



# Laser pulse evolution in non-linear plasma wakefield accelerators

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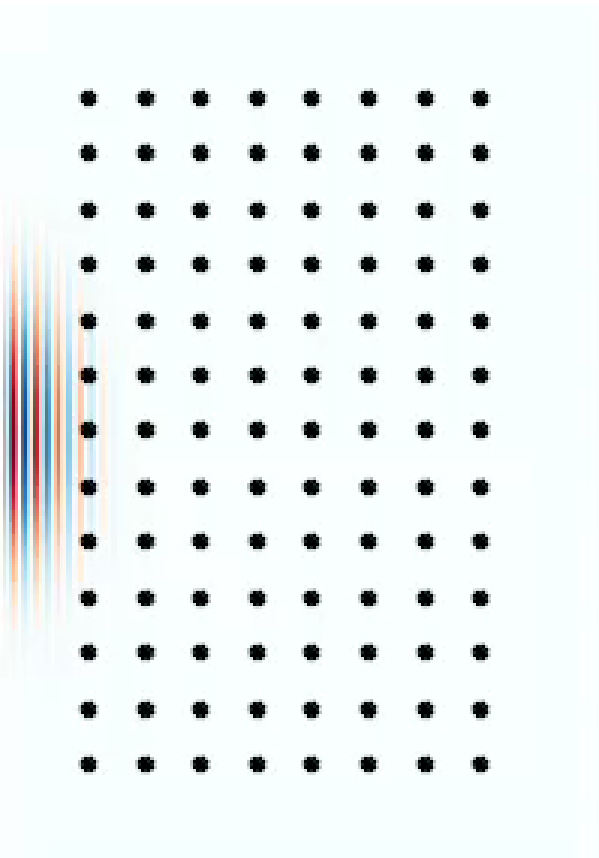
John Adams Institute for Accelerator Science, Imperial College London

Stating the obvious....

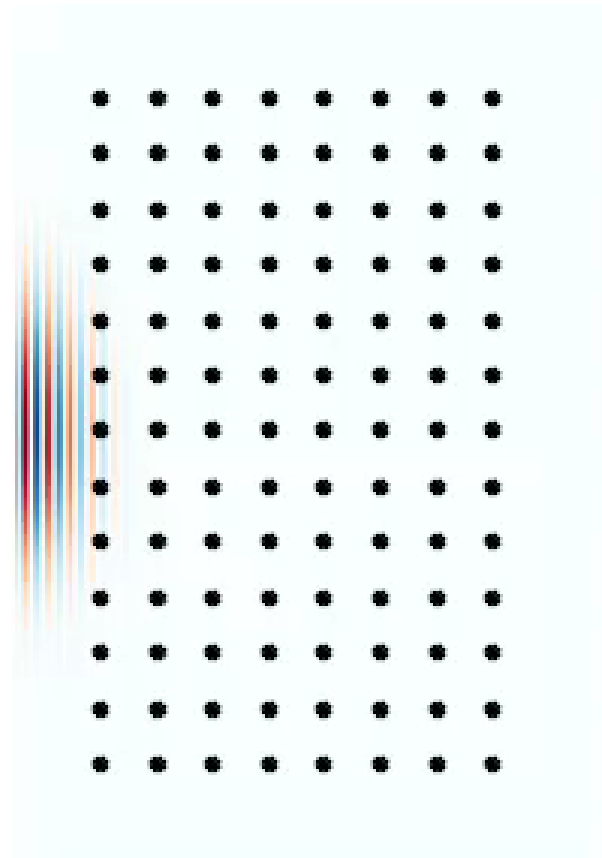
The plasma wave is generated by the drive laser

