

# Interplay between native state topology and sequence in two-state protein folding

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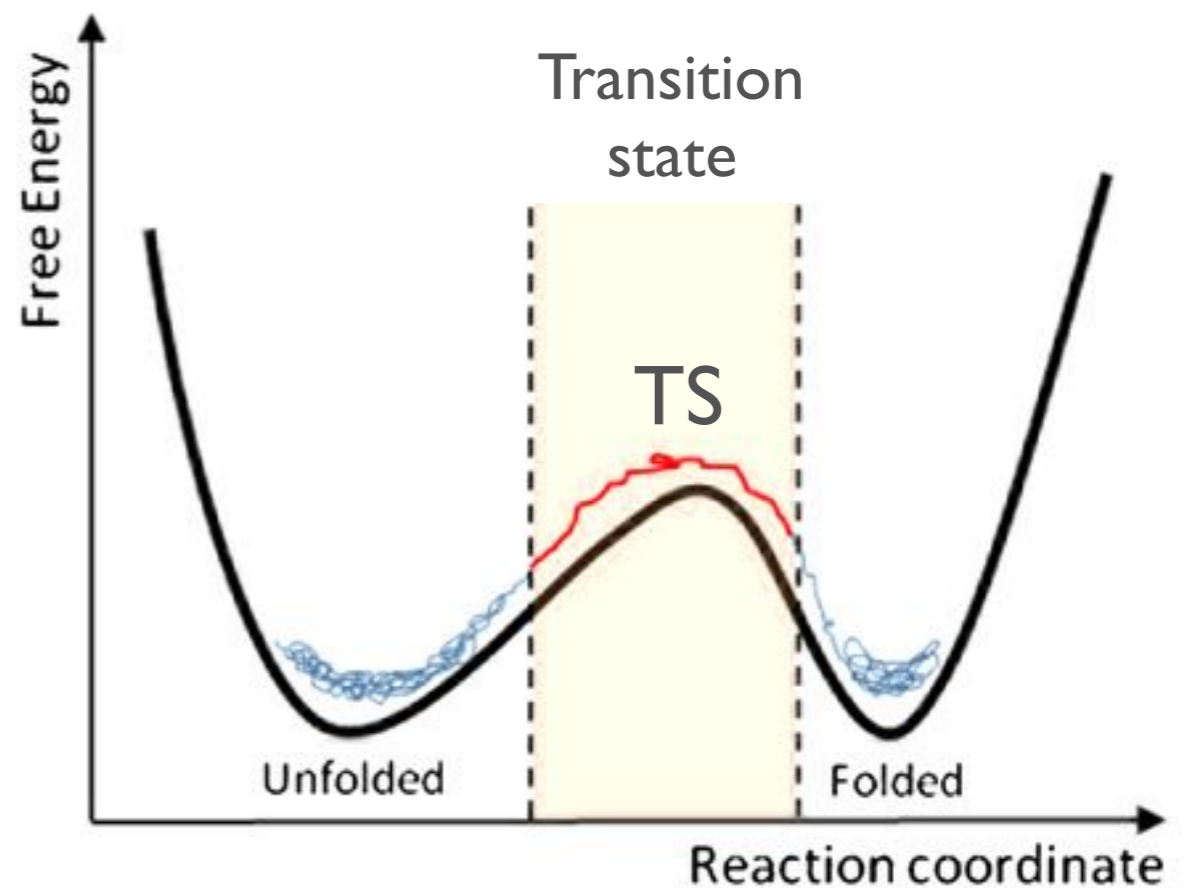
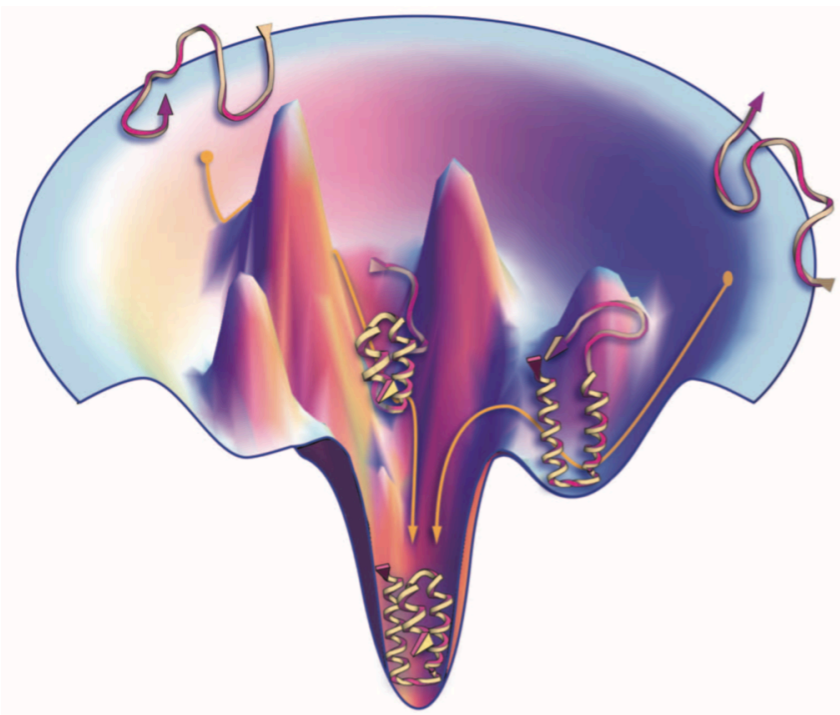
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# Two-state protein folding

- Many globular proteins of ~50-120 amino acids
- Two structurally distinct states, U and N, separated by a single free energy barrier (TS)
- *Minimal models* for folding.



