



# Differential Cross Section for Inclusive Jets and Event Properties in CMS Experiment



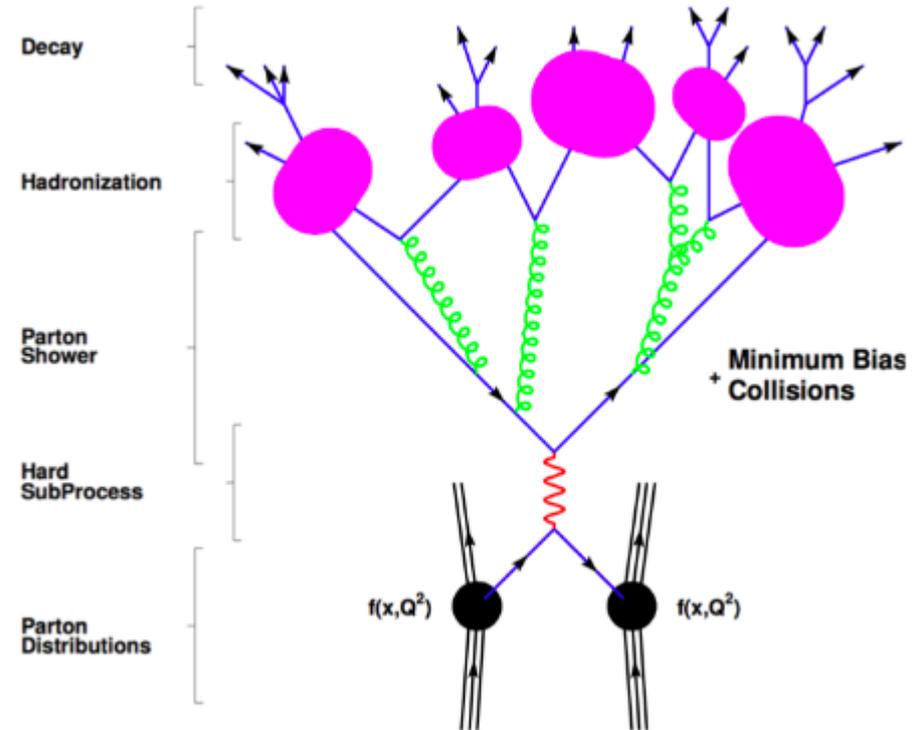
Suman Chatterjee  
Tata Institute of Fundamental Research  
Mumbai, India



# Inclusive Jets : Why?

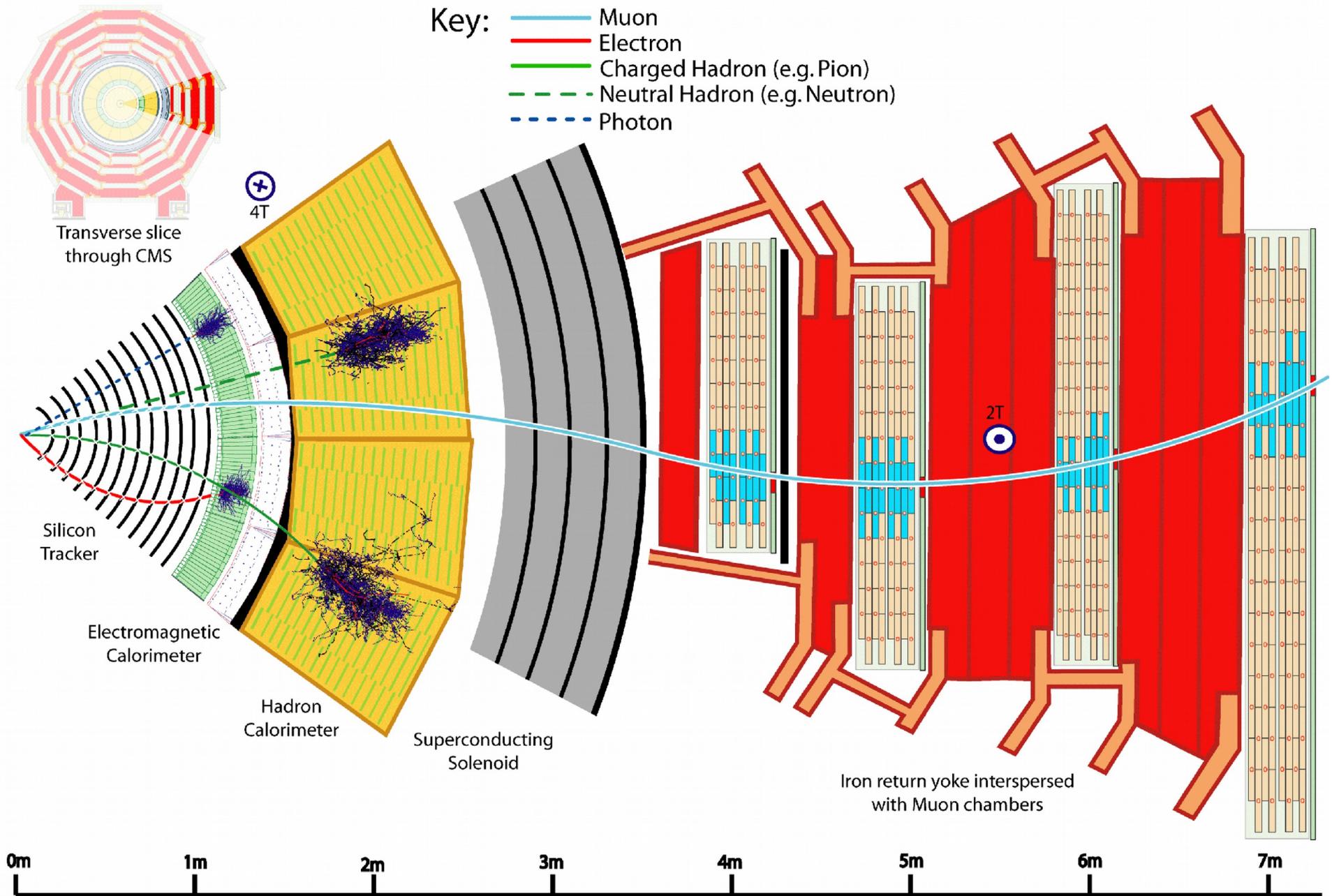
- Jets : collimated particle clusters in detector  
surrogates of quarks & gluons produced in hard interaction
- Inclusive Jets :  $p p \rightarrow \text{jets} + X$   
flooded by QCD
- Useful for
  - measurement of strong coupling constant
  - better determination of PDF
  - understanding the dynamics of p-QCD  
& resummation
  - tuning the general purpose  
event generators

...



Common bkg for BSM search with hadronic final states

# Skeleton of Compact Muon Solenoid

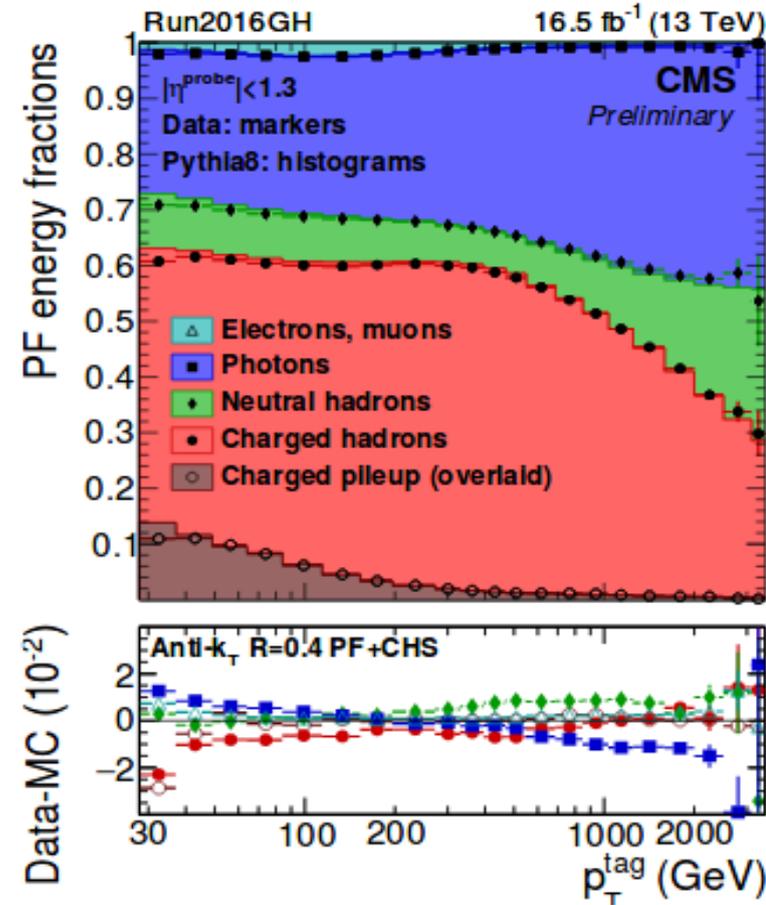
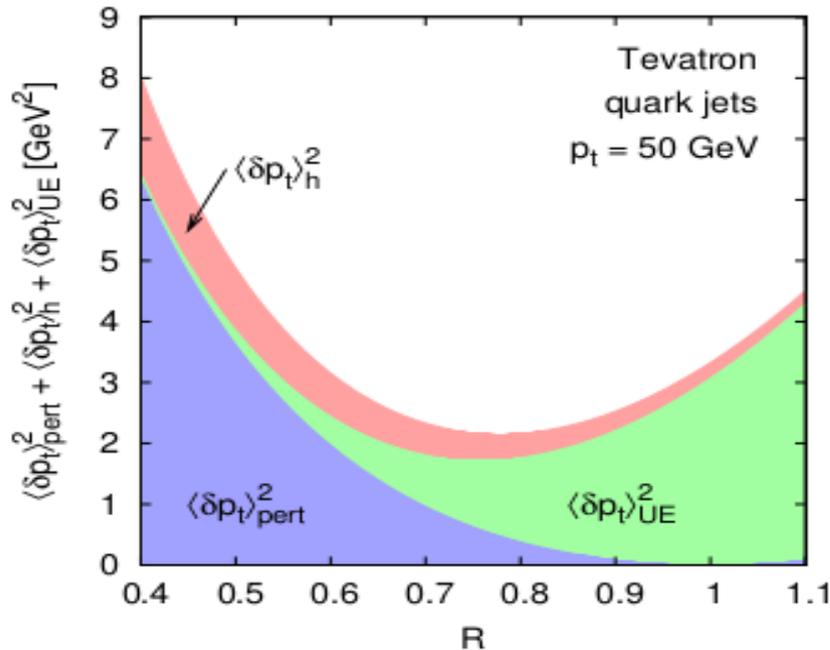


# Understanding Jets

- Information from all sub-detectors are combined to reconstruct and identify particles (Particle Flow)  $\rightarrow$  PF candidates
- Jets, in CMS, are reconstructed using PF candidates using anti-kT algorithm

## Choice of jet size :

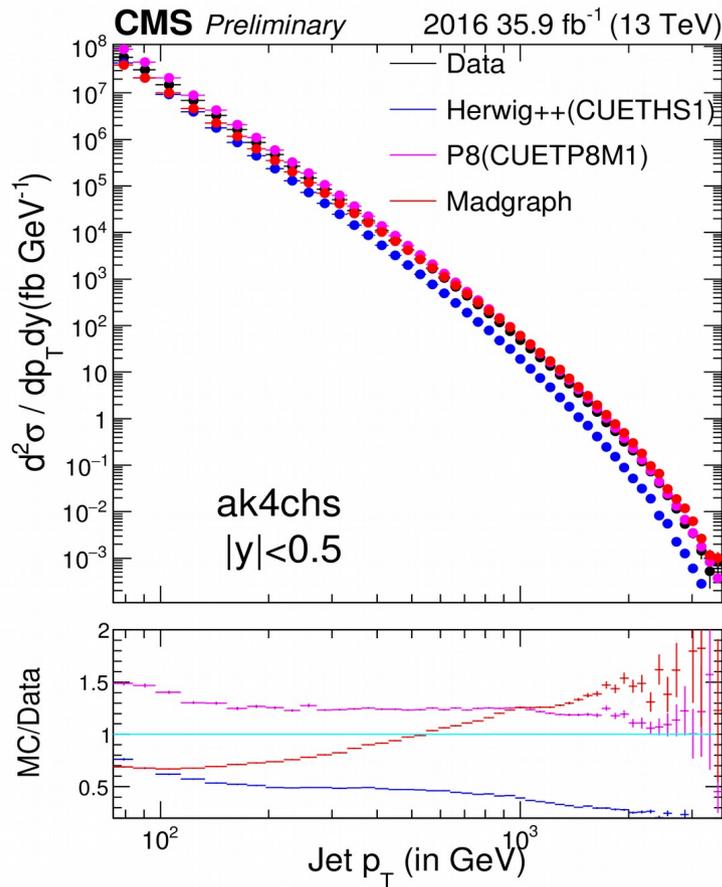
Interplay between losing radiation vs adding pile-up



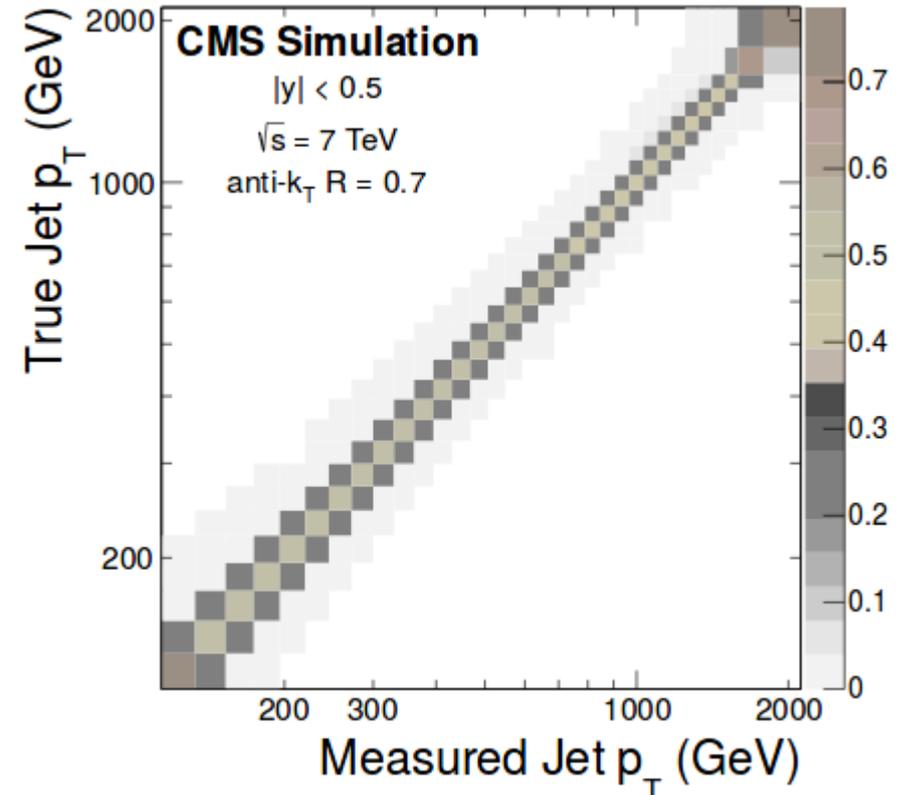
Excellent tracking performance even in  $\sim \text{TeV}$  scale

Higher  $P_T \Rightarrow$  Larger shower depth  
 $\Rightarrow$  Larger EM fraction

# Detector Level Spectra & Unfolding (Journey of Jets from Detector to Particle)



Unfolding removes detector effects  
(inefficiency & resolution)!



What we measure in data  
(MC with full detector simulation)

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Correlation between  
detector & particle level spectra!