$$a_0 = \frac{eE_0}{\omega m_e c}$$

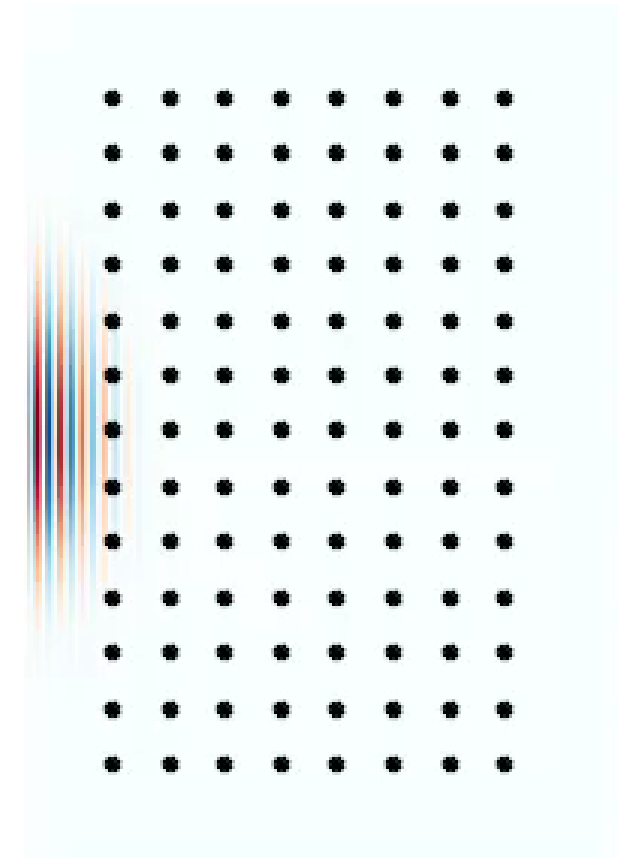
$$a_0 = 1$$



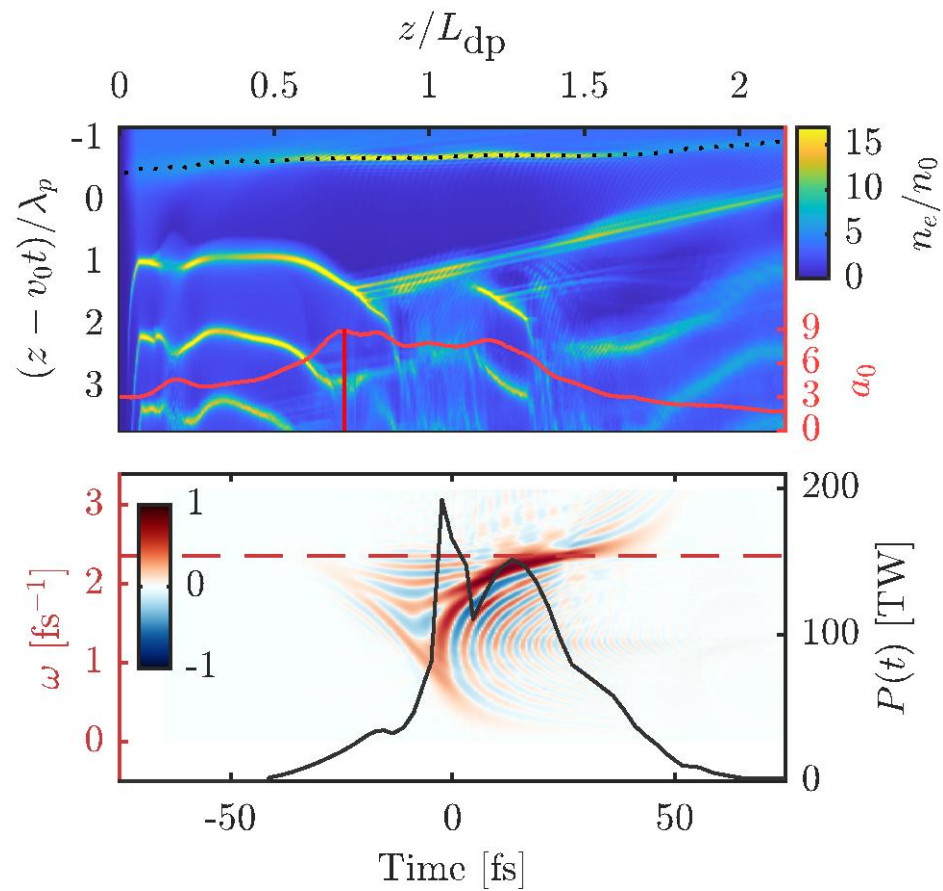
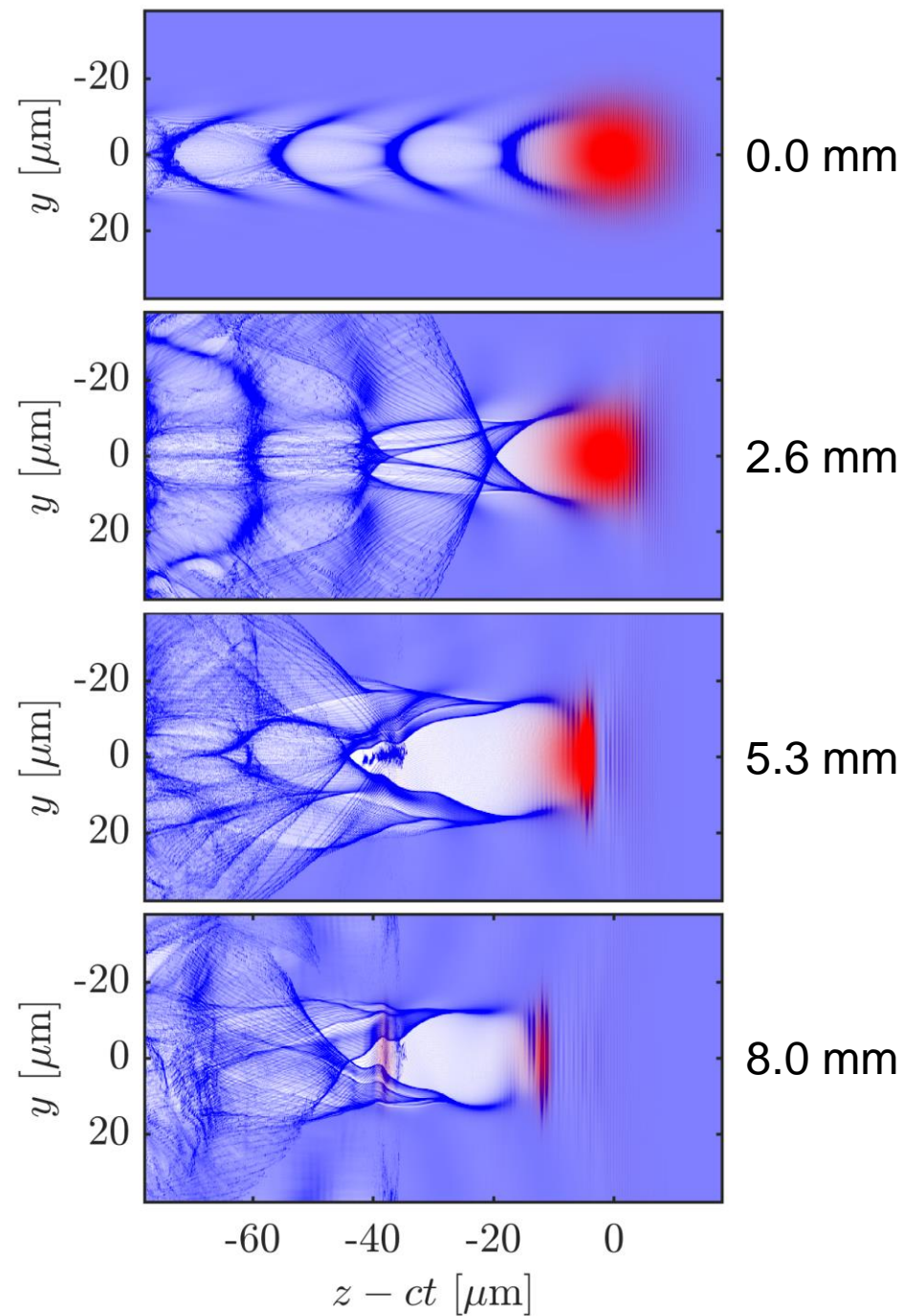
$$a_0 = 2$$



$$a_0 = 4$$



# The plasma response modifies the laser pulse



# Redshifted photons travel slower than the pulse front and cause power amplification

Group velocity of far redshifted photons can be less than the reduced group velocity of the laser

$$v_g(1) = v_g(0) - v_{\text{etch}}$$

$$c\sqrt{1 - \frac{\omega_p^2}{\omega_1^2}} = c\sqrt{1 - \frac{\omega_p^2}{\omega_0^2}} - \frac{\omega_p^2}{\omega_0^2}$$

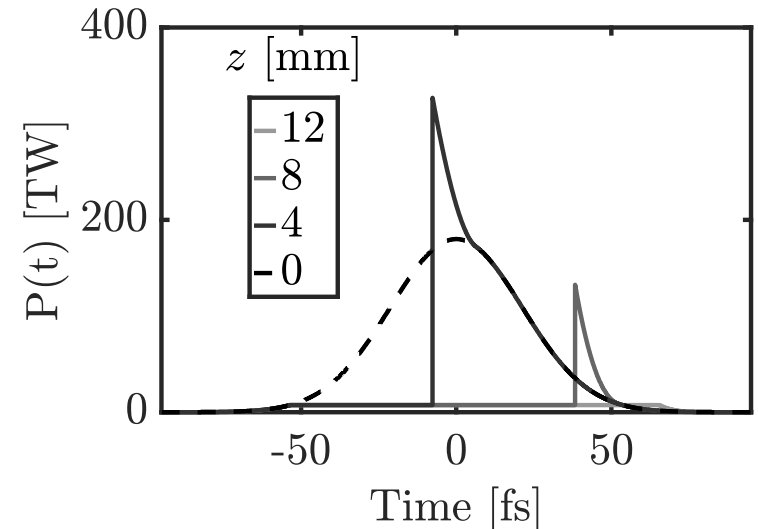
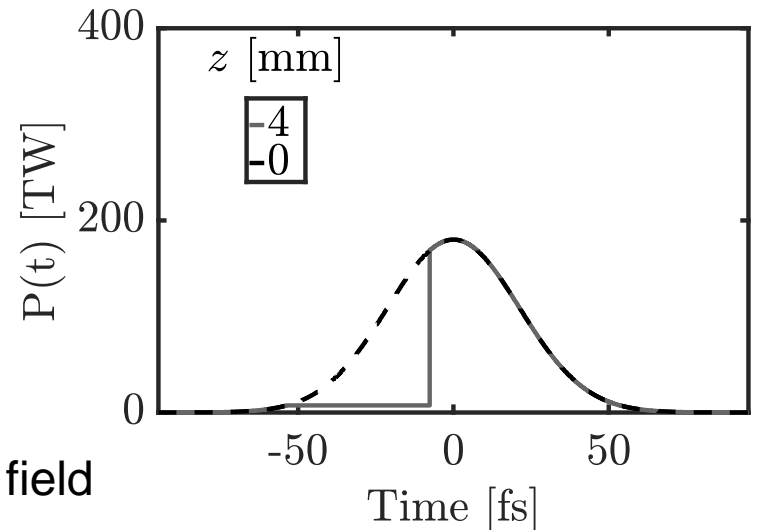
$$\omega_1 = \frac{\omega_0}{\sqrt{3}}$$

