

Refined mass window for a stable sexaquark

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With Glennys Farrar, 190X.XXXXX to appear

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What is sexaquark (S): $uuddss$ color-spin-flavor singlet

$$|S\rangle = \frac{1}{24} (\epsilon_{\alpha\mu\rho}\epsilon_{\beta\nu\sigma}\epsilon_{im}\epsilon_{jk}\epsilon_{ln} - \epsilon_{\alpha\beta\rho}\epsilon_{\mu\nu\sigma}\epsilon_{im}\epsilon_{jl}\epsilon_{kn}) u_{\alpha,i}^\dagger u_{\beta,j}^\dagger d_{\mu,k}^\dagger d_{\nu,l}^\dagger s_{\rho,m}^\dagger s_{\sigma,n}^\dagger |\Omega\rangle$$

(Farrar, Wintergerst, *in prep*)

- Quantum numbers: $Q = 0$, $B = 2$, $S = -2$, $P = 1$
- Compact in size $\sim 0.1 - 0.3$ fm,

$$r_S = \lambda_S + 0.5\lambda_{\omega-\phi}$$

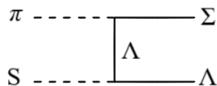
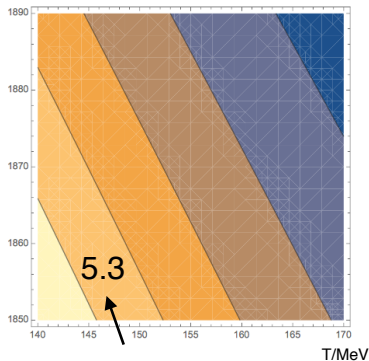
c.f. proton ~ 0.9 fm with pion clouds.

(Farrar 17)

Motivation: DM candidate

DM candidate in SM: abundance ~ 5 times of baryons from QCD plasma.

$m(S)/\text{MeV}$



Breakup of S by mesons, need vertex $g(S\Lambda\Lambda) \lesssim 10^{-6}$ to maintain $\Omega_{\text{DM}}/\Omega_b \sim 5$.

(Farrar 18)

Spatial overlap

Coupling constant $g(S\Lambda\Lambda) = \frac{\mathcal{O}_{sp}}{\sqrt{40}}$. Spatial wavefunction overlap

$$\mathcal{O}_{sp} = \langle \psi_{sp}(\Lambda_1) \psi_{sp}(\Lambda_2) | \psi_{sp}(S) \rangle \sim \left(\frac{r_S}{r_\Lambda} \right)^{18}.$$

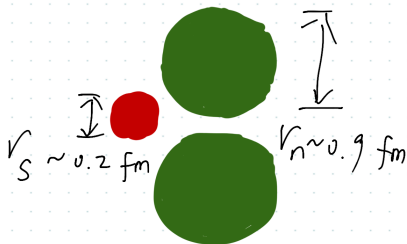
(Farrar, Zaharijas, 03)

Take $r_S = 0.2$ fm, $r_\Lambda = 0.9$ fm,

$$\mathcal{O}_{sp} \sim 10^{-12}.$$

DM abundance requirement

$\mathcal{O}_{sp} \lesssim 10^{-6}$ easily satisfied.



- Unstable for $m_S > 2(m_p + m_e) = 1877.6$ MeV

$$S \rightarrow ppe\bar{e}\bar{\nu}, npe\bar{\nu}, nn.$$

- Absolutely stable for $m_S < 1877.6$ MeV by B conservation. But nuclei could decay if S is too light.
- Narrow mass window for absolutely stable S and nuclei:

$$1877.6 - \text{B.E.} < m_S < 1877.6 \text{ MeV},$$

e.g. B.E. ~ 16 MeV in oxygen, ~ 2 MeV in deuteron.

- This work: for $m_S \sim 1382\text{-}2055$ MeV, how unstable are S and nuclei.

