

Deep Learning (and Deep Thinking) in Collider Physics

Jesse Thaler



Pheno 2019, University of Pittsburgh — May 8, 2019

Deep Learning

Inpainting



Corrupted



Deep image prior

increased computational power and large data sets

[Ulyanov, Vedaldi, Lempitsky, [1711.10925](#)]

Deep Learning (or Deep Thinking?)

Inpainting



Corrupted



Deep image prior

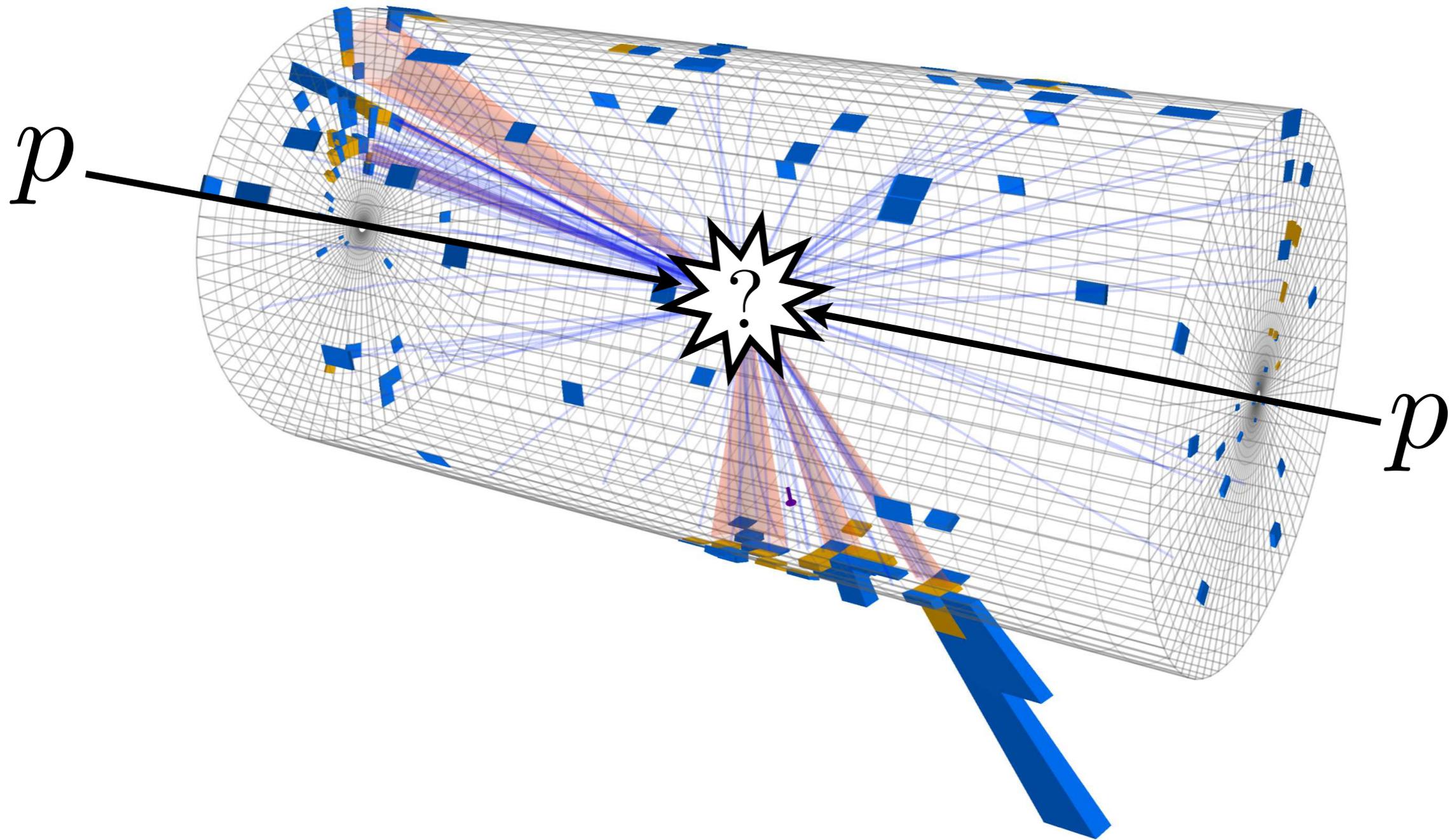
Using randomly initialized neural network (!)

Progress made by **understanding the structure** of problems
(not just **increased computational power** and large data sets)

[Ulyanov, Vedaldi, Lempitsky, [1711.10925](https://arxiv.org/abs/1711.10925)]

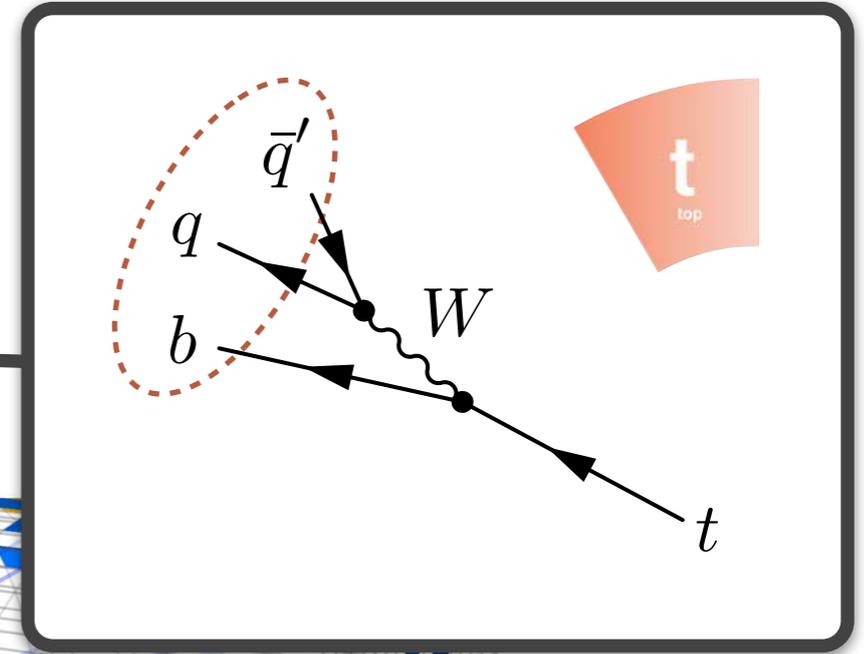
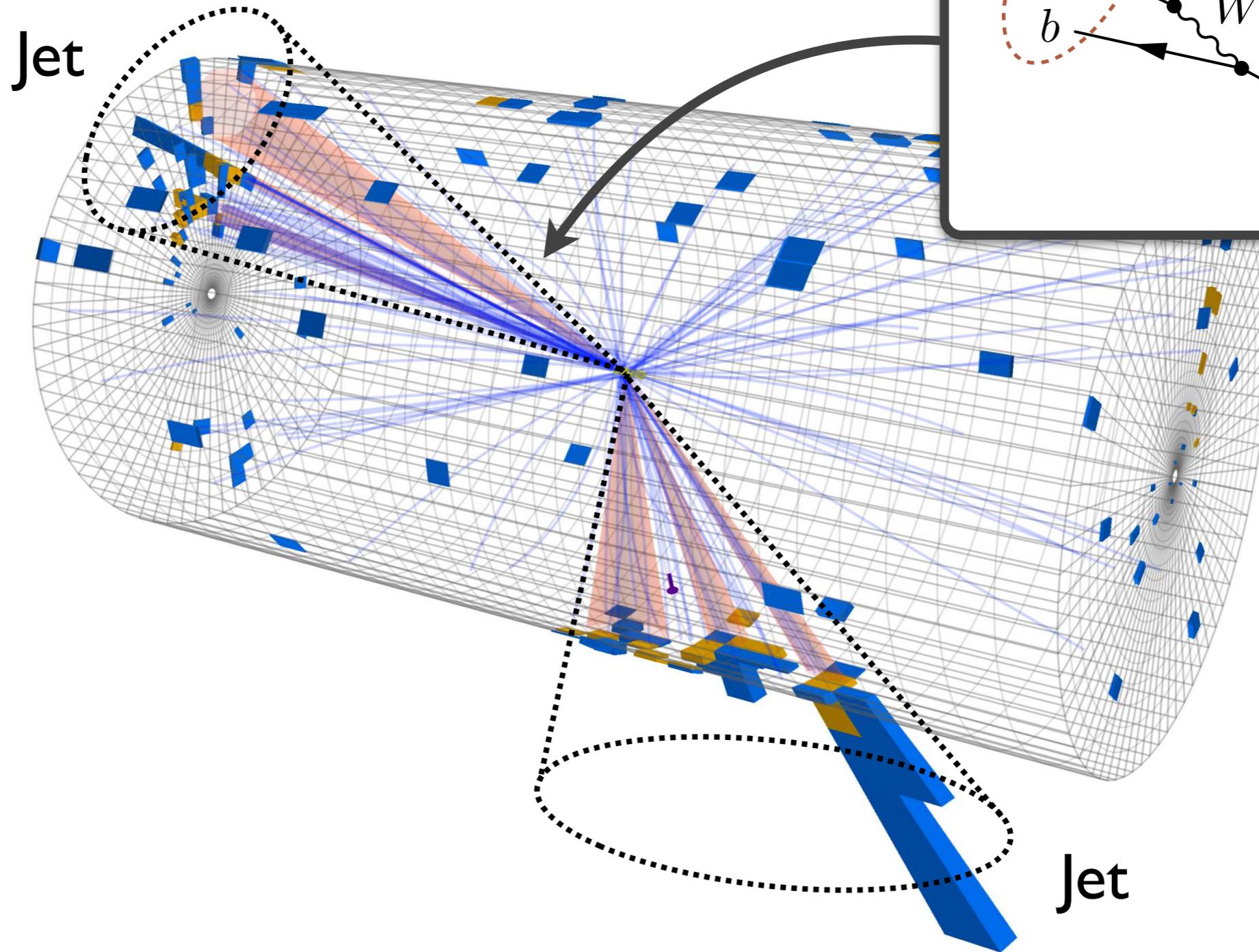


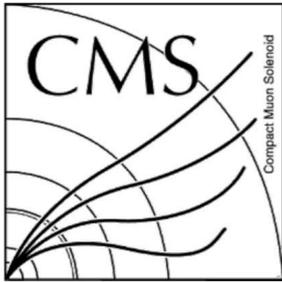
CMS Experiment at LHC, CERN
Data recorded: Sun Jul 12 07:25:11 2015 CEST
Run/Event: 251562 / 111132974
Lumi section: 122
Orbit/Crossing: 31722792 / 2253





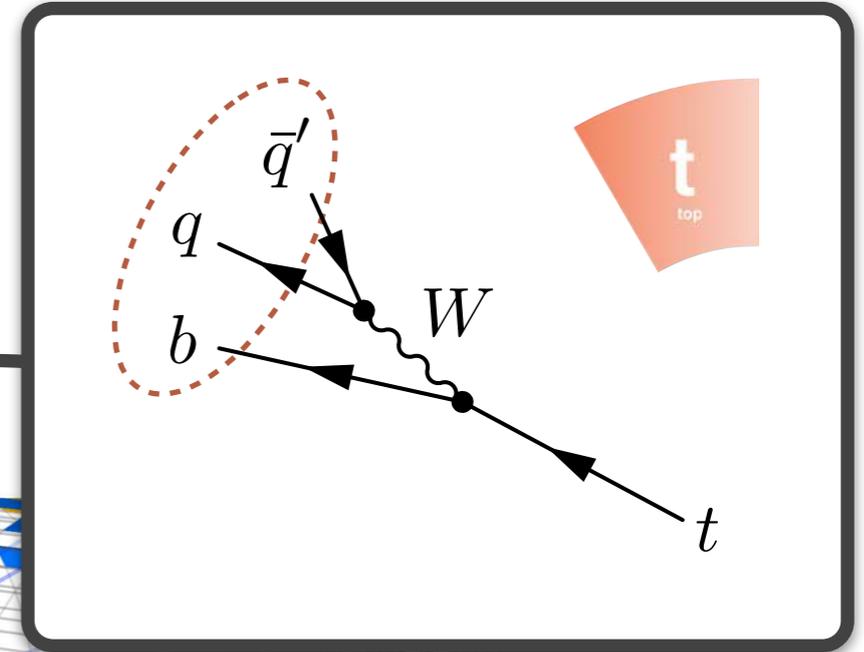
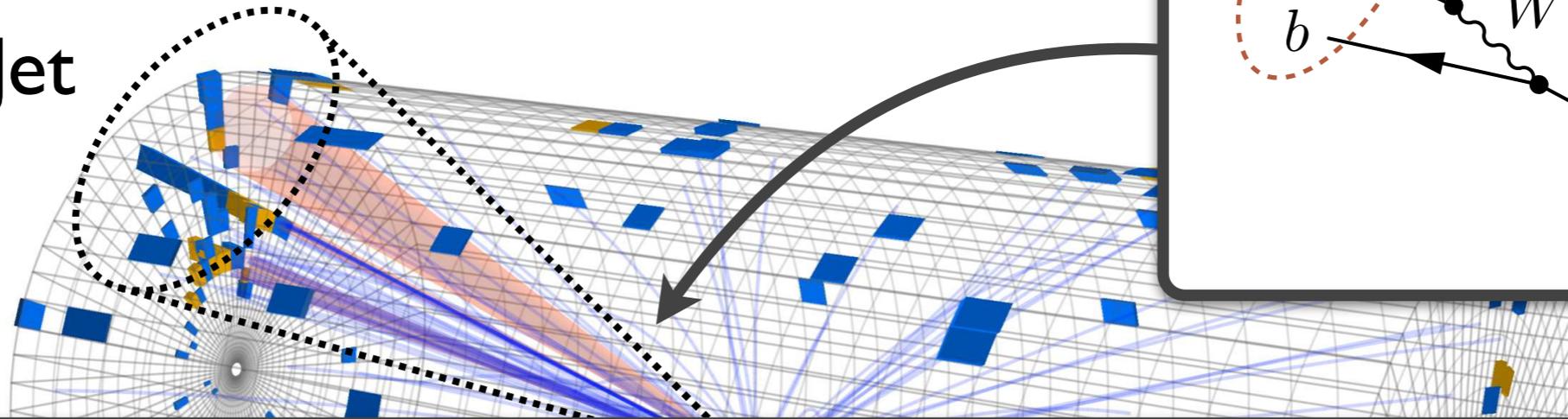
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CMS Experiment at LHC, CERN
 Data recorded: Sun Jul 12 07:25:11 2015 CEST
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 Lumi section: 122
 Orbit/Crossing: 31722792 / 2253

Jet



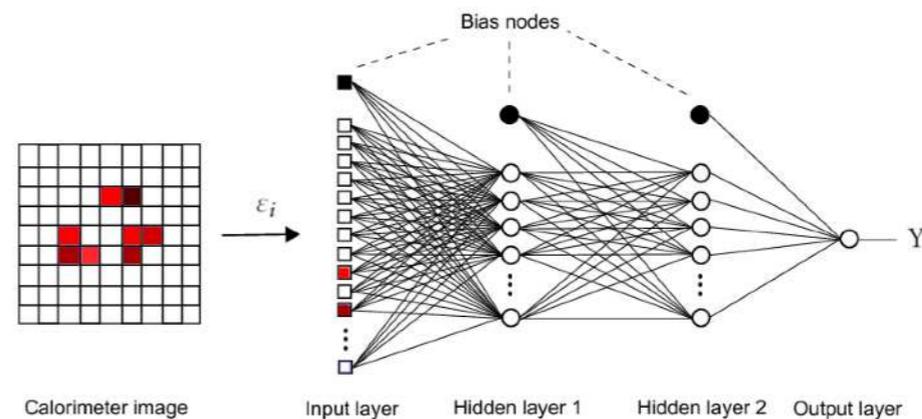
“Deep Thinking”?

[e.g. JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);
 rephrased in language of Komiske, Metodiev, JDT, [1902.02346](#)]

$$\tau_N(\mathcal{J}) = \min_{|\mathcal{J}'|=N} \text{EMD}(\mathcal{J}, \mathcal{J}')$$

“Deep Learning”?

[e.g. Almeida, Backović, Cliche, Lee, Perelstein, [1501.05968](#);
 review in Kasieczka, Plehn, et al., [1902.09914](#)]



Deep Learning at Pheno 2019



Tuesday @ 15:15 (Higgs II): [Jeong Han Kim](#)
“Portraying Double Higgs Production with *Deep Neural Networks*”

Tuesday @ 14:15 (BSM III): [Prasanth Shyamsundar](#)
“*Machine learning* in event selection: Improving the supervisory signal and output usage”

Tuesday @ 15:00 (BSM III): [Felix Kling](#)
“MadMiner: An *inference toolkit* for particle physics”

Please email me if I missed your talk!

Plus, public collider data:

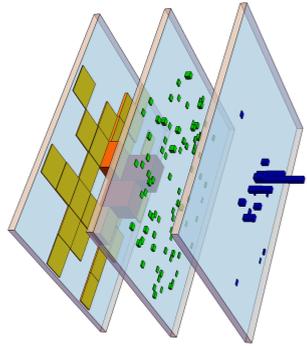


Tuesday @ 14:45 (BSM III): [Cari Cesarotti](#)
“Searching for New Dimuon Resonances
at the LHC with *CMS Open Data*”

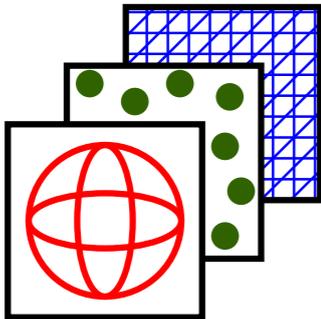


[Cesarotti, Soreq, Strassler, JDT, Xue, [1902.04222](#)]

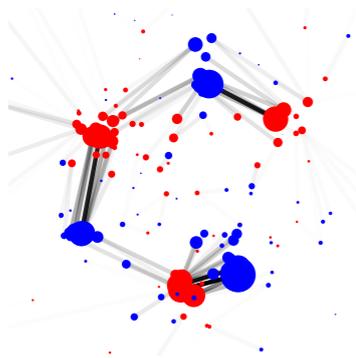
Outline



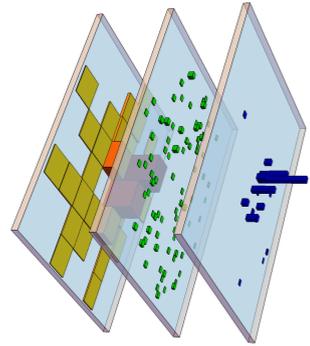
The Rise of Deep Learning



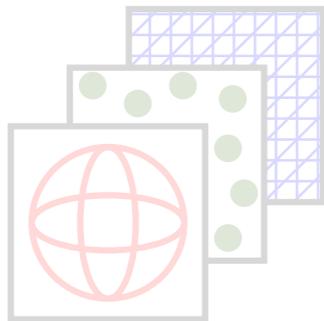
Looking Inside the Black Box



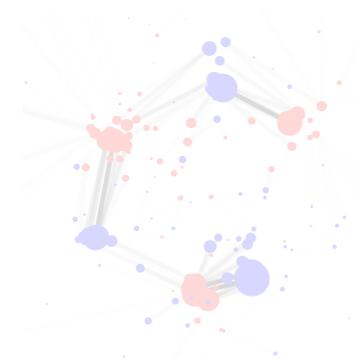
(Exploring the Space of Jets)



The Rise of Deep Learning



Looking Inside the Black Box



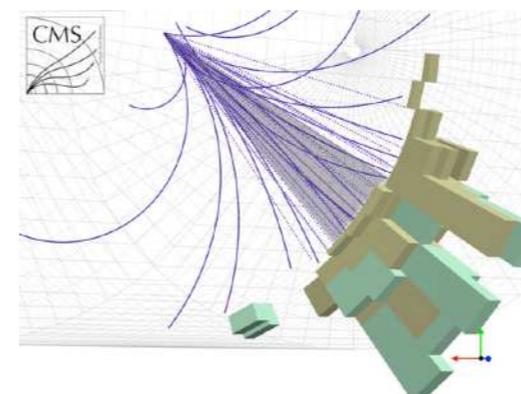
(Exploring the Space of Jets)

Cartoon of Machine Learning



E.g.: **Problem** = Minimize loss function
Solution = Multi-layer neural network
Strategy = Stochastic gradient descent

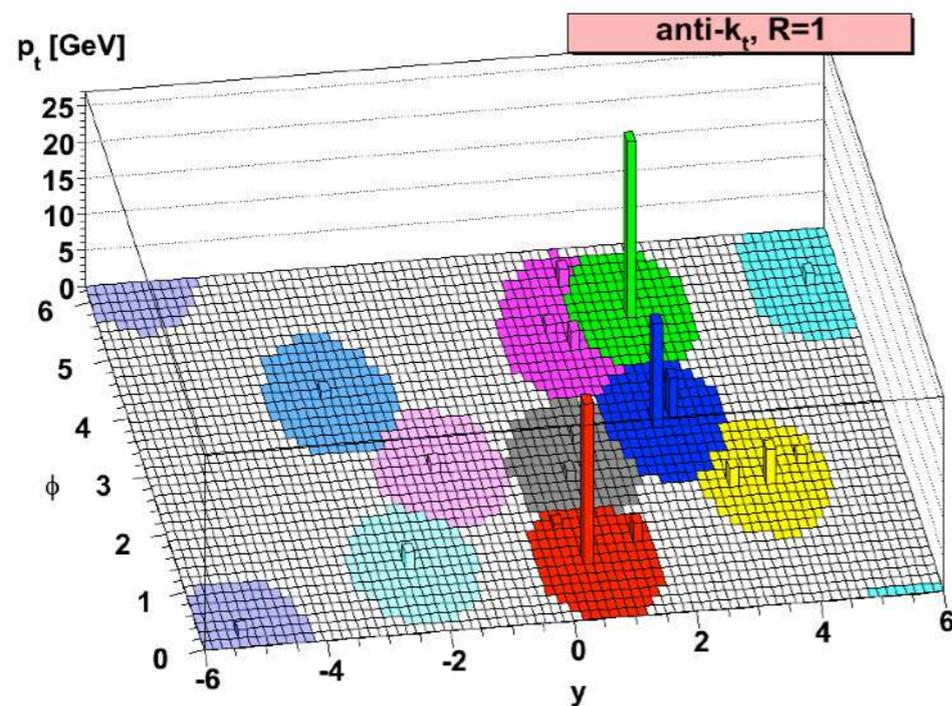
For most of this talk: \mathcal{J} = “jet”



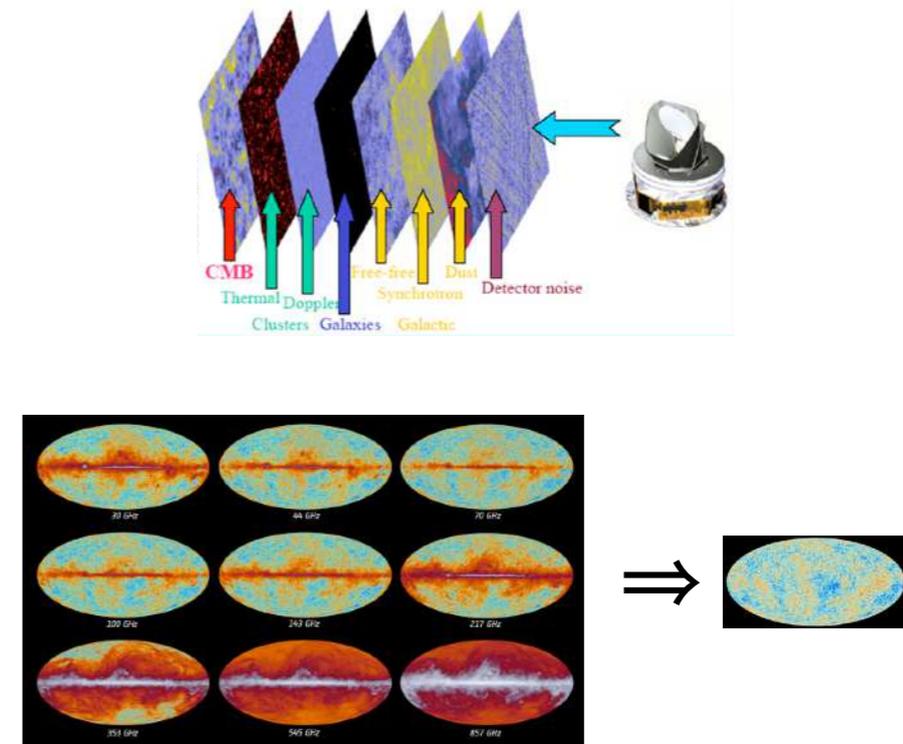
Examples of Unsupervised Learning

(see backup for probability modeling and anomaly detection)

Clustering



Topic Modeling



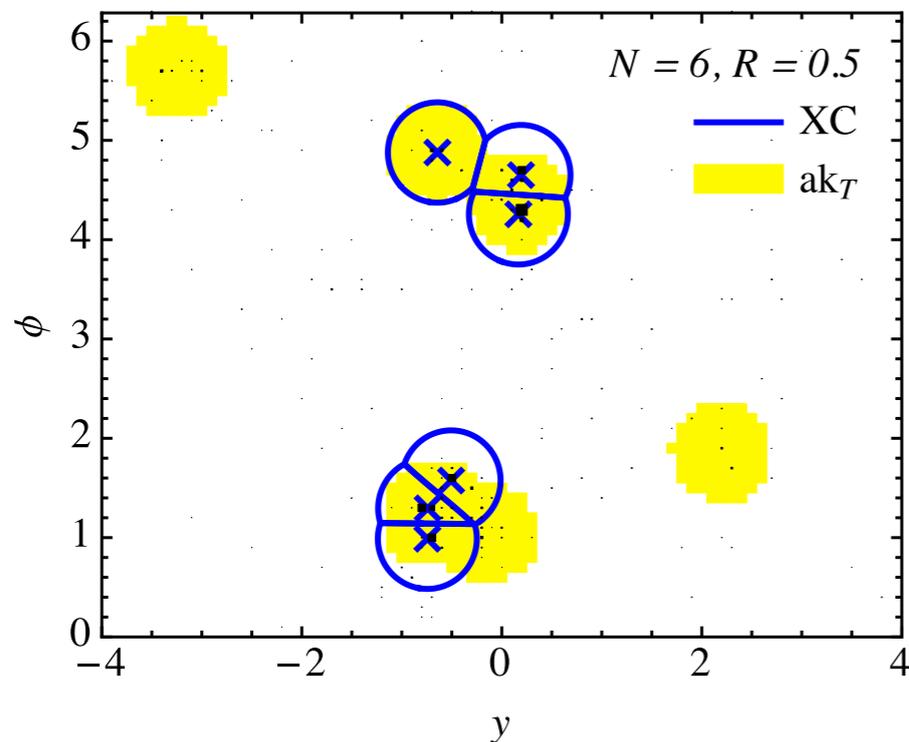
(Approximate) *solutions* to *properly specified problems*

