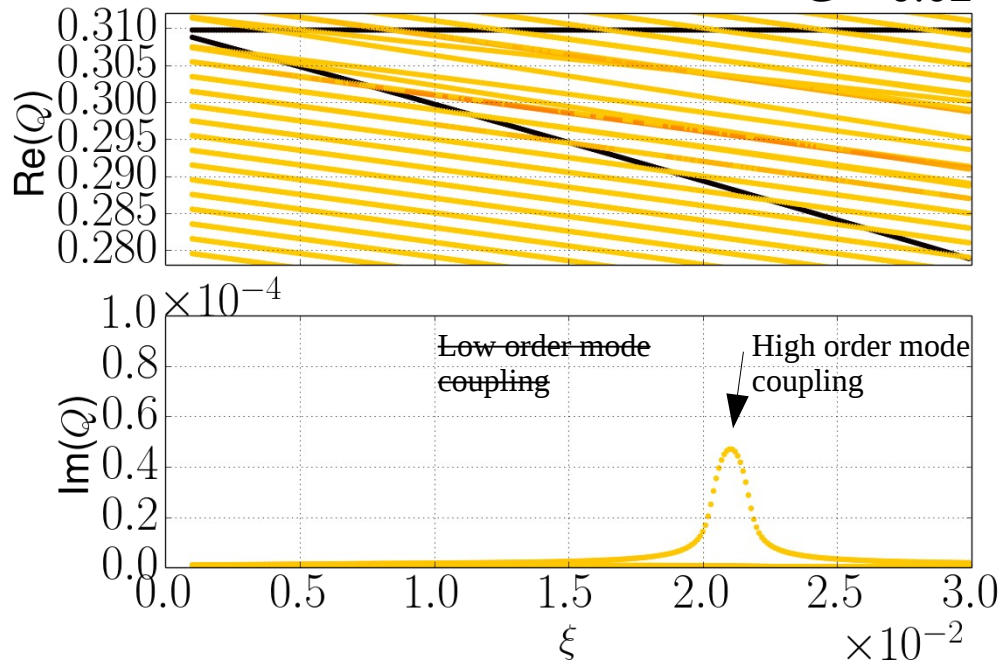


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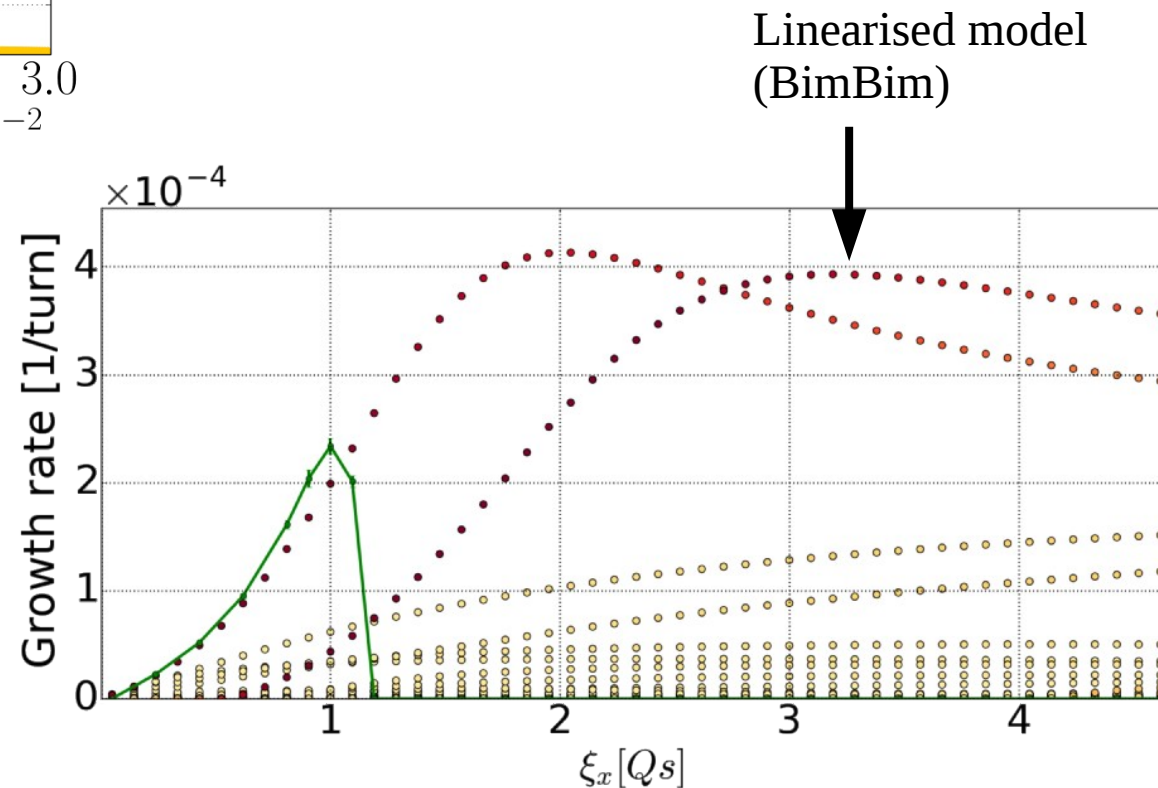


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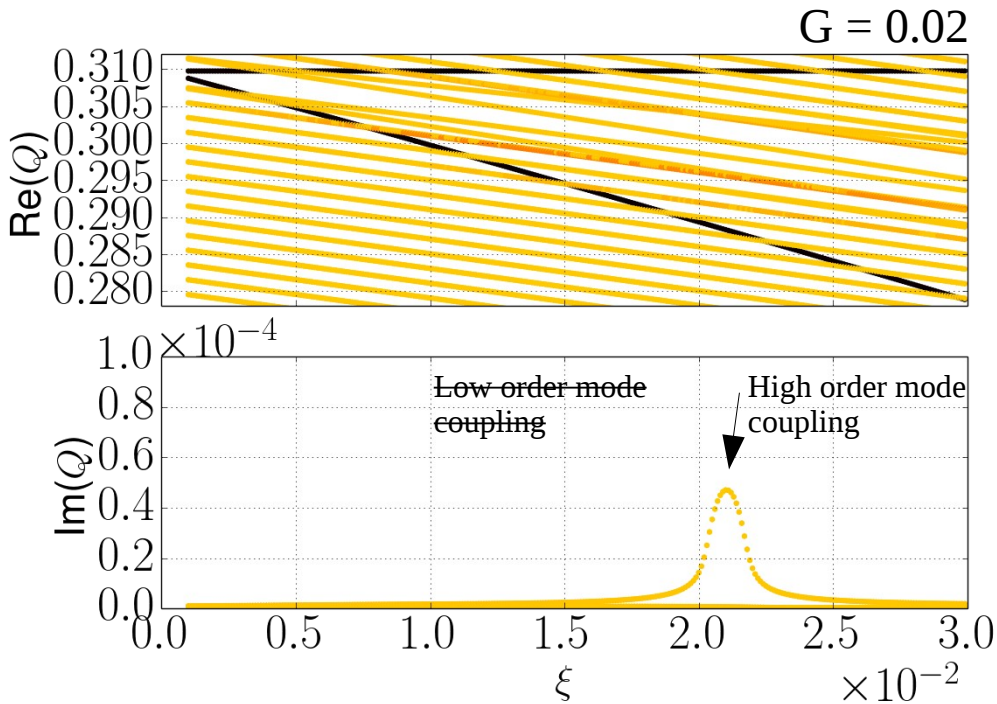
$G = 0.02$



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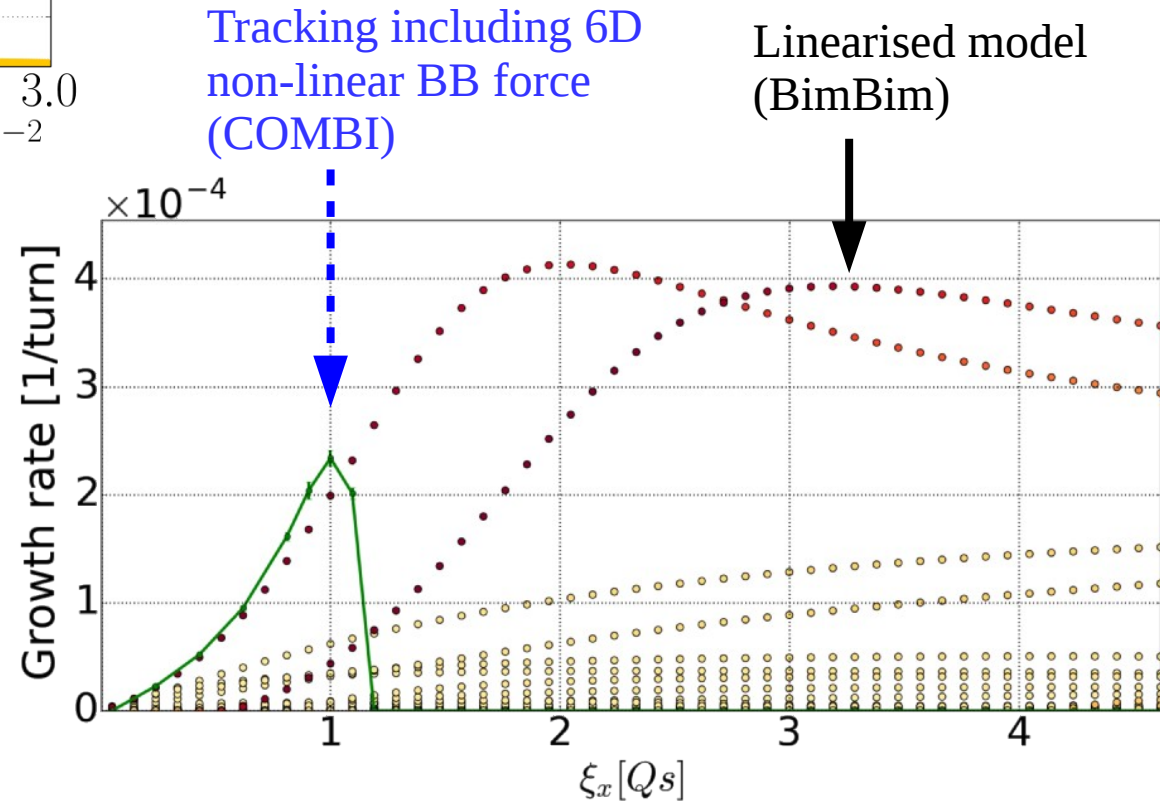
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- Landau damping by synchrotron side-bands (enabled by the large Piwinski angle or hourglass effect) is sufficient to ensure stability for beam-beam parameter larger than  $Q_s$  in the HL-LHC

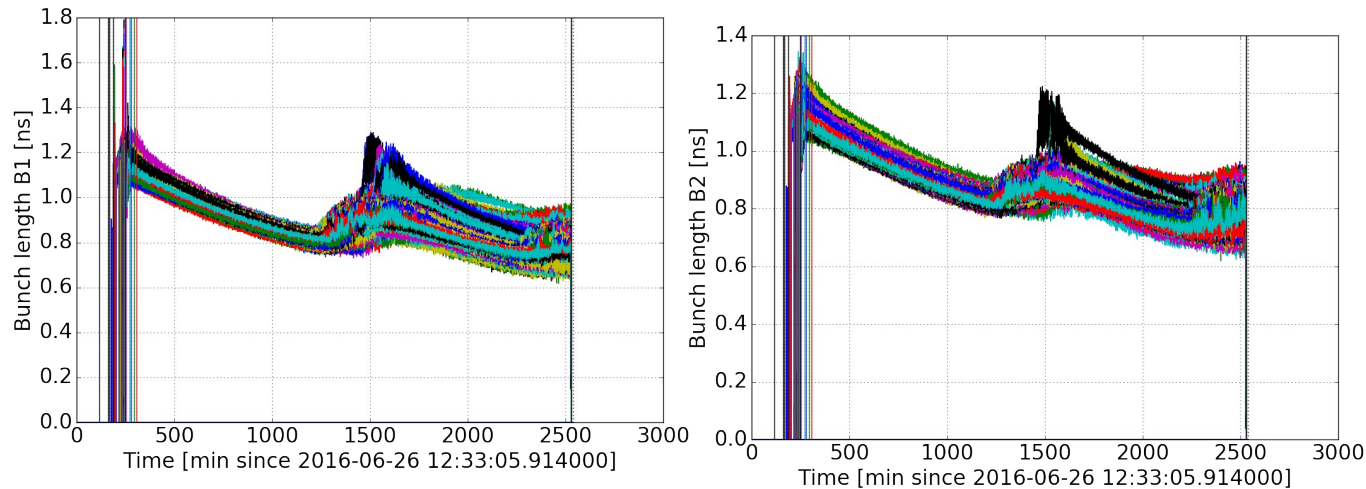
*L. Barraud, et al., CERN-ACC-NOTE-2019-0032*



# Las Ketchup instability

- In the presence of a crossing angle or hourglass effect, beam-beam interaction leads to an energy change

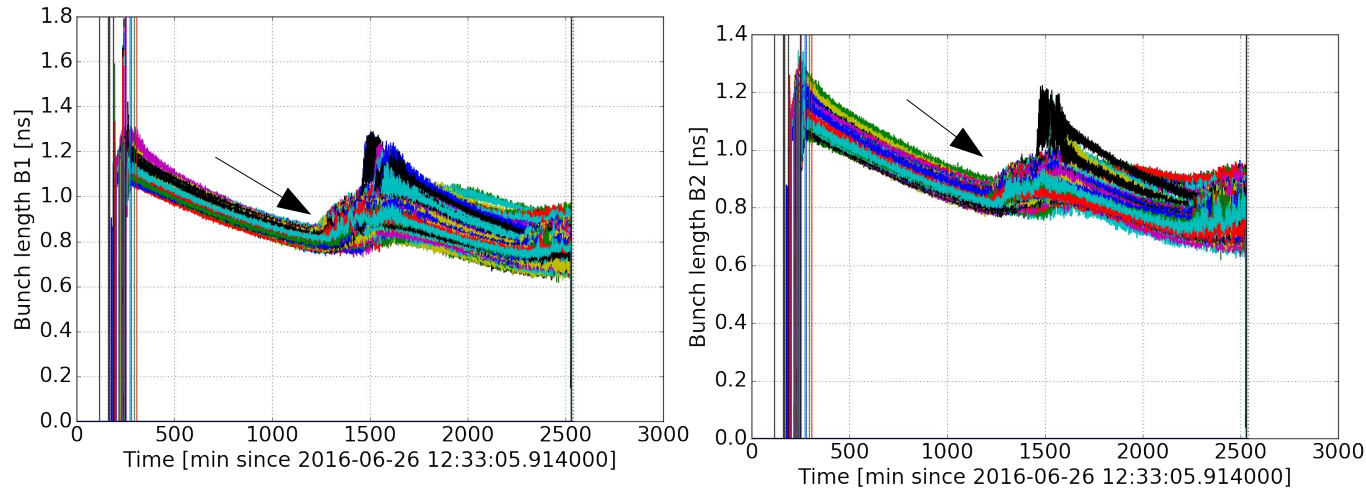
→ Longitudinal coherent beam-beam modes



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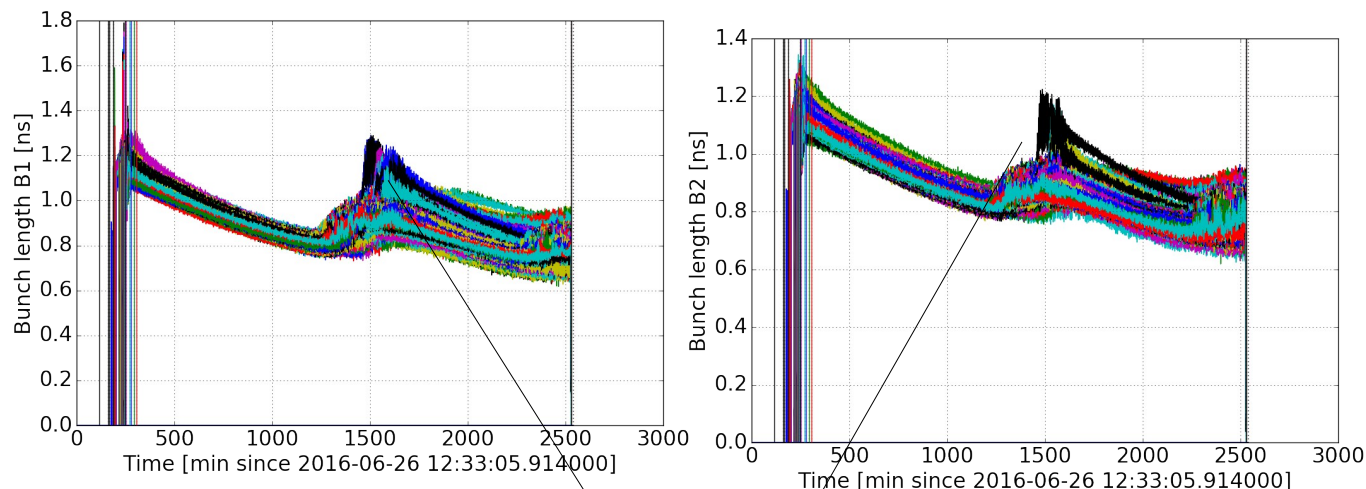


- In the first part of 2016, loss of Landau damping in the longitudinal plane was observed due to radiation damping  
H. Timko, Evian 2016