These photons drift backwards and contribute to field behind the depletion region

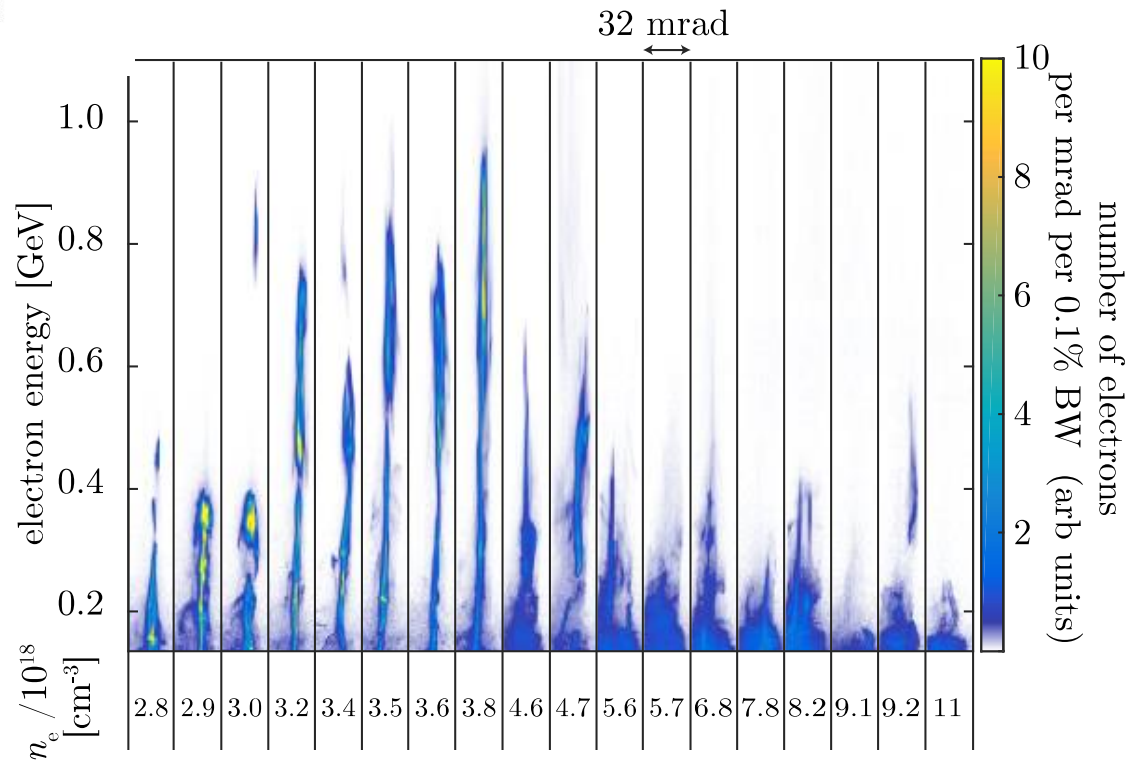
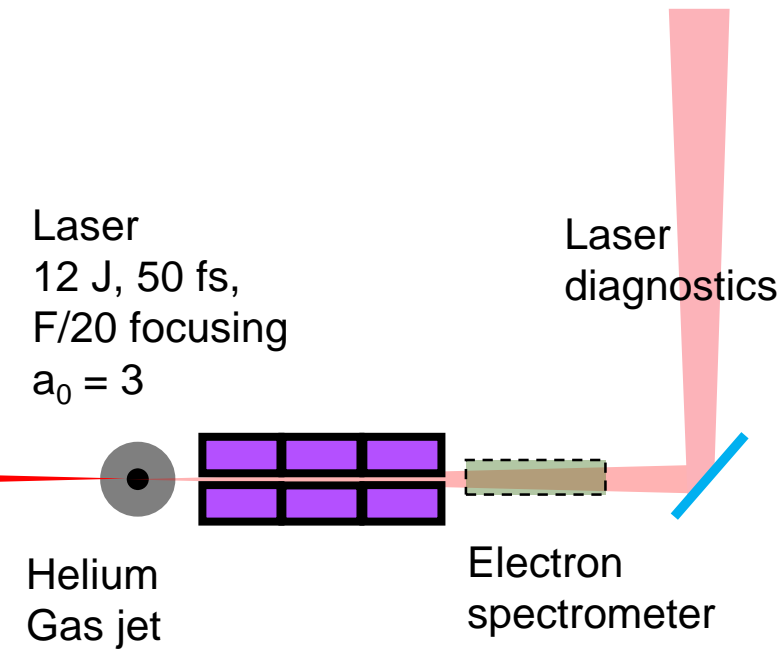
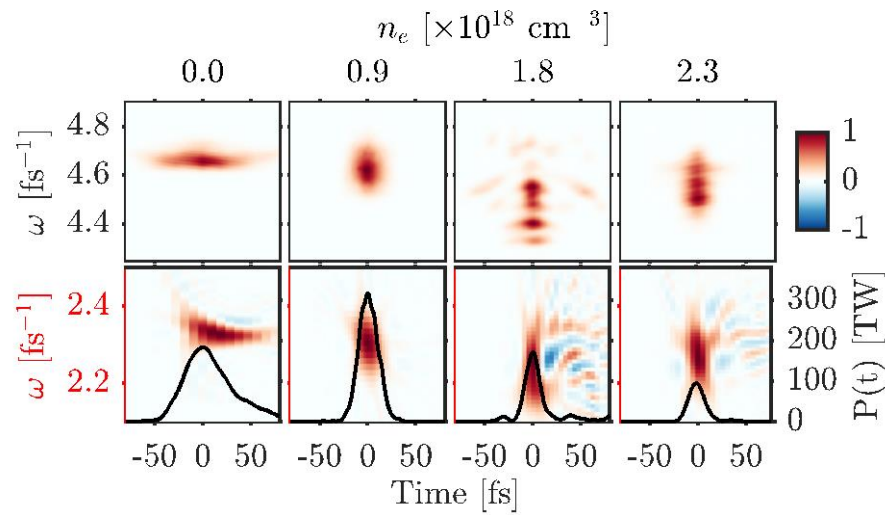
Pre-Injection Pulse Evolution length  
For a gaussian pulse=:

$$L_{\text{evol}} \approx \sigma_t c \left( \frac{2 \omega_0^2}{3 \omega_p^2} \right) \sqrt{\frac{1}{2} \ln \left( \frac{P_0}{P_c} \right)}$$