Untable S : $S \rightarrow nn$

Model $S \rightarrow nn$ by an effective Yukawa interaction

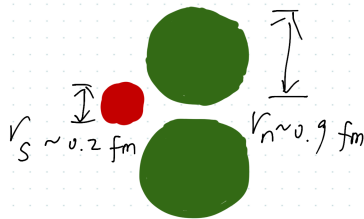
$$\mathcal{L} = gS\bar{n}n^C + \text{h.c.}$$

Coupling constant $g \propto \mathcal{O}_{\text{sp}} = \langle \psi_{\text{sp}}(n_1)\psi_{\text{sp}}(n_2) | \psi_{\text{sp}}(S) \rangle$. Take \mathcal{O}_{sp} as a free parameter.

Estimates for $r_S \sim 0.2 \text{ fm}$, $r_n \sim 0.9 \text{ fm}$,

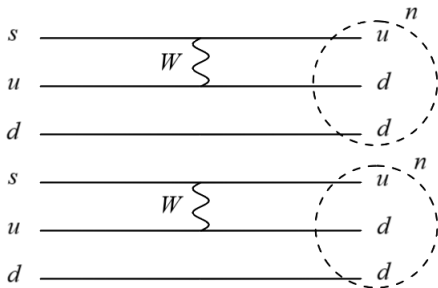
$$\mathcal{O}_{\text{sp}} \sim 10^{-12}.$$

But not enough yet: the weak interaction.



$S \rightarrow nn$: EFT

$\Delta S = \pm 2$, doubly-weak interaction of quarks: $g^2 \propto G_F^4 p^8 \sin^4 \theta_c$



Choice of p : Physical mass \sim MeV (ud) and \sim 100 MeV (s); $\Lambda_{\text{QCD}} \sim$ 100 MeV; Constituent mass \sim 300 MeV; Heisenberg uncertainty \sim GeV.

- Combine weak interaction and spatial overlap,

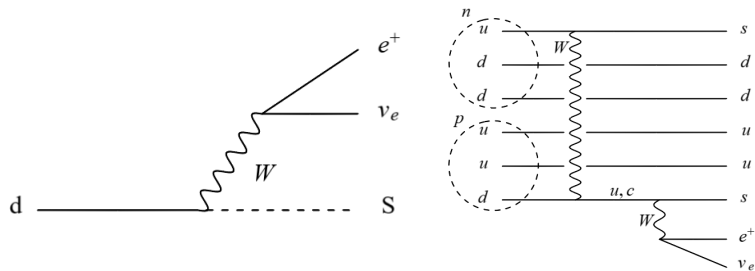
$$g^2 = \mathcal{O}_{\text{sp}}^2 \times \left(\frac{p}{\text{MeV}} \right)^8 \times 10^{-44}.$$

- Decay rate

$$\Gamma(S \rightarrow nn) = \frac{g^2 m_S}{8\pi} \left(1 - \frac{4m_n^2}{m_S^2} \right)^{3/2}$$

depends on m_S , \mathcal{O}_{sp} and p .

Unstable deuteron: $d \rightarrow Se^+\nu_e$

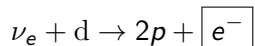
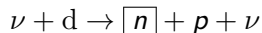


$$\mathcal{L} \supset gSd^\mu W_\mu + g_W W_\mu \bar{\psi} \gamma^\mu (1 - \gamma^5) \psi$$

$$g^2 \sim g_W^2 G_F^2 p^6 \sin^4 \theta_c \mathcal{O}_{sp}^2$$

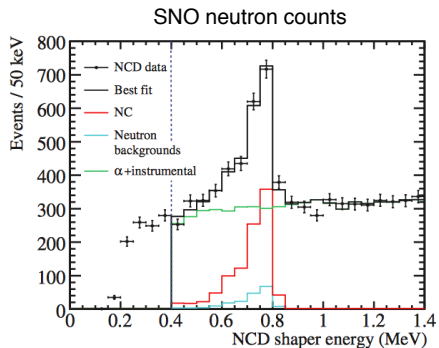
$$\frac{d\Gamma}{dE_e} = \frac{g^2 g_W^2}{3m_W^4} \frac{1}{32\pi^3 m_d m_S} \sqrt{E_e^2 - m_e^2} E_e (m_d - m_S - E_e)^2$$