[figures from Cacciari, Salam, Soyez, 0802.1189; Planck Outreach]

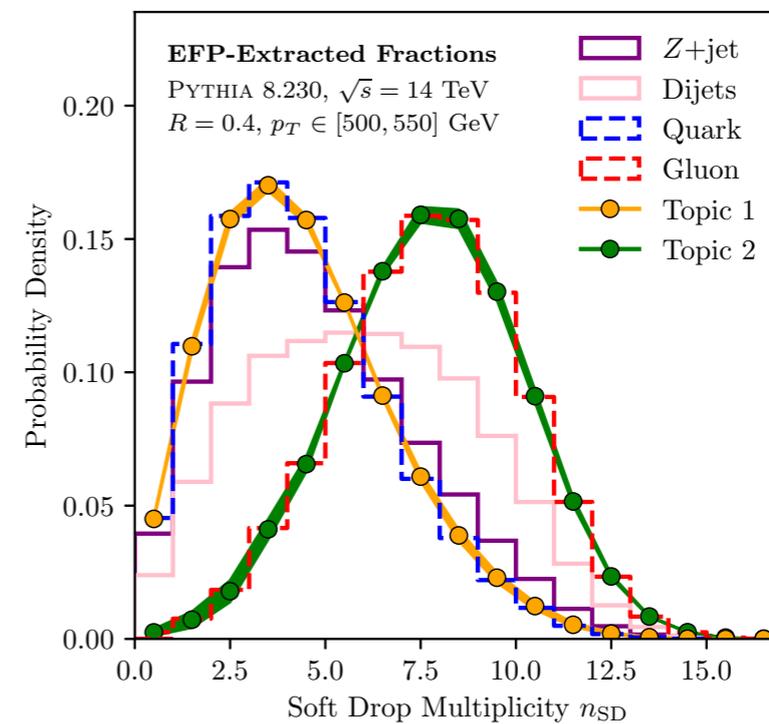
Examples of Unsupervised Learning

(see backup for probability modeling and anomaly detection)

XCone Jet Finding



Jet Topics



“Find N axes that minimize N -jettiness”

“Find two mutually irreducible distributions”

[Stewart, Tackmann, JDT, Vermilion, Wilkason, [1508.01516](#); based on Stewart, Tackmann, Waalewijn, [1004.2489](#)]
[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#); see also Dillon, Faroughy, Kamenik, [1904.04200](#)]

(Approximate) *solutions* to *properly specified problems*

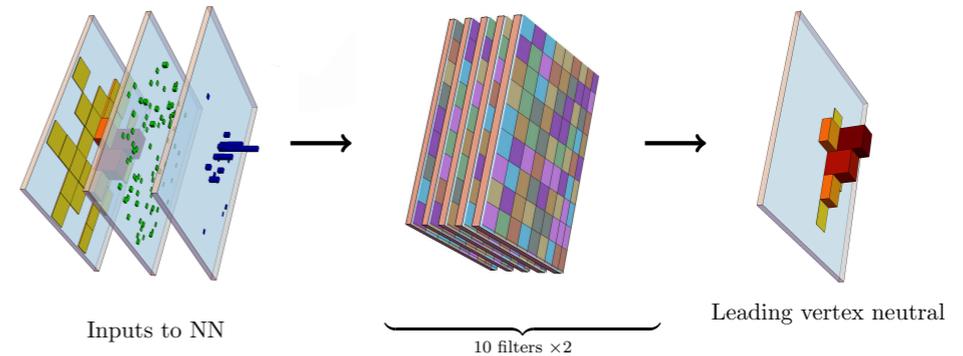
[figures from Cacciari, Salam, Soyez, [0802.1189](#); Planck Outreach]

Examples of Supervised Learning

Regression

e.g. *PUMML for pileup mitigation*

[Komiske, Metodiev, Nachman, Schwartz, [1707.08600](#);
see also Arjona Martínez, Cerri, Pierini, Spiropulu, Vlimant, [1810.07988](#)]



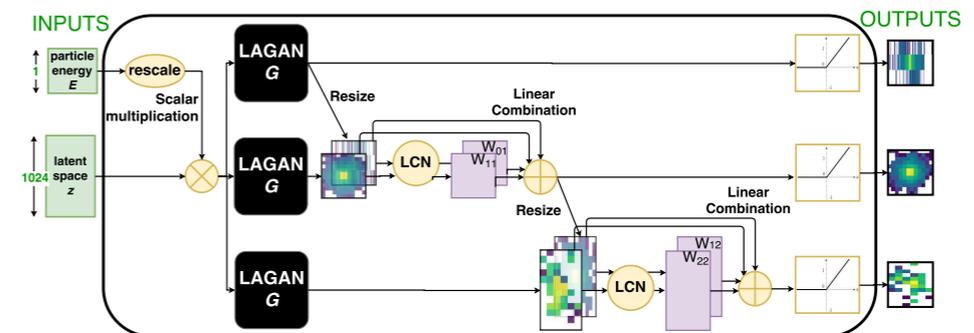
Labeled data: Objects J with property x

Solution: Map from J to x

Generation

e.g. *CaloGAN for fast detector simulation*

[Paganini, de Oliveira, Nachman, [1705.02355](#), [1712.10321](#);
see also de Oliveira, Michela Paganini, Nachman, [1701.05927](#)]

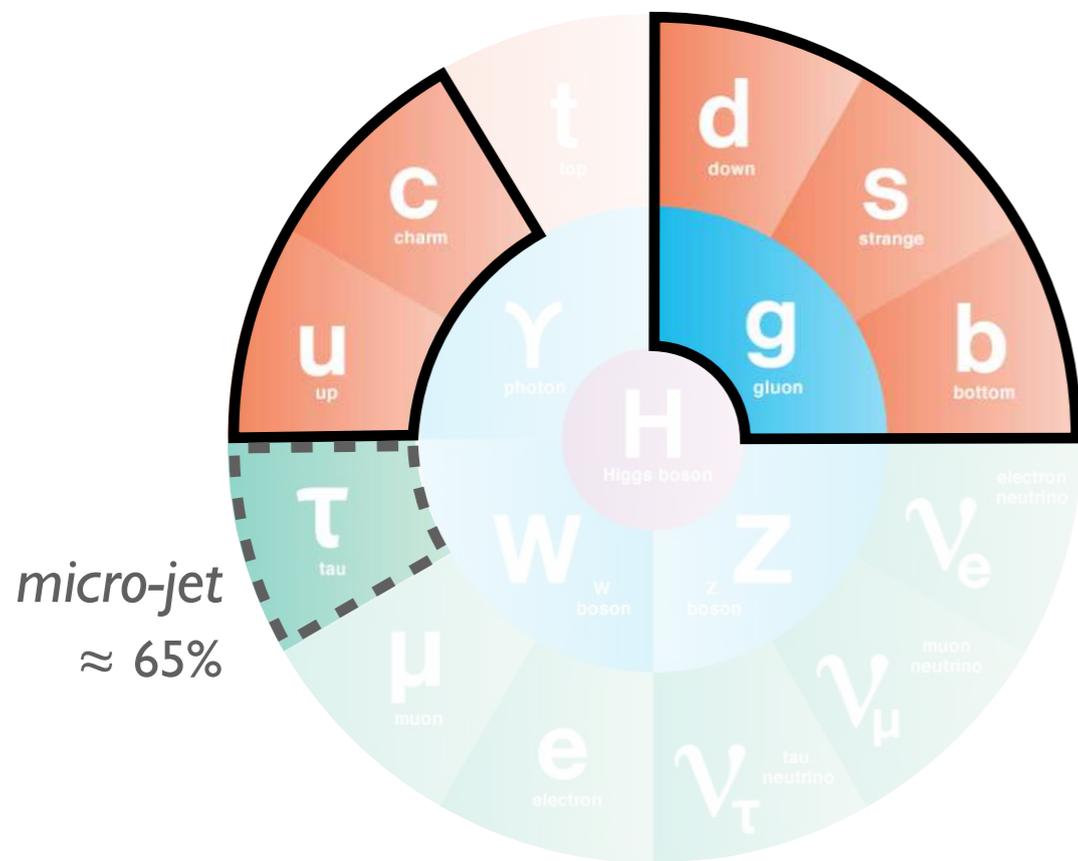


Labeled data: Objects J with property x

Solution: Map (conditioned on x)
from noise to J

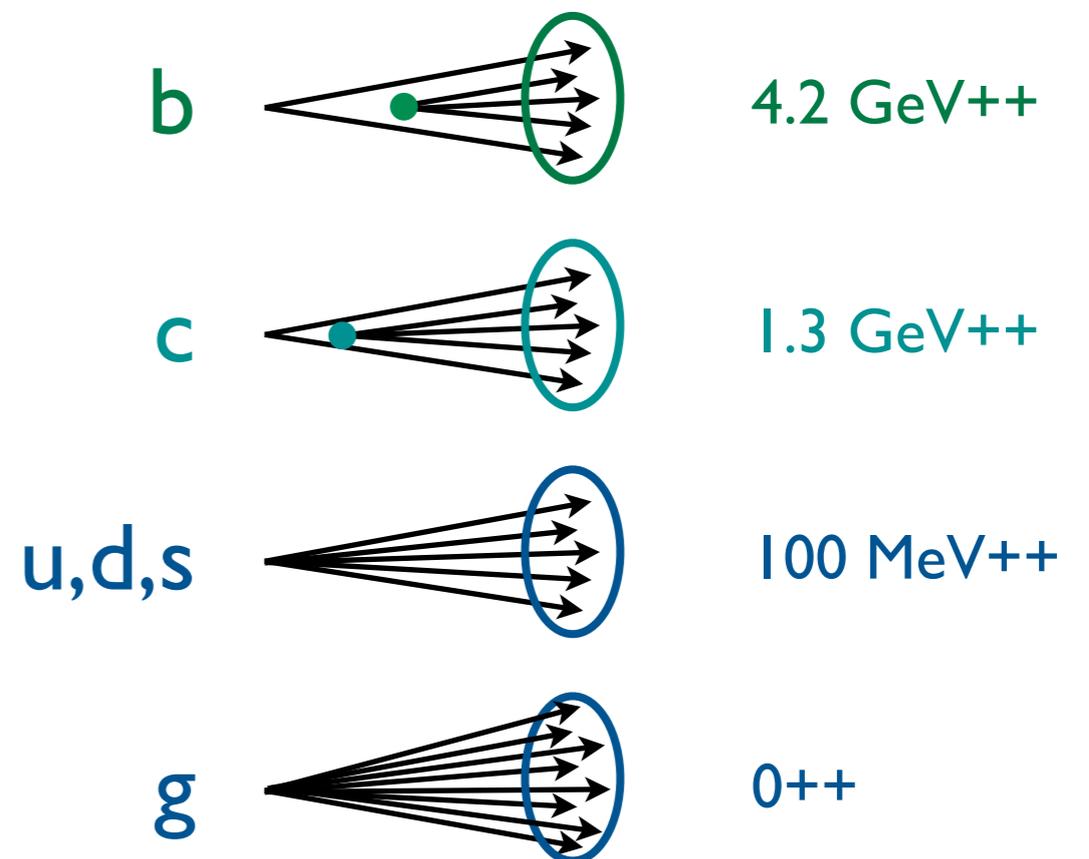
Jet Classification

Key supervised learning task at LHC



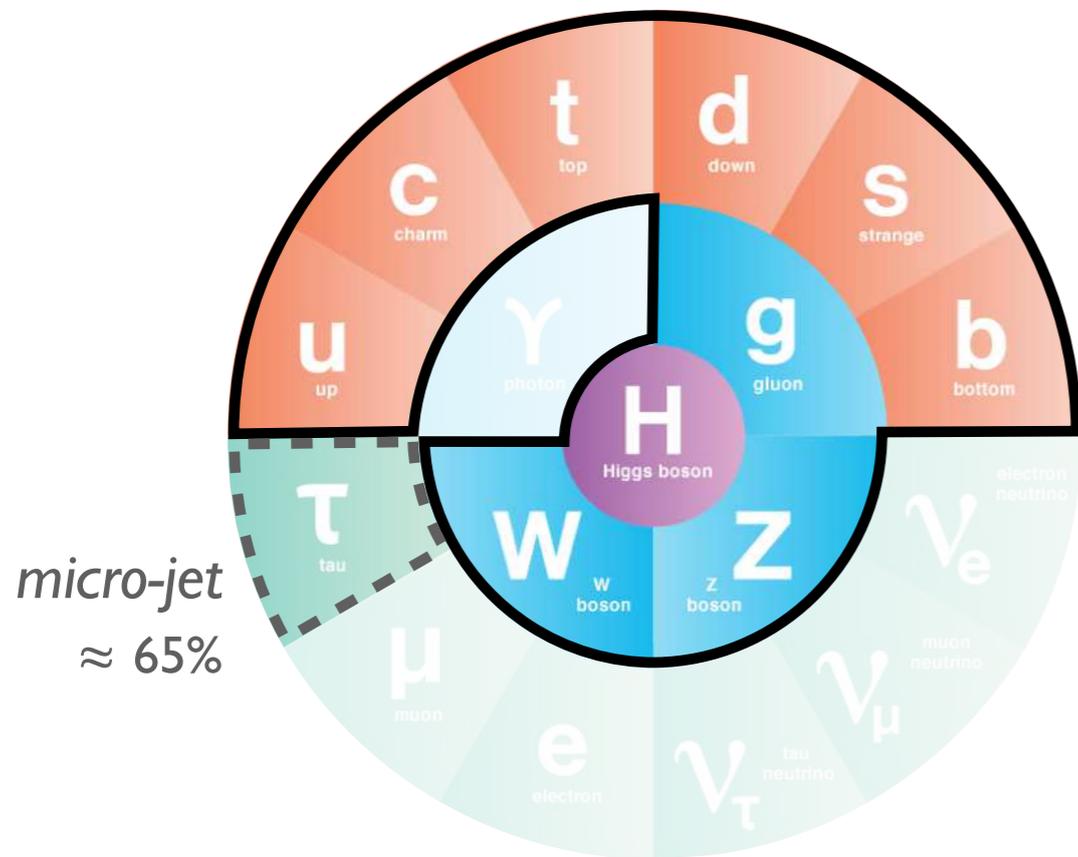
++ = Mass from QCD Radiation

[see review in Larkoski, Mout, Nachman, [1709.04464](#)]



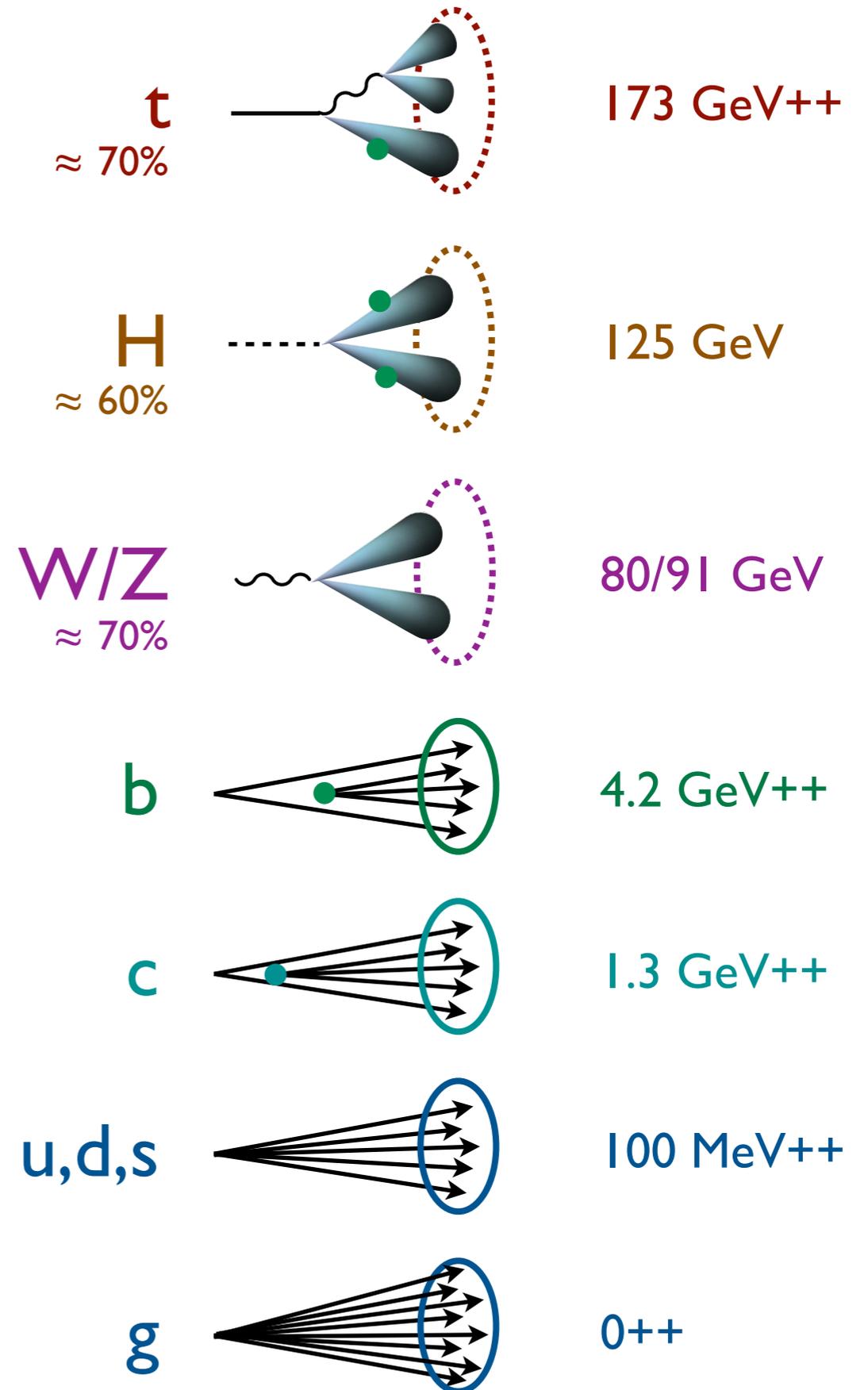
Jet Classification

Key supervised learning task at LHC



++ = Mass from QCD Radiation

[see review in Larkoski, Mout, Nachman, [1709.04464](#)]



BOSTON 2019

Phenomenology | Reconstruction | Searches | Algorithms | Measurements | Calculations
Modeling | Machine Learning | Pileup Mitigation | Heavy-Ion Collisions | Future Colliders

Local Organizing Committee:

Zeynep Demiragli (BU)
Philip Harris (MIT)
Yen-Jie Lee (MIT)
Matthew Schwartz (Harvard)
Jesse Thaler (MIT)

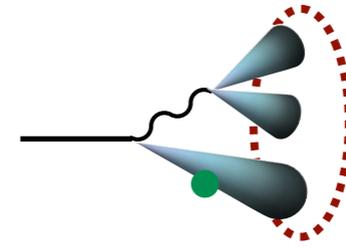
International Advisory Committee:

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Alexander Schmidt (Aachen)
Ariel Schwartzman (SLAC)
Gregory Soyez (CNRS)
Marcel Vos (Valencia)

July 22-26, 2019
Stata Center, MIT

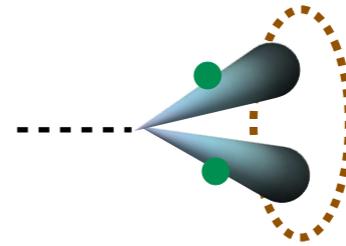
<https://indico.cern.ch/e/boost2019>

t
 $\approx 70\%$



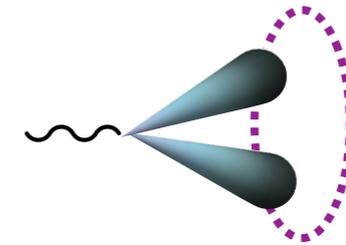
173 GeV++

H
 $\approx 60\%$



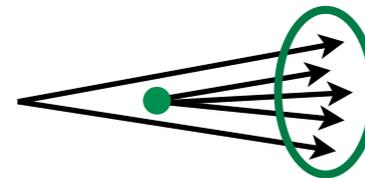
125 GeV

W/Z
 $\approx 70\%$



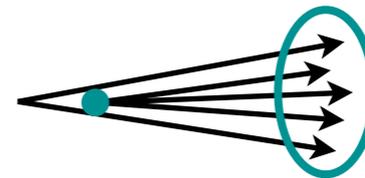
80/91 GeV

b



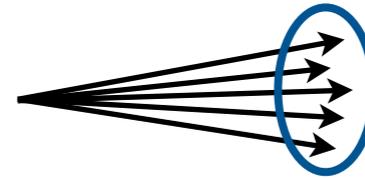
4.2 GeV++

c



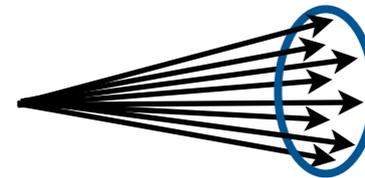
1.3 GeV++

u, d, s



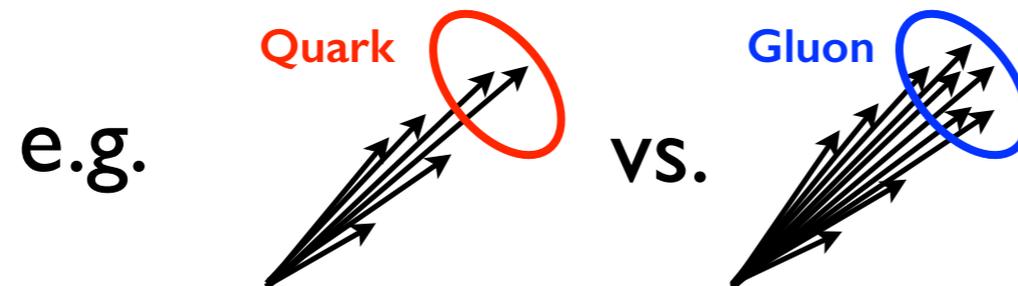
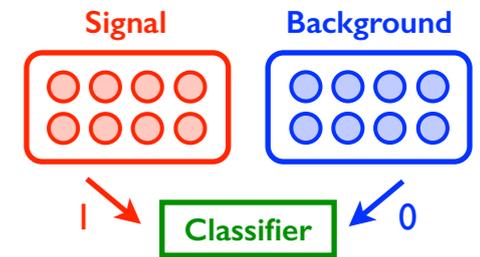
100 MeV++

gg

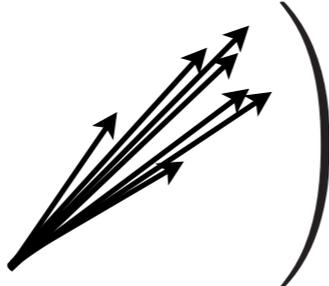


0++

Binary Classification



assuming trustable training data

Find h  such that

$$h(\text{Quark}) = 1$$
$$h(\text{Gluon}) = 0$$

Best you can do: $h(\mathcal{J}) = \frac{p(\mathcal{J}|\mathbf{Q})}{p(\mathcal{J}|\mathbf{Q}) + p(\mathcal{J}|\mathbf{G})}$
(Neyman-Pearson lemma)

