



University of
Zurich^{UZH}

Thermal-Dynamic Dark Matter

Finite Temperature Effects in the Early Universe

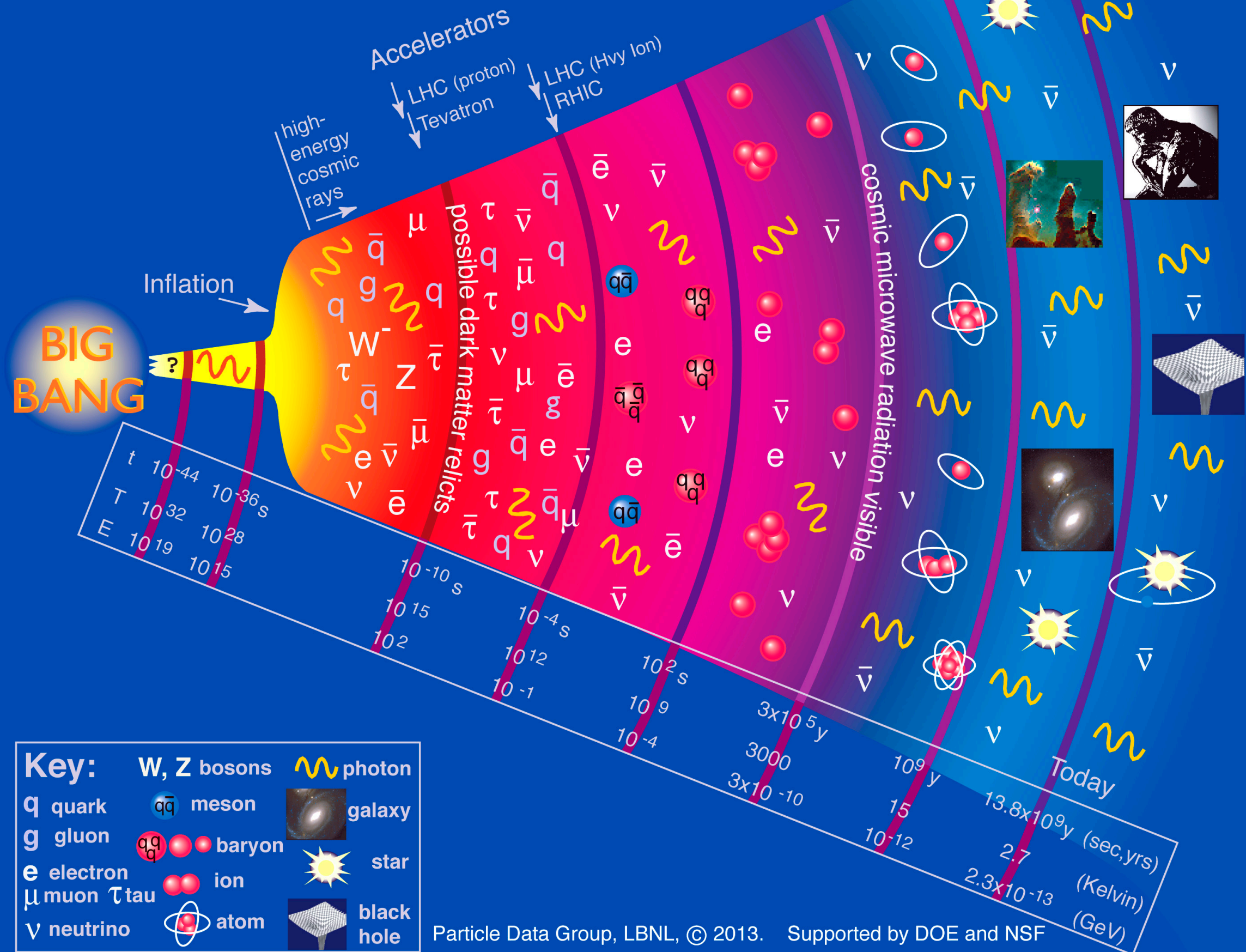
Michael J. Baker

Next Frontiers in the Search for Dark Matter, GGI
23 Sep 2019

Based on [1608.07578](#) (PRL), [1712.03962](#) (JHEP), and [1811.03101](#) (JHEP)

MJB, M. Breitbach, L. Mittnacht, J. Kopp

History of the Universe



The Main Message

Finite temperature effects, while often ignored, can have a dramatic consequence on the relic abundance of particles

Show this in several production mechanisms of dark matter

Approach

One BSM model with several new scenarios for producing DM:

- Instantaneous freeze-out
- Kinematically induced freeze-in
- Decaying dark matter

Main tools:

- One-loop effective potential at finite temperature
- Boltzmann equations

- Outline

- Model
- Particle physics and the effective potential at finite temperature
 - Instantaneous freeze-out
 - Kinematically induced freeze-in
- Two step phase transition (vev flip-flop)
 - Decaying dark matter

Model

- BSM Model

Field	Spin	\mathbb{Z}_2	mass scale
S	0	+1	0.1 GeV – 500 GeV
χ	$\frac{1}{2}$	−1	5 GeV – 5 TeV
ψ	$\frac{1}{2}$	−1	5 GeV – 5 TeV

$$\begin{aligned}
\mathcal{L} \supset & y_\chi \bar{\chi} \chi S + y_\psi \bar{\psi} \psi S + [y_{\chi\psi} \bar{\psi} \chi S + h.c.] + m_\chi \bar{\chi} \chi + \tilde{m}_\psi \bar{\psi} \psi \\
& + \mu_H^2 H^\dagger H - \lambda_H (H^\dagger H)^2 + \frac{1}{2} \mu_S^2 S^2 - \frac{\lambda_{S^4}}{4!} S^4 \\
& - \frac{\lambda_{S^3}}{3!} \mu_S S^3 - \lambda_{p3} \mu_S S (H^\dagger H) - \frac{\lambda_{p4}}{2} S^2 (H^\dagger H)
\end{aligned}$$

Particle Physics and the Effective Potential at Finite T

- Particle Physics at Finite Temperature

Can we apply our usual zero-T techniques?
What happens to vertices and propagators?

Imaginary-time formalism: field operators quantized on

$$0 \leq it \leq 1/T$$

‘The great advantage of this formalism is that perturbation theory may still be organised into a diagrammatic expansion with the same vertices as at $T = 0$.’ [Weldon, 1983]

- What happens to propagators?
-

The scalar two-point Green's function is

$$D(\omega_n, \vec{p}) = \frac{1}{\omega_n^2 - \vec{p}^2 - m^2 - \pi(\omega_n, \vec{p})}$$

$$\pi(\omega_n, \vec{p}) \underset{\text{I.R.}}{\overset{\text{1-loop}}{\approx}} \pi^{(1)}(\omega_n = 0, \vec{p} = \vec{0}) \stackrel{\text{e.g.}}{=} \frac{\lambda T^2}{4}$$

Propagator pole receives FT correction

Also for fermions, but negligible for us

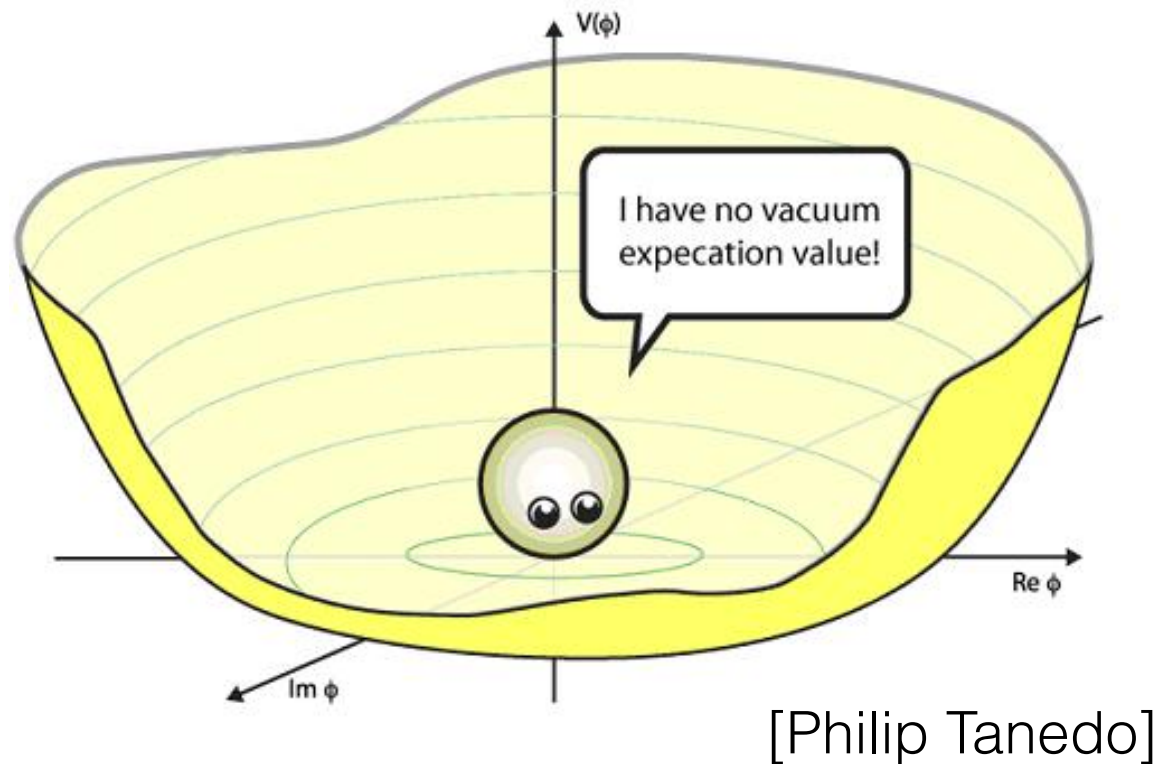
- Particle Physics at Finite Temperature

We can apply our usual zero-T Feynman rules,
after substituting T-dependent masses

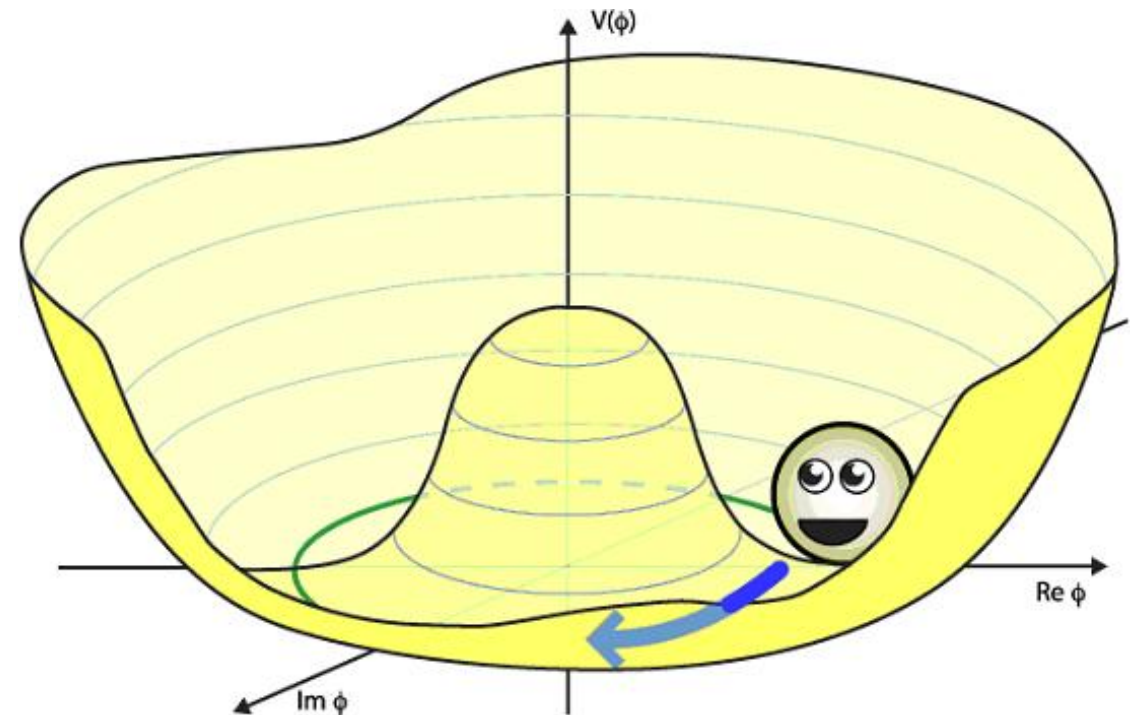
What about vevs?

- The Effective Potential

$$T \gg T_{EW}$$



$$T \sim 0$$



The effective potential can be calculated in FTQFT using a loop expansion, with leading contribution

$$V^{\text{eff}} = V^{\text{tree}} + V^{\text{CW}} + V^T + V^{\text{daisy}}$$

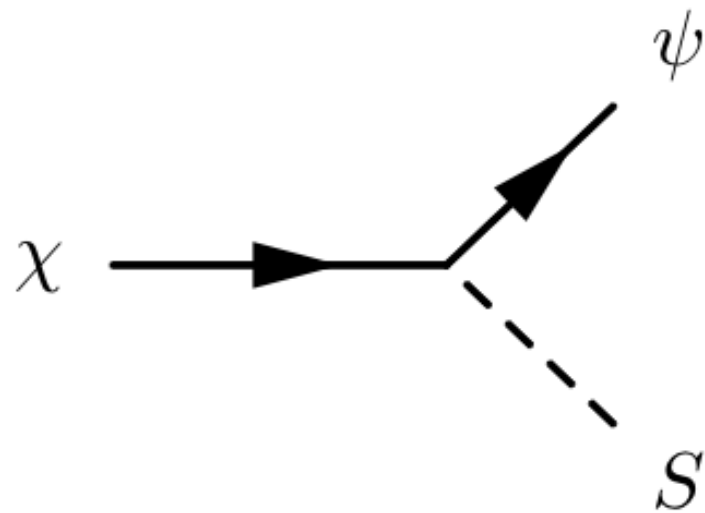
Instantaneous Freeze-out

- Instantaneous Freeze-out

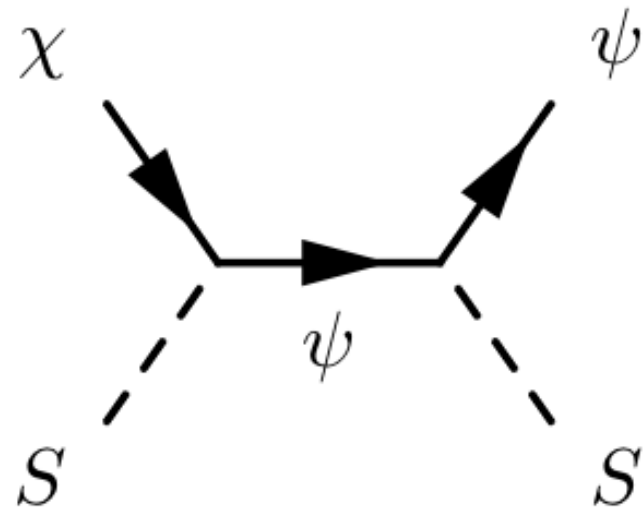
$$\begin{aligned}
 \mathcal{L} \supset & \overset{\sim 0}{\cancel{y_\chi \bar{\chi} \chi S}} + \overset{2}{y_\psi \bar{\psi} \psi S} + \overset{\sim 10^{-7}}{[y_{\chi\psi} \bar{\psi} \chi S + h.c.]} + m_\chi \bar{\chi} \chi + \tilde{m}_\psi \bar{\psi} \psi \\
 & + \mu_H^2 H^\dagger H - \lambda_H (H^\dagger H)^2 + \frac{1}{2} \mu_S^2 S^2 - \frac{\lambda_{S^4}}{4!} S^4 \overset{1}{\leftarrow} \\
 & - \frac{\lambda_{S^3}}{3!} \mu_S \cancel{S^3} - \lambda_{p3} \mu_S \cancel{S(H^\dagger H)} - \frac{\lambda_{p4}}{2} S^2 (H^\dagger H) \overset{\uparrow}{\leftarrow} \overset{10^{-5} - 10^{-3}}{}
 \end{aligned}$$

