

# Dark matter interpretation with global fits

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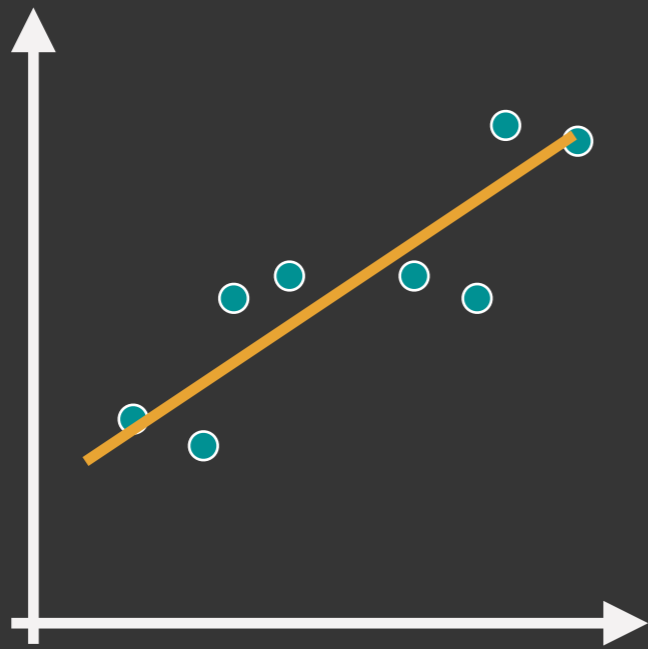
**Anders Kvellestad**, Imperial College London  
*on behalf of the GAMBIT Collaboration*

DM @ LHC, Seattle, 15 August 2019



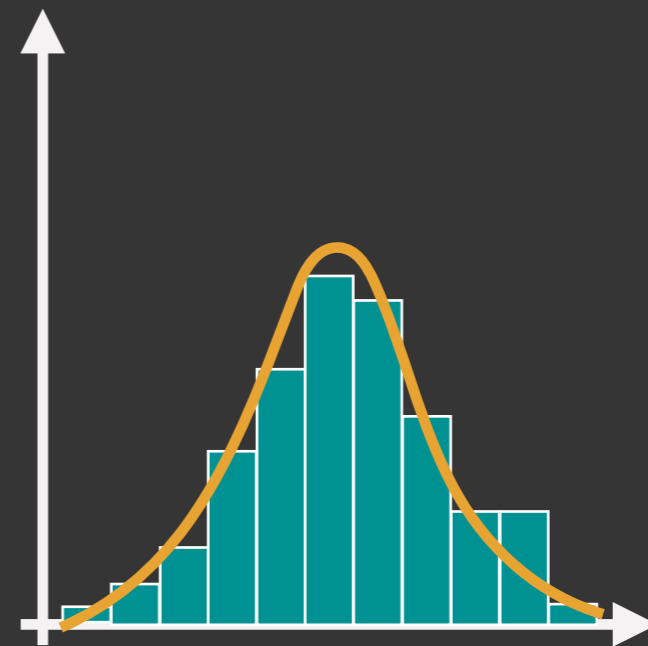
# I. Global fits?

# Statistical fits

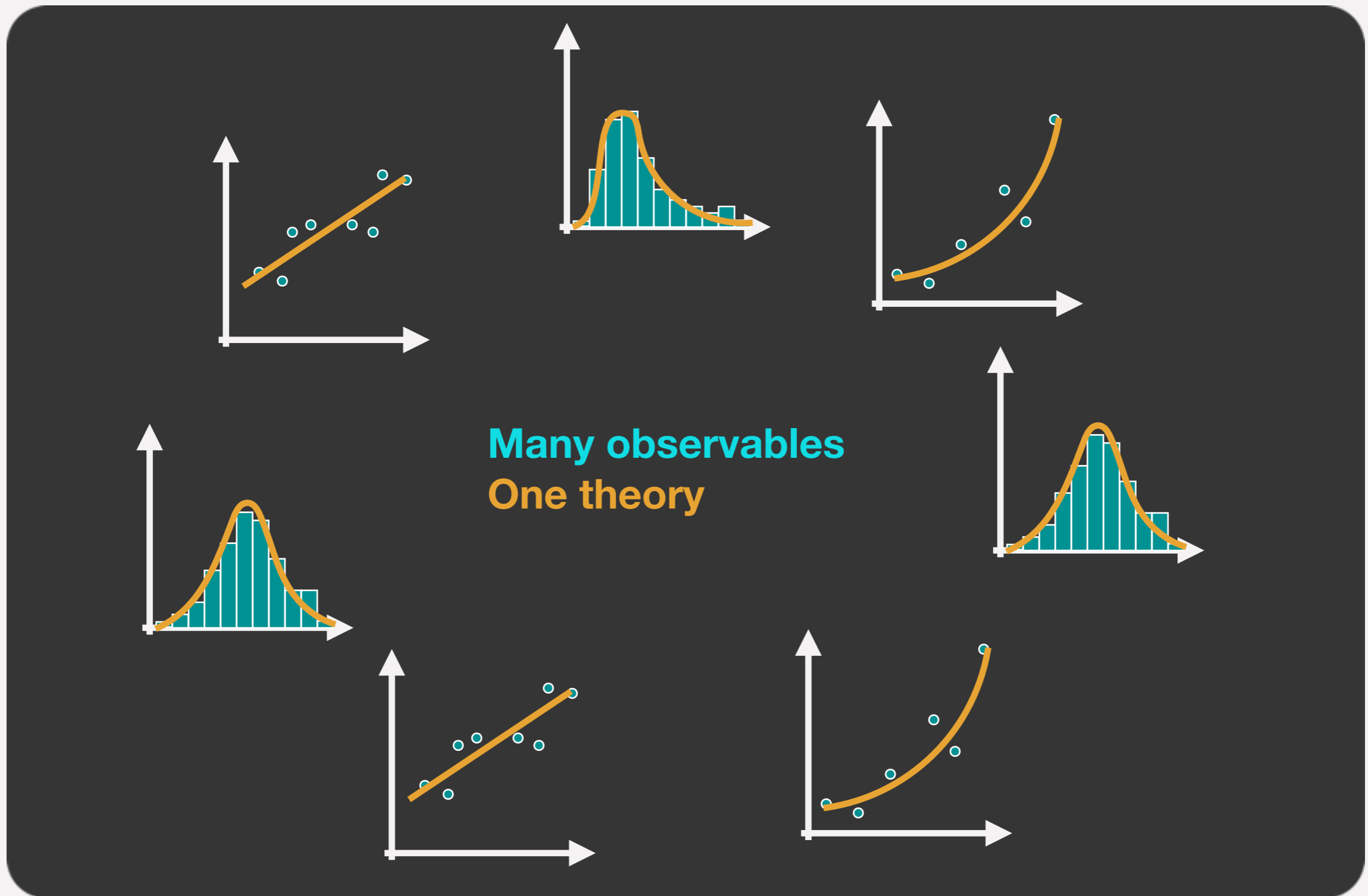


**Some observable**  
**Some model**

**Some other observable**  
**Some other model**



# Global fits



Many observables  
One theory

# The basic steps of a BSM global fit

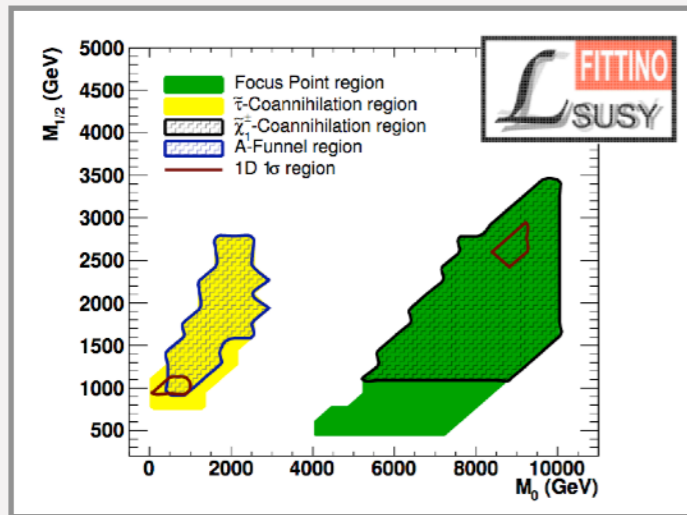
- Choose your **BSM model and parameterisation**
- Construct the **combined likelihood function** including observables from collider physics, dark matter, flavor physics, +++

$$\mathcal{L} = \mathcal{L}_{\text{collider}} \mathcal{L}_{\text{DM}} \mathcal{L}_{\text{flavor}} \mathcal{L}_{\text{EWPO}} \dots$$

- Use **sophisticated scanning techniques** to explore the likelihood function across the parameter space of the theory
- Test **parameter regions** in a statistically sensible way — not just single points (*parameter estimation*)
- Test **different theories the same way** (*model comparison*)

