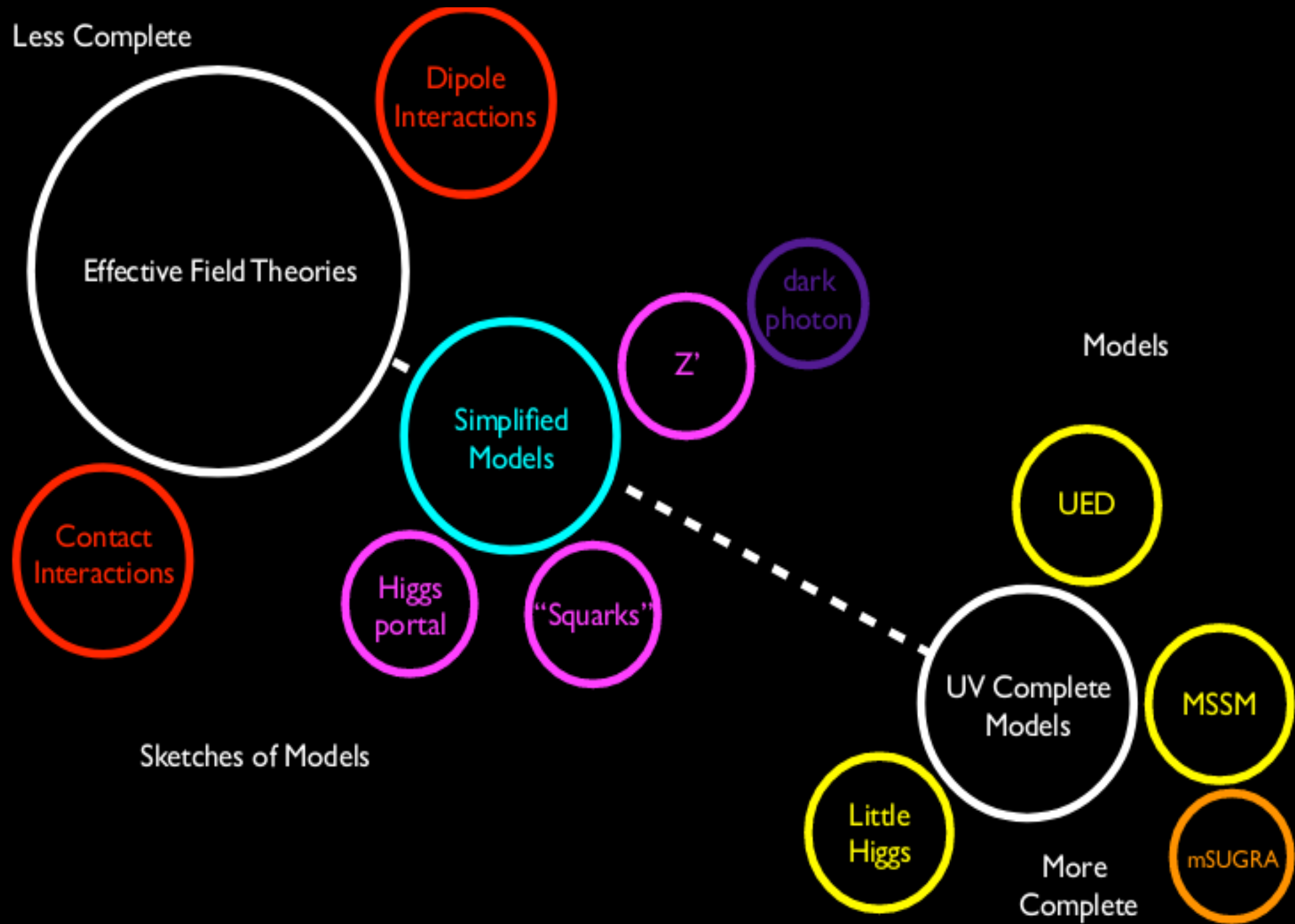


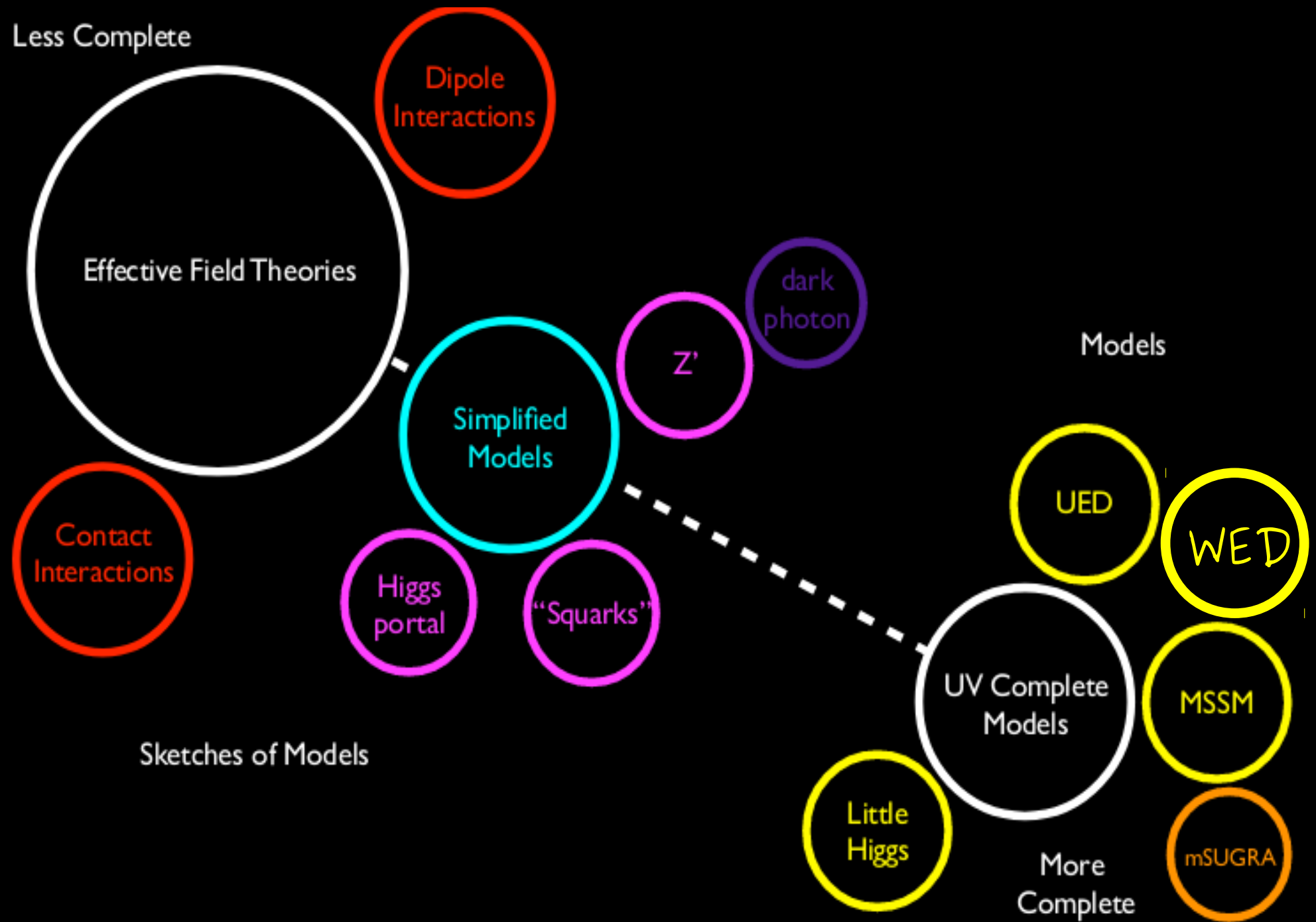
The warped dark sector

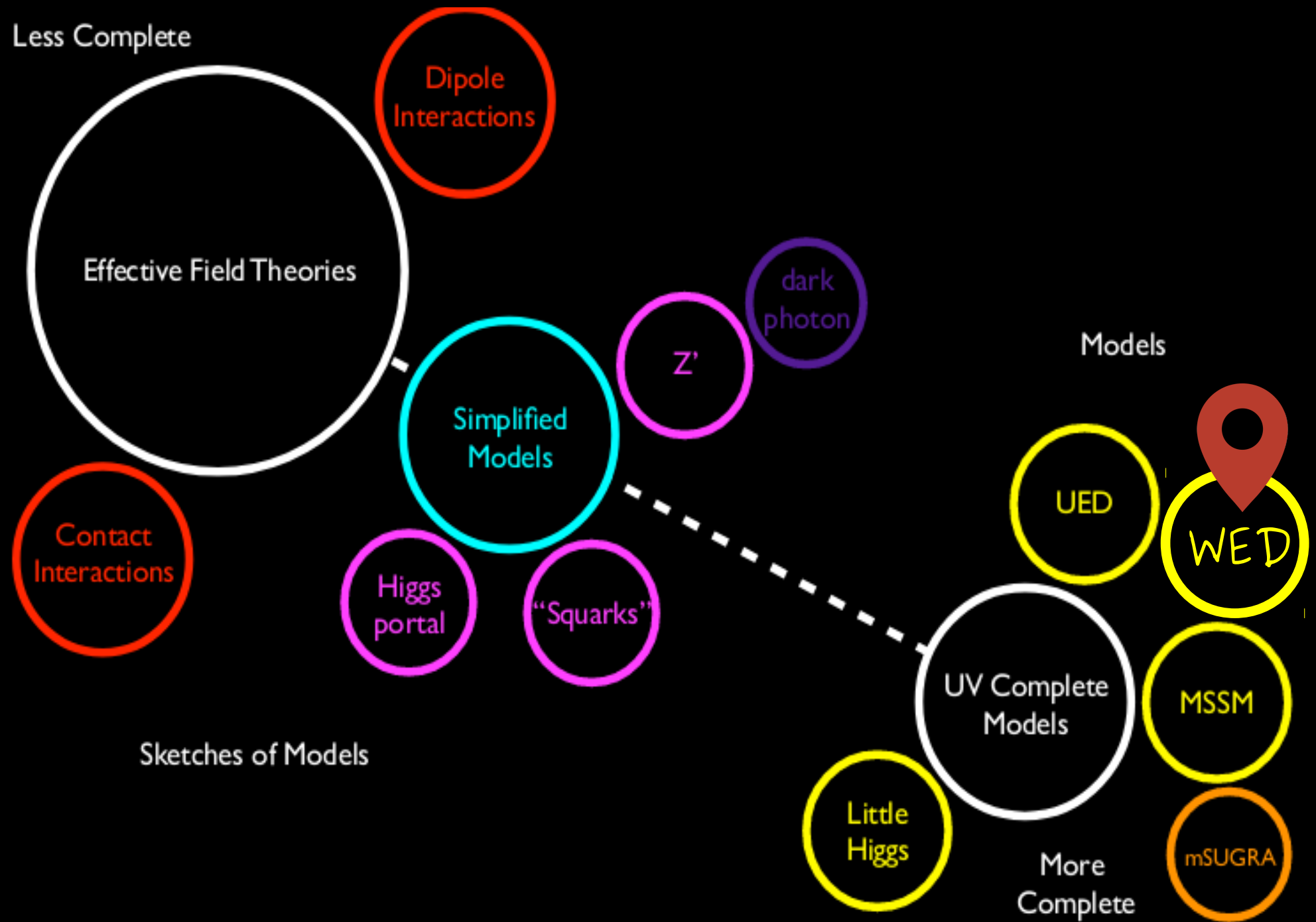
Sylvain Fichet
Caltech, ICTP/SAIFR

Based on

1906.02199 (with P. Brax, F. Tanedo)



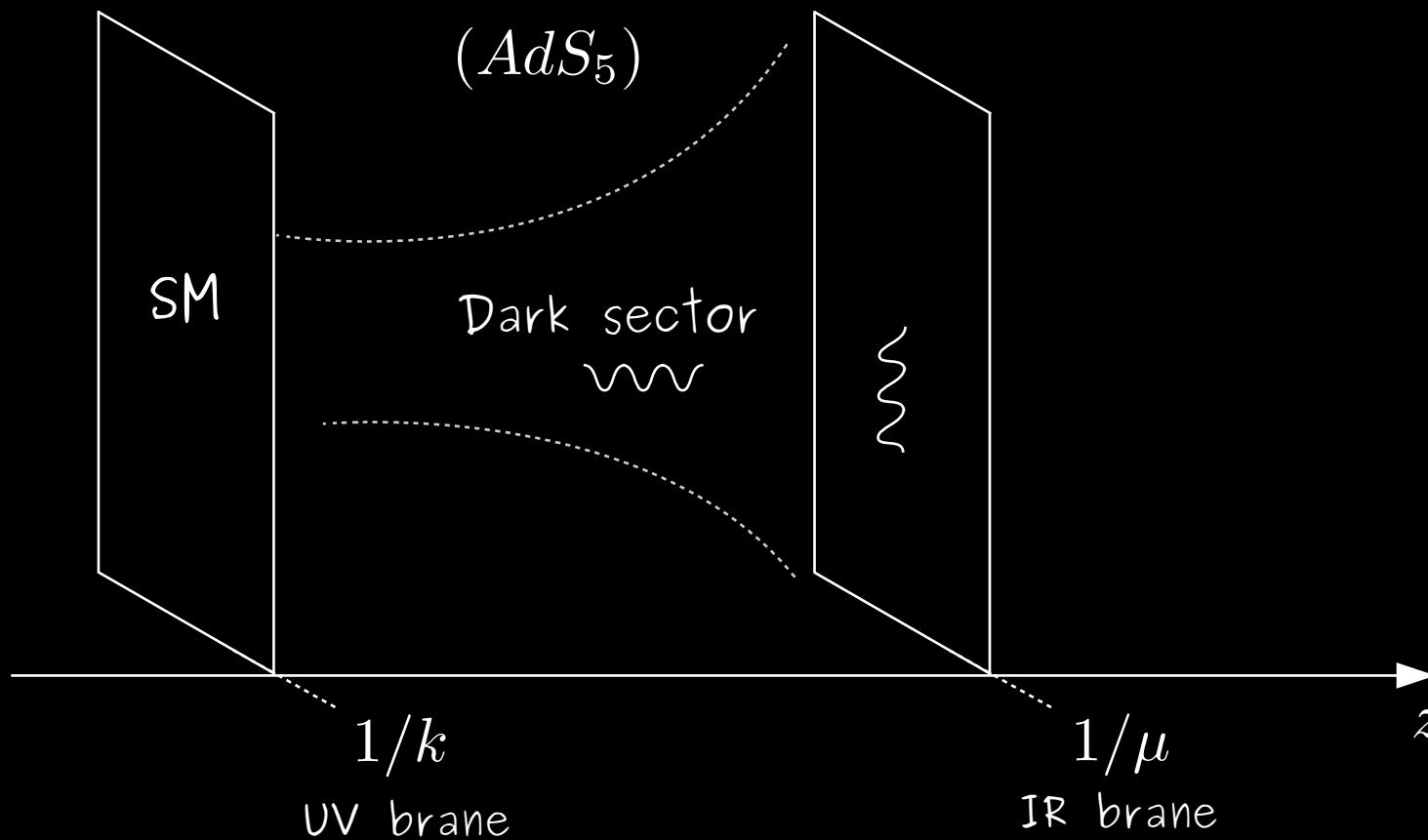




Today's focus

- Only the big picture, nothing too technical
