

Warsaw University  
of Technology

**Geometry and Dynamics in  
Heavy-ion Collisions Seen  
by the Femtoscopy  
in the STAR Experiment**

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# Outline

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## I) Introduction

- RHIC, STAR
- Femtoscopy

## II) Geometry aspects

- Centrality dependence
- Energy dependence
- System dependence

## III) Dynamics aspects

- Centrality dependence
- Energy dependence
- System dependence

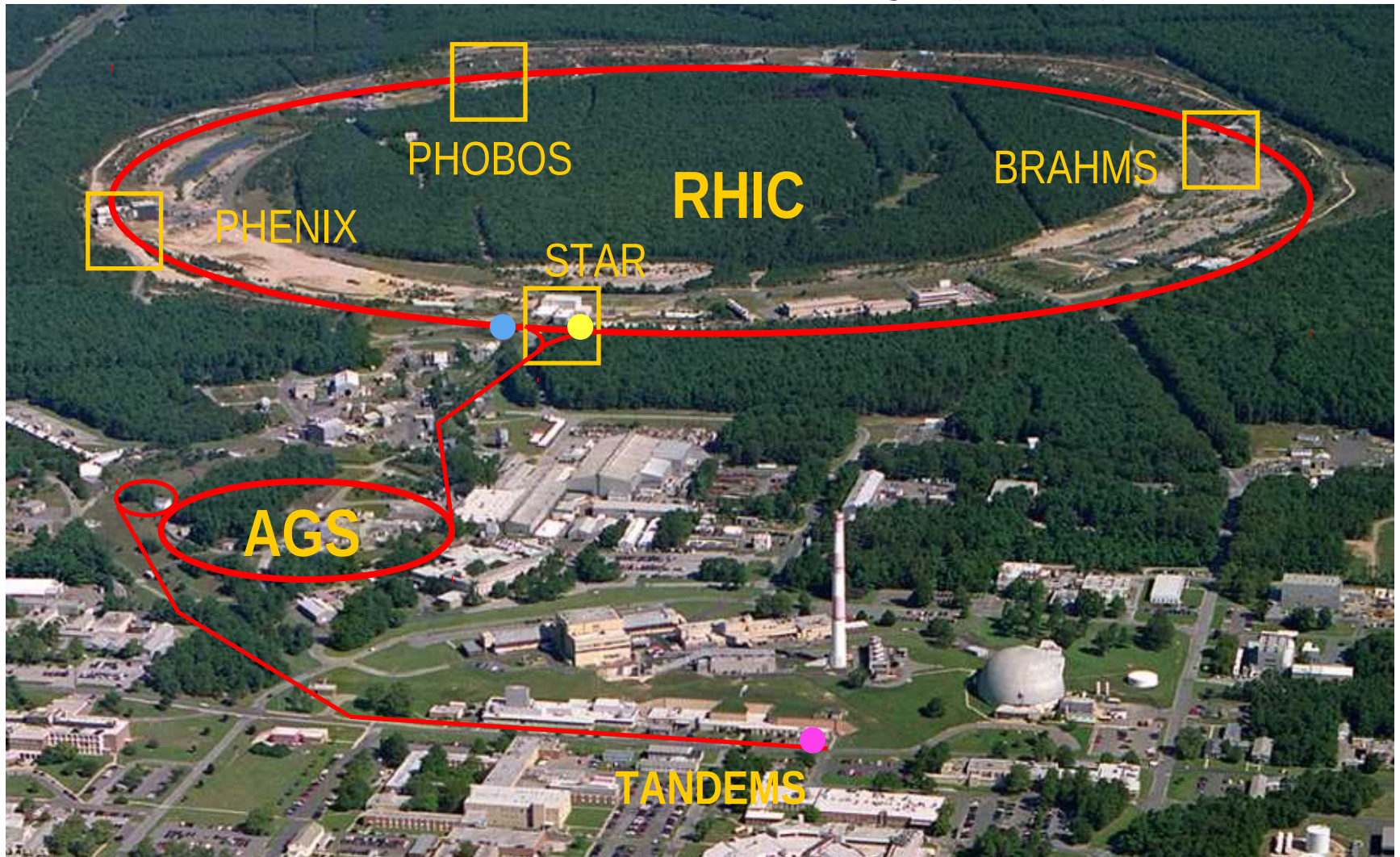
## IV) Conclusions and summary





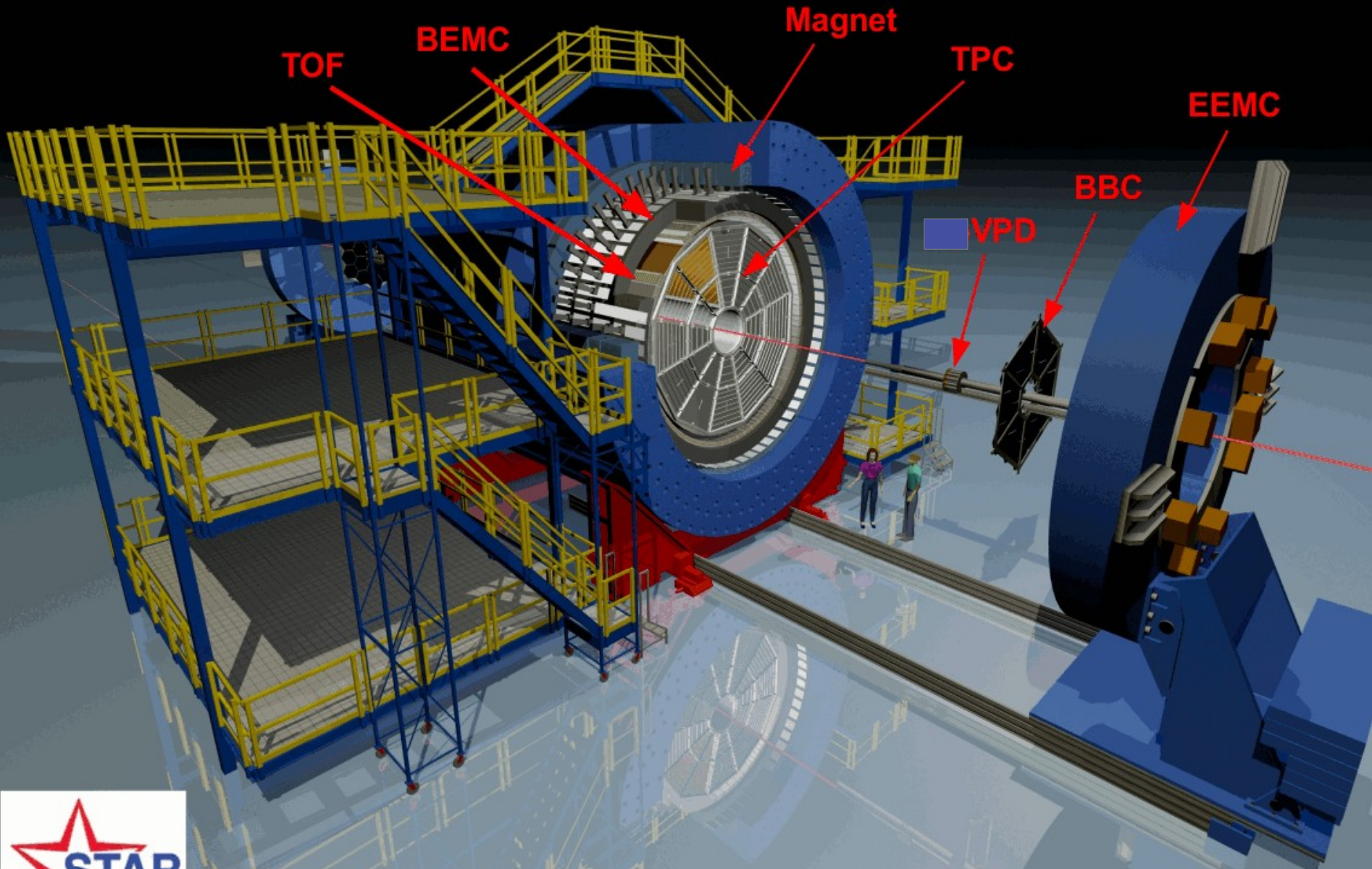
# Introduction

# Relativistic Heavy Ion Collider (RHIC) Brookhaven National Laboratory (BNL)

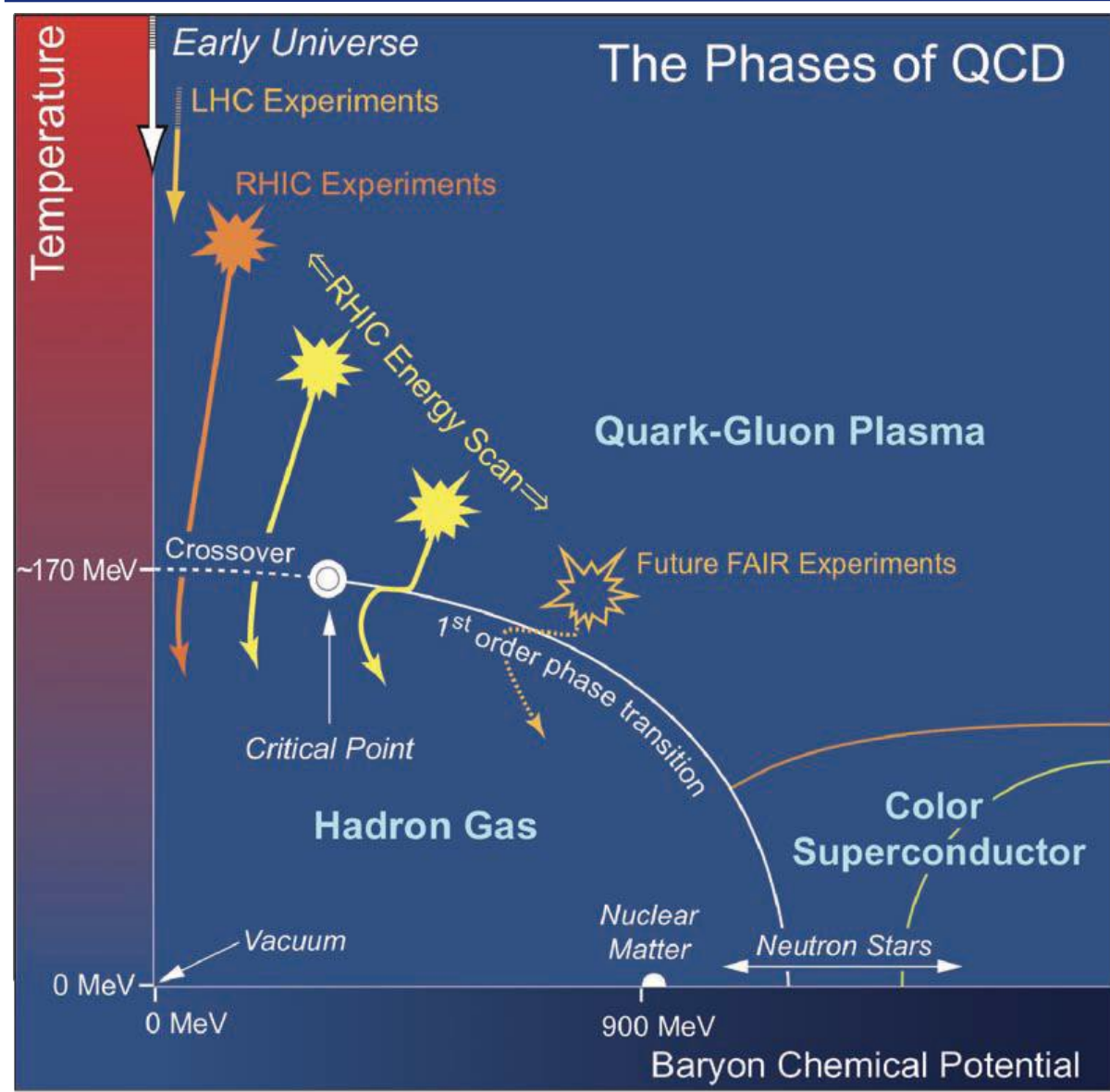


- 2 concentric rings of 1740 superconducting magnets
- 3.8 km circumference

# The Solenoidal Tracker At RHIC



# Introduction



**RHIC Top Energy**  
p+p, p+Al, p+Au, d+Au,  
