

Lensing limitations on bispectrum constraints of primordial non-Gaussianity

William Coulton, Daan Meerburg, David Baker,
Adriaan Duivenvoorden, Selim Hotinli and Alex
van Engelen

What is the bispectrum?

$$\frac{\Delta T(\vec{n})}{T} = \sum_{\ell, m} a_{\ell, m} Y_{\ell, m}(\vec{n})$$

- If CMB is purely Gaussian then the fluctuations can be fully described by the power-spectrum C_ℓ
- The bispectrum is the harmonic equivalent of the three point function
- For a homogeneous and isotropic universe it has the form:

$$\langle a_{\ell_1, m_1} a_{\ell_2, m_2} a_{\ell_3, m_3} \rangle = \mathcal{G}_{\ell_1, \ell_2, \ell_3}^{m_1, m_2, m_3} b_{\ell_1, \ell_2, \ell_3}$$

Geometric
factor

Reduced bispectrum
- contains the physics

- Vanishes for Gaussian fluctuations

Why study primordial non-Gaussianity?

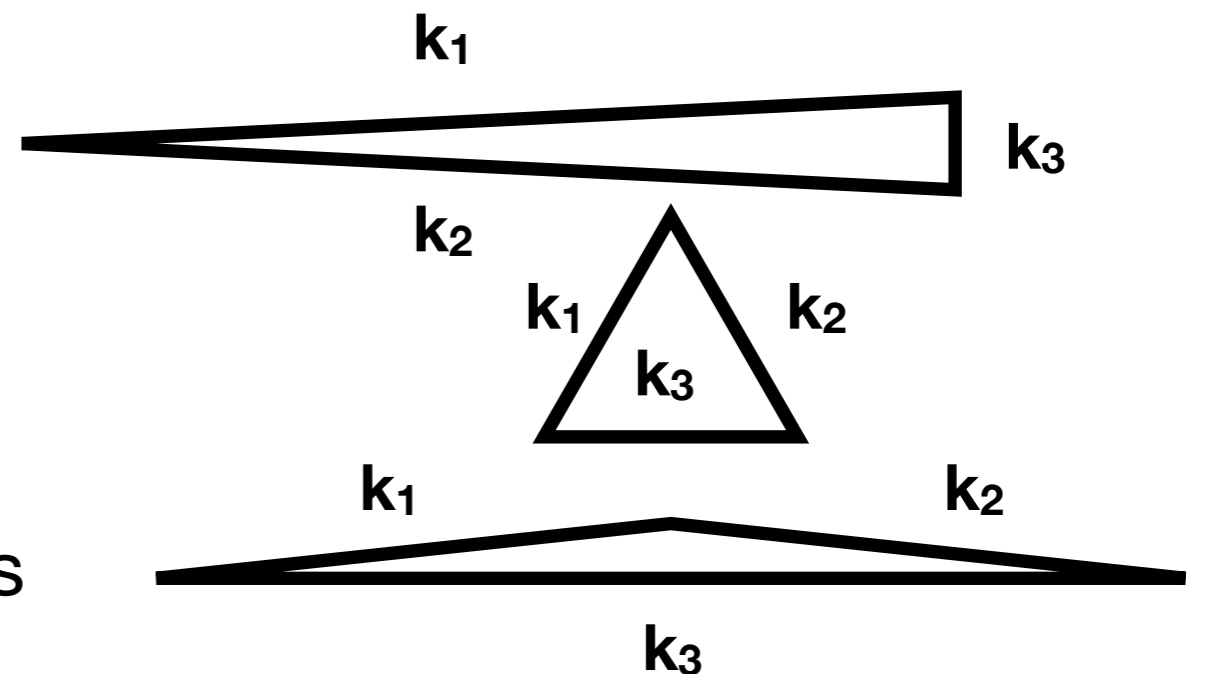
- Unique window into physics of early universe
 - Highly complementary to B mode searches

- Theoretical models of inflation give us predictions

$$\langle \zeta(k_1)\zeta(k_2)\zeta(k_3) \rangle \propto \text{shape} \times f_{NL}$$

- Three commonly studied shapes:

- Local - Multi-field inflation?
- Equilateral - $c_s \neq 1$?
- Orthogonal - Non-bunch Davies initial conditions?



See e.g. Chen (2010) for a review

How to measure non-Gaussianity?