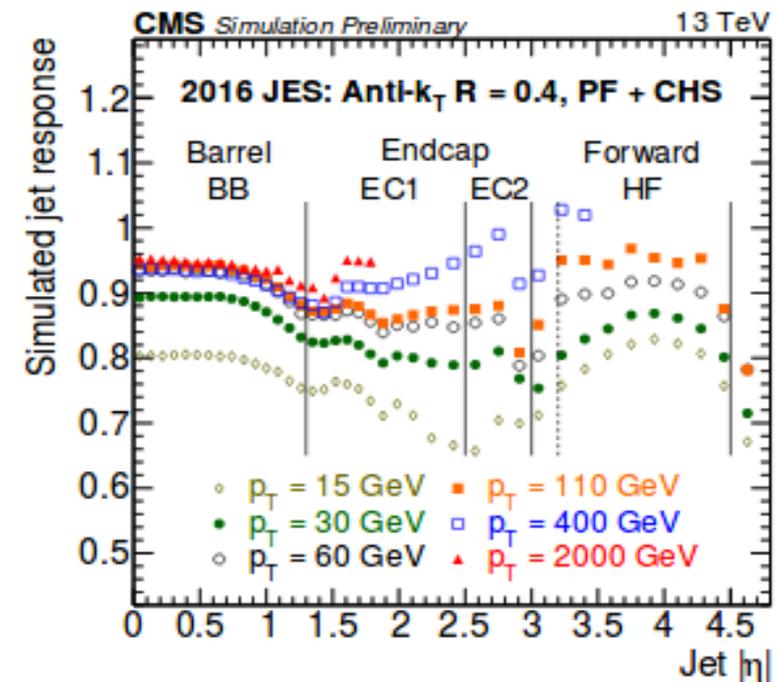
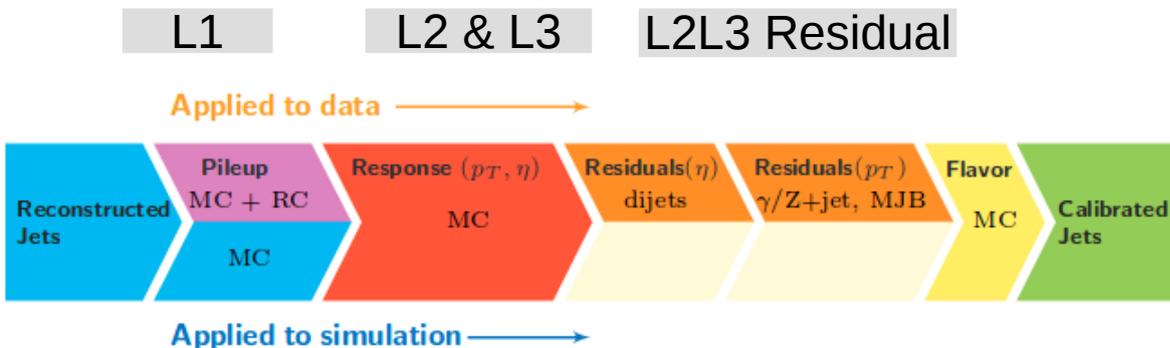
CMS QCD-11-004

Difference between unfolded and detector level spectra : 5-20%

# Jet Energy Calibration

- Cross-section measurement depends crucially on energy calibration and resolution → (steep spectra mis-measurement leads to bin migration)
- Factorised approach to match energy scale (mean of  $(p_{T, Det} - p_{T, Gen})/p_{T, Gen}$ ) of detector level jets to particle level jets (on average)

CMS DP-2018/028



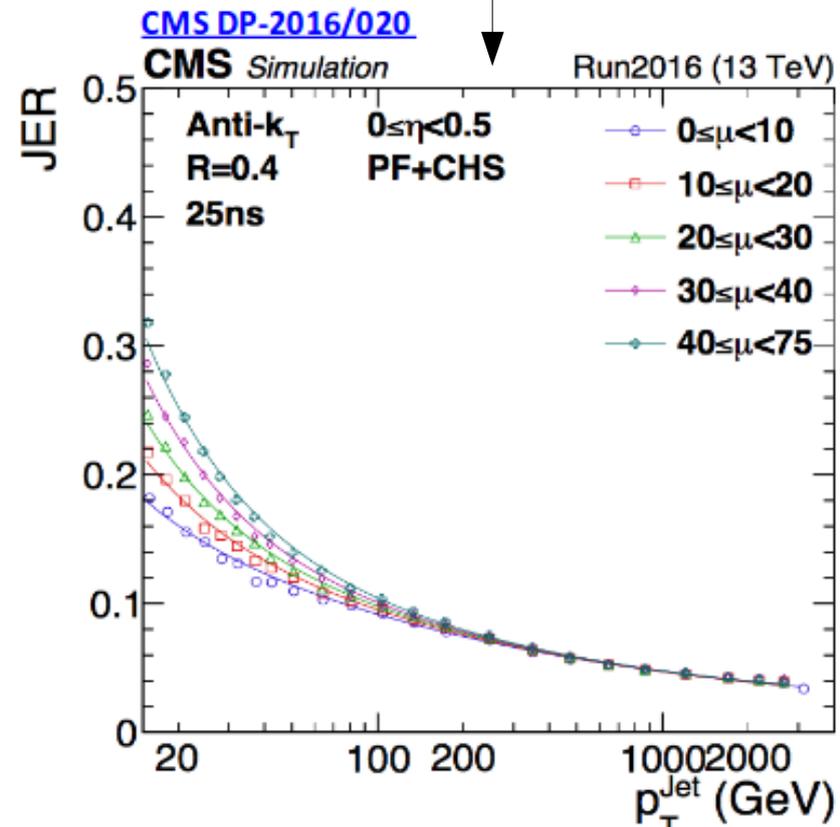
- **L1** : Pile-up subtraction by removing tracks coming from secondary vertices and neutrals by subtraction using pile-up simulation cone method)
- **L2 & L3**: Correction as a function of jet pseudorapidity and  $p_T$  based on simulation
- **L2L3** : Additional correction for data based on MET minimisation in  $\gamma/Z$  + jet, dijet events

# Jet Energy Resolution

- Cross-section measurement depends crucially on energy calibration and resolution → (steep spectra mis-measurement leads to bin migration)
- Resolution = spread in  $(pT_{Det} - pT_{Gen})/pT_{Gen}$
- Effect of energy resolution appears through unfolding => leads to systematic uncertainty
- Jet energy resolution (JER) in MC is obtained (after applying JEC) by matching detector level jets to particle level jets,
- Data/MC scale factor is derived using photon+jet balance, di-jet asymmetry
- Uncertainty in JER comes from ISR+FSR, pile-up contamination, OOC showering, difference in flavour response ...

CMS DP-2018/028

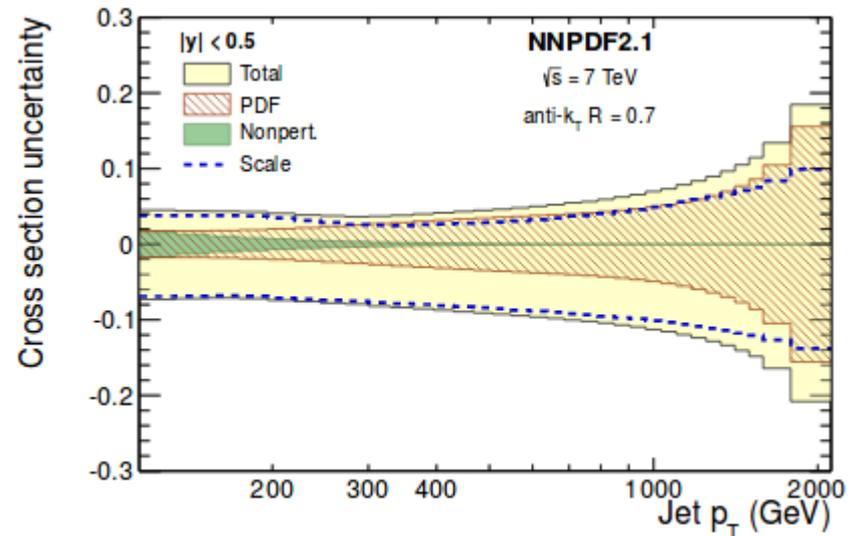
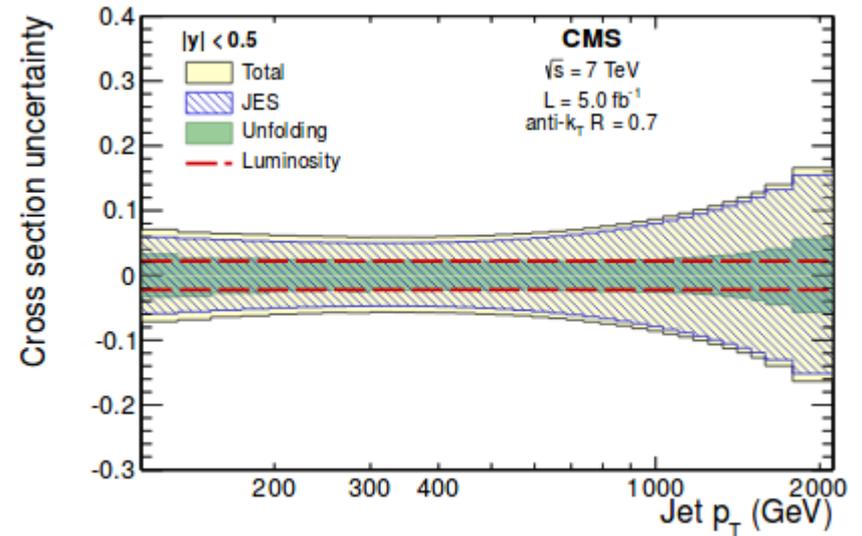
Effect of Pile up below  $p_T < 100$  GeV



# Systematics in Cross-Section Measurement

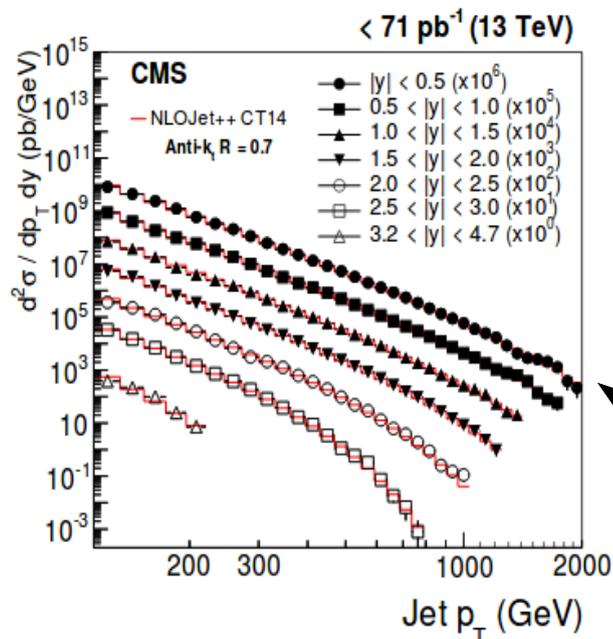
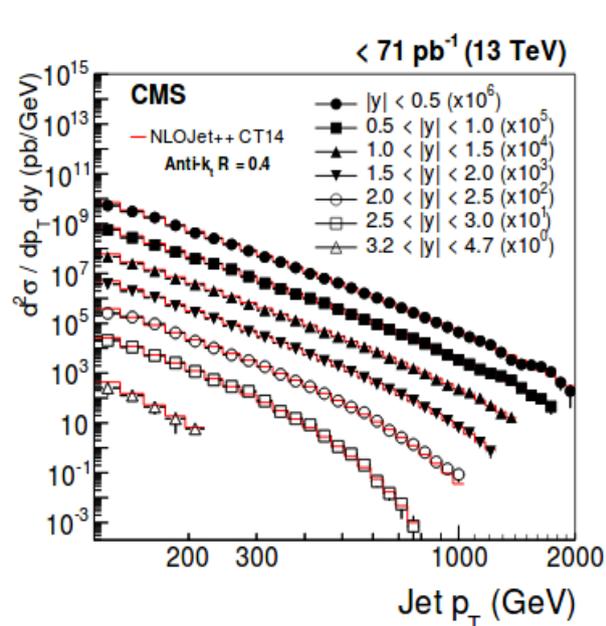
Experimental Sources	Theoretical Sources
Jet Energy Scale (JES) (8-65 % for AK4& AK7)	Scale choice (AK7 : 1-12% AK4 : 1-10%)
Jet Energy Resolution (JER) (1-2%)	PDF (AK7 : 1-8% AK4 : 2-10%)
Pile-up (~0.1%)	Non-perturbative cor (AK7 : 1%, AK4 : 2%)
Uncertainty in Luminosity (4.8%)	Uncertainty in $\alpha_s$ (~1%)
Unfolding (~1%)	Values quoted for 13 TeV Measurement (50 ns data)

These numbers are for inclusive jet  
Cross-section measurement



- JES dominates exp uncertainty
- Scale and PDF control theory systematics

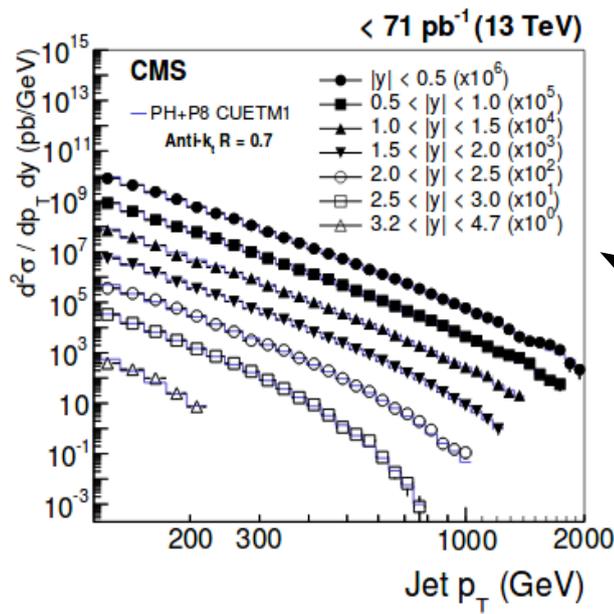
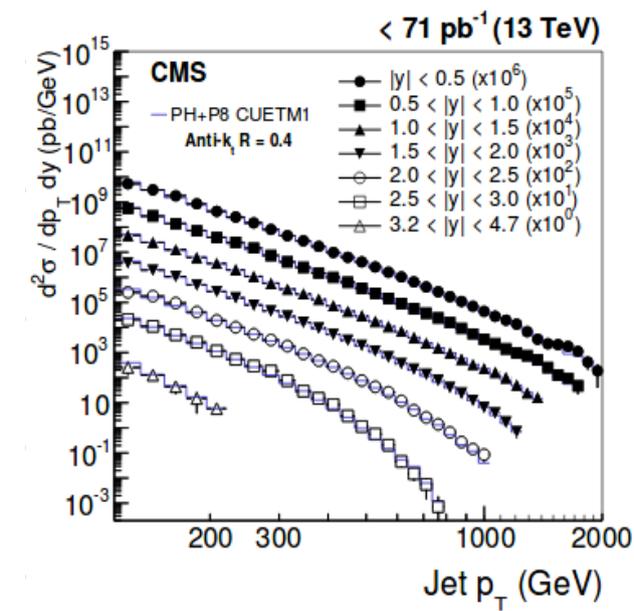
# Inclusive Jet Cross-Section at 13 TeV



Two different jet sizes to understand parton evolution

Fixed order (NLO) prediction  
 \* NP \* EW correction

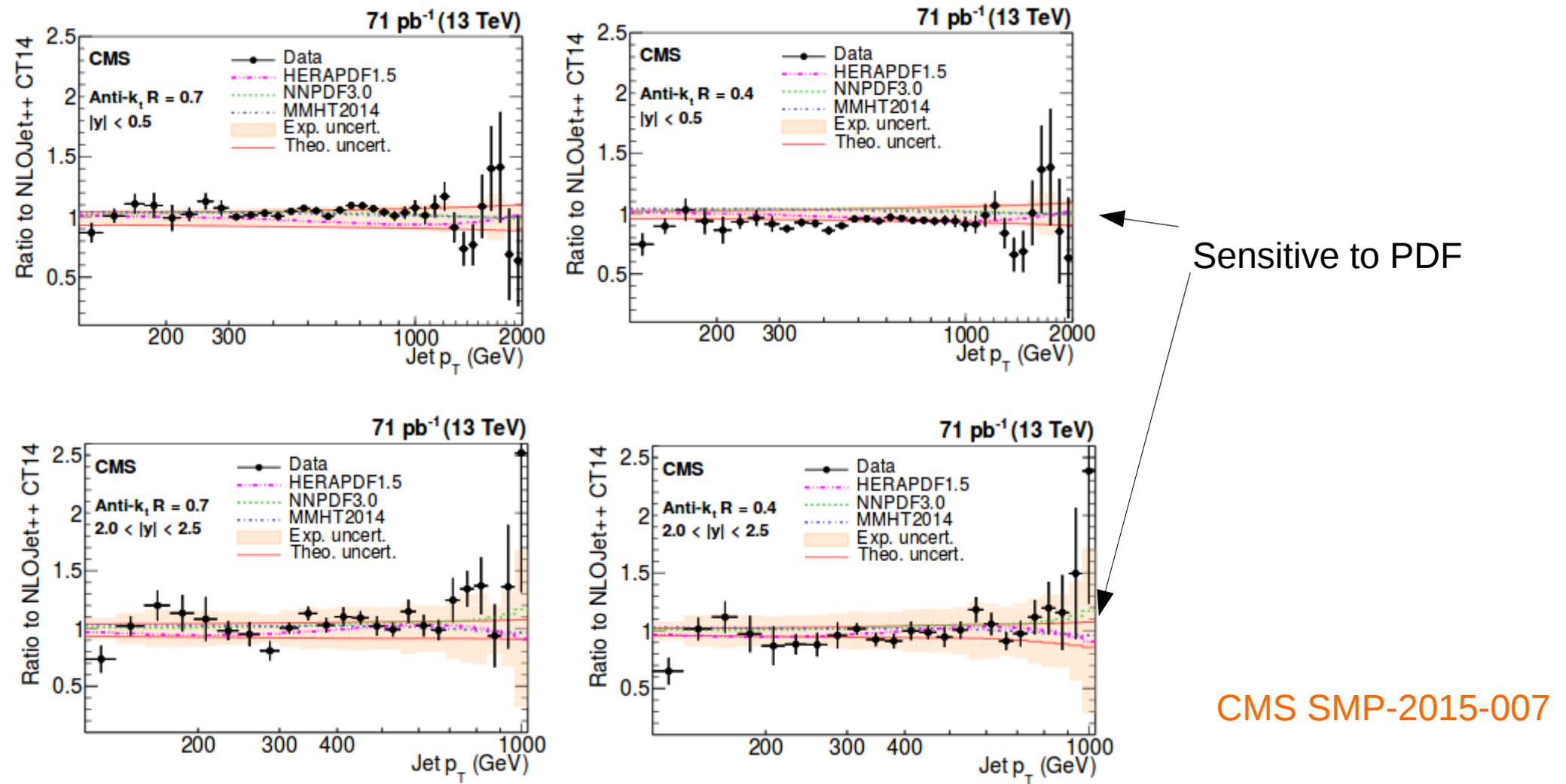
Correction for parton to hadron level change



