

The dS Swampland Conjecture, Non-BPS branes and K-theory

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Based on work with Ralph Blumenhagen and Andriana Makridou [[1906.06078](#)]

The Talk in a Nutshell:

Challenging the dS swampland conjecture

- Setup: Type IIA Orientifolds w/ fluxes and branes
- No-go theorem: no dS vacua in type IIA with standard ingredients
[Hertzberg,Kachru,Taylor,Tegmark'07]
- Non-BPS $\widehat{D}7$ branes evade the no-go theorem
- Explicitly find dS vacua in a toy model setup
- Reconcile this with the dS swampland conjecture by cancellation of K-theory charges:

Proposition:

If the (refined) de Sitter swampland conjecture is correct, then the K-theory charge on a compact space has to be trivial.

Basics of Type IIA orientifolds

Orientifold Projection

Consider type IIA orientifold on a CY 3-fold X .

Orientifold projection: $\Omega \bar{\sigma} (-1)^{F_L}$

$\Omega : (\tau, \sigma) \rightarrow (\tau, -\sigma)$ world-sheet parity transformation,
 $\bar{\sigma}$ an anti-holomorphic involution of the CY and
 F_L the left-moving space-time fermion number operator.

The orientifold breaks the $\mathcal{N} = 2$ supersymmetry to $\mathcal{N} = 1$.

Split (co)homology into $\bar{\sigma}$ equivariants $H^* = H_+^* \oplus H_-^*$.

Basics of Type IIA orientifolds

Classification via Cohomology

The massless spectrum in the closed string sector is determined by equivariant cohomology groups.

| $\mathcal{N} = 1$ multiplet | Moduli | Cohomology |
|-----------------------------|--------|------------|
| chiral | U | $H_+^3(X)$ |
| chiral | T | $H_-^2(X)$ |
| vector | V | $H_+^2(X)$ |

Orientifold even fluxes take values in equivariant cohomology groups.

| Flux | Cohomology |
|--------------------------|----------------------------------|
| H | $H_-^3(X)$ |
| $\{F_0, F_2, F_4, F_6\}$ | $\{H_+^0, H_-^2, H_+^4, H_-^6\}$ |

Stable non-BPS D -branes

Reminder: D -branes and K-theory

Physically: (stacked) D -branes \Leftrightarrow gauge fields

We can "add" ($\Leftrightarrow \oplus$) and "subtract" ($\Leftrightarrow ??$) D -branes and \bar{D} -branes.

K-theory allows us to do that:

Equivalence classes $[E, F]$ of gauge bundles:

$$[E, F] \sim [K, L] \iff \exists G : E \oplus L \oplus G \simeq F \oplus K \oplus G$$

Compare with $\mathbb{N} \rightarrow \mathbb{Z}$: [pos, neg] contributions

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Intuition:

of D -branes after annihilation \sim Equiv. class rep. $[E, 0]$

\Rightarrow K-theory charge \sim rank of E

Stable D -branes: any # of D -branes allowed, so the K-theory $\simeq \mathbb{Z}$

[Minasian, Moore'97; Witten'98; review: Evslin'06]

Stable non-BPS D -branes

Stabilization via Orientifold

Recall: non-BPS branes are usually unstable

No GSO projection to remove the Tachyon!

Orientifold projects out tachyon

This only works with a single non-BPS brane

\Rightarrow K-theory $\simeq \mathbb{Z}_2$

Well-known in Type I: [Frau,Gallot,Lerda,Strigazzi'99]

| non-BPS brane | K-theory |
|-------------------|-----------------------------|
| $\widehat{D}8$ | $KO(S^1) = \mathbb{Z}_2$ |
| $\widehat{D}7$ | $KO(S^2) = \mathbb{Z}_2$ |
| $\widehat{D}0$ | $KO(S^9) = \mathbb{Z}_2$ |
| $\widehat{D}(-1)$ | $KO(S^{10}) = \mathbb{Z}_2$ |

Stable non-BPS D-branes

Stable Configurations in Type IIA

Example: $\widehat{D}8$ brane

Consider type I on $(T^2)^3$ and T-dualize along one cycle each.
The anti-holomorphic involution acts as $\bar{\sigma} : z_i \rightarrow \bar{z}_i$.

$$\widehat{D}8_I \implies \widehat{D}5_{IIA} \text{ or } \widehat{D}7_{IIA},$$

dependent on original configuration.

Stable non-BPS D-branes

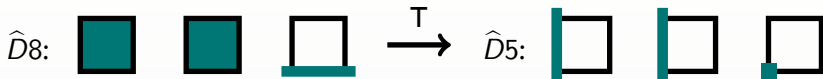
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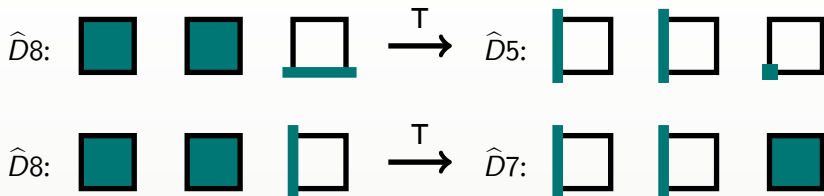
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Stable non-BPS branes in type IIA