Folding rate  $k_f \propto \exp(-\Delta G/k_B T)$

# Effects of topology and sequence on protein folding

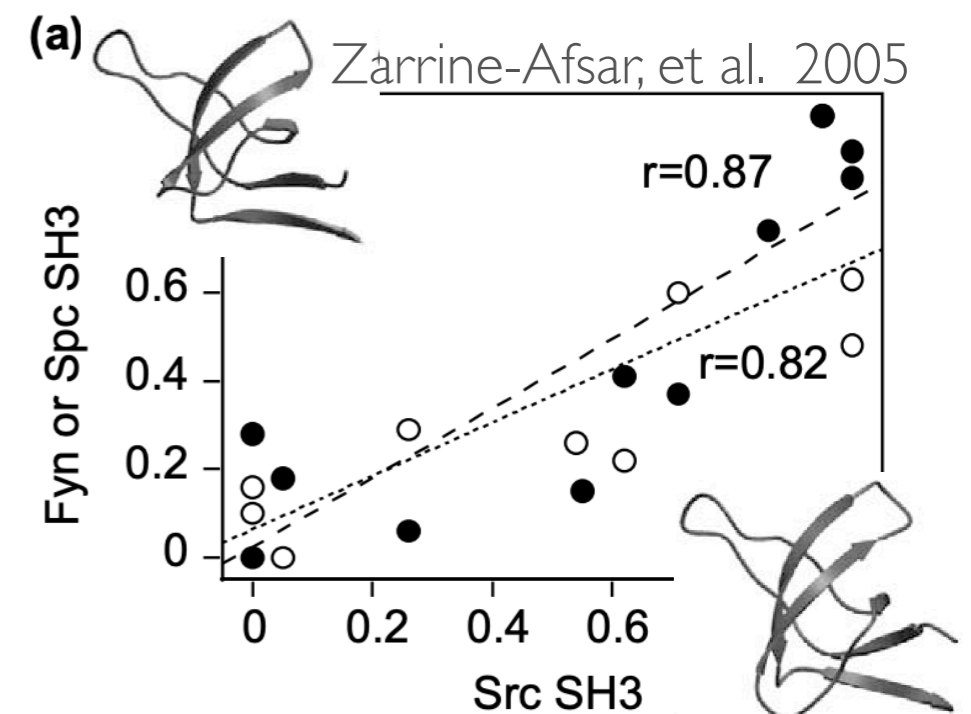
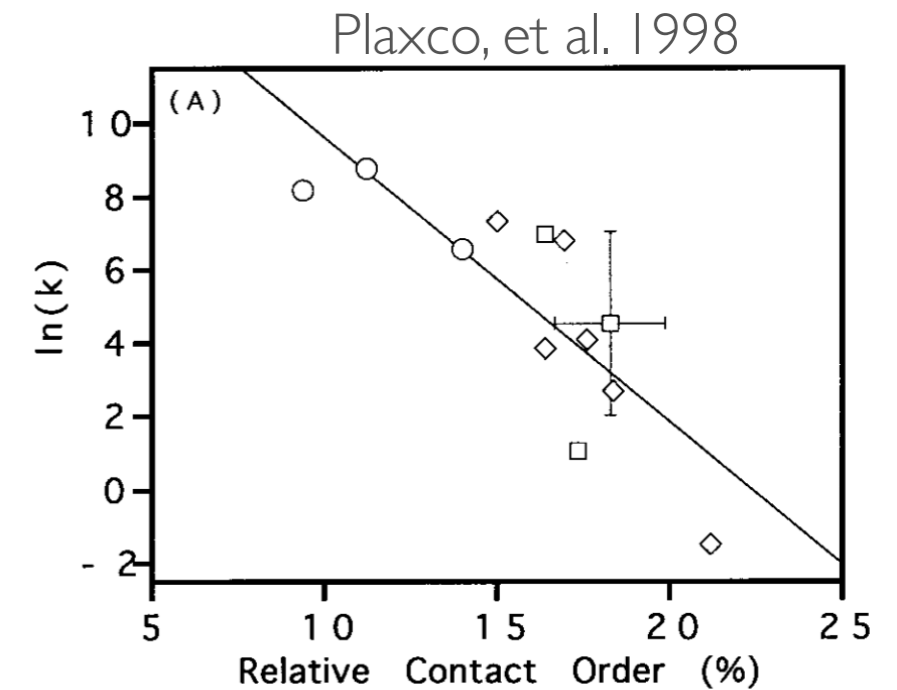
**Topology.** Folding rates  $k_f$  span  $\sim 6$  orders of magnitude

Higher number of “local” vs “nonlocal” contacts means higher folding rate.

RCO = average sequence separation  $|i - j|$  between contacts  $ij$  in native structure.

**Sequence.** Effects pronounced for some topologies but not others.

Two SH3 domains (Fyn and Spc) with only  $\sim 30\%$  sequence identity but conserved TS.



Why is folding into “non-local” folds, e.g.  $\beta$ -barrels, more robust to sequence changes than folding into “local” folds, such as  $\alpha$ -helical bundles?

# Coarse-grained “C $\beta$ model” for protein folding

[Bhattacharjee and Wallin, *Biophys J* 2012]

All-atom backbone/single-site sidechain representation.

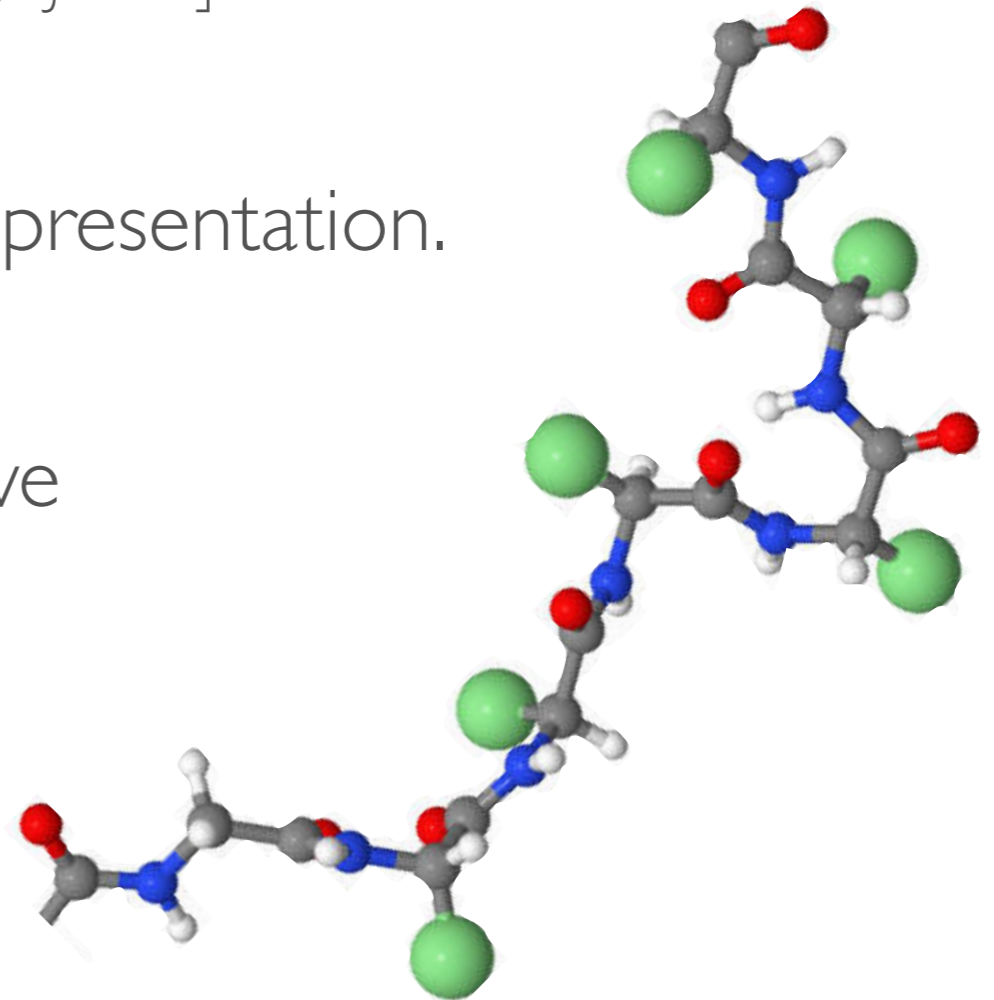
Potential energy function based on effective *hydrophobic forces* and *hydrogen bonding*.