Good agreement between Data and NLO prediction over 8 orders of magnitude

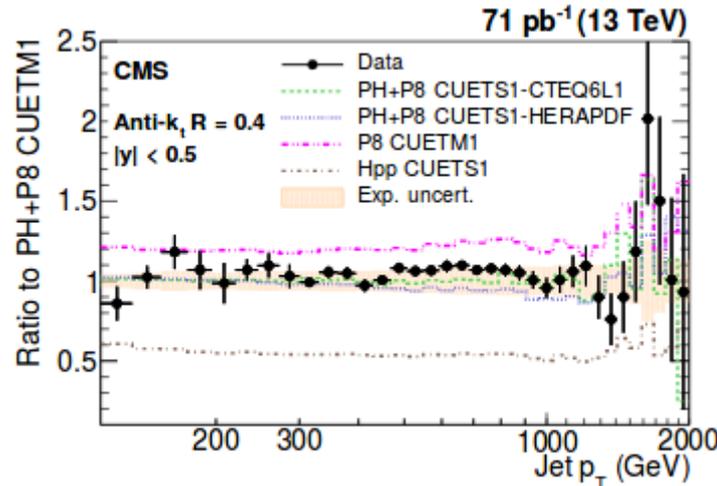
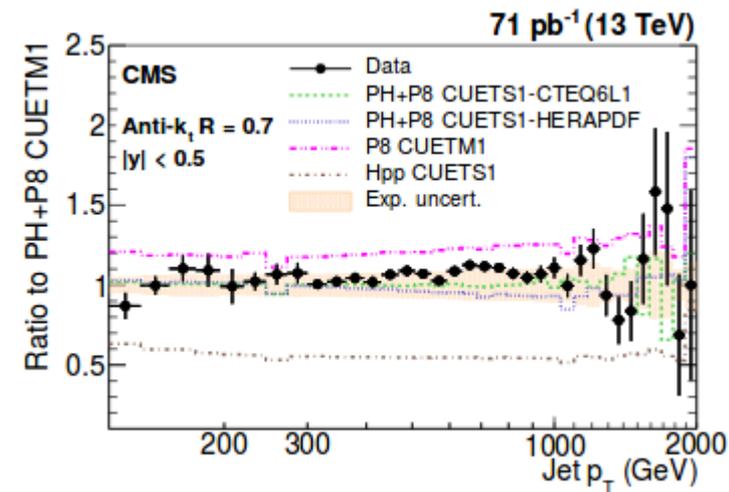
NLO + PS (parton shower)

# Comparison to Fixed Order Prediction at 13 TeV



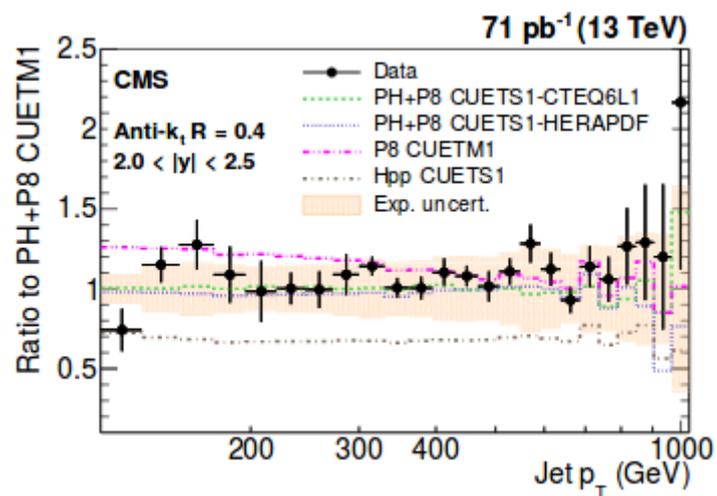
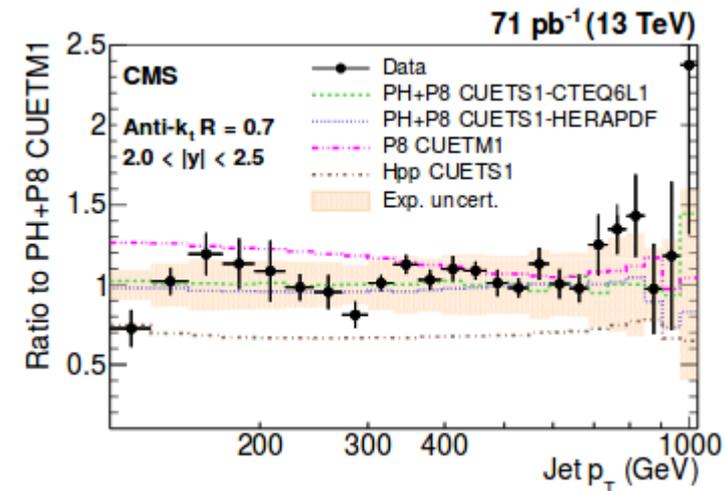
- Overall good agreement with NLO prediction for AK7 jets (with larger fluctuation in data in forward region)
- Cross-section is little overestimated for AK4 jets (resummation of radiated soft gluons is absent in NLO prediction : more important for jets of small sizes)

# Comparison to Parton Shower MC at 13 TeV



Two LO predictions are in opposite directions w.r.t. data

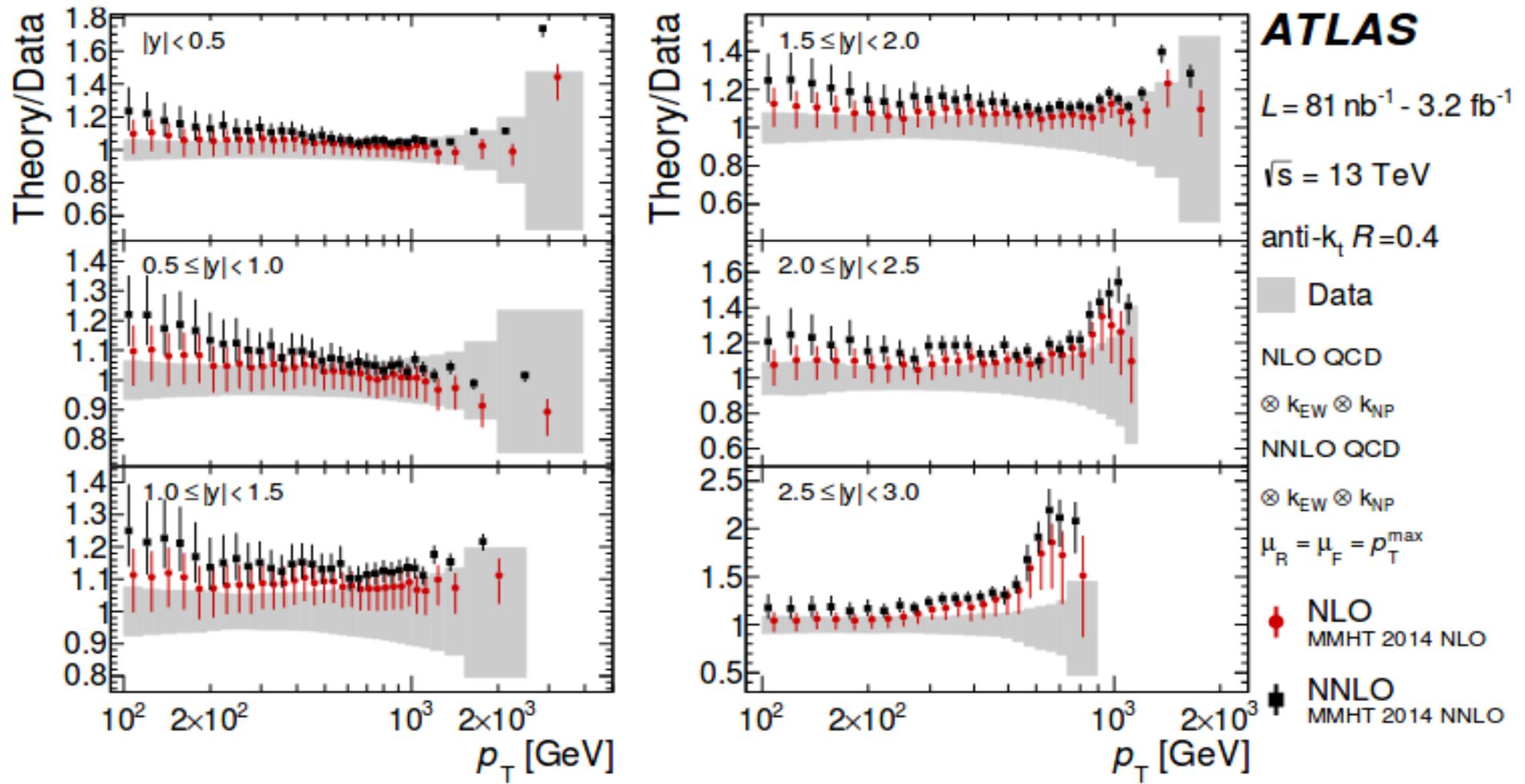
NLO is between PYTHIA8 & HERWIG++, describes data quite well



CMS SMP-2015-007

- For AK4 jets, NLO+PS provides better description compared to fixed order calculation
- For AK7 jets, prediction is quite similar to the one from fixed order NLO<sub>11</sub> calculation

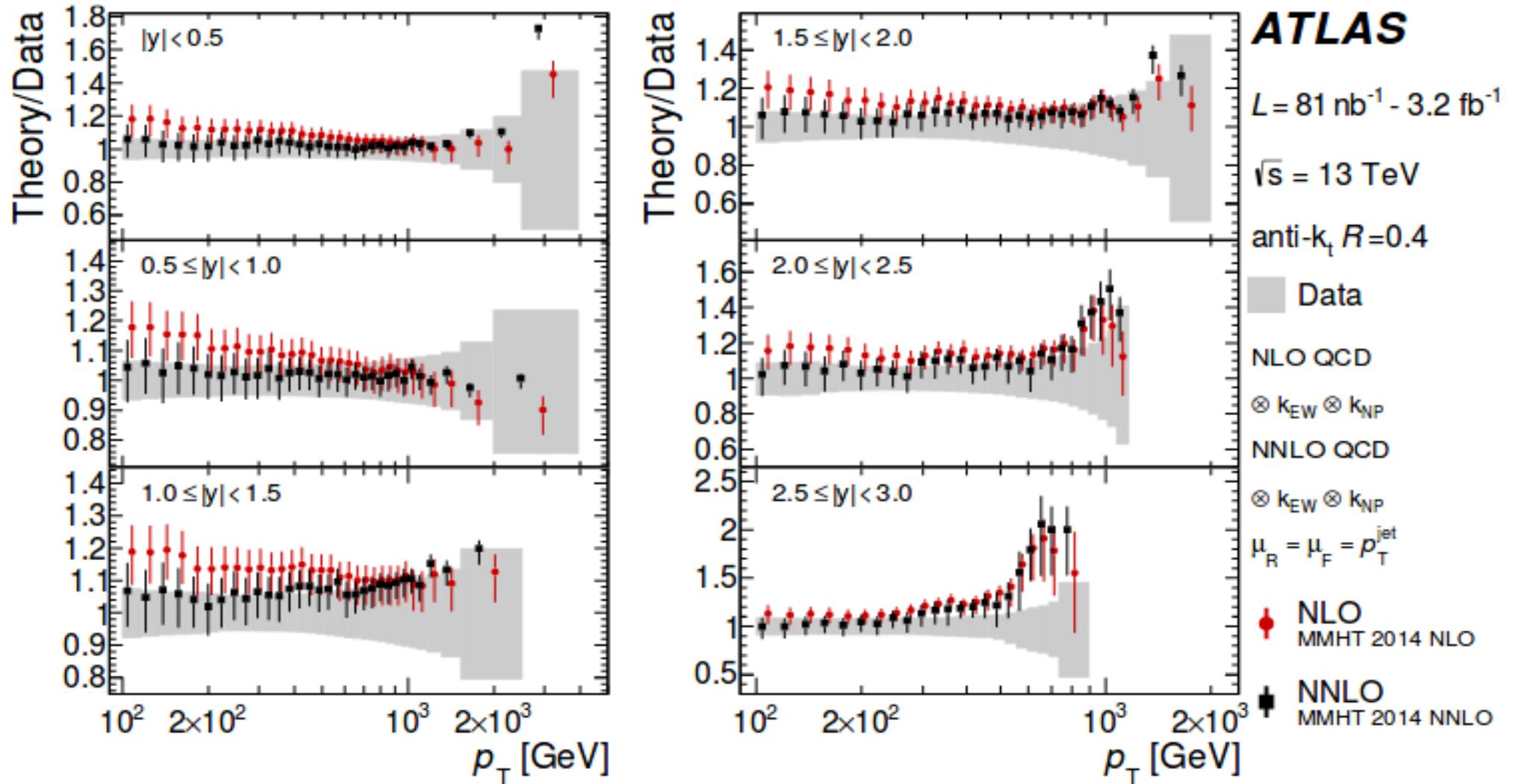
# Scale Choice for Higher Order Calculation



arXiv:  
1711.02692

- With  $p_T(\text{max})$  scale, NLO prediction describes data better

# Scale Choice for Higher Order Calculation



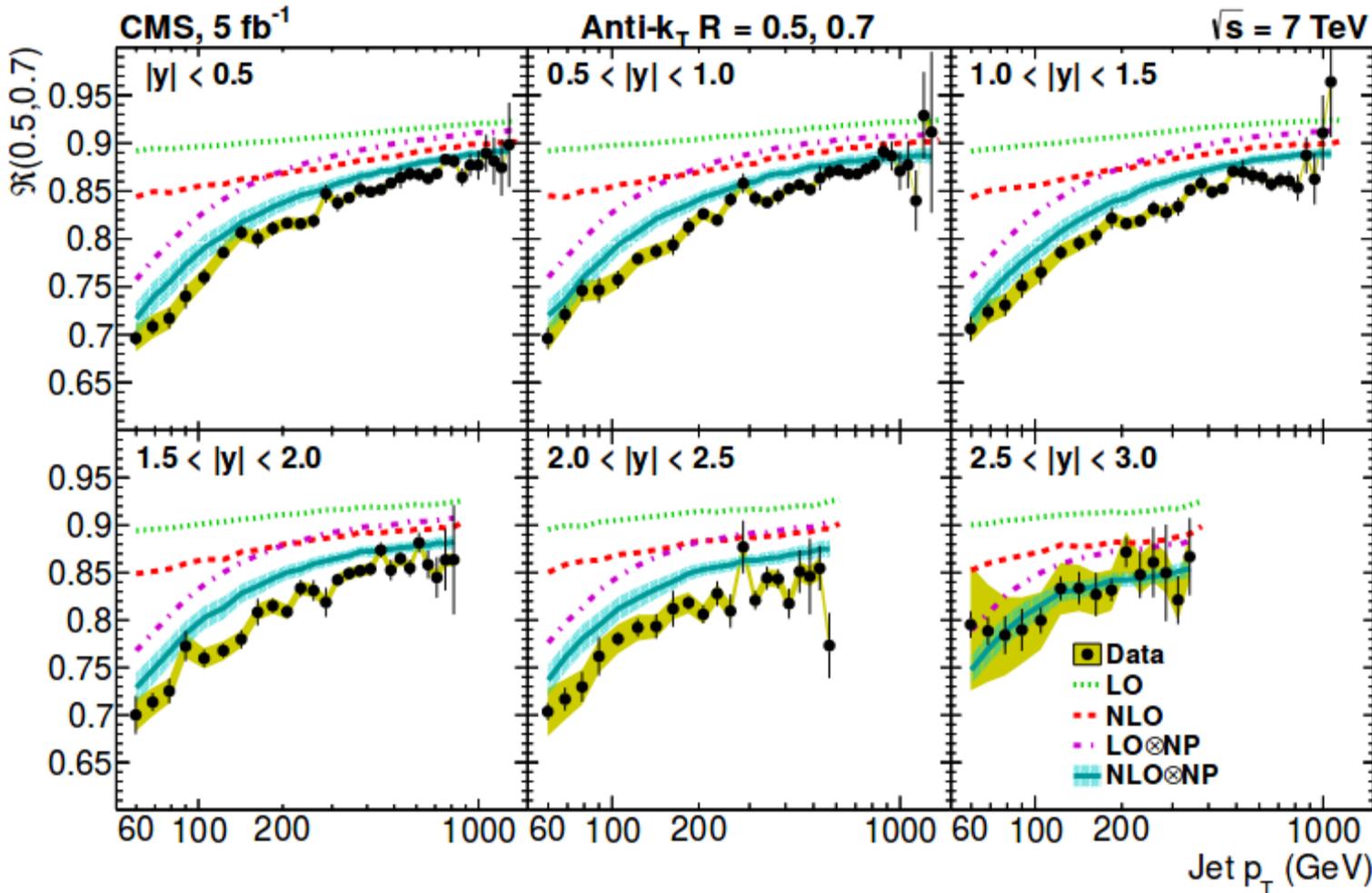
arXiv:  
1711.02692

- With  $p_T(\text{avg})$  scale, NNLO prediction describes data better

# Cross-Section Ratio of Two Jet Sizes

at  $\sqrt{s} = 7 \text{ TeV}$

: Power of Ratio



Many of the systematics (JES, luminosity for exp side PDF,  $\alpha_s$  for theory side) mostly cancel in ratio!

