



The Dominion of Light Dark Matter

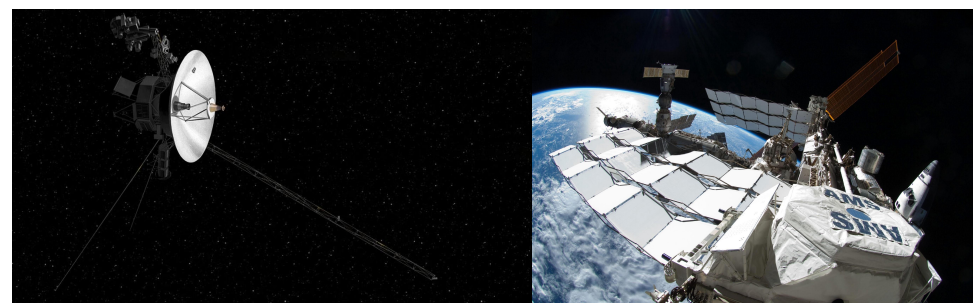
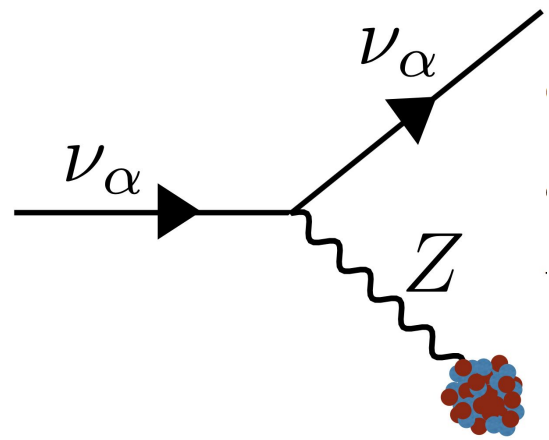
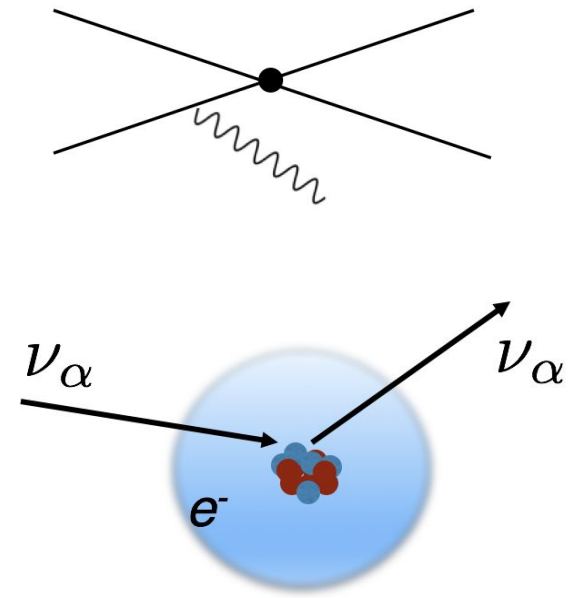
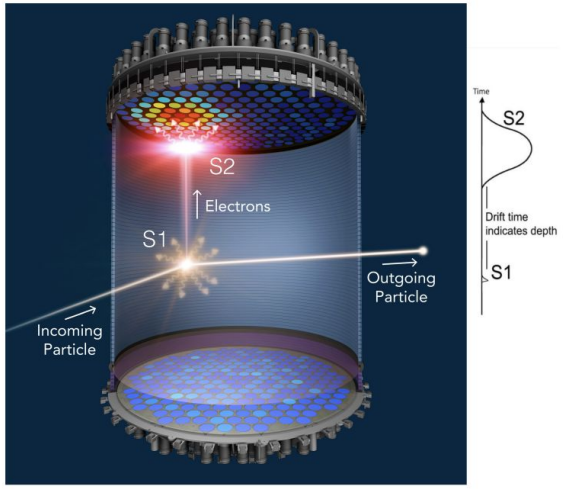
James Dent



Sam Houston State University

René Magritte, *L'empire des lumières*

Outline



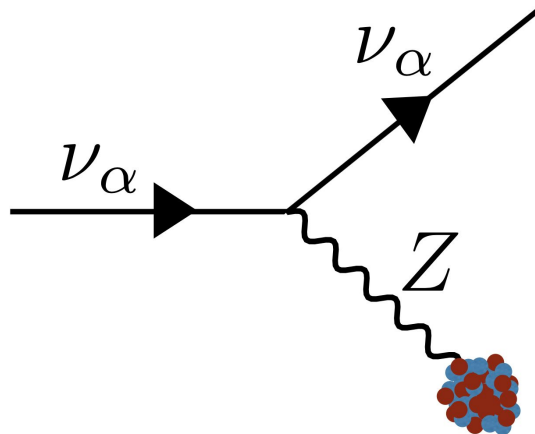
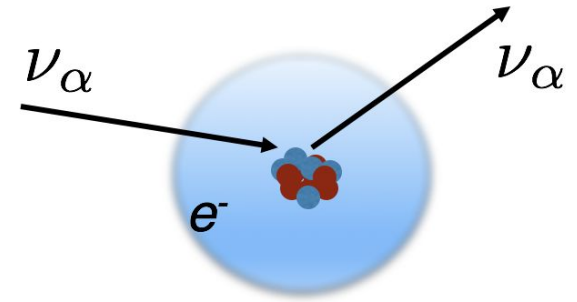
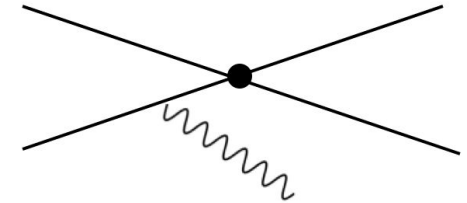
The Migdal Effect and Photon Bremsstrahlung in effective field theories of dark matter direct detection and coherent elastic neutrino-nucleus scattering

[arXiv:1905.00046](https://arxiv.org/abs/1905.00046)

Nicole Bell Jayden Newstead Subir Sabharwal Tom Weiler

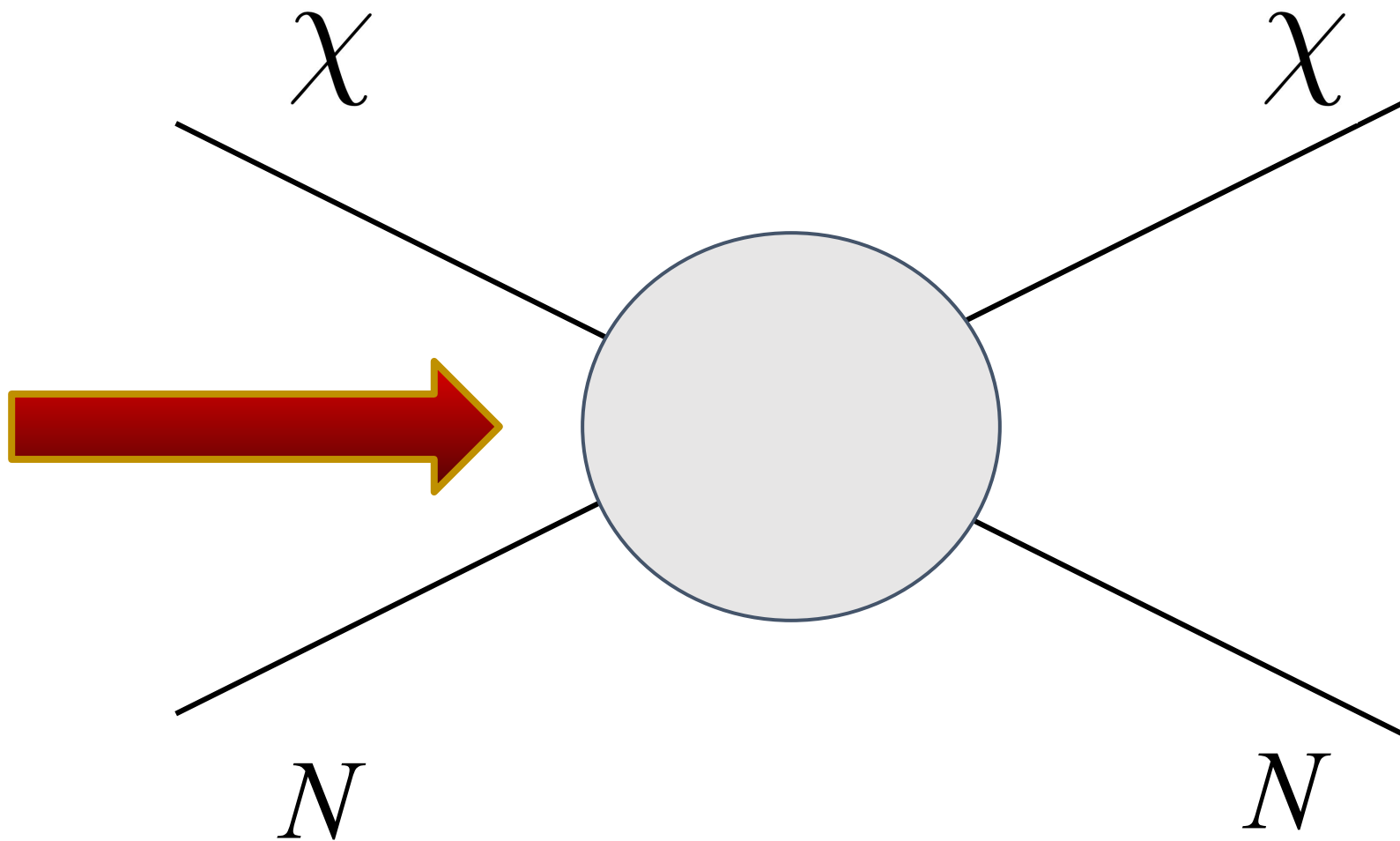


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Jayden Newstead
Bhaskar Dutta Ian Shoemaker





Direct Detection Review

Momentum Exchanged $O(<100\text{MeV})$

$$q = \sqrt{2m_T E_R}$$

Recoil energy $O(10\text{keV})$

$$E_R = \frac{\mu_{\chi T}^2 v^2}{m_T} (1 - \cos \theta)$$

Incident energy

$$E_i = \frac{m_\chi v^2}{2}$$

$$v \sim \mathcal{O}(10^{-3})$$

$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

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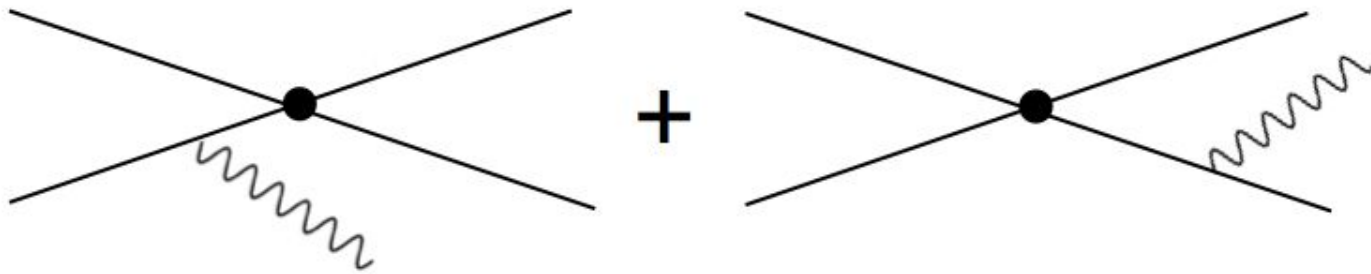
$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

For: $m_\chi = 100 \text{ GeV}$ $m_T = 130 \text{ GeV}$, $E_{R,\text{max}} \simeq 50 \text{ keV}$.

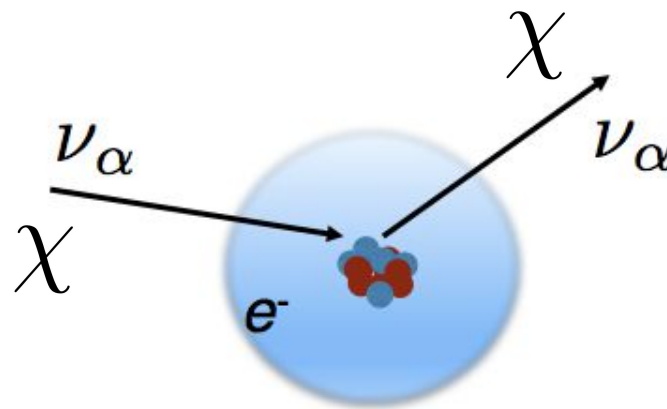
For: $m_\chi = 10 \text{ GeV}$ $m_T = 130 \text{ GeV}$, $E_{R,\text{max}} \simeq 1.3 \text{ keV}$.

Alternative Signals for sub-GeV Probes

Bremsstrahlung



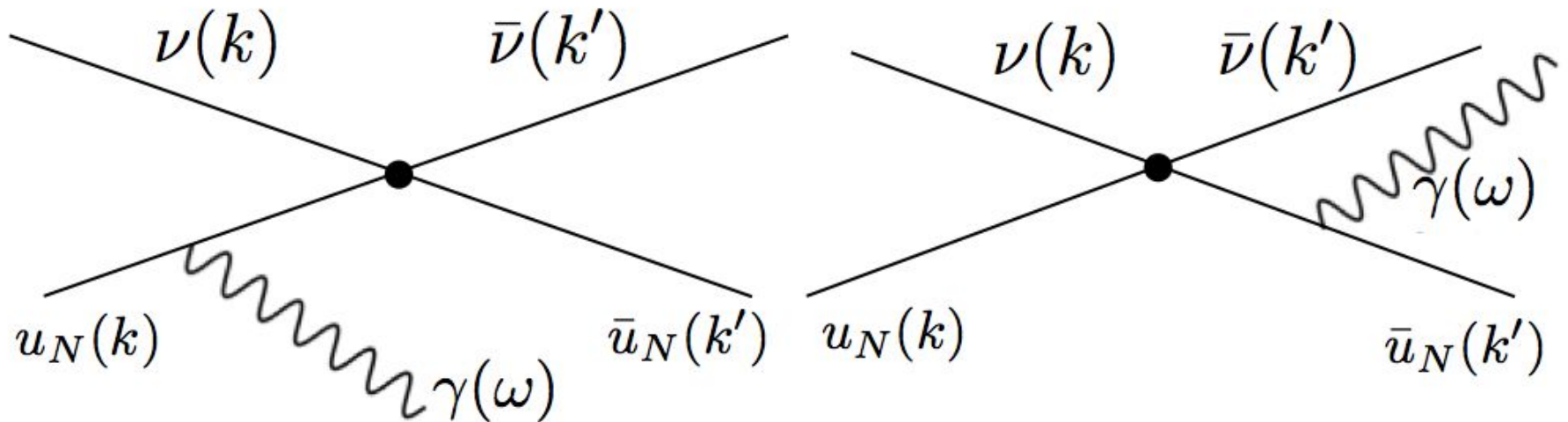
Migdal



Bremsstrahlung in $\chi + N \rightarrow \chi + N + \gamma$ DM scattering has been explored as a means of accessing sub-GeV mass DM

C. Kouvaris and J. Pradler, PRL 2017, 1607.01789

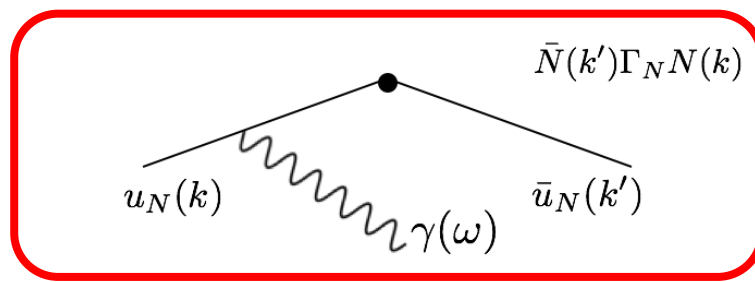
C.McCabe, PhysRevD (2017) 1702.04730



$$\nu + N \rightarrow \nu + N + \gamma$$

We want to examine the possibility of brem signals when nuclear recoil energies are below threshold.

Also see the recent paper: A.Millar, G.Raffelt, L.Stodolsky, and E.Vitagliano, 1810.06584 for very low E_ν with an examination of neutrino mass effects



Bremsstrahlung in the process $\chi + N \rightarrow \chi + N + \gamma$
 Can be used to detect scattering processes that produce nuclear recoils below detector thresholds.

