

# Proton-Radius Measurement in High-Energy Muon Scattering at COMPASS++/AMBER

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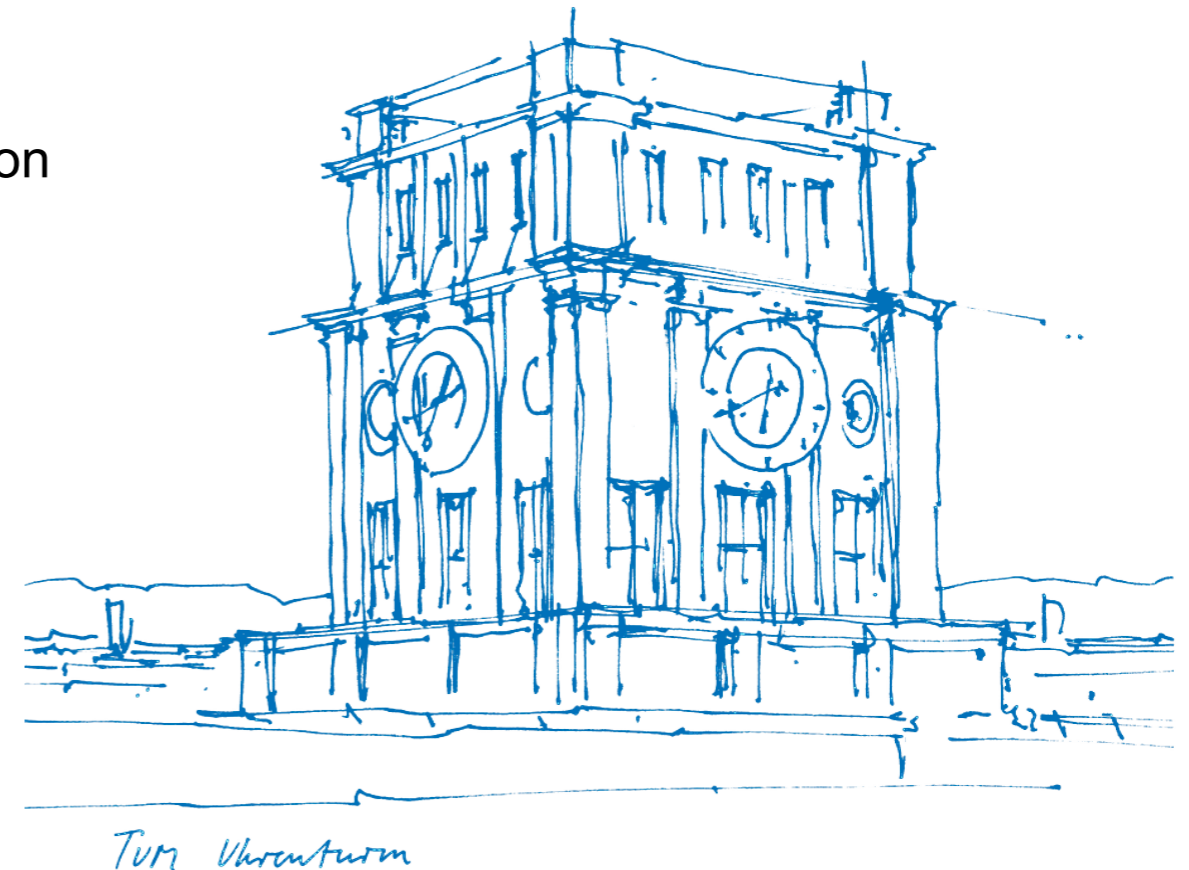
Physics Department

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On behalf of the COMPASS++/AMBER Proto-Collaboration