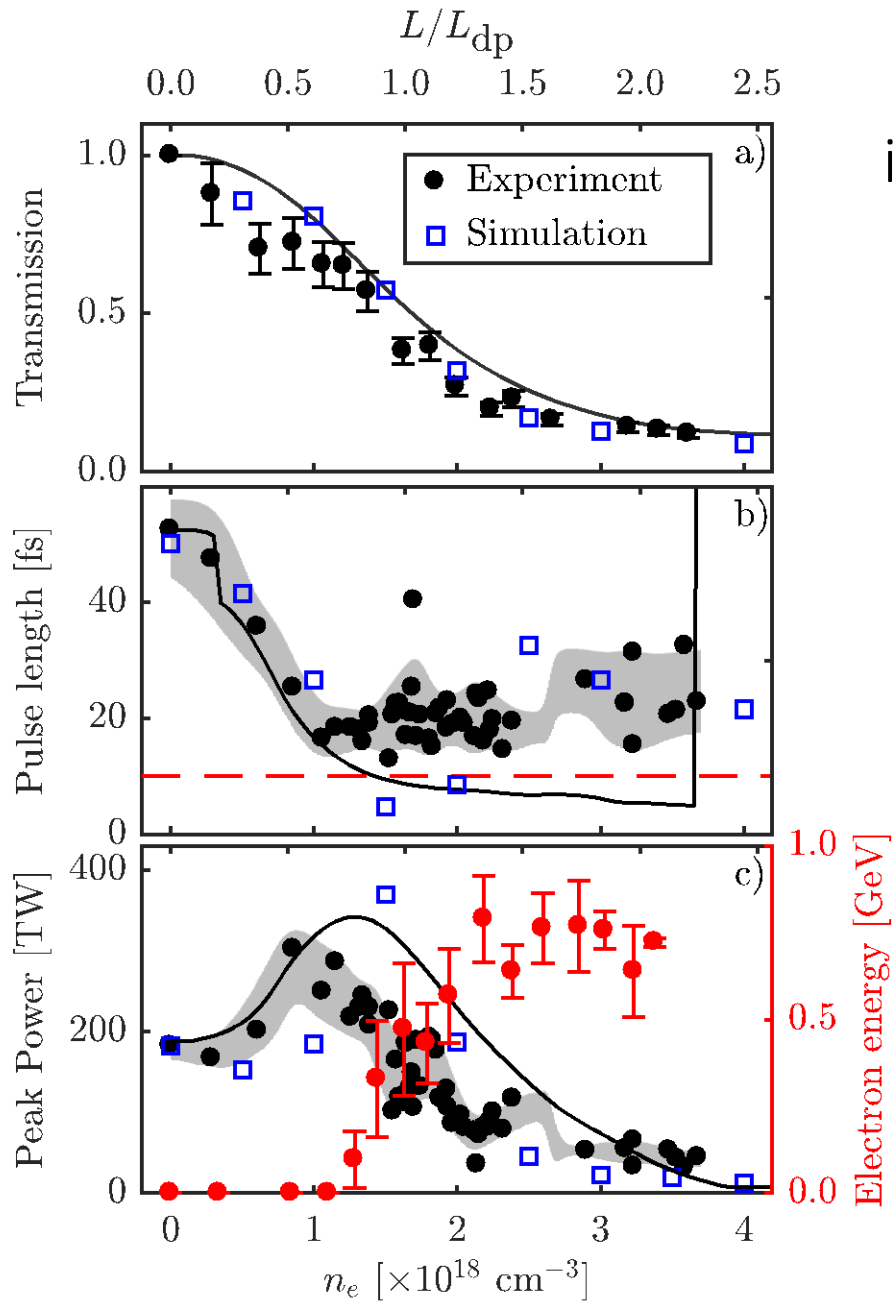
$$L_{\text{dp}} \approx 2L_{\text{evol}}$$



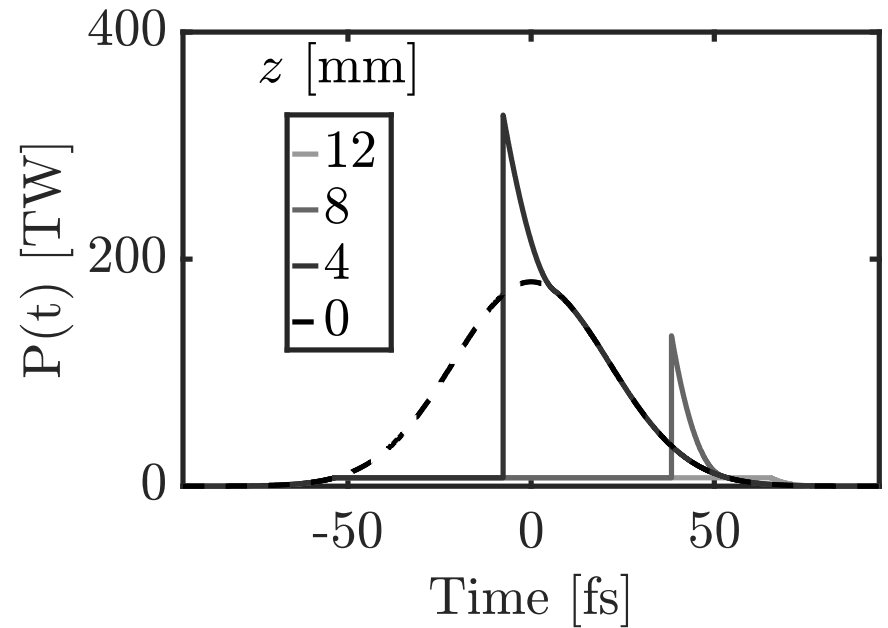
# An experiment to study laser, electron and x-ray beams simultaneously



