



Theory Developments in Heavy Flavor



Dean Robinson

DPF-APS

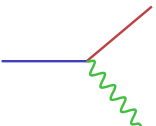
July 2019



SM Flavor

Nutshell: How do we describe quark/lepton interactions?

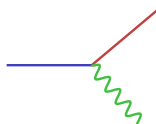
SM EW Lagrangian:

$$\mathcal{L}_{EW} = \frac{g_2}{\sqrt{2}} (u \quad c \quad t) \not{W} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$


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| | | |
|----------------------|----------------------|----------------------|
| CKM matrix | | |
| 3 × 3 unitary ~ | | |
| 1 | 0.2 | 4 × 10 ⁻³ |
| 0.2 | 1 | 4 × 10 ⁻² |
| 4 × 10 ⁻³ | 4 × 10 ⁻² | 1 |

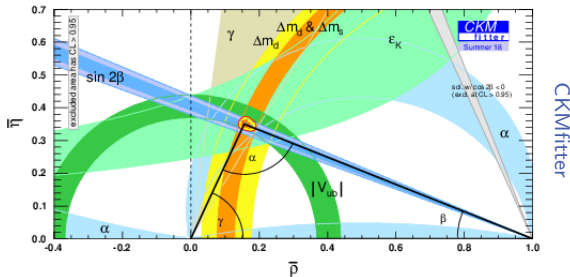
In the SM:

- Flavor changing processes through electroweak charged currents (CC)
- No tree-level flavor changing neutral currents (FCNC)
- Similar story for charged leptons with ν masses

Flavor Data

Can test SM flavor structure with CKM unitarity triangles, e.g.

$$V_{tb}^* V_{td} + V_{cb}^* V_{cd} + V_{ub}^* V_{ud} = 0$$



- **Huge multitude** of physical observables projected onto CKM parameter plane (from decays, (in)direct CP violation, mass splittings Δm ...) (see [S. Stone's talk for more details](#))
- SM \implies all allowed regions should intersect. **Lesson: Good agreement with SM flavor structure**
- Leads to **powerful constraints** and **powerful discovery potential**

New Physics (NP) Constraints

History:

- $n \rightarrow p e \nu$: Energy scale \sim MeV, **probes** EW current at \sim 100 GeV!
- $\Delta m_K / m_K \simeq 7 \times 10^{-15}$ **predicted** charm, $m_c \sim$ 1–2 GeV

New Physics (NP) Constraints

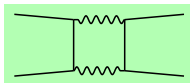
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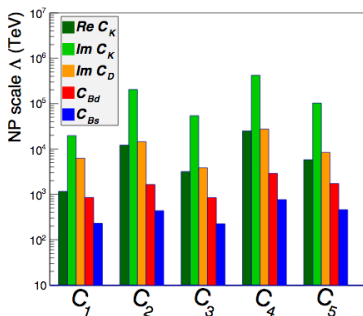
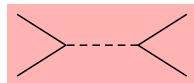
Constraints on 4-Fermi FCNC operators from e.g. **meson mixing**

$$\frac{(\bar{q}\Gamma q')(\bar{q}'\Gamma'q)}{\Lambda^2}$$

via:



vs



Indirect access to scales
 $\sim 10^4$ TeV **far above**
 LHC direct production!

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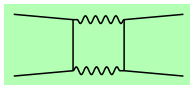
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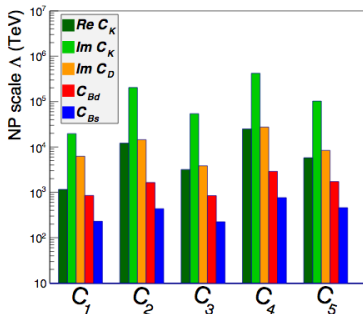
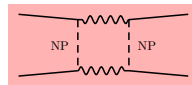
Constraints on 4-Fermi FCNC operators from e.g. **meson mixing**

$$\frac{V_{td} V_{ts}}{16\pi^2} \frac{(\bar{q}\Gamma q')(\bar{q}'\Gamma'q)}{\Lambda^2}$$

via:



vs



Indirect access to scales
 $\sim 10^4$ TeV **far above**
 LHC direct production!