The endpoints of the maximum nuclear recoil energy and emitted photon are key to the extended reach

$$v_{\min} = \frac{m_T E_R + \mu_T \delta}{\mu_T \sqrt{2m_T E_R}}$$

$$E_{R,\max} = \frac{2\mu_T^2 v_{\max}^2}{m_T},$$

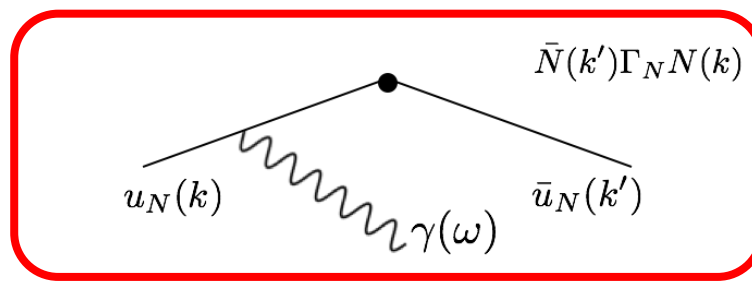
$$\delta_{\max} = \frac{\mu_T v_{\max}^2}{2}.$$

For the case of dark matter much lighter than the target nucleus

$$m_T \gg m_\chi$$

$$E_{R,\max} \approx 2 \left(\frac{m_\chi}{\text{GeV}} \right)^2 \left(\frac{\text{GeV}}{m_T} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV}$$

$$\delta_{\max} \approx \frac{1}{2} \left(\frac{m_\chi}{\text{GeV}} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV},$$



$$E_{R,\max} \approx 2 \left(\frac{m_\chi}{\text{GeV}} \right)^2 \left(\frac{\text{GeV}}{m_T} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV}$$

$$\delta_{\max} \approx \frac{1}{2} \left(\frac{m_\chi}{\text{GeV}} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV},$$

Typically one finds that sub-GeV dark matter creates

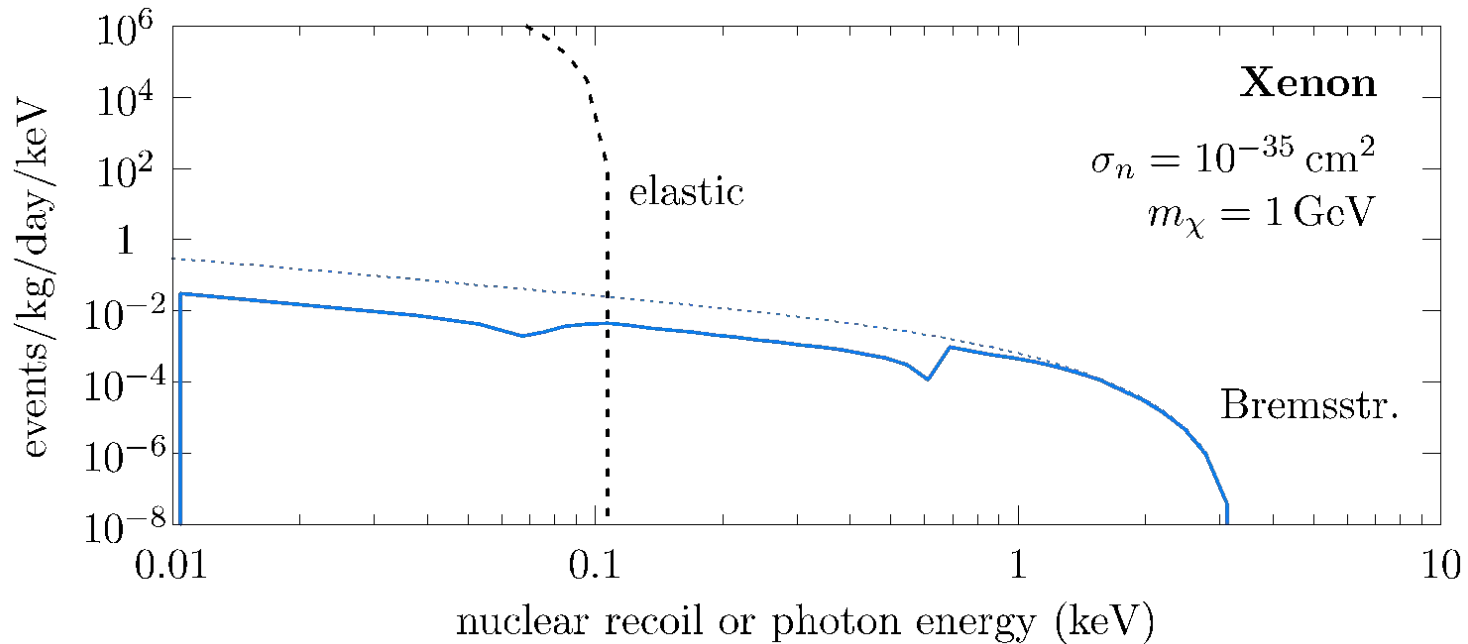
$$\delta_{\max} > E_{R,\max}$$

For example, a 1 GeV particle incident on xenon will produce

$$E_{R,\max} \lesssim 10^{-1} \text{keV} \text{ and } \delta_{\max} \sim 3 \text{keV}$$

The double differential cross-section factorizes into kinematic terms multiplied by the 2-2 elastic differential cross-section

$$\frac{d^2\sigma}{dE_R d\omega} = \frac{4\alpha Z^2}{3\pi} \frac{E_R}{m_T \omega} \left(\frac{d\sigma}{dE_R} \right)_{(2\rightarrow 2)}$$

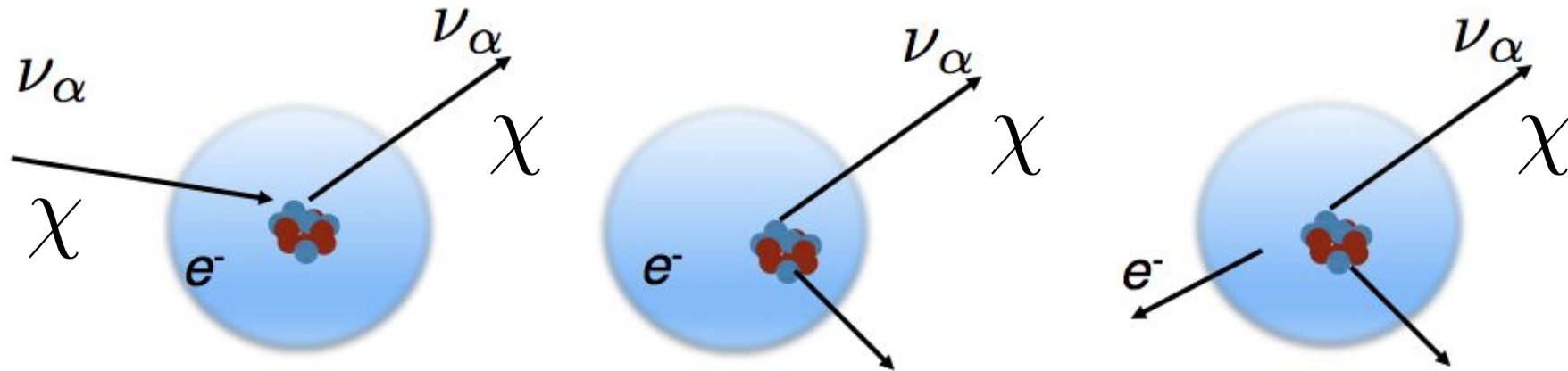


$$\frac{dR}{d\omega} = N_T \frac{\rho_\chi}{m_\chi} \int_{|\mathbf{v}| \geq v_{\min}} d^3\mathbf{v} v f_v(\mathbf{v} + \mathbf{v}_e) \frac{d\sigma}{d\omega}$$

The Migdal Effect

A.B.Migdal, J.Phys. USSR (1941), Landau & Lifschitz, QM Sec.41

Ionization and excitation of electron states from the relative momentum arising when the nucleus is given an impulse.



Proposed for dark matter detection years ago, and recently revisited in more detail.

M. Ibe, W. Nakano, Y. Shoji, and K. Suzuki, JHEP (2018) 1707.07258

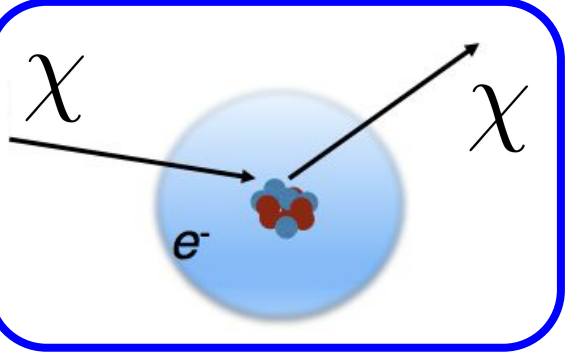
M. Dolan, F. Kahlhoefer, and C. McCabe, PRL(2018) 1711.09906

(above figure adapted from this paper)

Does *not* suffer from the same suppression as brem.

R. Bernabei et al., Int. J. Mod. Phys. A22, 3155 (2007), arXiv:0706.1421

B. M. Roberts, V. V. Flambaum, and G. F. Gribakin, Phys. Rev. Lett. 116, 023201 (2016), arXiv:1509.09044



The double differential cross-section factorizes into the ionization rate multiplied by the 2-2 elastic differential cross-section

$$\frac{d^2 R}{dE_R dv} = \frac{d^2 R_{\chi T}}{dE_R dv} \times |Z_{\text{ion}}|^2$$

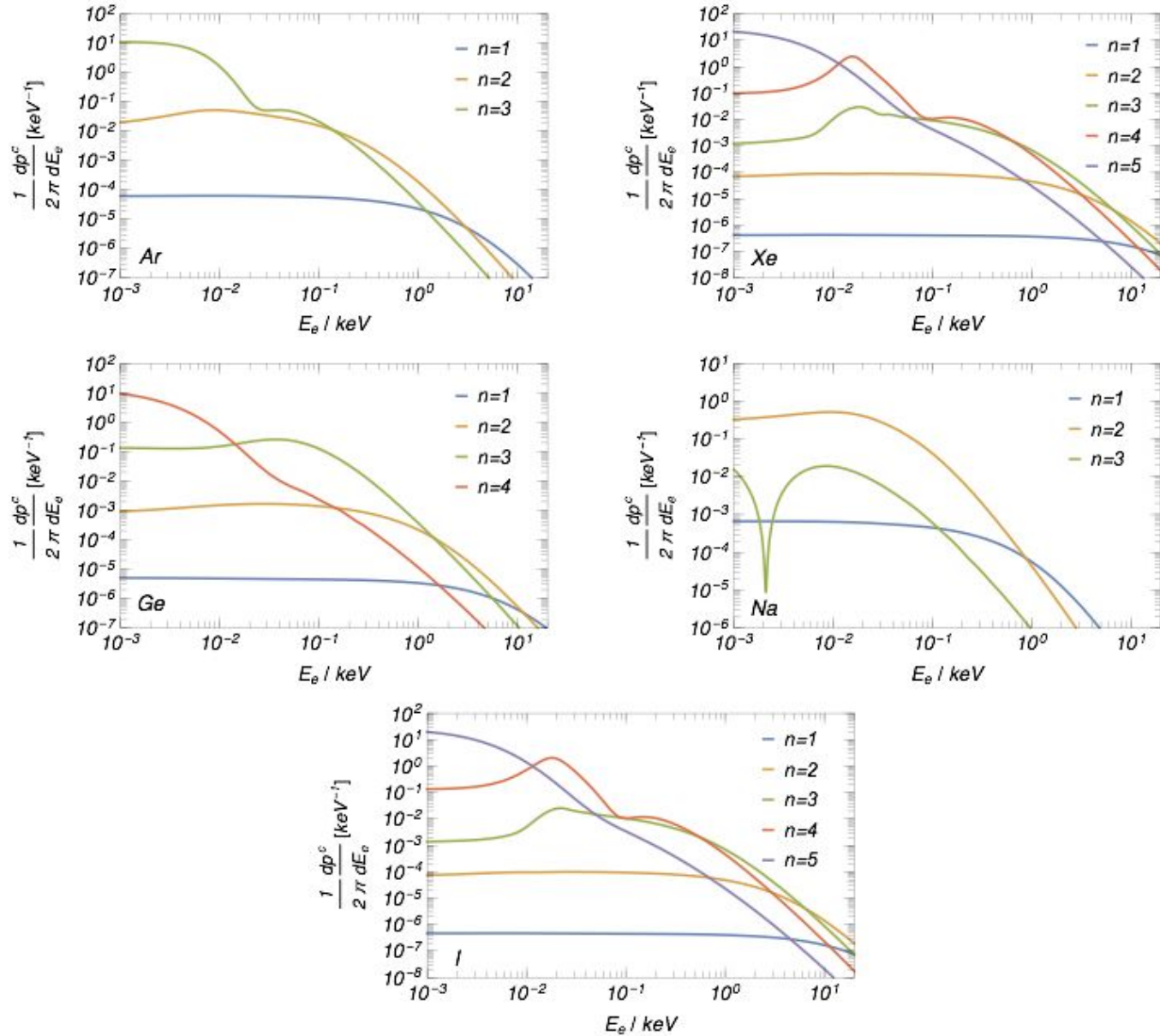
The ionization rate is given in terms of the ionization probability

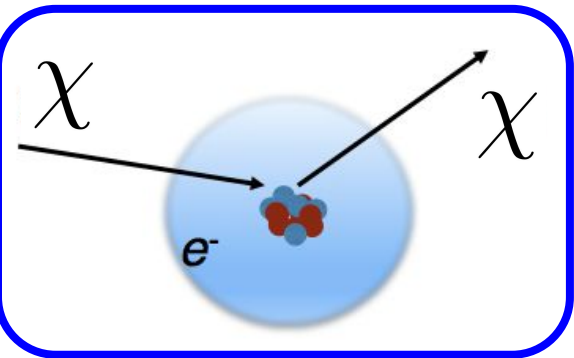
$$|Z_{\text{ion}}|^2 = \frac{1}{2\pi} \sum_{n,\ell} \int dE_e \frac{d}{dE_e} p_{q_e}^c(n\ell \rightarrow (E_e))$$

The differential rate is then

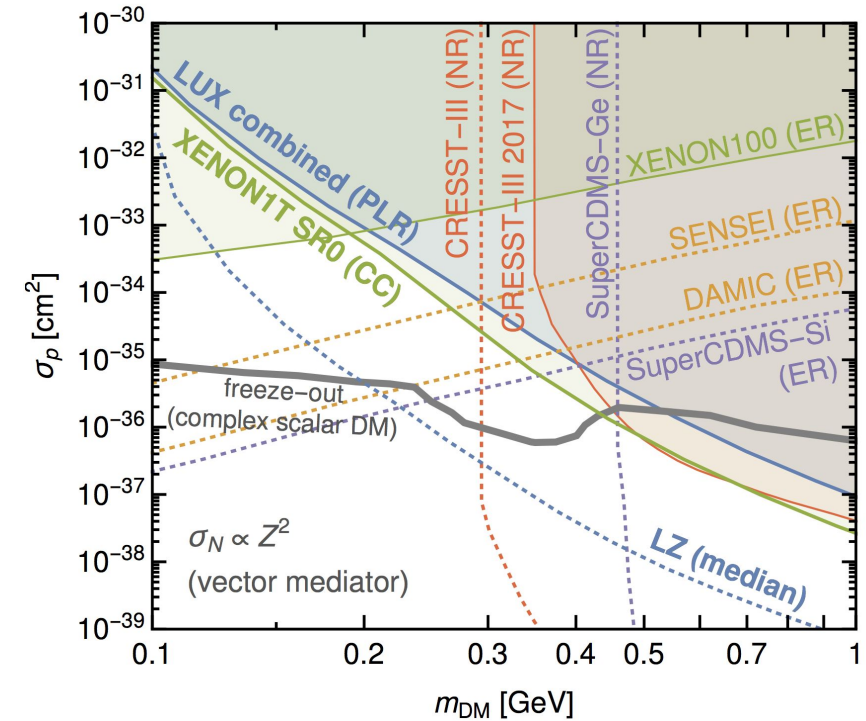
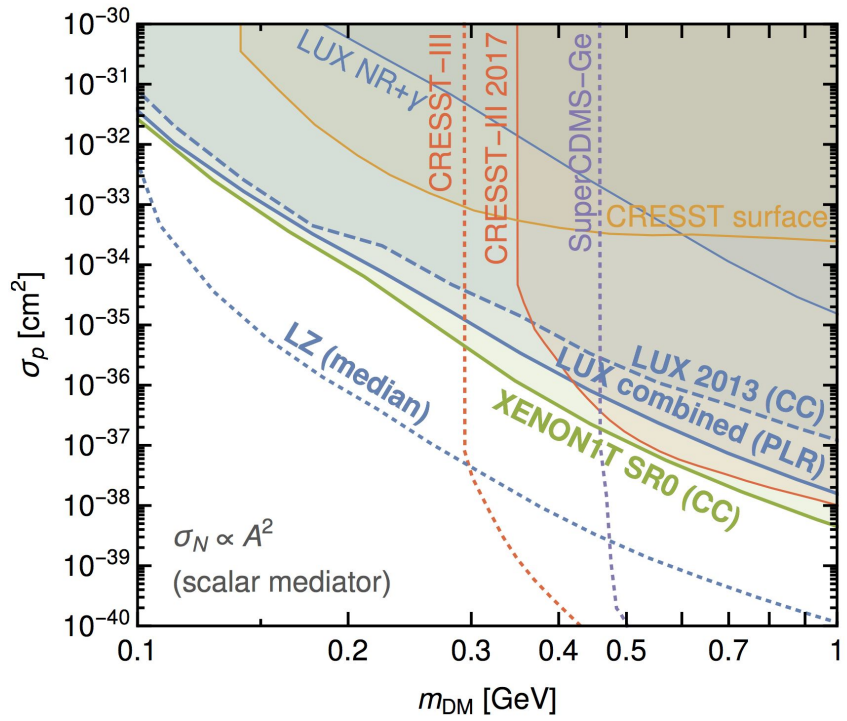
$$\frac{d^3 R}{dE_R dE_{\text{EM}} dv} = \frac{d^2 R_0}{dE_R dv} \times \frac{1}{2\pi} \sum_{n,\ell} \frac{d}{dE_e} p_{q_e}^c(n\ell \rightarrow (E_e))$$

Ionization Probabilities have been calculated: Flexible Atomic Code





The Migdal effect has been used to place new bounds on sub-GeV dark matter



The Migdal Effect and Photon Bremsstrahlung in effective field theories of dark matter direct detection and coherent elastic neutrino-nucleus scattering

[arXiv:1905.00046](https://arxiv.org/abs/1905.00046)

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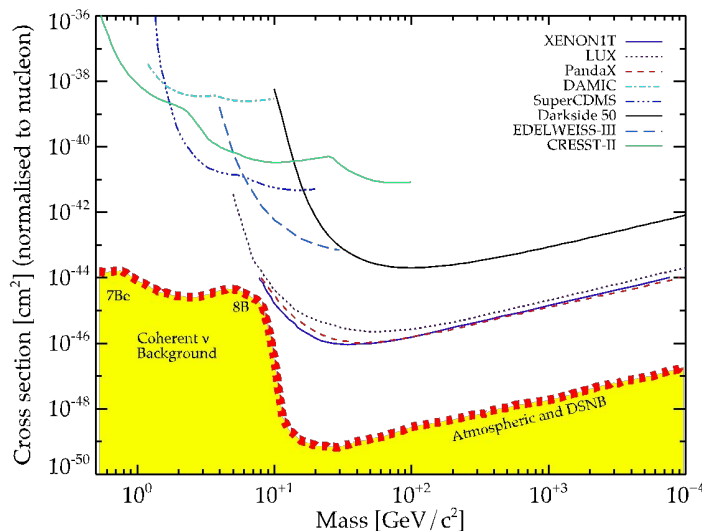


