

(Mis-)aligned Winding in

A. Hebecker, D. Junghans, AS,
arXiv: 1812.05626

and

A. Cole, AS, G. Shiu,
arXiv: 1907.xxxx

applying Genetic Algorithms to



Type IIB String Theory



Large Field Ranges from (Mis-)aligned Winding

A. Hebecker, D. Junghans, AS: 1812.05626

A key motivation for thinking about Swampland is **inflation**

Important constraints are

- **(refined) Swampland Distance Conjecture (SDC)**

Kläwer, Palti: 1610.00010

Vafa: hep-th/0509212
Ooguri, Vafa: hep-th/0605264

- **Weak Gravity Conjecture (WGC)**

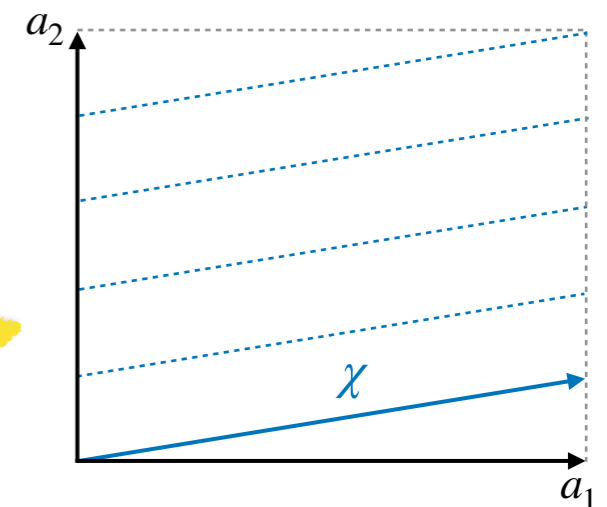
$$fS \lesssim q$$

Arkani-Hamed, Motl, Nicolis,
Vafa: hep-th/0601001

Typically forbid transplanckian decay constants, but several proposed loopholes...

Here: construct effective axionic trajectory χ
in **complex structure moduli space** of
type IIB flux compactifications

Kim, Nilles, Peloso:
hep-ph/0409138



Consider **Large Complex Structure Limit** for $U_1 = a_1 + iu_1$ and $U_2 = a_2 + iu_2$

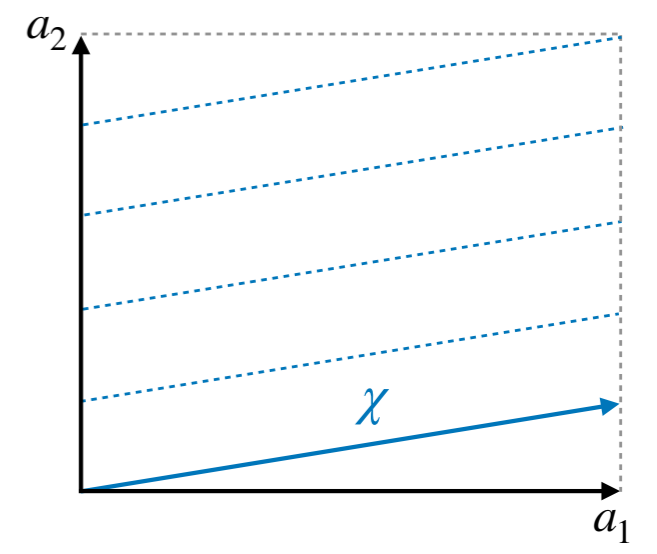
$\mathcal{K} \supset -\log \left[\mathcal{A}(Z, \bar{Z}, U_1 - \bar{U}_1, U_2 - \bar{U}_2) \right]$ $\xrightarrow{u_1, u_2 \gg 1}$ **shift symmetry:**
 Kähler potential ↑ ↑ ↑ complex structure moduli → a_1 and a_2 are axions

Align moduli via fluxes in the superpotential \rightarrow **Winding inflation** Hebecker, Mangat, Rompineve, Witkowski: 1503.07912

$\mathcal{W} = w(Z) + f(Z)(n_1 U_1 + n_2 U_2)$

see also Palti: 1508.00009, Baume, Palti: 1602.06517, Blumenhagen, Herschmann, Wolf: 1605.06299, 1704.04140

F-term conditions $\xrightarrow{\mathcal{W} \neq 0}$ $\frac{\mathcal{K}_{U_1}}{\mathcal{K}_{U_2}} = \frac{n_1}{n_2}$ $f(Z) + \frac{\mathcal{K}_{U_1}}{n_1} \mathcal{W} = 0$



Parametrise effective axionic trajectory χ $\rightarrow \begin{pmatrix} a_1 \\ a_2 \end{pmatrix} = \begin{pmatrix} -n_2 \\ n_1 \end{pmatrix} \chi$

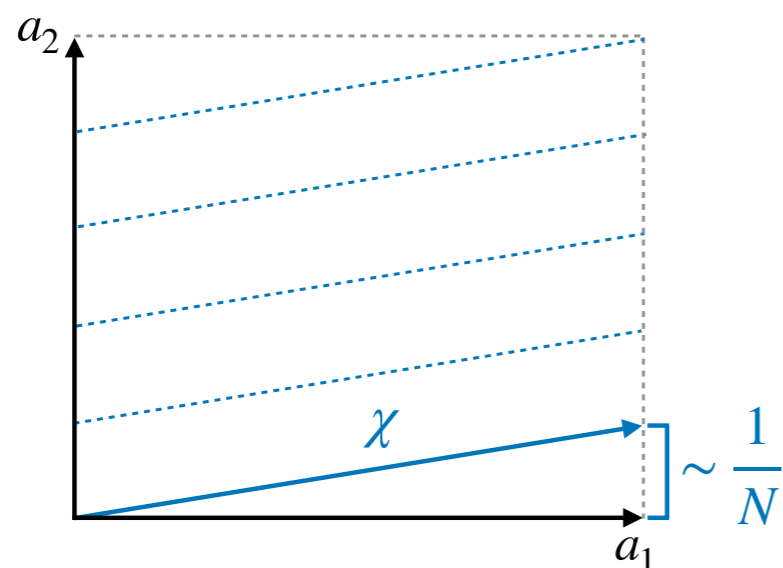
Effective axion decay constant and periods $f^2 = -n_2^2 \frac{\mathcal{A}_{11}}{\mathcal{A}} + 2n_1 n_2 \frac{\mathcal{A}_{12}}{\mathcal{A}} - n_1^2 \frac{\mathcal{A}_{22}}{\mathcal{A}}$ $\Pi_1 = \frac{f}{n_2}$ $\Pi_2 = \frac{f}{n_1}$

Notation: $\mathcal{A}_{11} = \partial_{U_1} \partial_{\bar{U}_1} \mathcal{A}$ etc. **Instanton actions:** $S_1 = u_1, S_2 = u_2$

$$\mathcal{W} = w(Z) + f(Z)(n_1 U_1 + n_2 U_2) \quad \frac{\mathcal{K}_{U_1}}{\mathcal{K}_{U_2}} = \frac{n_1}{n_2} \quad f^2 = -n_2^2 \frac{\mathcal{A}_{11}}{\mathcal{A}} + 2n_1 n_2 \frac{\mathcal{A}_{12}}{\mathcal{A}} - n_1^2 \frac{\mathcal{A}_{22}}{\mathcal{A}} \quad \Pi_1 = \frac{f}{n_2} \quad \Pi_2 = \frac{f}{n_1}$$

Aligned Winding

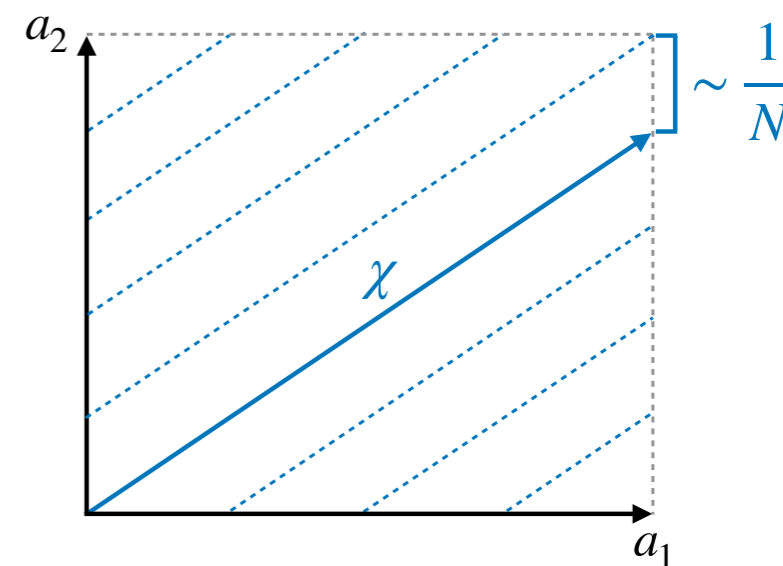
$$(n_1, n_2) \rightarrow (1, N) \quad N \gg 1$$



$$f^2 \leq 2N \frac{\mathcal{A}_{12}}{\mathcal{A}}$$

Misaligned Winding

$$(n_1, n_2) \rightarrow (N, N + 1) \quad N \gg 1$$

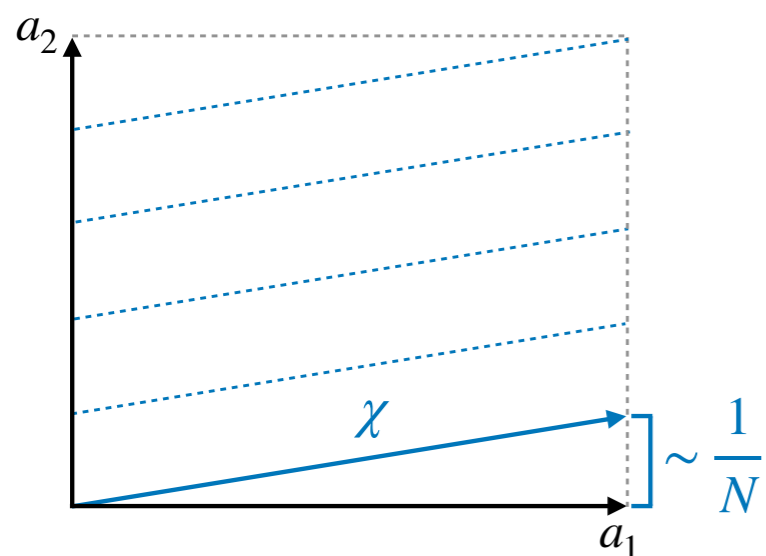


$$f^2 \leq 2N(N + 1) \frac{\mathcal{A}_{12}}{\mathcal{A}}$$

$$\mathcal{W} = w(Z) + f(Z)(n_1 U_1 + n_2 U_2) \quad \frac{\mathcal{K}_{U_1}}{\mathcal{K}_{U_2}} = \frac{n_1}{n_2} \quad f^2 = -n_2^2 \frac{\mathcal{A}_{11}}{\mathcal{A}} + 2n_1 n_2 \frac{\mathcal{A}_{12}}{\mathcal{A}} - n_1^2 \frac{\mathcal{A}_{22}}{\mathcal{A}} \quad \Pi_1 = \frac{f}{n_2} \quad \Pi_2 = \frac{f}{n_1}$$