But, with loop +
 CKM suppression:
 NP/SM $\sim 20\%$ in
 FCNC still compatible!

(Incomplete) Perspectives on Flavor

Precision Th.
Control

NP

Smoking Guns

Tensions:

Measurements vs predictions

- $|V_{cb}|, |V_{ub}|$
- $(g-2)_\mu$ (see J. Crnkovic's talk)
- ΔA_{CP} in charm
- $b \rightarrow s\mu\mu$
- ...

Precision Flavor

Flavor Models

Explain SM hierarchies:
Quark/lepton mass and mixing
Can imply NP signals

SM

Enhancement of
rare/forbidden SM

Flavor symmetry violation

- $K \rightarrow \pi\nu\nu$
- $\mu \rightarrow e$
- $b \rightarrow c\nu\nu$: τ vs e, μ
- $b \rightarrow s\nu\nu$: e vs μ
- ...

Constrain high NP scales
(no obs \gg SM prediction)

- $B_s \rightarrow \mu\mu$
- $\Delta M_{s,d}$
- $b \rightarrow s\nu\nu$
- ...

Theoretically
Clean

(Incomplete) Perspectives on Flavor

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Precision Flavor

We'll look at theory developments in understanding heavy flavor anomalies

els
hies:
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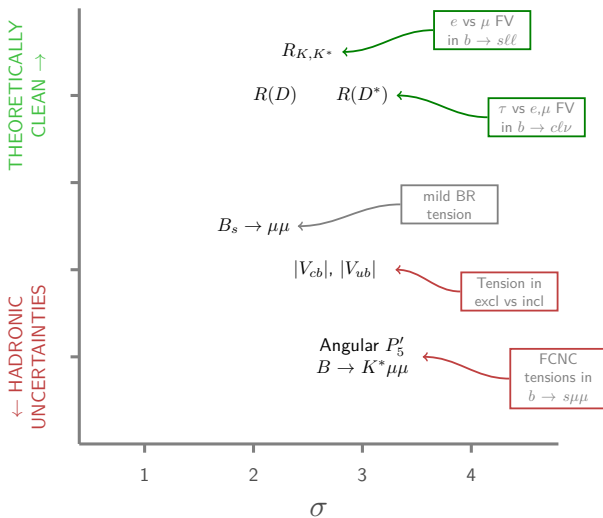
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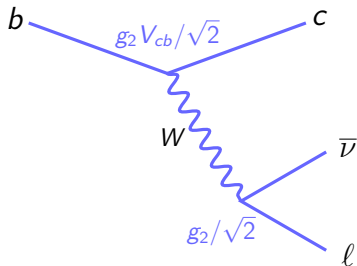
Space of Heavy Flavor Anomalies

Involving $B_q = (bq)$ mesons



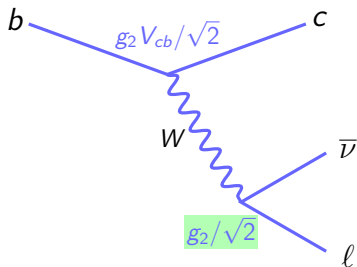
Adapted from Z Ligeti and W Altmannshofer

Semileptonic Decays: $b \rightarrow cl\nu$



- Tree-level W exchange (in the SM)
- Approx. 25% of all B decays: huge statistics!