## I. Sequence-based.

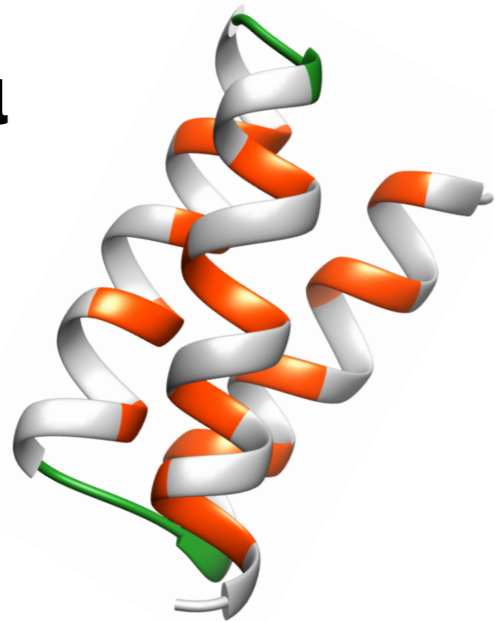
- 3 amino acid types: hydrophobic/polar/turn.
- not “Go-type” or structure-based.

## II. Model sequences fold into realistic protein folds

- both  $\alpha$ -helix and  $\beta$ -sheet structure

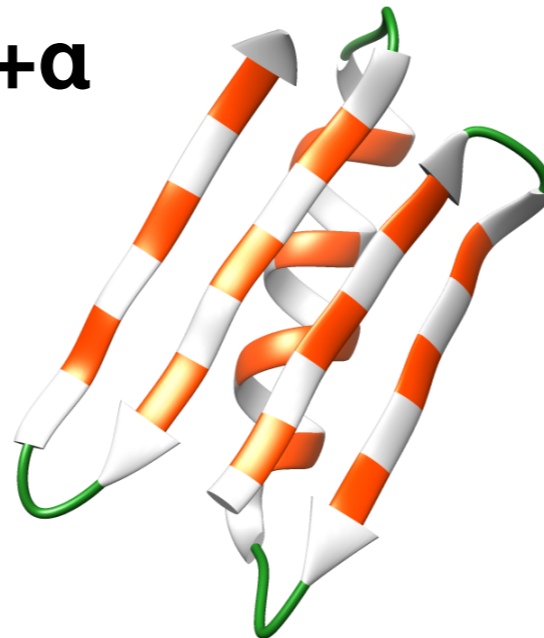


**3 $\alpha$**



$$L = 54$$

**4 $\beta$ + $\alpha$**



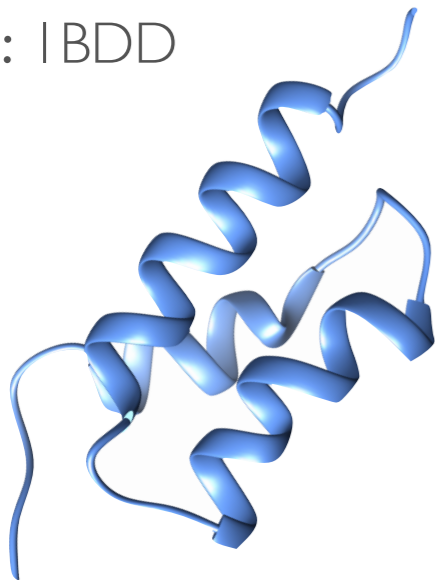
$$L = 54$$

**$\beta$ -barrel**



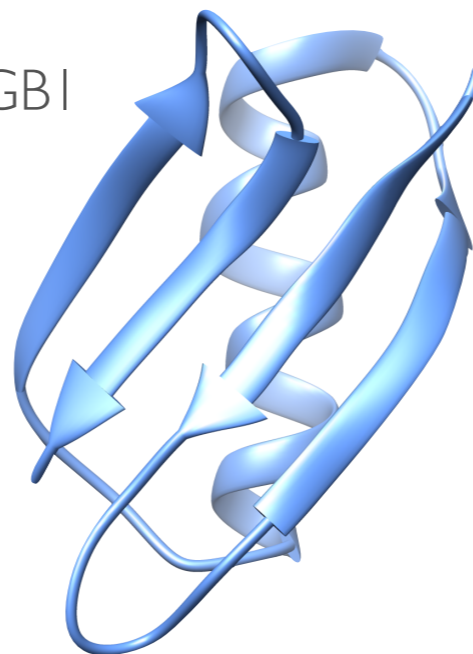
$$L = 35$$

PDB id: 1BDD



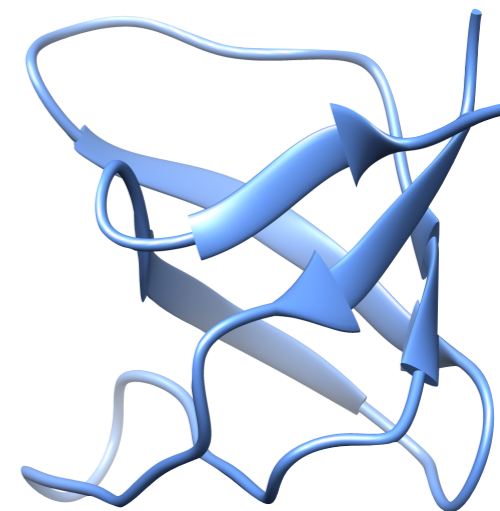
A domain of  
protein G

2GB1



B domain of  
protein G

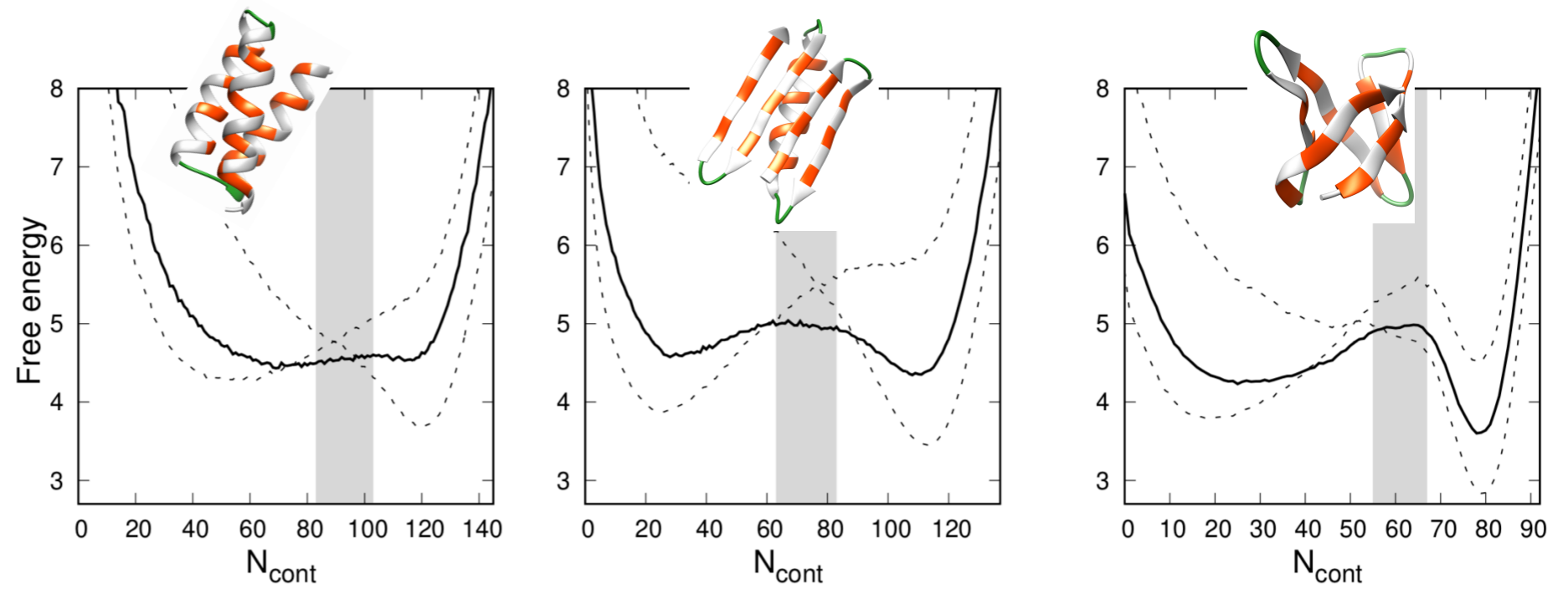