- Ideally measure every configuration

$$\langle a_{\ell_1, m_1} a_{\ell_2, m_2} a_{\ell_3, m_3} \rangle \propto \langle \zeta(k_1) \zeta(k_2) \zeta(k_3) \rangle$$

- Computational prohibitive and signal is any triplet is expected to be small
- Two broad classes of estimators
 - Compress the information - KSW estimator
 - Compress the data - Modal and Binned estimator
- Regardless of estimator, to measure f_{NL} need

$$\hat{f}_{NL} \propto \sum_{\ell_i} b_{\ell_1, \ell_2, \ell_3} a_{\ell_1, m_1} a_{\ell_2, m_2} a_{\ell_3, m_3}$$

Komatsu, Spergel and Wandelt (2005)
Bucher et al (2013,2015)
Fergusson et al (2009)

Current Constraints

Shape ($\zeta\zeta\zeta$)	Constraint
Local	-0.9 ± 5.1
Equilateral	-26 ± 47
Orthogonal	-38 ± 23
Shape ($\zeta\zeta h$)	Constraint
Local	-48 ± 28
Shape (hhh)	Constraint
Equilateral	8 ± 11

For context, when $f_{\text{NL}} \sim 1$
 $\frac{\langle \zeta(k_1)\zeta(k_2)\zeta(k_3) \rangle}{\sqrt{P_\zeta(k_1)P_\zeta(k_2)P_\zeta(k_3)}} \sim 10^{-5}$

See e.g. Azadeh's talk

Planck Collaboration XI (2019)

Shiraishi et al (2018)

Future Constraints

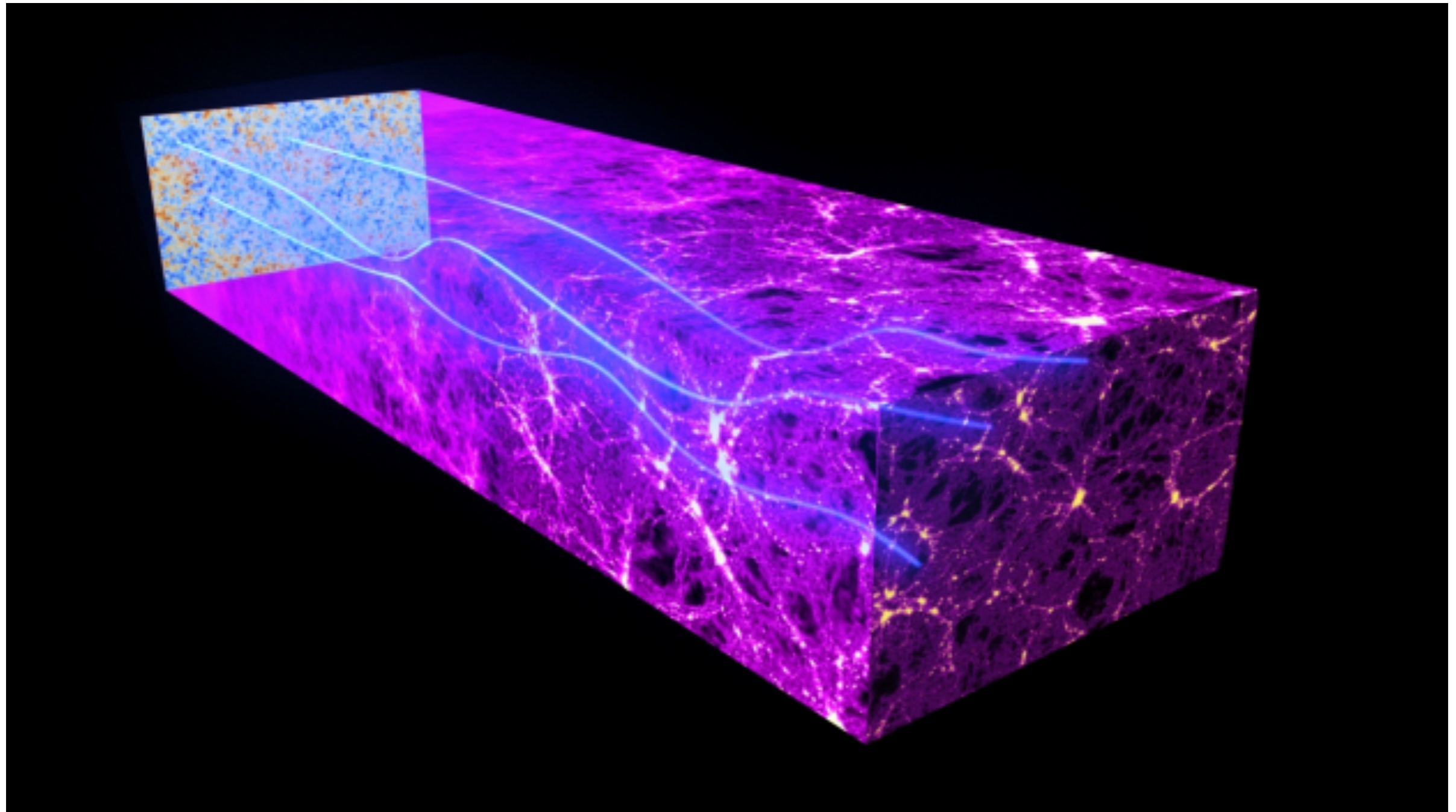
See e.g. David Alonso's talk yesterday for more information on the Simons Observatory (SO)