Data lies below the prediction almost everywhere

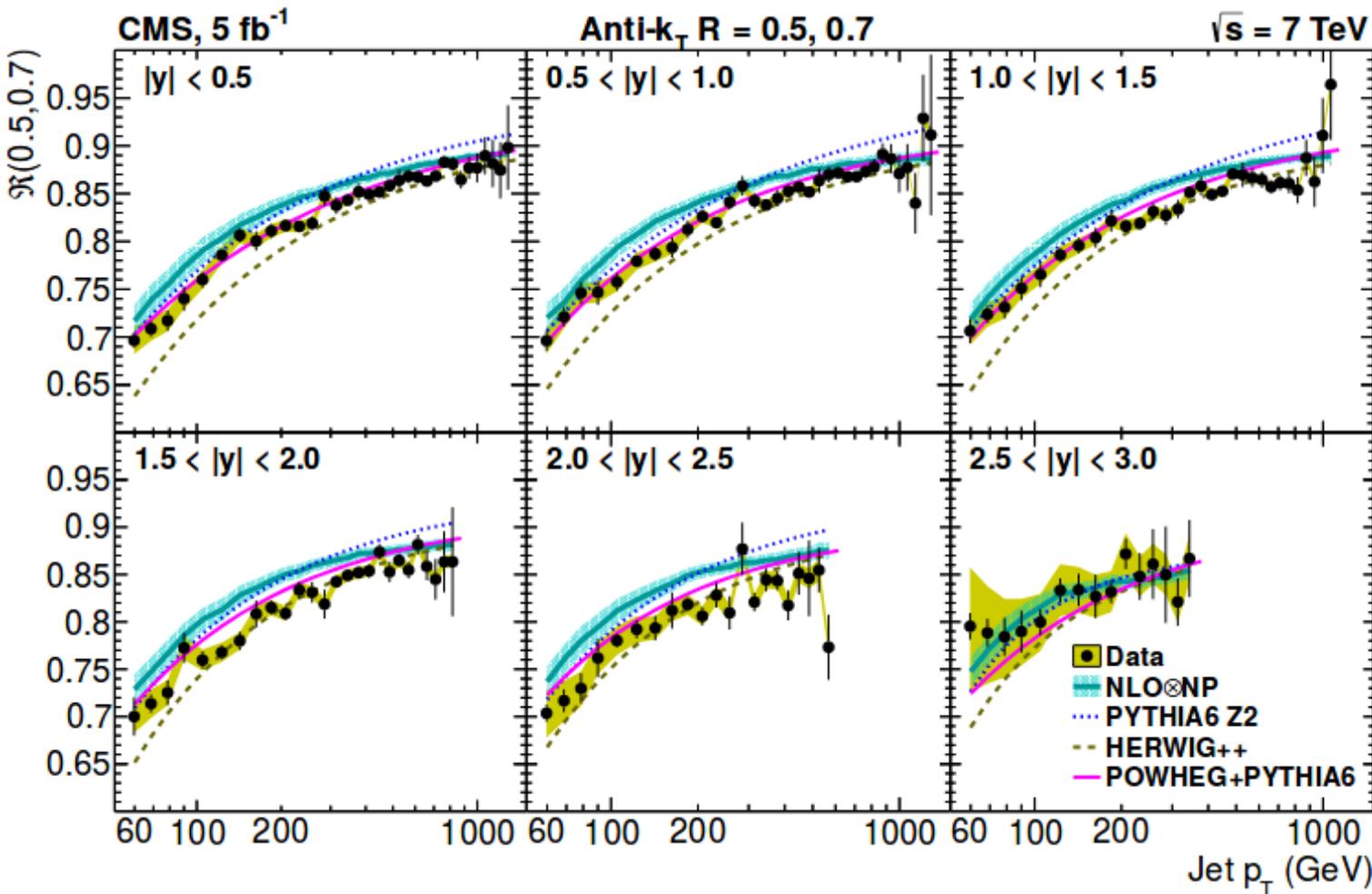
CMS SMP-2013-002

- Non-perturbative correction is evident to be essential to complement fixed order prediction
- NNLO prediction (effectively NLO for ratio) improves the agreement with data

# Cross-Section Ratio of Two Jet Sizes

at  $\sqrt{s} = 7$  TeV

: Power of Ratio



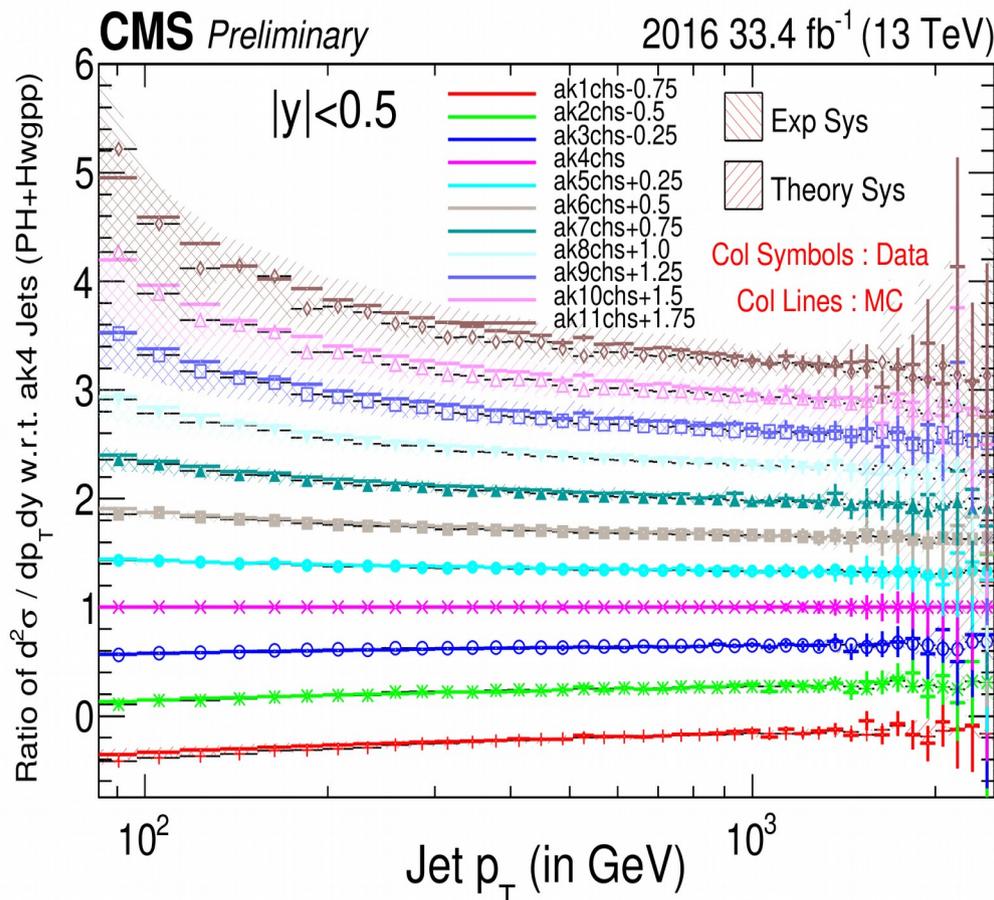
CMS SMP-2013-002

- Better modelling of data by using parton shower, best with NLO generator followed by parton shower
- Shows the importance of final state radiation to describe the ratio

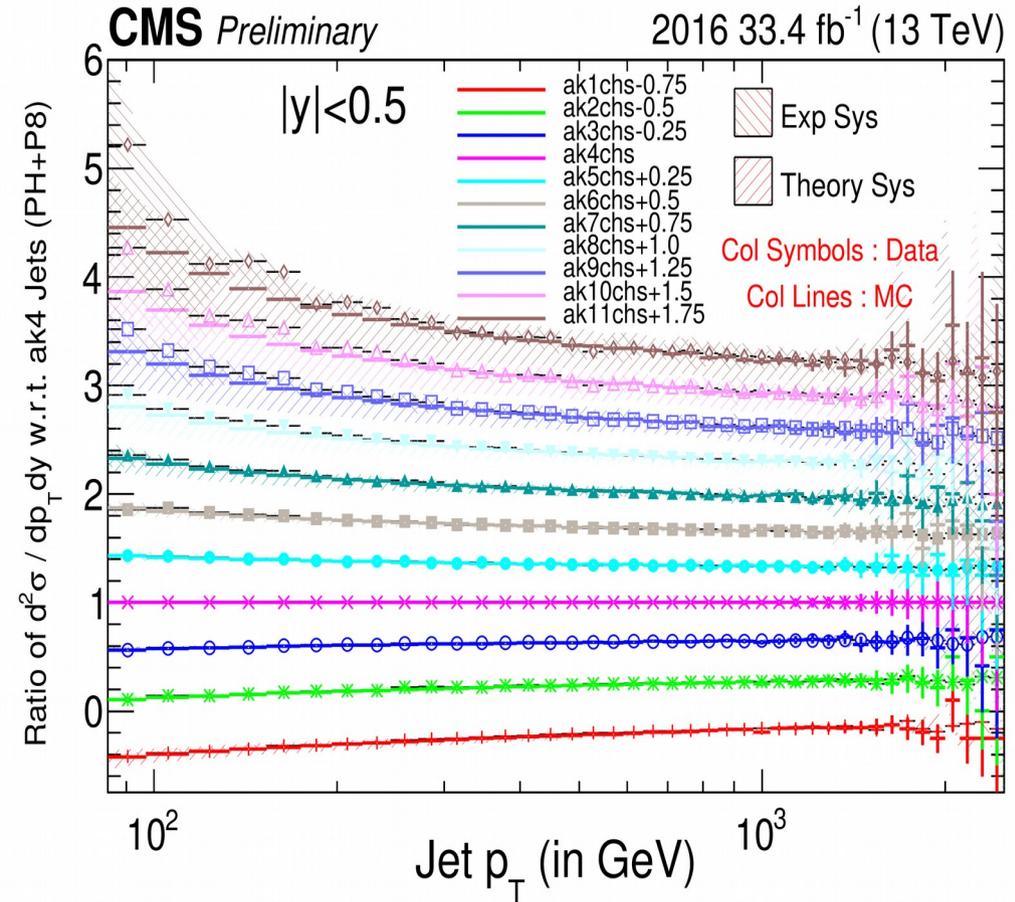
# Cross-Section Ratio of Different Jet Sizes

at  $\sqrt{s} = 13$  TeV

: Power of Ratio



Data & Powheg+Herwig++

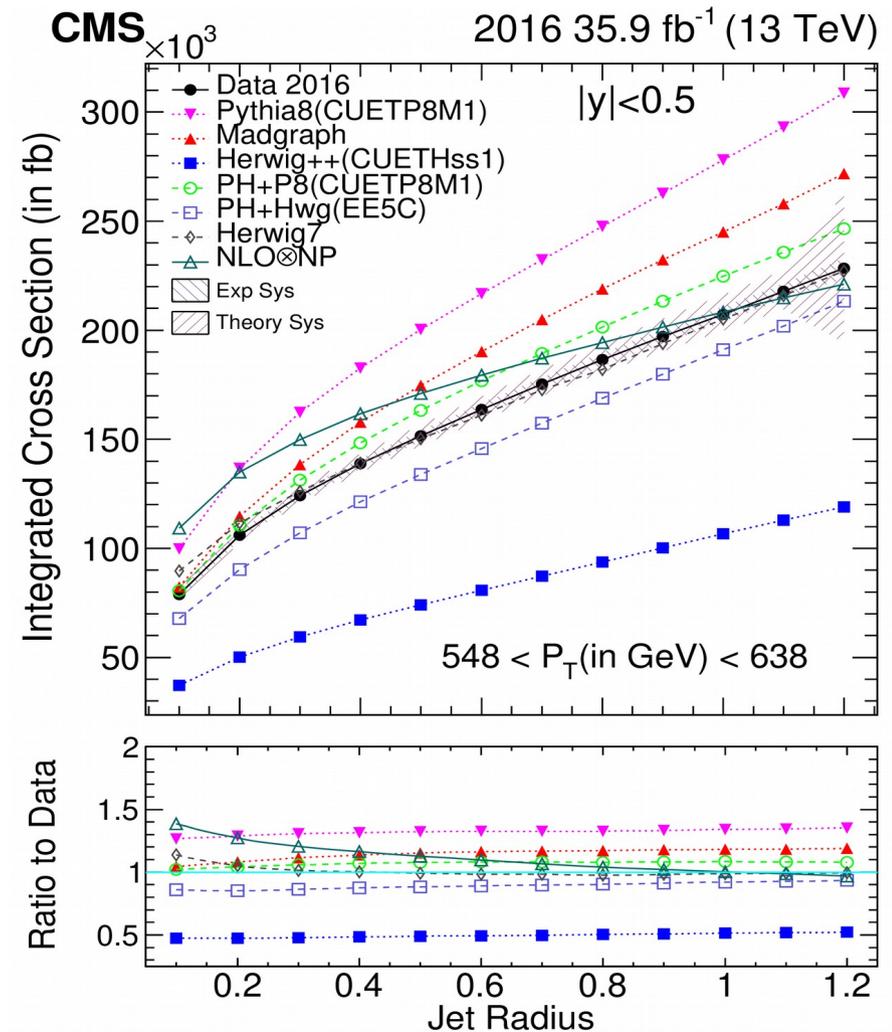
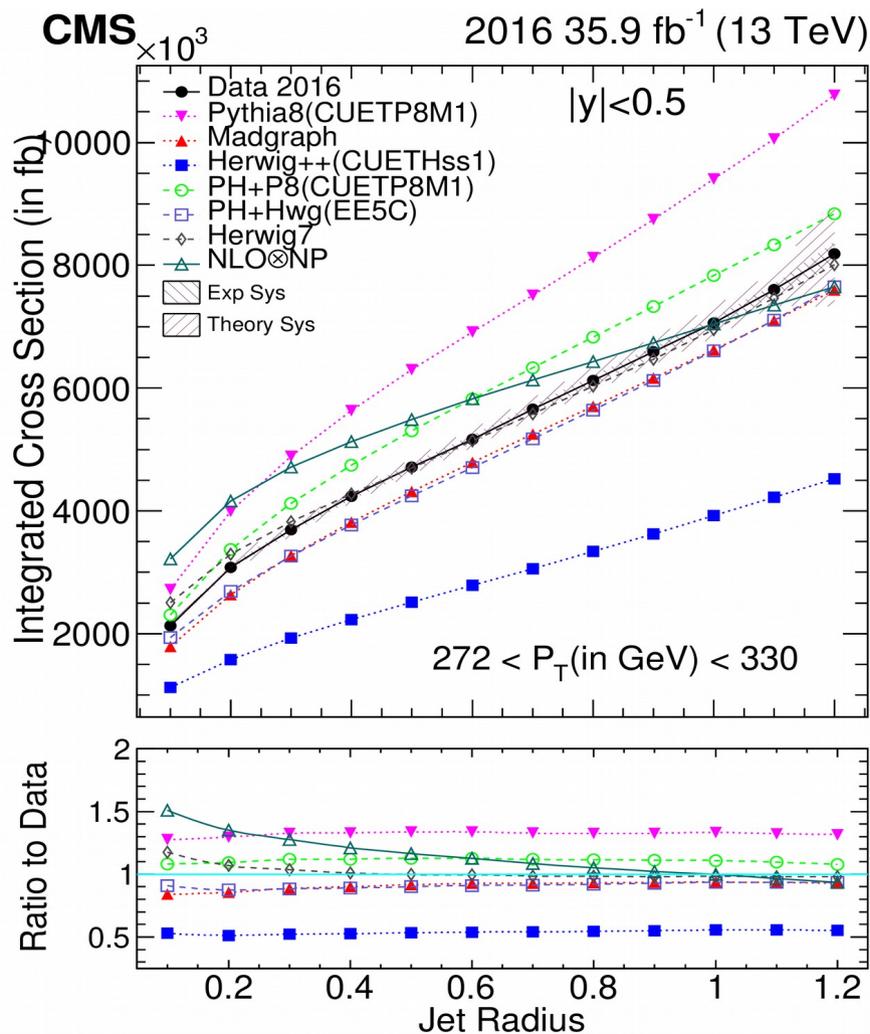


Data & Powheg+Pythia8

- Ratio is taken w.r.t. AK4 jets
- Powheg augmented with Pythia8 describes ratio for smaller jets better<sub>16</sub> & Powheg+Herwig++ is optimum for large radius jets

CMS private

# Integrated Cross-Section of Different Jet Sizes at $\sqrt{s} = 13$ TeV



Fixed order prediction (NLOJet++) is unable to describe the trend as a function of jet size :  
Need of resummation and higher order correction at low R