- Will highlight aspects of the model relevant for the topics discussed at the workshop. Right now these aspects are not very developed, but this is an opportunity for further discussion/work

The warped dark sector



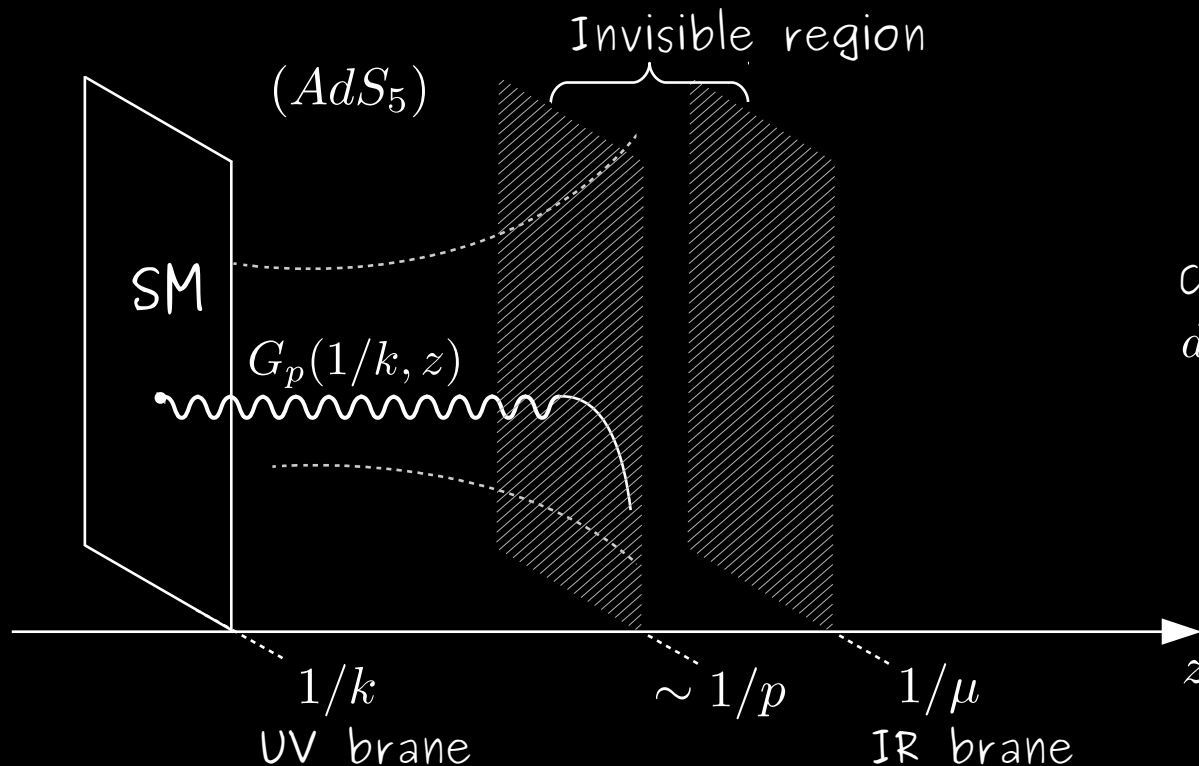
Metric (conformal coordinates): $ds^2 = (kz)^{-2}(\eta_{\mu\nu}x^\mu x^\nu - dz^2)$

