

BSM PHYSICS FOR MUON-ELECTRON SCATTERING

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In collaboration with C. Williams



MUON G-2

➤ Muon magnetic moment

$$\vec{\mu}_\mu = g_\mu \frac{Qe}{2m_\mu} \vec{s} \qquad g_\mu = 2(1 + a_\mu)$$

➤ High precision test of Standard model

- E821 experiment at BNL measured

$$a_\mu^{\text{E821}} = 116592091(63) \times 10^{-11}$$

Bennett et al. [Muon g-2 Collaboration]

- Standard model prediction

$$a_\mu^{\text{SM}} = 116591821(38) \times 10^{-11}$$

Keshavarzi, Nomura, Teubner

- 3σ difference

$$\Delta a_\mu = a_\mu^{\text{E821}} - a_\mu^{\text{SM}} = 270(74) \times 10^{-11}$$

➤ Muon g-2 experiment at FNAL is analyzing first run

- Could push difference to 5σ

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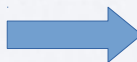
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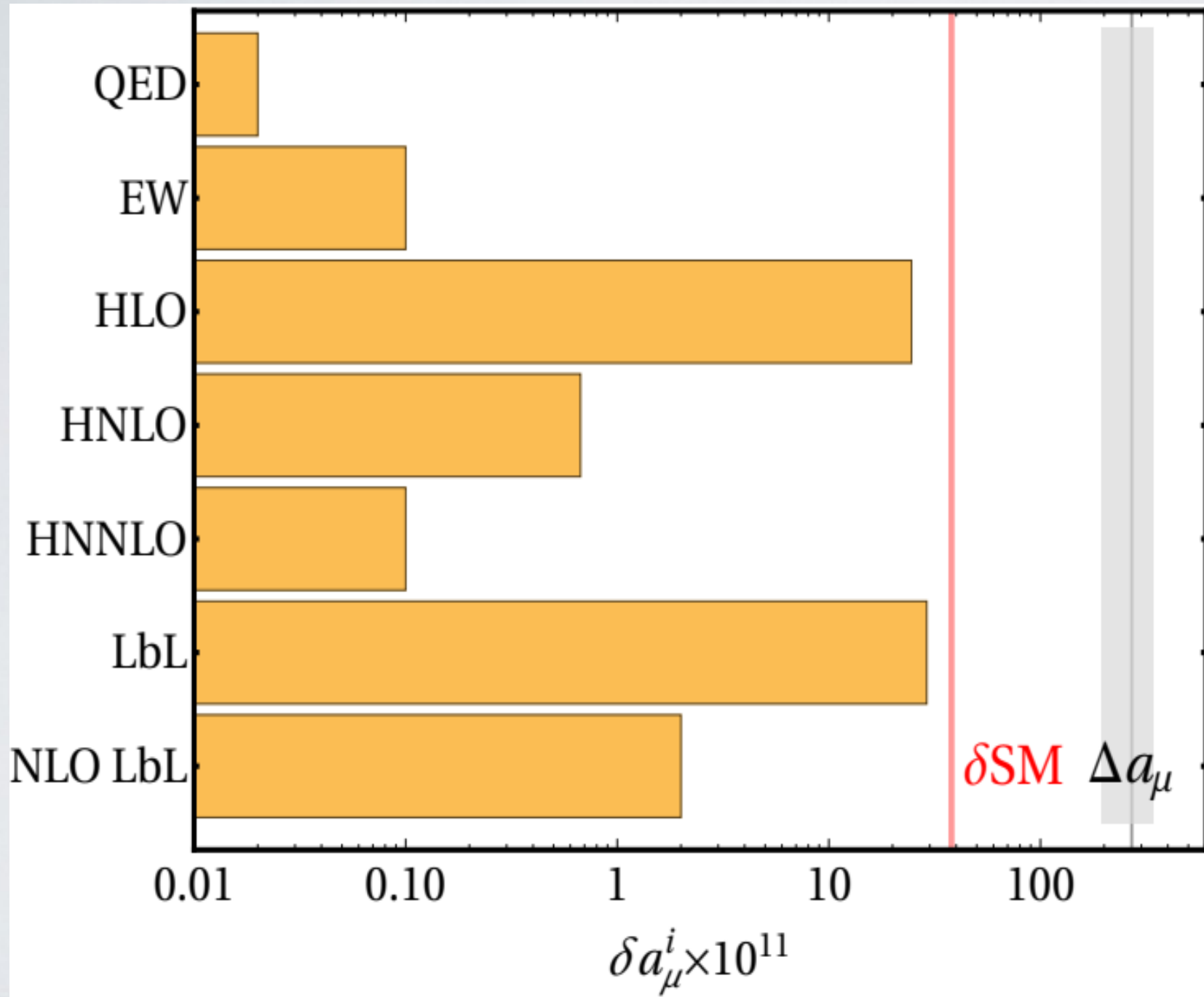
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➤ Muon g-2 experiment at FNAL is analyzing first run

- Could push difference to 5σ  **Ensure theoretical error**

THEORETICAL ERROR BUDGET



Aoyama, Kinoshita, Nio

Gneding, Stöckinger,
Stöckinger-Kim

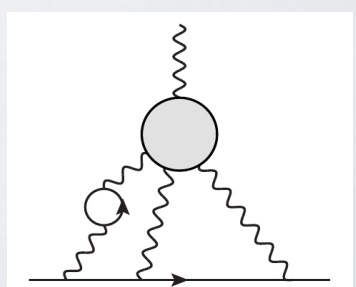
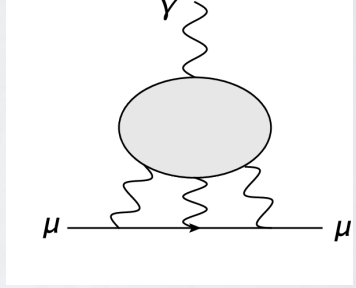
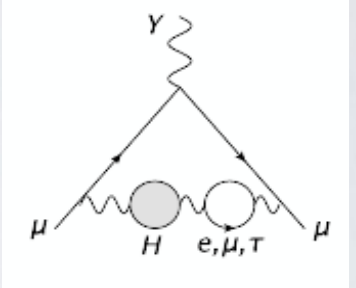
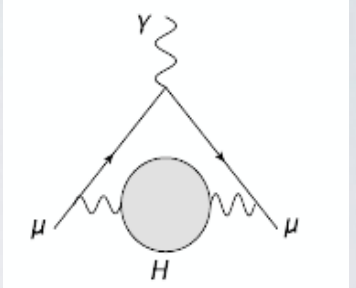
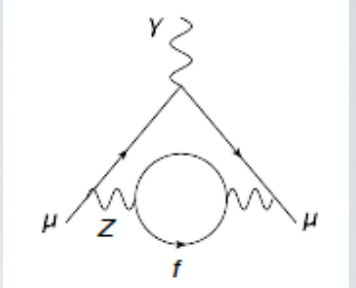
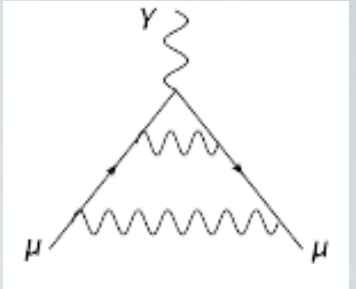
Keshavarzi, Nomura,
Teubner