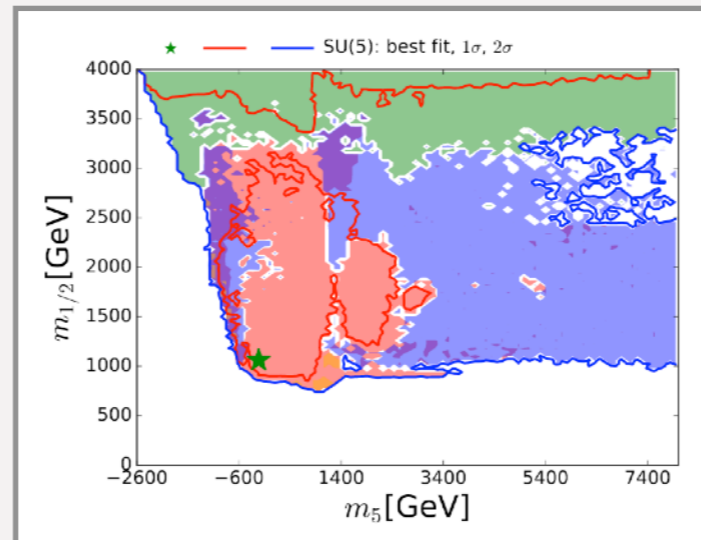
## 2. Recent(ish) DM global fits

# SUSY DM global fits (high scale)



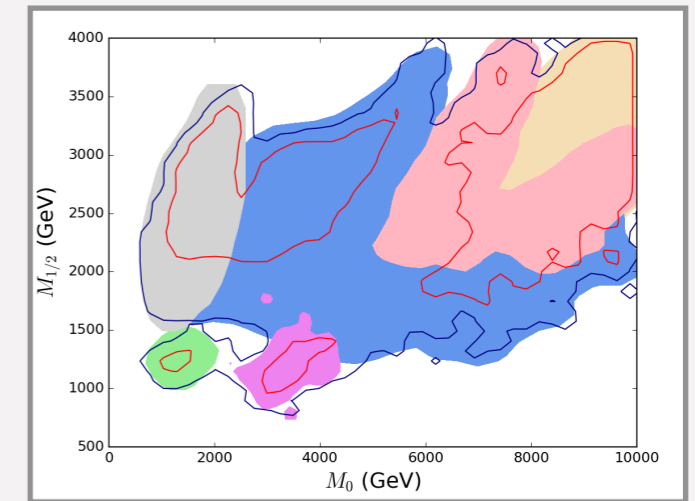
**CMSSM**

Fittino, [1508.05951](#)



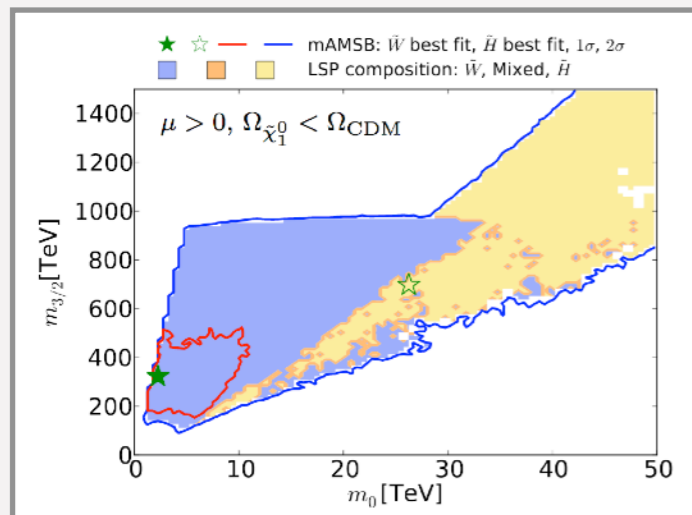
**SUSY SU(5) GUTs**

MasterCode, [1610.10084](#)



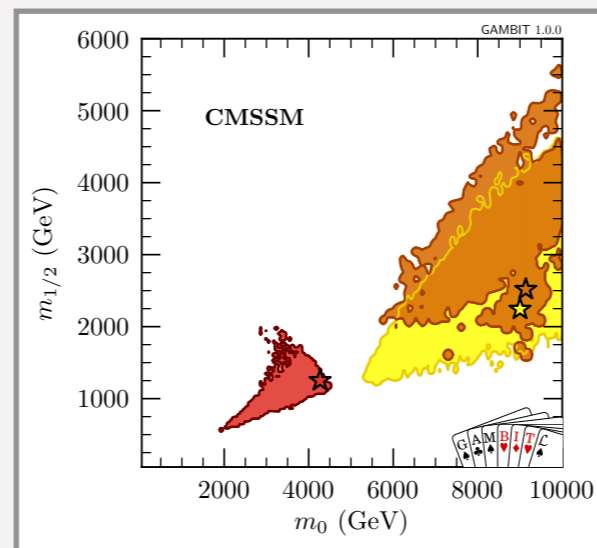
**CMSSM**

EasyScan\_HEP, [1612.02296](#)



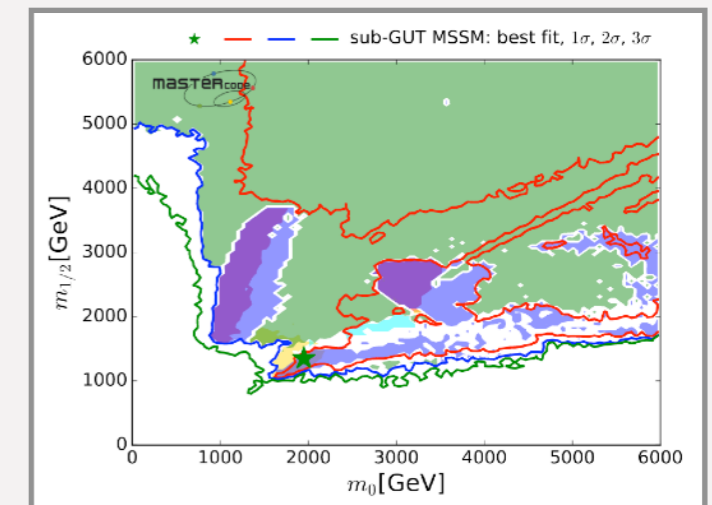
**mAMSB**

MasterCode, [1612.05210](#)



**CMSSM, NUHM1, NUHM2**

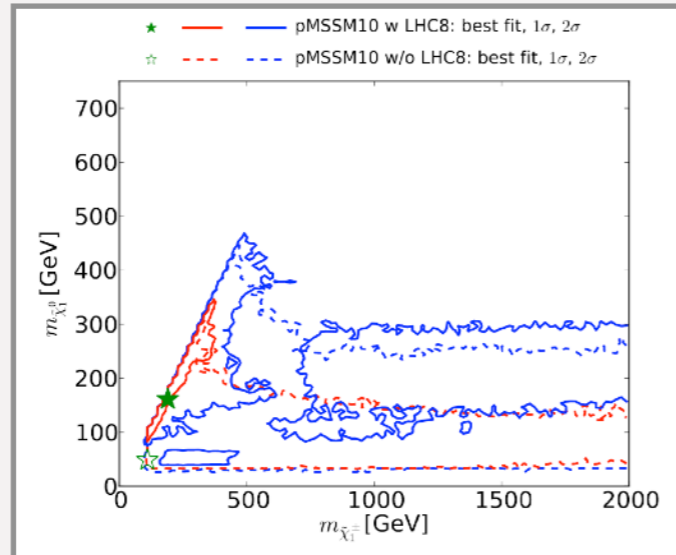
GAMBIT, [1705.07935](#)



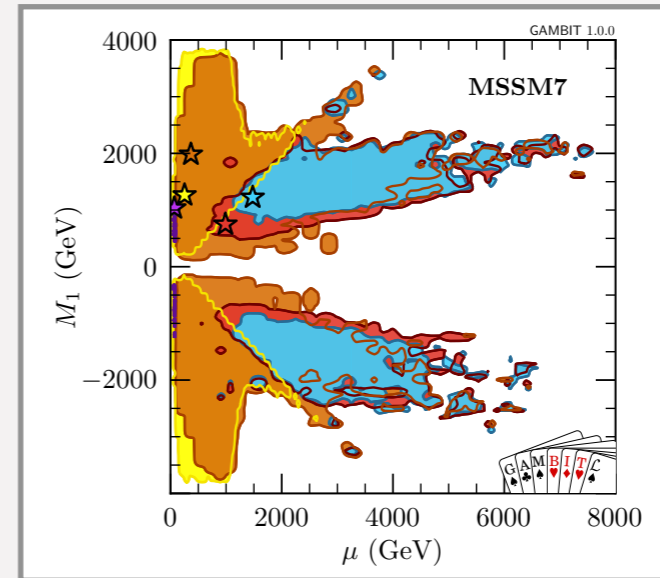
**sub-GUT MSSM**

MasterCode, [1711.00458](#)

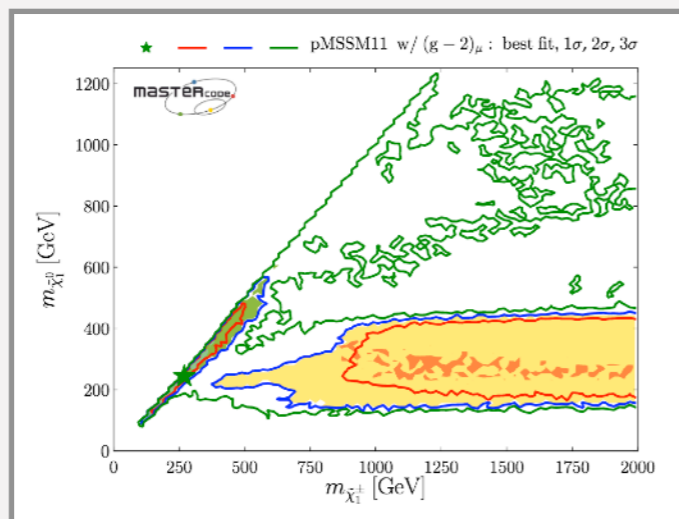
# SUSY DM global fits (weak scale)