1SHF



Fyn SH3 domain

# Model proteins exhibit topology-dependent folding

Rank-order of cooperativity follows RCO trend at folding temperature  $T_f$ .



Extract transition state ensemble (TS) from peak barrier location.

# Exploring the sequence effects on protein folding

1) Generate all possible hydrophobic/polar *single/double*-point mutants

$\approx 400$ -1200 possible such mutant sequences per protein

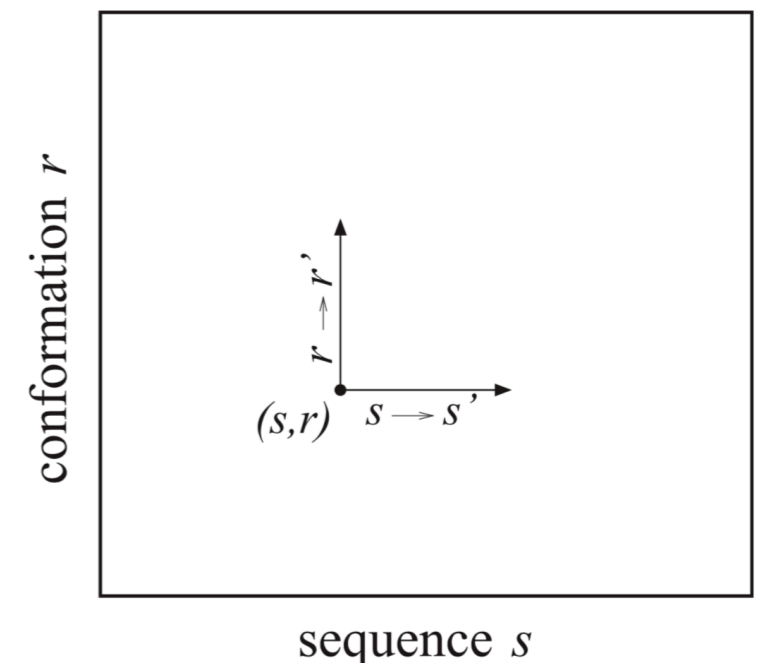
2) Determine equilibrium behaviour of all mutants at  $T = T_f$ .

Simulate the joint probability distribution  $P(s, r) \propto e^{-E(s, r)/k_B T + h(s)}$

