



Longitudinal beam profile diagnostics using coherent Cherenkov diffraction radiation at CLARA accelerator

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Coherent Cherenkov Radiation (CCR):

- Allow noninvasive diagnostic
- Relatively high intensity
- Highly directional
- New technique

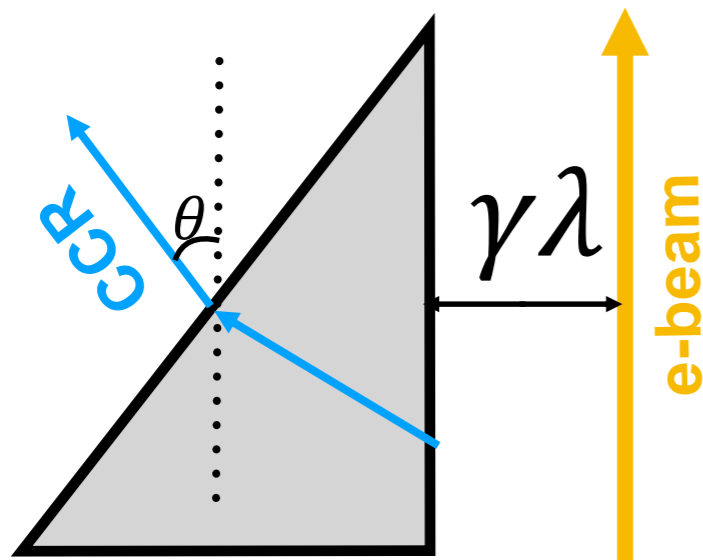


Fig.1 Schematic of CCR generation

Coherent Transition Radiation (CTR):

- Well studied

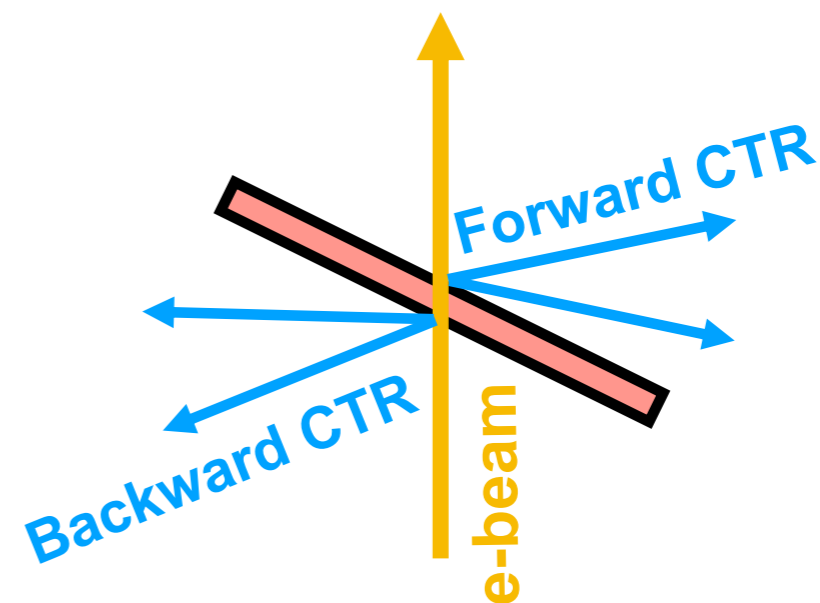


Fig.2 Schematic of CTR generation

How does CCR and CTR diagnostic work?

- The coherent spectral energy density produced by a bunch of N electrons is the product of the spectral energy density from by a single electron, the number of electrons squared and the absolute square of the form factor:

$$\begin{aligned} \left[\frac{d^2U}{d\omega d\Omega}\right]_{coh} &= N^2 \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} \left| \sum_{j=1}^N \exp(i\omega c^{-1} z_j) \right|^2 = \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} \sum_{j=1}^N \exp(i\omega c^{-1} z_j) \sum_{i=1}^N \exp(-i\omega c^{-1} z_i) = \\ &= \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} \left(N + \sum_{j=1}^N \exp(i\omega c^{-1} z_j) \sum_{\substack{j=1 \\ j \neq i}}^N \exp(-i\omega c^{-1} z_i) \right) = \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} \left(N + N(N-1) \left| \int \rho(z) \exp(i\omega c^{-1} z) dz \right|^2 \right) \end{aligned}$$

$$\left[\frac{d^2U}{d\omega d\Omega}\right]_{coh} = N^2 \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} |F(\omega)|^2 \quad \left[\frac{d^2U}{d\omega d\Omega}\right]_{coh} = N^2 \left[\frac{d^2U}{d\omega d\Omega}\right]_{single} \left[\int p(z) \cos\left(z \frac{\omega}{c}\right) dz \right]^2$$

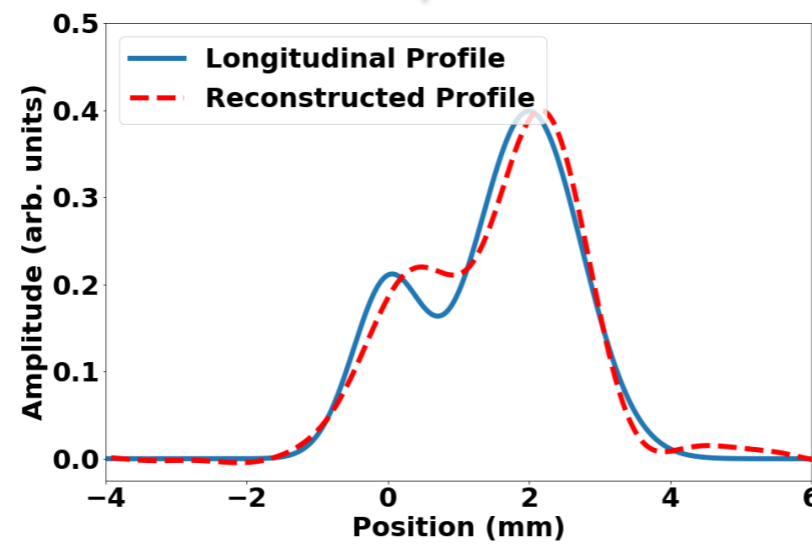
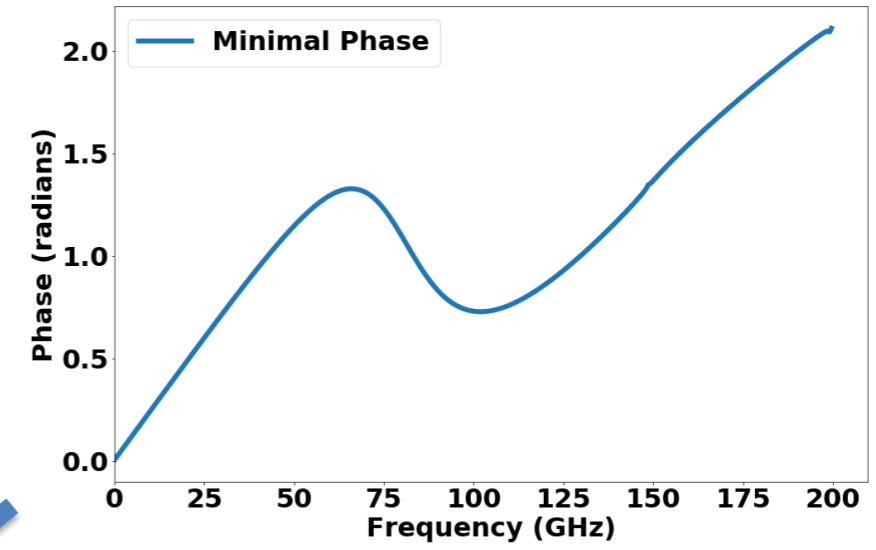
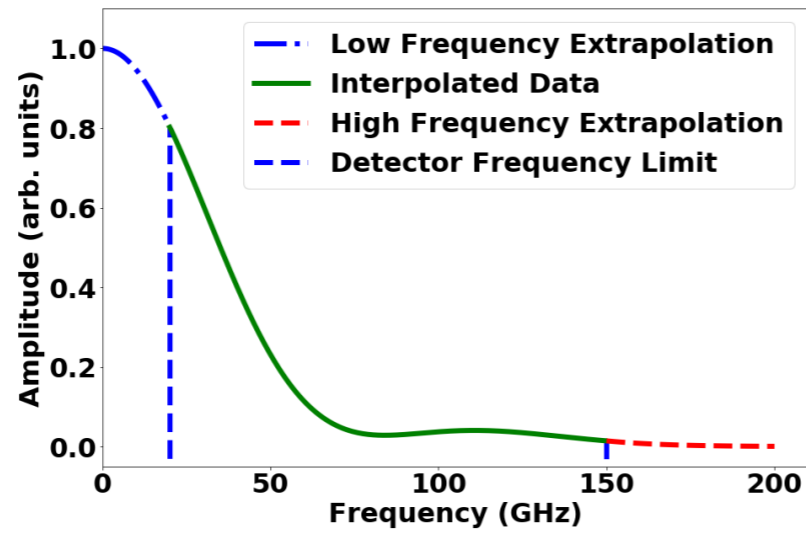
experimental data

$$p(z) = \frac{1}{\pi c} \int_0^\infty \sqrt{\frac{\left[\frac{d^2U}{d\omega d\Omega}\right]_{coh}}{\left[\frac{d^2U}{d\omega d\Omega}\right]_{single}}} \cos\left(\psi(\omega) - z \frac{\omega}{c}\right) d\omega$$

mathematical approach

How diagnostic is works?