Some context

- Not like a Randall-Sundrum model
- Reminiscent of braneworlds (RSII), but here with bulk matter and an IR brane.
- Recent dark sector works with flat extra dimensions [Rizzo '18, '19]...
- Only a few works exist in warped extra dimensions
[von Harling/McDonald '12, McDonald '12, McDonald/Morrisey '11, '12]
- Extra motivation: the model is the AdS dual of a 4d strongly interacting dark sector

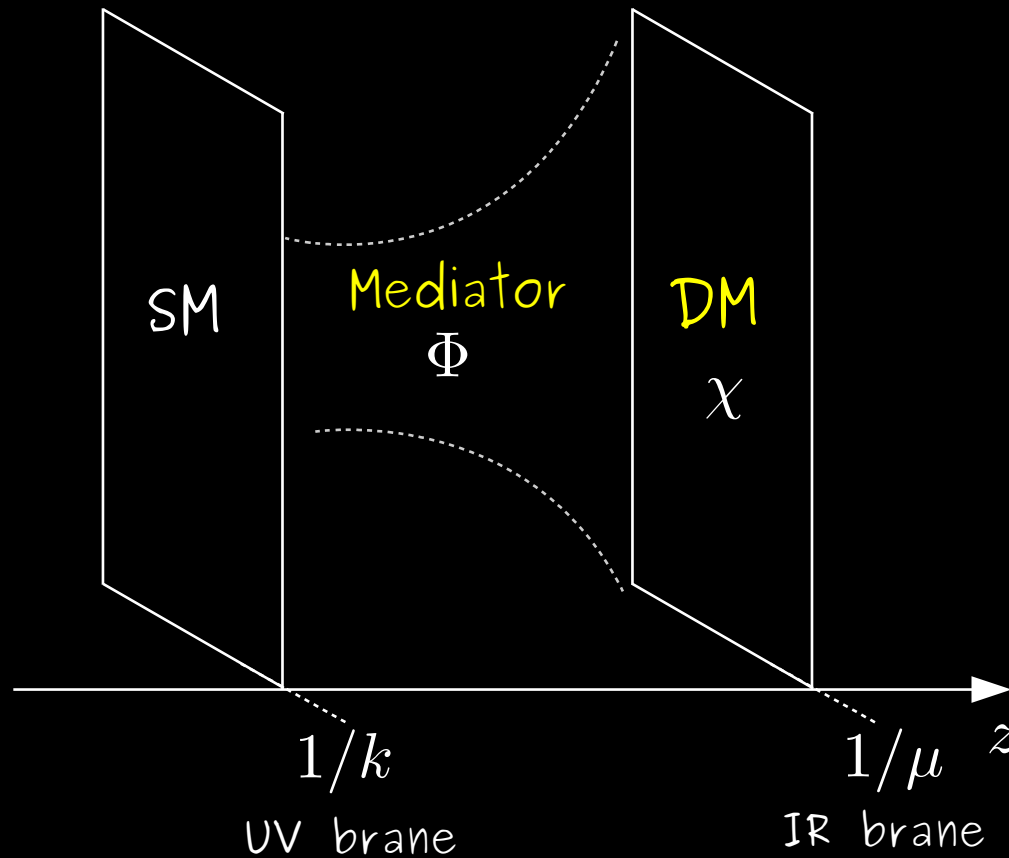
IR opacity

In conformal coordinates, consider UV-brane-to-bulk propagator $G_p(1/k, z)$, with $p = \sqrt{p_\mu p^\mu}$. In the IR region $p \gtrsim 1/z$, $G_p(1/k, z)$ is **exponentially suppressed**. [Gherghetta/Pomarol '03, SF '19]



Hence any field/operator localized near the IR brane is effectively “**emergent**” from the UV-brane standpoint. (No such effect in flat space)

Dark matter model



IR scale μ sets the dark sector mass scale and is the main parameter

To be concrete:

SM = quarks

Φ = scalar

χ = Dirac

$\mathcal{O}_{\text{SM}} = \bar{N}N(\bar{q}q)$

$\mathcal{O}_{\text{D}} = \bar{\chi}\chi$

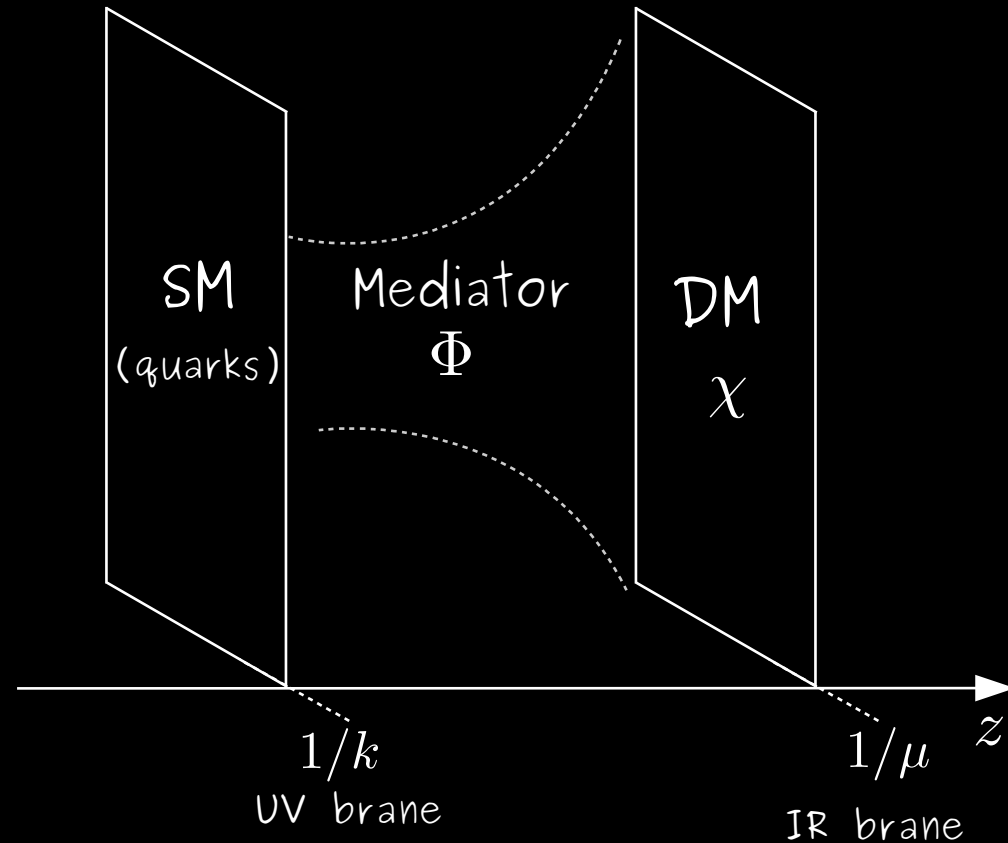
$k \sim M_{\text{Pl}}$

$$S \supset \int_{\text{bulk}} d^5 X \sqrt{|g|} \left(\frac{1}{2} \partial_M \Phi \partial^M \Phi - \frac{m_\Phi^2}{2} \Phi^2 \right) + \int_{\text{UV}} d^4 X \sqrt{|\gamma|} \left(\mathcal{L}_{\text{SM}} + \frac{\lambda}{\sqrt{k}} \mathcal{O}_{\text{SM}} \Phi - \frac{m_{\text{UV}}}{2} \Phi^2 \right) + \int_{\text{IR}} d^4 X \sqrt{|\gamma|} \left(\mathcal{L}_{\text{IR}} + \frac{\kappa}{\sqrt{k}} \mathcal{O}_{\text{D}} \Phi - \frac{m_{\text{IR}}}{2} \Phi^2 \right).$$

Dark matter model

- Low-energy (i.e. 4d) regime $|p| < \mu$

KK modes of Φ are integrated out, giving a familiar 4d **DM effective theory**, with $O(\mu)$ cutoff.



