

Di-Higgs Production in SUSY Models

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INTRODUCTION

Di-Higgs production through gluon fusion at 14TeV collider energy in the framework of Minimal Supersymmetric Standard Model(MSSM) and Next-to-Minimal Supersymmetric Standard Model(NMSSM).



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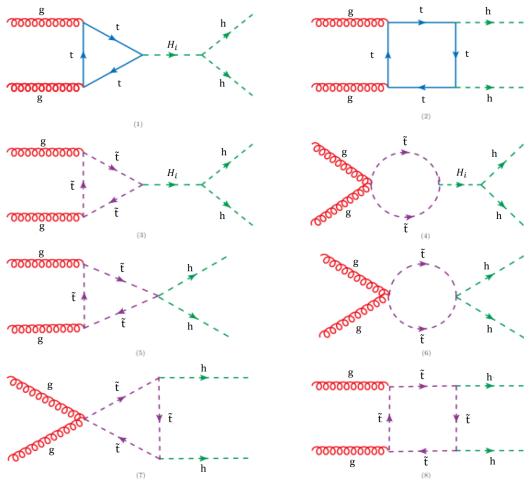
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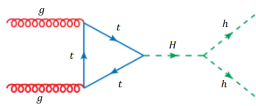
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 - ▶ allow us to study the interference between resonant and nonresonant amplitudes
- ▶ Includes both quark and squark loop contributions
- ▶ Separate the cross section into resonant, nonresonant, and interference parts
 - ▶ To better understand how SUSY Higgs pair production cross section is enhanced as compared to SM case

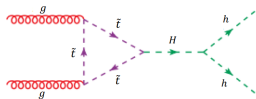
Leading order Feynman diagrams for Higgs pair production in MSSM:



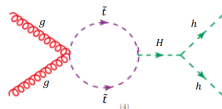
Resonant amplitude:



(1)

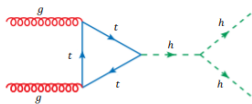


(3)

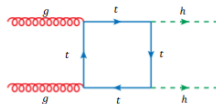


(4)

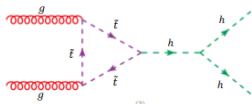
Nonresonant amplitude:



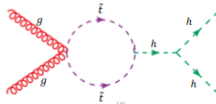
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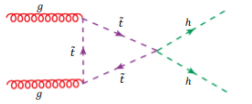
(2)



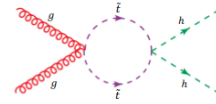
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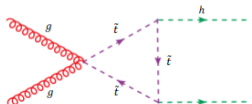
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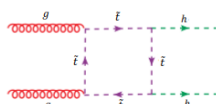
(5)



(6)



(7)



(8)

VALID PARAMETER SPACE

- ▶ Require mass of light CP-even Higgs boson to be 125 ± 0.5 GeV
 - ▶ Stop mixing parameter X_t can be determined by m_A and $\tan\beta$
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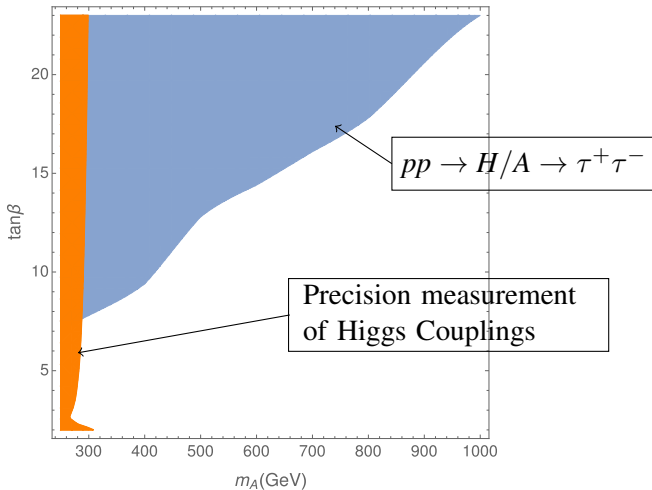
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 - ▶ ref: CMS PAS HIG-17-020
 - ▶ Upper bound of $\tan\beta$
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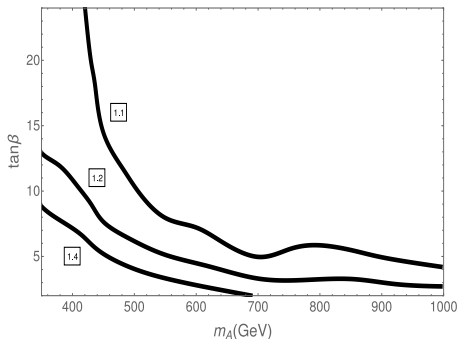
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 - ▶ ref: CMS PAS HIG-17-031
 - ▶ checked coupling modifiers: $\kappa_t, \kappa_b, \kappa_\tau, \kappa_\gamma, \kappa_g$
 - ▶ Lower bound of m_A