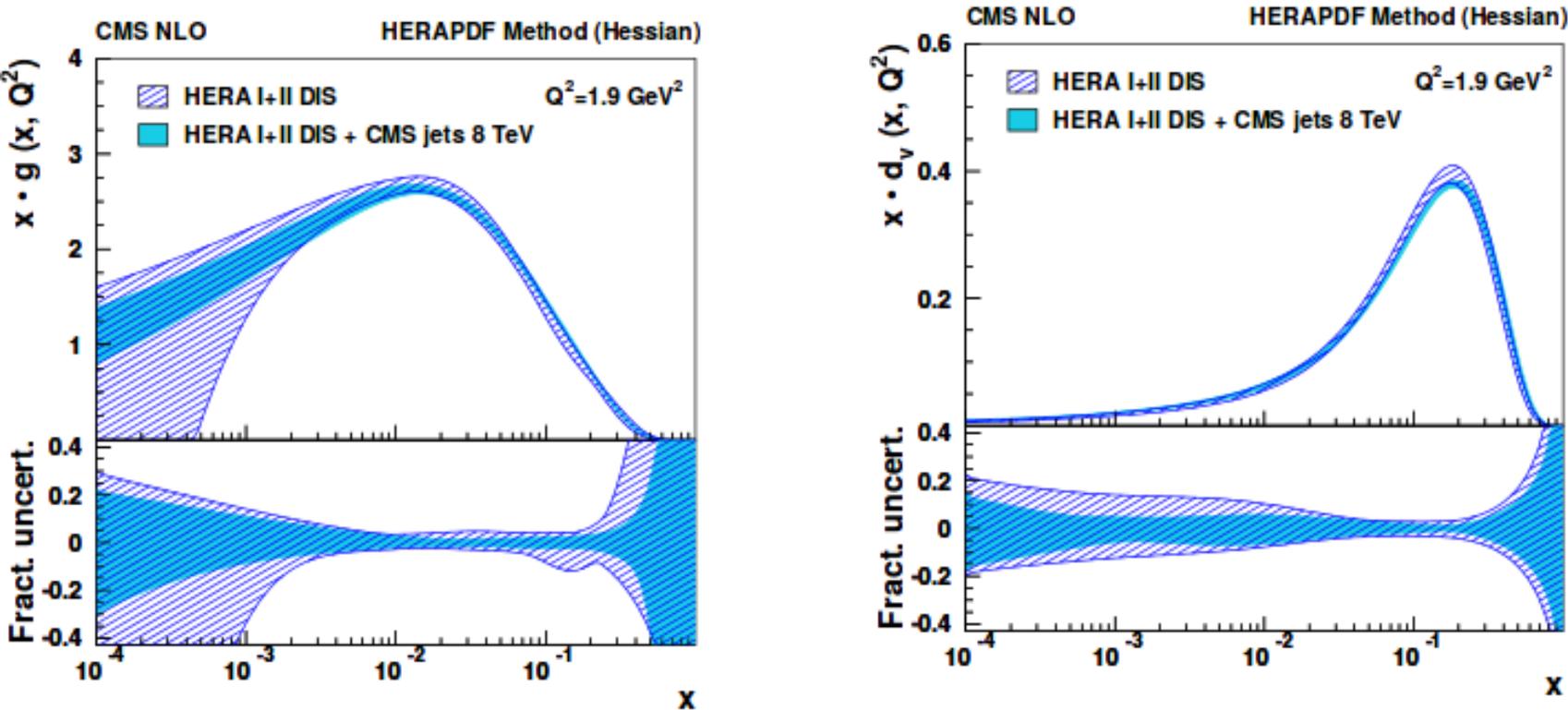
NLO Powheg with Pythia8 / Herwig++ PS are much closer to data than P8/Hwg alone : still on the opposite sides

MC generators supplemented by parton shower can describe the cross-section variation with jet size : parton shower helps!

# Impact of Inclusive Jets on PDF

- Dominated by  $gg \rightarrow gg$  at low  $p_T$ ,  $qg \rightarrow qg$  at medium  $p_T$  &  $qq \rightarrow qq$  at high  $p_T$   $\Rightarrow$  quark & gluon PDFs are sensitive

Low  $Q^2$



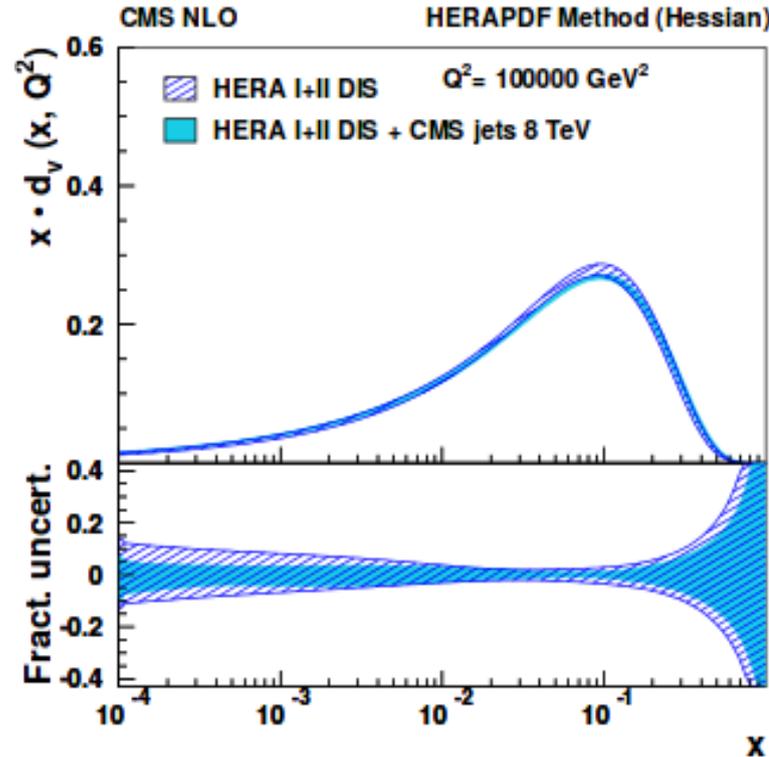
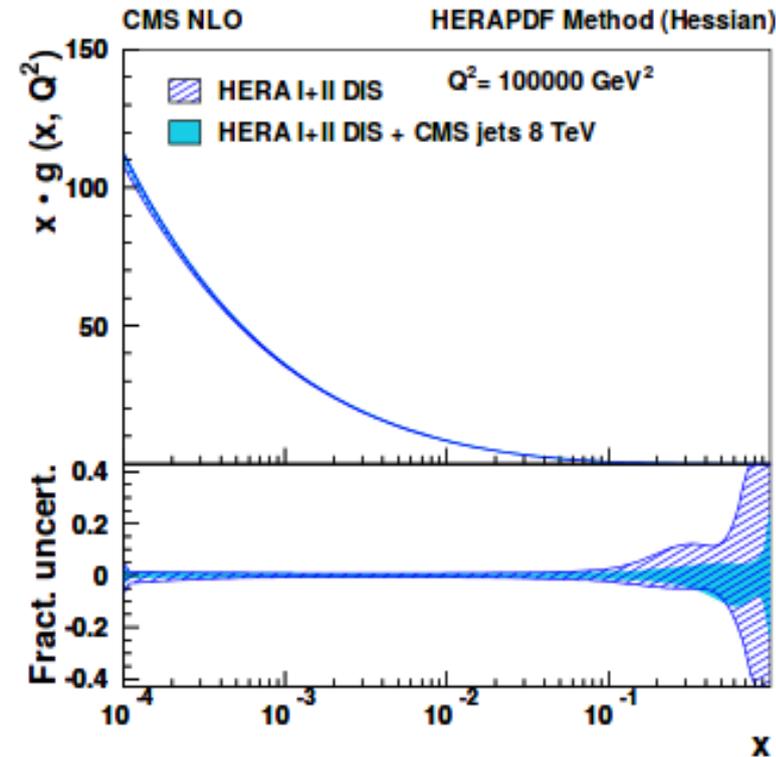
Using HERAFitter 1.1.1

- Significant reduction in uncertainty band for gluon both at low and high  $x$
- Improvement in valence d quark PDF in low  $x$  region

# Impact of Inclusive Jets on PDF

High  $Q^2$

- Dominated by  $gg \rightarrow gg$  at low  $p_T$ ,  $qg \rightarrow qg$  at medium  $p_T$  &  $qq \rightarrow qq$  at high  $p_T$   $\Rightarrow$  quark & gluon PDFs are sensitive



- Description of gluon improves at large  $x$   
.... Useful for BSM search ;)

# Determination of Strong Coupling Constant using Inclusive Jets

$$\frac{d\sigma}{dp_T} = \alpha_S^2(\mu_R) \hat{X}^{(0)}(\mu_F, p_T) [1 + \alpha_S(\mu_R) K1(\mu_R, \mu_F, p_T)]$$

NLO prediction

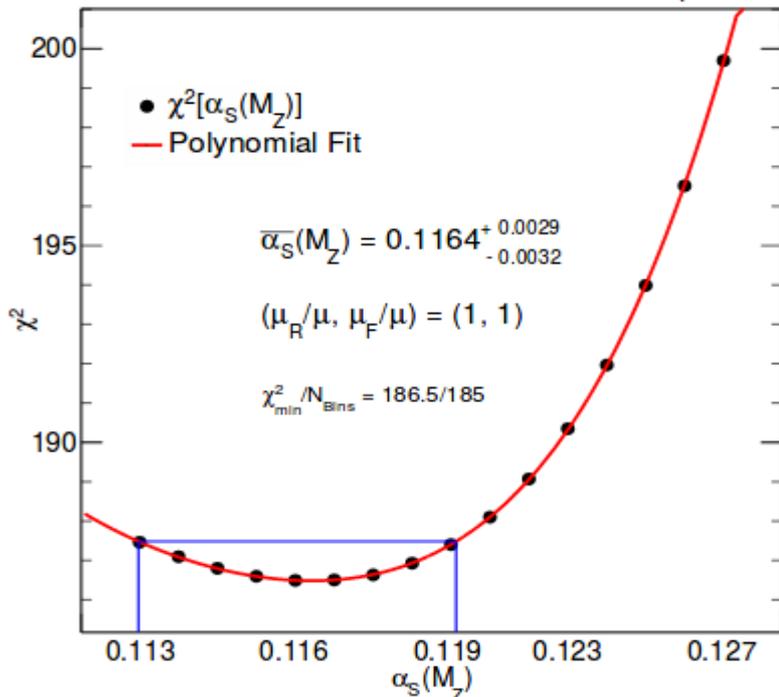
$$\chi^2(\alpha_S(M_Z)) = (D - T(\alpha_S(M_Z)))^T C^{-1} (D - T(\alpha_S(M_Z)))$$

$$C = C^{\text{stat}} + C^{\text{unfolding}} + \sum C^{\text{JES}} + C^{\text{uncor}} + C^{\text{lumi}} + C^{\text{PDF}} + C^{\text{NP}}$$

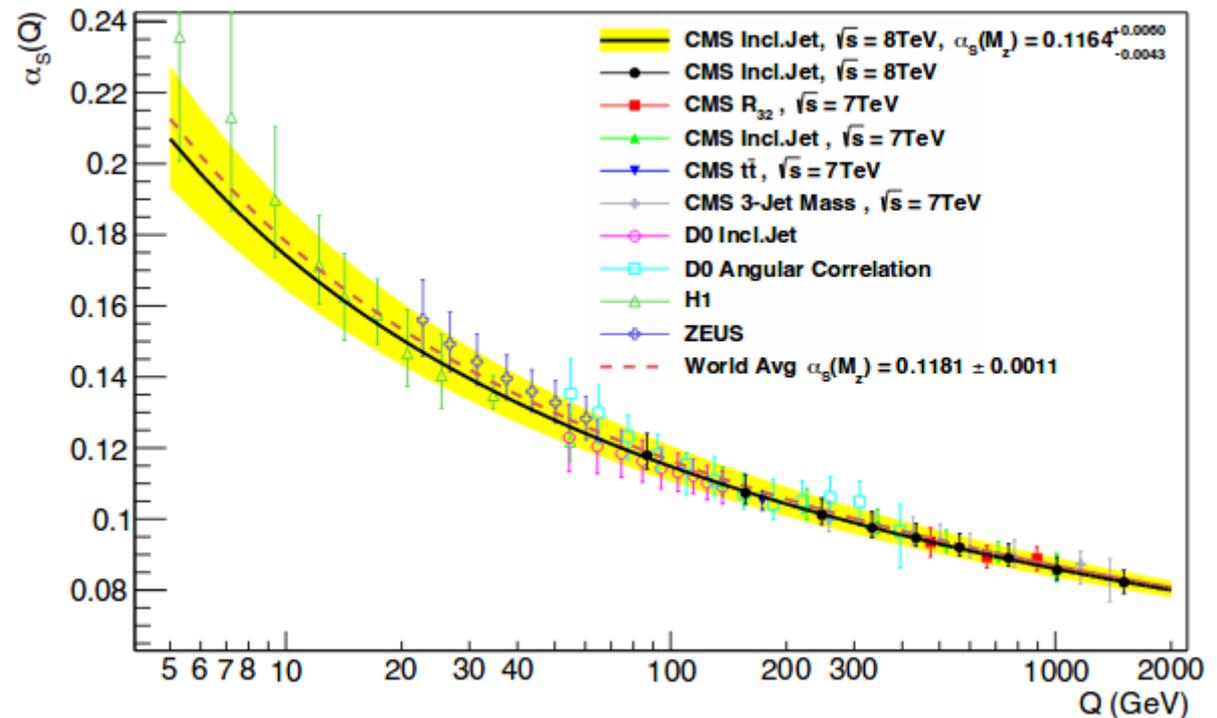
- $\chi^2$  has been computed between NLO prediction (with CT10 PDF) and measured data in both exclusive and inclusive  $p_T$  &  $\gamma$  bins with different choices of  $\alpha_S(M_Z)$  (in steps of 0.001 with range 0.112-0.127)
- $\alpha_S$  is determined in 9 bins in  $p_T$  range 74-2500 GeV (uncertainty from  $\Delta\chi^2 = 1$ )  
 $Q$  : x-section reweighted bin centre ( $\alpha_S(M_Z)$  evolved to  $Q$  scale using 2 loop 5F RG)

arXiv:1609.05331

CMS 19.7 fb<sup>-1</sup> (8TeV)



CMS



# Jet Mass at 13 TeV : Massive Story

- Jet mass is the most commonly used observable to discriminate jets containing heavy objects from QCD & in BSM searches

CMS SMP-2016-010

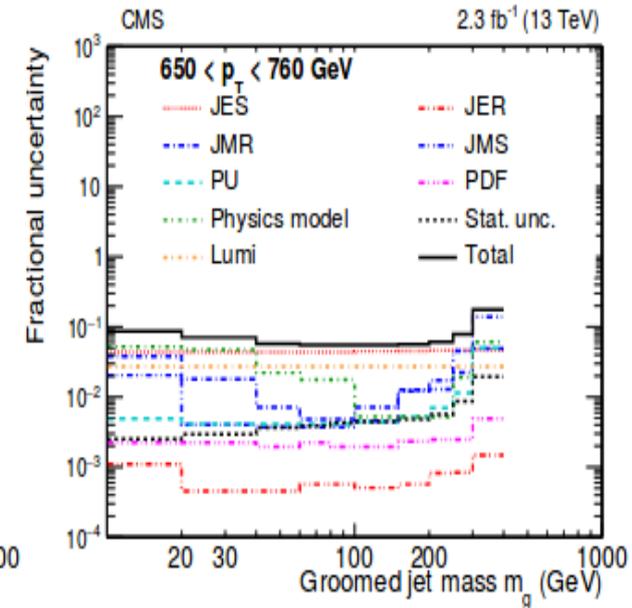
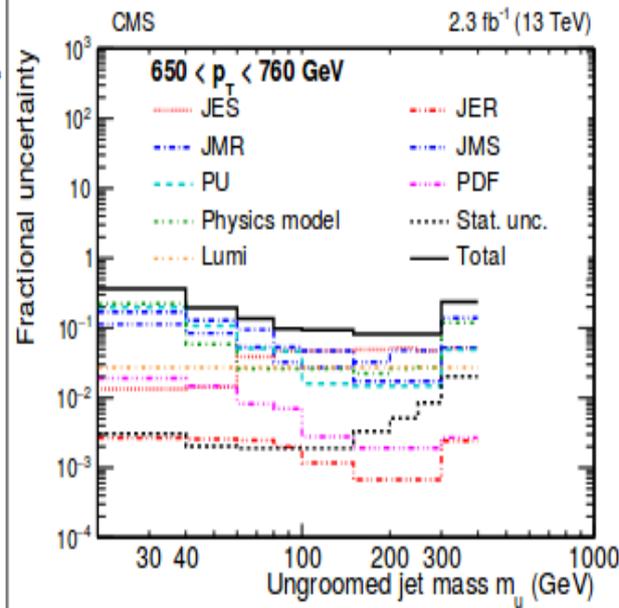
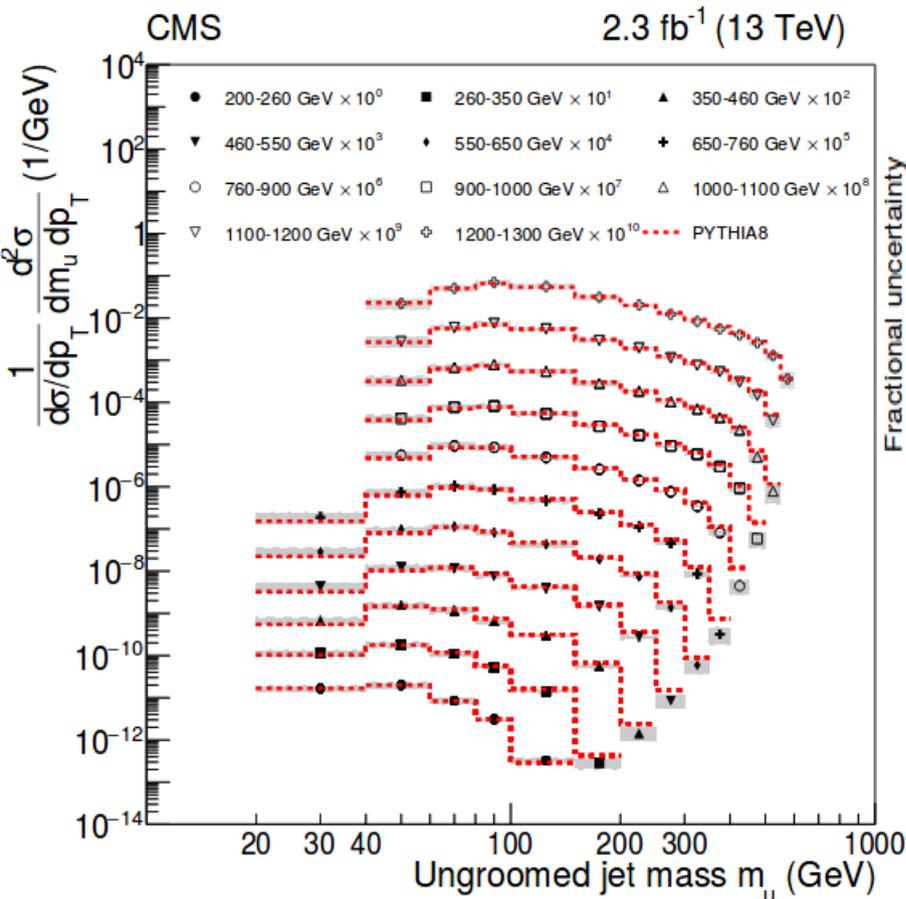
- In QCD, jet mass arises from radiation :  
Sensitive to dynamics of QCD evolution starting from a parton

