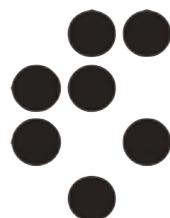


# Uncovering latent jet substructure

Jernej F. Kamenik

mostly based on 1904.04200

with D. A. Faroughy & B. M. Dillon + Manuel Szewc

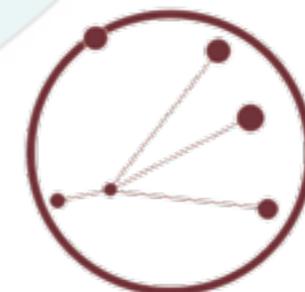


Institut  
"Jožef Stefan"  
Ljubljana, Slovenija



Univerza v Ljubljani

Fakulteta za matematiko in fiziko



**HC<sup>2</sup>NP**

Tenerife, 23-28 September 2019

# The Challenge

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How to disentangle NP from NP?

# The Challenge

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How to disentangle NP from NP?

QCD

UV

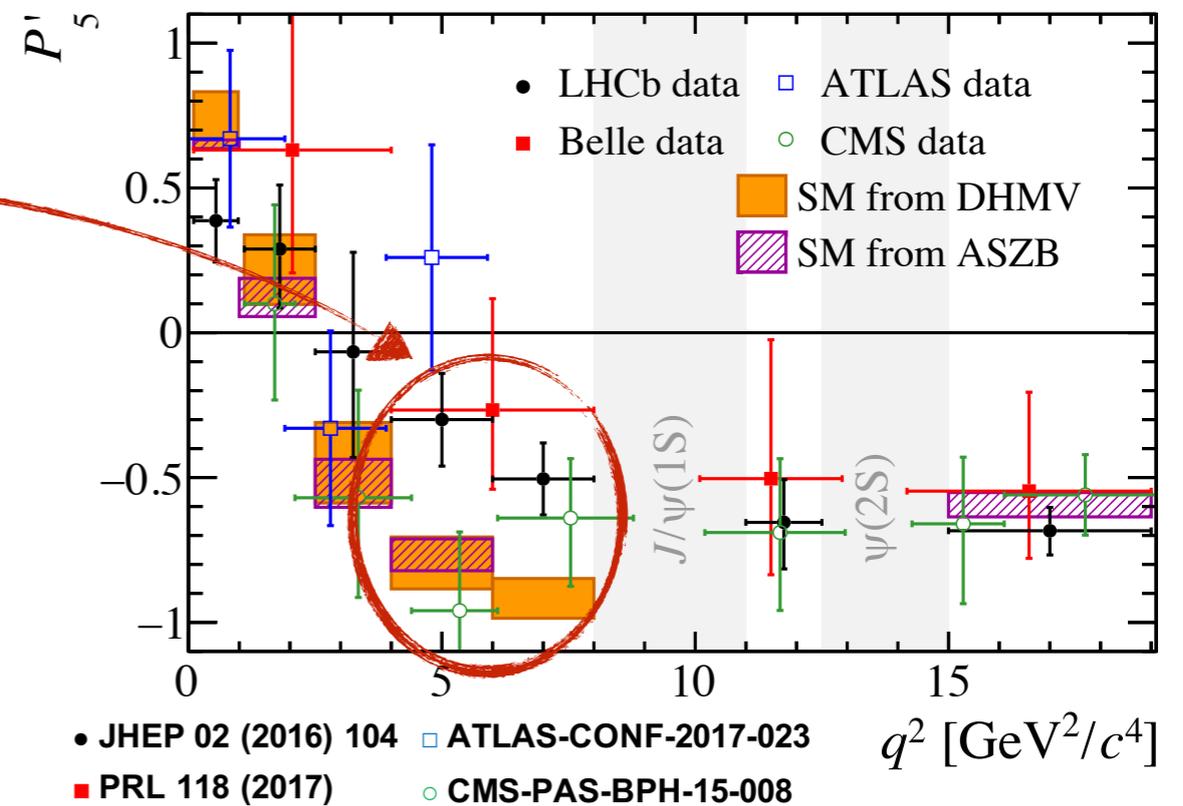
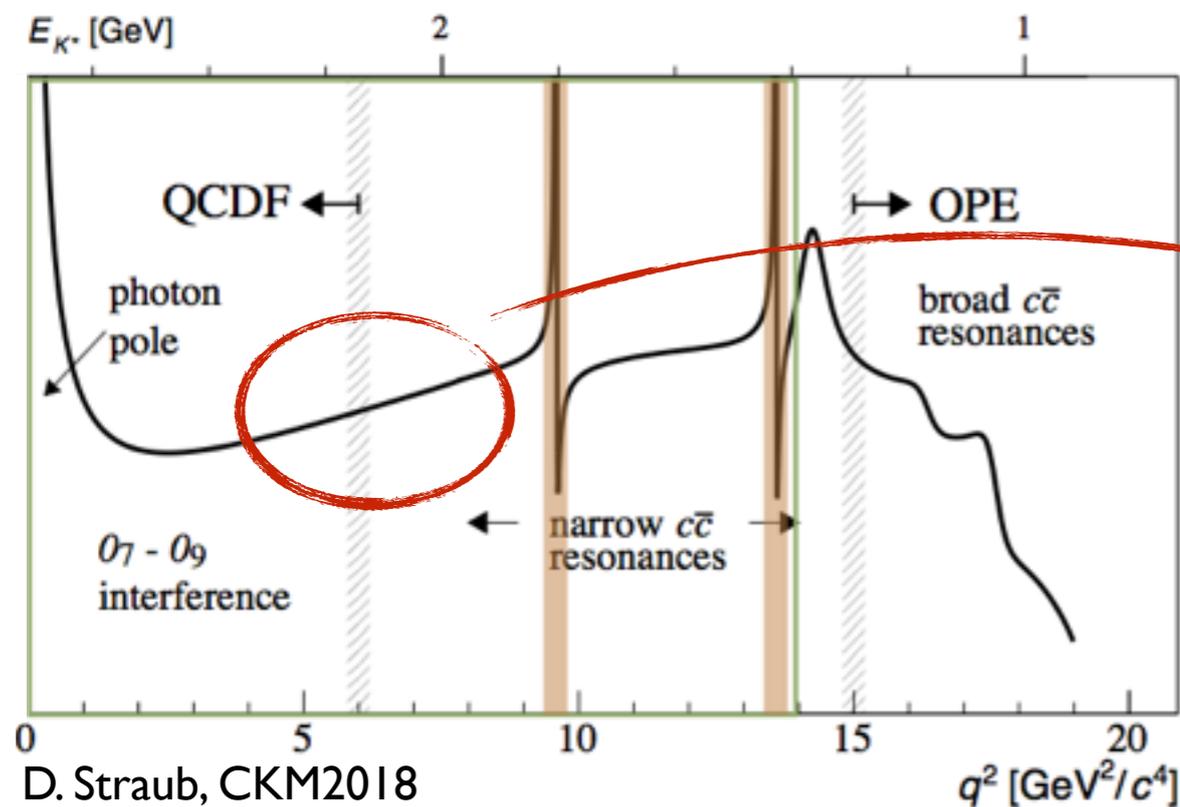
# The Challenge

How to disentangle NP from NP?

QCD UV

Example: spectrum of  $B \rightarrow K^* \ell^+ \ell^-$

also  $(g-2)_\mu, \epsilon'/\epsilon, \dots$



# The Challenge

How to disentangle NP from NP?

QCD

UV

Example: origin of jets at LHC

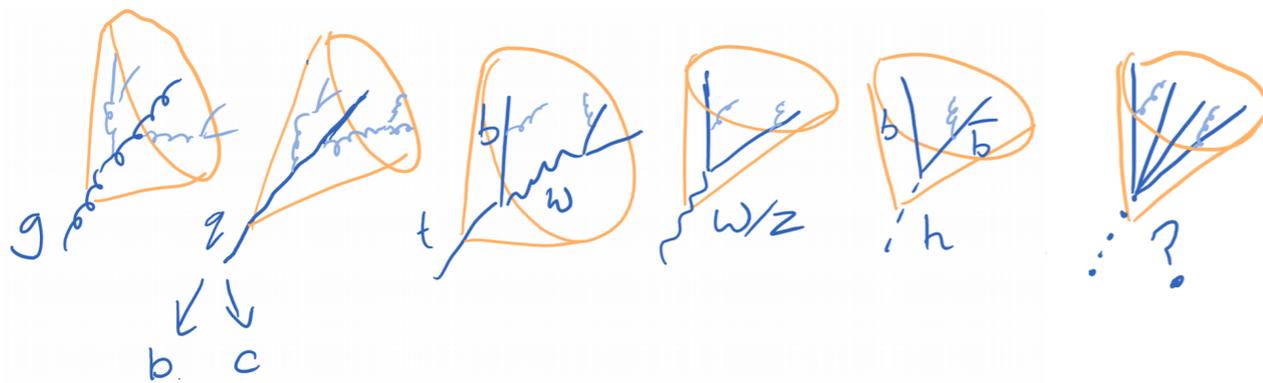
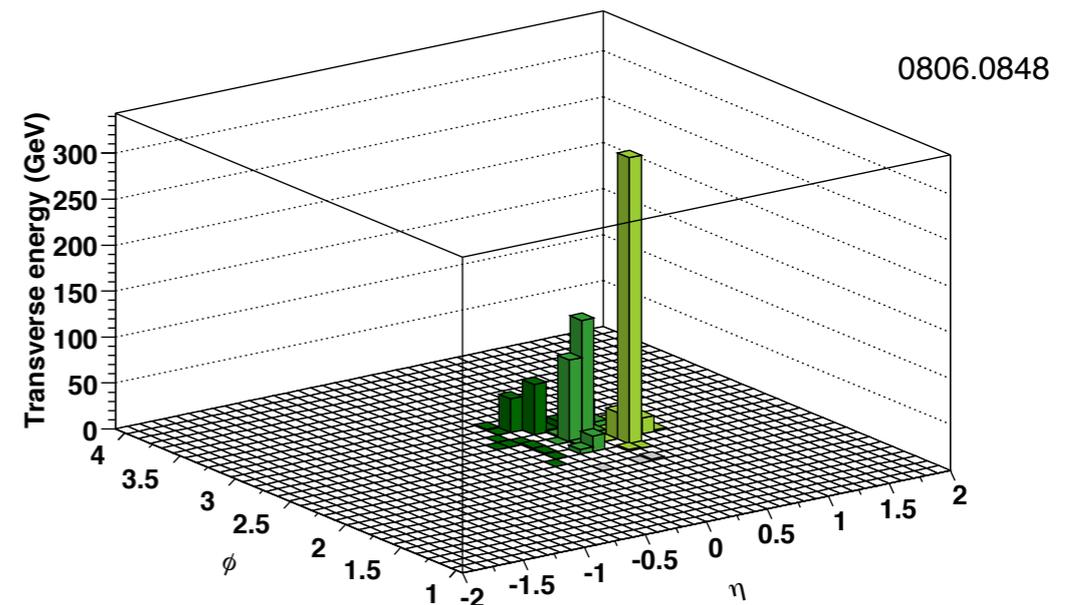


figure by J. Collins



# The Challenge

How to disentangle NP from NP?