Shape ($\zeta\zeta\zeta$)	Current	SO constraint
Local	-0.9 ± 5.1	3
Equilateral	-26 ± 47	24
Orthogonal	-38 ± 23	13
Shape ($\zeta\zeta h$)	Constraint	
Local	-48 ± 28	1
Equilateral	-	8
Orthogonal	-	3

Planck Collaboration (2019)

The Simons Observatory Collaboration XI (2018)

Recap: CMB lensing



Lensing effects on the bispectrum

- CMB is non-Gaussian:
 - Planck detected CMB lensing at $>40\sigma$!
- Two consequences for bispectra analyses:
 1. Signal contamination:
Bias of CMB lensing on primordial non-Gaussianity
This has been well studied e.g. Lewis et al (2011)
 2. Extra source of noise:
Degradation to the SNR of bispectrum estimators caused by lensing as first pointed out by Babich & Zaldarriaga (2004).

Bispectrum Variance

- Schematic variance of the primordial non-Gaussianity estimator

$$\langle f_{NL}^{local^2} \rangle \propto \sum_{\{l_i\}} b_{l_1, l_2, l_3} \langle a_{l_1, m_1} a_{l_2, m_2} a_{l_3, m_3} a_{l_4, m_4} a_{l_5, m_5} a_{l_6, m_6} \rangle b_{l_4, l_5, l_6}$$

- For a Gaussian CMB, this simplifies!

$$\langle f_{NL}^{local^2} \rangle \propto \sum_{\{l_i\}} b_{l_1, l_2, l_3} C_{l_1} C_{l_2} C_{l_3} b_{l_1, l_2, l_3}$$

- Diagrammatically (one perm. only)

$$\begin{array}{l} a_{l_1, m_1} \text{-----} a_{l_4, m_4} \\ a_{l_2, m_2} \text{-----} a_{l_5, m_5} \\ a_{l_3, m_3} \text{-----} a_{l_6, m_6} \end{array}$$

Lensing contributions

- As Kimmy and Toshiya described yesterday

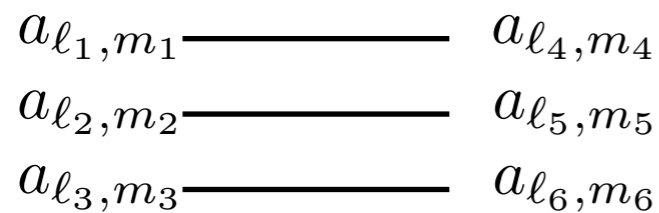
$$\langle a_{\ell,m} a_{\ell',m'} \rangle_{CMB} = \sum_{\ell_i, m_i} f_{\ell,\ell',L} \phi_{L,M}$$

where f is the lensing coupling kernel (Hu & Okamoto, 2002).

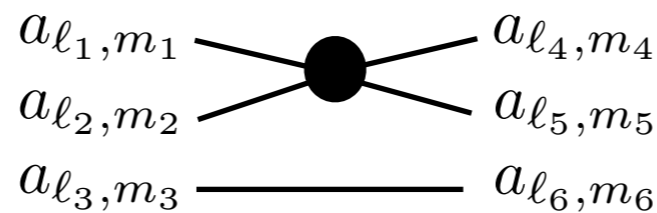
- This induces a connected four point function for the bispectrum variance

$$\langle f_{NL}^{local^2} \rangle \propto \langle f_{NL}^{local^2} \rangle_{gaus} + \sum_{\{\ell_i\}} b_{\ell_1,\ell_2,\ell_3} C_{\ell_1} T_{\ell_2,\ell_3,\ell_5,\ell_6} b_{\ell_1,\ell_5,\ell_6}$$

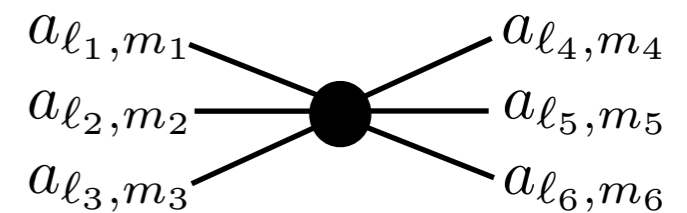
- Diagrammatically (one perm. only):