Stable (non-fluxed) non-BPS branes for the Type IIA orientifolds

After considering all configurations of spacetime filling branes, we find stable non-BPS branes in type IIA:

| Type I | Type IIA | Homology |
|----------------|----------------|------------|
| $\widehat{D}8$ | $\widehat{D}5$ | $H_2^+(X)$ |
| | $\widehat{D}7$ | $H_4^-(X)$ |
| $\widehat{D}7$ | $\widehat{D}4$ | $H_1^+(X)$ |
| | $\widehat{D}6$ | $H_3^-(X)$ |
| | $\widehat{D}8$ | $H_5^+(X)$ |

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| $\widehat{D}7$ | $\widehat{D}4$ | $H_1^+(X)$ | not supported on CY |
| | $\widehat{D}6$ | $H_3^-(X)$ | Freed-Witten anomaly |
| | $\widehat{D}8$ | $H_5^+(X)$ | not supported on CY |

Inflationary Constraints on Type IIA String Theory

Hertzberg, Kachru, Taylor, Tegmark '07 [0711.2512]

Study dependence of potential on volume and dilaton moduli

$$V = \frac{A_H}{s^2 t^3} + \sum_{p \text{ even}} \frac{A_{F_p}}{s^4 t^{p-3}} + \frac{A_{D6}}{s^3} - \frac{A_{O6}}{s^3}$$

Consider the combination

$$\underbrace{t \frac{\partial V}{\partial t} + 3s \frac{\partial V}{\partial s}}_{=0 \text{ in minimum}} = -9V - \sum_p p \frac{A_{F_p}}{s^4 t}$$

$\Rightarrow V$ cannot be positive in the vacuum!

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The authors comment that one way to avoid the no-go is with $D_{p>6}$ -branes, e.g. $\widehat{D7}$ -branes.

A Supergravity Toy Model

The model

Toroidal STU -model with $T = T_i$ and $S = U_i$ identified.

$$K = -3 \log(T + \bar{T}) - 4 \log(S + \bar{S})$$

$$W = -4ihS + f_6 + 3if_4T - 3f_2T^2 - if_0T^3$$

$$\Rightarrow V_F = \frac{h^2}{8s^2t^3} + \frac{f_0^2 t^3}{32s^4} + \frac{3f_4^2}{32s^4t} - \frac{f_0h}{4s^3}$$

Find exactly the scaling behaviour expected from the no-go.

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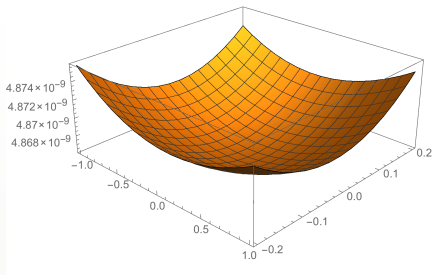
Add the non-BPS $\widehat{D7}$ -brane by hand.

A Supergravity Toy Model

The dS minimum

It is just a matter of choosing the fluxes such that there is a dS vacuum.

- First solve for $V=0$ minimum.
- Find relation between $A_{\widehat{D7}}$ and the fluxes h, f_0, f_4 .
- The real value $A_{\widehat{D7}} = \sqrt{2} \frac{3}{16}$ is fixed by dimensional reduction.
- Choose fluxes such that $A_{\widehat{D7}}$ almost satisfies the Minkowski relation.



Choosing $h = 3, f_0 = 2, f_4 = 23$
there is a minimum at

$$s_0 \approx 105.17 \text{ and}$$

$$t_0 \approx 6.54, \text{ with}$$

$$V_0 = 4.87 \cdot 10^{-9} M_{\text{pl}}^4.$$

Discussion

The (refined) dS swampland conjecture

$$|\nabla V| \geq \frac{c}{M_{\text{pl}}} \cdot V, \quad \text{or} \quad \min(\nabla_i \nabla_j V) \leq -\frac{c'}{M_{\text{pl}}^2} \cdot V$$

where $\min(\nabla_i \nabla_j V)$ is the minimal eigenvalue of the Hessian matrix and c, c' are of order one.

[Obied, Ooguri, Spodyneiko, Vafa '18; Garg, Krishnan '18; Ooguri, Palti, Shiu, Vafa '18]

The minimum we found above is in clear violation with

$$V = 4.87 \cdot 10^{-9} M_{\text{pl}}^4$$

$$|\nabla V| = 0$$

$$\min(\nabla_i \nabla_j V) \approx 3.711 \cdot 10^{-8} M_{\text{pl}}^2$$

The (refined) dS swampland conjecture

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K-theory charges on compact spaces

K-theory charges do not have Bianchi identities leading to tadpole conditions for the cancellation of charges!

Indirect argument:

K-theory charges manifest as a global gauge anomaly on the world-volume of suitable probe branes. [Uranga'00]

The (refined) dS swampland conjecture

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Proposition

If the (refined) de Sitter swampland conjecture is correct, then the K-theory charge on a compact space has to be trivial.

Summary

- Investigated stable non-BPS D-branes in type IIA
- Found toy model with dS vacuum using simple ingredients
 - Can provide arguments that such a setup can be controlled
- dS swampland conjecture implies something in our setup is wrong
 - Indeed, K-theory charges do not vanish

⇒ dS swampland conjecture implies vanishing of K-theory charges

More on non-BPS branes:

Scenarios with vanishing total K-theory charge, ... [Damian,Loaiza-Brito'19]

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Thank you for your attention!

Setup is likely to be controlled

Tension of non-BPS brane scales in the same way as tension of D-branes:

- Backreaction on the geometry controlled by g_s
- Small in weak coupling regime.

Must make sure that the branes do not have open string moduli:

- Separate non-BPS braes from other branes
- Attraction/repulsion with other branes is g_s suppressed.