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Example: origin of jets at LHC

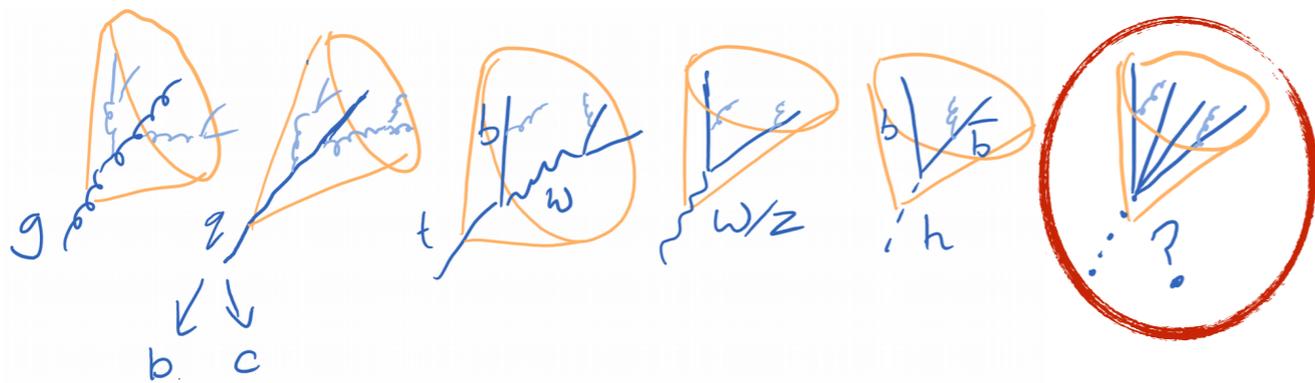
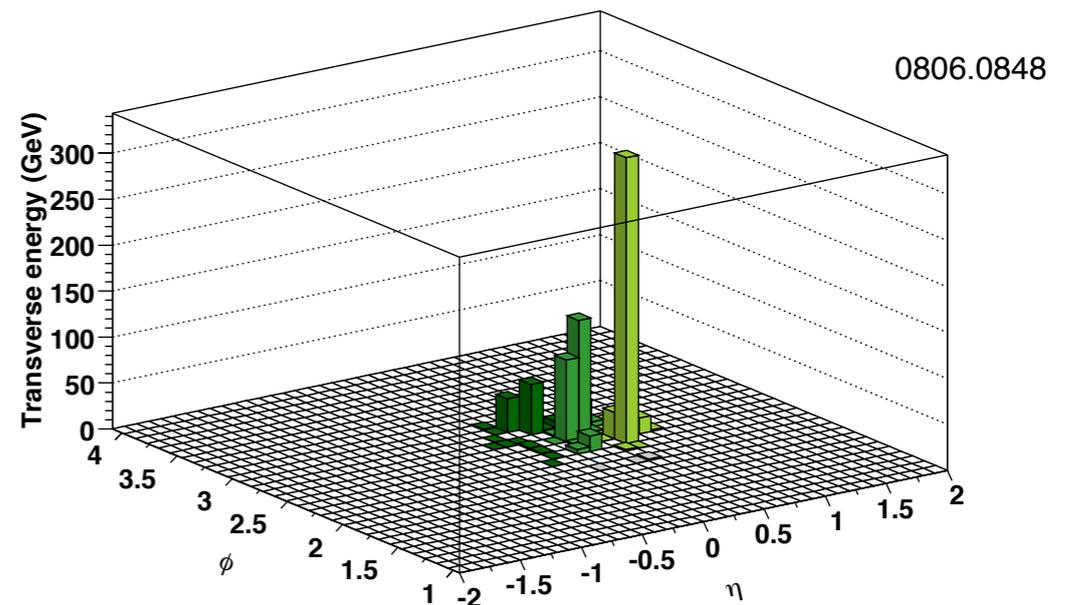


figure by J. Collins



# The Challenge

How to disentangle NP from NP?

QCD

UV

Example: origin of jets at LHC

Generic NP cascades:

$H^+ \rightarrow t b$  (hadronic + leptonic)

$X \rightarrow YY \rightarrow hhhh$

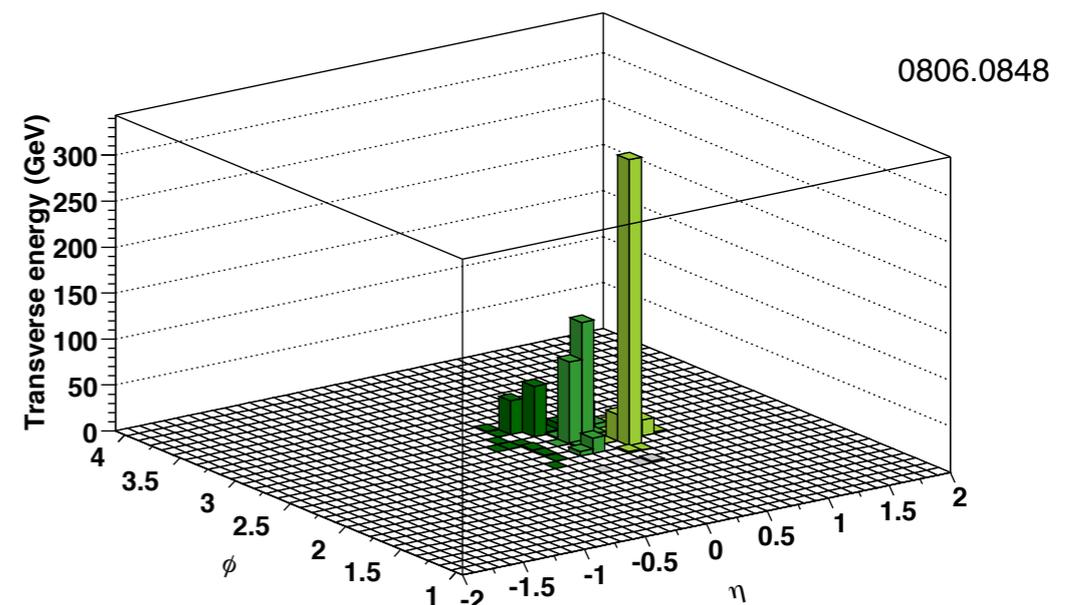
$X \rightarrow WW$  (hadronic + semi-leptonic)

$X \rightarrow AB \rightarrow \tau\tau gg$

....

O(300) possibilities for boosted  $X \rightarrow 4$  SM particles  
O(10k) possibilities for dijet combinations.

Dark quarks with BSM showers?



# The Challenge

---

How to disentangle NP from NP?

QCD

UV

## Task of classification

QCD Limited theoretical control & tools (pert. QCD, QCDF, sum rules, lattice, QCD shower & fragmentation models, ...)

UV Exhaustive exploration of NP model space?

+ experimental systematics, limited statistics, etc...

*How much can "we" learn directly from data?*

# Approaches to classification

---

## 1. Supervised (boosted decision trees, neural networks, ...)

train (general enough) model on (fit to) pre-labelled data

domain (QCD) knowledge through labelling/generation of training data

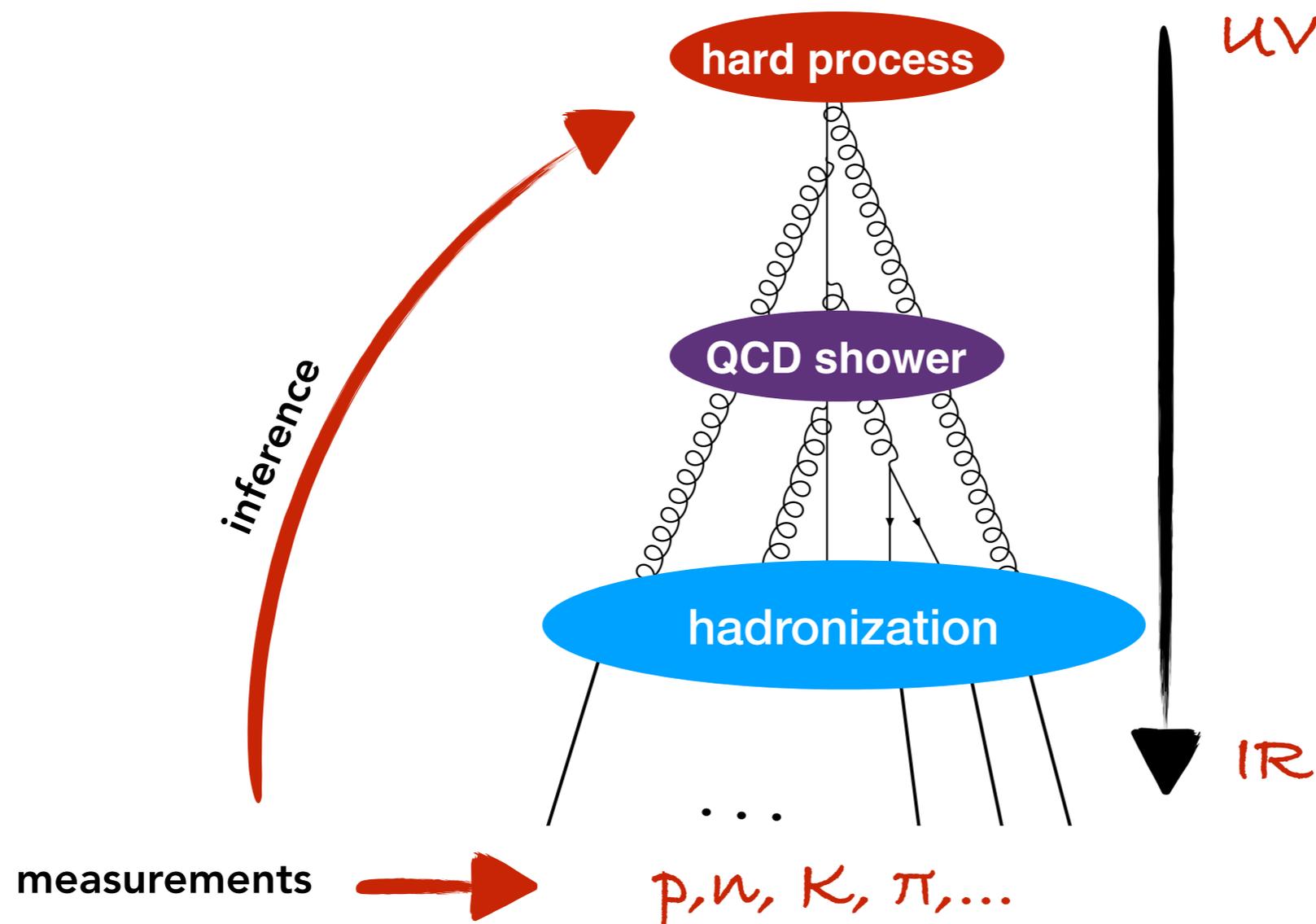
## 2. Unsupervised (e.g. (jet) clustering algorithms)

search for structures within (unlabelled) data using priors for the structure distributions

domain knowledge through choice of priors / clustering model

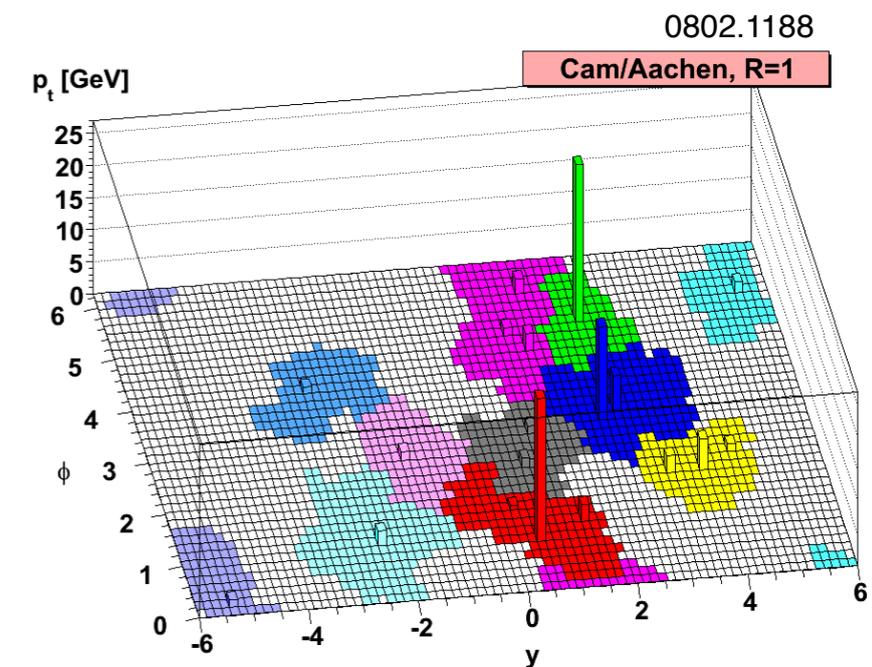
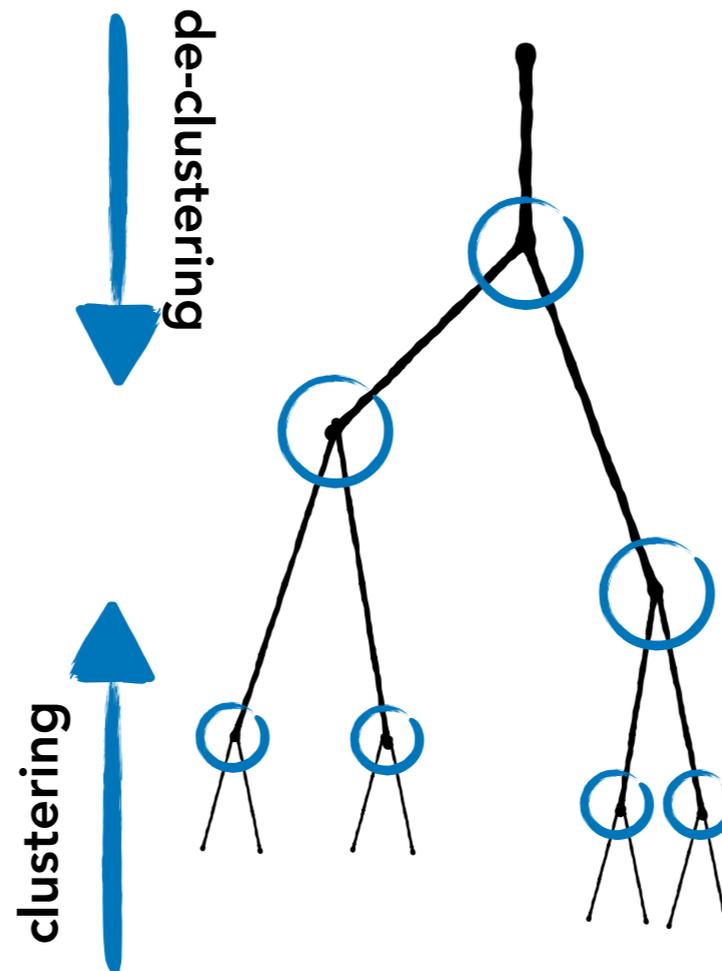
# How a jet is formed (& reconstructed)