Aligned Winding

$$(n_1, n_2) \rightarrow (1, N) \quad N \gg 1$$



Hierarchy:

$$\frac{\mathcal{K}_1}{\mathcal{K}_2} = \frac{1}{N} \ll 1$$

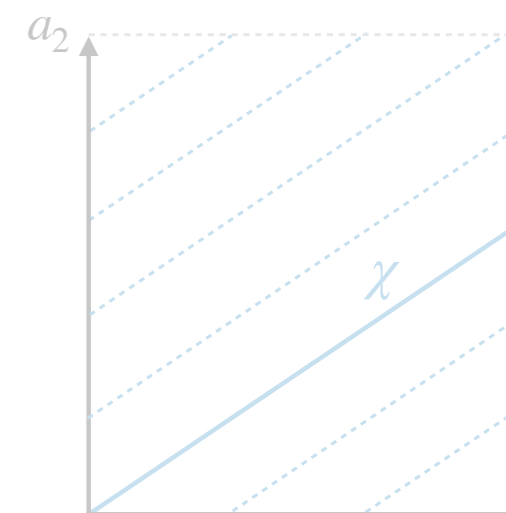
stabilisation condition for the saxions

$$f^2 \leq 2N \frac{\mathcal{A}_{12}}{\mathcal{A}} \ll 1$$

No go theorem holds for any form of the superpotential

Misaligned Winding

$$(n_1, n_2) \rightarrow (N, N + 1)$$

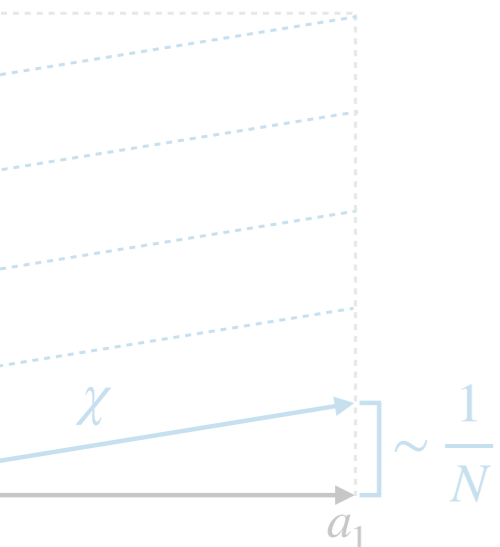


$$f^2 \leq 2N(N + 1)$$

$$\mathcal{W} = w(Z) + f(Z)(n_1 U_1 + n_2 U_2) \quad \frac{\mathcal{K}_{U_1}}{\mathcal{K}_{U_2}} = \frac{n_1}{n_2} \quad f^2 = -n_2^2 \frac{\mathcal{A}_{11}}{\mathcal{A}} + 2n_1 n_2 \frac{\mathcal{A}_{12}}{\mathcal{A}} - n_1^2 \frac{\mathcal{A}_{22}}{\mathcal{A}} \quad \Pi_1 = \frac{f}{n_2} \quad \Pi_2 = \frac{f}{n_1}$$

Aligned Winding

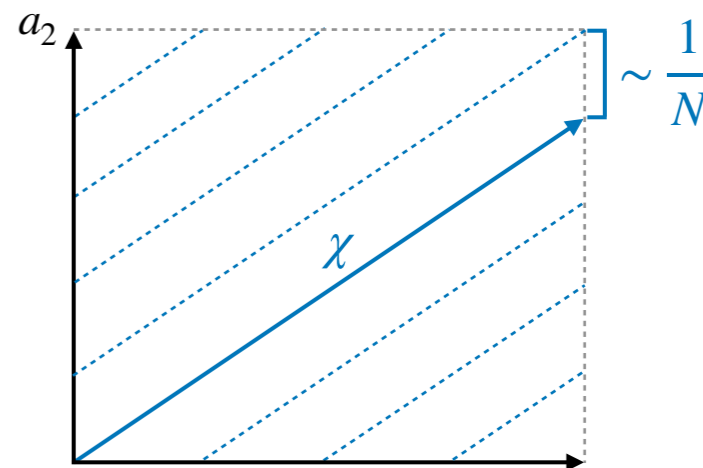
$(1, N) \quad N \gg 1$



$2N \frac{\mathcal{A}_{12}}{\mathcal{A}} \ll 1$

Misaligned Winding

$(n_1, n_2) \rightarrow (N, N + 1) \quad N \gg 1$



$f^2 \leq 2N(N + 1) \frac{\mathcal{A}_{12}}{\mathcal{A}}$

No hierarchy:

$\frac{\mathcal{K}_1}{\mathcal{K}_2} = \frac{N}{N + 1} \sim \mathcal{O}(1)$

stabilisation condition for the saxions

$\Pi_1, \Pi_2 \ll 1$

No inflation!!!

$f \gg 1$

Test of the WGC and SDC

No go theorem can be avoided if moduli stabilised accordingly

Further results: see [A. Hebecker, D. Junghans, AS: 1812.05626](#)

- mixing of three or more axions allows for **large periods** and possibly the realisation of **large field inflation**
- stabilising Kähler moduli using LVS gives rise to regime with **hierarchy** between **moduli masses and large-f axion potential**

How can we find suitable compactification spaces with relevant flux configurations?

 **Genetic Algorithms**

Applying Genetic Algorithms to the Landscape of Type IIB String Theory

A. Cole, AS, G. Shiu: 1907.xxxx

General motivation: find vacua with phenomenologically interesting features

Idea: mimic biology by imitating evolution

Holland 1960s

Previous works in physics context:

Allanach, Grellscheid, Quevedo: hep-ph/0406277

Akrami, Scott, Edsjo, Conrad, Bergstrom: 0910.3950

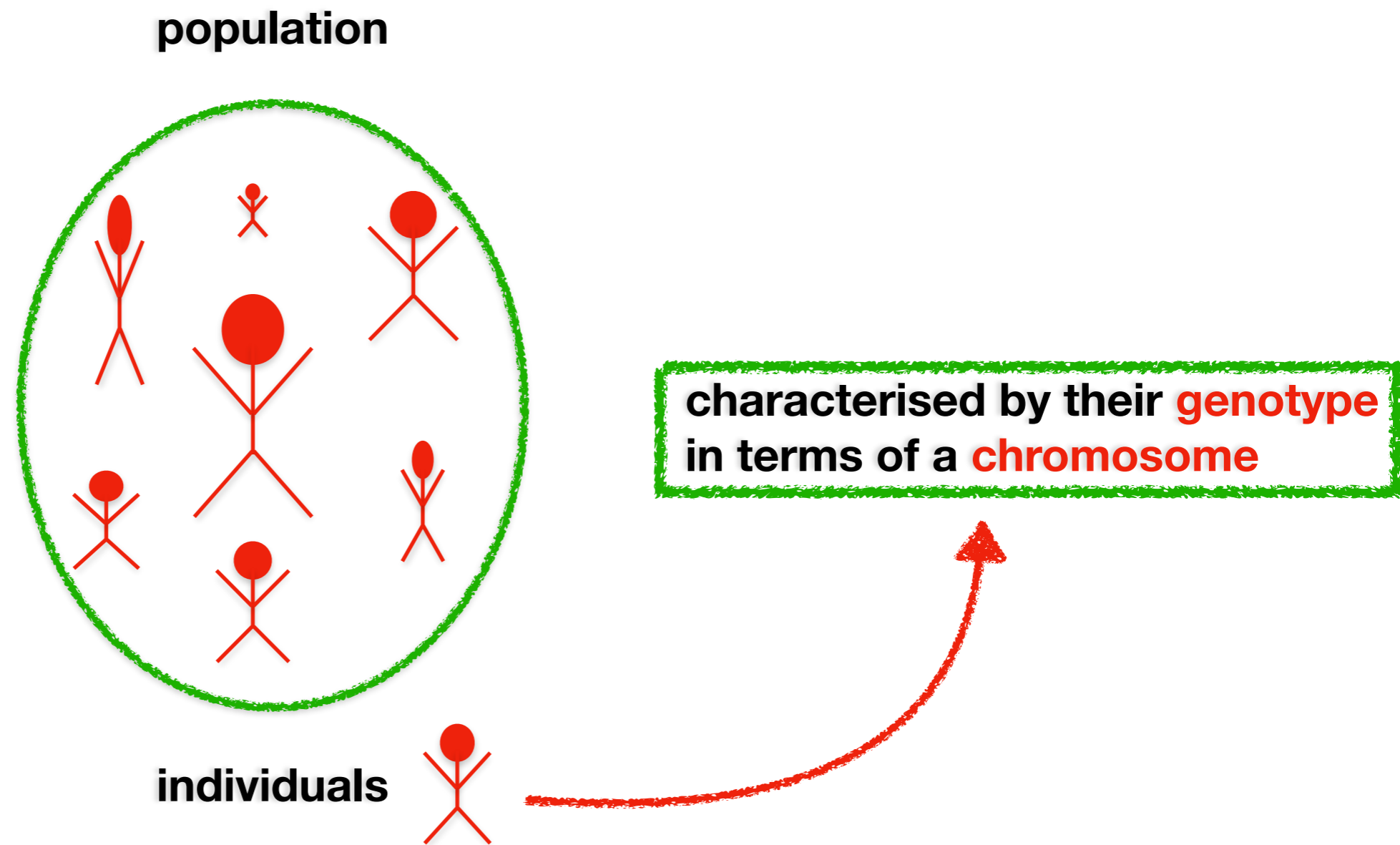
Blabäck, Danielsson, Dibitetto: 1301.7073, 1310.8300