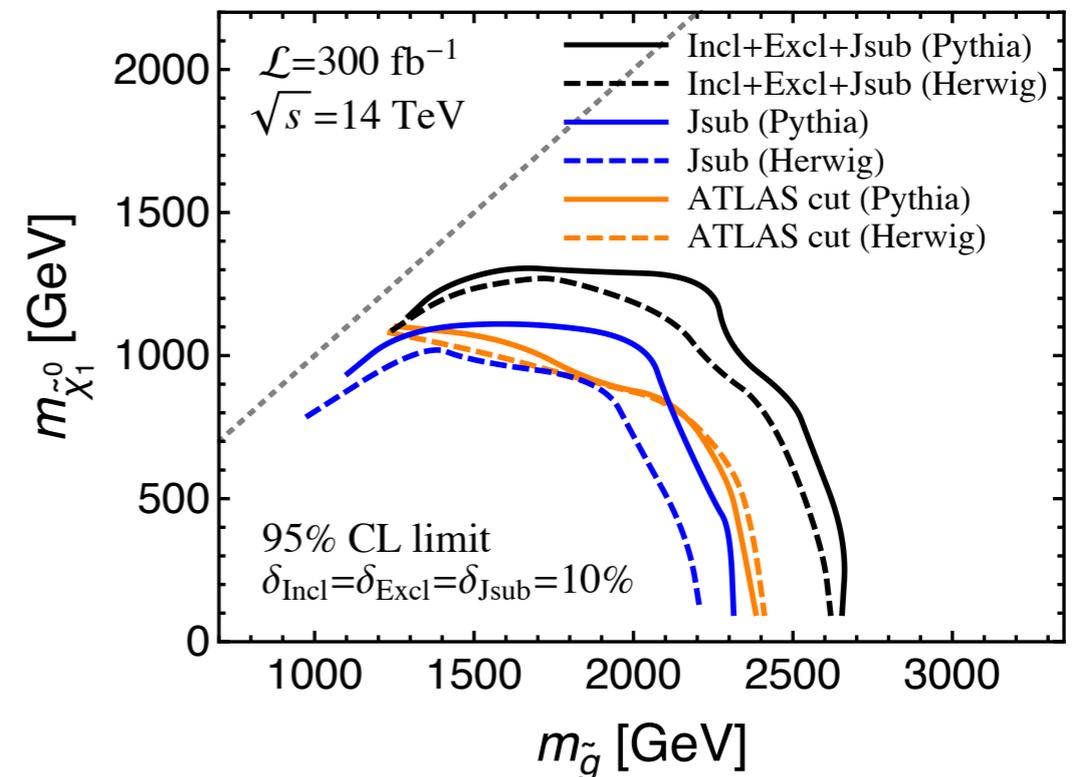
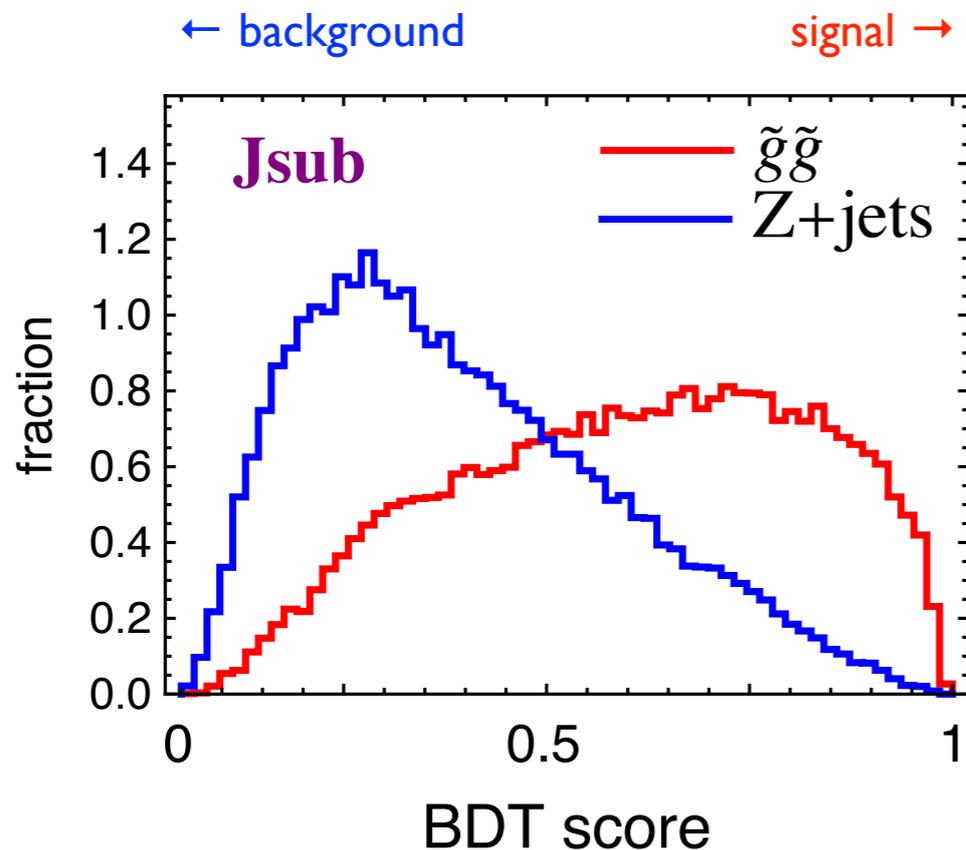
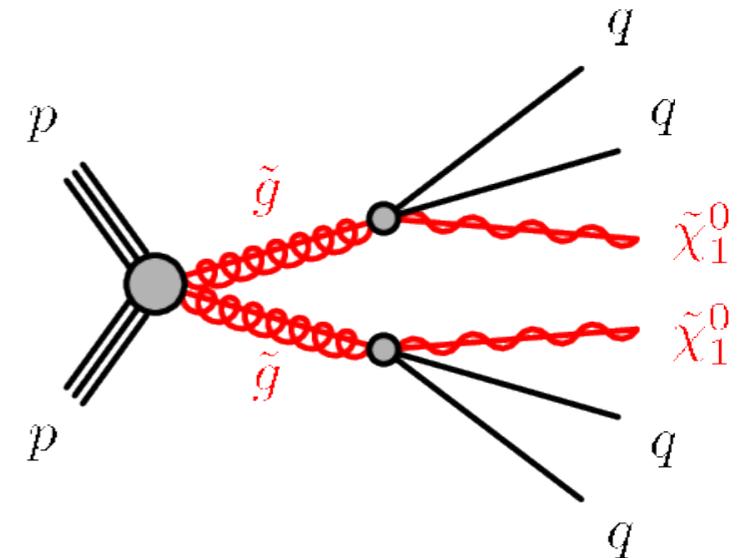
E.g. SUSY Search for Gluino Pairs

Classifier: Boosted decision tree (for each of 4 jets)

Inputs: Jet mass, width, track multiplicity

Signal: Quark enriched ($C_F = 4/3$)

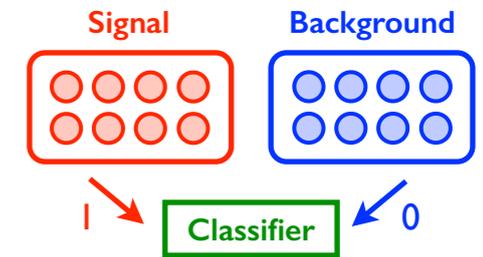
Background: Gluon enriched ($C_A = 3$)



[Bhattacharjee, Mukhopadhyay, Nojiri, Sakakie, Webber, [1609.08781](#)]

Jet Classification Studies

Mix and match



$$l_{\text{MSE}} = \left\langle (h(\vec{x}) - 1)^2 \right\rangle_{\text{signal}} + \left\langle (h(\vec{x}) - 0)^2 \right\rangle_{\text{background}}$$

Loss Function

Classifier

Inputs

Signal vs. Background

- Boosted Decision Tree
- Fisher Linear Discriminant
- Shallow Neural Network
- Deep Neural Network
- Convolutional Neural Network
- Recurrent Neural Network
- Recursive Neural Network
- Combination/Lorentz Layers
- ...

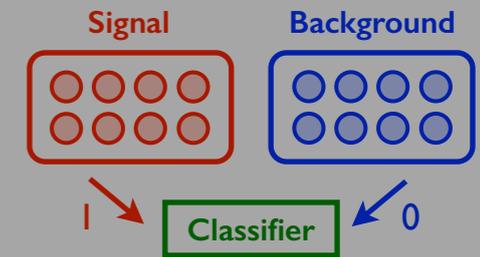
- High-Level Features
- Basis of High-Level Features
- Jet Image
- Multi-channel Jet Image
- Abstract Jet Image
- Sorted Four-Vectors
- Clustered Four-Vectors
- Lund Plane Emissions
- Kitchen Sink
- ...

- | | | |
|------------------------|-----|------------------|
| Quark Jets | vs. | Glue Jets |
| Up-type Quarks | vs. | Down-type Quarks |
| W/Z Bosons | vs. | QCD Jets |
| W Bosons | vs. | Z Bosons |
| Top Quarks | vs. | QCD Jets |
| Exotic Boosted Objects | vs. | QCD Jets |
| CMS Open Data Samples | vs. | Each other |
| ... | vs. | ... |

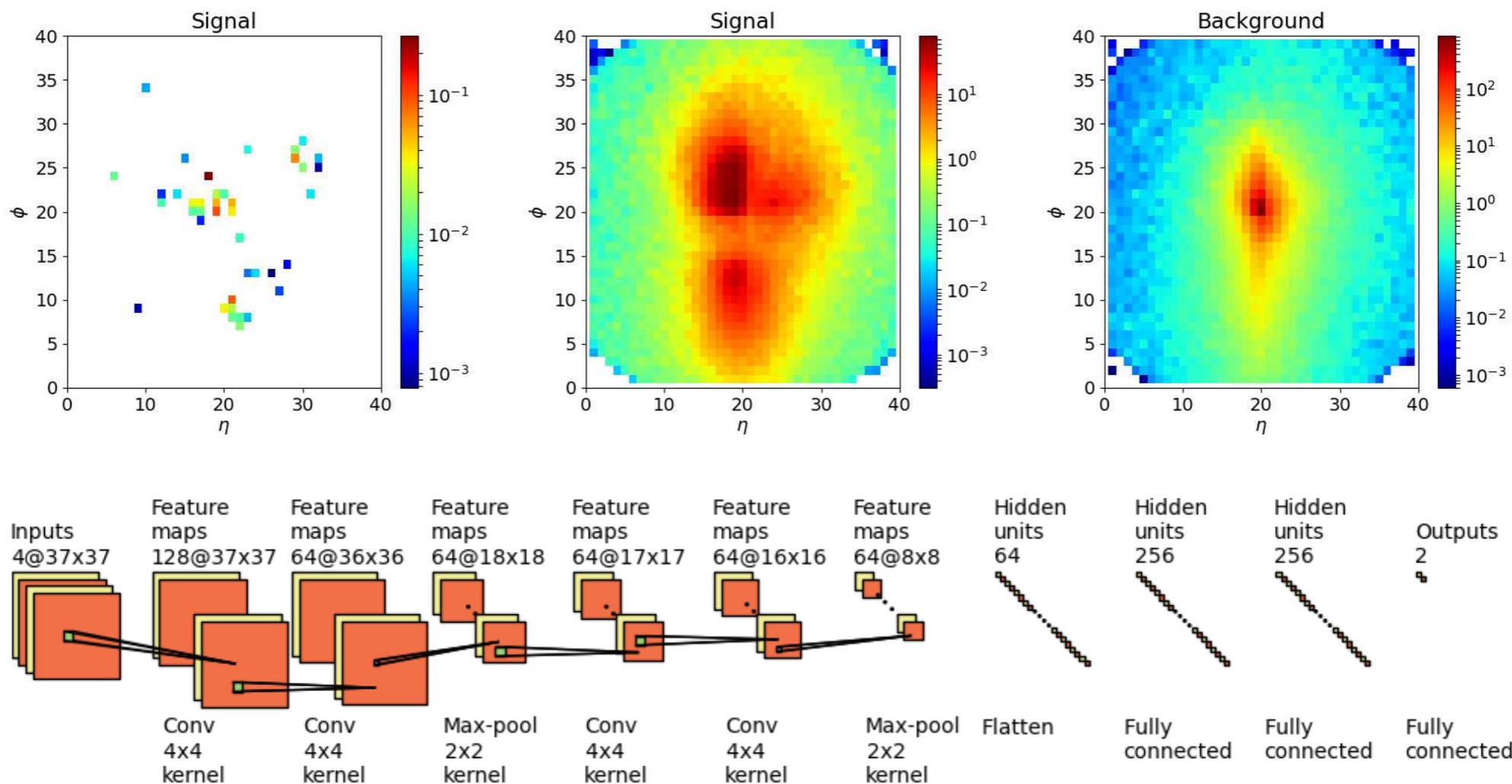
[Lönnblad, Peterson, Rognvaldsson, [PRL 1990](#), ..., Cogan, Kagan, Strauss, Schwartzman, [1407.5675](#); Almeida, Backović, Cliche, Lee, Perelstein, [1501.05968](#); de Oliveira, Kagan, Mackey, Nachman, Schwartzman, [1511.05190](#); Baldi, Bauer, Eng, Sadowski, Whiteson, [1603.09349](#); Conway, Bhaskar, Erbacher, Pilot, [1606.06859](#); Guest, Collado, Baldi, Hsu, Urban, Whiteson, [1607.08633](#); Barnard, Dawe, Dolan, Rajcic, [1609.00607](#); Komiske, Metodiev, Schwartz, [1612.01551](#); Kasieczka, Plehn, Russell, Schell, [1701.08784](#); Louppe, Cho, Becot, Cranmer, [1702.00748](#); Parkes, Fedorko, Lister, Gay, [1704.02124](#); Datta, Larkoski, [1704.08249](#), [1710.01305](#); Butter, Kasieczka, Plehn, Russell, [1707.08966](#); Fernández Madrazo, Heredia Cacha, Lloret Iglesias, Marco de Lucas, [1708.07034](#); Aguilar Saavedra, Collin, Mishra, [1709.01087](#); Cheng, [1711.02633](#); Luo, Luo, Wang, Xu, Zhu, [1712.03634](#); Komiske, Metodiev, JDT, [1712.07124](#); Macaluso, Shih, [1803.00107](#); Fraser, Schwartz, [1803.08066](#); Choi, Lee, Perelstein, [1806.01263](#); Lim, Nojiri, [1807.03312](#); Dreyer, Salam, Soye, [1807.04758](#); Moore, Nordström, Varma, Fairbairn, [1807.04769](#); plus many ATLAS/CMS performance studies; plus my friends who will scold me for forgetting their paper (and not updating this after July 23, 2018)]

Jet Classification Studies

Mix and match

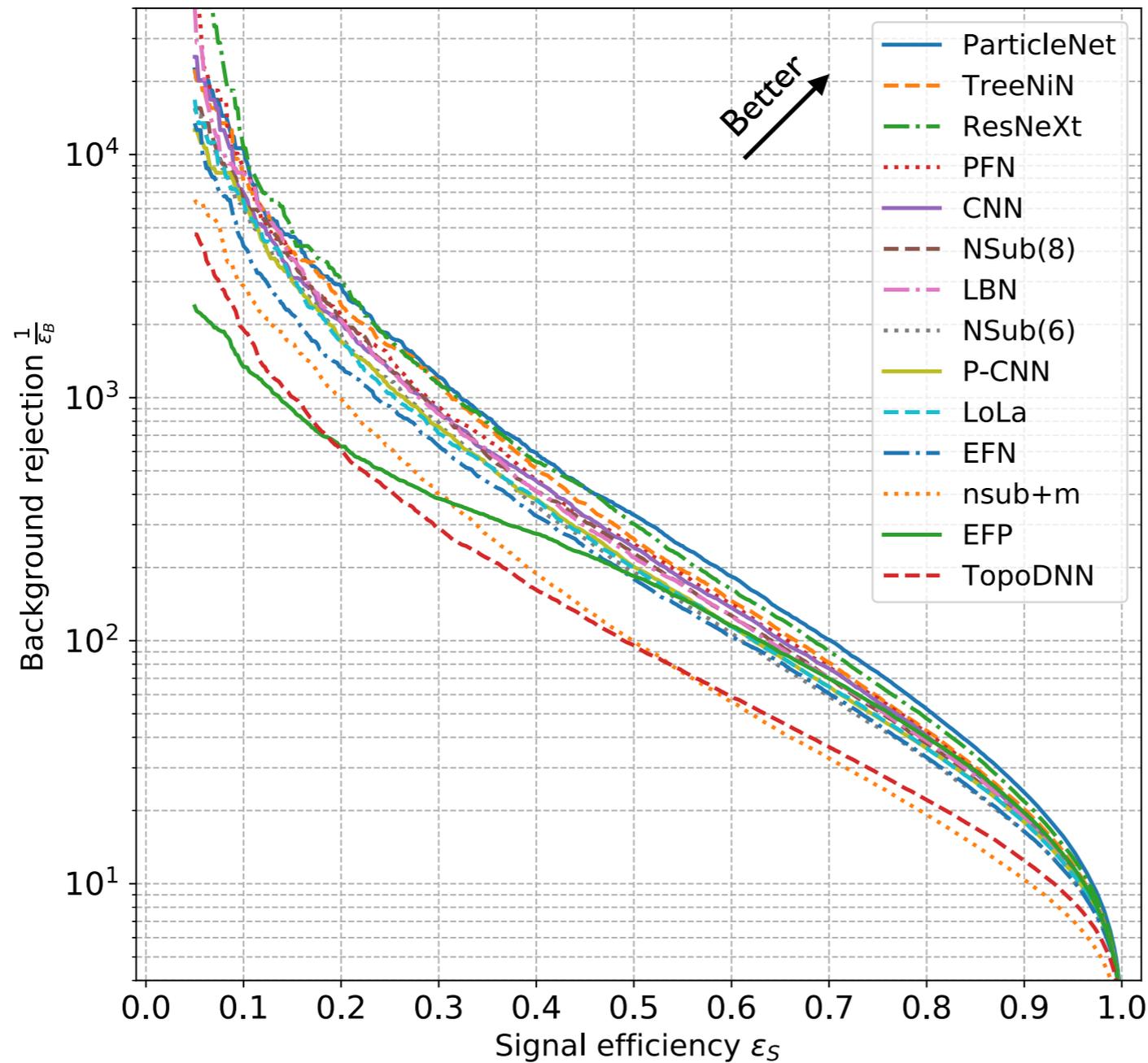
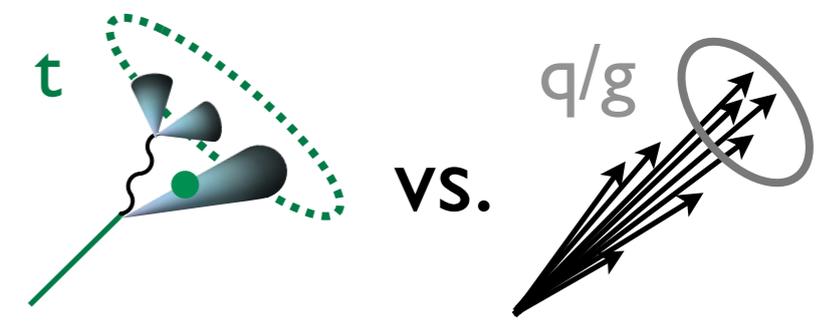


Deep Learning: Jet Image Strategy with CNNs



[Macaluso, Shih [1803.00107](#); building off Kasieczka, Plehn, Russell, Schell, [1701.08784](#); based on Cogan, Kagan, Strauss, Schwartzman, [1407.5675](#); de Oliveira, Kagan, Mackey, Nachman, Schwartzman, [1511.05190](#)]

Throwing Down the Gauntlet



← “Deep Pockets”
 ← Previous slide
 ← Next section
 ← “Deep Thinking”

[Kasieczka, Plehn, et al., [1902.09914](#);
 comparison of [JDT, Van Tilburg, 1011.2268, 1108.2701](#); [Xie, Girshick, Dollár, Tu, He, 1611.05431](#); CMS-DP-2017-049; Pearkes, Fedorko, Lister, Gay, [1704.02124](#);
 Butter, Kasieczka, Plehn, Russell, [1707.08966](#); Komiske, Metodiev, JDT, [1712.07124](#); [Macaluso, Shih 1803.00107](#); Moore, Nordström, Varma, Fairbairn [1807.04769](#);
 Komiske, Metodiev, JDT, [1810.05165](#); Erdmann, Geiser, Rath, Rieger, [1812.09722](#); Qu, Gouskos, [1902.08570](#); Macaluso, Cranmer, to appear]

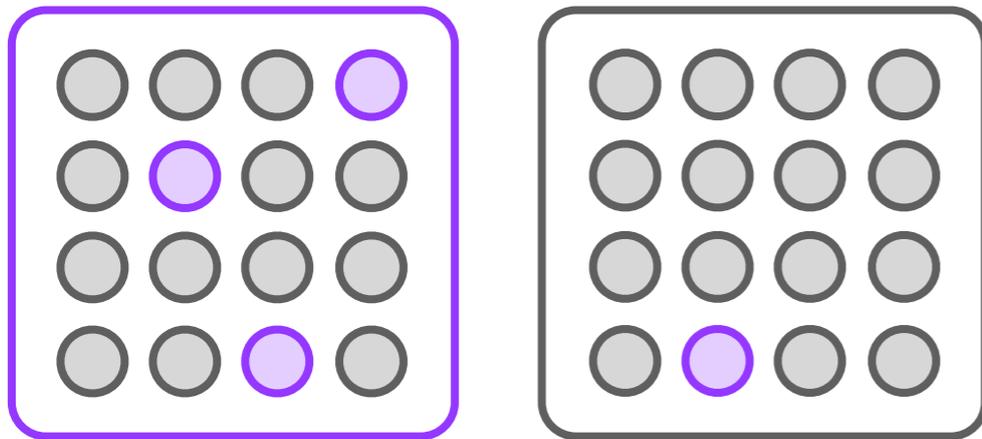
CWoLa Hunting

Using “Classification Without Labels”



Signal Region

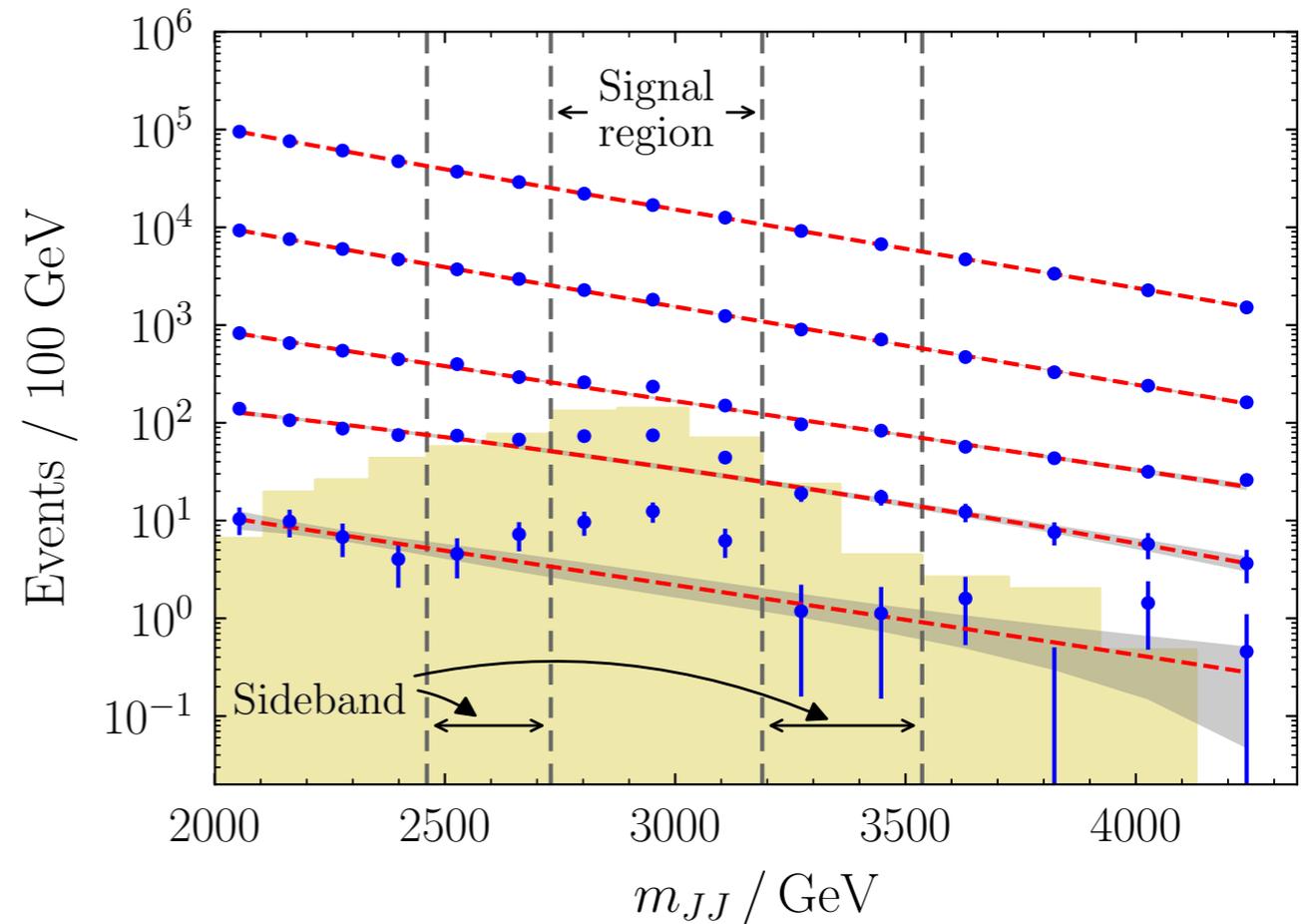
Sideband



Classifier

With enough data, monotonic
w.r.t. optimal classifier (!)