Jegerlehner

Kurz, Liu, Marquard,
Steinhauser

Jegerlehner

Colangelo, Hoferichter,
Nyffeler, Passera, Stoffer



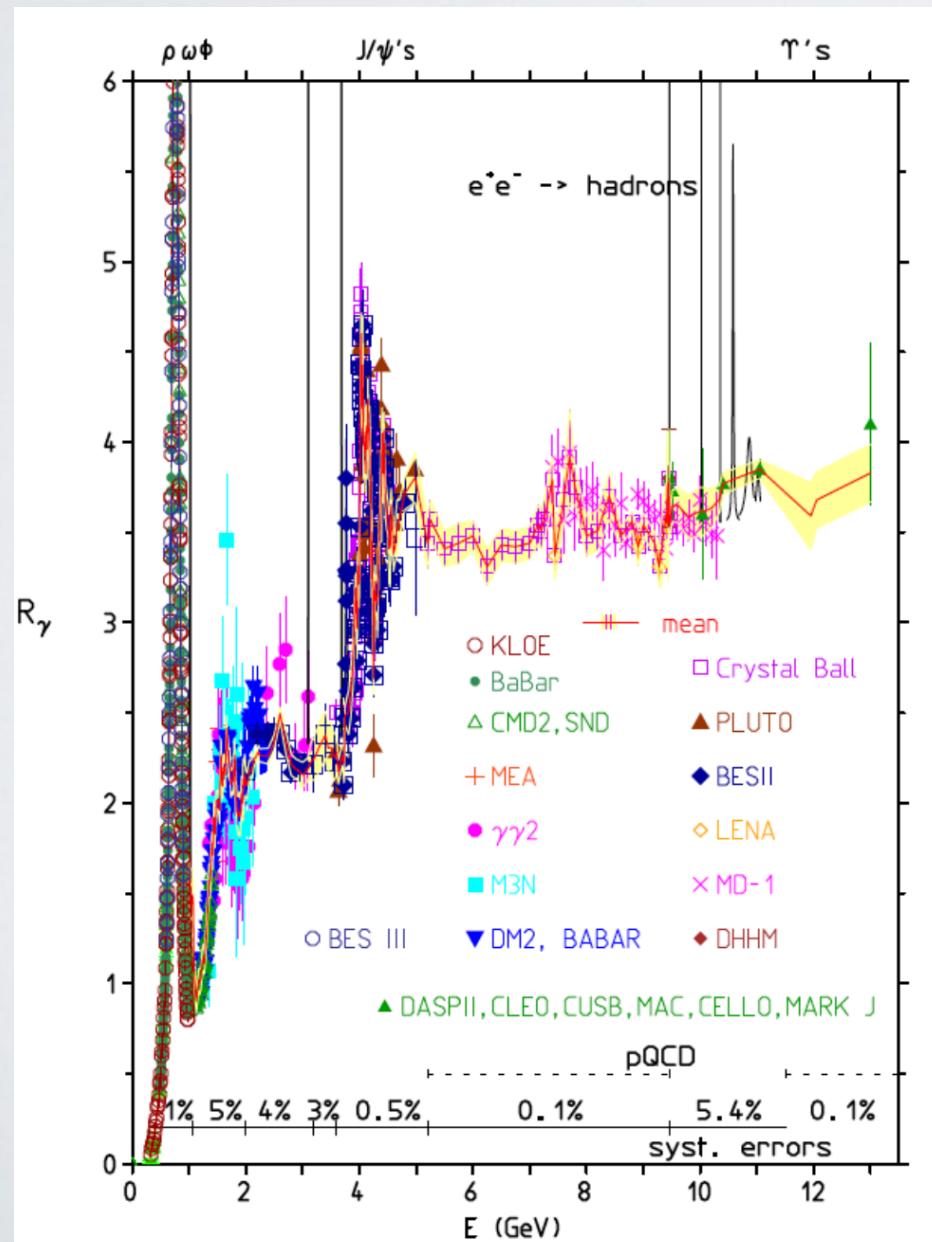
LEADING HADRONIC CONTRIBUTION

Time-like

➤ Extract a_{μ}^{HLO} from R-Ratio

Bouchiat; Michele; Durand; Gourdin, de Rafael

$$a_{\mu}^{\text{HLO}} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds \int_0^1 dx \frac{x^2(1-x)}{x^2 + (1-x)s/m_{\mu}^2} R^{\text{had}}(s)$$



