

# Highlights from NA61/SHINE: proton intermittency analysis

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**ZIMÁNYI SCHOOL'18**  
**WINTER WORKSHOP ON HEAVY ION PHYSICS**  
6 December 2018

# NA61/SHINE Experiment

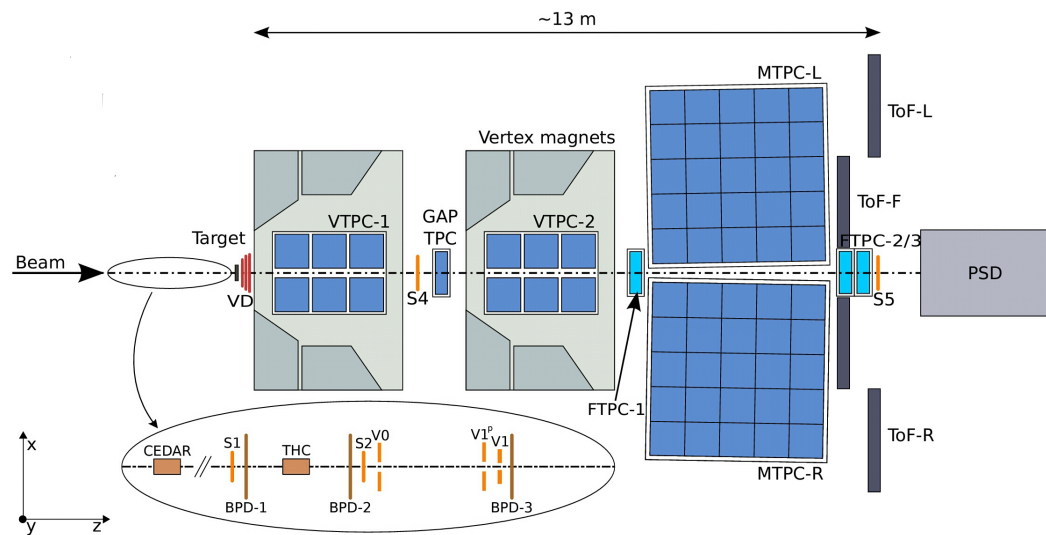


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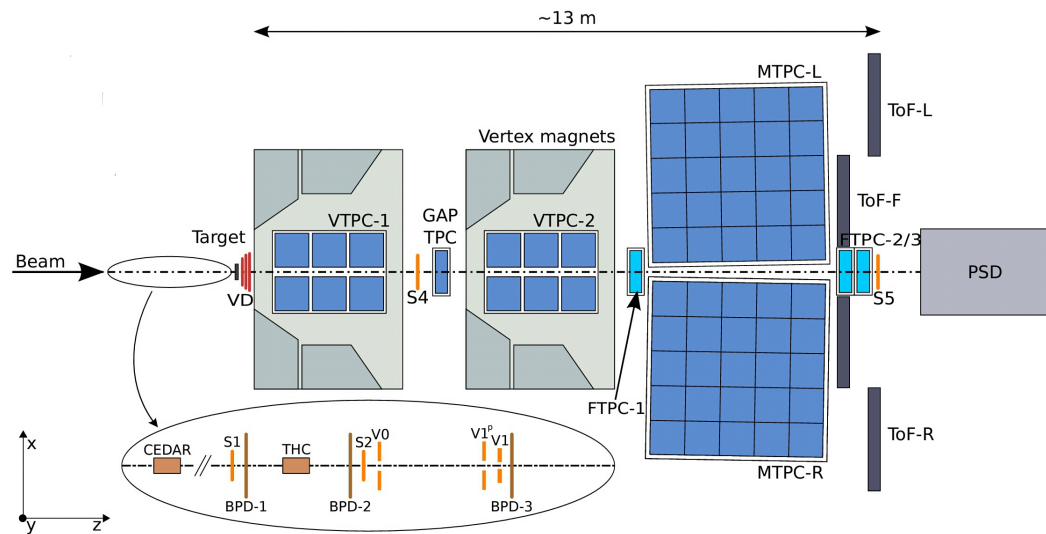


Schematic picture of the NA61/SHINE experiment NA61 INST 9: 06005

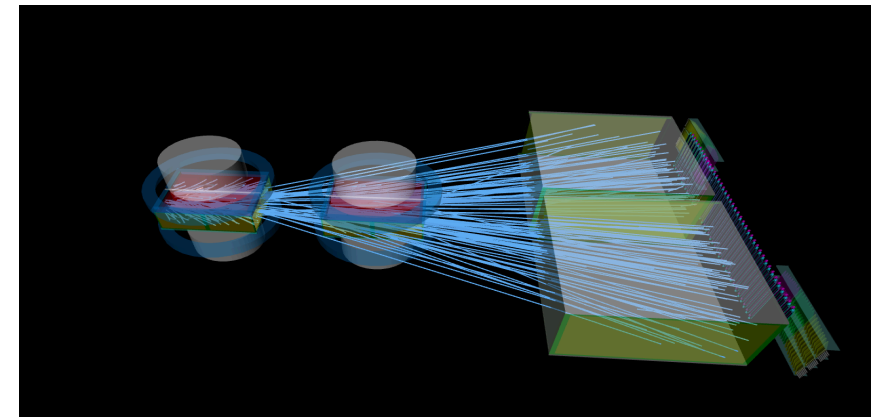
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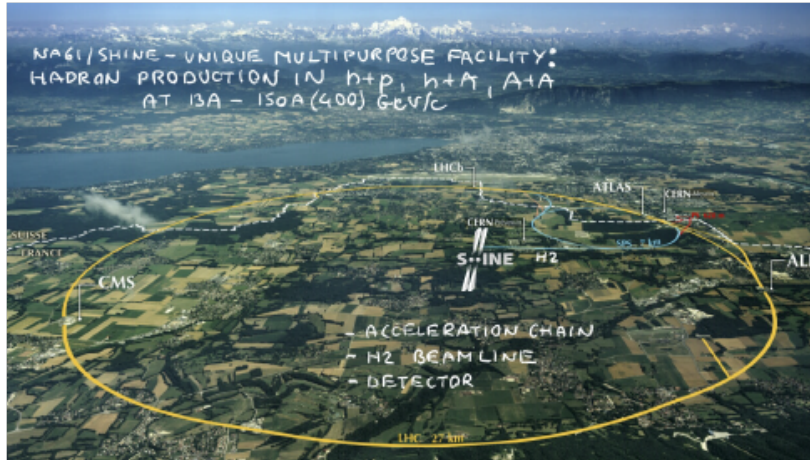
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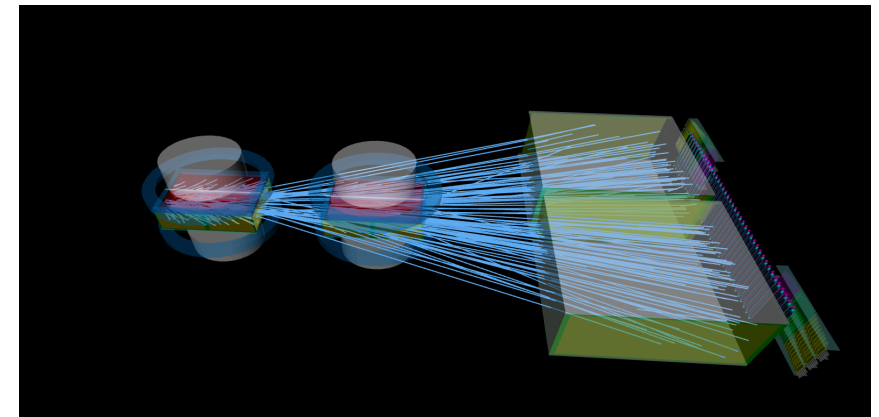
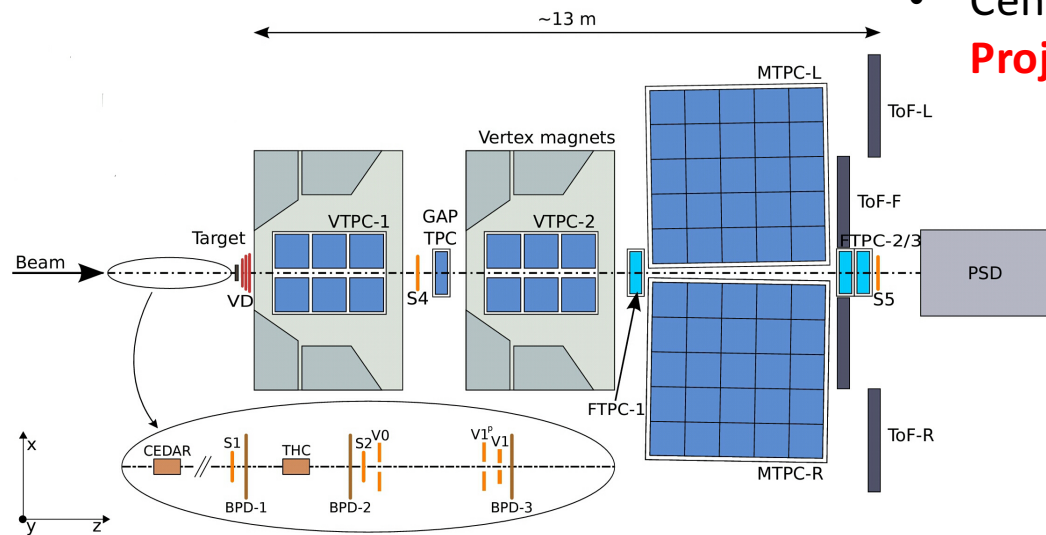
Event browser <http://shine3d.web.cern.ch/shine3d/>



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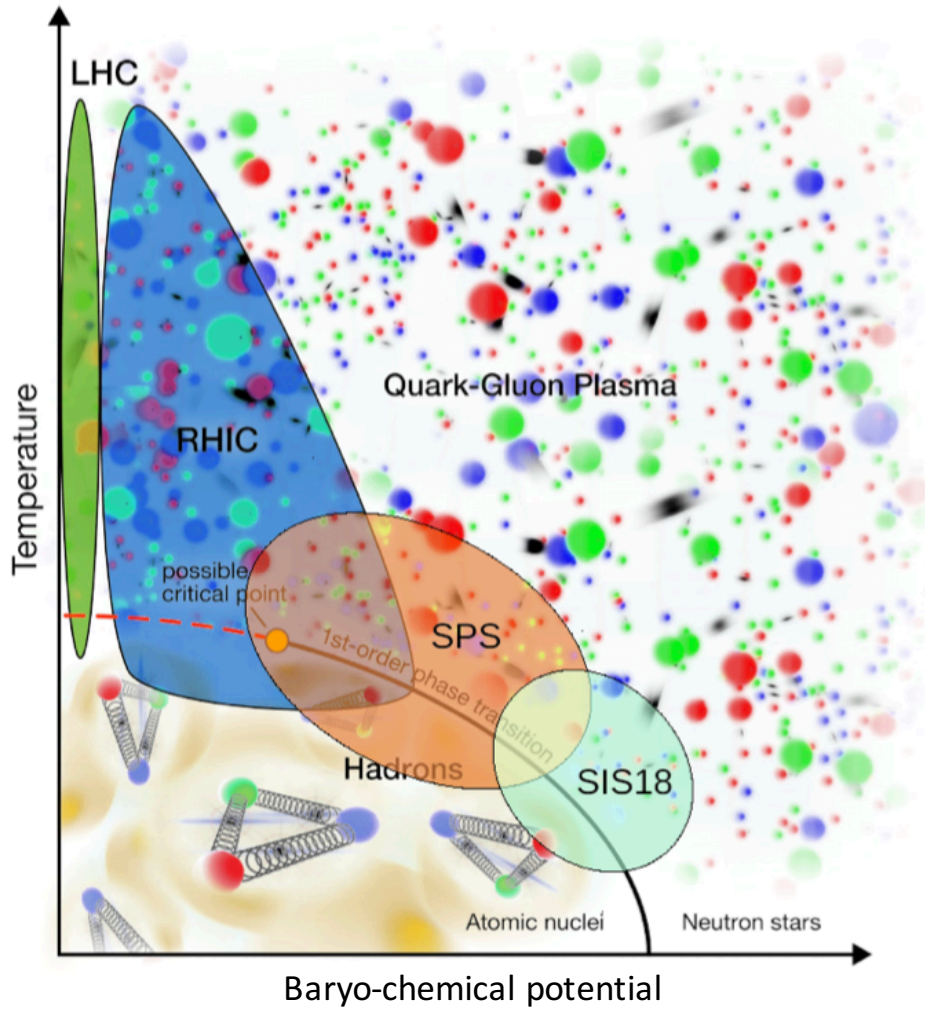
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- Centrality selection in A+A collisions by measuring of forward energy with **Projectile Spectator Detector** (PSD)



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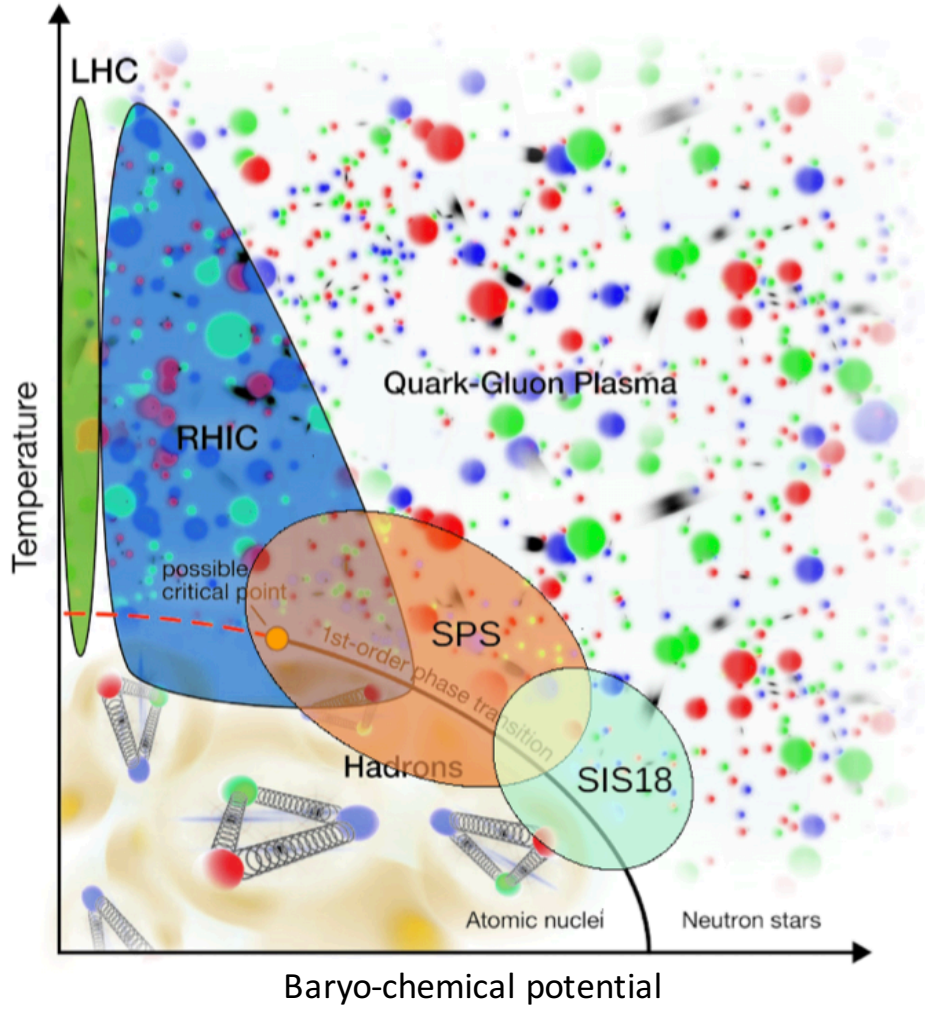
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# Strong interactions program at NA61/SHINE