<sup>3</sup>He+Au, Cu+Cu, Cu+Au,  
Ru+Ru, Zr+Zr, Au+Au, U+U  
QCD at high energy  
density/temperature  
Properties of QGP, EoS

**Beam Energy Scan**  
Au+Au 7.7-62 GeV  
QCD phase transition  
Search for critical point  
Turn-off of the QGP  
signatures

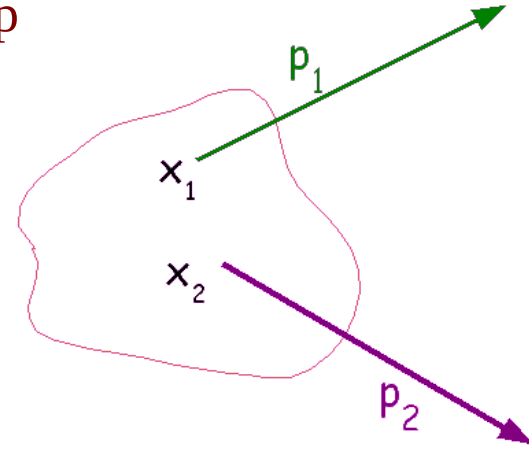
**Fixed-Target Program**  
Au+Au = 3.0-7.7 GeV  
High baryon density regime  
with 420-720 MeV

# Few Words About Femtoscopy

## Single- and two- particle distributions

$$P_1(p) = E \frac{dN}{d^3 p} = \int d^4 x S(x, p)$$

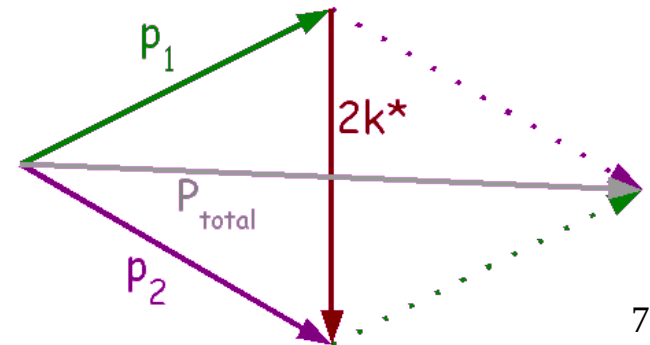
**S(x,p)** – emission function: the distribution of source density probability of finding particle with x and p



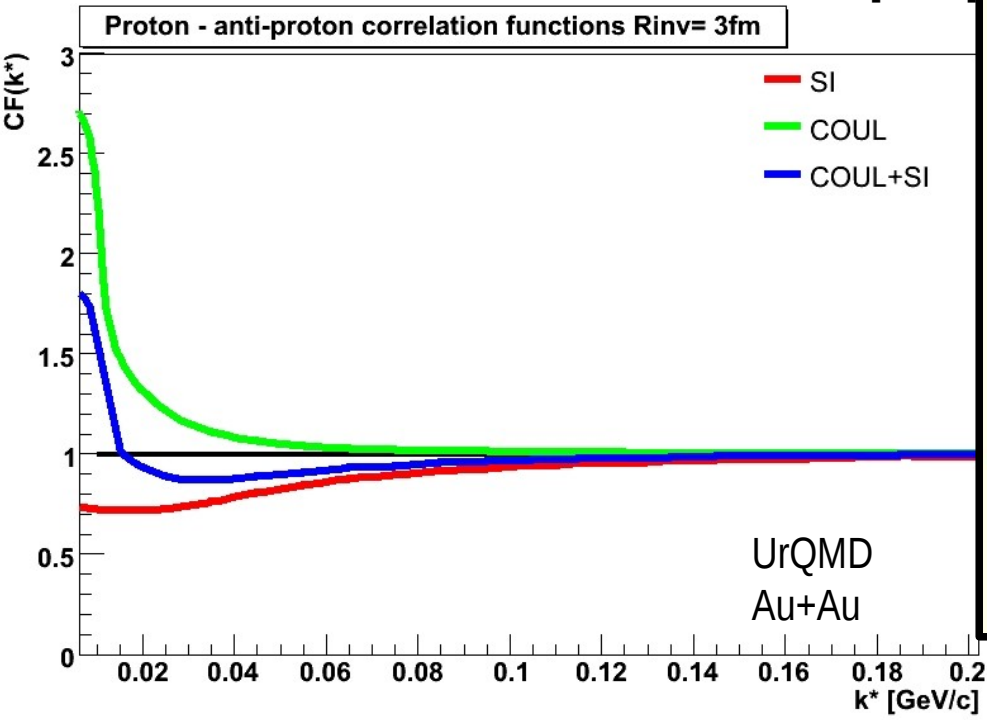
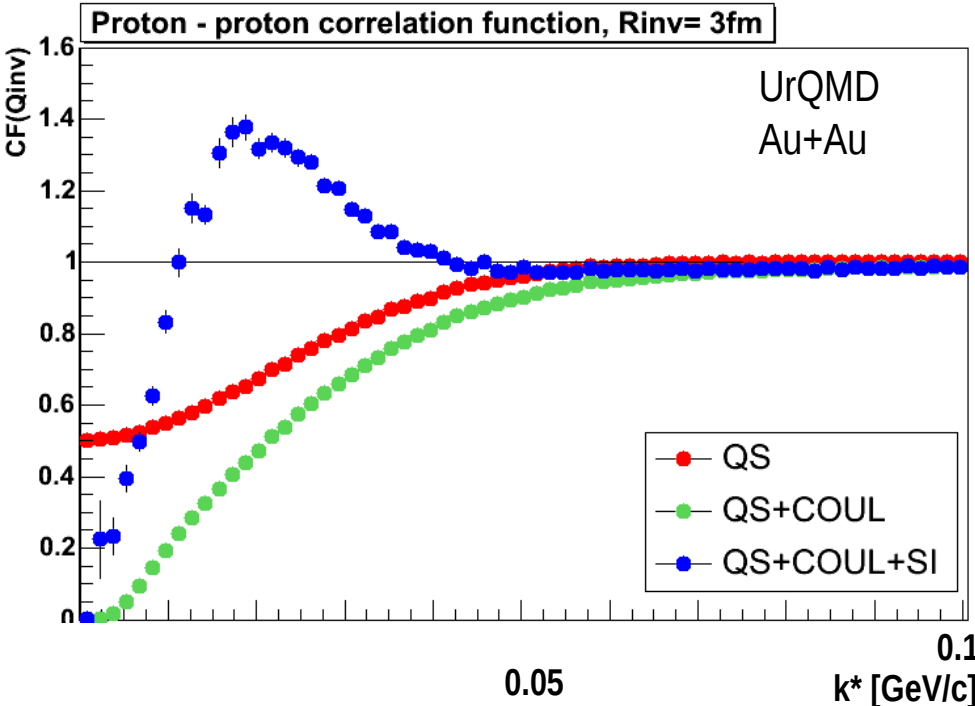
$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3 p_1 d^3 p_2} = \int d^4 x_1 S(x_1, p_1) d^4 x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$