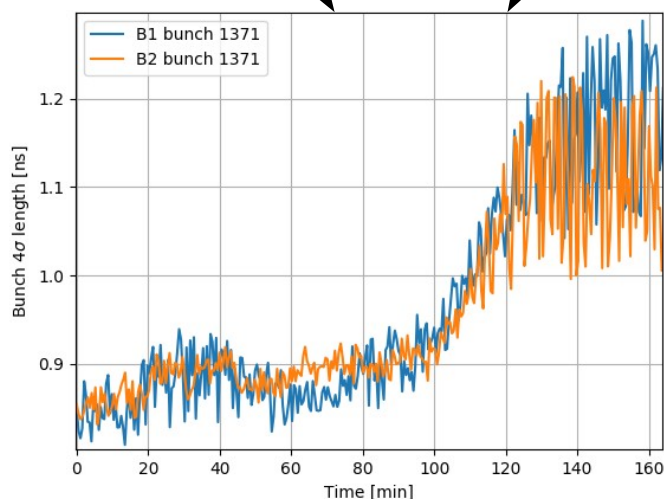
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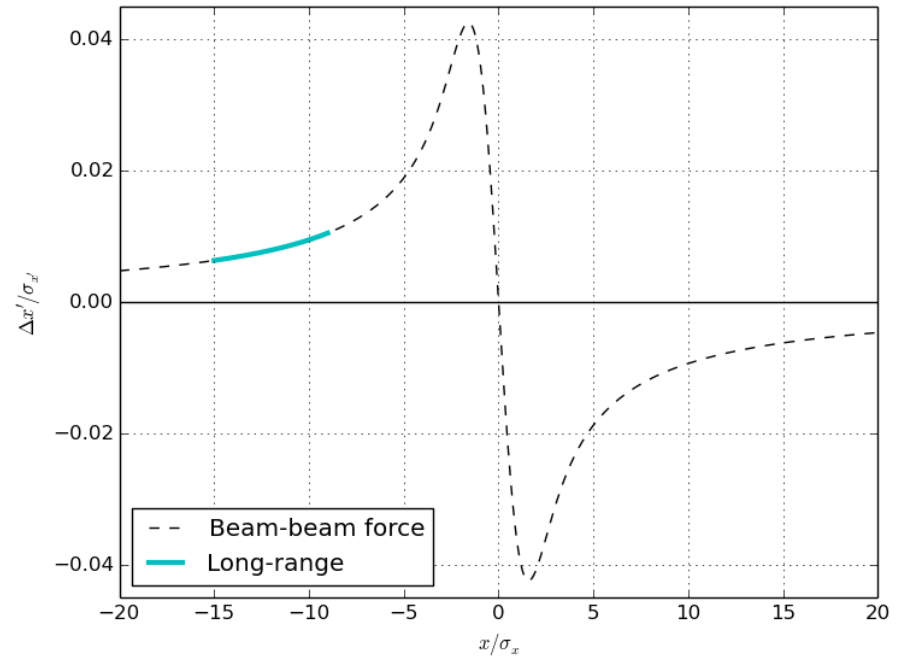
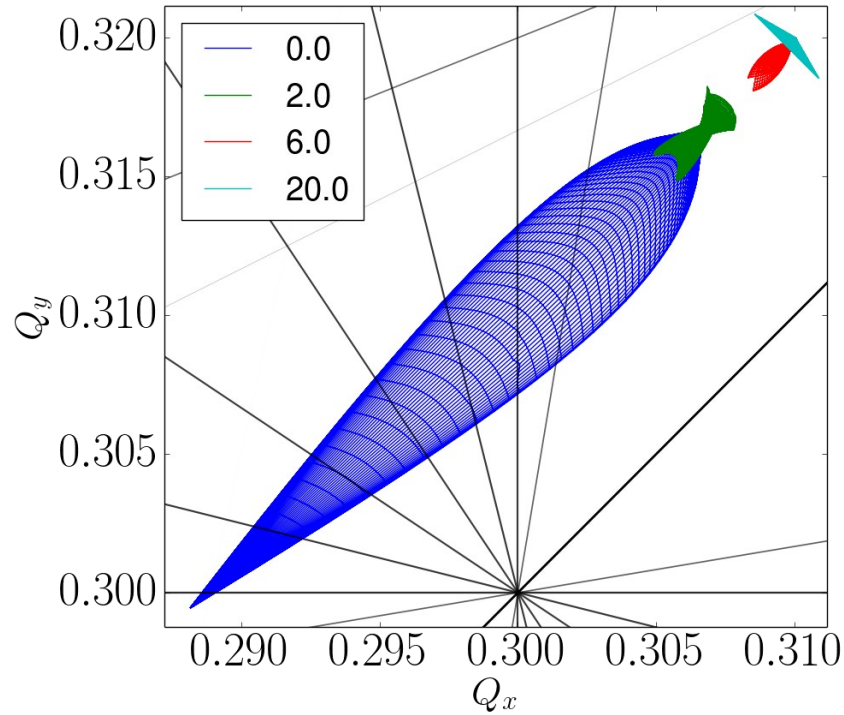


- Some signals are correlated in the two beams

→ Potential candidate for coherent longitudinal beam-beam mode, but not studied thoroughly

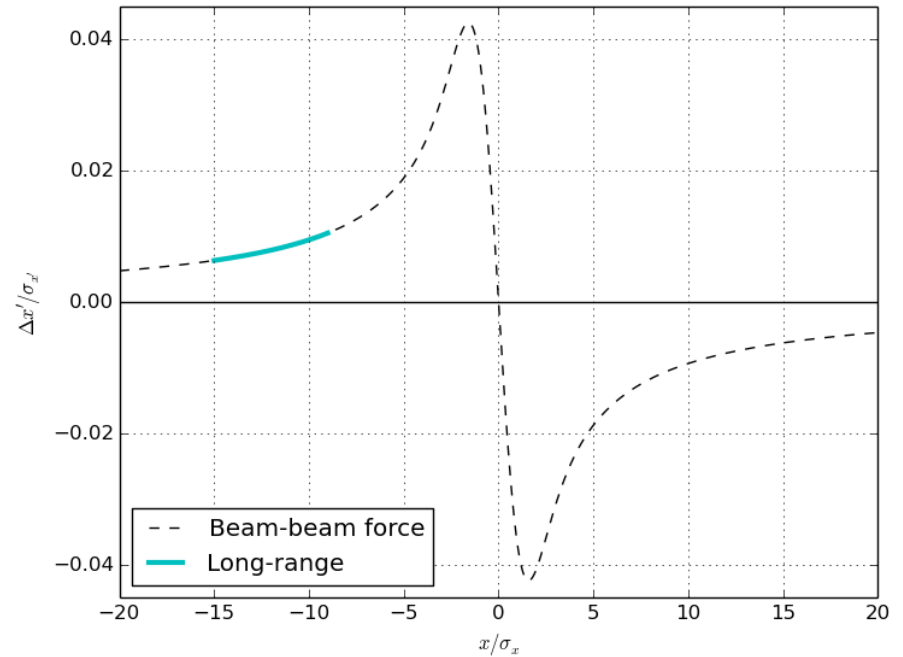
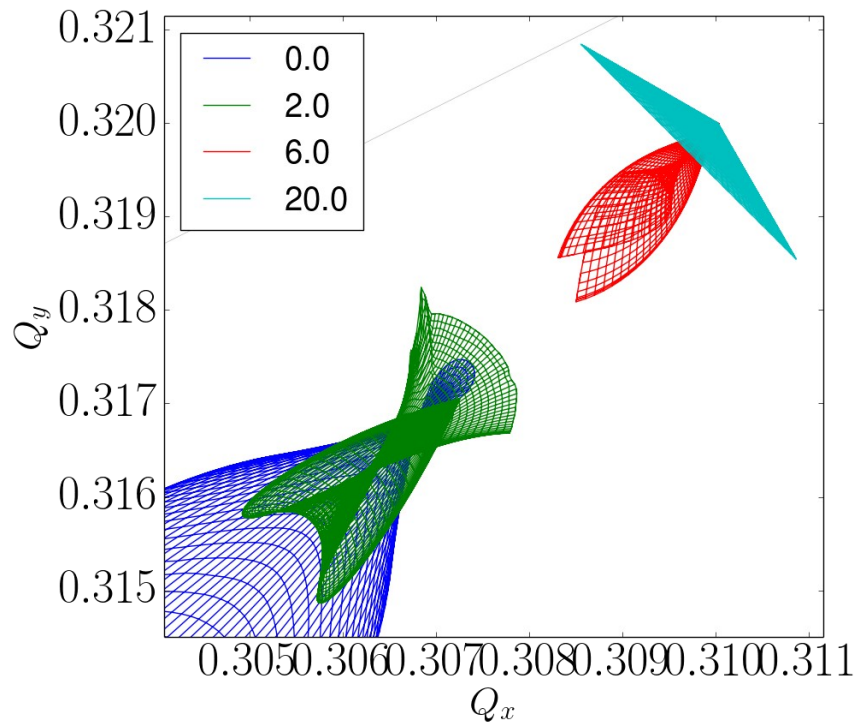


# Landau damping of head-tail modes



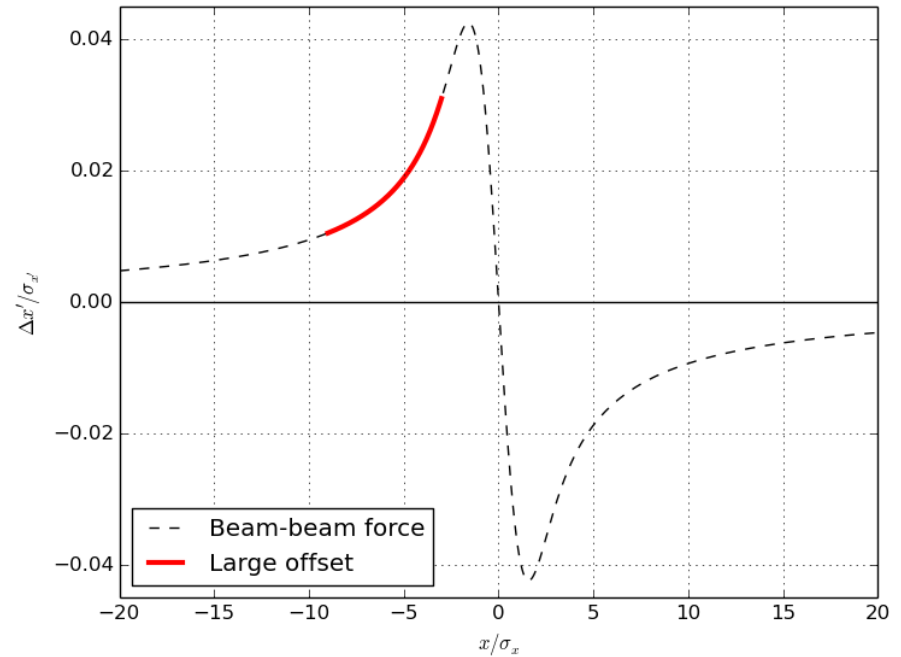
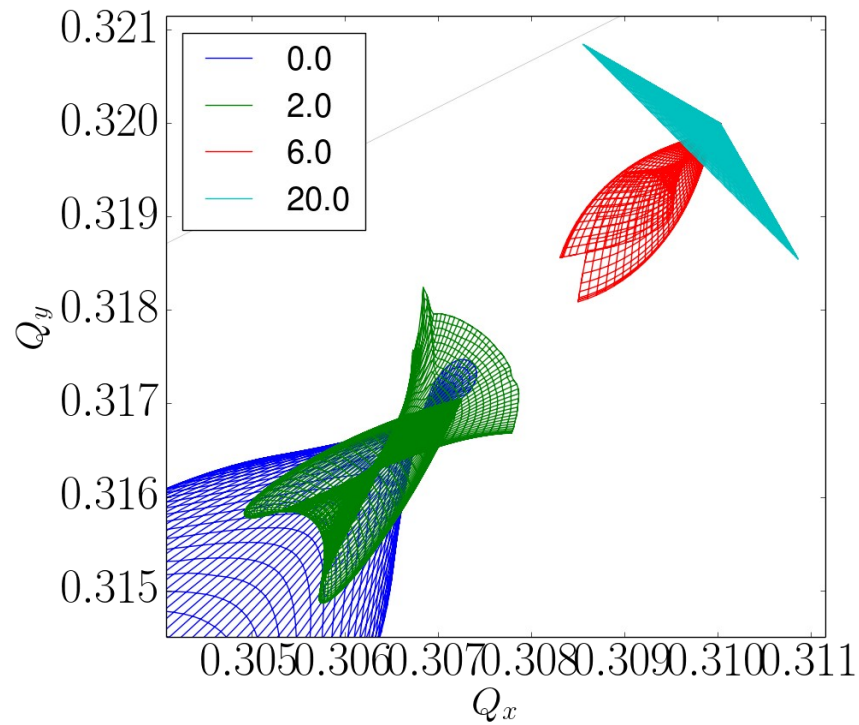
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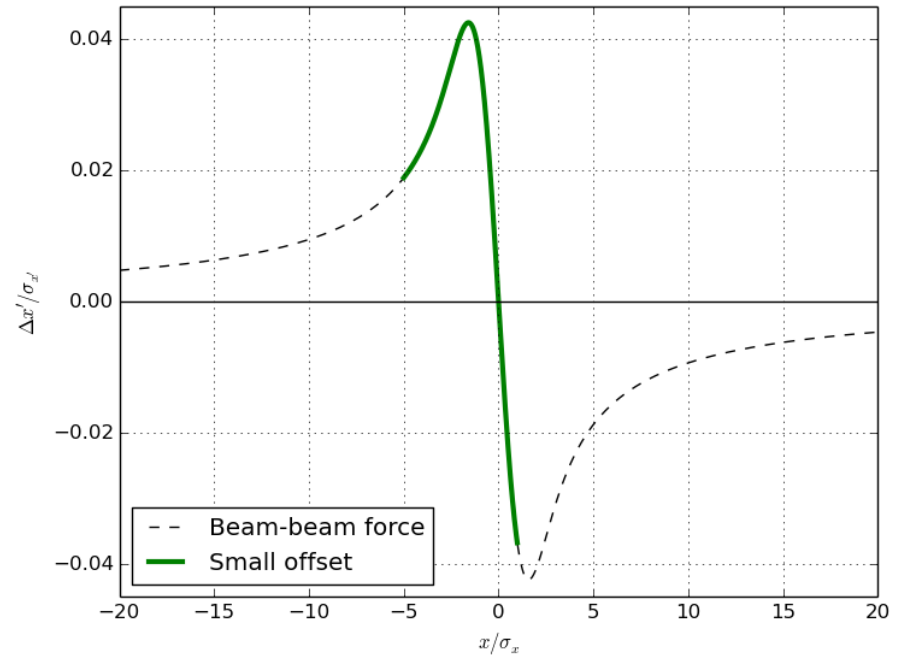
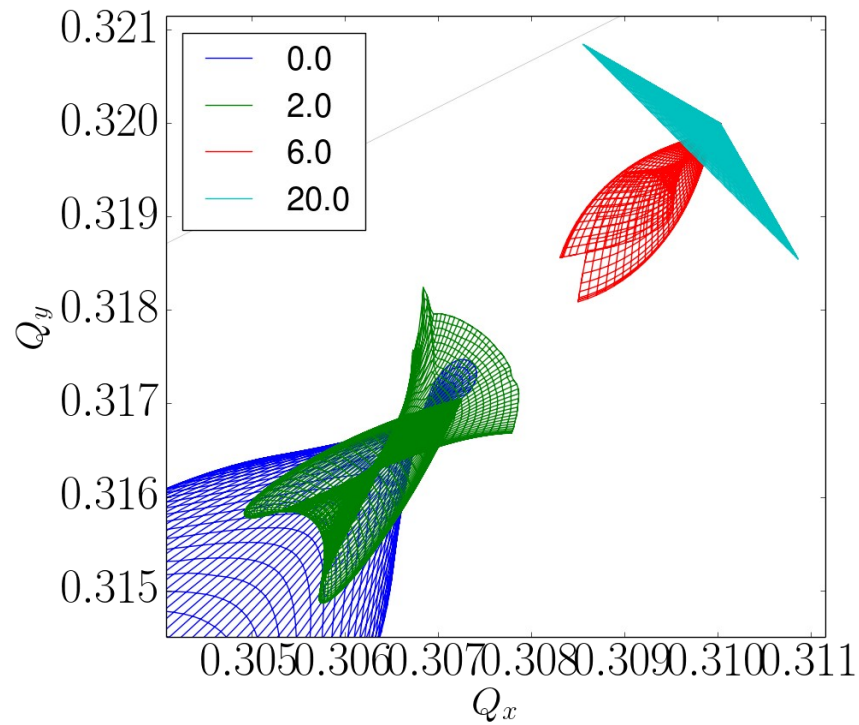
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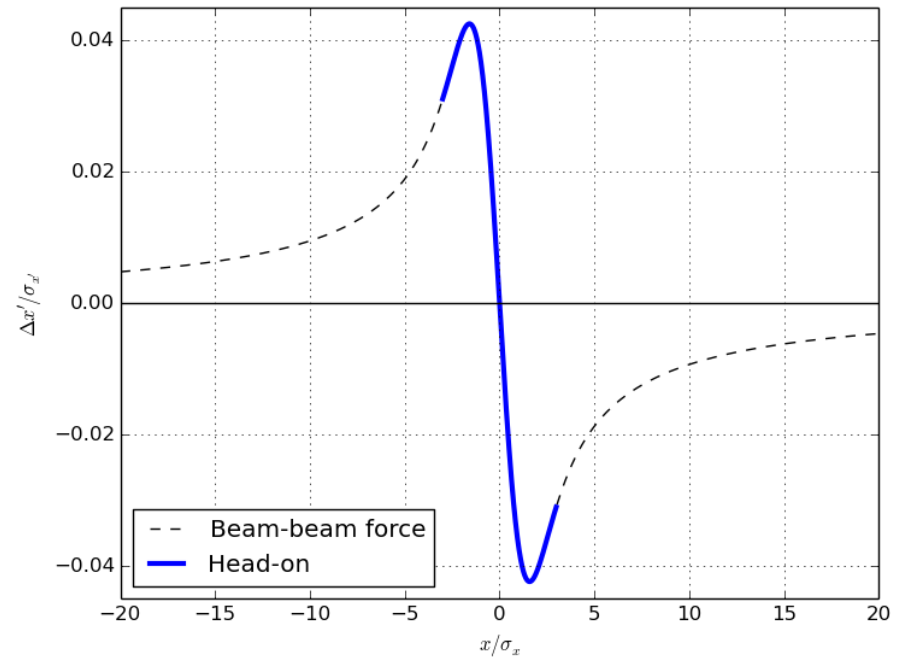
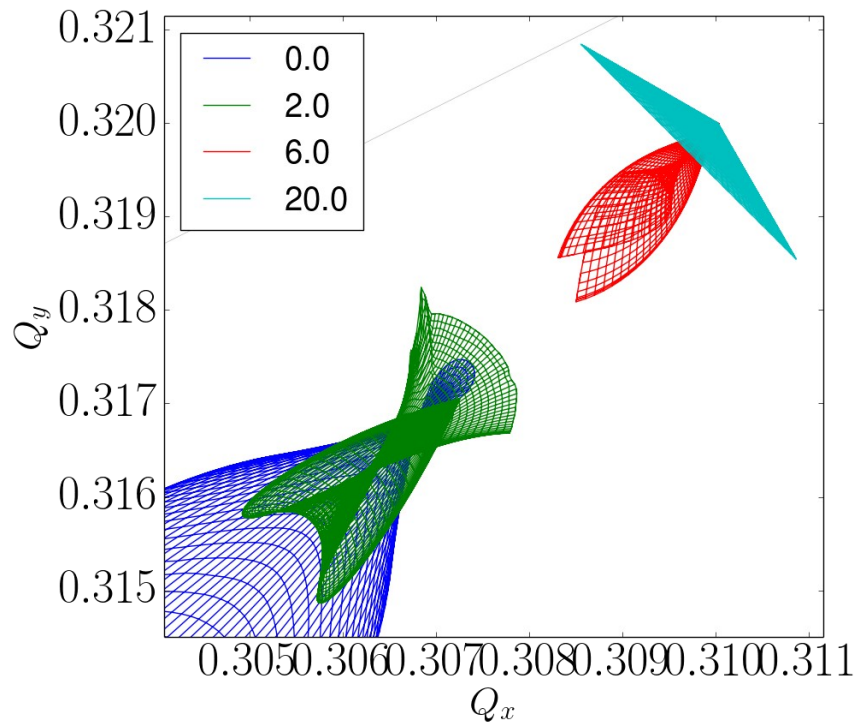