$$\text{4d EFT: } \mathcal{L}_{4d} \sim \lambda^2 \frac{\varepsilon^{2-2\alpha}}{\mu^2} (\mathcal{O}_{\text{SM}})^2 + \lambda \kappa \frac{\varepsilon^{1-\alpha}}{\mu^2} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{D}} + \kappa^2 \frac{1}{\mu^2} (\mathcal{O}_{\text{D}})^2 + \dots$$

$$\mathcal{O}_{\text{SM}} = \bar{N}N, \dots$$

$$\lambda, \kappa = O(1)$$

$$\mathcal{O}_{\text{D}} = \bar{\chi}\chi, \dots$$

$$\varepsilon \equiv \mu/k \ll 1 \quad \text{Warp factor. With e.g. } k \sim M_{\text{p}}$$

$$\alpha \in [0, 1] \quad \text{Controls } \Phi \text{ localization. } \alpha = \sqrt{4 + m_{\Phi}^2/k^2}$$

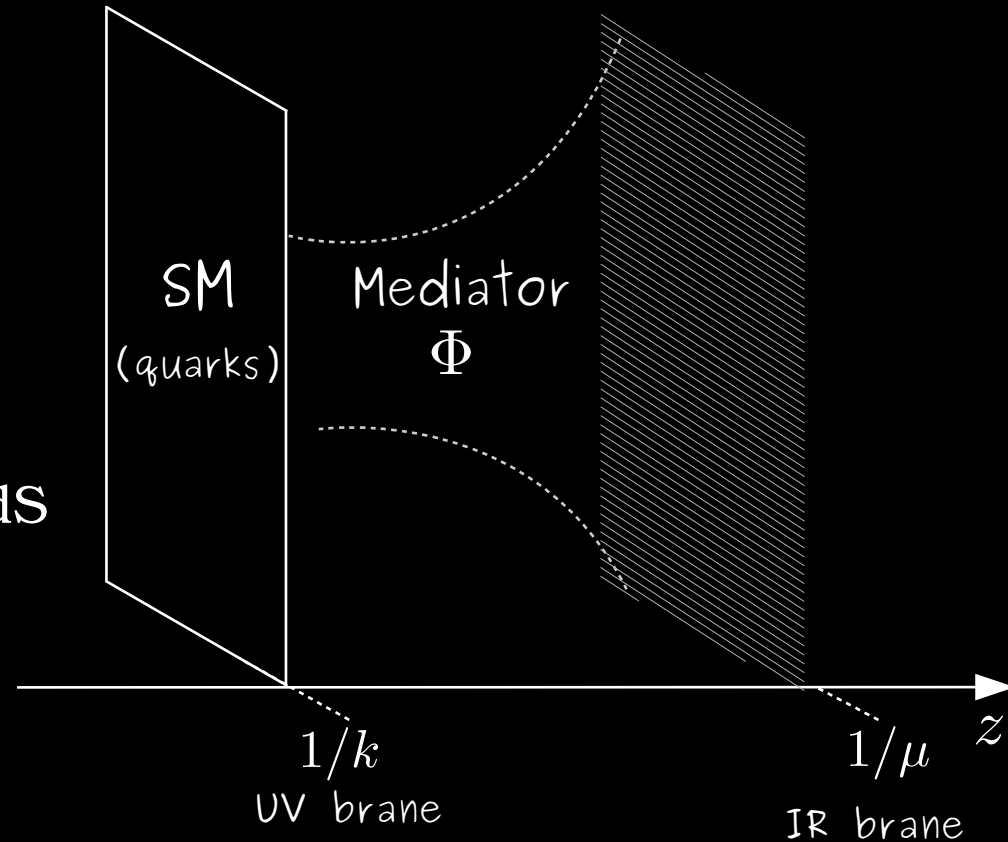
Dark matter model

- High-energy (i.e. 5d) regime $|p| > \mu$

DM **vanishes** from the amplitudes.
Amplitudes can be described by pure AdS with only mediator and SM as dofs,

$$\text{E.g. } \mathcal{A}(N\chi \rightarrow N\chi) \sim e^{-|p|/\mu}$$

for $|p| > \mu$



→ Dark matter observational complementarity is non-standard!

Exact holographic dual:

with $\Delta_{\text{CFT}} = 2 - \alpha$

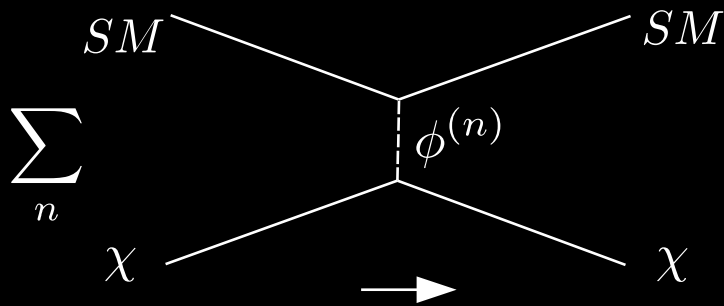
(Δ^- branch, valid for $\alpha \leq 1$)

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{CFT}} + \frac{1}{M^{\Delta_{\text{CFT}}-1}} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{CFT}}$$

Dark matter complementarity

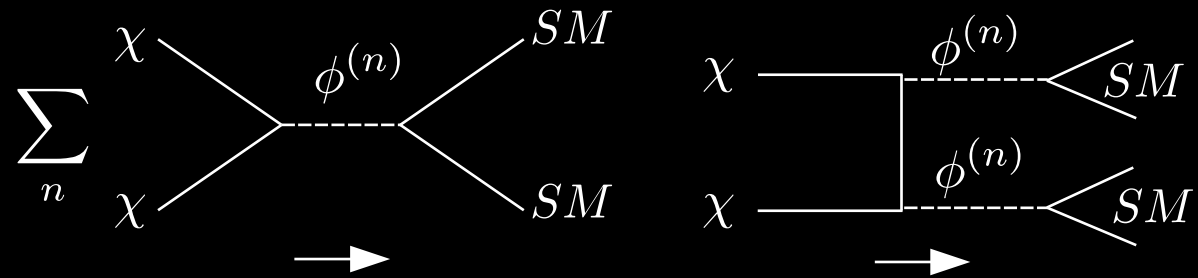
Let's take the 4d viewpoint $\Phi = \sum_n f_n(z) \phi^{(n)}(x^\mu)$. We have a **tower of mediators** (i.e. the KK modes) starting at mass $O(\pi\mu)$. Assume $m_\chi \sim 4\pi\mu$

Direct detection



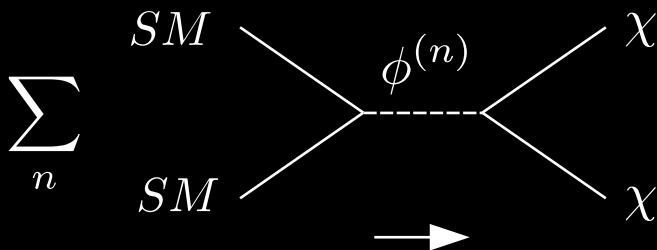
$\sqrt{|t|} < \mu$ hence all mediators are integrated \rightarrow 4d contact interaction

Indirect detection / relic density



$\sqrt{s} \sim \mu$ hence first KK modes can be on-shell

DM production (colliders)