## The correlation function

$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1) P_1(p_2)}$$



# Sources of Correlations



## Identical baryon- baryon

- Quantum Statistics- QS

- Final State Interactions- FSI

- Coulomb

- Strong

## Non-identical baryon- (anti)baryon

- Final State Interactions- FSI

- Coulomb

- Strong

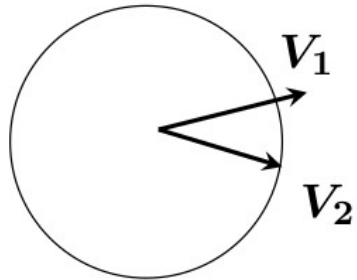


# Non-identical Particle Combinations

**Catching up**  
longer interaction,  
strong correlation

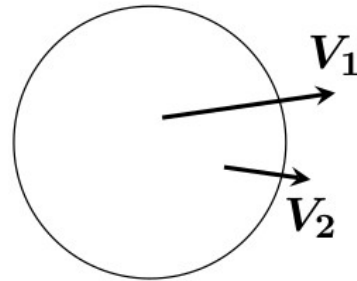
**Running away**  
shorter interaction,  
weak correlation

$$t_1 \neq t_2$$
$$\Delta r = 0$$

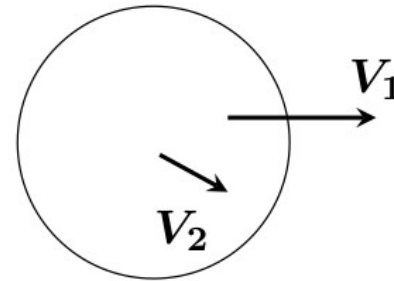


First particle (lighter) faster:

$$t_1 = t_2$$
$$\Delta r \neq 0$$



$$t_1 = t_2$$
$$\Delta r \neq 0$$



$t_1 > t_2$  - Catching up  
 $t_2 > t_1$  - Run away

Catching up

Run away

R. Lednicky, et al.,  
Phys. Rev. Lett. B373, 30-34  
(1996)

# Spherical Harmonics

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$$C(\mathbf{q}) = \sum_{l,m} C_l^m(q) Y_l^m(\theta, \phi)$$

$$C_l^m(q) = \int_{\Omega} C(q, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

$\Omega$  – full solid angle

$Y_l^m(\theta, \phi)$  – spherical harmonic function

$q = |\mathbf{q}|, \theta, \phi$  – spherical coordinates

$C_0^0$  -> sensitive to the size of the emitting source

$C_1^1$  -> sensitive to the emission asymmetry

P. Danielewicz and S.Pratt.  
Phys. Lett. B618: 60 2005

P. Danielewicz and S.Pratt.  
Phys. Rev. C75:034907 2007



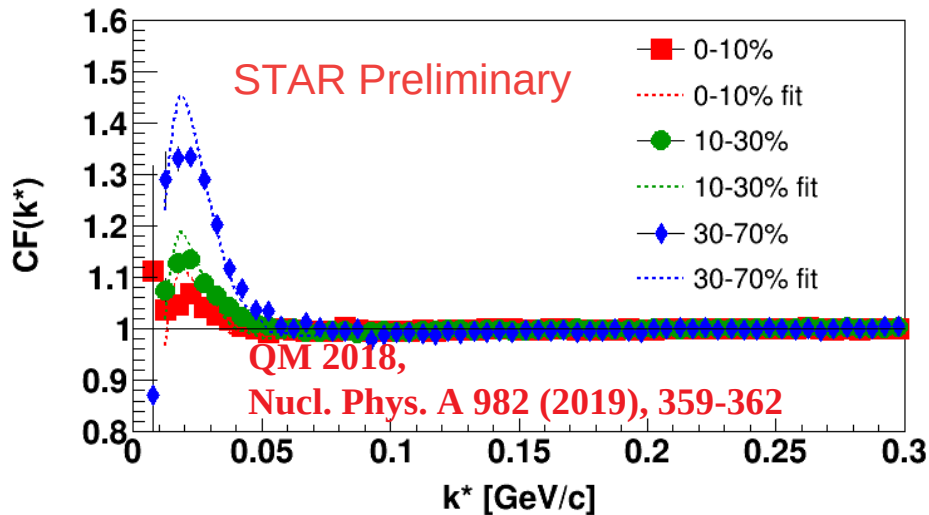
# Results



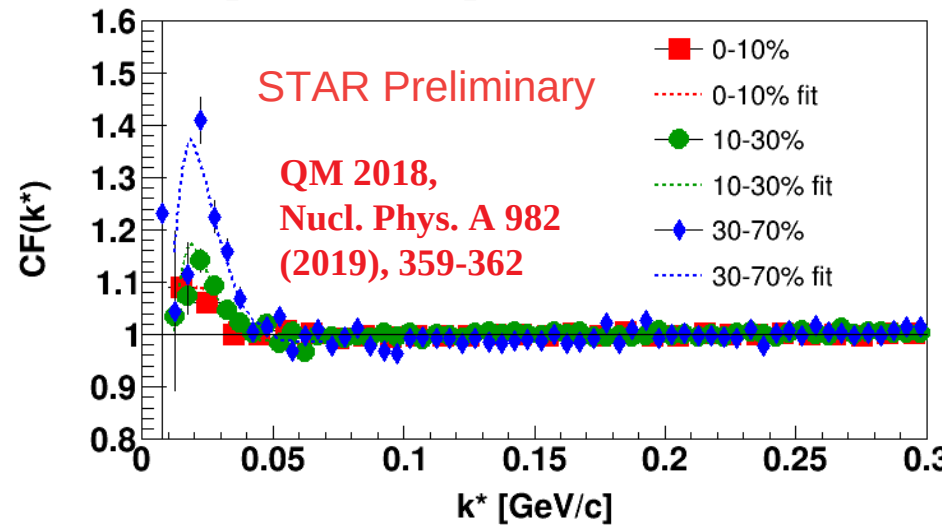
# Geometry

# Centrality Dependence in Proton Femtoscopy

proton-proton @39 GeV



antiproton-antiproton @39 GeV



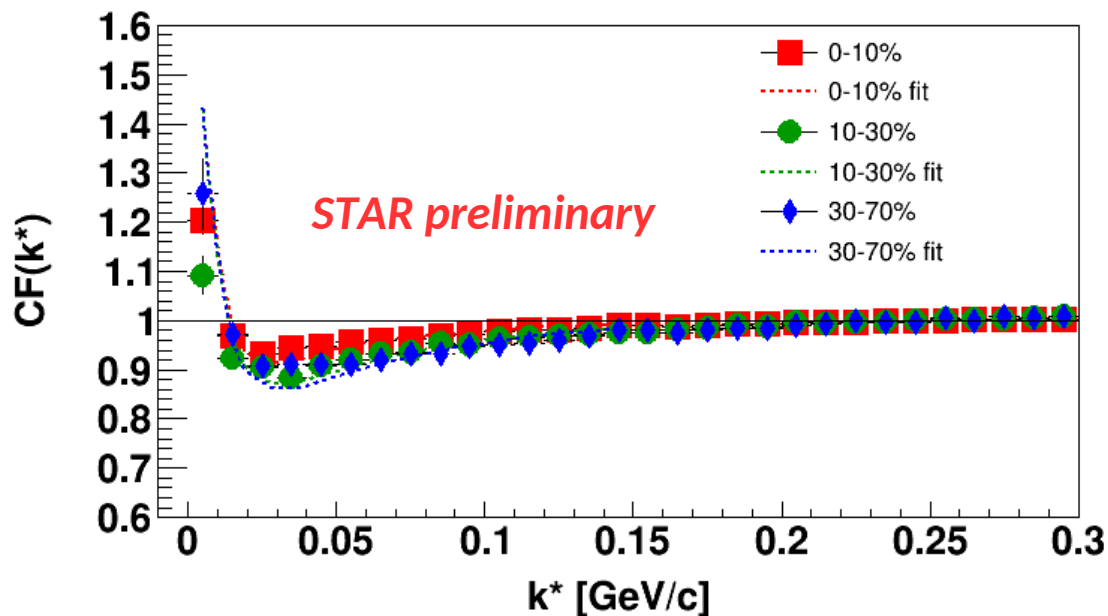
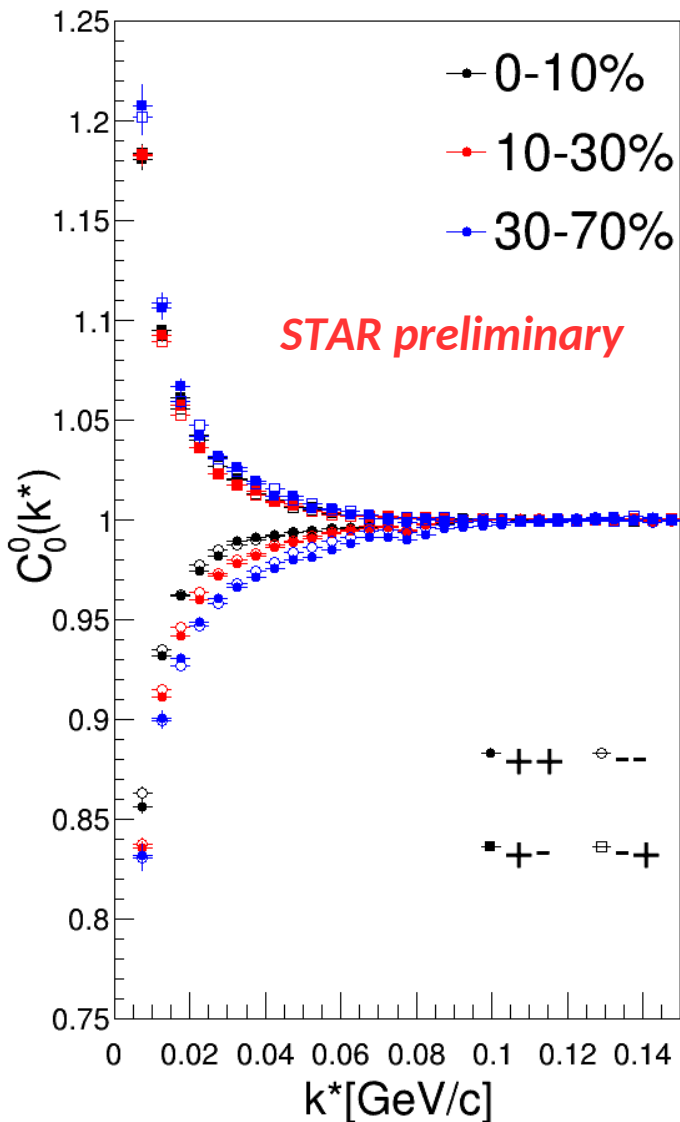
centrality	$R_{inv} p - p$ [fm]	$R_{inv} \bar{p} - \bar{p}$ [fm]	$R_{inv} p - \bar{p}$ [fm]
0-10%	$4.00 \pm 0.15 \pm 0.02$	$3.83 \pm 0.20 \pm 0.03$	$3.39 \pm 0.12 \pm 0.14$
10-30%	$3.61 \pm 0.13 \pm 0.17$	$3.68 \pm 0.15 \pm 0.11$	$2.69 \pm 0.10 \pm 0.12$
30-70%	$2.72 \pm 0.07 \pm 0.07$	$2.95 \pm 0.11 \pm 0.08$	$2.56 \pm 0.09 \pm 0.12$