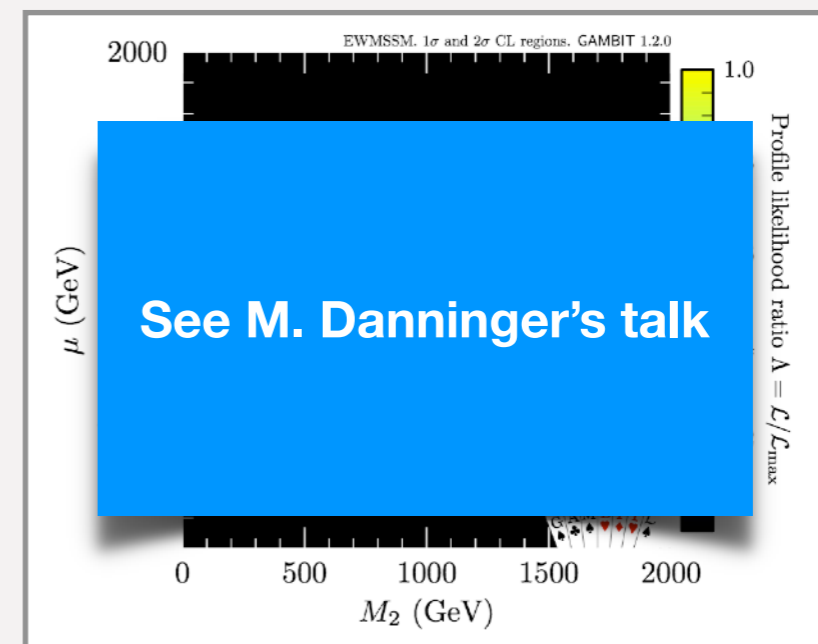
**MSSM10**  
MasterCode, 1504.03260



**MSSM7**  
GAMBIT, 1705.07917



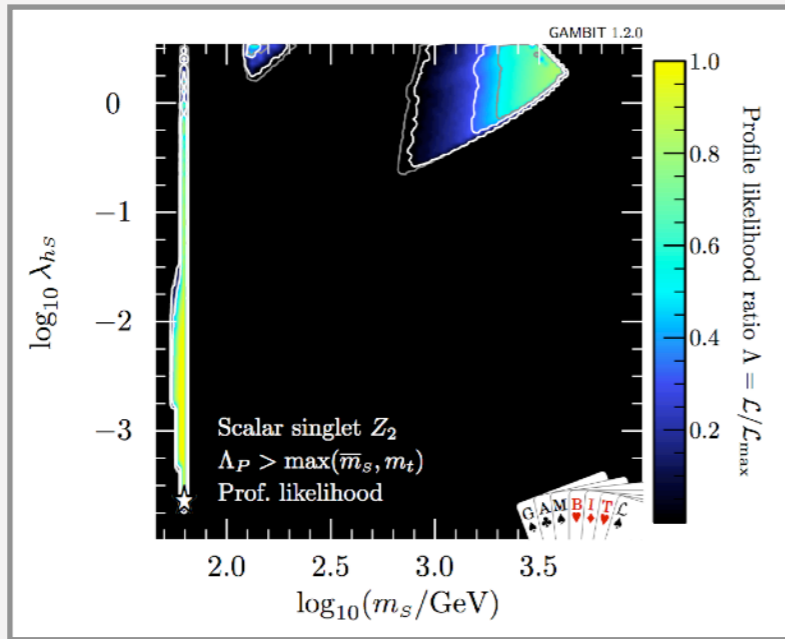
**MSSM11**  
MasterCode, 1710.11091



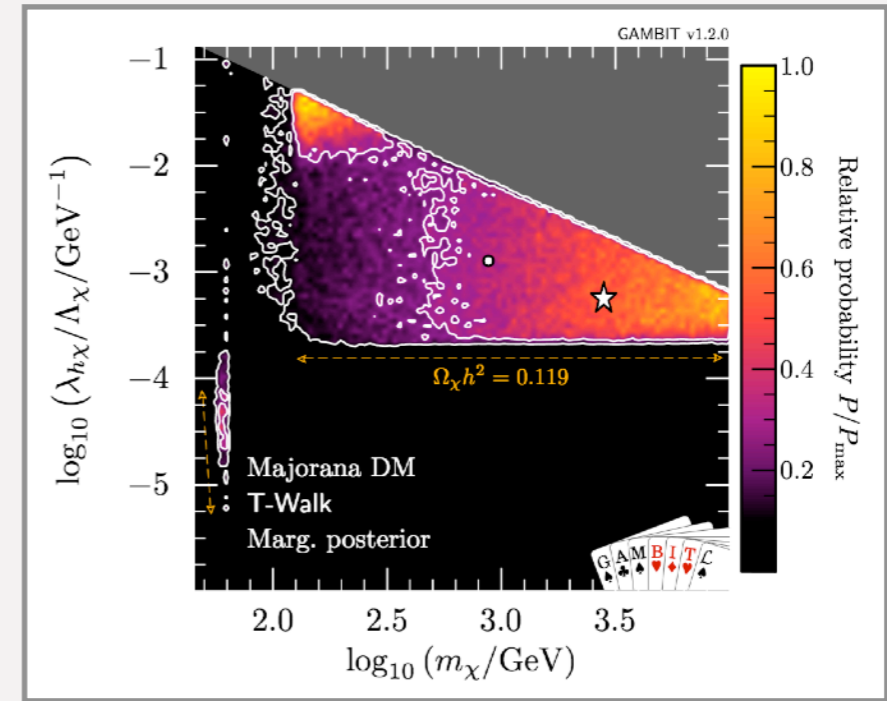
**EW-MSSM**  
GAMBIT, 1809.02097



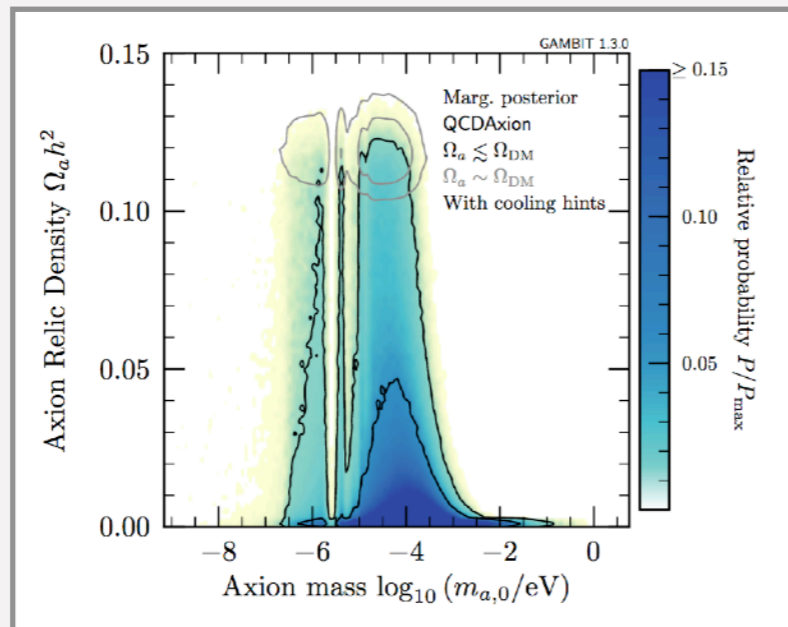
# Non-SUSY DM global fits



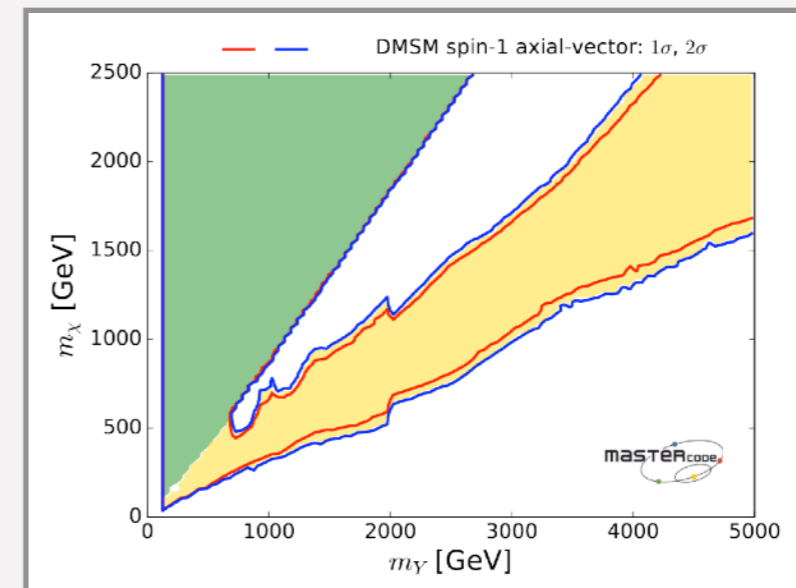
**Scalar Higgs portal DM (Z2 & Z3)**  
 GAMBIT, 1705.07931, 1806.11281