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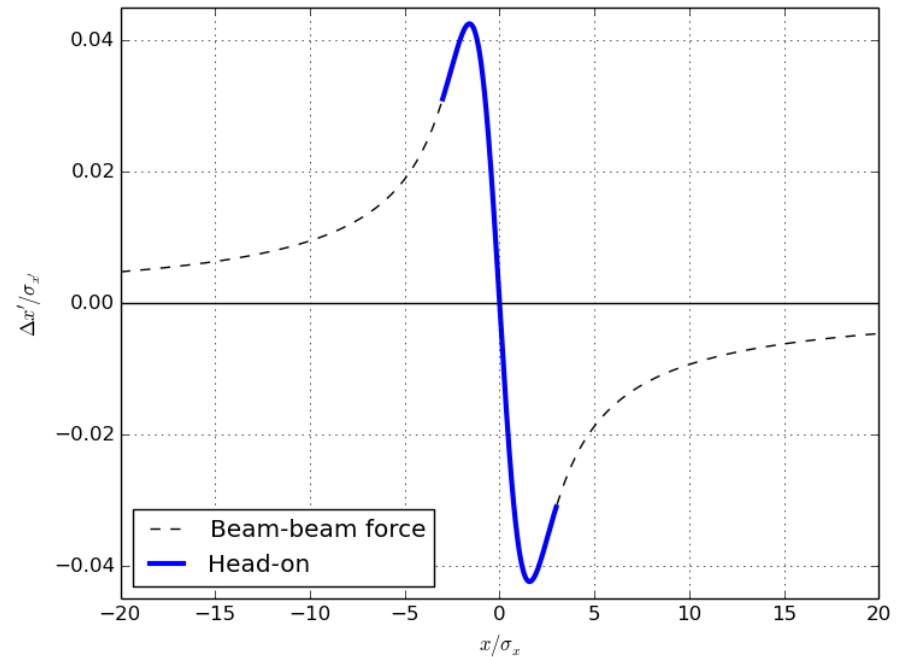
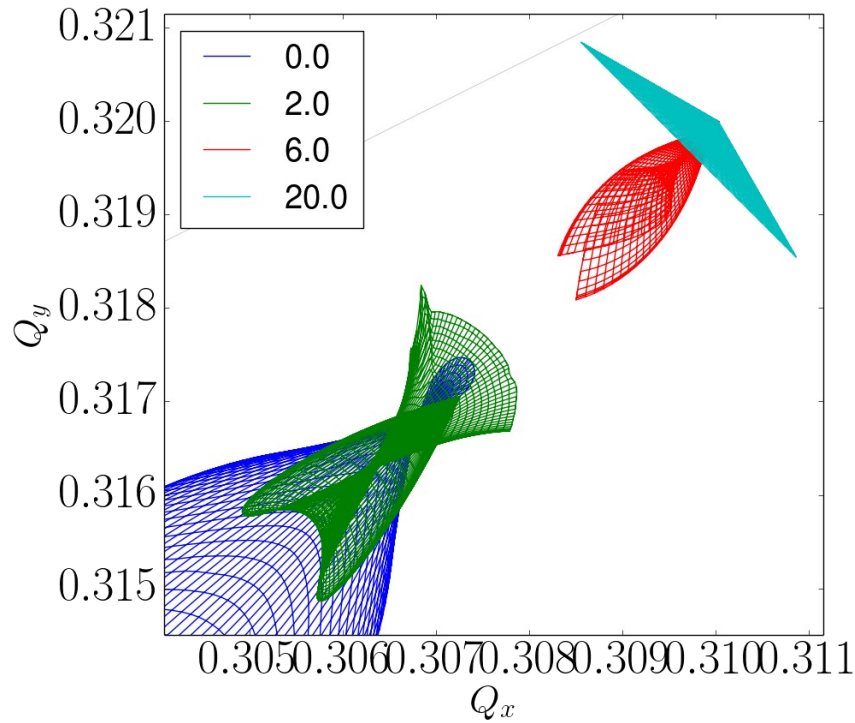
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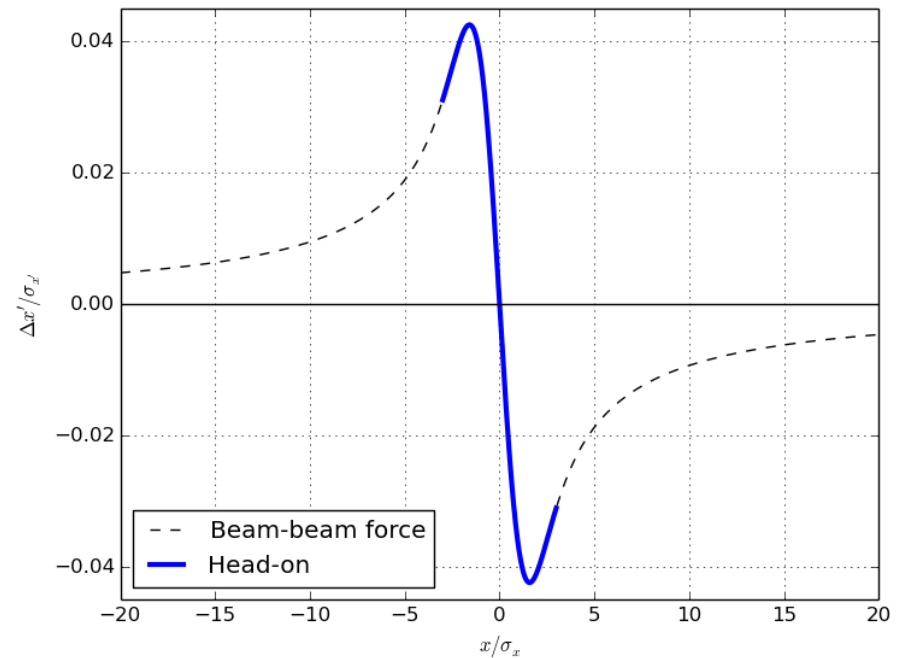
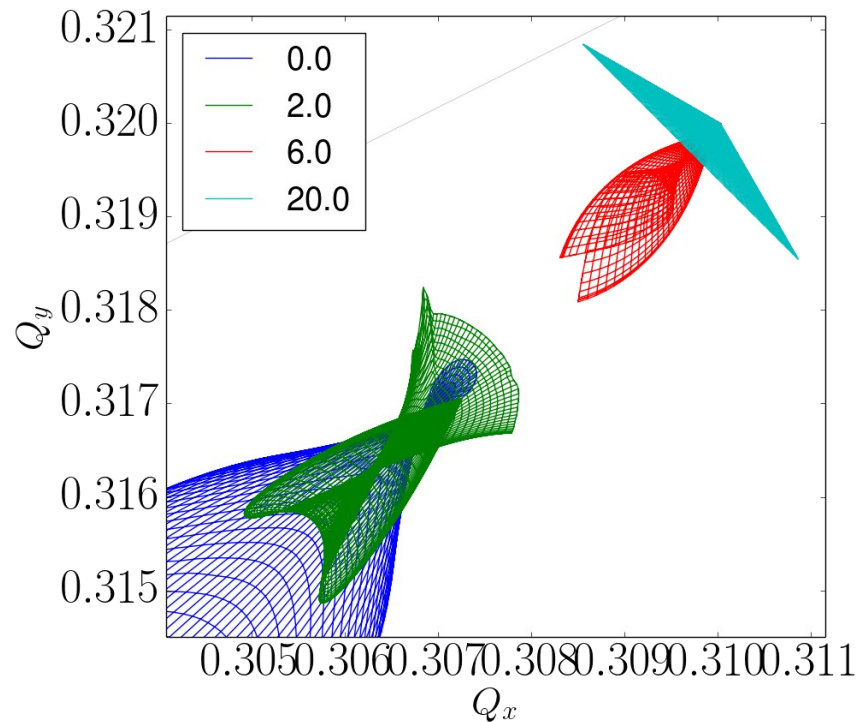
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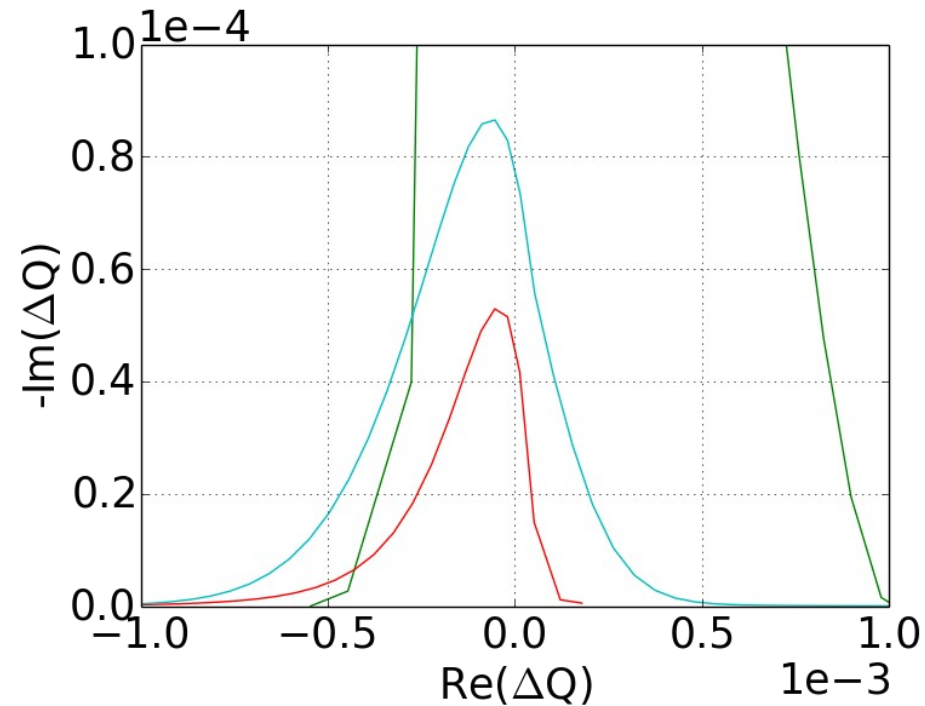
- Even when coherent beam-beam modes are stable, the non-linearity of the beam-beam interactions affect the single particle motion
  - The modification of the amplitude detuning affects Landau damping of single-beam head-tail modes

# Landau damping of head-tail modes



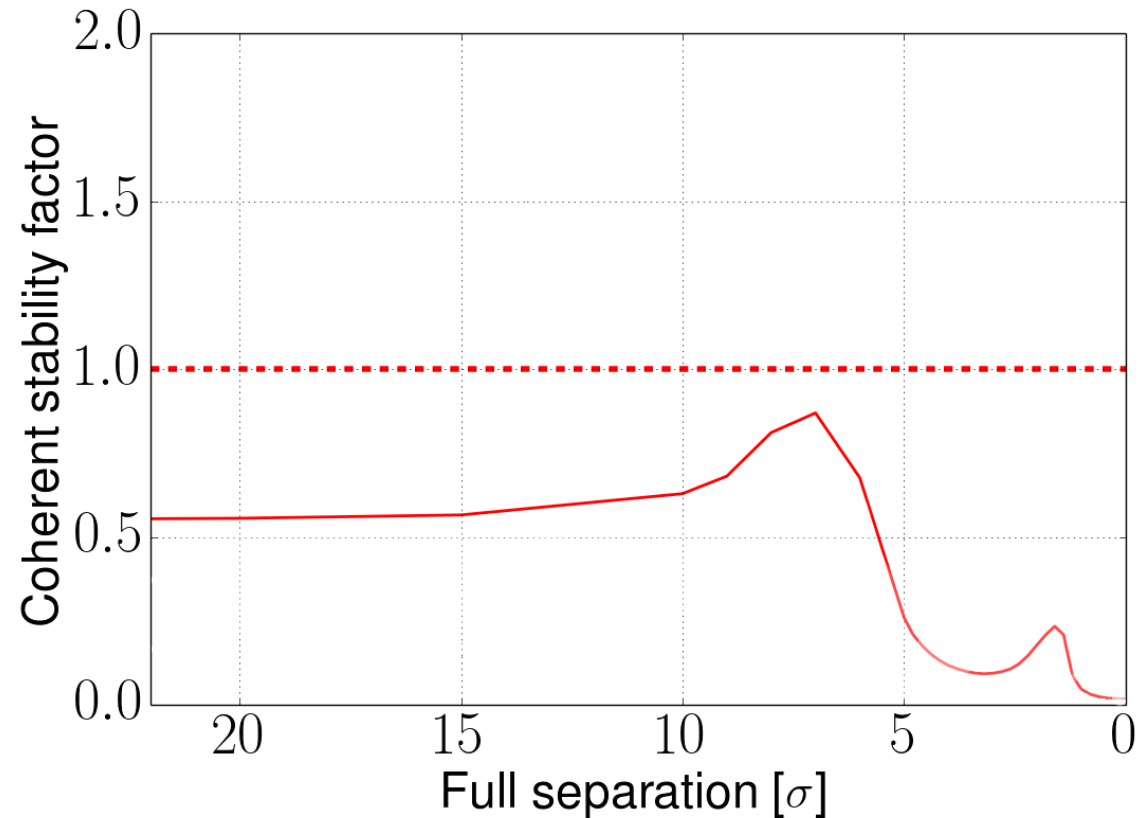
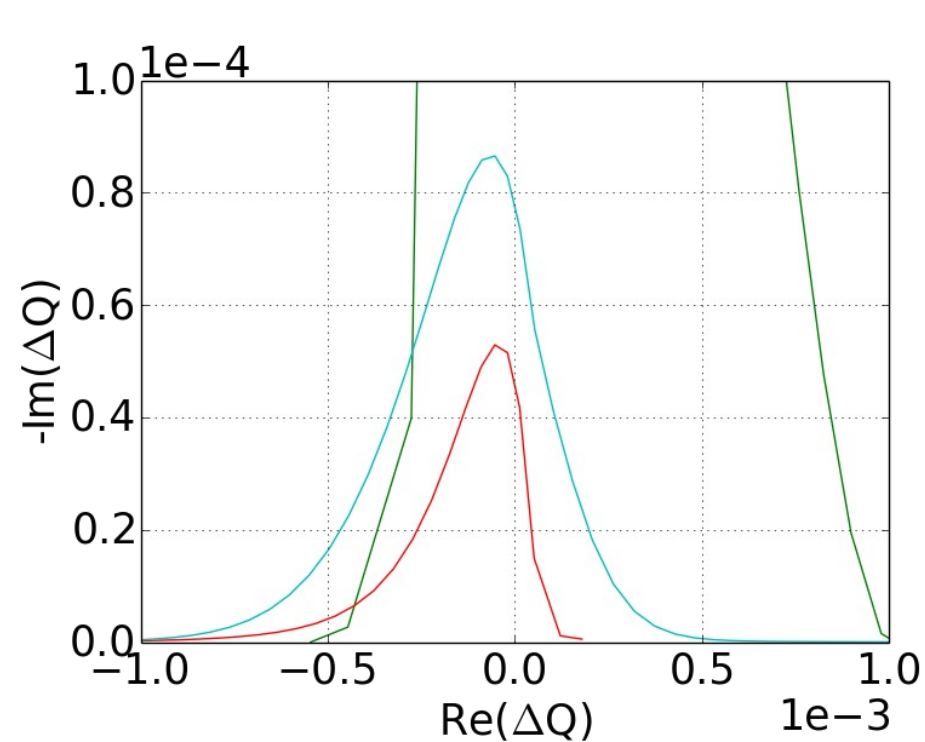
- Even when coherent beam-beam modes are stable, the non-linearity of the beam-beam interactions affect the single particle motion
  - The modification of the amplitude detuning affects Landau damping of single-beam head-tail modes
- The stability diagram can be obtained by numerical integration of the dispersion integral based on tracking data → PySSD *X. Buffat, et al., Phys. Rev. ST Accel. Beams 17, 111002 (2014)*

