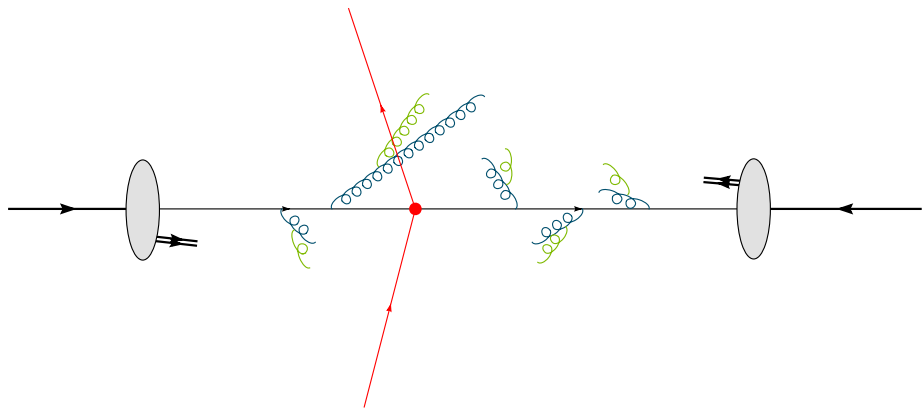
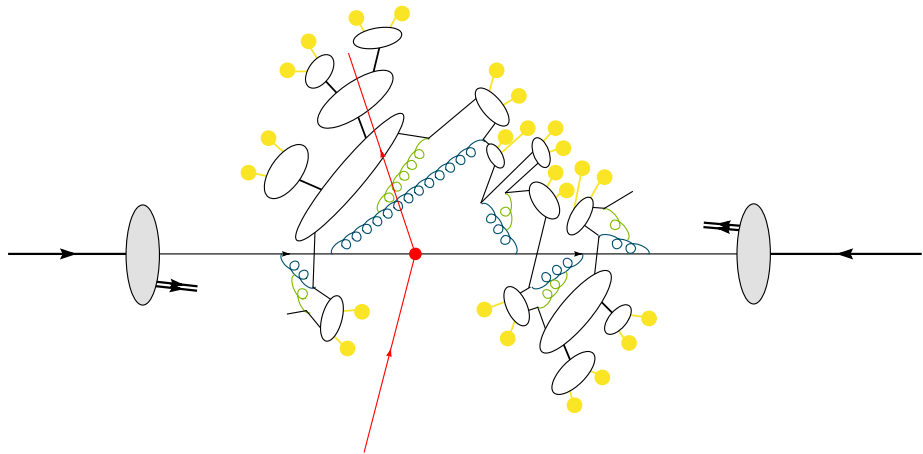


# Hadronization

# Parton shower



# Parton shower $\longrightarrow$ hadrons



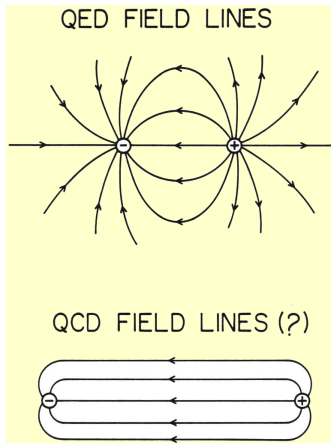
# Parton shower $\longrightarrow$ hadrons

- Parton shower terminated at  $t_0 =$  lower end of PT.
- Can't measure quarks and gluons.
- Degrees of freedom in the detector are **hadrons**.
- Need a description of **confinement**.

# Physical input

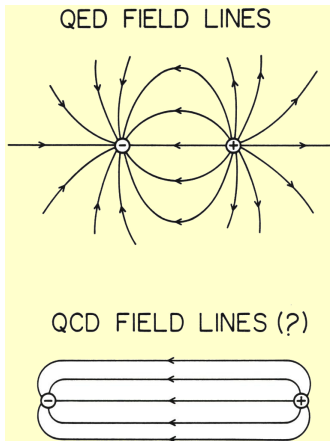
Self coupling of gluons

↔ “attractive field lines”

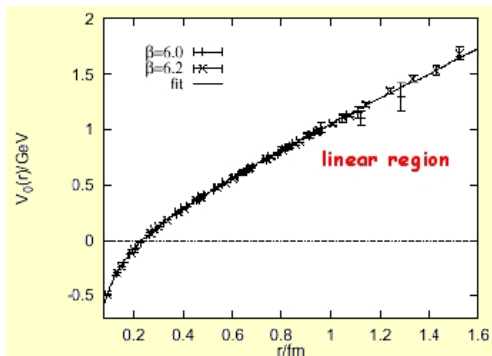


# Physical input

Self coupling of gluons  
↔ “attractive field lines”



Linear static potential  $V(r) \approx \kappa r$ .



Supported by lattice QCD,  
hadron spectroscopy.

# Hadronization models

Older models:

- Flux tube model.
- Independent fragmentation.

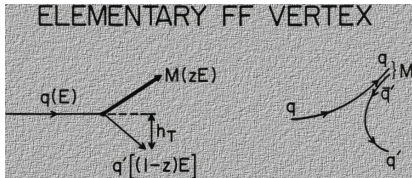
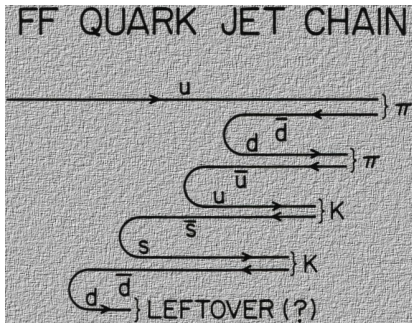
Today's models.

- Lund string model (Pythia).
- Cluster model (Herwig).