$$\sqrt{\frac{\left[\frac{d^2U}{d\omega d\Omega}\right]_{coh}}{\left[\frac{d^2U}{d\omega d\Omega}\right]_{single}}}$$



$$p(z) = \frac{1}{\pi c} \int_0^\infty \sqrt{F(W)} \cos\left(\psi(w) - z \frac{w}{c}\right) dw$$

$$|F(w)|^2 = \frac{S_{coh}(w)}{S_{single}(w)}$$

$$S_{coh}(w)$$

$$S_{single}(w)$$

Kramers-Kronig analysis



Transition radiation spectrum from a single electron

Models takes into account the following parameters:

- Energy
- TR target size
- Distance between target and detector
- Detector aperture

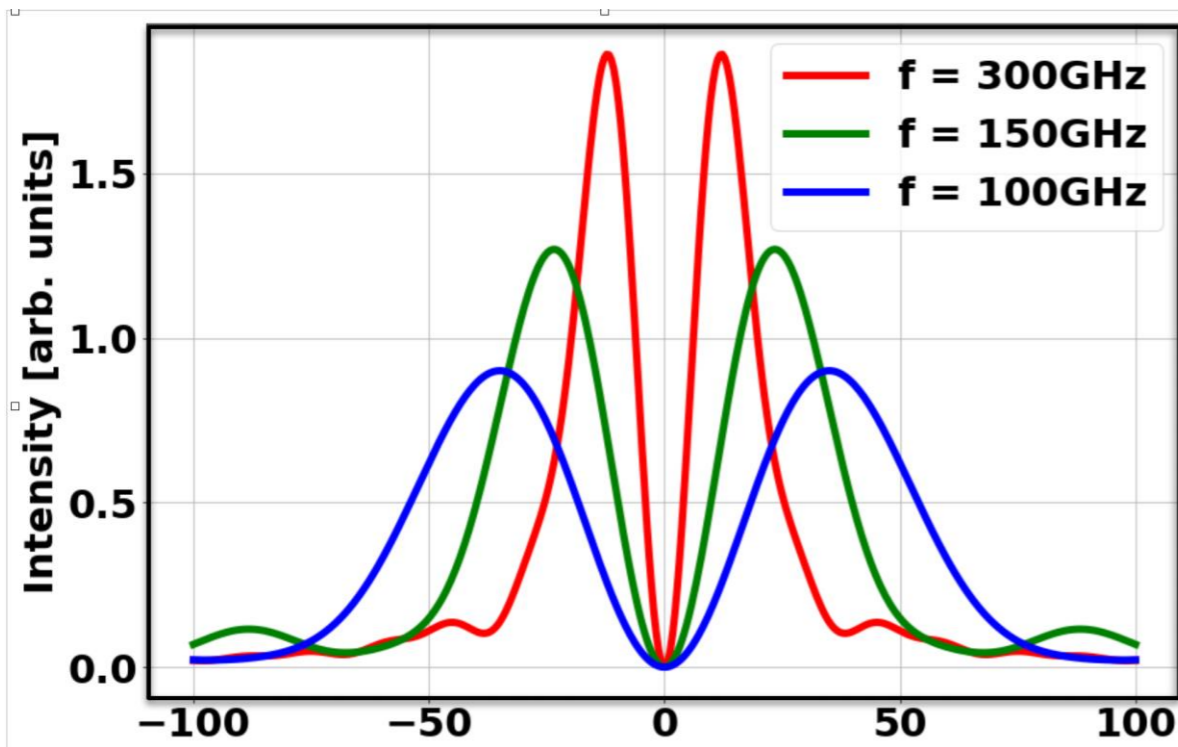


Fig.3 TR Spectral angular distribution from a single electron

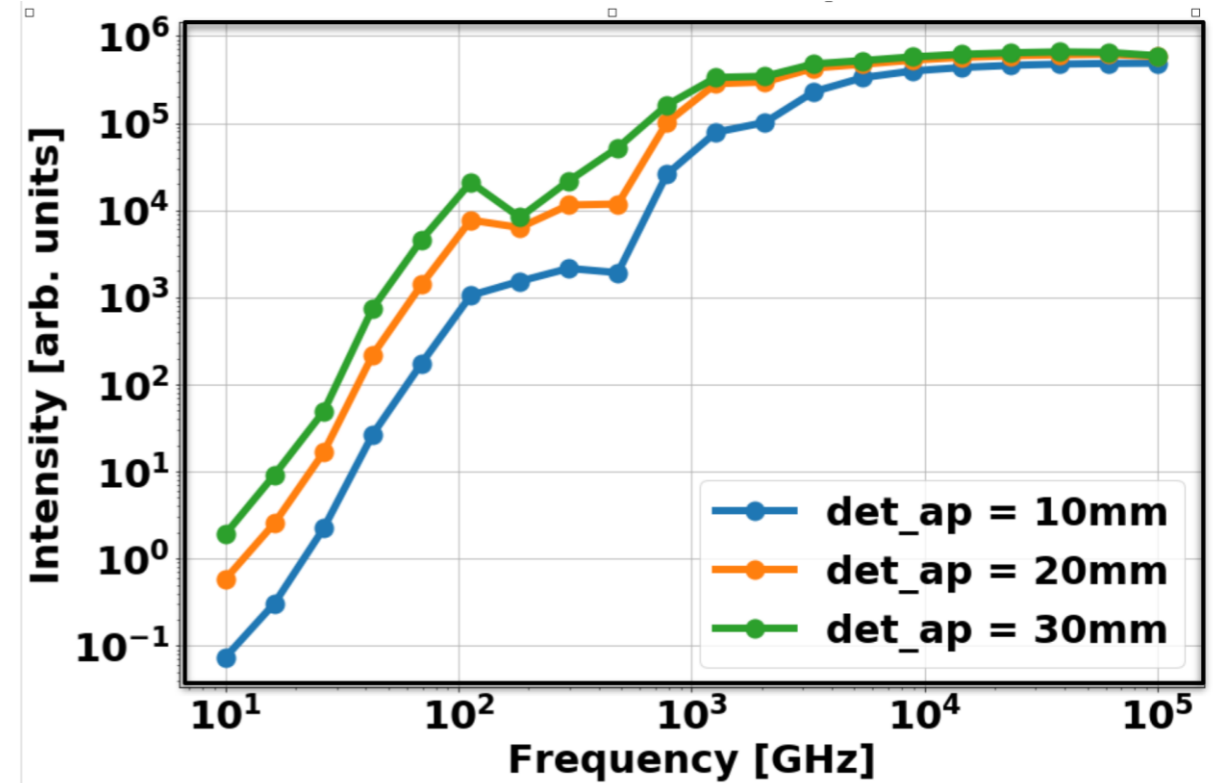


Fig.4 TR Spectrum for different detector apertures

Cherenkov radiation spectrum from a single electron

Models takes into account the following parameters:

- Energy
- Cherenkov target dimensions (prismatic target)
- Cherenkov target refractive index
- Distance between target and detector
- Detector aperture
- Impact parameter (distance between beam and target)
- Angle between target and particle direction