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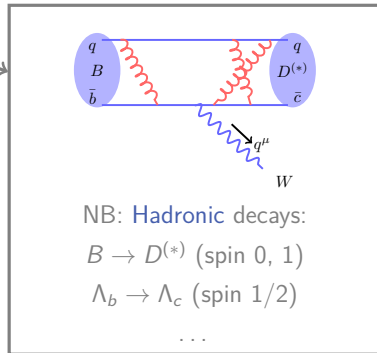
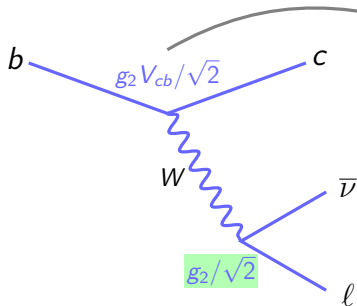
Probe of lepton flavor universality

g_2 ($\ell = e, \mu, \tau$) up to masses:

$m_\tau \simeq 1777\text{MeV}$ vs $m_\mu = 105\text{MeV}$;

PS and hadronic effects

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PS and hadronic effects

Hadronic matrix elements \implies **measure**

$|V_{cb}|$ in exclusive $l = e, \mu$ modes

(more details in tomorrow's parallel session)

Two Anomalies/Puzzles

1. **Inclusive** $B \rightarrow X_c l \nu$ versus **exclusive** $B \rightarrow D^* l \nu$

Measurement is done with $l = e, \mu$: The τ mode involves more ν 's from τ decays and less statistics

$$|V_{cb}|_{X_c} \simeq (42.2 \pm 0.8) \times 10^{-3}$$

$$|V_{cb}|_{D^*} \simeq (38.7 \pm 0.7) \times 10^{-3}$$

A 3σ tension?!?

2. Can factor out $|V_{cb}|$, and measure the ratios

$$R(D^{(*)}) \equiv \frac{\Gamma[B \rightarrow D^{(*)} \tau \nu_\tau]}{\Gamma[B \rightarrow D^{(*)} l \nu]}, \quad l = e, \mu.$$

$R(D^{(*)})$ anomaly

Persistent hints of **lepton flavor universality violation** for 7+ years

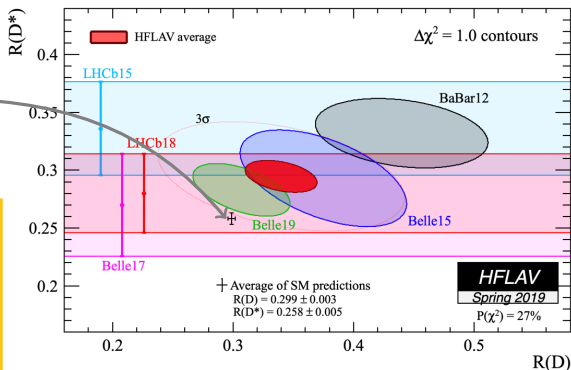
SM prediction

1703.05330 [Bernlochner,
Ligeti, Papucci, & DR]

1707.09509 [Bigi, Gam-
bino, Schacht]

~ 20-30% tension at
~ 3.1 σ level with SM
predictions

(was 4 σ < March)

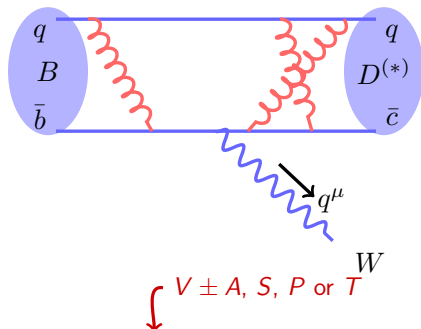


Also mild anomaly in $B_c \rightarrow J/\psi\tau\nu$, and (possibly) in $B \rightarrow X_c\tau\nu$.

- More **measurements** are coming! E.g. $R(D)$ or $R(\Lambda_b)$ from LHCb

Hadronic Matrix Elements

For **exclusive processes**: Main **theory uncertainty** is mapping partons \rightarrow hadrons:



- Need **predictions** for $\langle D^{(*)} | \bar{c} \Gamma b | \bar{B} \rangle$ for any NP/SM current
- Use **parametrizations** of form factors

$$\langle D^{*} | \bar{c} \Gamma^{\mu} b | \bar{B} \rangle \sim FF_{\varepsilon}(q^2) \varepsilon^{\mu} + FF_B(q^2) p_B^{\mu} + FF_{D^{*}}(q^2) p_{D^{*}}^{\mu}$$