# Independent fragmentation

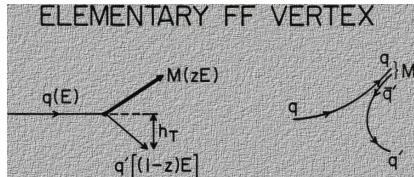
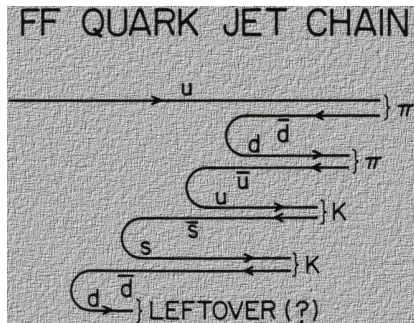
Feynman–Field fragmentation ('78).

- $q\bar{q}$  pairs created from vacuum to dress bare quarks.
- Fragmentation function  $f_{q \rightarrow h}(z) =$  density of momentum fraction  $z$  carried away by hadron  $h$  from quark  $q$ .
- Gaussian  $p_{\perp}$  distribution.





# Independent fragmentation



Feynman–Field fragmentation ('78).

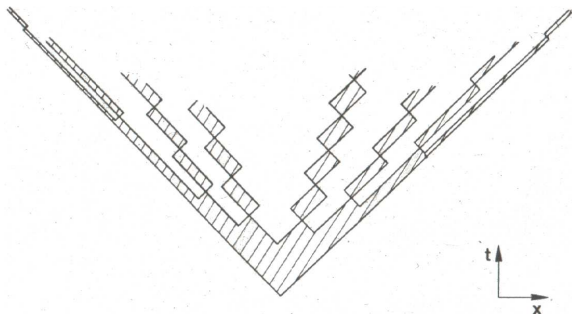
- $q\bar{q}$  pairs created from vacuum to dress bare quarks.
- Fragmentation function  $f_{q \rightarrow h}(z) =$  density of momentum fraction  $z$  carried away by hadron  $h$  from quark  $q$ .
- Gaussian  $p_{\perp}$  distribution.
- Problems:
  - "last quark".
  - not Lorentz invariant.
  - infrared safety.
  - ...
- Good at that time.
- Still useful for inclusive descriptions.

# Lund string model

String energy  $\sim$  intense chromomagnetic field.

$\rightarrow$  Additional  $q\bar{q}$  pairs created by QM tunneling.

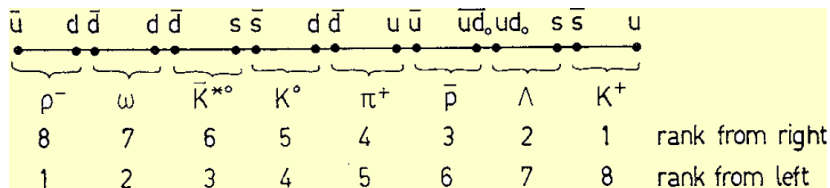
$$\frac{d\text{Prob}}{dxdt} \sim \exp\left(-\pi m_q^2/\kappa\right) \quad \kappa \sim 1 \text{ GeV}.$$



String breaking expected long before yoyo point.

# Lund string model

Adjacent breaks form hadrons.



Works in both directions (symmetry).

Lund symmetric fragmentation function

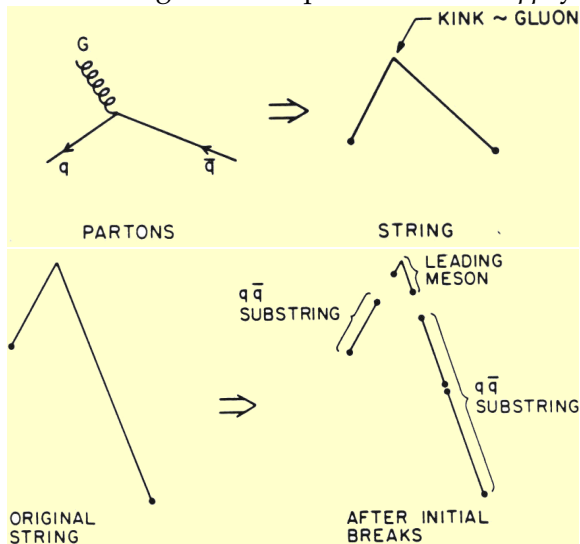
$$f(z, p_{\perp}) \sim \frac{1}{z} (1-z)^a \exp\left(-\frac{b(m_h^2 + p_{\perp}^2)}{z}\right)$$

$a, b, m_h^2$  main adjustable parameters.

Note: diquarks  $\rightarrow$  baryons.

# Lund string model

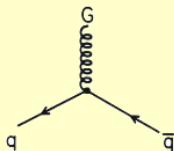
gluon = kink on string = motion pushed into the  $q\bar{q}$  system.



# Lund string model

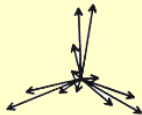
gluon = kink on string = motion pushed into the  $q\bar{q}$  system.

## SYMMETRIC PARTON CONFIGURATION

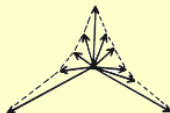


## HADRONIZATION

### INDEPENDENT FRAGMENTATION

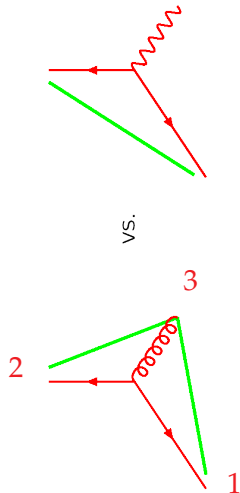


### LUND PICTURE

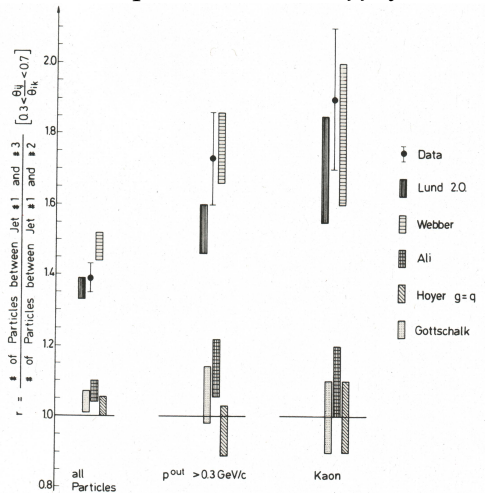


# Lund string model

gluon = kink on string = motion pushed into the  $q\bar{q}$  system.