No significant difference between proton-proton and antiproton-antiproton correlation functions

$R_{inv}$  – 1D radius in LCMS system

# Centrality Dependence in Nonidentical Particles @39 GeV

Proton-Antiproton CFs @ Au+Au 39GeV



Clear centrality dependence

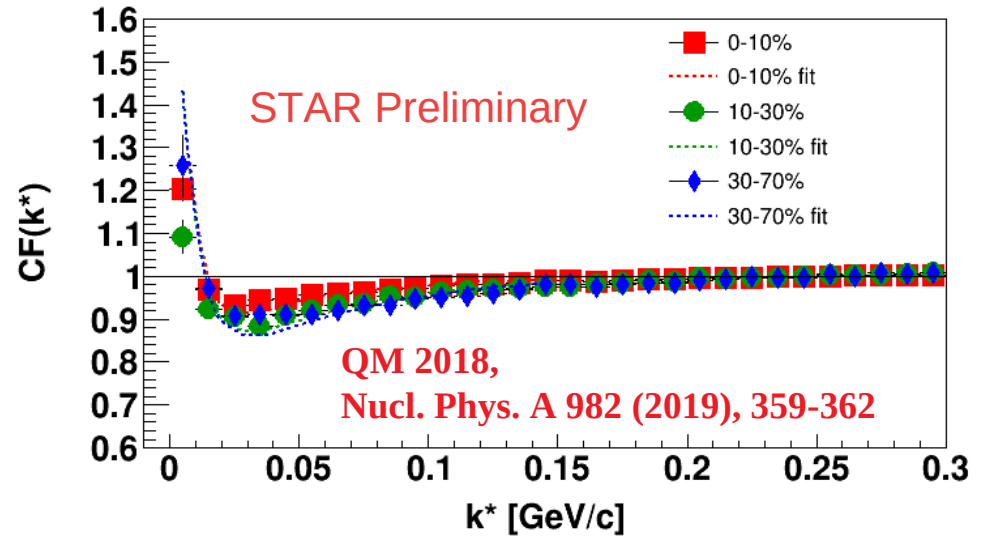
$$R(0 - 10\%) > R(10 - 30\%) > R(30 - 70\%)$$

QM 2018,  
Nucl. Phys. A 982 (2019), 359-362

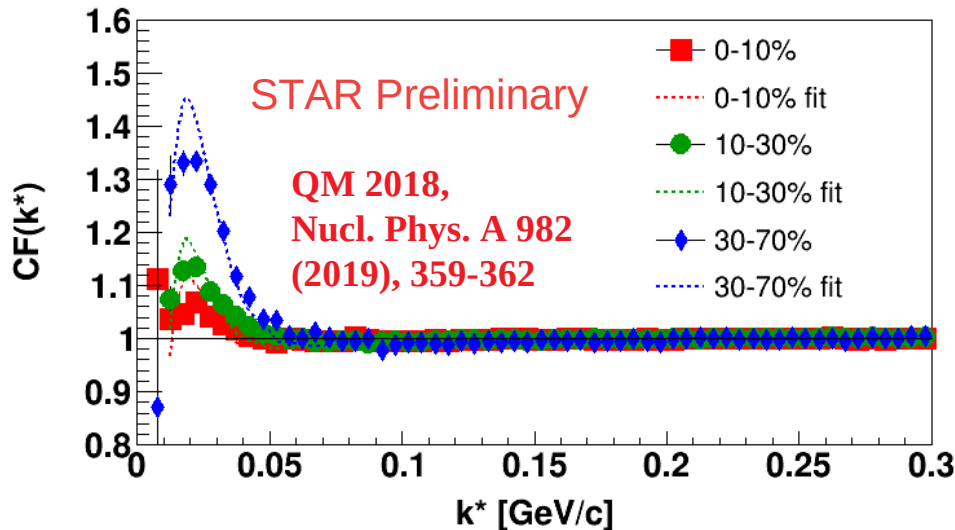
No significant difference  
between proton-proton  
and antiproton-antiproton  
correlation functions

# System Dependence in Proton Femtoscopy @39 GeV

Radii from proton-proton and antiproton-antiproton systems differ from those from proton-antiproton system  $\rightarrow$  Residual Correlations.  
Residual feed-down correction needs to be applied.

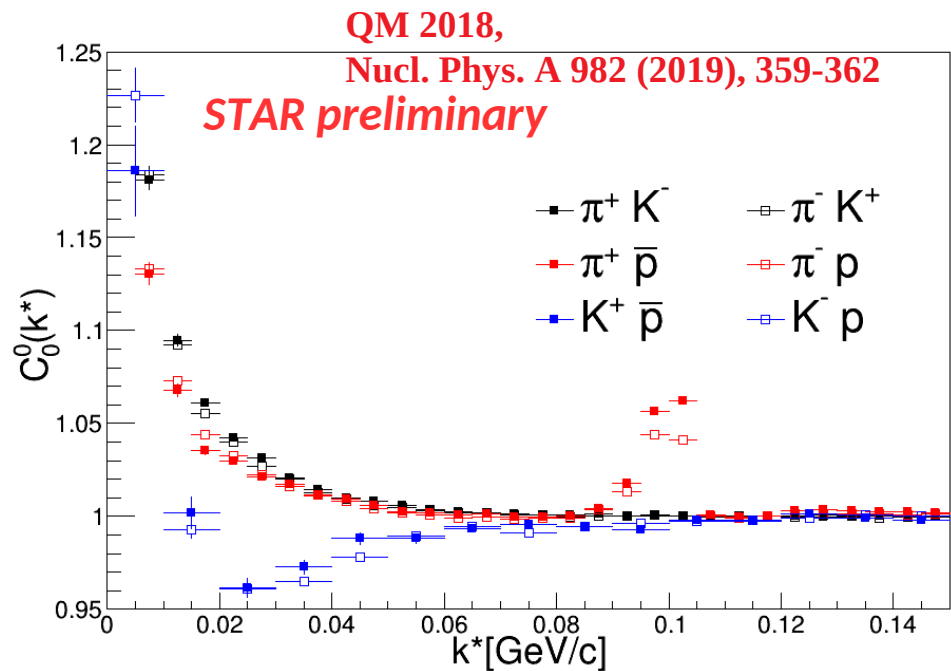
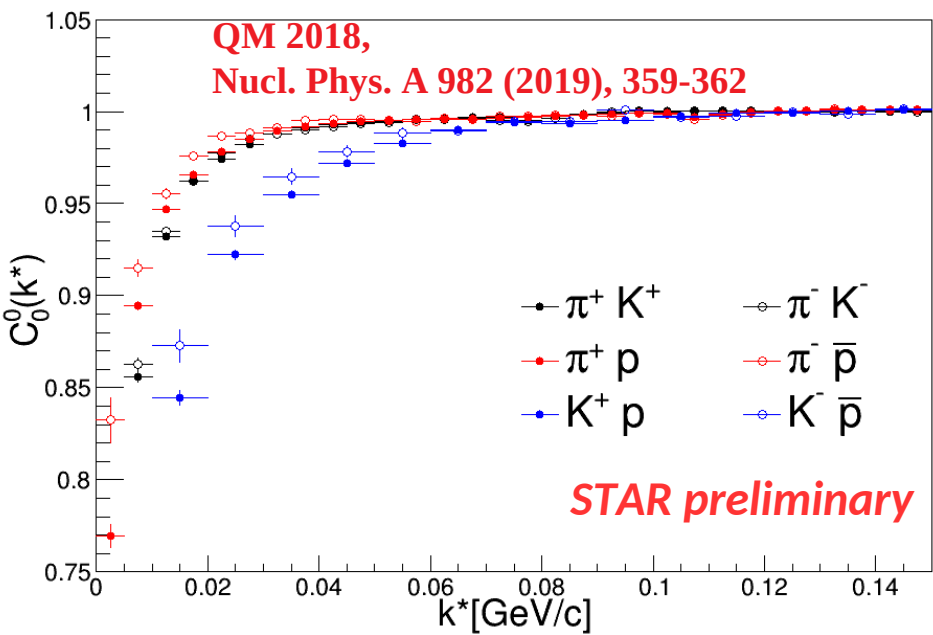


proton-proton @39 GeV



proton-antiproton @39 GeV

# System Dependence in Nonidentical Particles @39 GeV



Clear system dependence

Different shape due to strong interaction

Same sign: correlations dominated by Coulomb interaction

Opposite sign: interaction more complicated

Coulomb strength depends on Bohr radius of the pair

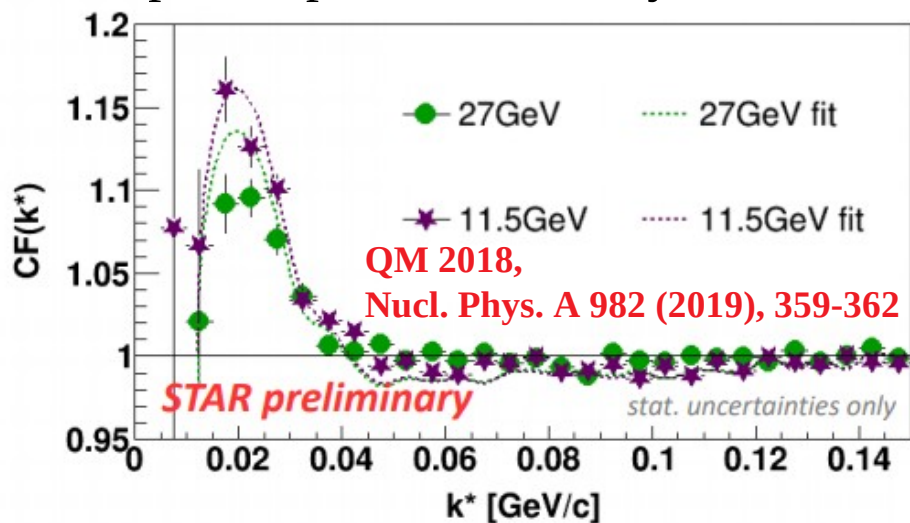
Strong interaction not negligible in  $K - p$ .