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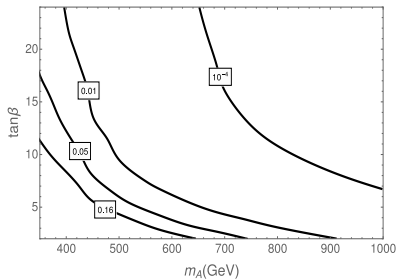
RESULTS



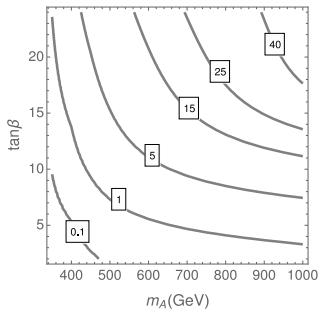
► $\sigma_{MSSM}^{LO} / \sigma_{SM}^{LO}$
 ($\sigma_{SM}^{LO} = 21.7$ fb)

- Always larger than SM cross section
 (10% ~ 40% enhancement)

RESULTS

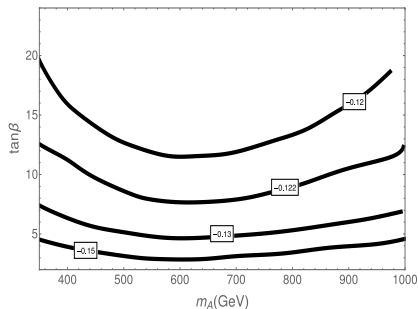


- ▶ $\sigma_{res} / \sigma_{SM}^{LO}$
- ▶ σ_{res} is largest when $\tan\beta$ and m_A are small
- ▶ σ_{nr} dominates when $\tan\beta$ and m_A are large



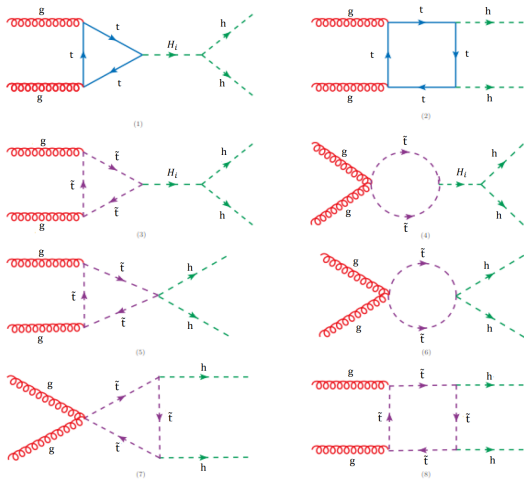
- ▶ $\sigma_{Int} / \sigma_{res}$
- ▶ When $\tan\beta$ and m_A are small, σ_{Int} can be as large as σ_{res}

RESULTS



- ▶ $\delta_3 = \frac{g_{hhh}^{MSSM} - g_{hhh}^{SM}}{g_{hhh}^{SM}}$
- ▶ Always smaller than SM value
($-12\% \sim -15\%$)
- ▶ $\kappa_t \approx 1$
- ▶ δ_3 is the main factor that increases σ_{nr} by about $8\% \sim 10\%$

Leading order Feynman diagrams for Higgs pair production in NMSSM:



PARAMETER SPACE SCAN RANGES

	$\tan\beta$	λ	κ	A_λ	A_κ	μ_{eff}	M_1	M_2	M_3	A_t	A_b	A_τ	m_{Q_3}	m_{L_3}
	(in TeV)													
min	1	0	-0.7	-1	-1	-0.5	0.1	0.2	1.3	-6	-6	-3	0.6	0.6
max	10	0.7	0.7	1	1	0.5	1	2	7	6	6	3	4	4

- ▶ Scanned by NMSSMTools5.4.0
- ▶ Choose $\lambda, \kappa < 0.7$ to ensure perturbativity
- ▶ Various phenomenological and theoretical constraints are checked by NMSSMTools