Jet formation: starting from a hard 'seed' - sequential combination of QCD showering, fragmentation and hadronization and possibly massive particle decays



# How a jet is formed (& reconstructed)

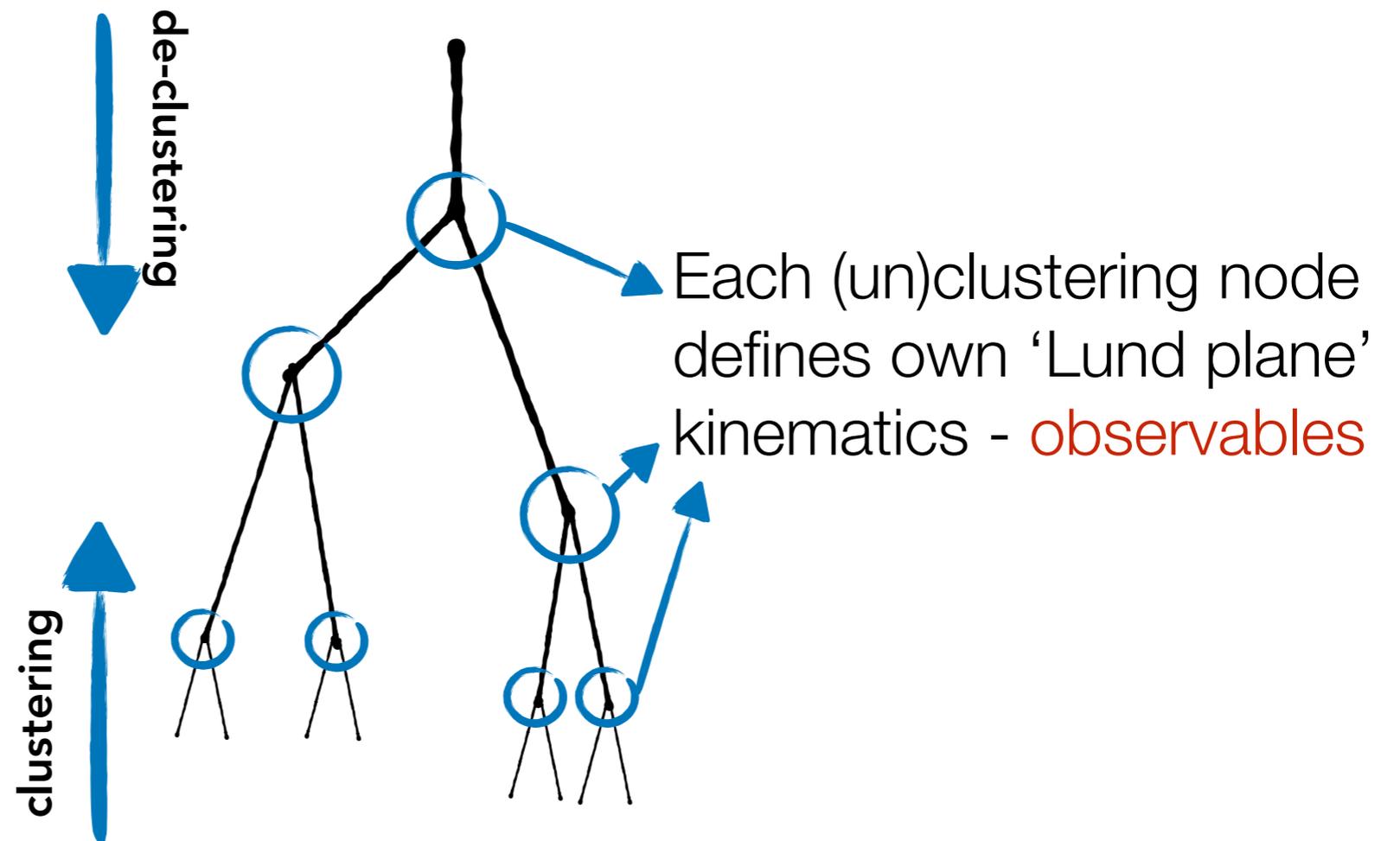
Jet reconstruction: sequential combination of energy/momentum (sub) clusters based on appropriate IRC safe measure (e.g.  $k_T$ )



Clustering history - proxy for how jet was formed

# How a jet is formed (& reconstructed)

Jet reconstruction: sequential combination of energy/momentum (sub) clusters based on appropriate IRC safe measure (e.g.  $k_T$ )



$$\Delta \equiv \Delta R_{ij},$$

$$z \equiv \frac{p_{tj}}{p_{ti} + p_{tj}},$$

$$k_t \equiv p_{tj} \Delta,$$

$$\kappa \equiv z \Delta,$$

$$m^2 \equiv (p_i + p_j)^2 \quad \text{Dreyer, Salam \& Soyez, 1807.04758}$$

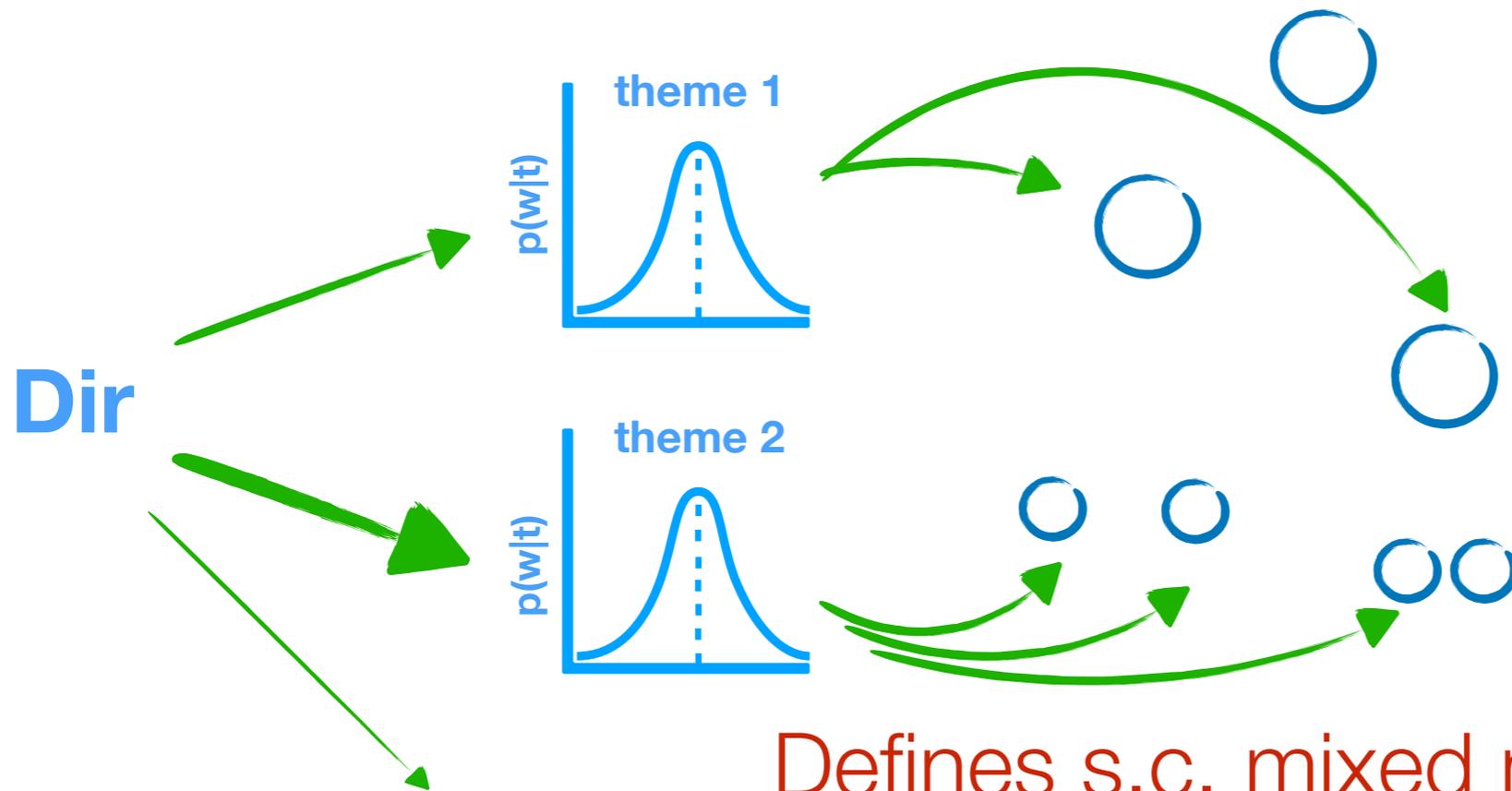
$$\psi \equiv \tan^{-1} \frac{y_j - y_i}{\phi_j - \phi_i}$$

# Simplified generative model of jet (observables)

---

Assume:

- most of useful jet information contained in node observables
- their values are generated by sampling from several underlying 'latent' distributions (e.g. QCD splitting, particle decay,...) - *themes*