*"String effect"*



# Lund string model

Some remarks:

- Originally invented without parton showers in mind.

# Lund string model

## Some remarks:

- Originally invented without parton showers in mind.
- Strong physical motivation.
- Very successful description of data.
- Universal description of data  
(fit at  $e^+e^-$ , transfer to hadron-hadron).
- Many parameters,  $\sim 1$  per hadron.
- Too easy to hide errors in perturbative description?



# Lund string model

Some remarks:

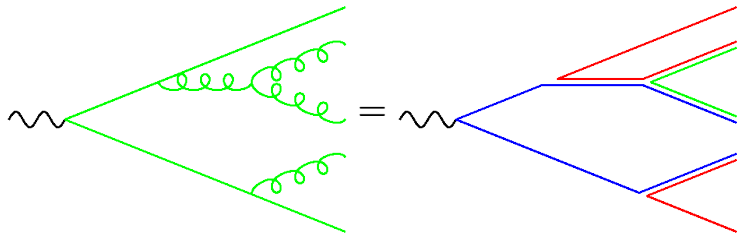
- Originally invented without parton showers in mind.
- Strong physical motivation.
- Very successful description of data.
- Universal description of data (fit at  $e^+e^-$ , transfer to hadron-hadron).
- Many parameters,  $\sim 1$  per hadron.
- Too easy to hide errors in perturbative description?

→ try to use more QCD information/intuition.

# Colour preconfinement

Large  $N_C$  limit  $\rightarrow$  planar graphs dominate.

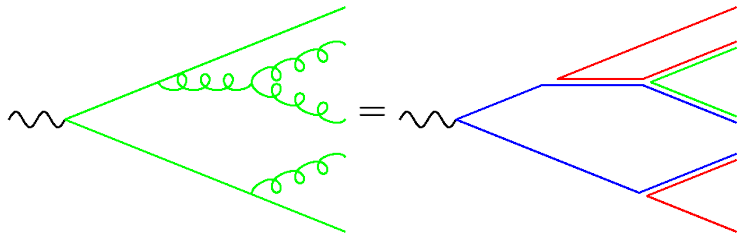
Gluon = colour — anticolourpair



# Colour preconfinement

Large  $N_C$  limit  $\rightarrow$  planar graphs dominate.

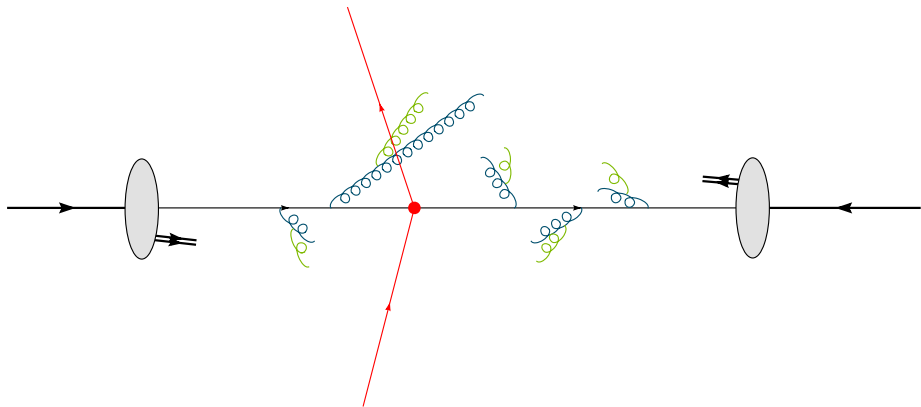
Glueon = colour — anticolourpair



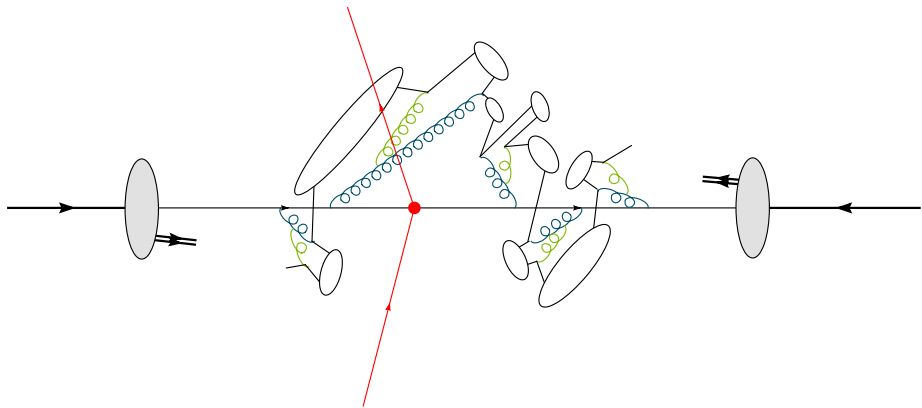
Parton shower organises partons in colour space. Colour partners (=colour singlet pairs) end up close in phase space.