- ψ and S will remain in contact with the thermal bath throughout
- $m_\psi(T) = \tilde{m}_\psi + y_\psi \langle S \rangle(T)$

- Instantaneous Freeze-out



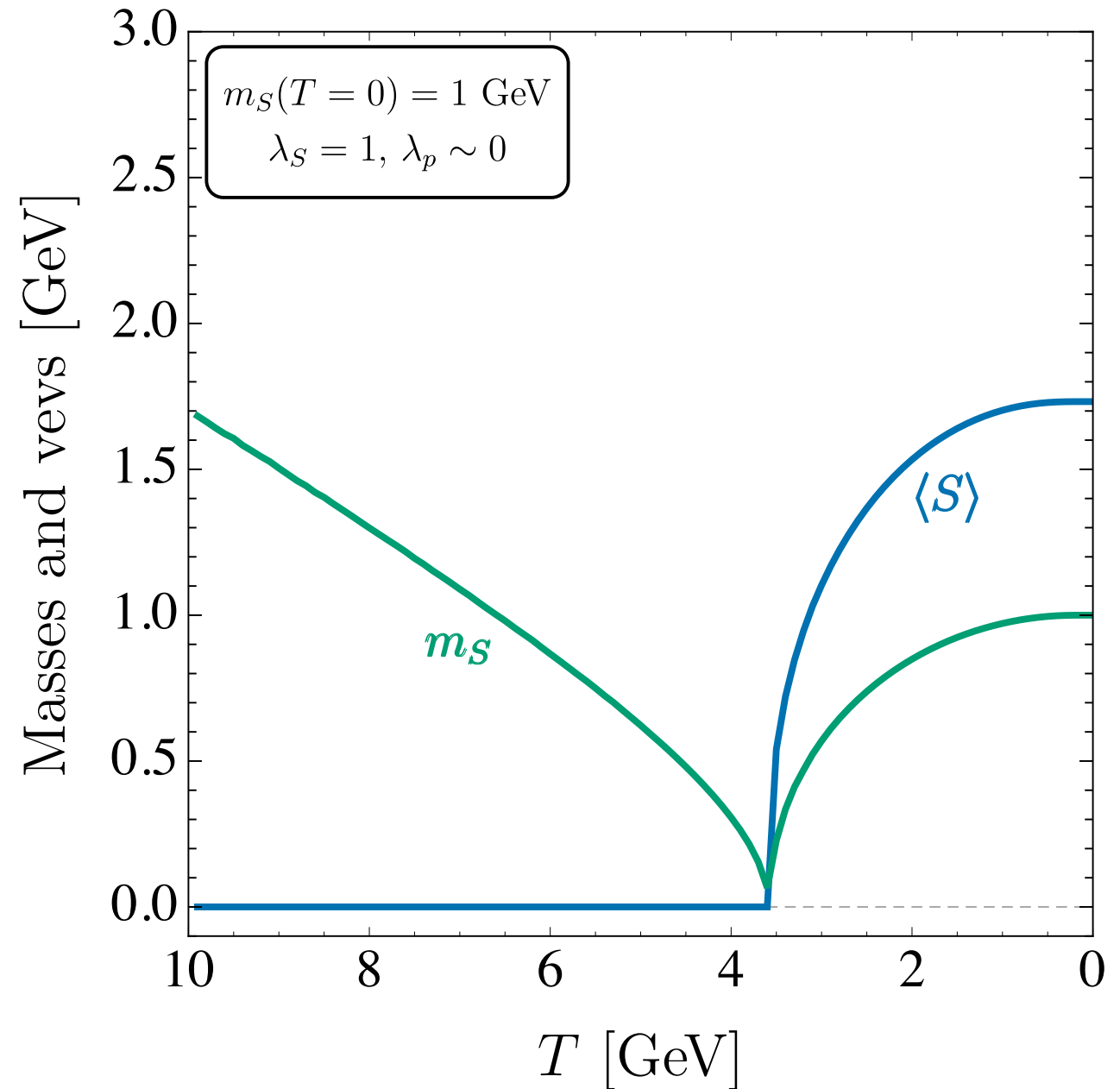
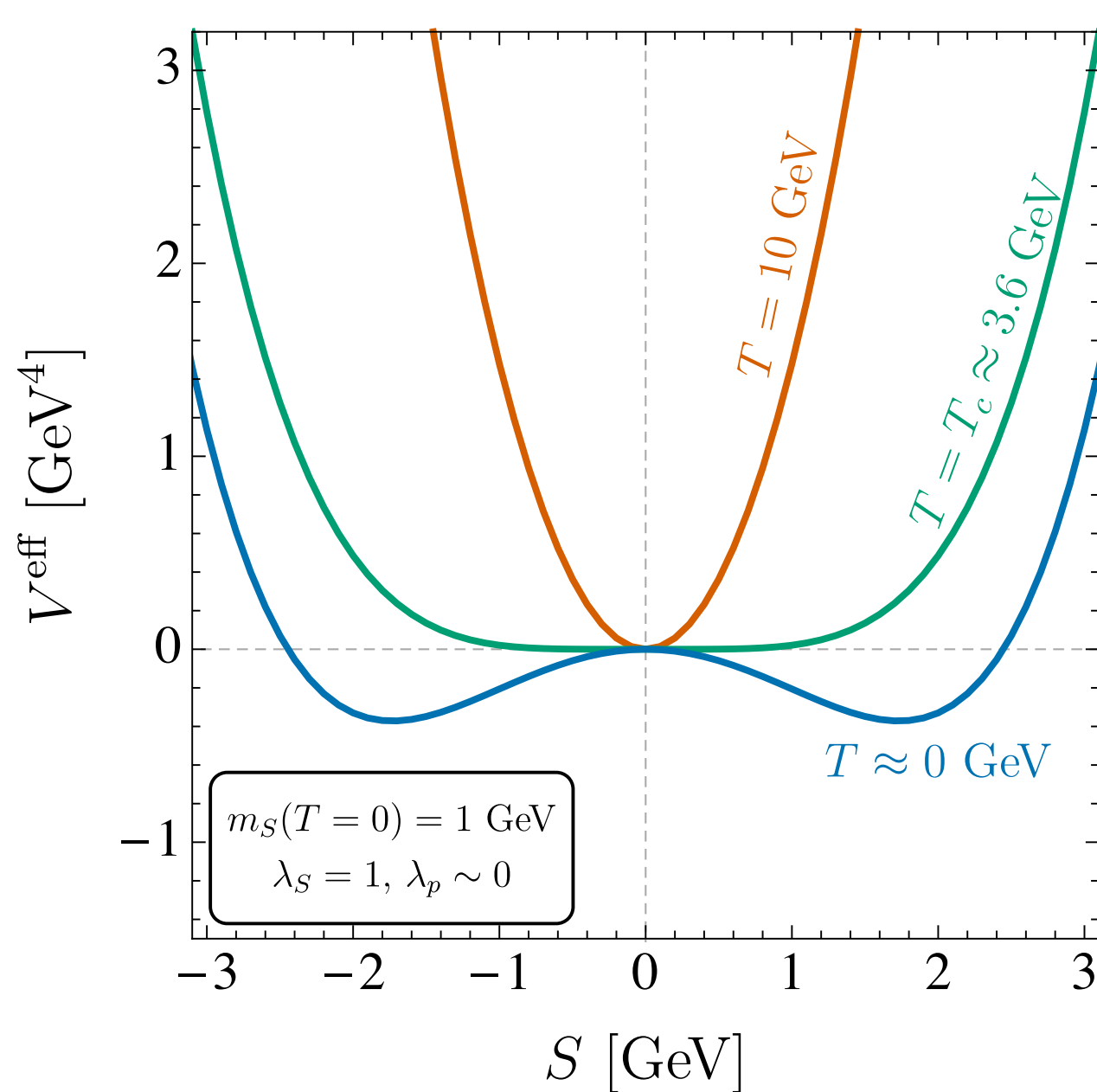
Open when
 $m_\chi > m_\psi(T) + m_S(T)$



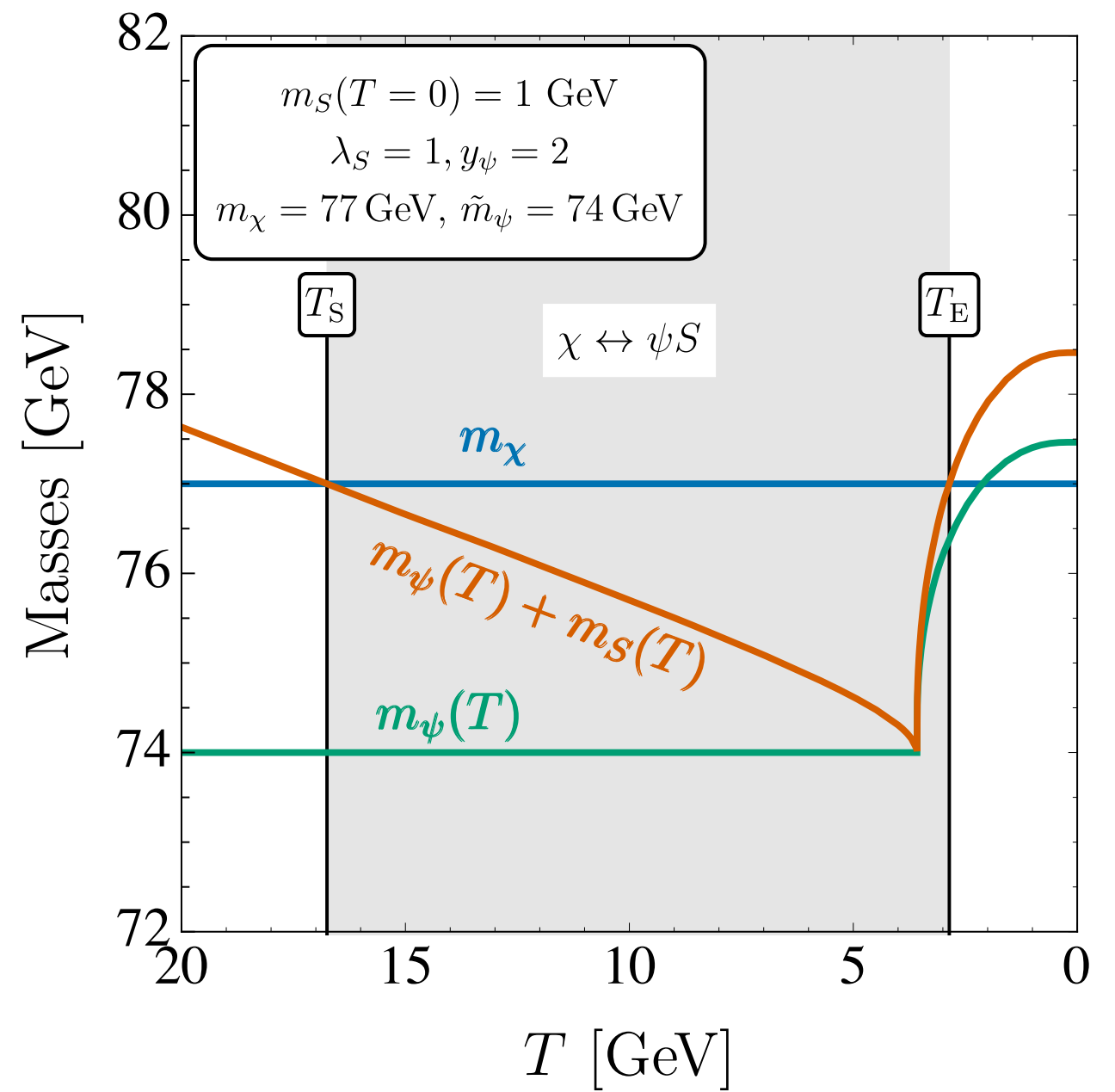
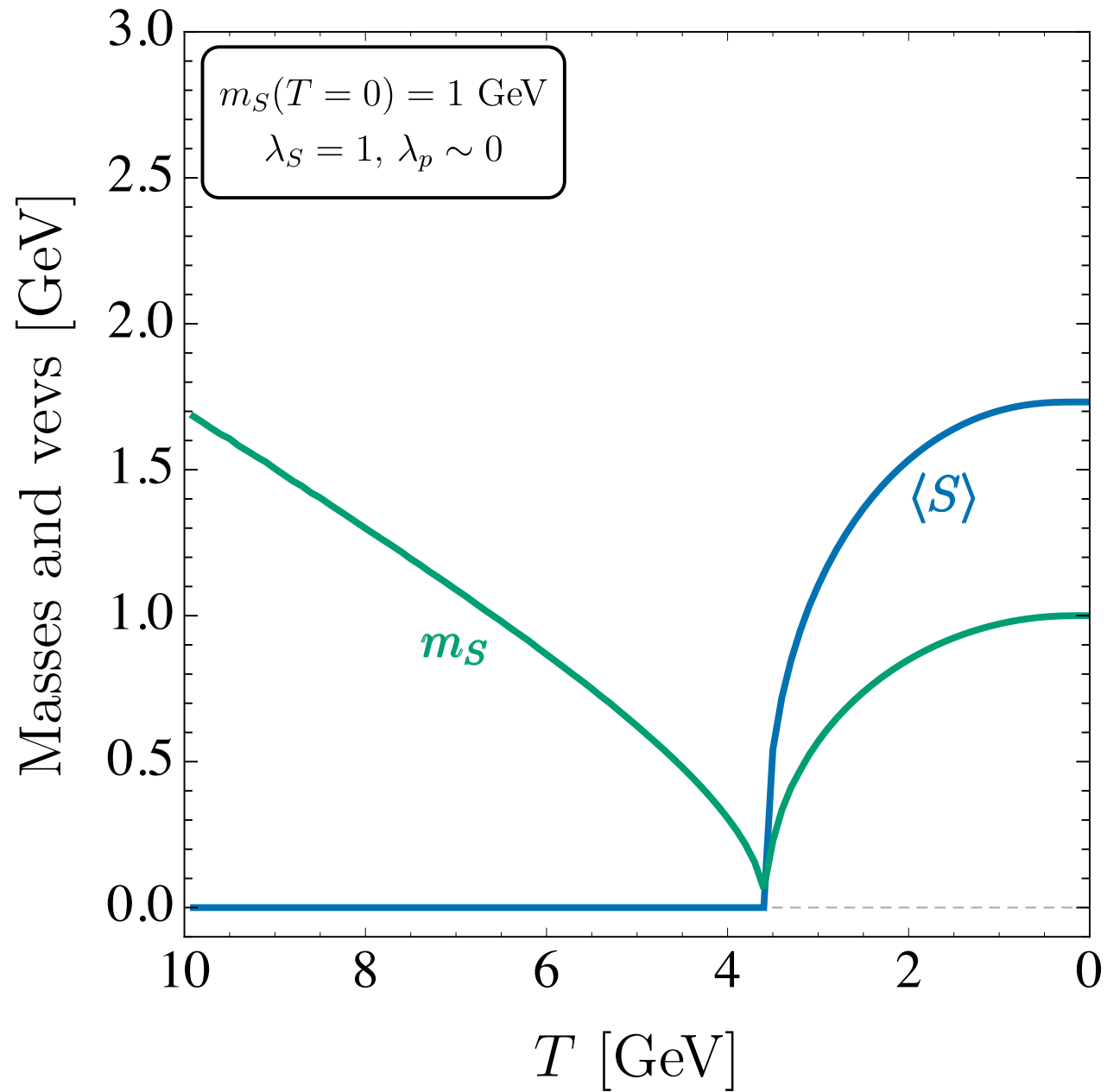
Suppressed by
 $x^3 = \left(\frac{m_\chi}{T}\right)^3$