# Laser evolution determines self-injection and acceleration behavior

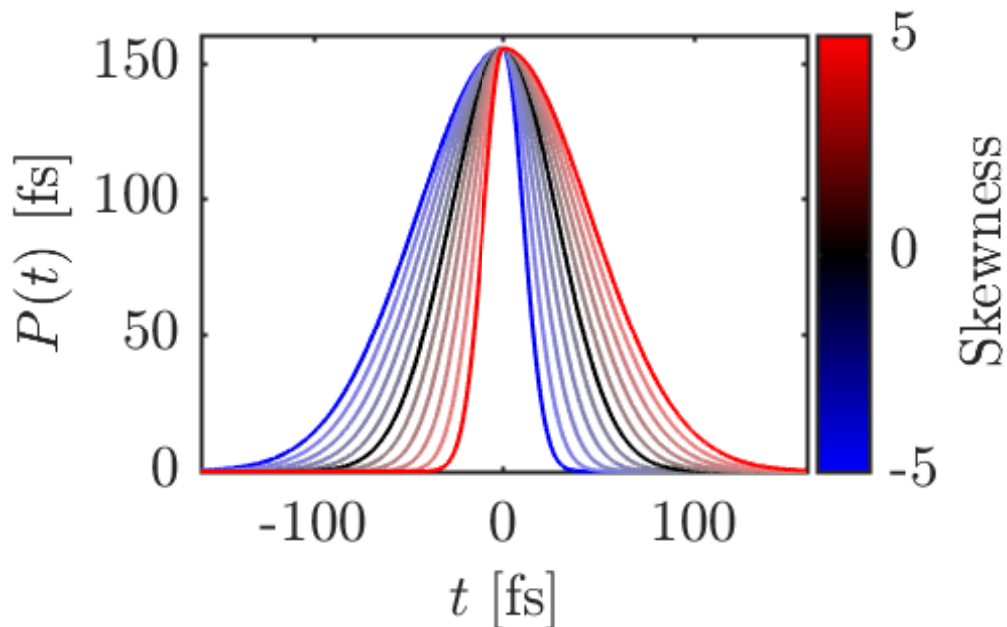


### Model of laser evolution

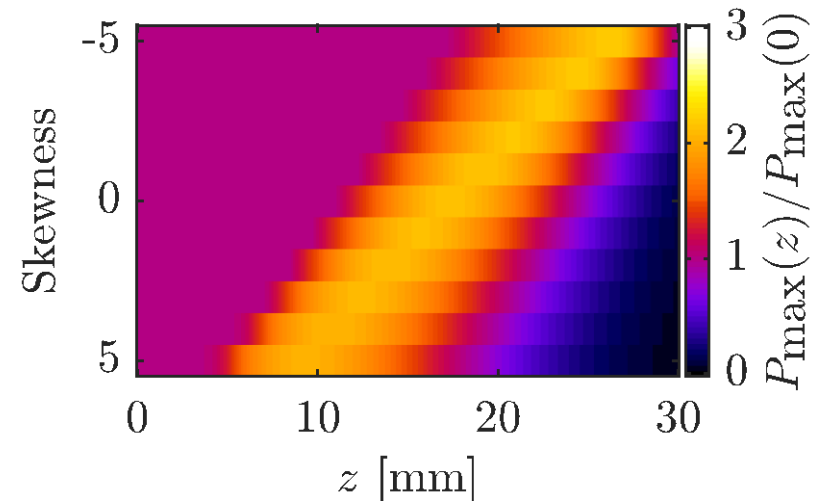


# Controlling the laser evolution by shaping the initial pulse profile

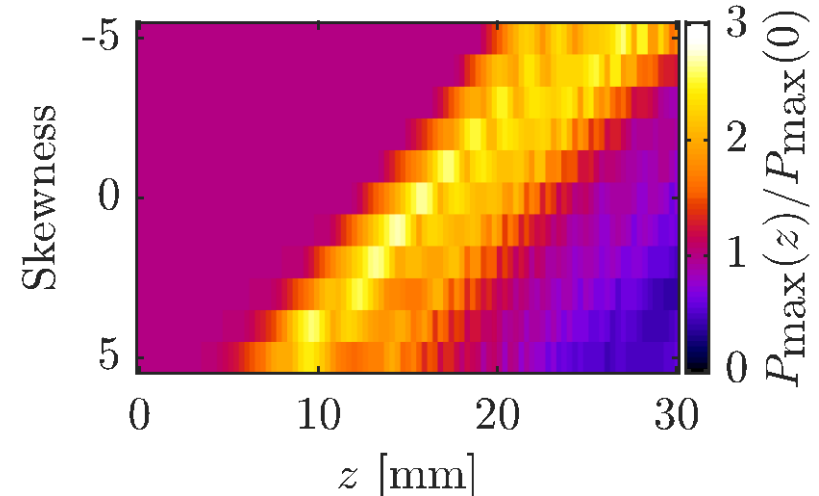
Input laser pulse shapes



Model prediction

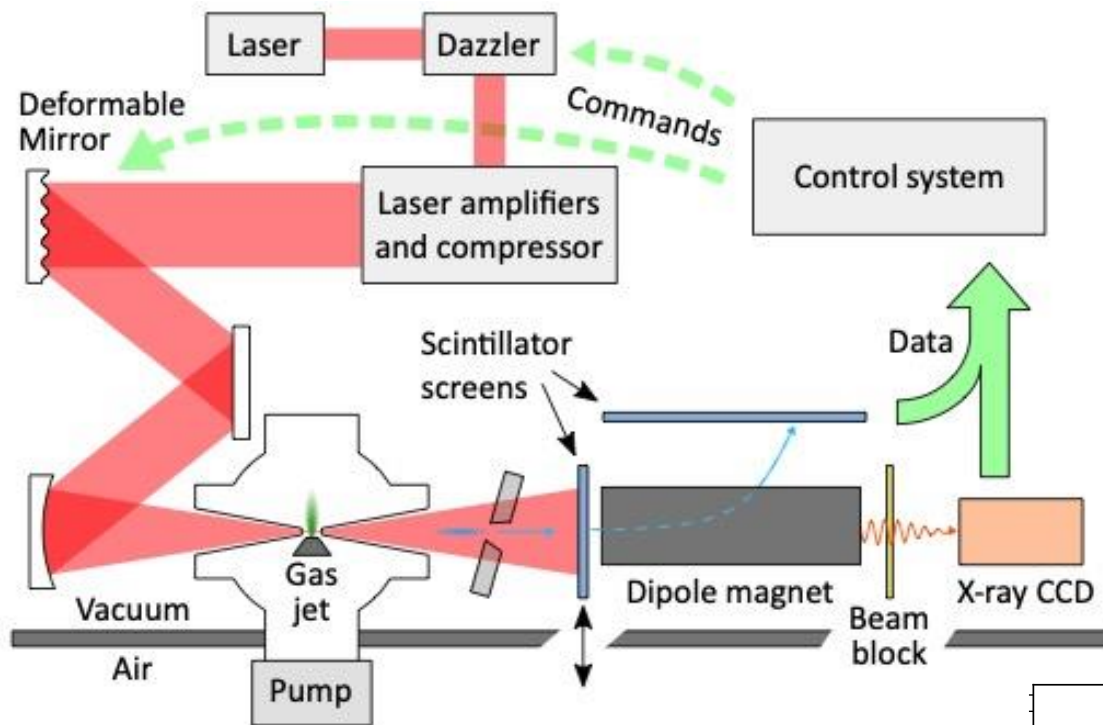


1D PIC simulations

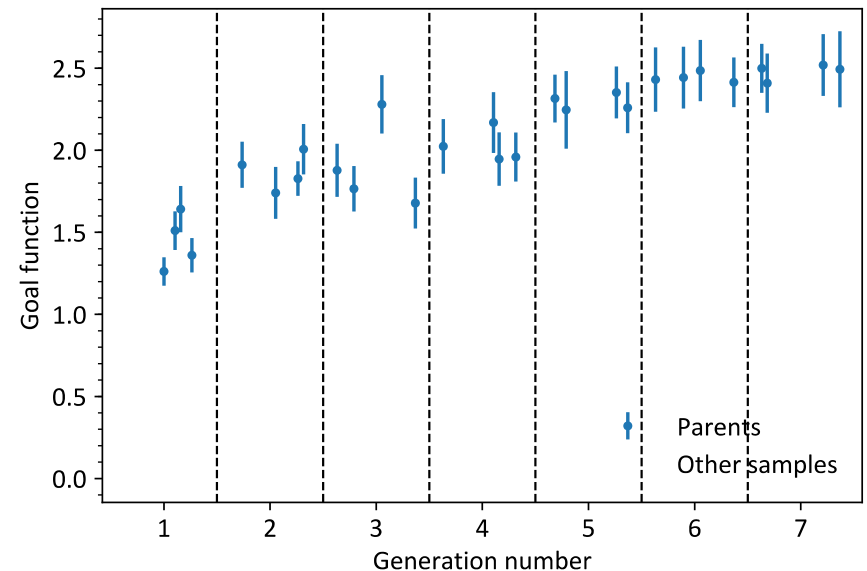
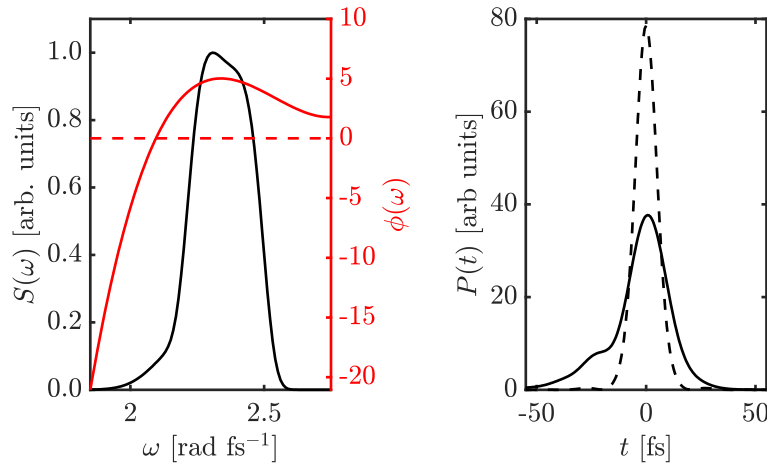