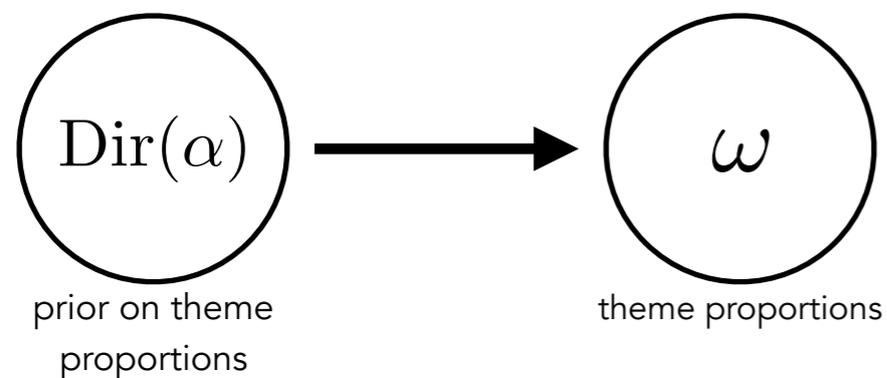


Defines s.c. mixed membership model  
of Latent Dirichlet Allocation

# Latent Dirichlet Allocation for jet observables

---

Construct the generative model for jets with  $K$  themes

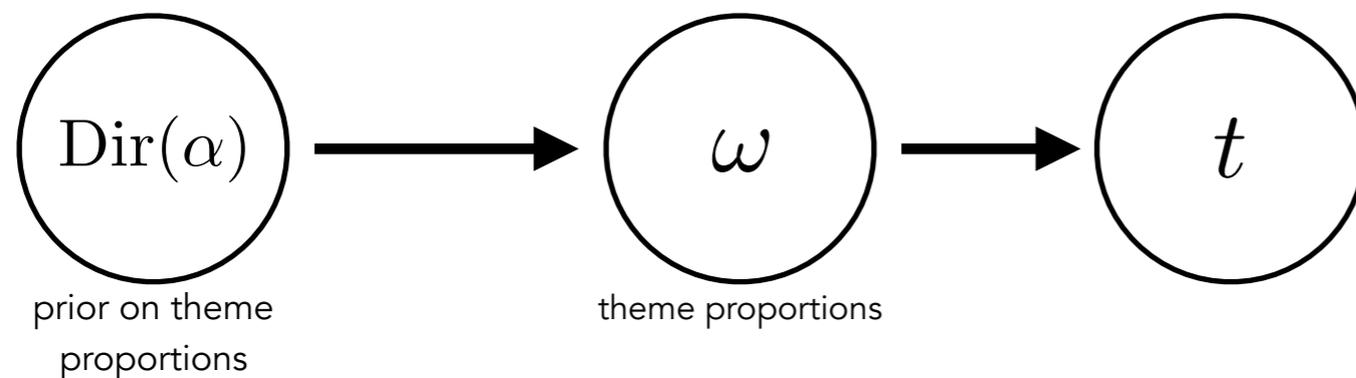


Step 1: sample proportions for each theme, a  $K$ -dimensional multinomial

# Latent Dirichlet Allocation for jet observables

---

Construct the generative model for jets with  $K$  themes

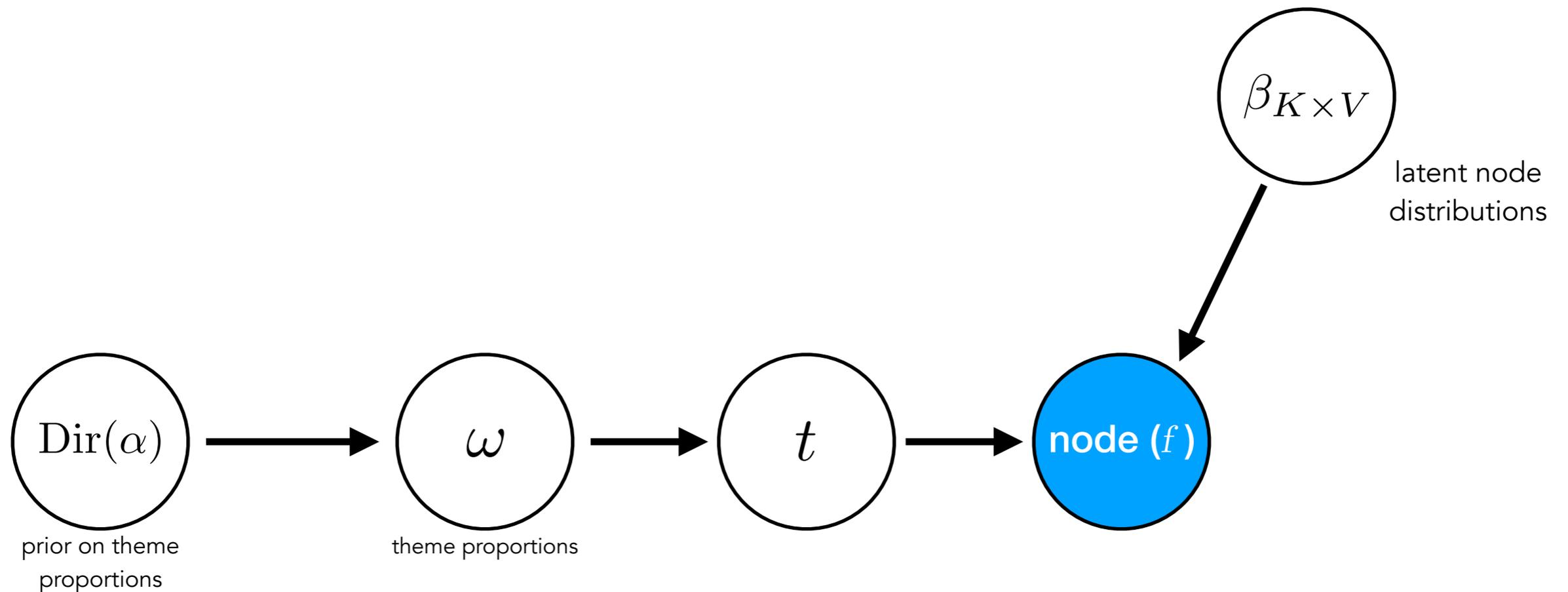


Step 2: sample a single theme from the multinomial

# Latent Dirichlet Allocation for jet observables

---

Construct the generative model for jets with  $K$  themes

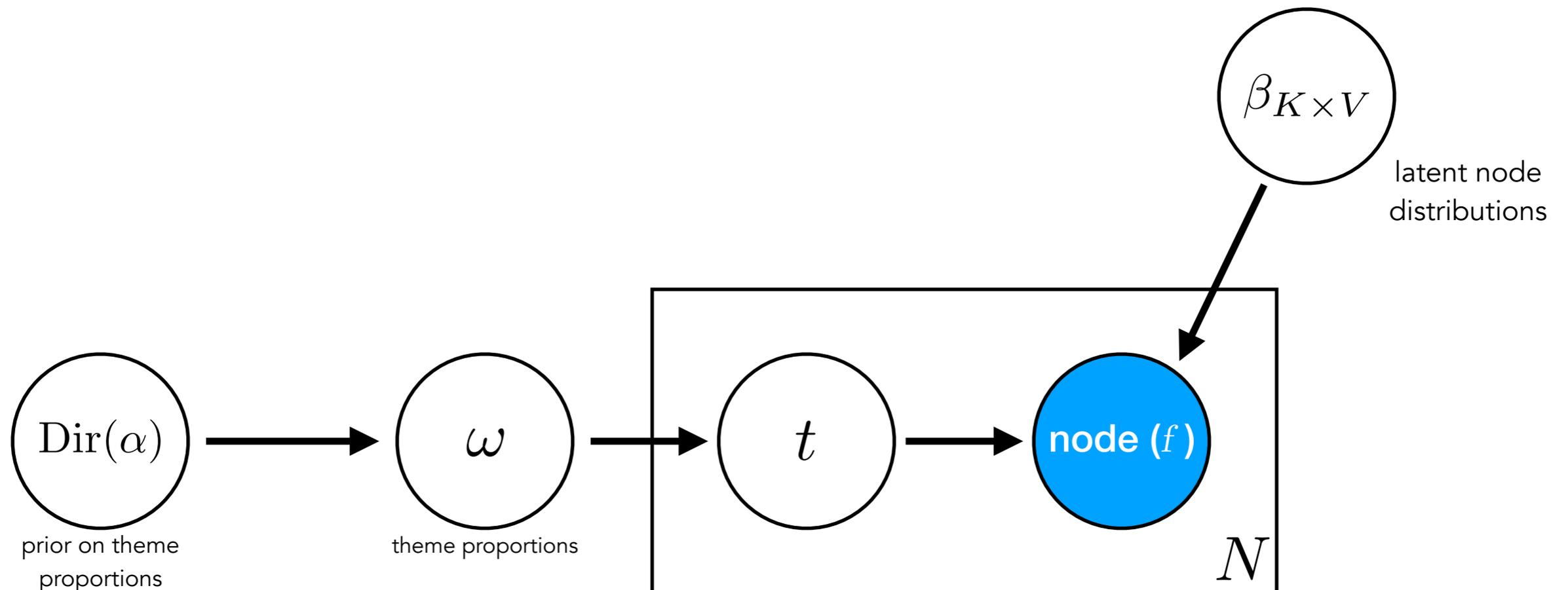


Step 3: sample a node from the appropriate theme distribution

# Latent Dirichlet Allocation for jet observables

---

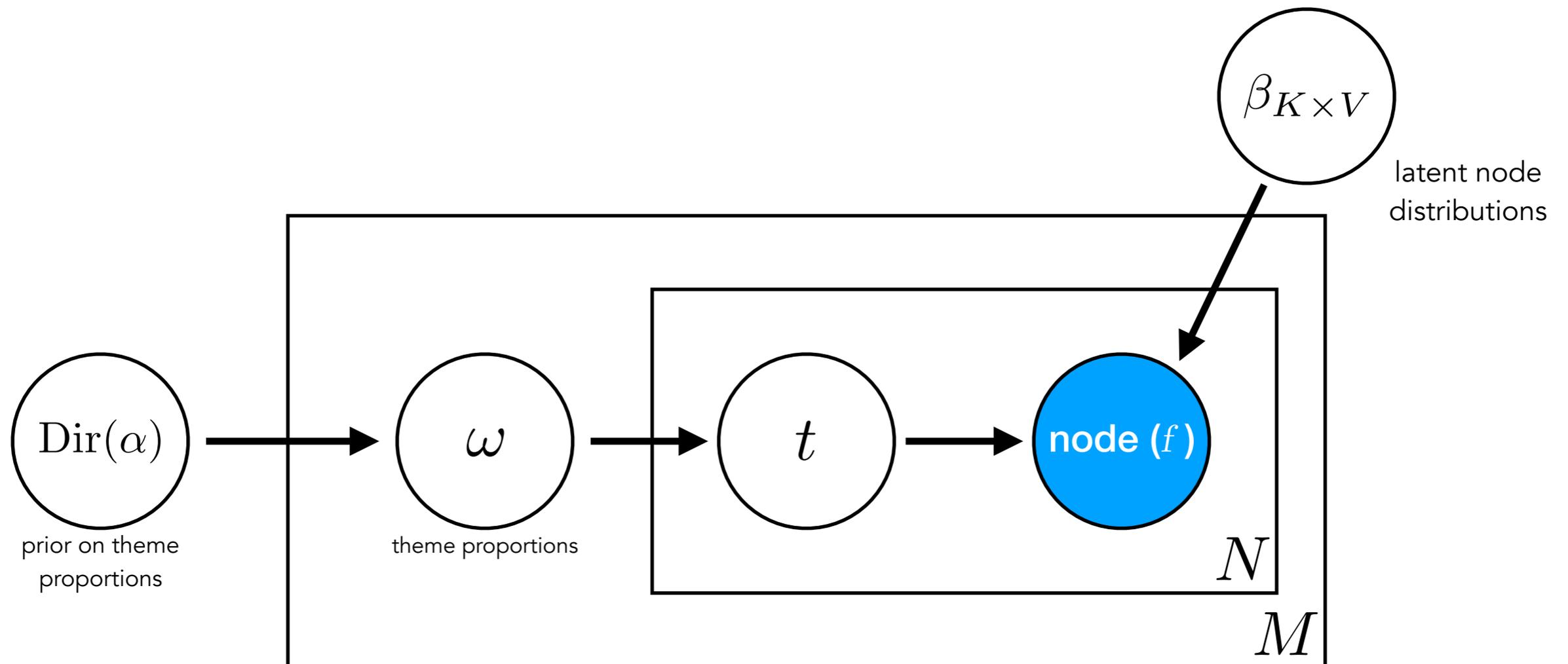
Construct the generative model for jets with  $K$  themes



- repeat this for each of the  $N$  nodes in the jet

# Latent Dirichlet Allocation for jet observables

Construct the generative model for jets with  $K$  themes



- repeat this for each of the  $N$  nodes in the jet
- repeat again for each of the  $M$  jets you want to generate

# Latent Dirichlet Allocation for jet observables

---

Construct the generative model for jets with  $K$  themes

Define probability to generate a set of node observables ( $f$ )

$$p(\text{jet}|\alpha, \beta) = \int_{\omega} p(\omega|\alpha) \prod_{f \in \text{jet}} \left( \sum_t p(t|\omega) p(f|t, \beta) \right)$$

Solve for latent theme distributions ( $\beta$ ) using Bayes theorem & approximate inference

$$\beta_{K \times V}^{\text{MLE}} = \underset{\beta}{\text{argmax}} \log \left( \prod_{i=1}^M p(\text{jet}_i|\alpha, \beta) \right)$$

Originally constructed for study of genotypes & text topics

Papadimitriou, Raghavan, Tamaki & Vempala (1998)

Hofmann (1999)

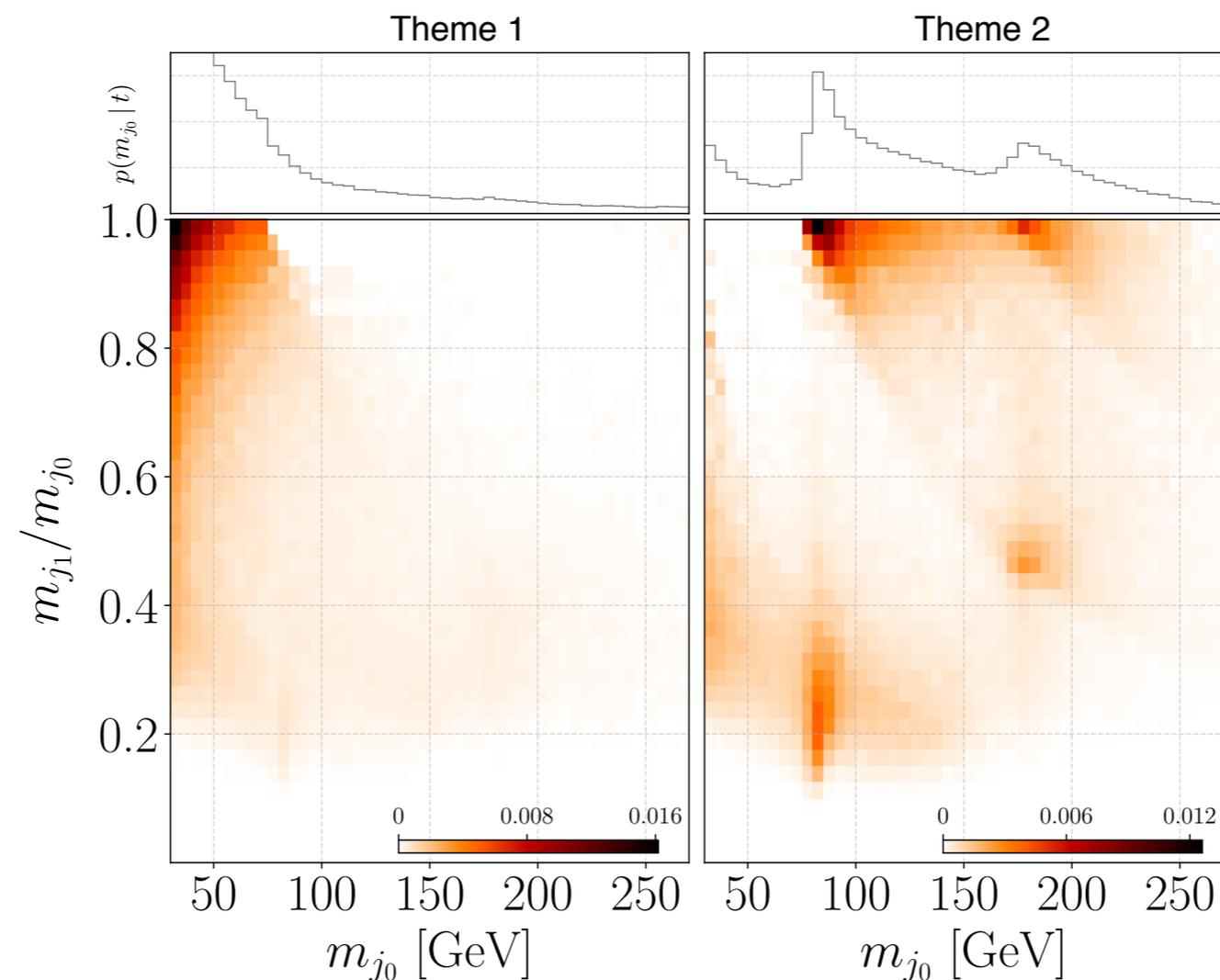
Blei, Ng, & Jordan (2002)