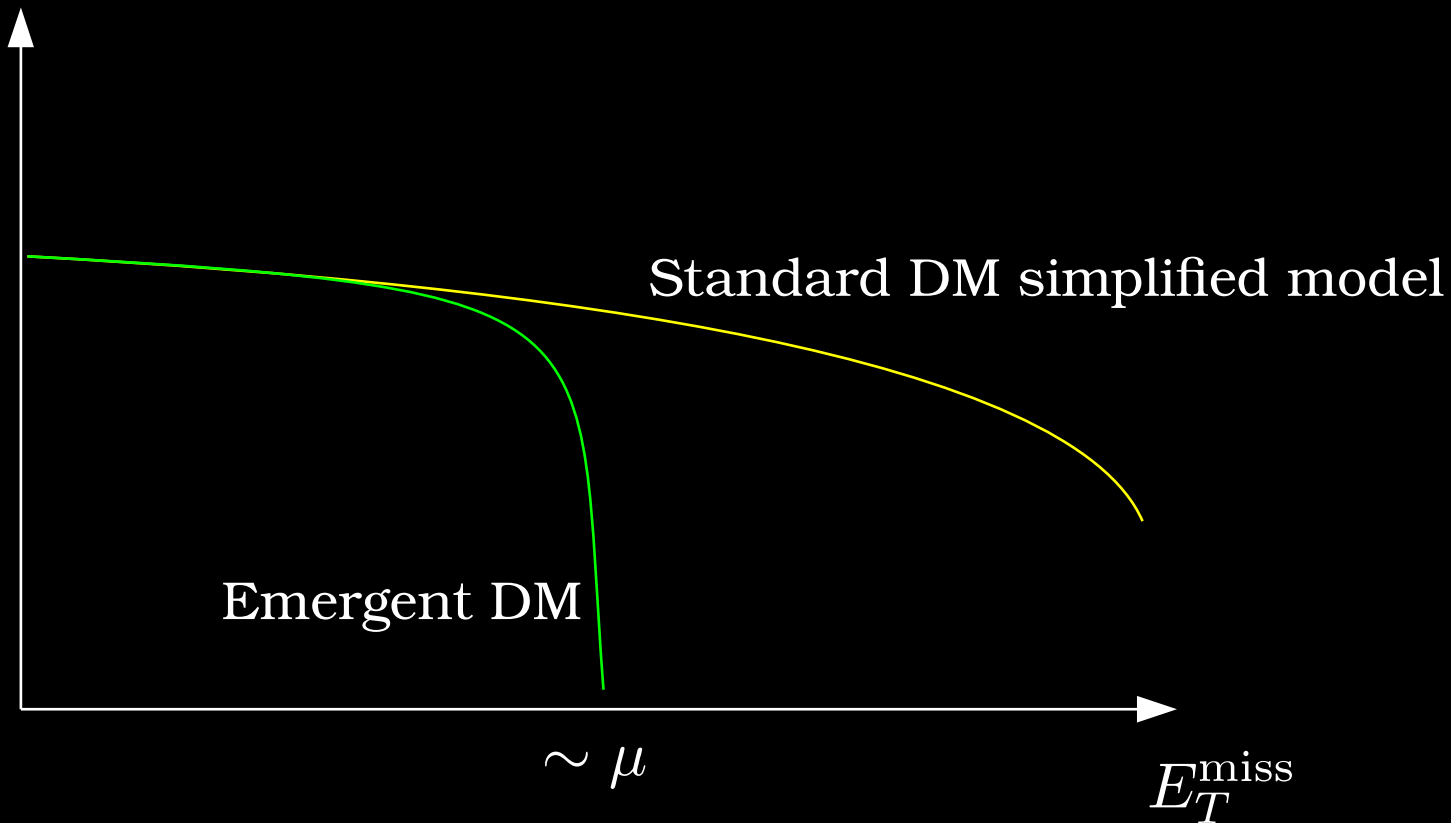


For $\sqrt{s} > \mu$, the mediators conspire such that the **full amplitude is exponentially suppressed**.

Hence one expects suppression of missing energy above the IR scale μ

(more on mediator-only processes in next slides)

Very very roughly:



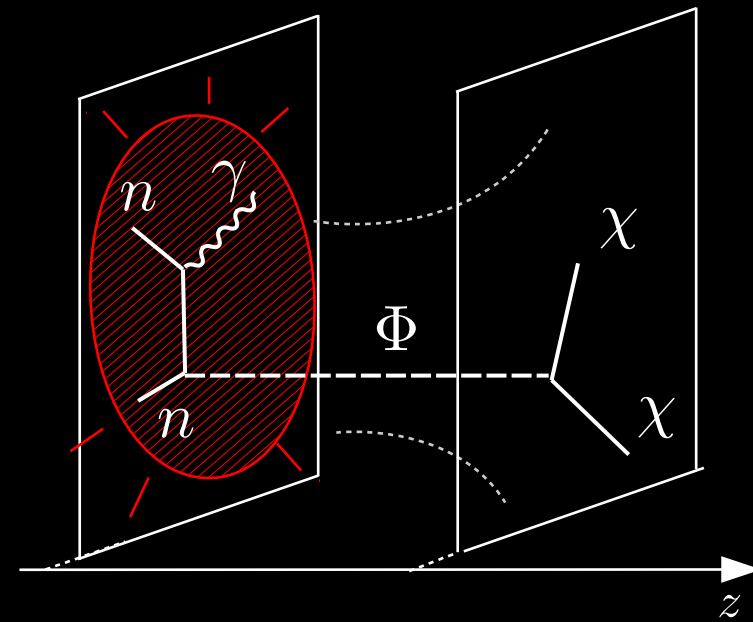
→ An example of behaviour qualitatively different from simplified models/SUSY-like expectations

Some generic signatures

Phenomenology of the warped model is rich and only partly familiar.

Some features:

- Non integer fifth force $V(r) \propto -\frac{k}{(kr)^{3-2\alpha}}$
active for $r < 1/\mu$
- Non-standard momentum losses
(meson decays, star cooling)
- Dark radiation $\rho_d \sim T^4 \left(\frac{T^2}{4k^2}\right)^{1-\alpha}$
for $T > \mu$
- Dark phase transition around $T \sim \mu$

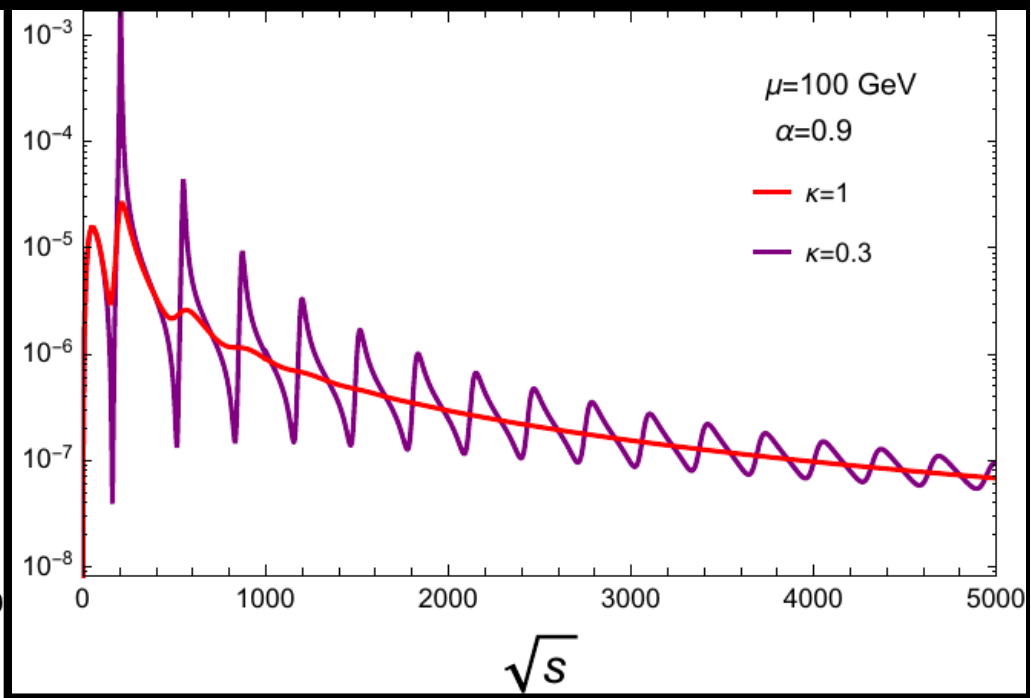
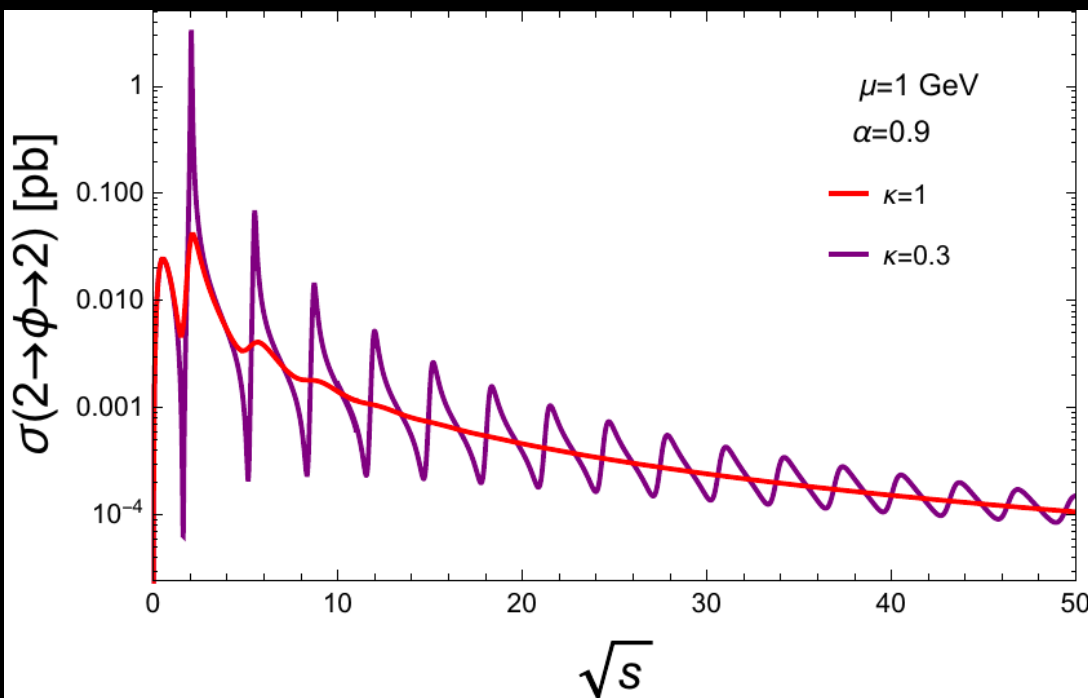
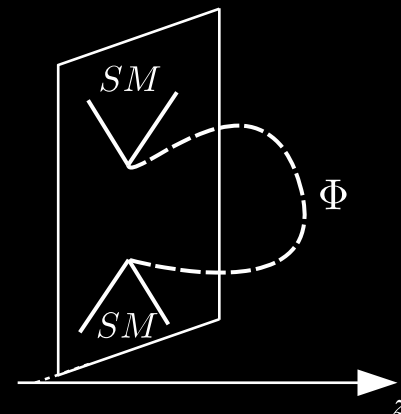