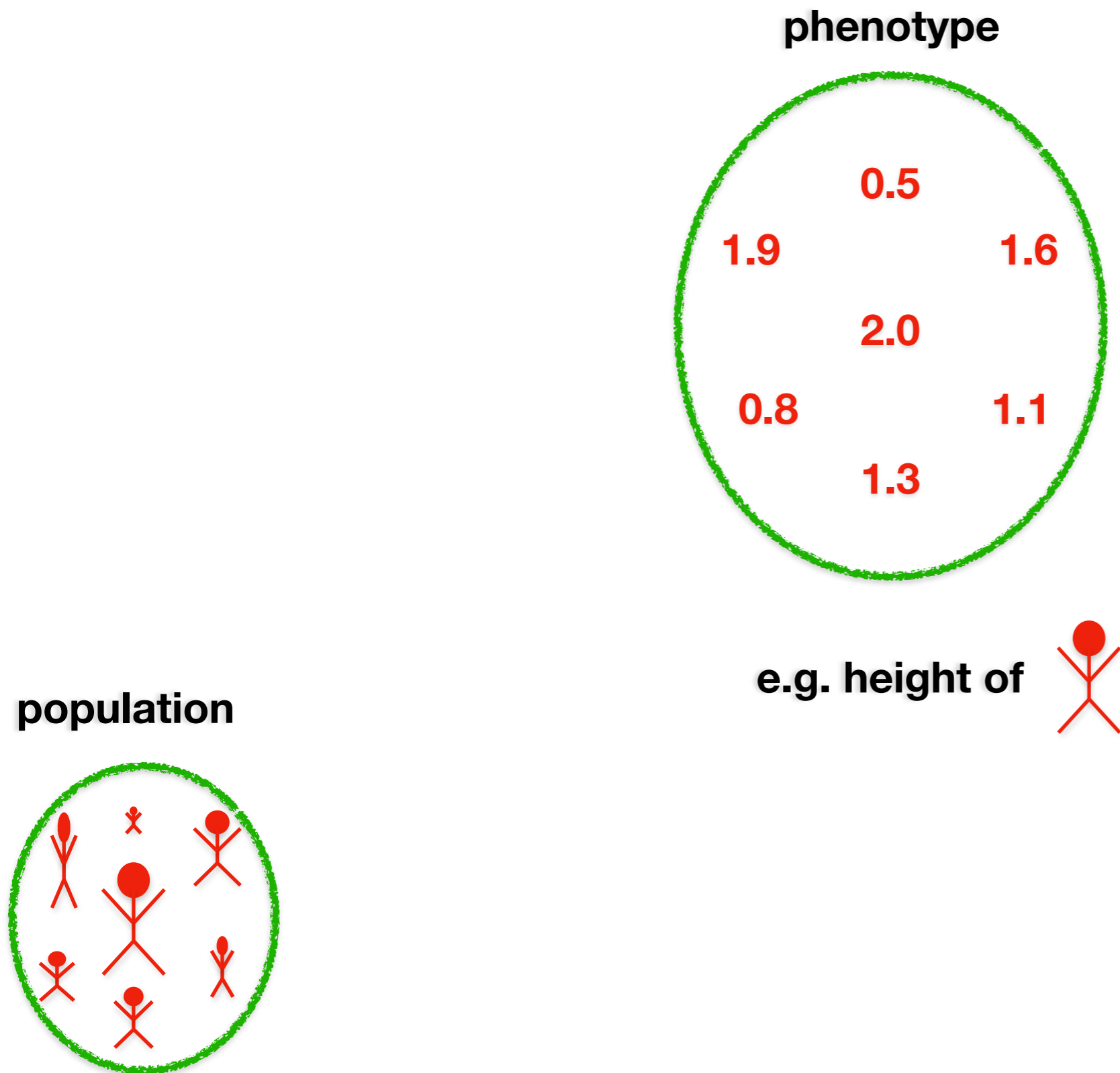
Abel, Rizos: 1404.7359, Ruehle: 1706.07024