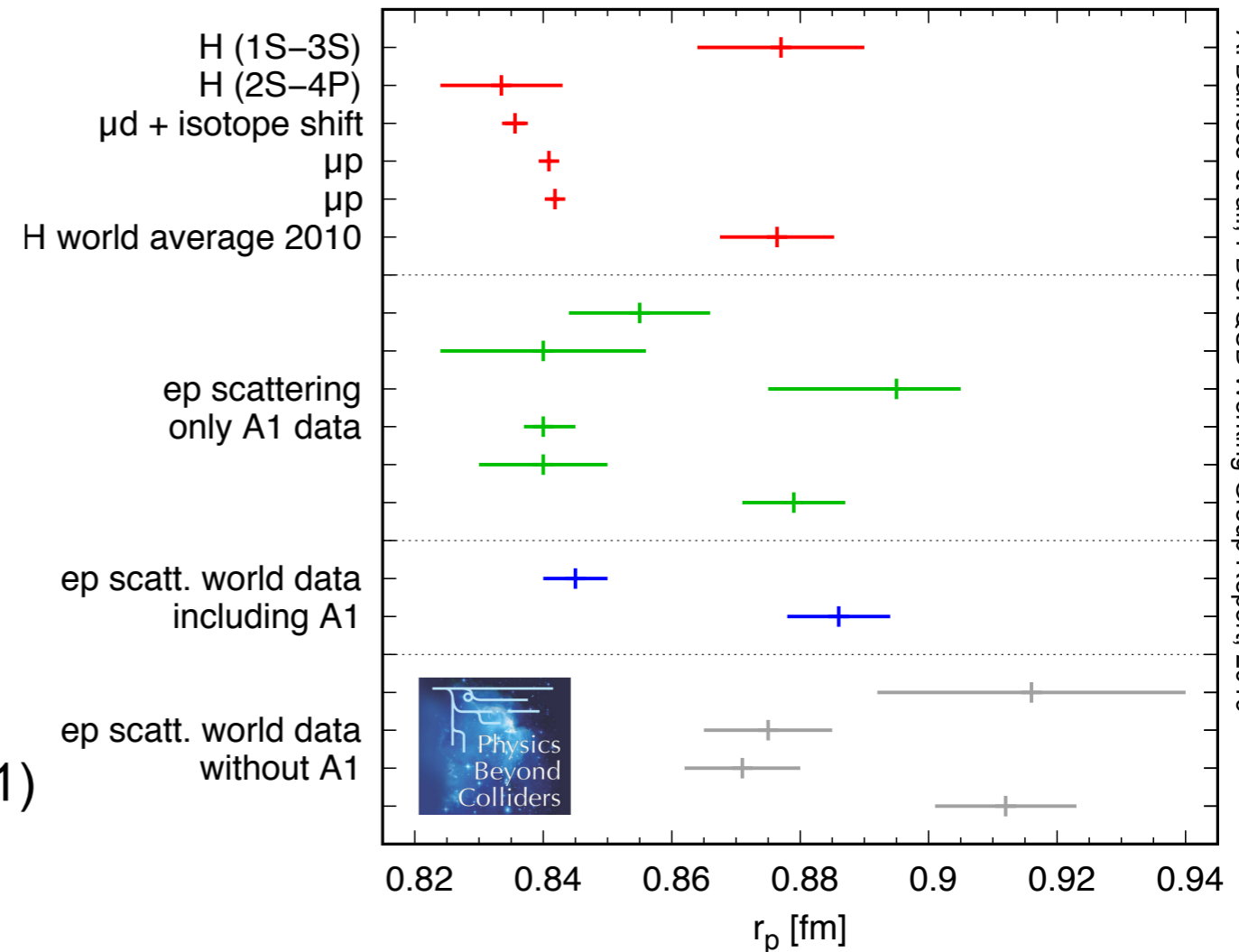


# The Proton-Radius Puzzle

## Data from spectroscopy and e-p scattering

Several experiments with different approaches measured the proton radius with contradicting results.

- Hydrogen spectroscopy:
  - muonic or ordinary hydrogen
  - highest precision using laser spectroscopy
  - favoured value of  $(0.841 \pm 0.01)$  fm
- Electron-hydrogen scattering:
  - measurement using momentum transfer
  - recent data: MAMI A1 (2010) or JLab (2011)
  - favoured value of  $(0.879 \pm 0.008)$  fm
- Two significantly different values obtained
  - the proton-radius puzzle



A. Dainese et al., PBC: QCD Working Group Report, 2019

# Upcoming Experiments Addressing the Puzzle

## New data from lepton-proton scattering

Several proposed and preparing experiments to solve the puzzle in the next years.