Tom Weiler



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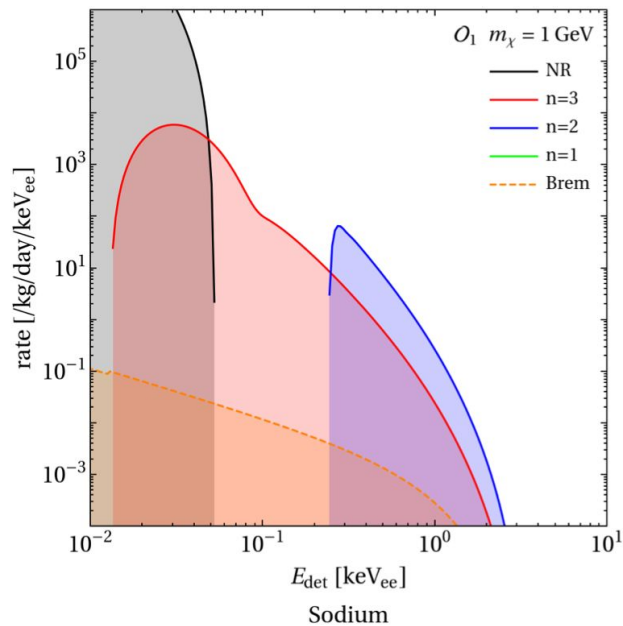
We have examined the Migdal effect and photon brem in the context of the EFT approach, placing new limits on Xe1T



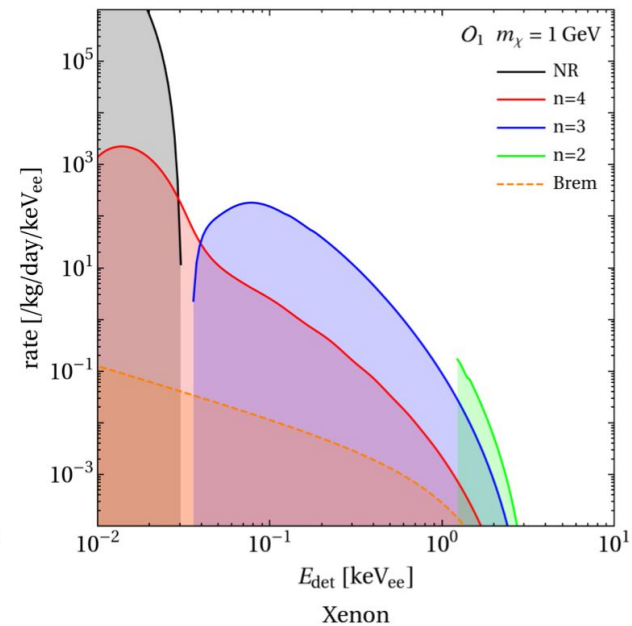
$$\begin{aligned}
 \mathcal{O}_1 & \quad \mathbb{1}_\chi \mathbb{1}_N \\
 \mathcal{O}_4 & \quad \vec{S}_\chi \cdot \vec{S}_N \\
 \mathcal{O}_6 & \quad \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi \right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N \right) \\
 \mathcal{O}_{10} & \quad \mathbb{1}_\chi \left(i \frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)
 \end{aligned}$$

We've also reassessed the neutrino background in the presence of these effects

Argon



Germanium

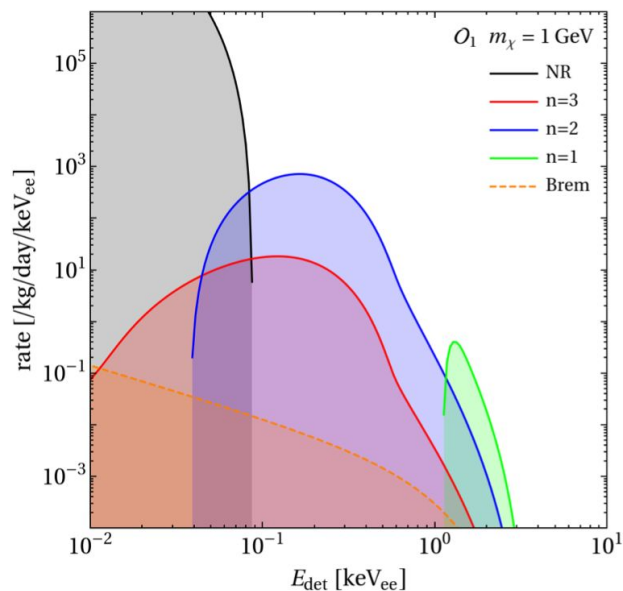


$$\rho_{\chi,\odot} = 0.3 \text{ GeV} \cdot \text{cm}^{-3}$$

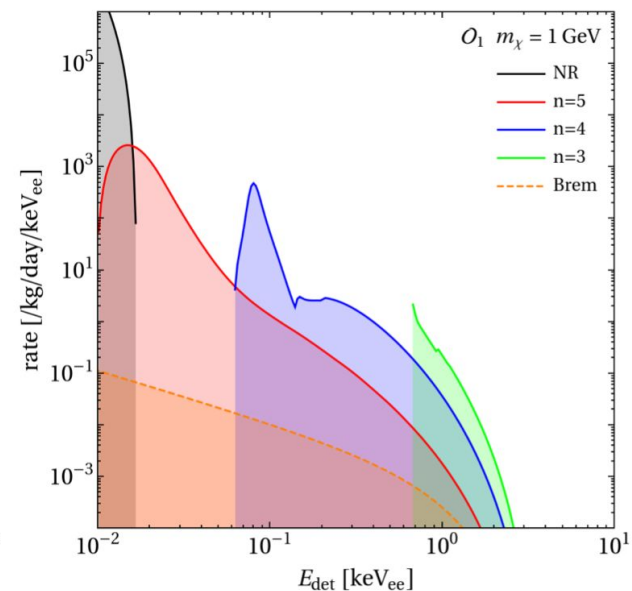
$$v_{\text{esc}} = 544 \text{ km} \cdot \text{s}^{-1}$$

$$v_0 = 220 \text{ km} \cdot \text{s}^{-1}$$

Sodium



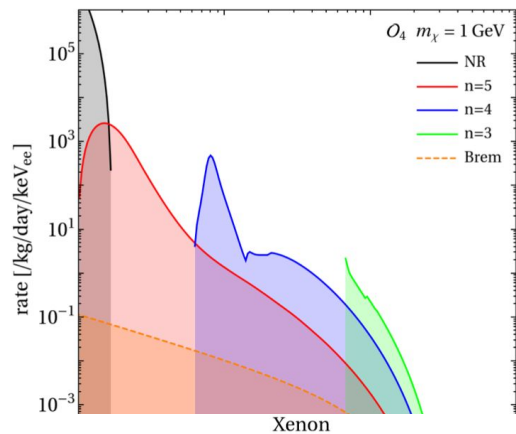
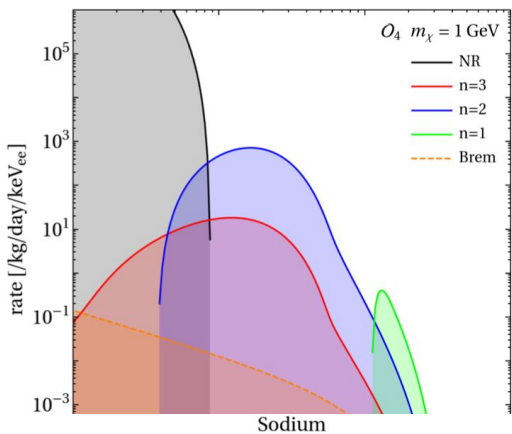
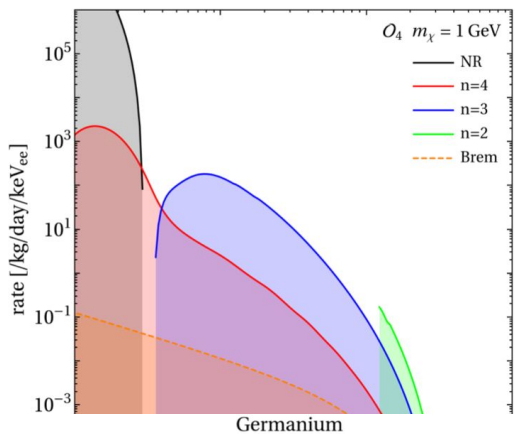
Xenon



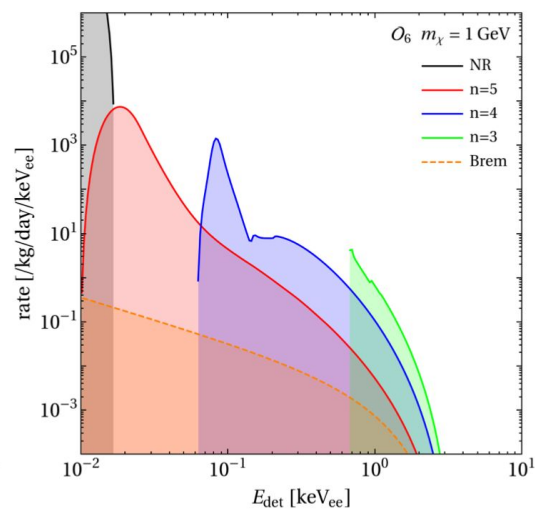
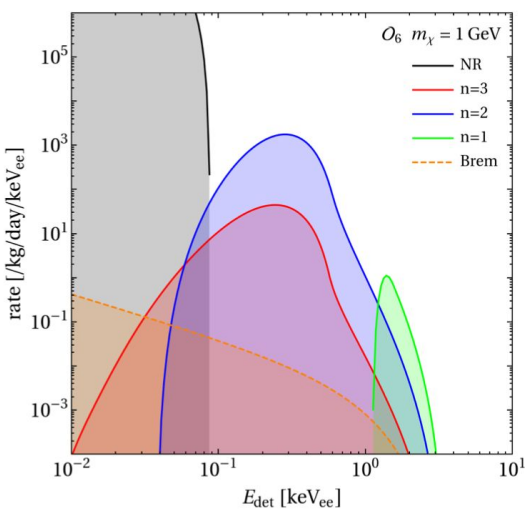
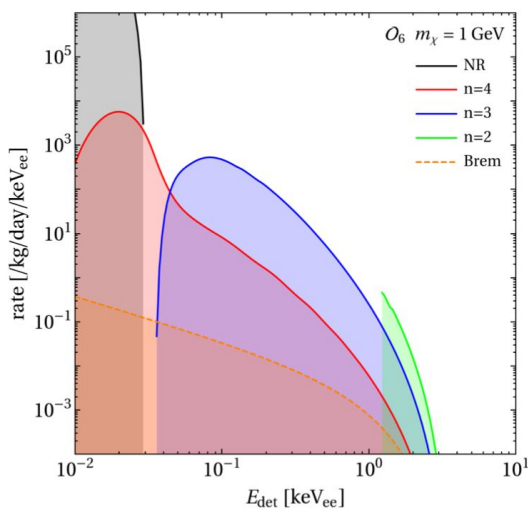
$$\frac{dR}{dE_R} = N_T \frac{\rho_{\chi,\odot}}{m_\chi m_T} \int_{v > v_{\text{min}}} \frac{d\sigma}{dE_R} v f(\vec{v}) d^3v.$$

 \mathcal{O}_1 $\mathbb{1}_\chi \mathbb{1}_N$

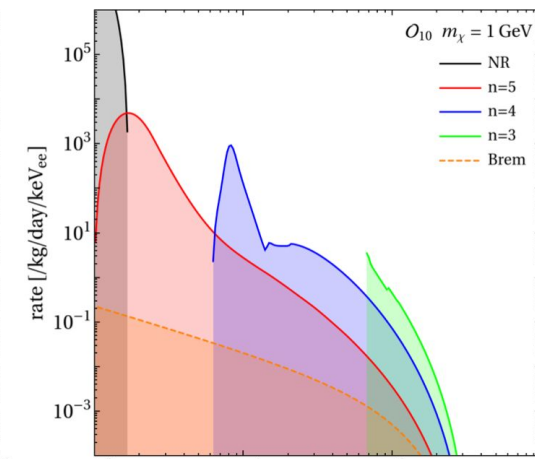
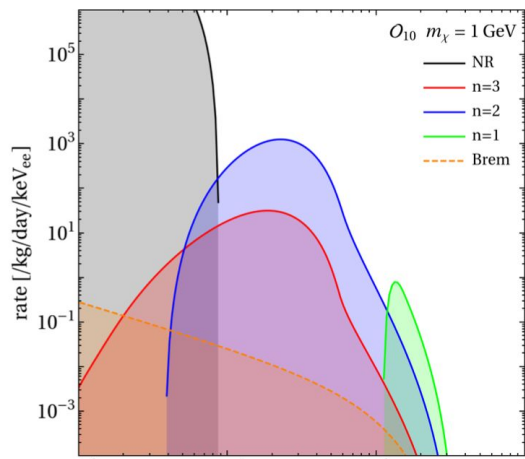
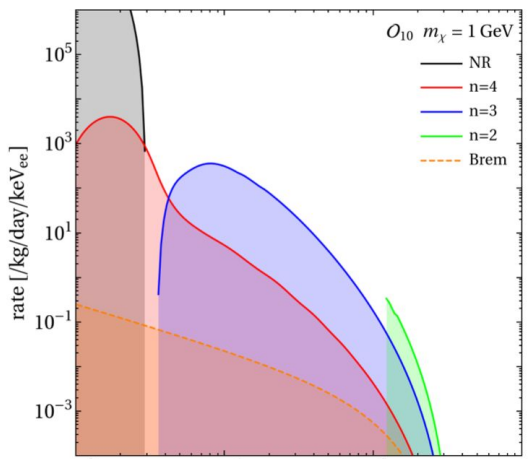
$$\vec{S}_\chi \cdot \vec{S}_N$$