Abel, Cerdezo, Robles: 1805.03615



Disclaimer: only sketch the general idea with dictionary to come later

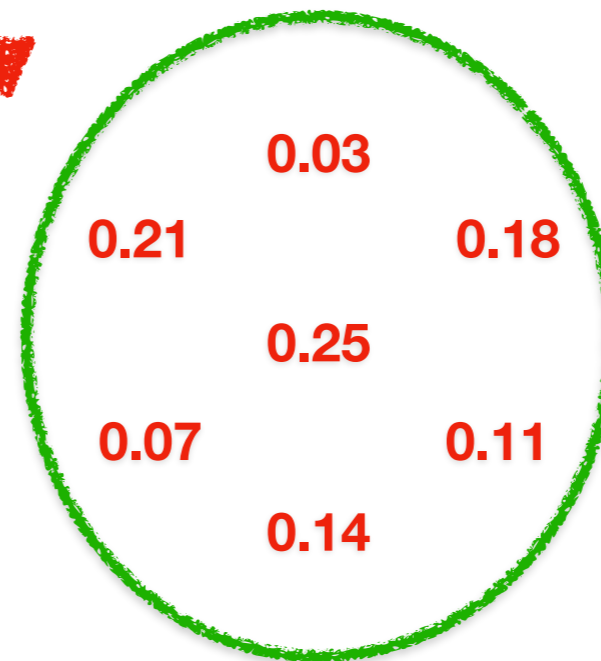




say we want to maximise the height of



fitness

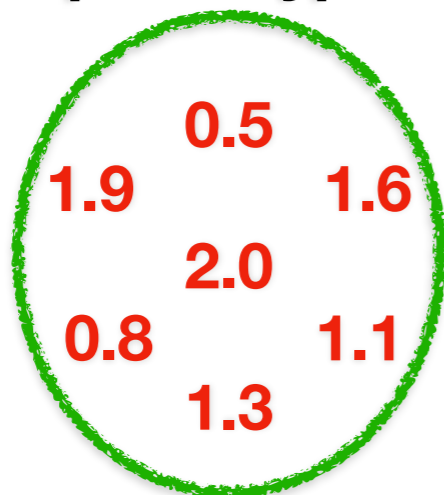


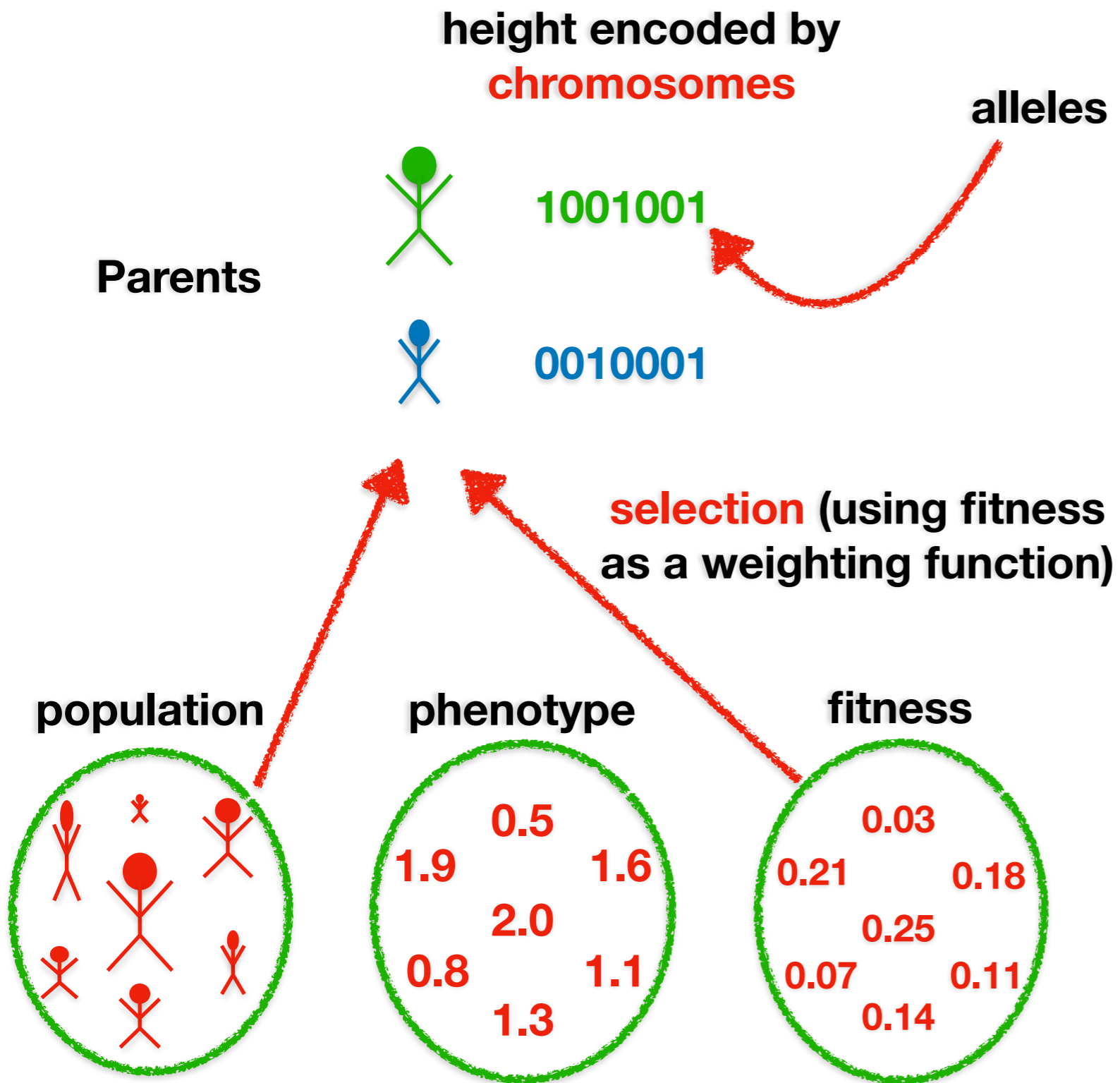
e.g. assign probabilities

population



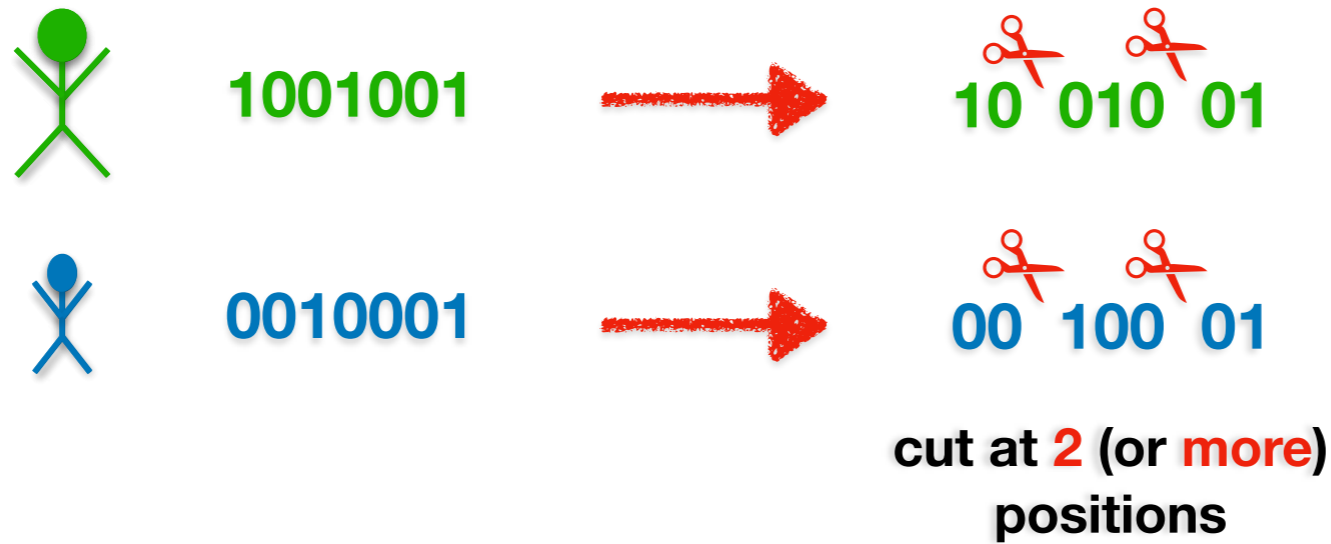
phenotype





height encoded by
chromosomes

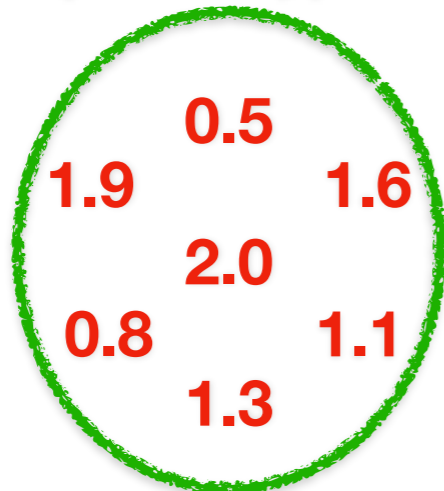
Parents



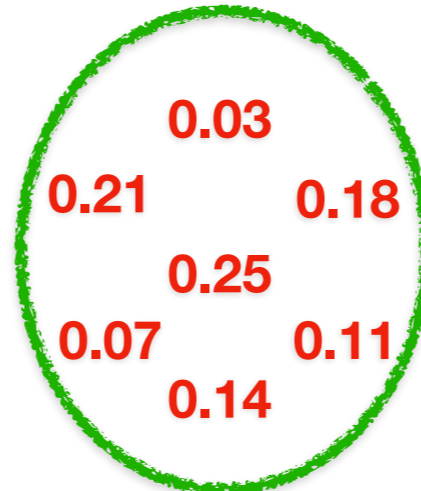
population

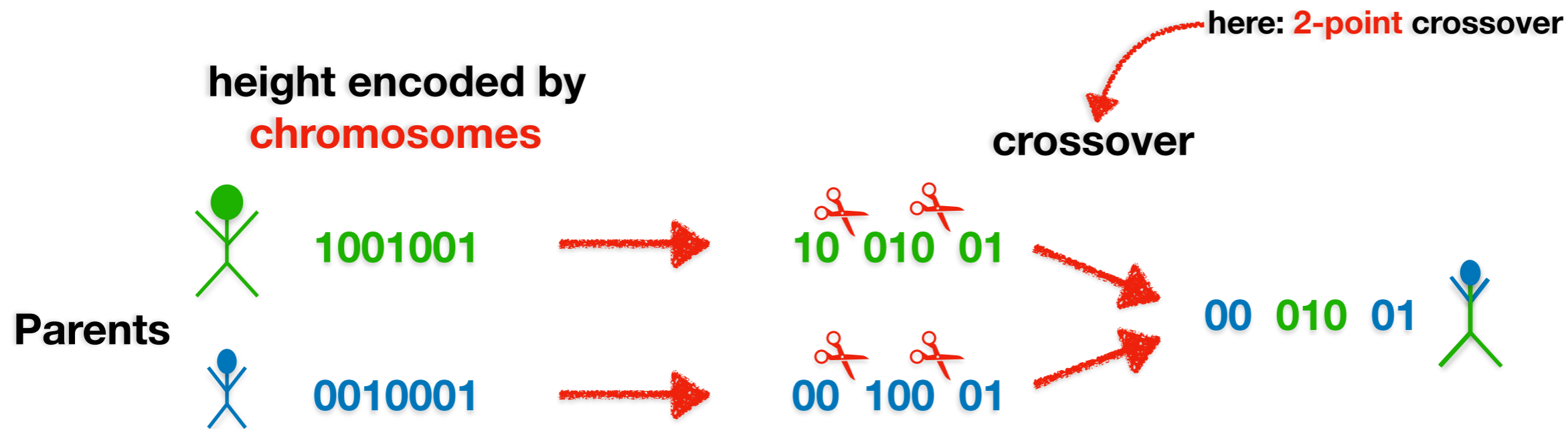


phenotype



fitness

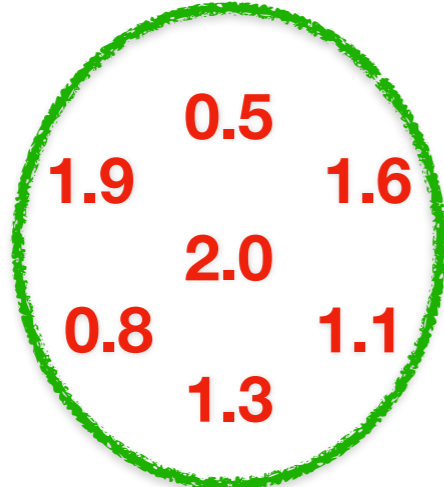




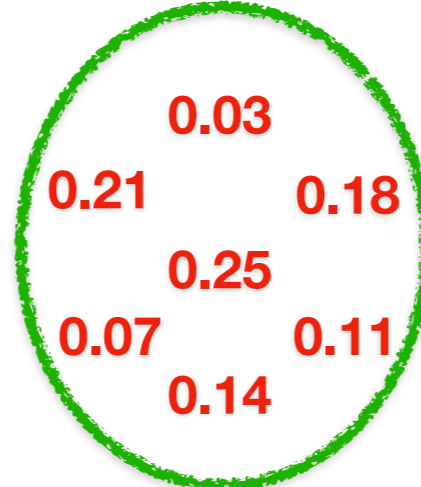
population



phenotype



fitness



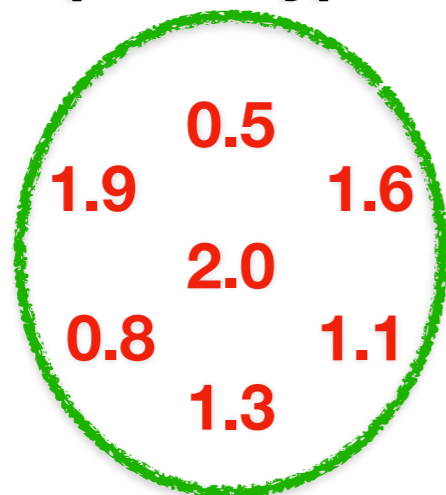


essential ingredient to ensure convergence
 around **global** fitness maximum
 (as we will see later)

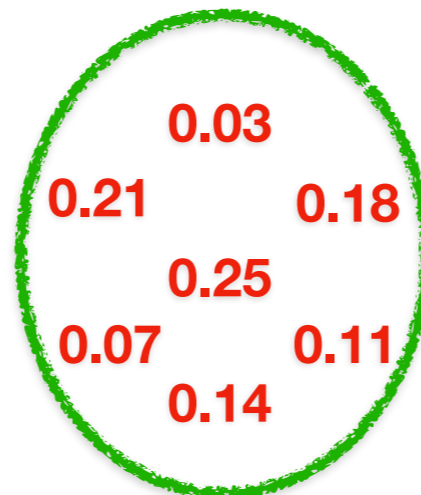
population



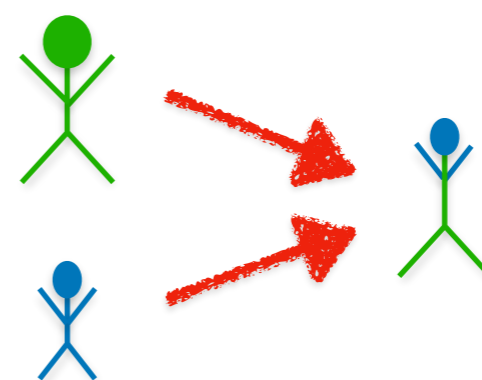
phenotype



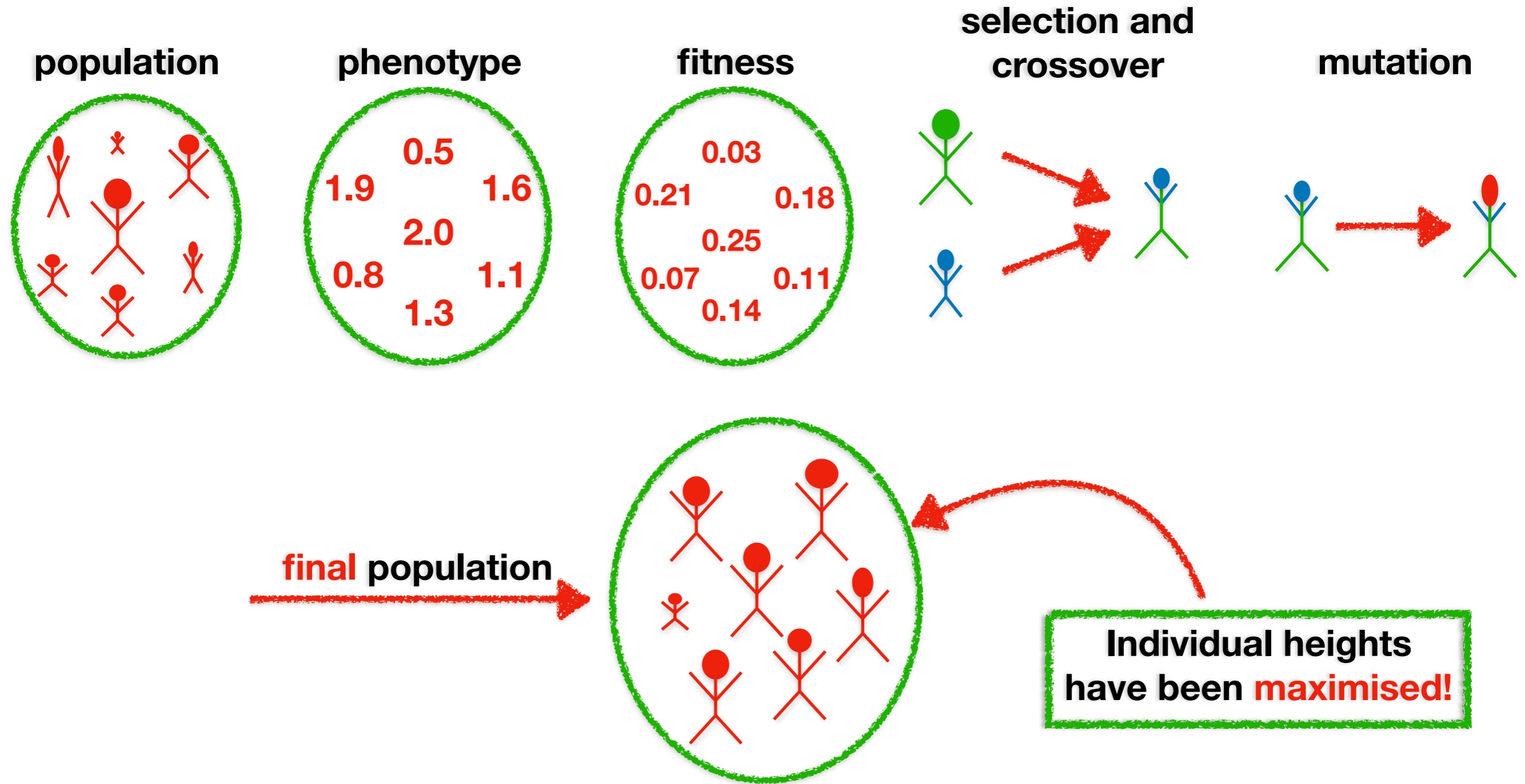
fitness



selection and crossover








For more details on the algorithm, see e.g. [Abel, Rizos: 1404.7359](#),
[Abel, Cerdeo, Robles: 1805.03615](#)