- Instantaneous Freeze-out

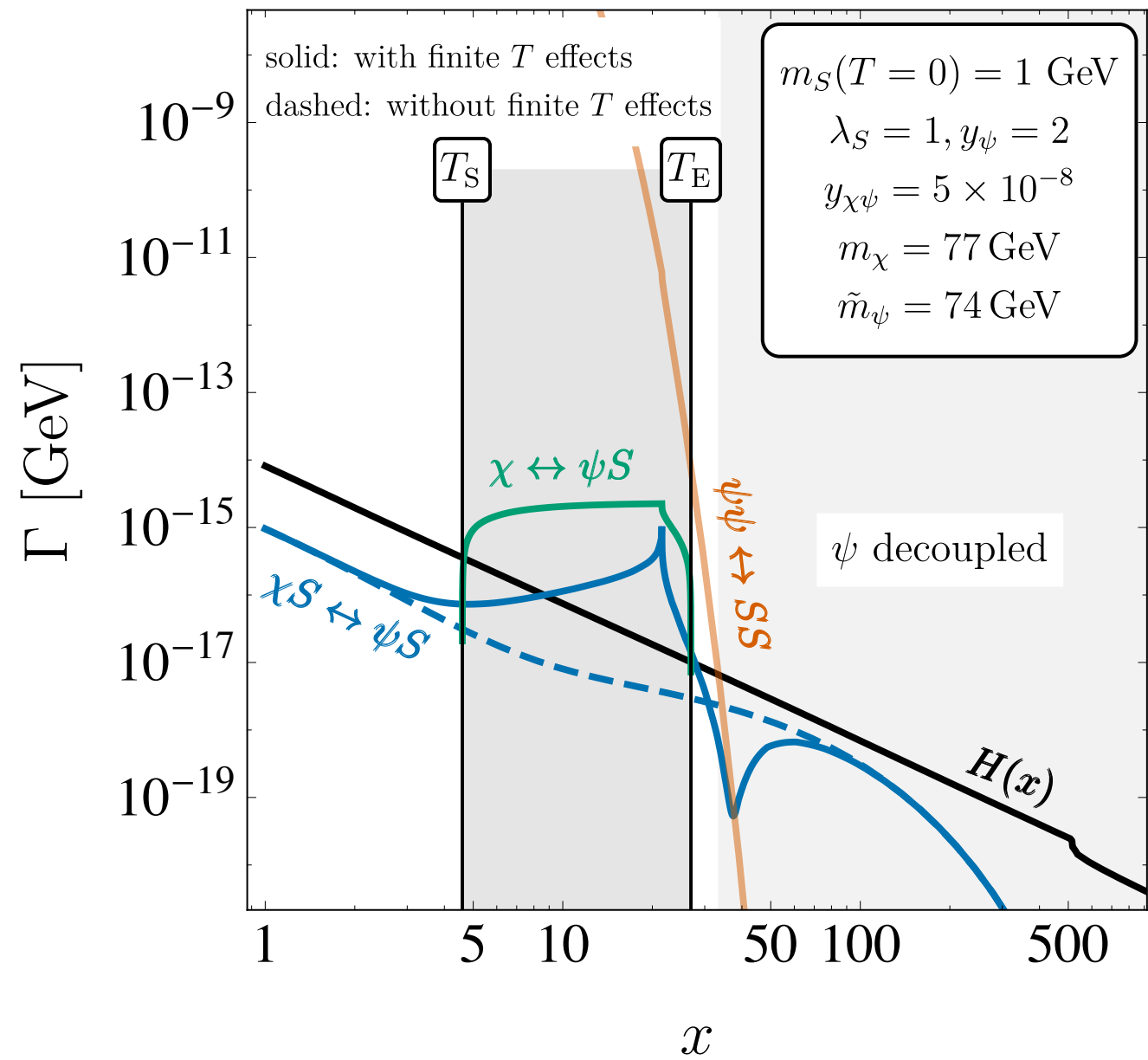
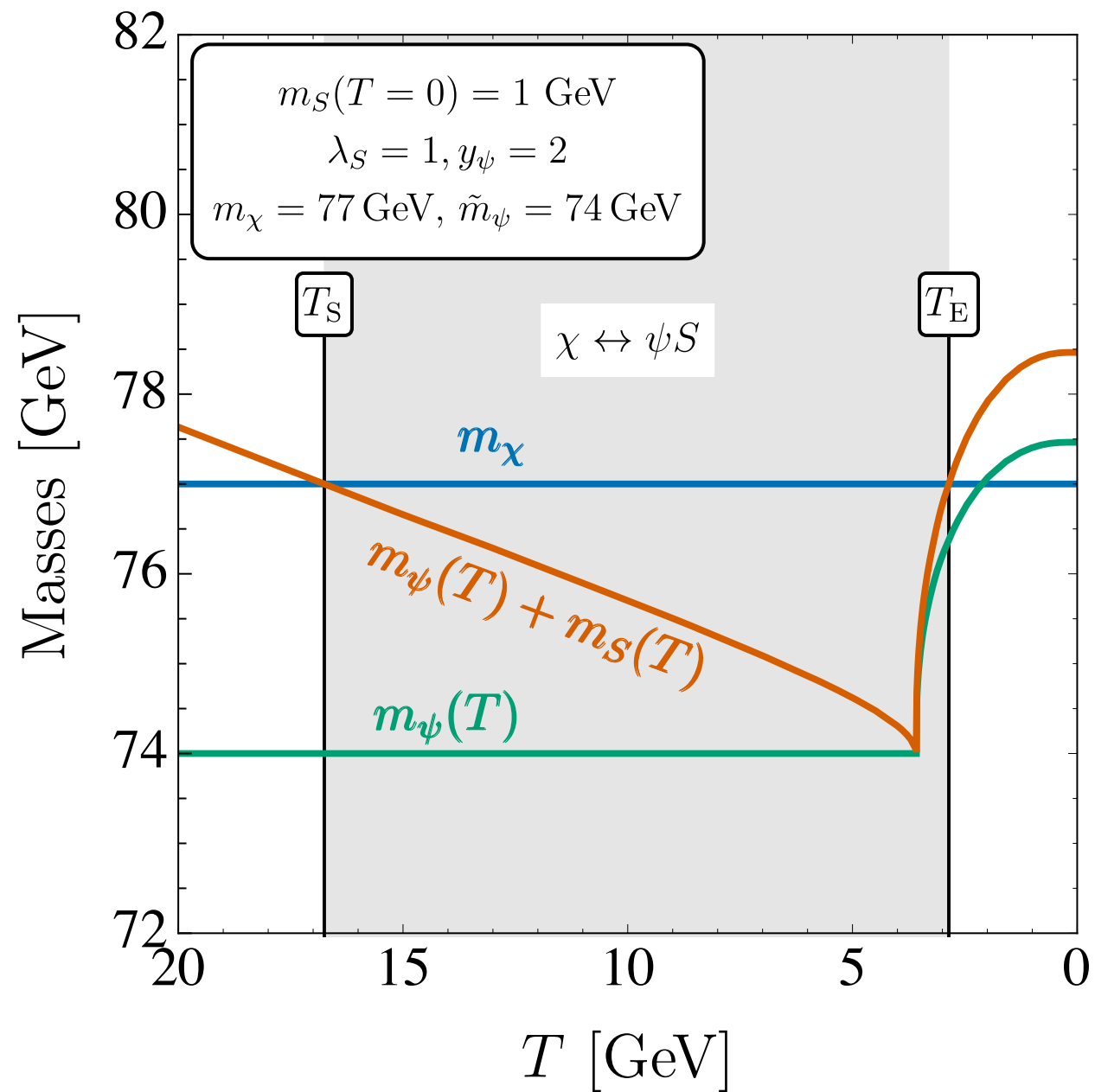
Portal coupling is small, so $V^{\text{eff}}(H, S, T) = V^{\text{eff}}(H, T) + V^{\text{eff}}(S, T)$



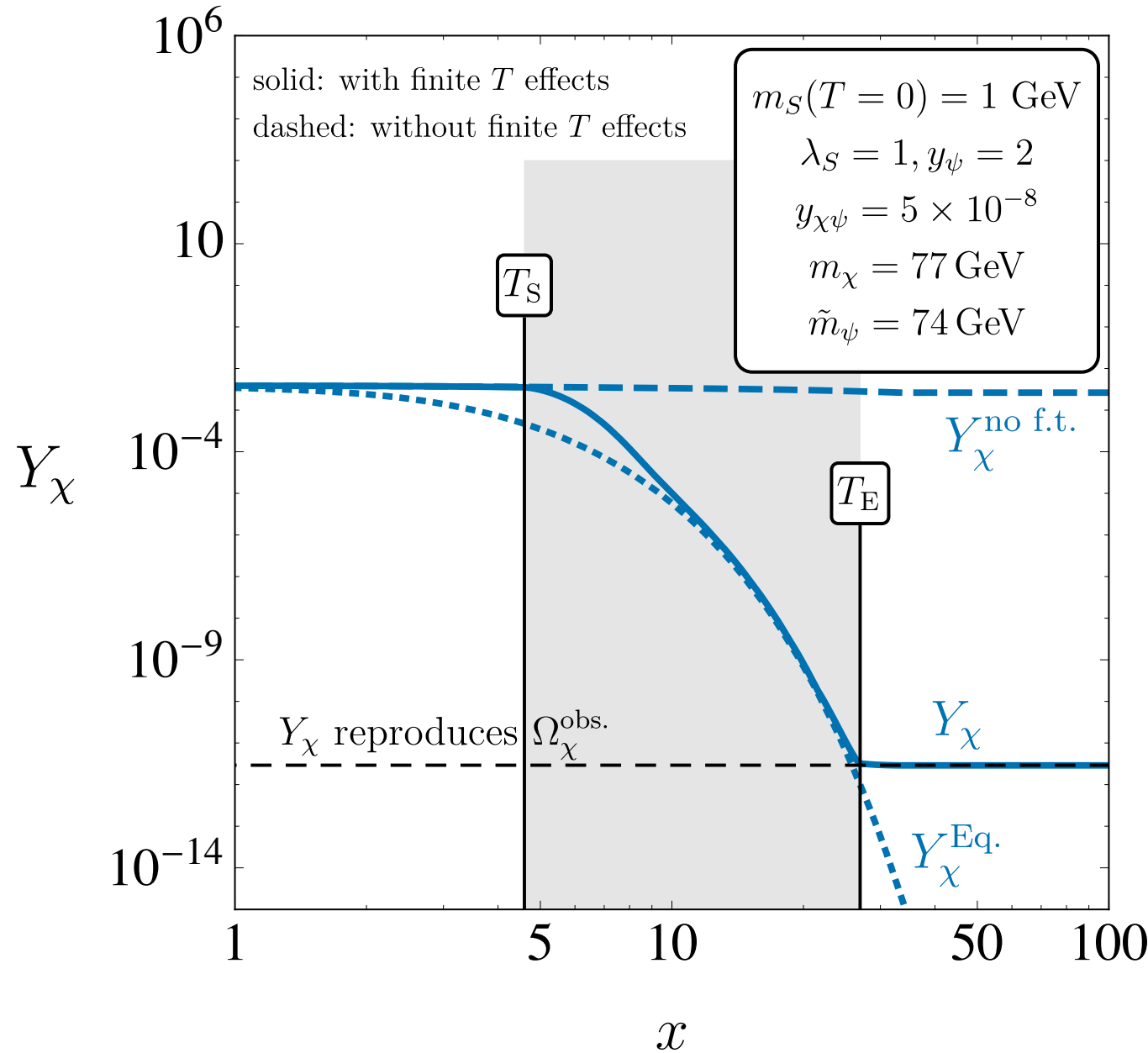
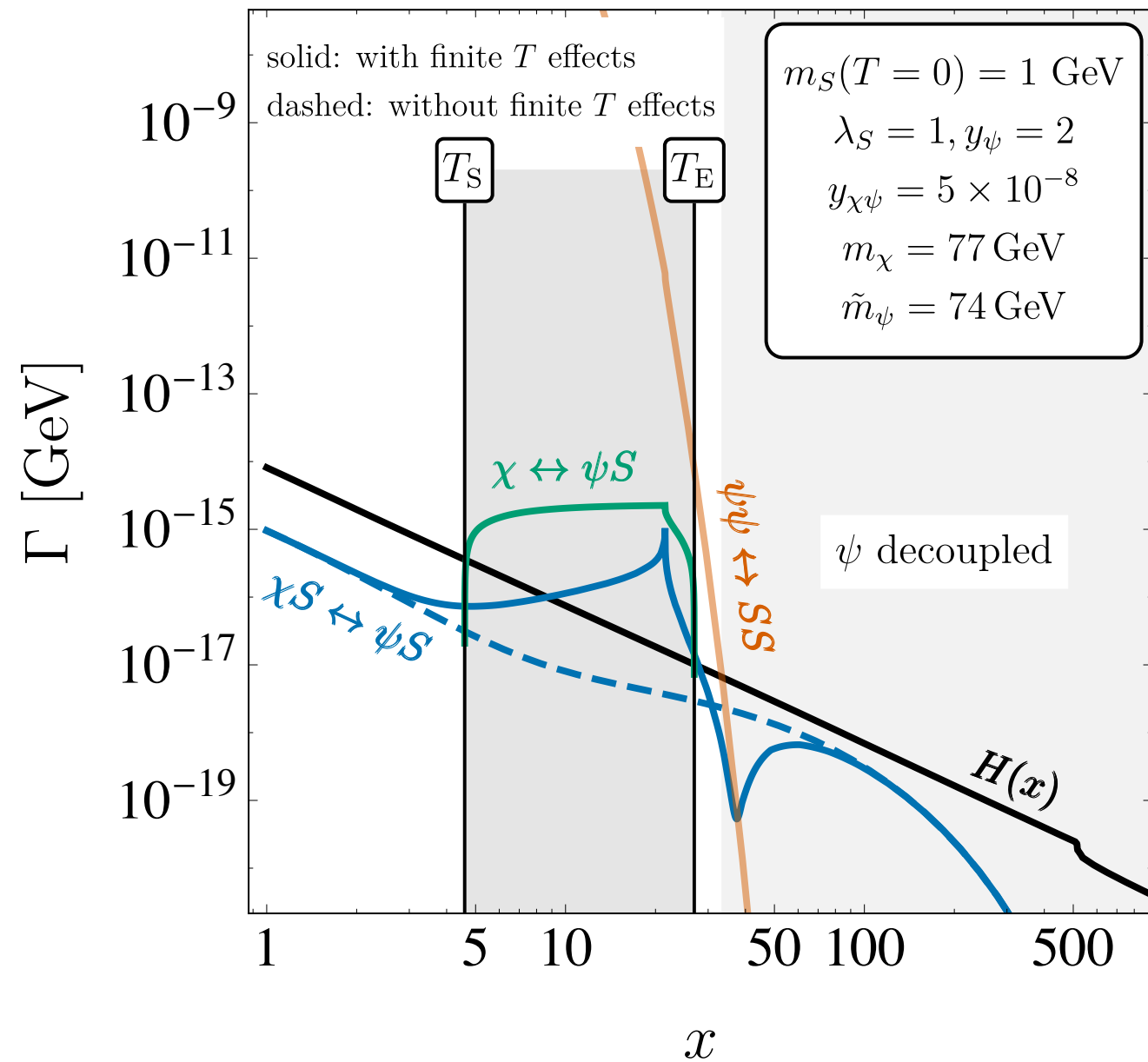
- Instantaneous Freeze-out