$K - p$  – lowest Bohr radius, strongest correlation

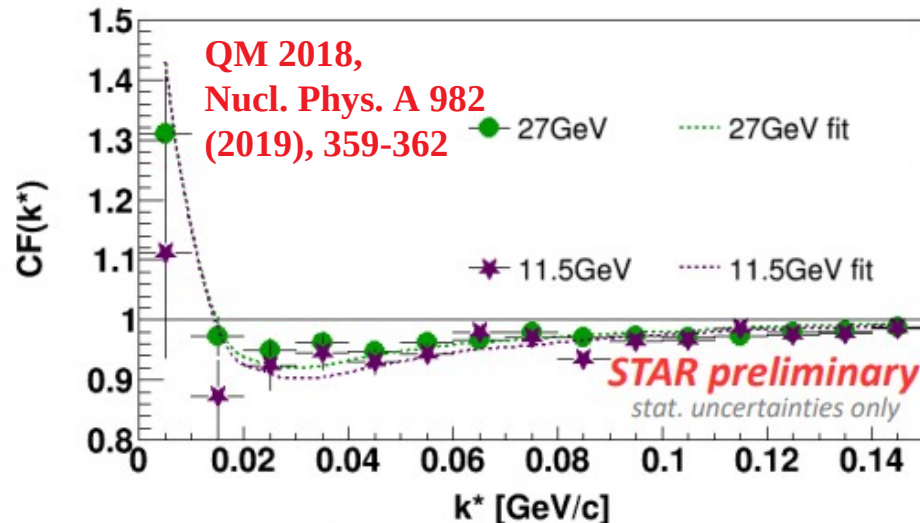


# Energy Dependence in Proton Femtoscopy

proton-proton, centrality 0-10%



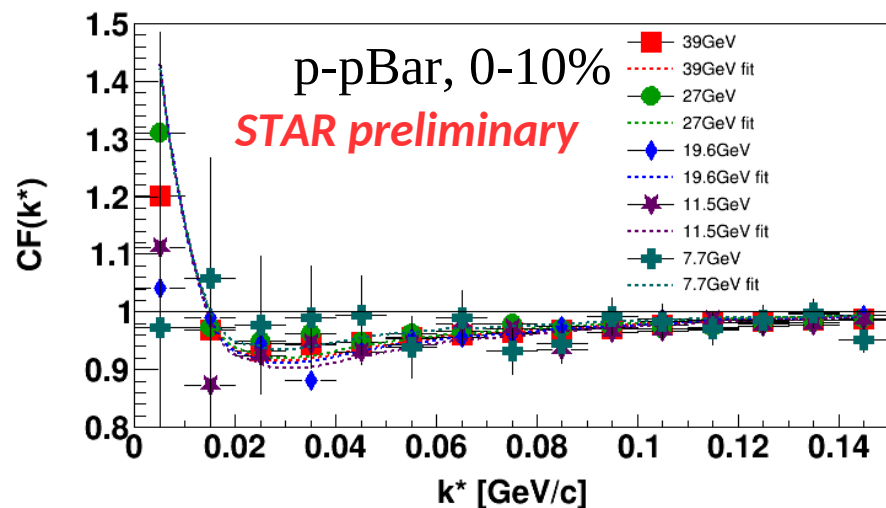
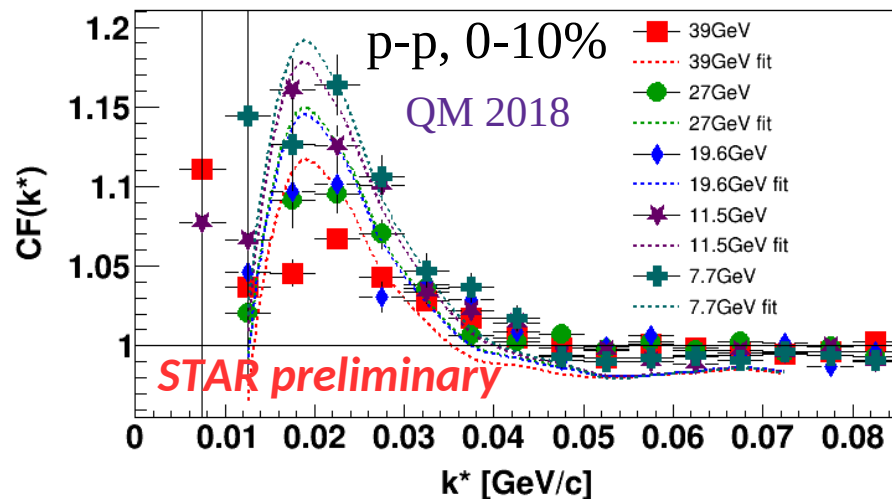
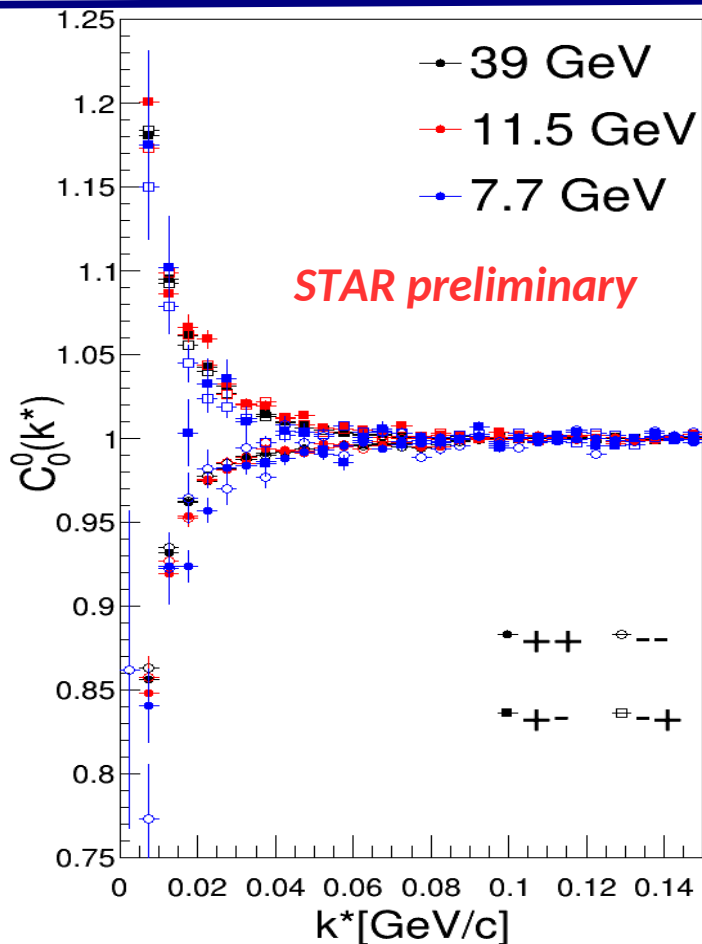
proton-antiproton, centrality 0-10%



energy	$R_{inv} p - p$ [fm]	$R_{inv} p - \bar{p}$ [fm]
7.7 GeV	$3.59 \pm 0.16 \pm 0.19$	
11.5 GeV	$3.66 \pm 0.08 \pm 0.05$	$3.30 \pm 0.42 \pm 0.28$
19.6 GeV	$3.82 \pm 0.15 \pm 0.06$	$3.32 \pm 0.25 \pm 0.13$
27 GeV	$3.80 \pm 0.12 \pm 0.08$	$3.49 \pm 0.25 \pm 0.16$
39 GeV	$4.00 \pm 0.15 \pm 0.02$	$3.39 \pm 0.12 \pm 0.14$

Energy dependence more significant for proton-proton than for proton-antiproton system.