$\rightarrow$  Cluster hadronization model

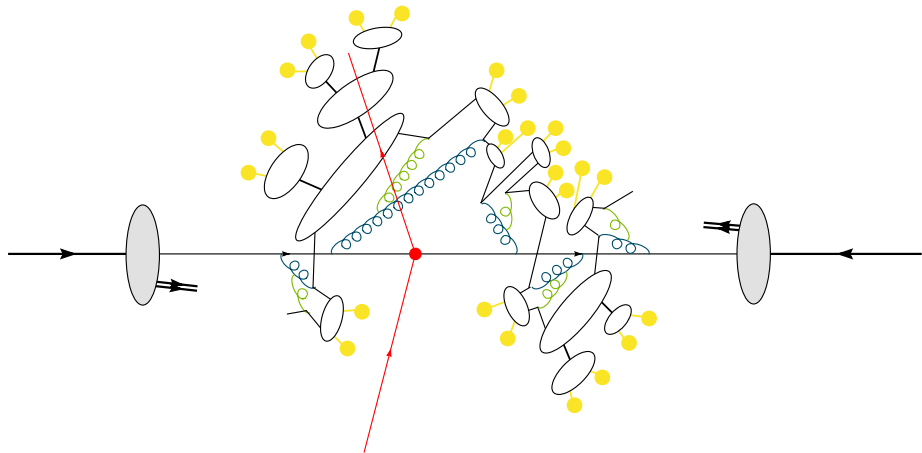
# Cluster hadronization



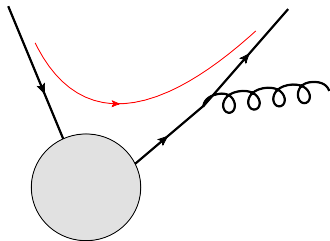
# Cluster hadronization



# Cluster hadronization

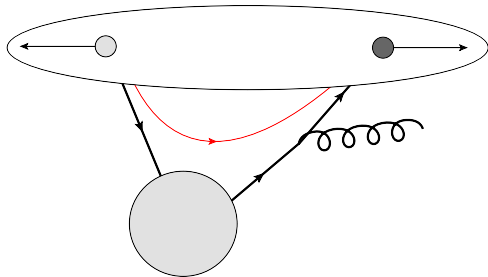


# Cluster Hadronization



After parton shower, partons on constituent mass shell  
Find colour singlets as  $3\text{-}\bar{3}$  pairs  $\rightarrow$  cluster  
Colour neighbours  $\sim$  neighbours in momentum space

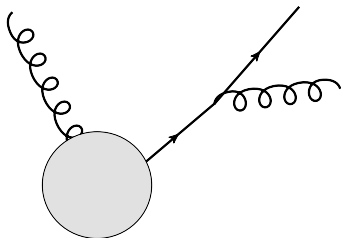
# Cluster Hadronization



After parton shower, partons on constituent mass shell  
Find colour singlets as  $3\text{-}\bar{3}$  pairs  $\rightarrow$  cluster  
Colour neighbours  $\sim$  neighbours in momentum space

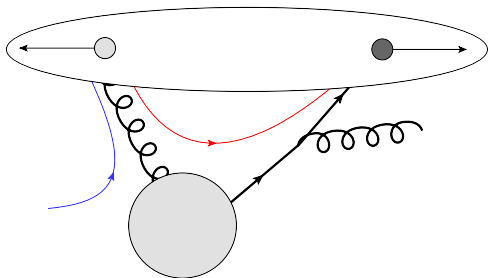


# Cluster Hadronization



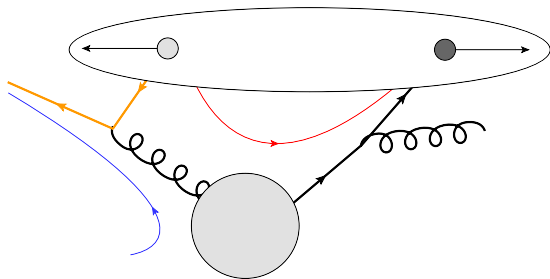
But gluons are not just 3 or  $\bar{3}$ !

# Cluster Hadronization



But gluons are not just  $3$  or  $\bar{3}$ !

# Cluster Hadronization



But gluons are not just 3 or  $\bar{3}$ !  
non-perturbative gluon splitting  
 $m_g > 2m_q$   
kinematics from masses  
quarks and diquarks possible

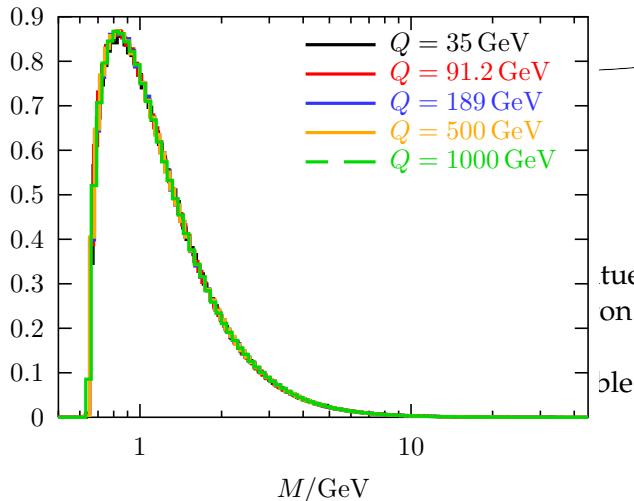
# Cluster Hadronization



Cluster carries net momentum of its constituents  
Spectrum determined by final state of parton shower  
Independent of hard scales  
Tail of *heavy clusters*, still large scale available