- Radiation from partons exited from jet cone adds NGL : hard to compute =>  
Use Soft Drop grooming to get rid of NGL

Event Selection:

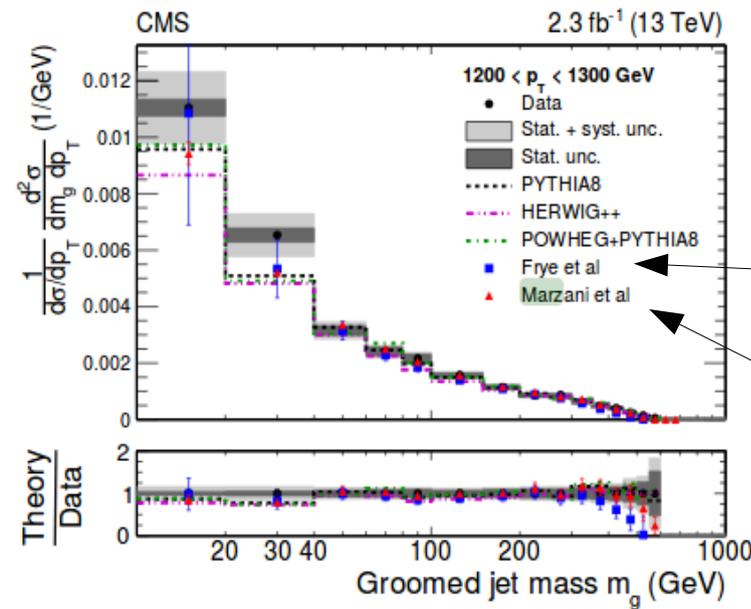
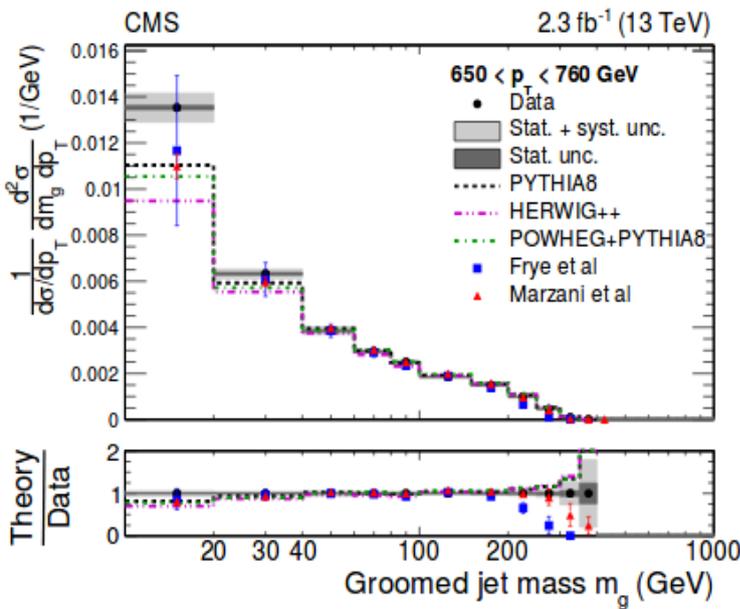
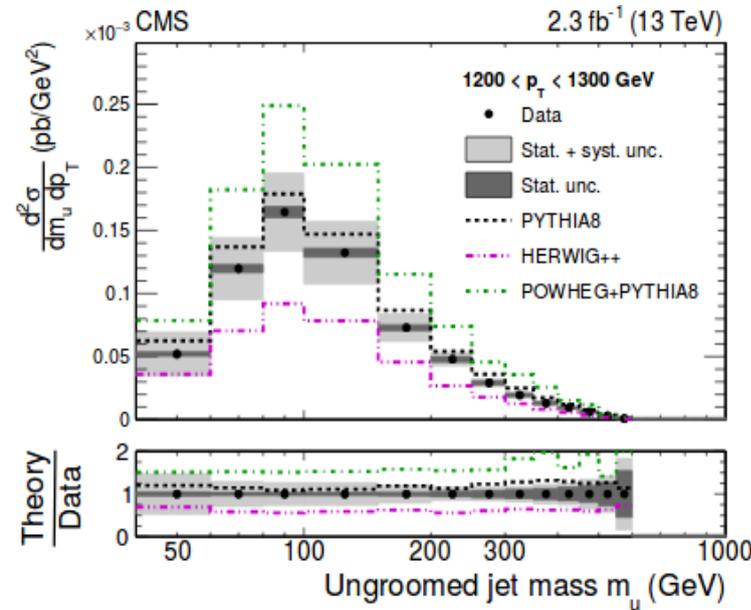
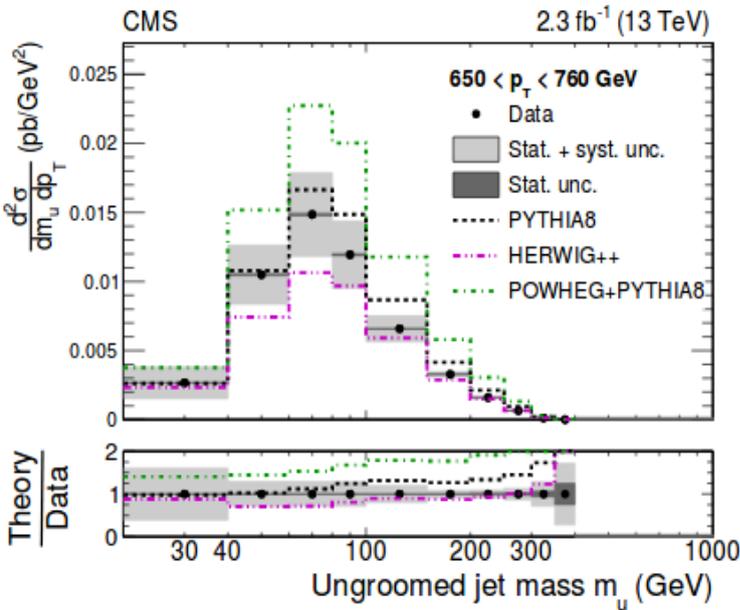
At least 2 AK8 jets,  $p_T > 200$  GeV,  $|y| < 2.4$  &

$$(p_{T1} - p_{T2}) / (p_{T1} + p_{T2}) < 0.3, \Delta(\phi_1 - \phi_2) > \pi/2.$$



With grooming, PU sensitivity is reduced  
Also modelling uncertainty is reduced  
as Soft Drop removes soft gluons (hard to model)

# Jet Mass at 13 TeV : Massive Story



Powheg + PYTHIA8 is unable to describe jet mass dist in data (for absolute x-section)

PYTHIA8 seems to be the best to predict distribution both for ungroomed & groomed jet mass

Analytic calculation can describe jet mass dist in data (for normalised x-section)

LO + NNLL (using SCET)

NLO + NLL

- Sudakov peak disappears in soft drop mass distribution

# Event Shapes

- Measures geometrical properties of hadronic energy flow in an event (IRC safe)
- Sensitive to hard scattering & soft radiation, hadronisation, MPI
- Used to tune MC generators and parton shower (LEP data)
- Also used on jet to tag boosted objects
- For this talk -
- **Thrust** :

Choose axis ( $\hat{n}_T$ ) maximizing  
the numerator

$$T_{\perp} \equiv \max_{\hat{n}_T} \frac{\sum_i |\vec{p}_{T,i} \cdot \hat{n}_T|}{\sum_i p_{T,i}}$$

$$\tau_{\perp} \equiv 1 - T_{\perp}$$

- **Broadening** :

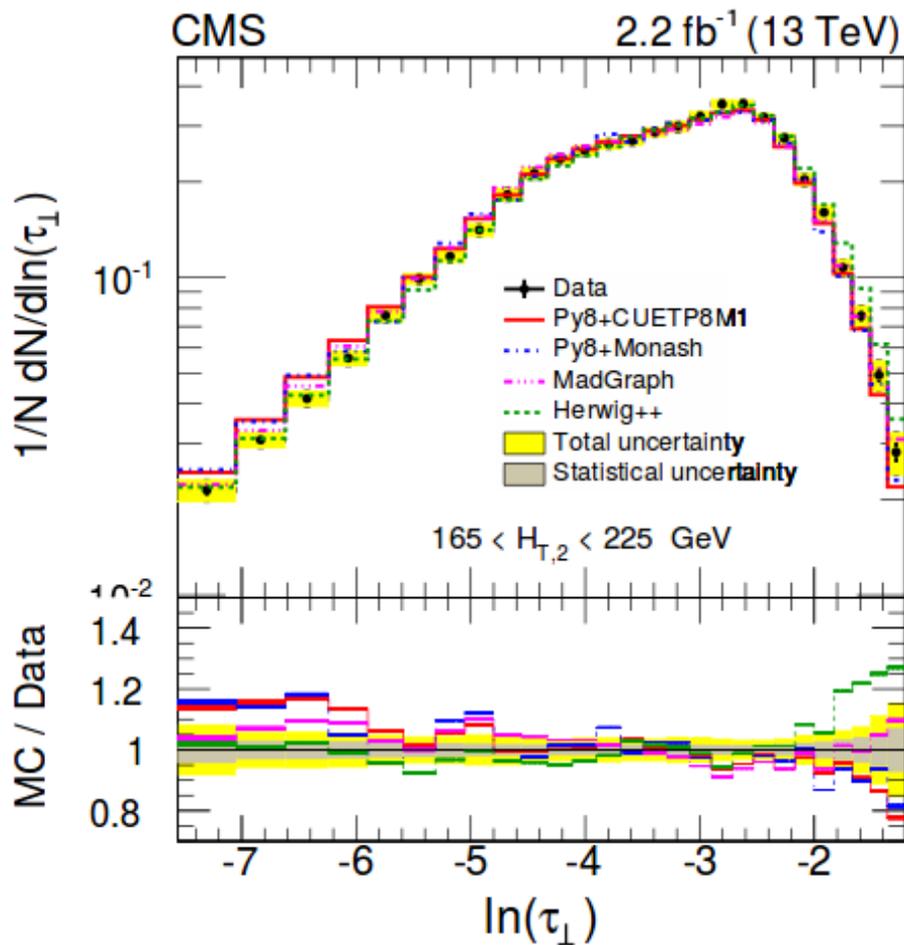
Thrust axis ( $\hat{n}_T$ ) divides the event  
into upper (U) and lower (L) regions  
(denoted commonly by X)

$$\eta_X \equiv \frac{\sum_{i \in X} p_{T,i} \eta_i}{\sum_{i \in X} p_{T,i}}, \quad \phi_X \equiv \frac{\sum_{i \in X} p_{T,i} \phi_i}{\sum_{i \in X} p_{T,i}}$$

$$B_X \equiv \frac{1}{2P_T} \sum_{i \in X} p_{T,i} \sqrt{(\eta_i - \eta_X)^2 + (\phi_i - \phi_X)^2}$$

$$B_{\text{Tot}} \equiv B_U + B_L$$

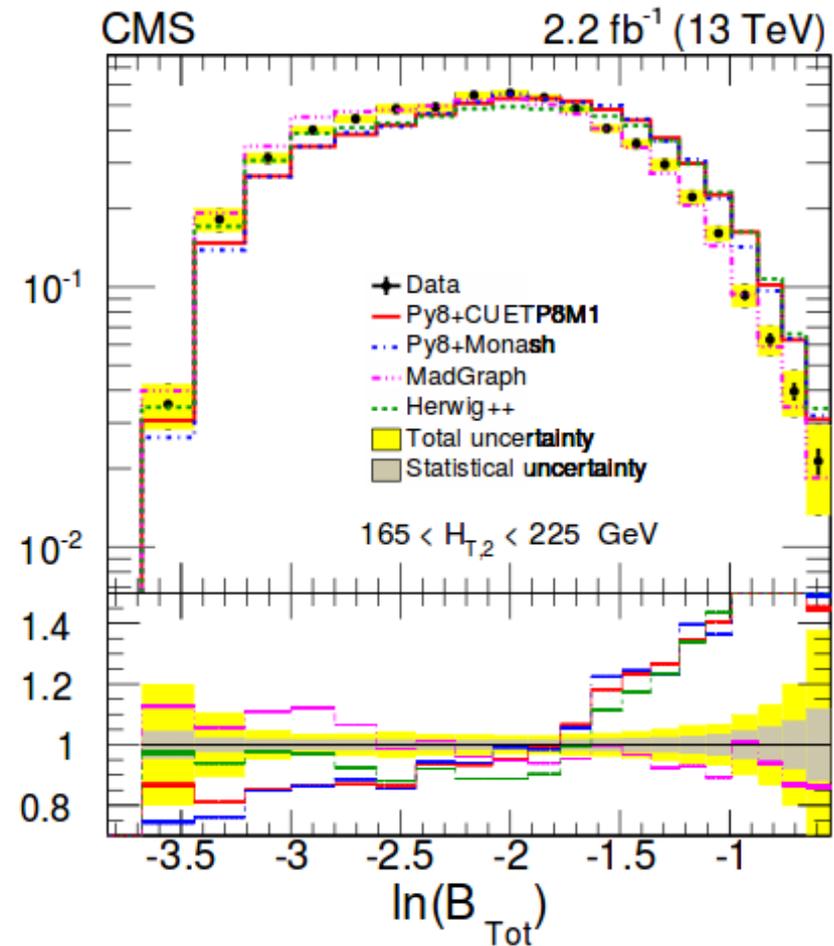
# Event Shapes : Data-MC Comparison



Sensitive to energy flow  
in transverse plane

Different tunes of pythi8  
agree well =>  
less sensitive to MPI tuning

Pythia8 moderately describes  
Energy flow in transverse plane  
But fails for out of plane flow