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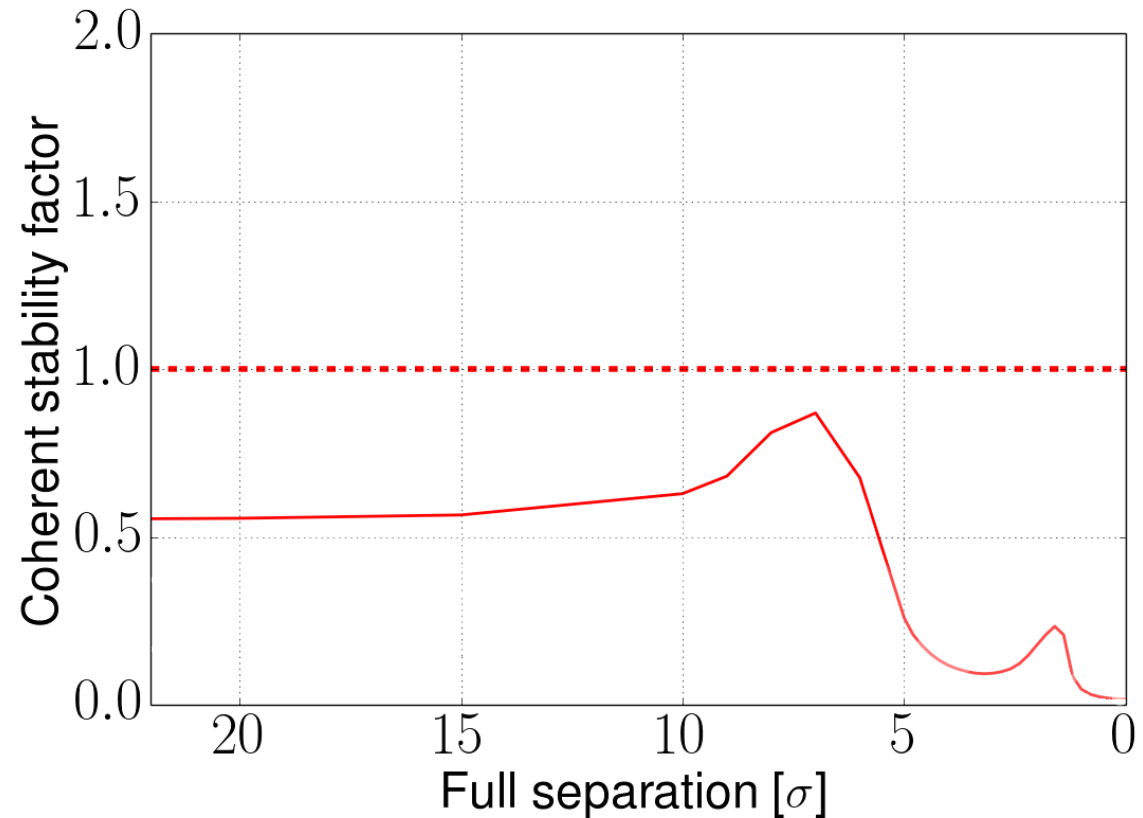
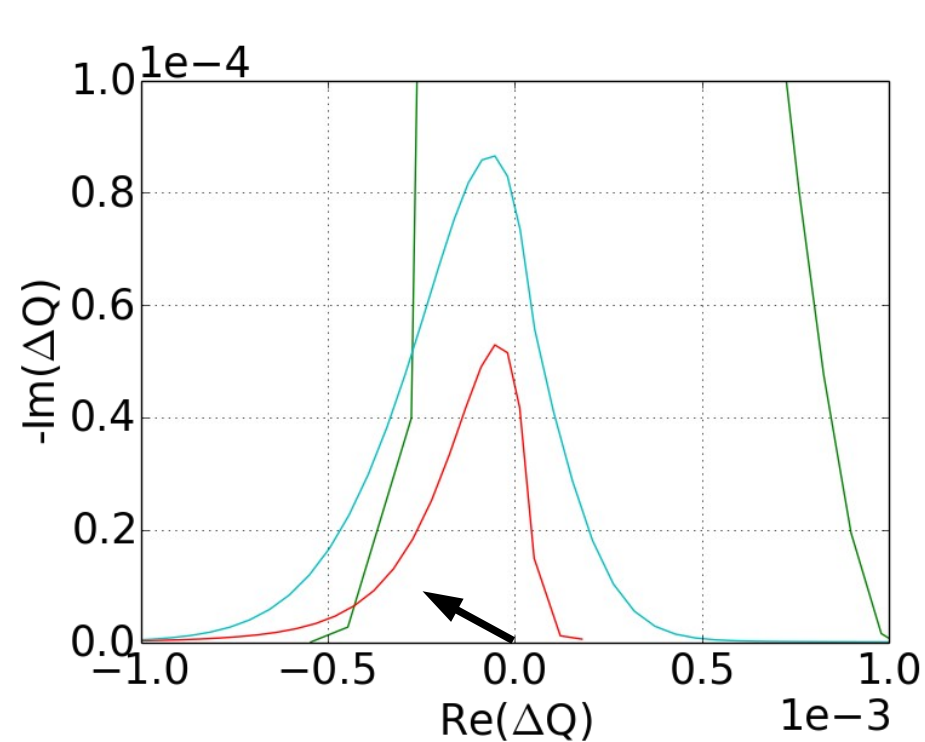
- The coherent stability factor indicates the criticality of Landau damping
  - Used to compare relatively the beam stability in complex configurations and complex processes (e.g. bringing the beams into collision)

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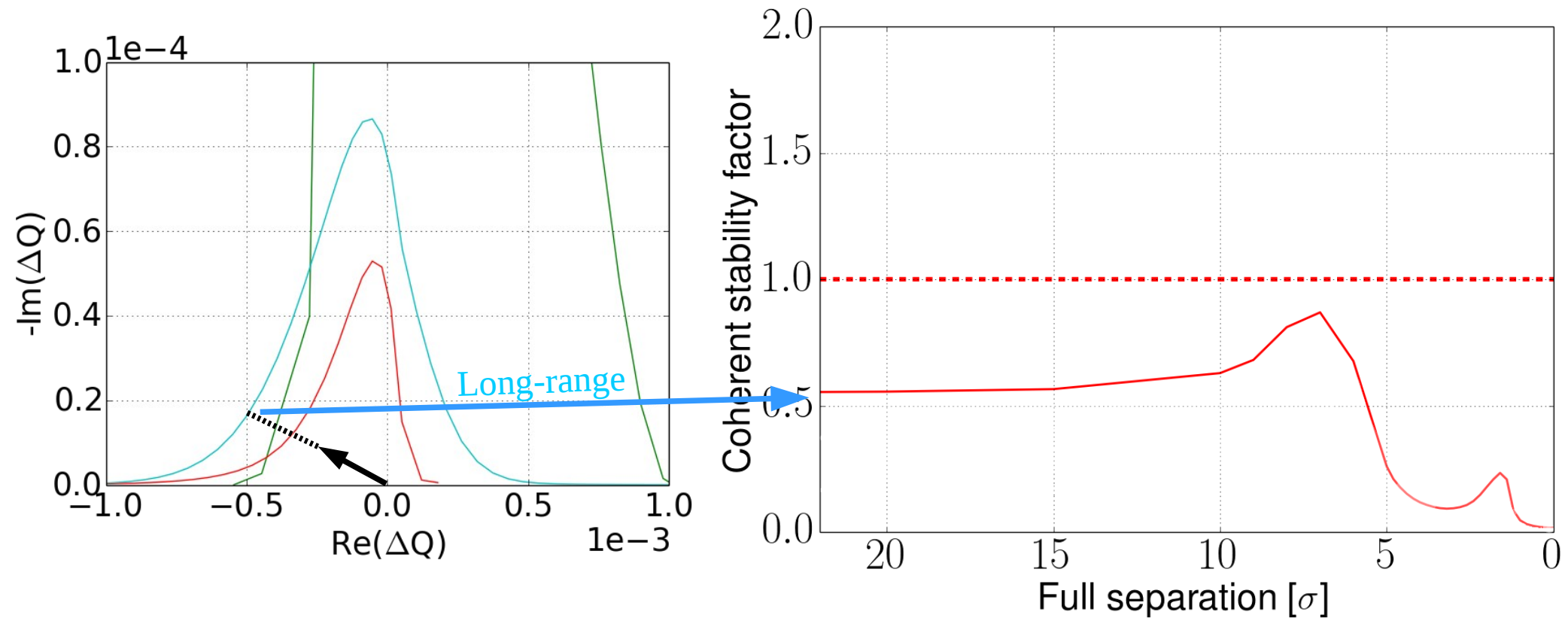
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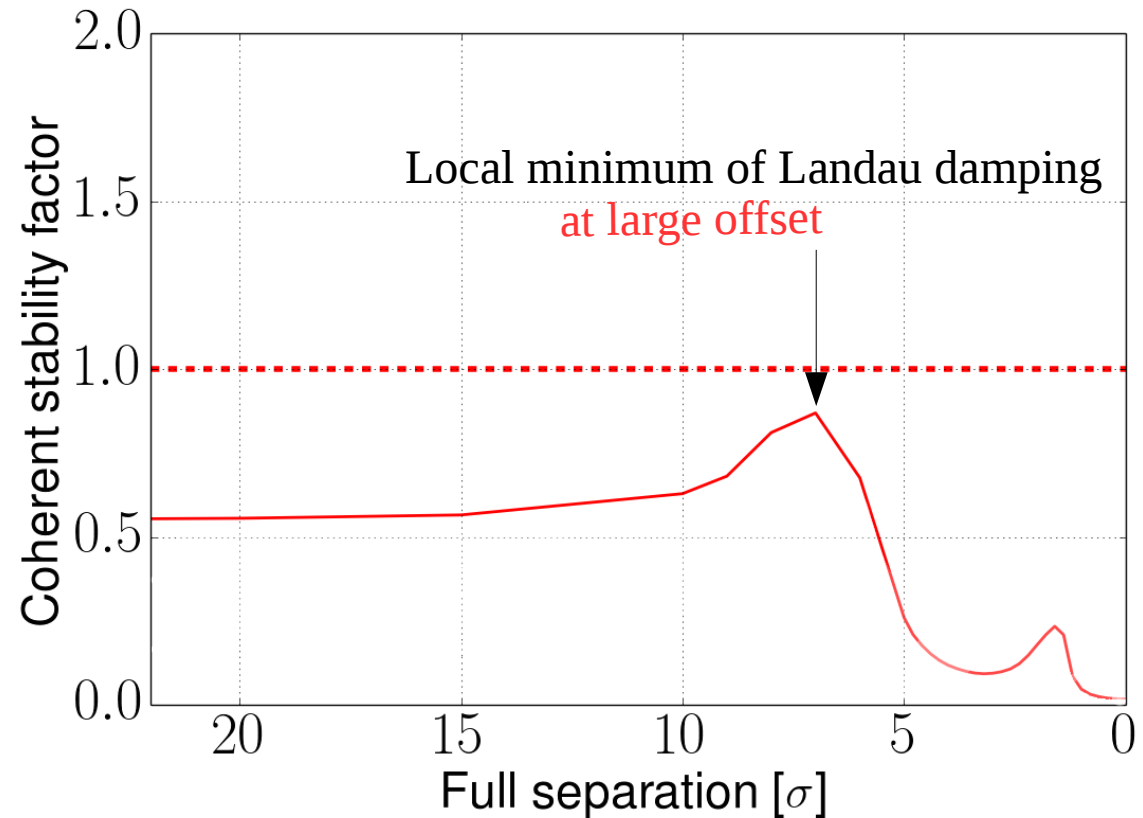
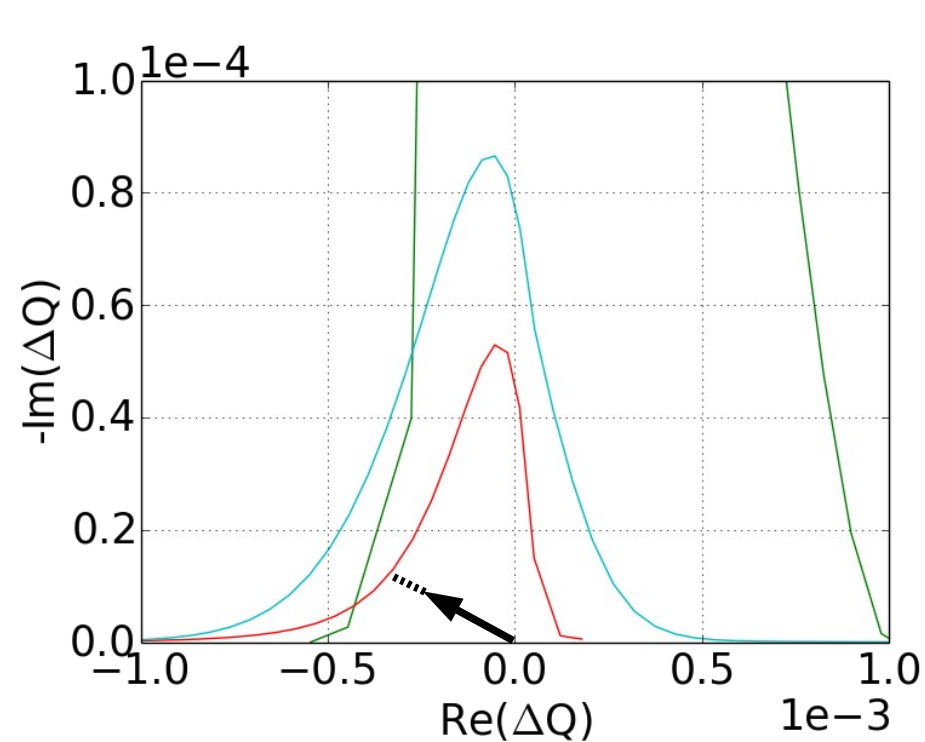
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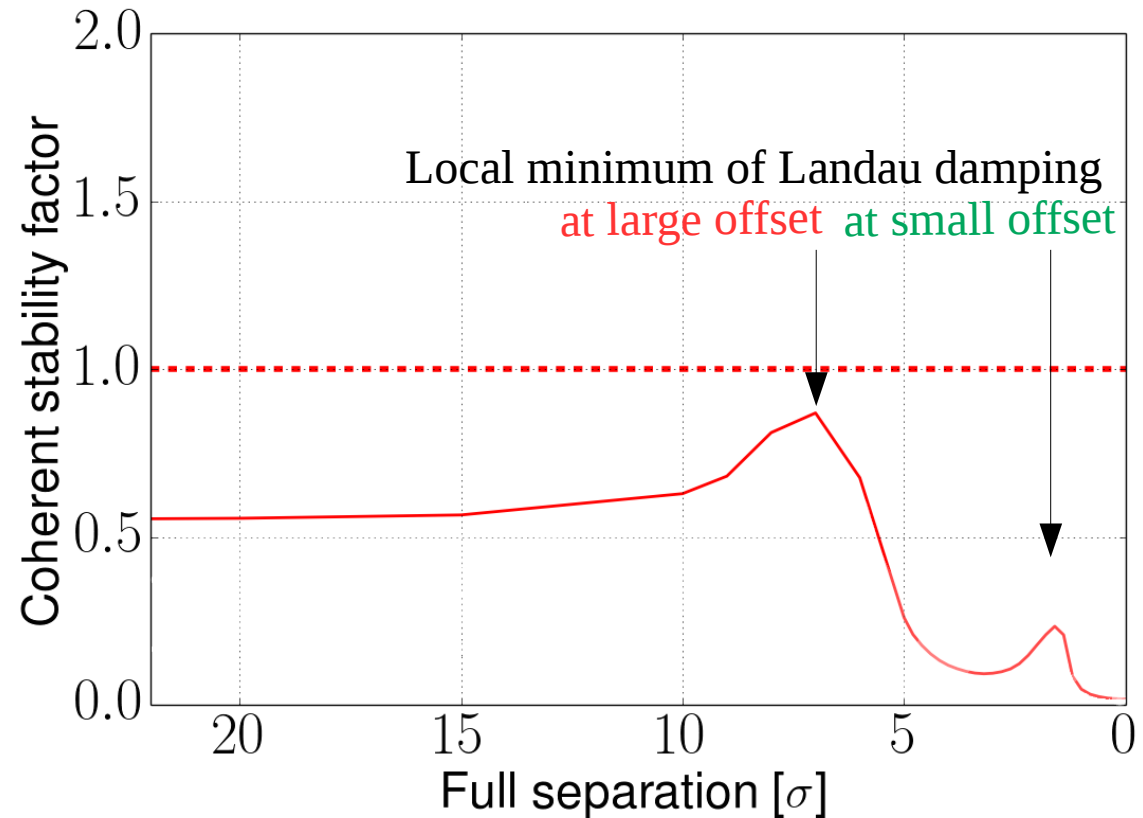
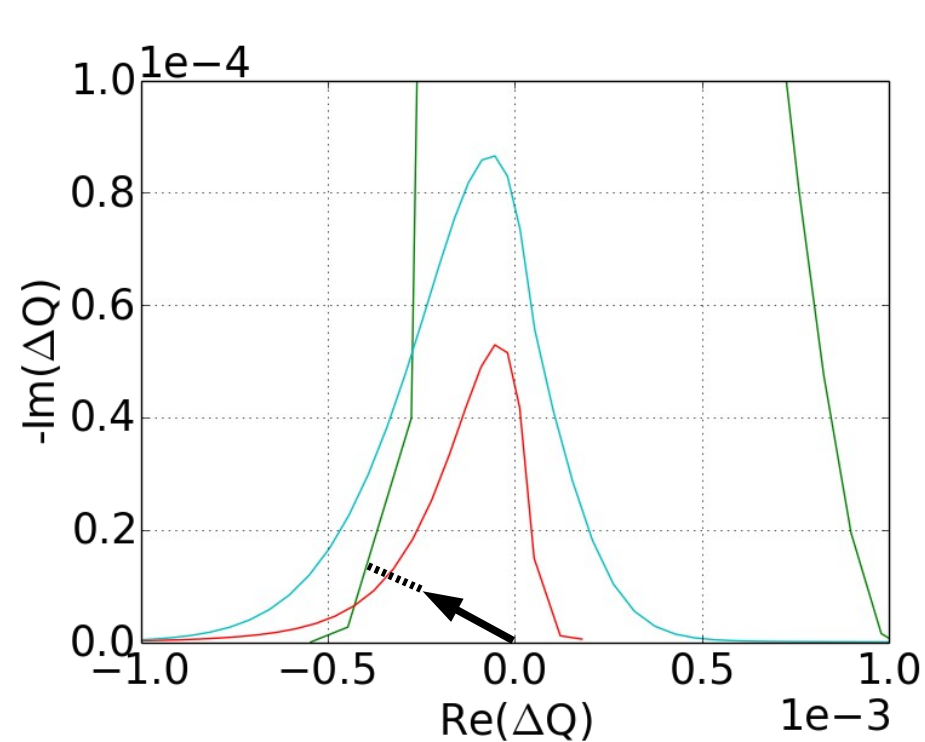