BENCHMARKS FOR HIGGS PAIR PRODUCTION IN NMSSM

$$\sigma_{SM}^{LO} = 21.7 \text{ fb}$$

$$\sigma_{SM}^{NLO} = 42.3 \text{ fb}$$

σ^{NLO} (fb)	66.52	72.78	50.97
σ^{LO} (fb)	33.91	37.21	26.08
σ_{res}^{LO} (fb)	3.22×10^{-6}	6.87	6.30×10^{-3}
σ_{nr}^{LO} (fb)	33.06	26.84	25.77
σ_{int}^{LO} (fb)	0.85	3.50	0.30
m_{H_1} (GeV)	124.8	124.8	110.1
m_{H_2} (GeV)	1315.9	440.6	125.2
m_{H_3} (GeV)	2550.9	534.0	629.7
$\tan\beta$	5.3	1.83	1.6
λ	0.70	0.50	0.58
κ	0.30	0.51	0.30
A_λ (GeV)	501.0	33.0	420.0
A_κ (GeV)	-500.0	358.0	-665.0
μ_{eff} (GeV)	200.0	-299.0	321.0

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▶ NMSSM:

- ▶ σ_{NMSSM} can be larger than σ_{SM} by 70%
- ▶ σ_{res} is large when $m_{H_2} \approx m_{H_3}$

INTERFERENCE TERM

$$\begin{aligned}
 |\mathcal{M}|^2 &\propto |A_{\triangleright}^H + A_{\triangleright}^{nr} + A_{\square}^{nr}|^2 \\
 &= |A_{\triangleright}^H|^2 + |A_{\triangleright}^{nr} + A_{\square}^{nr}|^2 + 2\text{Re}[A_{\triangleright}^H \times (A_{\triangleright}^{nr} + A_{\square}^{nr})^*]
 \end{aligned}$$

The interference term is

$$2\text{Re}[A_{\triangleright}^H \times (A_{\triangleright}^{nr} + A_{\square}^{nr})^*] = 2\text{Re}[A_{\triangleright}^H \times A_{\triangleright}^{nr*}] + 2\text{Re}[A_{\triangleright}^H \times A_{\square}^{nr*}].$$

Let $A^{nr} = |A^{nr}|e^{i\delta_{nr}}$, $a_{res} = C_{Hhh}C_{Htt}F_{\triangleright}$, then

$$\begin{aligned}
 A_{\triangleright}^H &= a_{res} \frac{\hat{s}}{\hat{s} - m_H^2 + i\Gamma_H m_H} \\
 &= |a_{res}| e^{i\delta_{res}} \hat{s} \frac{\hat{s} - m_H^2 - i\Gamma_H m_H}{(\hat{s} - m_H^2)^2 + (\Gamma_H m_H)^2}
 \end{aligned}$$

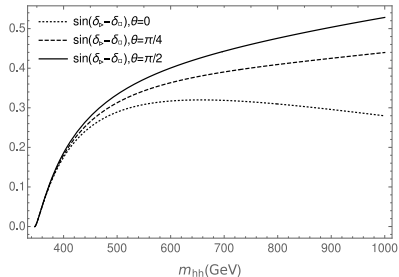
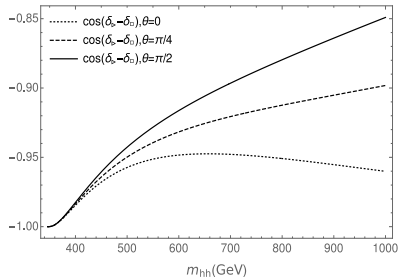
INTERFERENCE TERM

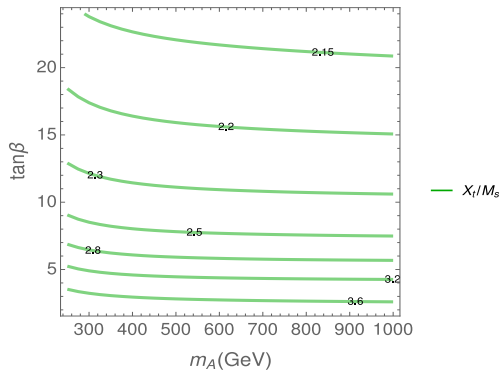
$$\begin{aligned}
 2\text{Re}[A_{\triangleright}^H \times A^{nr*}] &= 2\text{Re}[|a_{res}| |A^{nr}| e^{i(\delta_{res} - \delta_{nr})} \hat{s} \frac{\hat{s} - m_H^2 - i\Gamma_H m_H}{(\hat{s} - m_H^2)^2 + (\Gamma_H m_H)^2}] \\
 &= 2(R_{int} + I_{int})
 \end{aligned}$$