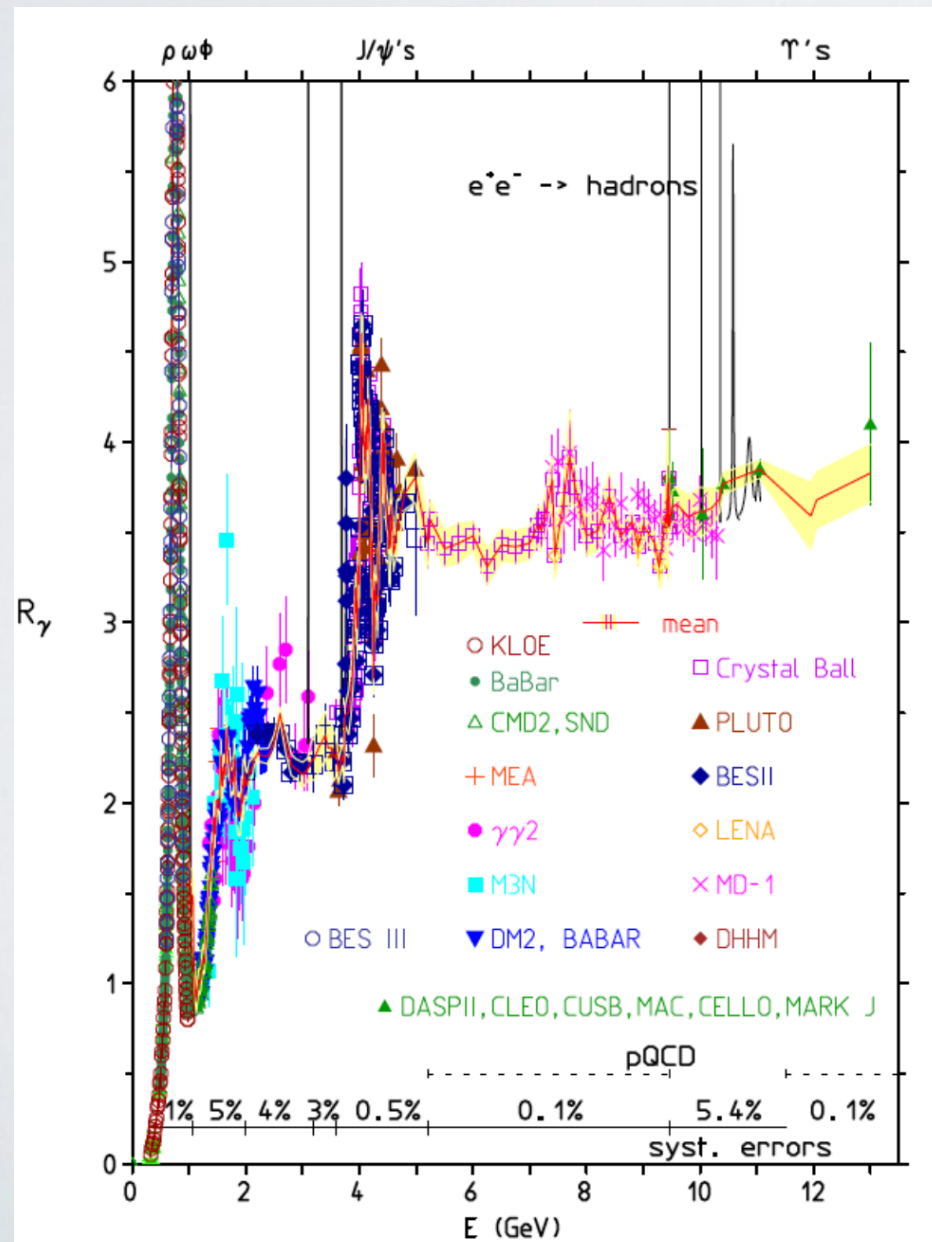
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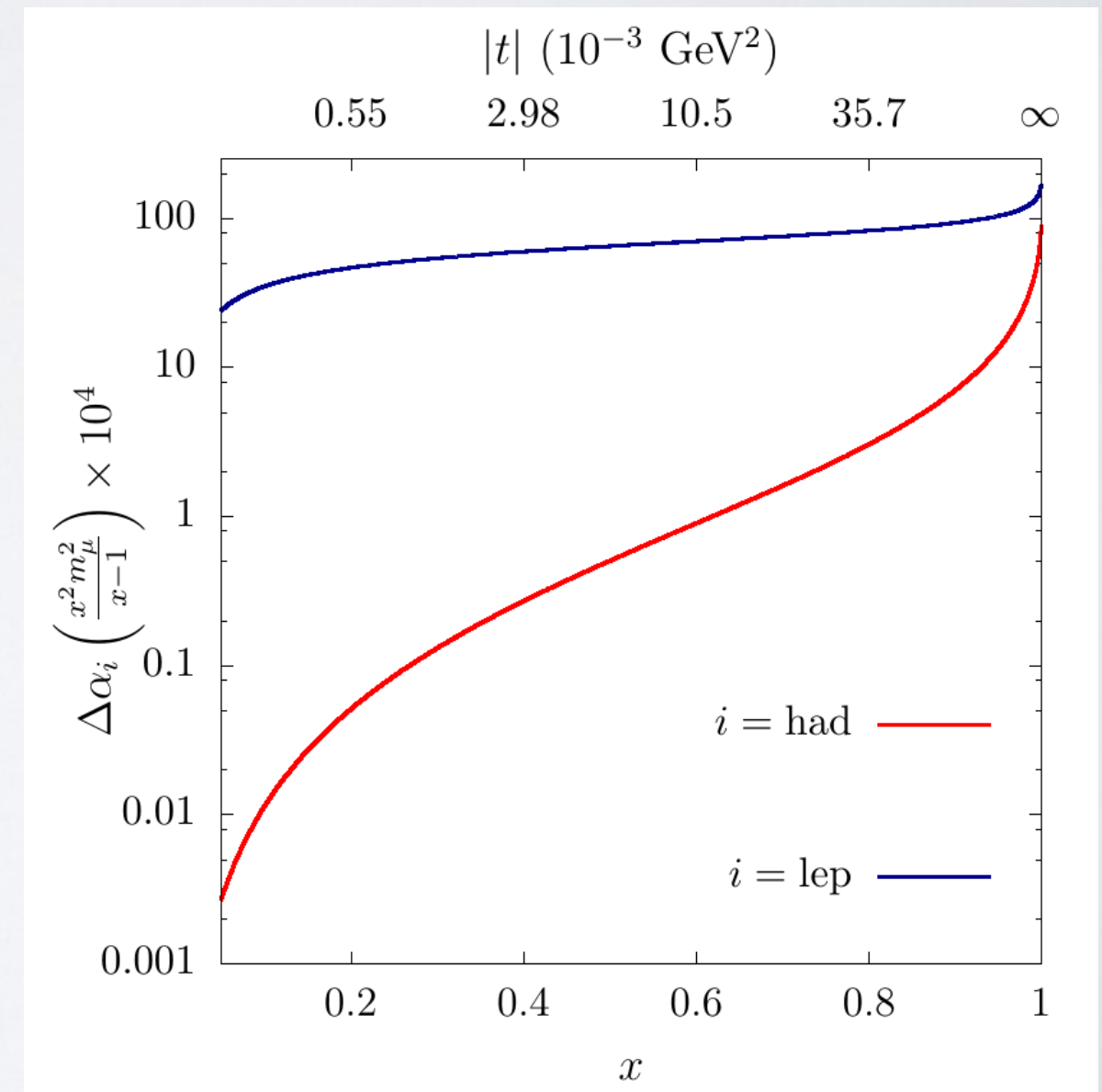


Space-like

➤ Extract a_μ^{HLO} from running of α

Carloni Calame, Passera, Trentadue, Venanzoni

$$a_\mu^{\text{HLO}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)]$$

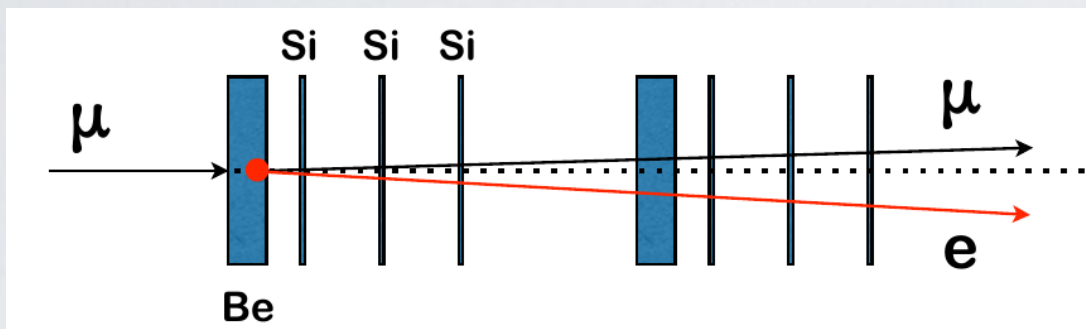




MUONE EXPERIMENT

Carlone Calame, Passera, Trentadue, Venanzoni

- Scatter 150 GeV muons of atomic electrons

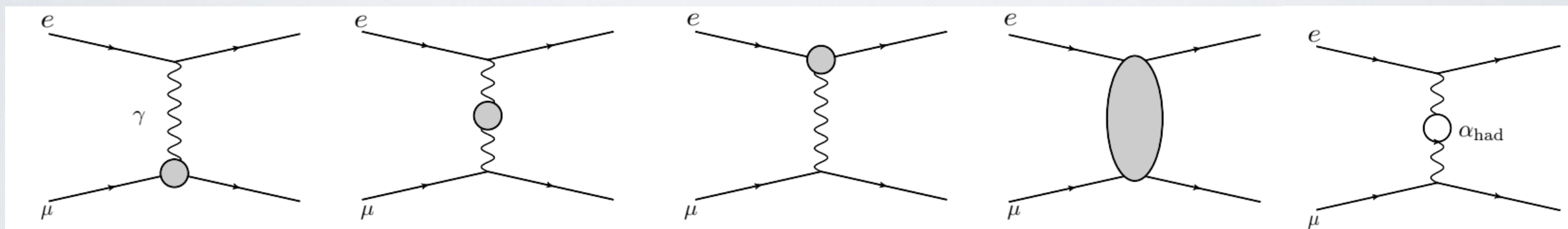


$$s = 0.164 \text{ GeV}^2$$

$$-0.143 \text{ GeV}^2 < t < 0 \text{ GeV}^2$$

$$0 < x < 0.93$$

- Extract $\Delta\alpha_{\text{Had}}$ from Muon-Electron scattering



- Unaccounted BSM contributions are fitted into $\Delta\alpha_{\text{Had}}$

$$\Delta\alpha_{\text{Had}} = \frac{\text{[Diagram with } \alpha_{\text{had}} \text{ loop]}}{\text{[Diagram with } \gamma \text{ exchange]}}$$

$$\Delta\alpha_{\text{BSM}} = \frac{\text{[Diagram with BSM loop]}}{\text{[Diagram with } \gamma \text{ exchange]}}$$