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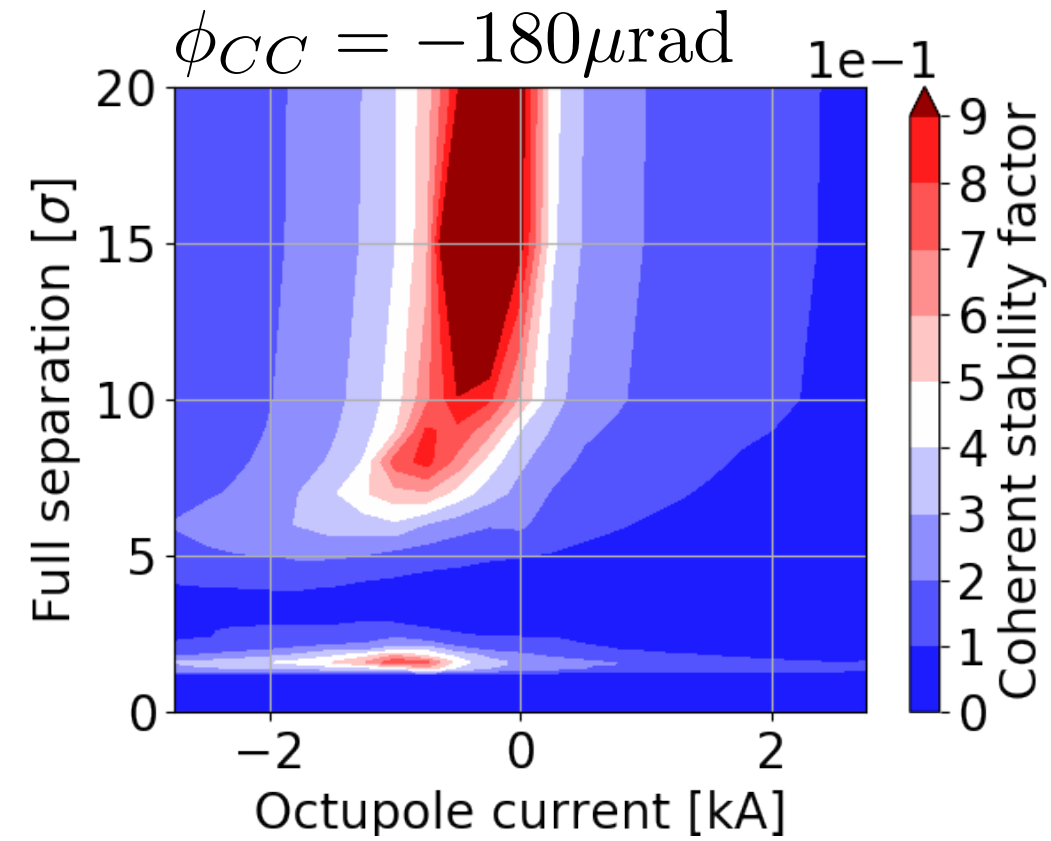
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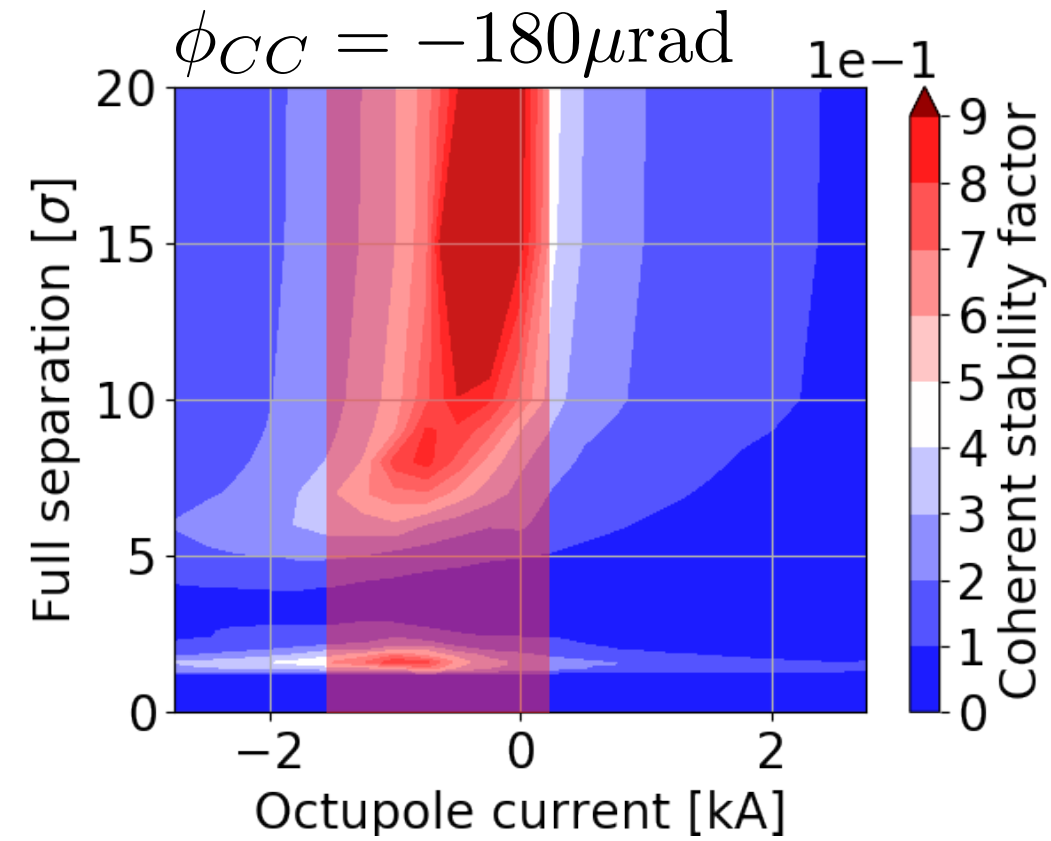


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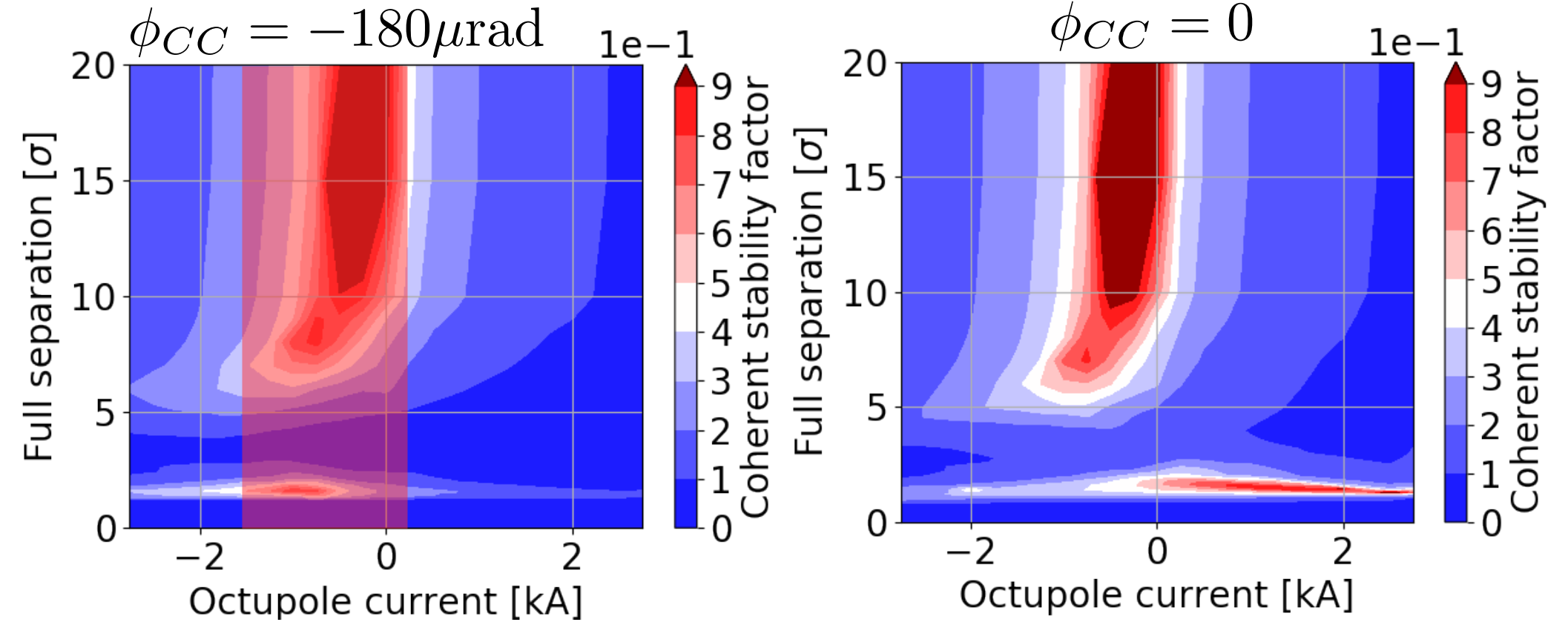
# Offset collisions



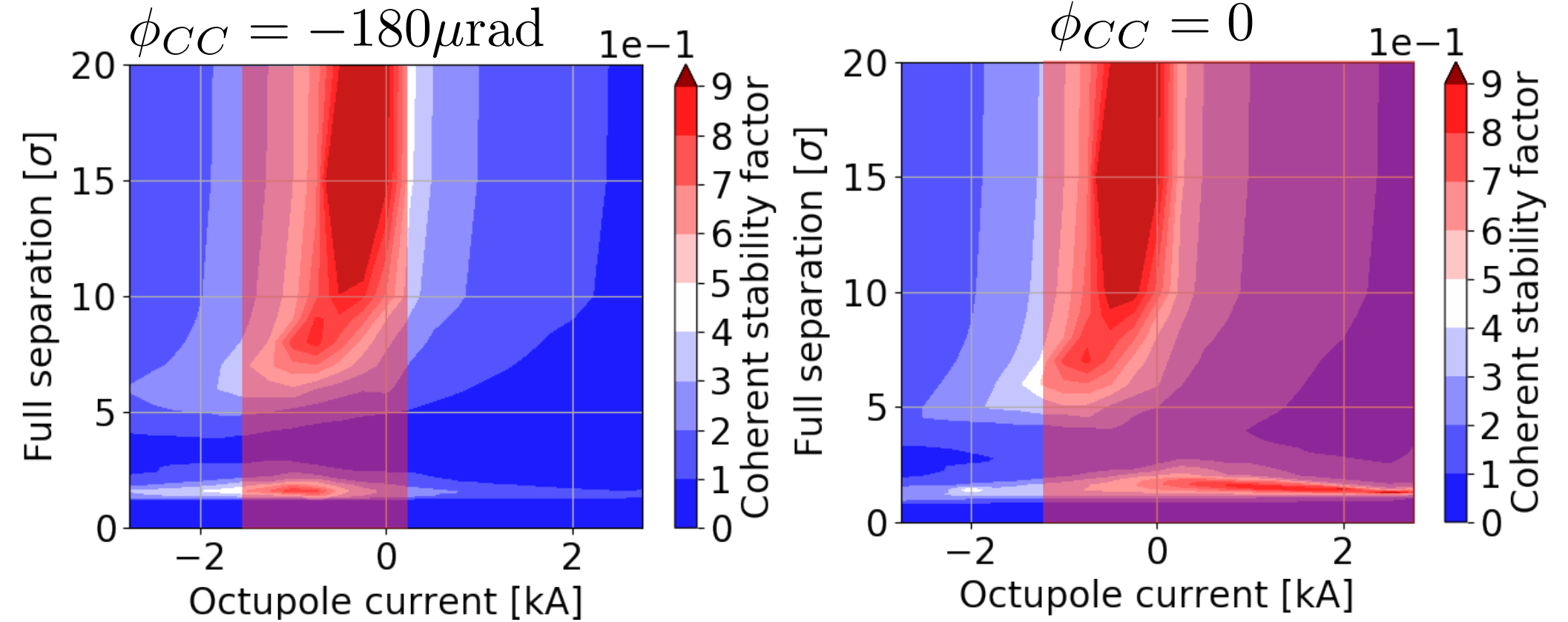
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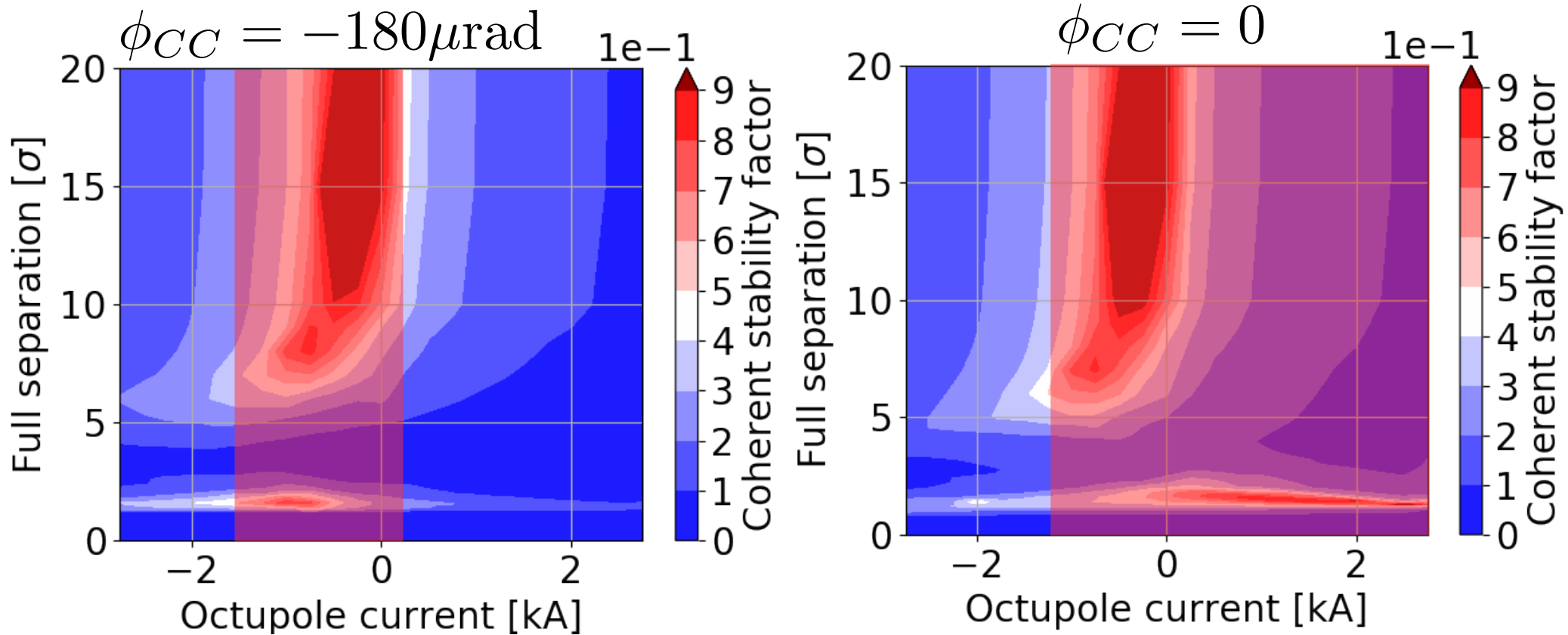


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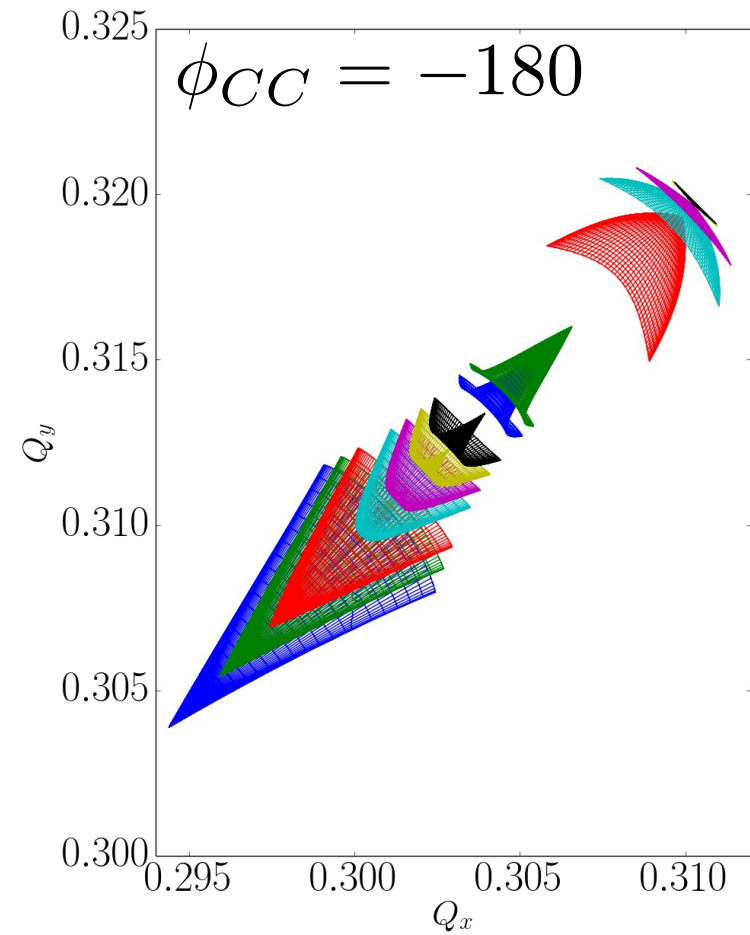