# Cluster Hadronization

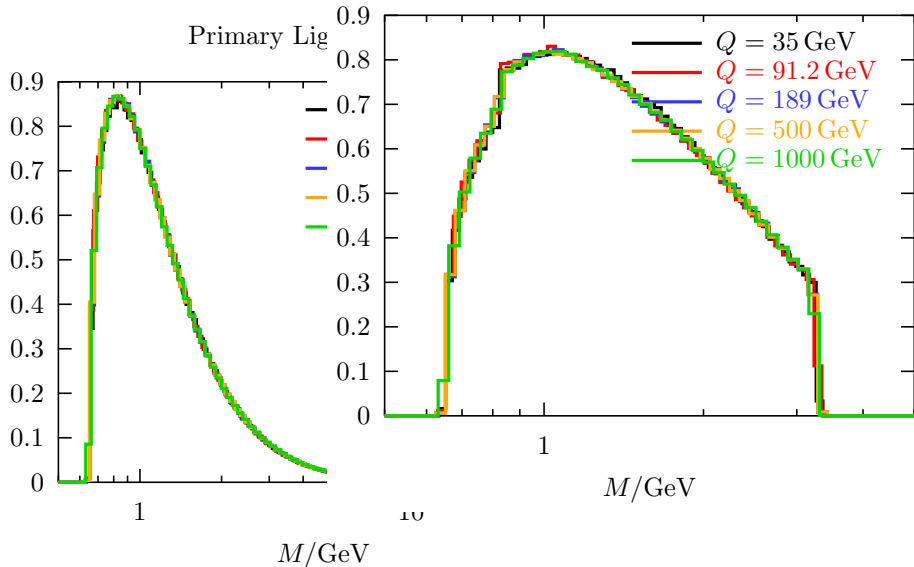
Primary Light Clusters



# Cluster Hadronization

## Secondary Light Clusters

Primary Lig



# Cluster Hadronization



Binary fission along quarks' direction of motion

Flavour introduced in  $q\bar{q}$  pairs

Mass  $\rightarrow$  multiplicity, momentum

Beam remnant clusters split off as very light clusters

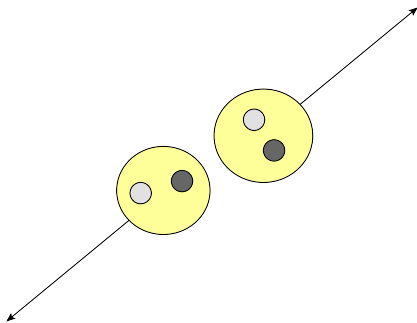
# Cluster Hadronization



End up with fairly light clusters  
too light? Decay into single hadron  
Exchange momentum with neighbour

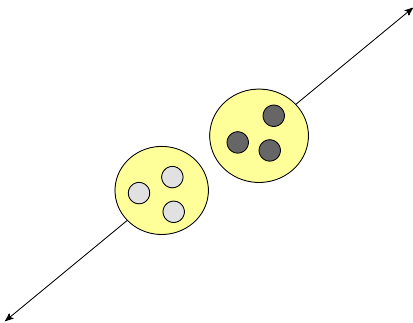


# Cluster Hadronization



Decay isotropically into hadron pairs  
Individual Hadrons get weight according to flavour multiplet,  
CM momentum, spin multiplicity etc.

# Cluster Hadronization



Baryon pairs possible

usually appear from clusters with 1 or 2 diquarks

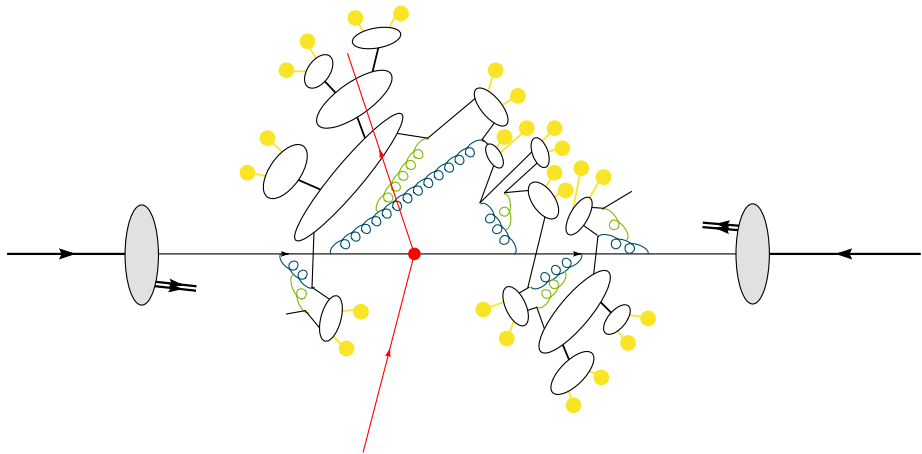
could also emerge in pairs from mesonic clusters

# Hadronization

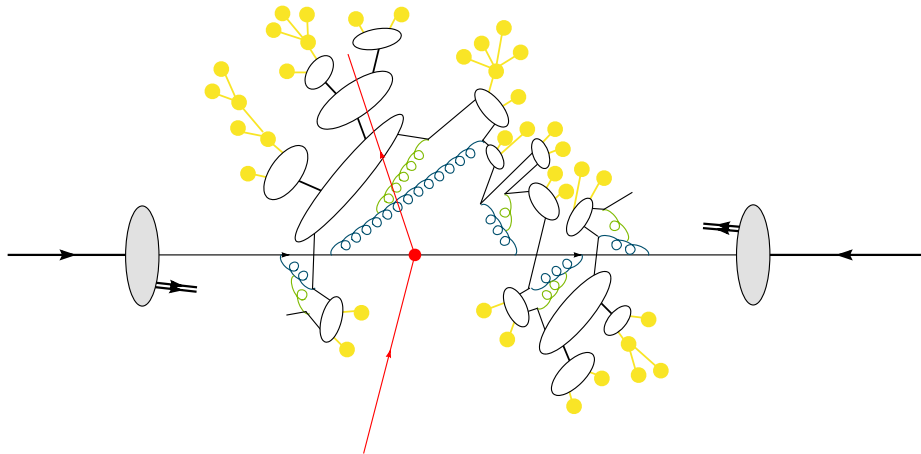
- Only string and cluster models used in recent MC programs.  
Independent fragmentation only for inclusive observables.
- Strings started non-perturbatively, improved by parton shower.
- Cluster model started mostly on perturbative side, improved by string like cluster fission.

# Hadronic Decays

# Hadronic decays



# Hadronic decays



# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

EM decay.



# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

Weak mixing.

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

Weak decay.

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

Strong decay.