Applying Genetic Algorithms to the **Landscape**... a dictionary:

Genetic Algorithms	Landscape
individuals	flux vacua
chromosome	flux vector
alleles	fluxes
phenotype	VEVs of moduli
fitness	function of VEVs (typically chosen to be Gaussian)
boundary conditions	SUSY condition, gauge fixing, tadpole


crossover interchanges flux numbers

Consider 2 examples with 1 complex structure modulus τ and axio-dilaton ϕ


- symmetric T^6
- hypersurface in $WP_{1,1,1,1,4}^4$

Search for supersymmetric vacua by solving $D_\phi \mathcal{W} = D_\tau \mathcal{W} = 0$

ignoring Kähler moduli!

8 independent flux numbers

Discuss only one example, for **more** applications see **A. Cole, AS, G. Shiu: 1907.xxxx**

 searching for g_s , mass scales and minimising \mathcal{W}_0

Hypersurface  **search for VEV of the flux superpotential \mathcal{W}_0**

For simplicity: consider absolute value of \mathcal{W}_0

$\mathcal{W}_0^* = 50000$
optimal solution

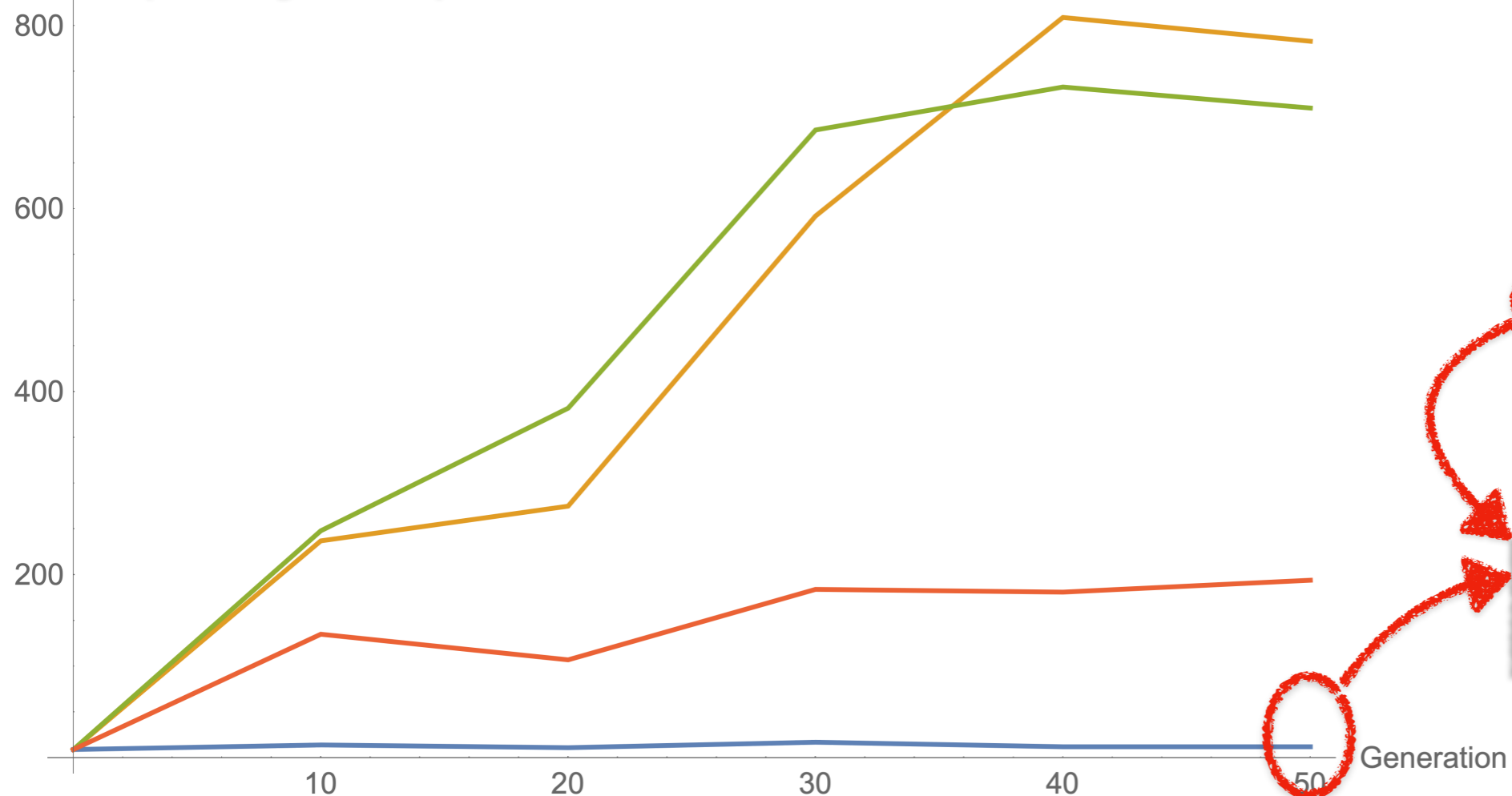
$p = 1000$
population size

KKLT: hep-th/0301240
LVS: hep-th/0502058
Westphal: hep-th/0611332

First: study different mutation rates q_{mut}

Motivation: magnitude of \mathcal{W}_0 relevant for the application of **KKLT, LVS** or **Kähler uplift**

Number of individuals around \mathcal{W}_0^*
(=convergence rate)



- ‡ mutations
- 0
 - 1 with $q_{mut}=0.2$
 - 1 with $q_{mut}=1.0$
 - 2 with $q_{mut}=0.1$

Mutation is essential

Hypersurface  **search for VEV of the flux superpotential \mathcal{W}_0**

For simplicity: consider absolute value of \mathcal{W}_0

$\mathcal{W}_0^* = 50000$
optimal solution

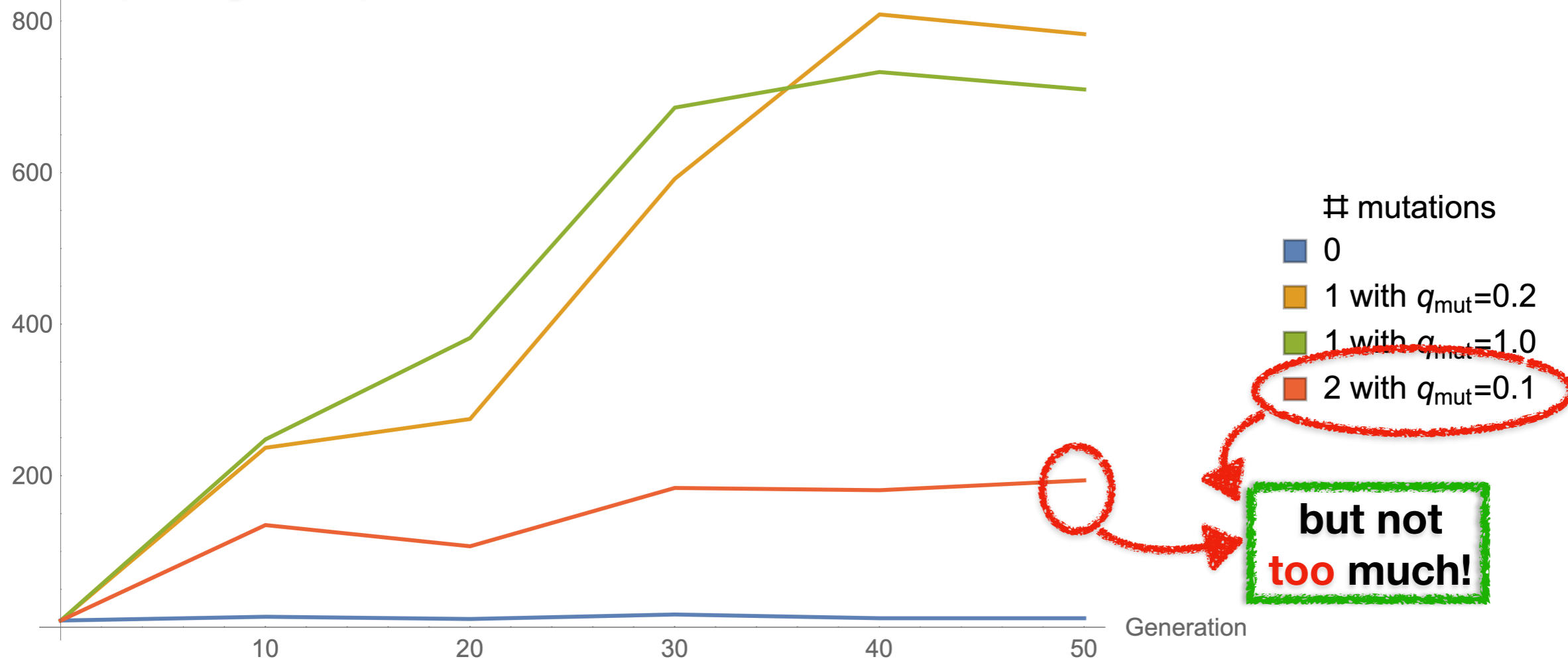
$p = 1000$
population size

KKLT: hep-th/0301240
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First: study different mutation rates q_{mut}

Motivation: magnitude of \mathcal{W}_0 relevant for the application of **KKLT, LVS** or **Kähler uplift**

Number of individuals around \mathcal{W}_0^*
(=convergence rate)



but not too much!