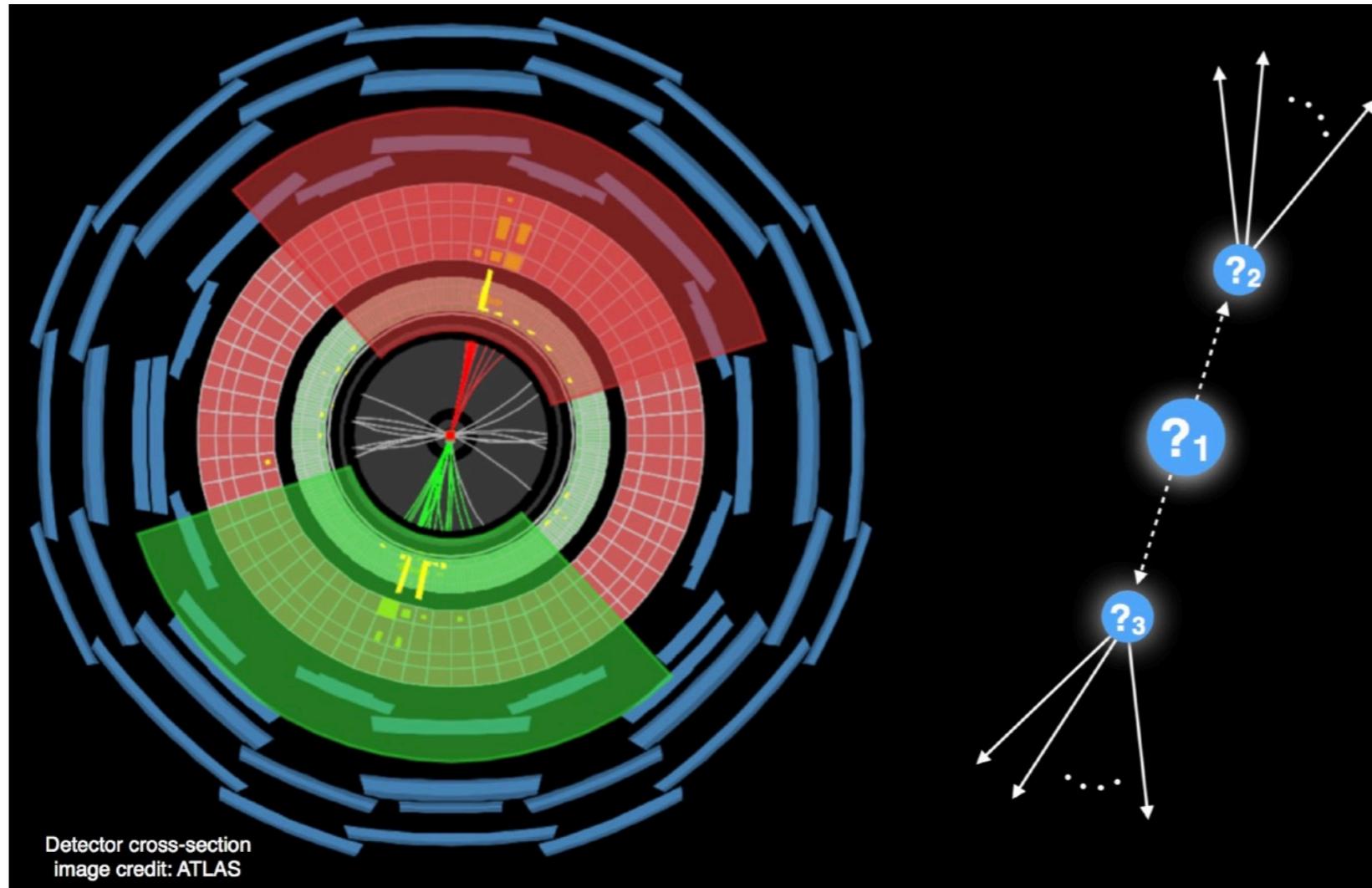
Model-Agnostic Bump Hunt



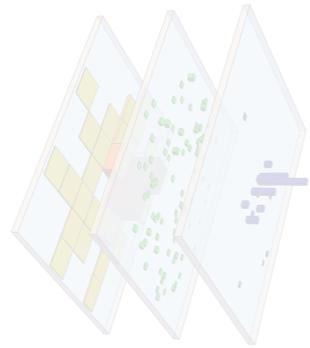
[Collins, Howe, Nachman, [1805.02664](#), [1902.02634](#); using Metodiev, Nachman, [JDT, 1708.02949](#); see also Blanchard, Flaska, Handy, Pozzi, Scott, [1303.1208](#); Cranmer, Pavez, Louppe, [1506.02169](#)]

LHC Olympics 2020

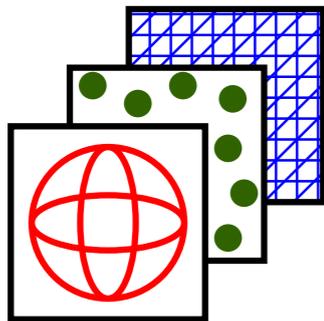
@ ML4Jets, NYU, January 15-17



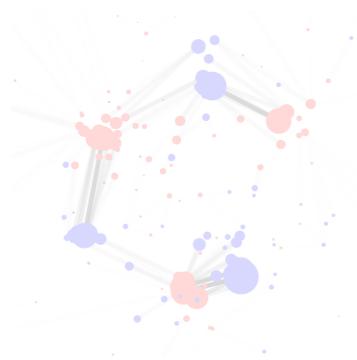
An opportunity to stress test new **anomaly detection** strategies



The Rise of Deep Learning



Looking Inside the Black Box

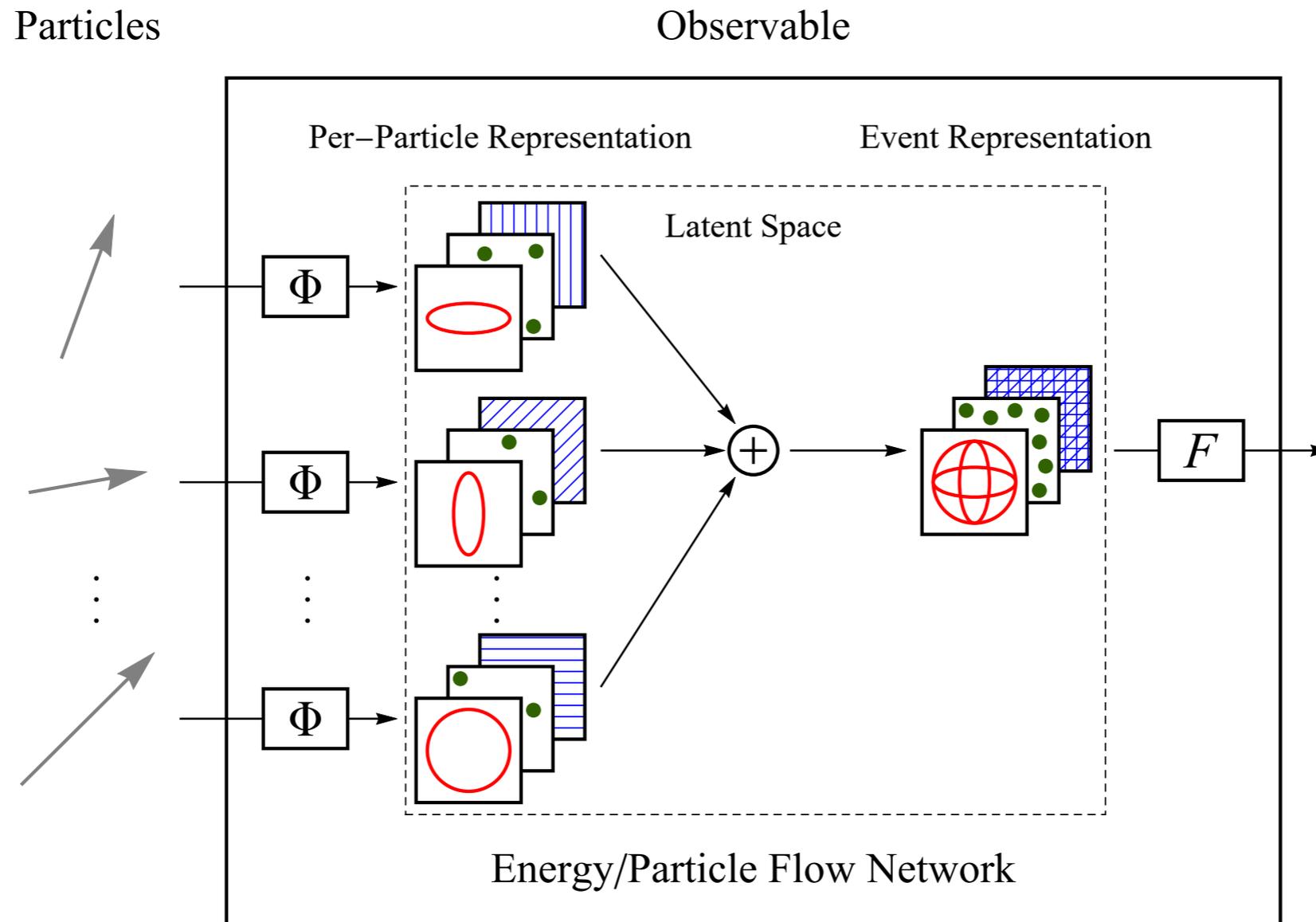


(Exploring the Space of Jets)

Introducing Energy Flow Networks

An architecture designed for interpretability

(see backup for detailed architecture)



[Komiske, Metodiev, JDT, [1810.05165](#);
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#)]

Introducing Energy Flow Networks

(see backup for detailed architecture)

An architecture designed for interpretability

$$S(\mathcal{J}) = F(V_1, V_2, \dots, V_\ell) \quad V_a(\mathcal{J}) = \sum_{i \in \mathcal{J}} p_{Ti} \Phi_a(y_i, \phi_i)$$

Latent space of dim ℓ

Linear weights

Parametrized with **Neural Networks**

Flexible enough to describe any* **IRC-safe** observable
(assuming large enough ℓ)

Generalization: Particle Flow Networks (aka “Deep Sets”)

[Komiske, Metodiev, JDT, [1810.05165](#);
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#)]

Introducing Energy Flow Networks

(see backup for detailed architecture)

An architecture designed for interpretability

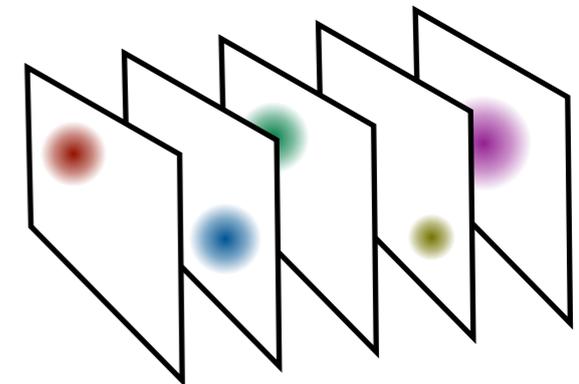
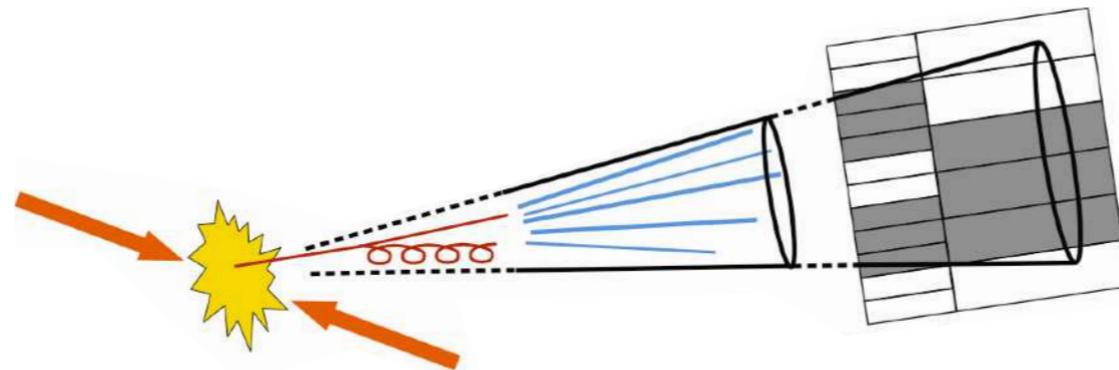
Visualization Strategy

$$S(\mathcal{J}) = F(V_1, V_2, \dots, V_\ell)$$

↑
Difficult to visualize
(unless ℓ is small)

$$V_a(\mathcal{J}) = \sum_{i \in \mathcal{J}} p_{Ti} \Phi_a(y_i, \phi_i)$$

↑
Easy to plot these!



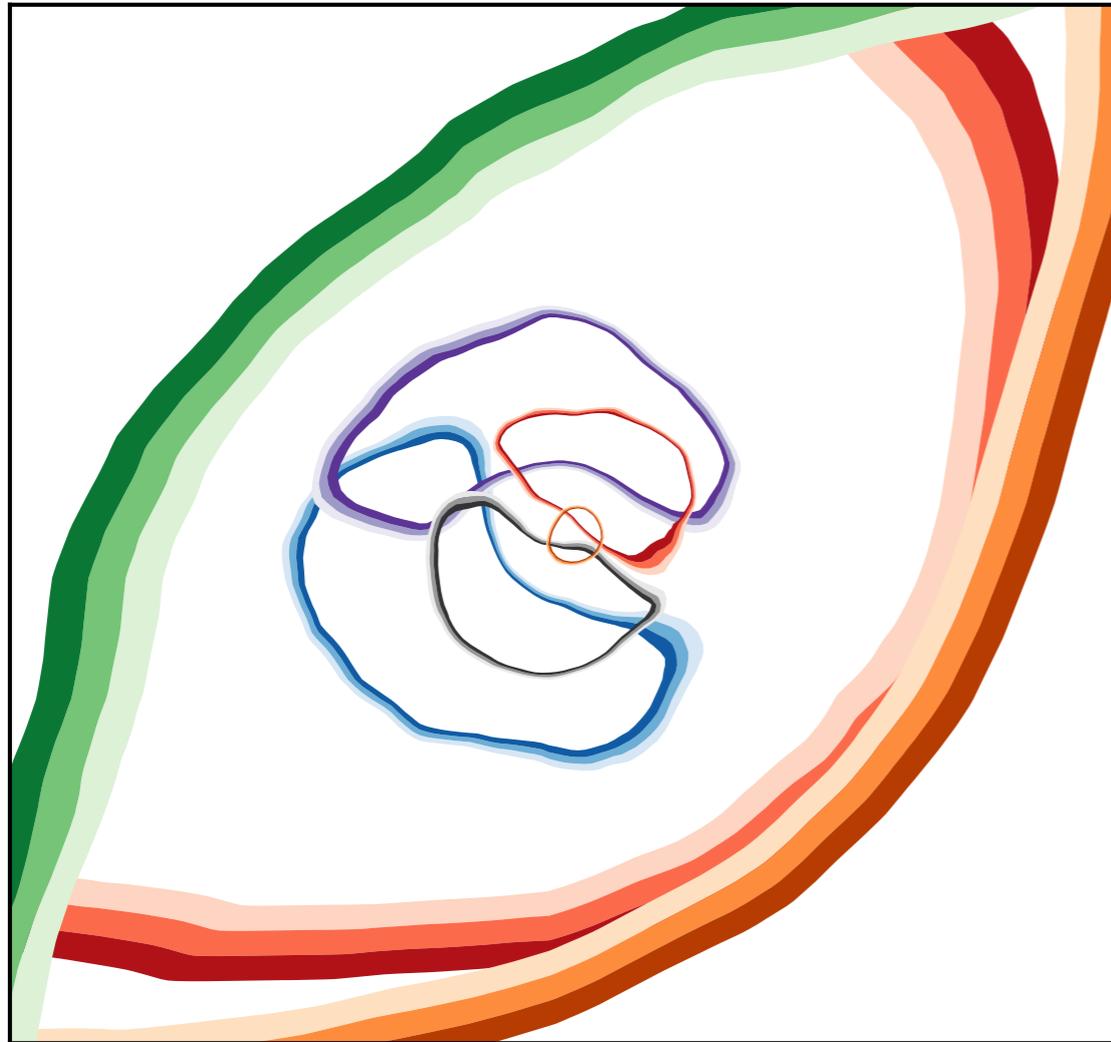
(similar to CNN
filter activation)

[Komiske, Metodiev, JDT, [1810.05165](#);
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#)]

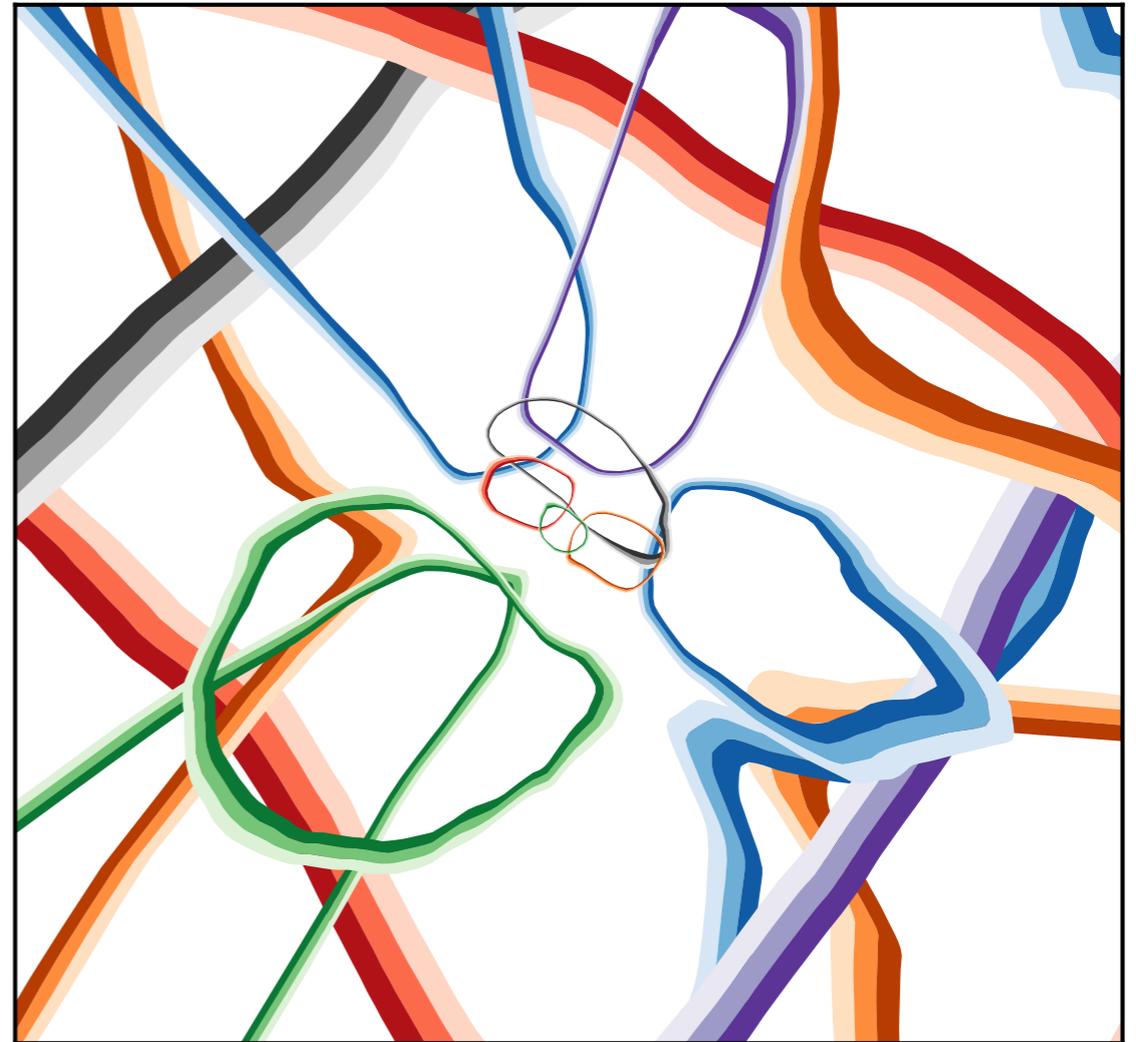
Psychedelic Network Visualization

(see backup for
how these are made)

Latent Dimension 8



Latent Dimension 16

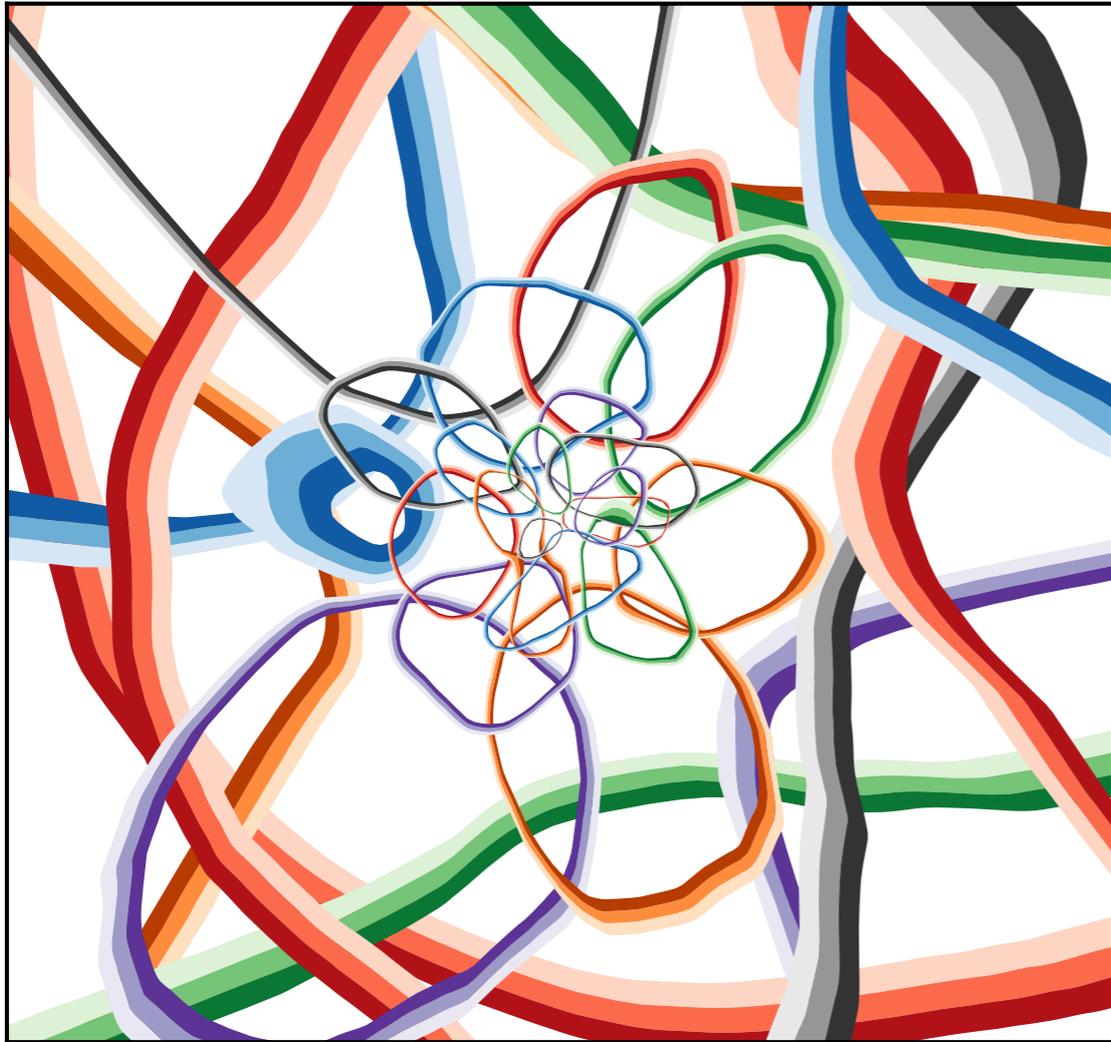


For the case of **quark** vs. **gluon** classification

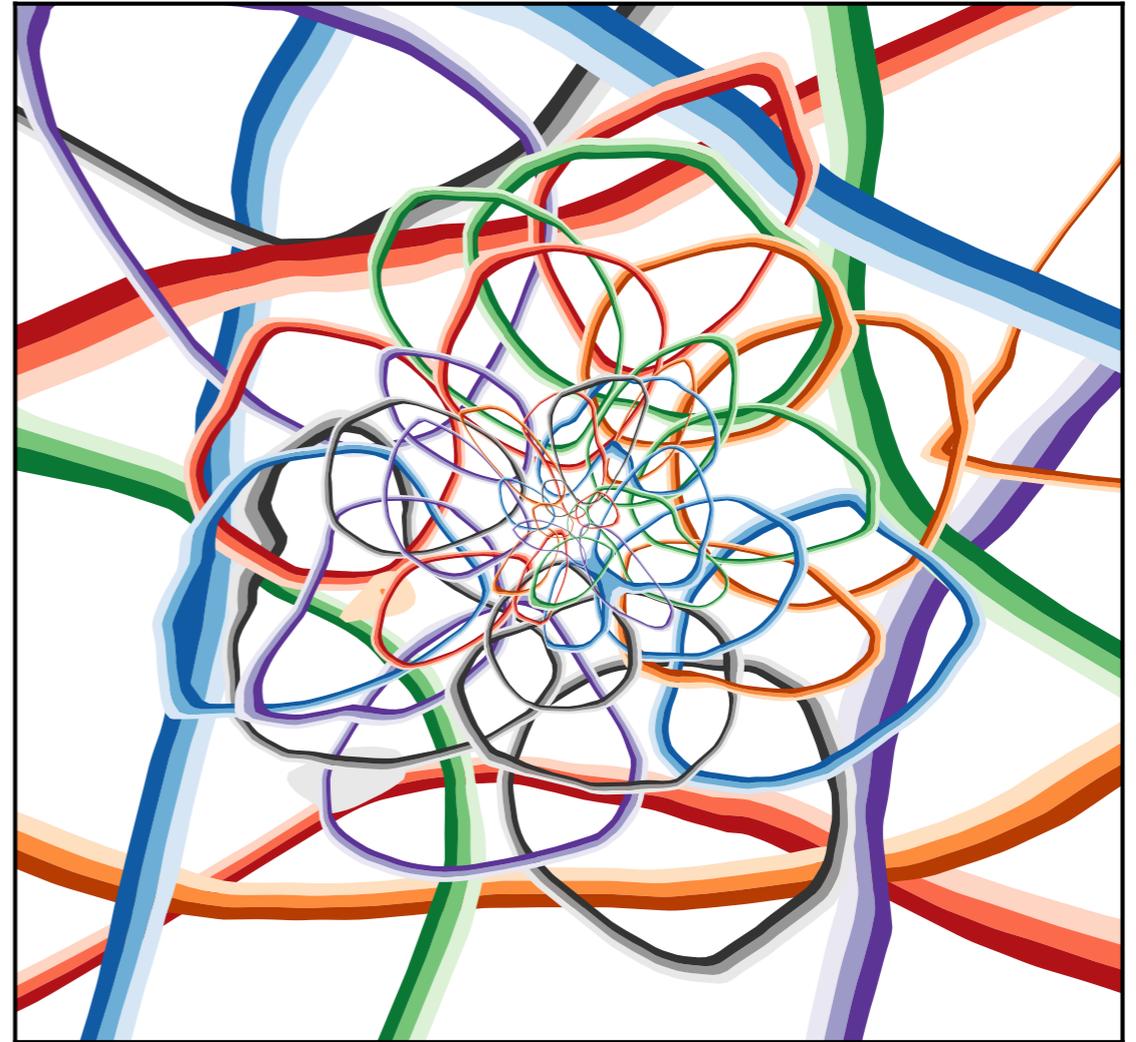
Psychedelic Network Visualization

(see backup for
how these are made)