- **PRad**: electron-proton with  $E_e = 1.1/2.2$  GeV  
→ data taken in 2016: working on systematics  
→ recent (preliminary) results: smaller value
- **MAMI**: electron-proton with  $E_e < 750$  MeV  
→ two new experiments in preparation
- **MAGIX-MESA**: electron-proton with  $E_e < 150$  MeV  
→ electric and magnetic form factor  
→ new accelerator - start in 2024
- **MUSE**: muon/electron-proton with  $E_{e,\mu} < 140$  MeV  
→ comparison of electron and muon scattering  
→ start of data taking in 2019
- **Missing**: muon-proton with  $E_\mu$  of  $\mathcal{O}(10 - 100)$  GeV  
→ data for high-energy elastic muon-proton scattering  
→ different systematics compared to other

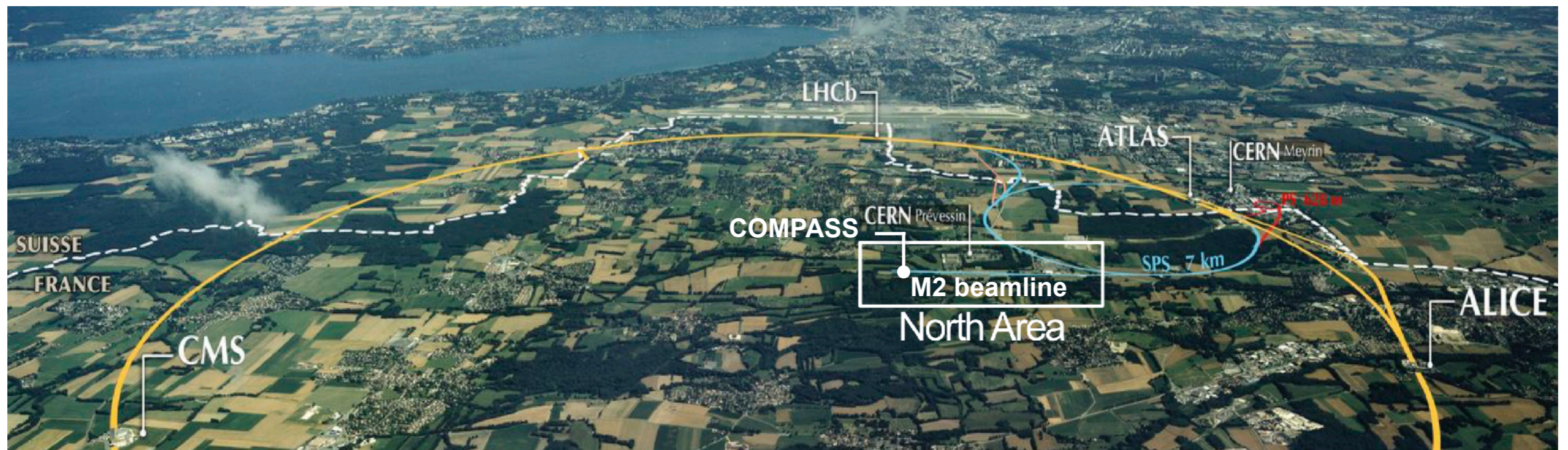
Proton Radius Experiment at Jefferson Lab



# Beamline for High-Energy Muon Beams

## The M2 beamline at CERN's SPS

Located at the North Area of CERN the unique M2 beamline provides a high-intensity muon beam.



- Muon momenta up to 200 GeV/c with a flux up to  $10^7 \mu/s$
- Measurement could be performed at the site of the current COMPASS experiment

# How to Determine the Proton Radius?

## Cross section, form factor, and the proton radius

Measurement of electric form factor allows to calculate proton radius.

- Electric form factor  $G_E$  defines the proton radius at momentum transfer  $Q^2 = 0$ :

$$\langle r_p^2 \rangle = -6\hbar^2 \cdot \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2 \rightarrow 0}$$

- Access to form factors  $G_E^2$  and  $G_M^2$  in Rosenbluth separation of cross section:

$$\frac{d\sigma^{\mu p \rightarrow \mu p}}{dQ^2} = \frac{4\pi\alpha^2}{Q^2} R (\epsilon G_E^2 + \tau G_M^2)$$

$$R = \frac{\vec{p}_\mu^2 - \tau (s - 2m_p^2(1 + \tau))}{\vec{p}_\mu^2(1 + \tau)} \quad \epsilon = \frac{E_\mu^2 - \tau (s - m_\mu^2)}{\vec{p}_\mu^2 - \tau (s - 2m_p^2(1 + \tau))} \quad \tau = \frac{Q^2}{(4m_p^2)}$$

- Suppress magnetic form factor  $G_M^2$ 
  - requires  $\tau \rightarrow 0$
  - Measurement at low- $Q^2$  values of  $\mathcal{O}(<10^{-2})$
- Measurement at high-energy  $\mathcal{O}(10 - 100 \text{ GeV})$ 
  - results in  $\epsilon \rightarrow 1$
  - cross-section directly proportional to  $G_E^2$