DARK PHOTON

$$s = 0.164 \text{ GeV}^2$$

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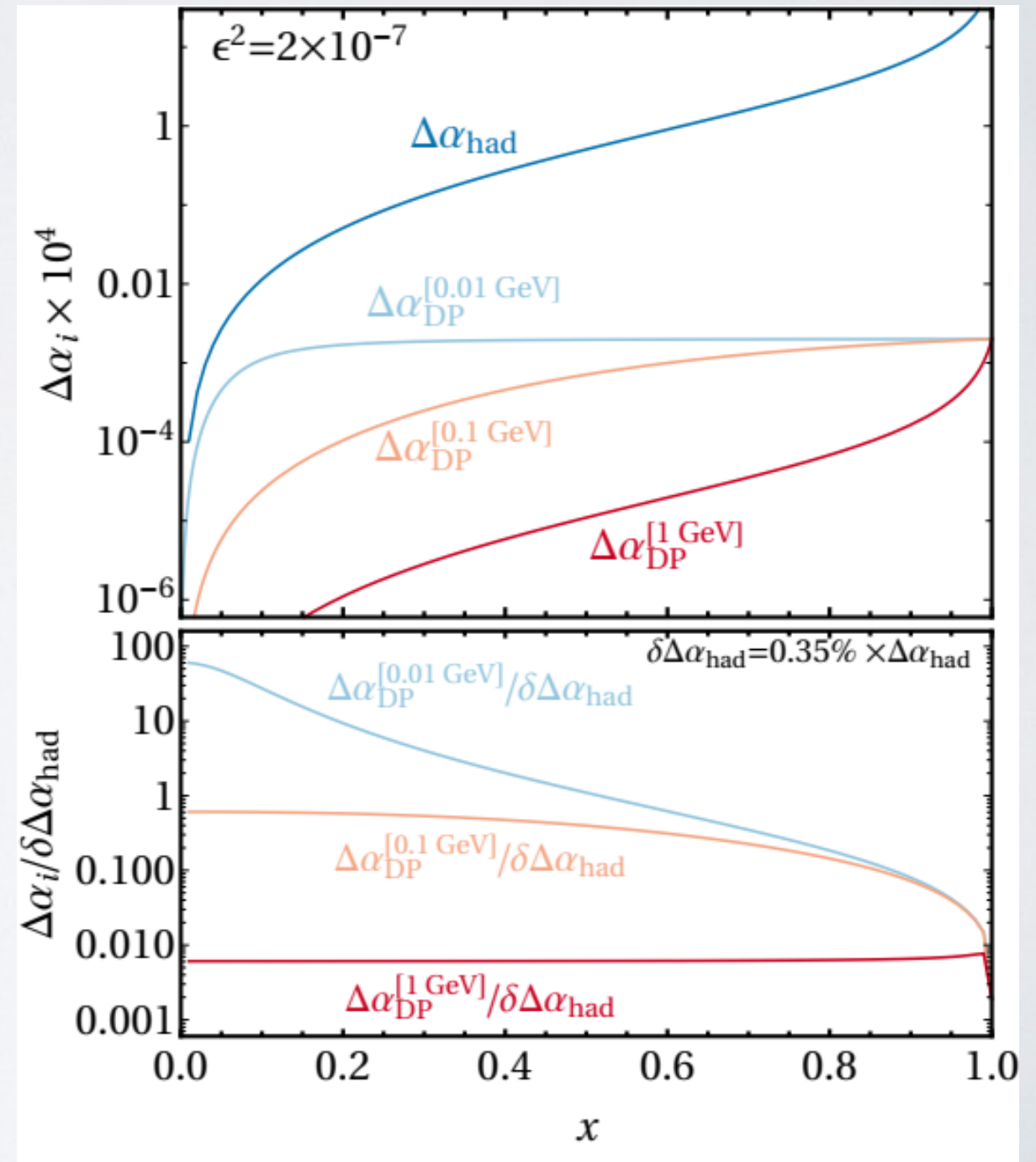
$$0 < x < 0.93$$

- Mixes with Standard Model photon

$$\Delta\alpha_{\text{DP}} = \frac{\epsilon^2 t}{t - m_{A'}^2}$$

$$\mathcal{L} = -\frac{1}{4}\hat{F}_{\mu\nu}\hat{F}^{\mu\nu} - \frac{\epsilon'}{2}\hat{F}_{\mu\nu}\hat{X}_{\mu\nu} - \frac{1}{4}\hat{X}_{\mu\nu}\hat{X}^{\mu\nu} - g' y_\mu^Y \hat{B}^\mu + \frac{1}{2}\hat{M}_X^2 \hat{X}_\mu X^\mu$$

- Gives measurable contribution



DARK PHOTON

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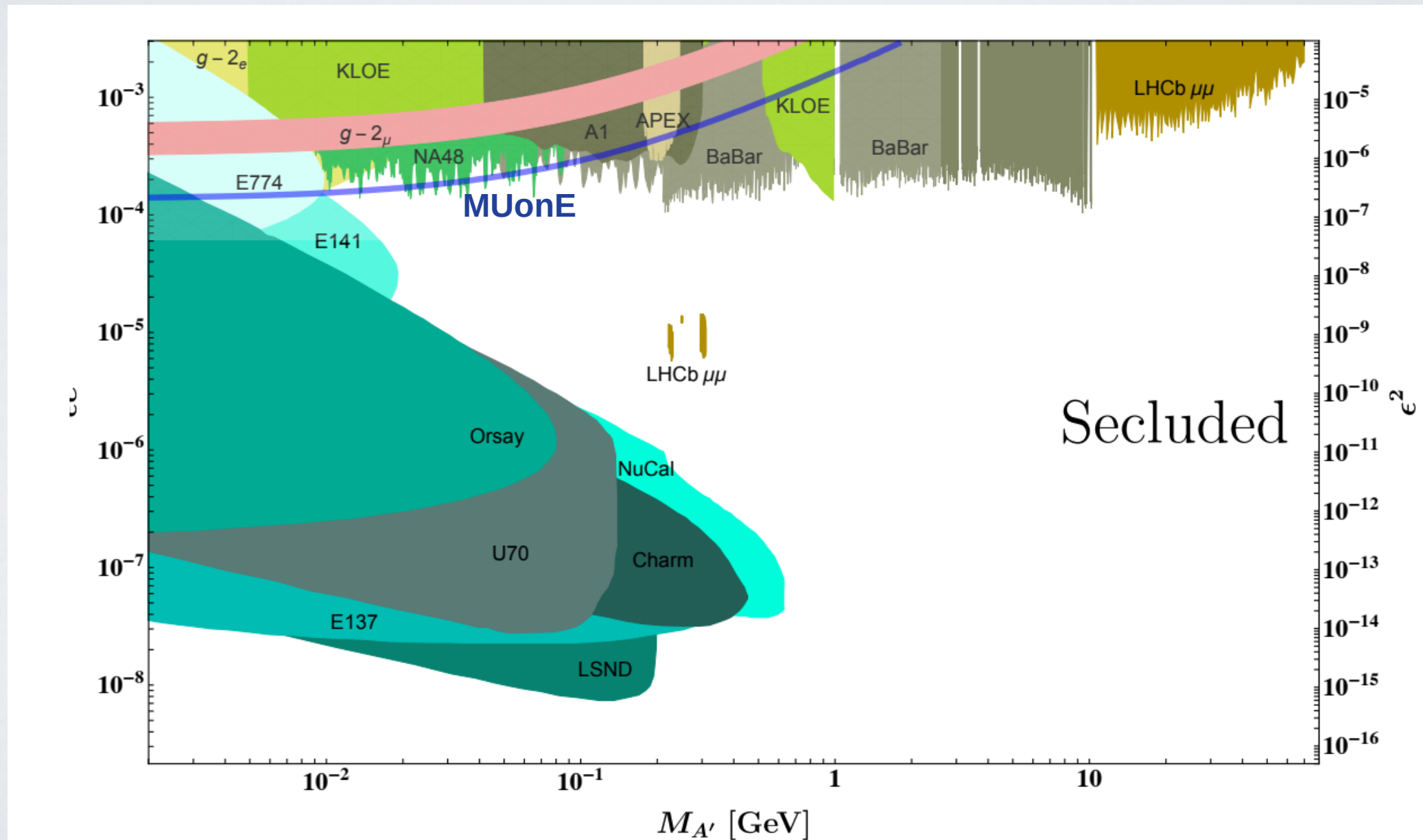
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- MuonE can set exclusion limits