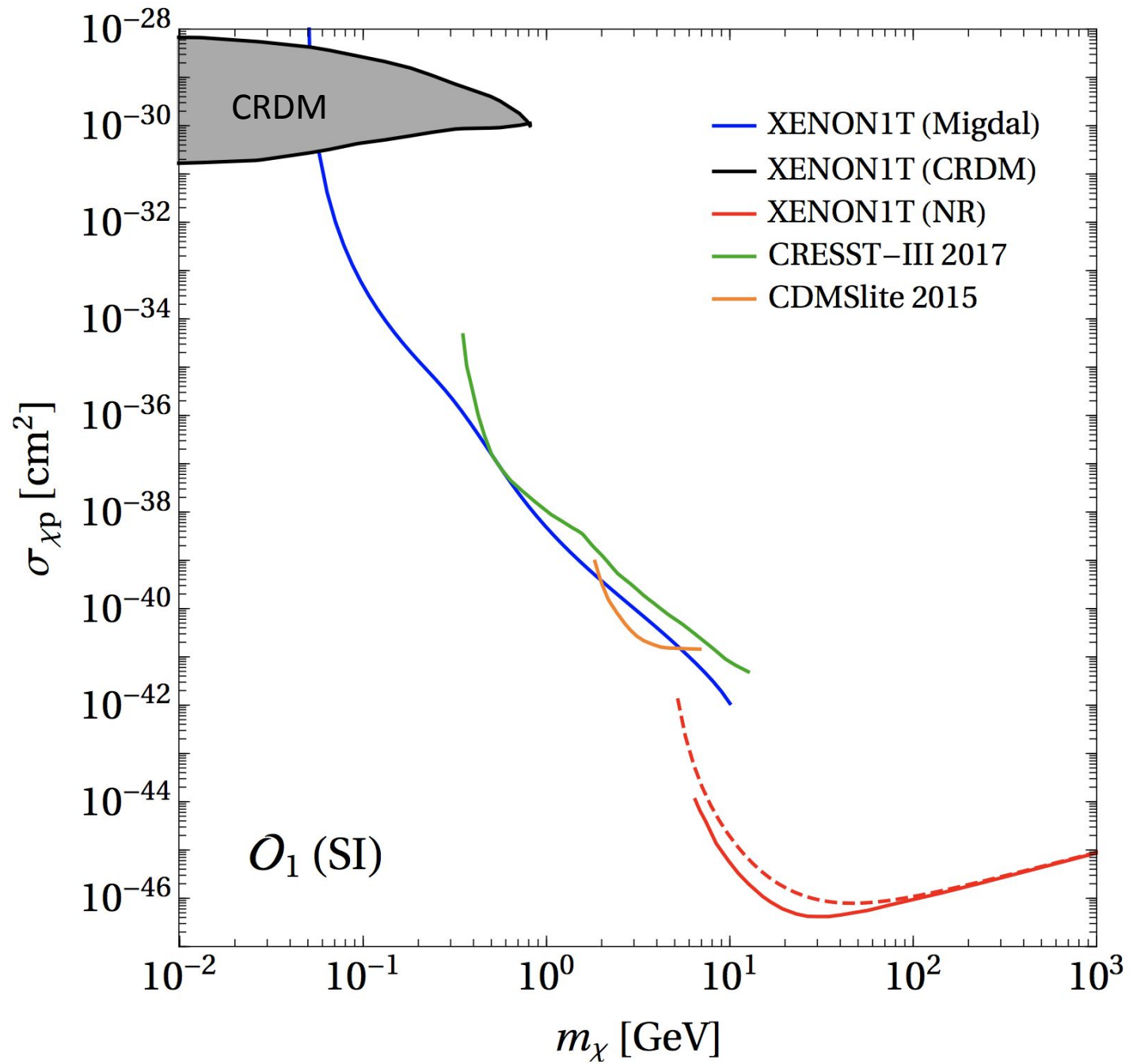


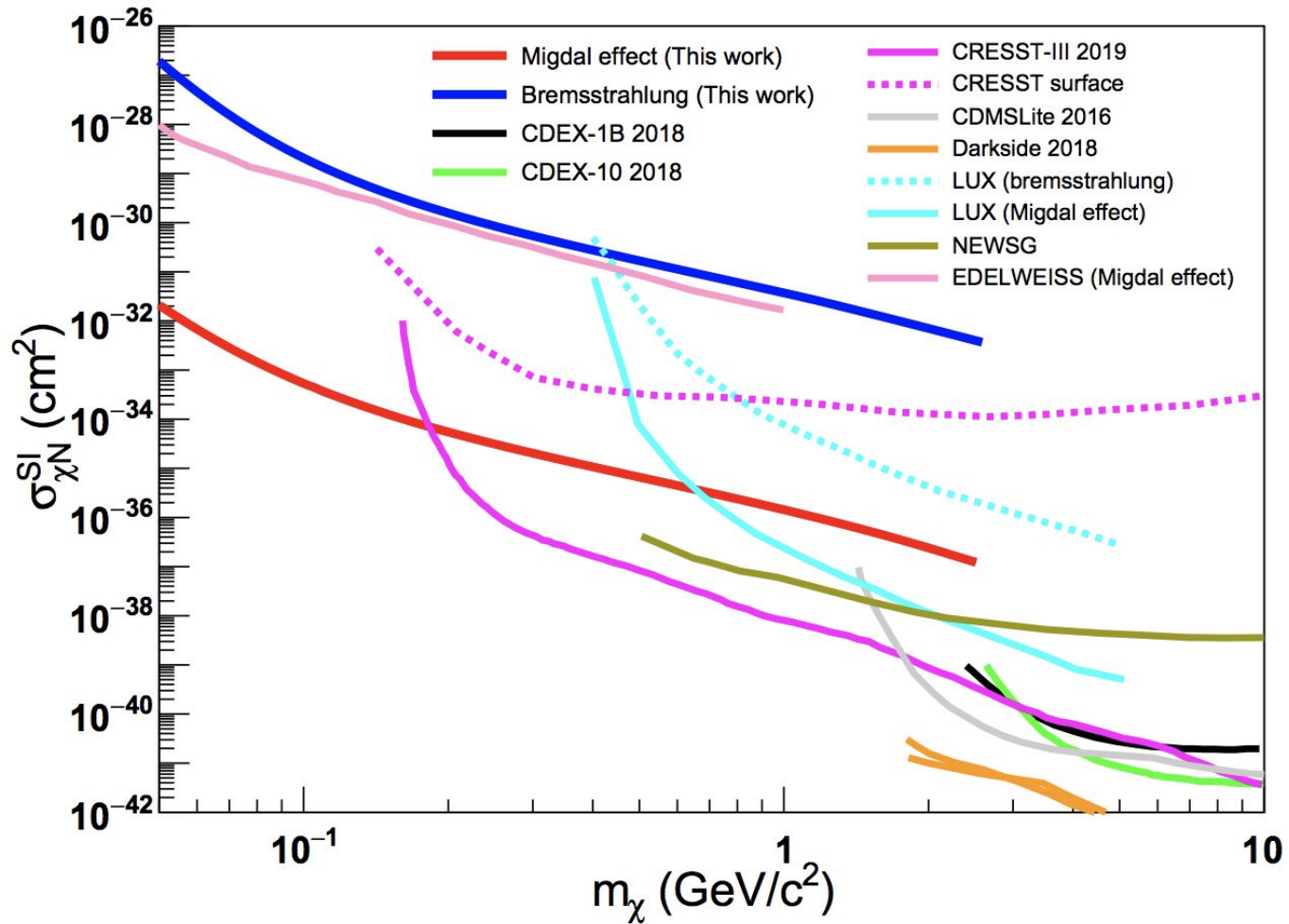
$$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi \right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)$$



$$\mathbb{1}_\chi \left(i \frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)$$





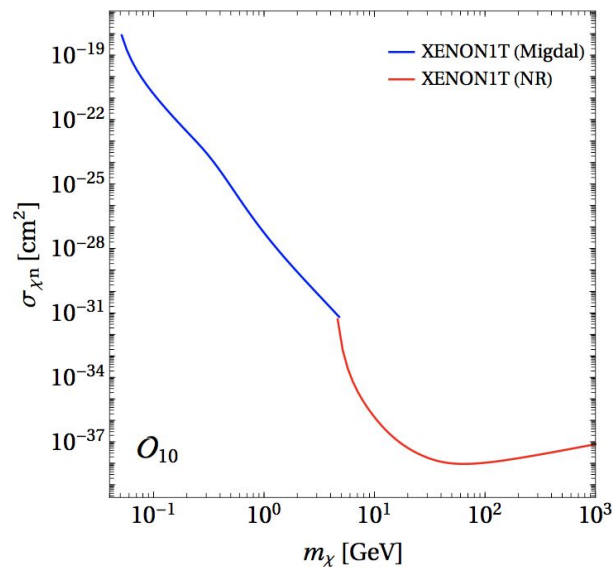
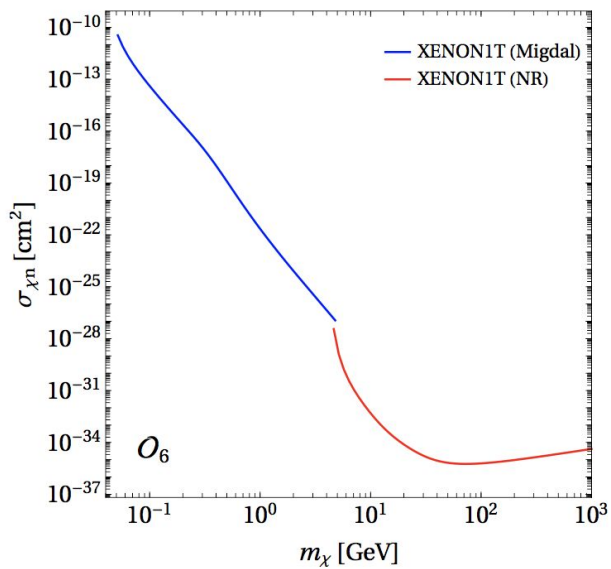
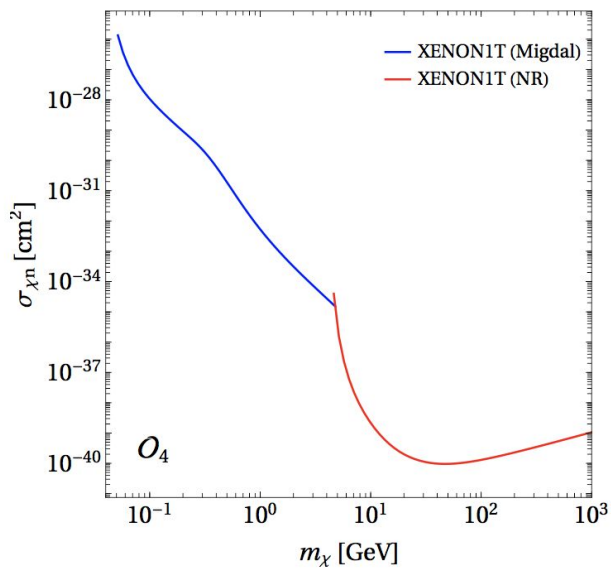
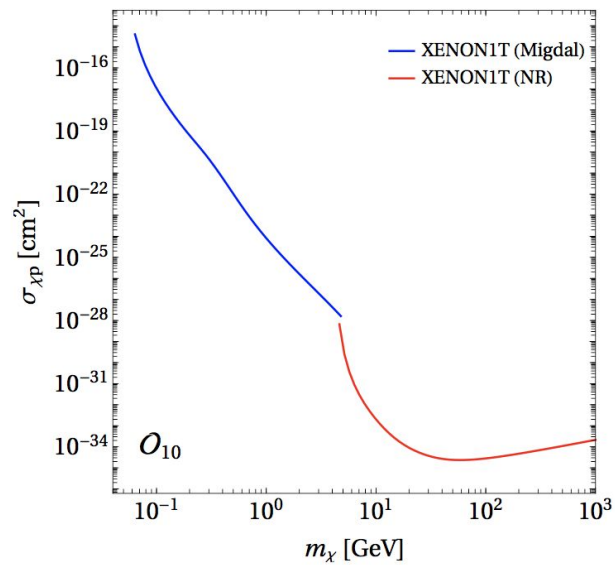
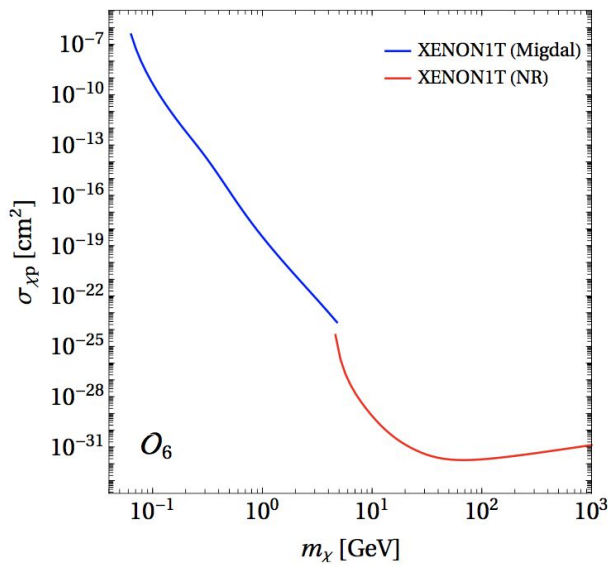
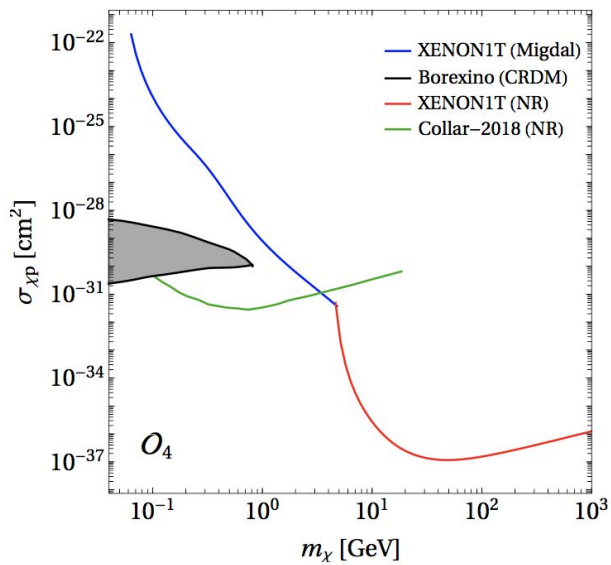


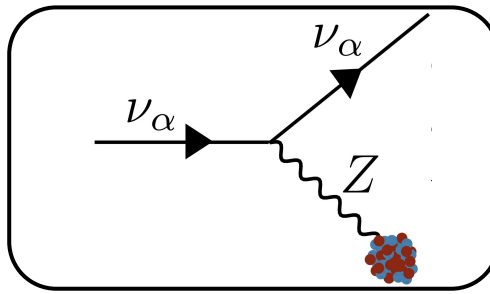
939 g Germanium detector at CJPL
 737.1 kg·day exposure and 160 eVee threshold

Constraints on spin-independent nucleus scattering with sub-GeV WIMP dark matter from the CDEX-1B Experiment at CJPL

CDEX Collaboration ([Z.Z. Liu](#) ([Tsinghua U., Beijing](#)) *et al.*). May 1, 2019. 5 pp.

e-Print: [arXiv:1905.00354](https://arxiv.org/abs/1905.00354) [hep-ex]





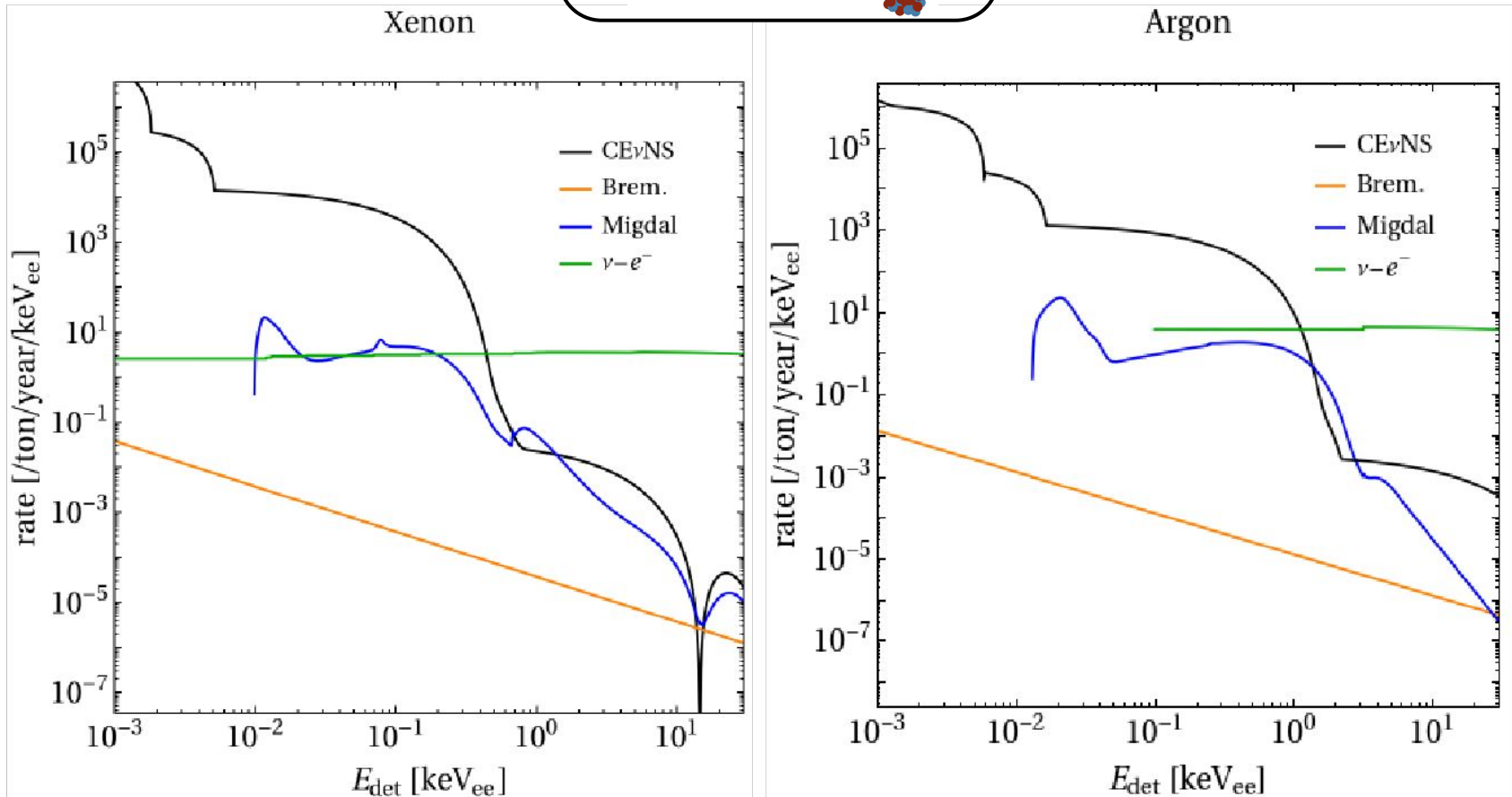
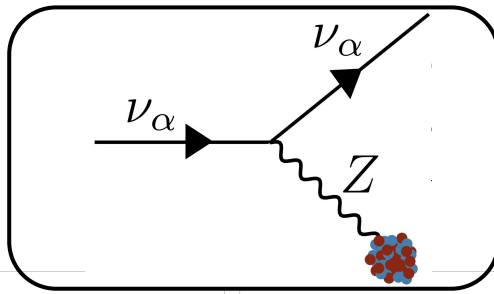
To include the Migdal effect for coherent neutrino-nucleus scattering, we include the ionization rate

$$\frac{d\sigma}{dE_R} = \frac{G_F^2}{4\pi} Q_V^2 m_T \left(1 - \frac{m_T E_R - E_{EM}^2}{2E_\nu^2} \right) F(q)^2 \times |Z_{FI}|^2$$

The kinematic endpoints are

$$\frac{(E_e + E_{nl})^2}{2m_T} < E_R < \frac{(2E_\nu - (E_e + E_{nl}))^2}{2(m_T + 2E_\nu)}$$

Including the incident fluxes from solar and atmospheric neutrinos, we have calculated the new rates as a function of detected energy