Sketch of the phase diagram of strongly interacting matter

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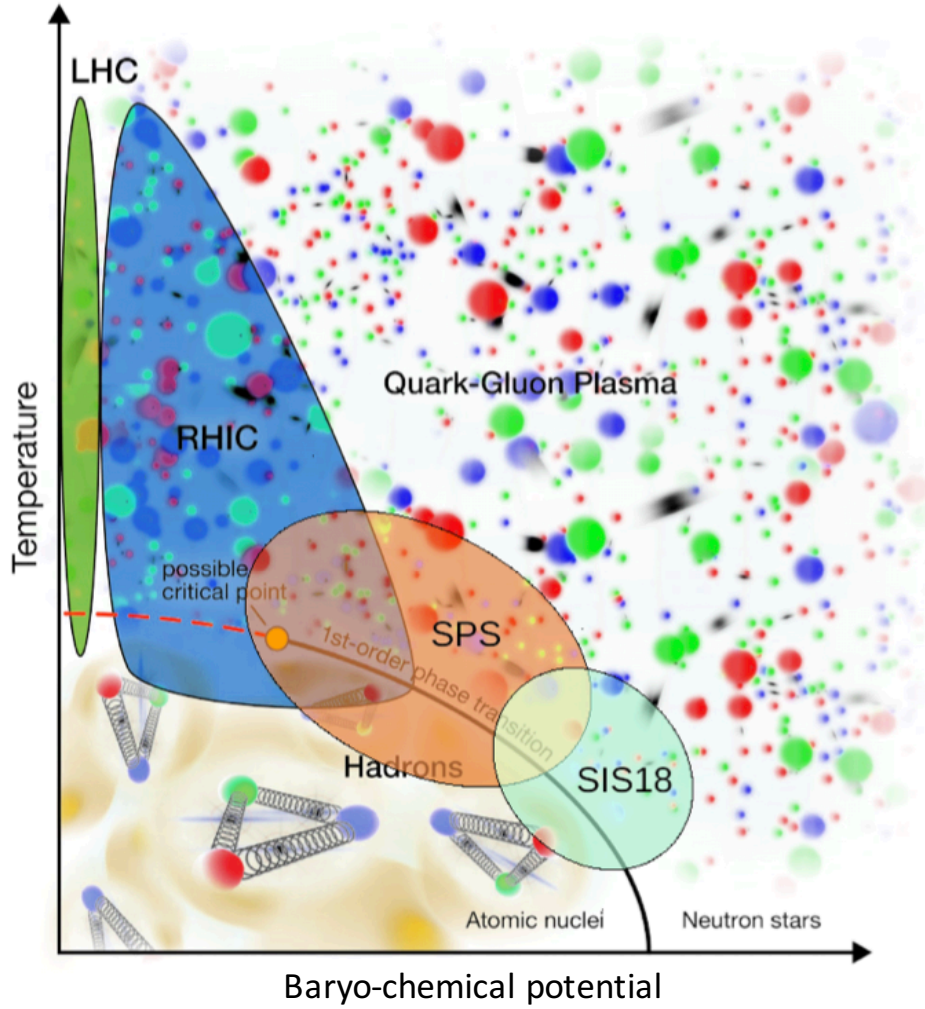


Sketch of the phase diagram of strongly interacting matter

- study the properties of the onset of deconfinement
- search for the critical point (CP) of strongly interacting matter

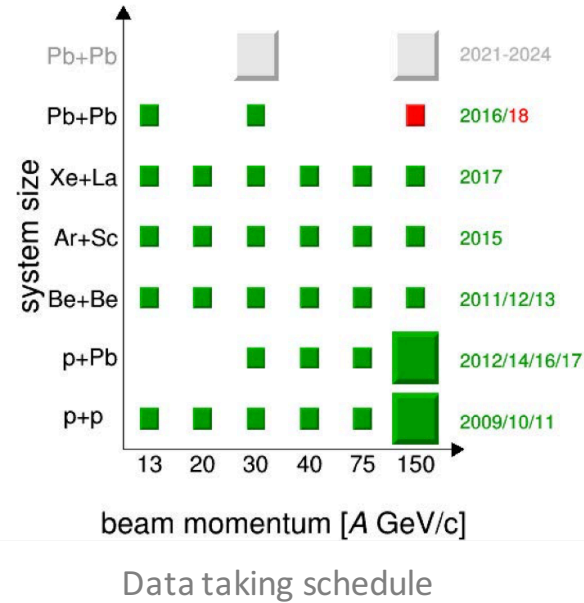


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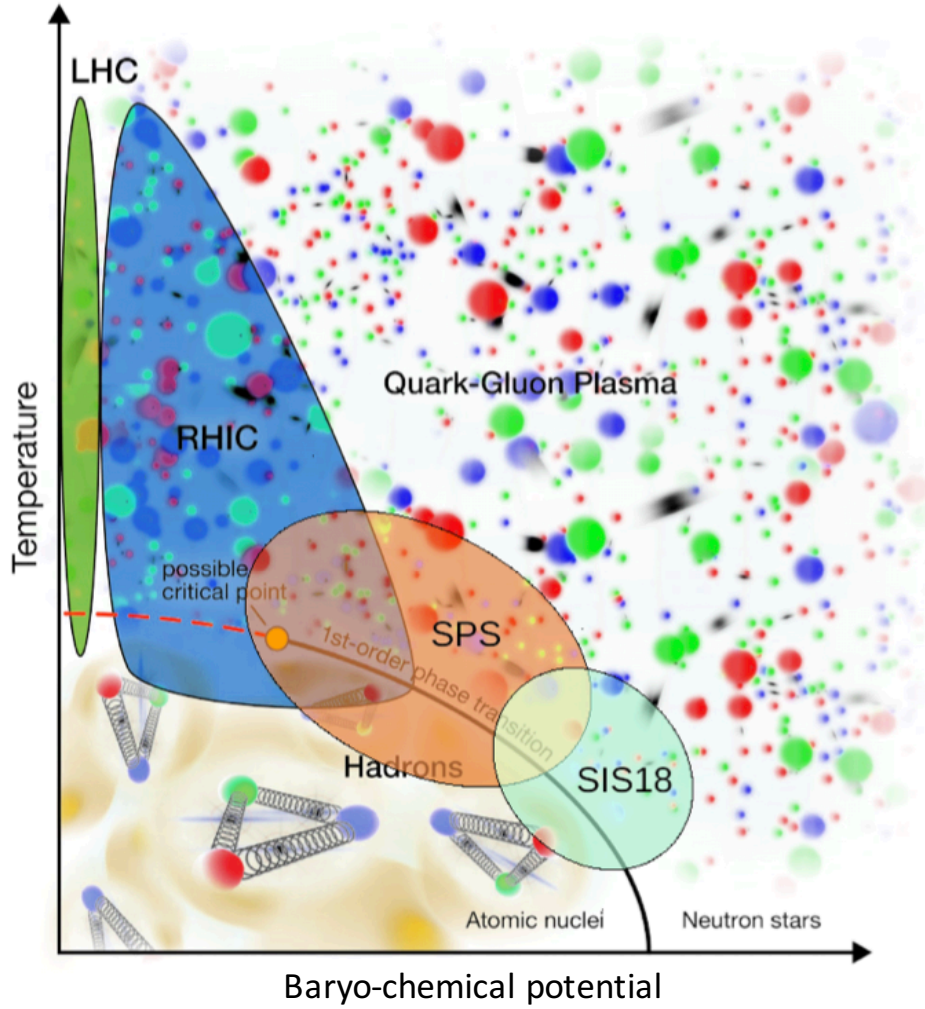
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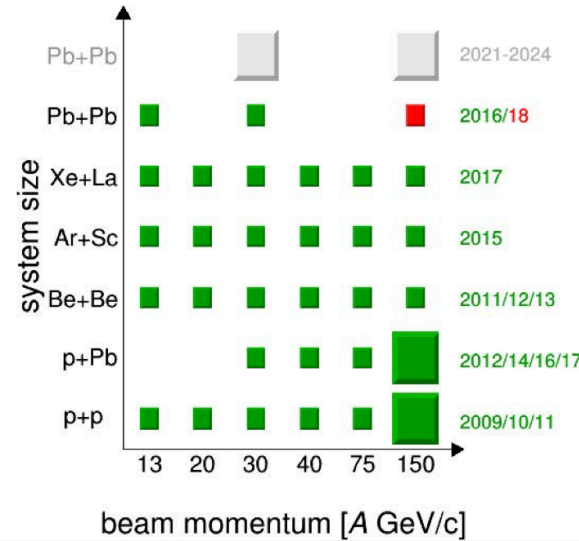


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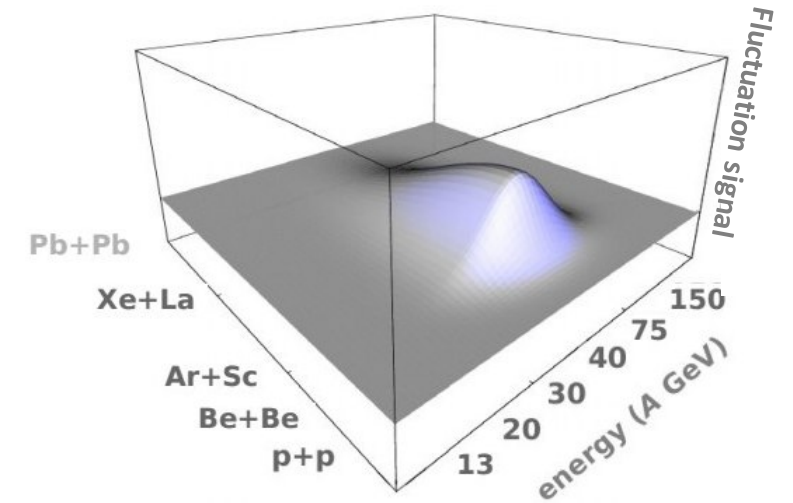


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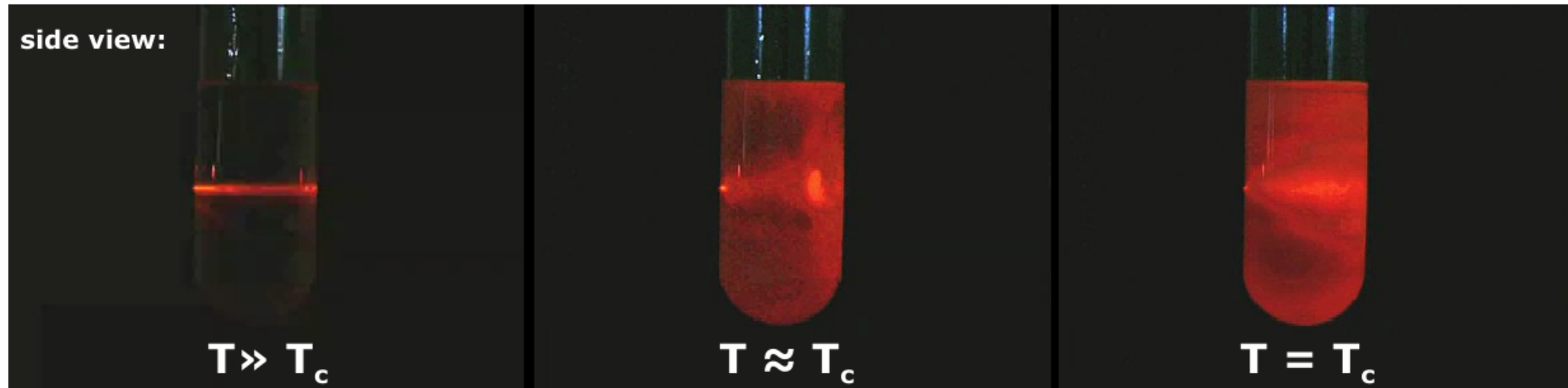
Data taking schedule



Sketch of the expected «critical hill»

# Critical behavior: back to school

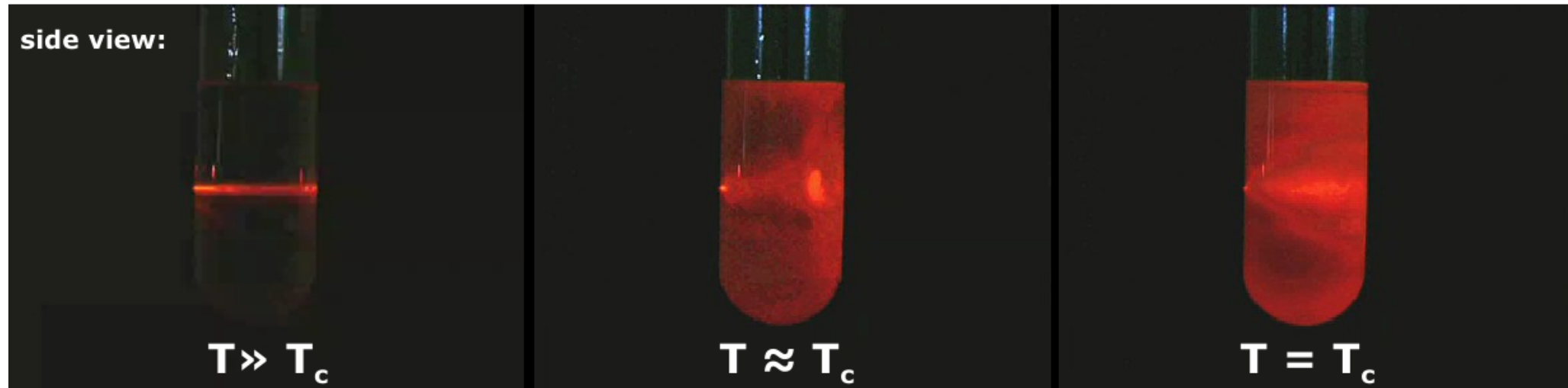
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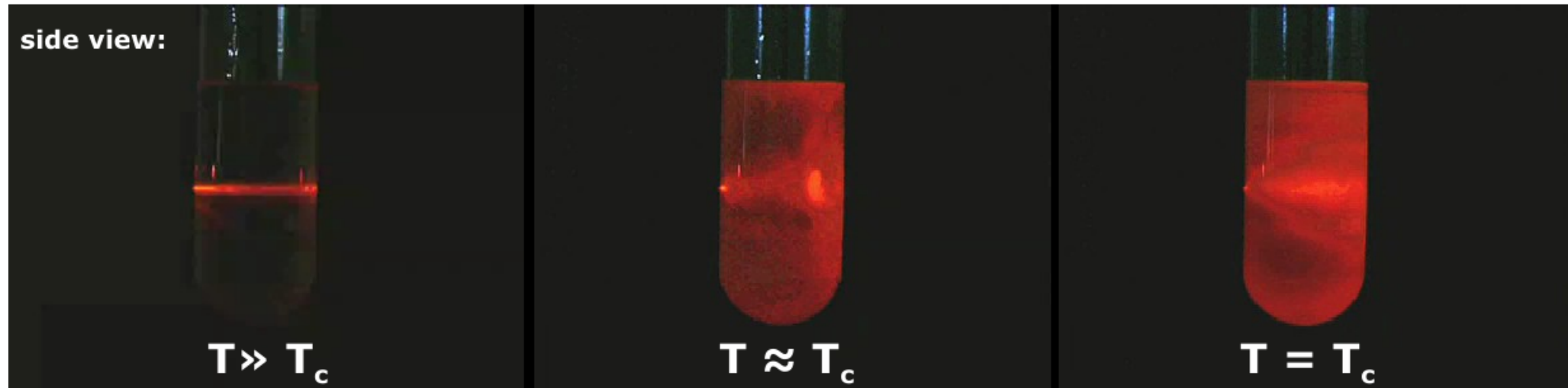


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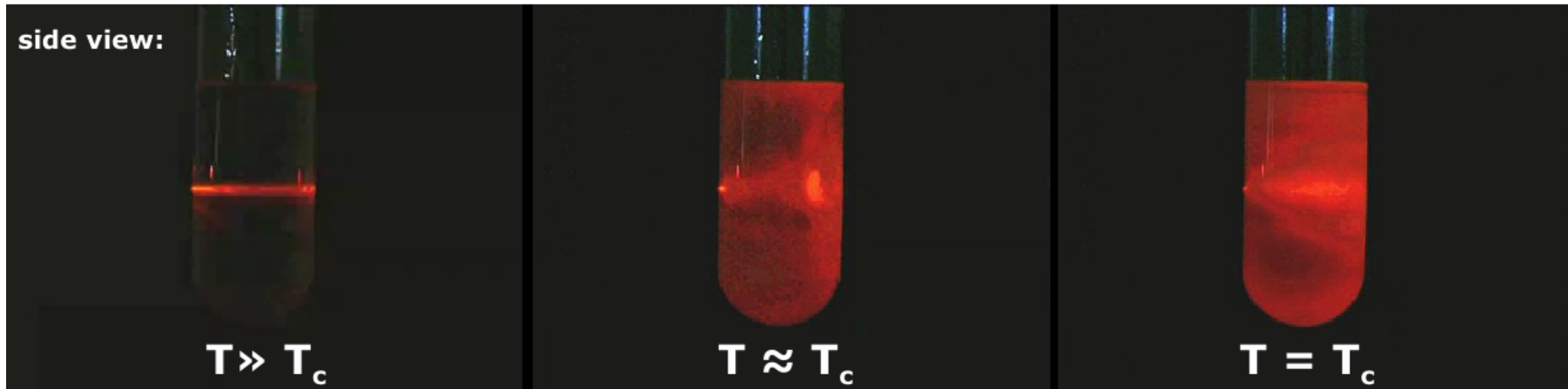
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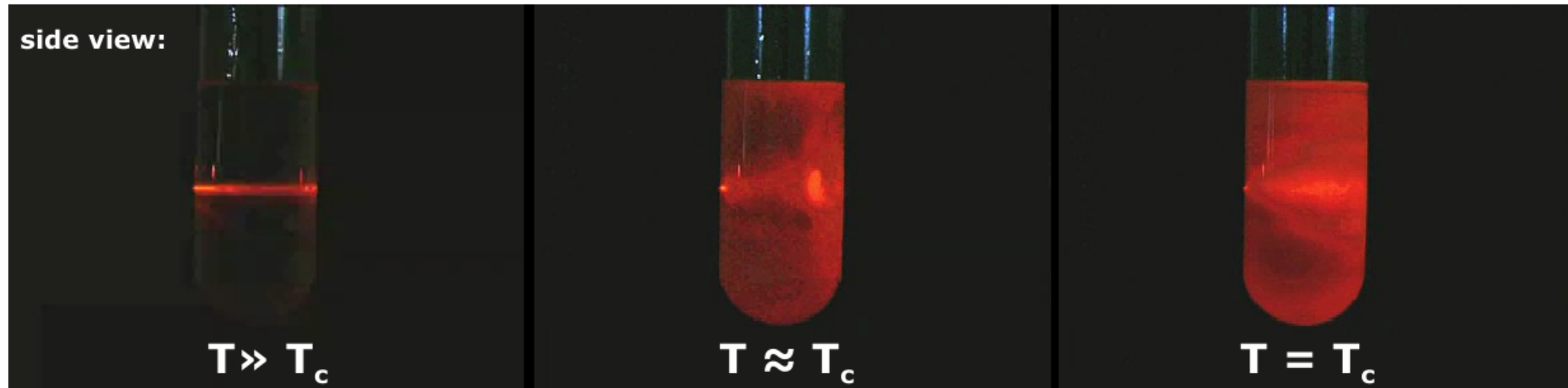