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

Weak decay,  $\rho^+$  mass smeared.

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

$\rho^+$  polarized, angular correlations.

# Hadronic decays

Many aspects:

$$B^{*0} \rightarrow \gamma B^0$$

$$\hookrightarrow \bar{B}^0$$

$$\hookrightarrow e^- \bar{\nu}_e D^{*+}$$

$$\hookrightarrow \pi^+ D^0$$

$$\hookrightarrow K^- \rho^+$$

$$\hookrightarrow \pi^+ \pi^0$$

$$\hookrightarrow e^+ e^- \gamma$$

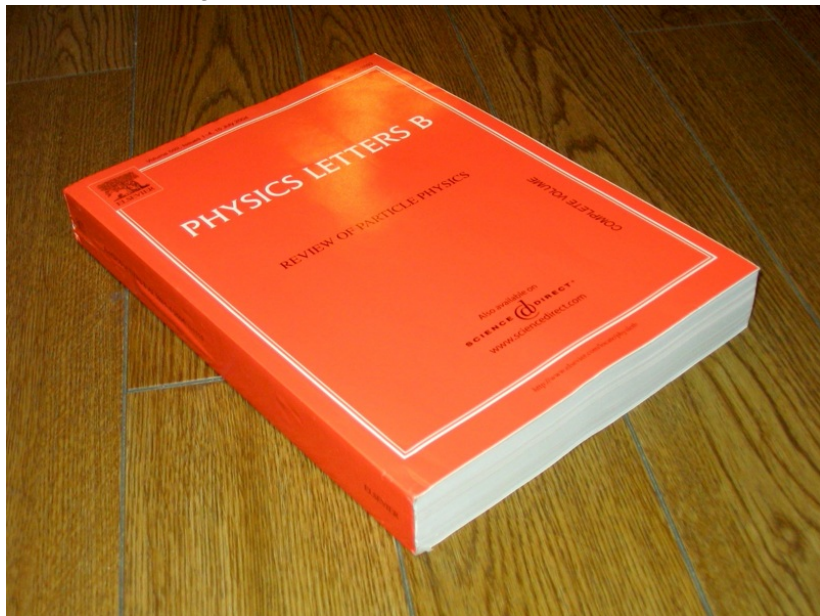
Dalitz decay,  $m_{ee}$  peaked.

# Hadronic decays

Tedious.

100s of different particles, 1000s of decay modes,  
phenomenological matrix elements with parametrized form  
factors...

# Hadronic decays





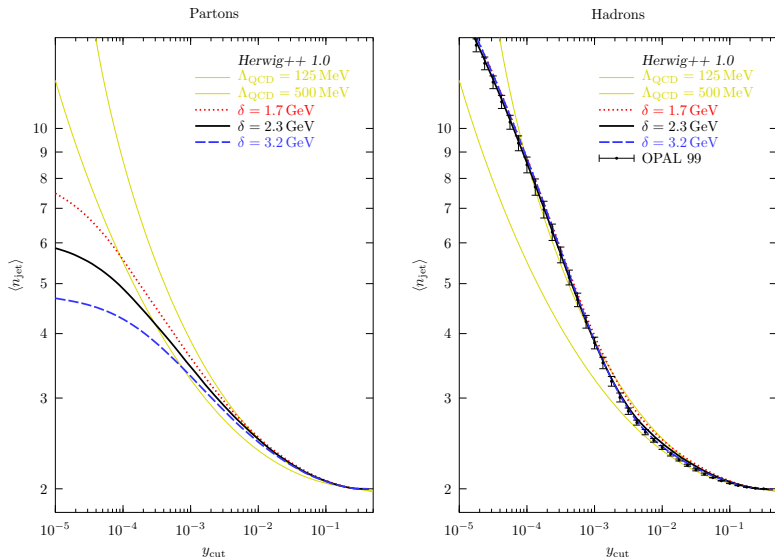
# A few plots

# How well does it work?

- $e^+e^- \rightarrow$  hadrons, mostly at LEP.
- Jet shapes, jet rates, event shapes, identified particles...
- 'Tuning' of parameters.
- Use *all* analyses available in Rivet.
- Want to get *everything* right with *one* parameter set.
- Compare to literally  $\approx 20000$  plots.
  
- Check out <http://herwig.hepforge.org>  
( $\rightarrow$  Plots) for many more and comparisons with the latest release.

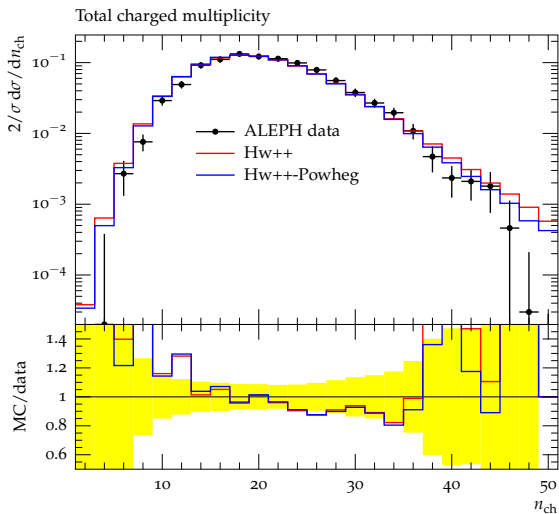
# How well does it work?

Smooth interplay between shower and hadronization.