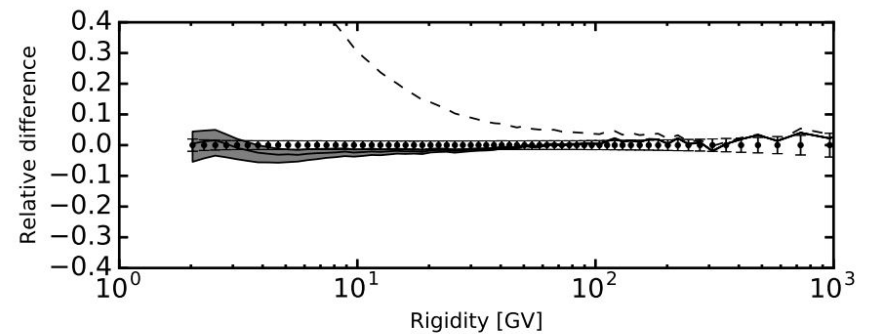
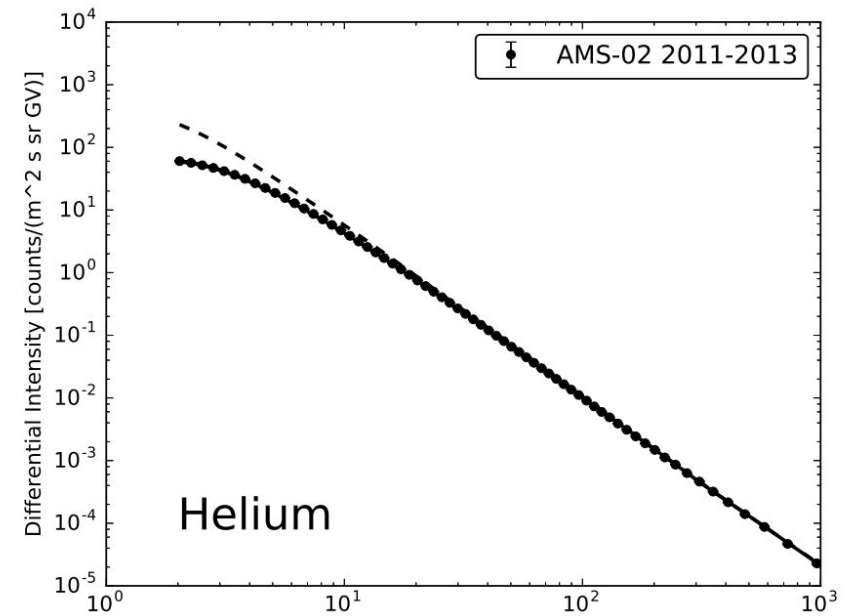
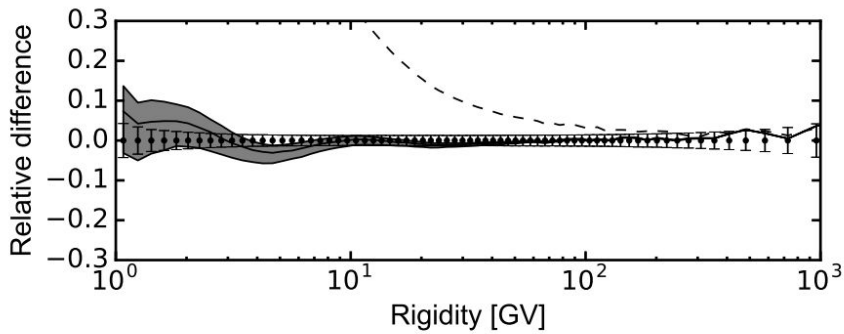
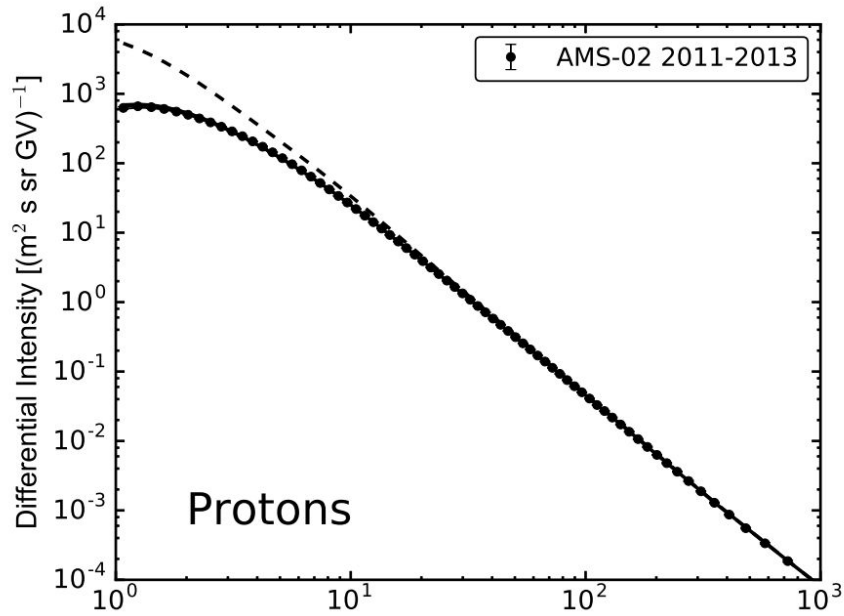
There is a small window where the Migdal effect induced signal is comparable in rate to the nuclear recoil signal.

Cosmic ray induced dark matter scattering

C.V. Cappiello, K.C.Y. Ng, and J.F. Beacom PRD 2019, 1810.07705

Bringmann and Pospelov PRL 2019, 1810.10543

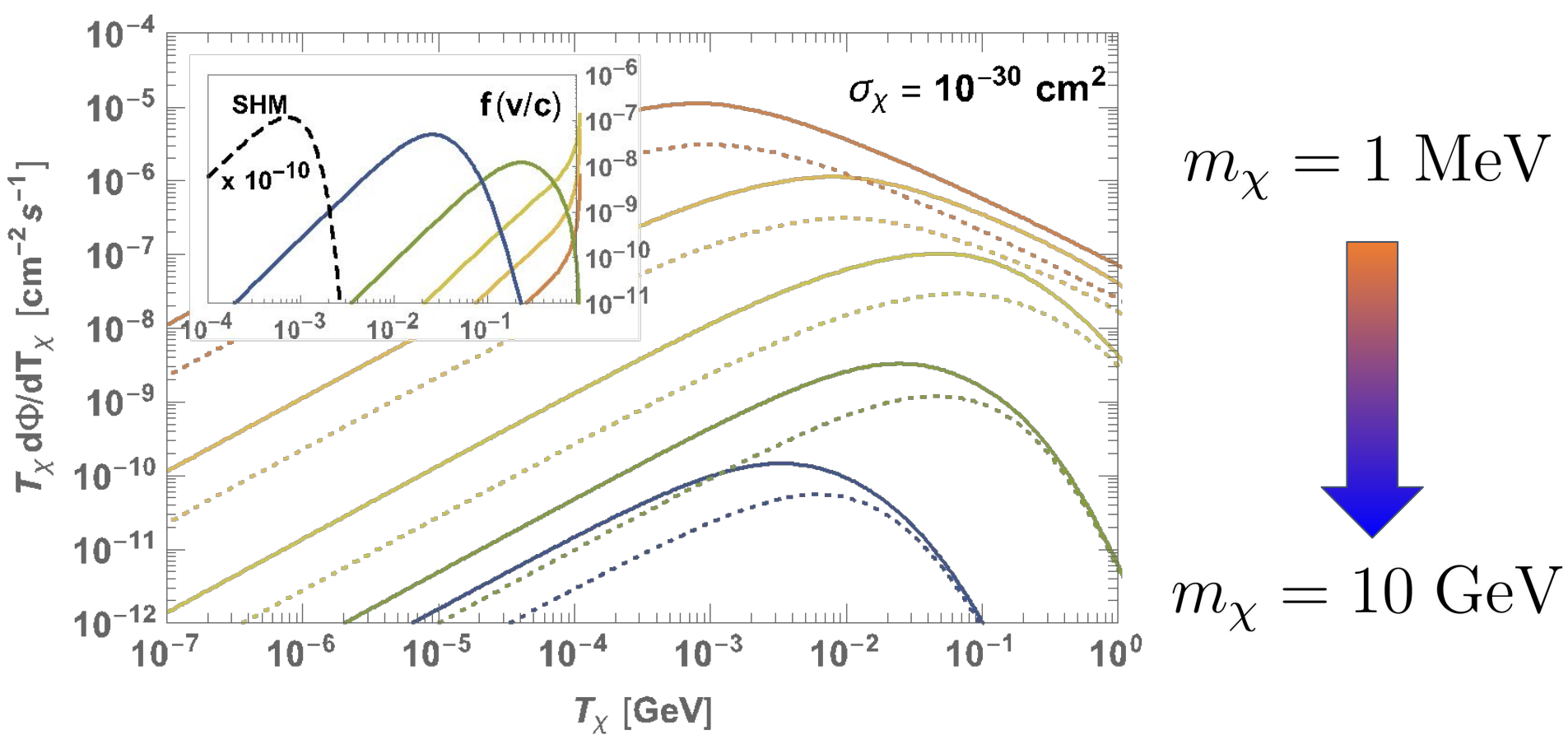
JBD, B.Dutta, J.L.Newstead, I.Shoemaker, to appear soon



From Observations near the Earth to the Local Interstellar Spectra

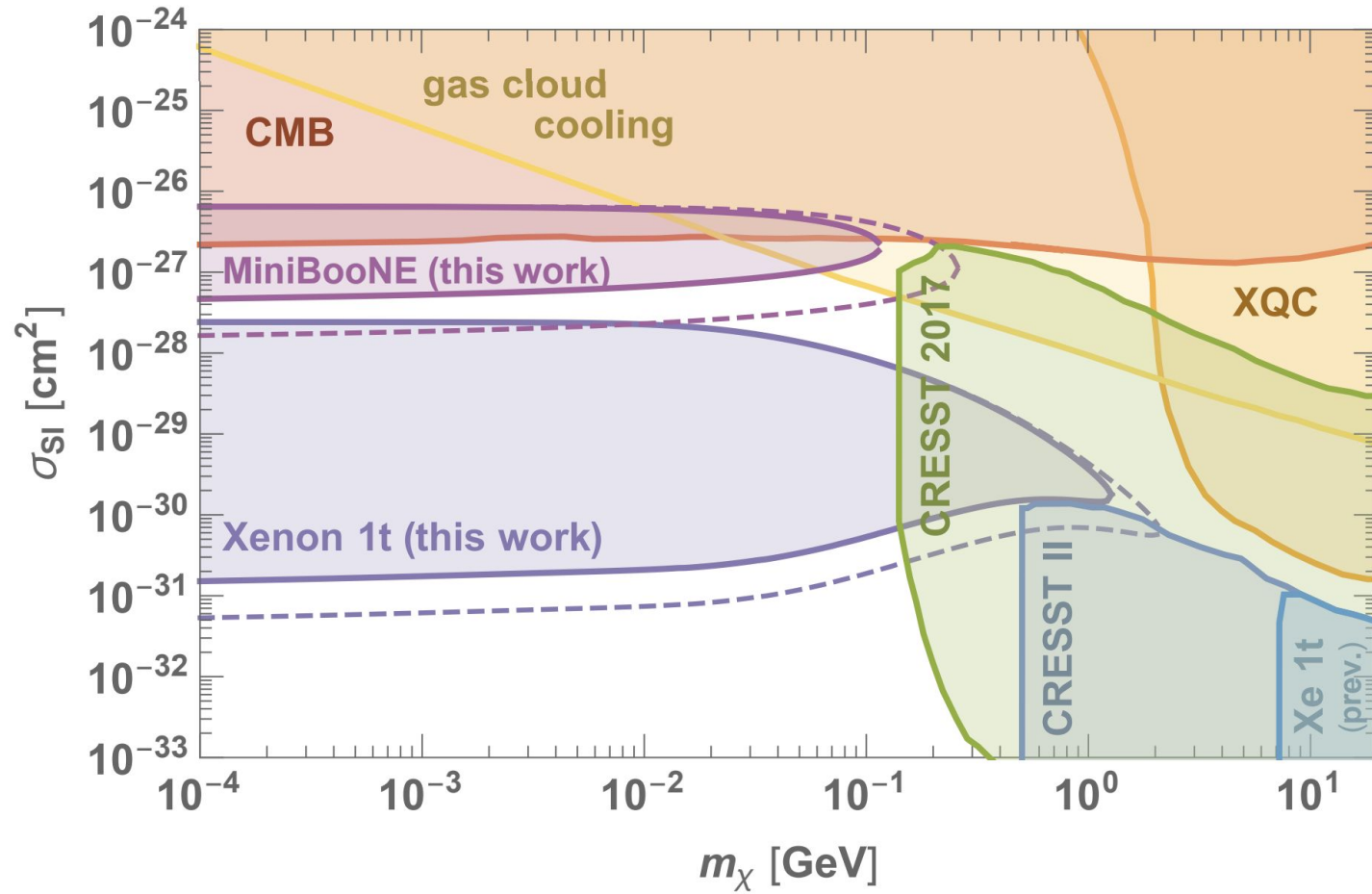
[S. Della Torre](#) ([INFN, Milan Bicocca](#)) *et al.*. Dec 29, 2016.

Conference: [C16-09-04.3](#)



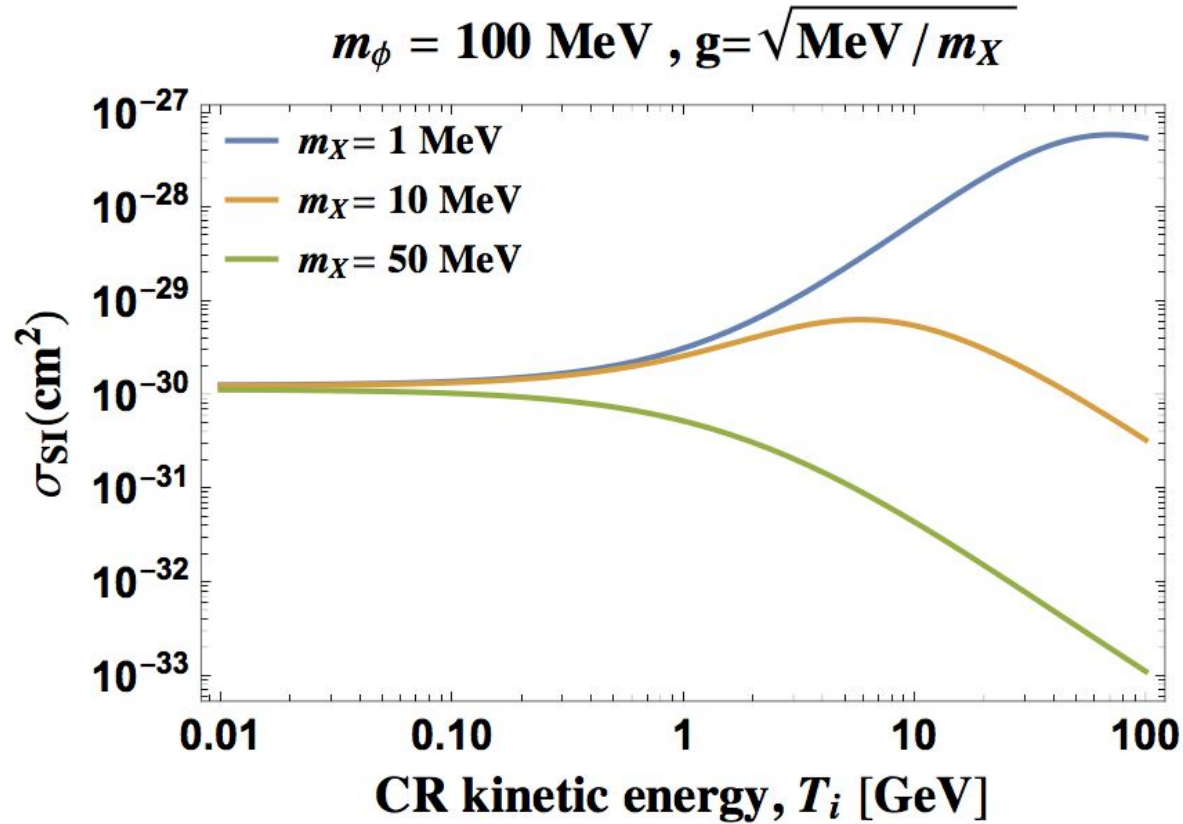
$$\frac{d\Phi_\chi}{dT_i} = \int \frac{d\Omega}{4\pi} \int_{l.o.s.} dl \sigma_{\chi i} \frac{\rho_\chi}{m_\chi} \frac{d\Phi_i}{dT_i} \equiv \sigma_{\chi i} \frac{\rho_\chi^{\text{local}}}{m_\chi} \frac{d\Phi_i^{\text{LIS}}}{dT_i} D_{\text{eff}}$$

$$\frac{d\Phi_\chi}{dT_\chi} = \int_0^\infty dT_i \frac{d\Phi_\chi}{dT_i} \frac{1}{T_\chi^{\text{max}}(T_i)} \Theta [T_\chi^{\text{max}}(T_i) - T_\chi]$$



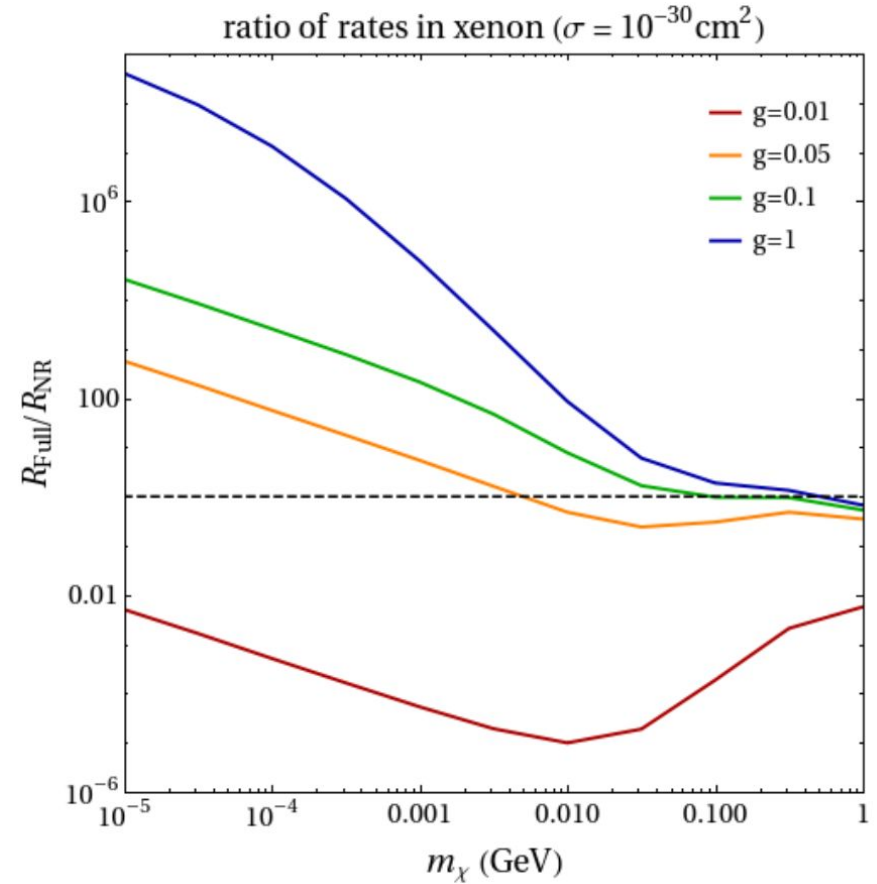
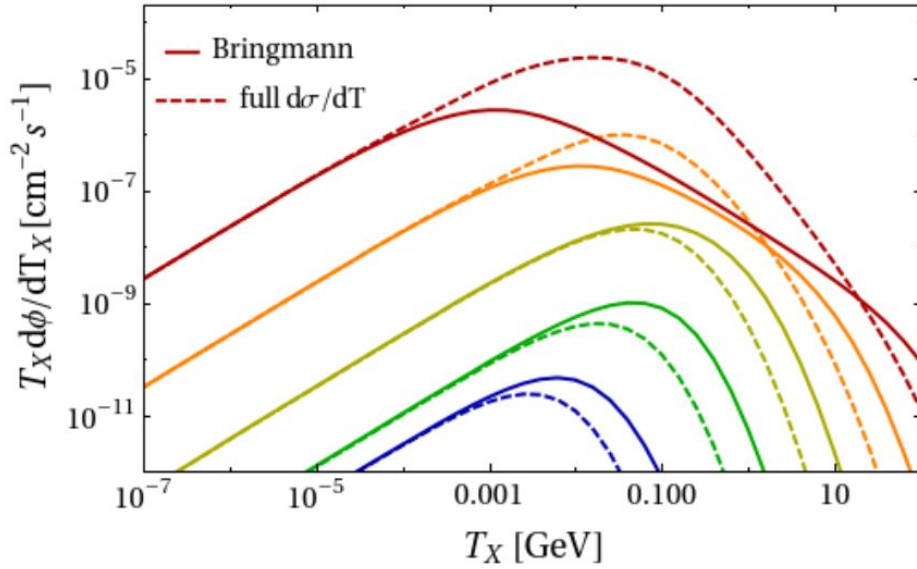
$$\mathcal{L} \supset g_\chi \phi \bar{\chi} \chi + g_n \phi \bar{n} n$$