Use transverse and longitudinal  
components equally

Herwig++ & Madgraph describes  
the full event structure better

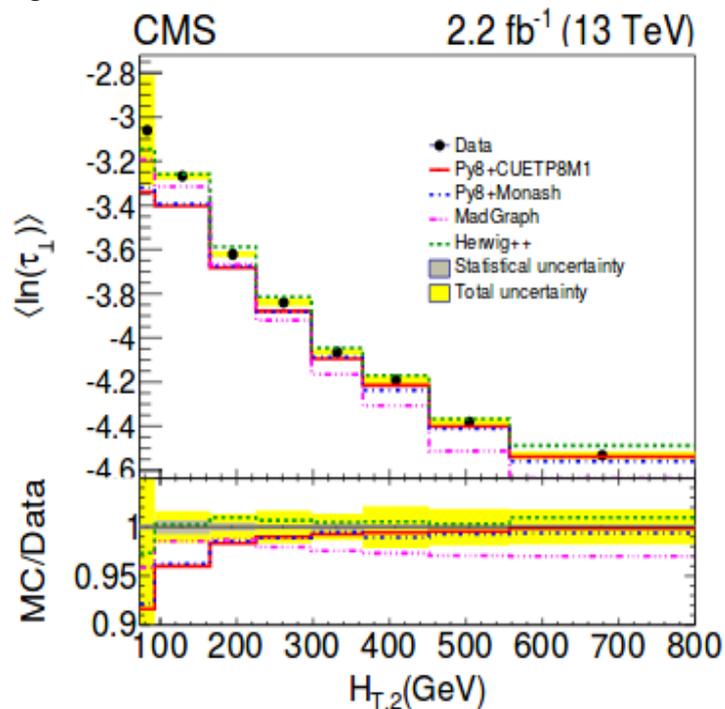
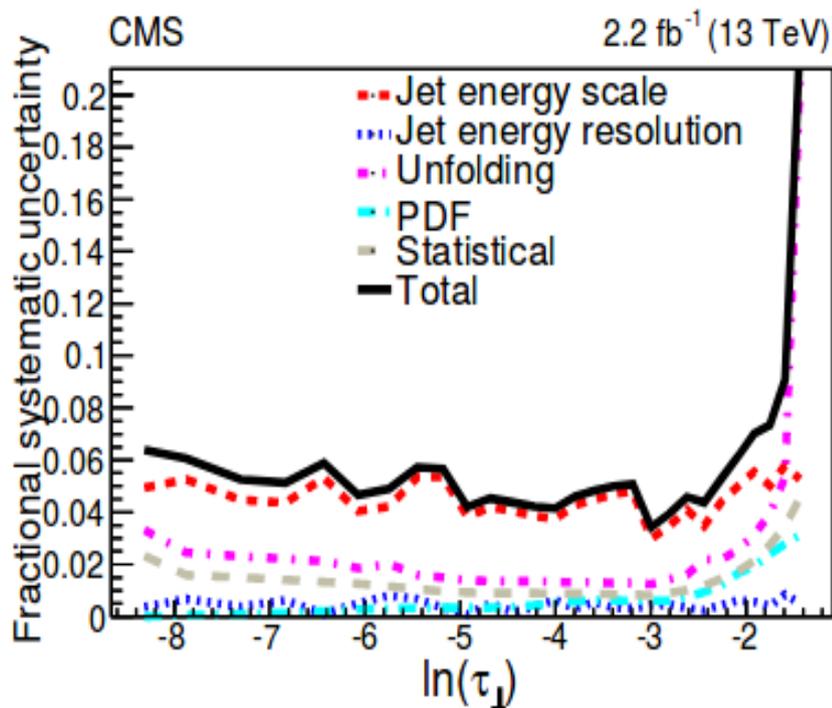
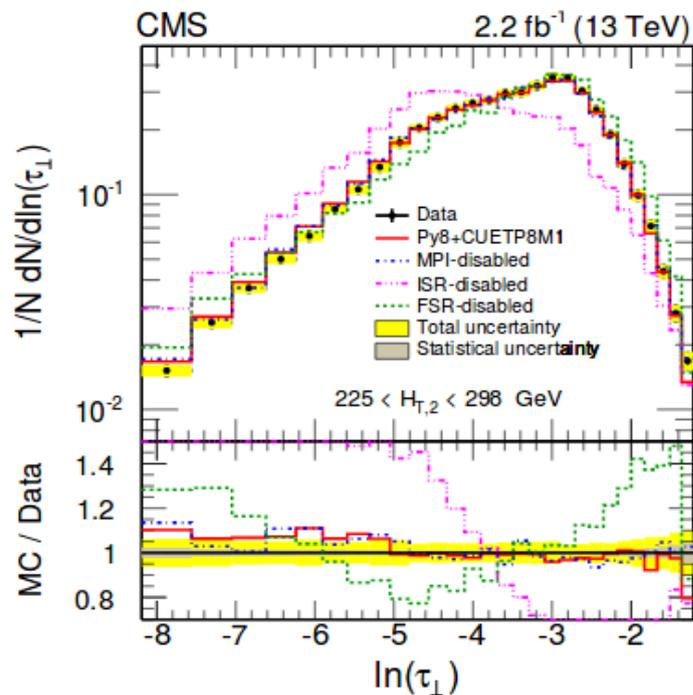
CMS-SMP-17-003

# Event Shapes : Systematics

ISR has significant effect to predict even-shape

FSR moderately affects the prediction

Sensitivity is very small for MPI

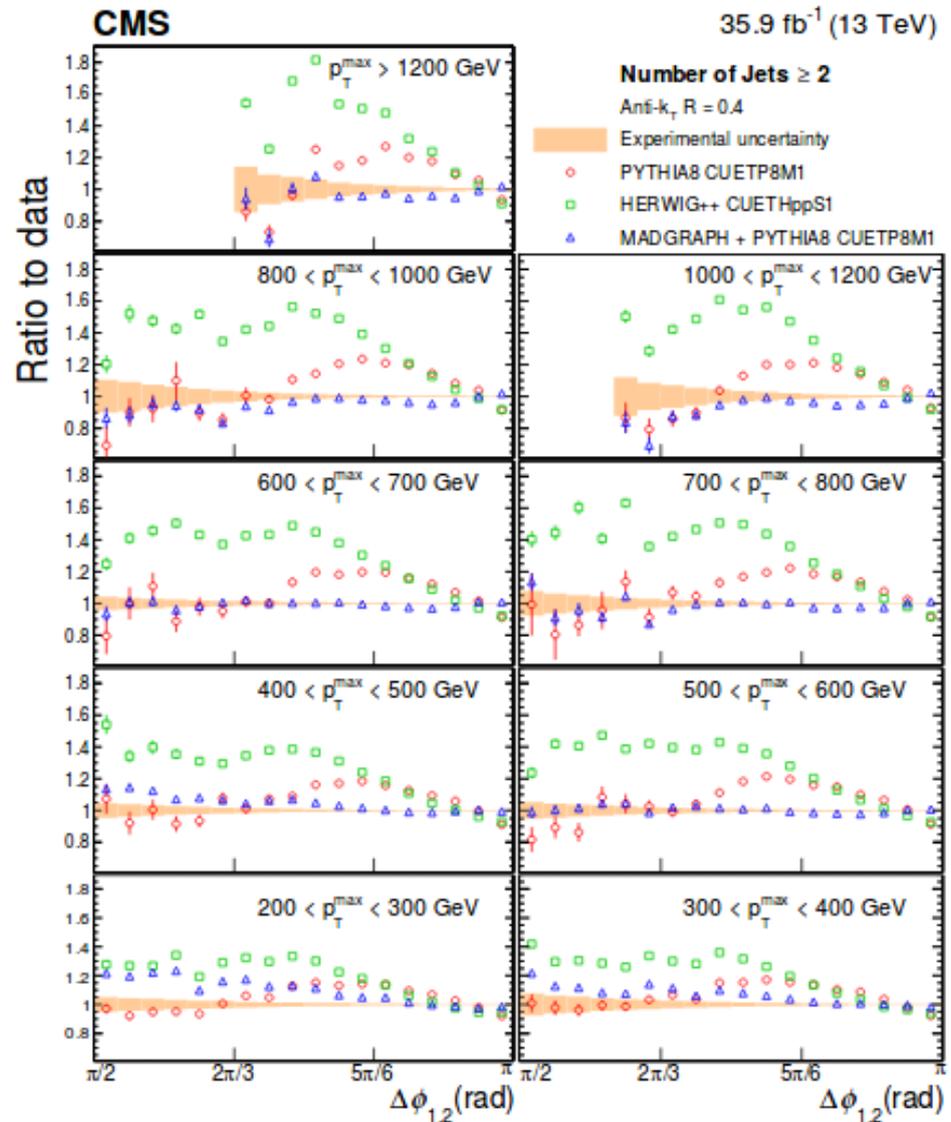
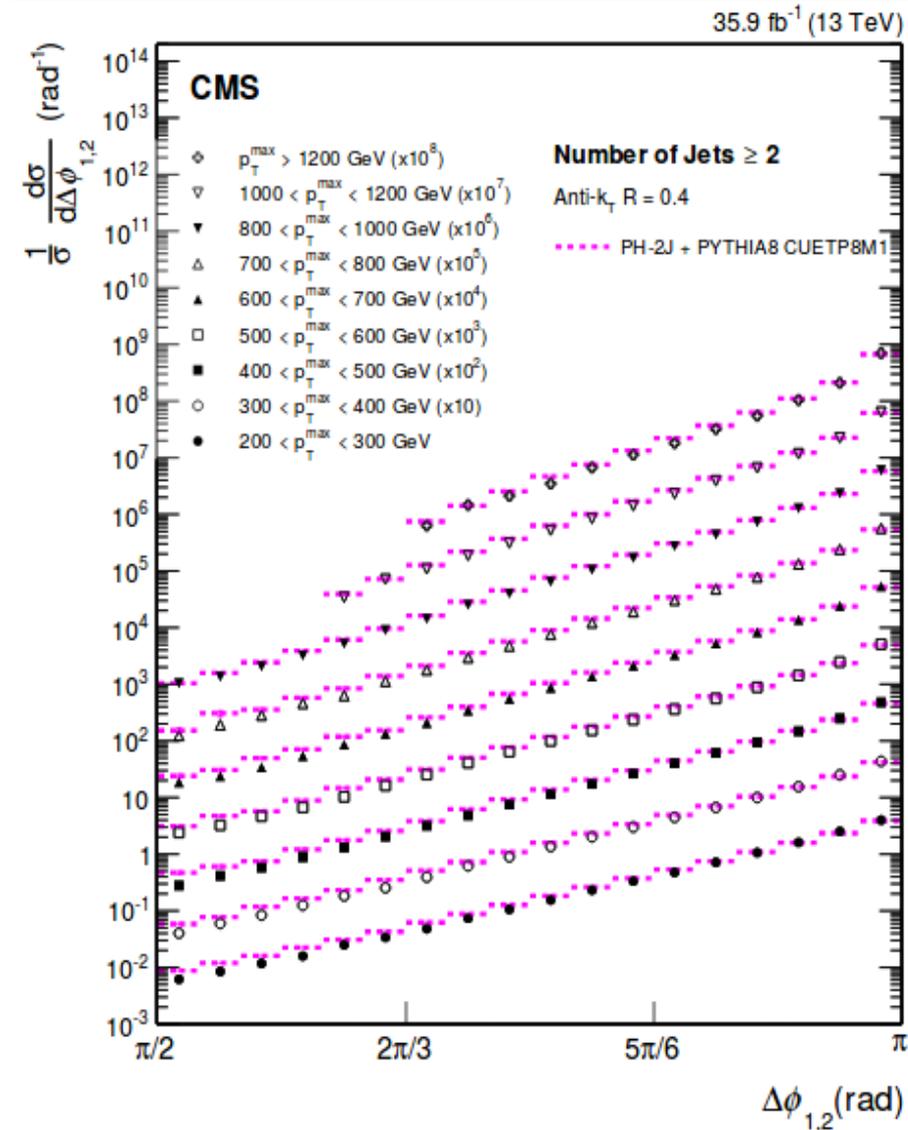


Very small theory uncertainty,  
jet energy calibration dominates the systematics

In highly energetic phase space,  $\alpha_s$  is smaller, less radiation  
=> event tends to dijet topology

# Dijet Azimuthal Correlation

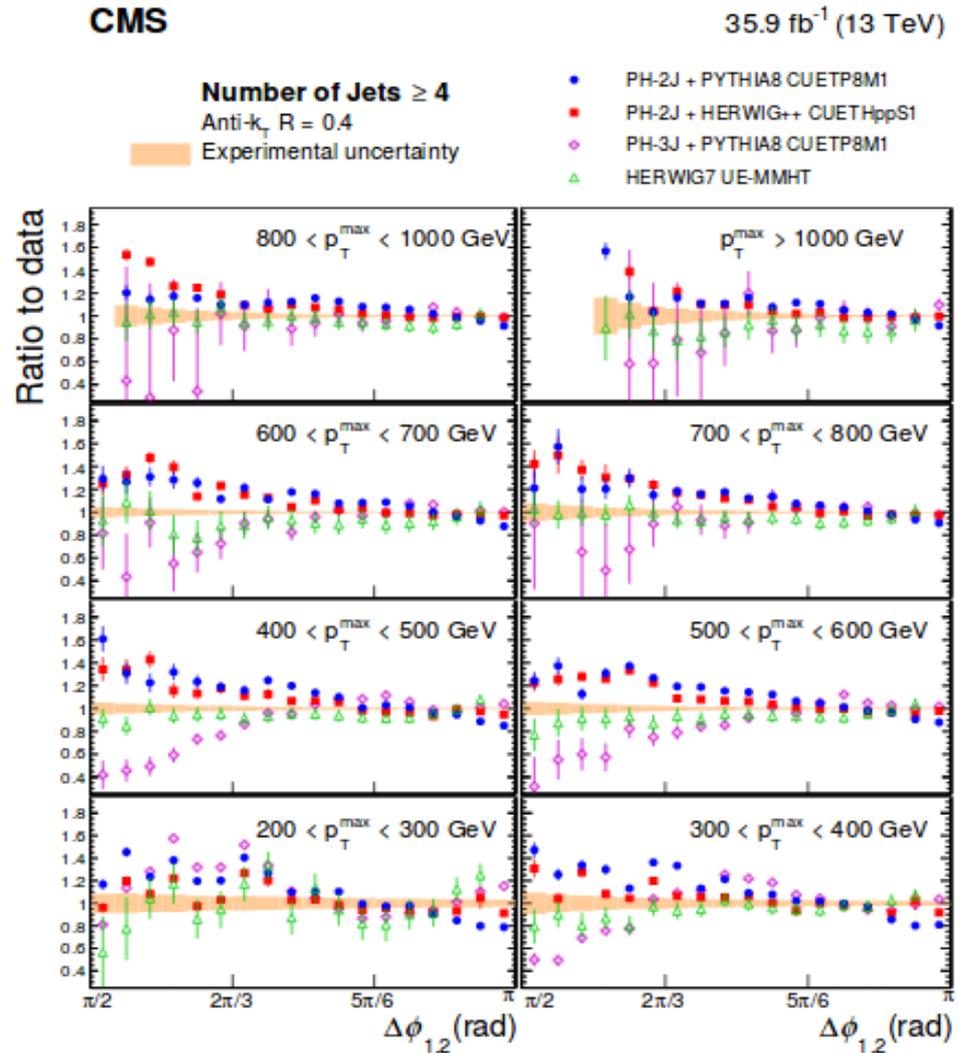
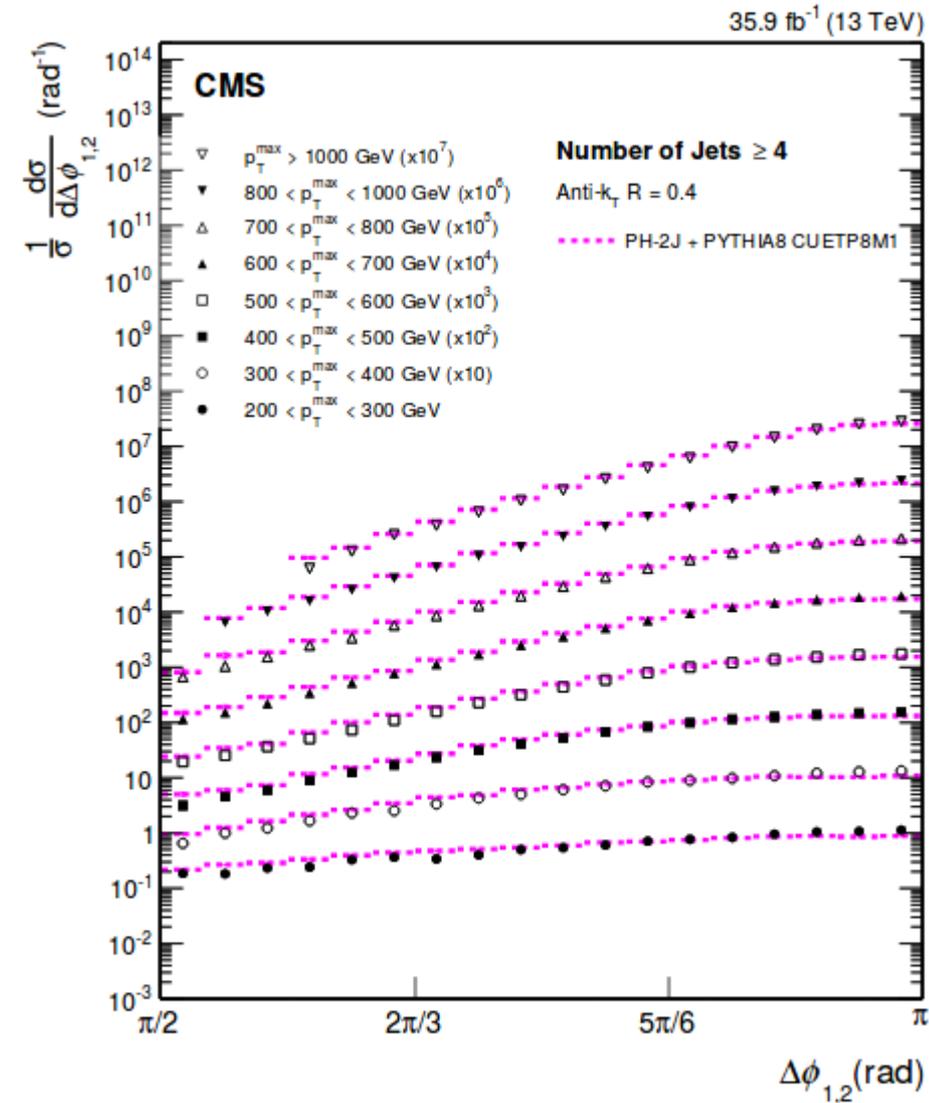
- Sensitive to radiation from hard leg & correlation between jets



- Choice of MC generator is crucial to describe the data
- Jet size also plays a threshold on lower side of  $\Delta\phi$

# Dijet Azimuthal Correlation

- Sensitive to radiation from hard leg & correlation between jets



- Even NLO generator is unable to describe data in parts of phase space
- Herwig7 (NLO generator + PS from Herwig++) performs best

# Conclusion

- CMS has a wealth of results on inclusive jets (many more to come)
- Inclusive jets have been established as a powerful tool to understand QCD, measure  $\alpha_s$ , constrain PDFs, ...
- Better calibration helps to make measurements more precise
- Experimental uncertainty is similar or less than theoretical uncertainty
- Fixed order NLO prediction (with NP & EW correction) describes large jets almost all over the phase space
- NLO+PS are found to make better prediction for small R jets, angular correlation and also for the cross-section ratio of two jet sizes
- Motivates higher order calculation with resummation to be **the state-of-the-art**

THANK YOU!