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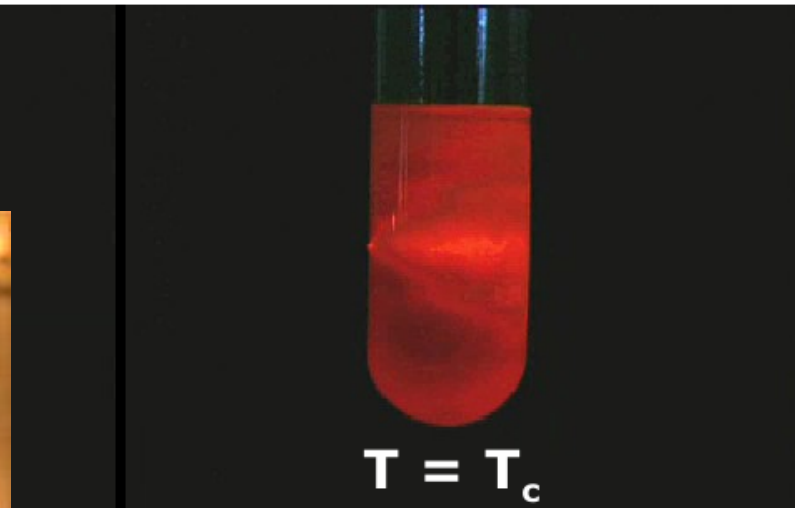
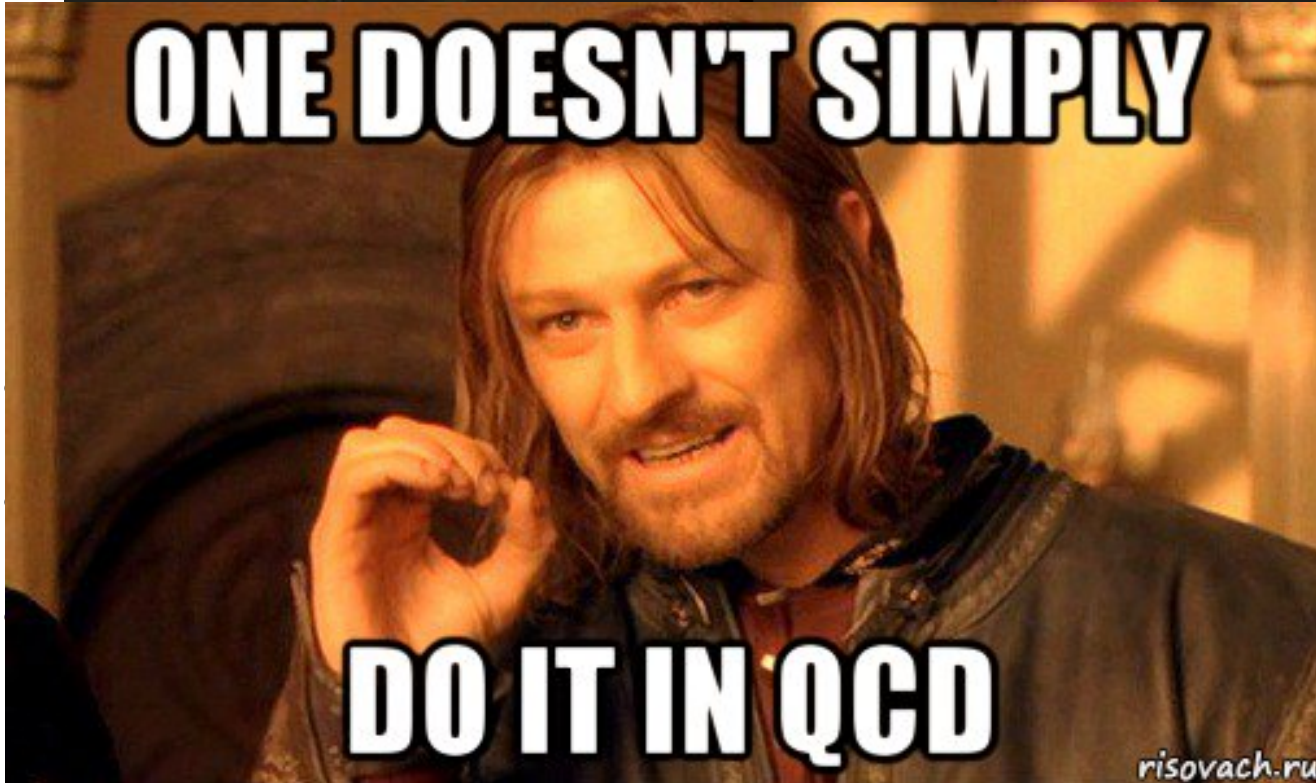
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Finally, we see a signature of a second order phase transitions and the **critical point is reached**

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side view:



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**The order parameters of QCD** are the chiral condensate and the net-baryon density. Critical fluctuations show up in fluctuations of the net-baryon density and can be observed by **intermittent behavior of the net-proton or proton density**

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**In this talk I will present:**

- theoretical aspects formulated by **Fotios Diakonov** at NA61/SHINE theory virtual meetings, can be found also at [https://indico.cern.ch/event/760216/contributions/3154442/attachments/1722303/2781998/Diakonos\\_cpod2018v2.pdf](https://indico.cern.ch/event/760216/contributions/3154442/attachments/1722303/2781998/Diakonos_cpod2018v2.pdf)
- experimental approach and results by **Nikolaos Davis** in collaboration with **Nikolaos Antoniou & Fotios Diakonov** for the NA61/SHINE collaboration based on NA61/SHINE and NA49 data with full information being available at: [https://indico.cern.ch/event/760216/contributions/3153684/attachments/1721653/2779754/Davis\\_CPOD2018.pdf](https://indico.cern.ch/event/760216/contributions/3153684/attachments/1721653/2779754/Davis_CPOD2018.pdf)

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**QCD vacuum** is chemically and thermally excited



**Momentum of produced particles** is our tool instead of scattered photons momentum in ordinary QED matter.  
**We can look at produced protons and pions**

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Our system has a finite size **L**



This introduces an additional length scale **L**, with exponent **p** describing the **scaling** of thermodynamic quantities for finite systems:

Q – any thermodynamic quantity

f – scaling function

$\xi_\infty$  - correlation length

$$Q_L(t_\pm) = L^p f_\pm(L/\xi_\infty(t_\pm)) \quad ; \quad t = \pm \frac{T - T_c}{T} \quad \text{reduced temperature}$$



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Hence, power-law  $\langle n_B(\mathbf{r}_1)n_B(\mathbf{r}_2) \rangle \sim |\mathbf{r}_1 - \mathbf{r}_2|^{-(d-d_F)}$  behavior in configuration space near the Critical Point could be observed for distances of the order of the correlation length, and therefore larger than system size **L**:  $|\mathbf{r}_1 - \mathbf{r}_2| \approx \xi_\infty \gtrsim L$  - **Finite Size Scaling (FSS) regime**

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Of course, we have a **cutoff on L in the real system** and after performing Fourier transform:

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**long-range correlations in r-space** for distances of the order of the correlation length, and therefore larger than system size **L**:  $|\mathbf{r}_1 - \mathbf{r}_2| \approx \xi_\infty \gtrsim L$  - **Finite Size Scaling (FSS) regime**

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**The power-law decay in r-space leads to power-law singularity of the density-density correlation function in p-space**

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 scattered photons momentum in order to probe the QCD vacuum.  
 We can look at produced protons and neutrons.

Our system has a finite size  $L$



This introduces an additional length scale  $L$  in addition to the correlation length  $\xi_\infty$  and the momentum  $p$  describing the scaling of thermodynamic quantities in finite systems:

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long-range correlations

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**Intermittency ~ critical opalescence in heavy ion collisions \***

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critical pions



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**Pro:** large statistics

**Contra:** large combinatorial background of non-critical pions; fluctuations might wash-out quickly due to pions being a “fast component”

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[N.G. Antoniou, N. Davis and F.K. Diakonov PRC 93, 014908 (2016)]

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will perform analysis in **transverse momentum space**

Fractal dimension in transverse plane:  $d_{F,\perp} = \frac{2}{3}d_F \approx \frac{5}{3}$  And after Fourier:  $\tilde{d}_{F,\perp} = 2 - d_{F,\perp} \approx \frac{1}{3}$

What is our **order parameter**? (density fluctuations in case of critical opalescence)

critical pions



**Sigma-field**

or

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[Y. Hatta and M. A. Stephanov, PRL91, 102003 (2003)]

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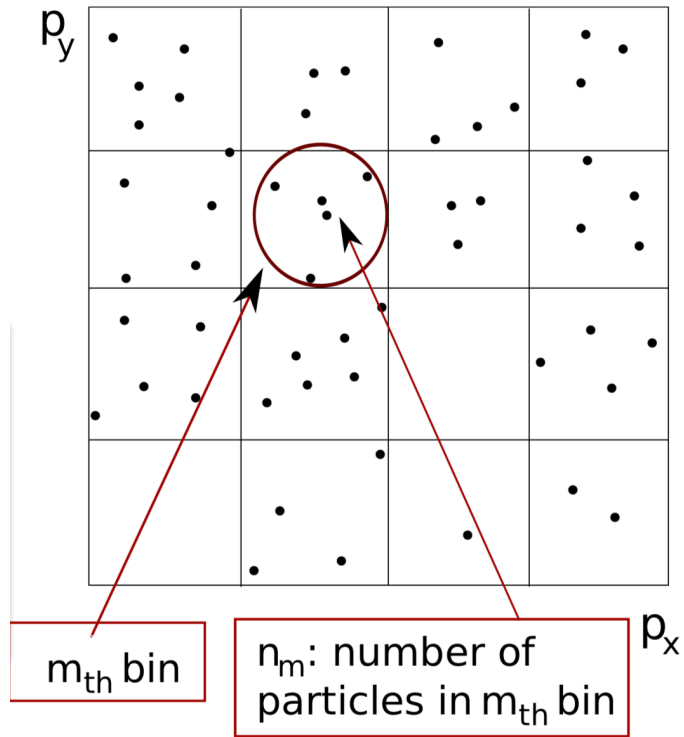
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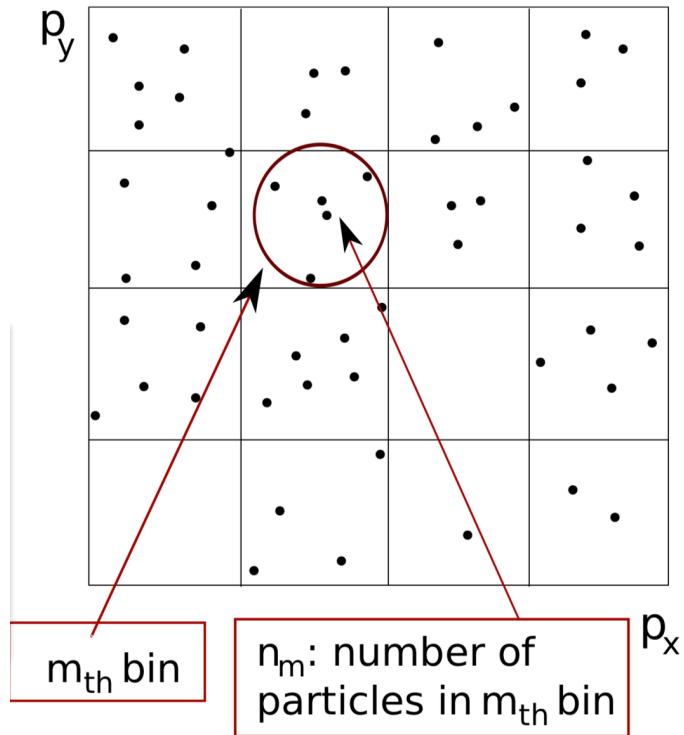
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# Intermittency analysis: factorial moments



Experimental observation of local, **power-law** distributed fluctuations

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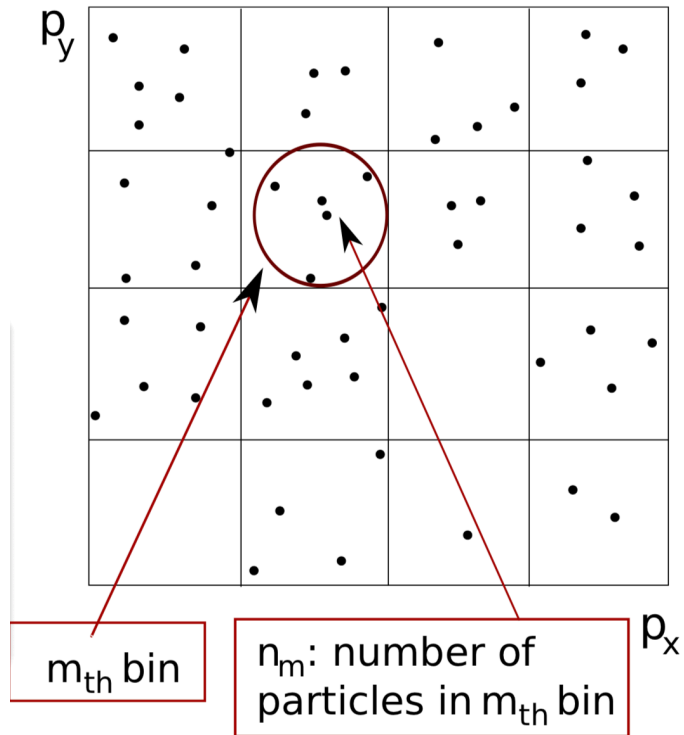
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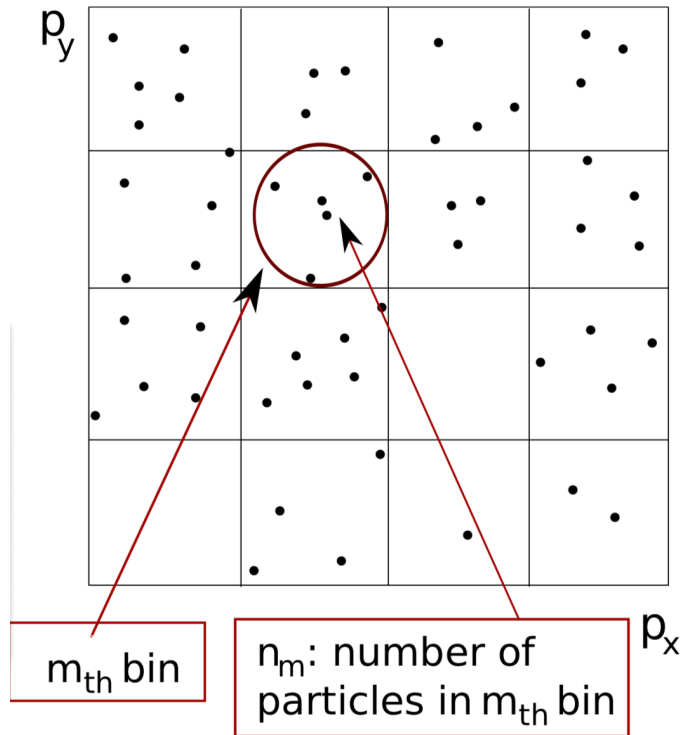
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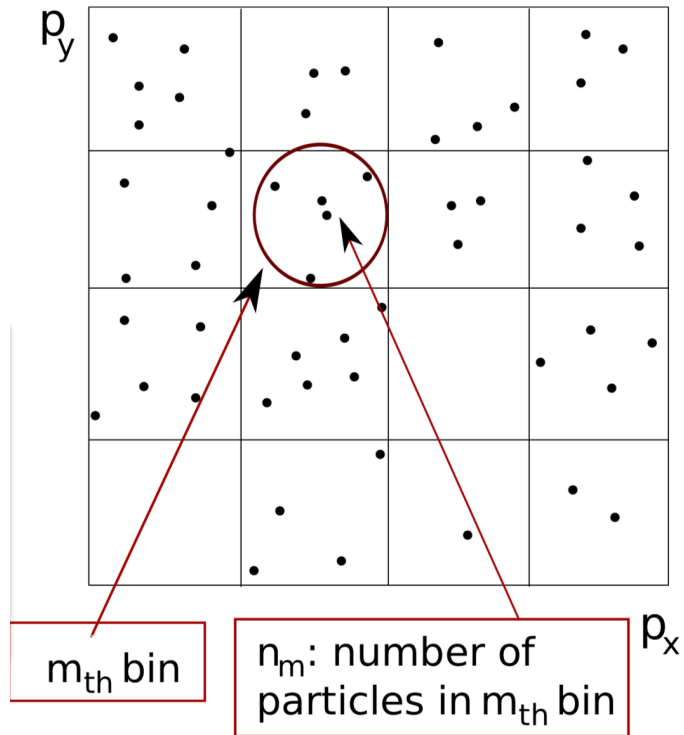
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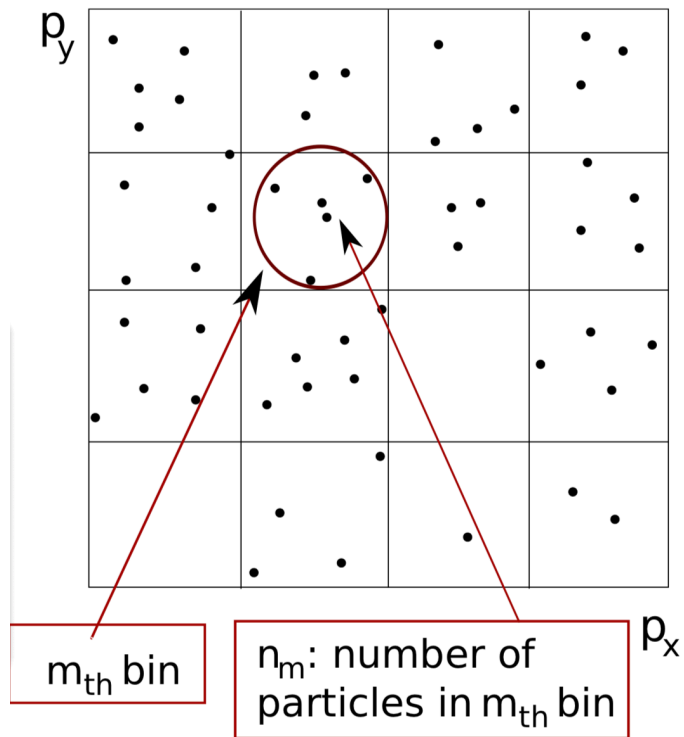
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- Calculate second factorial moments  $F_2(M)$  as a function of cell size  $\Leftrightarrow$  number of cells  $M$

