

# Collider and Gravitational Wave Complementarity in Exploring the Singlet Extension of the Standard Model

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based on [arXiv:1812.09333](https://arxiv.org/abs/1812.09333) [JHEP]  
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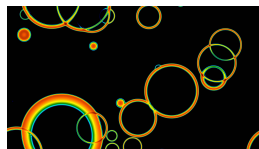
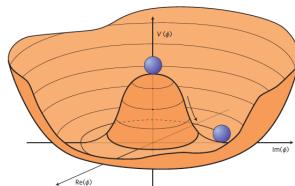
# Outline

- 1 Introduction
- 2 Electroweak Phase Transition
- 3 Hydrodynamics
- 4 Gravitational Waves
- 5 Model
- 6 Results
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# Introduction

- The Higgs potential is still largely unknown
- New scalars may provide an insight into the EWPT in the early universe
- Baryogenesis through a strongly first order EWPT  $\Rightarrow$  SM + S
- GWs produced by bubble nucleation and expansion
- Complementarity between GWs and colliders

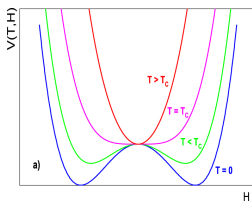
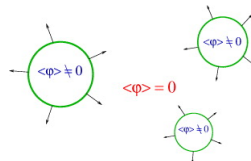


# Electroweak Phase Transition

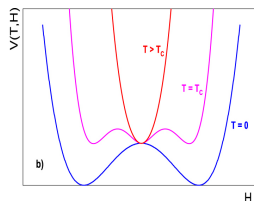


# EWPT

- Essential step in EWBG by providing an out of equilibrium environment
- Electroweak symmetry restoration at high T
- Strongly first order phase transition proceeds through bubble nucleation
  - Requires  $\left. \frac{v_h(T)}{T} \right|_{T=T_n} \gtrsim 1$
- Dynamics of nucleated bubbles in the plasma will generate GW



2nd Order PT



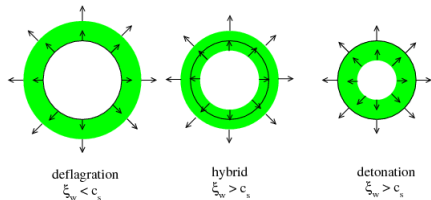
1st Order PT

# Hydrodynamics



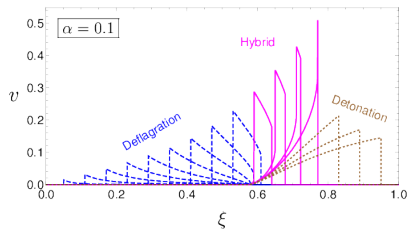
# Hydrodynamics <sup>1</sup>

- EWBG  $\Rightarrow$  subsonic  $v_w$
- GWs  $\Rightarrow$  large  $v_w$
- $v_+$  instead of  $v_w$  enters EWBG calculations:  $v_+ = 0.05$
- Detonation mode will not work



## Velocity Profile

$$2 \frac{v}{\xi} = \frac{1 - v\xi}{1 - v^2} \left[ \frac{\mu^2}{c_s^2} - 1 \right] \partial_\xi v$$



<sup>1</sup>arXiv:1004.4187



# Gravitational Waves





# Gravitational Waves

## Full Spectrum

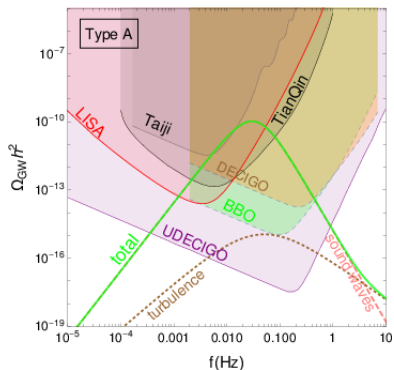
$$h^2 \Omega_{GW} = h^2 \Omega_{col} + h^2 \Omega_{sw} + h^2 \Omega_{turb}$$

## Sound Wave

$$h^2 \Omega_{SW} = 2.65 \times 10^{-6} \left( \frac{H_*}{\beta} \right) \left( \frac{\kappa \nu \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{1/3} \\ \times v_w \left( \frac{f}{f_{SW}} \right)^3 \left( \frac{7}{4 + 3(f/f_{SW})^2} \right)^{7/3}$$

$$f_{SW} = 1.9 \times 10^{-5} \frac{1}{v_w} \left( \frac{\beta}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{1/6}$$