- Instantaneous Freeze-out



- Instantaneous Freeze-out



We have demonstrated a new method of obtaining the relic abundance
 Without finite T effects, yield would be 10 orders of magnitude too large

Kinematically Induced Freeze-in

- Kinematically Induced Freeze-in

we'll assume ψ stays in thermal equilibrium via other NP

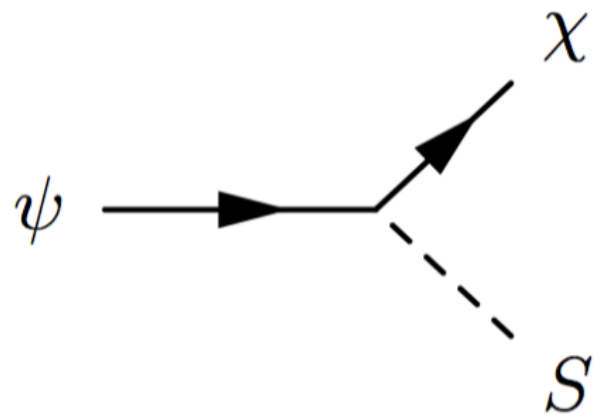
$$\begin{aligned}
 \mathcal{L} \supset & \cancel{y_\chi \bar{\chi} \chi S} + y_\psi \bar{\psi} \psi S + [y_{\chi\psi} \bar{\psi} \chi S + h.c.] + m_\chi \bar{\chi} \chi + \tilde{m}_\psi \bar{\psi} \psi \\
 & + \mu_H^2 H^\dagger H - \lambda_H (H^\dagger H)^2 + \frac{1}{2} \mu_S^2 S^2 - \frac{\lambda_{S4}}{4!} S^4 \quad 1 \\
 & - \cancel{\frac{\lambda_{S3}}{3!} \mu_S S^3} - \cancel{\lambda_{p3} \mu_S S (H^\dagger H)} - \frac{\lambda_{p4}}{2} S^2 (H^\dagger H)
 \end{aligned}$$

Annotations:
 - 0.01 points to y_ψ
 - $\sim 10^{-12}$ points to $y_{\chi\psi}$
 - 1 points to λ_{S4}
 - $\sim 10^{-3}$ points to λ_{p4}

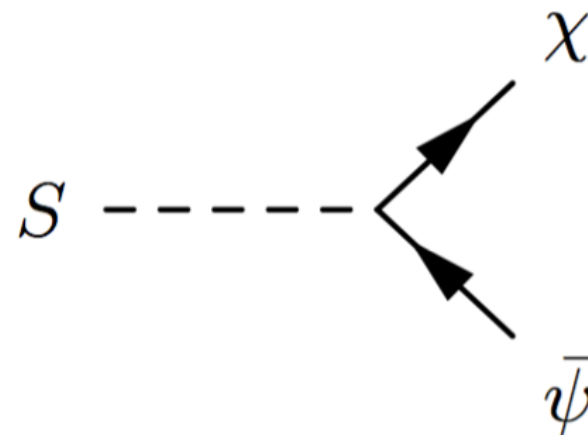
- $m_\psi \neq m_\psi(T)$

- Kinematically Induced Freeze-in

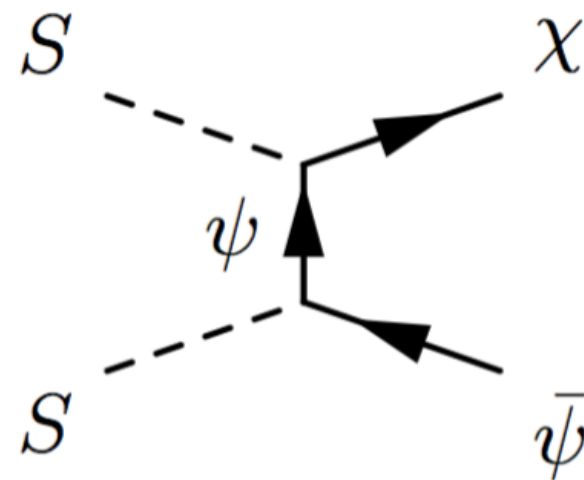
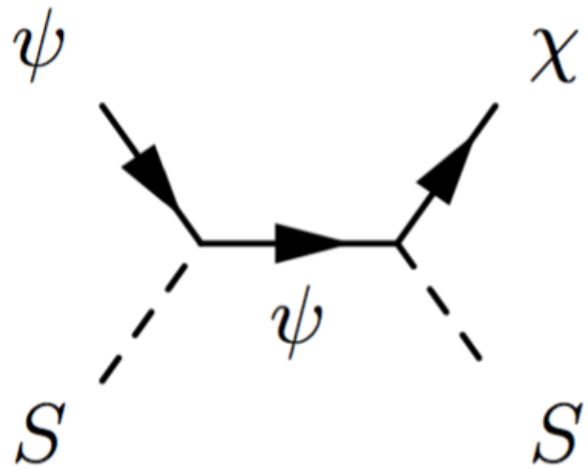
Assume χ begins with negligible abundance



$$m_\psi > m_\chi + m_S(T)$$

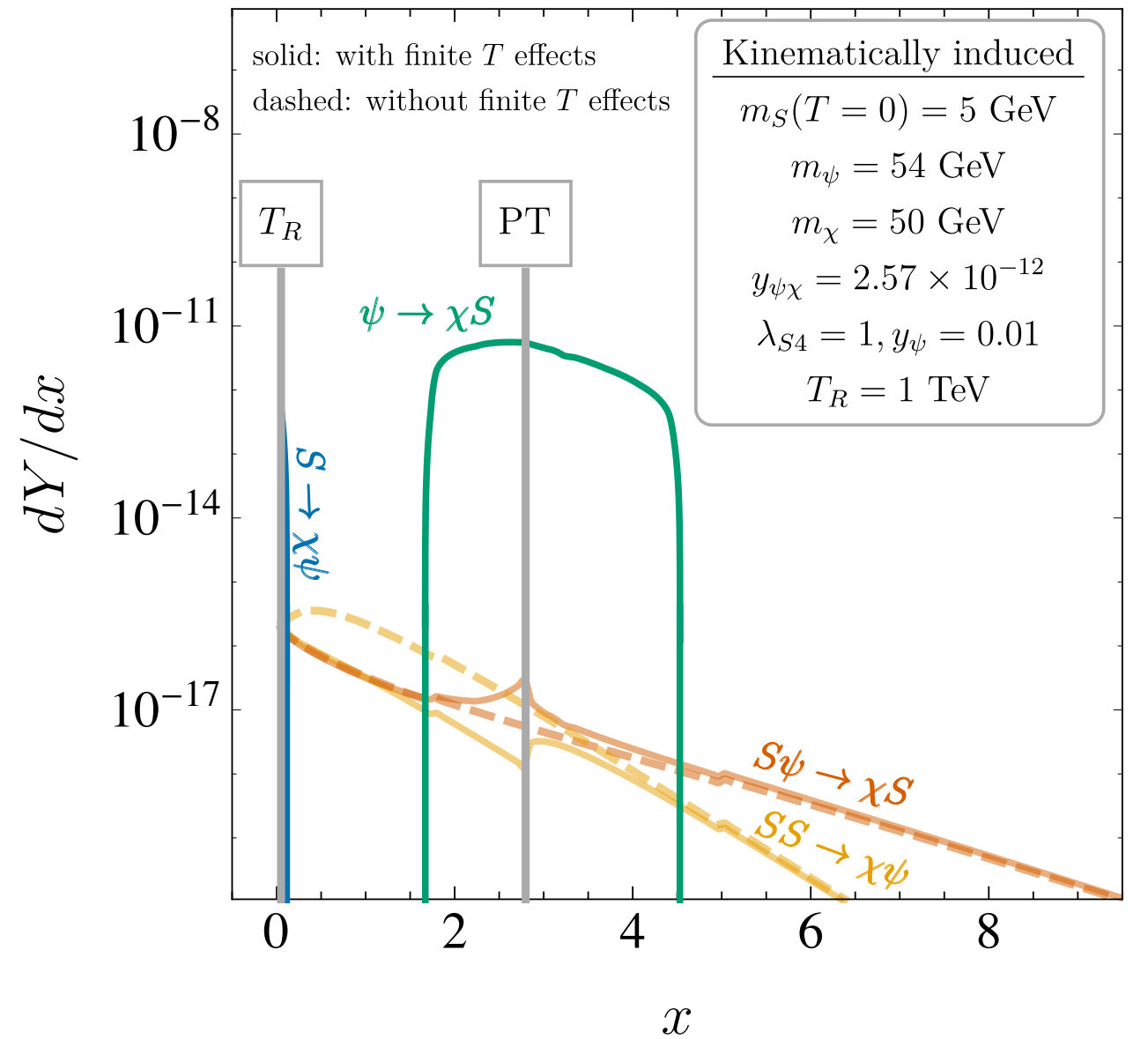
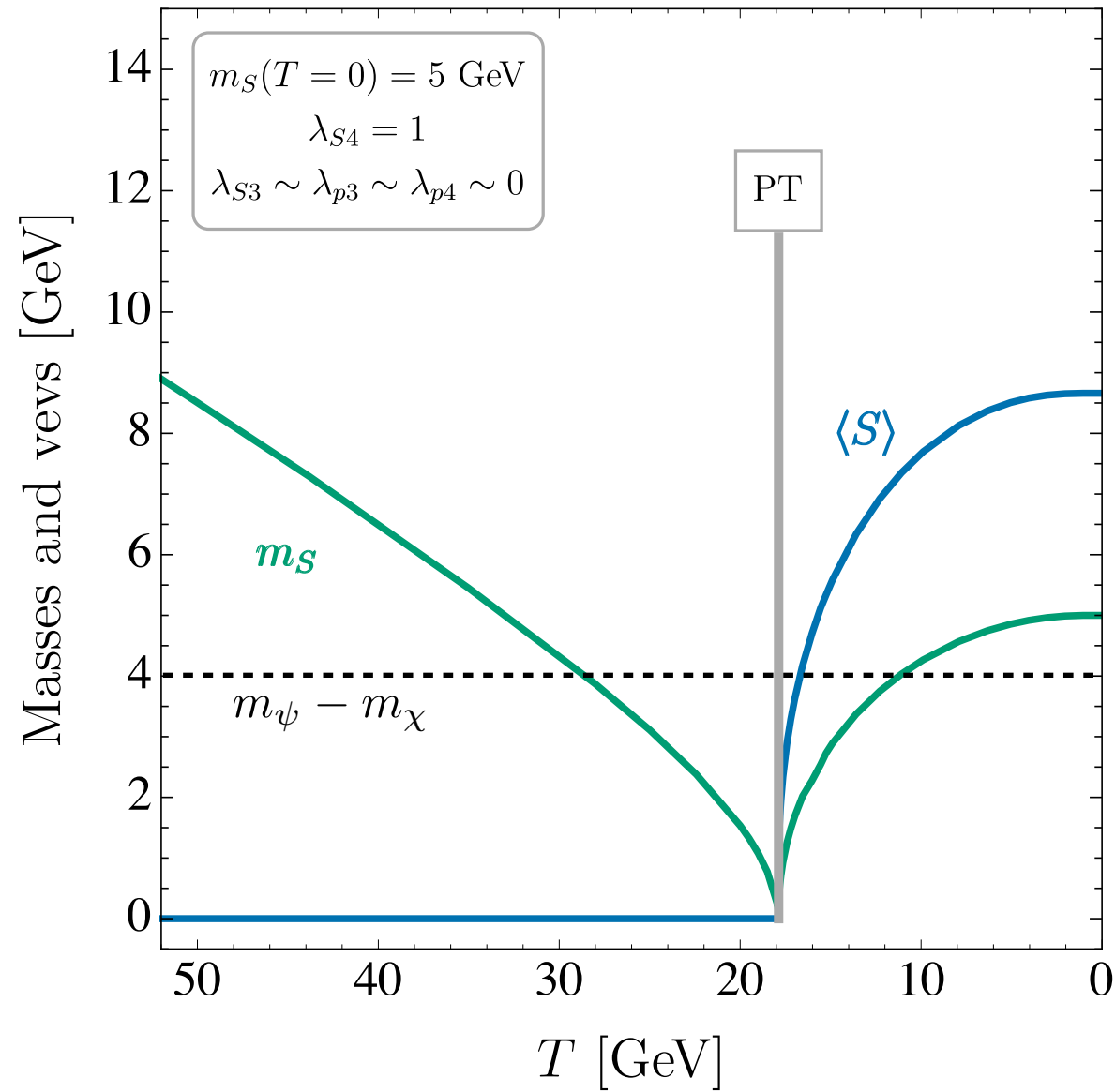