- Sudbury Neutrino Observatory (SNO):

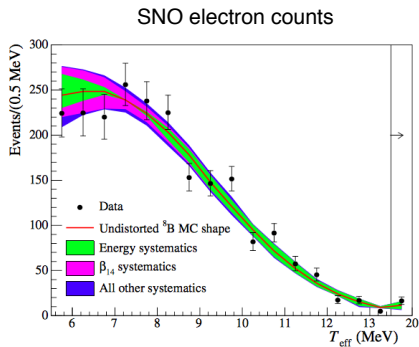


- S trapped in Earth crust $\sim 10^{14}/\text{cm}^3$ (Neufeld, Farrar, McKee 2018). Neutrons from $S \rightarrow nn$ may be detected by SNO.
- In SNO heavy water tank, $\#d \sim 10^{32}$. Positrons from $d \rightarrow Se^+\nu_e$ produces identical signals as electrons.
- SNO neutron and electron counts place upper limits on $\Gamma_{S \rightarrow nn}$ and $\Gamma_{d \rightarrow Se\nu}$.

SNO neutron and electron counts



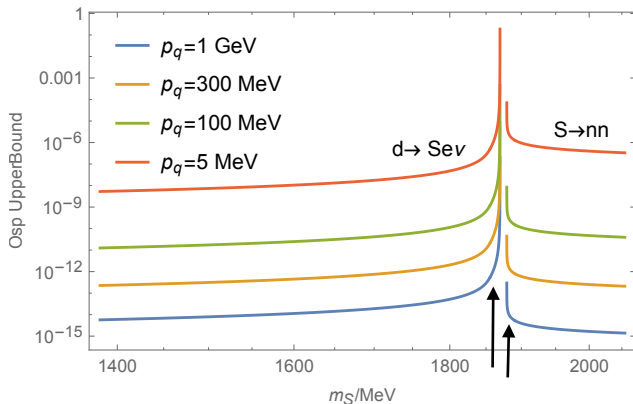
(a) $\Gamma_{S \rightarrow nn}^{-1} > 10^{19}$ yr.
 \gg age of universe



(b) $\Gamma_{d \rightarrow Se\nu}^{-1} > 10^{28}$ yr.

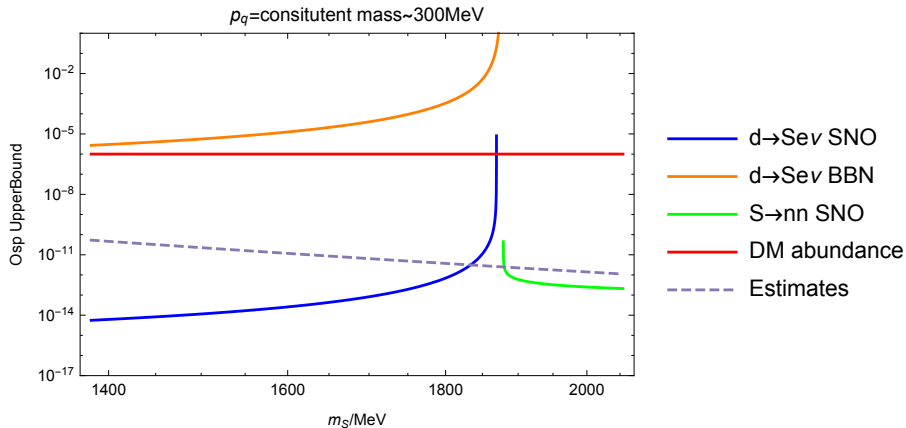
(SNO 1602.02469)