- Logic: **Fit to $l = e, \mu$ SM** measurements; **predict SM or NP τ modes**
- **Ultimate**: Lattice calculations! But only limited results currently available

$|V_{cb}|$ developments

- The Belle expt published an **unfolded** $B \rightarrow D^* l \nu$ dataset [1702.01521](#). Permits theorists to fit with **different** FF parametrization choices
- Using parametrization based on just **analyticity** and **unitarity** ('BGL'):

$$|V_{cb}|_{\text{'CLN'}} = (38.2 \pm 1.5) \times 10^{-3}, \quad \text{1702.01521 [Belle]}$$

$$|V_{cb}|_{\text{'BGL'}} = (41.7_{-2.1}^{+2.0}) \times 10^{-3}, \quad \text{1703.06124, 1707.09509 [Bigi, Gambino, Schacht]}$$

$$|V_{cb}|_{\text{'BGL'}} = (41.9_{-1.9}^{+2.0}) \times 10^{-3}, \quad \text{1703.08170 [Grinstein, Kobach]}$$

- Compare with $|V_{cb}|_{\text{incl}} = (42.2 \pm 0.8) \times 10^{-3}$
- **Does this resolve $|V_{cb}|$ incl vs excl tension?**

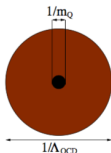
Tensions

Fits that lift $|V_{cb}|$ lead to **Heavy Quark Effective Theory (HQET)**

tensions Bernlochner, Ligeti, Papucci, DR [1708.07134, 1902.09553]

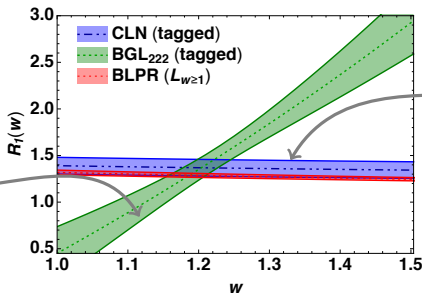
HQ is a **static color source**

Like atomic physics:
electronic states
insensitive at LO to
nuclear spin/flavor



- EFT of **light dofs** dressing a heavy quark Q ($m_Q \gg \Lambda_{\text{QCD}}$)
- Implies relations between SM, NP FFs
- Corrections to HQ limit $\sim 20\%$; FF ratios

$$R = 1(0) + \mathcal{O}(\Lambda_{\text{QCD}}/m_Q, \alpha_s) + \dots$$



New choice:
radical departure
from HQET

Usual exp choice:
consistent with
HQET $R_1 \sim 1 + \dots$

1902.09553 [Bernlochner, Ligeti, DR]

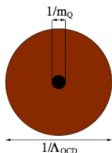
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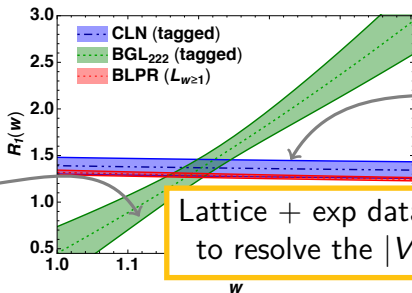
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Lattice + exp data is needed
to resolve the $|V_{cb}|$ puzzle

1902.09553 [Bernlochner, Ligeti, DR]

NP Explanations: General 4-Fermi basis

At dimension-6

$$\mathcal{O}_6 \sim \frac{C}{\Lambda^2} (\bar{c}\Gamma b) (\bar{\tau}\Gamma'\nu) \quad C \in \mathbb{C} (\Rightarrow \text{CPV})$$

Wilson coefficients:

Simplified models:

LH (RH) $\nu_{L(R)}$

Vector: $C_{LL(LR)}^V, C_{RL(RR)}^V,$

Scalar: $C_{LL(LR)}^S, C_{RL(RR)}^S,$

Tensor: $C_{LL(RR)}^T,$

EW scalars C^S

W' C^V

Scalar/Vector LQ $C^V, C^{S\pm T}$

Normalized against SM: $\Lambda \sim (2\sqrt{2}G_F V_{cb})^{-1/2} \sim 870 \text{ GeV}.$