**Vector and fermion Higgs portal DM**  
 GAMBIT, 1808.10465.



**Axions and axion-like particles**  
 GAMBIT, 1810.07192



**DM w/ leptophobic mediator**  
 MasterCode, 1905.00892

# 3. GAMBIT

# GAMBIT: The Global And Modular BSM Inference Tool

[gambit.hepforge.org](http://gambit.hepforge.org)

EPJC 77 (2017) 784

arXiv:1705.07908

- Extensive model database – not just SUSY
- Extensive observable/data libraries
- Many statistical and scanning options (Bayesian & frequentist)
- *Fast* LHC likelihood calculator
- Massively parallel
- Fully open-source
- Fast definition of new datasets and theories
- Plug and play scanning, physics and likelihood packages



## Recent collaborators:

Peter Athron, Csaba Balázs, Ankit Beniwal, Sanjay Bloor, Torsten Bringmann, Andy Buckley, José Eliel Camargo-Molina, Marcin Chrzastecz, Jonathan Cornell, Matthias Danninger, Joakim Edsjö, Ben Farmer, Andrew Fowlie, Tomás E. Gonzalo, Will Handley, Sebastian Hoof, Selim Hotinli, Felix Kahlhoefer, Anders Kvellestad, Julia Harz, Paul Jackson, Farvah Mahmoudi, Greg Martinez, Are Raklev, Janina Renk, Chris Rogan, Roberto Ruiz de Austri, Pat Scott, Patrick Stöcker, Aaron Vincent, Christoph Weniger, Martin White, Yang Zhang

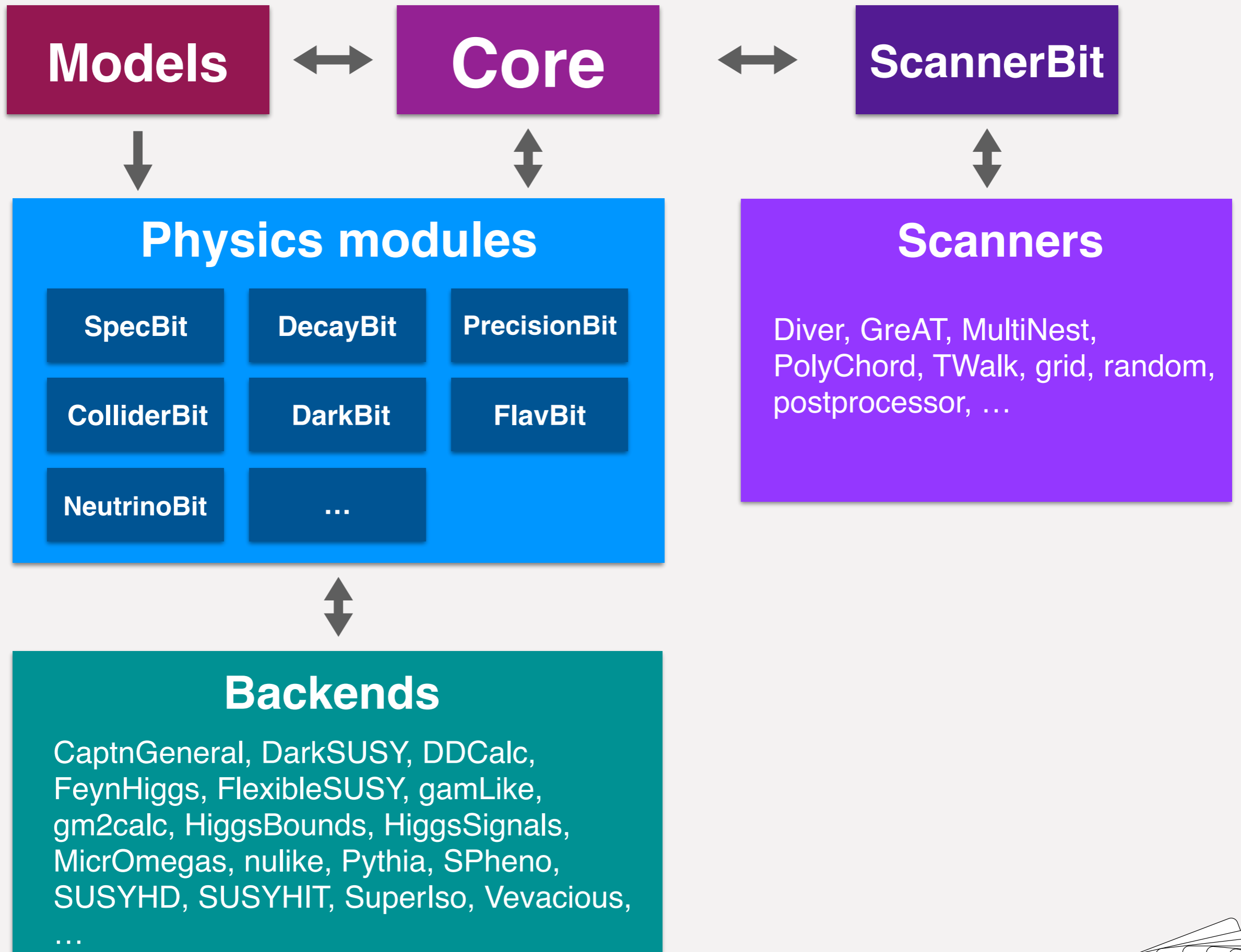
## Members of:

ATLAS, Belle-II, CLiC, CMS, CTA, *Fermi*-LAT, DARWIN, IceCube, LHCb, SHiP, XENON

## Authors of:

DarkSUSY, DDCalc, Diver, FlexibleSUSY, gamlike, GM2Calc, IsaTols, nulike, PolyChord, Rivet, SoftSUSY, SuperISO, SUSY-AI, WIMPSim

**40+ participants in 11 experiments and 14 major theory codes**



# Results: SUSY dark matter

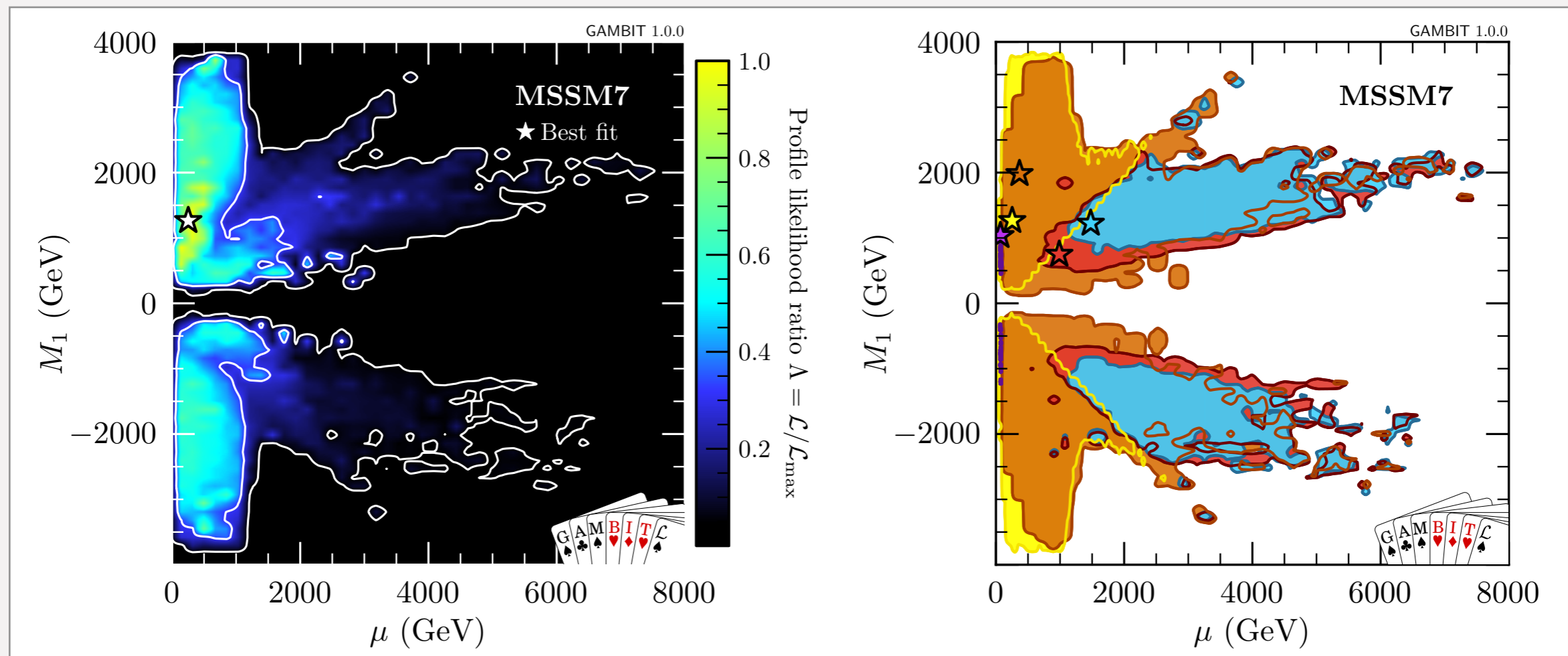


# Likelihoods

- Nuisance parameter likelihoods (SM, local halo model, nuclear matrix elements)
- DM relic density *as upper bound*
- DM Indirect detection
  - Gamma rays: Fermi-LAT (dwarf spheroidal galaxies)
  - Neutrinos from DM annihilation in the Sun: IceCube79
- DM Direct detection:
  - XENON100 (2012)
  - LUX (2016)
  - Panda-X (2016)
  - PICO (2015)
  - SuperCDMS (2014)
  - SIMPLE (2014)
- Electroweak precision observables
  - W mass
  - muon g-2
- 59 flavour observables
- Higgs mass and signal strengths
- SUSY cross section limits from LEP
- SUSY searches at LHC (simulated)
  - 0 lepton searches (Run I & II, ATLAS & CMS)
  - Stop searches (Run I, ATLAS & CMS)
  - 2 & 3 lepton searches (Run I, ATLAS & CMS)