$$F_2(M) \equiv \frac{\left\langle \frac{1}{M^2} \sum_{i=1}^{M^2} n_i (n_i - 1) \right\rangle}{\left\langle \frac{1}{M^2} \sum_{i=1}^{M^2} n_i \right\rangle^2}$$

[N. Davis, CPOD 2018 talk] 8/15

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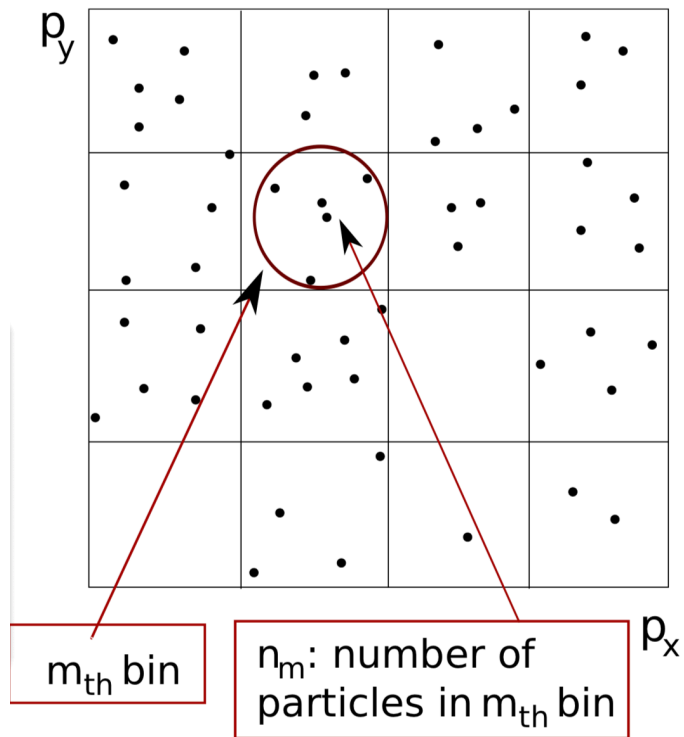


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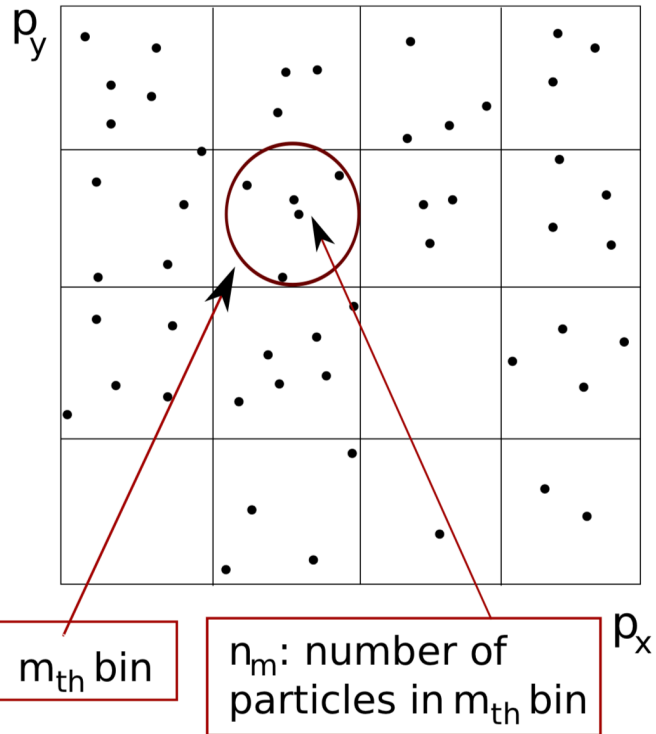
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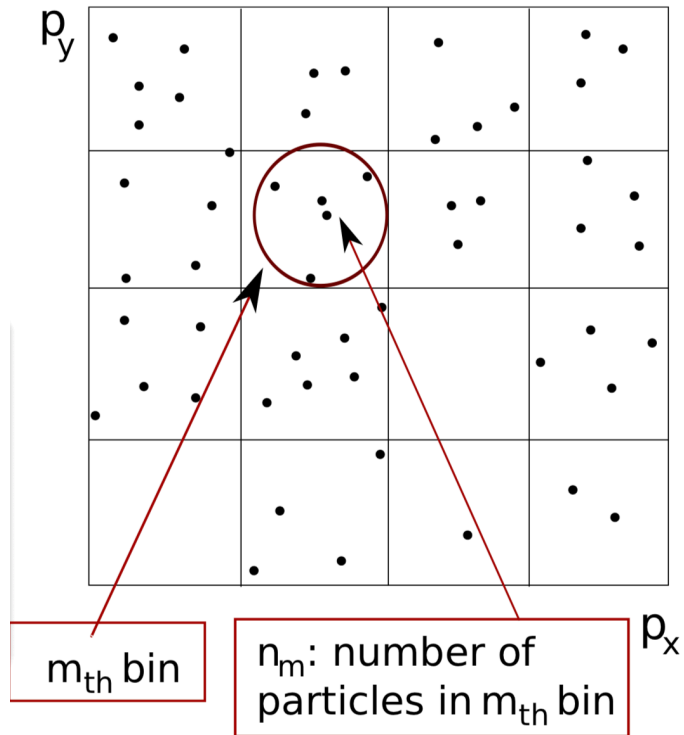
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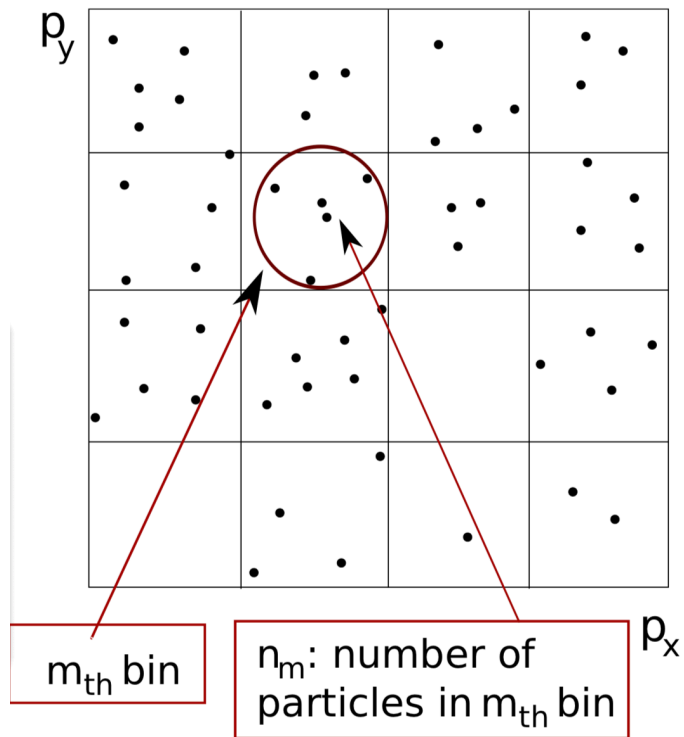
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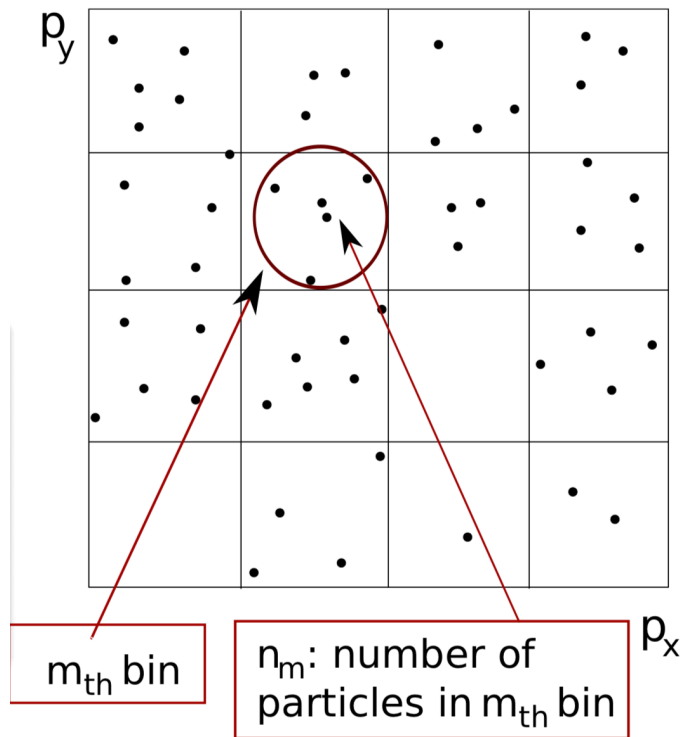
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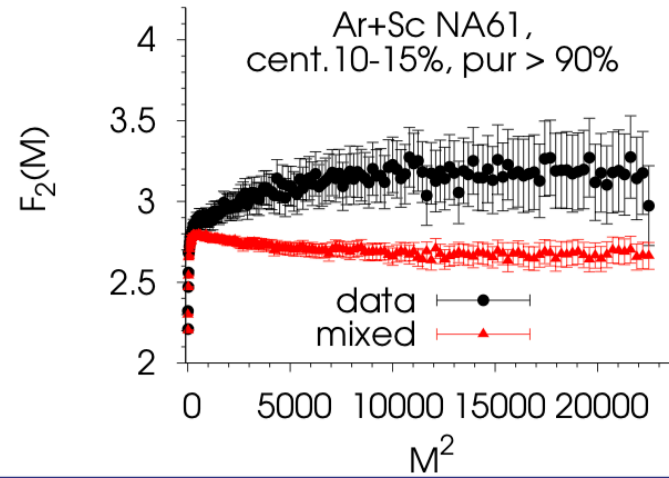
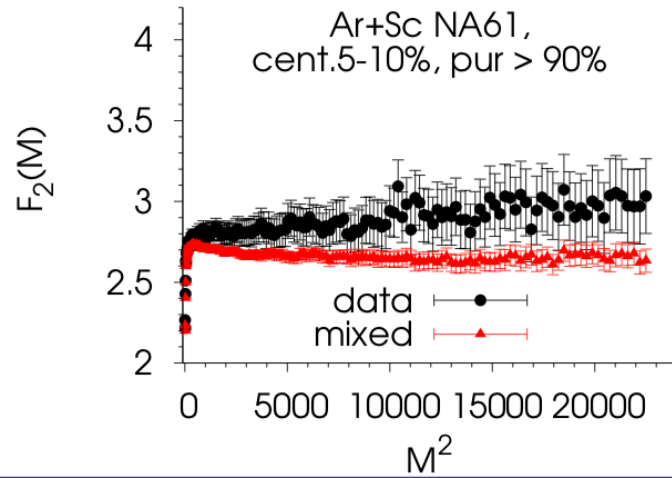
← **3d-Ising effective action**  
9/15

# Intermittency analysis results: Ar+Sc at 150A GeV/c

Centrality 5-10%

NA61/SHINE preliminary results

Centrality 10-15%



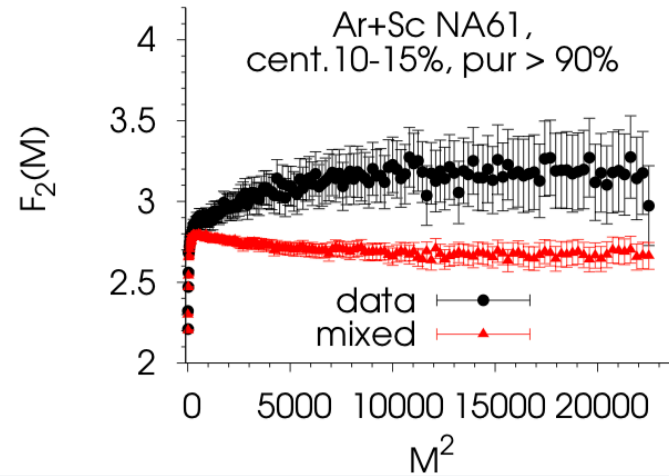
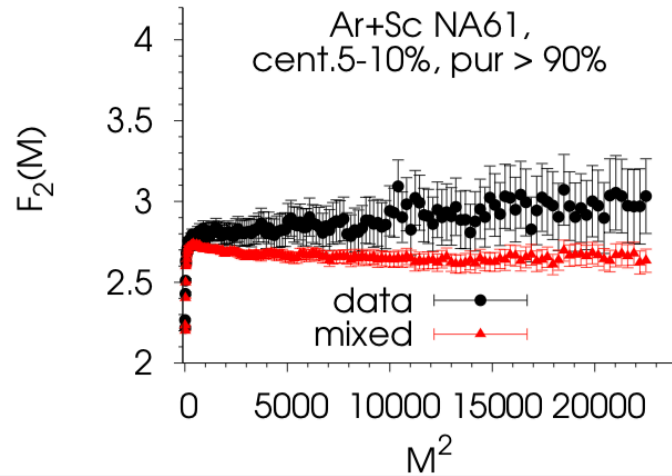
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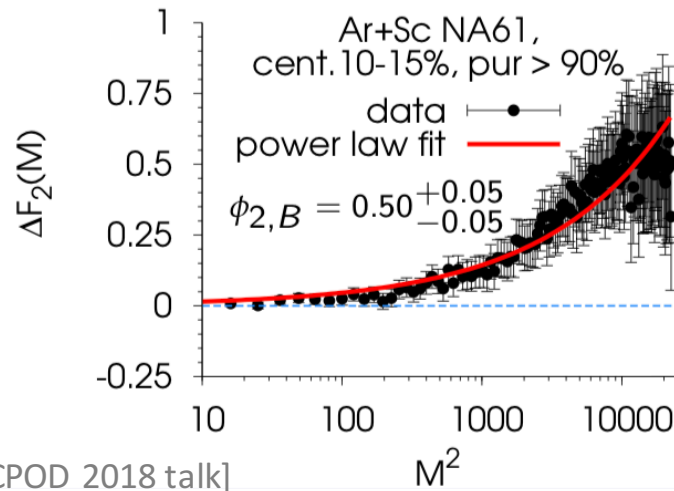
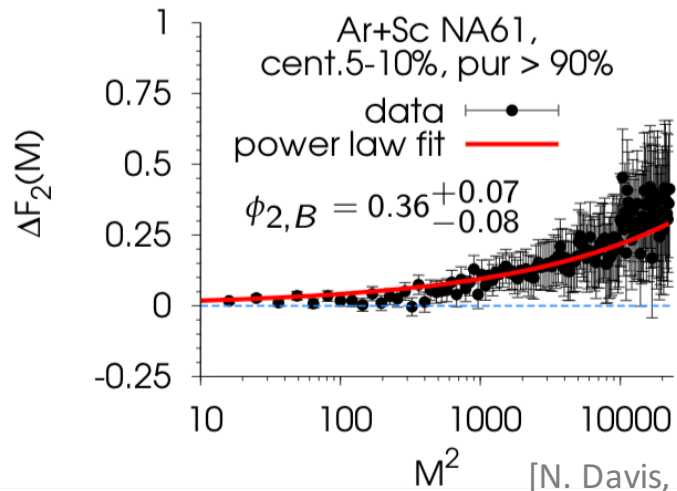
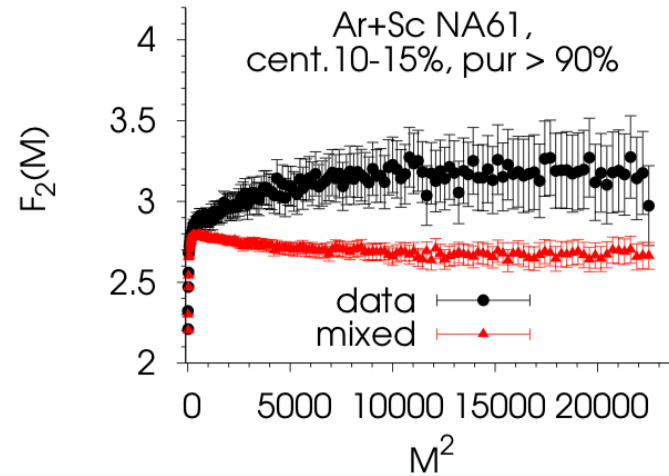
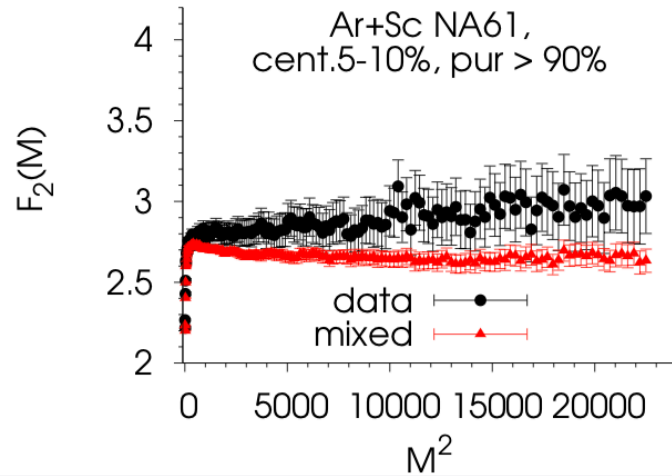
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Bootstrap calculation of  $\phi_2$  confidence intervals