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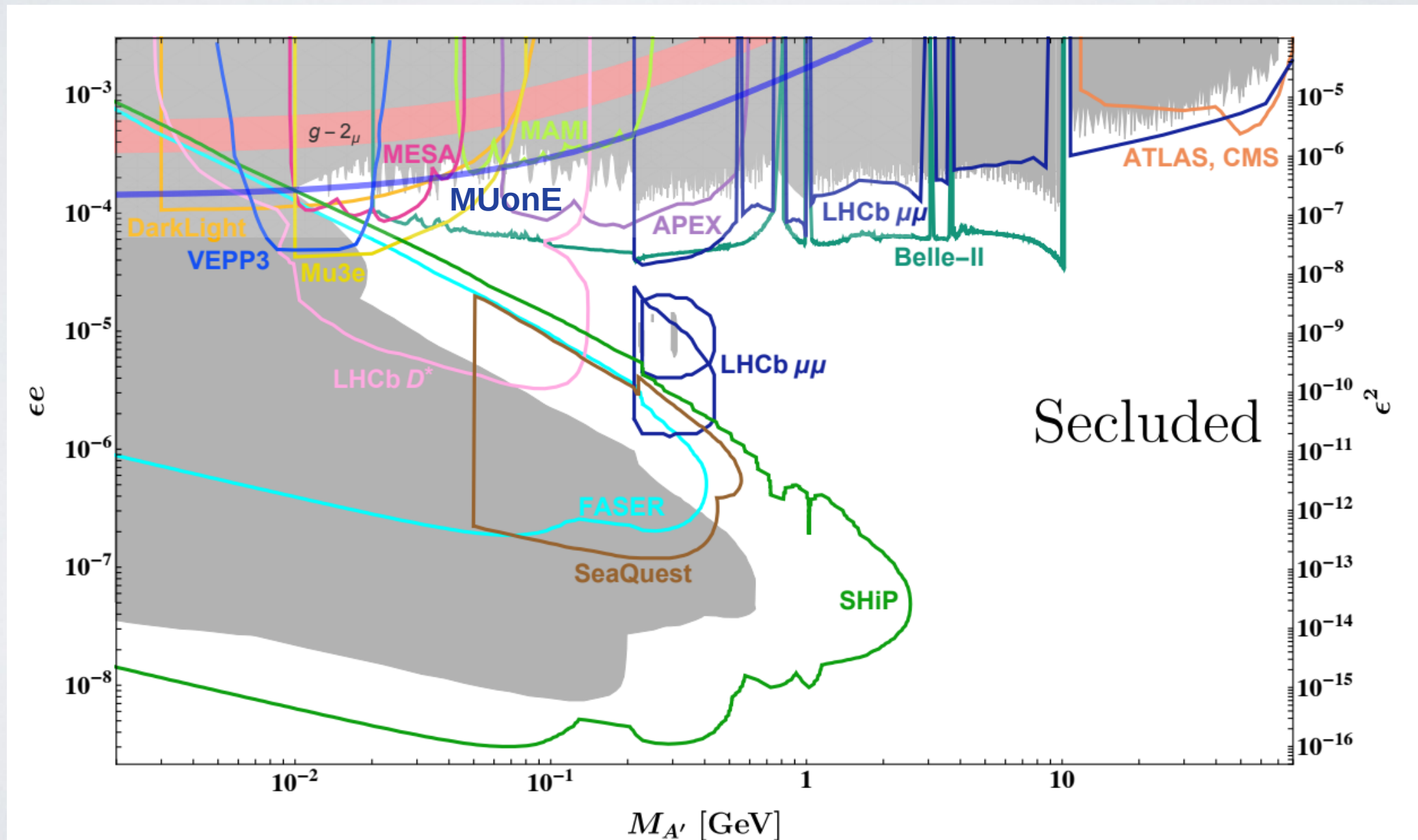
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BSM @ ONE-LOOP

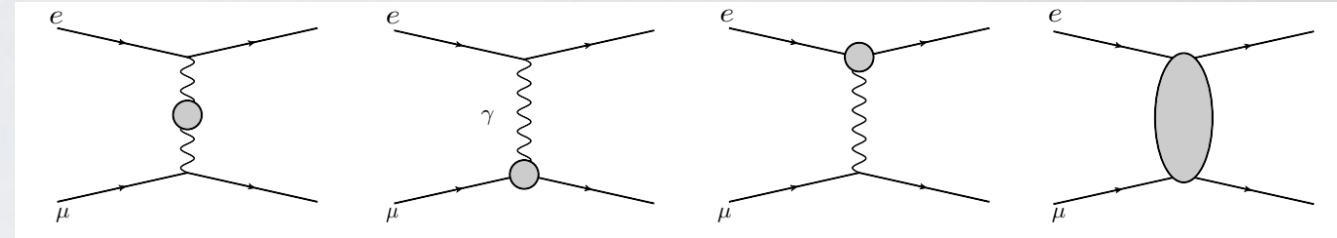
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➤ Photon propagator corrections