# MSSM 7

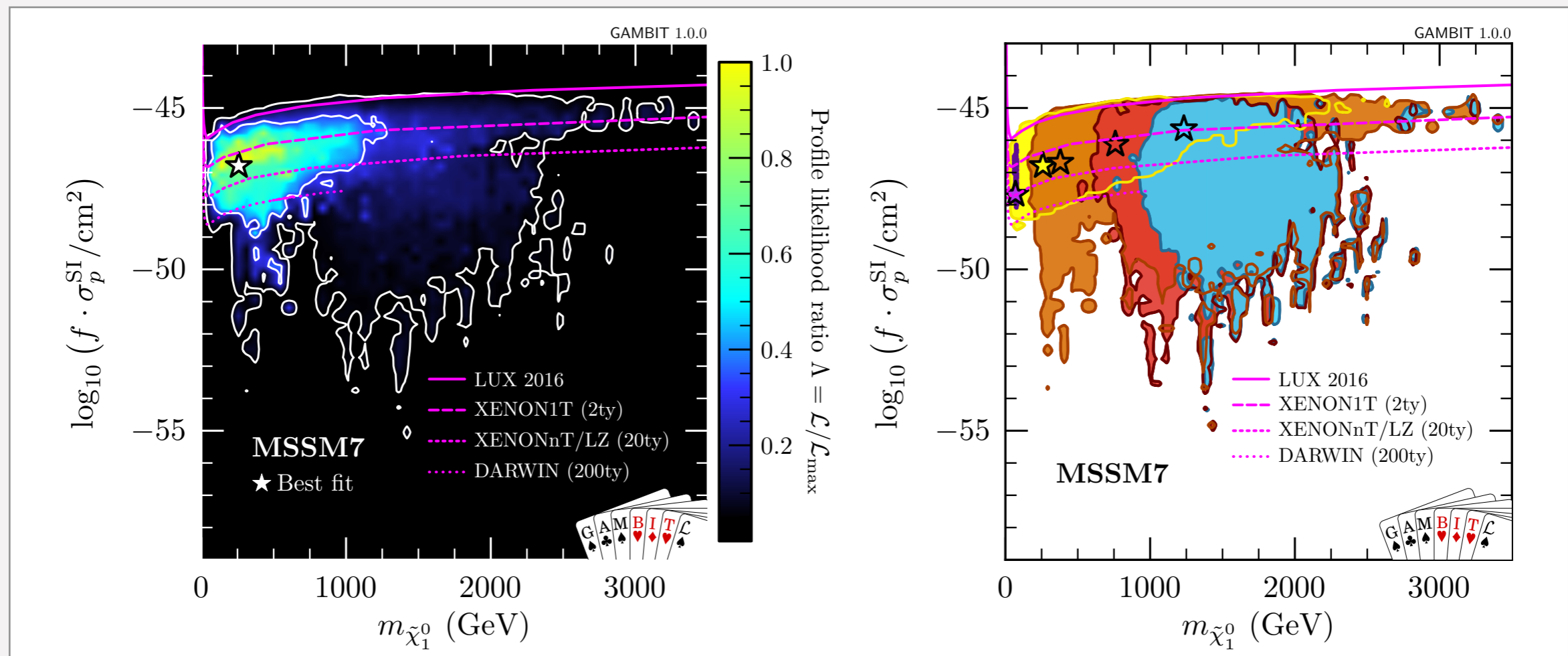


■  $\tilde{t}_1$  co-annihilation  
 ■  $A/H$  funnel  
 ■  $\tilde{\chi}_1^\pm$  co-annihilation  
 ■  $\tilde{b}_1$  co-annihilation  
 ■  $h/Z$  funnel

- Three neutralino scenarios: higgsino-dominated, higgsino/bino mix, bino-dominated
- Wino-dominated neutralino not possible due to GUT relation ( $M_2 \sim 2M_1$ )



# MSSM 7



■  $\tilde{t}_1$  co-annihilation  
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 ■  $\tilde{\chi}_1^\pm$  co-annihilation  
 ■  $\tilde{b}_1$  co-annihilation  
 ■  $h/Z$  funnel

- Best fit point in chargino co-annihilation region (chargino/neutralino mass  $\sim 260$  GeV)
- Mass difference  $< 10$  GeV (challenging for LHC)
- Under-abundant relic density at best fit point (but  $\sim$ equally good fit with 1 TeV higgsinos)
- Entire chargino co-ann. and light Higgs funnel regions will be probed by future DD





# Results: Higgs portal dark matter

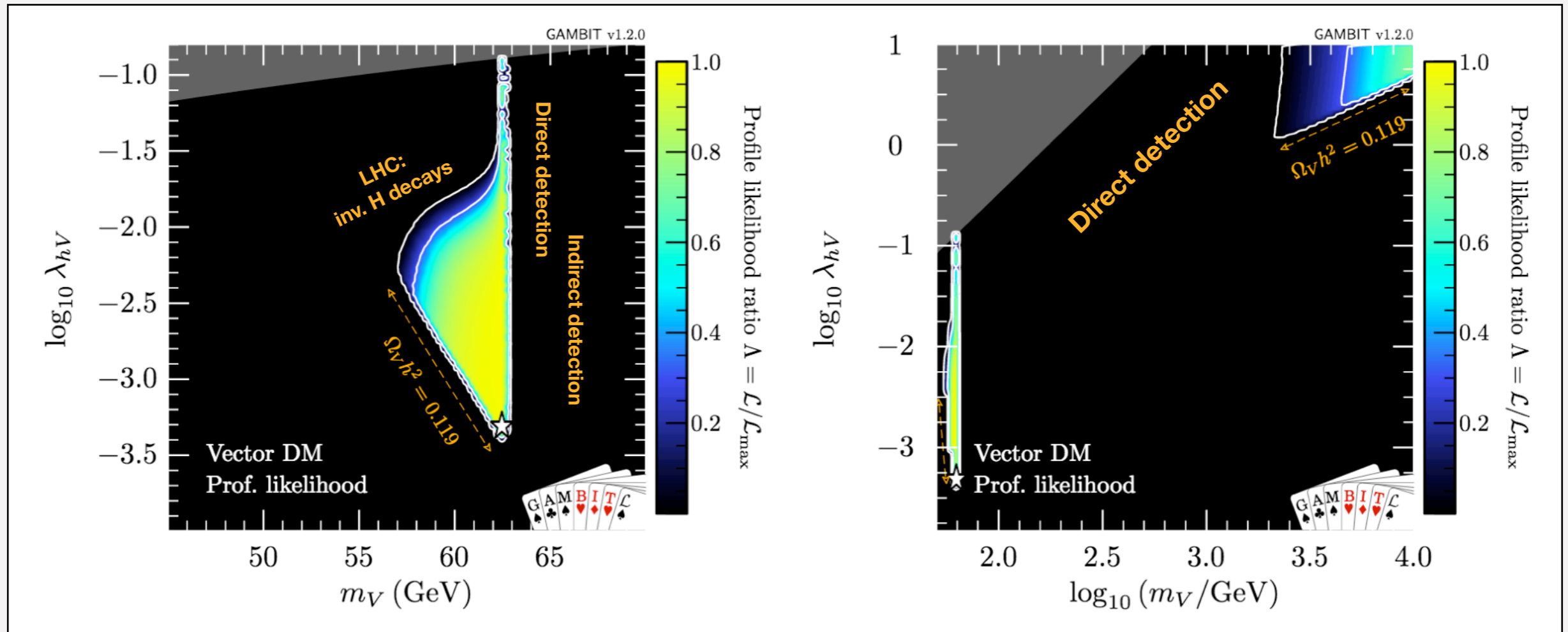


# Likelihoods

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(SM, local halo model, nuclear matrix elements)
- DM relic density *as upper bound*
- DM Indirect detection
  - Gamma rays: Fermi-LAT  
(dwarf spheroidal galaxies)
  - Neutrinos from DM annihilation in the Sun:  
IceCube79
- DM Direct detection:
  - XENON1T 2018
  - LUX 2016
  - Panda-X 2016, 2017
  - CDMSlite
  - CRESST-II
  - PICO-60
  - DarkSide-50
- Higgs invisible decay width
- Perturbative unitarity and EFT validity