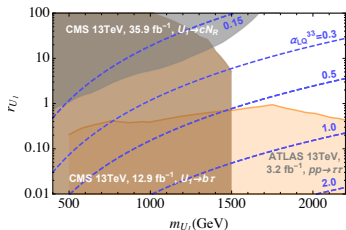
For 20–30% enhancement, **expect TeV scale NP**

- No* NP in $B \rightarrow D^{(*)}l\nu$: $|V_{cb}|$ constraints
- **Huge literature** for NP model building for $R(D^{(*)})$
- Simplified model mediators: EW charged scalars, W' 's or leptoquarks ($\tilde{R}_2, S_1, U_1, \dots$)

NP Status

- Tensions on W' and leptoquark C_V and $C_{S\pm T}$ type models
 - LHC: $pp \rightarrow \tau\tau/\tau\nu$
 - LHC: single or pair production + bc , $b\tau$, $c\tau$ final states
 - Flavor: b - s bounds (If there is a quark doublet involved)
- Pure C_S (Φ, \tilde{R}_2) leptoquark models face $B_c \rightarrow \tau\nu$ tensions

Eg. LHC exclusions/allowed regions for a vector leptoquark ($U_1 \sim (3, 1)_{2/3}$)



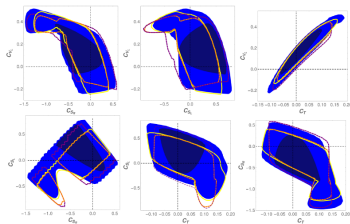
1807.04753 [DR, Shakya, Zupan]

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Latest (post-Moriond) **global** fits to $R(D^{(*)})$, plus other obs.

[1904.09311](#), [1904.10432](#)



[1904.09311](#) [Murgui, Penuelas, Jung, Pich]

NP Status

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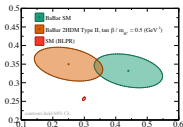
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Latest (pos)

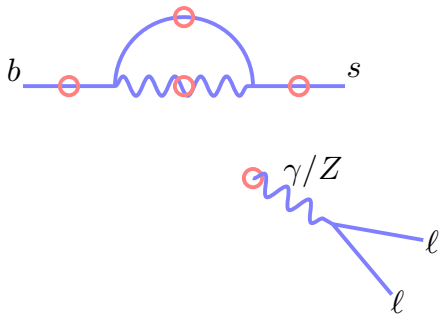
1904.09311, 190

Caveat: Measurement is a simultaneous BG + signal fit

- Naive global fits miss large SM/NP model template dependence
- Can't take fit exclusions/allowed regions too seriously
- Extensive program to correct this: expt reweighting software tool for direct WC fits Hammer [Bernlochner, Duell, Ligeti, Papucci, DR] hammer.physics.lbl.gov



Rare decays: $b \rightarrow sll$

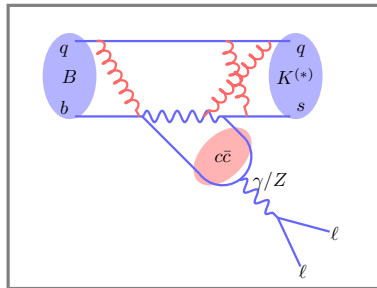
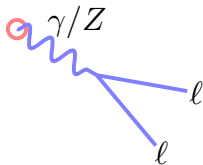
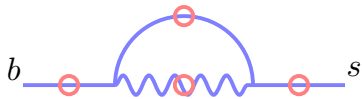


- Loop (penguin) process

$$\mathcal{M} \sim \frac{1}{16\pi^2} \frac{g^4}{m_W^2} V_{ts} V_{tb} \frac{m_t^2}{m_W^2}$$

- Experimentally clean signal: $B \rightarrow K^{(*)} ll$

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- But **hadronic uncertainties** less clear (long distance $c\bar{c}$)

Lepton Universality Tests

Factor out hadronic uncertainties: Consider **ratio** (see S. Sandilya's talk!)