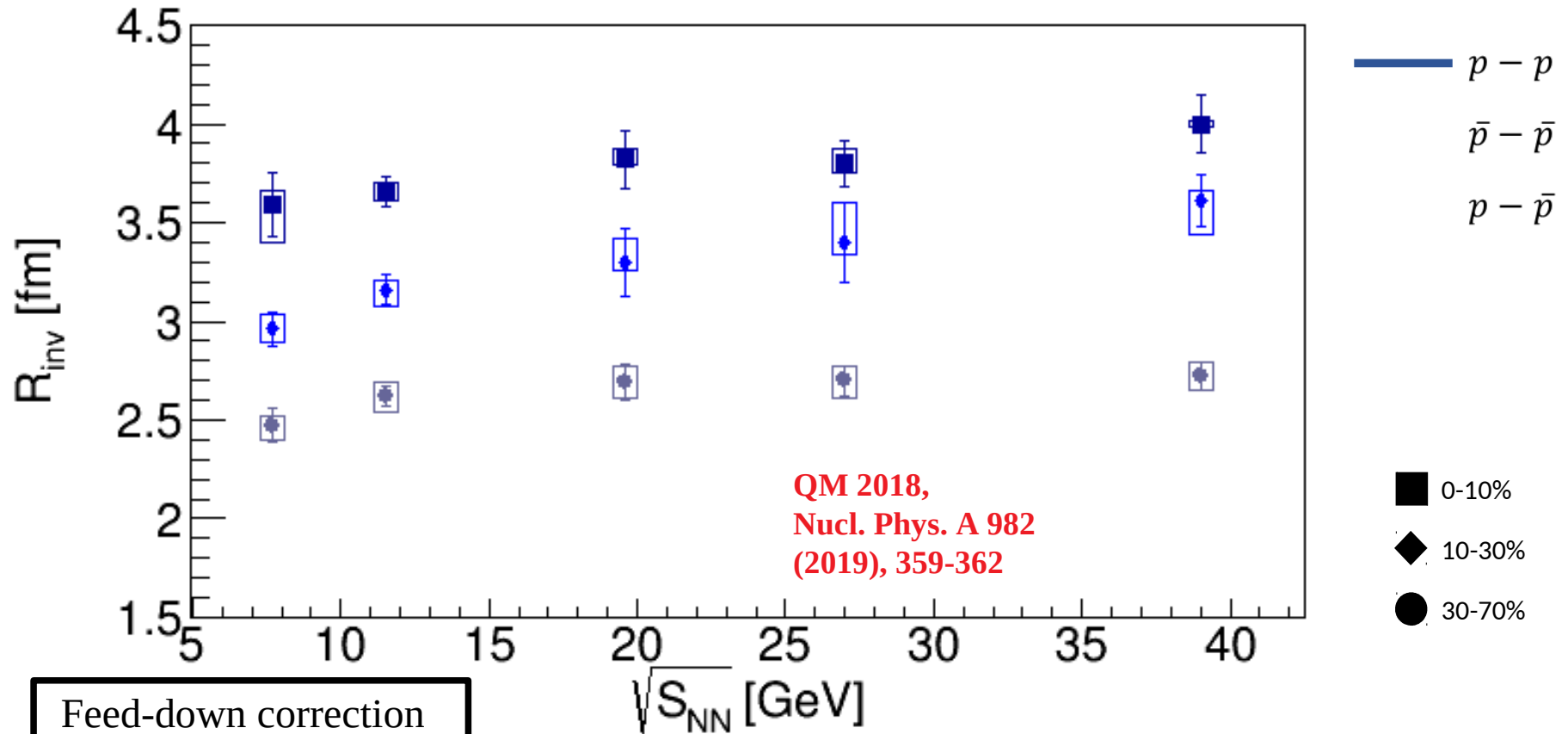
# Energy Dependence in Various Systems



Energy dependence more significant for proton-proton than for proton-antiproton and pion-kaon systems.

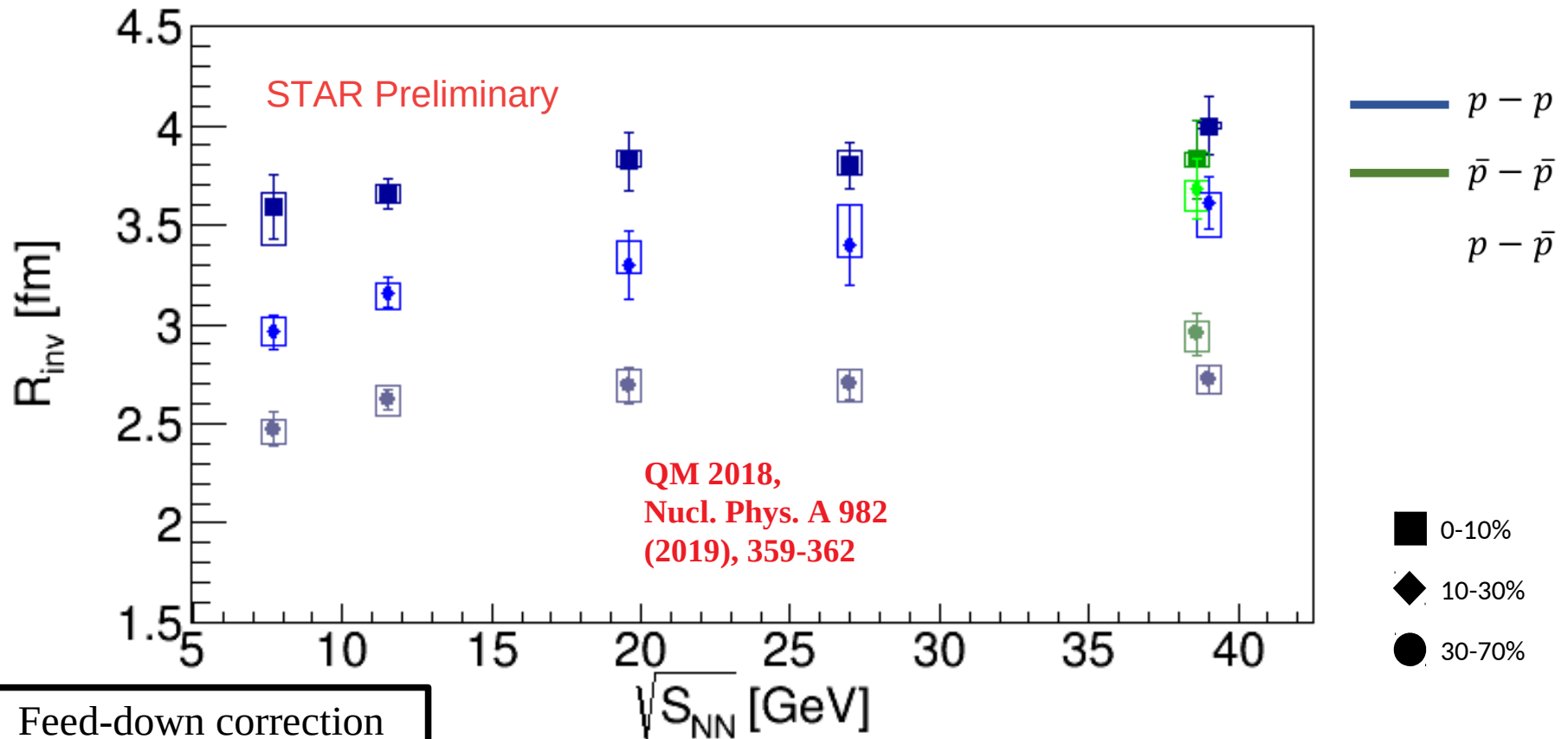
QM 2018,  
 Nucl. Phys. A 982 (2019), 359-362

# Proton Femtoscropy in BES



Feed-down correction  
may decrease  
significance of the  
centrality dependence.

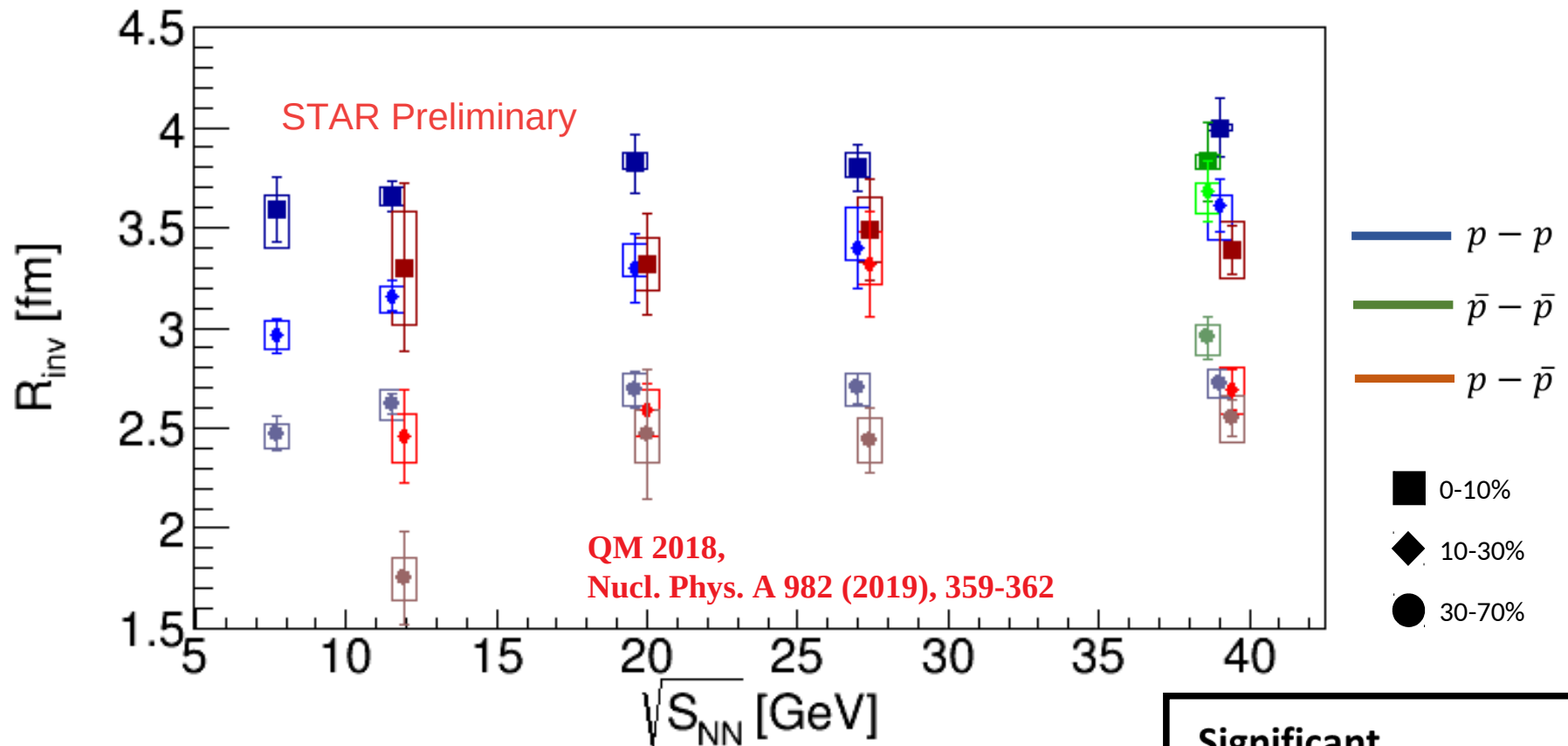
# Proton Femtoscropy in BES



Feed-down correction  
may decrease  
significance of  
centrality dependence.