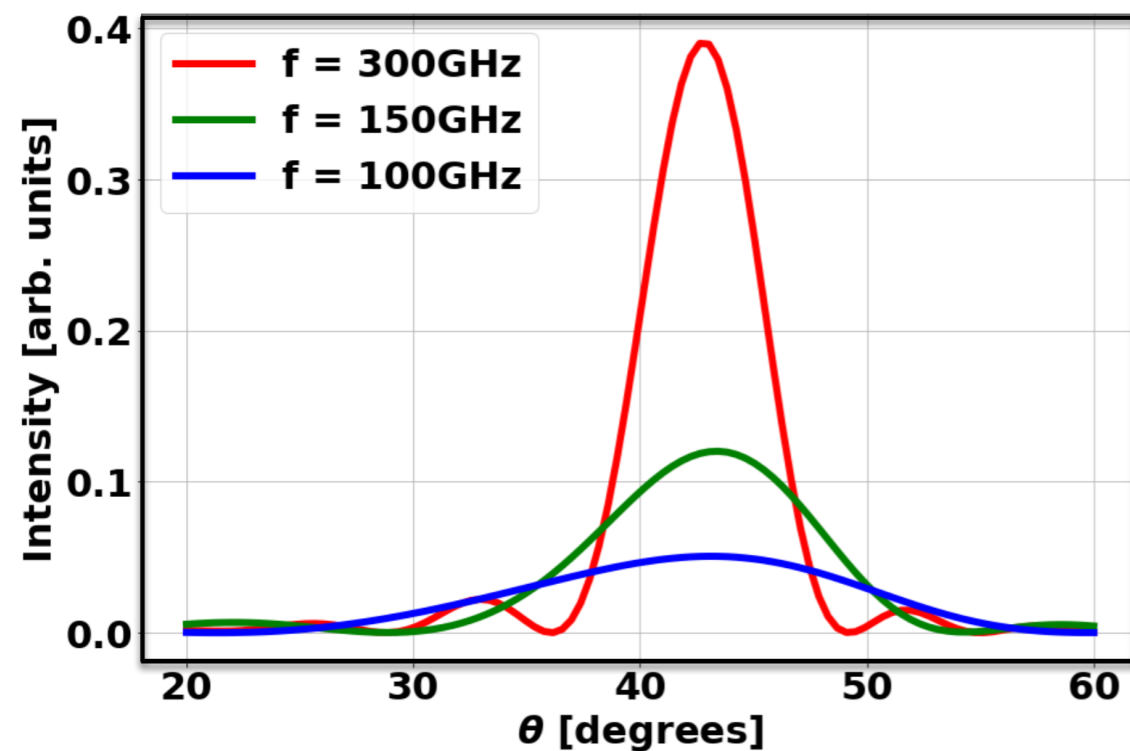


Fig. 5 VCR Spectral angular distribution from a single electron

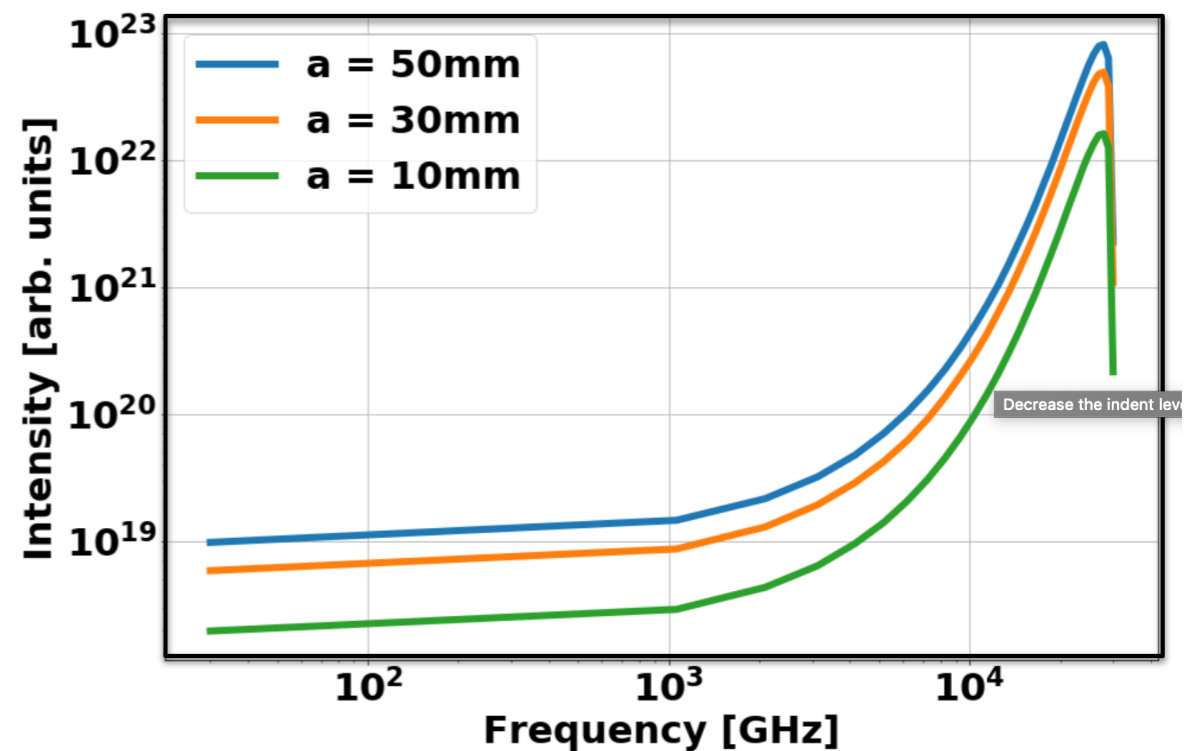
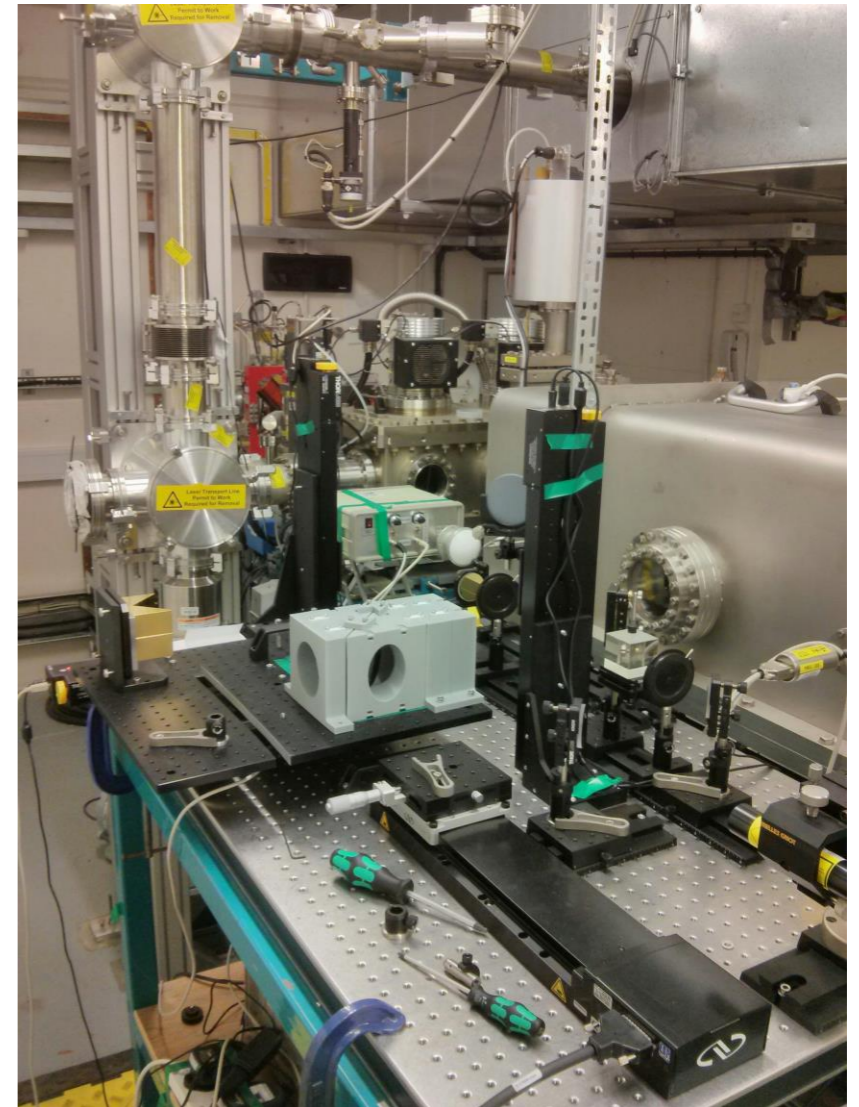
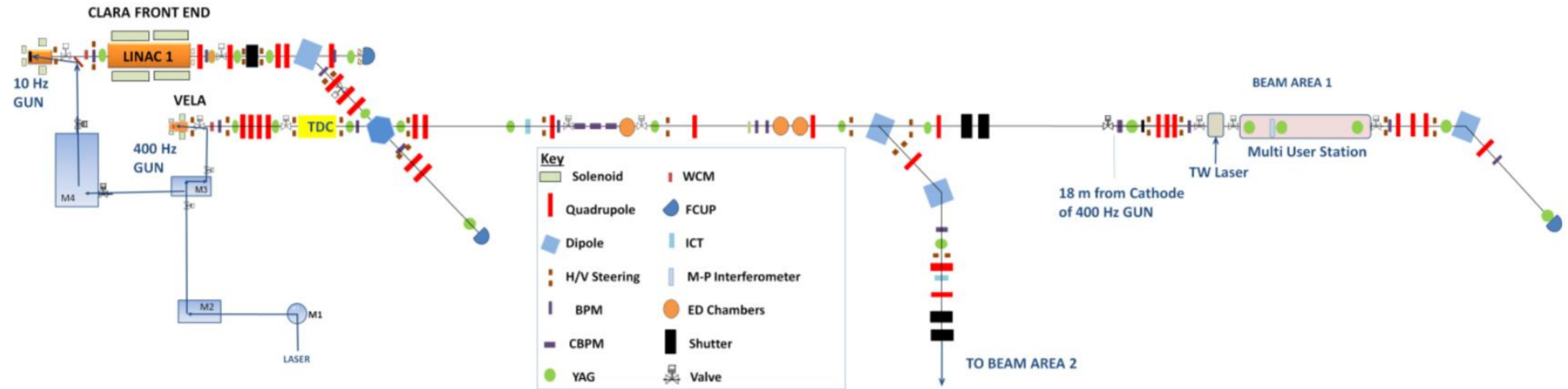
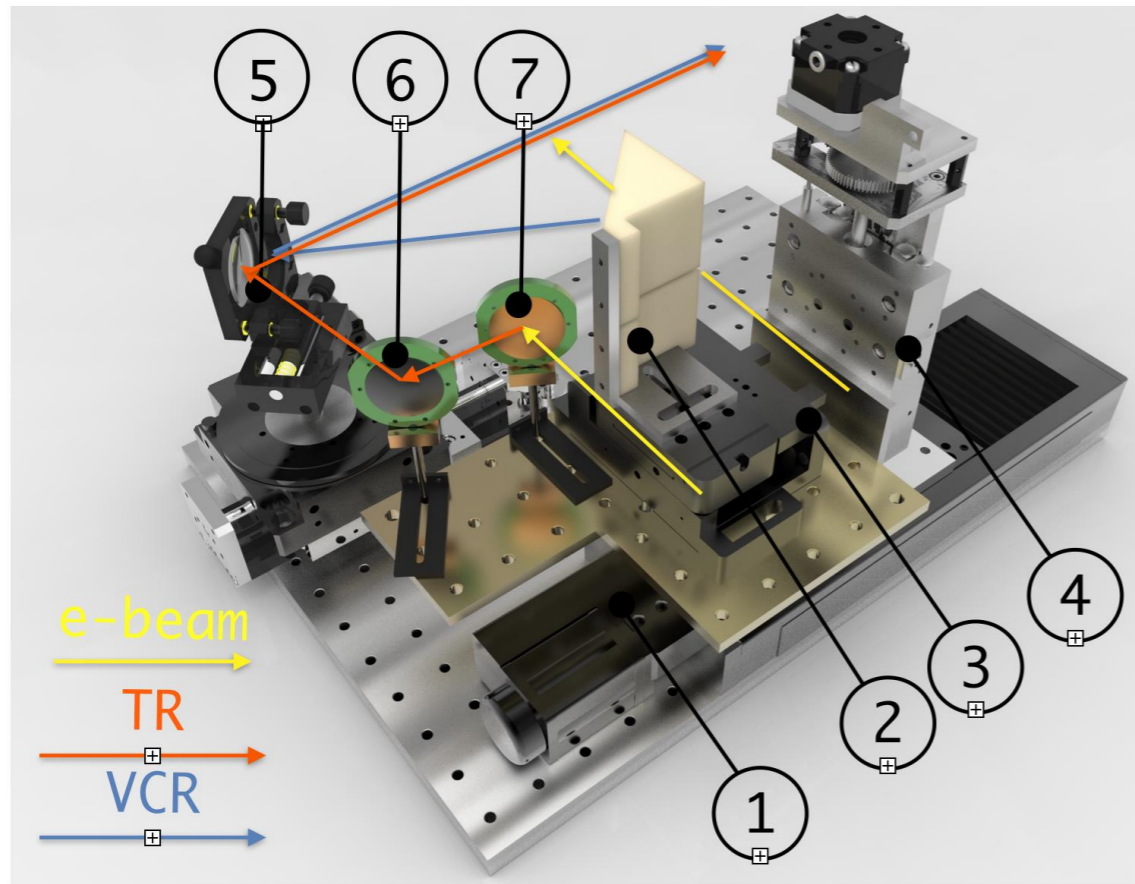