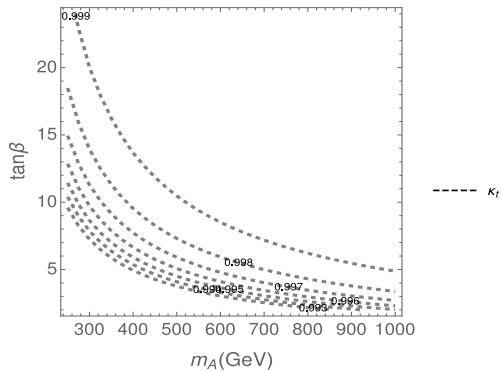
$$R_{int} = |a_{res}| |A^{nr}| \cos(\delta_{res} - \delta_{nr}) \hat{s} \frac{\hat{s} - m_H^2}{(\hat{s} - m_H^2)^2 + (\Gamma_H m_H)^2}$$

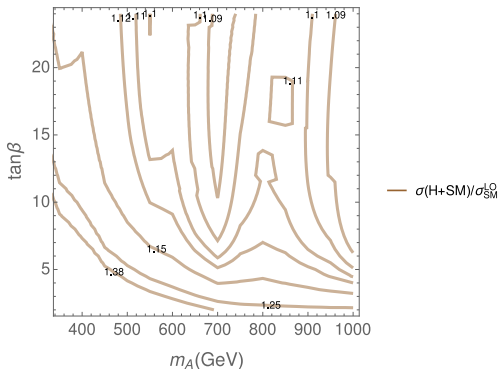
$$I_{int} = |a_{res}| |A^{nr}| \sin(\delta_{res} - \delta_{nr}) \hat{s} \frac{\Gamma_H m_H}{(\hat{s} - m_H^2)^2 + (\Gamma_H m_H)^2}$$

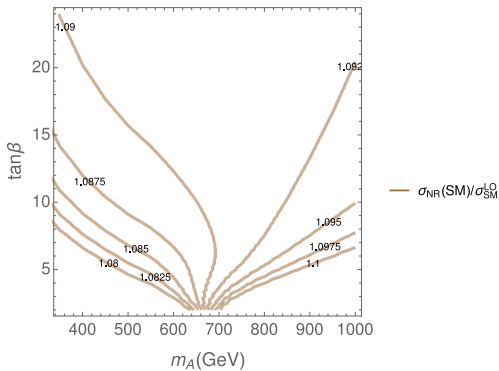
INTERFERENCE TERM



X_t/M_S CONTOUR PLOT

κ_t CONTOUR PLOT

$\sigma_{MSSM}^{LO}(no \tilde{t}) / \sigma_{SM}^{LO}$ CONTOUR PLOT


$\sigma_{nr} / \sigma_{SM}^{LO}$ CONTOUR PLOT

NMSSM CONSTRAINTS

PROB(1) chargino too light

PROB(2) excluded by $Z \rightarrow$ neutralinos

PROB(3) charged Higgs too light

PROB(4) excluded by $ee \rightarrow hZ$

PROB(5) excluded by $ee \rightarrow hZ$, $h \rightarrow bb$

PROB(6) excluded by $ee \rightarrow hZ$, $h \rightarrow \tau\tau$

PROB(7) excluded by $ee \rightarrow hZ$, $h \rightarrow$ invisible

PROB(8) excluded by $ee \rightarrow hZ$, $h \rightarrow 2\text{jets}$

PROB(9) excluded by $ee \rightarrow hZ$, $h \rightarrow 2\text{photons}$

PROB(10) excluded by $ee \rightarrow hZ$, $h \rightarrow AA \rightarrow 4bs$

PROB(11) excluded by $ee \rightarrow hZ$, $h \rightarrow AA \rightarrow 4\tau$

PROB(12) excluded by $ee \rightarrow hZ$, $h \rightarrow AA \rightarrow 2bs 2\tau$

PROB(13) excluded by $Z \rightarrow hA$ (Z width)