# Higgs portal (vector/fermion)

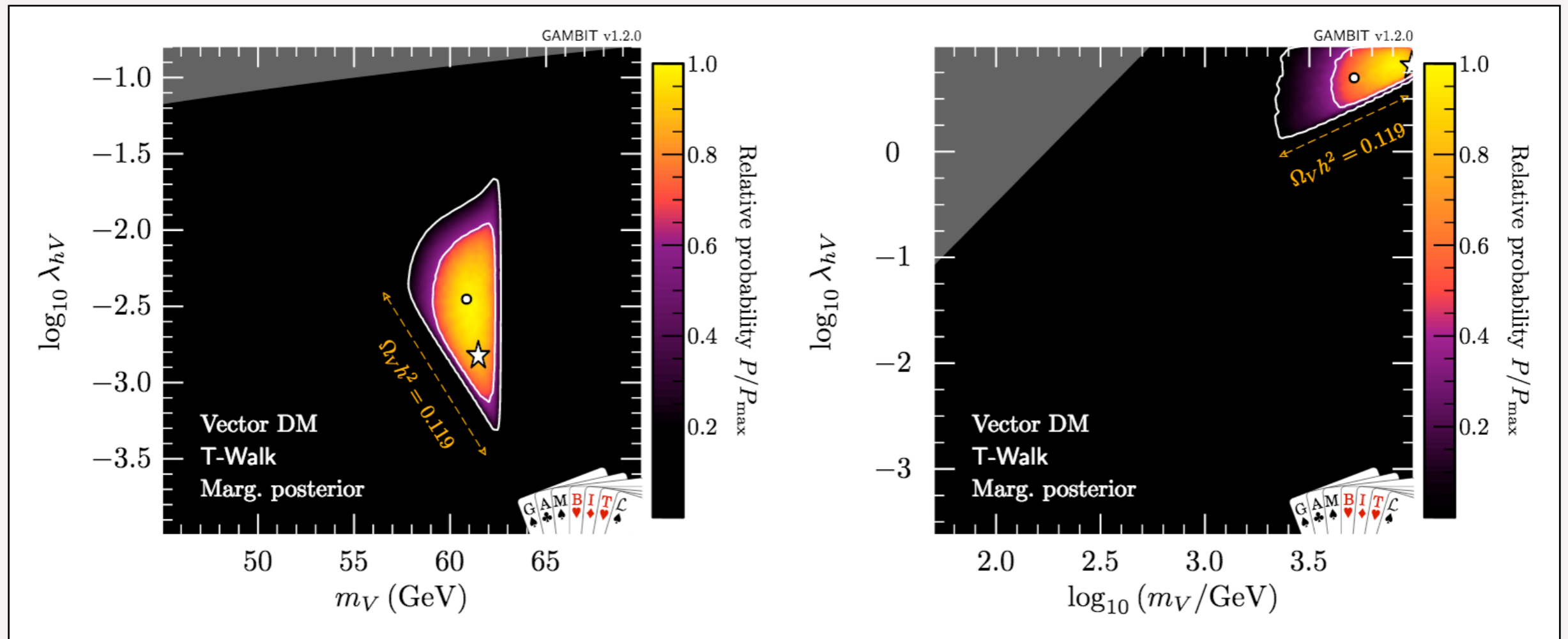


## Vector DM model

- Higgs resonance region and high-mass region consistent with all experiments
- Direct detection generally very constraining, but invisible H decays also important



# Higgs portal (vector/fermion)

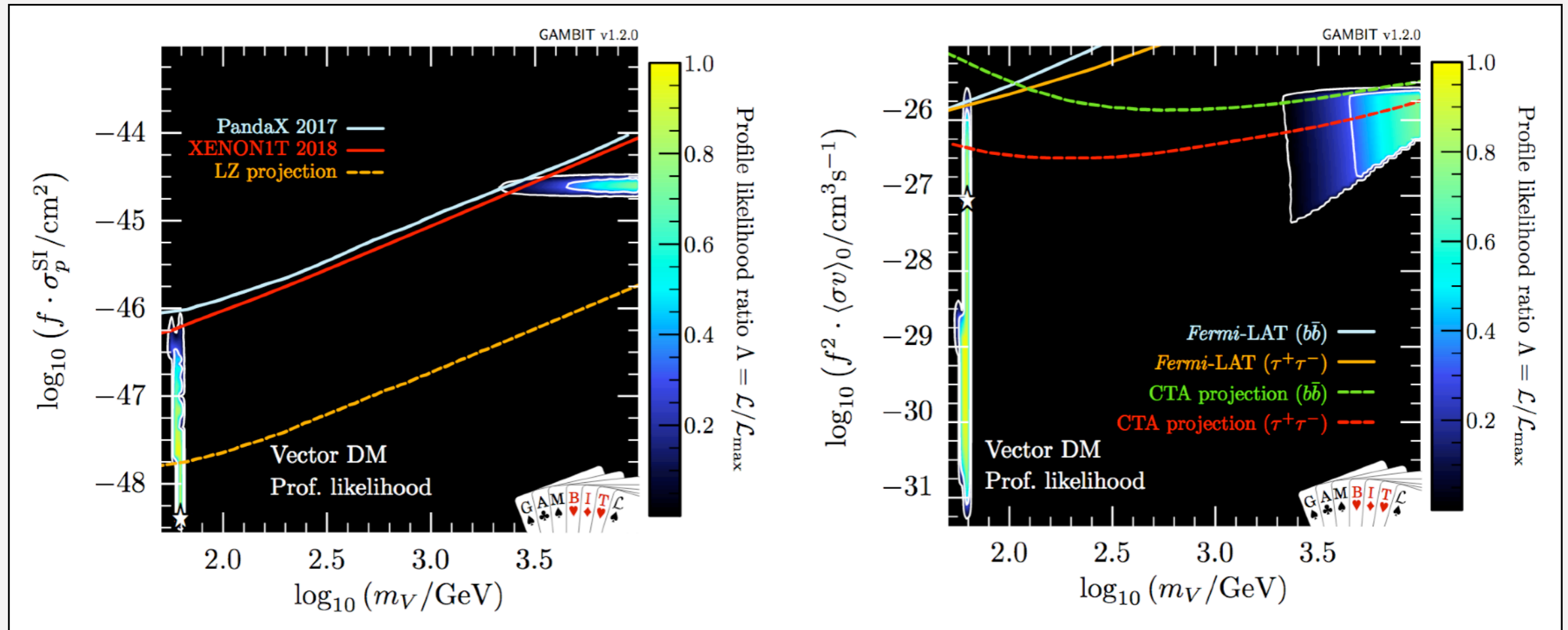


## Vector DM model

- Bayesian posterior distributions: resonance region disfavoured due to being fine-tuned
- Similar effect seen for the scalar and fermion DM models



# Higgs portal (vector/fermion)

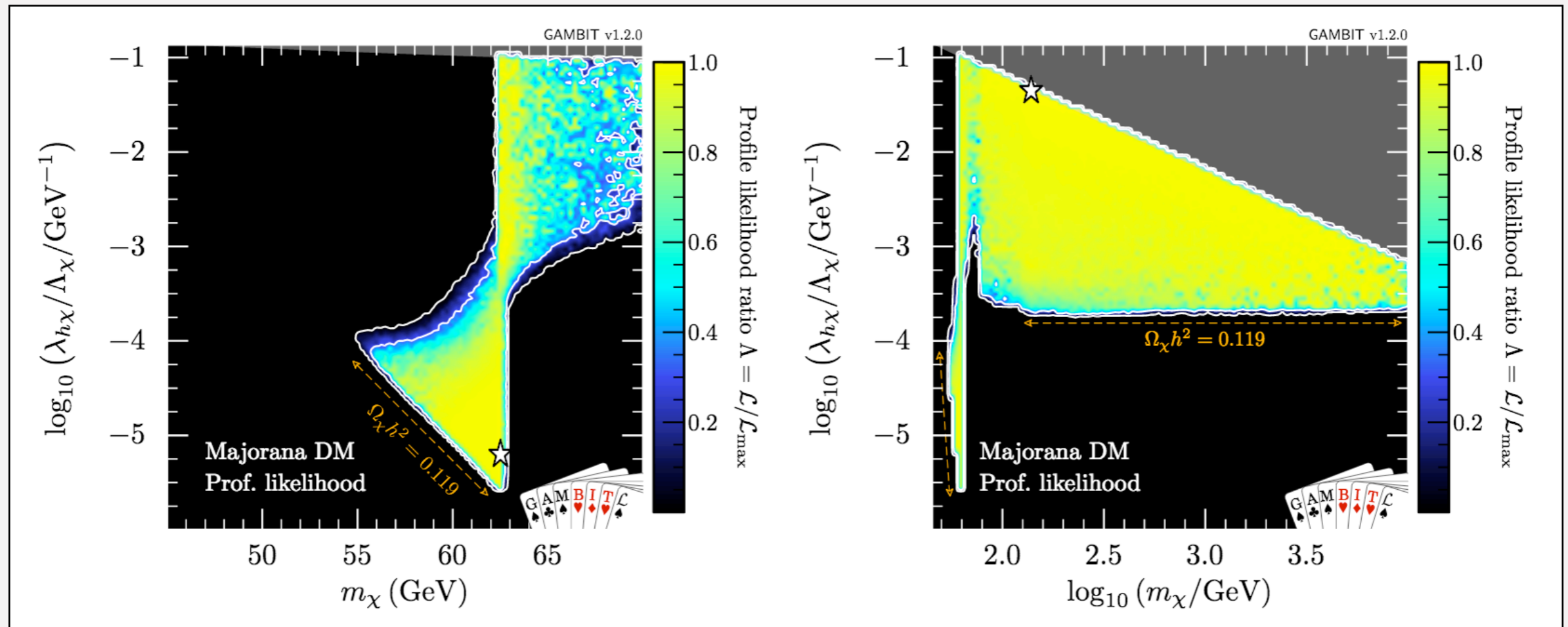


## Vector DM model

- Future experiments will probe entire high-mass region and part of resonance region