- $T_* = T_n (1 + \kappa_T \alpha)^{1/4}$
- $h^2 \Omega_{col}$  can be neglected



$$\text{SNR} = \sqrt{\delta \times \mathcal{T} \int_{f_{min}}^{f_{max}} df \left[ \frac{h^2 \Omega_{GW}(f)}{h^2 \Omega_{exp}} \right]^2}$$



# Model



# xSM: SM + S<sup>3</sup>

## Potential

$$V_0(H, S) = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 + \frac{a_1}{2} H^\dagger H S + \frac{a_2}{2} H^\dagger H S^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

- $H^T = (G^+, (v_{ew} + h + iG^0)/\sqrt{2})$  and  $S = v_s + s$
- $\mu^2$  and  $b_2$  replaced by model parameters using minimization condition ( $v_{ew}, v_s$ )
- Rotate  $(h, s)$  into physical basis  $(h_1, h_2)$  by mixing angle  $\theta$
- Free parameters of model  $\Rightarrow (v_s, m_{h_2}, \theta, b_3, b_4)$
- Tadpole basis  $\langle S \rangle = 0$ :  $V \rightarrow V' = V + b_1 S^2$

<sup>2</sup>arXiv:1701.08774

<sup>3</sup>arXiv:0705.2425, 1407.5342, and 1701.04442



# Effective Potential <sup>4</sup>

$V_{\text{eff}} = V_0 + V_T$  in high-T expansion

$$V_{\text{eff}}(h, s, T) = -\frac{1}{2}[\mu^2 - \Pi_h(T)]h^2 + \frac{1}{2}[b_2 + \Pi_s(T)]s^2 \\ + \frac{1}{4}\lambda h^4 + \frac{1}{4}a_1 h^2 s + \frac{1}{4}a_2 h^2 s^2 + \frac{b_3}{3}s^3 + \frac{b_4}{4}s^4$$

## Thermal Masses

$$\Pi_h(T) = \left( \frac{2m_W^2 + m_Z^2 + 2m_t^2}{4v^2} + \frac{\lambda}{2} + \frac{a_2}{24} \right) T^2 \\ \Pi_s(T) = \left( \frac{a_2}{6} + \frac{b_4}{4} \right) T^2$$

## Phase Transition Patterns

- (a)  $(0, 0) \rightarrow (v_H \neq 0, v_S \neq 0)$
- (b)  $(0, 0) \rightarrow (v_H = 0, v_S \neq 0) \rightarrow (v_H \neq 0, v_S \neq 0)$
- (c)  $(0, 0) \rightarrow (v_H \neq 0, v_S = 0) \rightarrow (v_H \neq 0, v_S \neq 0)$

<sup>4</sup>High-T expansion - arXiv:1101.4665



# Results



# Constraints

## Bounded from below

$$\lambda > 0, b_4 > 0, a_2 \geq -2\sqrt{\lambda b_4}$$

## Stability

$$\frac{\partial V}{\partial \phi_i} = 0, \text{ and } \frac{\partial^2 V}{\partial \phi_i \partial \phi_j} > 0, \phi_{i,j} = h, s$$

## Higgs Signal Strength

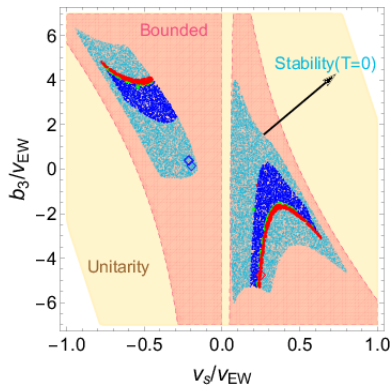
$$\text{Higgs signal strength: } \mu_H = \cos^2 \theta \Rightarrow |\sin \theta| > 0.33$$

## Perturbative Unitarity S Matrix

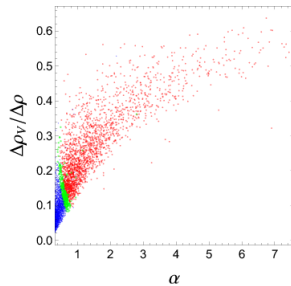
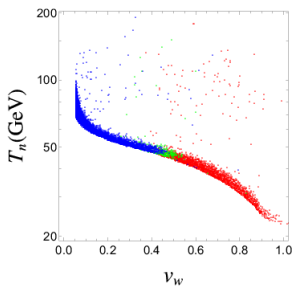
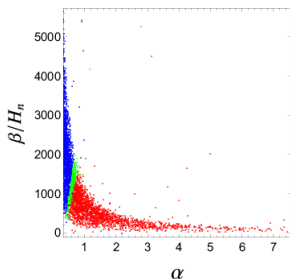
Eigenvalues of S greater than  $(1/2 \times 16\pi)$