PROB(14) excluded by $ee \rightarrow hA \rightarrow 4bs$

PROB(15) excluded by $ee \rightarrow hA \rightarrow 4\tau$

- PROB(16) excluded by $ee \rightarrow hA \rightarrow 2bs \ 2\tau$ s
- PROB(17) excluded by $ee \rightarrow hA \rightarrow AAA \rightarrow 6bs$
- PROB(18) excluded by $ee \rightarrow hA \rightarrow AAA \rightarrow 6\tau$ s
- PROB(19) excluded by $ee \rightarrow Zh \rightarrow ZAA \rightarrow Z + \text{light pairs}$
- PROB(20) excluded by $\text{stop} \rightarrow b \ l \ \text{sneutrino}$
- PROB(21) excluded by $\text{stop} \rightarrow \text{neutralino } c$
- PROB(22) excluded by $s_{\text{bottom}} \rightarrow \text{neutralino } b$
- PROB(23) squark/gluino too light
- PROB(24) selectron/smuon too light
- PROB(25) stau too light
- PROB(26) lightest neutralino is not LSP or $< 511 \text{ keV}$
- PROB(27) Landau Pole in l, k, ht, hb below MGUT
- PROB(28) unphysical global minimum
- PROB(29) Higgs soft masses $\gg M_{\text{susy}}$
- PROB(30) excluded by DM relic density (checked only if $\text{OMGFLAG} \neq 0$)

- PROB(31) excluded by DM SI WIMP-nucleon χs (checked if $|\text{OMGFLAG}| = 2$ or 4)
- PROB(32) $b \rightarrow s$ gamma more than 2 sigma away
- PROB(33) ΔM_s more than 2 sigma away
- PROB(34) ΔM_d more than 2 sigma away
- PROB(35) $B_s \rightarrow \mu^+ \mu^-$ more than 2 sigma away
- PROB(36) $B \rightarrow \tau \nu_\tau$ more than 2 sigma away
- PROB(37) $(g - 2)_\mu$ more than 2 sigma away
- PROB(38) excluded by Upsilon(1S) $\rightarrow A$ gamma
- PROB(39) excluded by $\eta_b(1S)$ mass measurement
- PROB(40) $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$ more than 2 sigma away
- PROB(41) excluded by $ee \rightarrow hZ$, $h \rightarrow AA \rightarrow 4\tau$ (ALEPH analysis)
- PROB(42) excluded by top $\rightarrow b H^+$, $H^+ \rightarrow c s$ (CDF, D0)
- PROB(43) excluded by top $\rightarrow b H^+$, $H^+ \rightarrow \tau \nu_\tau$ (D0)
- PROB(44) excluded by top $\rightarrow b H^+$, $H^+ \rightarrow W^+ A1$, $A1 \rightarrow 2\tau$ (CDF)
- PROB(45) excluded by $t \rightarrow b H^+$ (LHC)

- PROB(46) No Higgs in the MHmin-MHmax GeV range
- PROB(47) $\chi^2_{\text{gam}} > \chi^2_{\text{max}}$
- PROB(48) $\chi^2_{\text{bb}} > \chi^2_{\text{max}}$
- PROB(49) $\chi^2_{\text{zz}} > \chi^2_{\text{max}}$
- PROB(51) excluded by $H/A \rightarrow \tau\tau$
- PROB(52) Excluded by $H \rightarrow AA \rightarrow 4\text{leptons}/2\text{lept.}+2b$ (LHC)
- PROB(53) excluded by $ggF \rightarrow H/A \rightarrow \text{gamgam}$ ($65\text{GeV} < M < 122\text{GeV}$, ATLAS)
- PROB(55) $b \rightarrow d$ gamma more than 2 sigma away
- PROB(56) $B_d \rightarrow \mu^+ \mu^-$ more than 2 sigma away
- PROB(57) $b \rightarrow s$ nu nubar more than 2 sigma away
- PROB(58) $b \rightarrow c$ tau nu more than 2 sigma away (as SM)
- PROB(59) $K \rightarrow \pi$ nu nubar more than 2 sigma away
- PROB(60) DMK / epsK more than 2 sigma away
- PROB(61) excluded by DM SD WIMP-neutron xs (checked if $|\text{OMGFLAG}| = 2$ or 4)
- PROB(62) excluded by DM SD WIMP-proton xs (checked if $|\text{OMGFLAG}| = 2$ or 4)

ALL INPUT PARAMETERS OF NMSSM BENCHMARKS

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μ_{eff} (GeV)	200.0	-299.0	321.0
M_1 (GeV)	124	457	608
M_2 (GeV)	248	386	546
M_3 (GeV)	744	6345	6778
A_t (GeV)	1500	5134	1092
A_b (GeV)	1500	-2908	-4015
A_τ (GeV)	1500	-667	2370
m_{Q_3} (GeV)	1000	3175	2574
m_{L_3} (GeV)	200	1276	790