# Higgs portal (vector/fermion)



## Majorana fermion DM model (similar results for Dirac fermion)

- Additional free parameter: CP phase of portal interaction
- CP-violating interaction
  - momentum suppression in DD cross-section
  - larger viable parameter space



# Higgs portal (vector/fermion)

Model	Comparison model and priors			Odds
$\xi = 0$	$m_\chi: \log$	$\lambda_{h\chi}/\Lambda_\chi: \log$	$\xi: \text{flat}$	70:1
$g_p/\Lambda_p = 0$	$m_\chi: \log$	$g_s/\Lambda_s: \log$	$g_p/\Lambda_p: \log$	140:1

Model	Parameters and priors			Odds
$S$	$m_S: \log$	$\lambda_{hS}: \log$		1:1
$V_\mu$	$m_V: \log$	$\lambda_{hV}: \log$		6:1
$\chi$	$m_\chi: \log$	$\lambda_{h\chi}/\Lambda_\chi: \log$	$\xi: \text{flat}$	1:1
$\psi$	$m_\psi: \log$	$\lambda_{h\psi}/\Lambda_\psi: \log$	$\xi: \text{flat}$	1:1

## Bayesian model comparisons

- Fermion DM: **CP-conserving vs CP-violating portal coupling?**  
→ «Strong evidence» against pure CP-conserving case (Jeffrey's scale)
- **Scalar, fermion or vector DM?**  
→ «Positive evidence» against vector DM model, compared to scalar model



# Summary





# Summary

- There are *many* observables that may have implications for dark matter → **need global fits** to get the complete picture
- **Global fits for *any* BSM model?** GAMBIT is your friend!  
(But it's not automatic... yet...)
- SUSY global fits are still going strong
- Many constraints, but «**vanilla**» **MSSM dark matter remains viable and well-motivated**
- If you believe in fermion singlet dark matter, you **should not expect a CP-conserving Higgs portal interaction**
- Interesting parameter regions for MSSM and Higgs portal dark matter will be probed in upcoming experiments — in particular in direct detection
- *GAMBIT v1.4 is out:* [gambit.hepforge.org](https://gambit.hepforge.org)

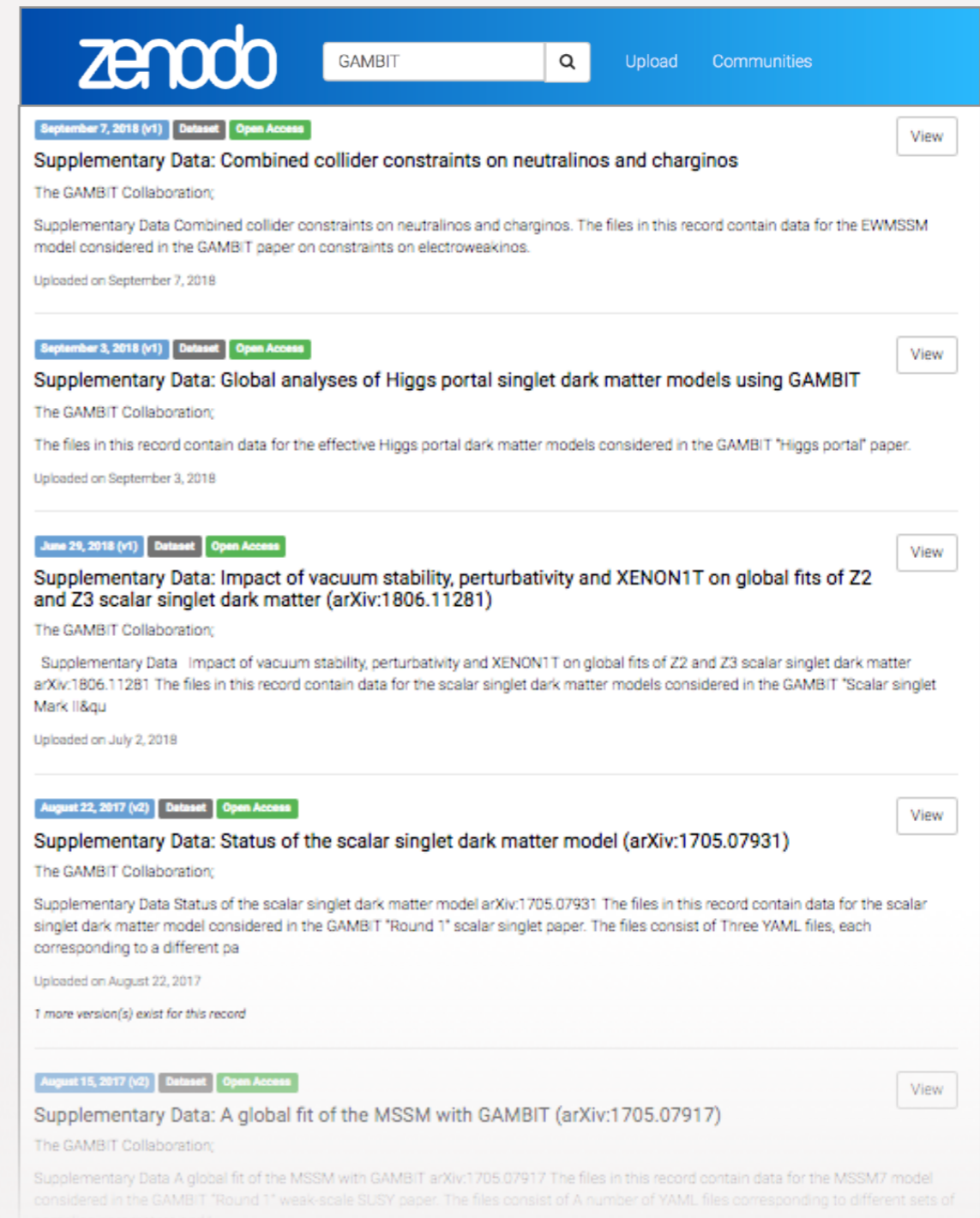


# All GAMBIT results are publicly available

## Results available on [zenodo.cern.ch](https://zenodo.cern.ch)

- Parameter point samples (hdf5 files)
- GAMBIT input files for all scans
- Example plotting routines
- SLHA files for benchmark points

## Links at [gambit.hepforge.org/pubs](https://gambit.hepforge.org/pubs)



The screenshot displays the Zenodo website interface. At the top, there is a blue header with the Zenodo logo, a search bar containing the text "GAMBIT", and navigation links for "Upload" and "Communities". Below the header, a list of datasets is shown, each with a date, version, and "Open Access" status. The datasets listed are:

- September 7, 2018 (v1)** Dataset Open Access: **Supplementary Data: Combined collider constraints on neutralinos and charginos**. Description: The GAMBIT Collaboration; Supplementary Data Combined collider constraints on neutralinos and charginos. The files in this record contain data for the EWMSSM model considered in the GAMBIT paper on constraints on electroweakinos. Uploaded on September 7, 2018.
- September 3, 2018 (v1)** Dataset Open Access: **Supplementary Data: Global analyses of Higgs portal singlet dark matter models using GAMBIT**. Description: The GAMBIT Collaboration; The files in this record contain data for the effective Higgs portal dark matter models considered in the GAMBIT "Higgs portal" paper. Uploaded on September 3, 2018.
- June 29, 2018 (v1)** Dataset Open Access: **Supplementary Data: Impact of vacuum stability, perturbativity and XENON1T on global fits of Z2 and Z3 scalar singlet dark matter (arXiv:1806.11281)**. Description: The GAMBIT Collaboration; Supplementary Data Impact of vacuum stability, perturbativity and XENON1T on global fits of Z2 and Z3 scalar singlet dark matter arXiv:1806.11281 The files in this record contain data for the scalar singlet dark matter models considered in the GAMBIT "Scalar singlet Dark Matter II" paper. Uploaded on July 2, 2018.
- August 22, 2017 (v2)** Dataset Open Access: **Supplementary Data: Status of the scalar singlet dark matter model (arXiv:1705.07931)**. Description: The GAMBIT Collaboration; Supplementary Data Status of the scalar singlet dark matter model arXiv:1705.07931 The files in this record contain data for the scalar singlet dark matter model considered in the GAMBIT "Round 1" scalar singlet paper. The files consist of Three YAML files, each corresponding to a different parameter set. Uploaded on August 22, 2017. 1 more version(s) exist for this record.
- August 15, 2017 (v2)** Dataset Open Access: **Supplementary Data: A global fit of the MSSM with GAMBIT (arXiv:1705.07917)**. Description: The GAMBIT Collaboration; Supplementary Data A global fit of the MSSM with GAMBIT arXiv:1705.07917 The files in this record contain data for the MSSM7 model considered in the GAMBIT "Round 1" weak-scale SUSY paper. The files consist of A number of YAML files corresponding to different sets of parameters.