# How well does it work?

$N_{\text{ch}}$  at LEP. Crucial for  $t_0$  (Herwig++ 2.5.2)



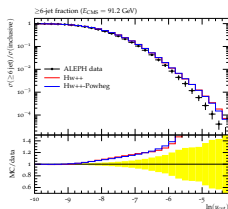
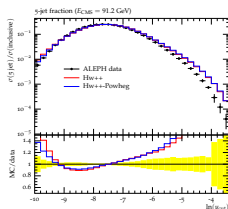
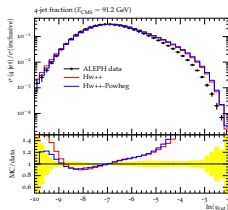
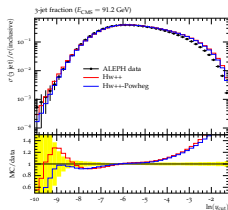
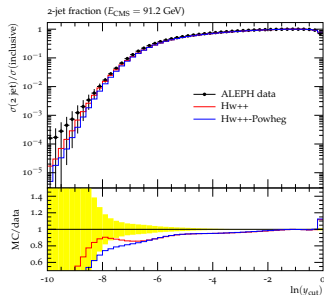
# How well does it work?

## Jet rates at LEP.

$$R_n = \sigma(n\text{-jets})/\sigma(\text{jets})$$

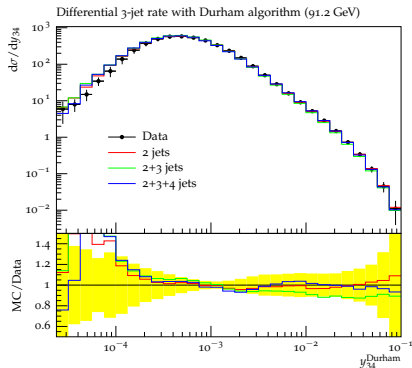
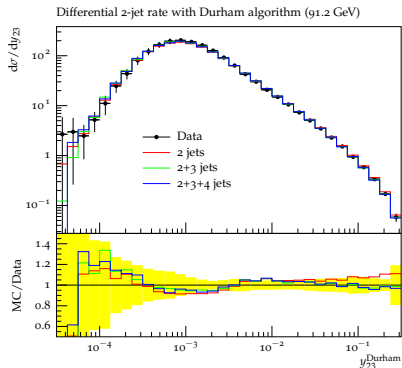
$$R_6 = \sigma(> 5\text{-jets})/\sigma(\text{jets})$$

(Herwig++ 2.5.2j)



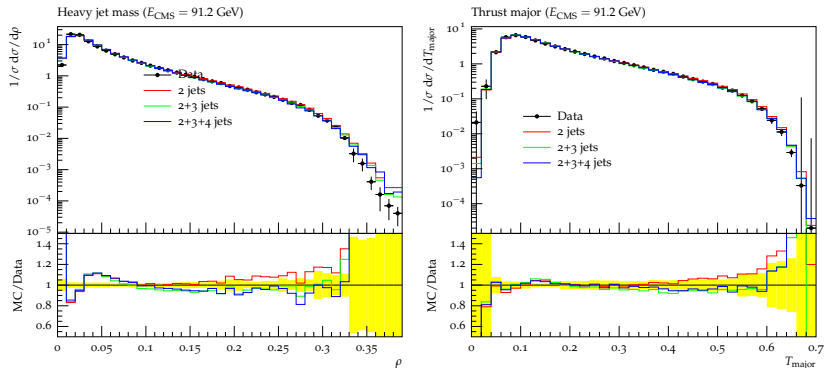
# How well does it work?

## Differential Jet Rates at LEP (Herwig++ pre-3.0). Dipole shower + some merging



# How well does it work?

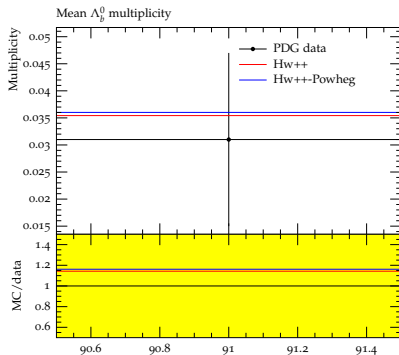
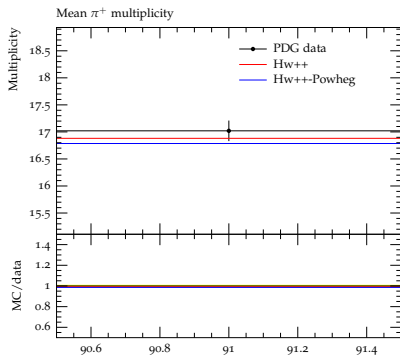
Event Shapes at LEP (Herwig++ pre-3.0).  
Dipole shower + some merging



Parton showers do very well, today!

# How well does it work?

Hadron Multiplicities at LEP (e.g.  $\pi^+$ ,  $\Lambda_b^0$ ).