$$\Delta\alpha_{BSM}^\gamma = \Re[\Sigma^r(t)]$$

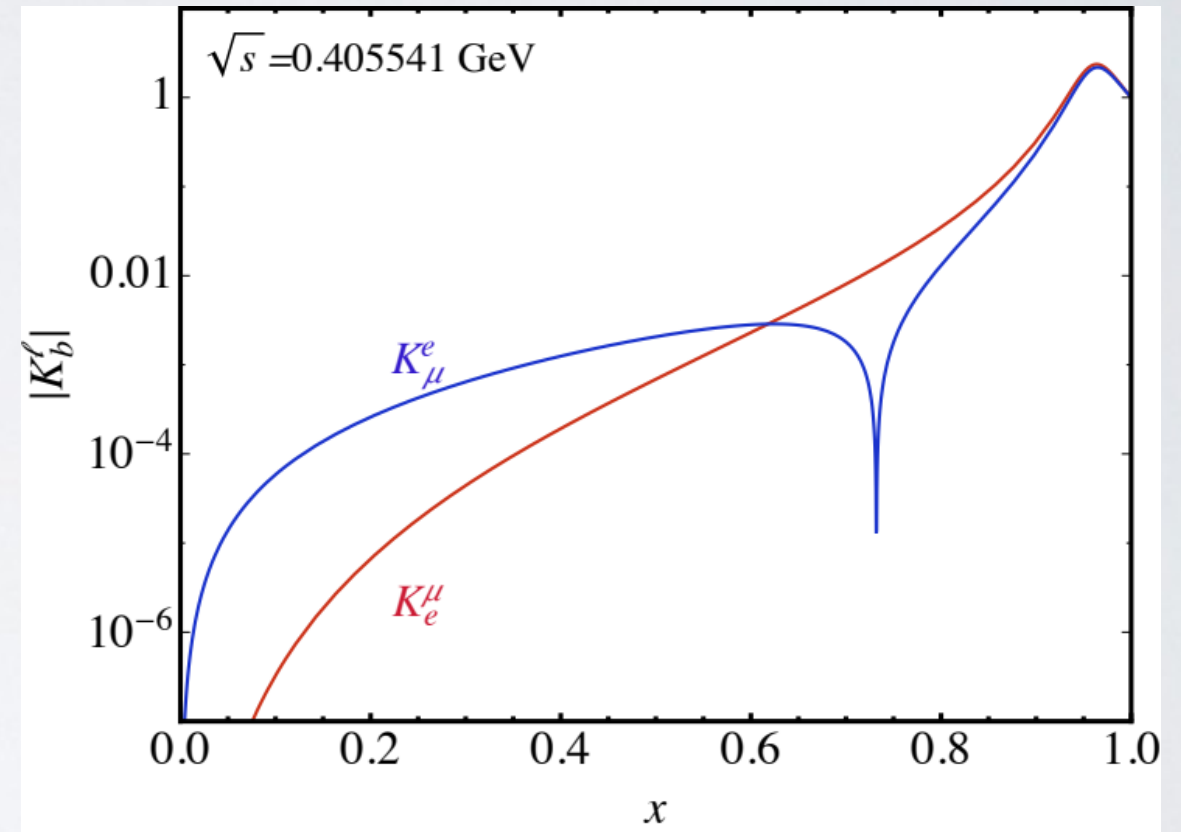


➤ Vertex corrections

$$\Delta\alpha_{BSM}^\ell = F_e^{r,\ell}(t) + K_b^\ell F_m^{r,\ell}(t)$$

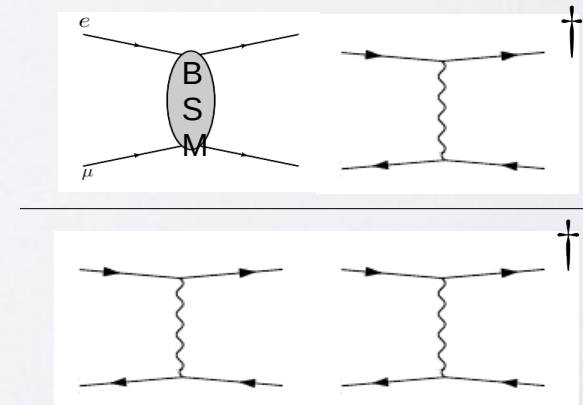
Recall:

$$F_m^{r,\ell}(0) = a_l$$



➤ Box corrections

Suppressed by massless propagator



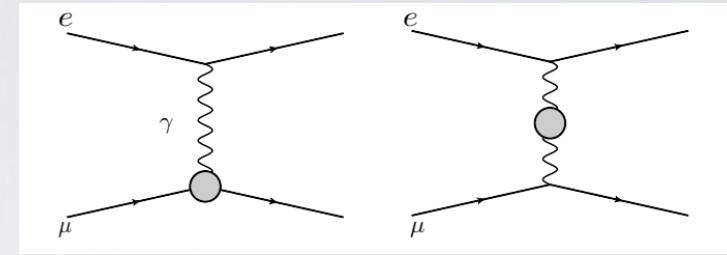
BSM @ ONE-LOOP

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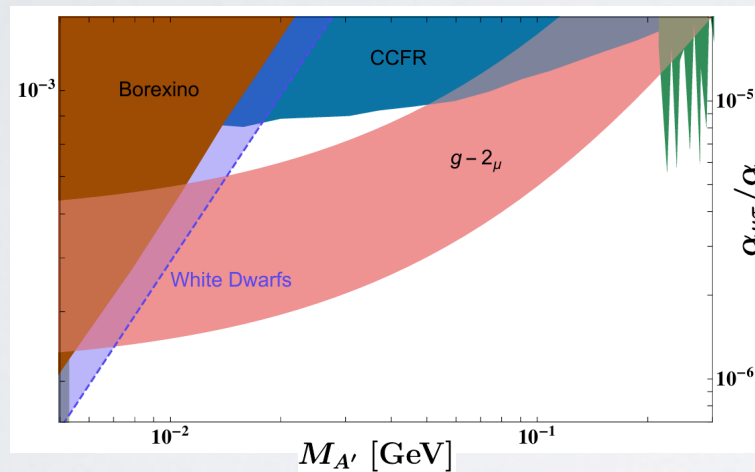
$$-0.143 \text{ GeV}^2 < t < 0 \text{ GeV}^2$$

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➤ Dark photon coupling to μ and τ