Fig. 5 VCR Spectrum for different detector apertures

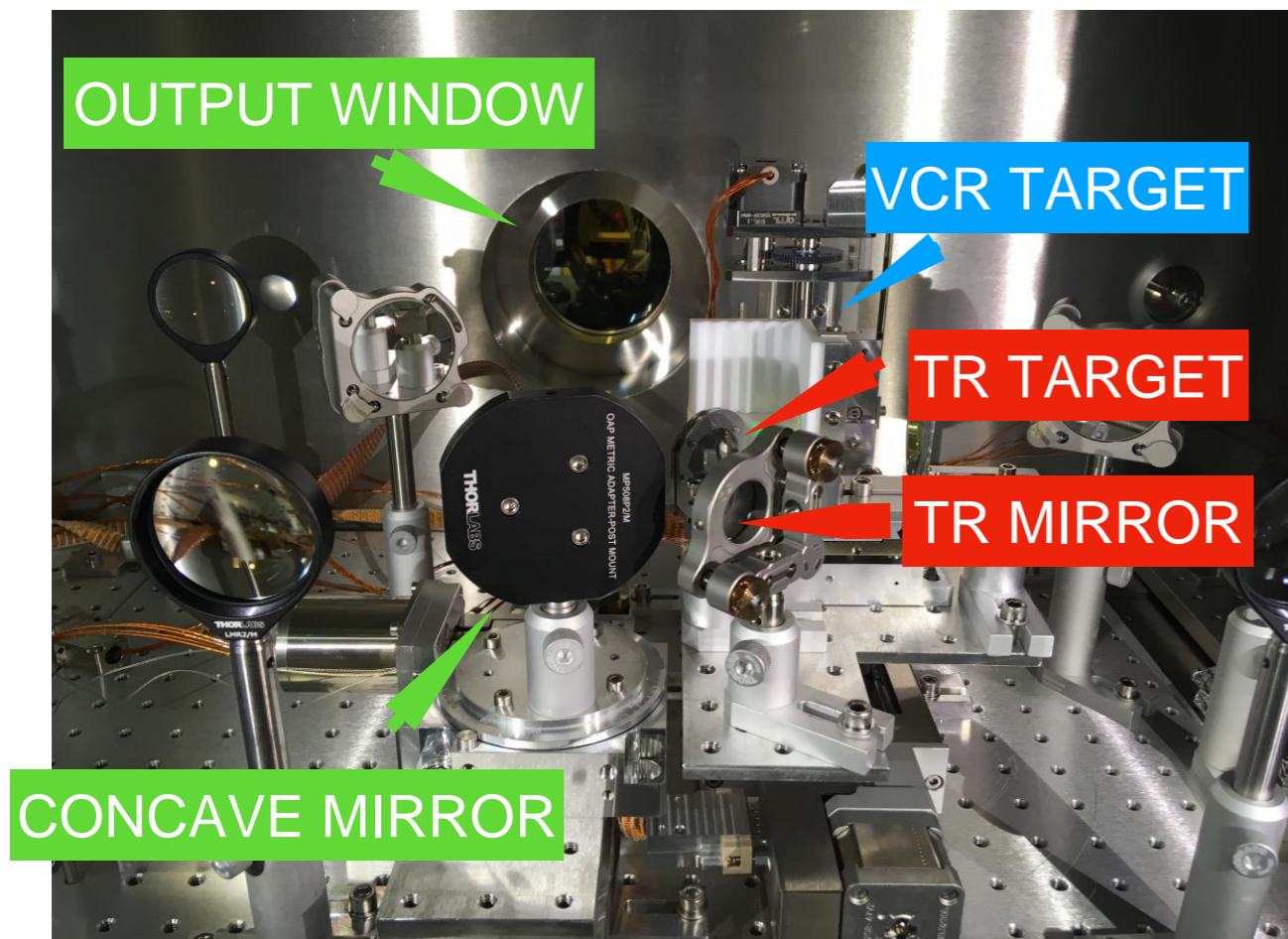
Experimental work at CLARA



Setup inside of chamber

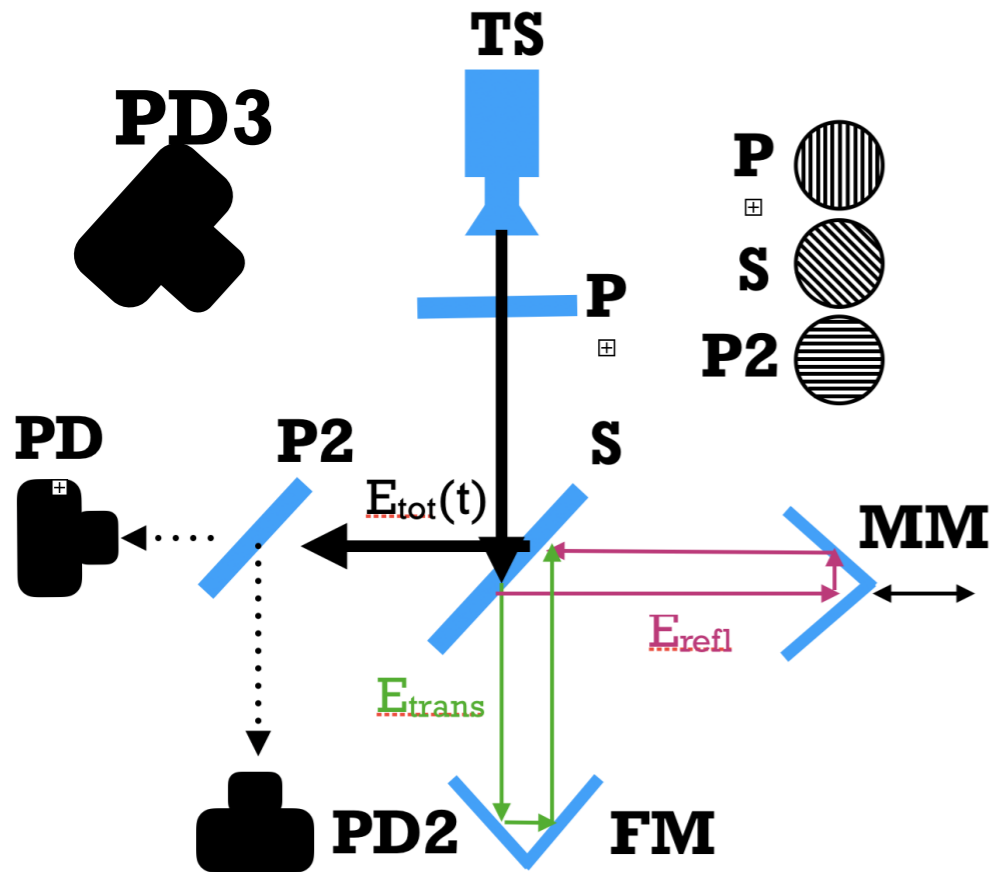


- 1 — Horizontal positioning stage
- 2 — Teflon (VCR) target
- 3 — Tip-Tilt stage
- 4 — Vertical positioning stage
- 5 — Concave mirror
- 6 — mirror
- 7 — Foil (TR) target