Gaussian/ Disconnected



Connected Four Point



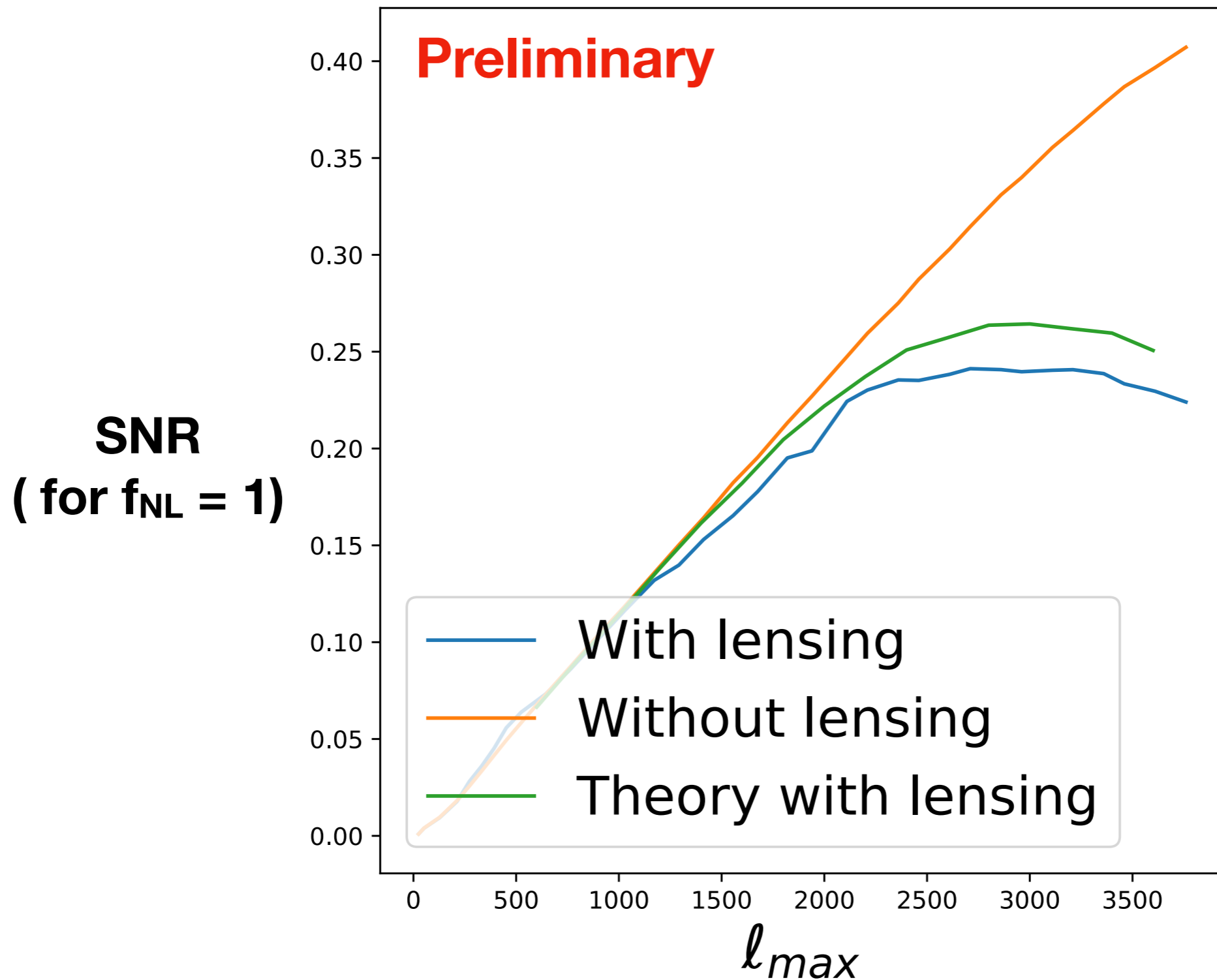
Connected Six point

(higher order term)

- Acts like extra noise to hinder bispectrum measurements!!