$$m_S(T) > m_\chi + m_\psi$$

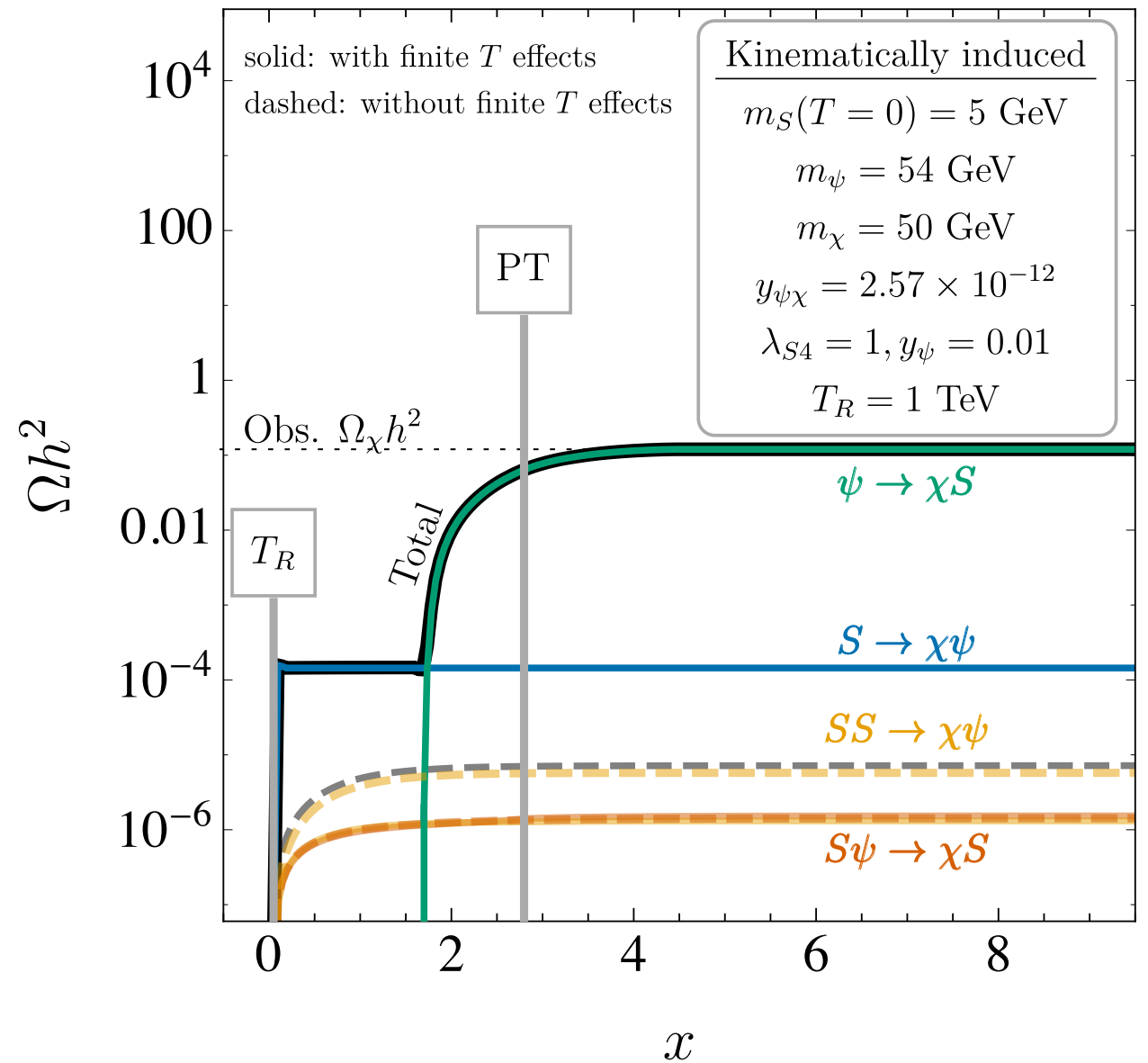
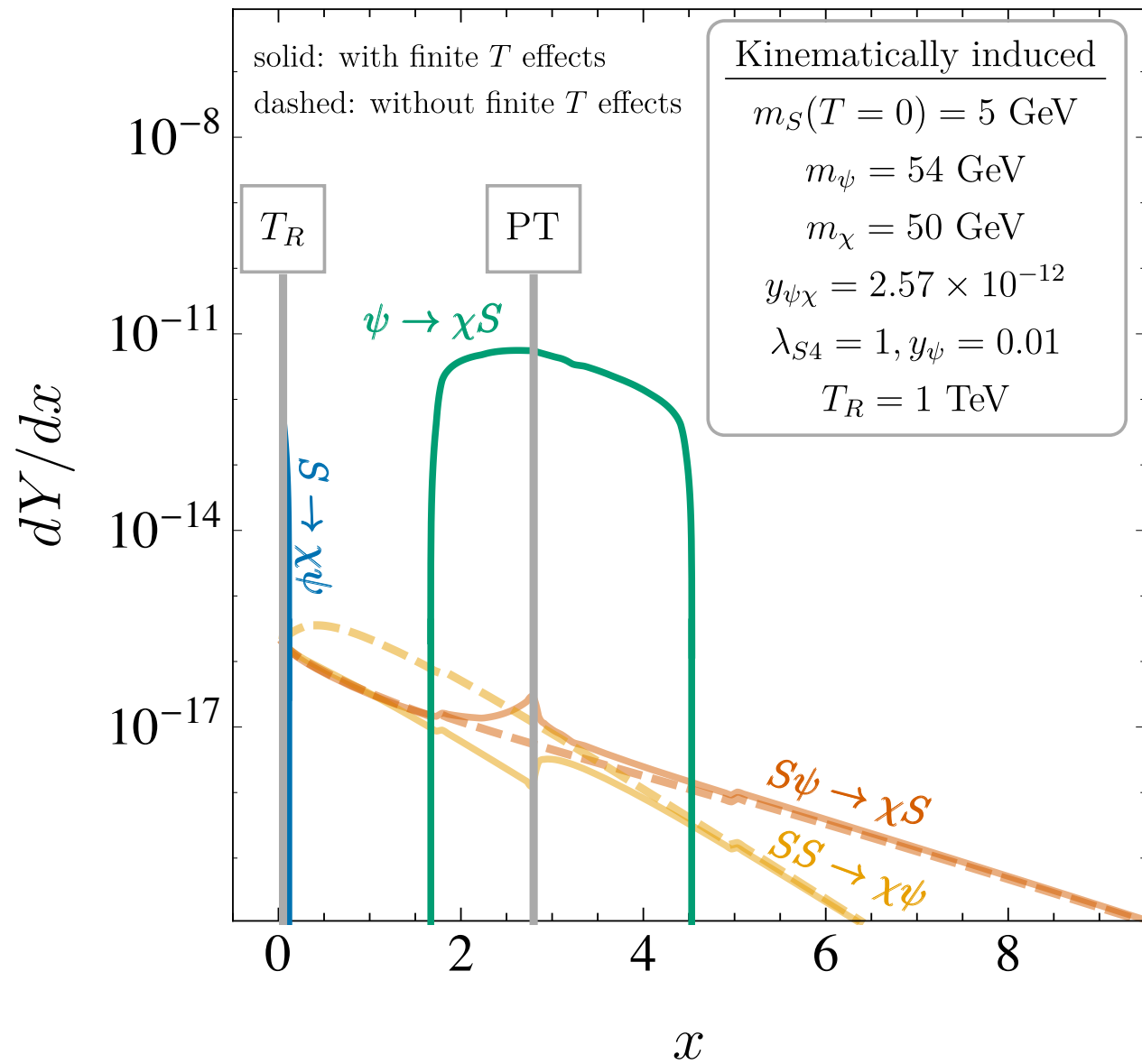


Suppressed by $y_\psi = 0.01$

Kinematically Induced Freeze-in - Results



Kinematically Induced Freeze-in - Results



Thermal effects increase relic abundance by orders of magnitude

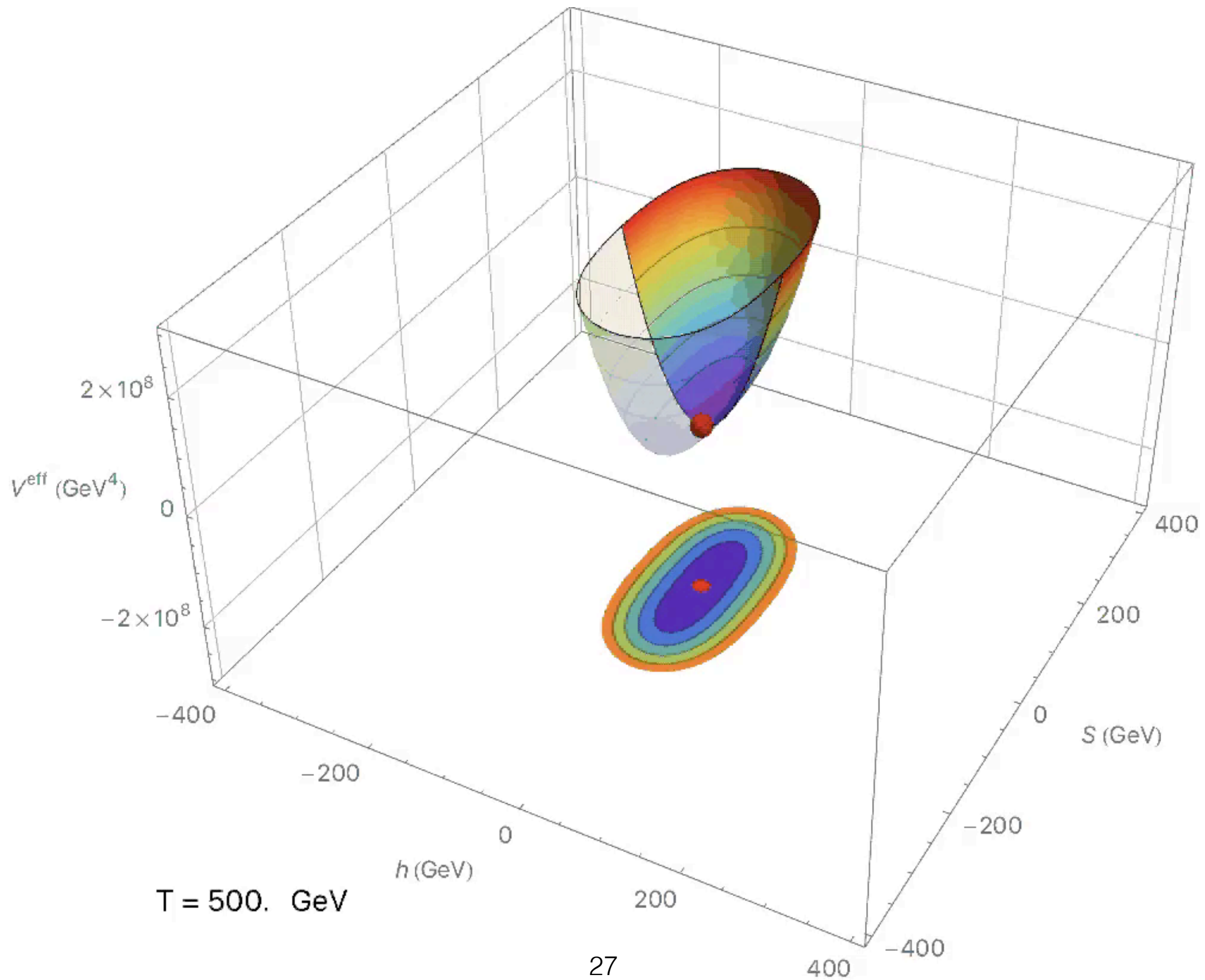
Decaying Dark Matter

- Vev Flip-Flop: Decaying Dark Matter

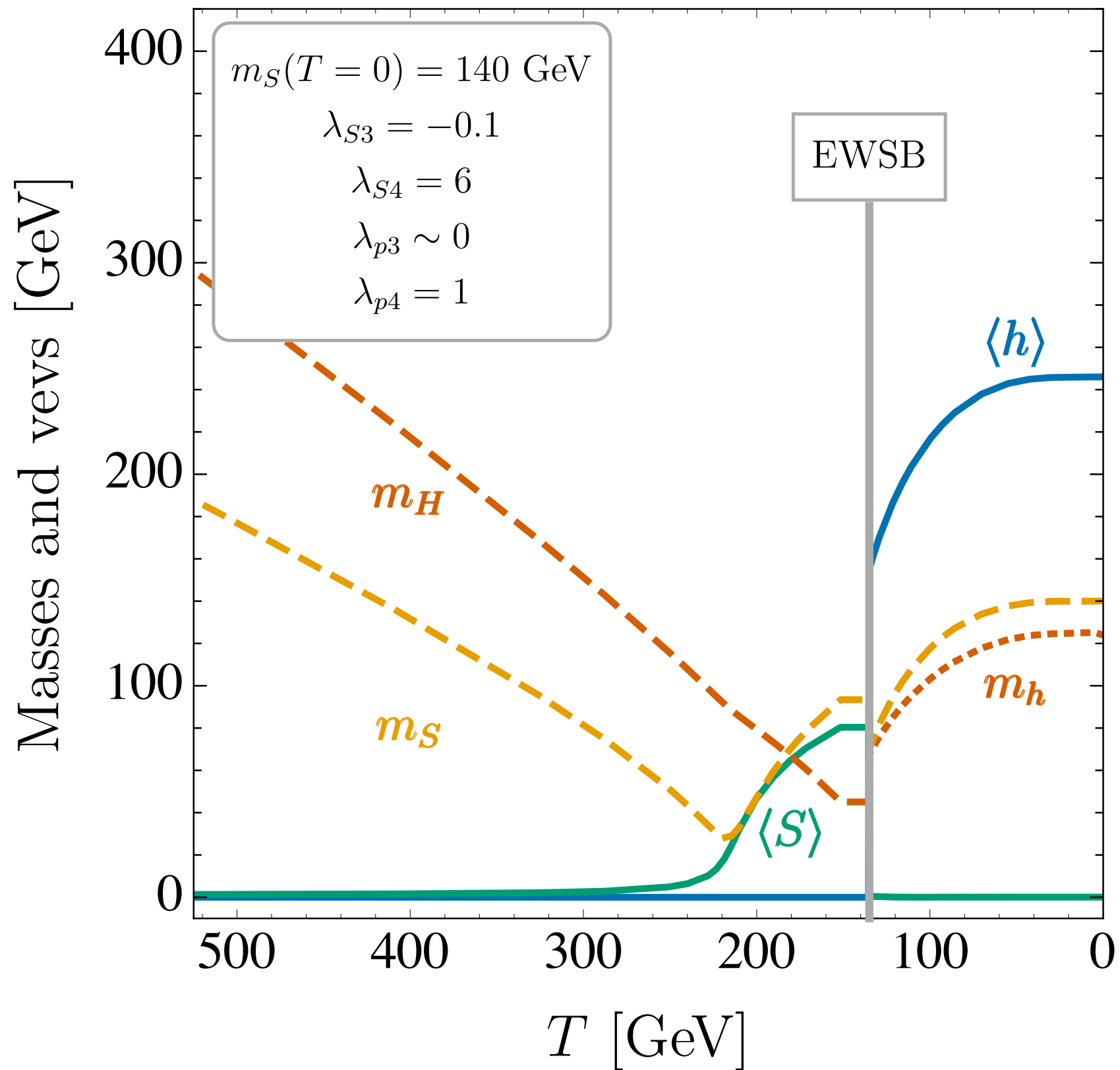
$$\begin{aligned}
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 & + \mu_H^2 H^\dagger H - \lambda_H (H^\dagger H)^2 + \frac{1}{2} \mu_S^2 S^2 - \frac{\lambda_{S4}}{4!} S^4 \quad \sim 1 \\
 & - \frac{\lambda_{S3}}{3!} \mu_S S^3 - \lambda_{p3} \mu_S S (H^\dagger H) - \frac{\lambda_{p4}}{2} S^2 (H^\dagger H) \\
 & \quad \quad \quad \sim 1
 \end{aligned}$$

$$V^{\text{eff}}(H, S, T) \neq V^{\text{eff}}(H, T) + V^{\text{eff}}(S, T)$$

- Two Step Phase Transition: Effective Potential

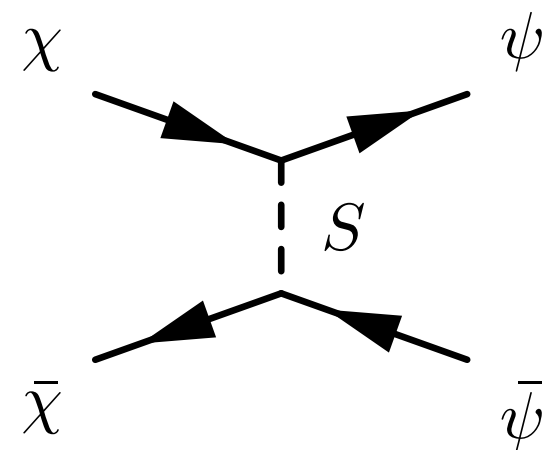
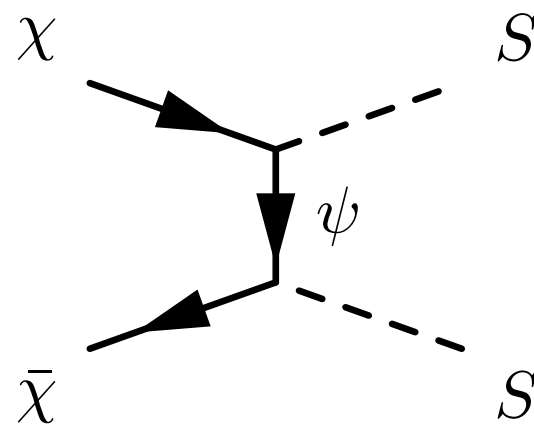
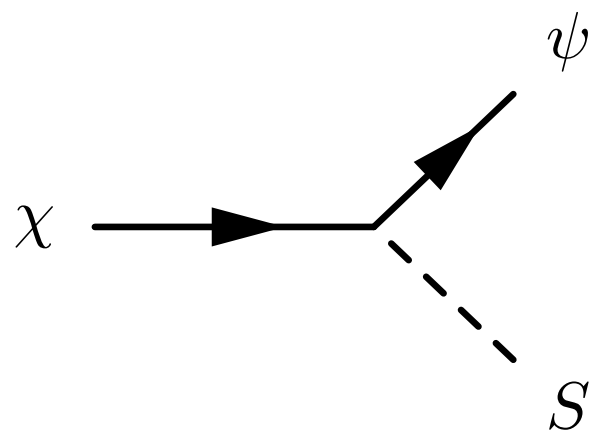