CRDM Preliminary Results



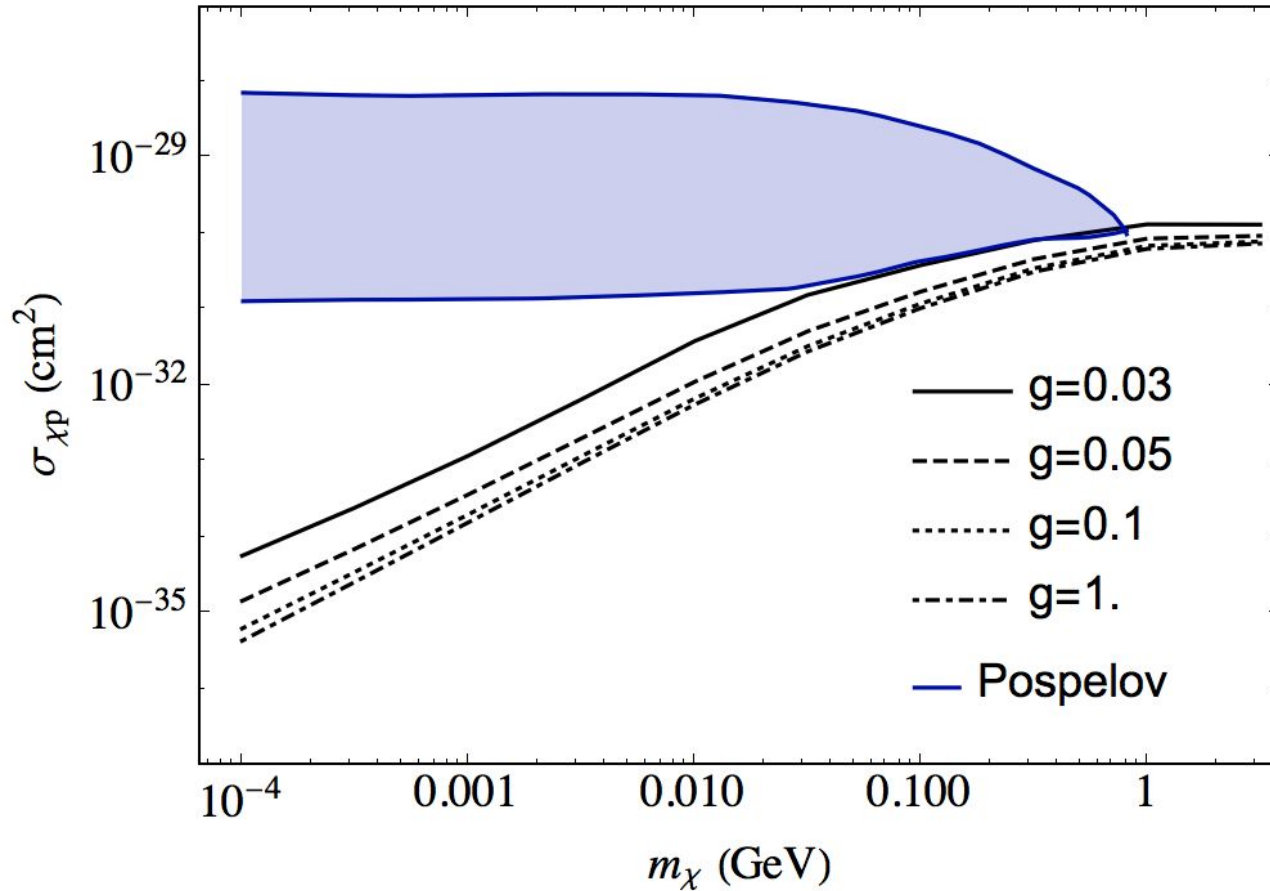
$$\left(\frac{d\sigma}{dT_\chi} \right)_{\text{scalar, CR}} = g_{s\chi}^2 g_{s\text{CR}}^2 \frac{(4m_\chi m^2 + 2T_\chi(m_\chi^2 + m^2) + m_\chi T_\chi^2)}{8\pi(2m_\chi T_\chi + m_\phi^2)^2(T_i^2 + 2mT_i)}$$

CRDM Preliminary Results



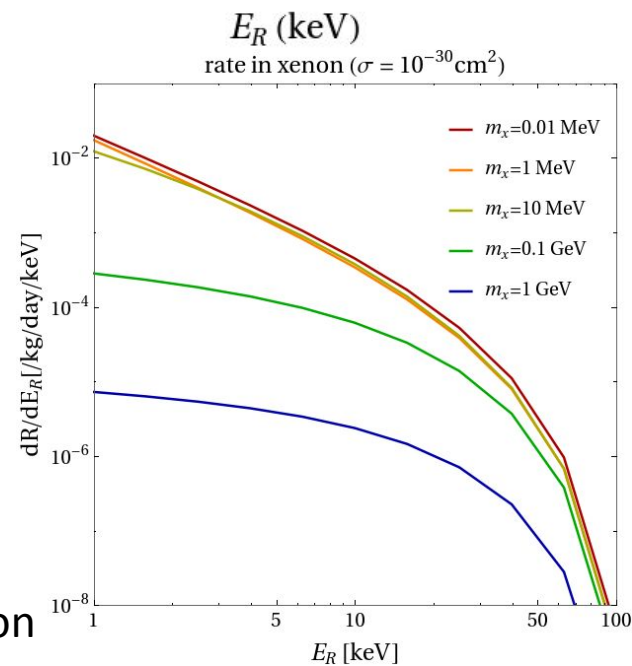
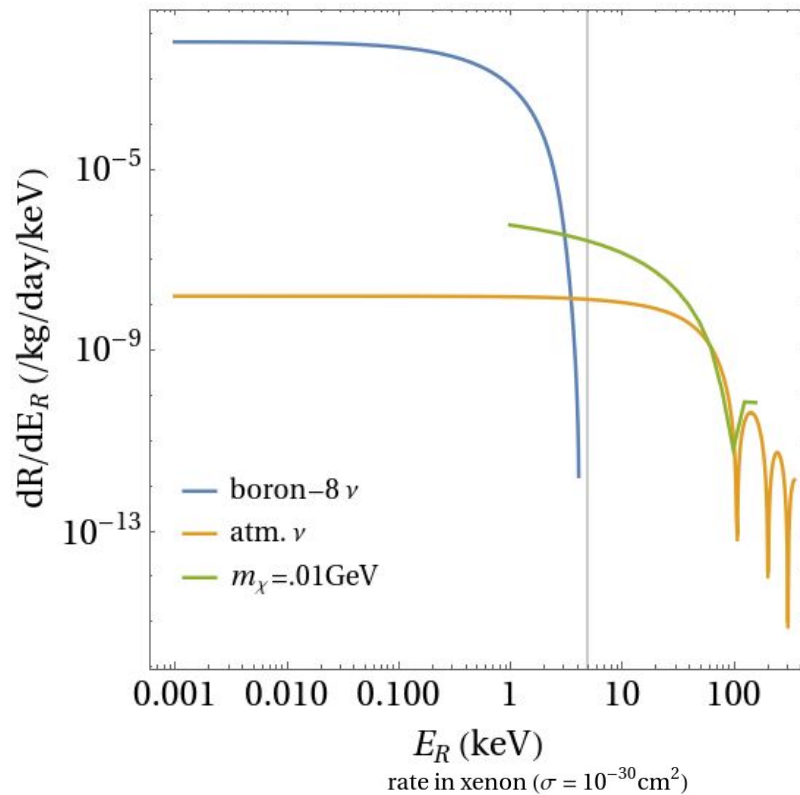
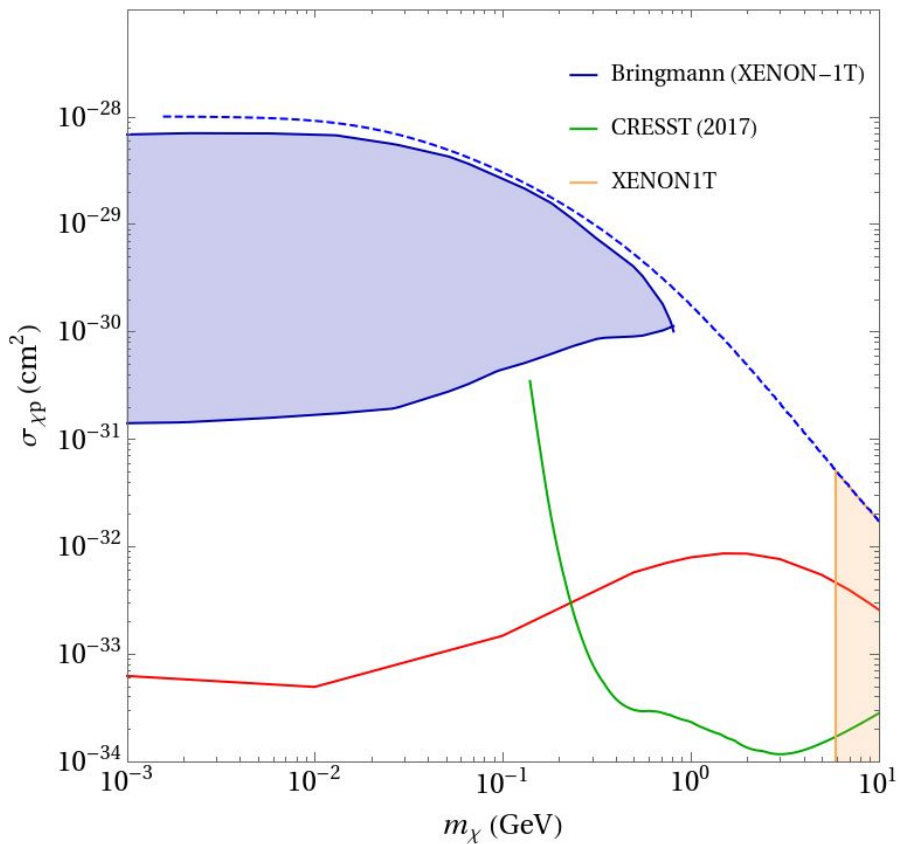
$$\frac{dR}{dE_T} = \frac{1}{m_N} \int_{T_\chi^{\min}}^{\infty} dT_\chi \frac{d\Phi_\chi}{dT_\chi} \frac{d\sigma_{\chi-n}}{dE_T}$$

Energy dependence must be accounted for on the direct detection side as well



Extension of the constraints for a scalar mediated interaction

CRDM Preliminary Results



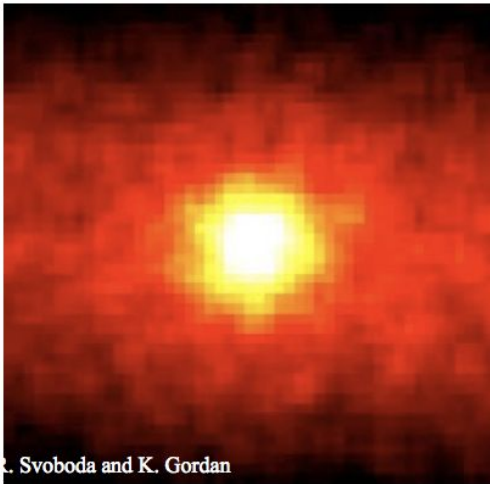
JBD, B.Dutta, J.L.Newstead, I.Shoemaker, to appear soon

Summary

A tremendous variety of searches are being carried out for sub-GeV mass dark matter.

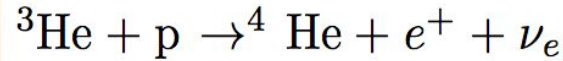
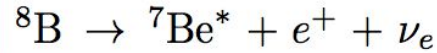
Utilizing complementary approaches from experiment and theory in astrophysics, cosmology, and particle physics, we expect a continued coverage of unexplored regions of parameter space.

Neutrino Floor



S. Svoboda and K. Gordan

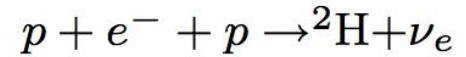
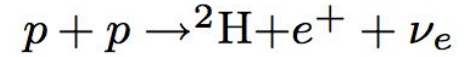
Solar neutrinos



hep

electron capture on ${}^7\text{Be}$

pp



pep

neutrinos from the CNO cycle

An irreducible background
for direct DM searches

Atmospheric neutrinos

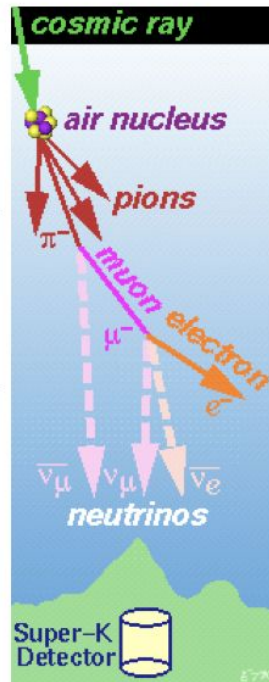
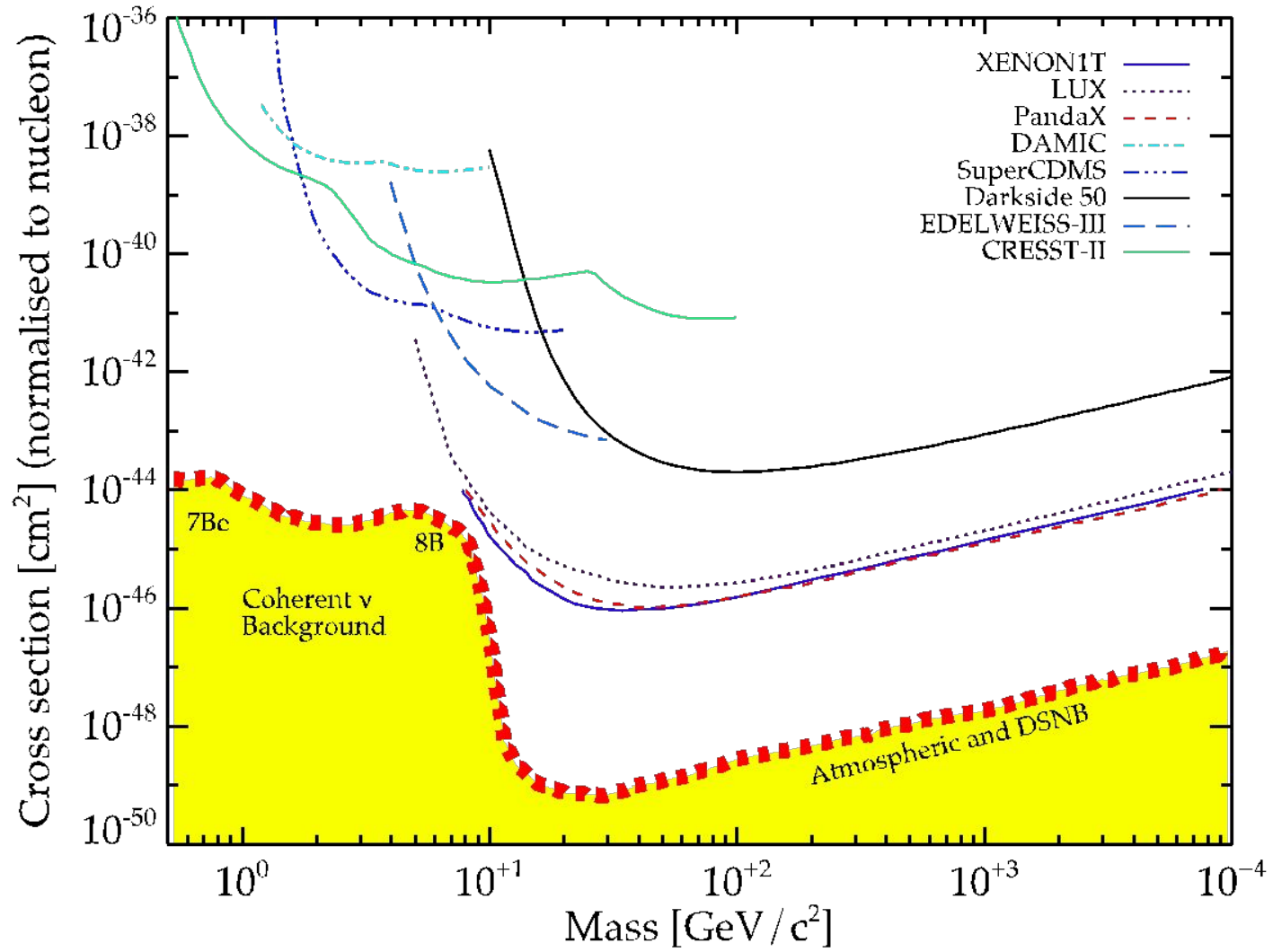
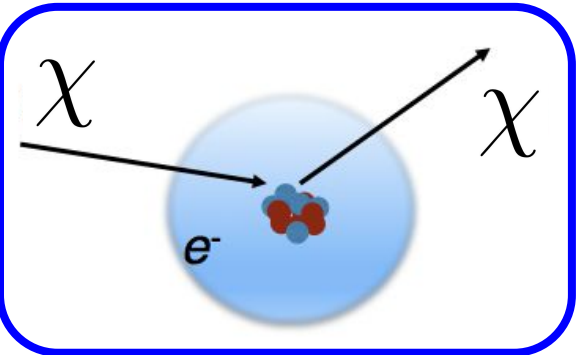