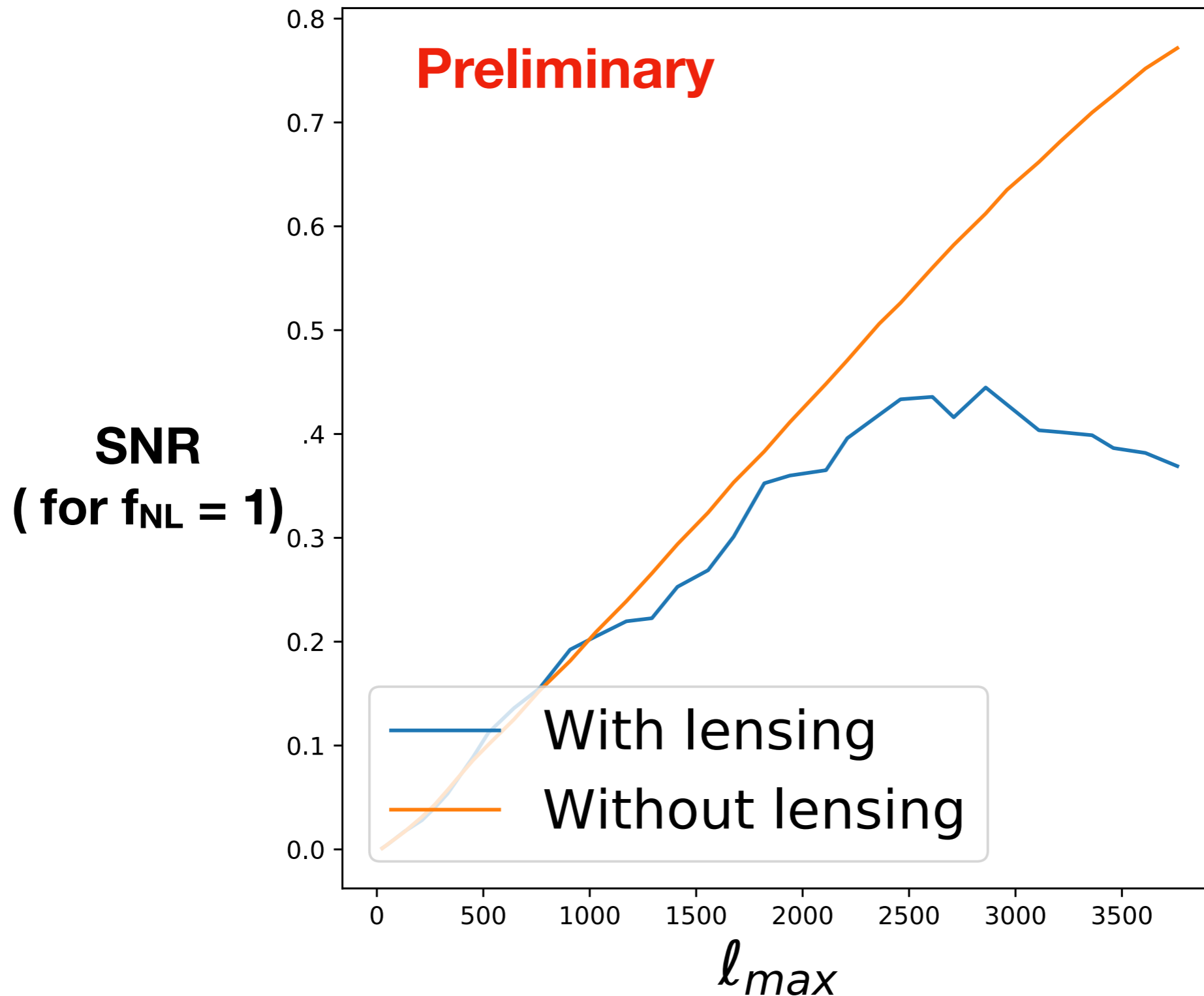
How important is this effect?

Local non-Gaussianity SNR for temperature measurements
CV limit



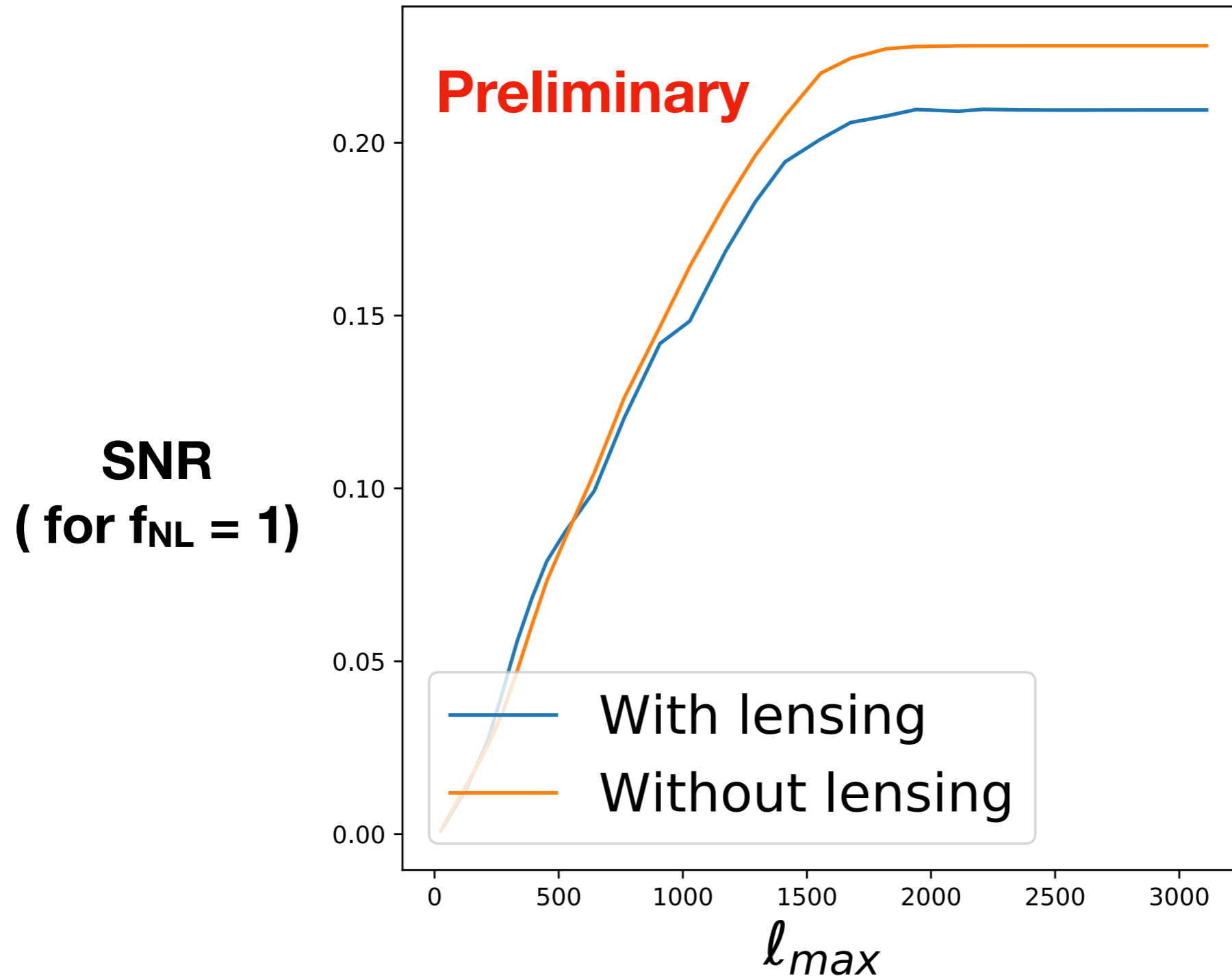
How important is this effect?