## Electroweak Precision Measurements

$$\left. \begin{array}{l} m_W^{\text{exp}} = 80.385 \pm 0.015 \text{ GeV} \\ S, T, \text{ and } U \end{array} \right\} (\theta, m_{h_2})$$



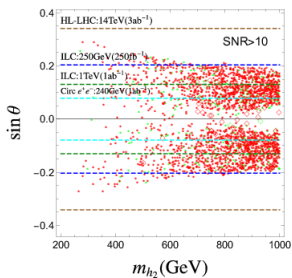
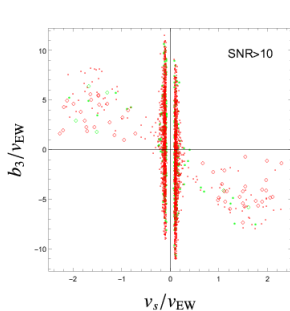
# EWPT and GW



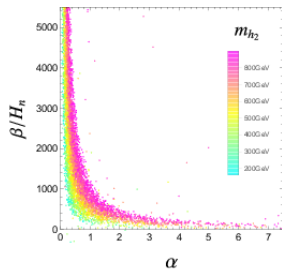
- EWPT Type: (A) 99 %, (B) 1 %, (C) 0 %
- LISA: SNR < 10 (blue - 28 %), 10 < SNR < 50 (green - 50%), and SNR > 50 (red - 22 %)
- Larger  $\alpha$  and smaller  $\beta \Rightarrow$  larger SNR



# Parameter Space Giving Detectable GW



arXiv:1407.5342

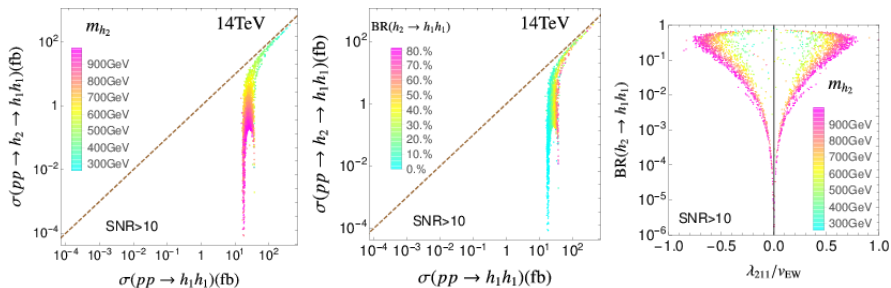


- Bounded from below:  $20 \text{ GeV} \lesssim |v_s| \lesssim 50 \text{ GeV}$
- Larger  $m_{h_2}$  preferred
- W-mass constraint:  $\theta \lesssim 0.2$





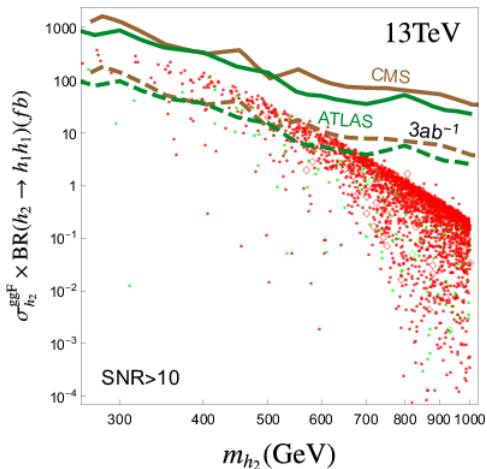
# Correlation with Double Higgs Production Searches



- $\Gamma_{h_2} = \sin^2 \theta \Gamma_{SM}(h_2 \rightarrow X_{SM}) + \Gamma(h_2 \rightarrow h_1 h_1)$
- $\sigma(pp \rightarrow h_1 h_1) = \sigma(pp \rightarrow h_2) BR(h_2 \rightarrow h_1 h_1)$
- **Large**  $m_{h_2} \Rightarrow$  **small**  $Br(h_2 \rightarrow h_1 h_1) \Rightarrow$  **small**  $\sigma(pp \rightarrow h_2 \rightarrow h_1 h_1)$



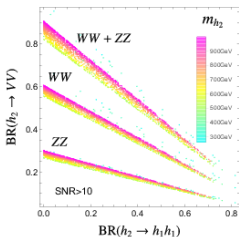
# Correlation with Double Higgs Production Searches