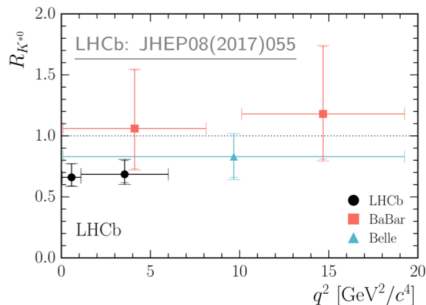
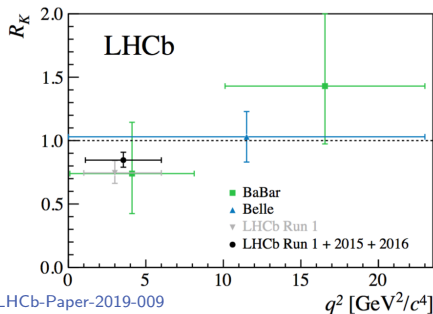
$$R_{K^{(*)}} = \frac{B \rightarrow K^{(*)} ee}{B \rightarrow K^{(*)} \mu\mu} \quad (\text{in various } q^2 \text{ binnings})$$

Should be 1.00 ± 0.01 in SM!

Bordone, Isidori, Pattori [1605.07633]

$$R_{K^+} = 0.846^{+0.060+0.016}_{-0.054-0.014}$$

$$R_{K^{*0}} = 0.69^{+0.11}_{-0.07} \pm 0.05,$$



Deviations of about 2.5σ in each $mode/q^2$ bin

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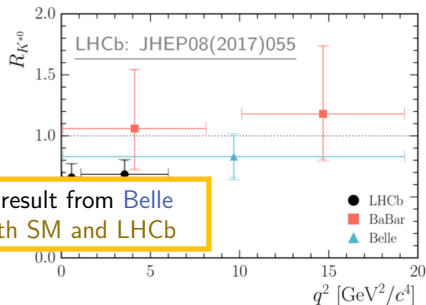
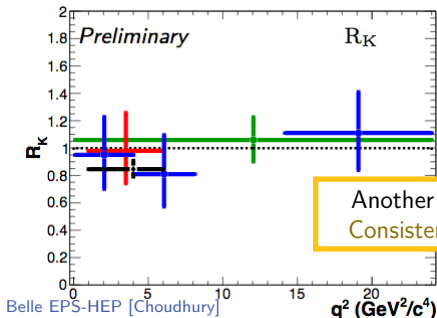
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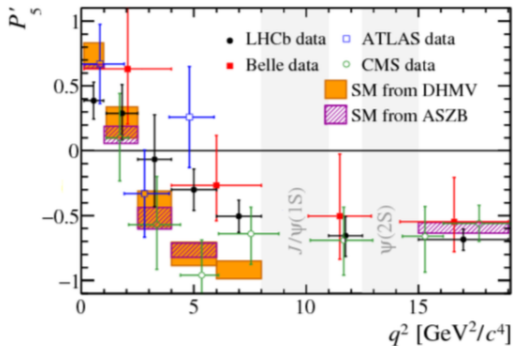


Deviations of about 2.5σ in each mode/ q^2 bin

Puzzle: Precision moments

Measure angular distributions in

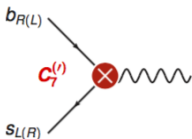
$$B \rightarrow K^*(\rightarrow K\pi)\mu\mu$$



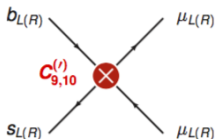
Deviations of about 2.5σ in several q^2 bins, but SM predictions are hard.