- Two Step Phase Transition: Effective Potential



- Vev Flip-Flop: Decaying Dark Matter

Assume χ begins with thermal abundance

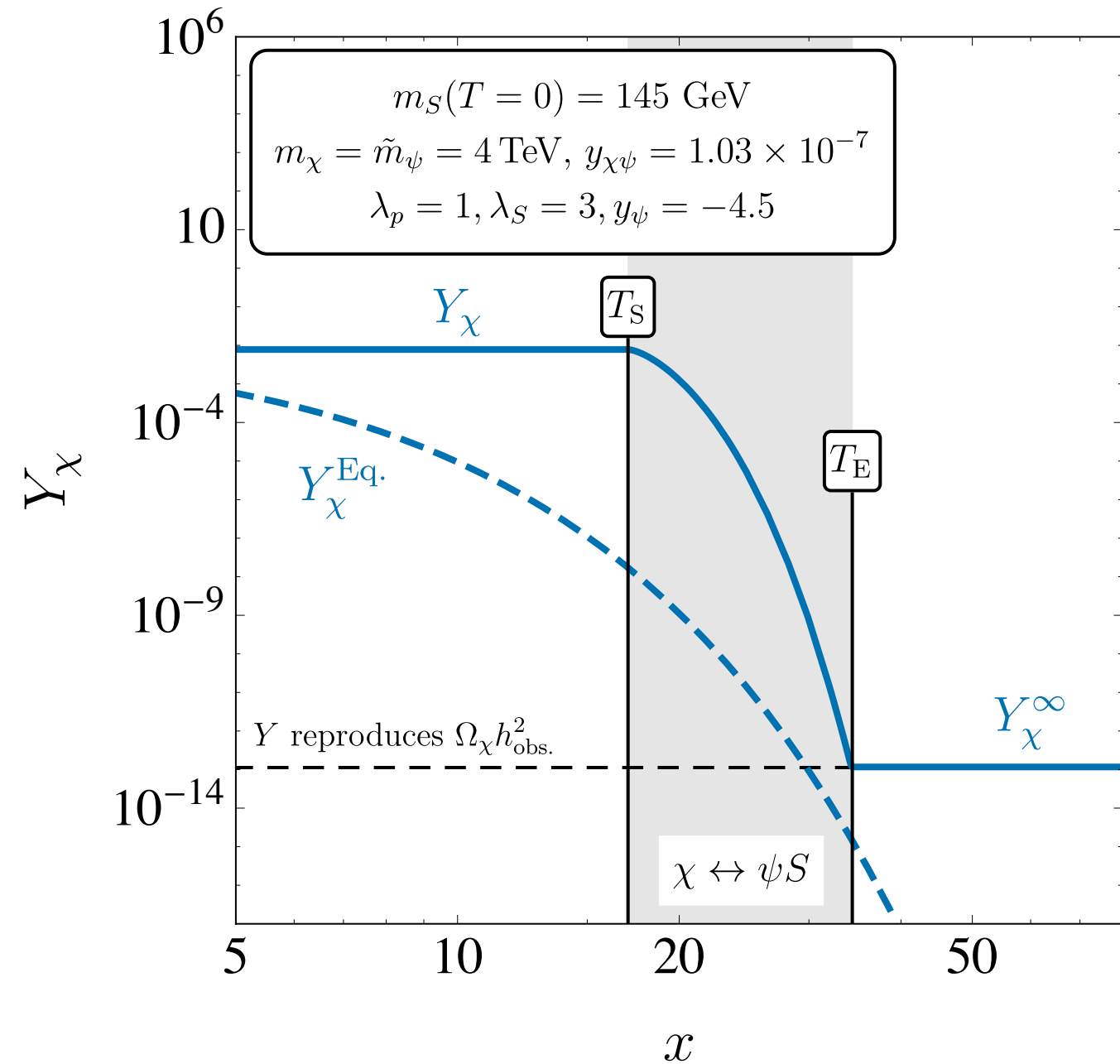
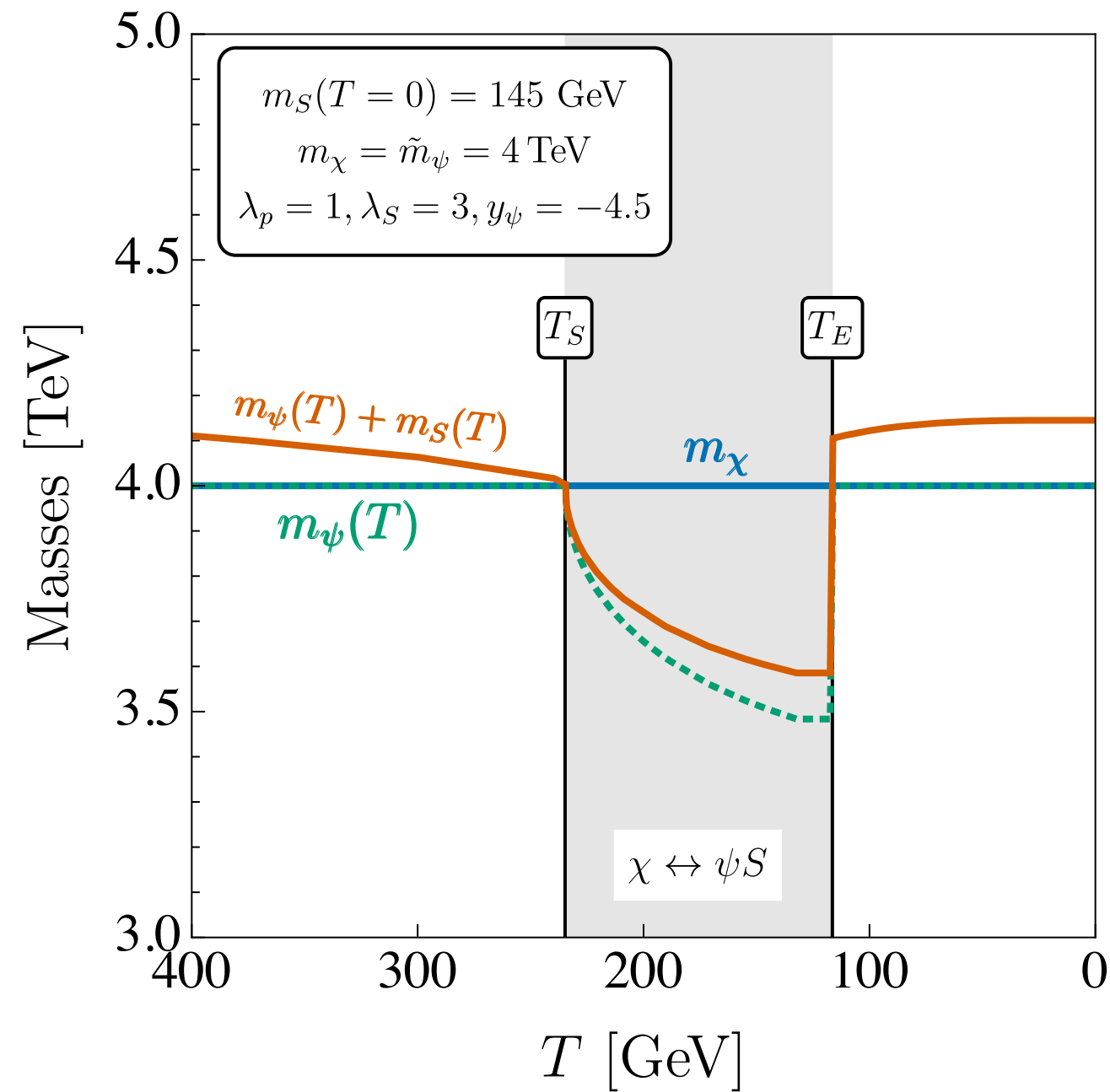


Open when

$$m_\chi > m_\psi(T) + m_S(T)$$

Suppressed by $y_{\chi\psi} \sim 10^{-7}$

- Vev Flip-Flop: Decaying Dark Matter



We have demonstrated another new method of obtaining the relic abundance

Conclusions

- Conclusions

- Thermal effects are important in the early universe!
- Temperature dependent masses affect kinematic thresholds
- NP scalars may temporarily obtain vevs
- This can have a dramatic influence on DM abundance
- Illustrated this with three scenarios, more are possible

Thank you!

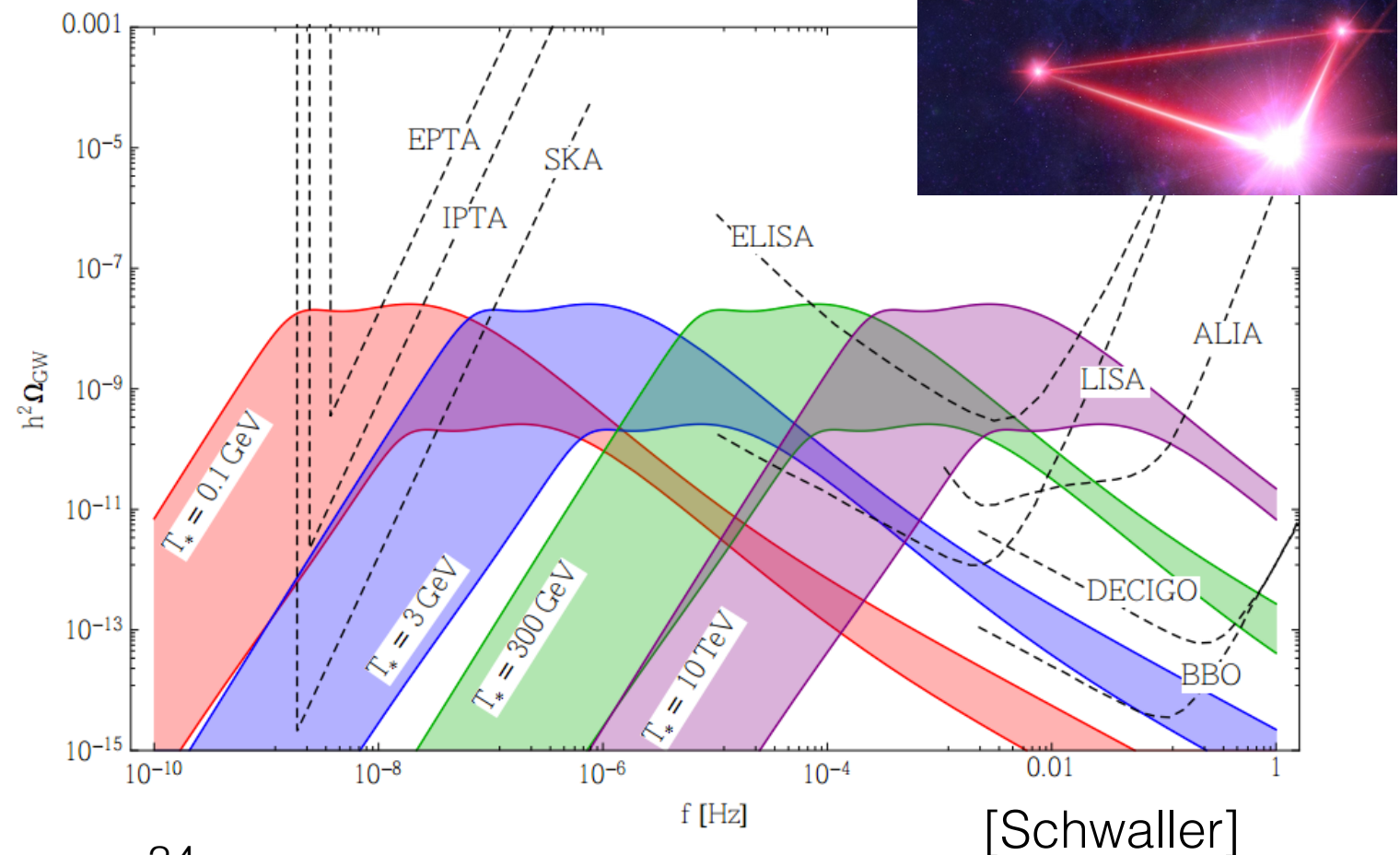
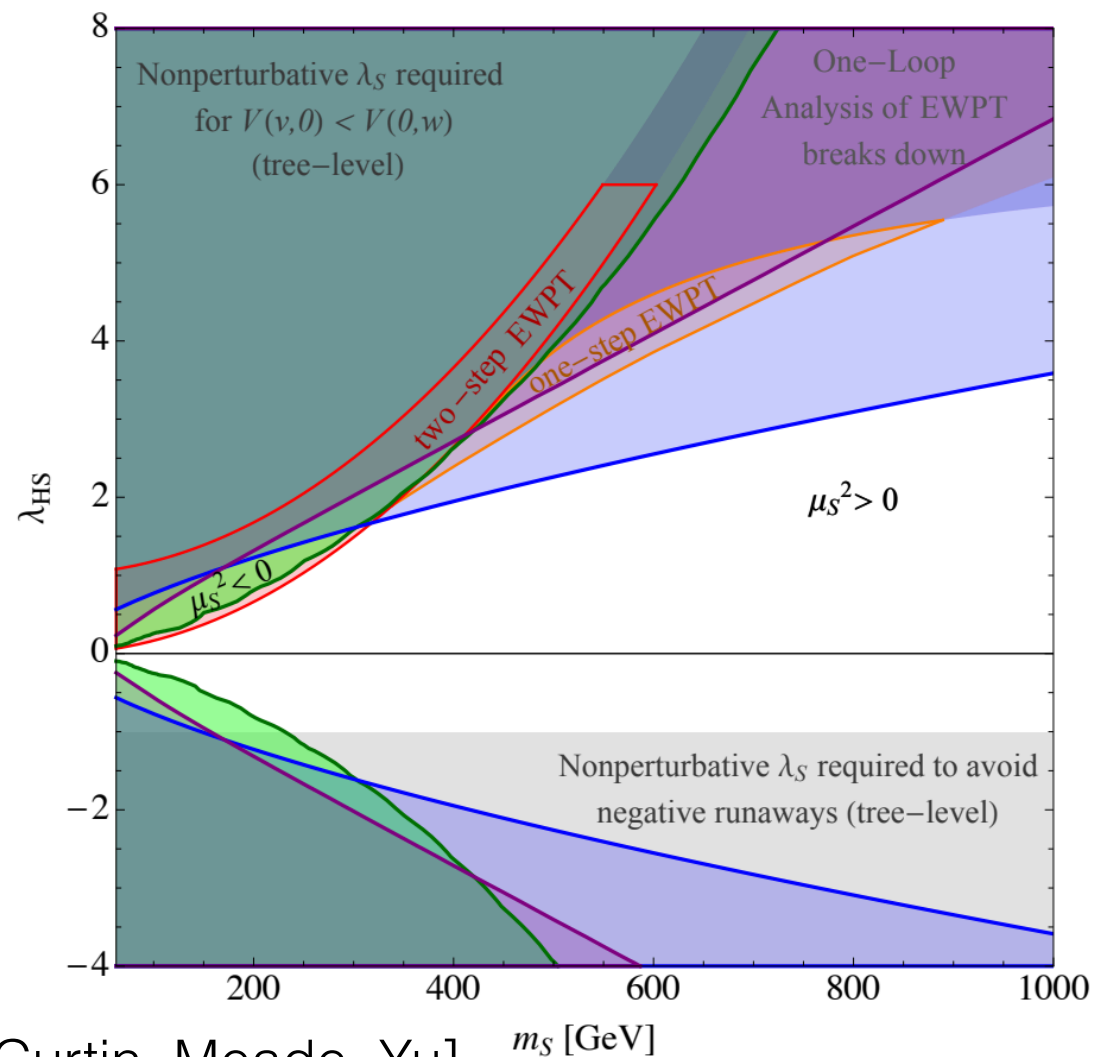
Experimental Probes