Electron density for calculations and simulations

$$n_e = 2 \times 10^{18} \text{ cm}^{-3}$$



Using active feedback to optimize laser pulse shape



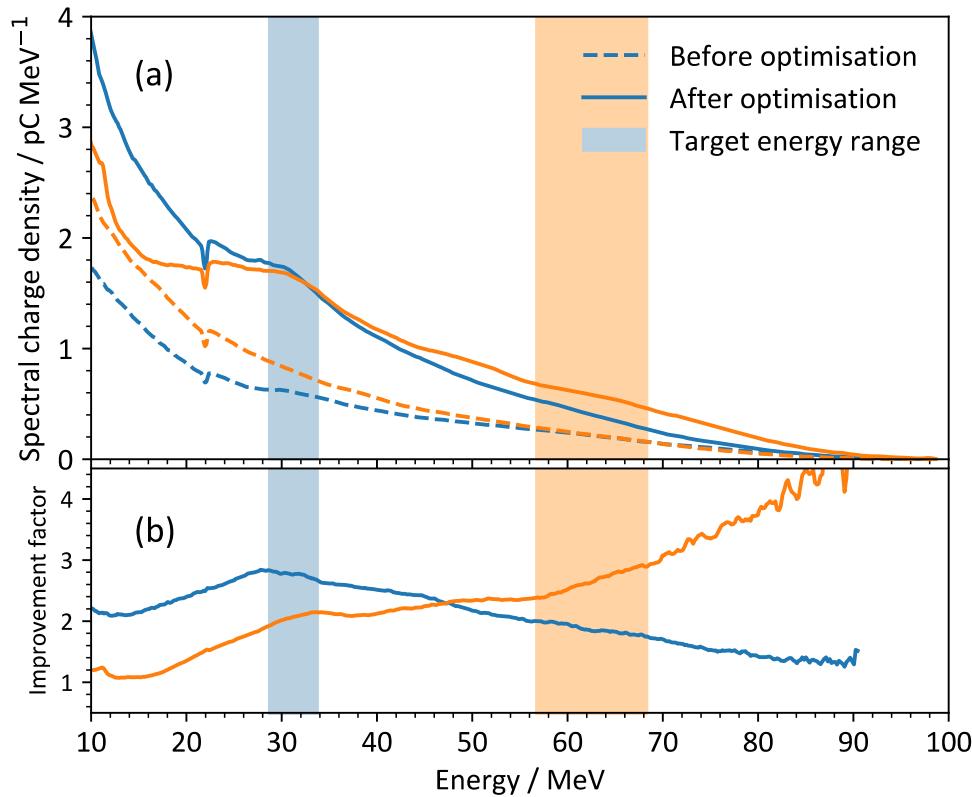
Streeter, M. J. V., et al. (2018). *Applied Physics Letters*, 112(24), 244101. <https://doi.org/10.1063/1.5027297>