**No significant difference between  
 $p - p$  and  $\bar{p} - \bar{p}$  correlation  
functions at  $\sqrt{S_{NN}} = 39$  GeV**

# Proton Femtoscscopy in BES



Feed-down correction may decrease significance of centrality dependence.

**No significant difference between  $p - p$  and  $\bar{p} - \bar{p}$  correlation functions at  $\sqrt{s_{NN}} = 39$  GeV**

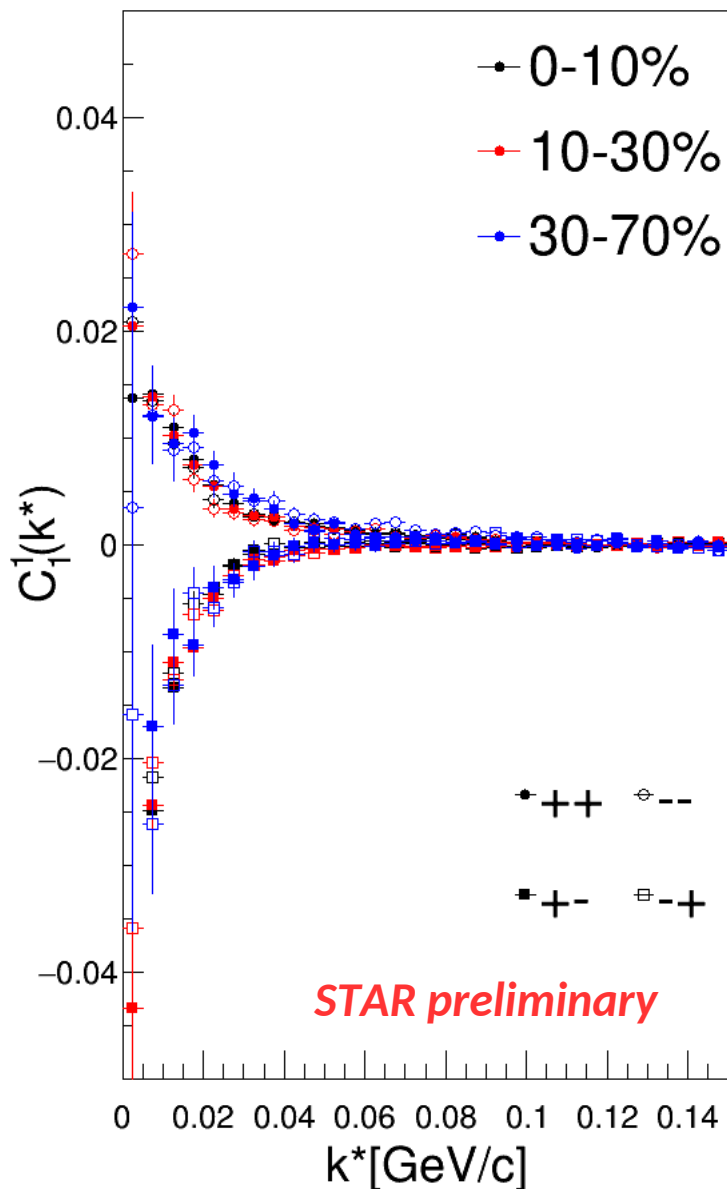
**Significant centrality dependence.**

**$\sqrt{s_{NN}}$  dependence weak for all centralities.**



# Dynamics

# Centrality and Energy Dependencies in $\pi$ - $K$ systems

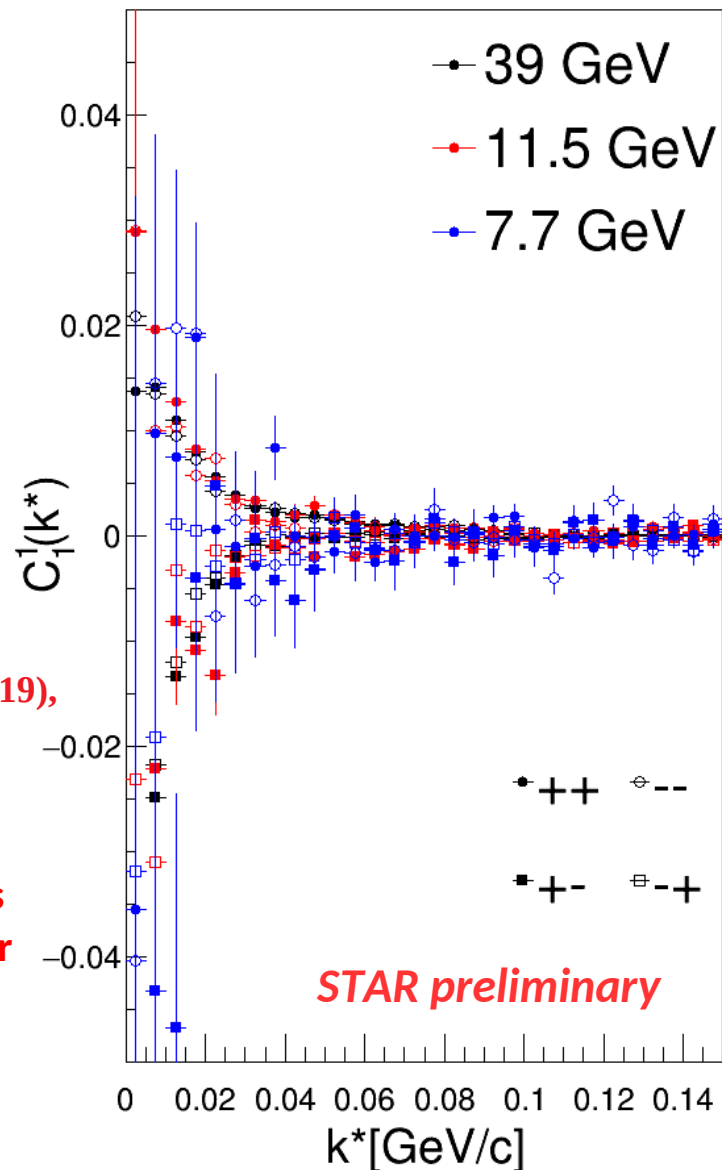


Clear signal of emission asymmetry

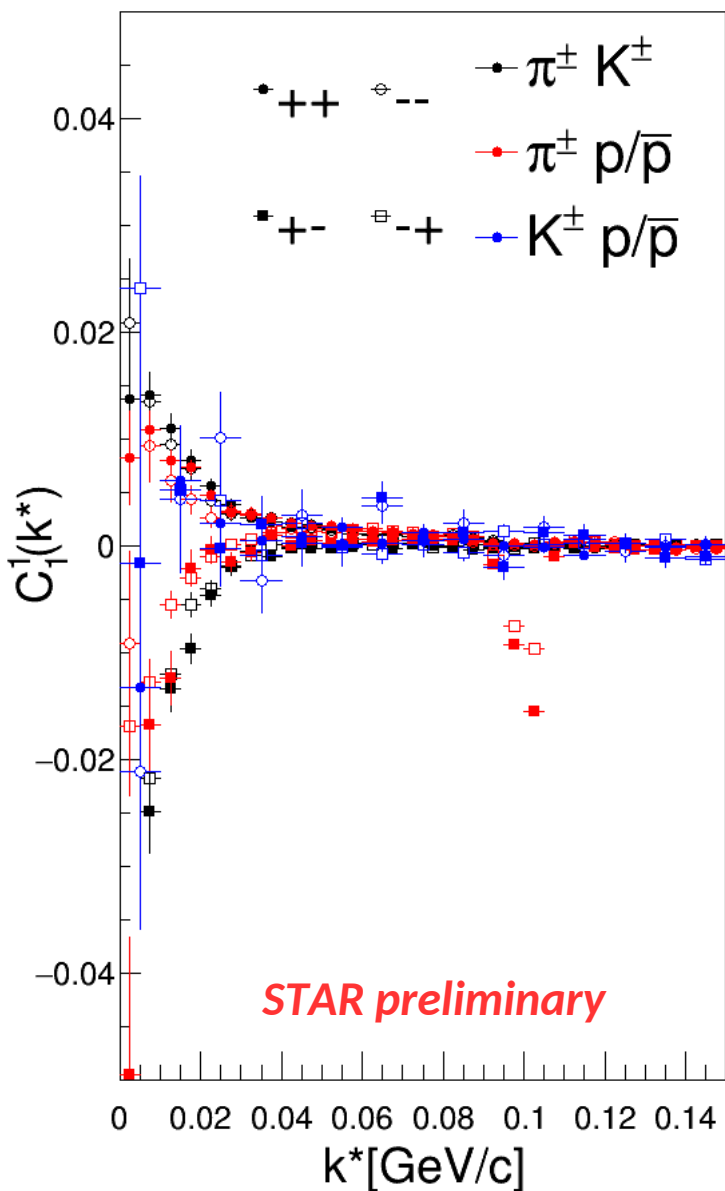
Pions emitted closer to center and/or later than Kaons

QM 2018,  
Nucl. Phys. A 982 (2019),  
359-362

Asymmetry does not disappear for low energies.