1. Conformational  
update

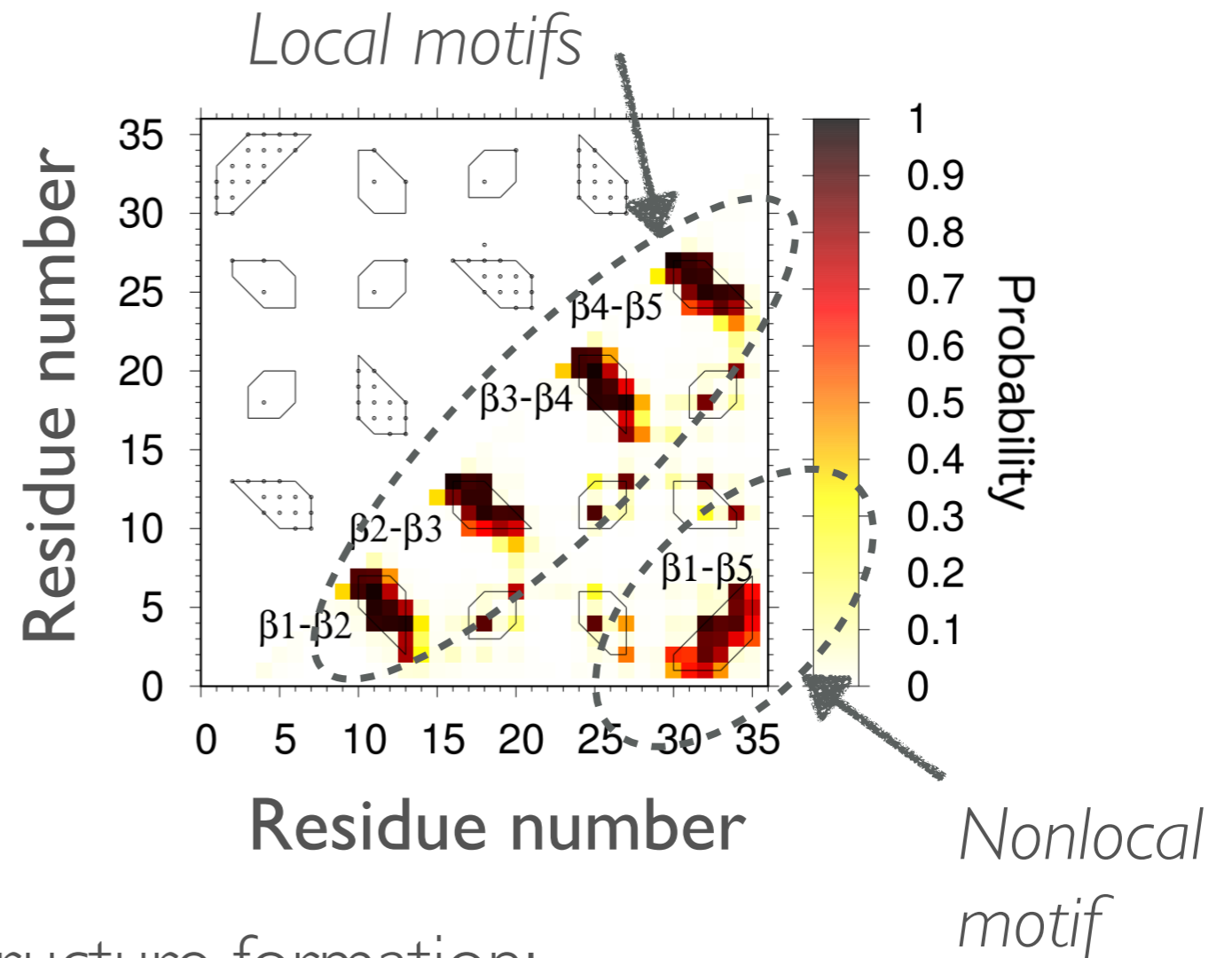
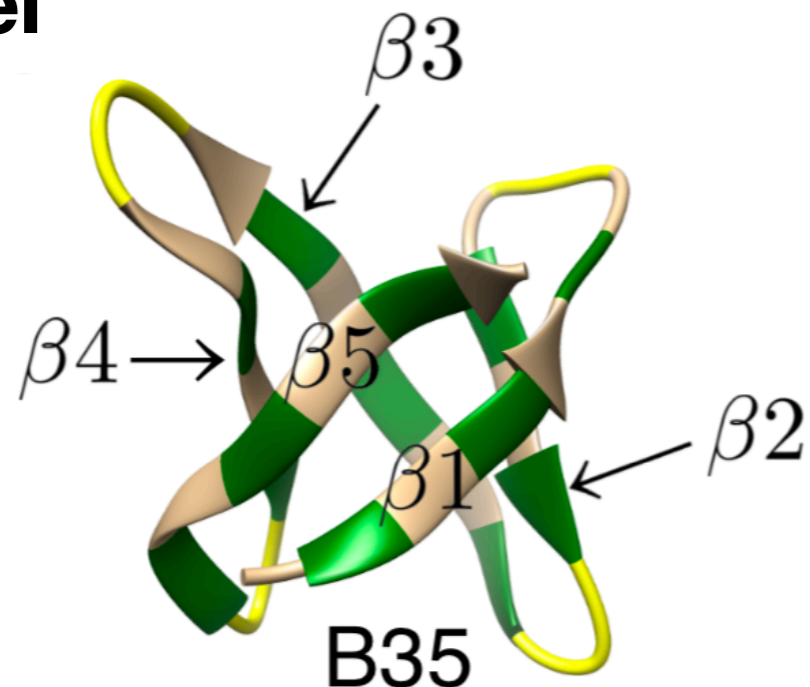


2. Sequence  
update



# Monitoring structure formation during folding

## $\beta$ -barrel



Two different variables describe structure formation:

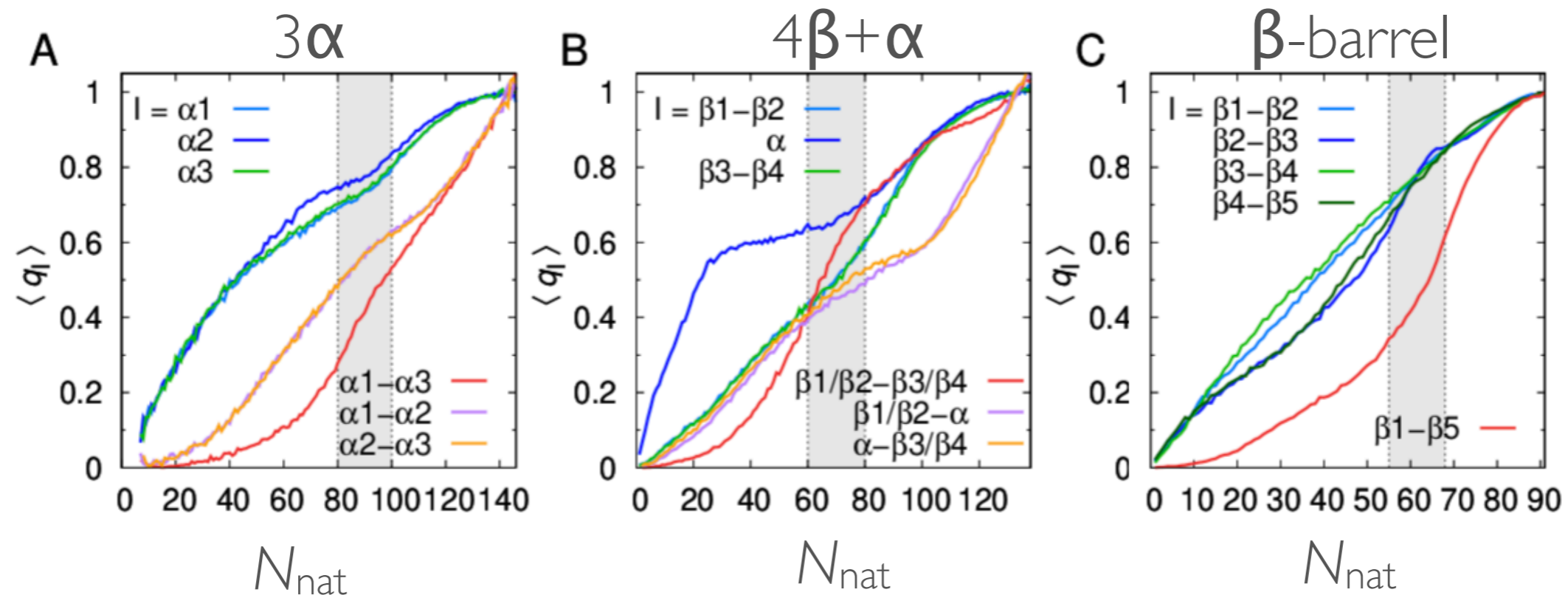
$q_l$  = fraction of native contacts formed in motif  $l$