10/15

Daria Prokhorova for NA61/SHINE Collaboration

3-7 December 2018, Zimanyi School, Budapest

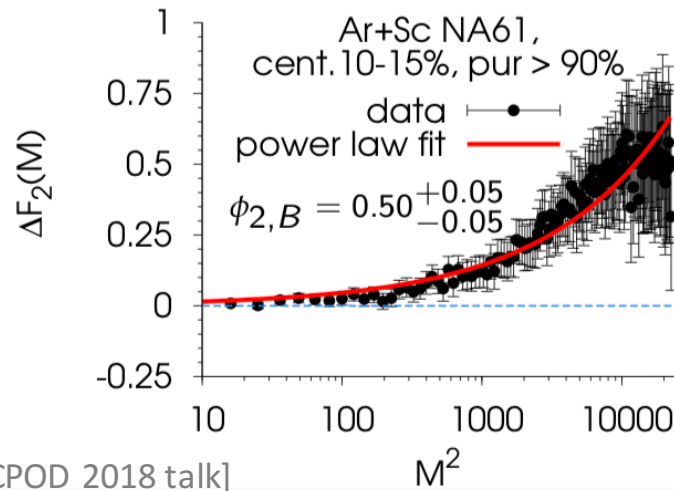
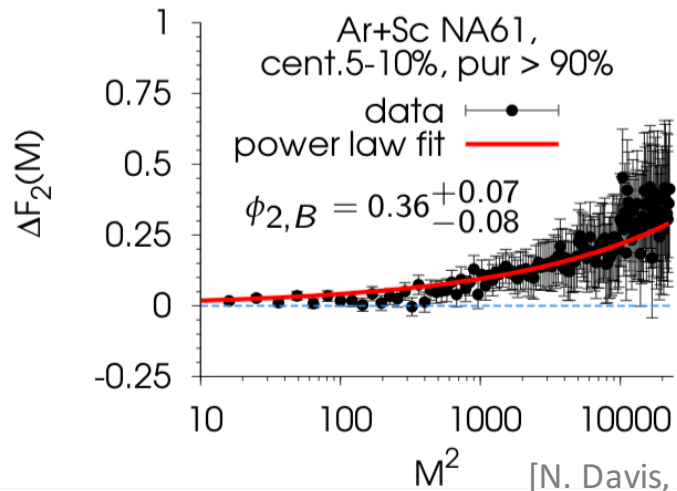
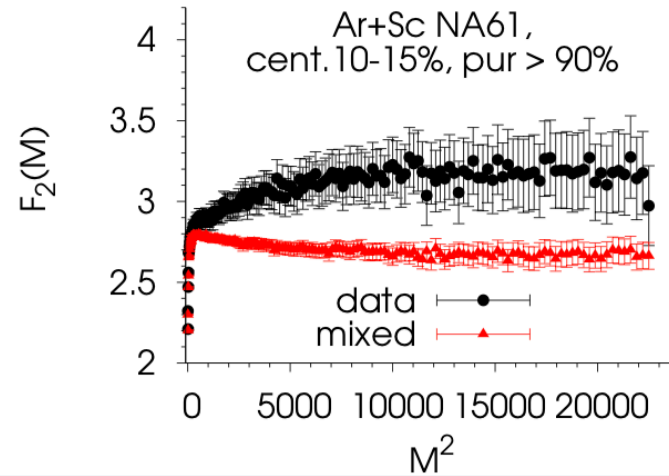
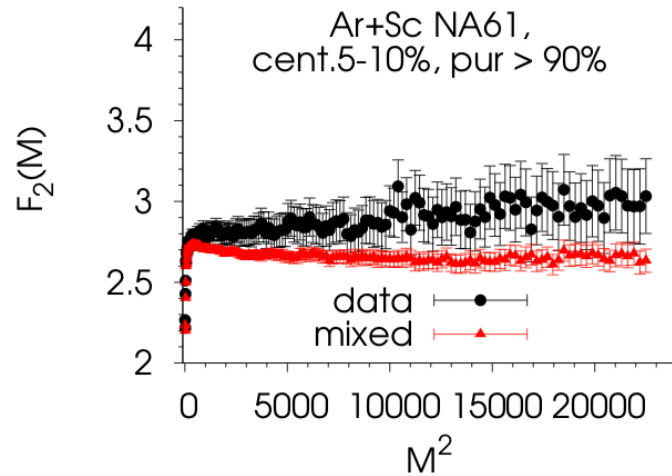
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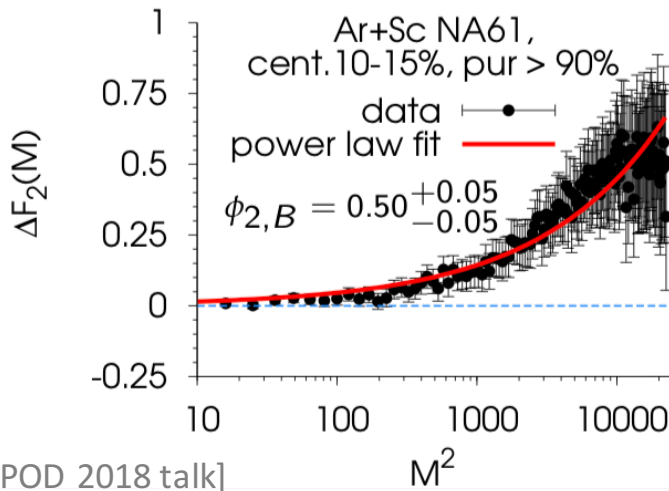
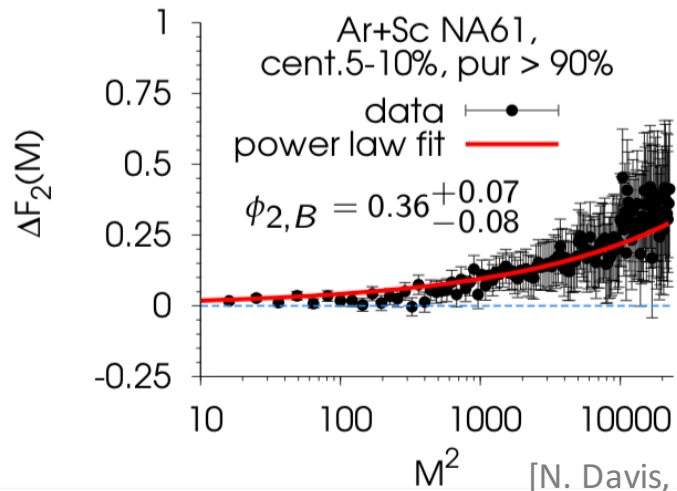
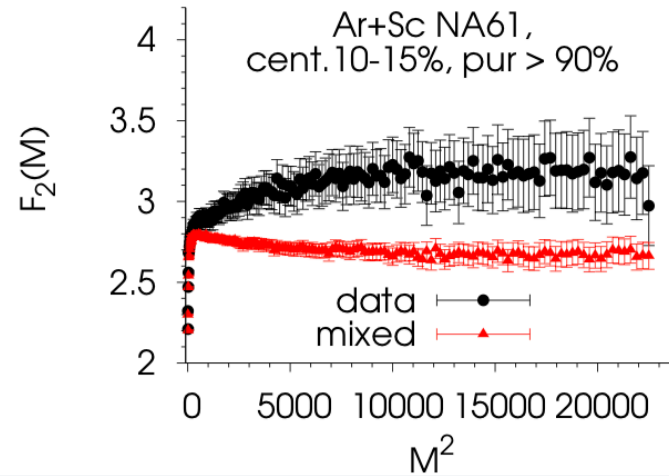
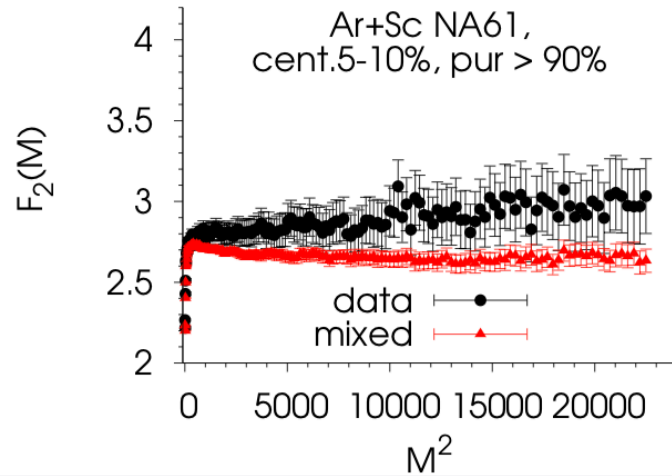
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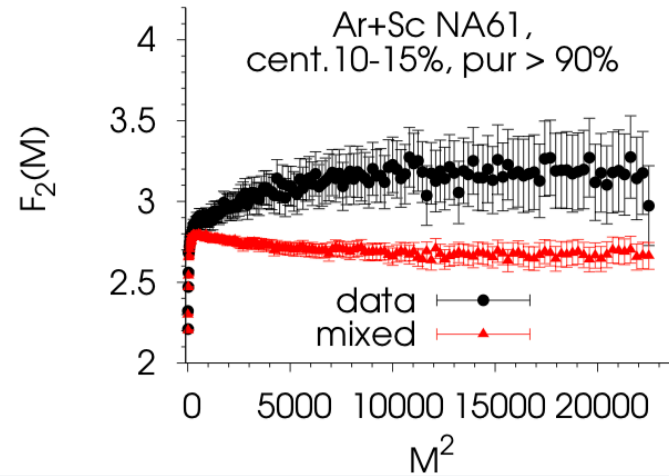
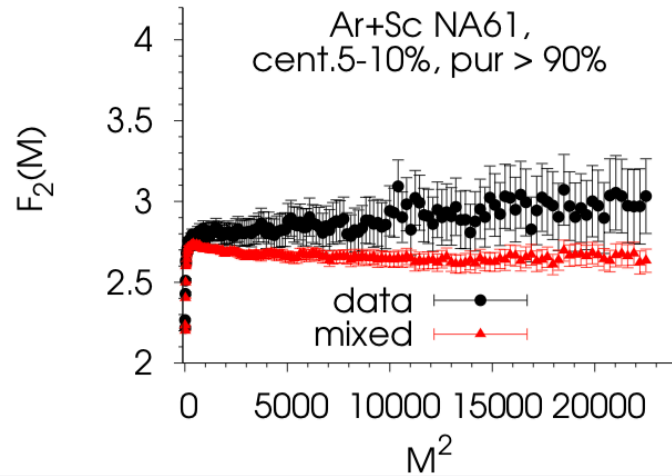
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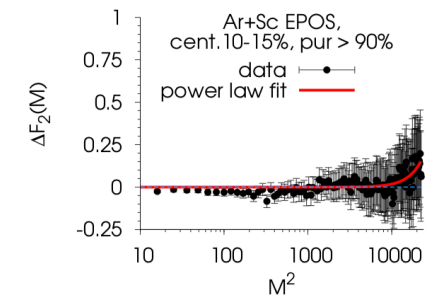
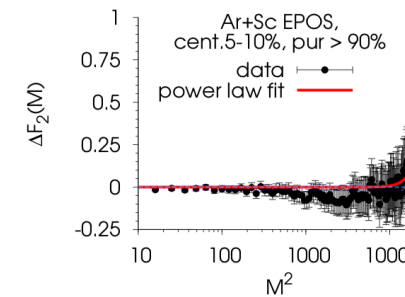
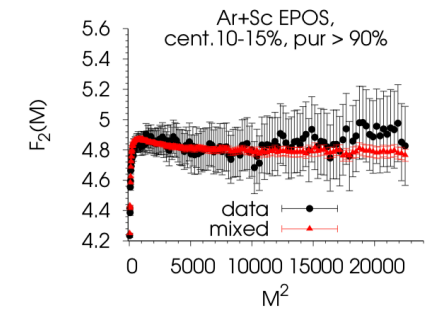
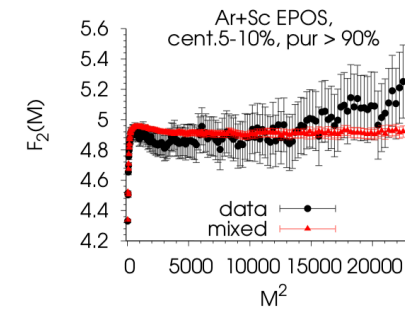
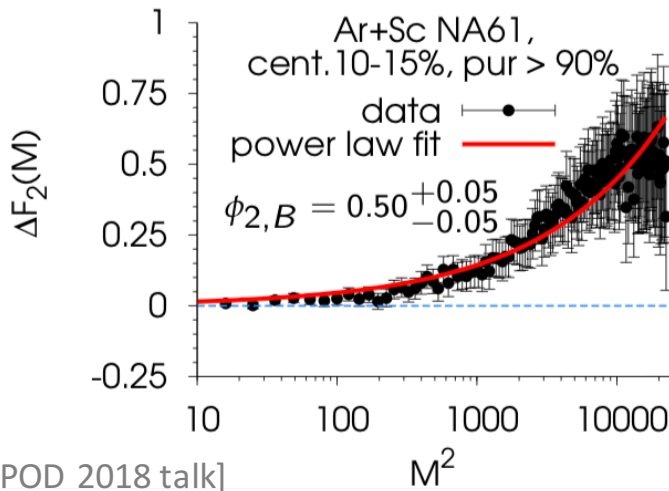
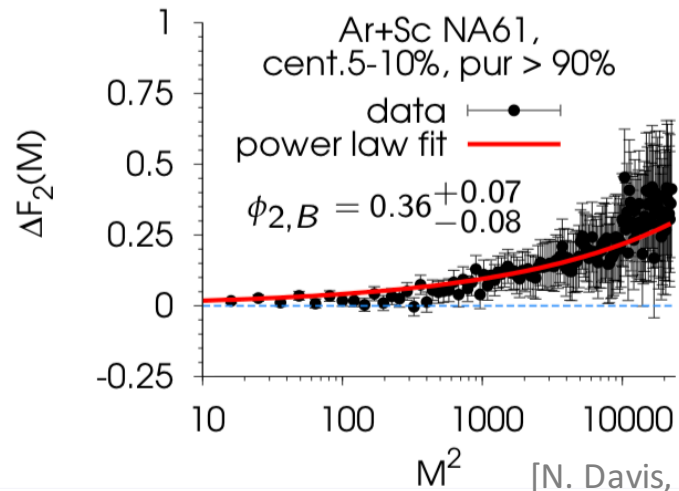
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EPOS simulations