- Experimental Probes

Detection of χ hindered by small couplings

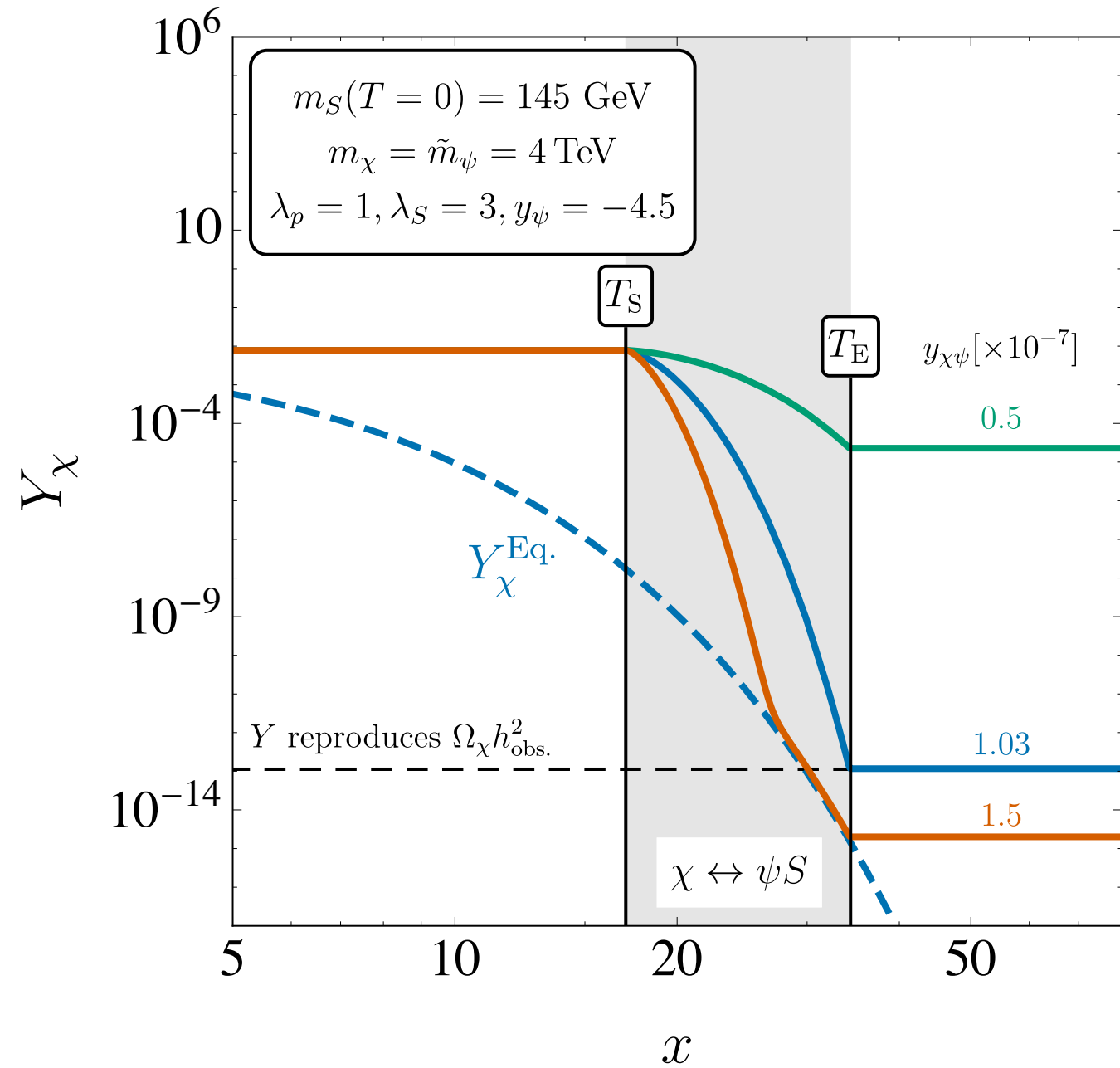
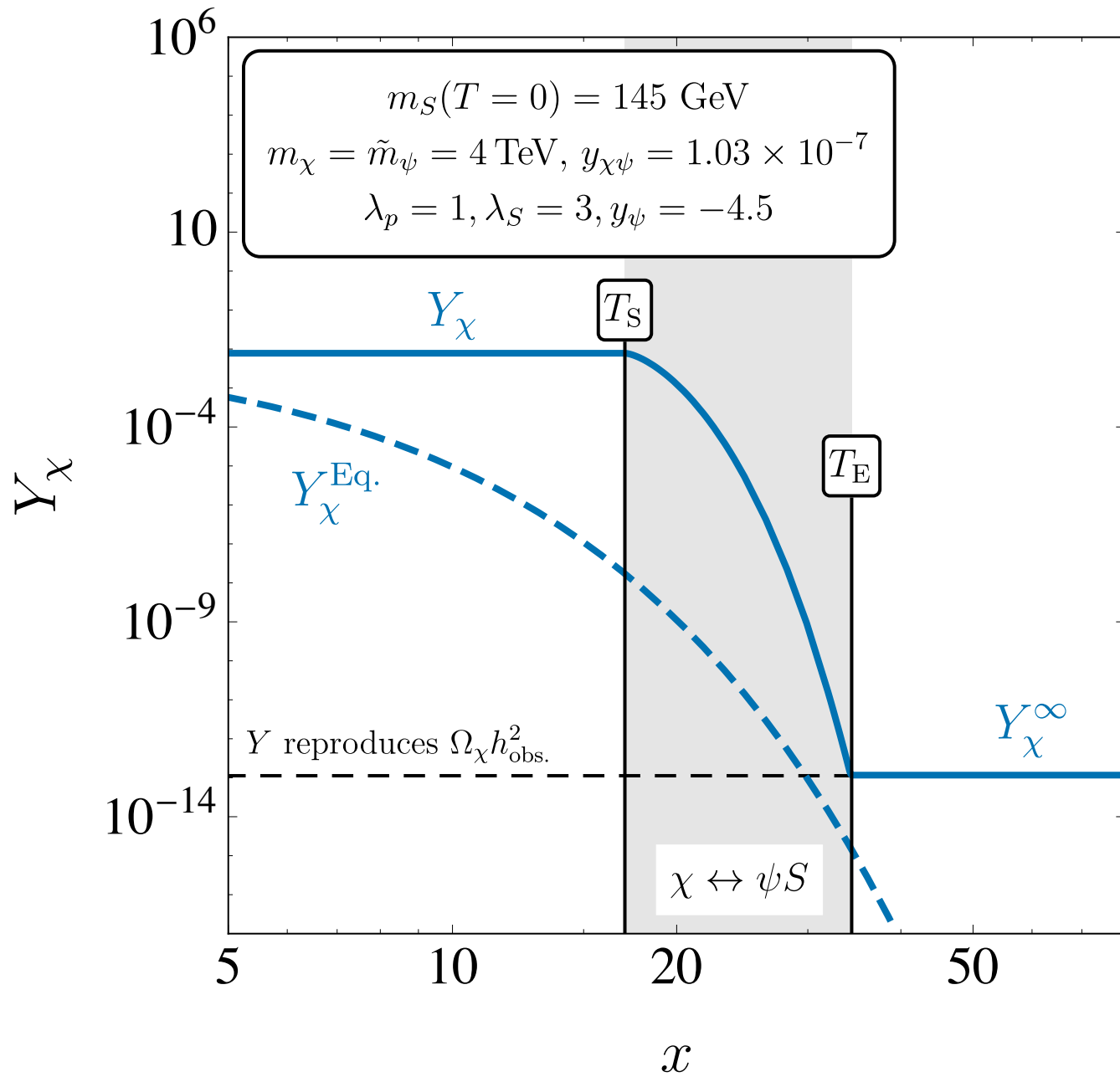
But S and ψ couplings can be relatively large, so can be produced

Two-step phase transition scenarios may give a subdominant population of S and ψ

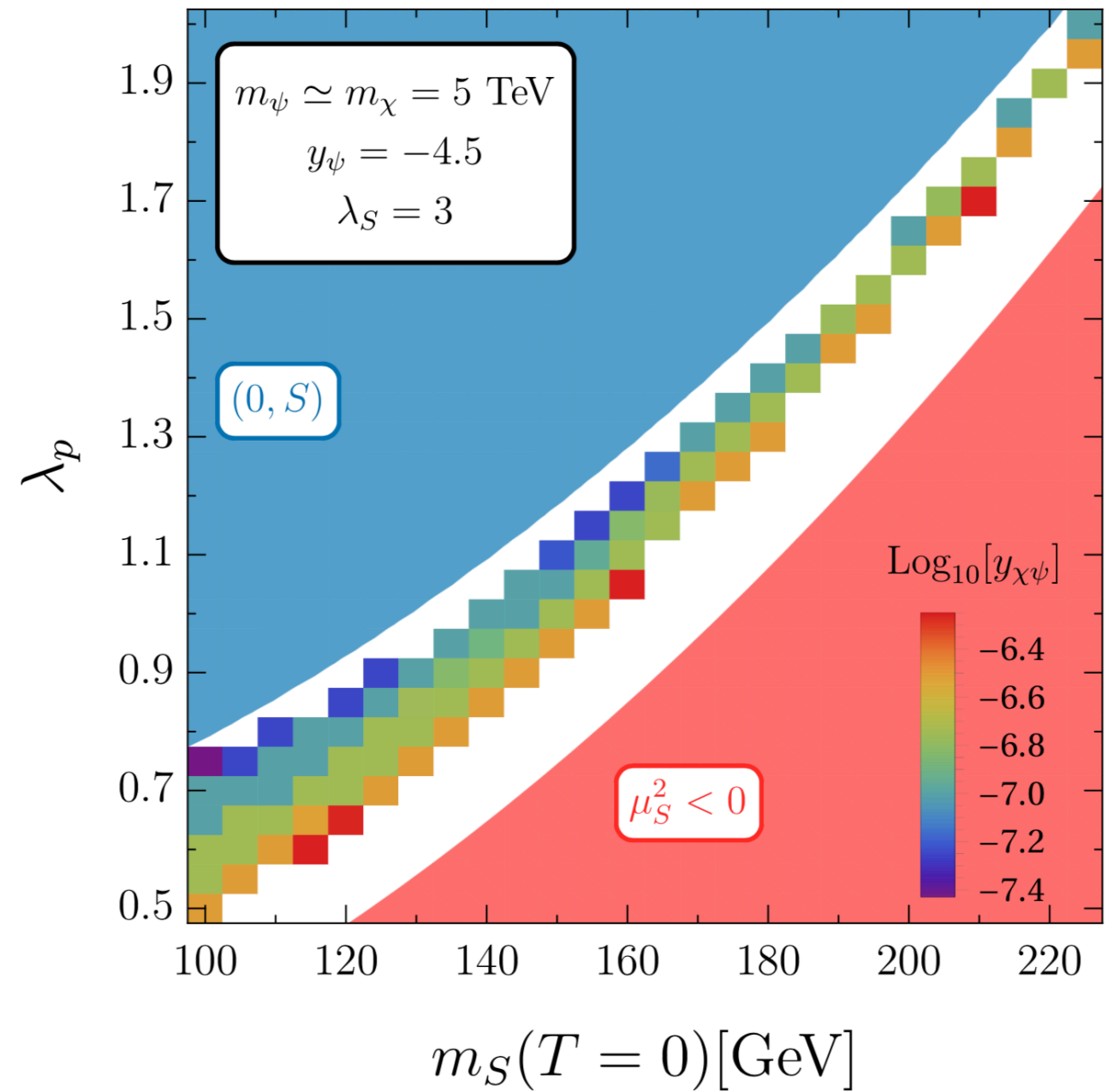
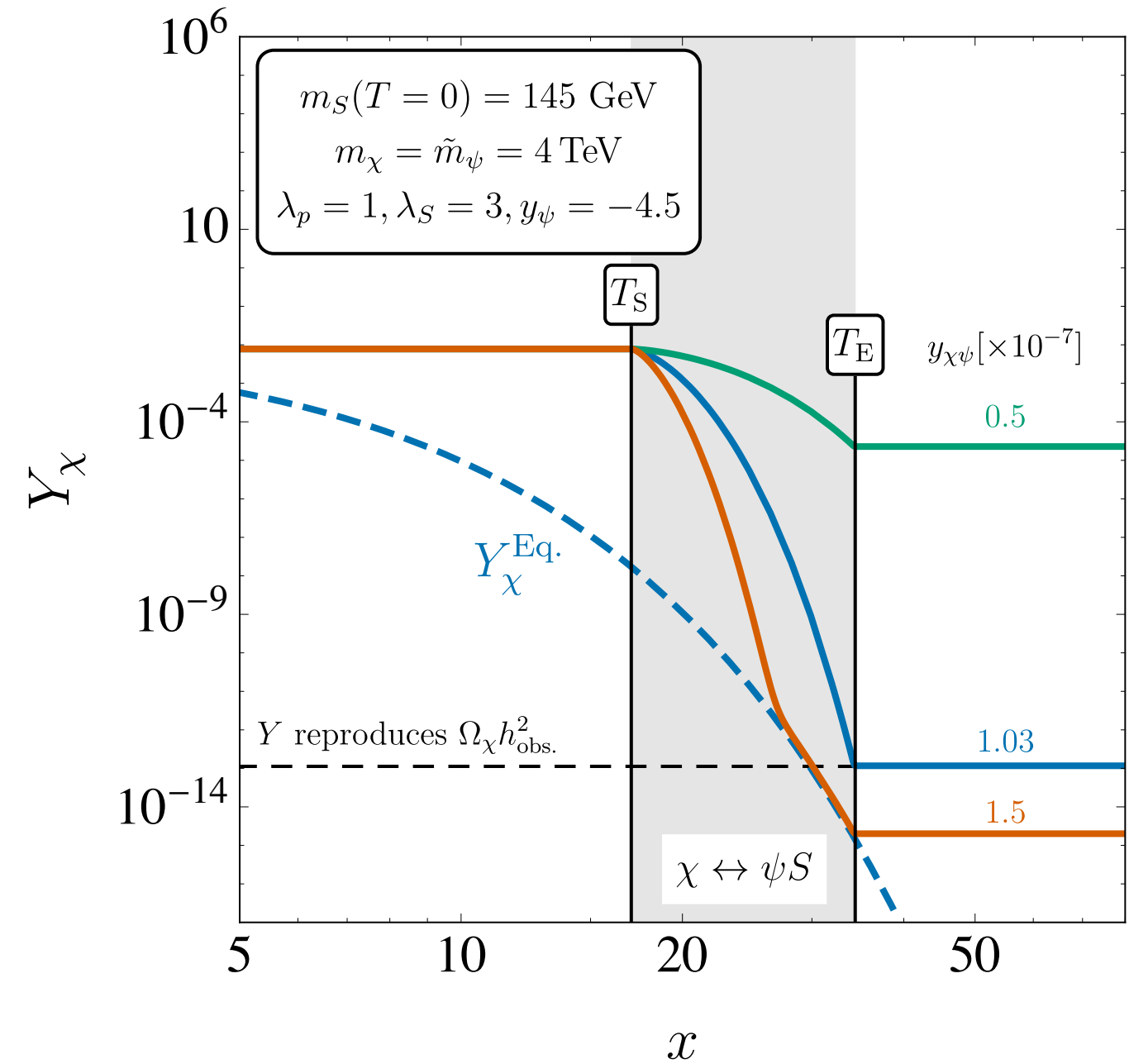