$\phi_i$  = fraction of native contacts formed for residue position  $i$

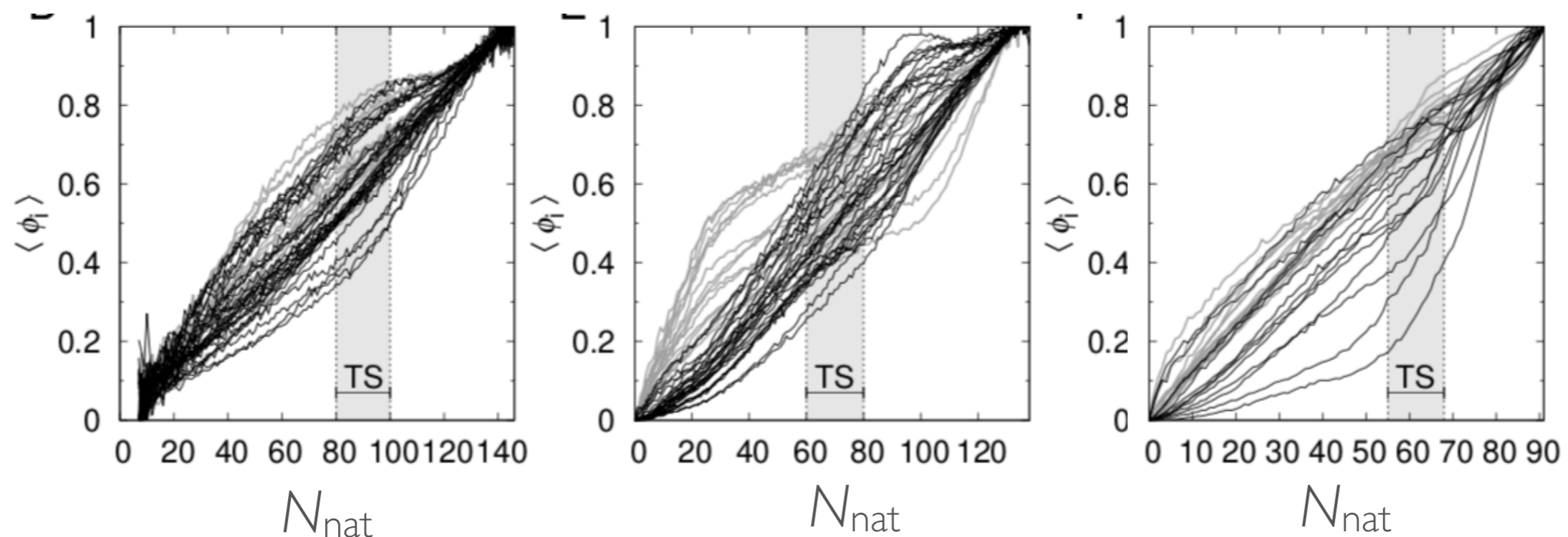
Overall folding progress:

$N_{\text{nat}}$  = total number of native contacts formed

Formation of *nonlocal* contacts drive cooperativity in folding

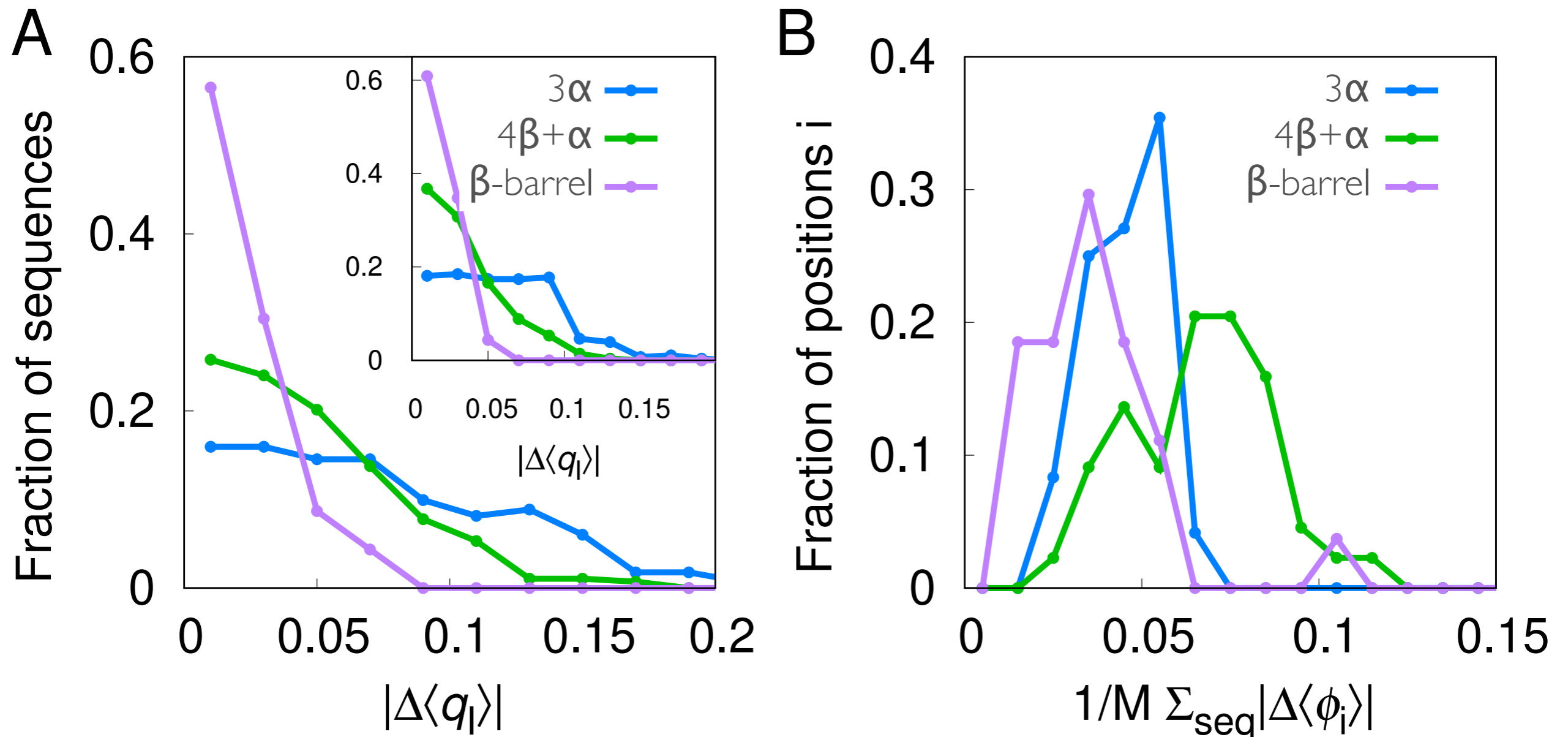


... and underlie a greater  $\phi$ -value diversity in all- $\beta$  protein



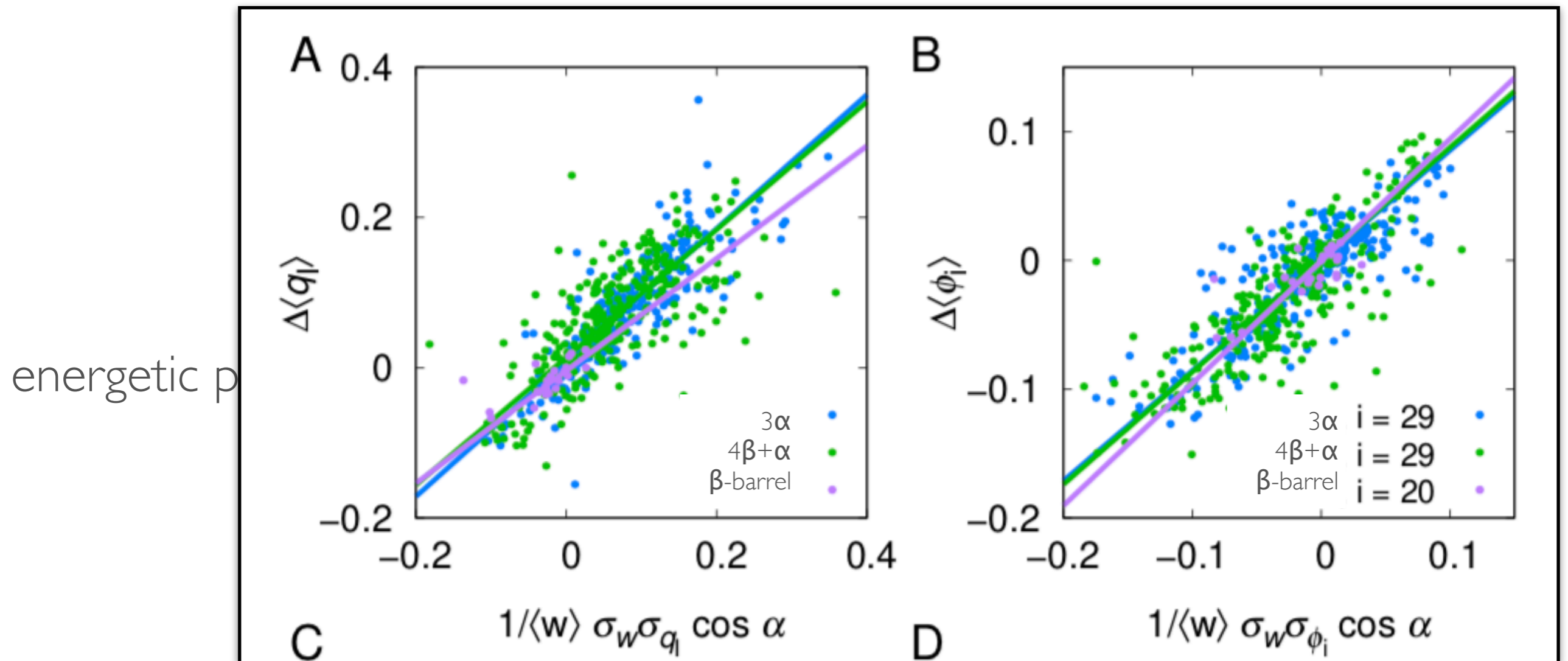
# Sequence effects on folding TS

Mutations induce shifts in equilibrium quantities, e.g.,  $\Delta\langle q_i \rangle = \langle q_i \rangle - \langle q_i \rangle_0$



- $q_i$  and  $\phi_i$ -values of  $\beta$ -barrel protein least perturbed by mutations

Can features of the “parent” protein explain the observed mutational response?