Local non-Gaussianity SNR for temperature and polarisation measurements
CV limit



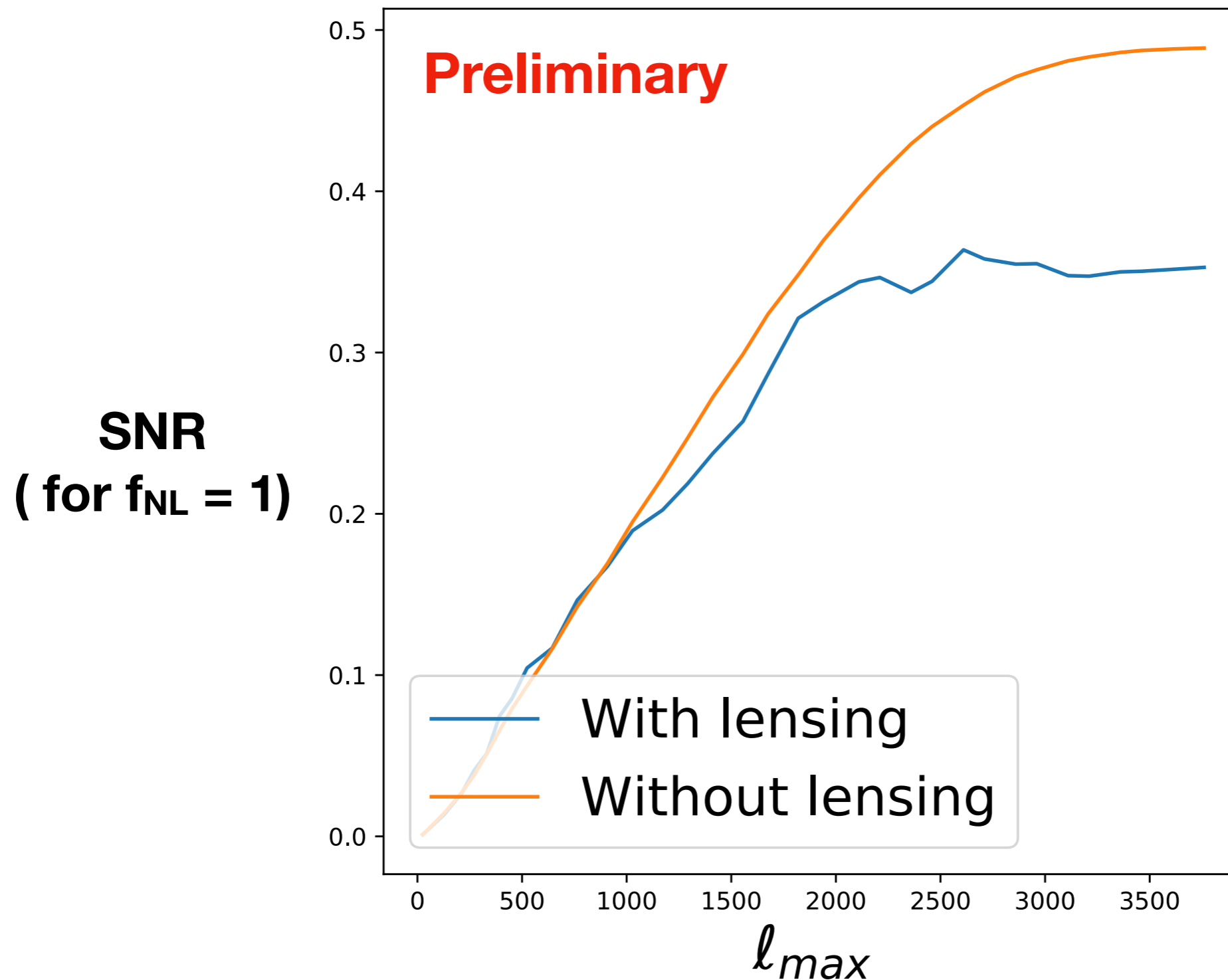
How important was this effect for Planck?