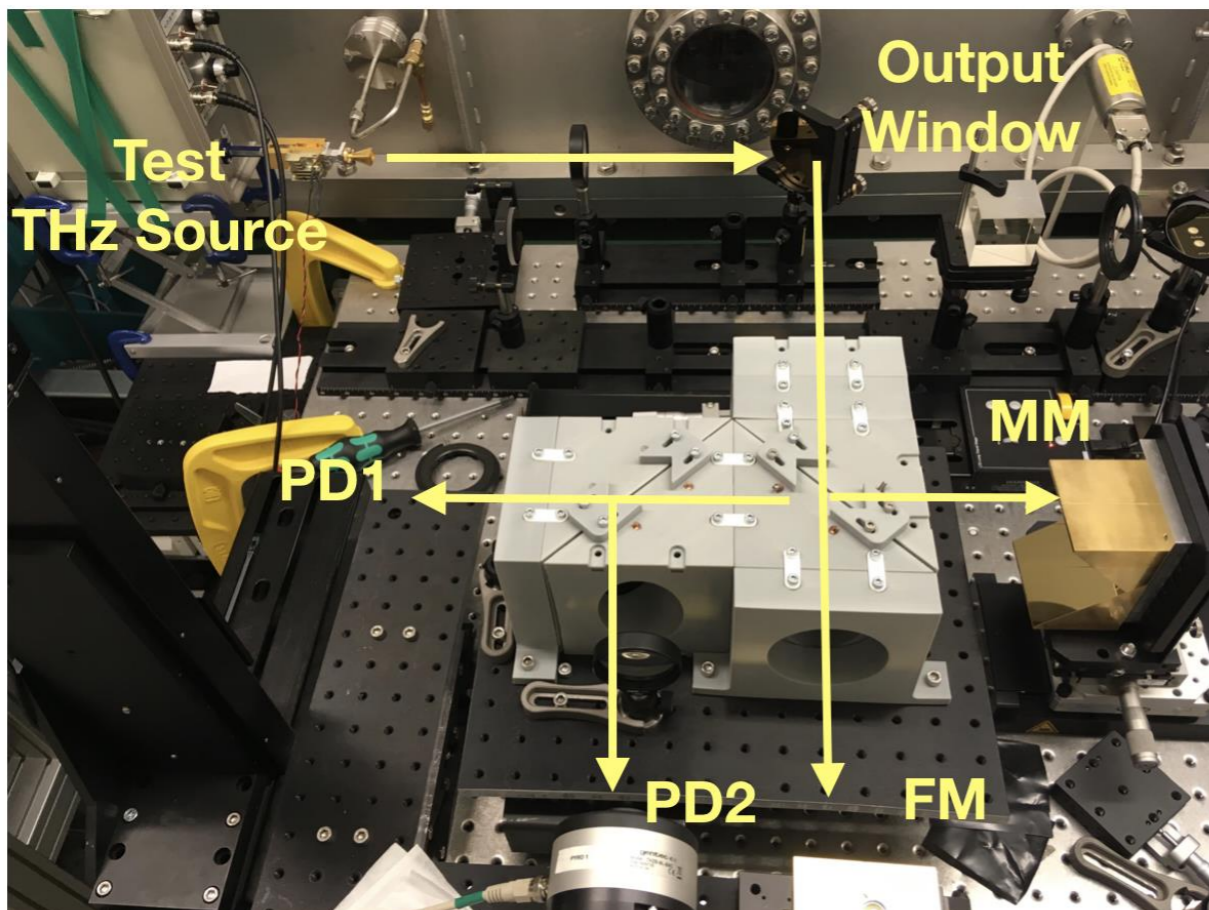
- Setup inside of vacuum chamber allows us to register VCR and TR during single accelerator run.

MPI Interferometer



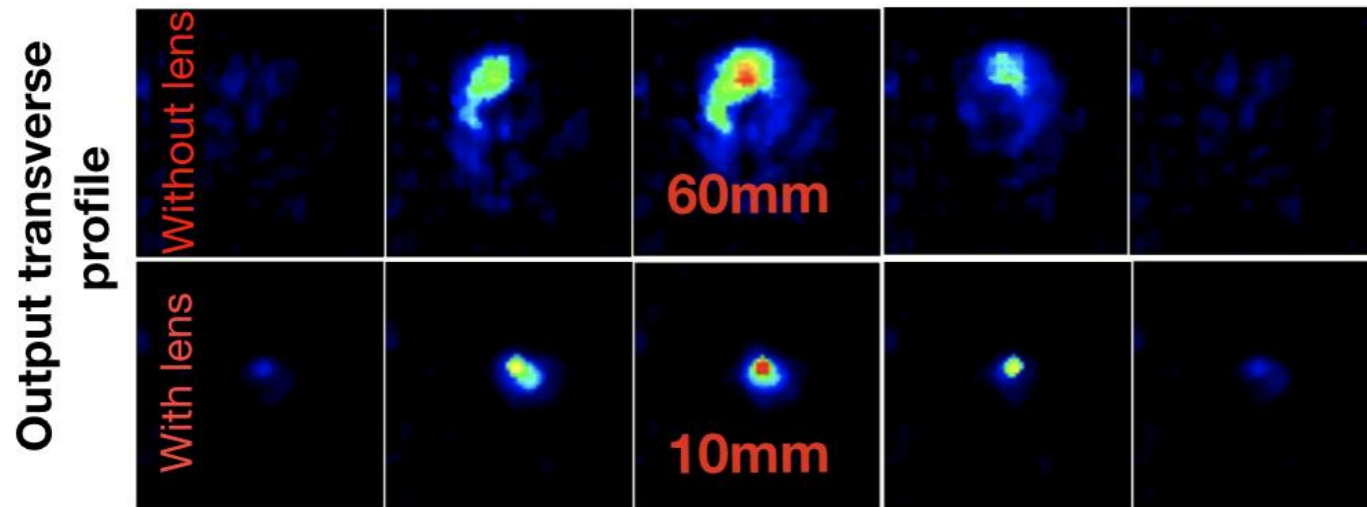
Martin-Pupplet interferometer has a higher signal to noise ratio and there is possibility to use two different output and make a noise normalisation:

$$I(x) = \frac{U_h(x) - U_v(x)}{U_h(x) + U_v(x)}$$



MPI precise alignment

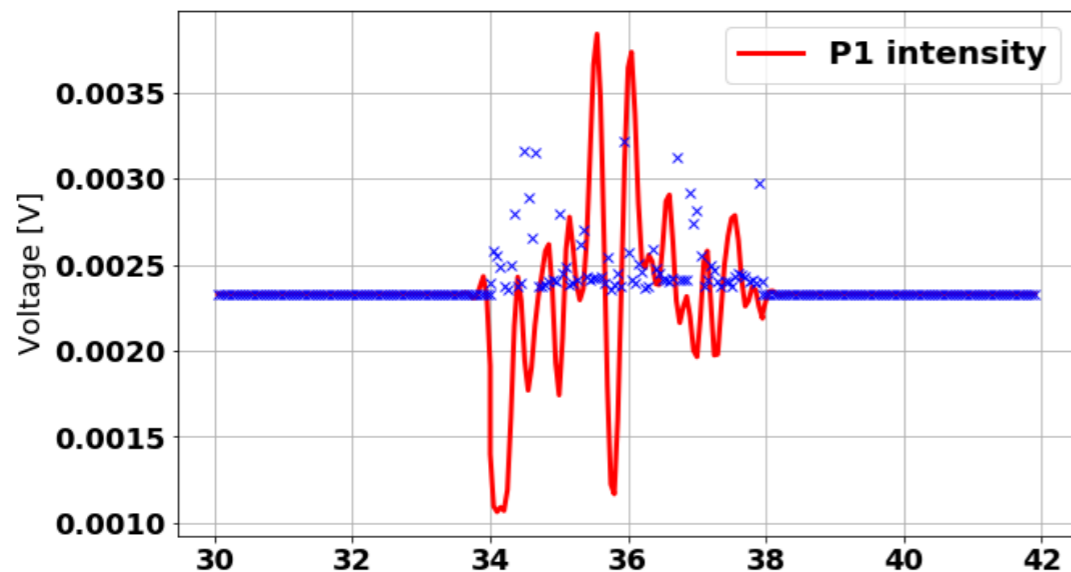
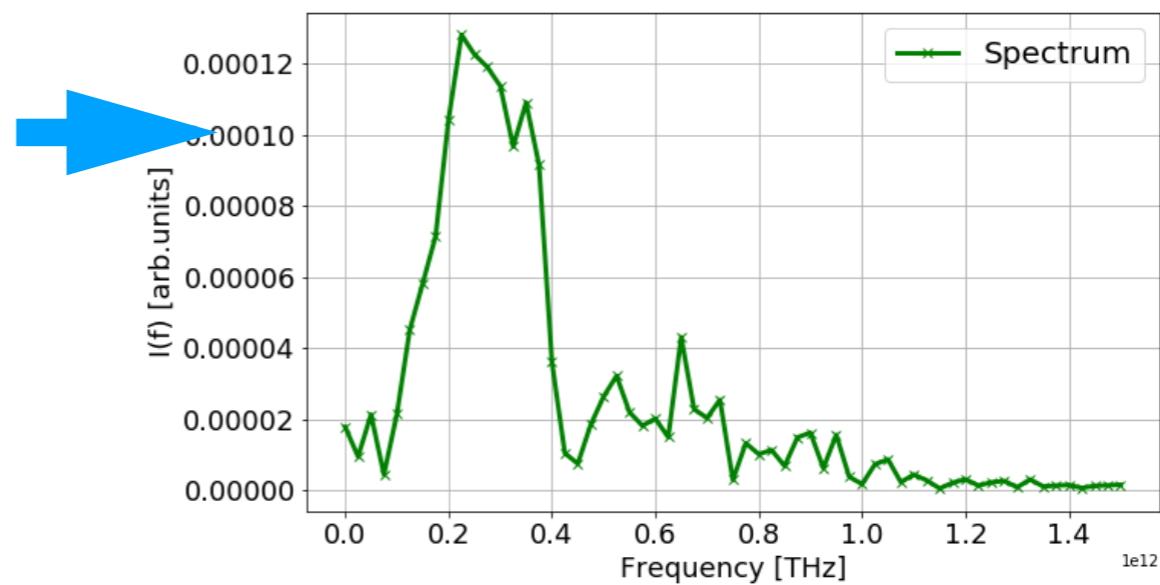
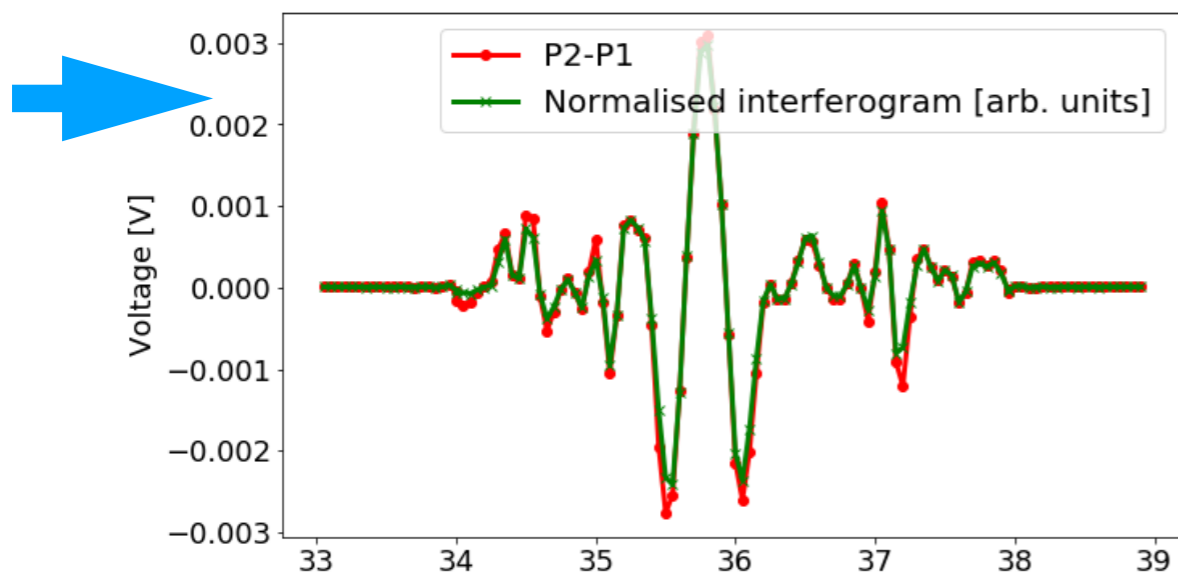
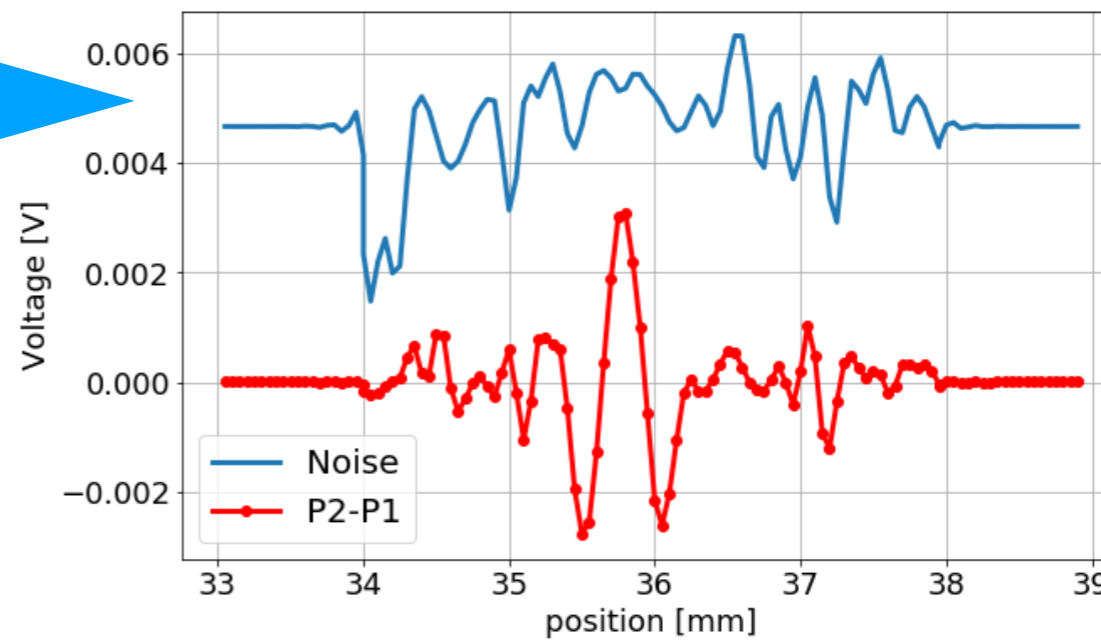
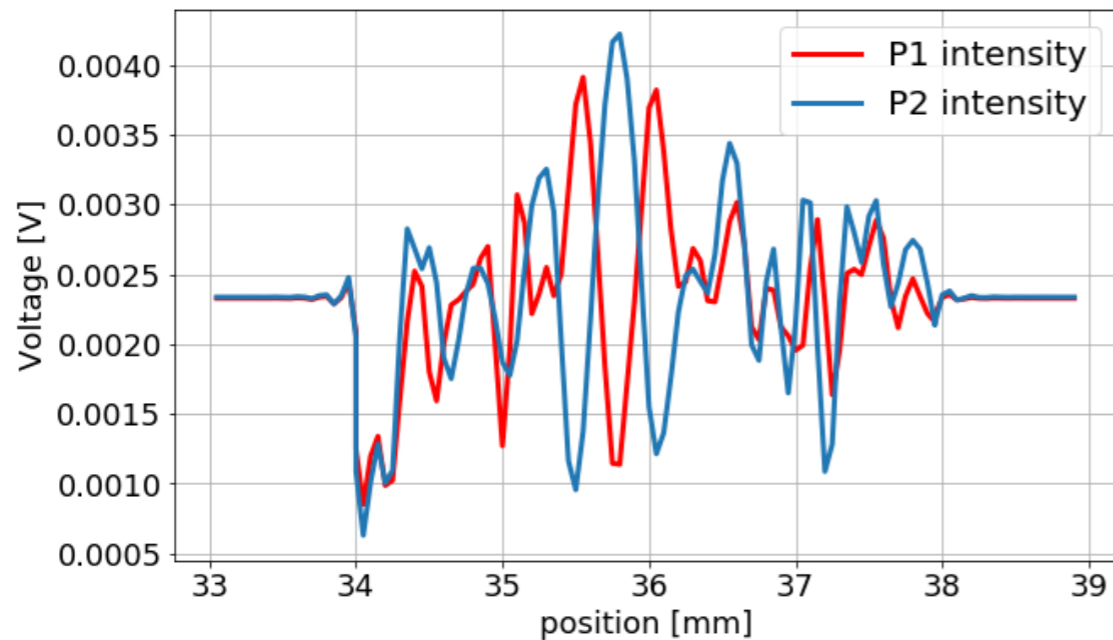
By using THz camera and test THz source we were able to align interferometry system with good precision.