Upper limits on \mathcal{O}_{sp} by SNO neutron and electron counts



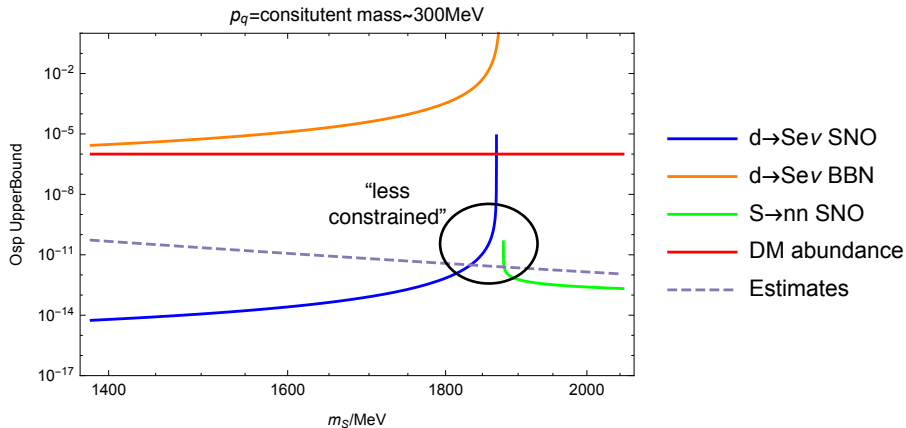
Combined limits on \mathcal{O}_{sp}

Combined upper limits on \mathcal{O}_{sp} with $p = 300$ MeV



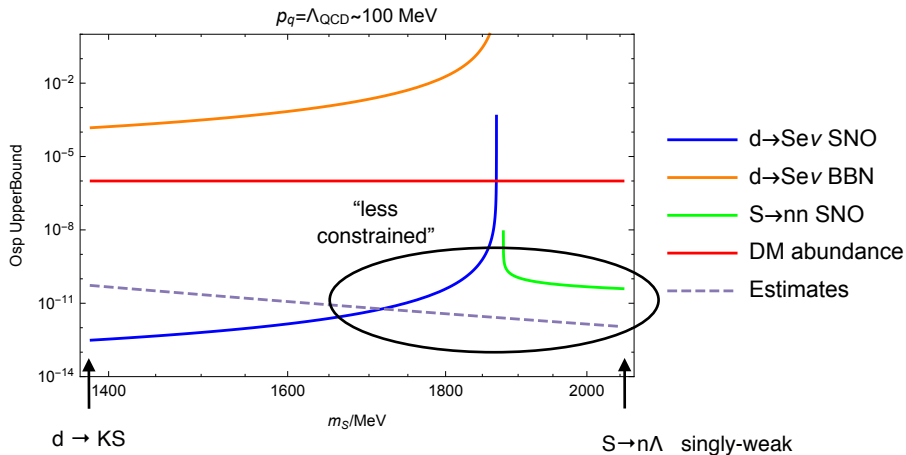
Combined limits on \mathcal{O}_{sp}

Combined upper limits on \mathcal{O}_{sp} with $p = 300$ MeV



Combined limits on \mathcal{O}_{sp}

Combined upper limits on \mathcal{O}_{sp} with $p = 100$ MeV



Range of m_S

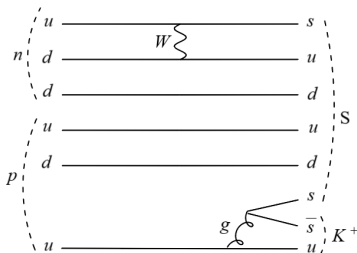
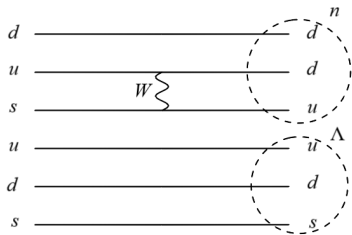
- $m_S > m_n + m_\Lambda = 2055$ MeV, singly-weak decay of S

$$S \rightarrow n\Lambda$$

- $m_S < m_d - m_K = 1382$ MeV, singly-weak decay of d with a gluon

$$d \rightarrow K^+ S$$

- Beyond there, need much smaller \mathcal{O}_{sp} because of shorter lifetime.