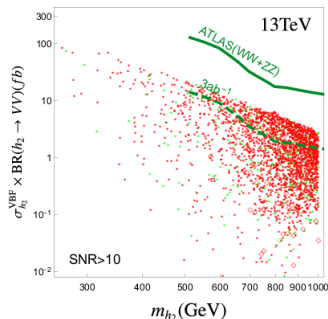
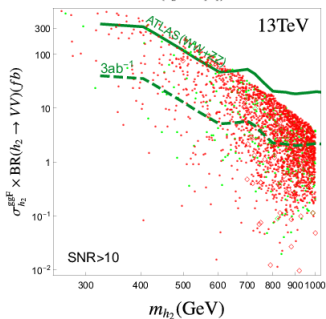
- SNR > 50 (red) and 50 > SNR > 10 (green)
- $m_{h_2} \lesssim 500 \text{ GeV}$  can be probed by both  $3 \text{ ab}^{-1}$  (13 TeV) HL-LHC and space-based GW detectors



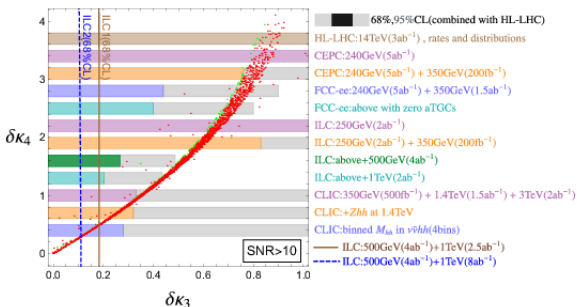
# Diboson Resonance Searches



- $SNR > 50$  (red) and  $50 > SNR > 10$  (green)
- Most of  $h_2$  decays in  $WW$ ,  $ZZ$ , and  $h_1 h_1$  channels
- HL-LHC will probe large fraction of parameter space in ggF and VBF channels



# Higgs Cubic and Quartic Couplings



arXiv:1711.03978

- SNR > 50 (red) and SNR > 10 (green)
- Precise measurements can be used to reconstruct the Higgs potential
- $\Delta\mathcal{L} = -\frac{1}{2} \frac{m_{h_1}^2}{v} (1 + \delta\kappa_3) h_1^3 - \frac{1}{8} \frac{m_{h_1}^2}{v^2} (1 + \delta\kappa_4) h_1^4$
- Correlation given by  $\delta\kappa_4 \approx \eta \delta\kappa_3$  for  $\eta \in (2, 4)$



# Conclusion



# Conclusion

- Electroweak Phase Transitions lead to a GW spectrum
- Singlet-extended SM Higgs sector offers a wide range of parameter space with large SNR at LISA
- Di-Higgs searches can probe lighter masses at HL-LHC
- Weak diboson resonance searches can probe a large fraction of the parameter space
- Modification to Higg's cubic and quartic couplings
- Main features of the parameter space:  $20 \text{ GeV} \lesssim |v_s| \lesssim 50 \text{ GeV}$ ,  $\theta \lesssim 0.2$ ,  $\delta\kappa_4 \approx (2 - 4)\delta\kappa_3$ , and large  $m_{h_2}$  preferred for SNR



## Some References

- W-mass: [arXiv:1203.0275](https://arxiv.org/abs/1203.0275)
- Higgs signal strength: [arXiv:1606.02266](https://arxiv.org/abs/1606.02266), and [arXiv:1801.00794](https://arxiv.org/abs/1801.00794)
- Sound waves: [arXiv:1504.03291](https://arxiv.org/abs/1504.03291)



# EWPT Definitions

- Key parameters:  $T_c$ ,  $T_n$ ,  $\alpha$ ,  $\beta$ , and  $v_w$

## Euclidean Action of the critical bubble

$$S_3(\vec{\phi}, T) = 4\pi \int r^2 dr \left[ \frac{1}{2} \left( \frac{d\vec{\phi}(r)}{dr} \right)^2 + V(\vec{\phi}, T) \right]$$

$$\left. \frac{d\vec{\phi}(r)}{dr} \right|_{r=0} = 0, \quad \vec{\phi}(r = \infty) = \vec{\phi}_{out}$$

## Inverse time duration of PT

$$\beta = H_n T_n \left. \frac{d(S_3/T)}{dT} \right|_{T_n}$$

## Bubble Nucleation Rate

$$\Gamma \sim \mathcal{A}(T) e^{-S_3/T}$$

## Bubble Nucleation

$$\int_0^{t_n} \Gamma V_H(T) dt = \int_{T_n}^{\infty} \frac{dT}{T} \left( \frac{2\xi M_{pl}}{T} \right)^4 e^{-S_3/T} = \mathcal{O}(1)$$

$$\frac{S_3(T)}{T} \approx 140$$

## Vacuum energy released from PT

$$\alpha = \frac{\Delta\rho}{\rho_R} = \frac{1}{\rho_R} \left[ -V(\vec{\phi}_b, T) + T \frac{\partial V(\vec{\phi}_b, T)}{\partial T} \right] \Big|_{T=T_n}$$