Hypersurface  **search for VEV of the flux superpotential \mathcal{W}_0**

For simplicity: consider absolute value of \mathcal{W}_0

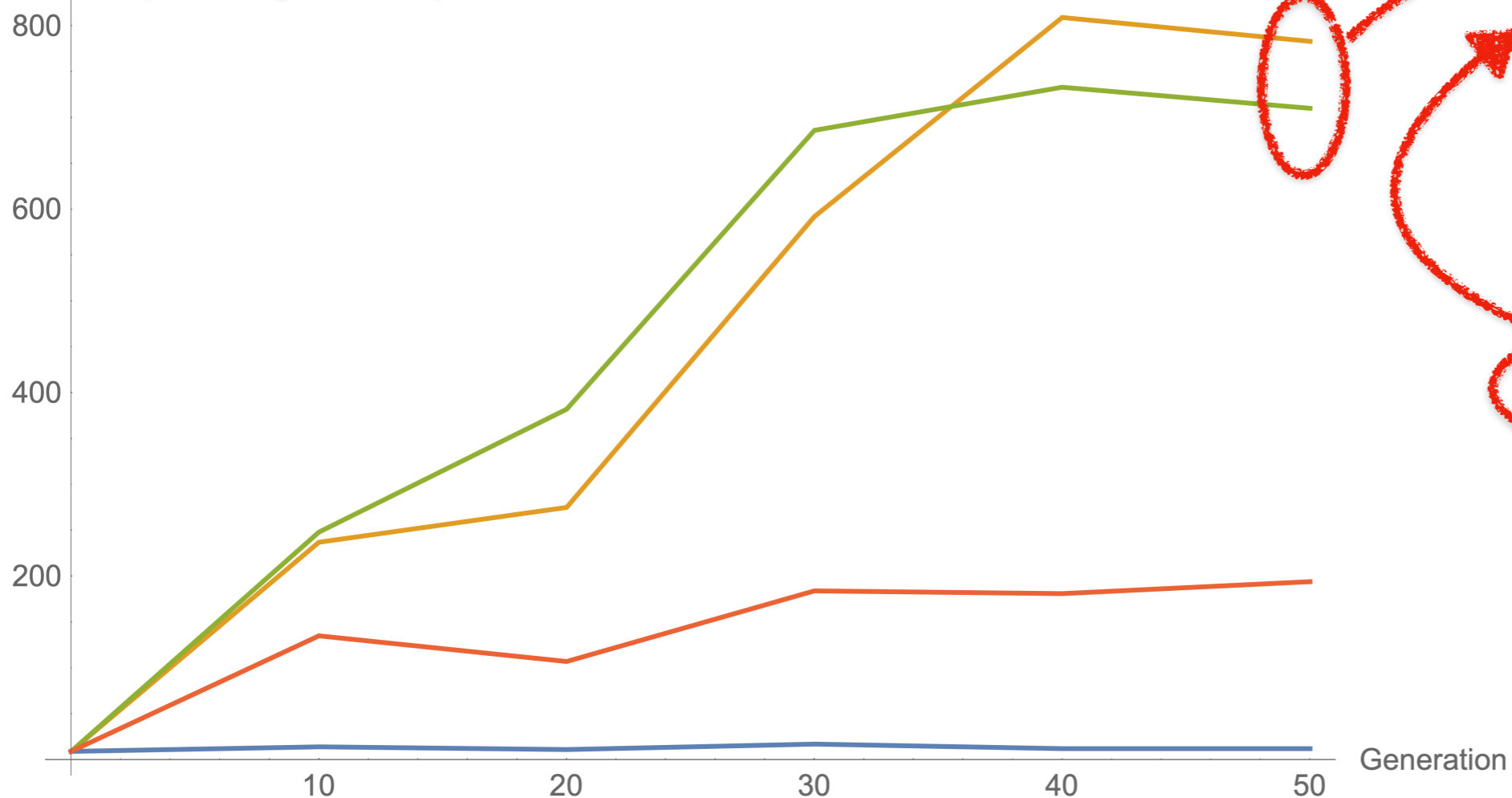
$\mathcal{W}_0^* = 50000$
optimal solution

$p = 1000$
population size

Motivation: magnitude of \mathcal{W}_0 relevant for the application of **KKLT, LVS** or **Kähler uplift**

First: study different mutation rates q_{mut}

Number of individuals around \mathcal{W}_0^*
(=convergence rate)

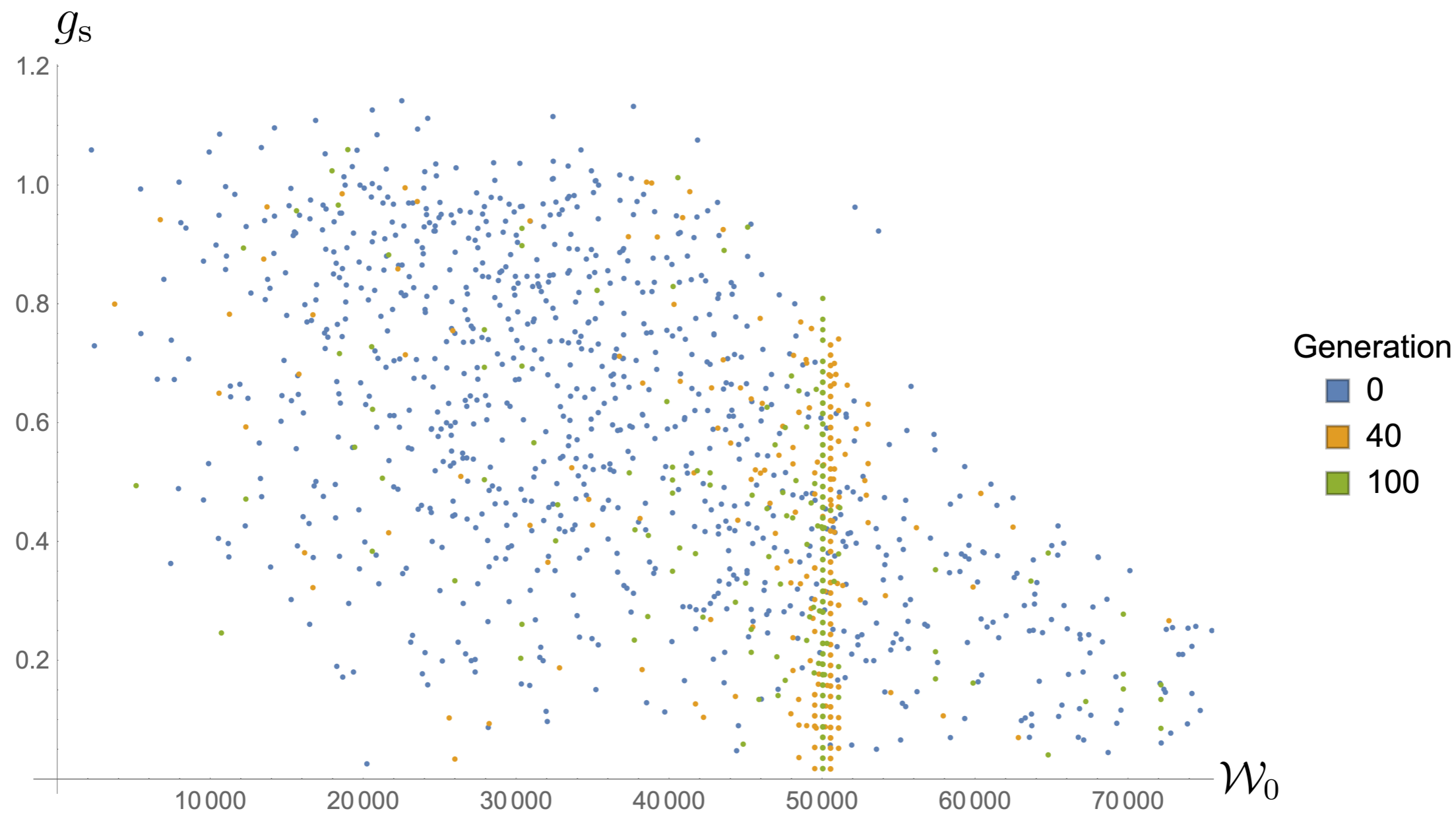


Mutation rate determines final result

- # mutations
- 0
 - 1 with $q_{mut}=0.2$
 - 1 with $q_{mut}=1.0$
 - 2 with $q_{mut}=0.1$

Running Genetic Algorithm for **100 generations**:

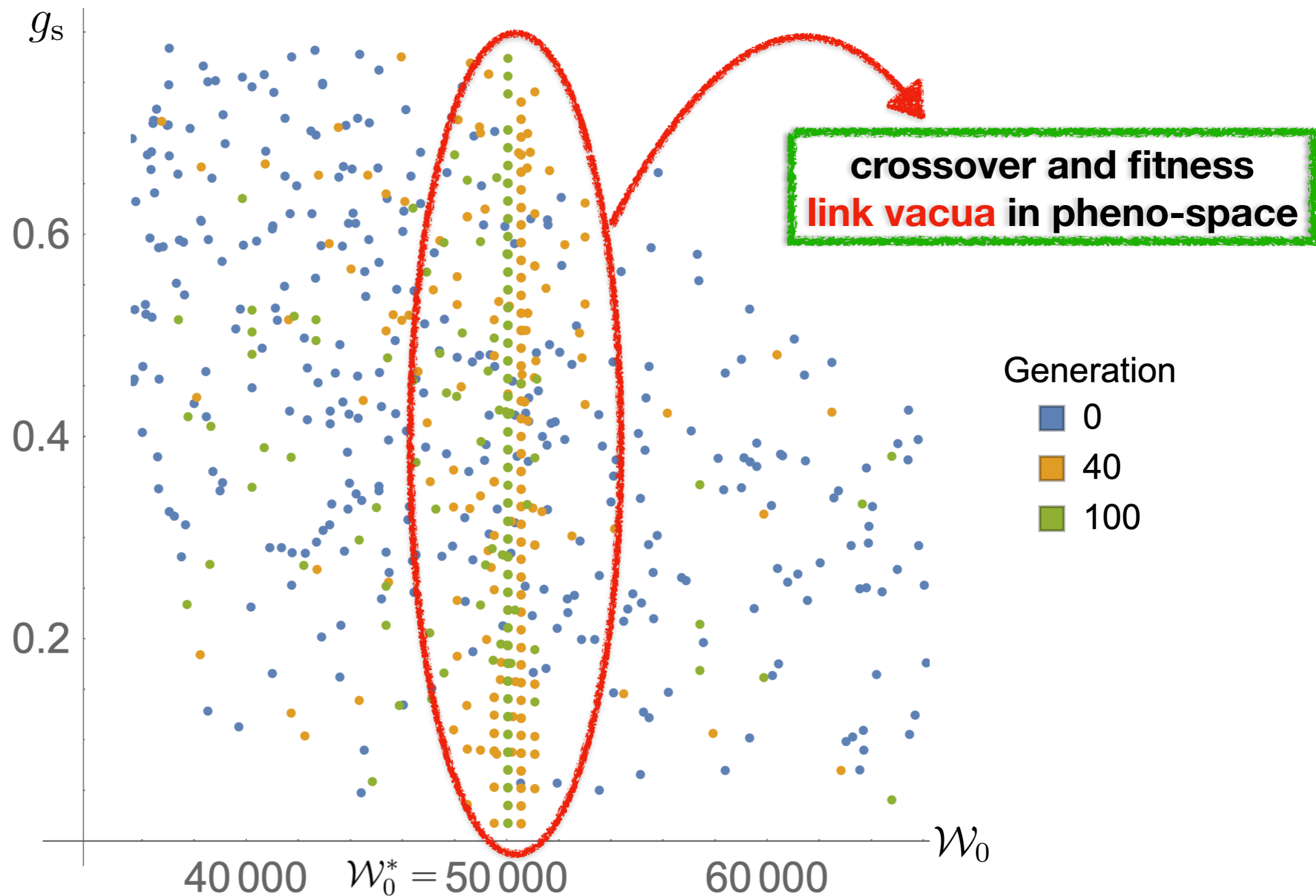
$$\mathcal{W}_0^* = 50000 \quad p = 1000$$