# Bonus tracks



# Parameters and likelihoods

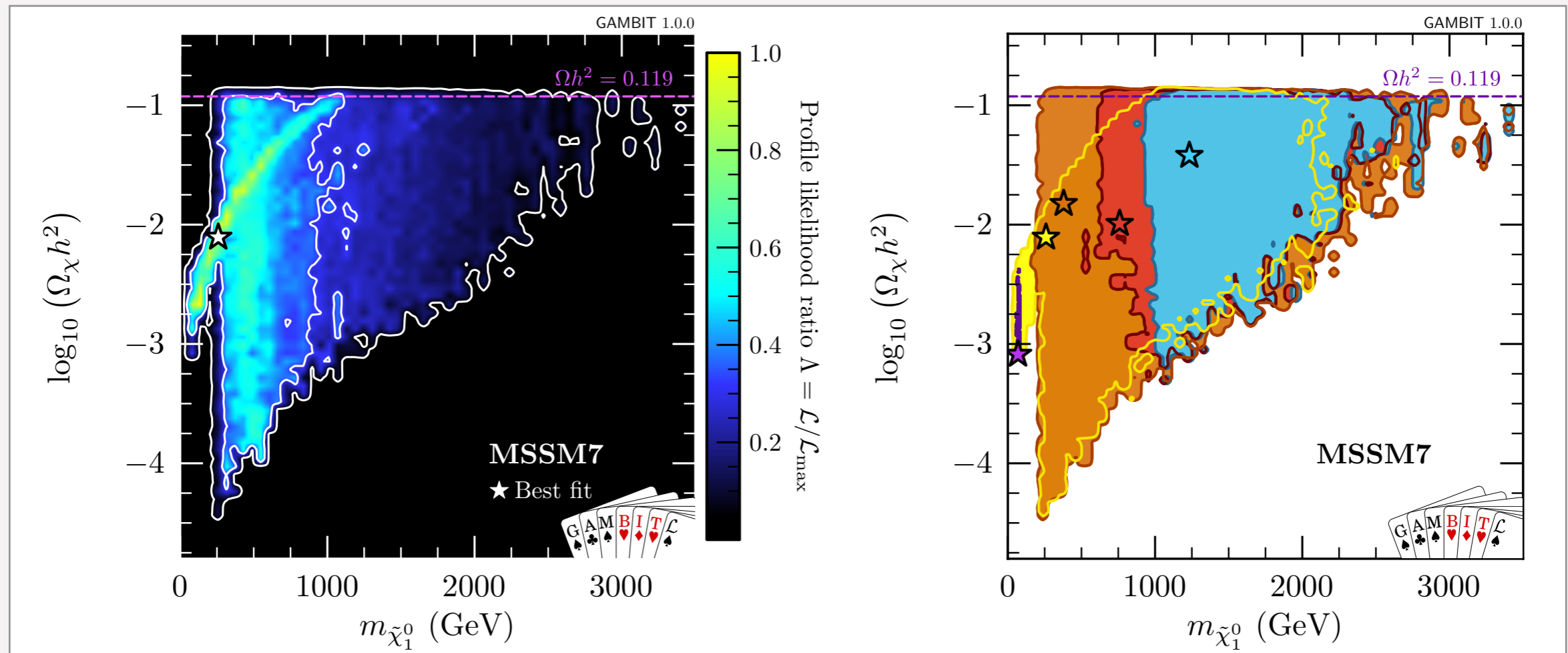
Parameter	Minimum	Maximum	Priors
$A_{u_3}(Q)$	$-10 \text{ TeV}$	$10 \text{ TeV}$	flat, hybrid
$A_{d_3}(Q)$	$-10 \text{ TeV}$	$10 \text{ TeV}$	flat, hybrid
$M_{H_u}^2(Q)$	$-(10 \text{ TeV})^2$	$(10 \text{ TeV})^2$	flat, hybrid
$M_{H_d}^2(Q)$	$-(10 \text{ TeV})^2$	$(10 \text{ TeV})^2$	flat, hybrid
$m_{\tilde{f}}^2(Q)$	0	$(10 \text{ TeV})^2$	flat, hybrid
$M_2(Q)$	$-10 \text{ TeV}$	$10 \text{ TeV}$	split; flat, hybrid
$\tan \beta(m_Z)$	3	70	flat
$\text{sgn}(\mu)$		+	fixed
$Q$		1 TeV	fixed

- 7 MSSM parameters + 5 nuisance parameters
- Assume GUT-inspired relation on gaugino mass parameters:

$$\frac{3}{5} \cos^2 \theta_W M_1 = \sin^2 \theta_W M_2 = \frac{\alpha}{\alpha_s} M_3$$

- Same likelihoods as for the GUT-scale models

# MSSM 7



■  $\tilde{t}_1$  co-annihilation  
 ■  $A/H$  funnel  
 ■  $\tilde{\chi}_1^{\pm}$  co-annihilation  
 ■  $\tilde{b}_1$  co-annihilation  
 ■  $h/Z$  funnel

- Best fit point in chargino co-annihilation region (chargino/neutralino mass  $\sim 260$  GeV)
- Mass difference  $< 10$  GeV (challenging for LHC)
- Under-abundant relic density

- $H^\dagger H$  – lowest dimensional, gauge-invariant operator.
- Vector ( $V_\mu$ ) and Majorana fermion<sup>1</sup> ( $\chi$ ) fields with  $\mathbb{Z}_2$  symmetry:

$$(V_\mu, \chi) \rightarrow - (V_\mu, \chi). \quad (2)$$

- Lagrangians after EWSB and chiral rotation:  $\chi \rightarrow e^{i\gamma_5\alpha/2} \chi$  are

$$\mathcal{L}_V \supset \frac{1}{2} m_V^2 V_\mu V^\mu + \frac{1}{2} \lambda_{hV} V_\mu V^\mu (v_0 h + \frac{1}{2} h^2), \quad (3)$$

$$\mathcal{L}_\chi \supset \frac{1}{2} \bar{\chi} (i\not{\partial} - m_\chi) \chi - \frac{1}{2} \frac{\lambda_{h\chi}}{\Lambda_\chi} (\cos \xi \bar{\chi} \chi + \sin \xi \bar{\chi} i\gamma_5 \chi) (v_0 h + \frac{1}{2} h^2). \quad (4)$$

**Note:**  $\xi = 0, \pi (\pi/2) \implies$  pure scalar (pseudo-scalar) interaction.

- Free model parameters:  $m_V, \lambda_{hV}$  (Vector DM);  $m_\chi, \lambda_{h\chi}/\Lambda_\chi$  and  $\xi$  (Majorana fermion DM).

<sup>1</sup>Similar for a Dirac fermion field  $\psi$ .



# Constraints

## Observational constraints

- Thermal relic density;
- Higgs invisible decays;
- Indirect detection using  $\gamma$  rays;
- Direct detection, e.g., XENON1T, LUX;
- Solar DM capture and annihilation.

## Theoretical constraints

- Perturbative unitarity of  $VV \rightarrow hh$  scattering amplitudes,
- EFT validity of Majorana fermion DM model,

$$0 \leq \lambda_{hV} \leq \frac{2m_V^2}{v_0^2}.$$

$$\frac{\lambda_{h\chi}}{\Lambda_\chi} < \frac{4\pi}{2m_\chi}.$$

Include 7 important Standard Model (SM), nuclear and astrophysical *nuisance parameters*.



# Free model and nuisance parameters

Model	Parameter	Minimum	Maximum	Prior type
Vector DM	$\lambda_{hV}$	$10^{-4}$	10	Log
	$m_V$ (low mass)	45 GeV	70 GeV	Flat
	$m_V$ (high mass)	45 GeV	10 TeV	Log
Majorana/Dirac DM	$\lambda_{h\chi, h\psi} / \Lambda_{\chi, \psi}$	$10^{-6} \text{ GeV}^{-1}$	$1 \text{ GeV}^{-1}$	Log
	$\xi$	0	$\pi$	Flat
	$m_{\chi, \psi}$ (low mass)	45 GeV	70 GeV	Flat
	$m_{\chi, \psi}$ (high mass)	45 GeV	10 TeV	Log

**Table 1:** Free model parameter ranges and priors.

Parameter		Value ( $\pm$ Range)
Local DM density	$\rho_0$	0.2–0.8 $\text{GeV cm}^{-3}$
Most probable speed	$v_{\text{peak}}$	240 (24) $\text{km s}^{-1}$
Galactic escape speed	$v_{\text{esc}}$	533 (96) $\text{km s}^{-1}$
Nuclear matrix element	$\sigma_s$	43 (24) MeV
Nuclear matrix element	$\sigma_l$	50 (45) MeV
Higgs pole mass	$m_h$	124.1–127.3 GeV
Strong coupling	$\alpha_s^{\overline{\text{MS}}}(m_Z)$	0.1181 (33)

**Table 2:** 7 SM, nuclear and astrophysical parameters varied simultaneously in our scans.