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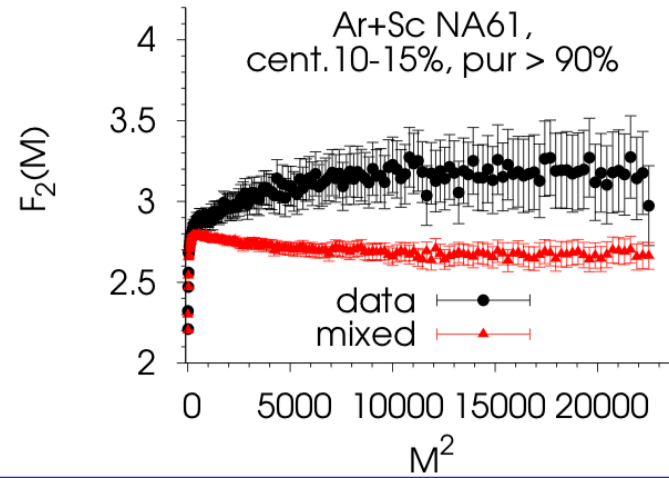
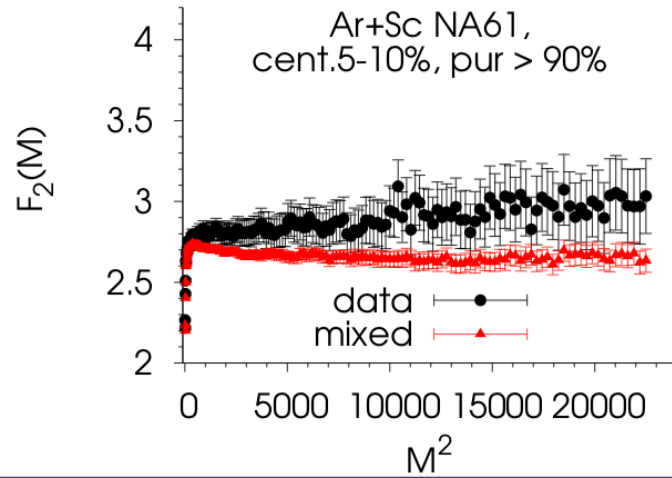
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NA61/SHINE preliminary results

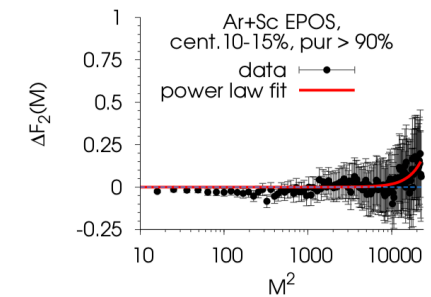
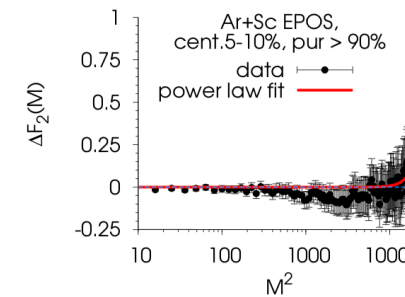
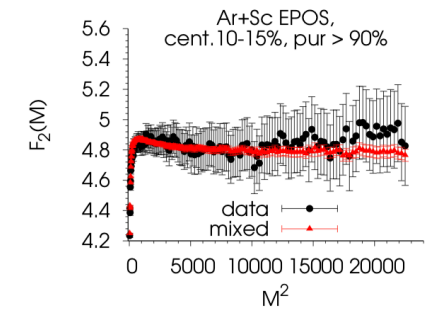
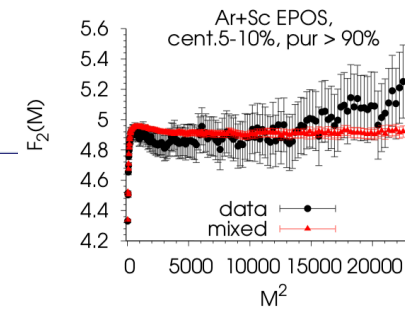
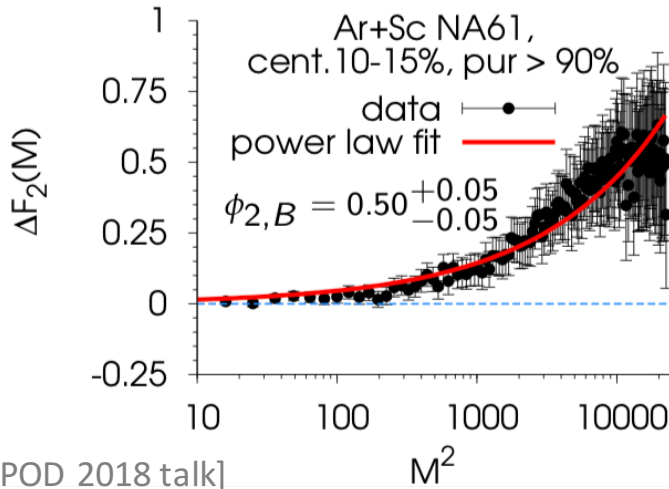
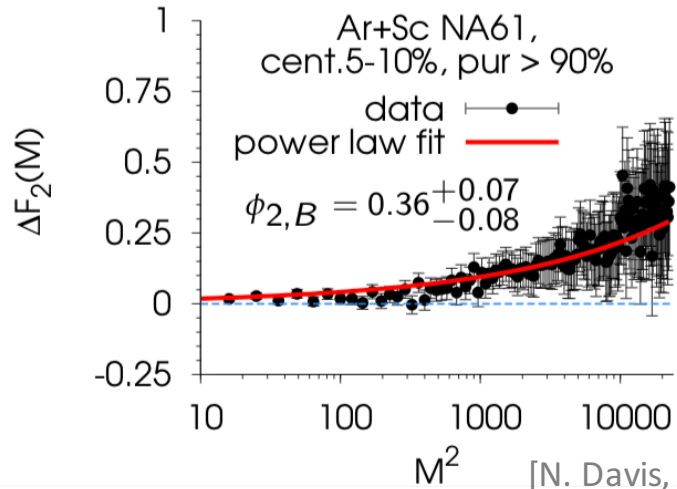
Centrality 10-15%

Result depends on the centrality of the collision, which is likely due to the change of baryo-chemical potential and the small region of criticality in the phase diagram [N. G. Antoniou, F. K. Diakonov, X. N. Maintas and C. E. Tsagkarakis, Phys. Rev. D 97, 034015 (2018)]



EPOS simulations

EPOS does not reproduce observed effect



Centrality 5-10%

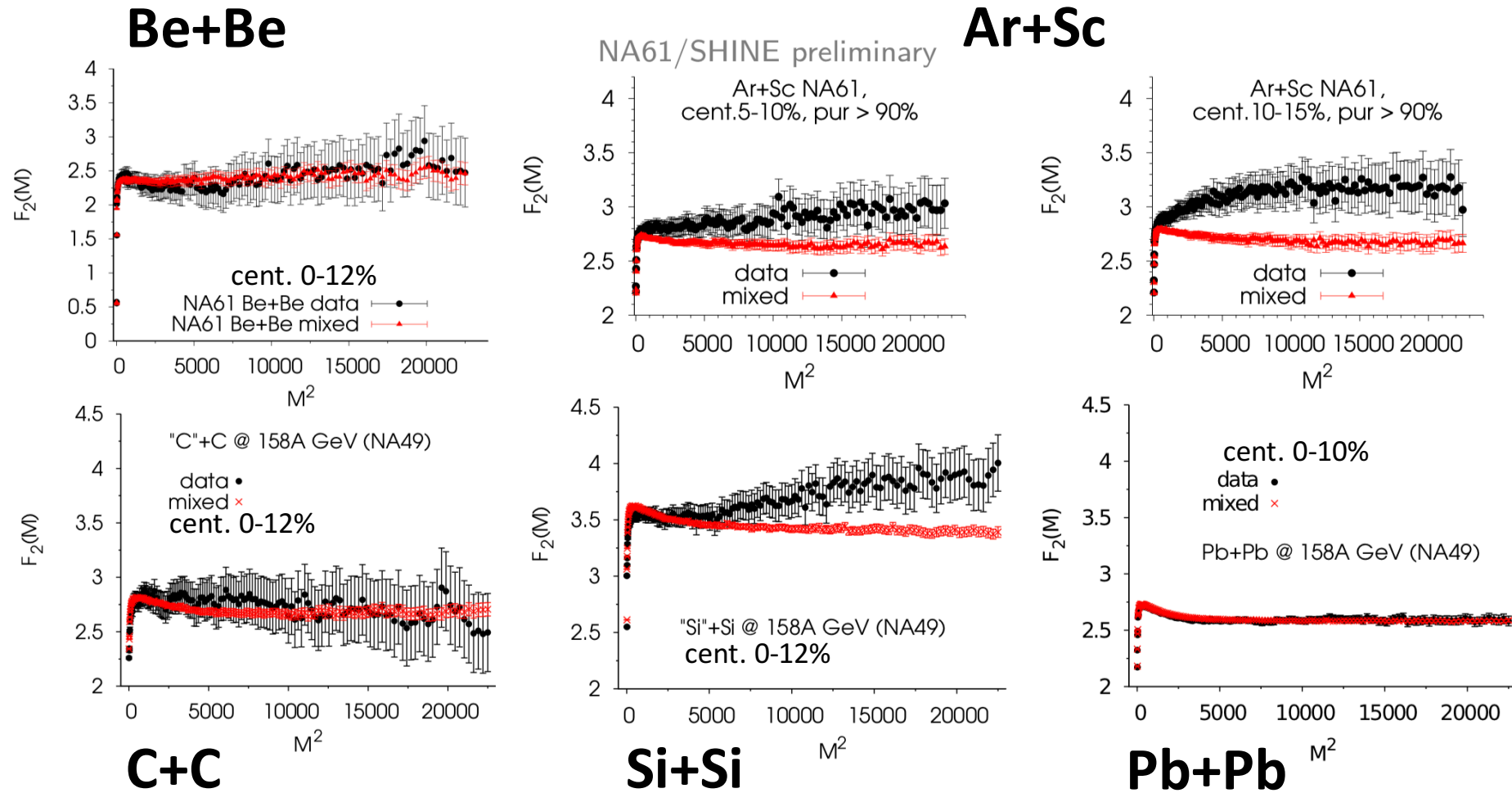
Centrality 10-15%<sub>10/15</sub>

Bootstrap calculation of  $\phi_2$  confidence intervals

Daria Prokhorova for NA61/SHINE Collaboration

3-7 December 2018, Zimanyi School, Budapest

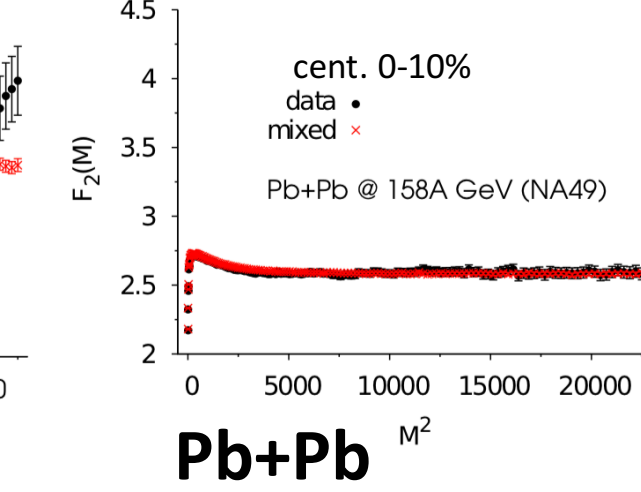
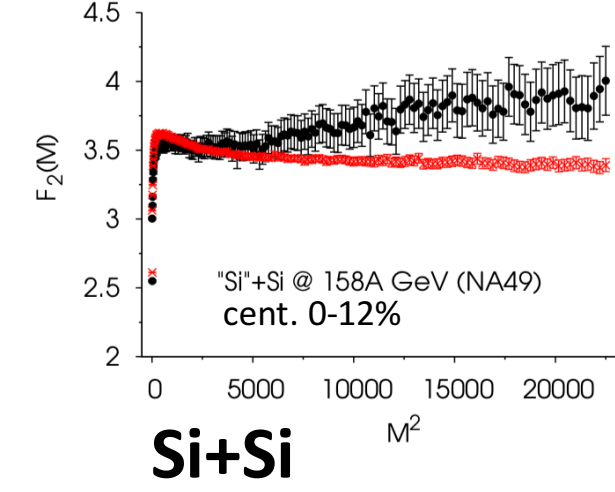
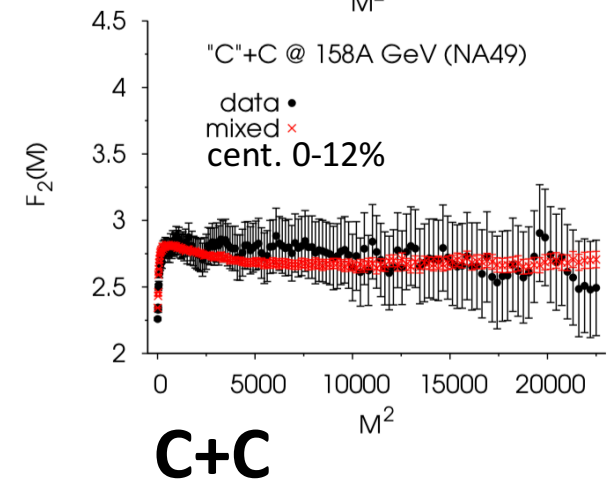
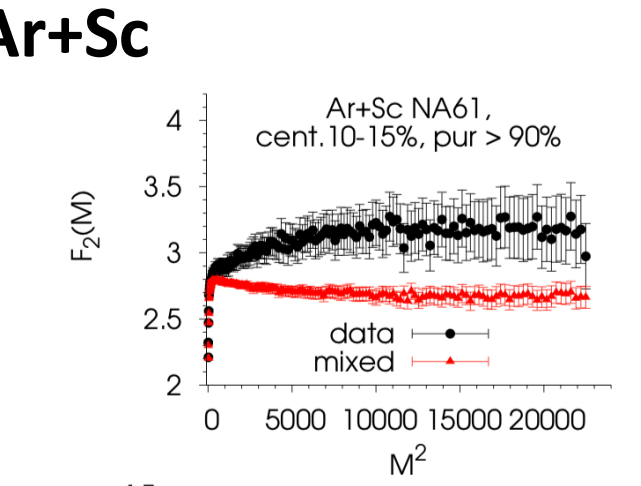
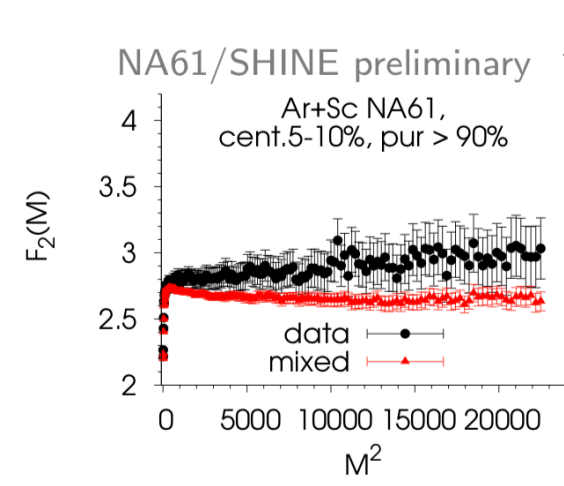
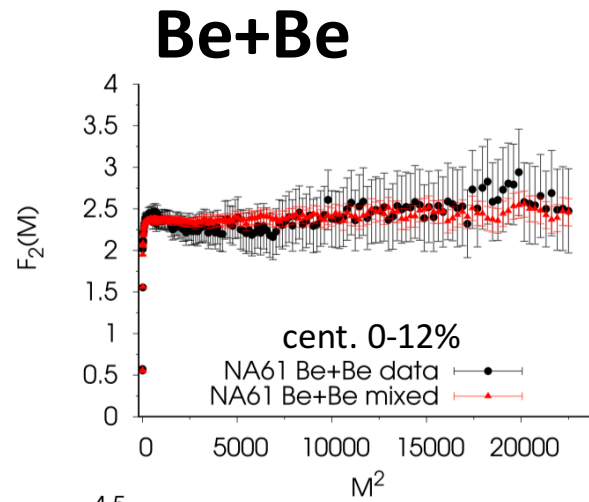
# Intermittency analysis: summary NA49 and NA61/SHINE