Latent Dimension 32



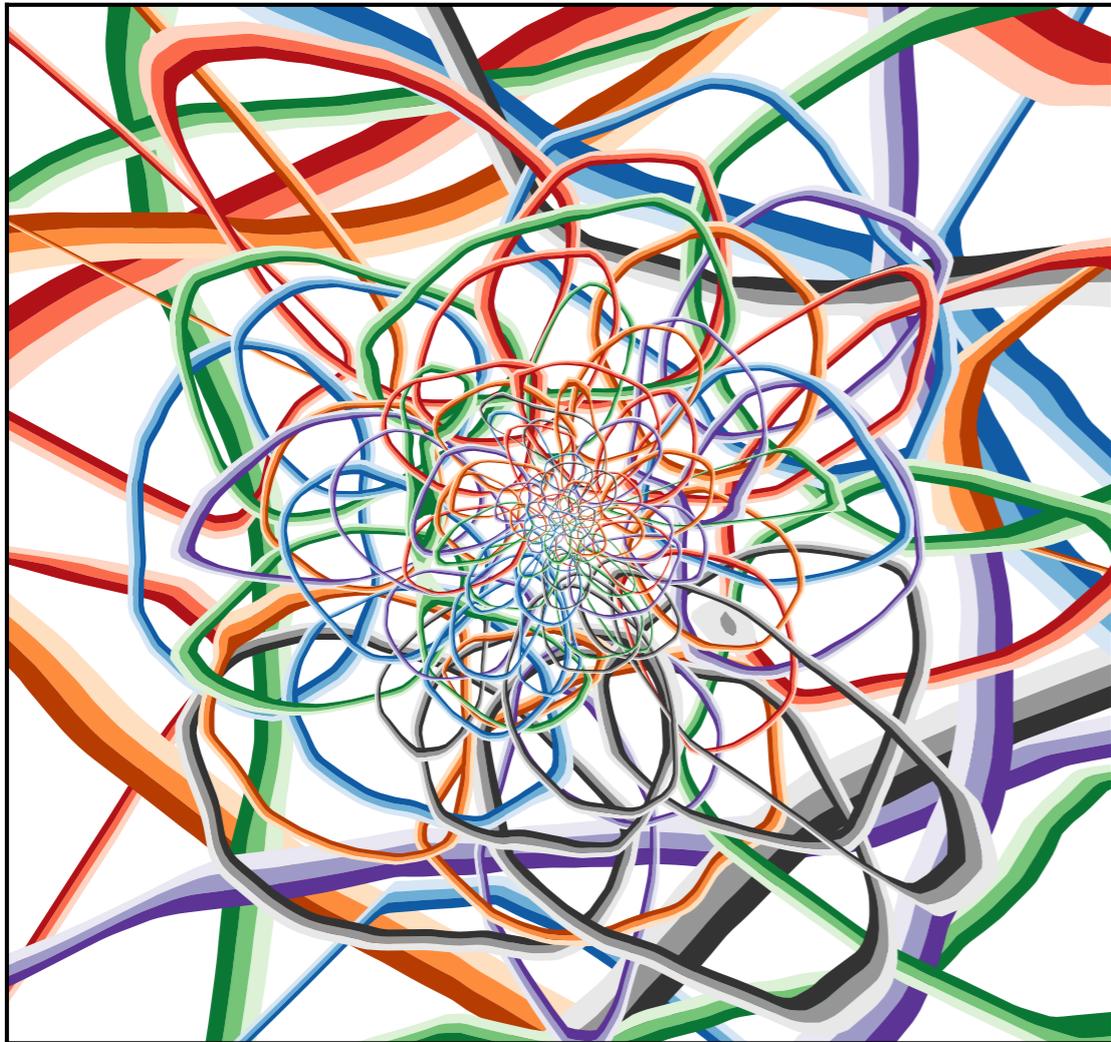
Latent Dimension 64



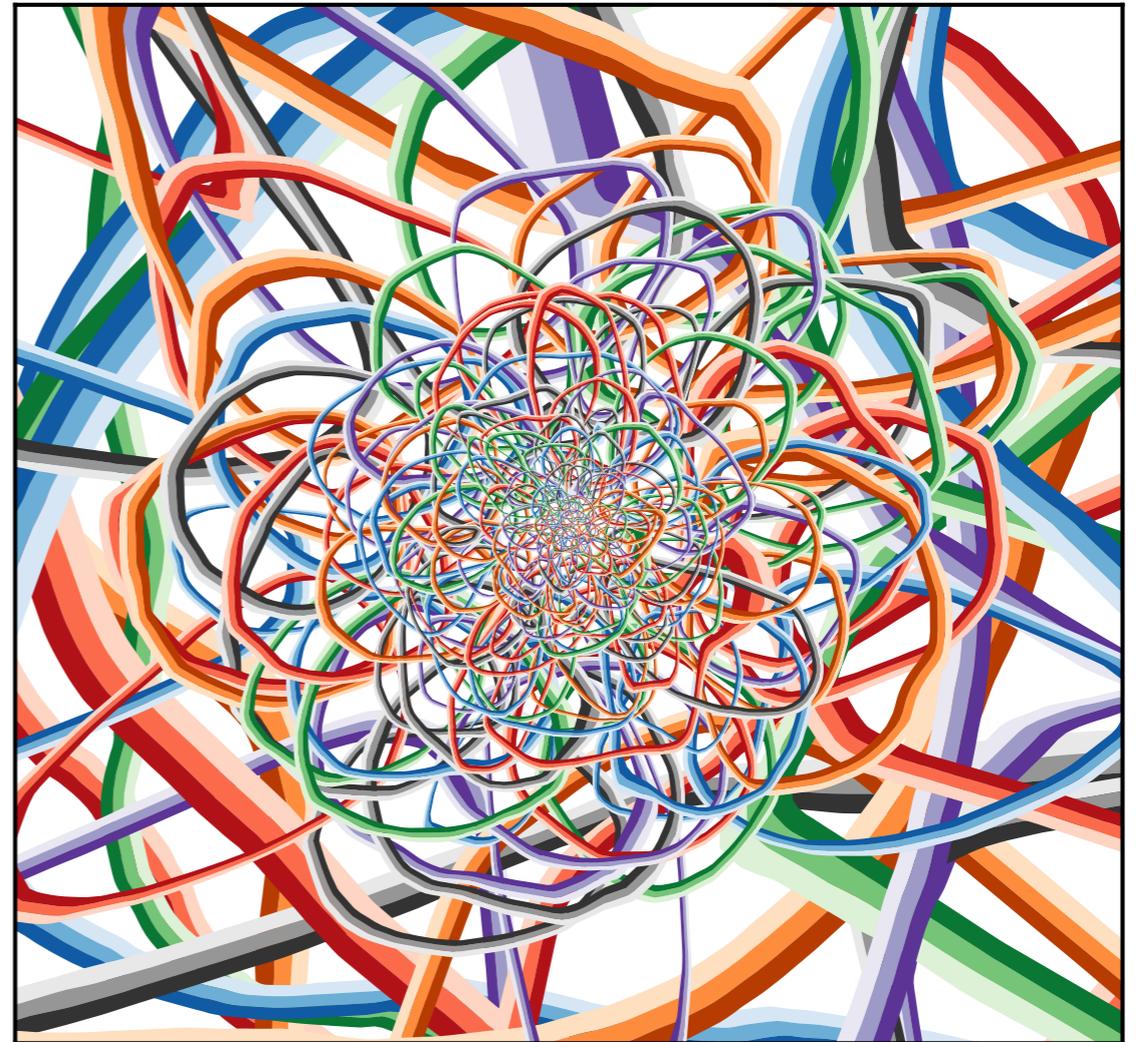
Psychedelic Network Visualization

(see backup for
how these are made)

Latent Dimension 128

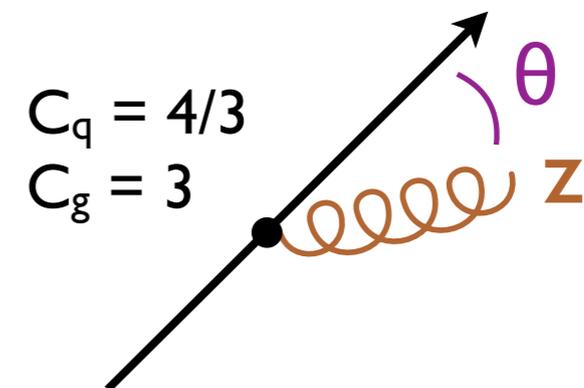
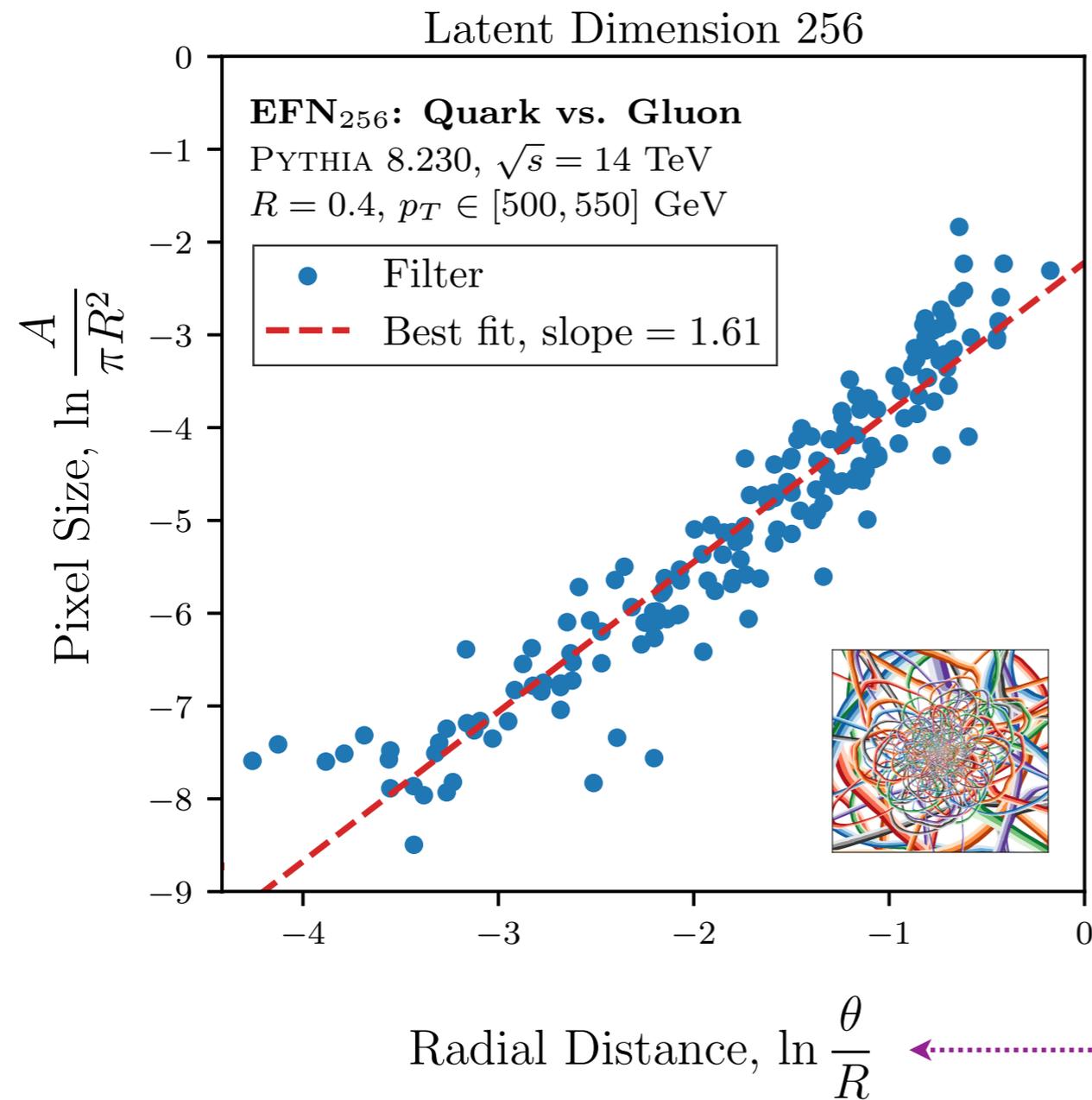


Latent Dimension 256



Singularity structure of QCD!

Putting the AI in Altarelli-Parisi

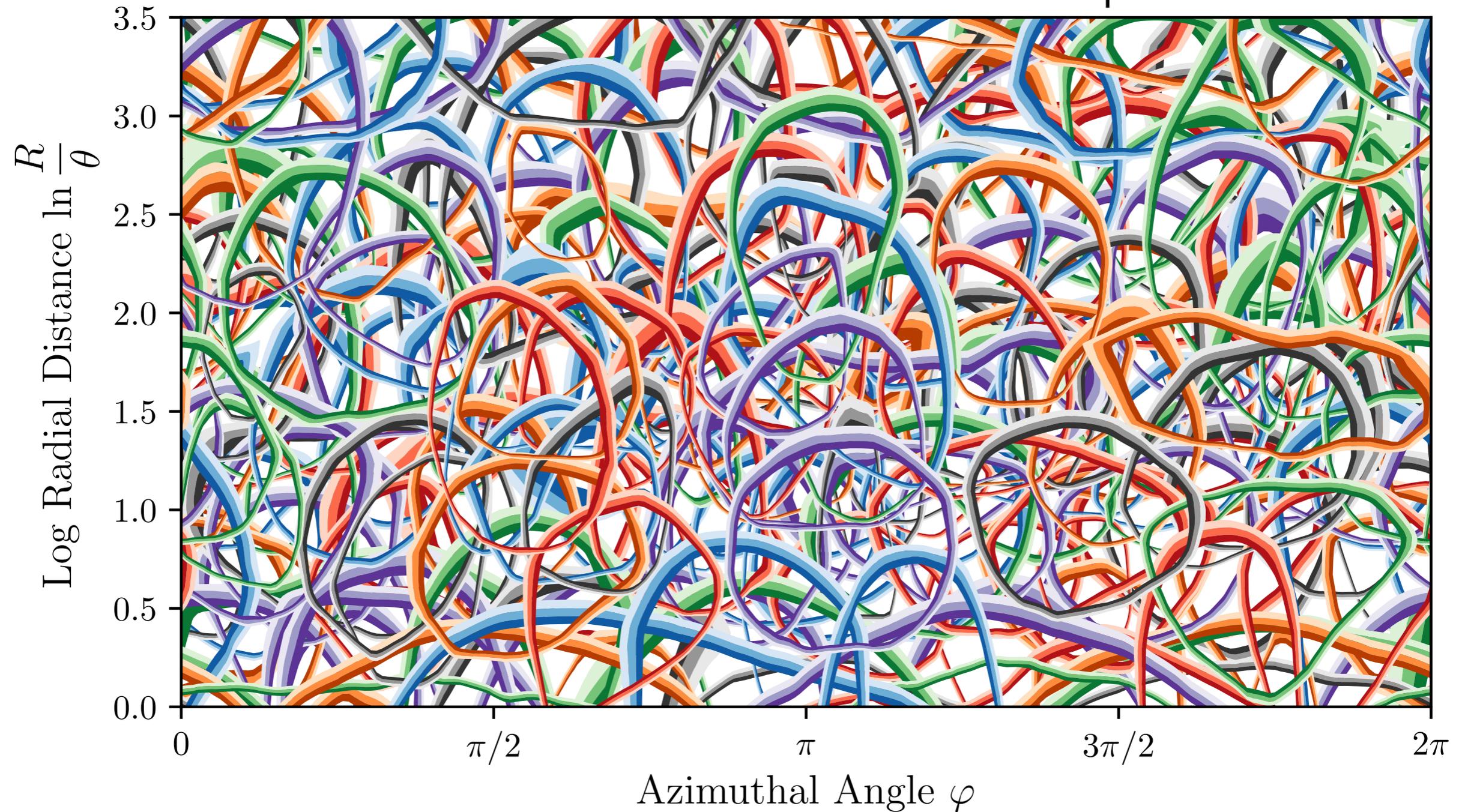


$$dP_{i \rightarrow ig} \simeq \frac{2\alpha_s}{\pi} C_i \underbrace{\frac{d\theta}{\theta}}_{\text{Collinear}} \underbrace{\frac{dz}{z}}_{\text{Soft}}$$

[Komiske, Metodiev, JDT, 1810.05165]

Ready for the CMOA?

Coordinate transformation to the emission plane

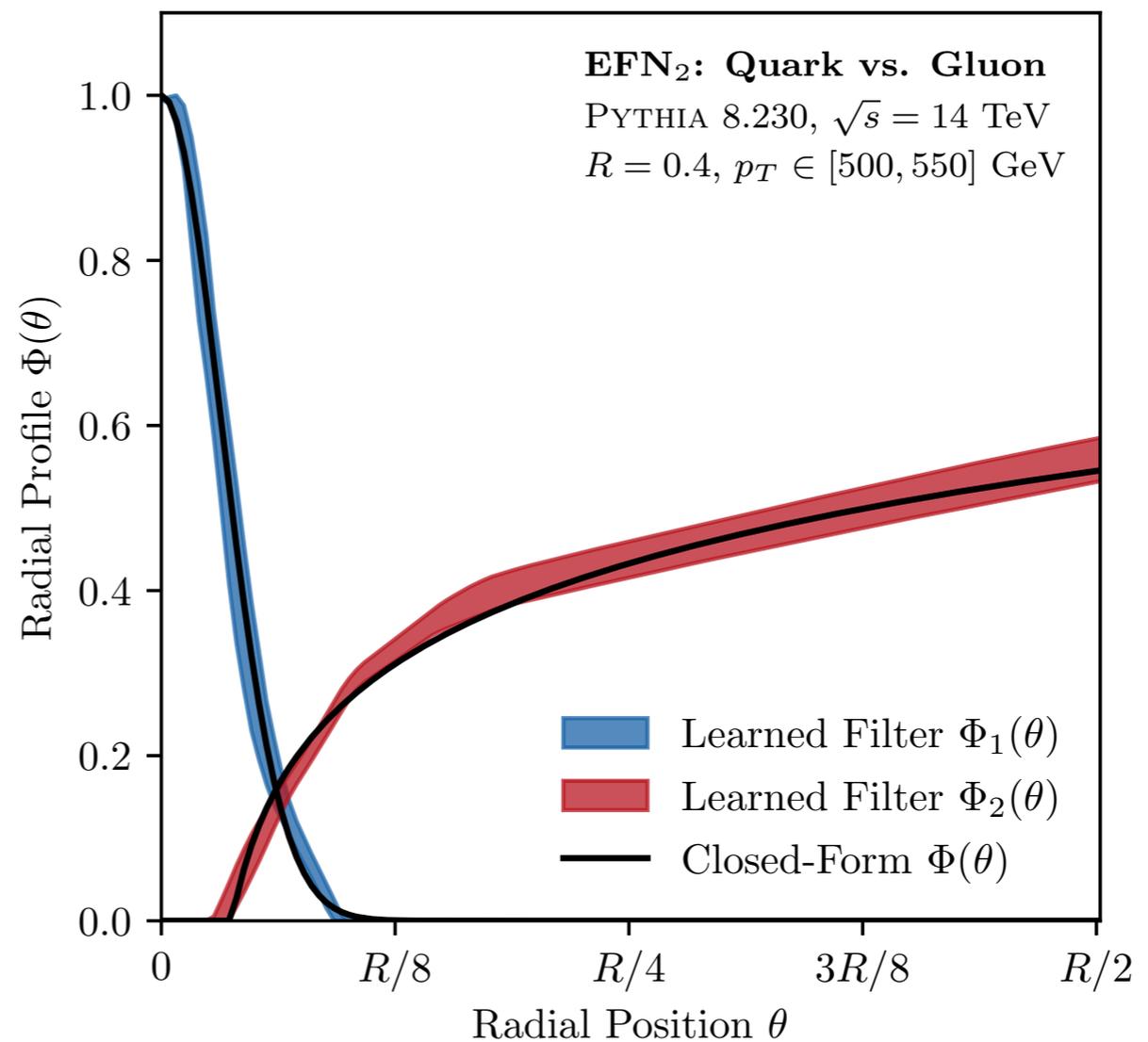
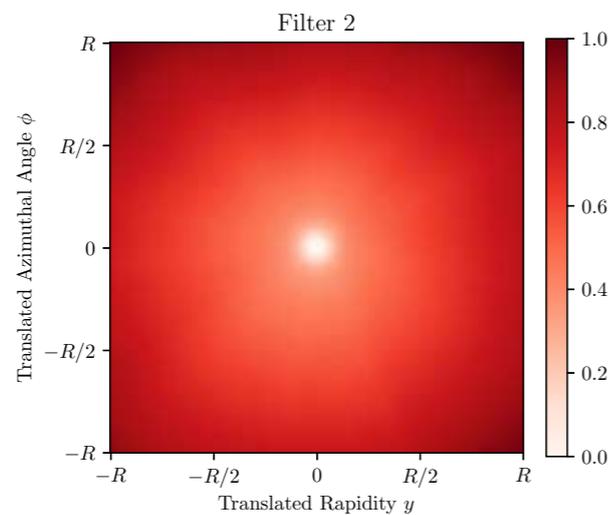
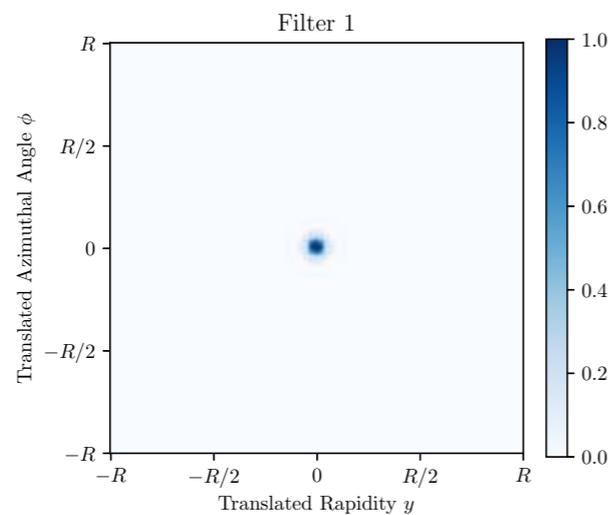


[Komiske, Metodiev, JDT, [1810.05165](#); see also Dreyer, Salam, Soyez, [1807.04758](#)]

*“Ok, but did you really learn something
you didn’t already know?”*

Learning from the Machine

For $\ell = 2$ EFN, radial moments: $\sum_{i \in \text{jet}} z_i f(\theta_i)$ cf. Angularities:
 $f(\theta) = \theta^\beta$

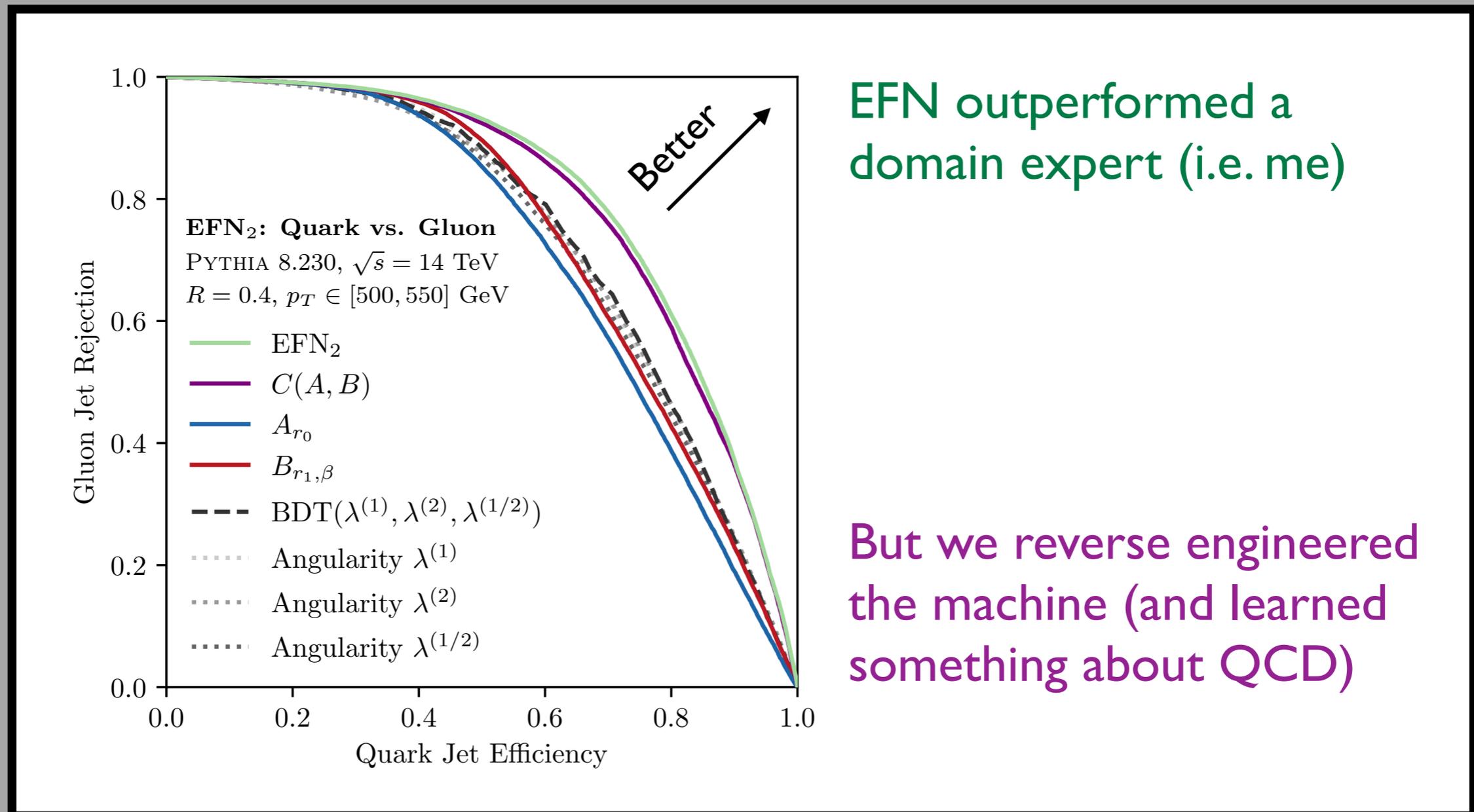


[Komiske, Metodiev, JDT, 1810.05165]

Learning from the Machine

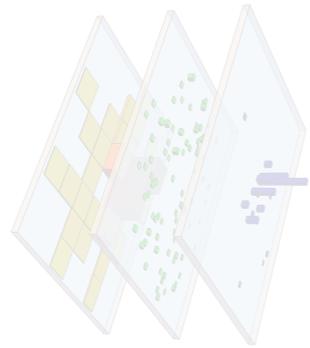
For $\ell = 2$ EFN, radial moments: $\sum_{i \in \text{jet}} z_i f(\theta_i)$

cf. Angularities:
 $f(\theta) = \theta^\beta$

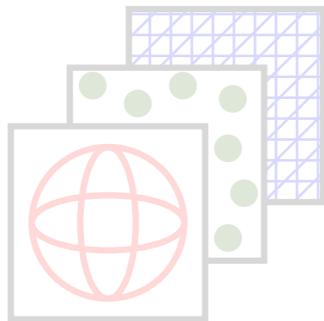


EFN outperformed a domain expert (i.e. me)

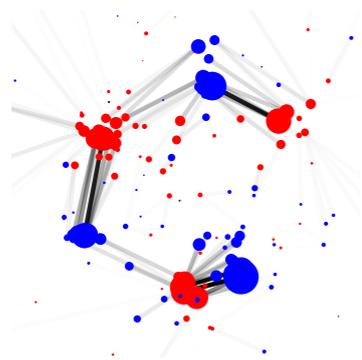
But we reverse engineered the machine (and learned something about QCD)



The Rise of Deep Learning



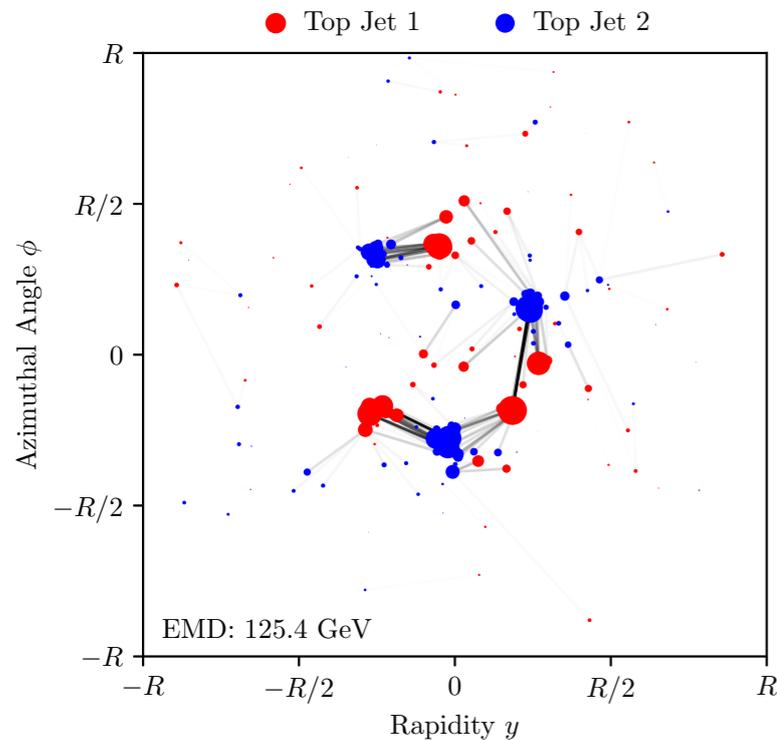
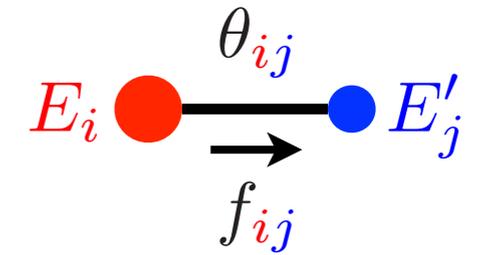
Looking Inside the Black Box



(Exploring the Space of Jets)

The Energy Mover's Distance

Closely related to 1-Wasserstein metric



Optimal transport between energy flows...