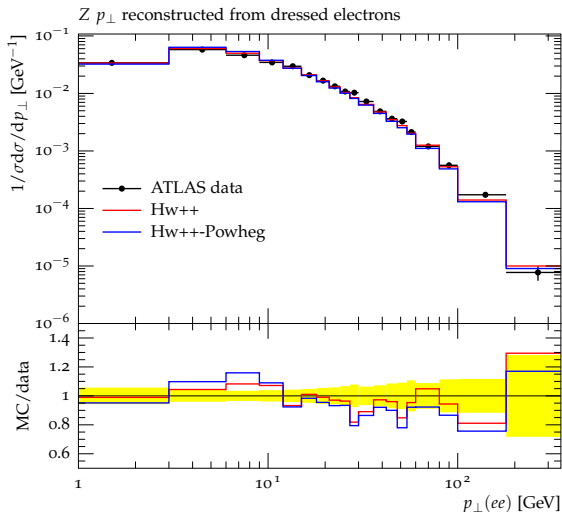




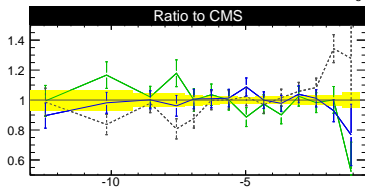
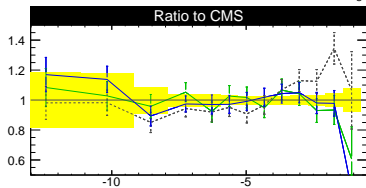
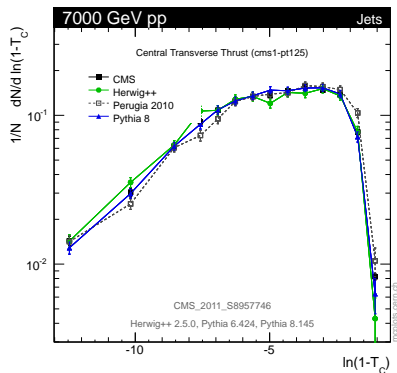
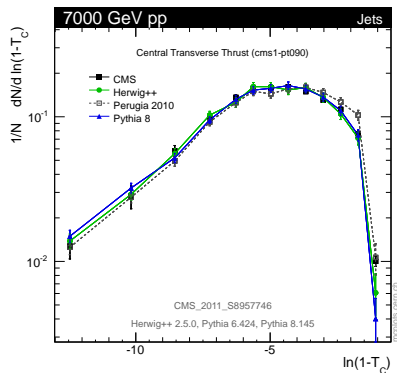
# How well does it work?

$p_{\perp}(Z^0) \rightarrow$  intrinsic  $k_{\perp}$  (LHC 7 TeV).

See also in context of matching/marging.

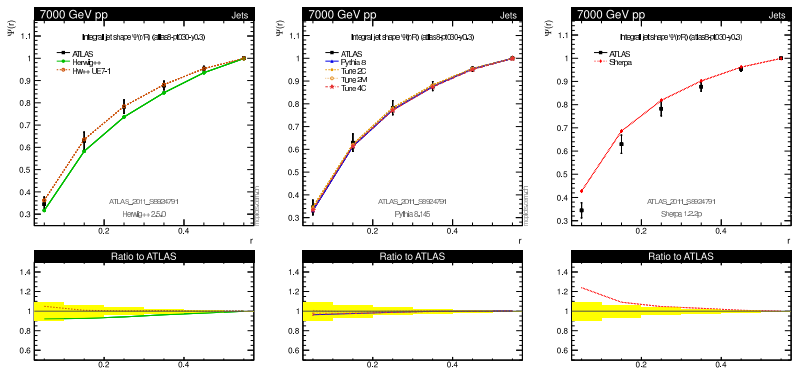


# Transverse thrust



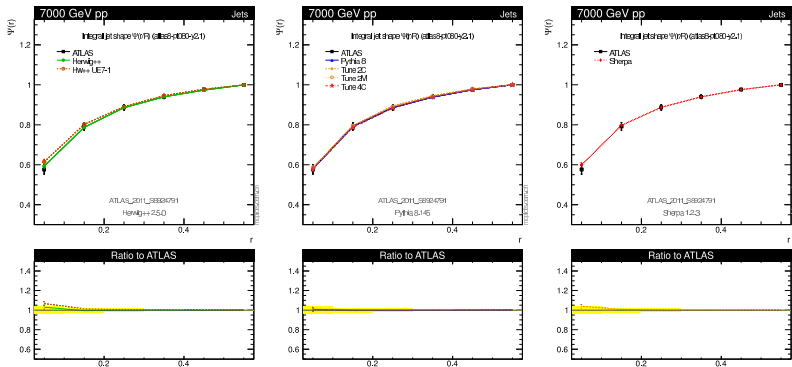
# Integral jet shapes

not too hard, central ( $30 < p_T/\text{GeV} < 40; 0 < |y| < 0.3$ )



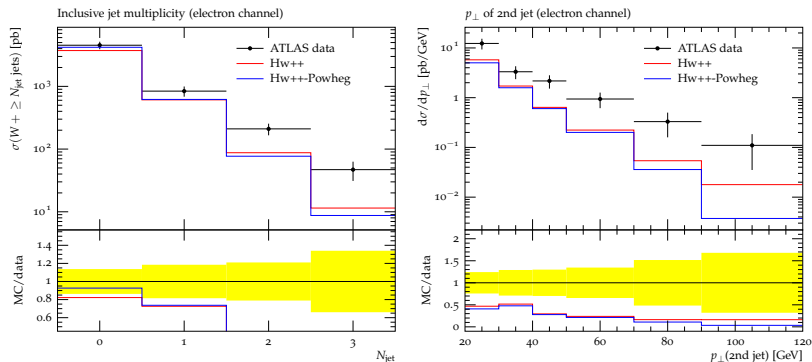
# Integral jet shapes

harder, more forward ( $80 < p_T/\text{GeV} < 110; 1.2 < |y| < 2.1$ )



# Limits of parton showers

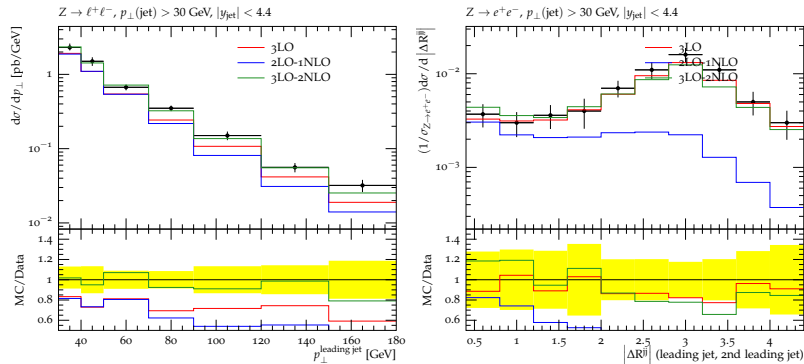
$W + \text{jets}$ , LHC 7 TeV.



Higher jets not covered by parton shower only  $\rightarrow$  merging.

# Unitarized Matching/Merging

Preliminary example: Z production, jet-jet correlation.



[J. Bellm, KIT]

3LO-2NLO = Z+0, 1, 2 (tree) and Z+0,1 NLO (virtual).