At the LHC: Periodic signals

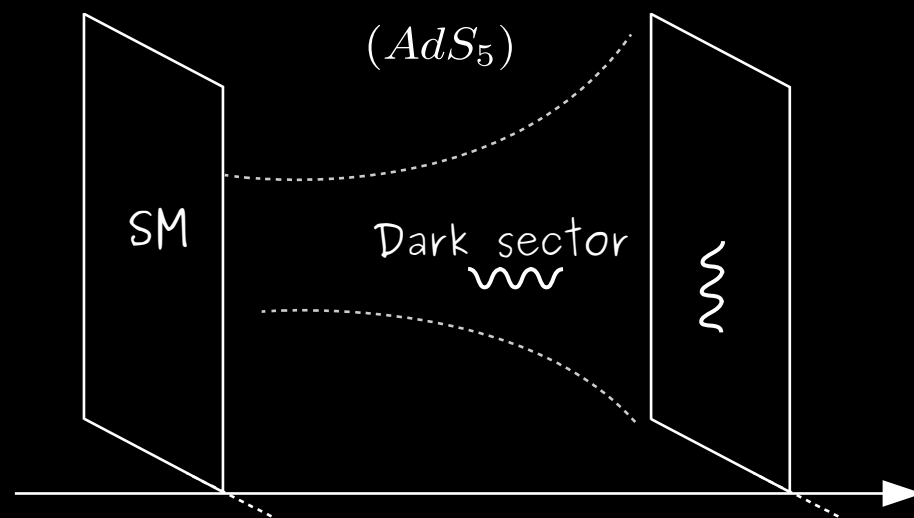
- Collider signals with periodic bumps and dips

(Similar signal pointed out in linear dilaton model [Giudice et al '18])

- Smearing of structures depends on $\kappa = k/M_p$
- Here only the cross section for $|\mathcal{M}_{\text{BSM}}|^2$ is shown
- Search for signal by taking the Fourier transform of the lineshape (recent technical developments in [Beauchesne/Kats '19])

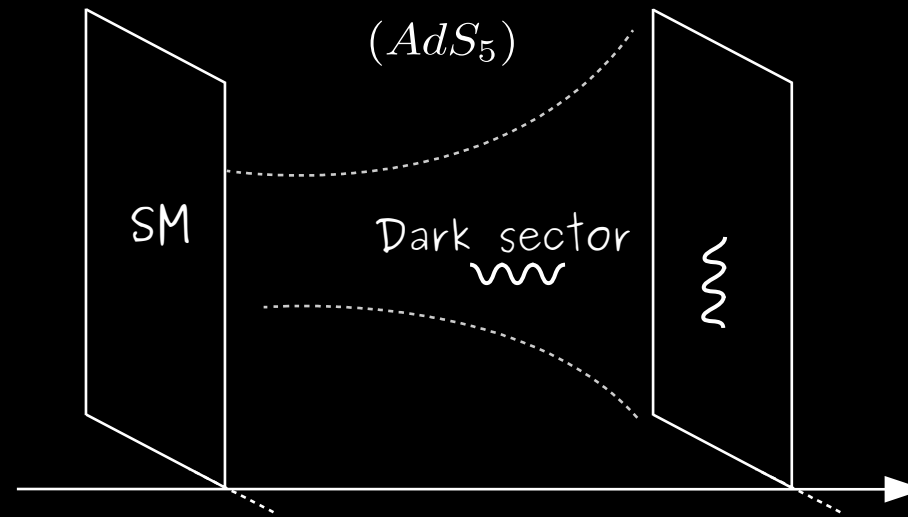


Summary and outlook



- A warped extradimension naturally gives rise to dark sector physics. A conceptually simple possibility, which is further motivated as the AdS dual of a composite dark sector.
- If DM is on IR brane, it is effectively “emergent”: At high-energy it vanishes from all amplitudes as a result of IR opacity. This implies non-standard DM complementarity.
- Model features a variety of “exotic” signatures. At the LHC, periodic signals and vanishing of E_T^{miss} above IR scale

Summary and outlook

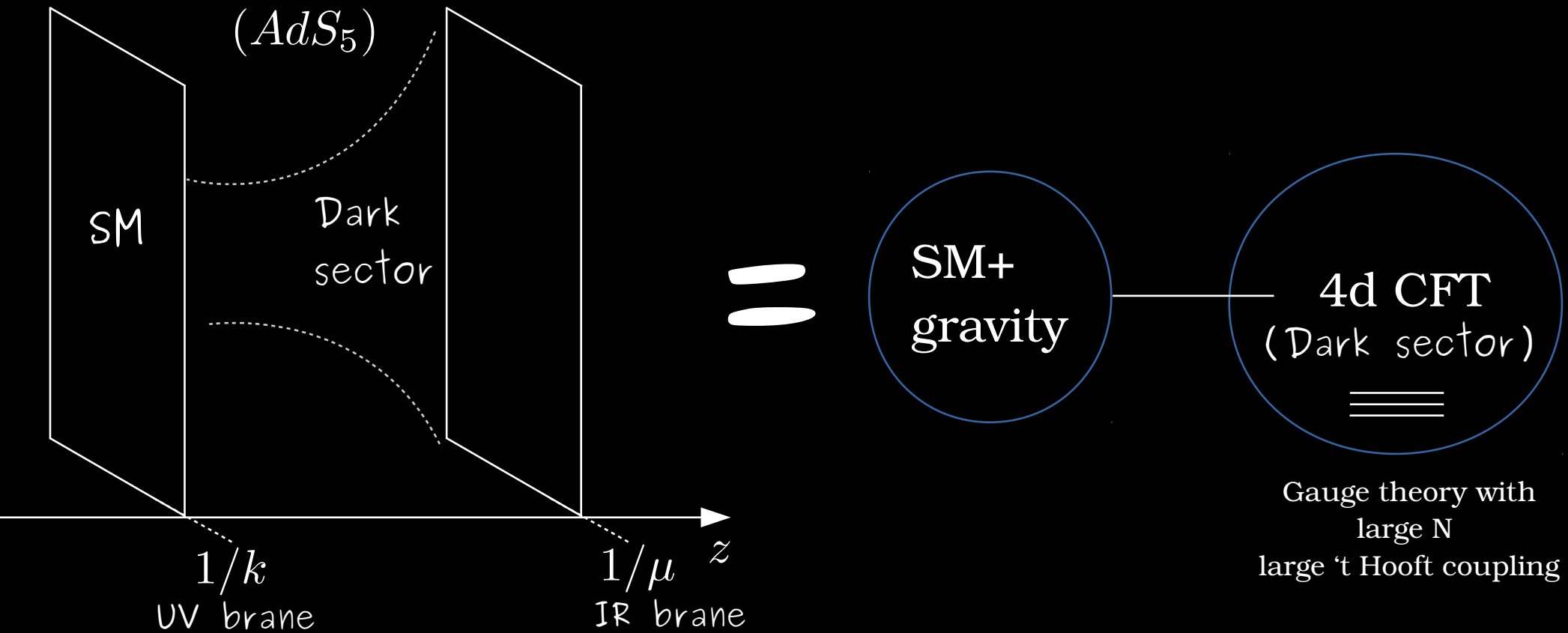


- Many important developments remain to be done, both on theoretical and phenomenological sides. The next papers on our to-do list are about
 - dark photon
 - dark radiation (cosmology)
 - screened modified gravity
 - more phenomenology: leptophilic case, stellar bounds, ...
- A collider-oriented study, for instance using the recent developments from [\[Beauchesne/Kats '19\]](#), would be very welcome!
Let me know if you are interested