# Example LDA models: top jets

2-theme LDA trained on mixed sample (**S+B**) using jet mass

**B**: QCD dijets

**S**:  $pp \rightarrow t\bar{t} \rightarrow W^+W^-b\bar{b}$ ,  $S/B = 1$

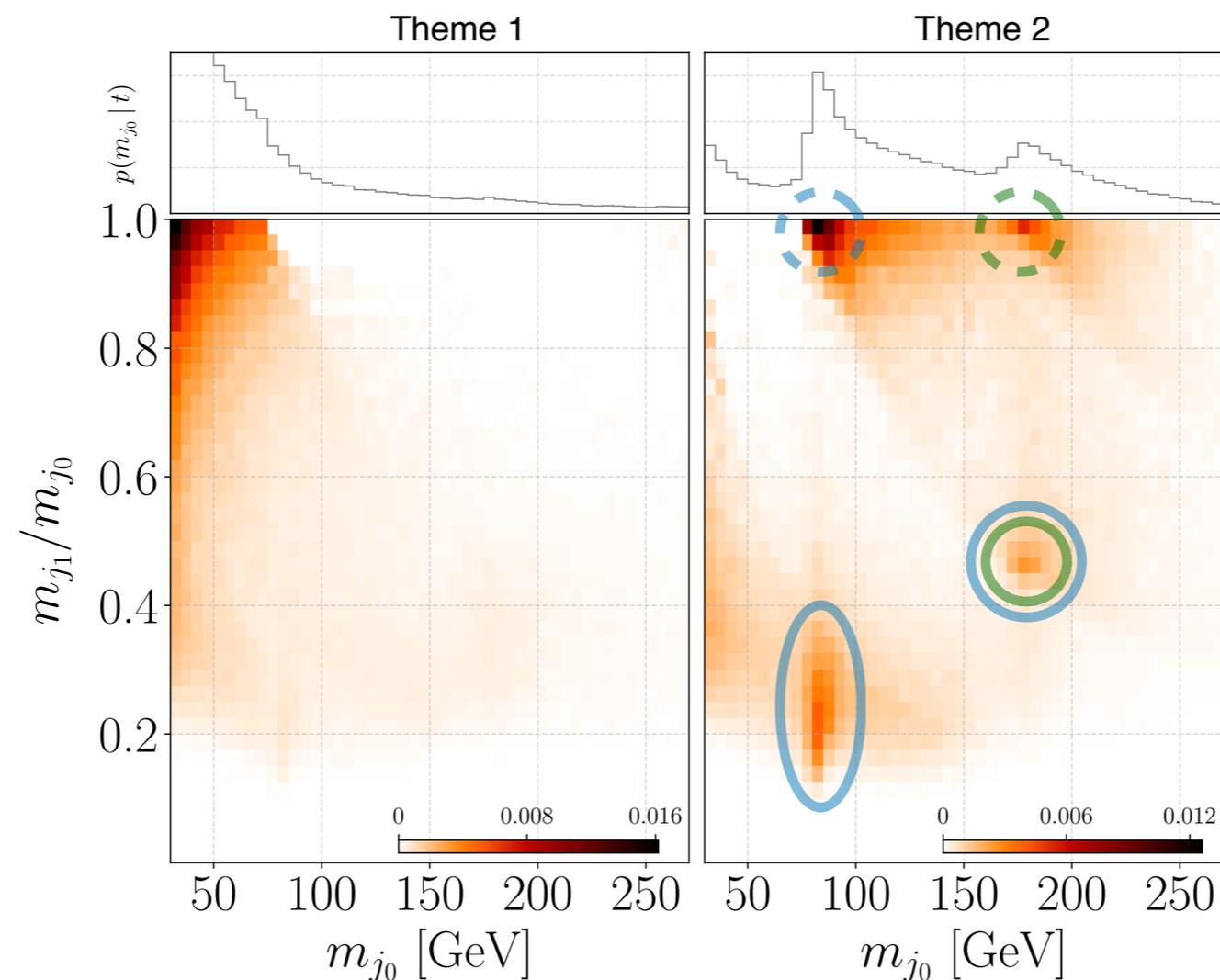


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# Example LDA models: NP jets

---

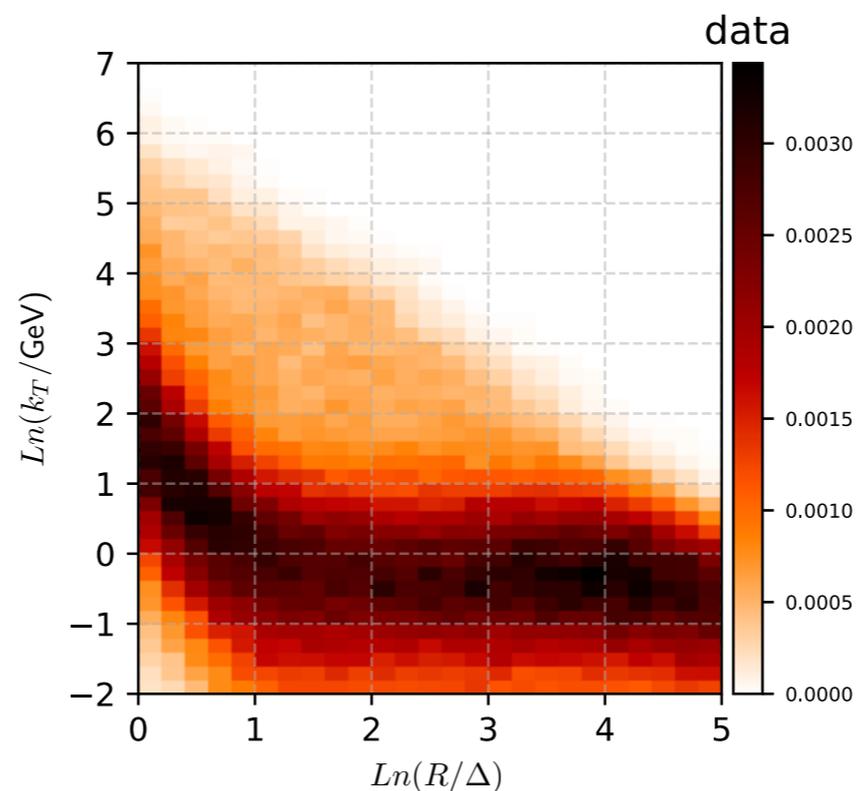
2-theme LDA trained on mixed sample (**S+B**) in Lund plane

**B**: QCD dijets

**S**:  $pp \rightarrow W' \rightarrow W\phi \rightarrow WZb\bar{b}$        $S/B = 0.011$

$m_{W'} = 3 \text{ TeV}, m_\phi = 400 \text{ GeV}$        $m_{jj} \in 2730 - 3190 \text{ GeV}$