➔ Find about **85% of individuals** in range $[\mathcal{W}_0^* - 250, \mathcal{W}_0^* + 250]$

Running Genetic Algorithm for **100 generations**:

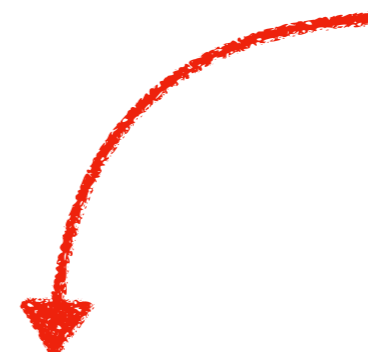
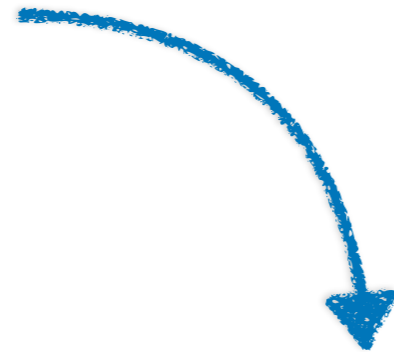
$$\mathcal{W}_0^* = 50000 \quad p = 1000$$



→ Find about **85% of individuals** in range $[\mathcal{W}_0^* - 250, \mathcal{W}_0^* + 250]$

(Mis-)aligned Winding as testing ground?

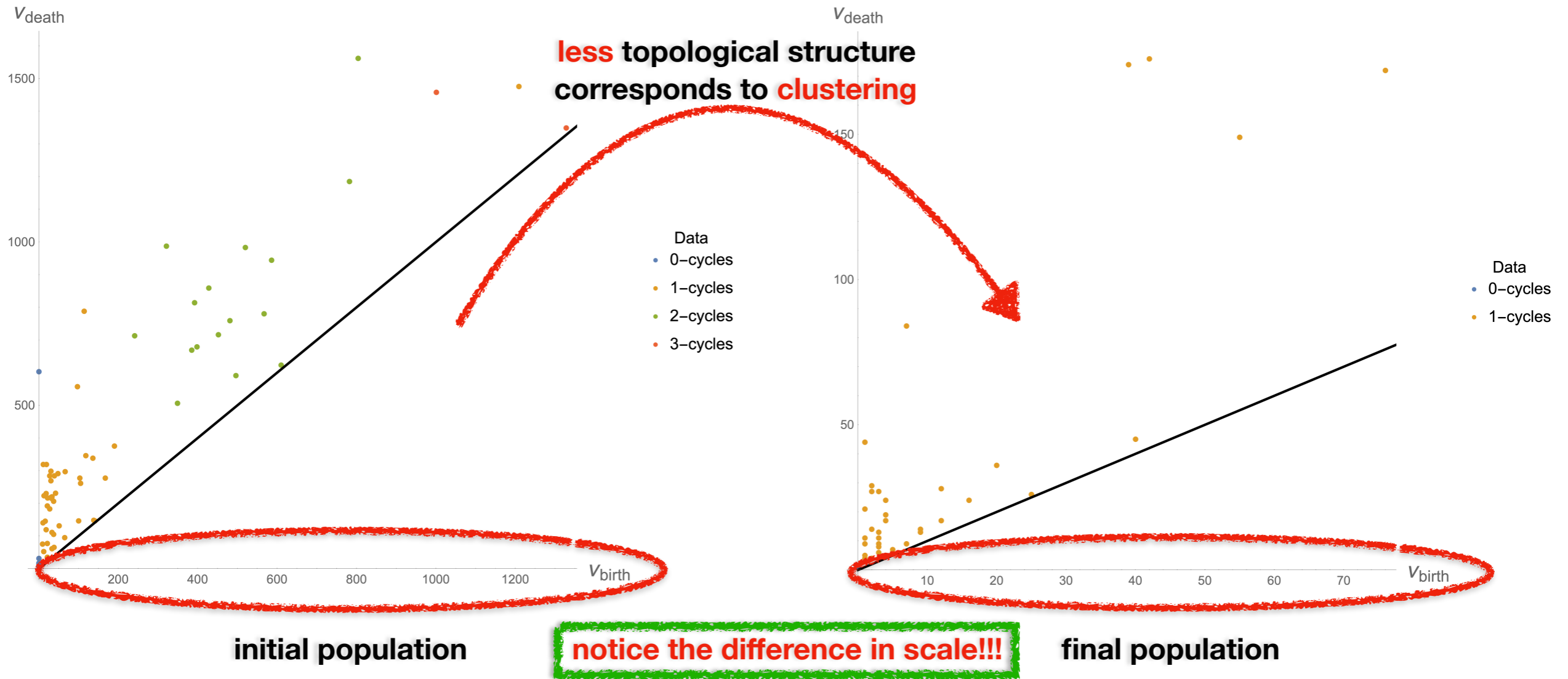
Genetic Algorithms as testing method?



Test Swampland Conjectures with Genetic Algorithms?!

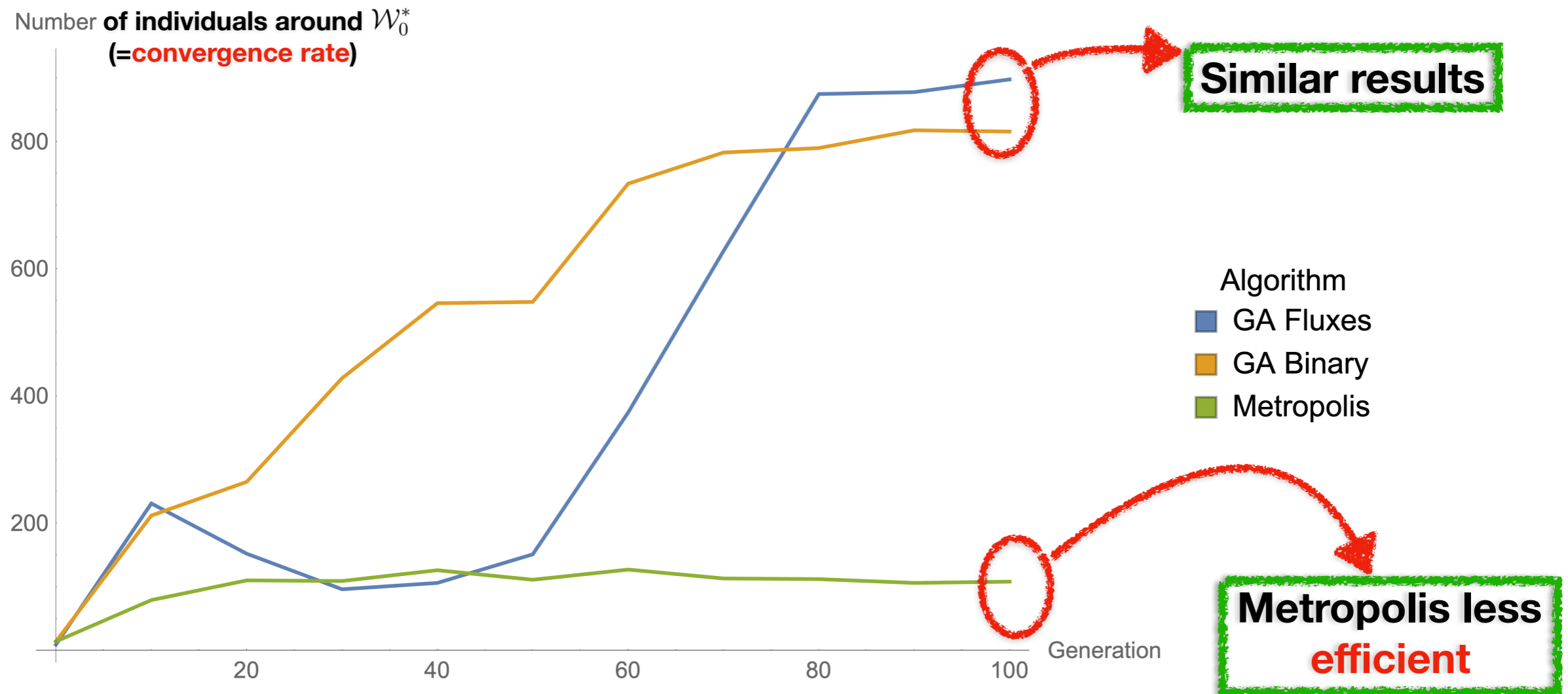
Thank you!!!