[N. Davis, CPOD 2018 talk]

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**NA61/SHINE**  
[Preliminary]



[N. Davis, CPOD 2018 talk]

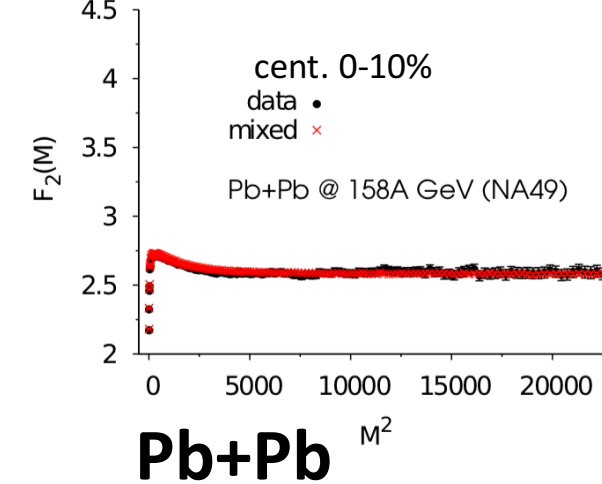
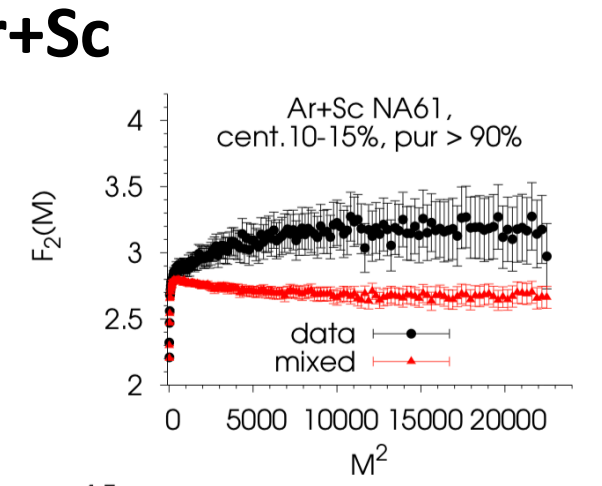
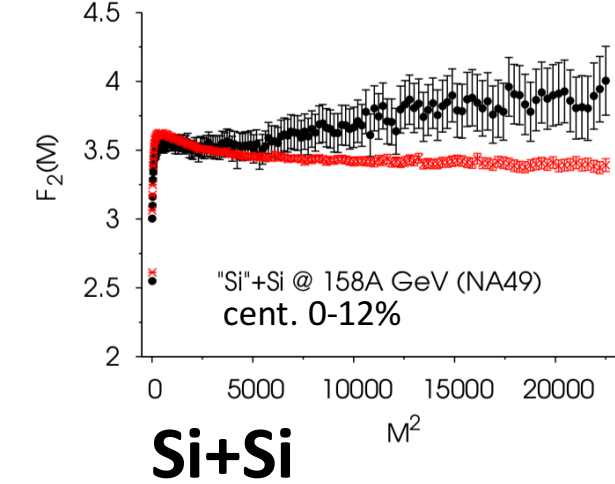
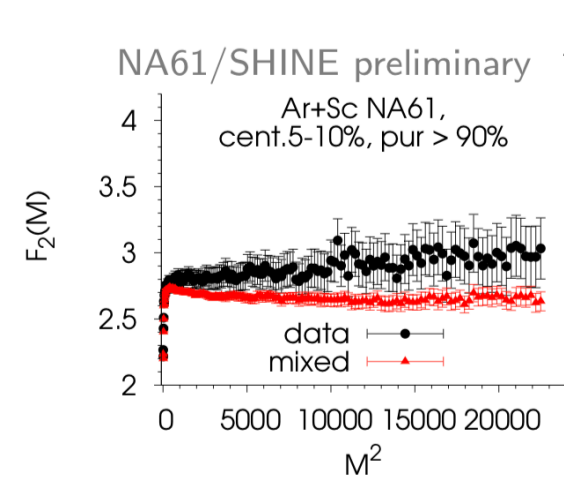
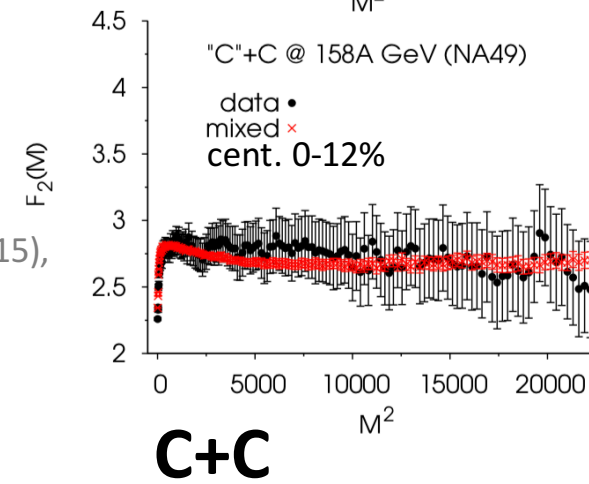
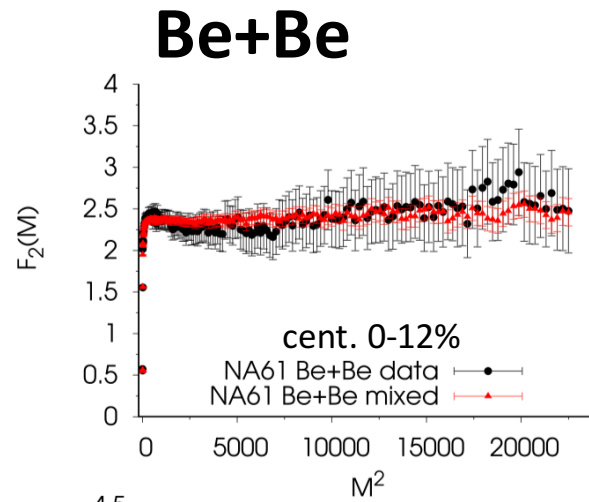
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[Preliminary]

**NA49**

[T. Anticic et al., Eur. Phys. J. C 75:587 (2015), arXiv:1208.5292v5]



[N. Davis, CPOD 2018 talk]



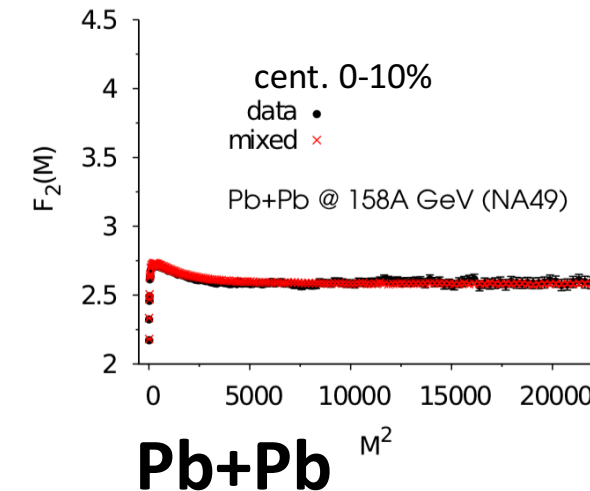
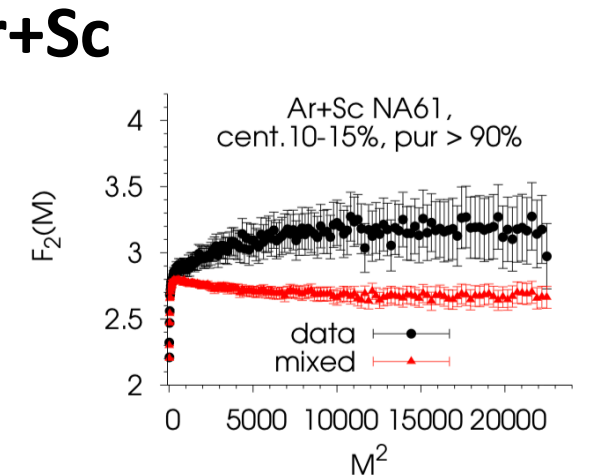
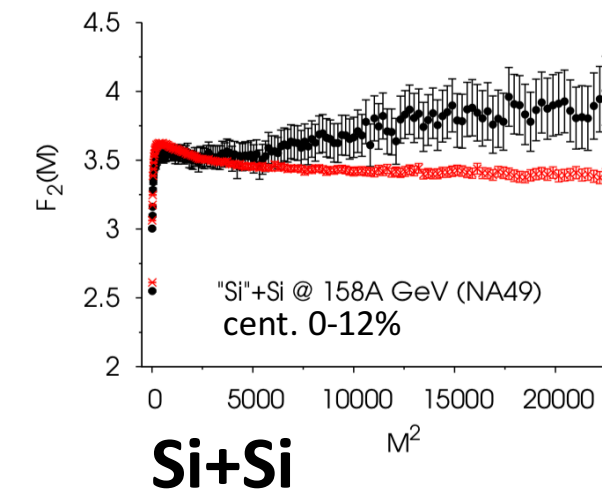
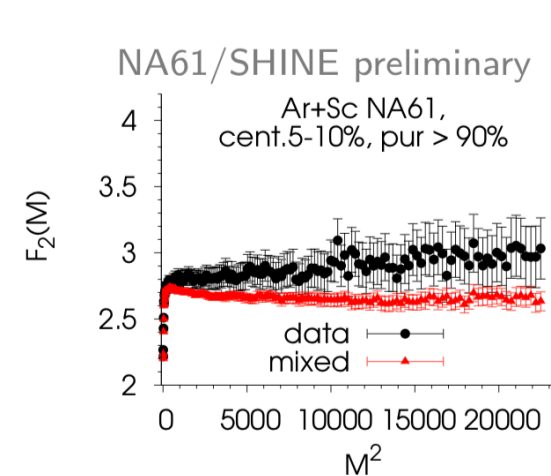
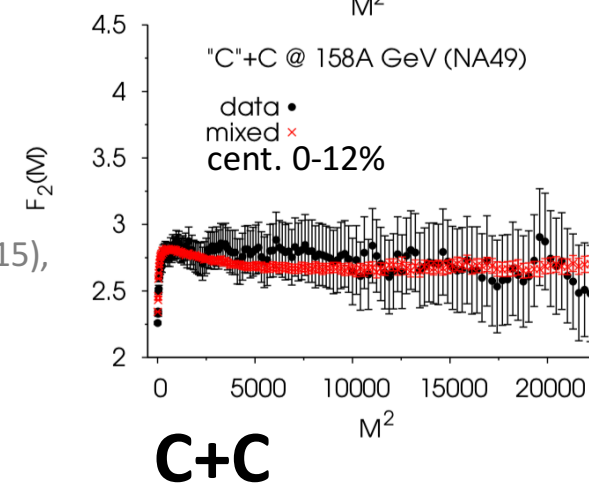
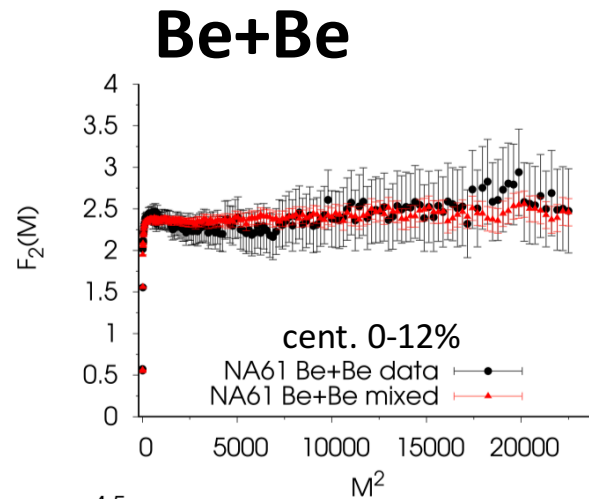
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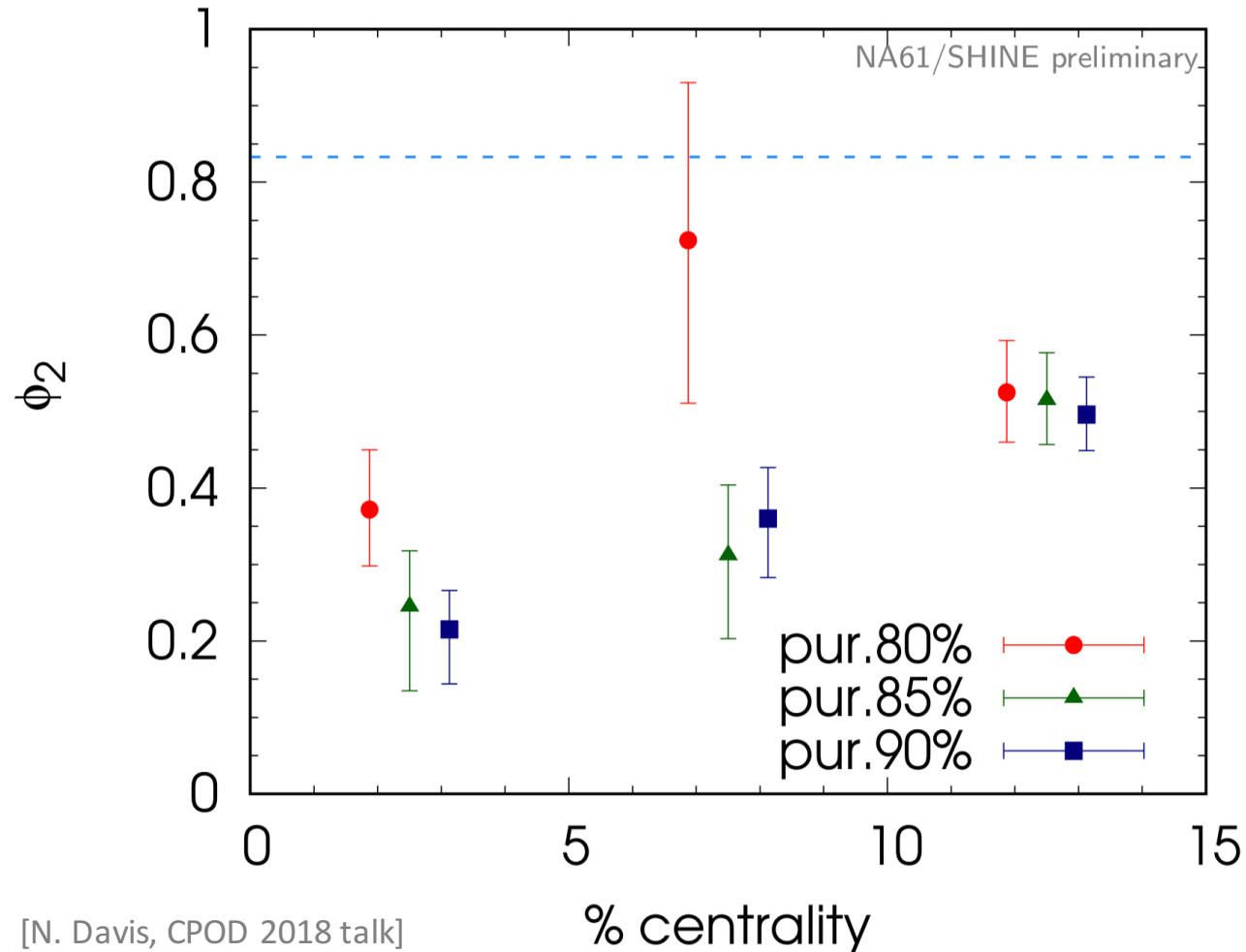
[N. Davis, CPOD 2018 talk]

What are the **intermittency indexes** for these systems?