J. H. Collins, K.  
Howe, B. Nachman  
(2019)



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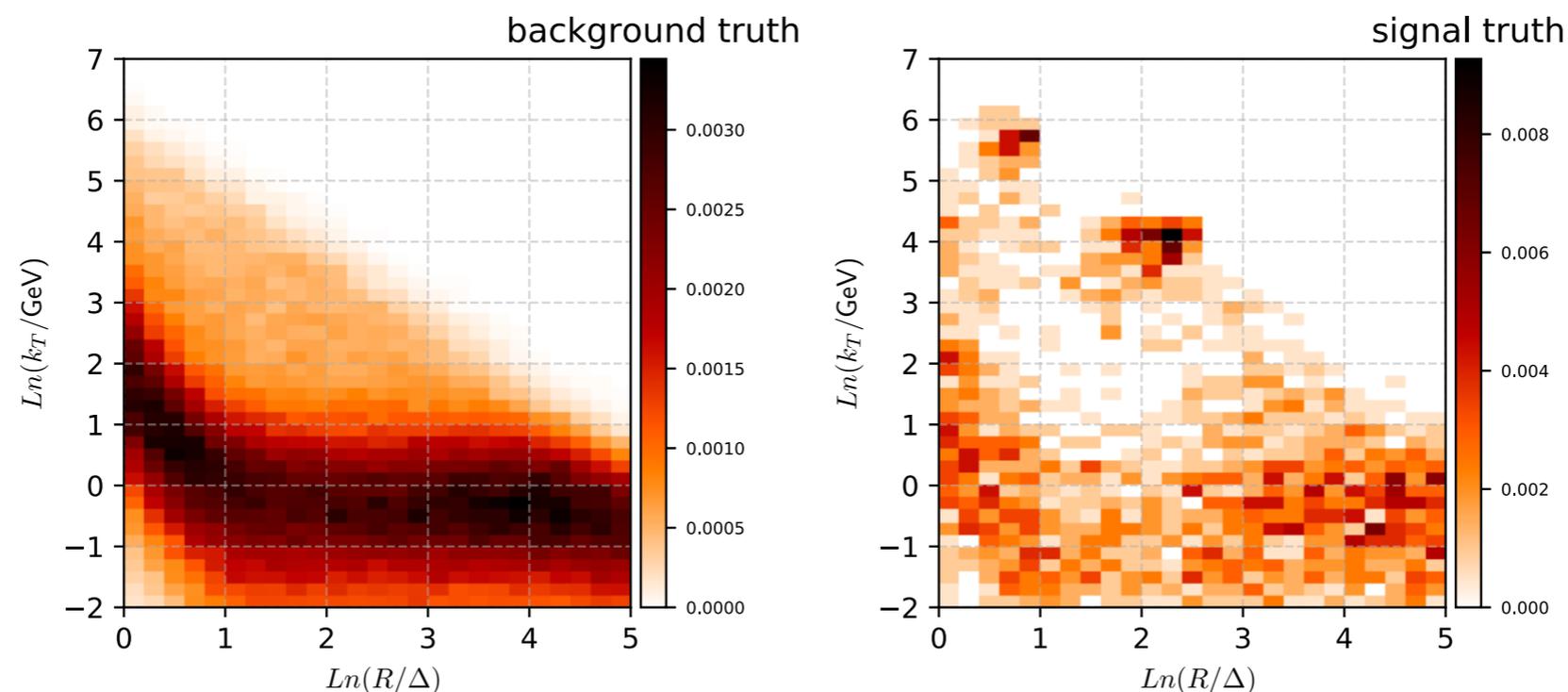
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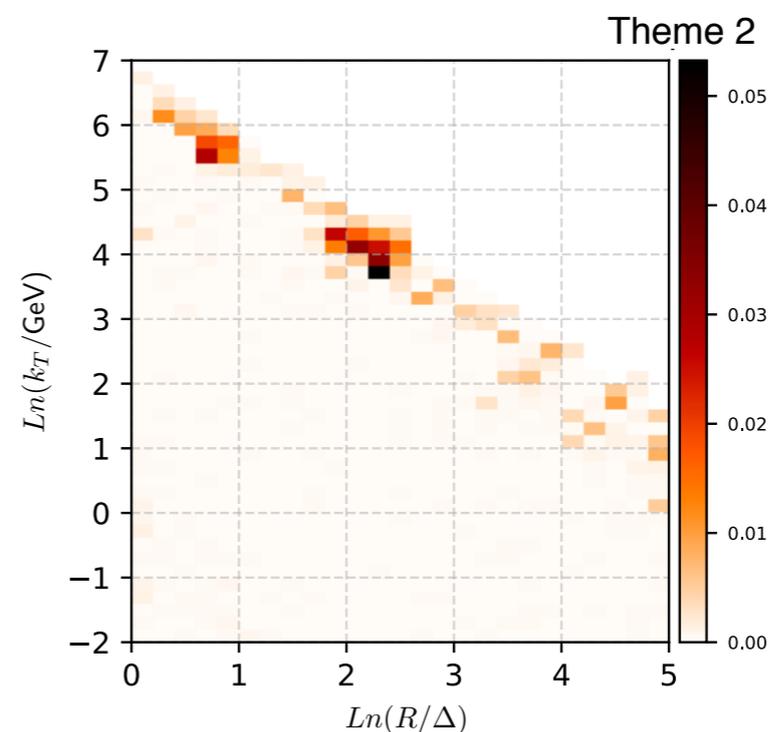
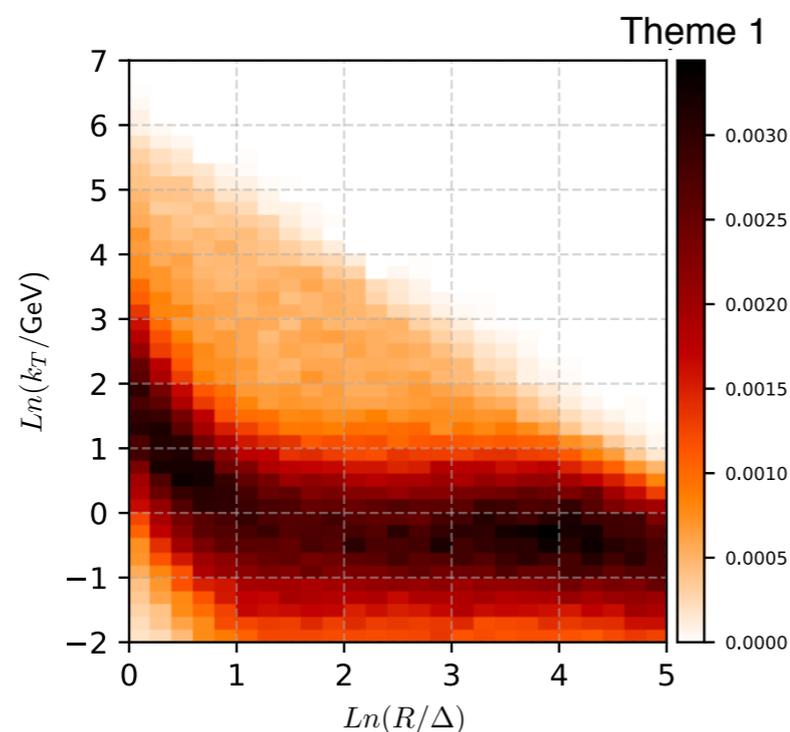
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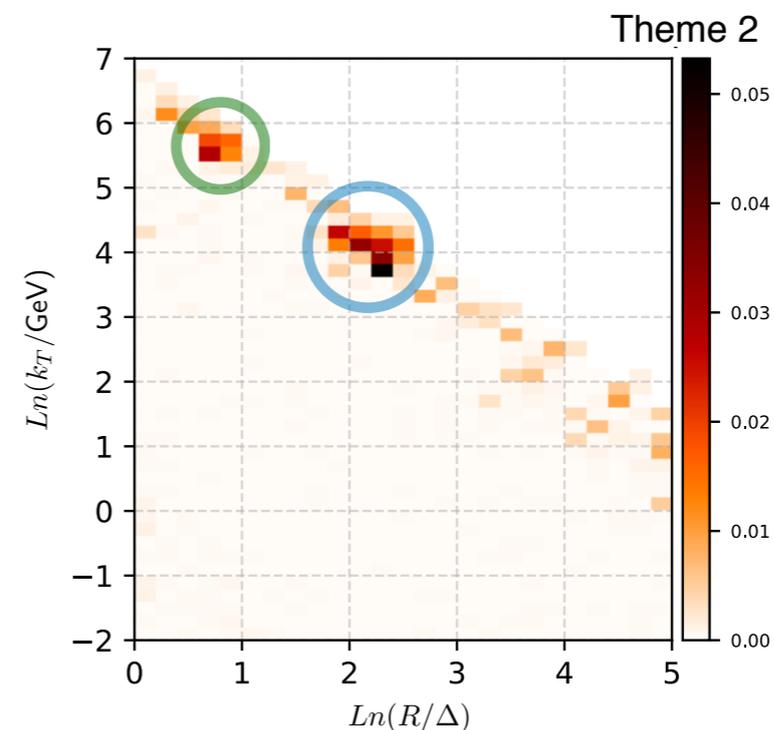
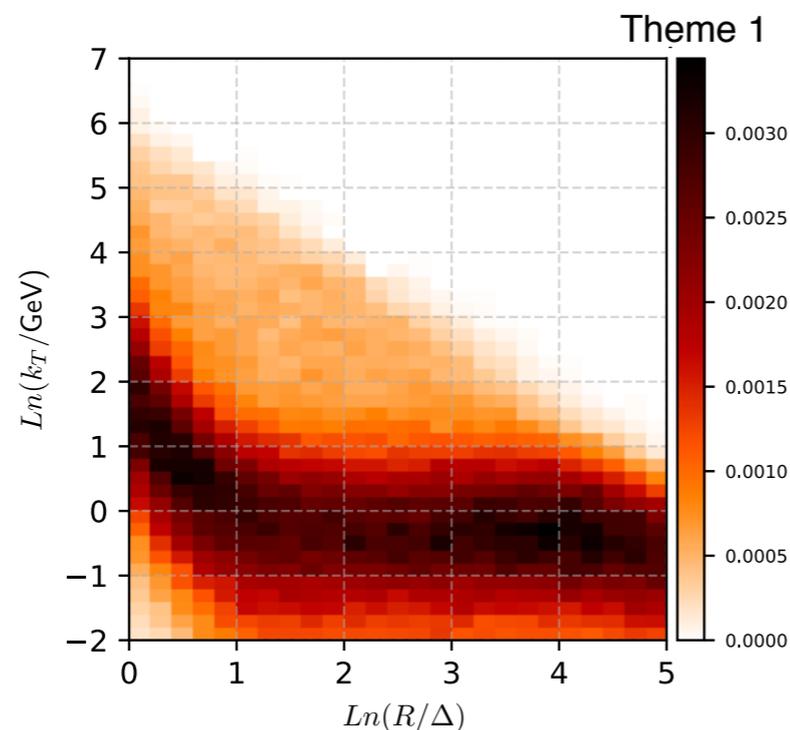
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J. H. Collins, K.  
Howe, B. Nachman  
(2019)



Can we use this information to classify QCD from UV?

# Jet classification: basics

---

$\mathbf{x}$  list of observables useful for distinguishing  $S$  from  $B$

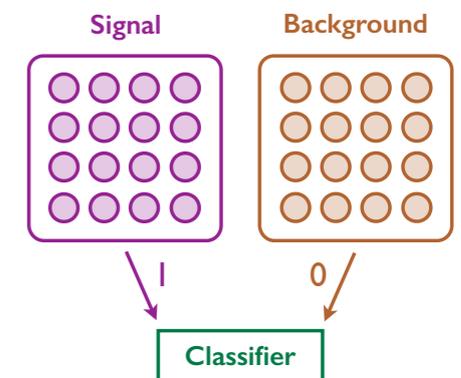
$p_S(\mathbf{x})$  and  $p_B(\mathbf{x})$  - probability distributions of  $\mathbf{x}$  for  $S$  and  $B$

classifier  $h(\mathbf{x})$  close to 1 for  $S$  and close to 0 for  $B$  - to be learned by minimizing loss function (e.g mean-square)

receiver operating characteristic (ROC) curve

$$\epsilon_S = \int d\vec{x} p_S(\vec{x}) \Theta(h(\vec{x}) - c)$$

$$\epsilon_B = \int d\vec{x} p_B(\vec{x}) \Theta(h(\vec{x}) - c)$$



Neyman-Pearson lemma:  $h_{\text{optimal}}(\vec{x}) = p_S(\vec{x})/p_B(\vec{x})$  (likelihood ratio)

If  $\mathbf{x}$  - low dimensional, can use histograms directly, otherwise use supervised ML (BDTs, NNs, ...)

# Jet classification: basics

x list of o

$p_S(x)$  and

classifier

learned k

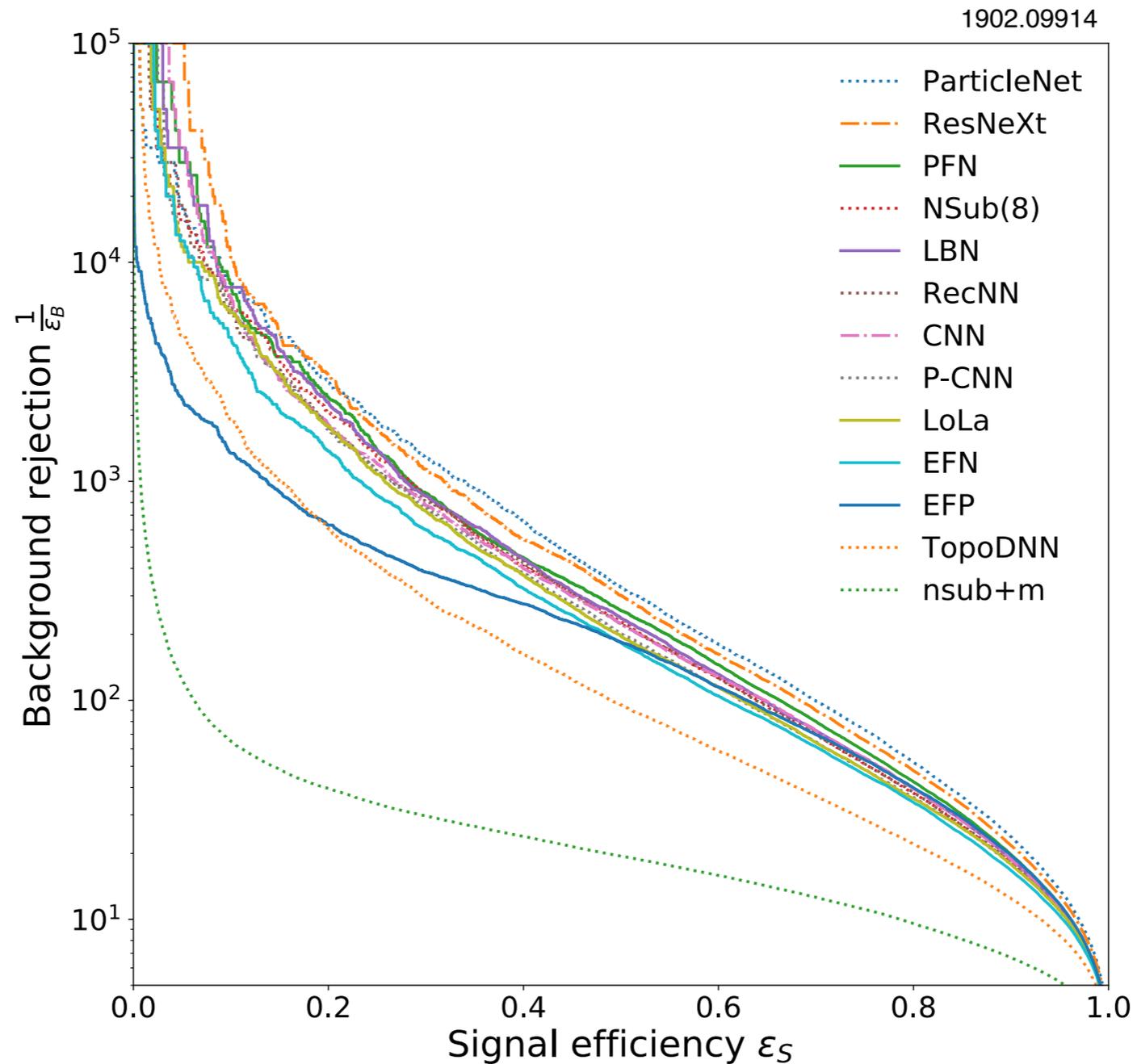
receiver o

Neyman-

If x - low

otherwise

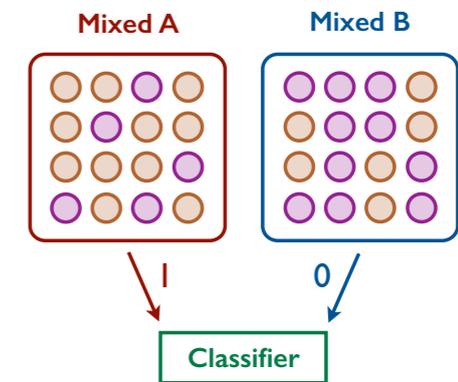
Example: QCD j vs. t classification (top-tagging)



# Jet classification: mixed samples

Classification from mixed samples: pure samples not available in real data

$$p_{M_1}(\vec{x}) = f_1 p_S(\vec{x}) + (1 - f_1) p_B(\vec{x}),$$
$$p_{M_2}(\vec{x}) = f_2 p_S(\vec{x}) + (1 - f_2) p_B(\vec{x}),$$



1.) Assume  $f_1, f_2$  known (e.g. from MC), then simply

$$h_{\text{optimal}}^{M_1/M_2}(\vec{x}) = p_{M_1}(\vec{x}) / p_{M_2}(\vec{x})$$

2.) Assume only  $f_1 > f_2$  then use monotonicity of

$$\frac{p_{M_1}}{p_{M_2}} = \frac{f_1 p_S + (1 - f_1) p_B}{f_2 p_S + (1 - f_2) p_B} \quad (\text{Classification Without Labels})$$