# More Material ..

# Impact of Inclusive Jets on PDF

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} (1 + E_g x^2) - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + D_{u_v} x + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}} (1 + D_{d_v} x),$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}} (1 + D_{\bar{D}} x + E_{\bar{D}} x^2).$$

• [arXiv:1609.05331](https://arxiv.org/abs/1609.05331)

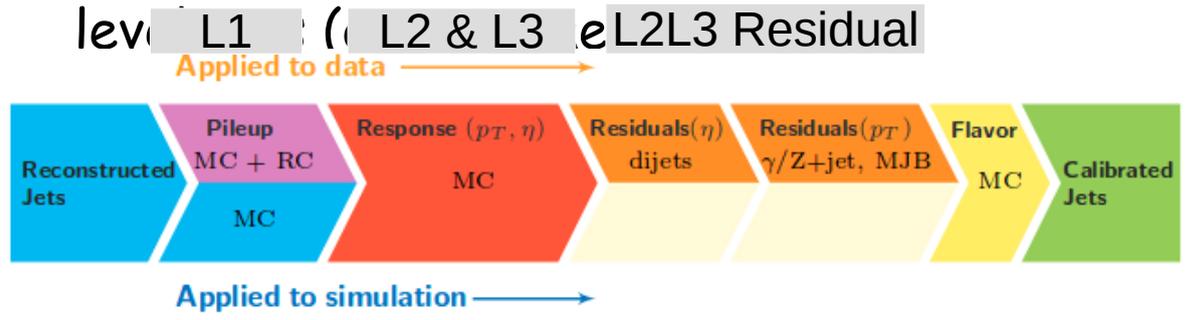
$$\alpha_S(\hat{M}_Z) = 0.1185^{+0.0019}_{-0.0021} (\text{exp})^{+0.0002}_{-0.0015} (\text{model})^{+0.0000}_{-0.0004} (\text{param})^{+0.0022}_{-0.0018} (\text{scale})$$

•

- For PDF Experimental uncertainty using Hessian method  
Modelling uncertainty from b-mass, c-mass,  $Q_{\min}$   
Parameterisation uncertainty from additional terms in function

# Jet Energy Calibration : Prep for Measurement

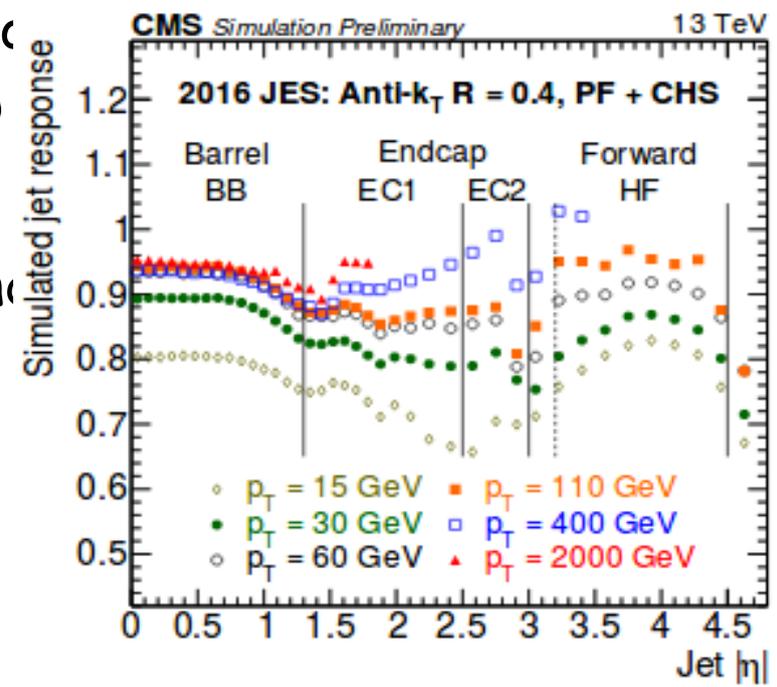
- Cross-section measurement depends crucially on energy calibration (steep spectra → mis-measurement leads to bin migration)
- Factorised approach to match energy scale of detector level jets to particle level



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- Pile-up subtraction by removing tracks coming from neutrals by hybrid area-subtraction using pile-up method
- Correction as a function of jet pseudorapidity and based on simulation

Stable response  
In barrel,  
Requires pt dependent  
Correction in EC & HF

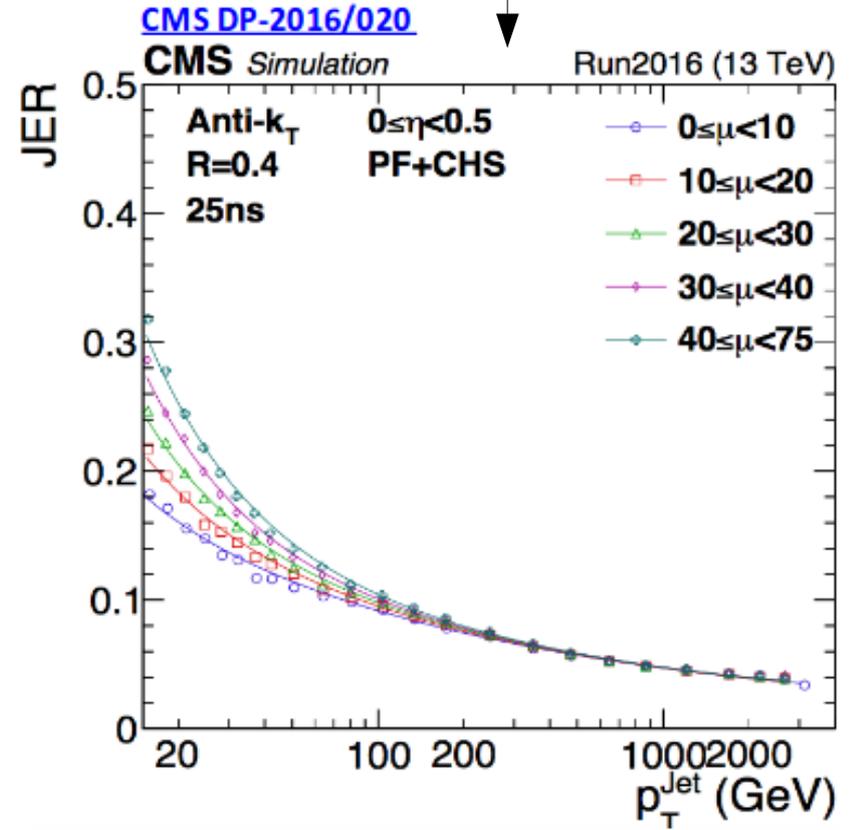
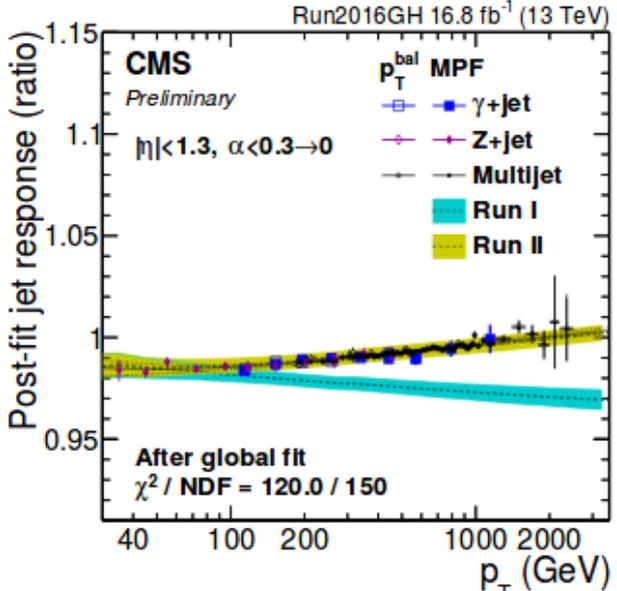
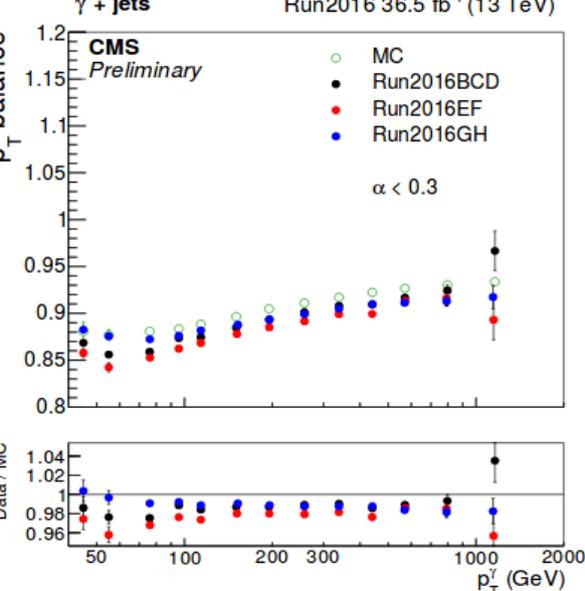
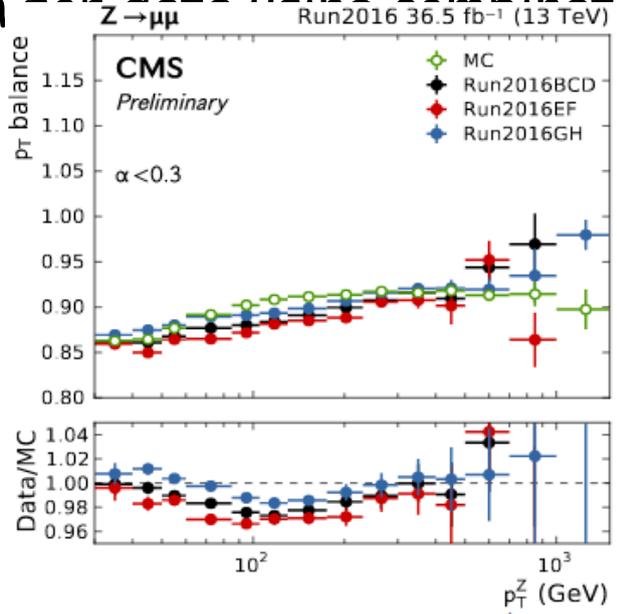
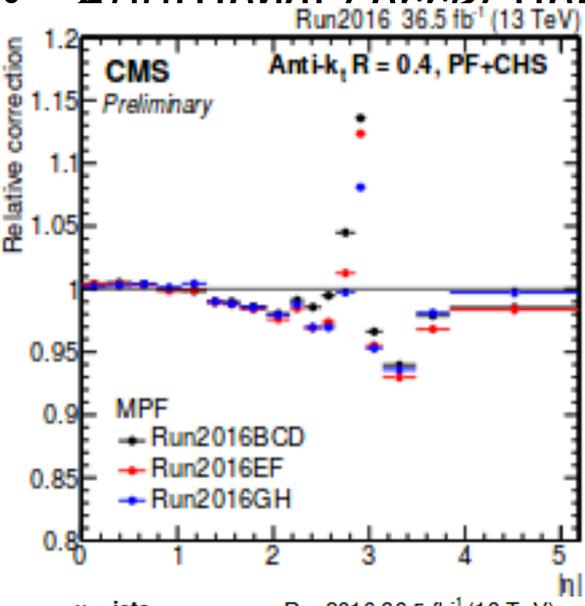


# Jet Energy Calibration & Resolution

- Response correction as a function of  $\eta$  by balancing dijet / minimising MET (MPF)
- Absolute scale correction using photon+jet, Z+jet balance
- Additional correction for data using combination of photon+jet, Z+jet, multijet

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Effect of Pile up below  $p_T < 100$  GeV

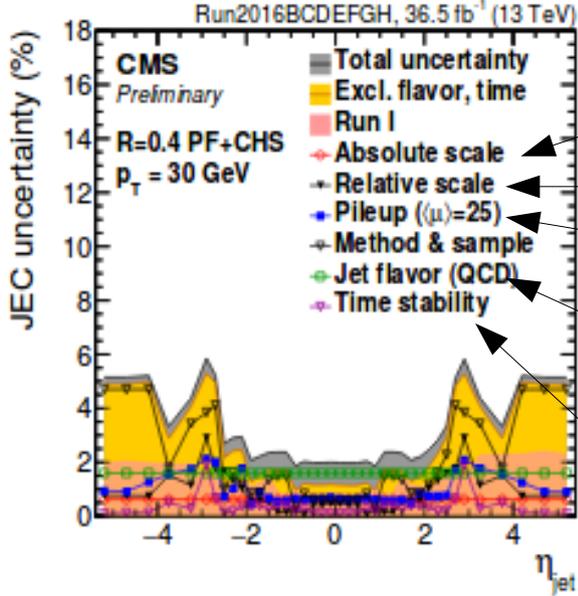
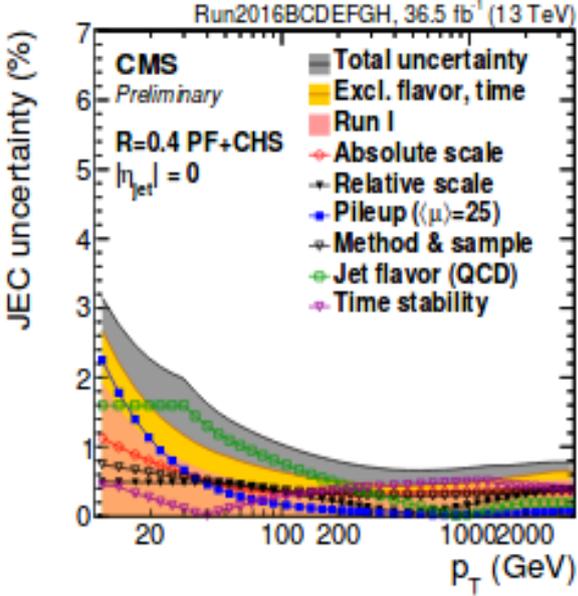


# Uncertainty Jet Energy Calibration

- Normally below 1-2% in the phase space used for differential cross-section measurement

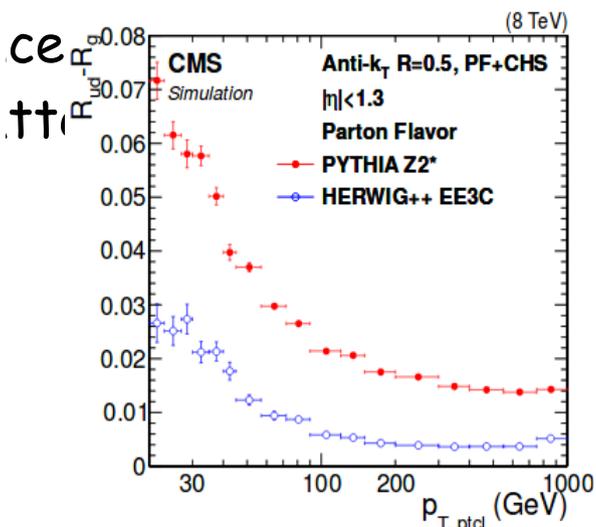
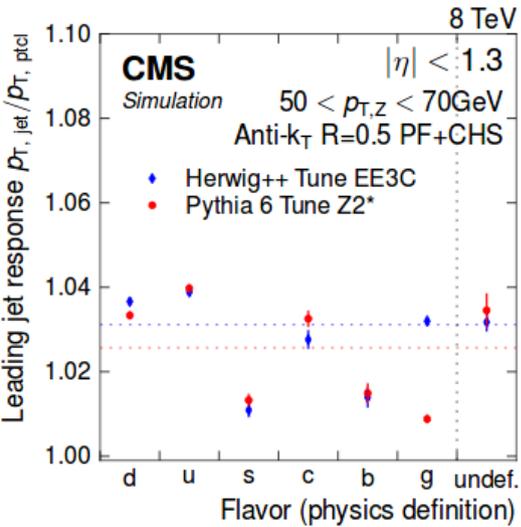
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## Uncertainty Components:



Combined  $\gamma$ , Z $\rightarrow$  ee, Z $\rightarrow$   $\mu\mu$  reference scale & ISR-FSR  
 JER SF & ISR-FSR  
 Bias from residual offset

PYTHIA8 / HERWIG++ difference for parton response after data-based JEC  
 Closure of lumi weighted correction per era



ion is crucial  
 rton shower)  
 CMS JME-2013-004