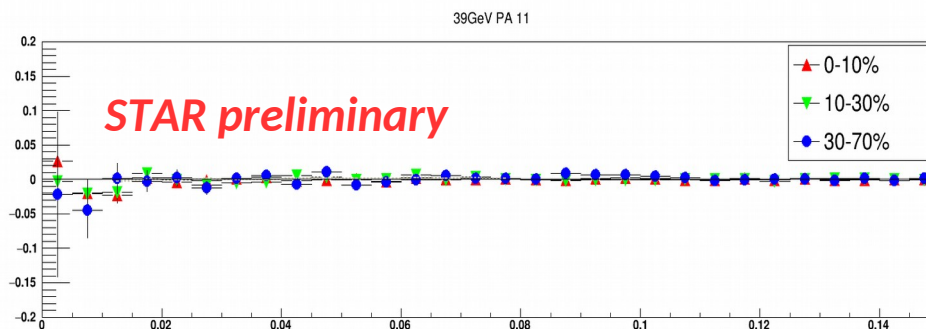
# System Dependence @39 GeV



Expected ordering of particles:

**Lighter particle is emitted closer to the center and/or later.**

No visible asymmetry between protons and antiprotons  
- similar masses.

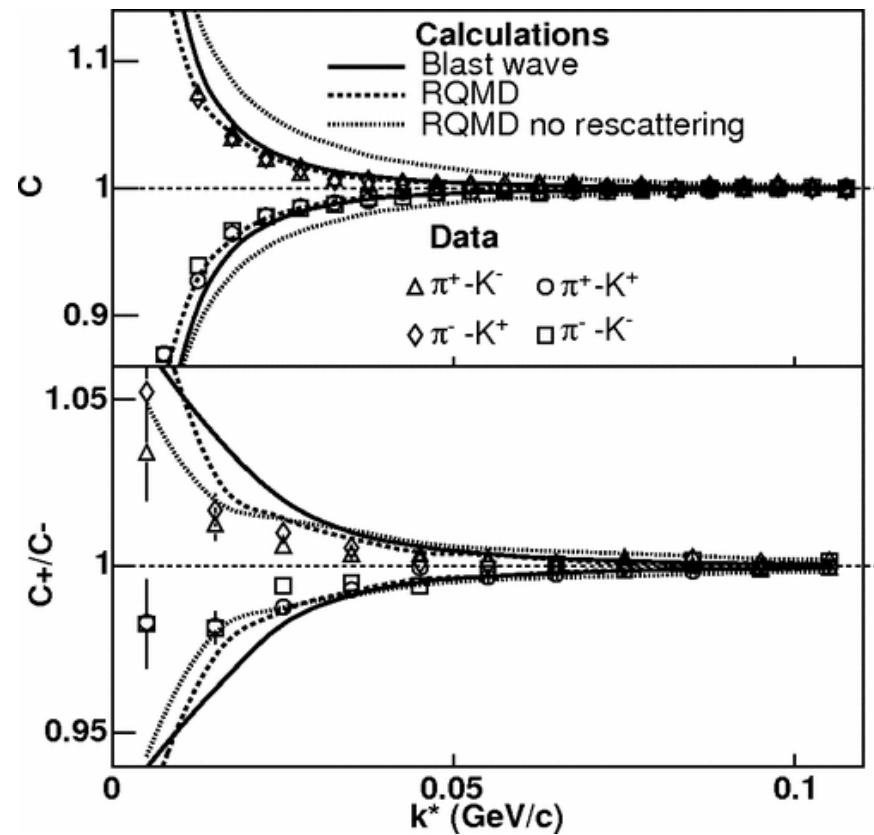
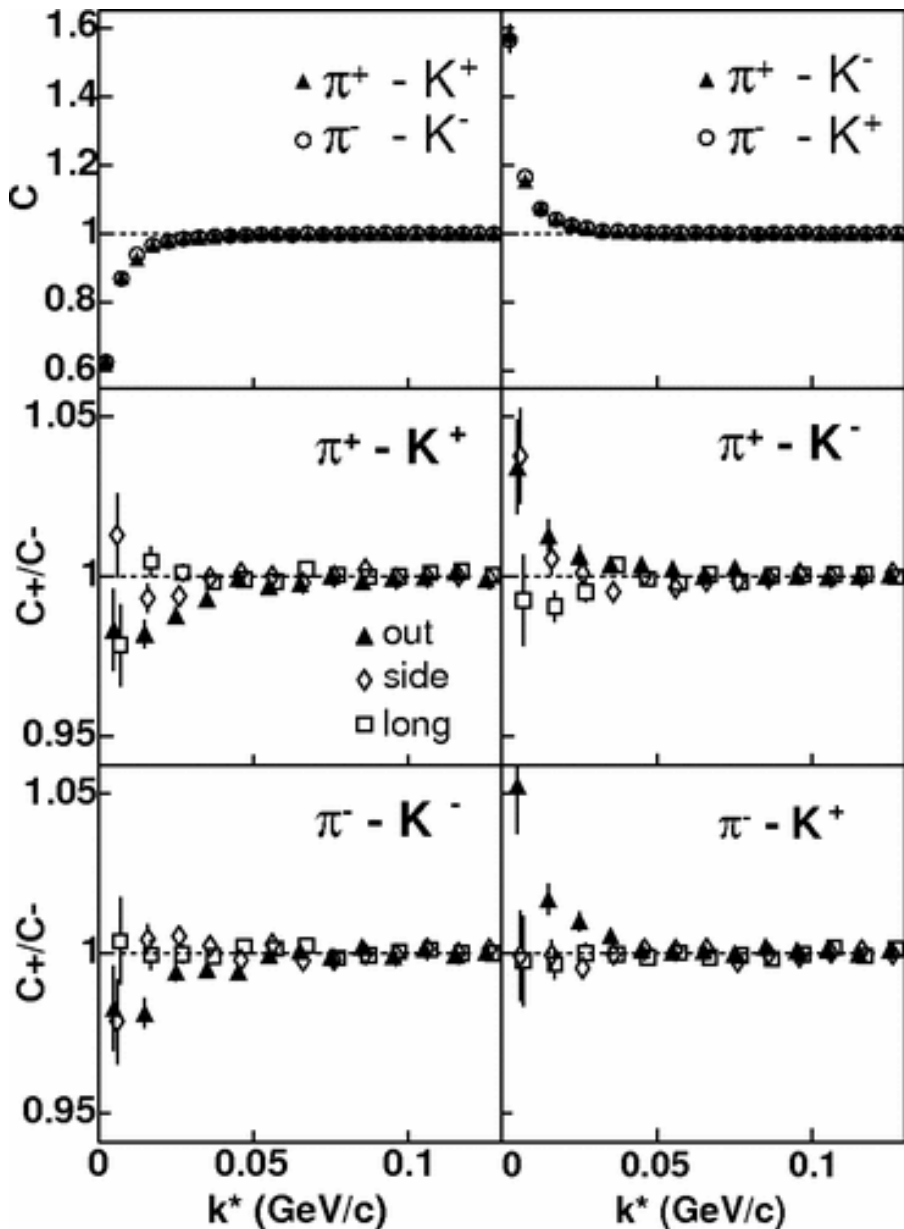


QM 2018,  
Nucl. Phys. A 982 (2019), 359-362

**Heavier particles pushed by flow  
outwards stronger than lighter particles.**



# Pion-Kaon Results @ 130GeV



	$\sigma$ (fm)	$\langle \Delta r_{out}^* \rangle$ (fm)	$\chi^2 / \text{dof}$
Data	$12.5 \pm 0.4_{-3}^{+2.2}$	$-5.6 \pm 0.6_{-1.3}^{+1.9}$	134.5/110
RQMD	$11.8 \pm 0.4$	$-8.0 \pm 0.6$	205/54
RQMD no rescattering	$5.8 \pm 0.1$	$-2.0 \pm 0.3$	940/54
BWP	$9.9 \pm 0.1$	$-6.9 \pm 0.3$	1020/118

**Kaons are emitted earlier and/or further than Pions.**



# Conclusions & Summary

# Summary about Geometry

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Geometry:

- Clear centrality dependence of source size at BES energies
- Clear system dependence of source size at BES energies
- Visible energy dependence of source size at BES energies

**No visible difference between Proton-Proton and Antiproton-Antiproton correlation functions**

**Correlation functions contaminated by residual correlations – residual correction required**

**Strong interaction seen not negligible in Kaon-Proton**

# Summary about Dynamics

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Clear signal of emission asymmetry for particles with different masses at BES energies

Asymmetry not disappeared for low energies

**Lighter particles emitted closer to the center of the source and/or later than heavier particles – flow pushes heavier particles harder to the edge**

**Thank you!**

# Backup

# Correlation Function

$$CF(k^*) = \frac{\sum_{pair} \delta(k_{pair}^* - k^*) w(k^*, r^*)}{\sum_{pair} \delta(k_{pair}^* - k^*)}$$

$$w(k^*, r^*) = |\psi_{-k^*}^{S(+)}(r^*) + (-1)^S \psi_{k^*}^{S(+)}(r^*)|^2 / 2$$

$$\psi_{-k^*}^{S(+)}(r^*) = e^{i\delta_c} \sqrt{A_c(\eta)} [e^{-ik^* r^*} F(-i\eta, 1, i\xi) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*}]$$

$$f_c(k^*) = \left[ \underbrace{1}_{f_0} + \frac{1}{2} \underbrace{d_0}_{d_0} k^{*2} - \frac{2}{a_c} h(k^* a_c) - ik^* A_c(k^*) \right]^{-1}$$

is the s-wave scattering amplitude renormalized by Coulomb interaction.

$$A_c(k^*) = (2\pi/k^* a_c) \frac{1}{\exp(2\pi/k^* a_c) - 1}, \quad h(x) = \frac{1}{x^2} \sum_{n=1}^{\infty} \frac{1}{n(n^2 + x^2)} - C + \ln|x|,$$

and  $\tilde{G}(\rho, \eta) = \sqrt{A_c(k^*)} (G_0(\rho, \eta) + iF_0(\rho, \eta))$  is a combination of regular ( $F_0$ ) and singular ( $G_0$ ) s-wave Coulomb functions.