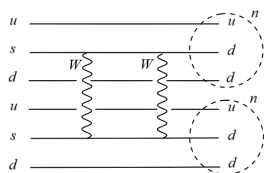
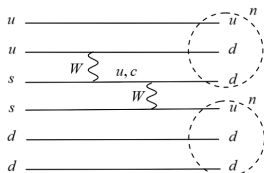
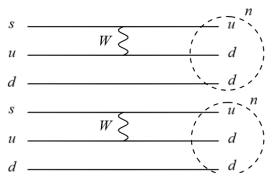


Conclusions

- For $m_S \sim 1382\text{-}2055$ MeV, S and deuteron are not so unstable if \mathcal{O}_{sp} is sufficiently small.
- For m_S not too away from $2m_n$, \mathcal{O}_{sp} is less constrained (above the estimated curve).
- Future work: oxygen in SuperK might place stronger bounds for $m_S < 2m_p$?

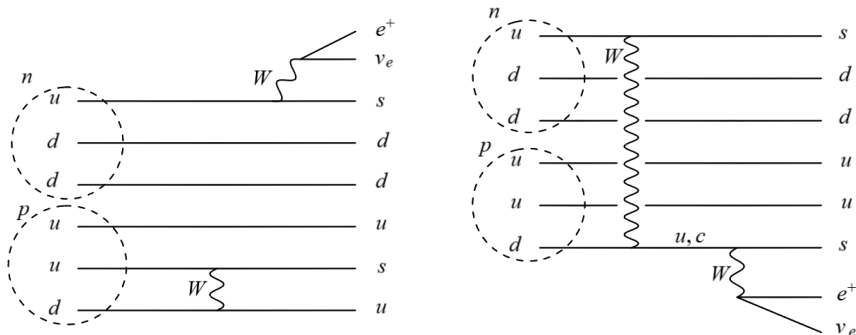
Thank you!

Back up slides



Sum over color-spin-flavor wavefunctions of S and n .

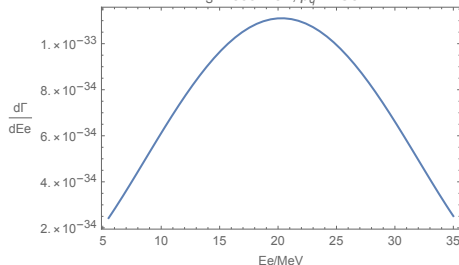
Back up slides



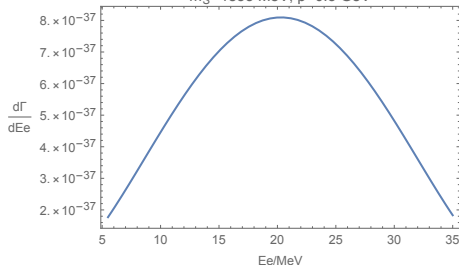
Sum over color-spin-flavor wavefunctions of d (n and p) and S .

$$\frac{d\Gamma}{dE_e} = \frac{g^2 g_W^2}{3m_W^4} \frac{1}{32\pi^3 m_d m_S} \sqrt{E_e^2 - m_e^2} E_e (m_d - m_S - E_e)^2$$

$m_S=1835$ MeV, $p_q=1$ GeV

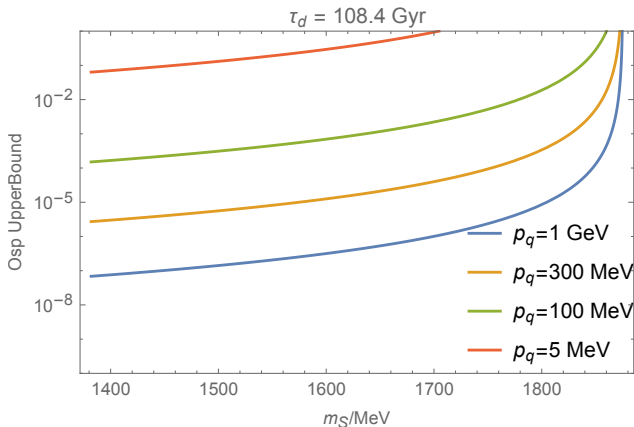


$m_S=1835$ MeV, $p=0.3$ GeV



$d \rightarrow Se^+ \nu_e$: BBN limit

$\Gamma_{d \rightarrow Se\nu}$ not too large to mess up the BBN deuteron abundance



Much weaker than SNO.