# W-mass Constraint

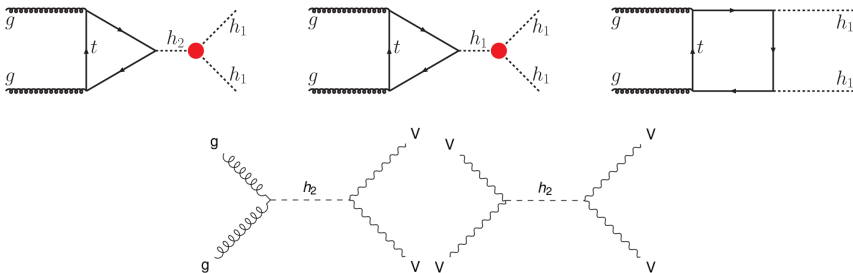


arXiv:1406.1043v2

- W mass calculated from experimentally measured values of  $G_F$ ,  $m_Z$ , and  $\alpha(0)$
- Functions relating these parameters depends on the loop calculations to the vector boson self-energies



# Feynman Diagrams for Double Higgs Production and Weak Boson Pairs



# Double Higgs Production Channels

## CMS

- $35.9 \text{ fb}^{-1}$  at 13 TeV
- di-Higgs decay channels:  $b\bar{b}\gamma\gamma$ ,  $b\bar{b}\tau^+\tau^-$ ,  $b\bar{b}b\bar{b}$ , and  $b\bar{b}WW/ZZ$
- arXiv:1811.09689 for recent combination

## ATLAS

- $36.1 \text{ fb}^{-1}$  at 13 TeV
  - Di-Higgs decay channels:  $\gamma\gamma b\bar{b}$ ,  $b\bar{b}\tau^+\tau^-$ ,  $b\bar{b}b\bar{b}$ ,  $WW^*WW^*$ , and  $b\bar{b}WW^*$
  - "Combination of searches for Higgs boson pairs in pp collisions at 13 TeV with the ATLAS experiment." for recent combination
- 
- Cross sections calculated at NNLO-NNLL for gluon fusion



# Diboson-Resonances

- ATLAS combined results at 13 TeV with  $36 \text{ fb}^{-1}$  data
- VBF at NNLO
- ggF at NNLO-NNLL
- Decay channels:  $WZ \rightarrow qq\bar{q}\bar{q}, l\nu q\bar{q}, l\nu ll$ ,  $WW \rightarrow qq\bar{q}\bar{q}, l\nu q\bar{q}, l\nu l\nu$ ,  $ZZ \rightarrow qq\bar{q}\bar{q}, \nu\nu q\bar{q}, llq\bar{q}, ll\nu\nu, ll ll$ , and  $WH \rightarrow qq\bar{b}\bar{b}, l\nu b\bar{b}, ZH \rightarrow qq\bar{b}\bar{b}, \nu\nu b\bar{b}, llb\bar{b}$ , and  $l\nu, ll$
- arXiv:1808.02380



# Higgs Cubic and Quartic Deviations at Lepton Colliders

- (Higgsstrahlung):  $e^+e^- \rightarrow hZ$
- (WW-fusion):  $e^+e^- \rightarrow \nu\bar{\nu}h$
- (WW-pair production):  $e^+e^- \rightarrow WW$
- Higgs decays into  $ZZ^*$ ,  $WW^*$ ,  $\gamma\gamma$ ,  $Z\gamma$ ,  $gg$ ,  $b\bar{b}$ ,  $c\bar{c}$ ,  $\tau^+\tau^-$ , and  $\mu^+\mu^-$
- Global Analysis: arXiv:1711.03978



# Perturbative Unitarity S-Matrix

- Eleven  $2 \rightarrow 2$  channels
- Charge neutral channels ( $h_1 h_1, h_2 h_2, h_1 h_2, h_1 Z, h_2 Z, ZZ, W^+ W^-$ )
- Charge-1 channels ( $h_1 W^+, h_2 W^+, ZW^+$ )
- Charge-2 channels ( $W^+ W^-$ )
- Leading partial wave amplitudes of these scatterings are given collectively by a symmetric matrix  $S = S_0 \oplus S_1 \oplus S_2$