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \underbrace{\sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R}}_{\text{Cost to move energy}} + \underbrace{\left| \sum_i E_i - \sum_j E'_j \right|}_{\text{Cost to create energy}}$$

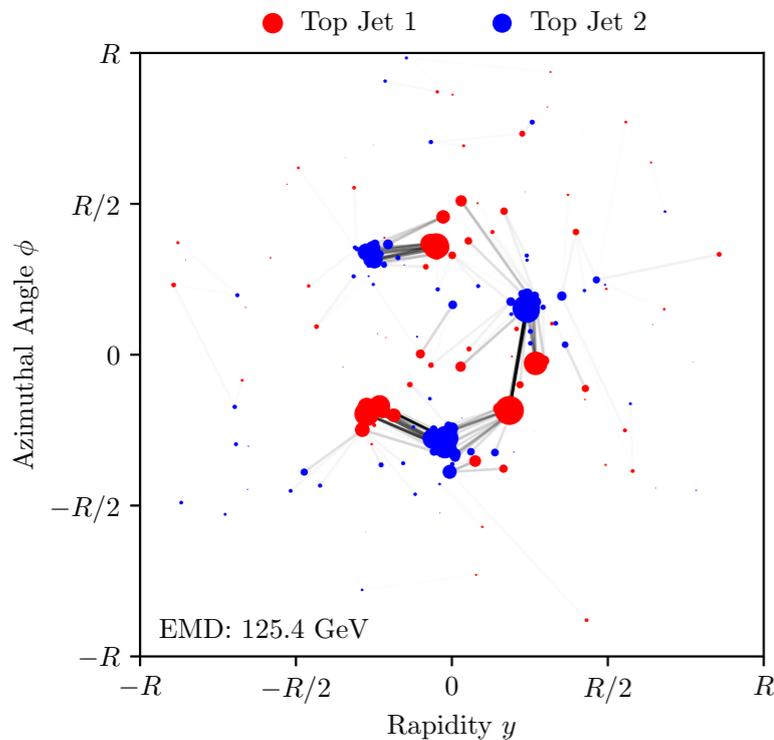
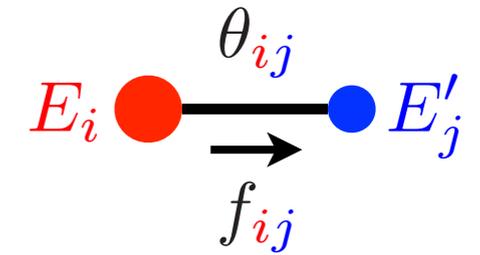
in GeV

[Komiske, Metodiev, JDT, 1902.02346;

see also Peleg, Werman, Rom, IEEE 1989; Rubner, Tomasi, Guibas, ICCV 1998, ICJV 2000; Pele, Werman, ECCV 2008; Pele Taskar, GSI 2013]

The Energy Mover's Distance

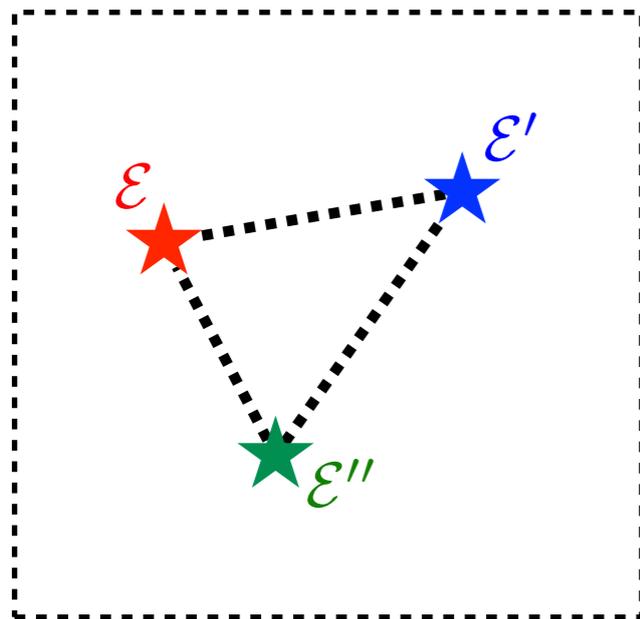
Closely related to 1-Wasserstein metric



Optimal transport between energy flows...

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \underbrace{\sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R}}_{\text{Cost to move energy}} + \underbrace{\left| \sum_i E_i - \sum_j E'_j \right|}_{\text{Cost to create energy}}$$

↑
in GeV



...defines a metric on the space of events

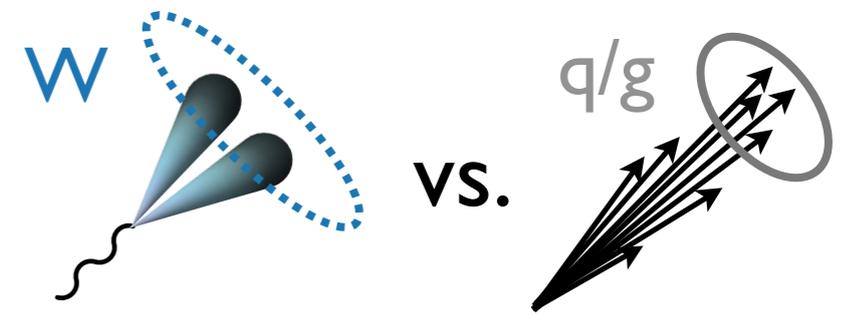
$$0 \leq \text{EMD}(\mathcal{E}, \mathcal{E}') \leq \text{EMD}(\mathcal{E}, \mathcal{E}'') + \text{EMD}(\mathcal{E}', \mathcal{E}'')$$

(assuming $R \geq \theta_{\max}/2$, i.e. $R \geq$ jet radius for conical jets)

[Komiske, Metodiev, JDT, 1902.02346;

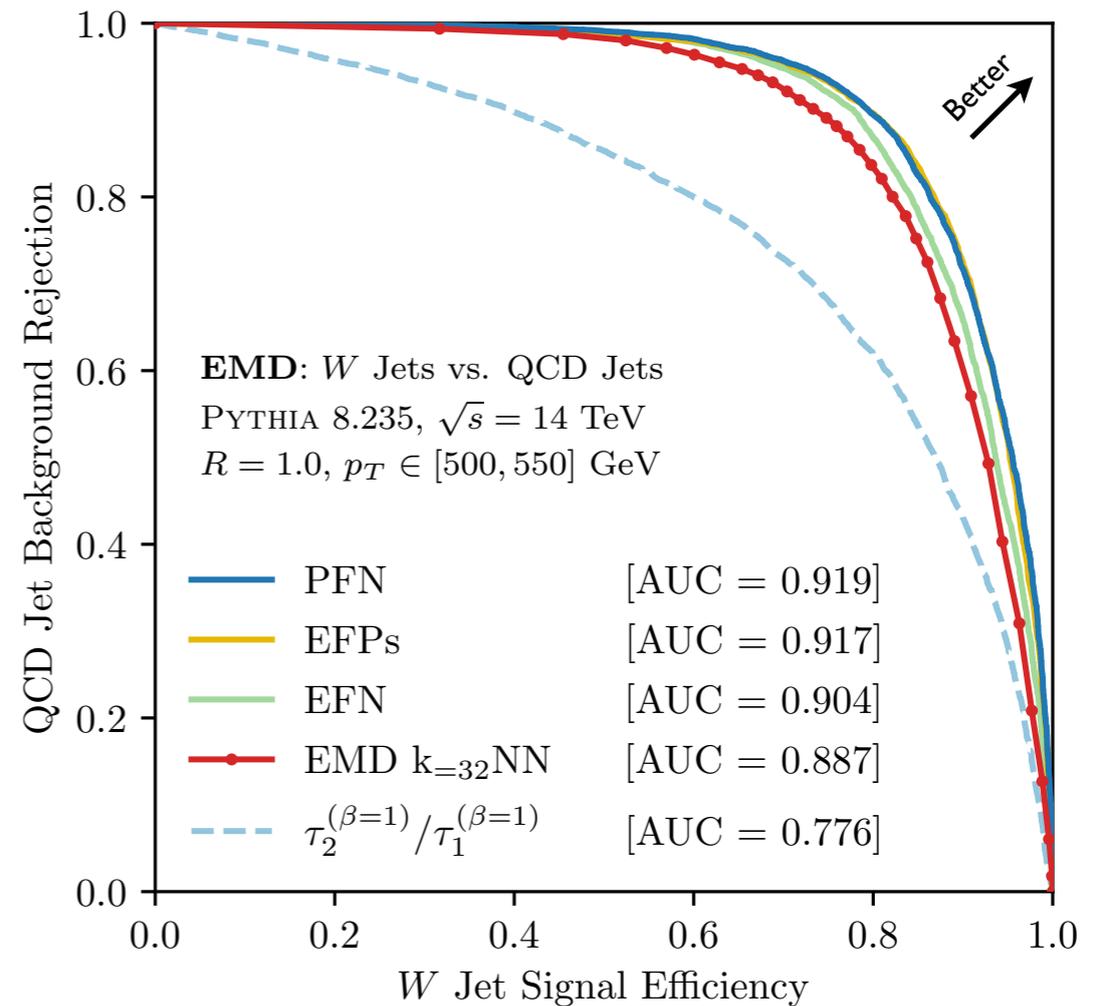
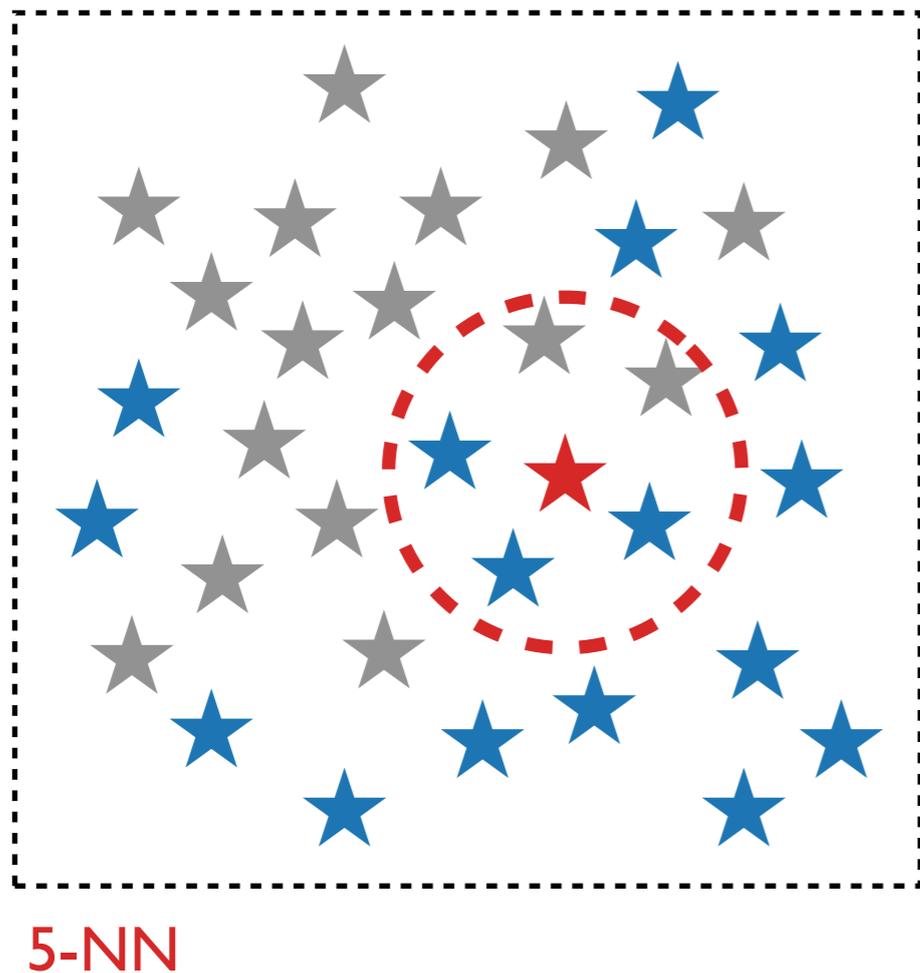
see also Peleg, Werman, Rom, IEEE 1989; Rubner, Tomasi, Guibas, ICCV 1998, ICJV 2000; Pele, Werman, ECCV 2008; Pele Taskar, GSI 2013]

Revisiting Jet Classification



Estimate jet label by **k nearest neighbors** in training data

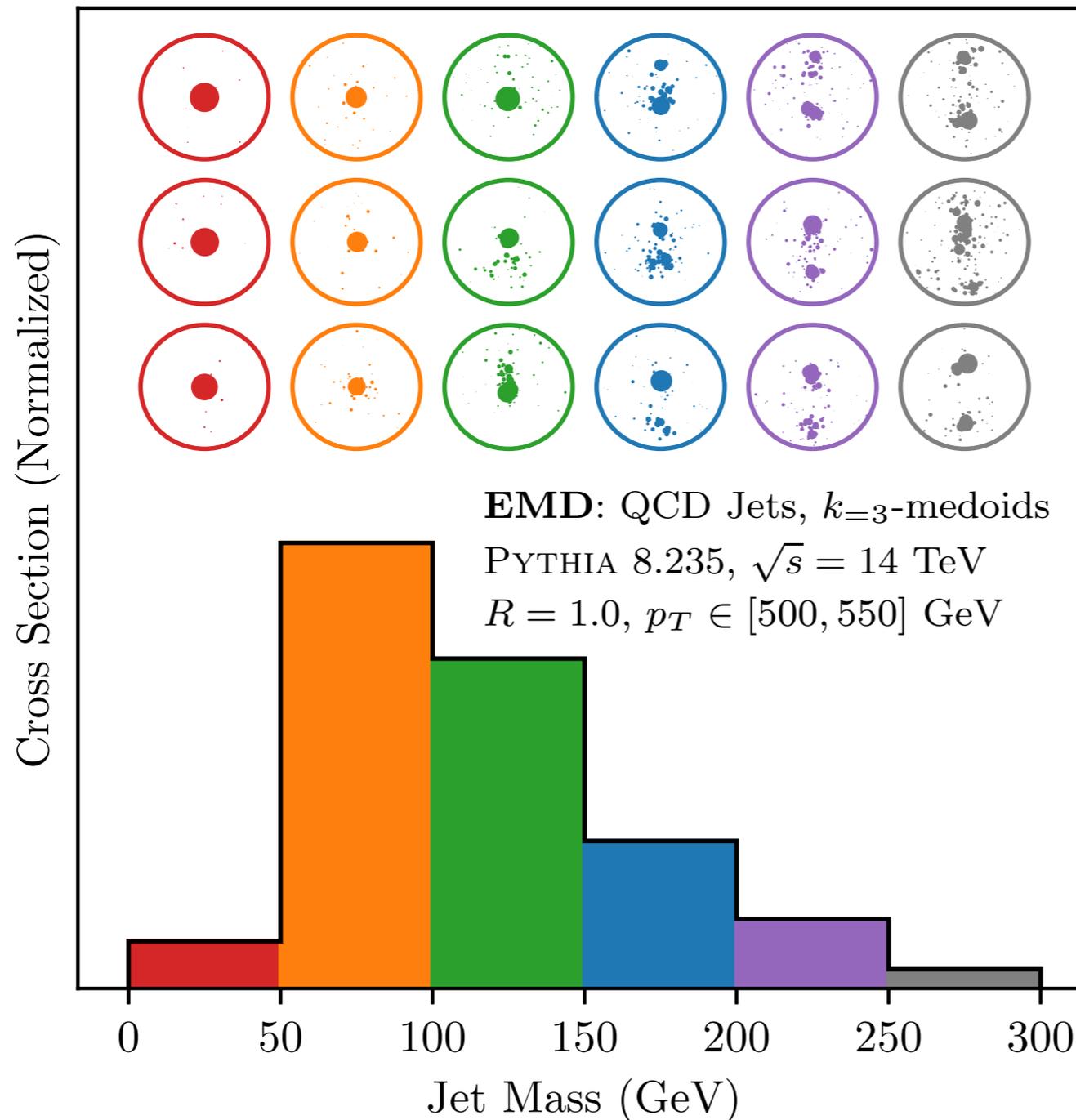
Approaches performance of **modern machine learning**



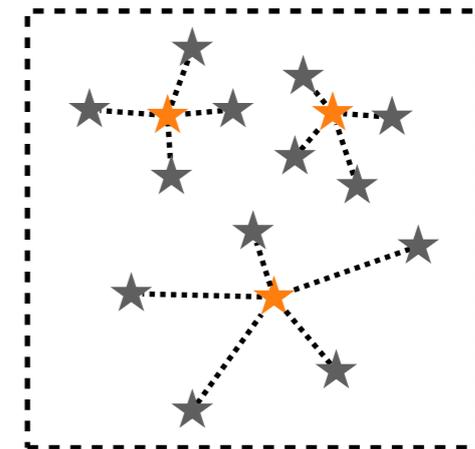
[Komiske, Metodiev, JDT, 1902.02346;

comparison to JDT, Van Tilburg, 1011.2268, 1108.2701; Komiske, Metodiev, JDT, 1712.07124, 1810.05165]

Histograms meet Event Displays

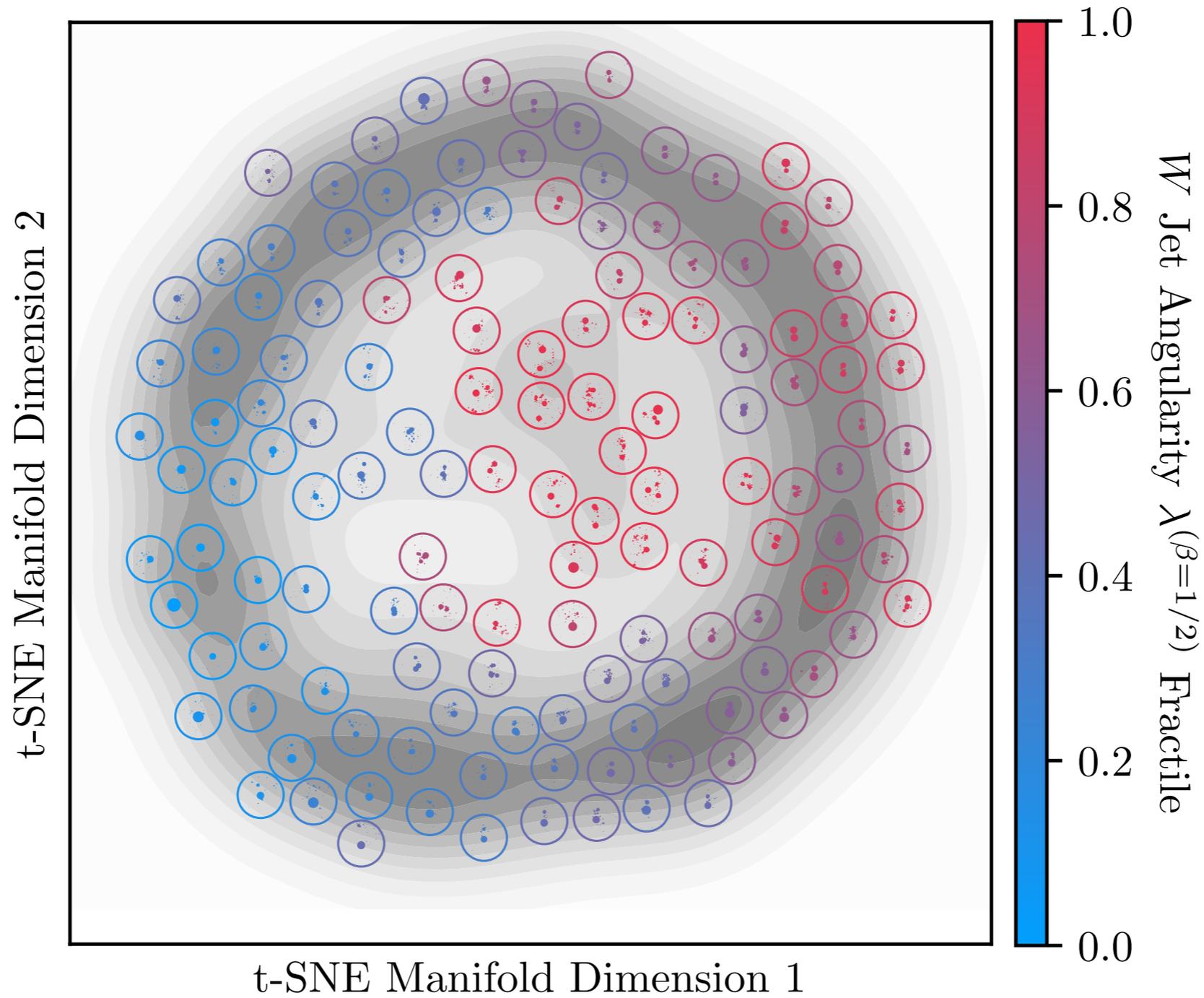
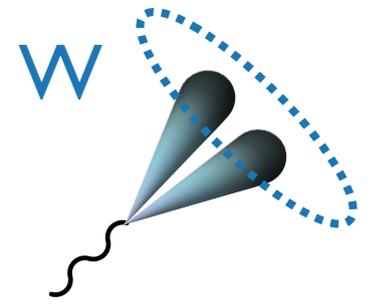


3-medoid: Three most representative jets in each bin



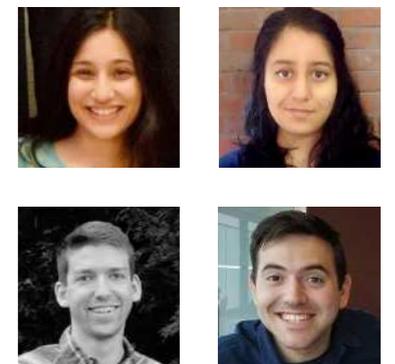
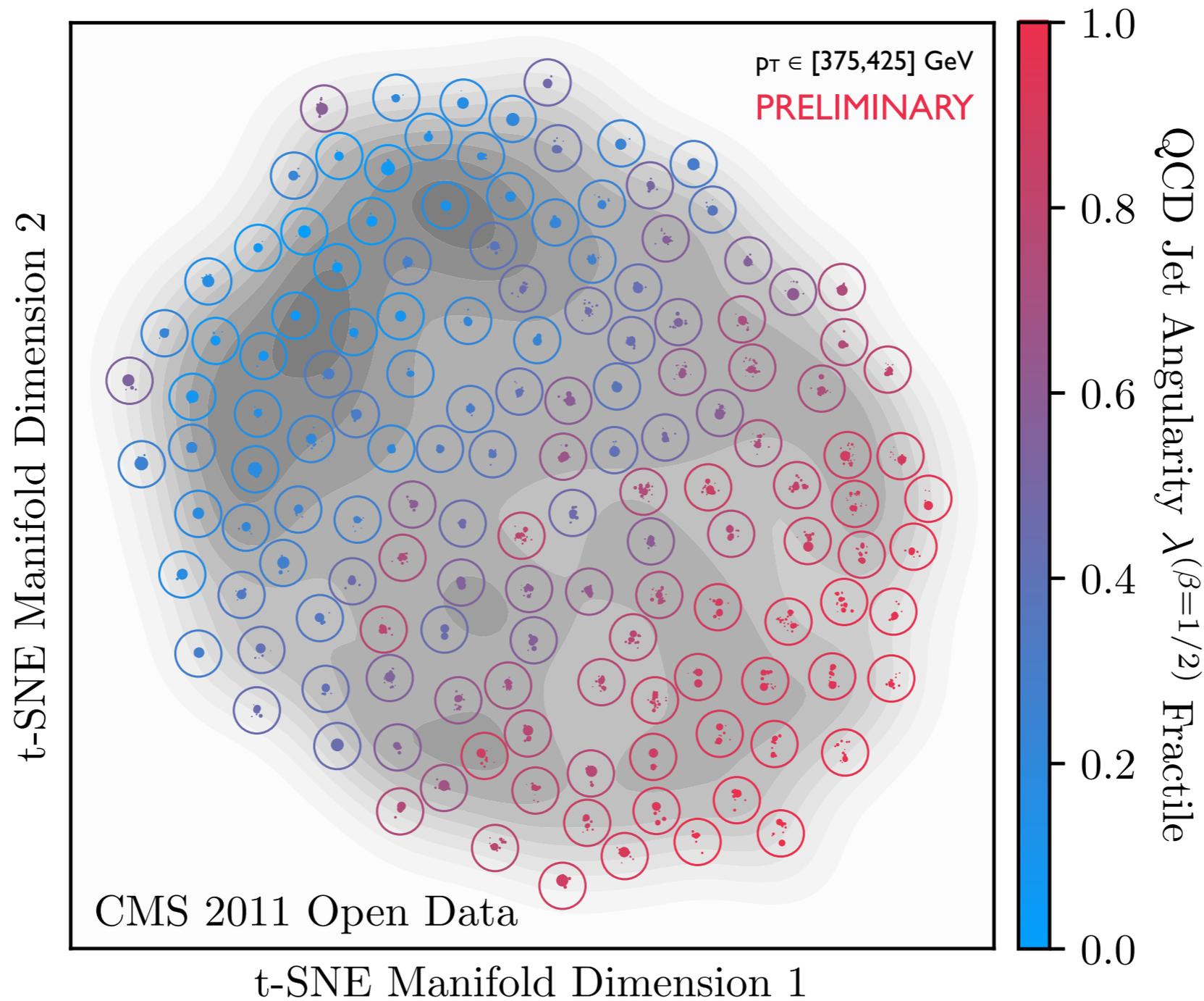
[Komiske, Metodiev, JDT, [1902.02346](#)]