Use **Persistence Homology** to study the distribution of fluxes



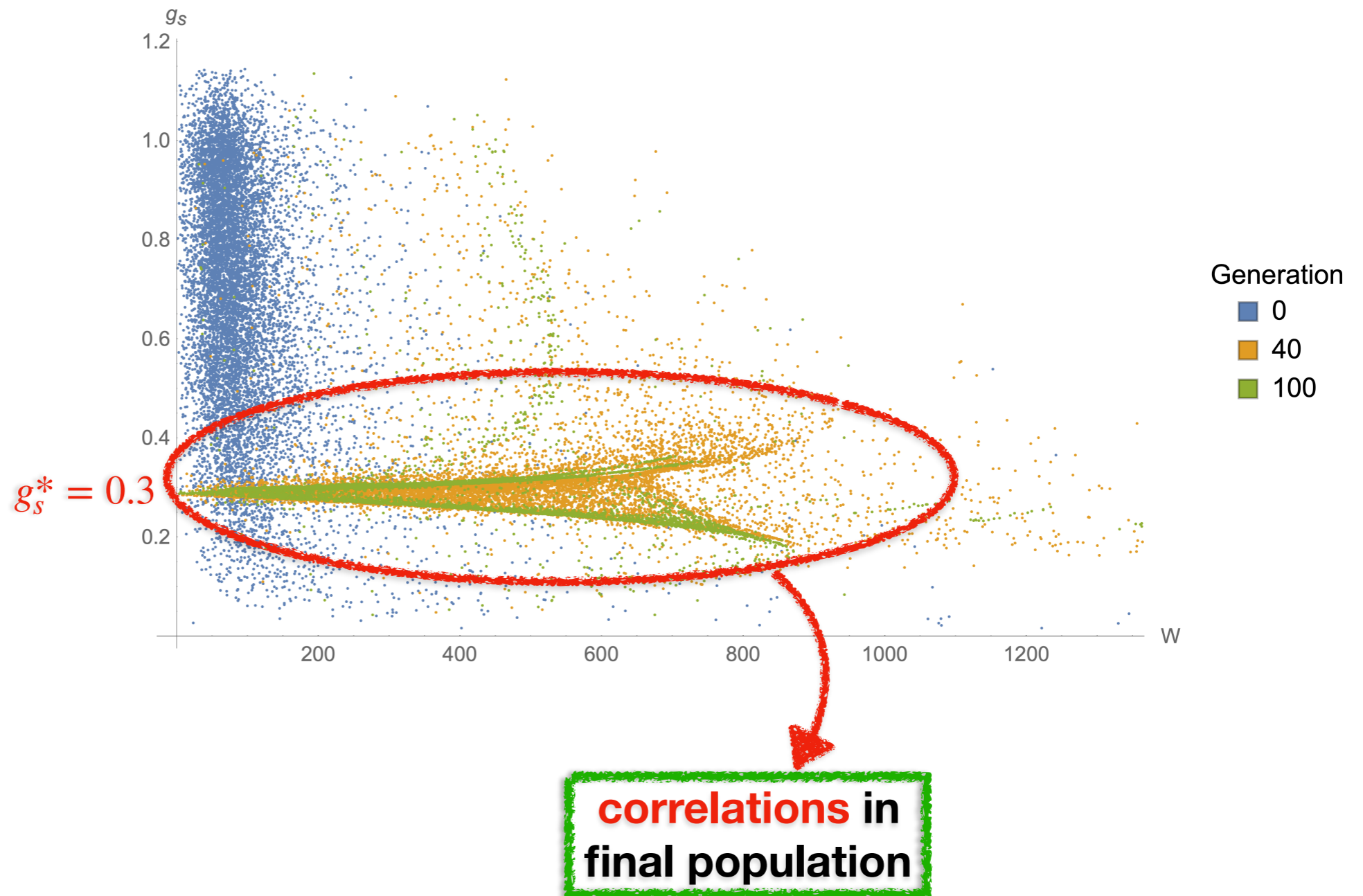
Comparison with two other algorithms

- **Metropolis algorithm (random walk in flux space)**
- **Genetic algorithm with binary crossover (replace flux numbers by their binary encoding)**

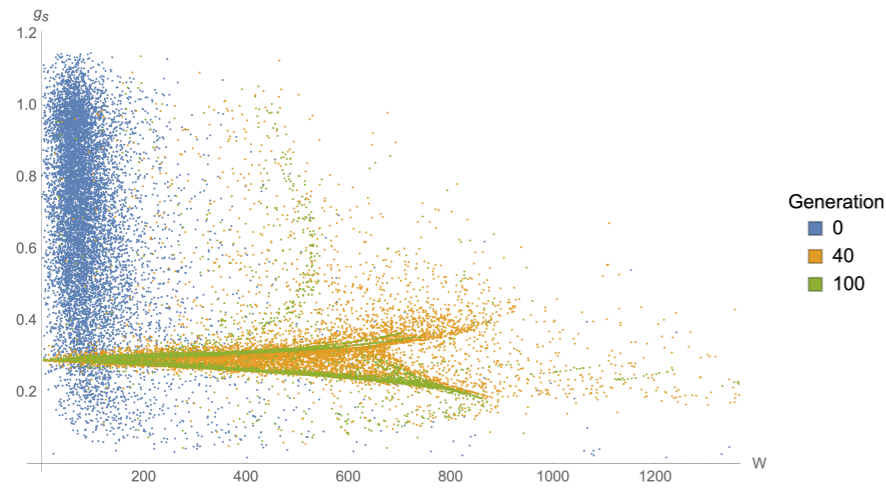


Other searches for the symmetric T^6 with $p = 10000$

1.) searching for values of g_s

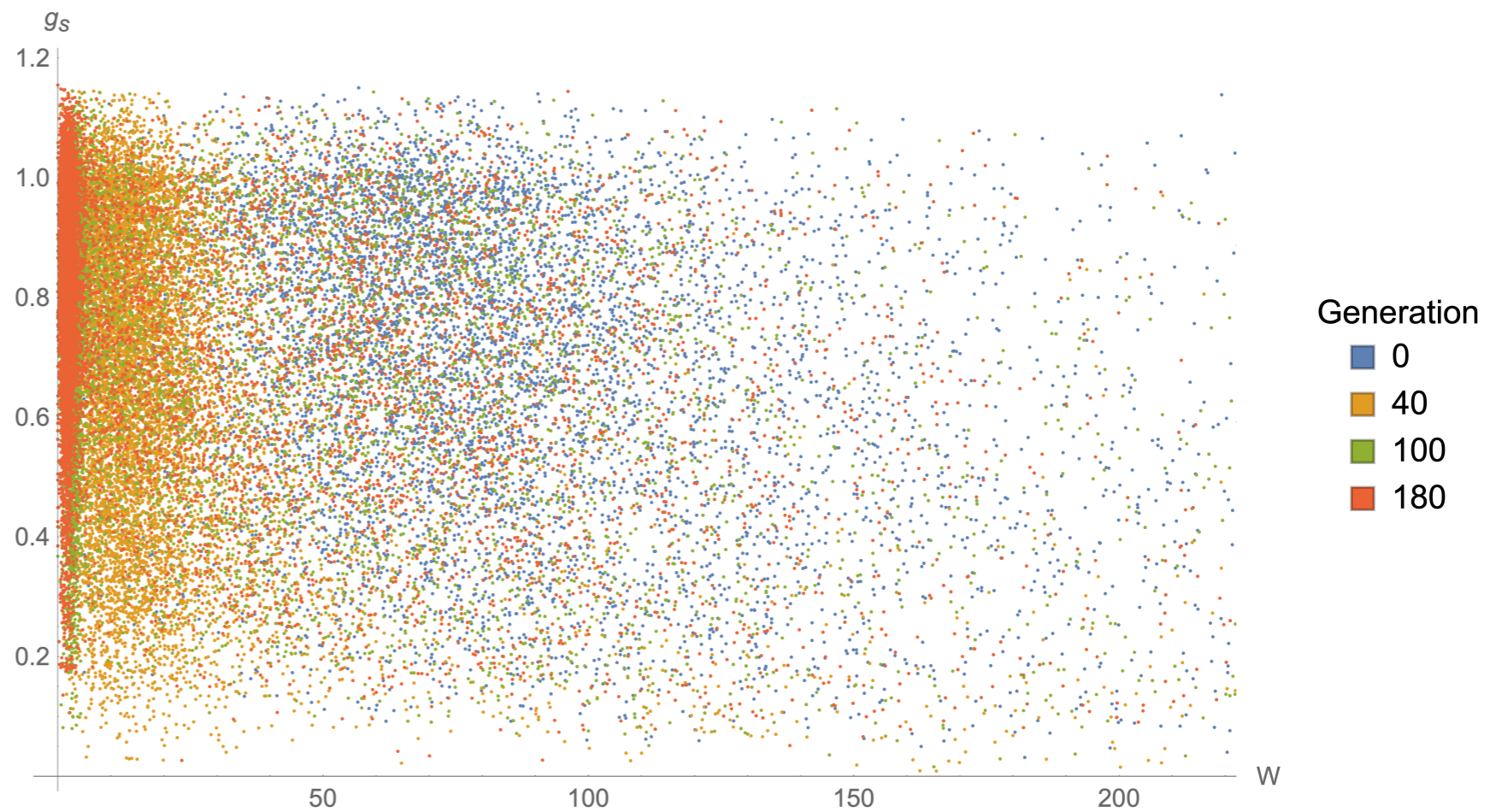


Other searches for the symmetric T^6 with $p = 10000$

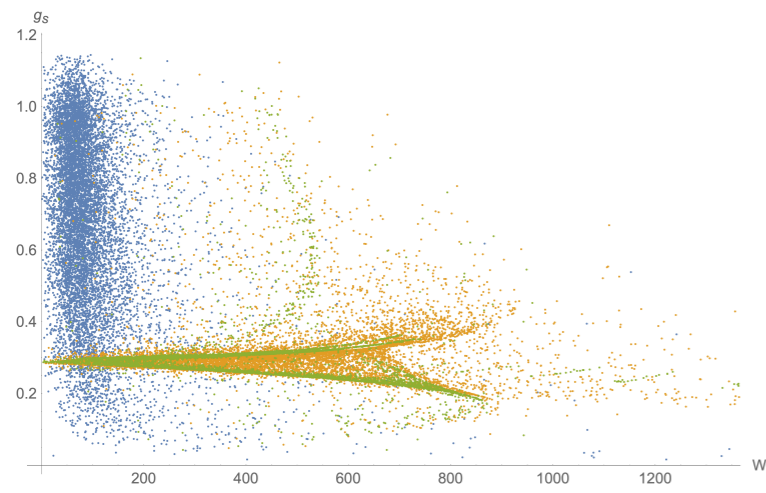


1.) searching for values of g_s

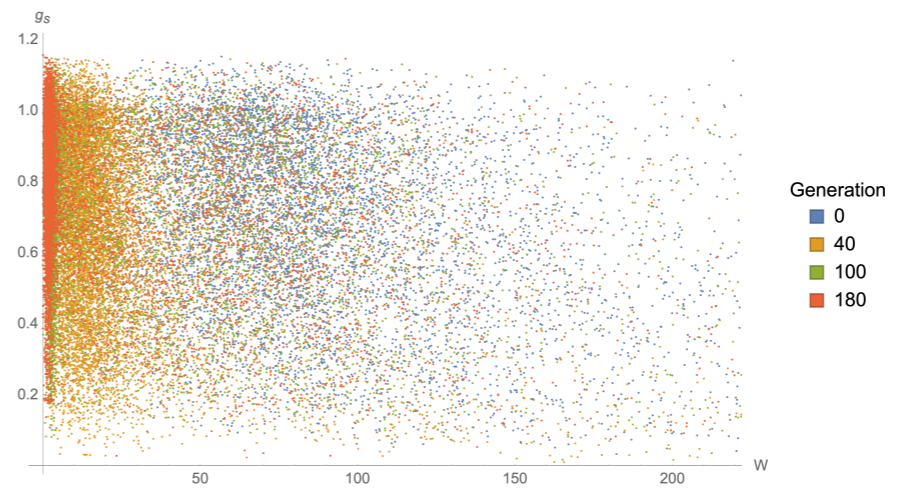
2.) minimising \mathcal{W}_0



Other searches for the symmetric T^6 with $p = 10000$



1.) searching for values of g_s



2.) minimising \mathcal{W}_0

3.) searching for **four** mass scales

study of **different selection methods**

- rank weighting
- tournament