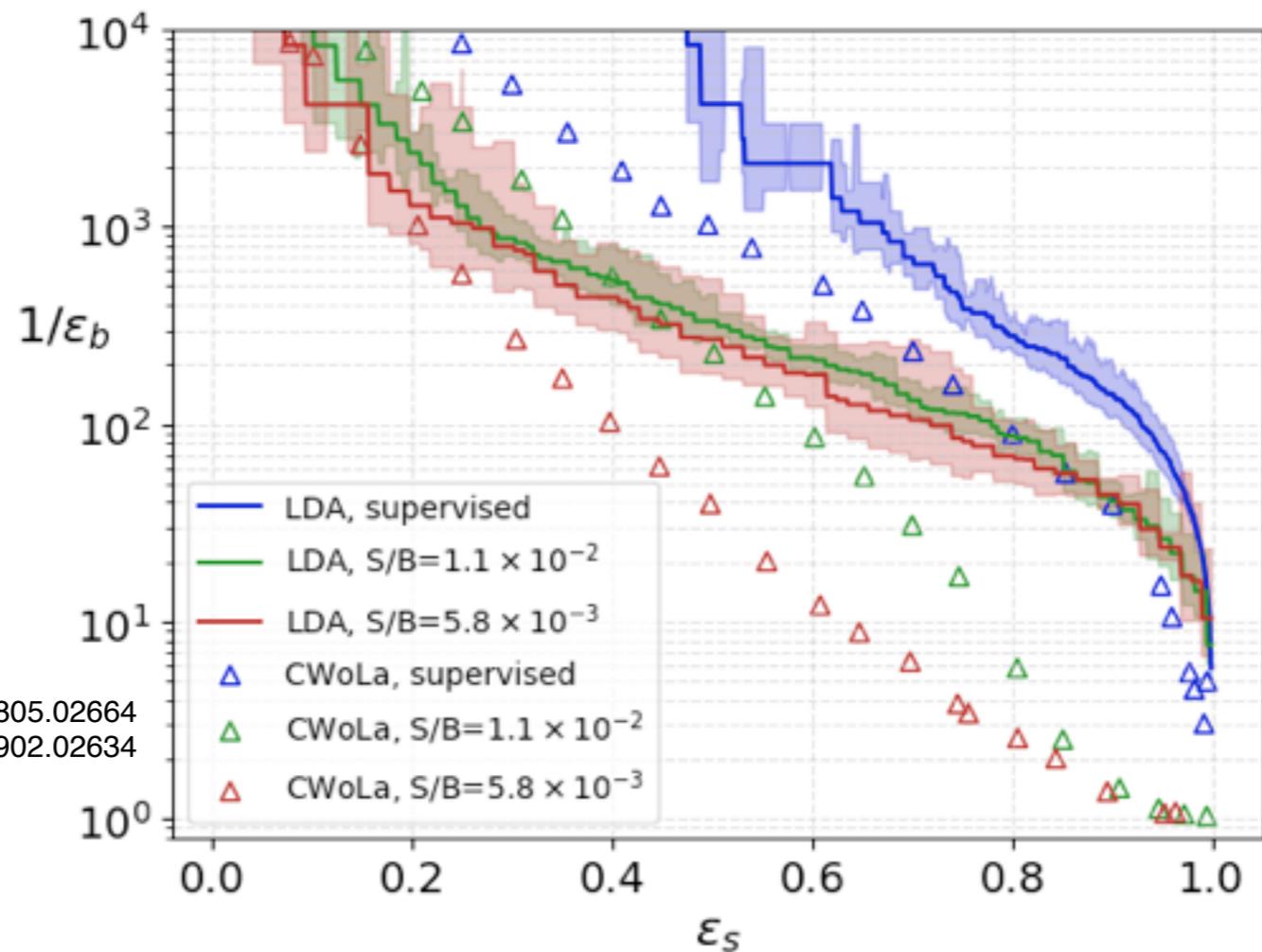
Metodiev, Nachman & Thaler, 1708.02949

Can be used directly on latent theme distributions!  
(alternatively use inference on  $\omega$ )

# Jet classification with LDA

NP example:  $pp \rightarrow W' \rightarrow W \phi \rightarrow W Z b \bar{b}$

$$m_{W'} = 3 \text{ TeV}, m_{\phi} = 400 \text{ GeV} \quad m_{jj} \in 2730 - 3190 \text{ GeV}$$



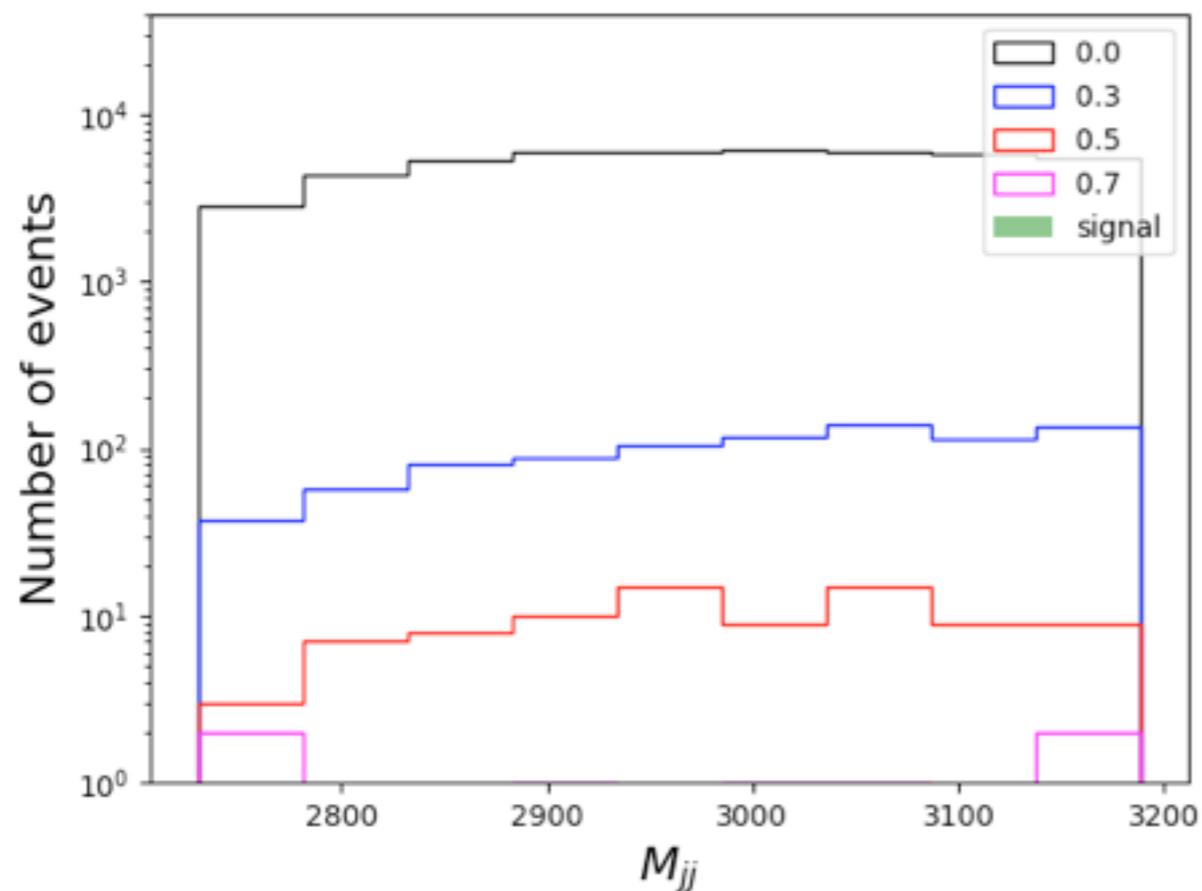
Collins, Howe & Nachman, 1805.02664  
1902.02634

errors estimated using k-folding, with k=10

# Bump hunting with LDA

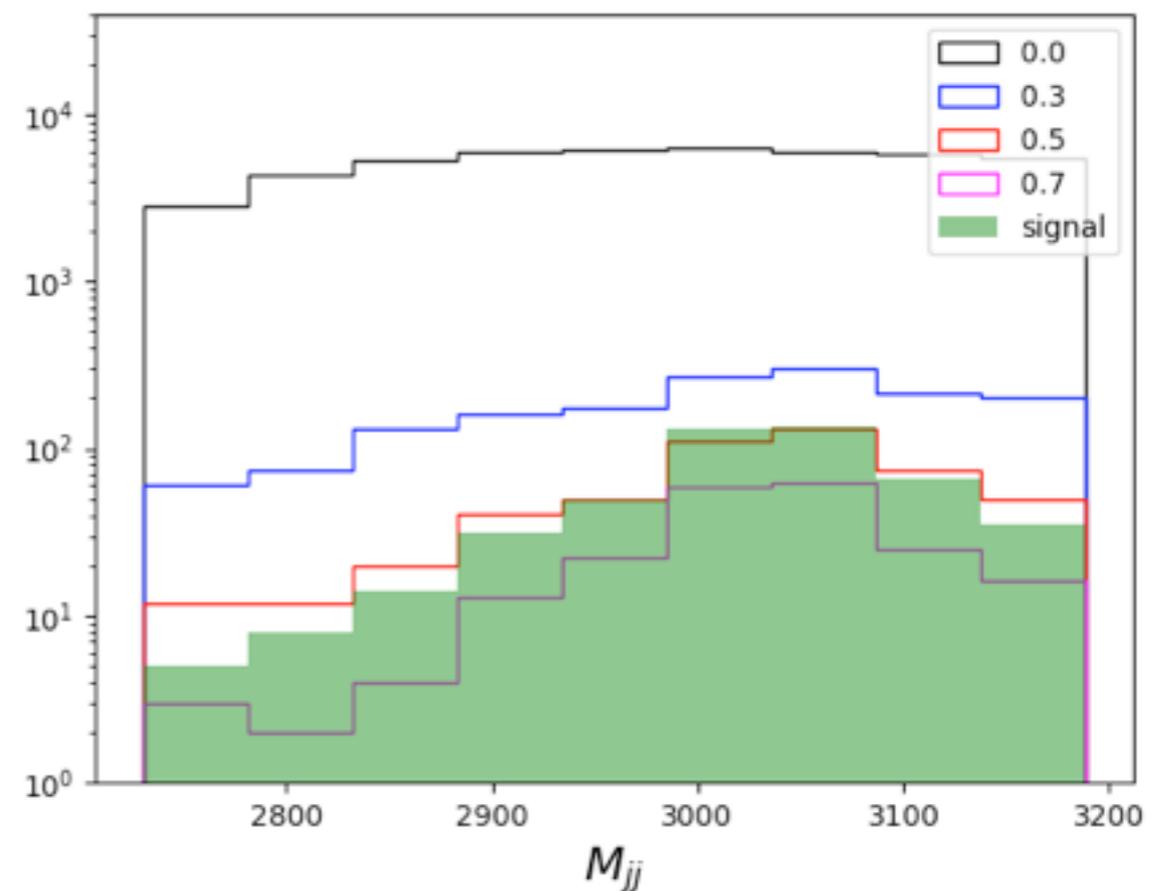
NP example:  $pp \rightarrow W' \rightarrow W \phi \rightarrow W Z b \bar{b}$

$$m_{W'} = 3 \text{ TeV}, m_{\phi} = 400 \text{ GeV} \quad m_{jj} \in 2730 - 3190 \text{ GeV}$$



LDA with no signal

vs



LDA with signal

# Conclusions

---

Latent Dirichlet Allocation addresses several interesting problems in NP (*QCD*) vs NP ( *$\mu\nu$* ) classification:

- ✓ train on mixed, unlabelled, imbalanced samples
- ✓ sensitivity to small S/B ( $\sim 1\%$ )
- ✓ extract descriptions of signal and background
- ✓ interpret 'what the machine has learned'
- ✓ no control/side-band regions

So far, this is proof-of-concept.

Next steps:

- \* explore classifiers with more than two themes
- \* hierarchical theme models: extract optimal #themes from data
- \* can observables' space be optimised with deep learning?
- \* more applications: category based searches, pile-up mitigation, ...