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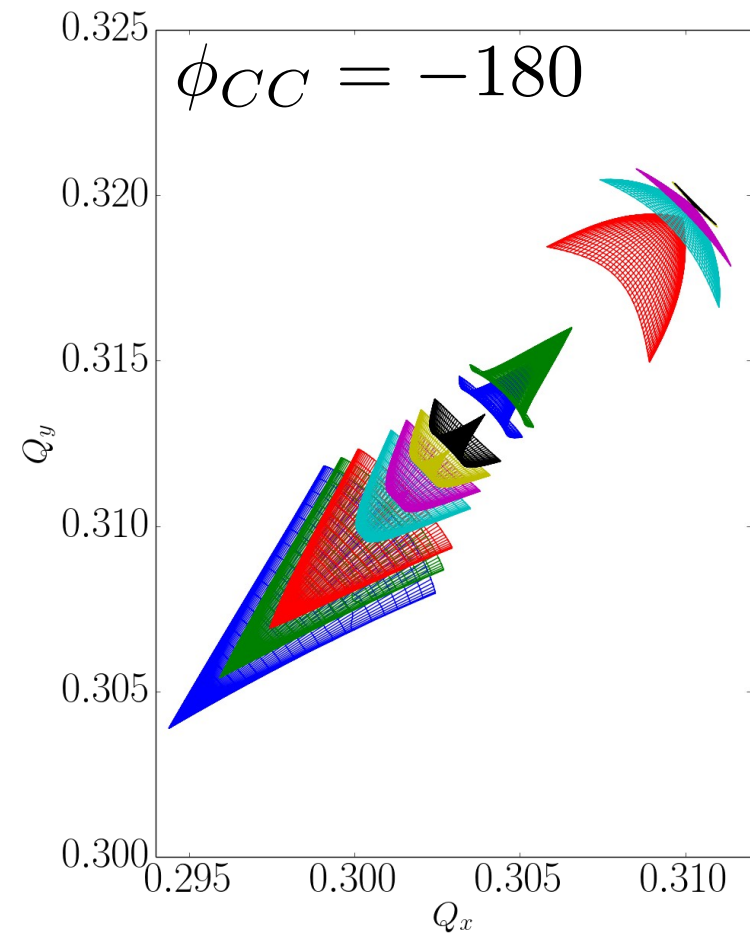
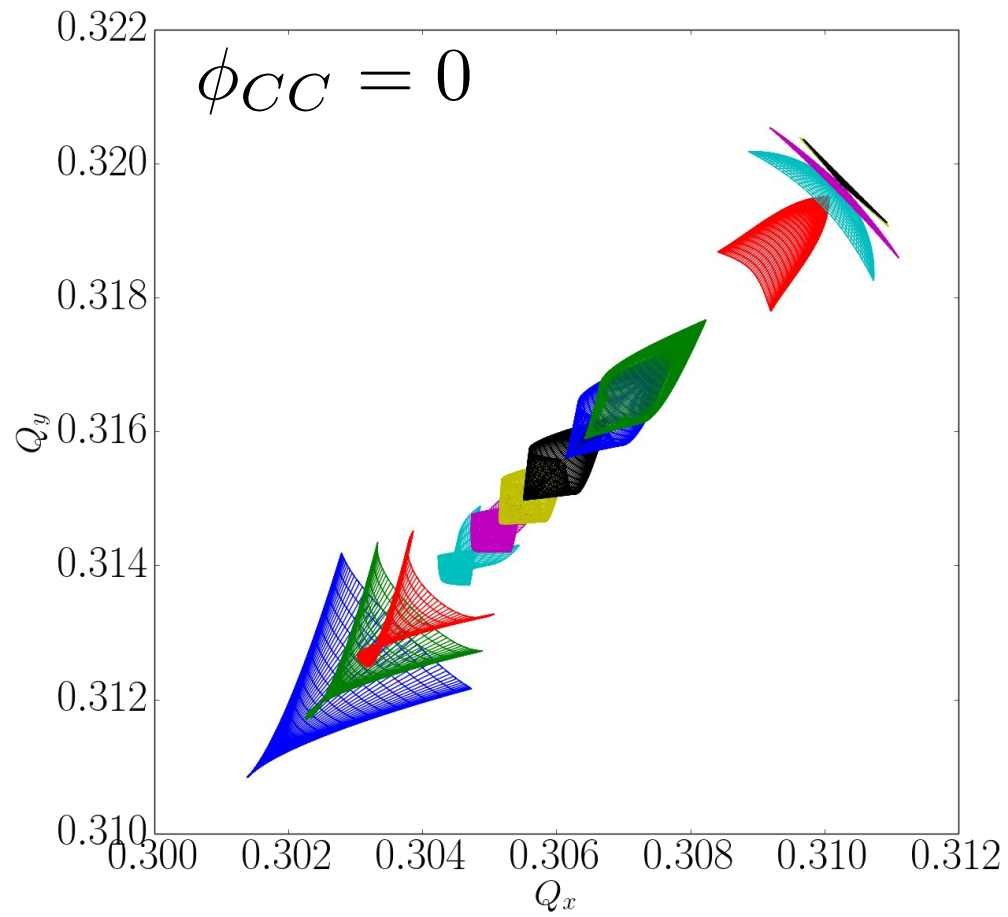


- The operation of the crab cavities with offset beams affects the beam stability as well as the interplay with the amplitude detuning driven by the octupoles
- So does:
  - The  $\beta^*$
  - The crossing / crab angle
  - The plane and synchronisation of the separation bumps in the different IPs

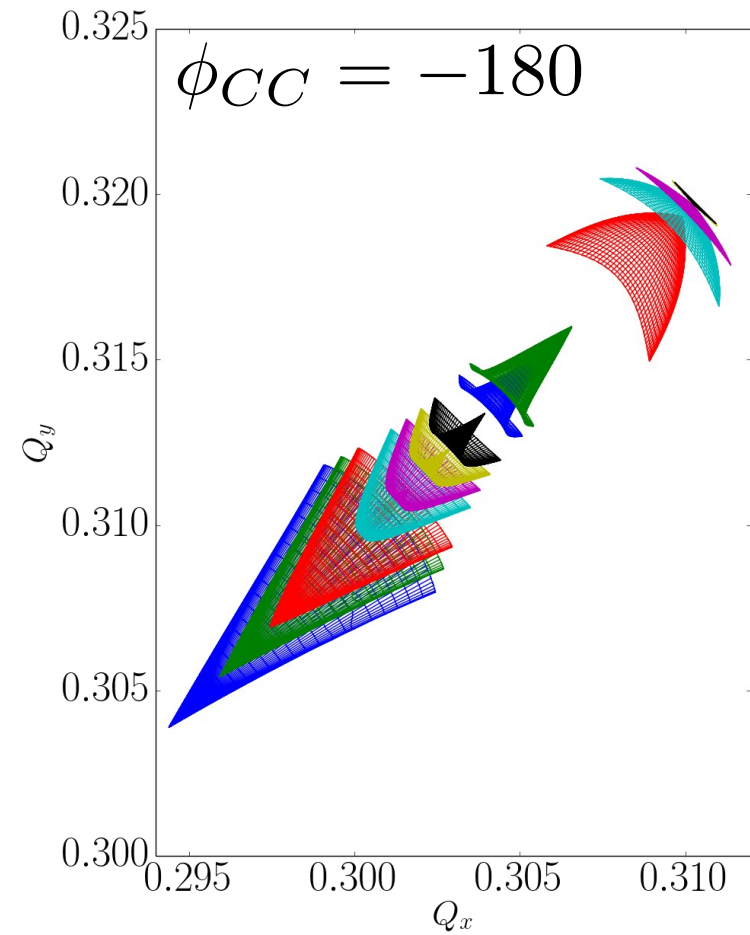
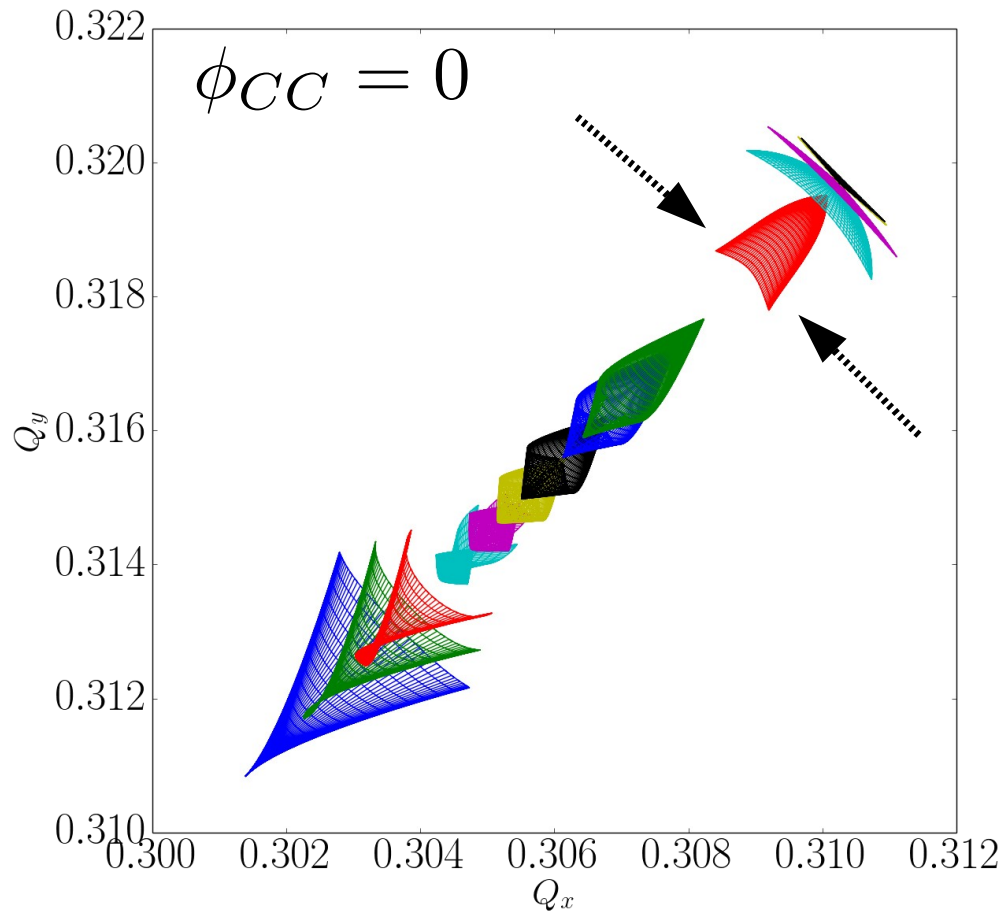
# The Shakiri effect



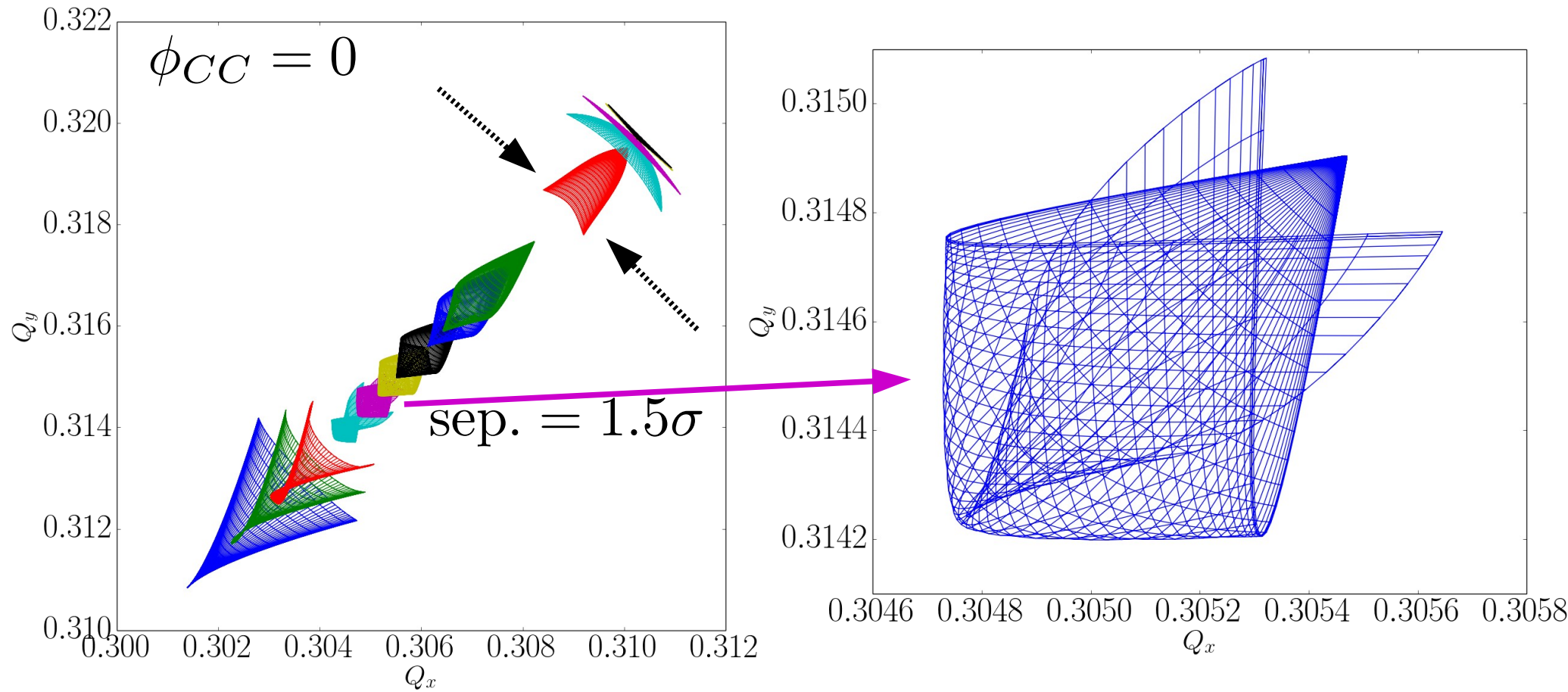
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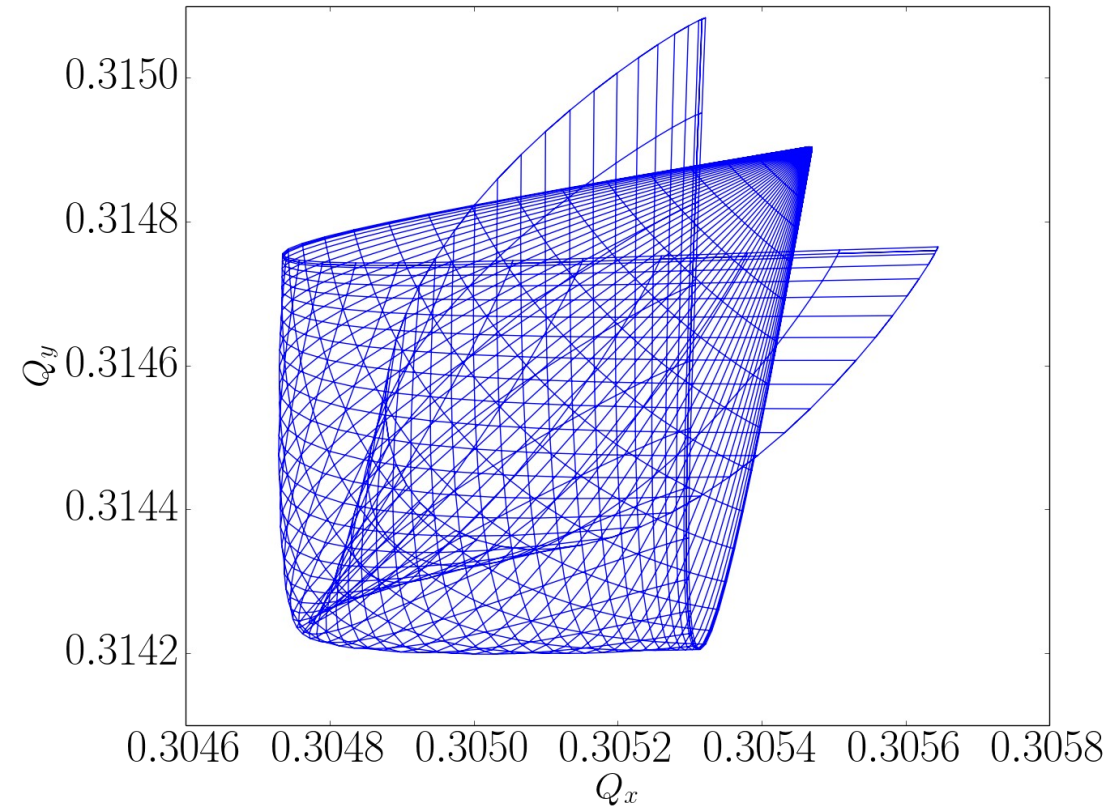


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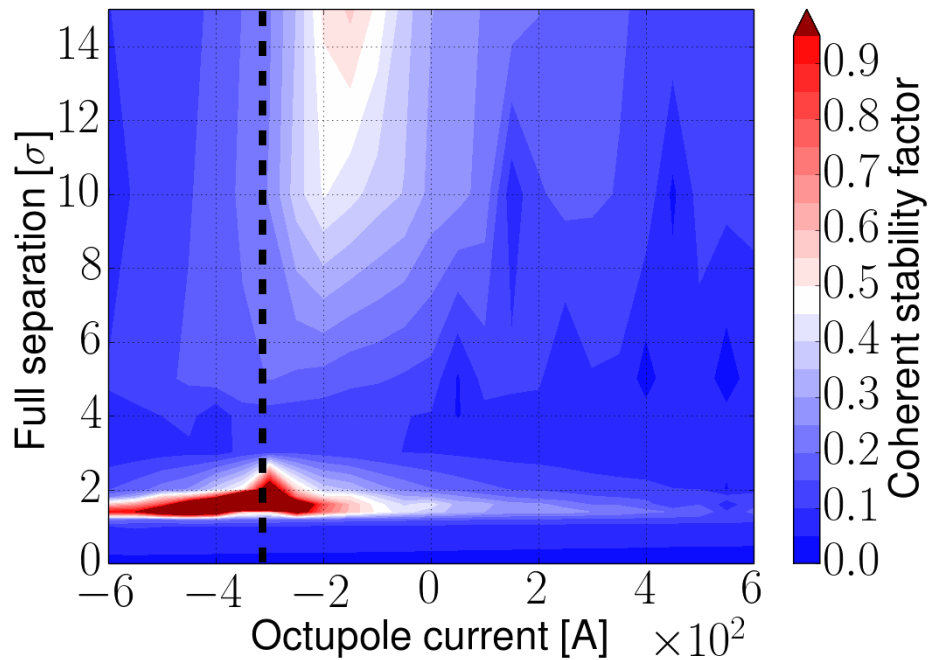


- Xherdan Shakiri was misunderstood: he was trying to tell us about a mitigation strategy for the loss of Landau damping with offset beams