NP Explanations

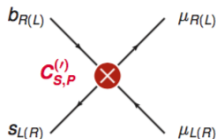
magnetic dipole operators



semileptonic operators



scalar operators



Courtesy W Altmannshofer

SM-like SL operators at dimension-6:

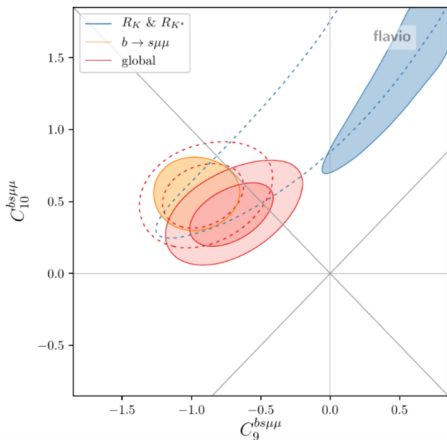
$$\frac{C_9^{(l)}}{\Lambda^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\mu \gamma^\mu \mu) + \frac{C_{10}^{(l)}}{\Lambda^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\mu \gamma^\mu \gamma^5 \mu)$$

Normalized against loop SM: $\Lambda \sim 4\pi v / \sqrt{V_{tb} V_{ts}} \sim 10 \text{ TeV}$.
 Expect 10 TeV scale NP

- Large amount of NP model building
- Typically leptoquarks or Z' models (e.g. gauged $L_\mu - L_\tau$)
- Some attempts to relate to $R(D^{(*)})$.

Global Fits

$C_{S,P}$ operators bounded by $B_s \rightarrow \mu\mu$; C_7 from $b \rightarrow s\gamma$; $C'_{9,10}$ highly disrupt angular fits: **focus on $C_{9,10}$**

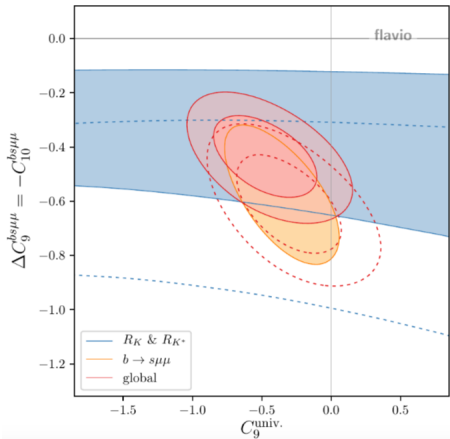


- Non-trivial: Mild coincidence for $R_{K^{(*)}}$ and P'_5 explanations

Aebischer et al [1903.10434]

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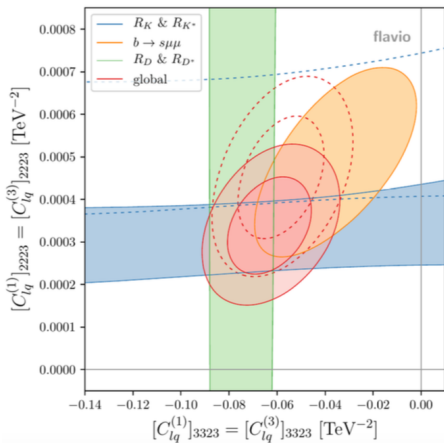


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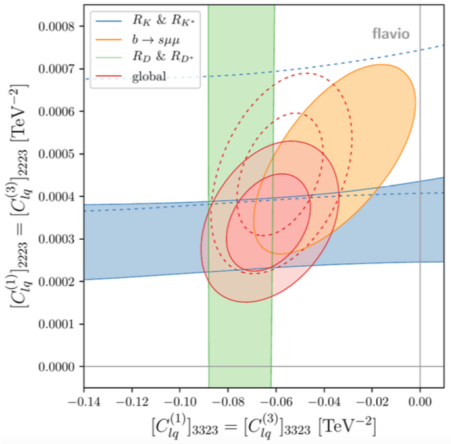
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Naive global combination with $R(D^{(*)})$
 \Rightarrow **vector leptoquark $U_1 \sim (3, 1)_{2/3}$**

But same cautions apply for $R(D^{(*)})$
 data

Global Fits

$C_{S,P}$ operators bounded by $B_s \rightarrow \mu\mu$; C_7 from $b \rightarrow s\gamma$; $C'_{9,10}$ highly disrupt angular fits: **focus on $C_{9,10}$**



Aebischer et al [1903.10434]