Dann, S. J. D. et al (2018) *In prep for submission*

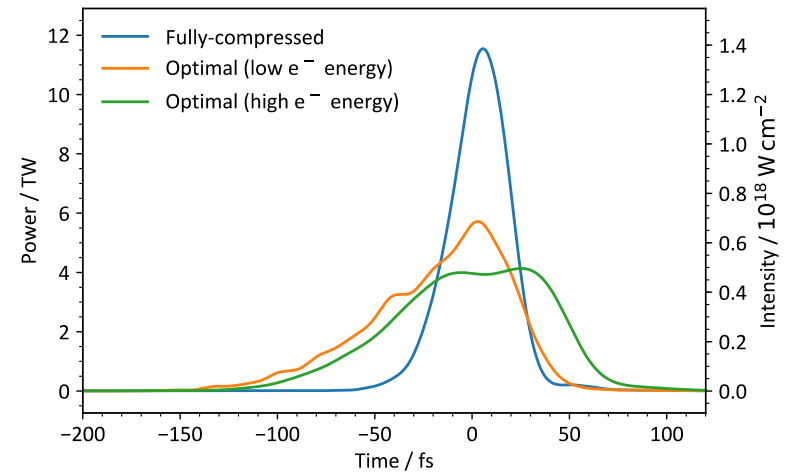


# Algorithm autonomously improved electron spectrum through control of initial pulse shape

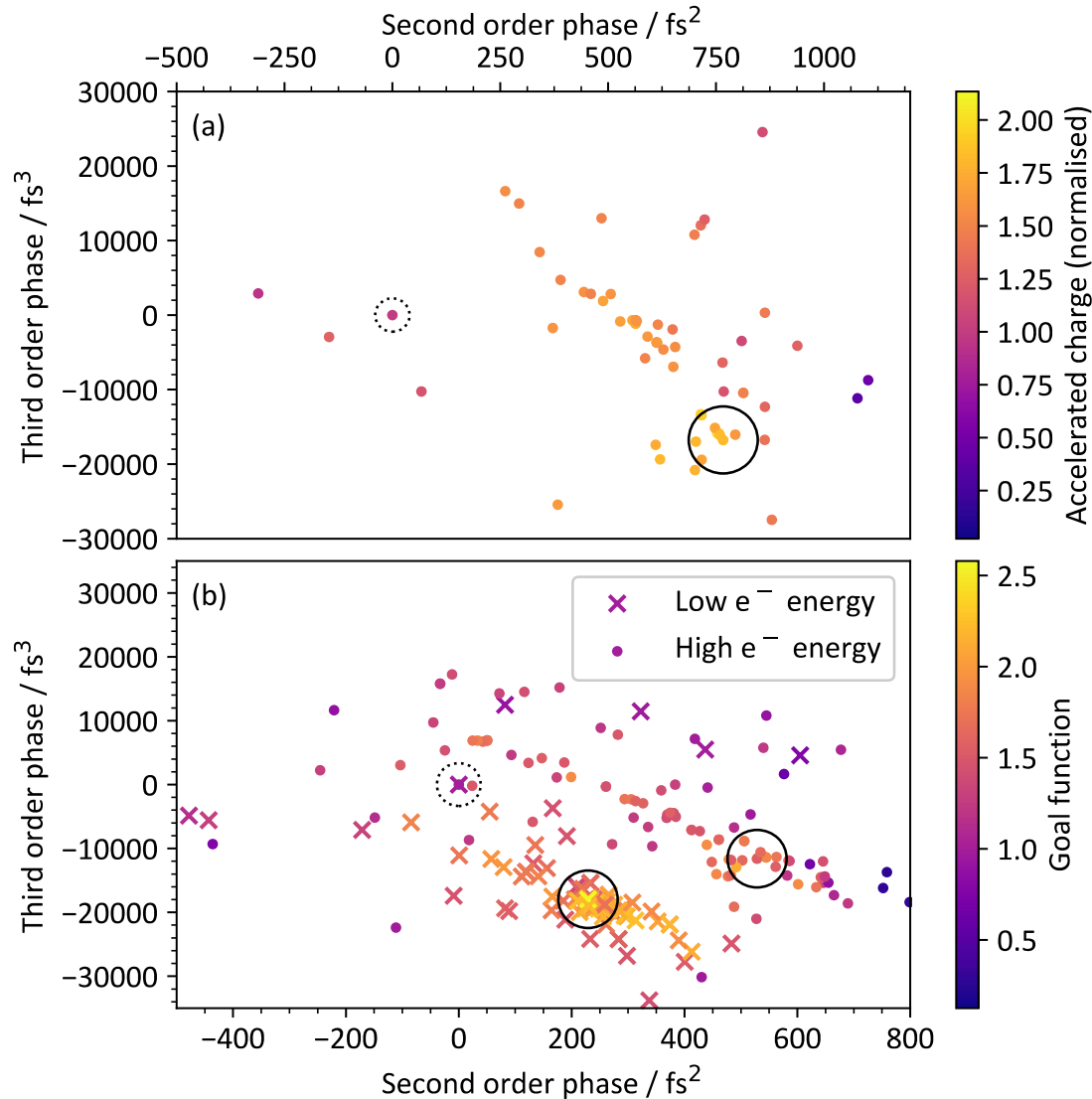
## Electron spectrum before and after



## Fully compressed pulse shape and optimized cases



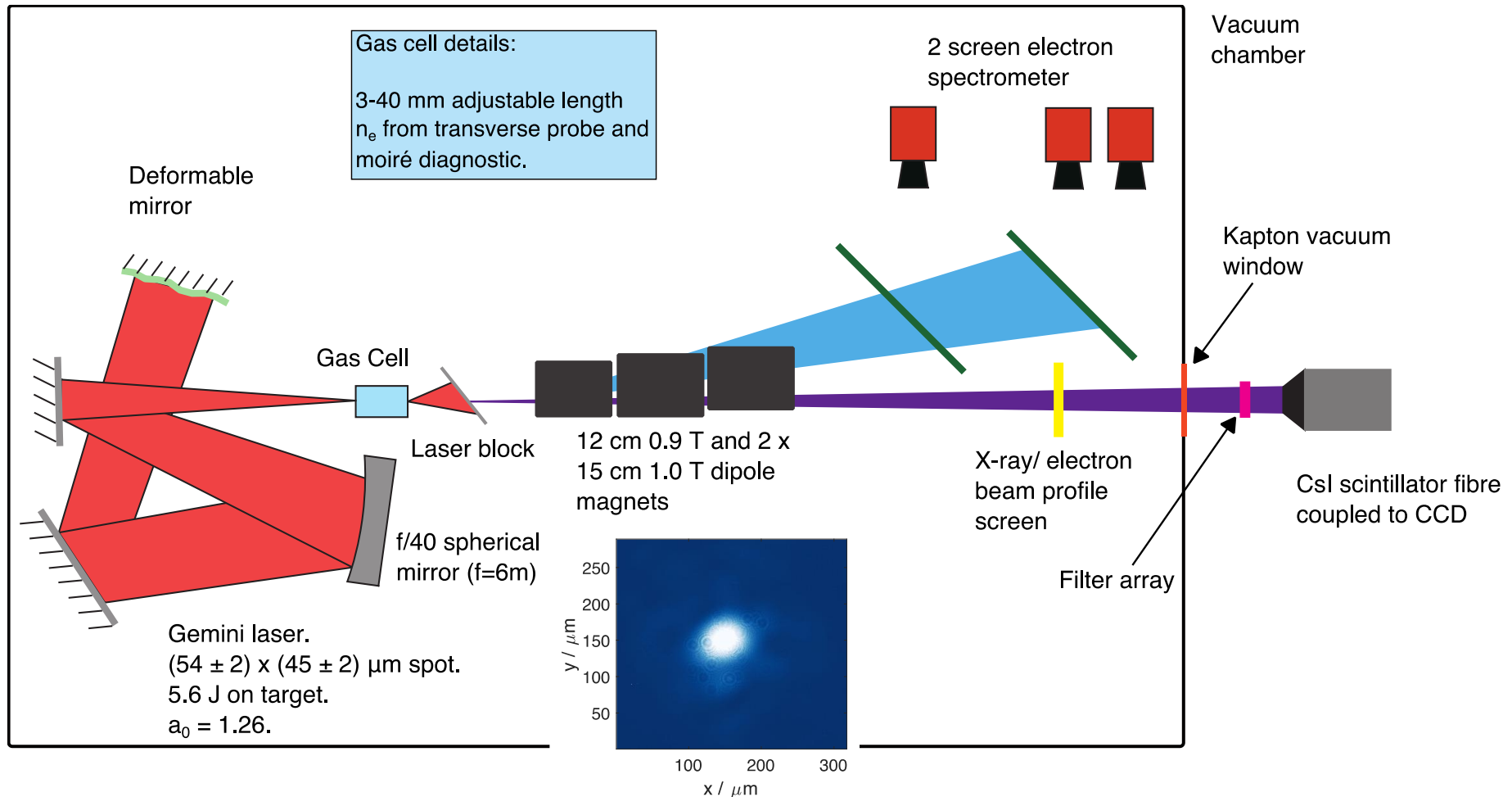
# Machine learning used to explore multi-dimensional parameter space and identify interesting regions for further study



Streeter, M. J. V., et al. (2018). *Applied Physics Letters*, 112(24), 244101. <https://doi.org/10.1063/1.5027297>