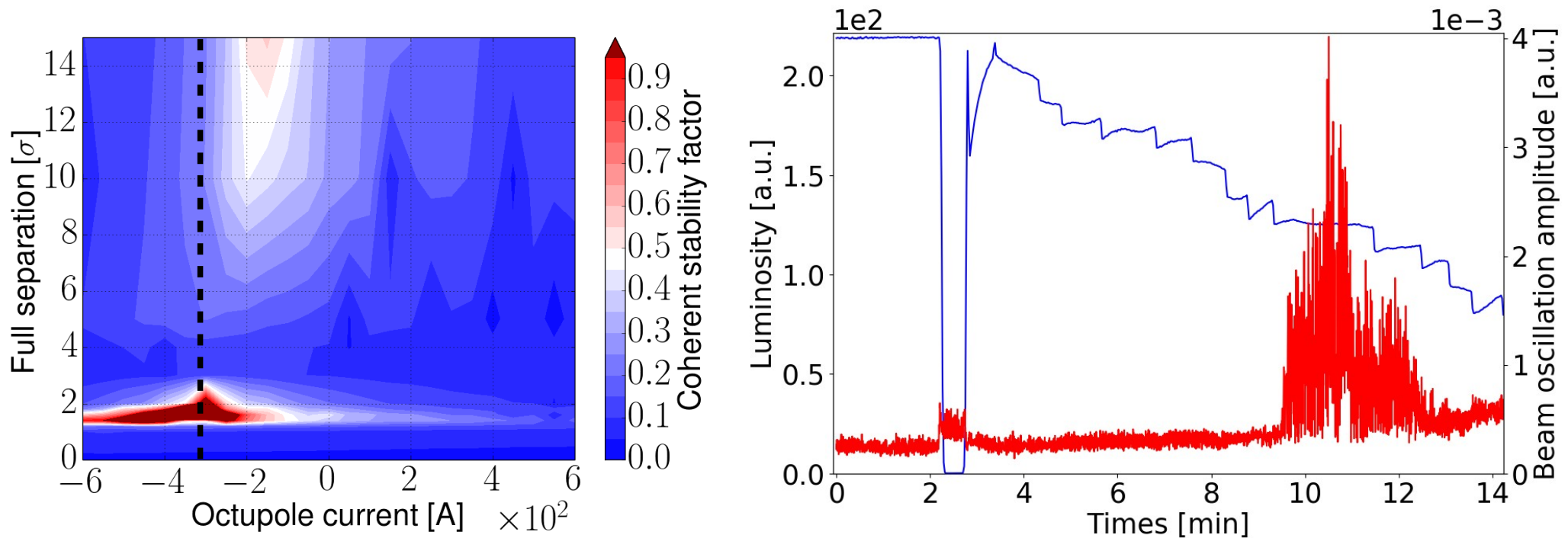
# Observations

- First observations in 2012, due to offset levelling in IP8
- Dedicated experiment in 2018, demonstrating mitigation by fast crossing of the unstable condition S. Fartoukh, et al., CERN-NOTE-2019, in prep.
  - This mitigation is not suitable for luminosity levelling



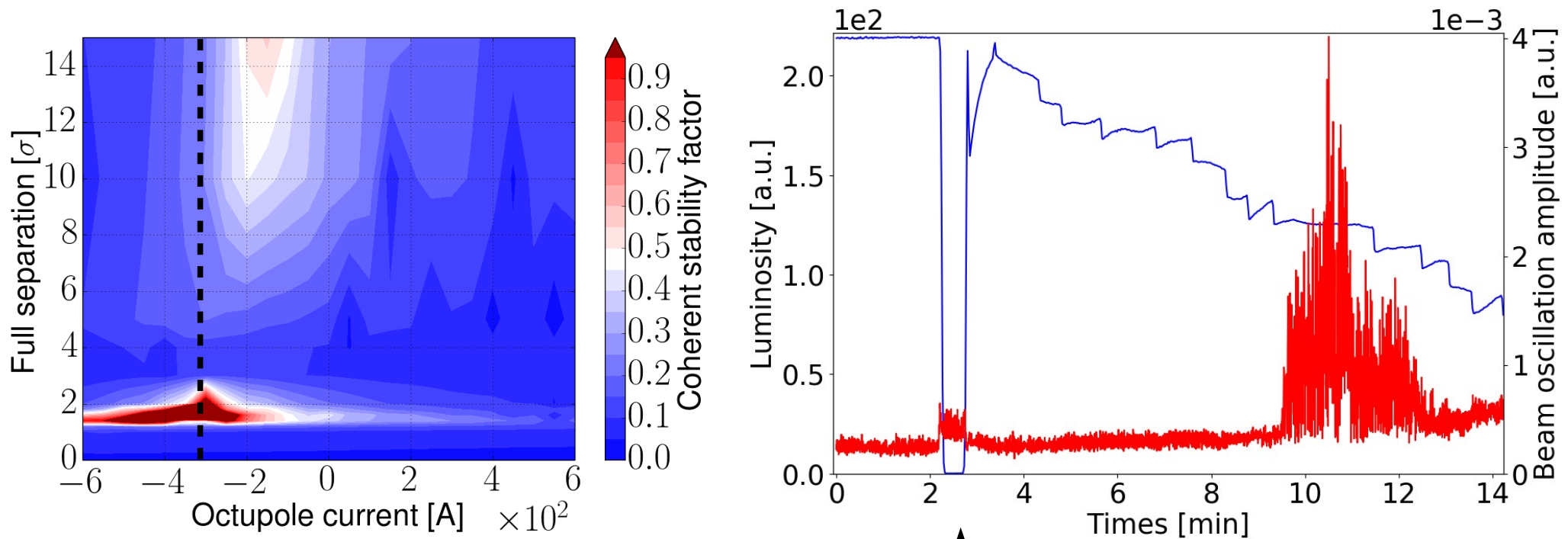
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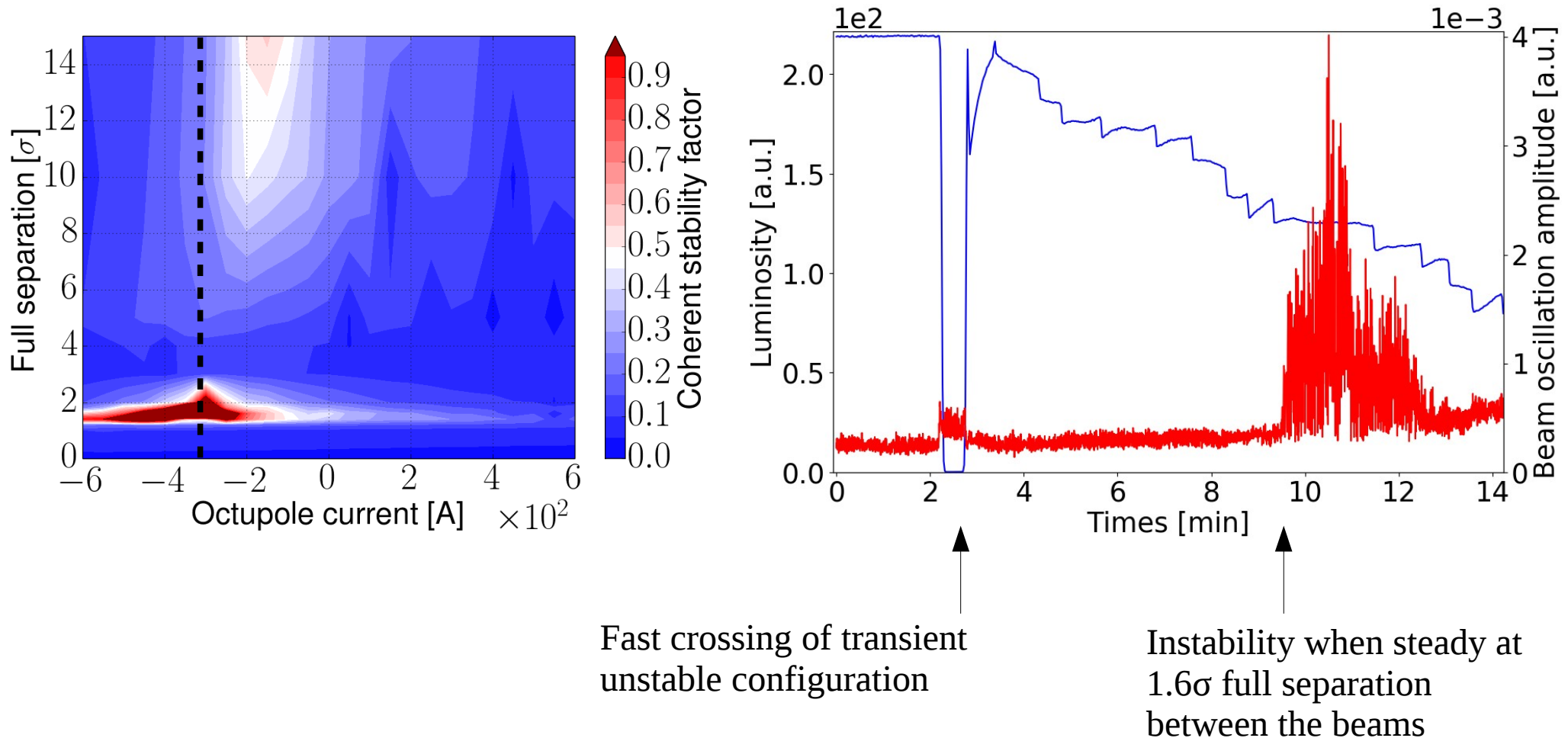
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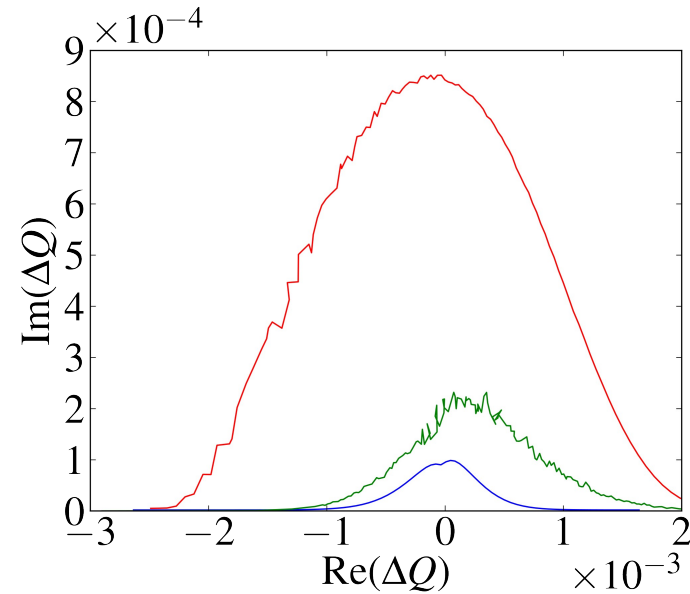
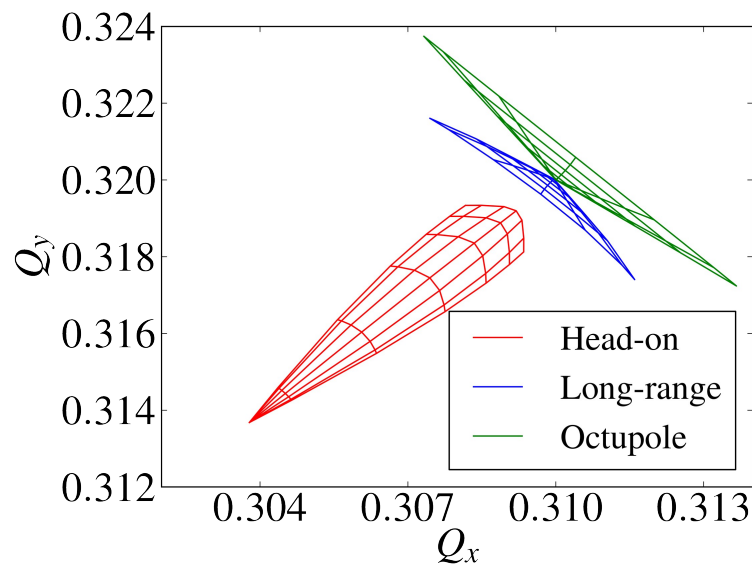
Fast crossing of transient  
unstable configuration

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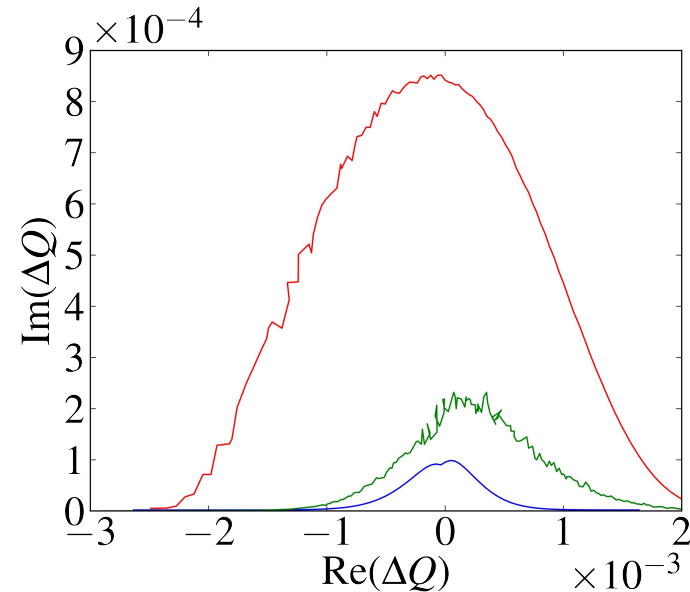
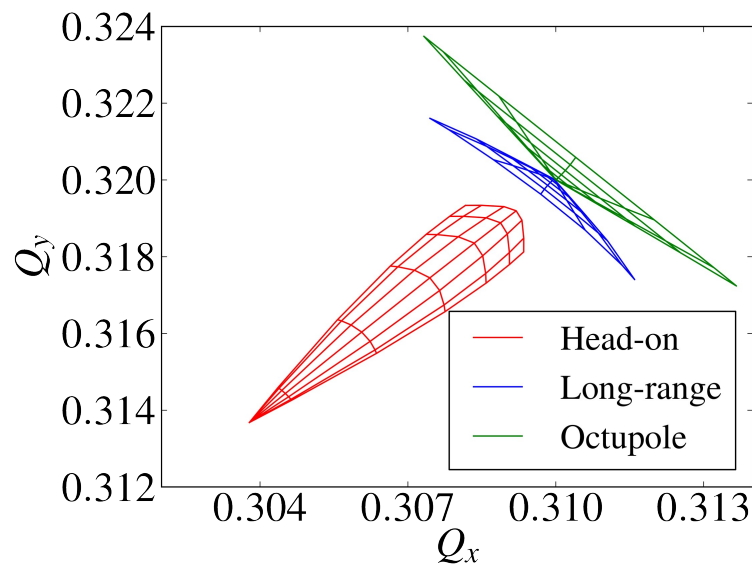


# Head-on interaction

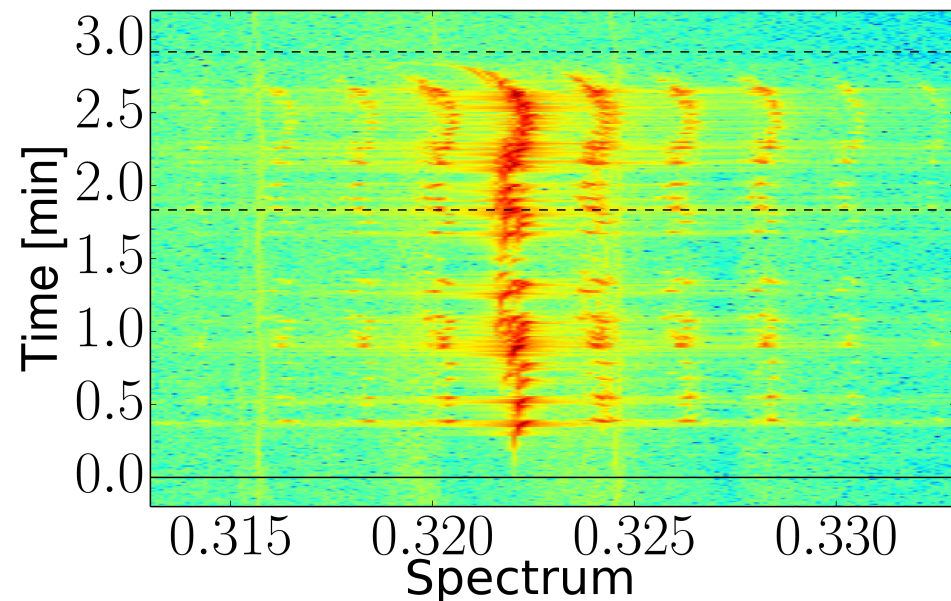


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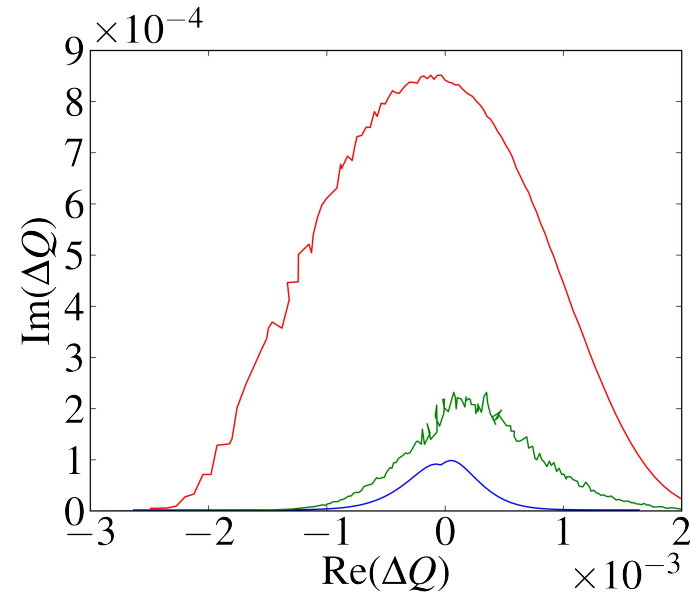
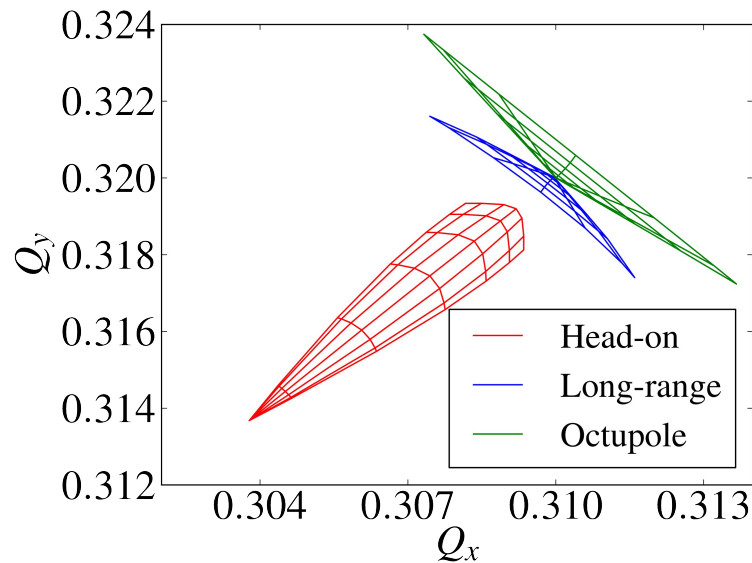