Local non-Gaussianity SNR for measurements with Planck levels of noise



How important is this effect for SO?

Local non-Gaussianity SNR for measurements with SO levels of noise



Why is this effect so large?

- Local primordial non-Gaussianity
 - Modulation of small scale power by large wavelength mode
- CMB Lensing:
 - Modulation of small scale power by intervening degree scale lens
- Small scale part of local bispectrum estimation like suboptimal lensing reconstruction! Thus it becomes sensitive to the lensing four point function.

Is there a simple solution?

- Subtract from the estimator a similar term which explicitly picks up the lensing modes
 - i.e. deproject the lensing modes

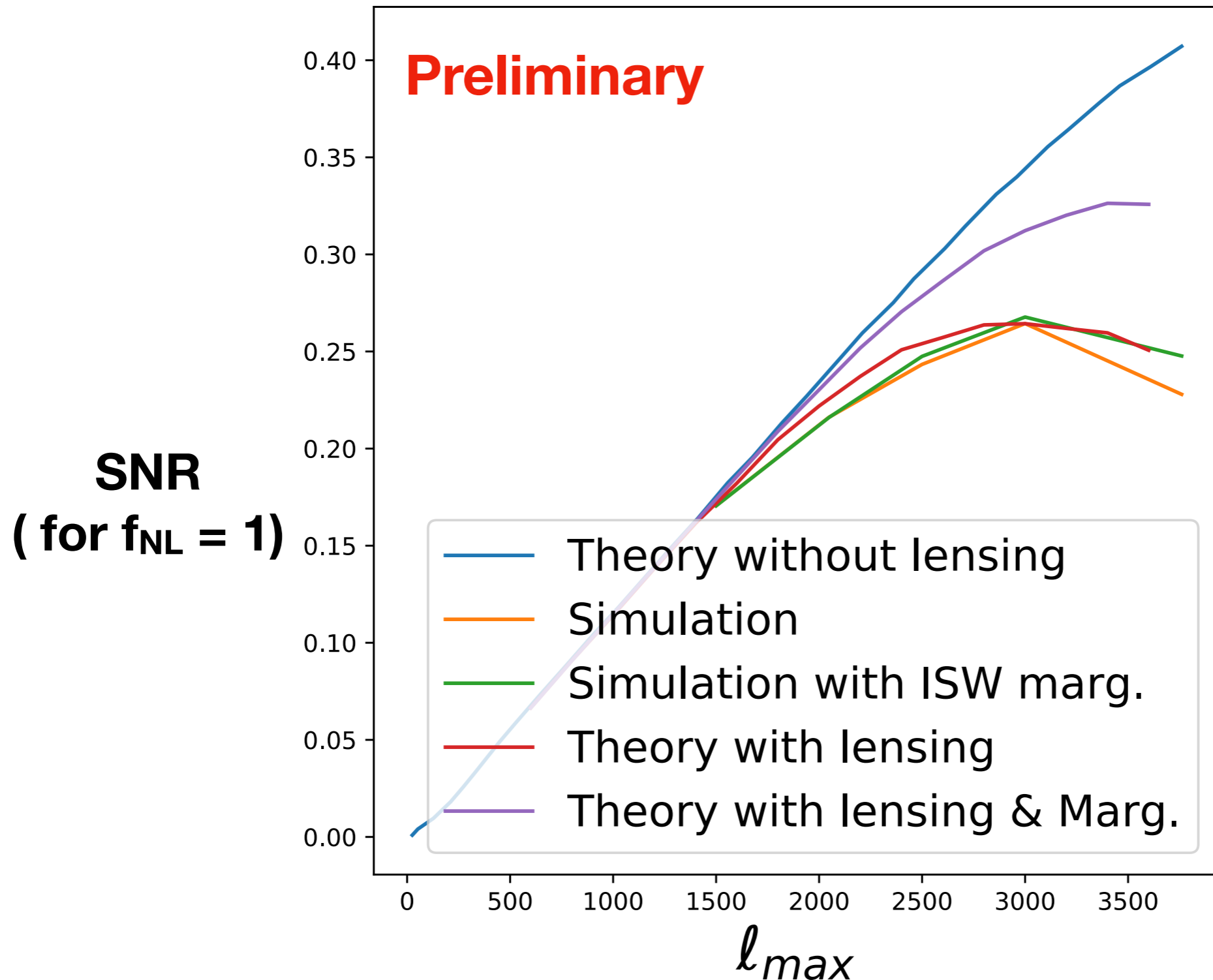
- Schematically:

$$f^{\text{lensing-free}} = f^{\text{local}} - \sum_{\ell} W(\ell) a_{\ell,m} \hat{\phi}$$

- where $\hat{\phi}$ is the quadratically reconstructed lensing field
- ISW-lensing marginalisation does this!