Parameter Space

- Vev Flip-Flop: Decaying Dark Matter



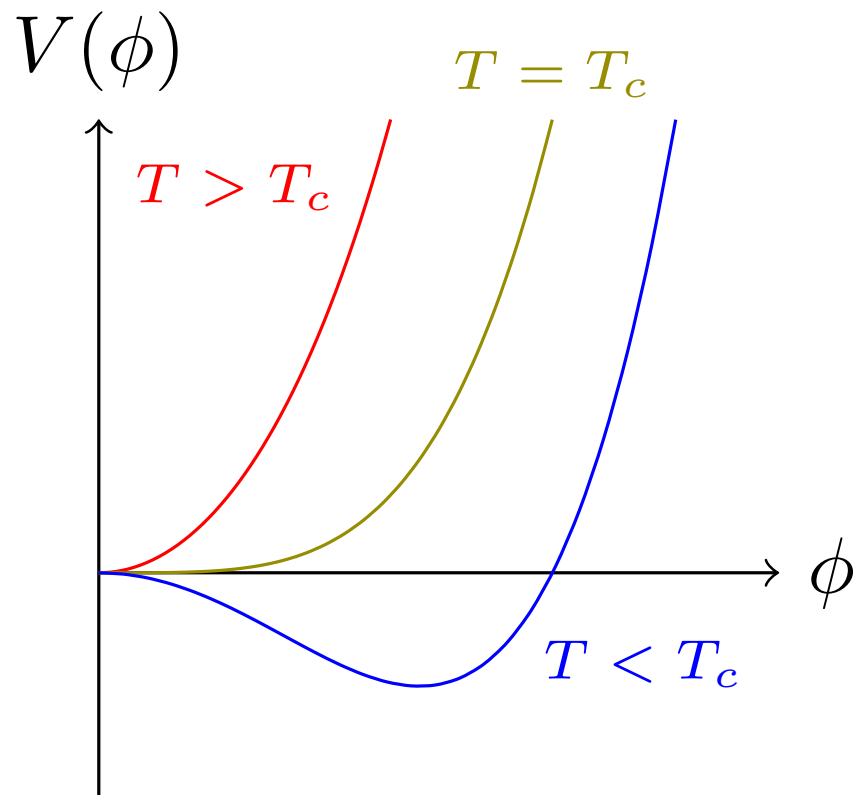
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Two Step Phase Transition

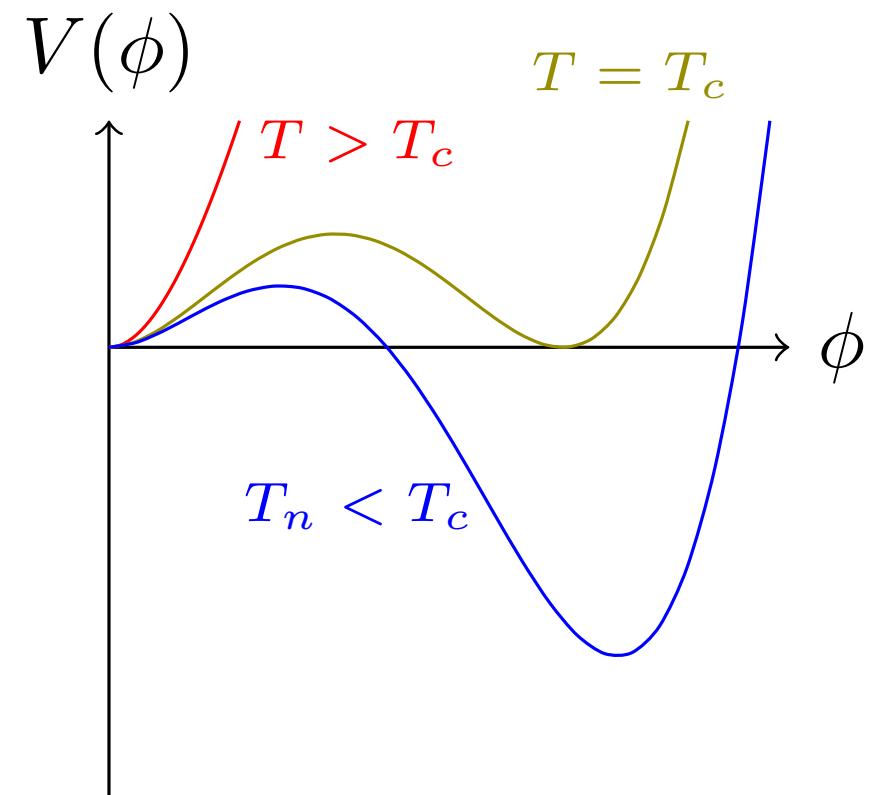
- Phase Transitions

Second Order Phase Transitions



$$T_{\text{PT}} = T_c$$

First Order Phase Transitions



$$T_n < T_c$$

- Bubble nucleation and Cosmotransitions

Bubble nucleation rate per volume:

$$\frac{\Gamma}{V} = Ae^{-S_E/T} \quad + m_\chi \bar{\chi}\chi + \tilde{m}_\psi \bar{\psi}\psi$$

P(one bubble nucleation per Hubble volume) ~ 1

$$\frac{S_E}{T} \sim 140$$

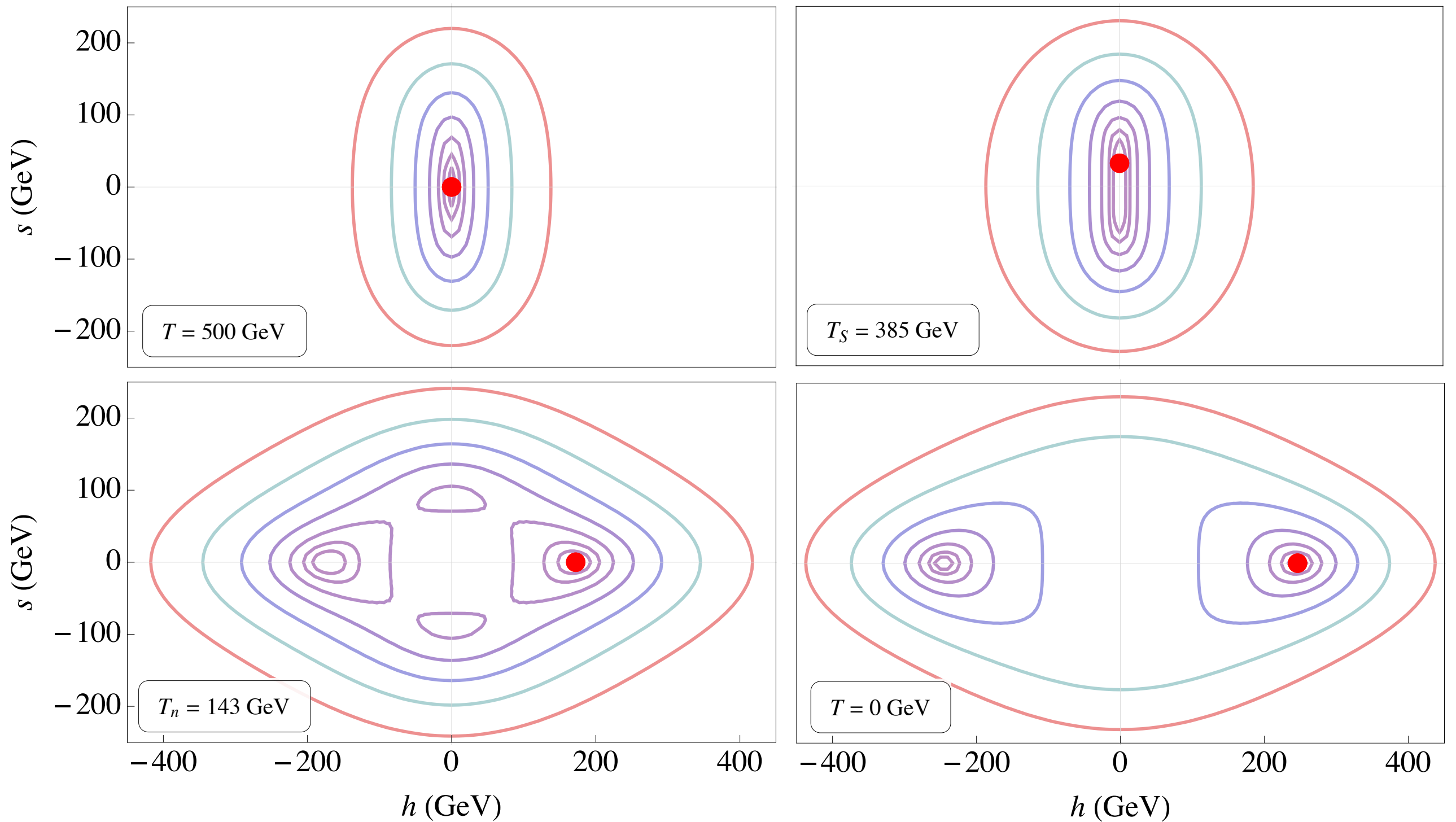
Linde, 1983

Anderson & Hall, 1992

Use cosmotransitions

Wainwright, 2011

- Vev Flip-Flop: Effective Potential



The Effective Potential

• The Effective Potential

At zero temperature:

“It would be wonderful if, in the full quantum field theory, there were a function whose minimum gave the exact value of $\langle\phi\rangle$. We will exhibit a function with these properties, called the *effective potential*.”

(Peskin & Schroeder)

$$V^{\text{eff}} = V^{\text{tree}} + V^{\text{1-loop}} + \dots$$

$$V^{\text{CW}}(h, S) = \sum_i \frac{n_i}{64\pi^2} m_i^4(h, S) \left[\log \frac{m_i^2(h, S)}{\Lambda^2} - \frac{3}{2} \right]$$

$$\text{E.g., } m_t^2(h) = \frac{1}{2} y_t^2 h^2$$

Coleman & Weinberg, 1973

- The Effective Potential

In finite temperature QFT, we can't rely on asymptotic states. Instead, we apply ideas from thermodynamics, then express the partition function as a path integral in imaginary time with periodic boundary conditions. The one-loop expansion of the effective potential then becomes

$$V^{\text{eff}} = V^{\text{tree}} + \sum_i \frac{n_i T}{2} \sum_{n=-\infty}^{+\infty} \int \frac{d^3 \vec{k}}{(2\pi)^3} \log \left[\vec{k}^2 + \omega_n^2 + m_i^2(h, S) \right] + \dots$$

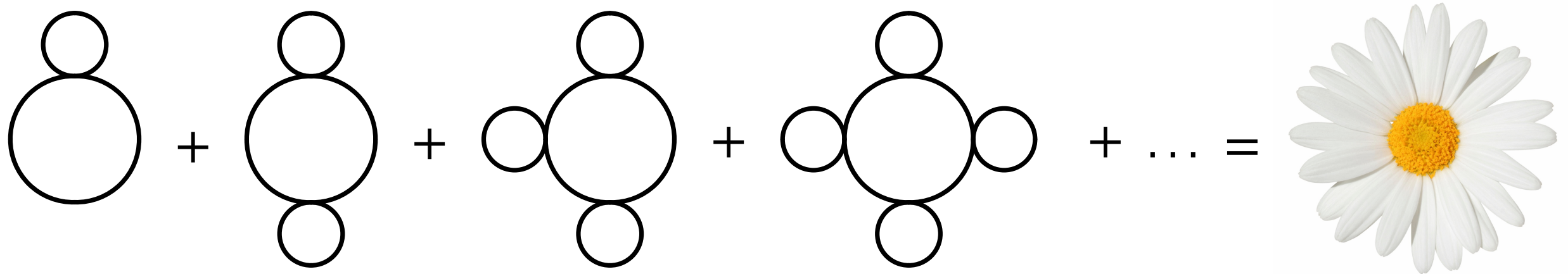
$$V^{\text{eff}} = V^{\text{tree}} + V^{\text{CW}} + V^T + V^{\text{daisy}}$$

$$V^T(h, S) = \sum_i \frac{n_i T^4}{2\pi^2} \int_0^\infty dx x^2 \log \left[1 \pm \exp \left(- \sqrt{x^2 + m_i^2(h, S)}/T \right) \right]$$

Dolan & Jackiw, 1974

- The Effective Potential

$$V^{\text{eff}} = V^{\text{tree}} + V^{\text{CW}} + V^T + V^{\text{daisy}}$$



$$V^{\text{daisy}} = -\frac{T}{12\pi} \sum_i n_i \left([m_i^2(h, S) + \Pi_i(T)]^{\frac{3}{2}} - [m_i^2(h, S)]^{\frac{3}{2}} \right)$$

$$\text{E.g., } \Pi_{h, G^0, G^+} = \frac{1}{48} T^2 (9g^2 + 3g'^2 + 24\lambda_H + 12y_t^2 + 2\lambda_p)$$

Dolan & Jackiw, 1974