- But maybe some things aren't meant to be combined?
- plus

Bonus: Long-lived Particles (LLPs)

Emerging **hot topic** for future LHC searches:
Look for displaced decays-in-flight of exotic LLPs

E.g. in the SM: K_L , π^+ , n , μ

- Occur generically in beyond SM extensions with **small couplings** or **scale (or loop) hierarchies** or **phase space suppression**: SUSY, Composite Higgs, Hidden Valleys, (inelastic) DM, neutrino masses

broken sym
weak mixing/ marginal operator
technically natural

$$\Gamma \sim \varepsilon^2 \left(\frac{m}{M} \right)^n \text{PS}$$

$m \ll M$, typically $n \geq 4$
loop factors

squeezed spectra
approx sym
multibody decays

- If SM backgrounds are controlled: **clean signature of NP**

Beyond LHC: A large number of proposals
SHiP, MATHUSLA, FASER, CODEX-b, ...

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Dominant production portals may
occur through **FCNC** processes

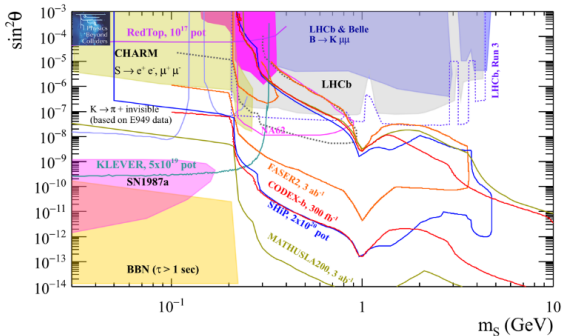
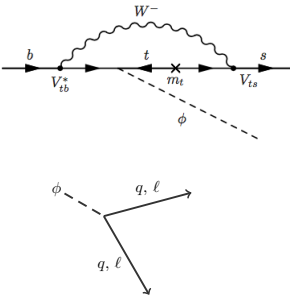
E.g. Dark scalar ϕ via $b \rightarrow s\phi$

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Beyond LHC: A large number of proposals
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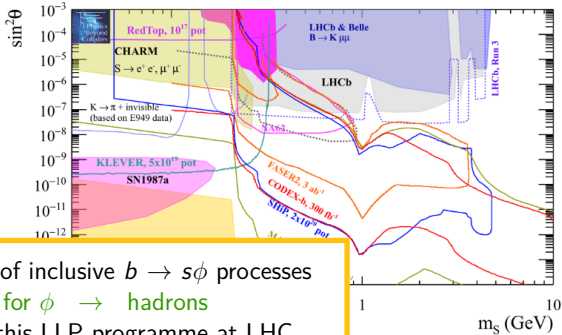
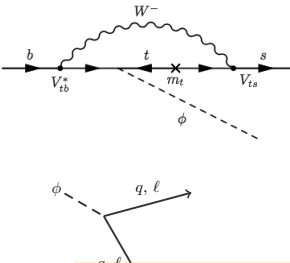
E.g. Higgs-scalar mixing

- $\mathcal{L} \sim \phi H^\dagger H$
- Higgs-scalar mixing angle θ induces Yukawa $y_f \sin\theta \phi \bar{f} f$
- Production via $b \rightarrow s\phi$ and decay controlled by single parameter



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Theoretical control of inclusive $b \rightarrow s\phi$ processes and rates for $\phi \rightarrow$ hadrons will be crucial to this LLP programme at LHC
 Similar: Heavy neutral lepton searches, ...

Summary

- Space of **smoking guns** and **precision** measurements: lots of heavy flavor mysteries to be understood!
- Precision tensions in $|V_{cb}|$, $b \rightarrow s\mu\mu$ will be **established** or **resolved** with more data
- **Smoking gun anomalies** suggest leptoquarks, but more careful, self-consistent study is needed (at least for $b \rightarrow c\tau\nu$, $R(D^{(*)})$ interpretations)
- Emerging and crucial role for flavor in development of the **LLP program** at LHC and beyond

Thanks!