Image Credit: NASA/ESA/HEIC and The Hubble Heritage Team (STScI/AURA)

Diffuse SN background



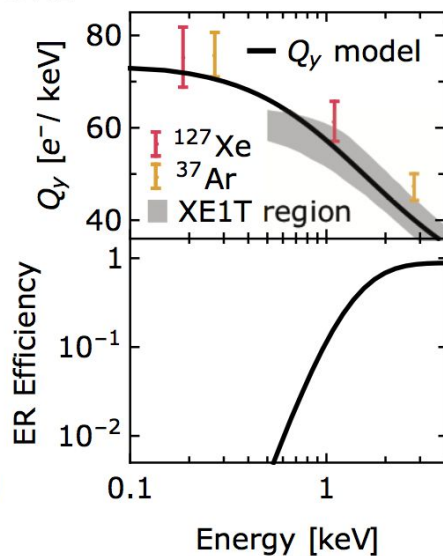
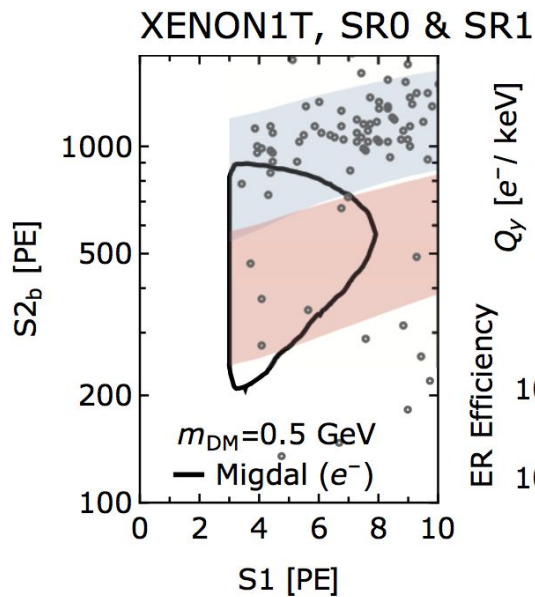
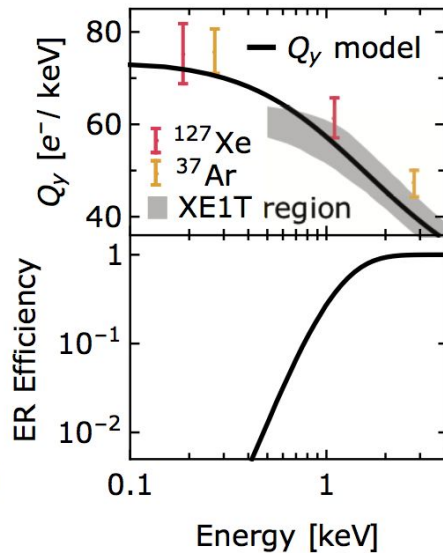
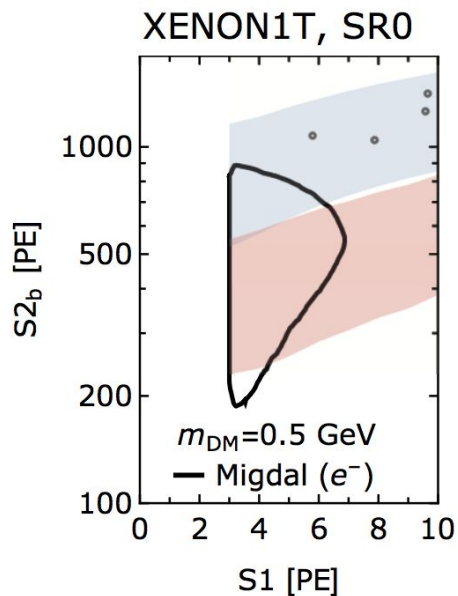
Akimov *et al.* 1803.09183, Figure by L. Strigari



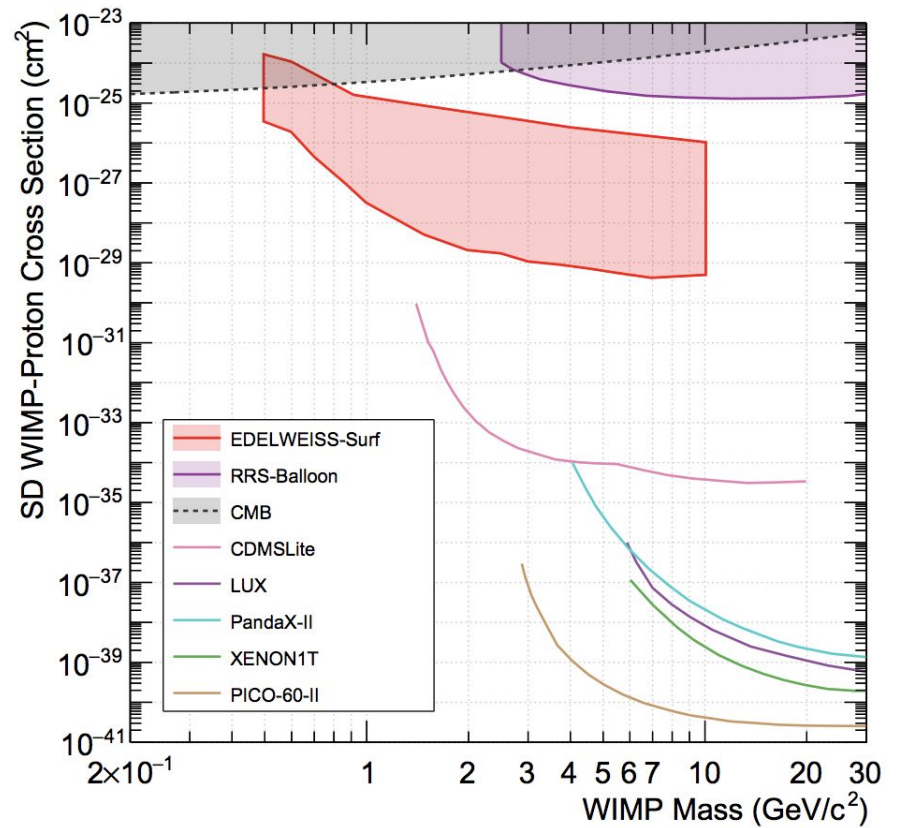
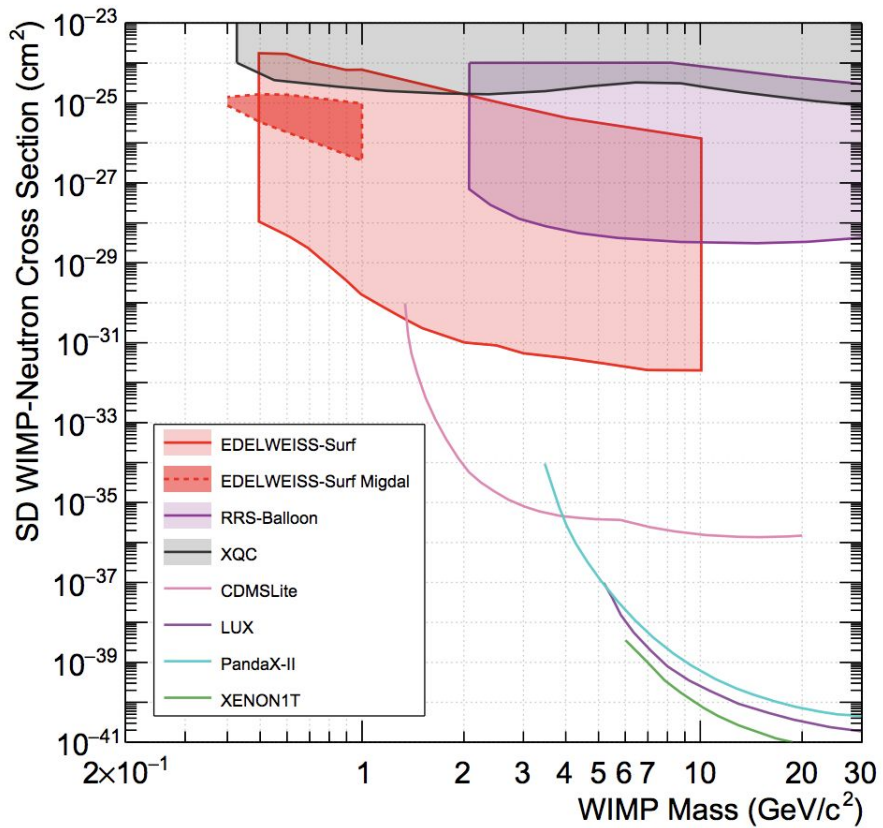
$$S1 = g_1 L_y E_{EM}$$

$$S2 = g_2 Q_y E_{EM}$$

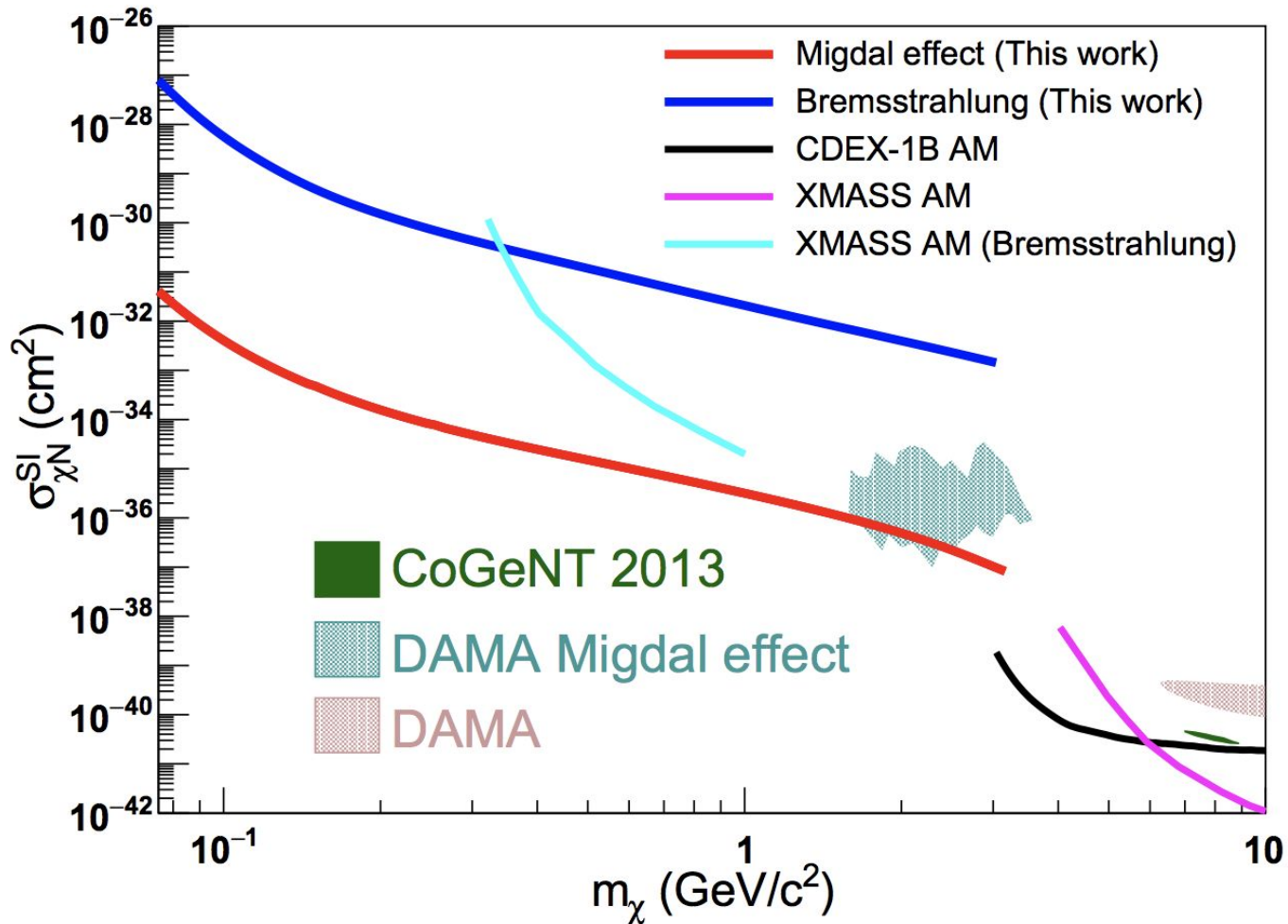
$$\frac{1}{W} = L_y + Q_y$$



Migdal and Brem limits and experimental results



33.4 g Ge, 60 eV threshold

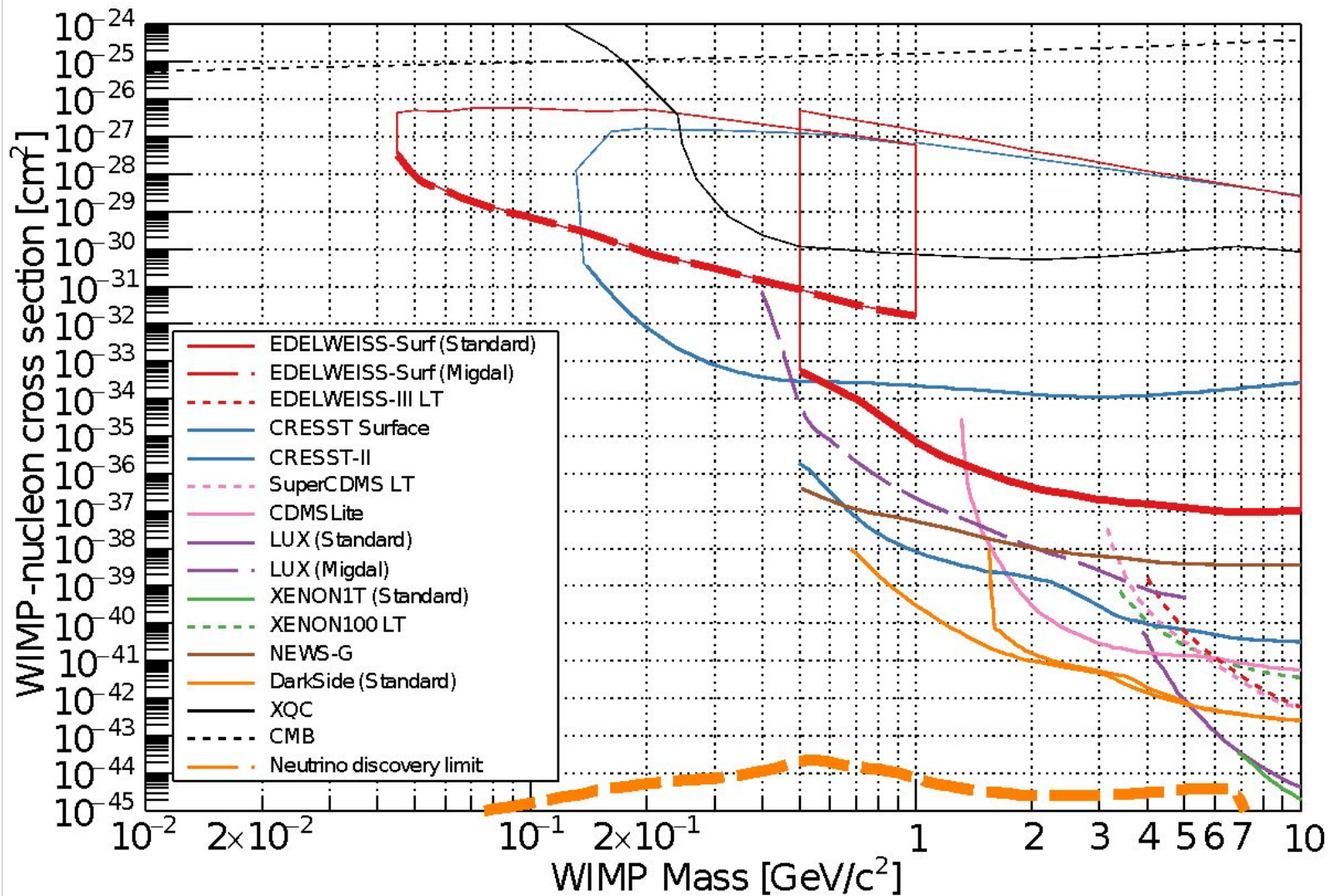


939 g Germanium detector at CJPL
 1107.5 kg·day exposure and 250 eVee
 threshold for annual modulation search