# Intermittency index: NA61/SHINE

Intermittency index  $\phi_2$  for Ar+Sc at 150A GeV/c (80, 85 and 90% purity selection for protons)

$$\mathcal{P}_p = p / (\pi + K + p + e)$$



[N. Davis, CPOD 2018 talk]

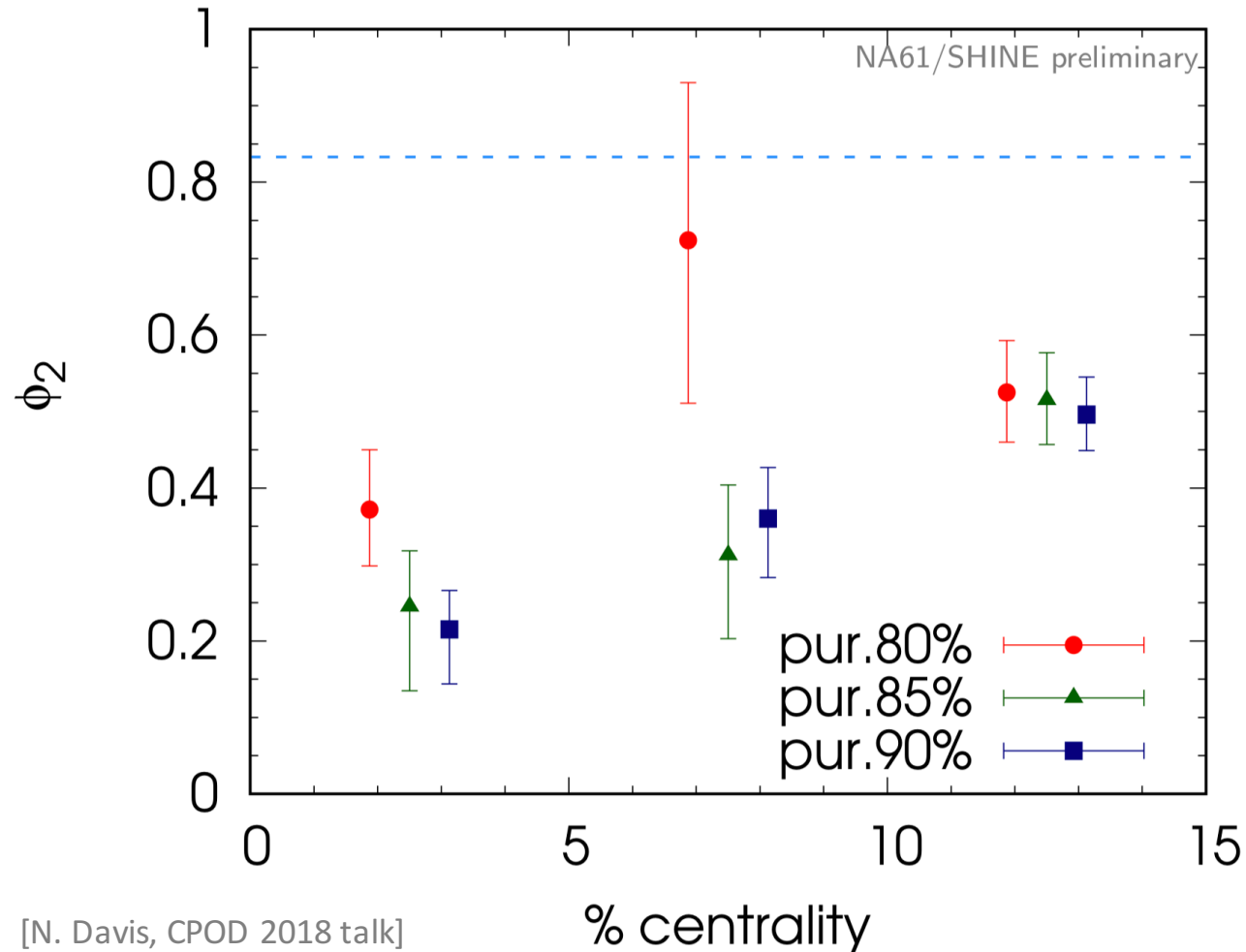
12/15



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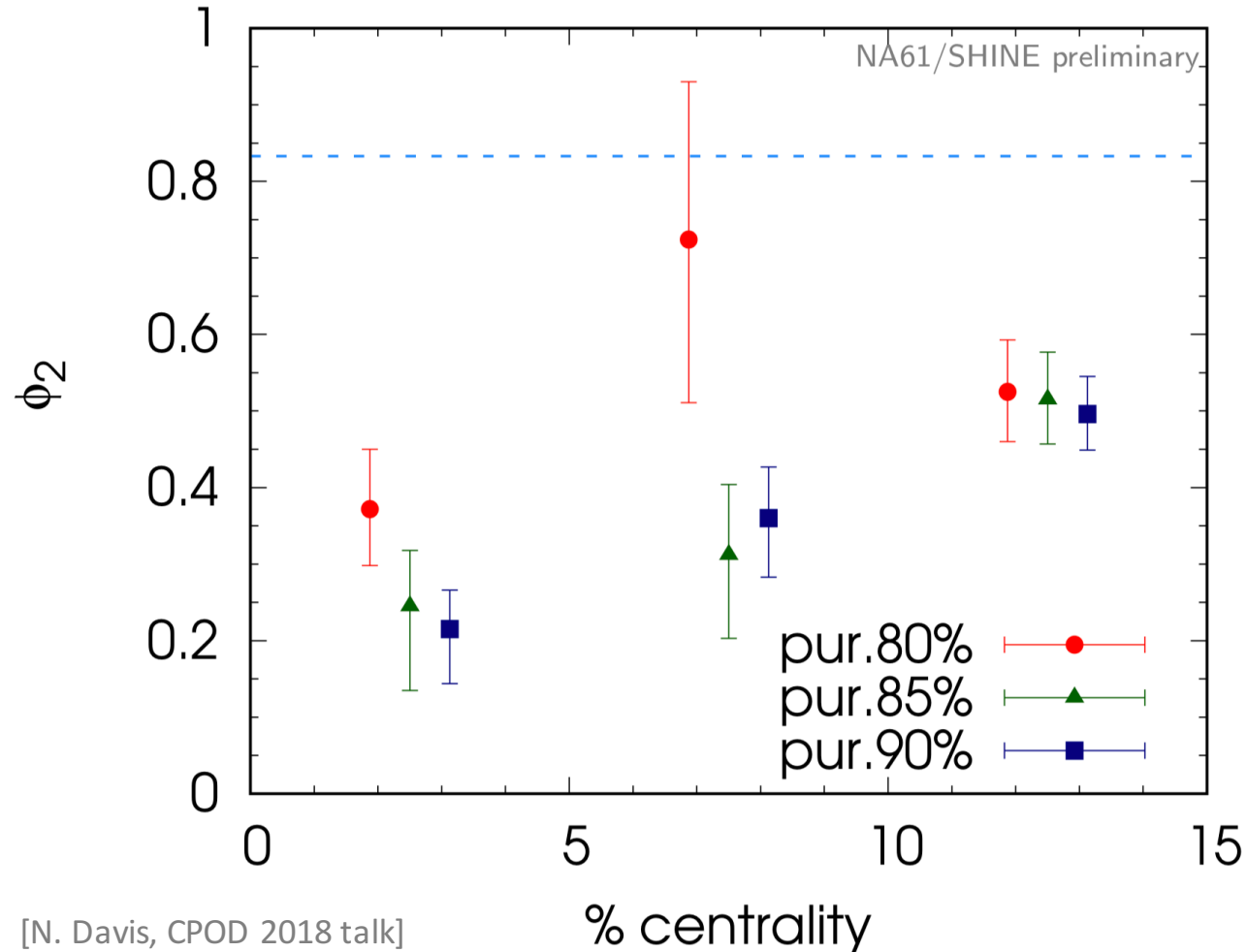
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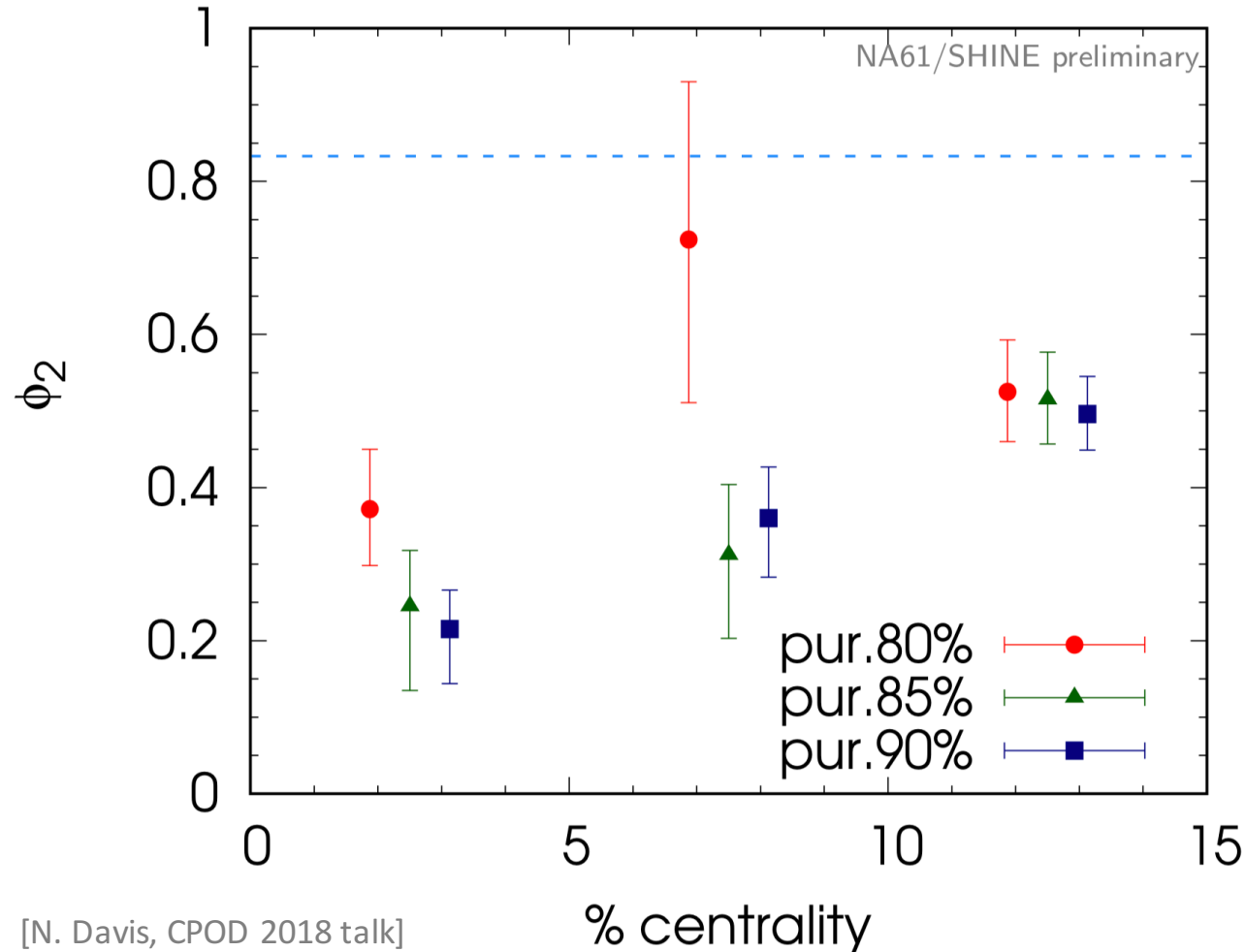
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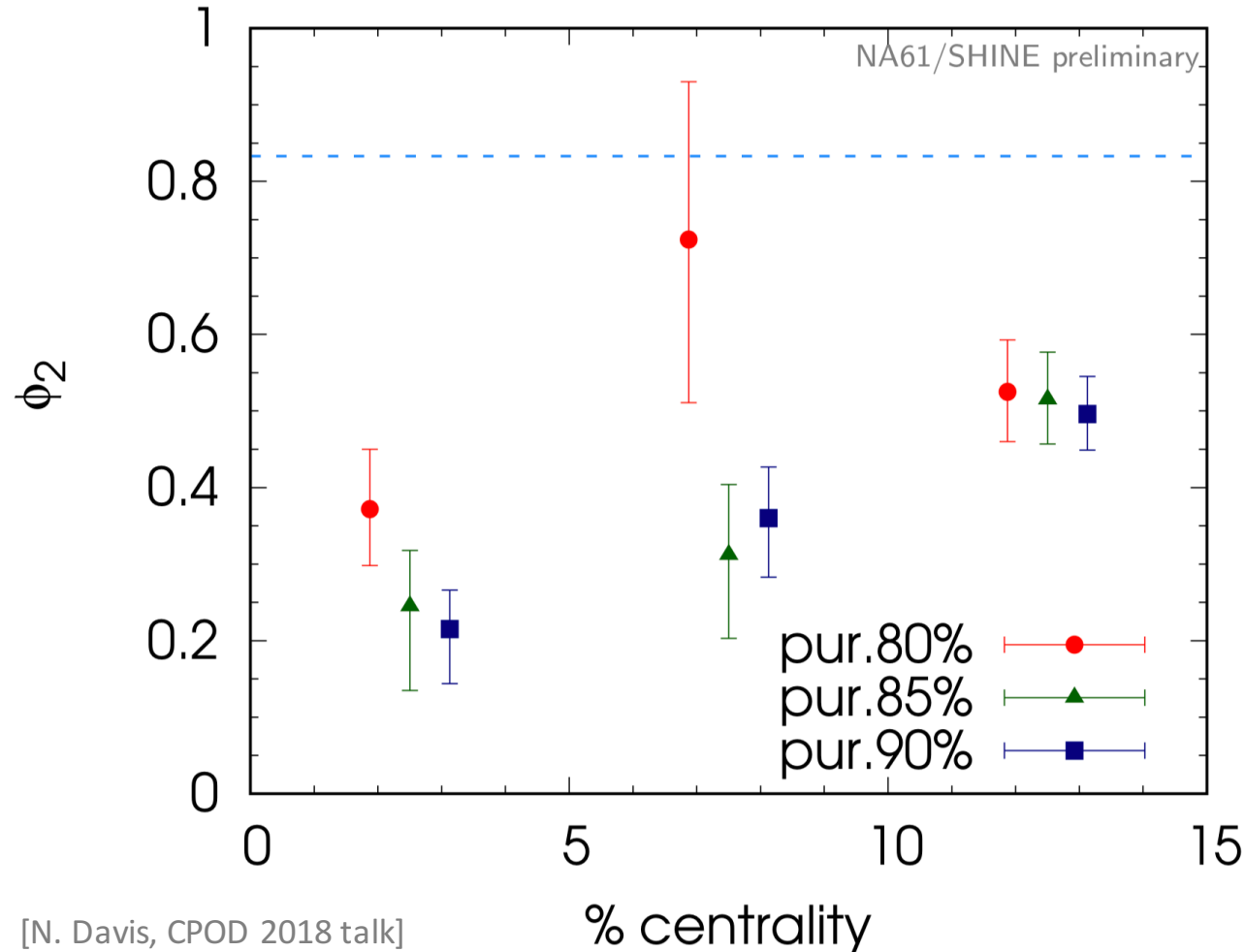
[N. Davis, CPOD 2018 talk]

12/15

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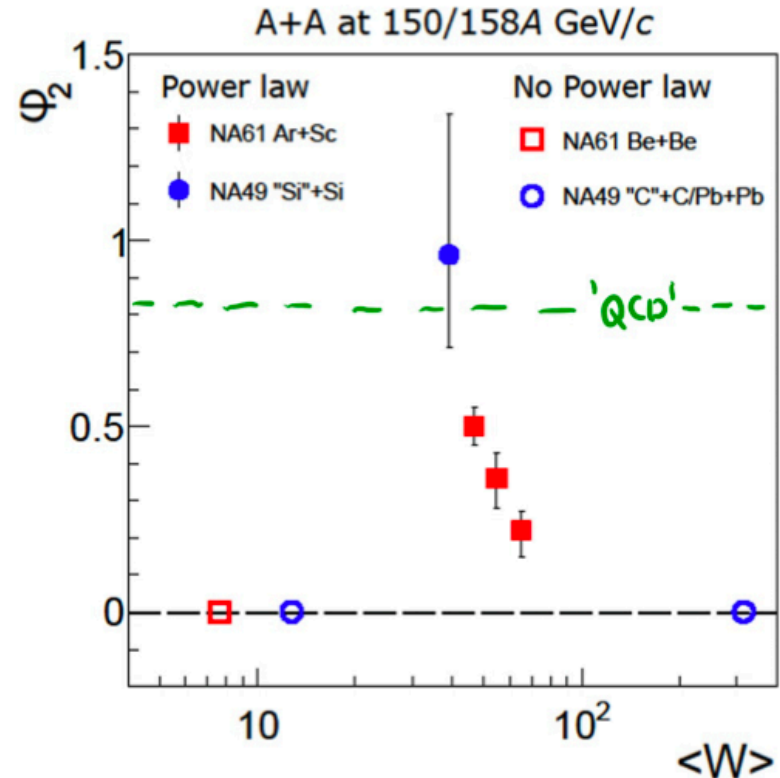
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[M. Gazdzicki, indico.cern.ch]

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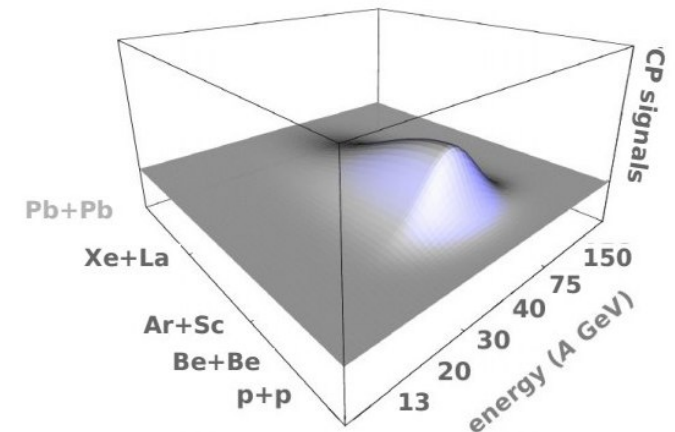
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Stay tuned and have a **SHINY** day!