THANKS

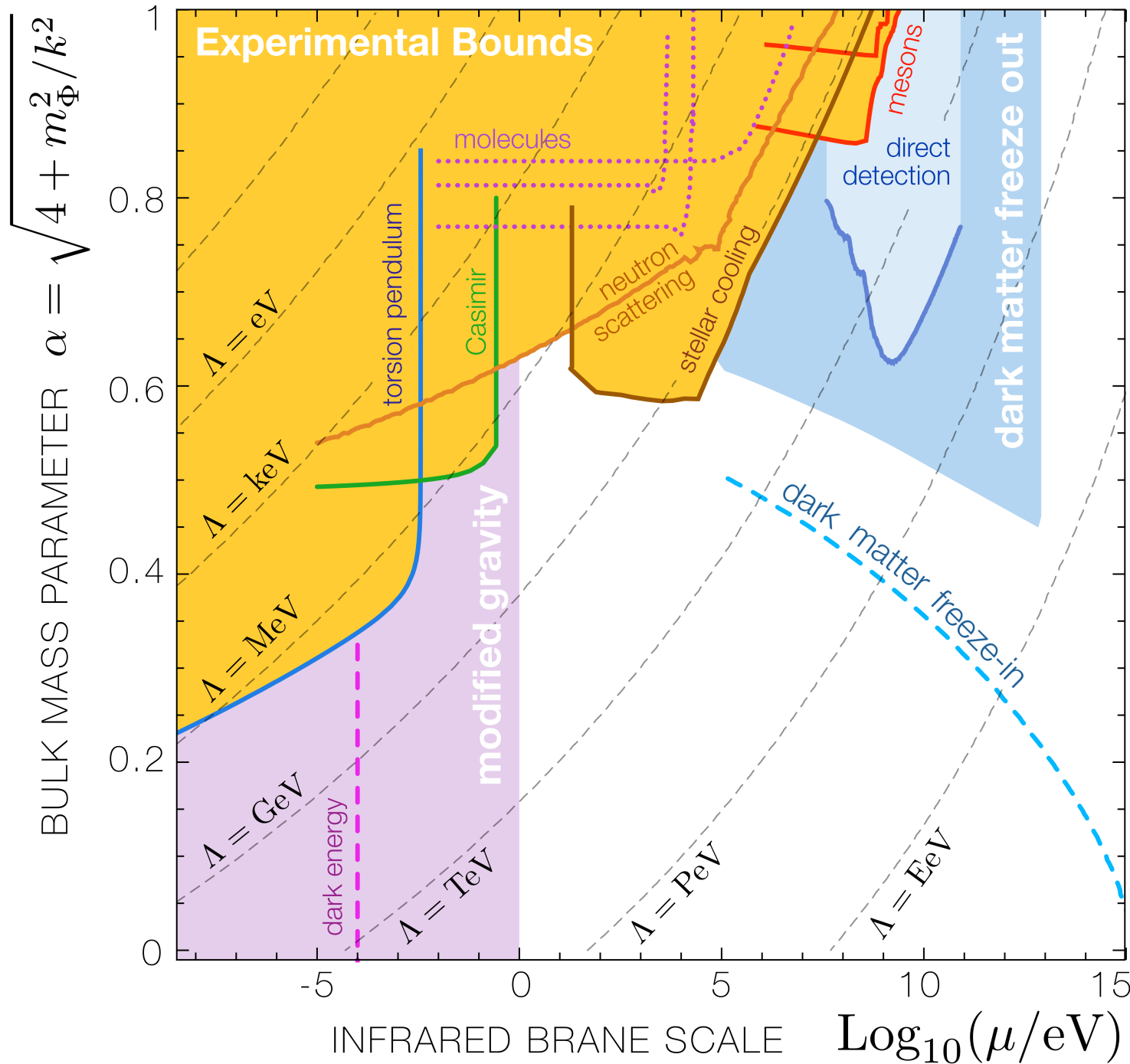
More

Duality



AdS model is the holographic description of a strongly interacting dark sector with IR confinement scale at $\sim \mu$.

Bounds in hadronic case



Λ^{-2} is the low-energy SM-DS effective coupling

$$\mathcal{L} \supset \frac{1}{\Lambda^2} \bar{N} N \bar{\chi} \chi$$

Cutoff of the low-energy 4d EFT is $O(\mu)$

μ and Λ can be very low and still evade bounds

Some formalism

5d action (an exact slice of AdS):

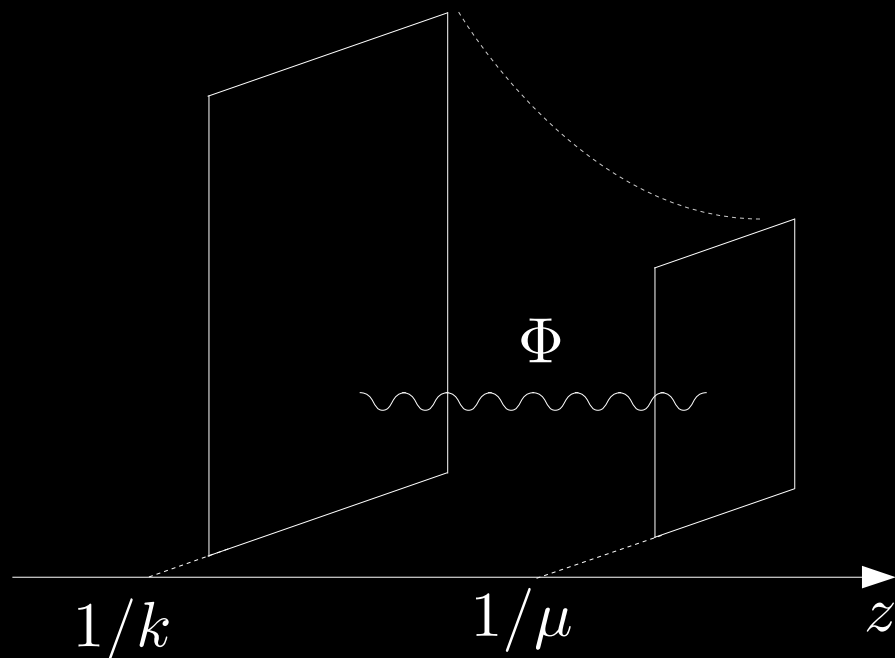
$$S_{\text{AdS}} = \int d^5 x^M \sqrt{g} \left(\frac{1}{2} \nabla_M \Phi \nabla^M \Phi - \frac{1}{2} m_\Phi^2 \Phi^2 \right) + S_{\mathcal{B}} + S_{\text{int}}$$

Metric (conformal coordinates):

$$ds^2 = g_{MN} dx^M dx^N = (kz)^{-2} (\eta_{\mu\nu} x^\mu x^\nu - dz^2)$$

Brane mass terms:

$$S_{\mathcal{B}} = \int d^5 x^M \sqrt{g} \frac{1}{2} (\delta(z - z_0) M_{\text{UV}} - \delta(z - z_1) M_{\text{IR}}) \Phi^2$$



Some definitions:

$$z_0 = 1/k, \quad z_1 = 1/\mu$$

$$M_{\text{UV}} = (\alpha - 2)k - b_{\text{UV}}k,$$

$$M_{\text{IR}} = (\alpha - 2)k + b_{\text{IR}}k.$$

spectrum has a massless mode for

$$b_{\text{UV}} = b_{\text{IR}} = 0, \quad 2\alpha$$

Some formalism

Green function:

$$\langle \hat{\Phi}(z) \hat{\Phi}(z') \rangle \equiv iG_p(z, z') = i \frac{\pi k z z'}{2} \frac{\left[\tilde{Y}_\alpha^{\text{UV}} J_\alpha(pz_{<}) - \tilde{J}_\alpha^{\text{UV}} Y_\alpha(pz_{<}) \right] \left[\tilde{Y}_\alpha^{\text{IR}} J_\alpha(pz_{>}) - \tilde{J}_\alpha^{\text{IR}} Y_\alpha(pz_{>}) \right]}{\tilde{J}_\alpha^{\text{UV}} \tilde{Y}_\alpha^{\text{IR}} - \tilde{Y}_\alpha^{\text{UV}} \tilde{J}_\alpha^{\text{IR}}}$$

Structure of the propagator in different regions, away from the poles:

$$p < \mu \quad G_p(z, z') = f(z, z', b_{\text{UV}}, b_{\text{IR}}) \quad (+ \text{ possible light mode})$$

Holomorphic

Contact interaction

Encodes heavy KK modes

b_{IR} dependence vanishes for $z_{>} < 1/\mu$

Has branch cut

Encodes light continuum of KK modes

CFT-like

$$\mu < p < \frac{1}{z_{>}}$$

$$G_p(z, z') = f(z, z', b_{\text{UV}}, 0) + h(z, z', b_{\text{UV}}) p^{2\alpha}$$

$$\frac{1}{z_{>}} < p < \frac{1}{z_{<}}$$

$$G_p(z, z') = j(z, z', b_{\text{UV}}) \frac{\cos\left(\frac{p}{\mu} - pz_{>}\right)}{\cos\left(\frac{p}{\mu} + \frac{\pi}{4}(1 - 2\alpha)\right)}$$

Exponentially suppressed
if p has imaginary part

A KK continuum trick

It can be often useful to think in terms of Kaluza Klein modes,

$$G_p(z, z') = \sum_{n=0}^{\infty} \frac{f_n(z) f_{n'}(z')}{p^2 - m_n^2}$$

But a sum over KK modes can be tricky to perform. Consider for instance, KK mode emission from the brane,

$$\sum_{n=0}^{n_{\text{th}}} \int d\Phi_2 \left| \begin{array}{c} \text{---} \\ \text{---} \end{array} \right. \left. \begin{array}{c} \phi^{(n)} \\ \text{---} \end{array} \right| \equiv \sum_{n=0}^{n_{\text{th}}} f_n(z_0)^2 \Gamma_n = ?$$