Spares

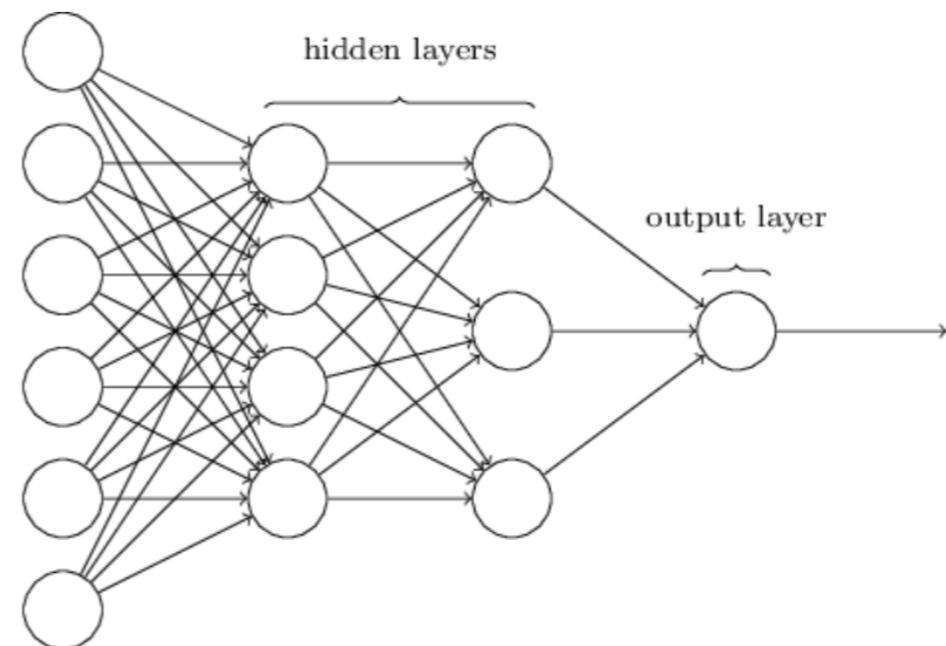
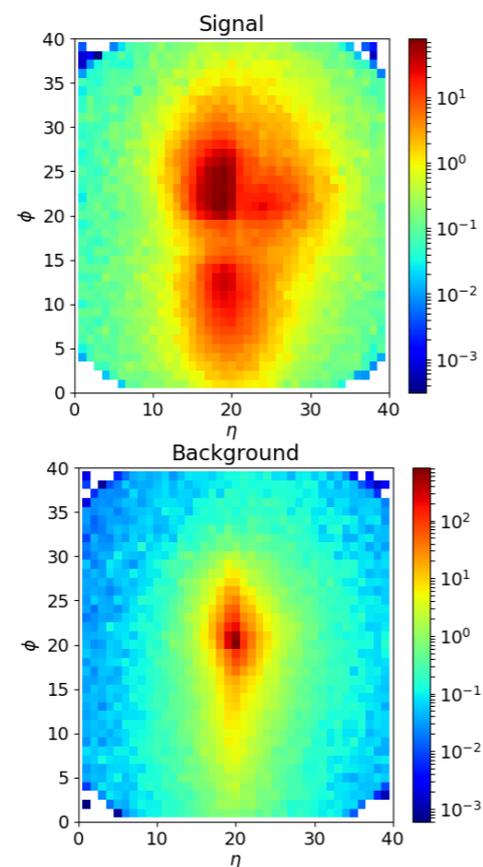


# Jet tagging

Recent ML revolution:

see 1902.09914 for recent review

- train NNs on (low level) jet info (jet images, particle four vectors) using (MC generated) pure S & B samples



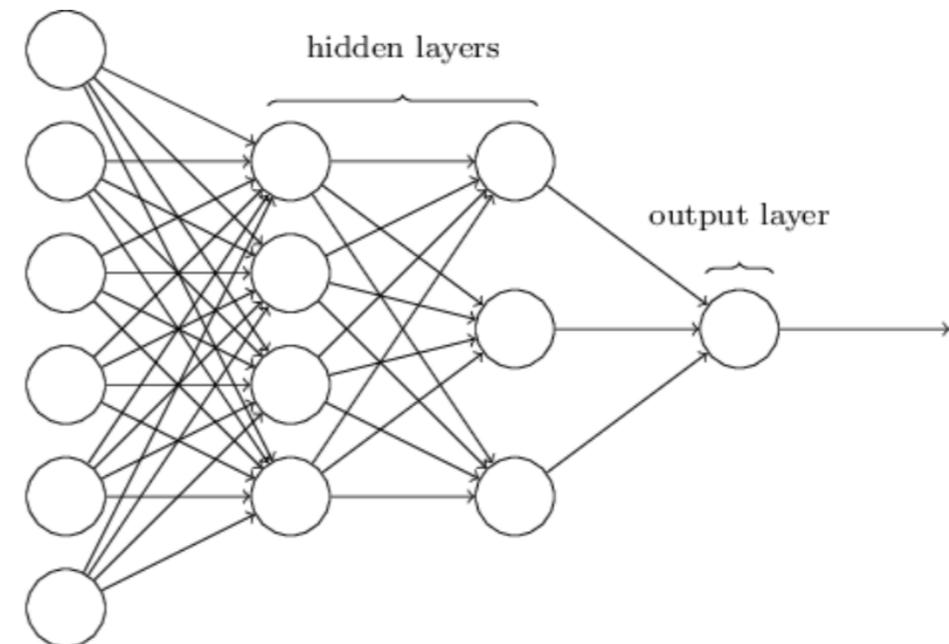
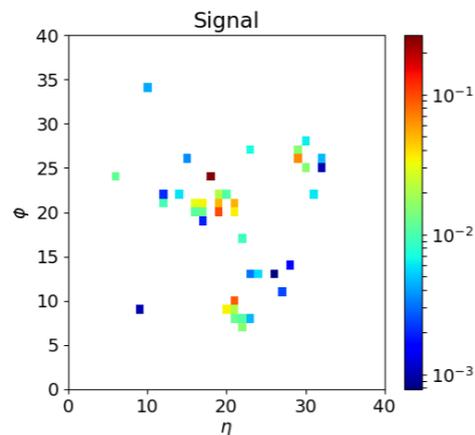
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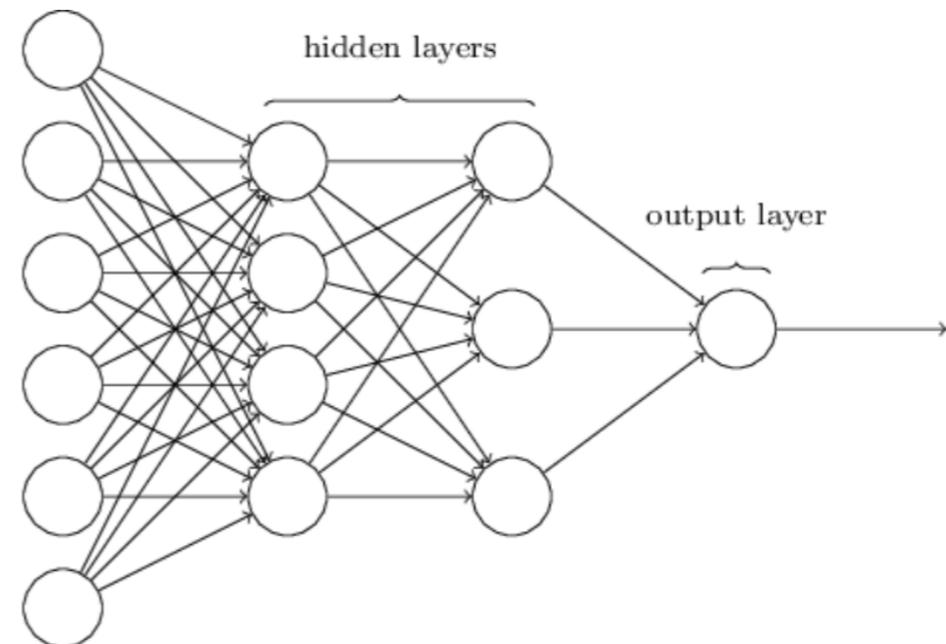
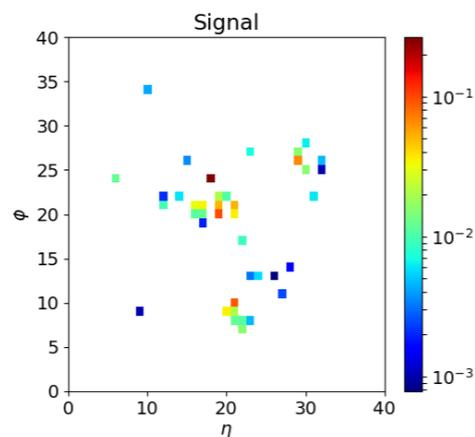


# Jet tagging

Recent ML revolution:

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Key challenge: knowing what the machine has learned (genuine SD physics or MC implementation particularities)

# What exactly is the Dirichlet Distribution

---

Multivariate equivalent of Beta distribution  
(e.g. dice factory vs. coin factory)

$$p(\theta|\alpha) = \frac{\Gamma(\sum_{i=1}^k \alpha_i)}{\prod_{i=1}^k \Gamma(\alpha_i)} \prod_{i=1}^k \theta_i^{\alpha_i - 1}$$

$\alpha_i$  determines prior - mean shape and sparsity

Dirichlet is defined over (k-1) simplex (k non-negative arguments which sum to one)

Dirichlet is conjugate prior to multinomial distribution -  
posterior is also Dirichlet

In jet LDA, themes are V-dimensional Dirichlet; theme proportions are K-dimensional Dirichlet

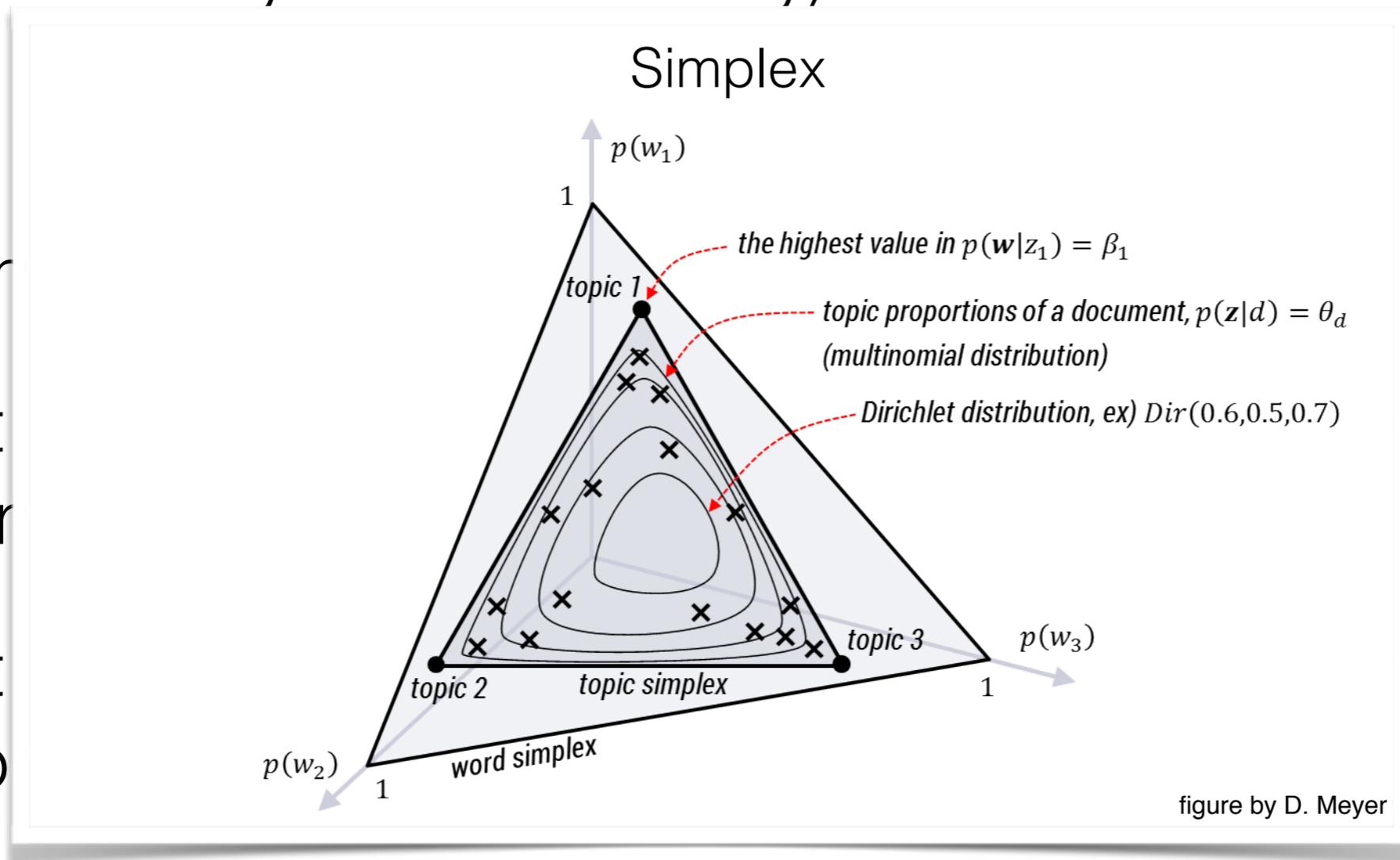
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$\alpha_i$  deter

Dirichlet  
argumer

Dirichlet  
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