The Space of Boosted W Bosons



[Komiske, Metodiev, JDT, [1902.02346](#)]

The Space of Quark/Gluon Jets

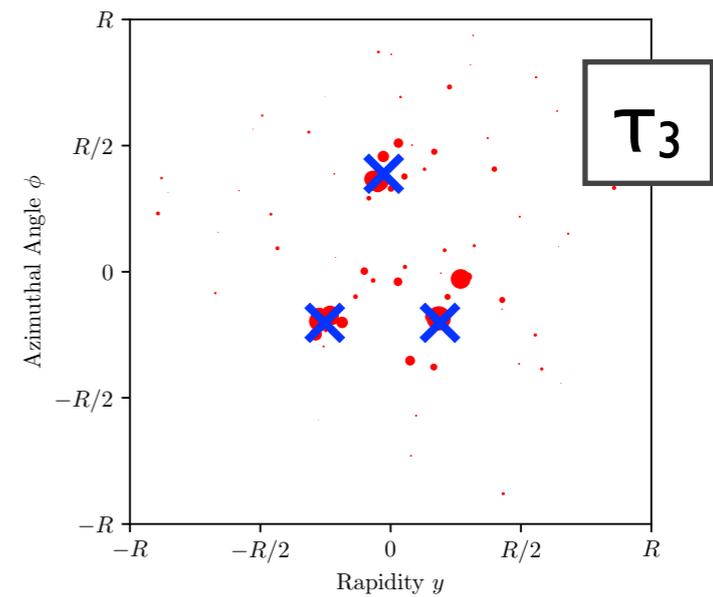
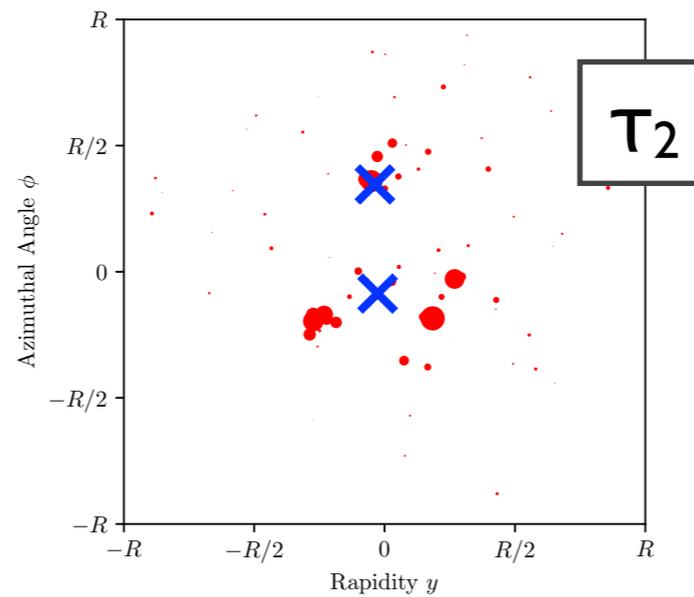
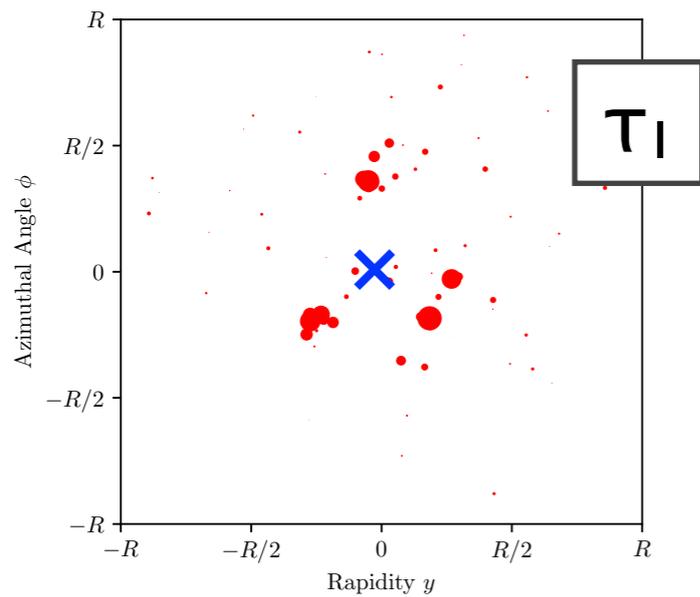


[Mastandrea, Naik, Komiske, Metodiev, JDT, in preparation]

Insight into N-subjettiness

$$\tau_N^{(\beta)}(\mathcal{E}) = \min_{N \text{ axes}} \sum_i E_i \min \left\{ \theta_{1,i}^\beta, \theta_{2,i}^\beta, \dots, \theta_{N,i}^\beta \right\}$$

↑ IRC safe
 ↑ kind of arbitrary

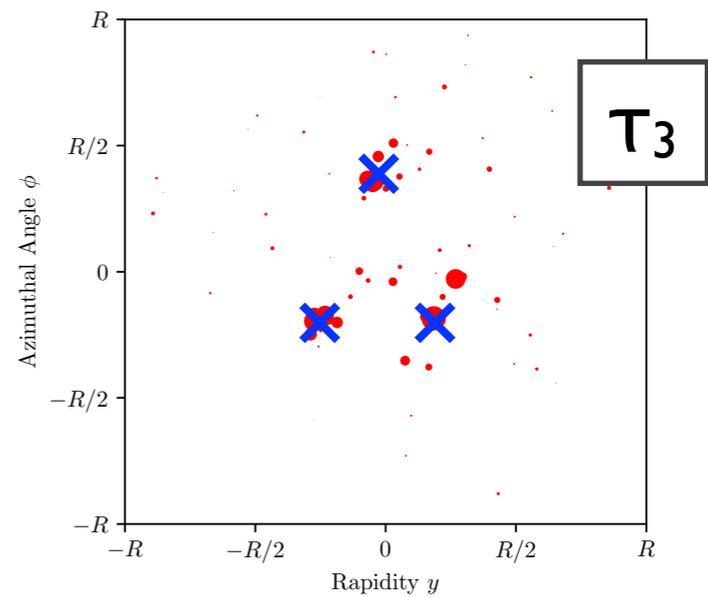
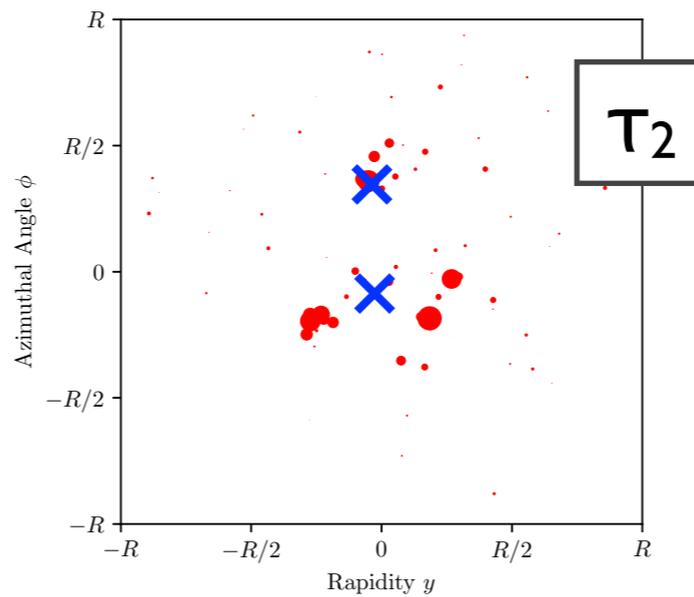
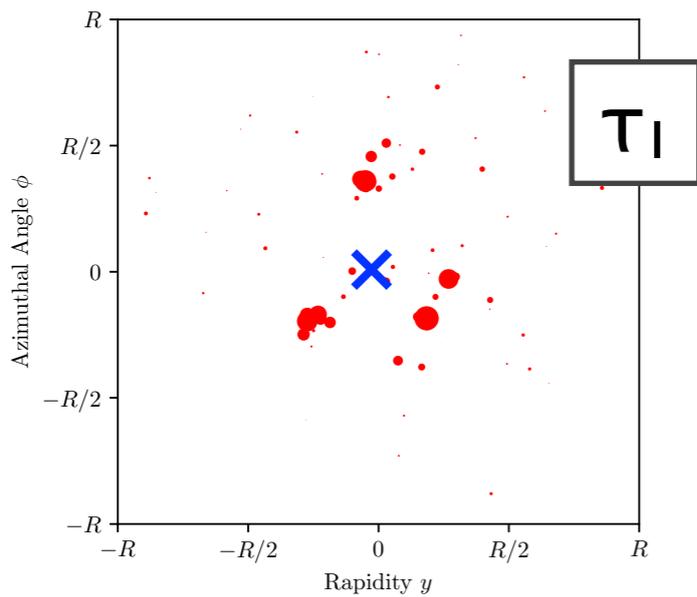


[JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);
based on Brandt, Dahmen, [ZPC 1979](#); Stewart, Tackmann, Waalewijn, [1004.2489](#)]

Insight into N-subjettiness

$$\tau_N^{(\beta)}(\mathcal{E}) = \min_{N \text{ axes}} \sum_i E_i \min \left\{ \theta_{1,i}^\beta, \theta_{2,i}^\beta, \dots, \theta_{N,i}^\beta \right\}$$

↑
IRC safe
↑
kind of arbitrary

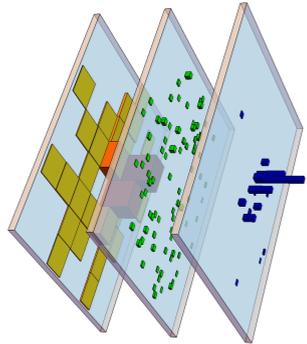


$$\tau_N(\mathcal{E}) = \min_{|\mathcal{E}'|=N} \text{EMD}(\mathcal{E}, \mathcal{E}') \quad \text{for } \beta = 1$$

↑
 very satisfying

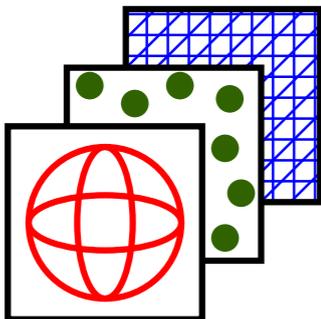
Related to p-Wasserstein metric for $p = \beta > 1$

Summary



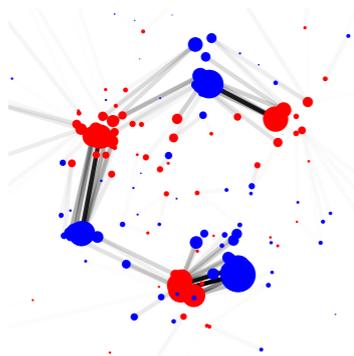
The Rise of Deep Learning

Leveraging computational power to solve well-posed problems



Looking Inside the Black Box

Designing network architectures around symmetries and interpretability



(Exploring the Space of Jets)

Computational geometry as a new collider data analysis strategy



Patrick Komiske



Eric Metodiev

(Theoretical)
High Energy
Physics

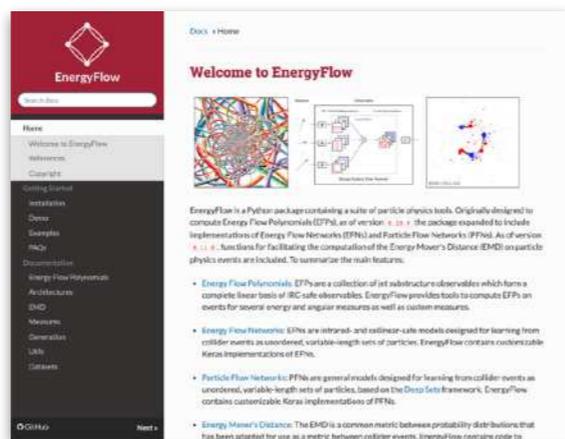


Mathematics,
Statistics,
Computer Science



Energy Flow Package

<https://energyflow.network/>

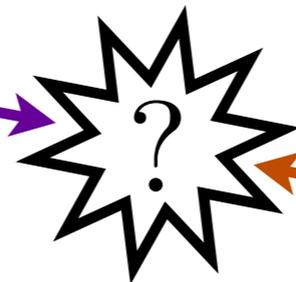


Backup Slides

“Collision Course”

*“Theoretical Physics for Machine Learning”
Aspen Center for Physics, January 2019*

(Theoretical)
High Energy
Physics

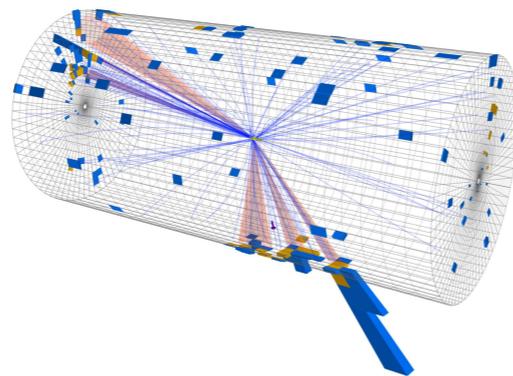


Mathematics,
Statistics,
Computer Science

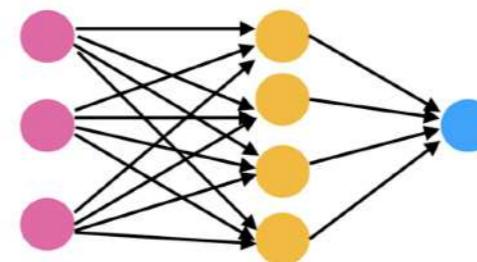
This talk

ML4HEP

Solving complex
problem with
neural networks

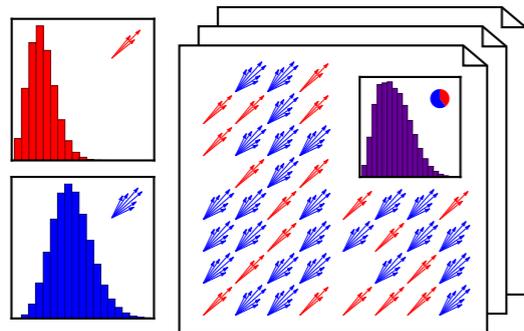


HEP4ML



Studying neural
networks like
physical systems

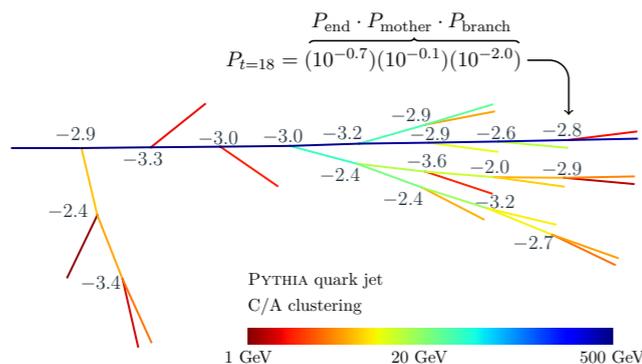
The Rise of Unsupervised Learning



Jet Topics

Blind Source Separation

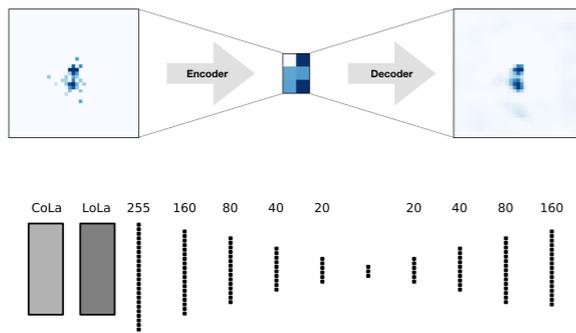
[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#);
see also Metodiev, Nachman, JDT, [1708.02949](#)]



JUNIPR

Probability Modeling

[Andreassen, Feige, Frye, Schwartz, [1804.09720](#);
see also Monk, [1807.03685](#)]



Autoencoders

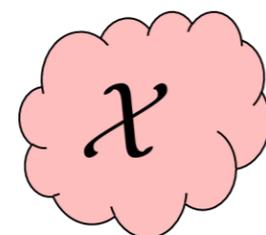
Anomaly Detection

[Hajer, Li, Liu, Wang, [1807.10261](#); Heibel, Kasieczka, Plehn, Thompson, [1808.08979](#);
Farina, Nakai, Shih, [1808.08992](#); Cerri, Nguyen, Pierini, Spiropulu, Vlimant, [1811.10276](#);
see also Collins, Howe, Nachman, [1805.02664](#), [1902.02634](#); De Simone, Jacques, [1807.06038](#)]

*Common theme: Analyze **event ensembles**, not individual events*

Meanwhile in ML-Land: Deep Sets

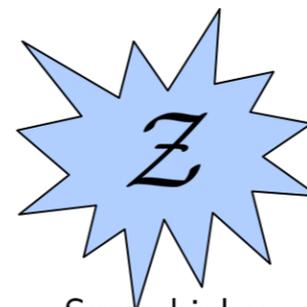
Theorem 2 A function $f(X)$ operating on a set X having elements from a countable universe, is a valid set function, i.e., **invariant** to the permutation of instances in X , iff it can be decomposed in the form $\rho\left(\sum_{x \in X} \phi(x)\right)$, for suitable transformations ϕ and ρ .



Original space

Variable-Length
Unordered Set
of Particles

$$\xleftrightarrow[\text{Homeomorphism}]{z = E(X) = \sum_{x \in X} \phi(x)}$$



Some higher dim space

Additive
Latent Space

$$\xrightarrow[\text{Continuous map}]{\rho(z) = f(E^{-1}(z))}$$



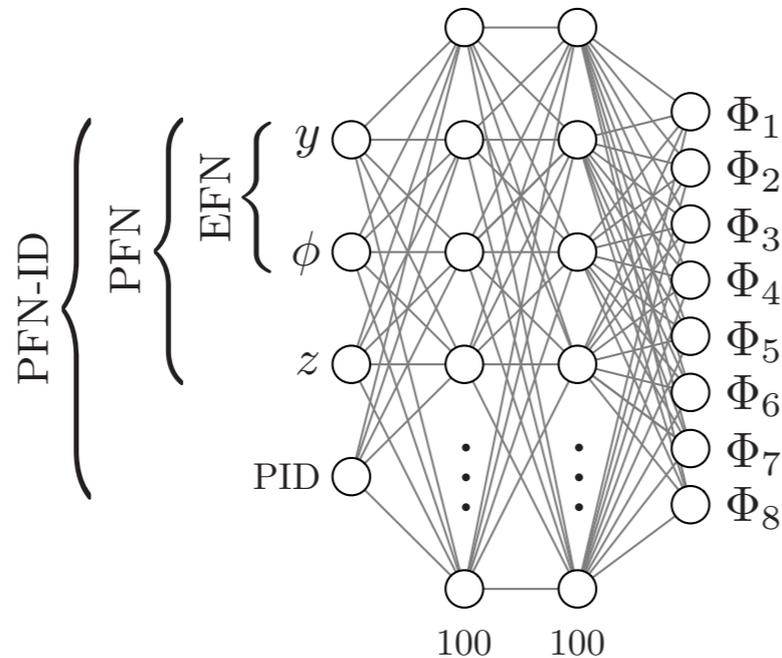
Target space

Generic
Observable

[Zaheer, Kottur, Ravanbakhsh, Póczos, Salakhutdinov, Smola, [1703.06114](#); see also Vinyals, Bengio, Kudlur, [1511.06391](#); Qi, Su, Mo, Guibas, [1612.00593](#)]

Technical Implementation

Per-Particle Network: Φ

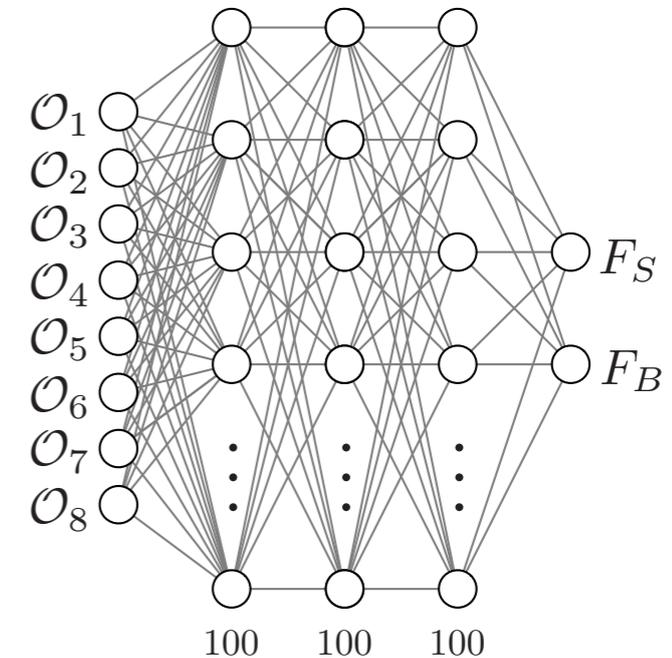


Per-Jet (Latent Space):

$$\text{EFN: } \mathcal{O}_a = \sum_{i \in \text{jet}} z_i \Phi_a(y_i, \phi_i) \quad z_i = \frac{p_{Ti}}{\sum_j p_{Tj}}$$

$$\text{PFN: } \mathcal{O}_a = \sum_{i \in \text{jet}} \Phi_a(y_i, \phi_i, z_i, \text{PID}_i)$$

Latent Combiner: F

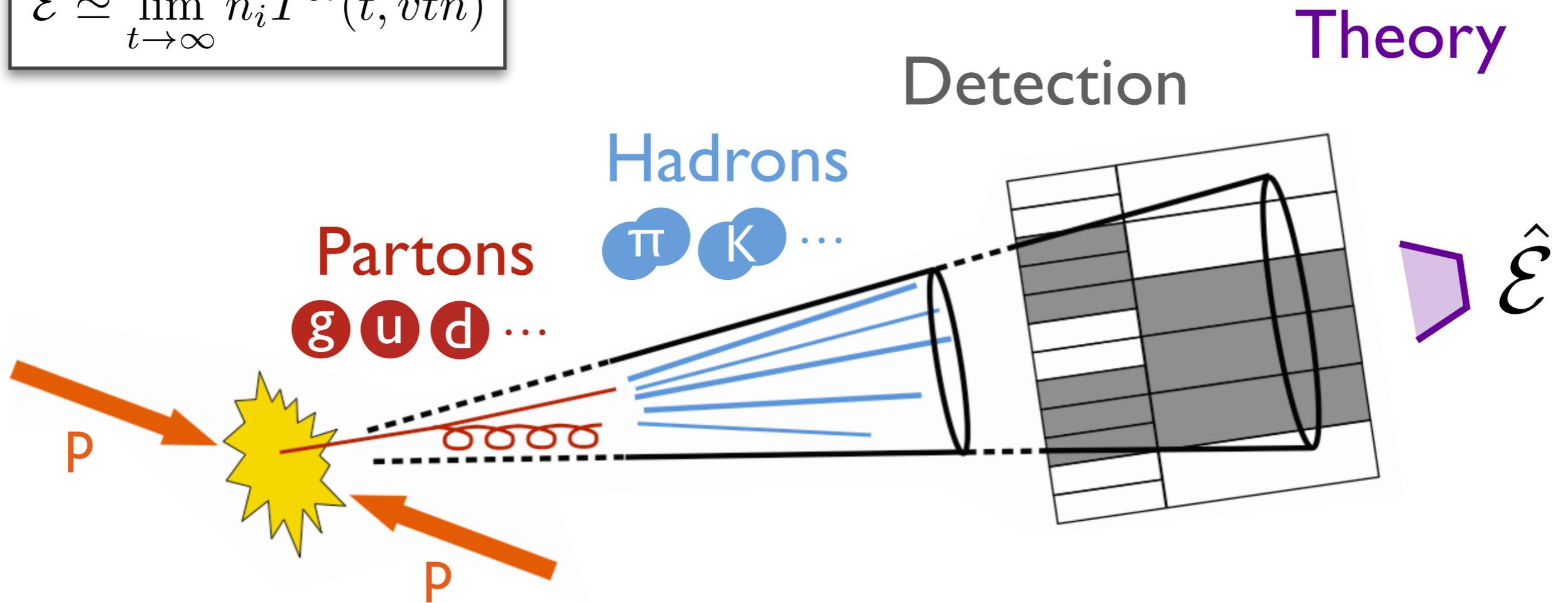


Final Discriminant:

$$\text{softmax}(F_S, F_B)$$

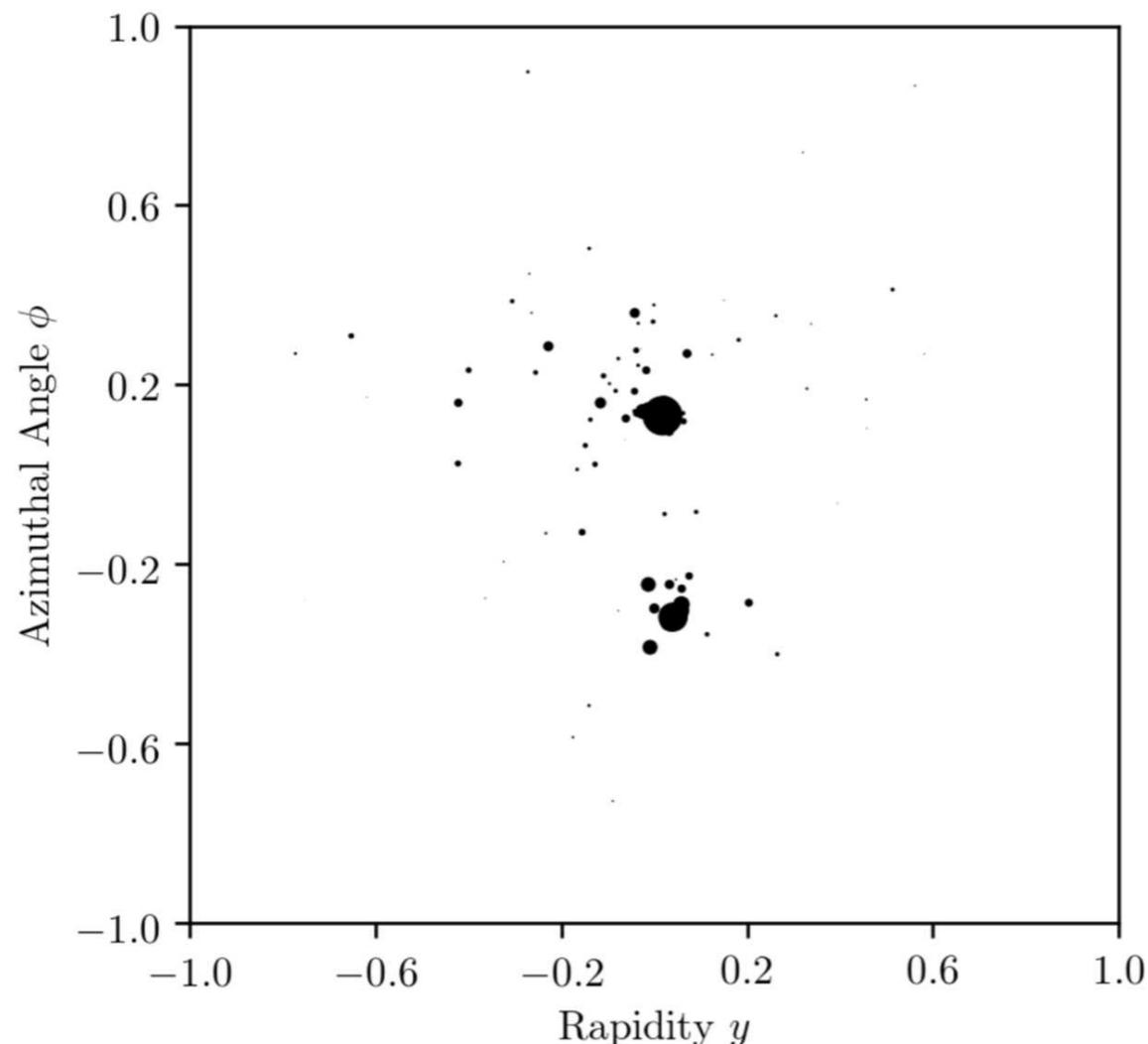
Focus on Energy Flow

$$\hat{\mathcal{E}} \simeq \lim_{t \rightarrow \infty} \hat{n}_i T^{0i}(t, vt\hat{n})$$