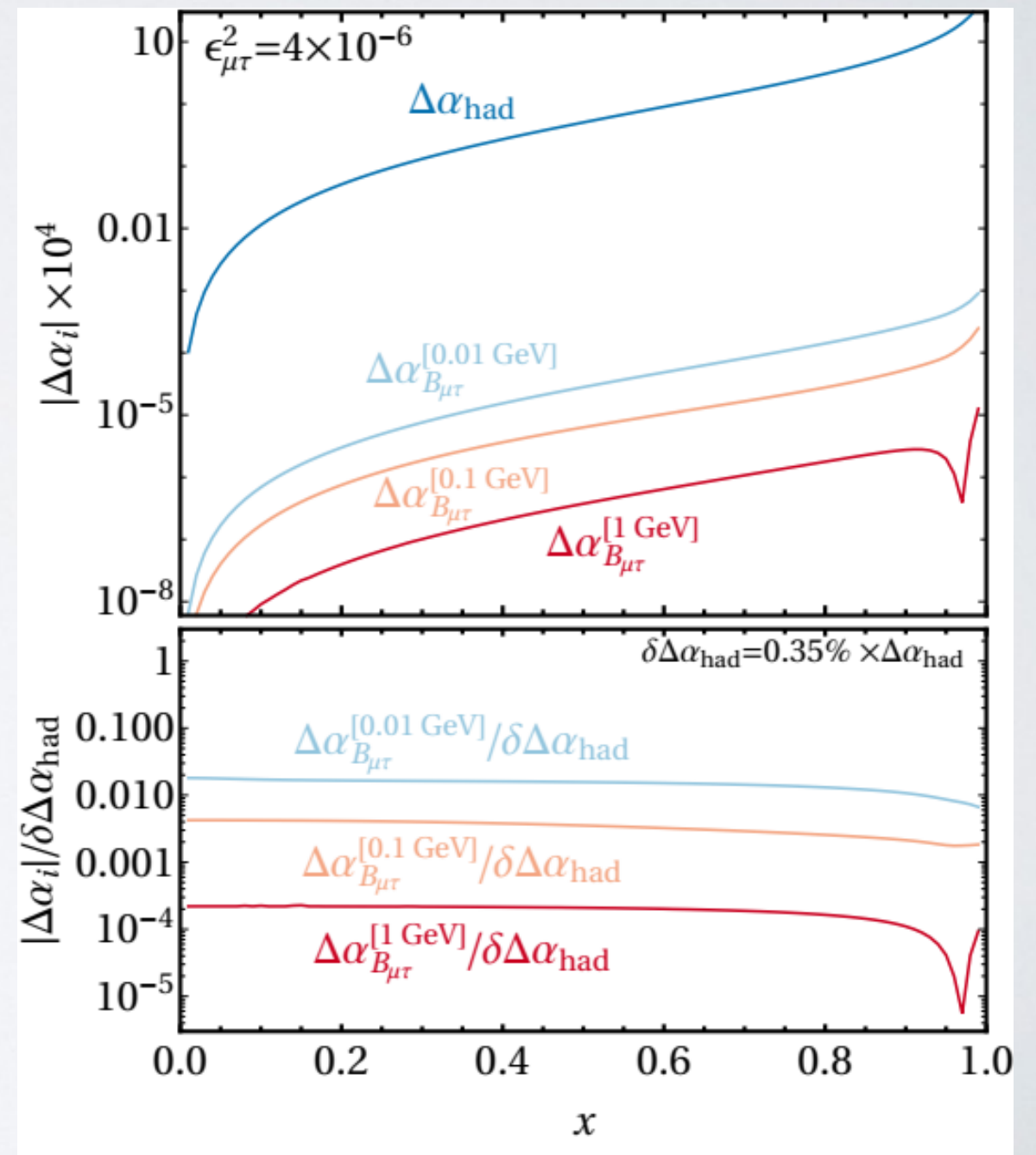


➤ Viable muon $g-2$ explanation



Bauer, Foldenauer, Jaeckel

➤ Negligible contribution to MUonE



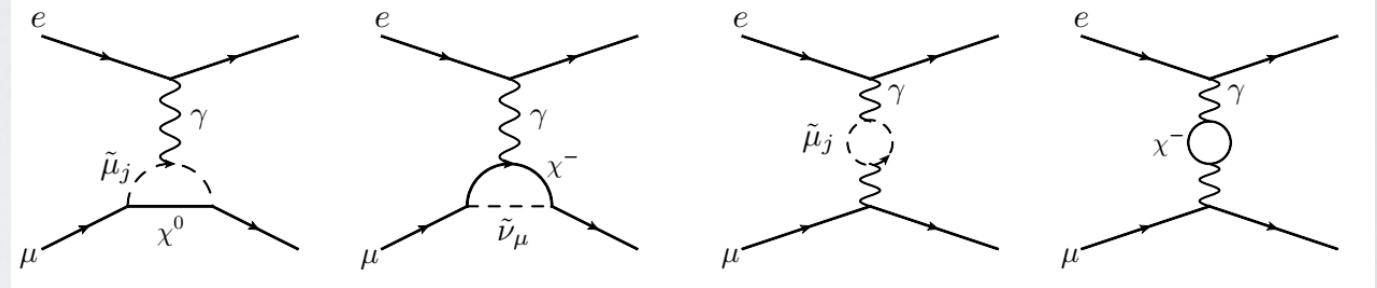
MSSM

$$s = 0.164 \text{ GeV}^2$$

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$$0 < x < 0.93$$

➤ Contribution from Smuons-Neutralinos and Chargino-Sneutrinos



➤ Negligible contribution to MUonE

L :

$$M_2 = 200 \text{ GeV}$$

$$\mu = 200 \text{ GeV}$$

$$\tan \beta = 4$$

$$m_{\mu,L} = 100 \text{ GeV}$$

$$m_{\mu,R} = 100 \text{ GeV}$$

$$A_\mu = 0$$

H :