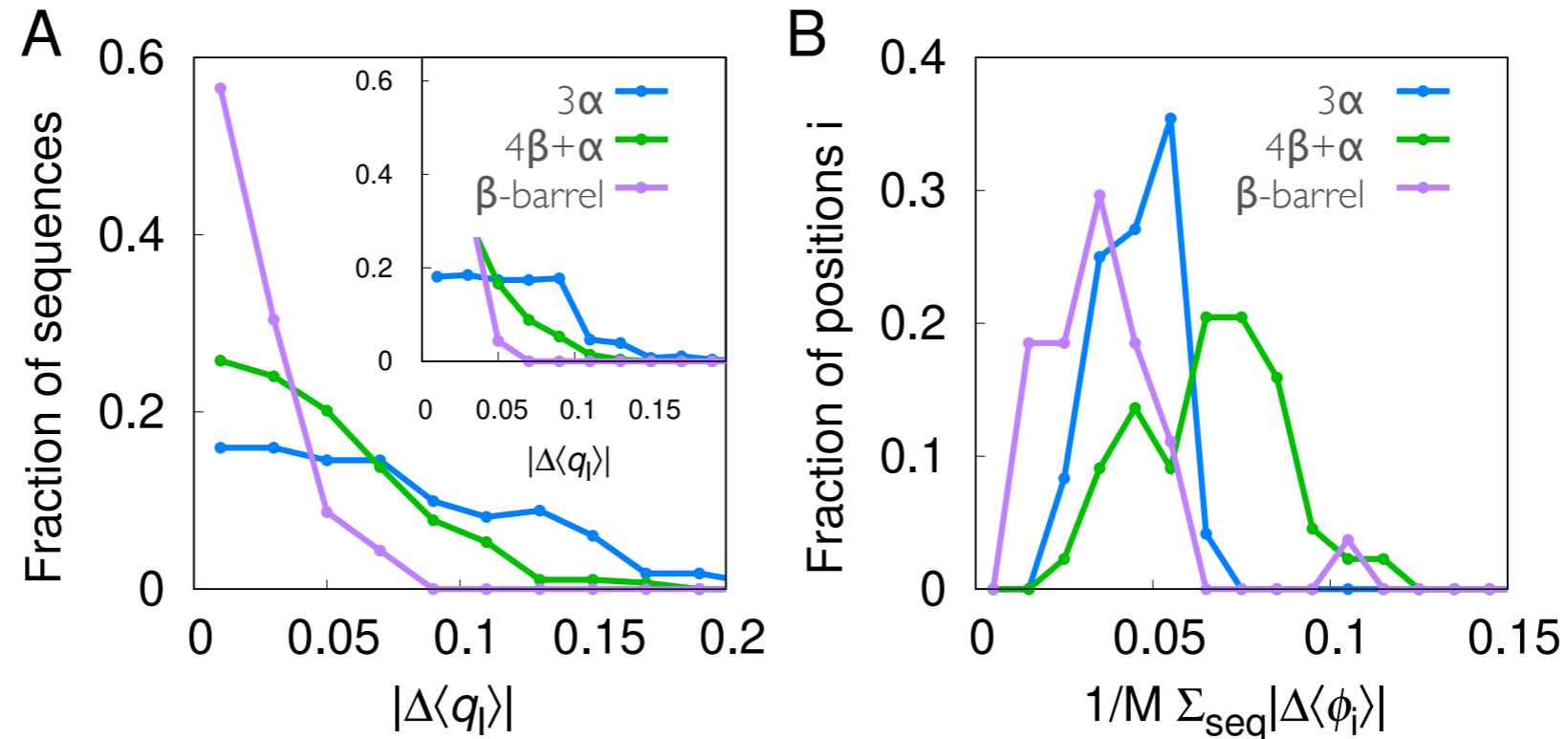


$$\Delta\langle X \rangle = \frac{1}{\langle w \rangle_s} \sigma_w \sigma_X \cos \alpha$$

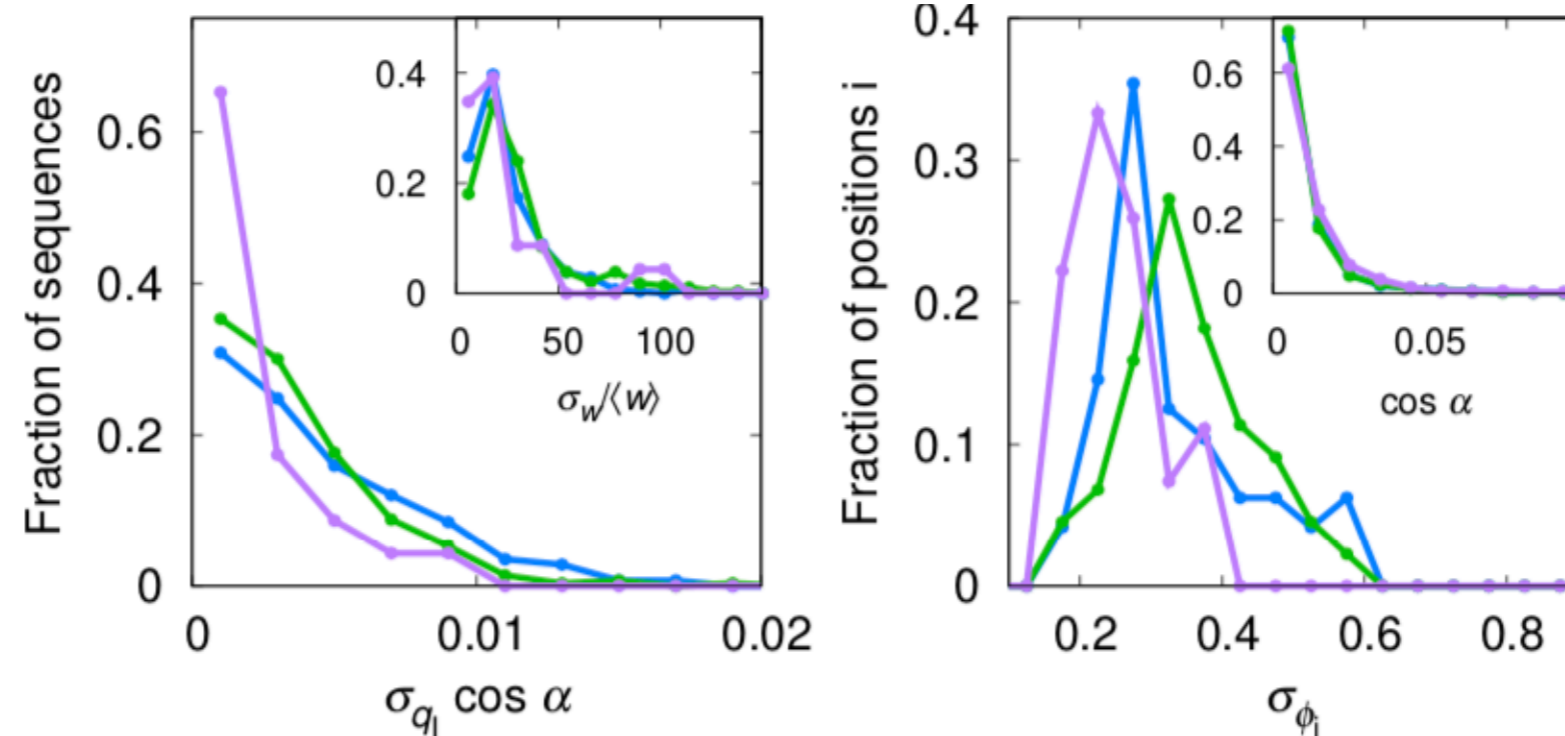
relevant observable  $X$  ( $q_i$  or  $\phi_i$ )

# Can features of the “parent” protein explain the observed mutational response?

Observed  
mutational  
response  
on TS...

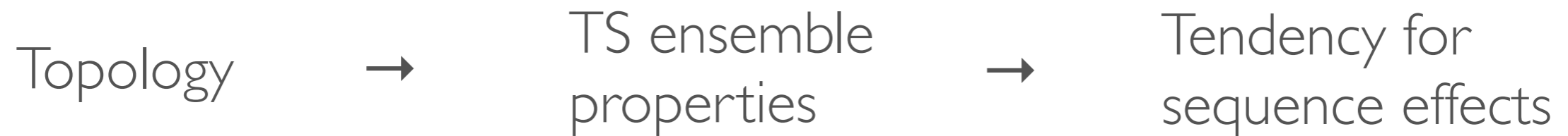


...can be  
explained  
by factors  
 $\sigma_X \cos \alpha$   
alone



# Conclusion

**Topology and sequence effects in protein folding are coupled:**



**I. Conformational diversity.** TS of all- $\beta$  proteins more structurally restricted than for all- $\alpha$  proteins, leading to weaker mutational response.

In particular,  $\phi$ -values at positions with a broad distribution  $P(\phi)$  should tend to diverge with sequence.

**II. Mutational-energetic correlations.** Conformational variations in TS of all- $\beta$  proteins less “aligned” with energetic changes than in all- $\alpha$ , again weakening mutational response.