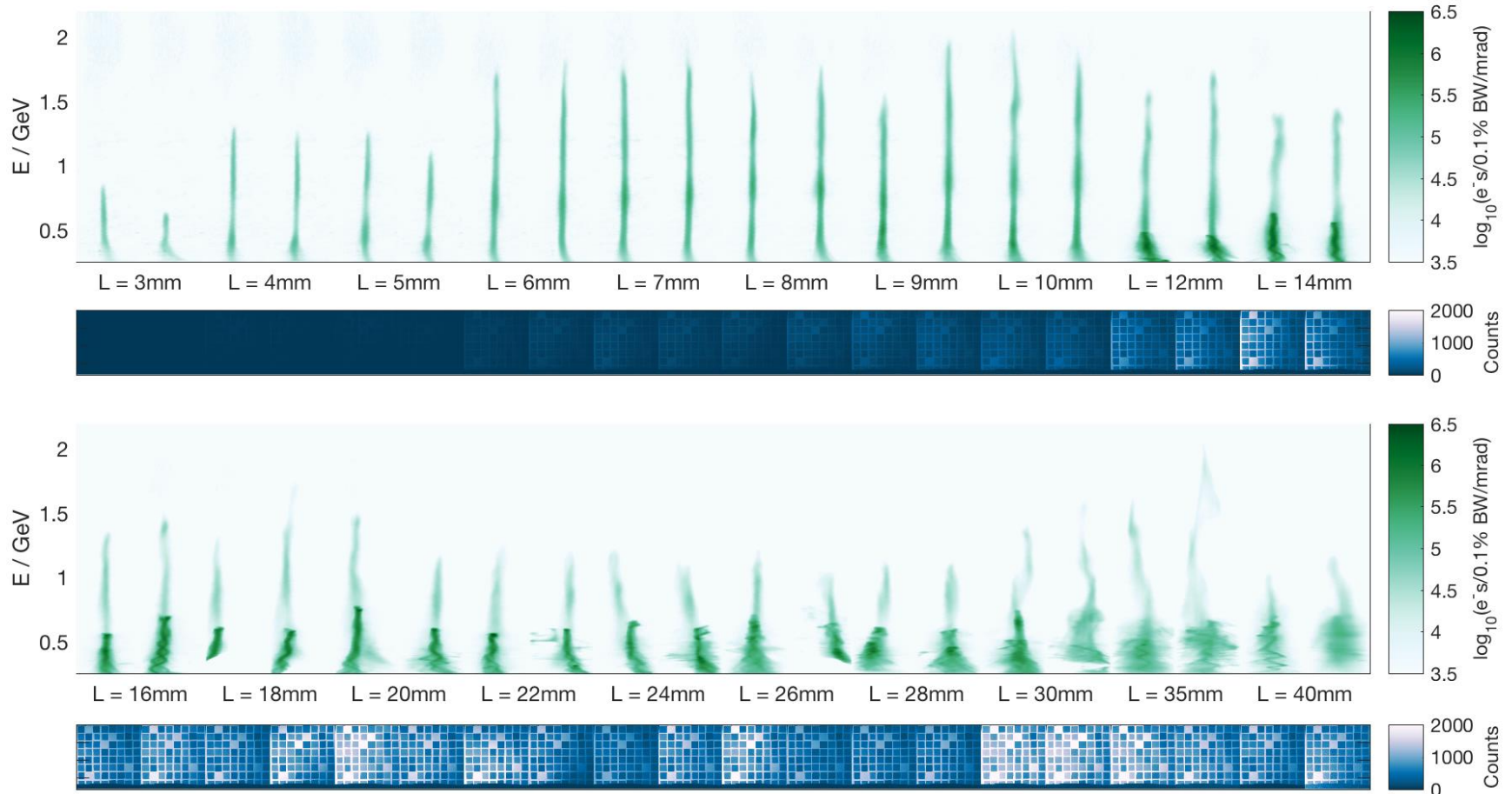
Dann, S. J. D. et al *In prep for submission*

# Experiment with Long Focal Length focusing optic and variable length gas cell

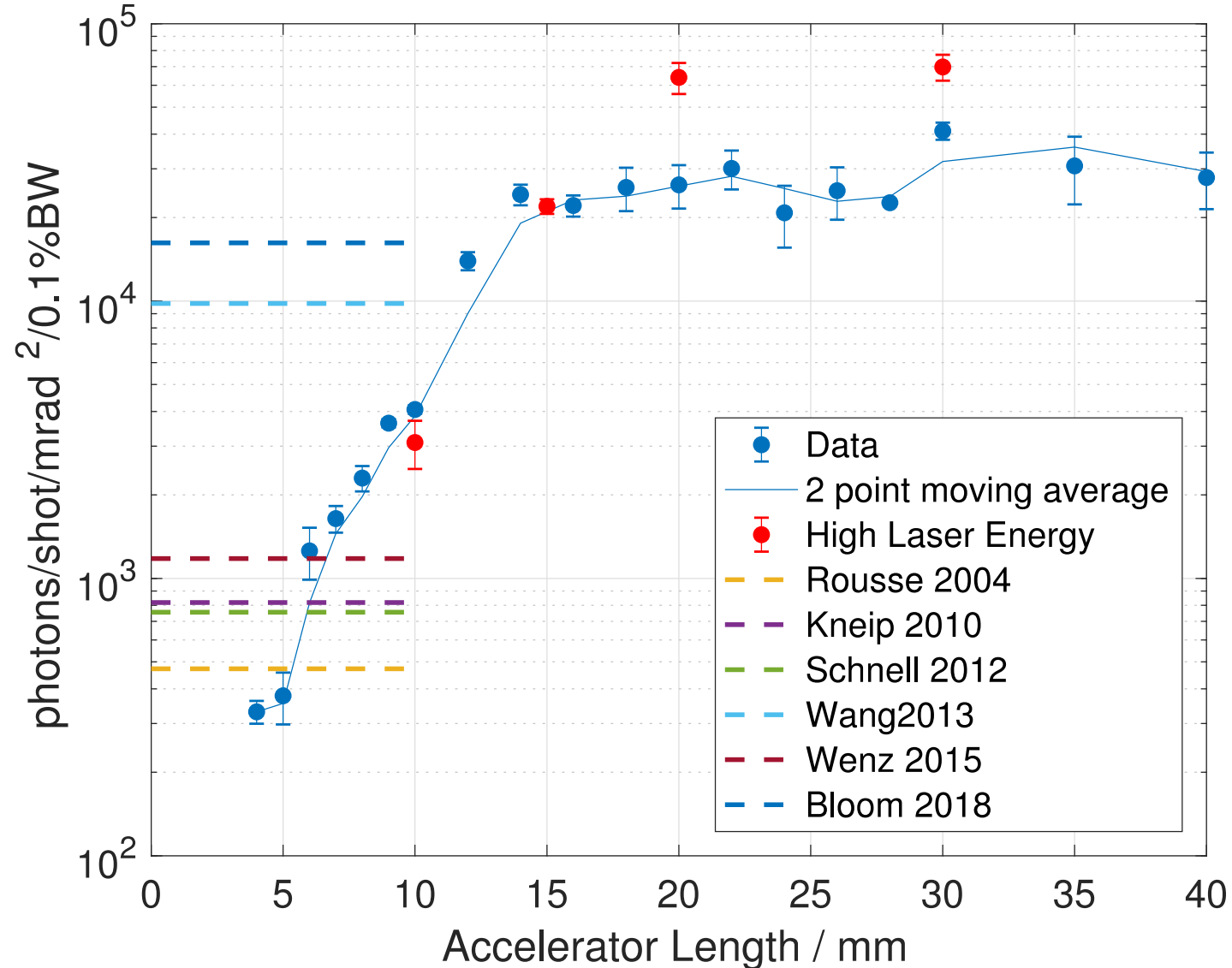


# Large charge, high divergence electron beam injected at depletion length

For  $n_e = 2.3 \times 10^{18} \text{ cm}^{-3}$  depletion length  $L_d = \frac{\omega_L^2}{\omega_p^2} c\tau_L \approx 11 \text{ mm}$



# Extending interaction length as leads to a huge increase in x-ray flux



# Conclusion

- Detailed studies of laser pulse evolution are essential for understanding LWFA
- Wakefield amplitude and size can vary dramatically in a constant plasma density
- Great potential for optimization of electron and x-ray beams

## Thank you to all co-investigators of this work...

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