$$M_2 = 700 \text{ GeV}$$

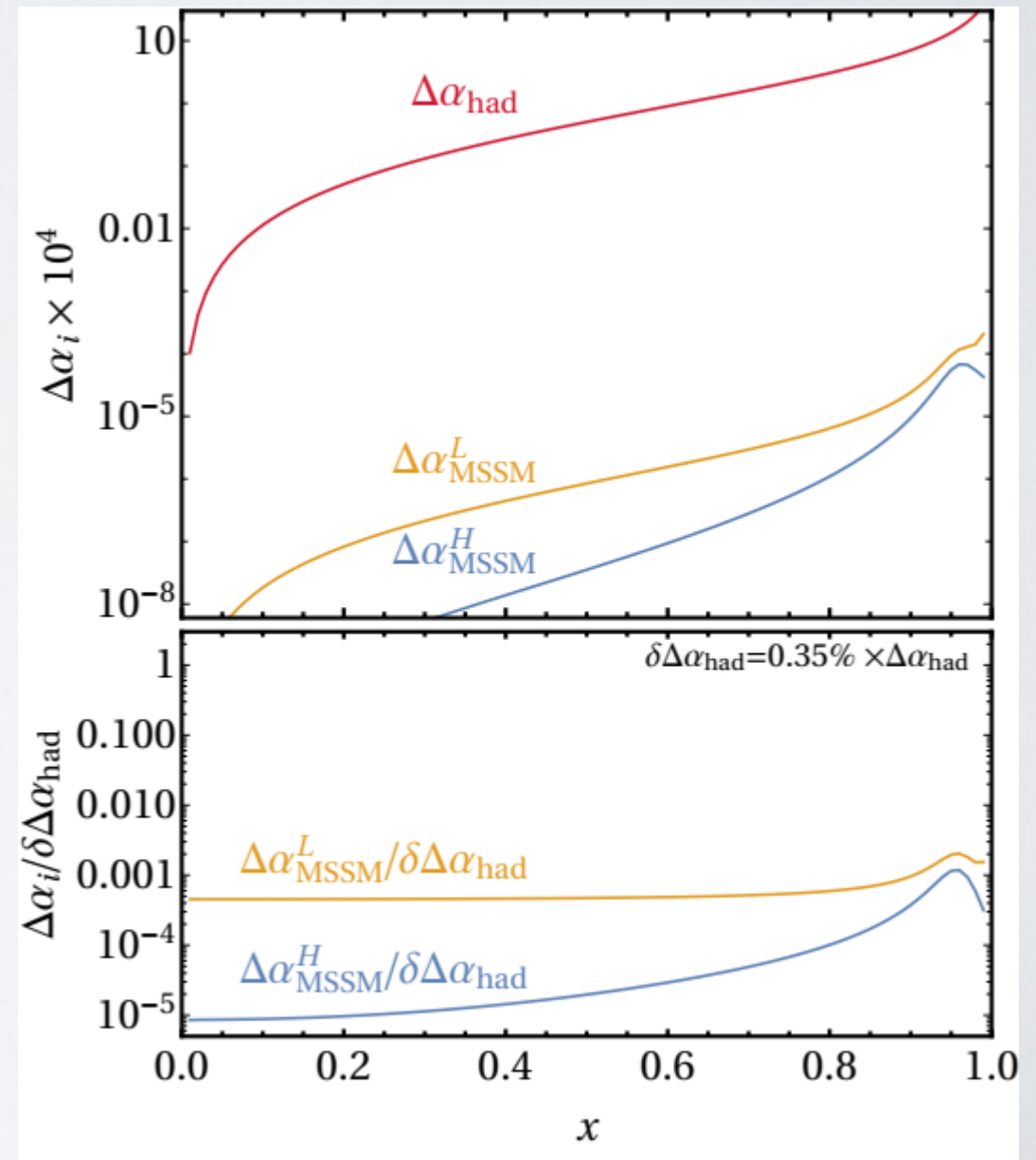
$$\mu = 700 \text{ GeV}$$

$$\tan \beta = 30$$

$$m_{\mu,L} = 300 \text{ GeV}$$

$$m_{\mu,R} = 100 \text{ GeV}$$

$$A_\mu = 0$$



CONCLUSIONS

- **New results from Muon g-2 at Fermilab expected this summer**
 - **Could push tension with Standard Model to 5σ**
- **Main theoretical errors from $\delta a_{\mu}^{\text{HLO}}$ and $\delta a_{\mu}^{\text{LbL}}$**
- **MUonE provides new and independent way to measure a_{μ}^{HLO}**
- **Unaccounted BSM physics contributes to $\delta a_{\mu}^{\text{HLO}}$**
- **Light new physics coupling at tree-level has biggest impact**
 - **MuonE could set exclusion limits on dark photon models**
- **BSM explanations of g-2 are kinematically suppressed**
 - **Loop contributions from MSSM and $B_{\mu\tau}$ negligible**

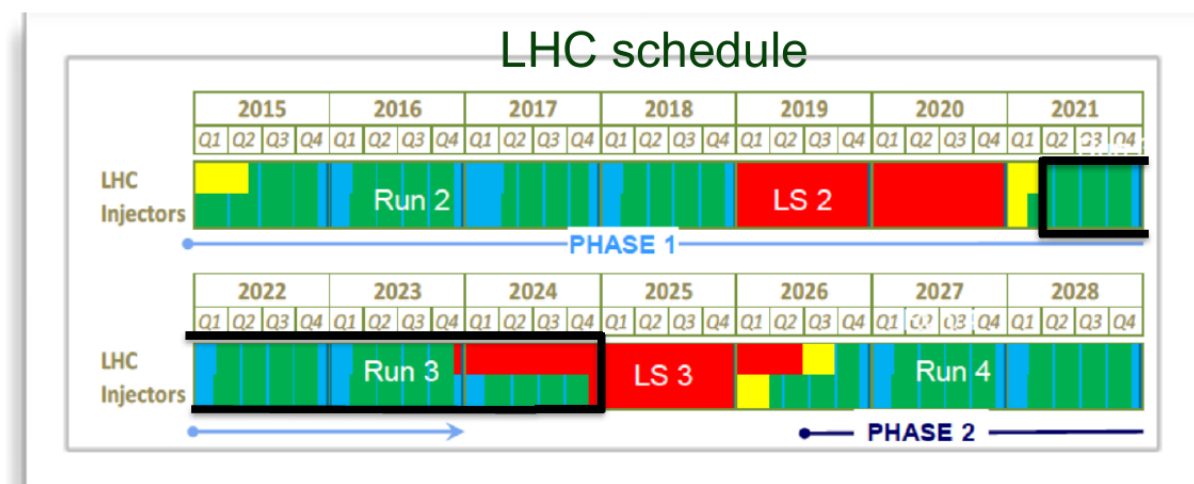
BACKUP SLIDES

- CERN's **Physics Beyond Colliders Working Group Report**:
 “The aim of the MUonE proposal... would be an extremely valuable independent determination for the value of $(g-2)_\mu$ ”

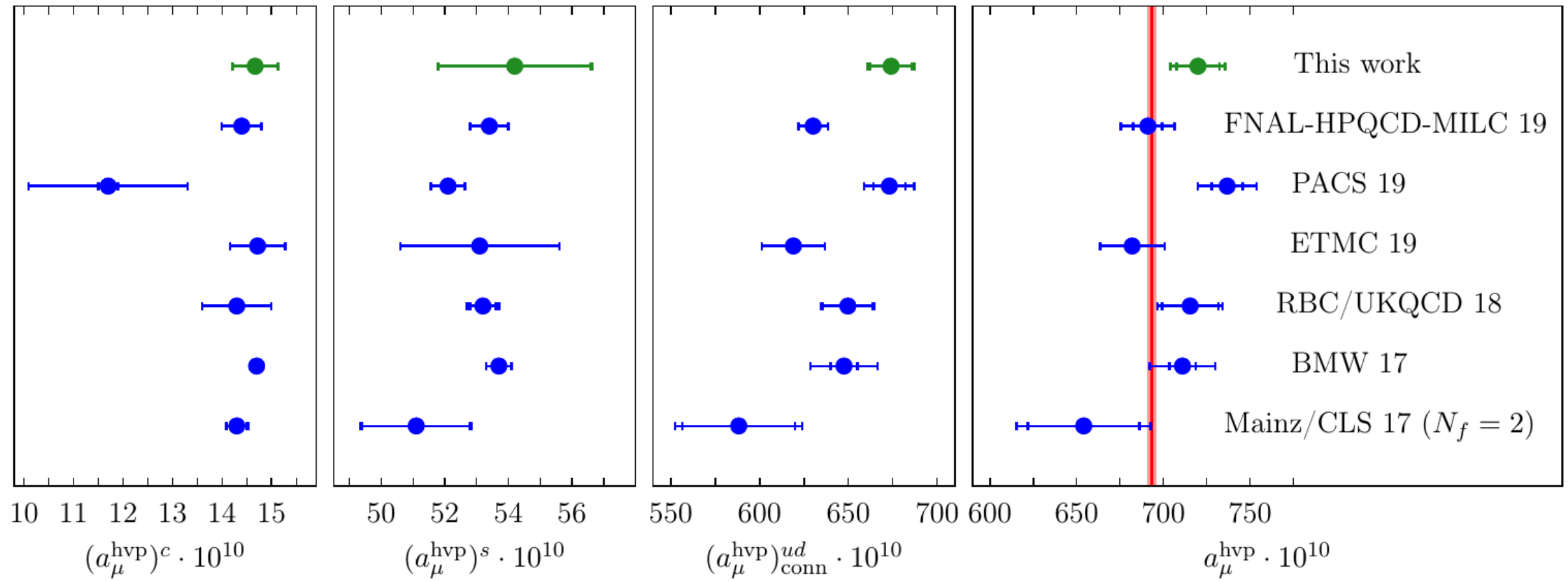
A. Dainese et al., CERN-PBC-REPORT-2018-008, arXiv:1901.04482

- **2019**
 - Letter of Intent planned to CERN's SPSC
 - Detector optimisation-test beam
- **2020-21**
 - Detector construction & installation
 - Pilot run in 2021
- **2022-24**
 - 1st run: scaled detector and reduced accuracy

See Marconi's & Venanzoni's talks



LATTICE RESULTS



Gérardin, Cè, von Hippel, Hörz, Meyer, Mohler, Ottnad, Wilhelm, Wittig