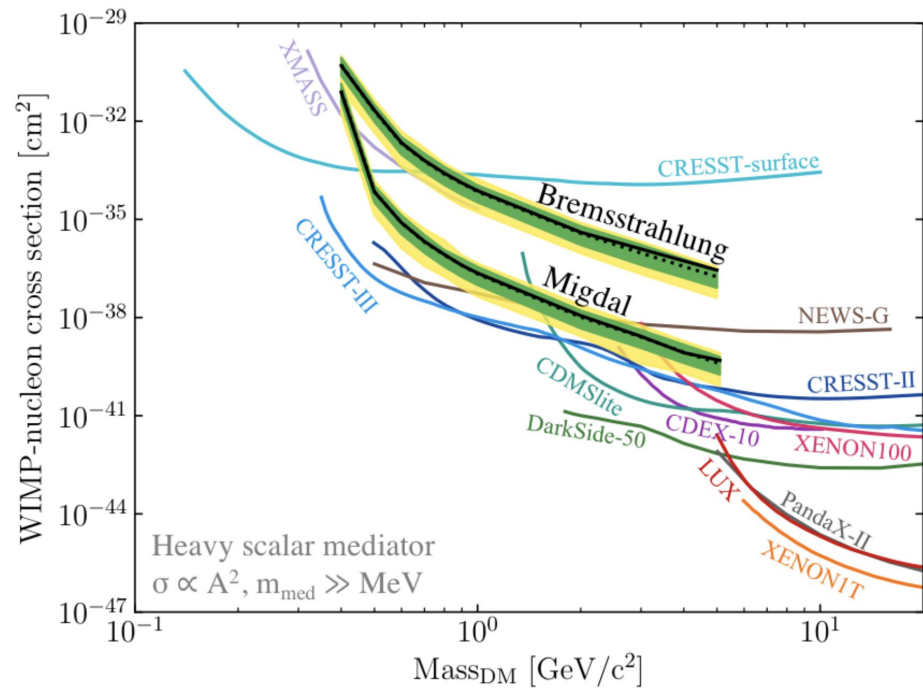
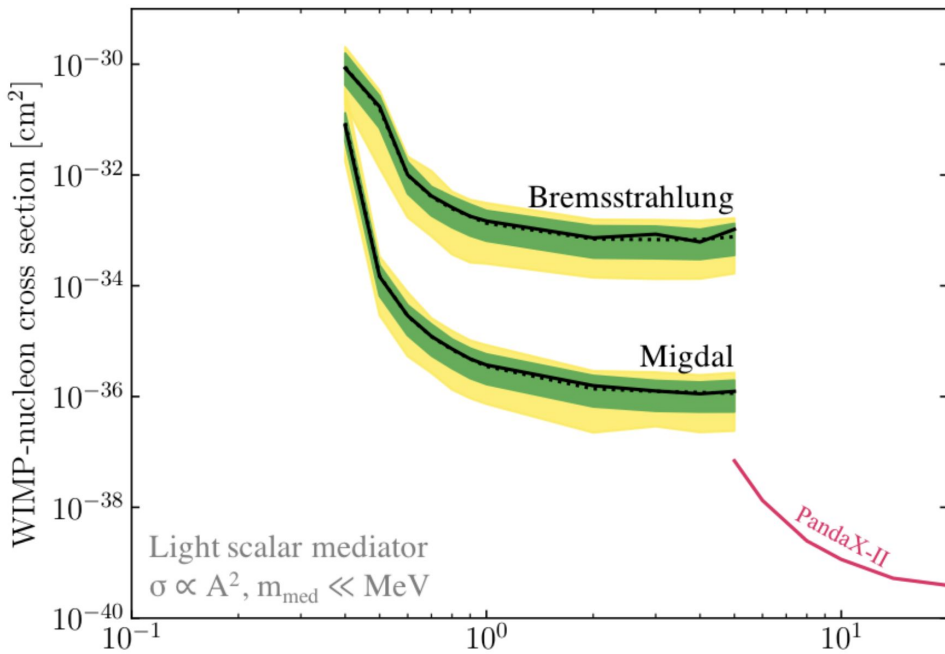
**Constraints on spin-independent nucleus scattering with
 sub-GeV WIMP dark matter from the CDEX-1B Experiment
 at CJPL**

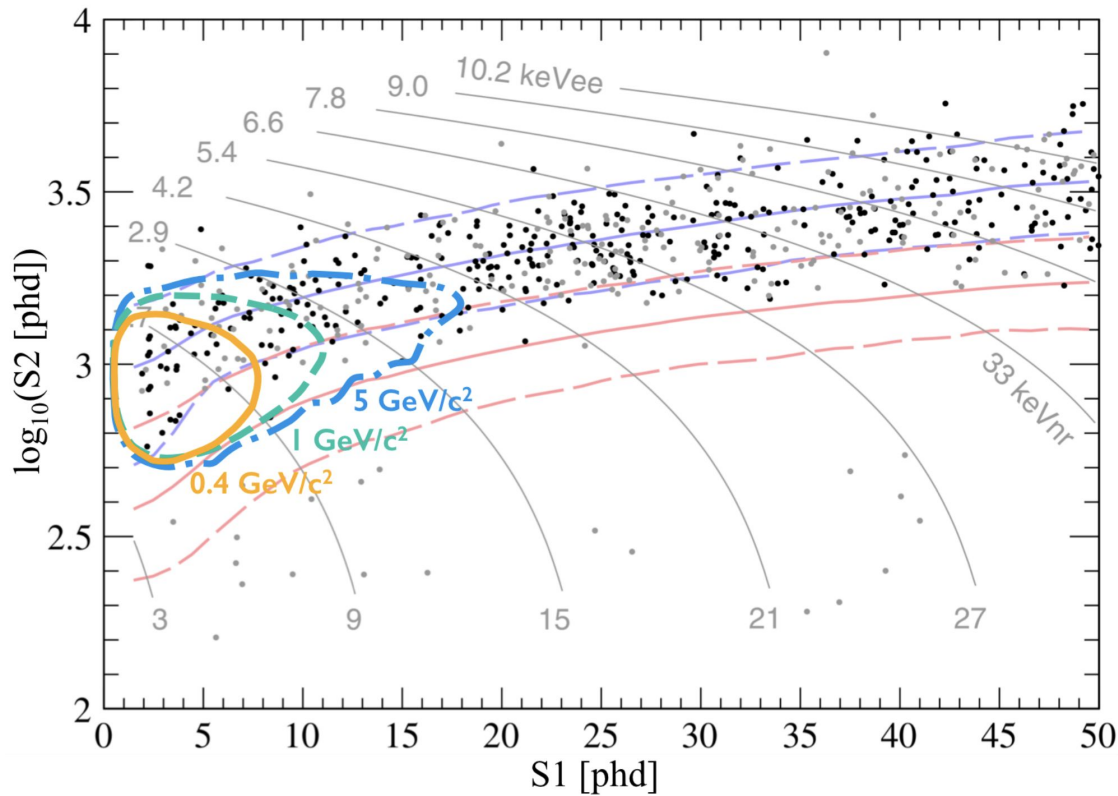
CDEX Collaboration ([Z.Z. Liu](#) ([Tsinghua U., Beijing](#)) *et al.*). May
 1, 2019. 5 pp.

e-Print: [arXiv:1905.00354](#) [hep-ex]

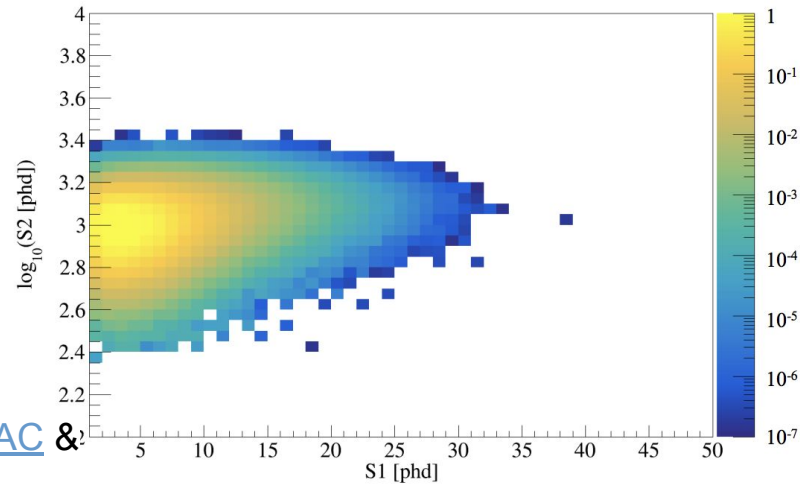


33.4 g Ge, 60 eV threshold



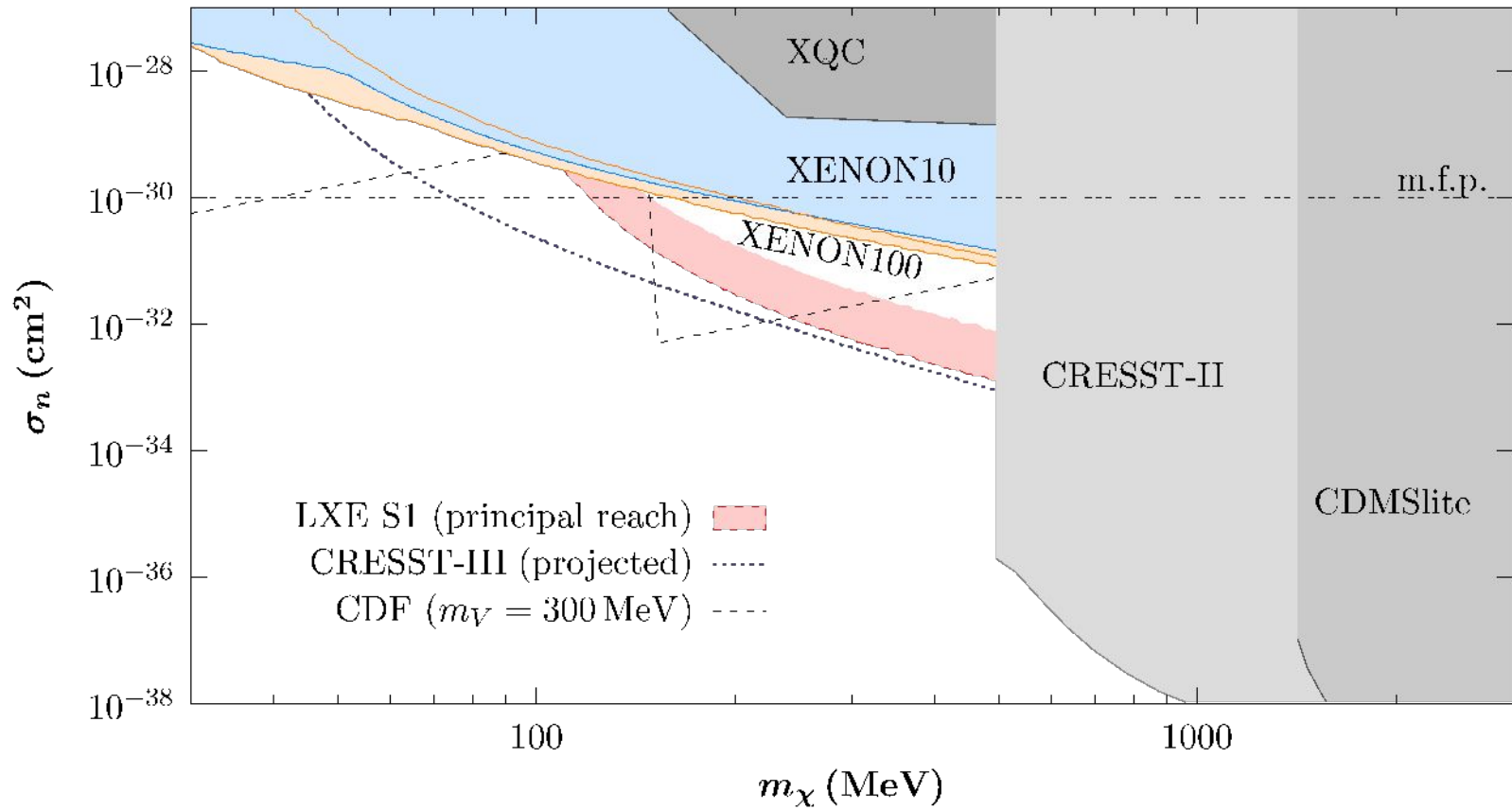


$$E = W (n_{\gamma} + n_e) = W \left(\frac{S1}{g_1} + \frac{S2}{g_2} \right)$$



LUX Collaboration ([D.S. Akerib \(Case Western Reserve U. & SLAC & KIPAC, Menlo Park\) et al.](#)). Nov 27, 2018. 7 pp.

Published in **Phys.Rev.Lett.** **122** (2019) no.13, 131301

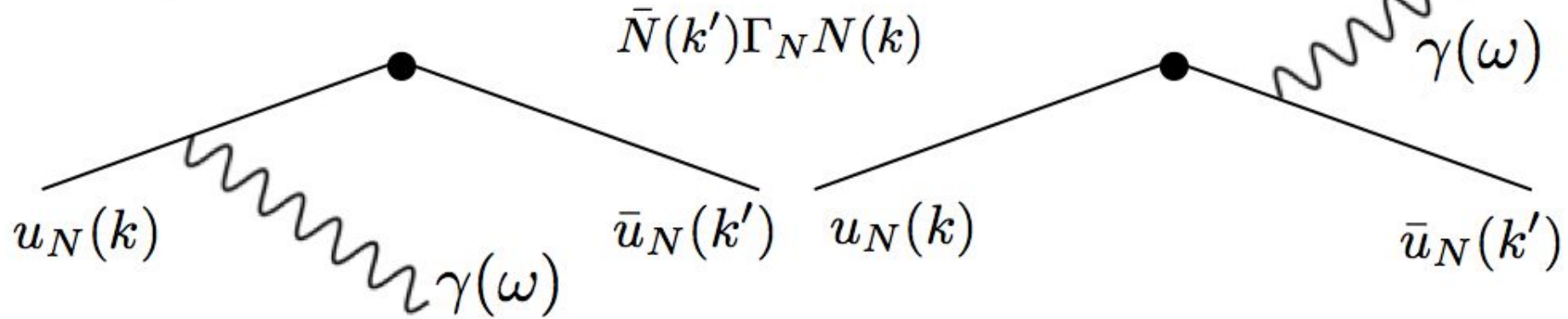


Matrix element factorization for 2-to-3
into 2-2+ kinematic factors

$$\omega/m_\chi \ll 1$$

$$\vec{q} \equiv \vec{p}' - \vec{p}$$

$$\vec{q}_T \equiv \vec{k} - \vec{k}' = \vec{q} + \vec{\omega}$$

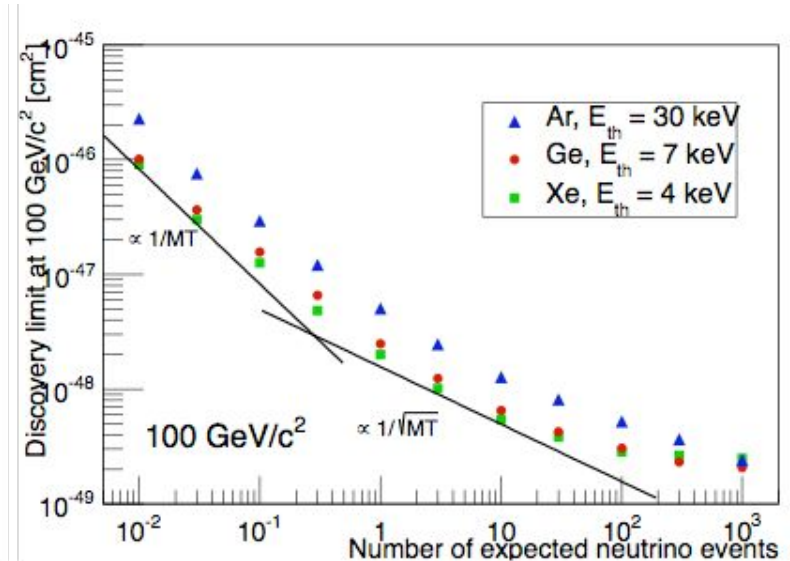
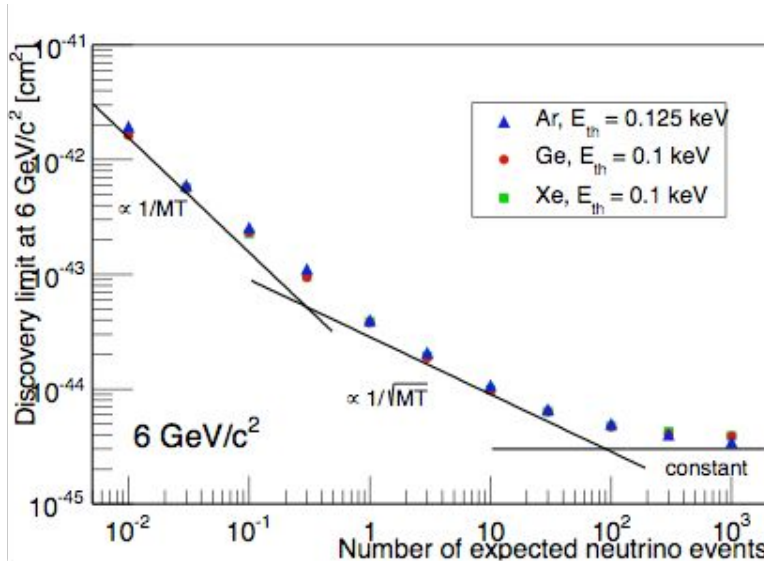


$$\bar{u}_N(k') \left[\Gamma_N \left(\frac{\not{k} + m_N}{(k - \omega)^2 - m_N^2} - \frac{\not{\omega}}{(k - \omega)^2 - m_N^2} \right) \not{\epsilon} + \not{\epsilon} \left(\frac{\not{k}' + m_N}{(k + \omega')^2 - m_N^2} + \frac{\not{\omega}}{(k + \omega)^2 - m_N^2} \right) \Gamma_N \right] u_N(k)$$

$$\bar{u}(k') \Gamma_N u(k) \left(-\frac{k \cdot \epsilon}{k \cdot \omega} + \frac{k' \cdot \epsilon}{k' \cdot \omega} \right)$$

$$\rightarrow |\mathcal{M}|_{2-2}^2 (Ze)^2 \left(\frac{\vec{q} \cdot \vec{\epsilon}}{m_T \omega} \right)^2$$

Discovery Evolution



Discovery limits as a function of background neutrino events for Argon, Germanium, and Xenon.

A given experiment has a 90% probability to obtain at least a 3 σ detection

6GeV WIMP: Ge 240 kg-yr, Xe 130 kg-year

100GeV WIMP: Ge 32.5 ton-yr, Xe 21.5 ton-year

The issue is that the spin-independent (and spin-dependent) WIMP-Nucleus scattering is practically indistinguishable from the coherent neutrino-nucleus scattering.

Direct Detection Review

Momentum Exchanged $O(<100\text{MeV})$

$$q = \sqrt{2m_T E_R}$$

Recoil energy $O(10\text{keV})$

$$E_R = \frac{\mu_{\chi T}^2 v^2}{m_T} (1 - \cos \theta)$$

Incident energy

$$E_i = \frac{m_\chi v^2}{2}$$

$$v \sim \mathcal{O}(10^{-3})$$

$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

$$\frac{dR}{dE_R} = N_T \frac{\rho_{\chi,\odot}}{m_\chi m_T} \int_{v > v_{\text{min}}} \frac{d\sigma}{dE_R} v f(\vec{v}) d^3 v$$