*Stress-energy flow: Measure of event/jet structure robust to non-perturbative and detector effects (i.e. **IRC safe**)*

Focus on Energy Flow



Represent jet as:

$$\rho(\hat{p}) = \sum_{i \in \text{jet}} E_i \delta(\hat{p} - \hat{p}_i)$$

Energy (pT) Direction (y,φ)

Safe to infrared & collinear splittings
No flavor/charge information
No pixelation needed

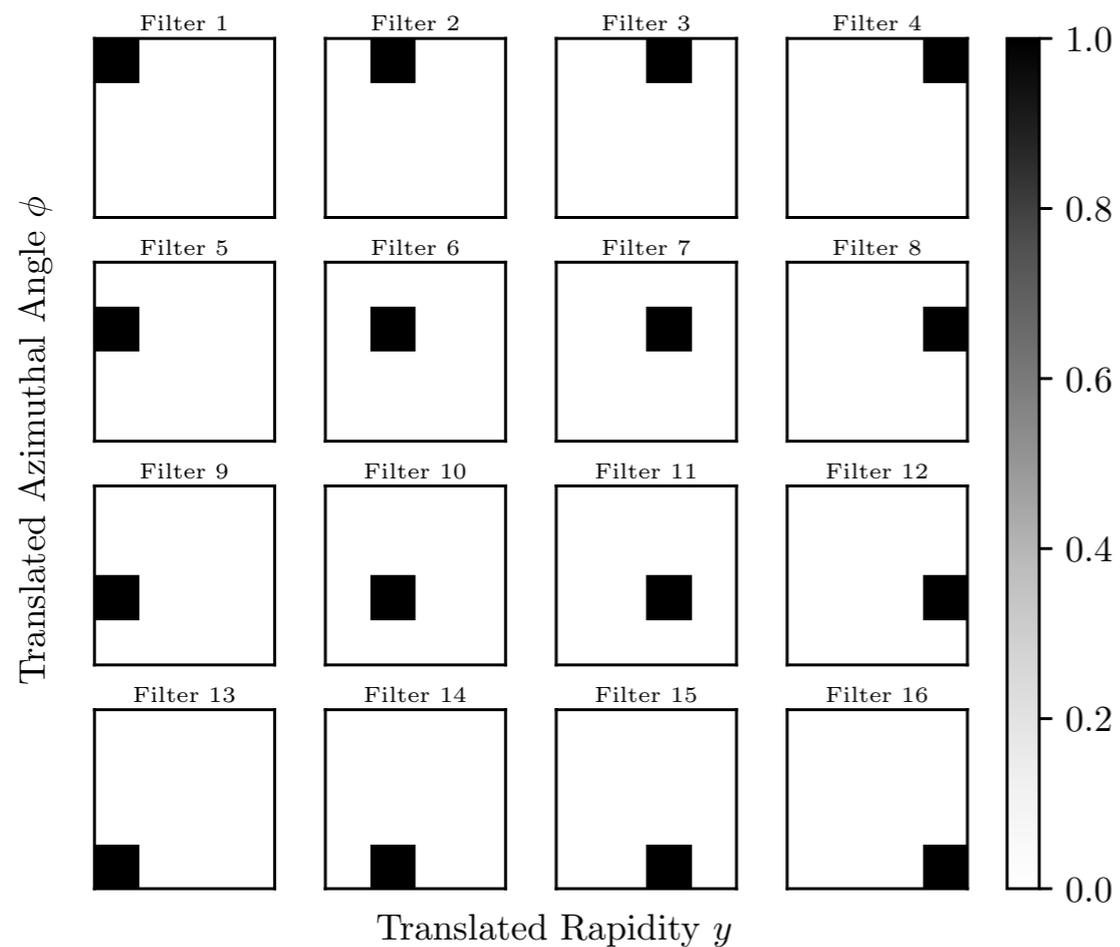
*Stress-energy flow: Measure of event/jet structure
robust to non-perturbative and detector effects (i.e. IRC safe)*

Latent Space Visualization

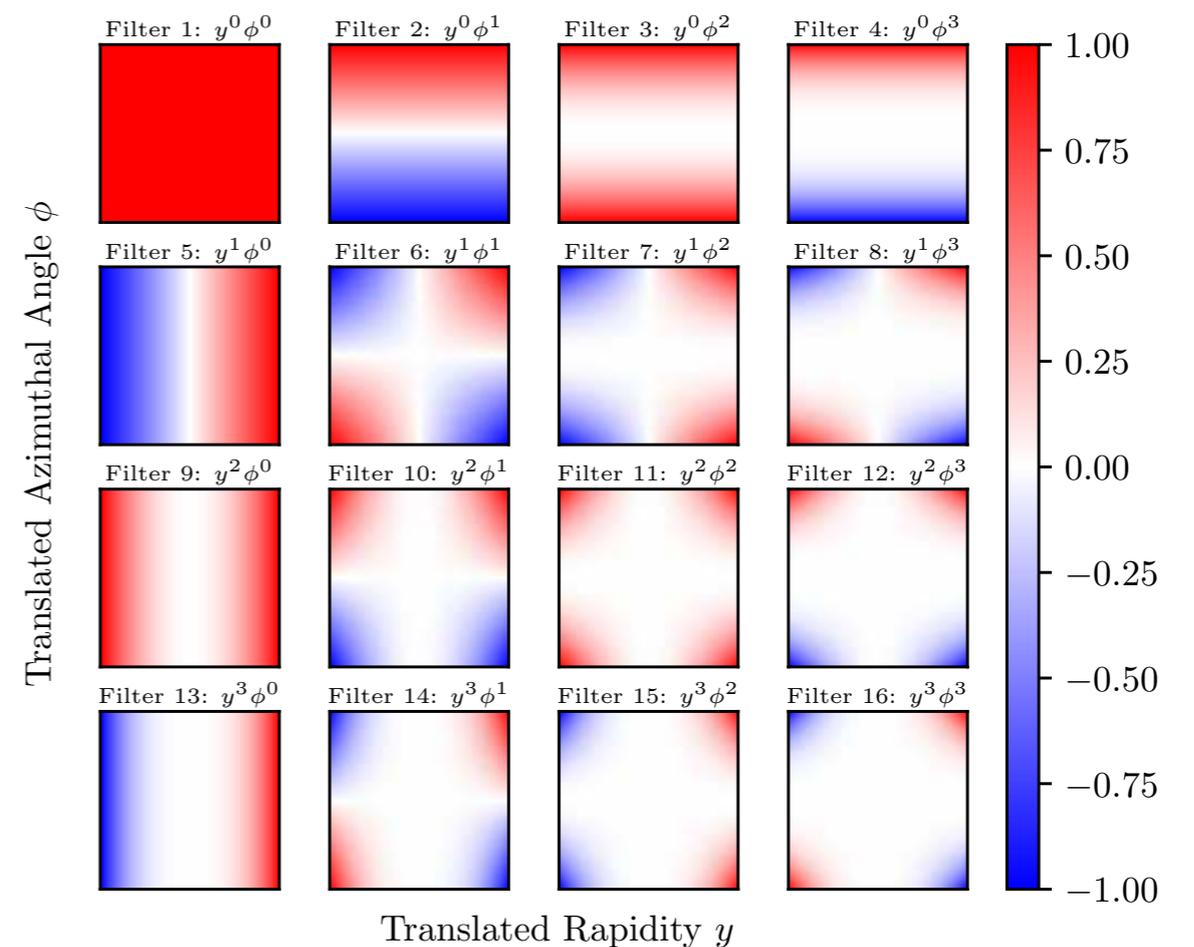
$$\mathcal{O}(\{p_i^\mu\}) = F(\mathcal{O}_1, \mathcal{O}_2, \dots, \mathcal{O}_\ell)$$

$$\text{IRC-safe: } \mathcal{O}_a = \sum_{i \in \text{jet}} E_i \Phi_a(\hat{p}_i)$$

Calorimeter Pixels



Radiation Moments

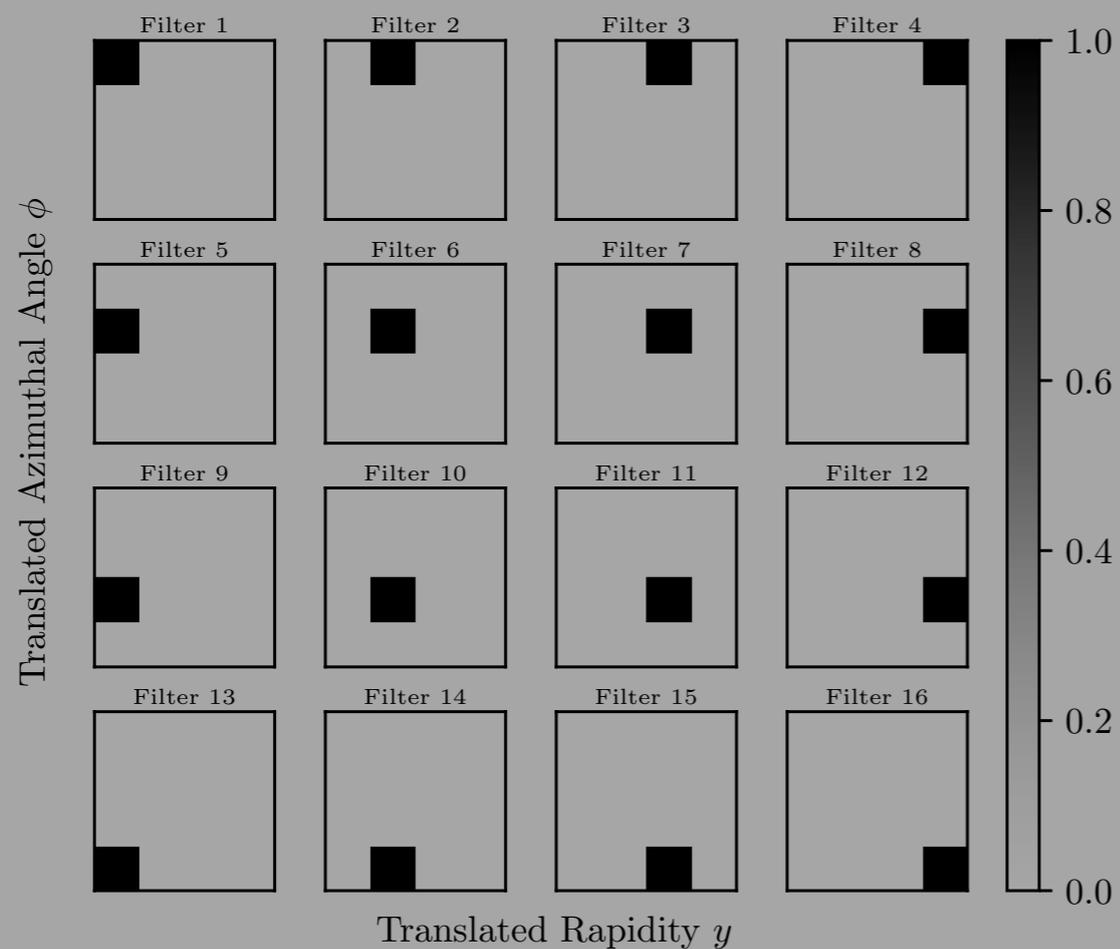


Latent Space Visualization

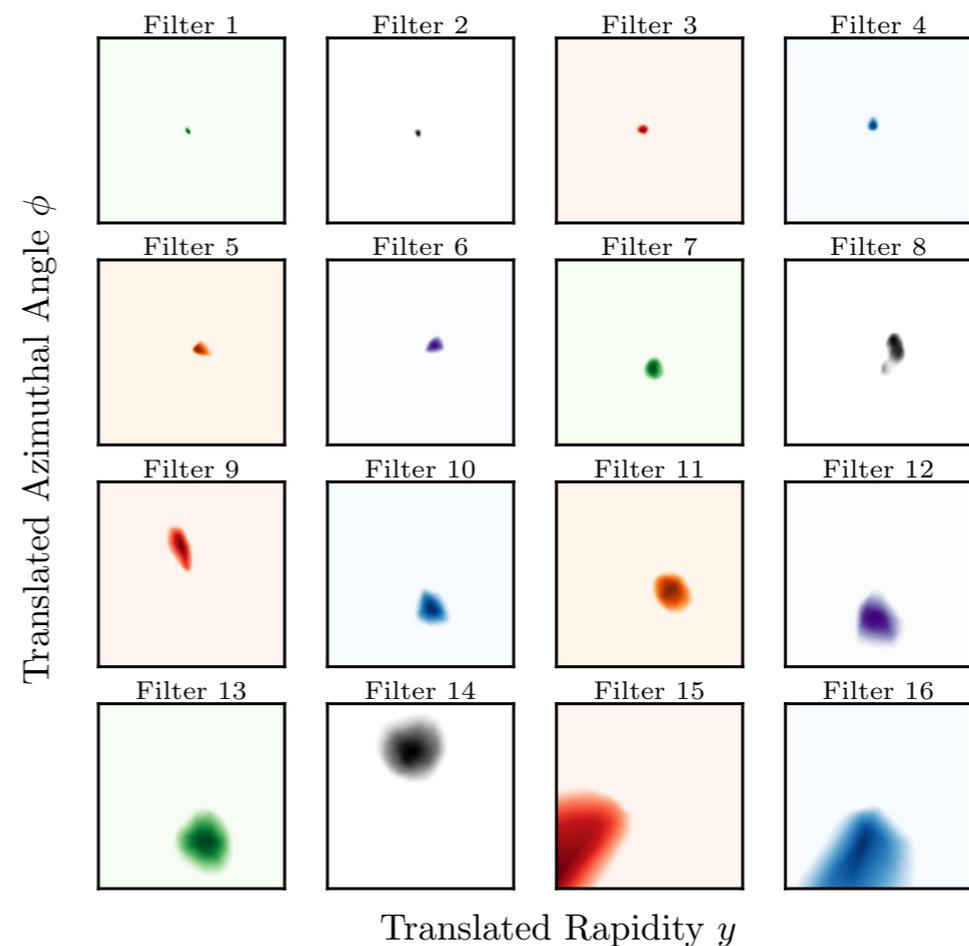
$$\mathcal{O}(\{p_i^\mu\}) = F(\mathcal{O}_1, \mathcal{O}_2, \dots, \mathcal{O}_\ell)$$

$$\text{IRC-safe: } \mathcal{O}_a = \sum_{i \in \text{jet}} E_i \Phi_a(\hat{p}_i)$$

Calorimeter Pixels

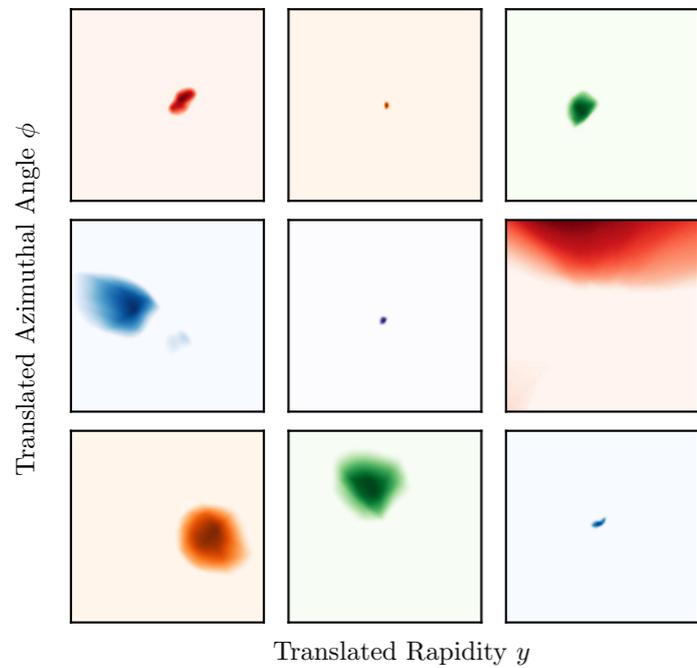


EFNs: Dynamic Pixelation

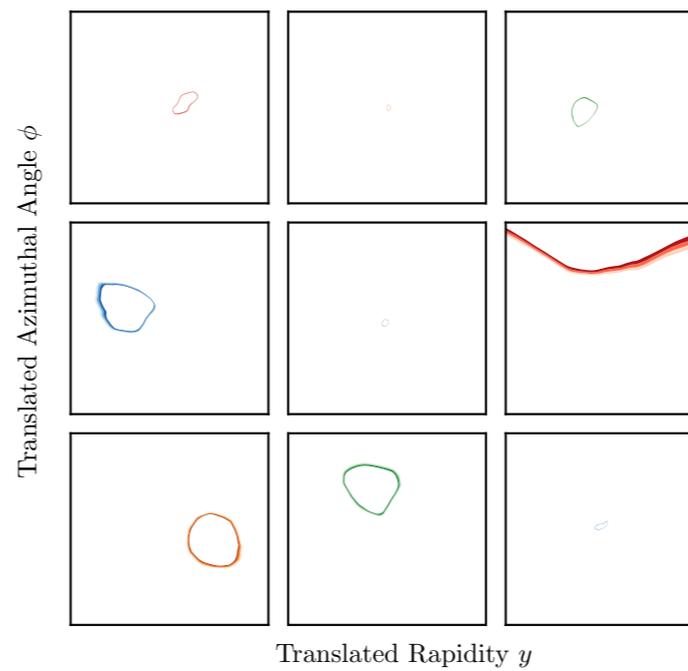


Psychedelic Network Visualization

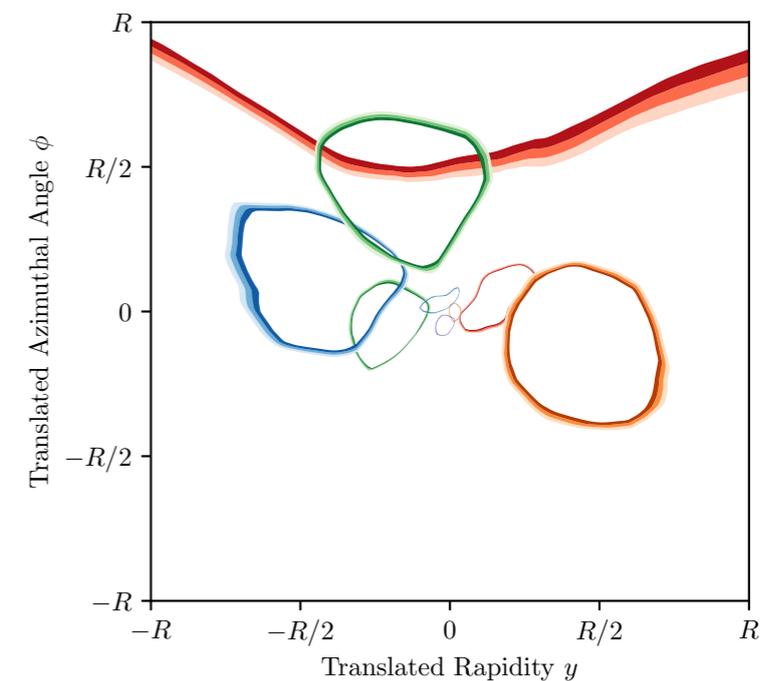
Latent Filters



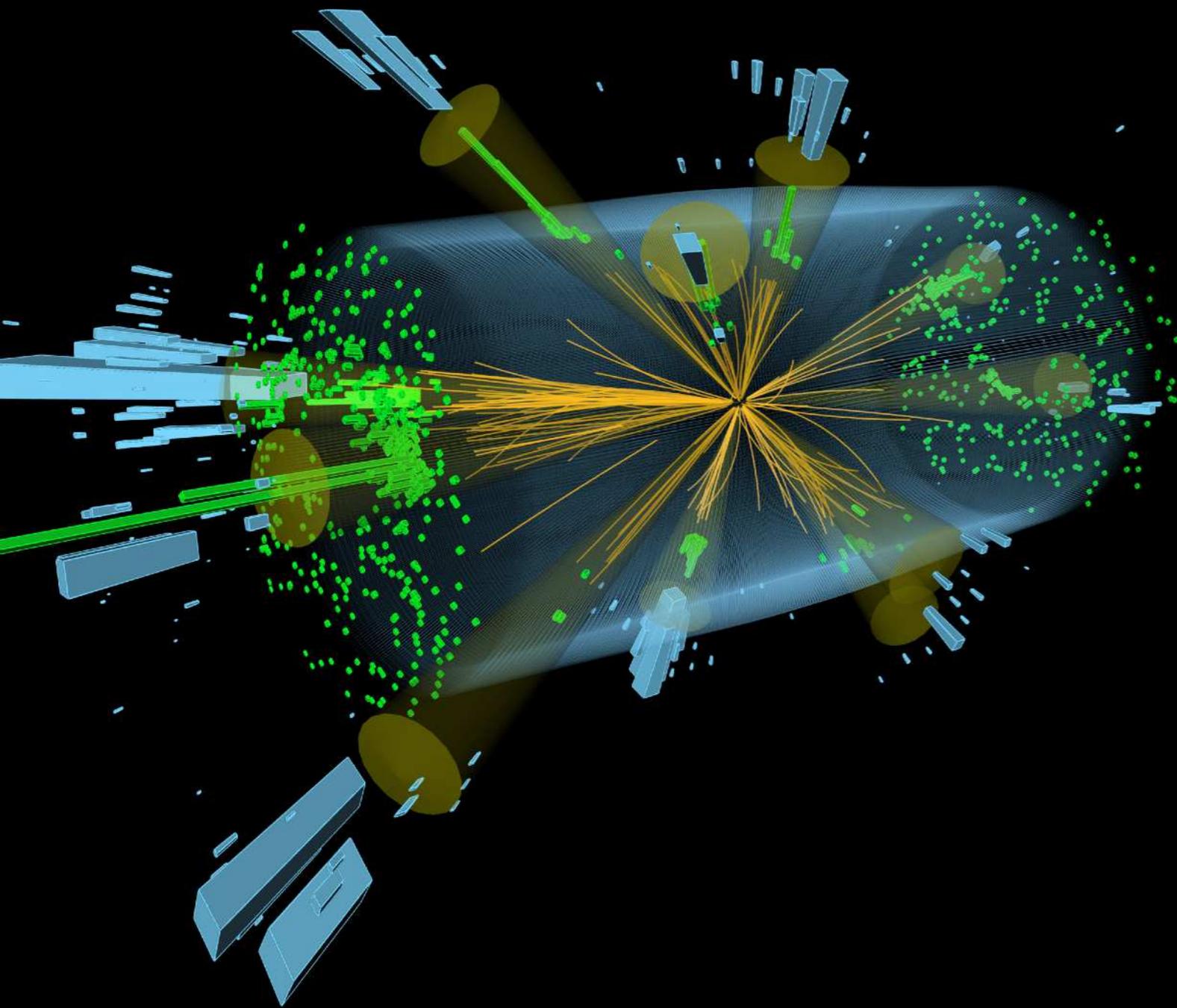
50% Contours



Overlay



What is a Collision Event?



T E H M

	●		γ	photon	elementary	
	●	●	e^{\pm}	electron		
	●	●	●	●		μ^{\pm}
	●	●	●	π^{\pm}	pion	composite
	●	●	●	K^{\pm}	kaon	
		●	●	K_L^0	K-long	
	●	●	●	p/\bar{p}	proton	
		●	●	n/\bar{n}	neutron	

elementary

composite

Point Cloud



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