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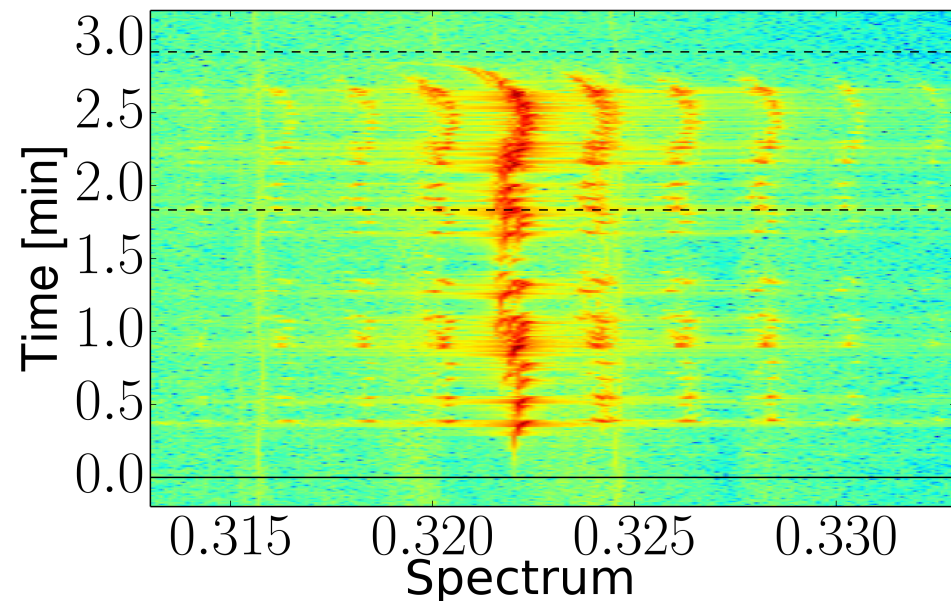
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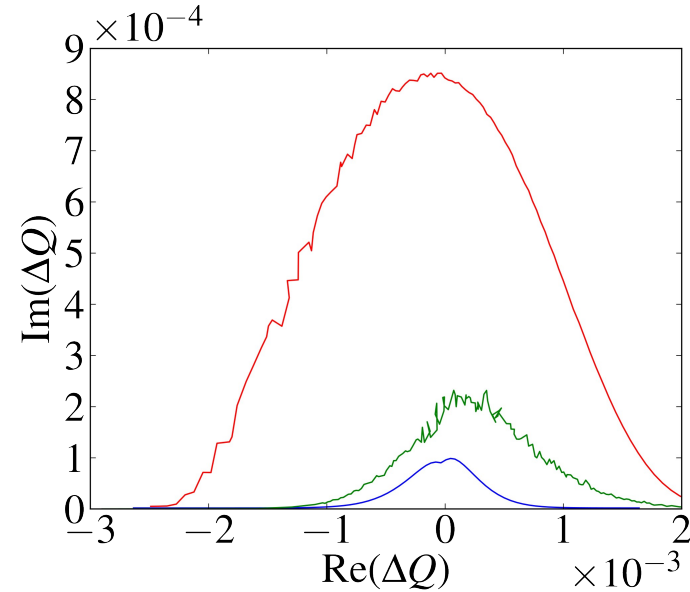
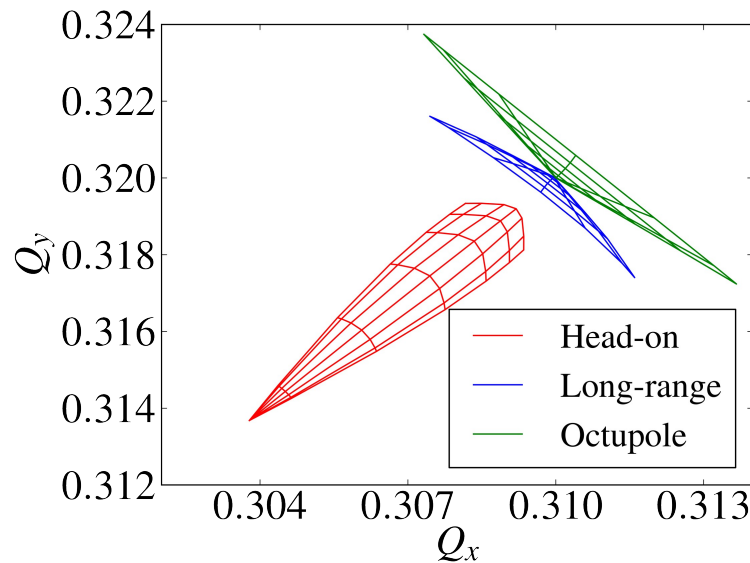
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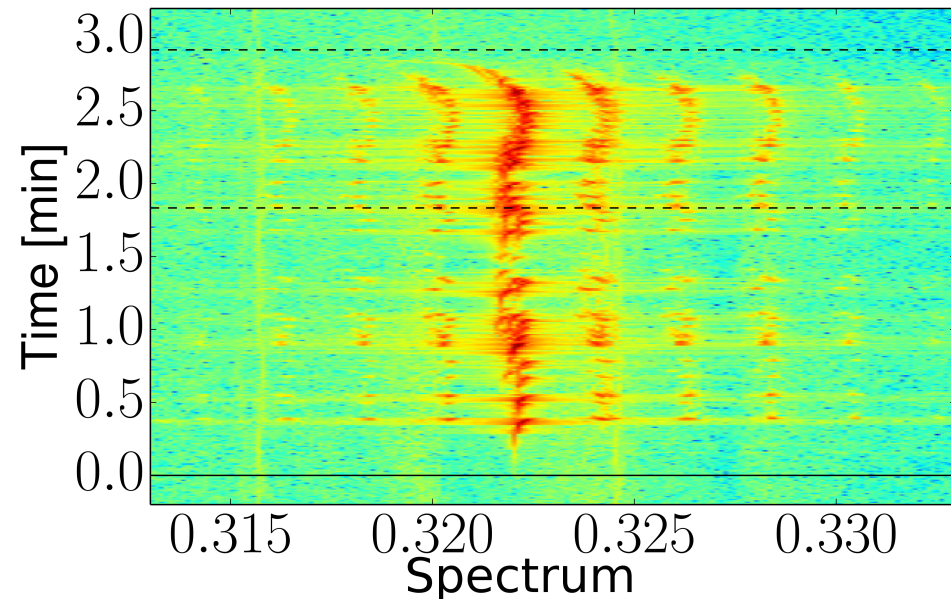
A. Romano, et al., Phys. Rev. Accel. Beams 21, 061002 (2018)



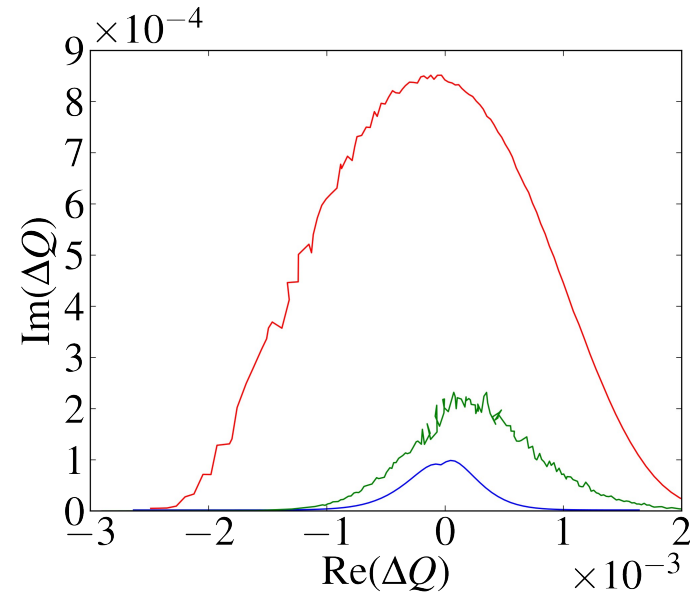
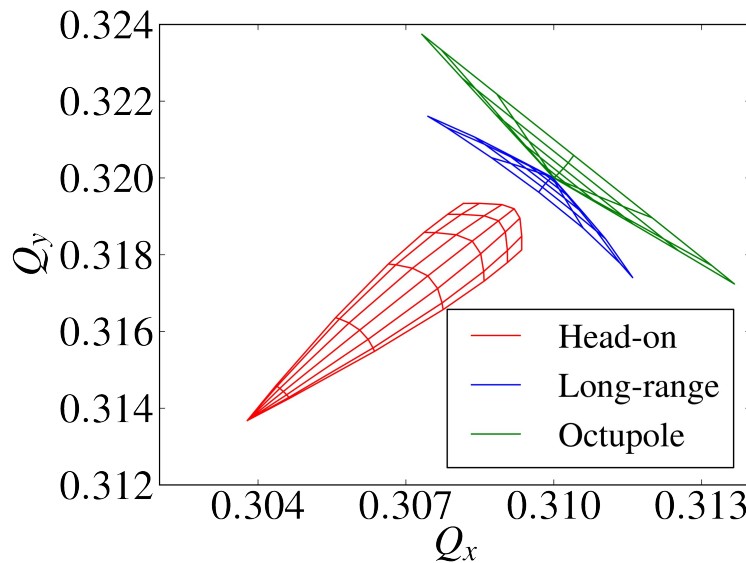
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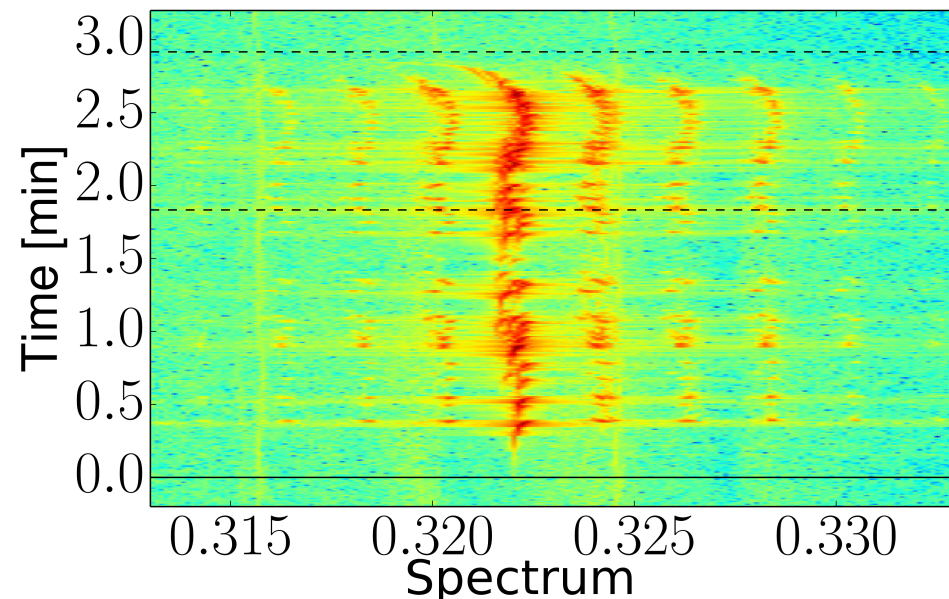


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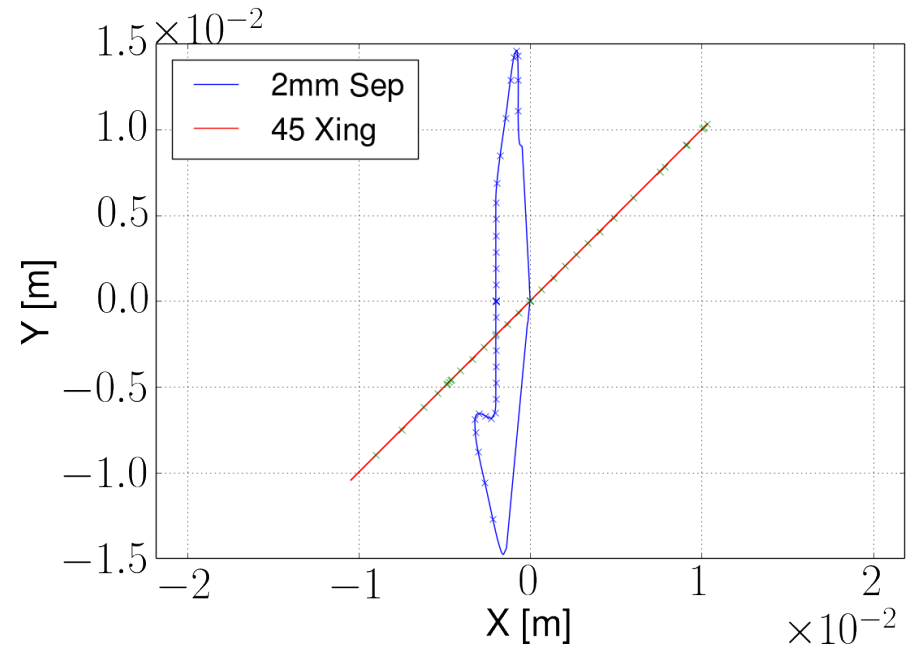
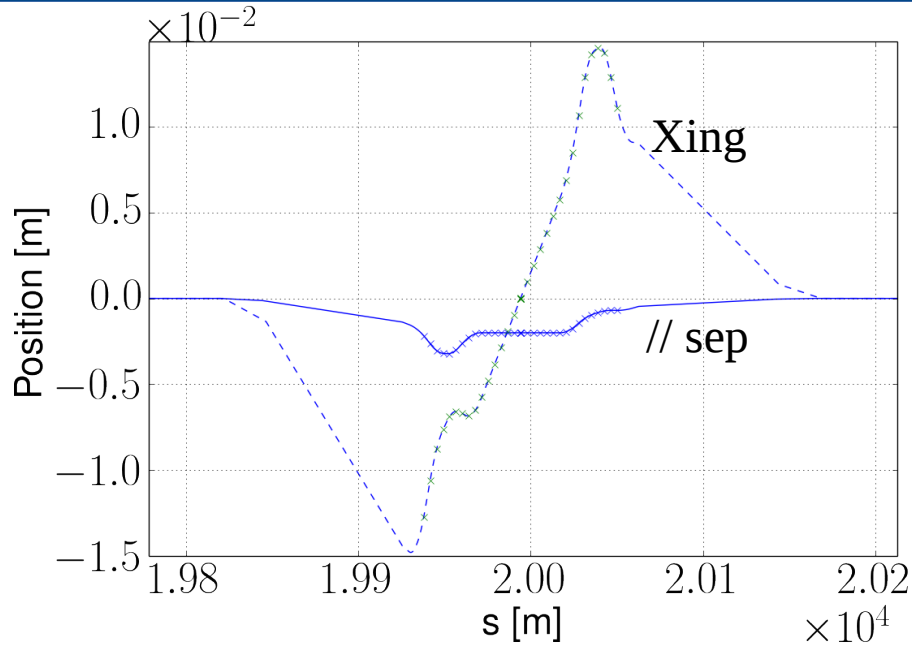


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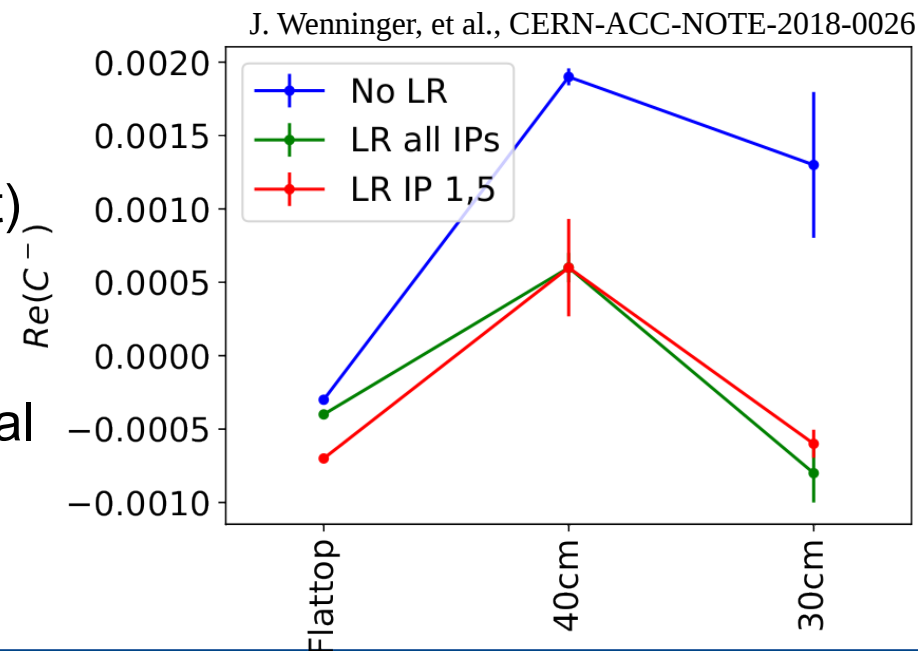
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- An e-lens mimicking this behaviour would have a similar potential as a MCBI  
V. Shiltsev, et al., Phys. Rev. Lett. 119, 134802 (2017)



# Linear coupling due to beam-beam interactions



- Long-range beam-beam interactions on a skew plane generate coupling and therefore can reduce Landau damping
- Missing long-range interaction (PACMAN effect) makes this contribution uncorrectable for all bunches A. Ribes Metidieri, et al., CERN-ACC-NOTE-2019-0037
- The control of the orbit in the IR becomes critical for the beam stability





# Summary

- The mitigation of coherent beam-beam instabilities starts with the rings' layout mostly for asymmetric *periodic* colliders
- The interaction of coherent beam-beam modes with the machine impedance can lead to mode coupling instabilities
  - Depending on the impedance and the interaction type (long-range, head-on, crossing angle, crab angle,  $\beta^*/\sigma_s$ ) a transverse feedback may constitute an effective mitigation
  - Intrinsic Landau damping from the non-linearity of the interaction may be controlled through phase advances between IP(s) in each beam
- The impact of beam-beam interactions on amplitude detuning can be
  - Beneficial for Landau damping mainly thanks to the strong impact of head-on beam-beam interaction on the core of the beam distributions
  - Detrimental for Landau damping mainly by compensating other sources of tune spread
    - The mitigation of the loss of Landau damping with offset beams require a detail understanding of the impact of the non-linearities on the tune spread and the stability diagram (crossing / crab angle,  $\beta^*$ ,  $\varepsilon$ ,  $\sigma_s$ )