- Frequency range: 10 GHz — 1THz;
- 4096 pixels (64 x 64 array)
- 1.5mm pixel pitch
- Framerate, exposure and accumulation control
- NEP=1nW/sqrt(Hz)

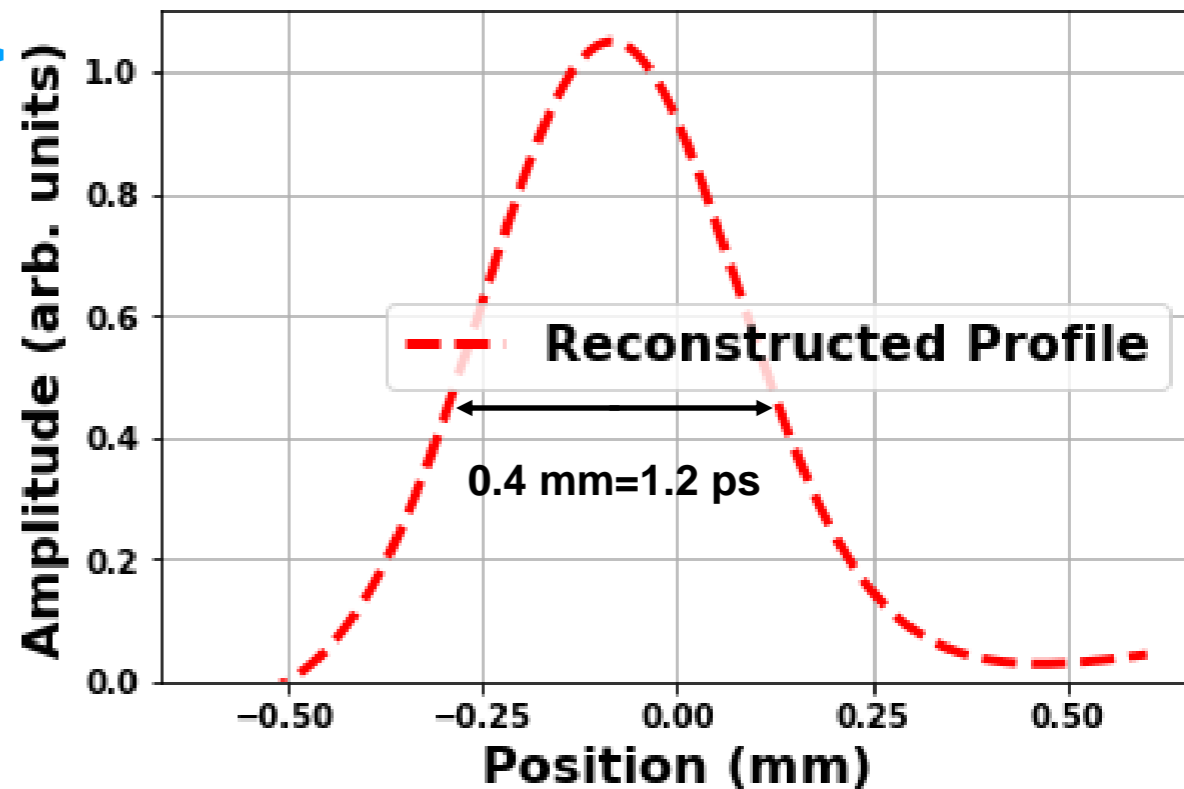
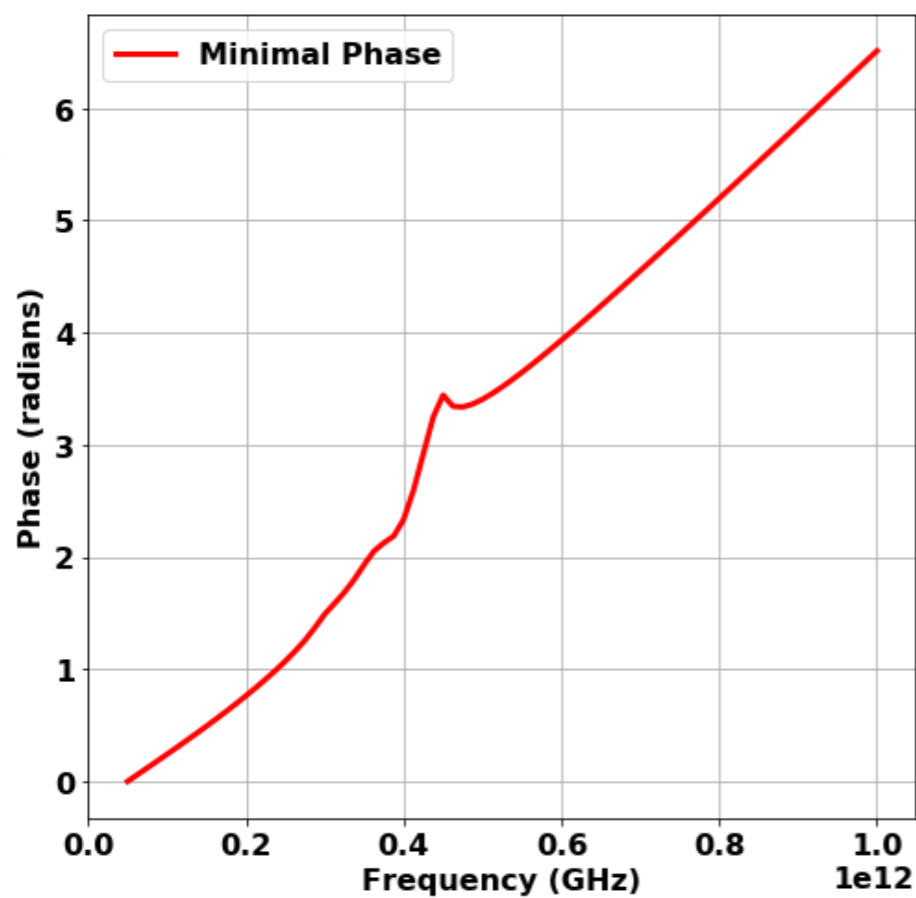
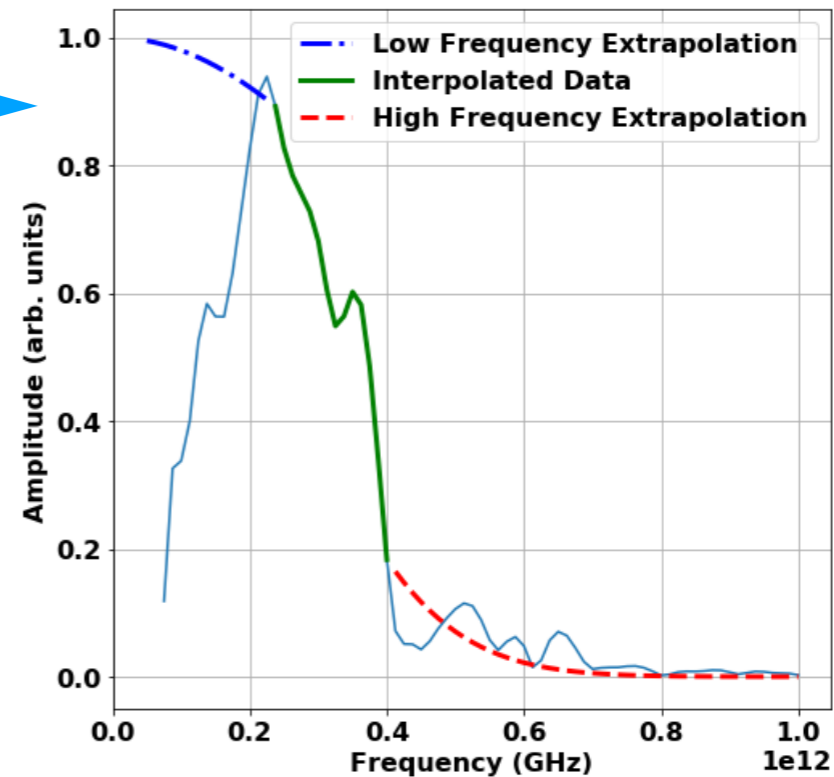
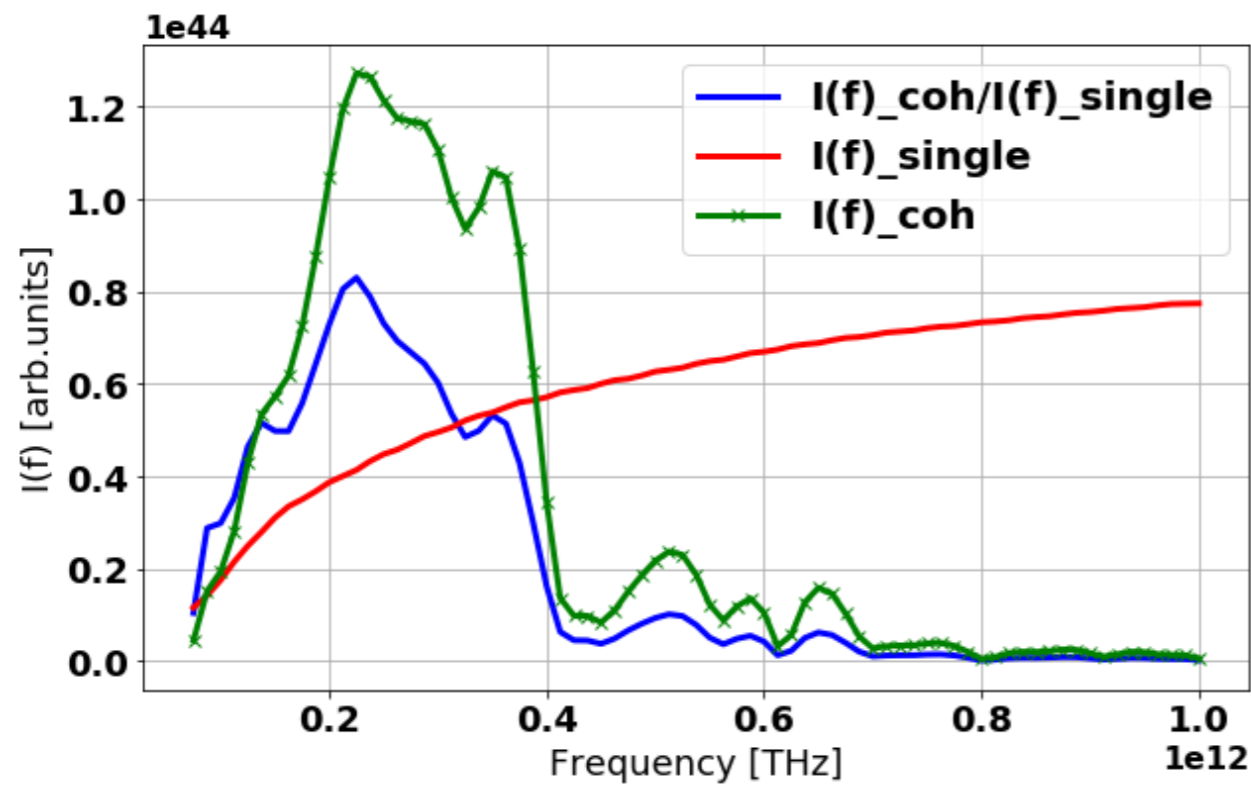
Experimental results:

CCR, $h=2\text{mm}$, 80-70pC, 200 microns RMS transversal bunch size, $E=40\text{MeV}$

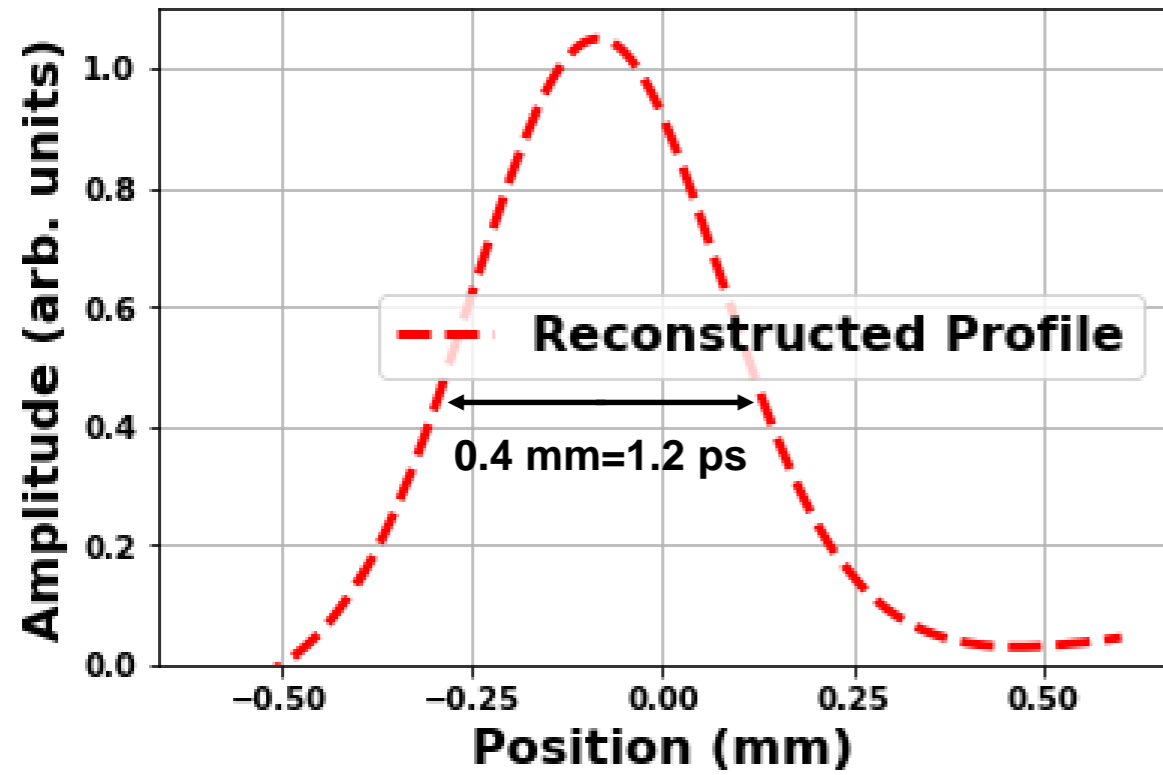


- Error bar
- Appodization
- Filtering

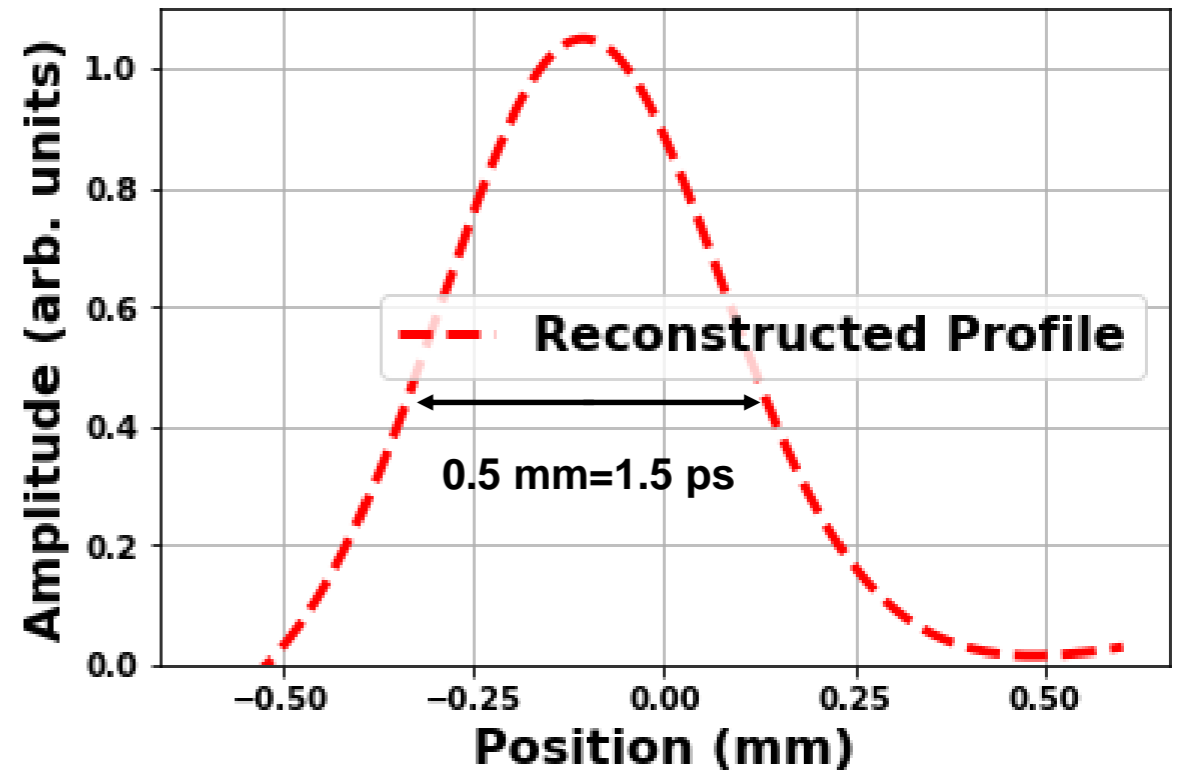
Experimental results



Experimental results. Two different klystron phase



-6deg



-11deg

Conclusion

- **Set of data for CTR for different klystron phases**
 - **Set of data for CCR for different klystron phases**
 - **CCR vs impact parameter (distance between target and beam)**
 - **CCR vs target-beam angle**
-
- **Improve optical alignment**
 - **Optics for lower frequencies**
 - **Quasi-optical detector (with higher sensitivity)**

Thank you for your attention!