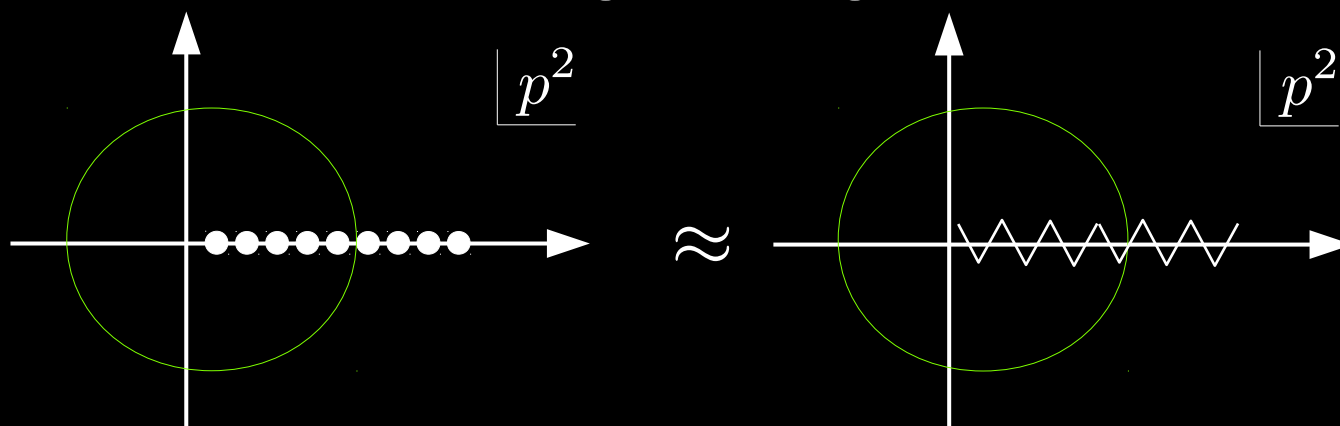
A KK continuum trick

Trick: re-express the sum as a contour integral of the propagator, enclosing the poles allowed by the process.

$$\sum_{n=0}^{n_{\text{th}}} \int d\Phi_2 \left| \text{---} \text{---} \phi^{(n)} \right|^2 \equiv \sum_{n=0}^{n_{\text{th}}} f_n(z_0)^2 \Gamma_n$$

$$= \frac{1}{2i\pi} \int_{\mathcal{C}[n_{\text{th}}]} d\rho \Gamma(\sqrt{\rho}) G_{\sqrt{\rho}}(z_0, z_0)$$

Then, evaluate the contour integral using the explicit expression for G_p



The contact term does not contribute. Main contribution comes from the non-holomorphic $p^{2\alpha}$ term. This provides a very simple way to perform KK sums.

Dressed propagator

The dressed propagator satisfies the “dressed EOM”:

$$\frac{1}{\sqrt{g}} \partial_M (g^{MN} \sqrt{g} \partial_N \Delta(X, X')) + \int dY \underset{\uparrow}{\Pi(X, Y)} \Delta(Y, X') = -i \frac{1}{\sqrt{g}} \delta^{(d)}(X).$$

The 1PI subdiagram.

Contains the bulk mass $\Pi(X, X') \supset M^2 \delta^{(d)}(X - X')$

$$\Delta(X, X') = \text{---} + \text{---} \text{---} \textcircled{i\Pi} \text{---} + \dots$$

Our interest is in the imaginary part induced by bulk interactions. Let us first consider a cubic scalar interaction λ . Focussing on the potentially exponentially suppressed regime $1/z_{>} < p$, we get (using the continuum trick)

$$\text{Im}\Pi(z, z') \approx \lambda^2 \frac{1}{k^6 z^3 z'^3} \frac{1}{64\pi^3} \frac{\pi^2 k^2}{\Gamma^2(\beta + 1)\Gamma^2(\beta + 2)} \left(\frac{z_{<}}{2z_{>}} \right)^{4\beta+2}$$

Dressed propagator

Then let us consider a narrow width expansion:

$$\Pi(z, z') = F_0(z)\delta(z, z') - F_1(z)\delta^{(1)}(z, z') + \frac{1}{2}F_2(z)\delta^{(2)}(z, z') + \dots$$

where $F_i(z) = \int dz' z'^i \Pi(z, z')$

($F_i(z)/F_0(z)$ are the moments of the distribution)

Results take the form

$$F_0(z) = \lambda^2 k C_0 \frac{1}{(kz)^5}, F_1(z) = \lambda^2 C_1 \frac{1}{(kz)^4}, F_2(z) = \frac{\lambda^2}{k} C_2 \frac{1}{(kz)^3},$$

C_0 gives an imaginary bulk mass

C_1 gives an imaginary bulk mass and some harmless phases

C_2 gives an imaginary part to the 4-momentum!

Hence the propagator with timelike momentum is exponentially suppressed as

$$G_p^{1\text{-loop}}(z, z') \propto e^{-\lambda^2 \frac{C_2}{2k} pz}.$$

Cascade decays

Even though the propagators with timelike momentum cannot access the deep IR, another possibility may be the **cascade decay** of the continuum.

As the field fragments, p reduces and the daughters progressively reach further in the IR.

One finds an approximate recursion relation

$$\int dz dz' d\Phi_3 \left| \text{Diagram 1} \right|^2 \approx a \int d\Phi_2 \left| \text{Diagram 2} \right|^2$$

$$a = \frac{\lambda^2}{k} \frac{\Gamma(-\alpha)^2}{(\Gamma(\alpha+1)\Gamma(\alpha+2))^2} \frac{1}{16\pi^2} \frac{1}{(3\alpha+1)^2} \frac{1}{4^{5\alpha+4}} \ll 1$$

λ is cubic scalar coupling
Uncertainty is likely $O(1)$

This can be used to estimate the rate of a cascade decay:

$$|\mathcal{M}|^2(1 \rightarrow n) \sim a^{2^n - 1}$$

Cascade decays

Moreover, from the KK continuum trick, one has

$$\frac{1}{2i\pi} \int_{\mathcal{C}_{[n_{\text{th}}]}} d\rho \Gamma(\sqrt{\rho}) \underbrace{G_{\sqrt{\rho}}(z, z')}_{\propto \rho^\alpha} \quad \text{which means that decays into heaviest modes are preferred.}$$

(Implies that events will tend to be spherical and soft, same conclusion as [Csaki/Reece/Terning '08])

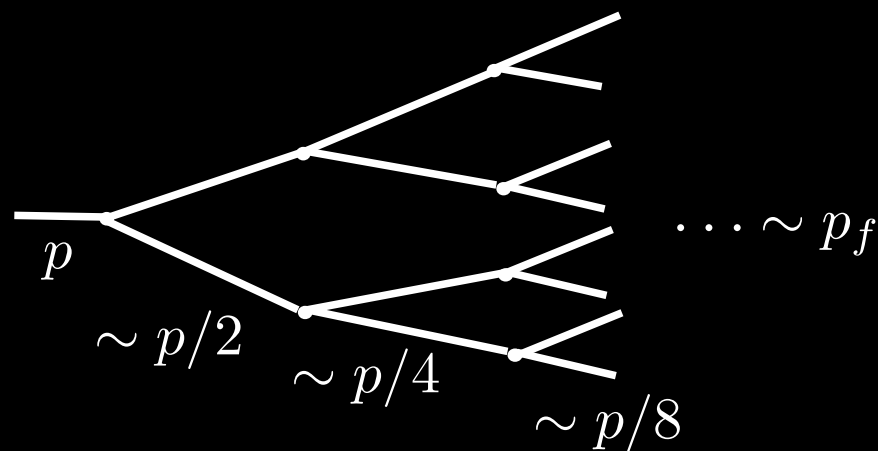
To make a gross estimate, let us consider the most likely phase space configuration,

For final states with momentum $p_f = p/2^n$ we have thus

$$|\mathcal{M}|^2 \sim a^{p/p_f - 1}$$

Since $a \ll 1$, this is a strong exponential suppression.

(The value chosen for p_f depends on the other scales of the object considered (detector, star...), because lifetime of final states depends on p_f)



DM low-energy EFT

At energies $E < \Lambda$

$$\begin{array}{c}
 SM \quad \chi \\
 \diagdown \quad / \\
 \text{[Shaded Circle]} \\
 / \quad \diagdown \\
 SM \quad \chi
 \end{array}
 =
 \begin{array}{c}
 SM \quad \chi \\
 \diagdown \quad / \\
 \text{[White Circle]} \\
 / \quad \diagdown \\
 SM \quad \chi
 \end{array}
 \cdot \left(1 + O\left(\frac{1}{\Lambda}\right) \right)$$

Low-energy effective description based on local operators (DM EFT):

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{DM}} + \frac{1}{\Lambda} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{DM}} + \dots$$

with \mathcal{O}_{DM} bilinear in χ

Interaction described by local operators of higher dimension.

Valid up to $E \sim \Lambda$