Only to first order!

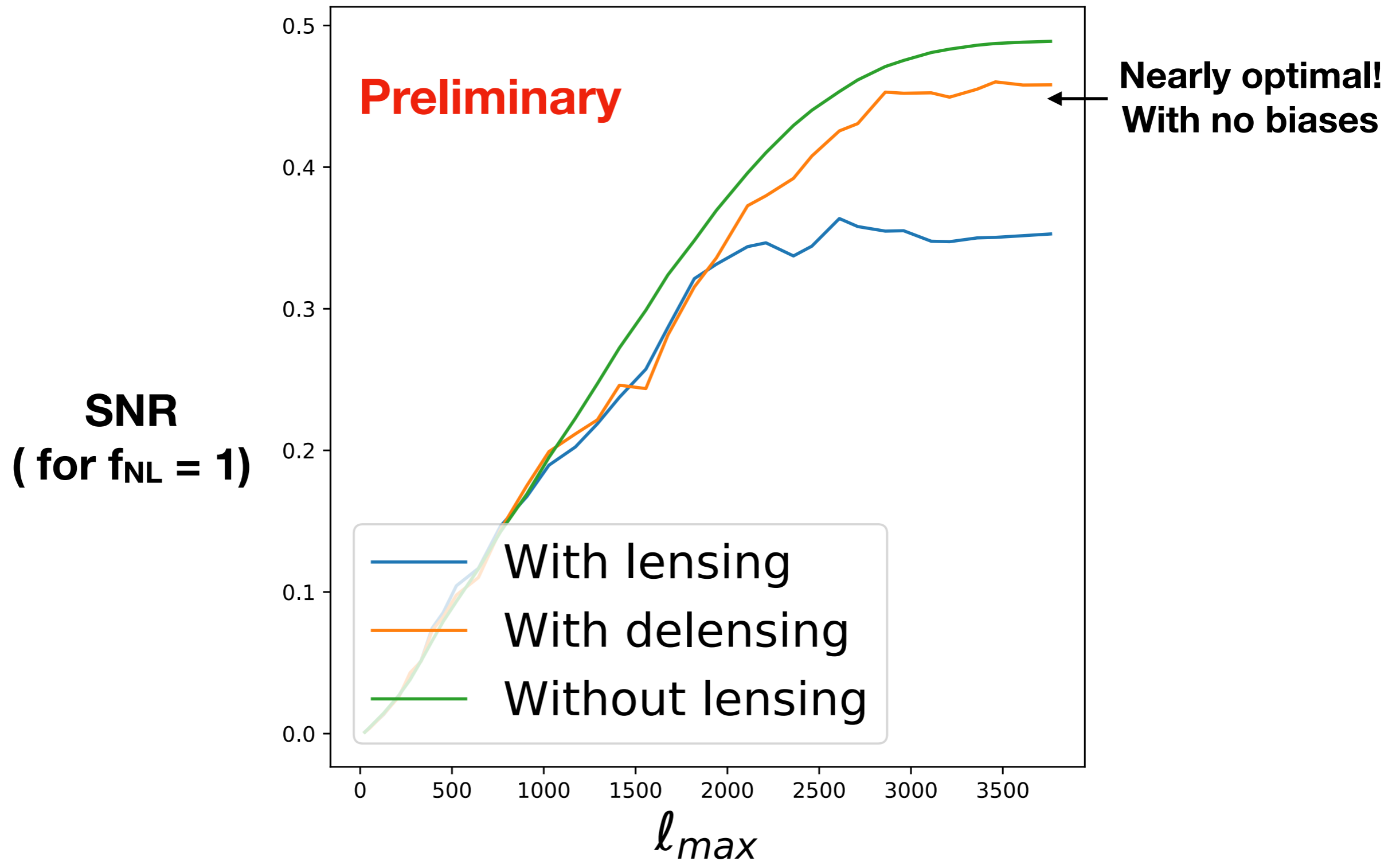
Local non-Gaussianity SNR for temperature measurements



Delensing the CMB

- What is delensing?
 - Remap the pixels using an estimated lensing potential to reconstruct the fluctuations as seen at the LSS.
 - Lensing is: $T(\vec{n}) = \tilde{T}(\vec{n} + \nabla\phi)$
 - Delensing is: $\hat{\tilde{T}}(\vec{n}) \approx \tilde{T}(\vec{n} - \nabla\hat{\phi})$
- Potential biases from correlations between reconstruction noise and estimator maps

Delensing for an SO-like experiment



Conclusions

- Simons Observatory will extend beyond Planck's constraints on primordial non-Gaussianity!
 - Step towards $f_{\text{NL}} \sim 1$
- Lensing of the CMB can act like noise for local (and orthogonal) primordial bispectrum estimators
- For next generation surveys delensing can remove this excess noise to achieve almost optimum performance
- Beside B mode delensing, most useful application of delensing!