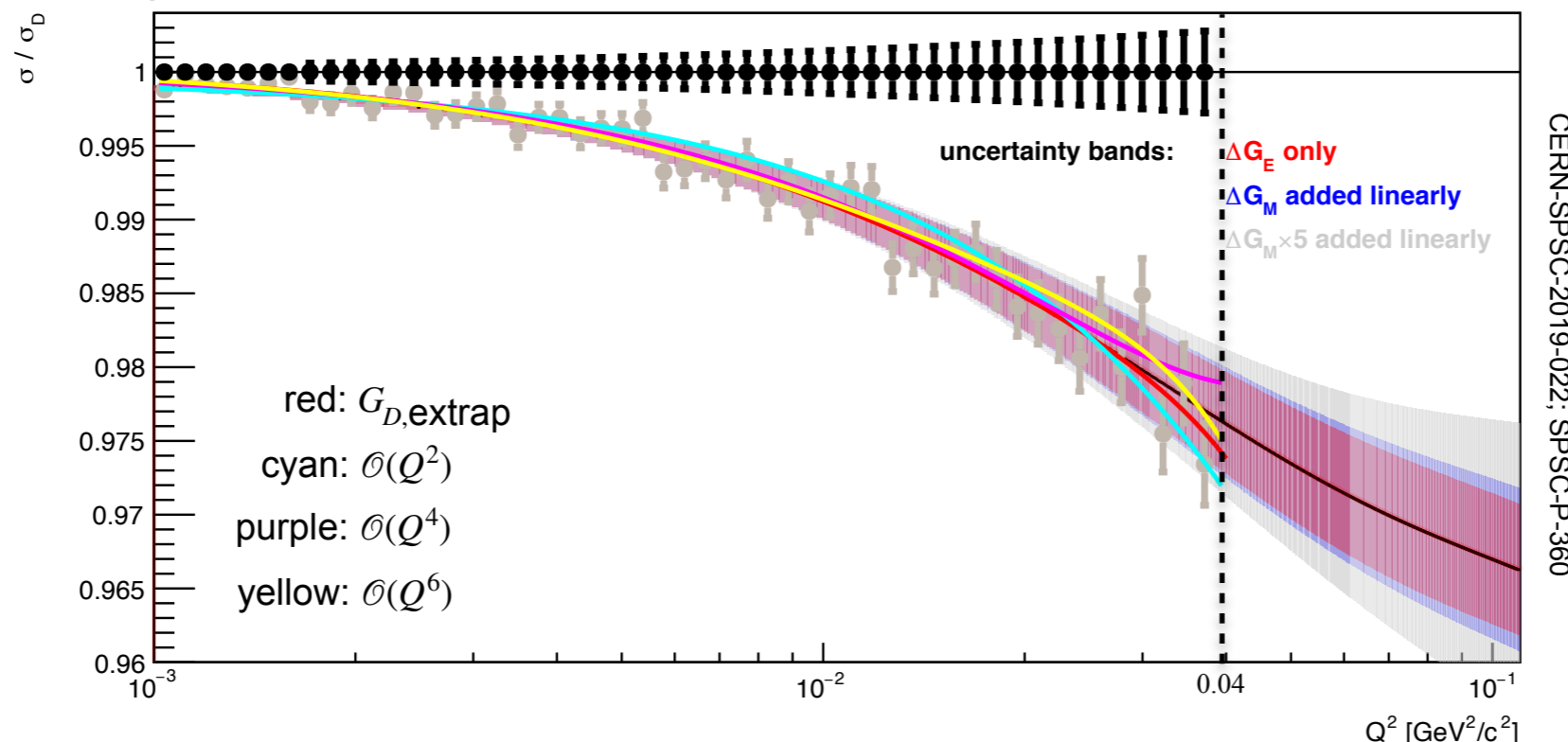
# Proposal of a New Measurement

## High-energy elastic muon-proton scattering

Measurement of the cross section of elastic muon-proton scattering using CERN's M2 beamline at the site of the current COMPASS experiment.

- Measure as close as possible to  $Q^2 = 0$
- Sufficient range to determine radius
  - aimed precision of 1 %
  - aimed  $Q^2$ -range: 0.001 - 0.04  $\text{GeV}^2/c^2$

- Below  $Q^2 = 0.001 \text{ GeV}^2/c^2$ :
  - deviation from point-like proton level of  $\mathcal{O}(10^{-3})$
  - smaller than unavoidable systematic effects
- Above  $Q^2 = 0.04 \text{ GeV}^2/c^2$ :
  - non-linearity of the cross section
  - predominant source of uncertainty

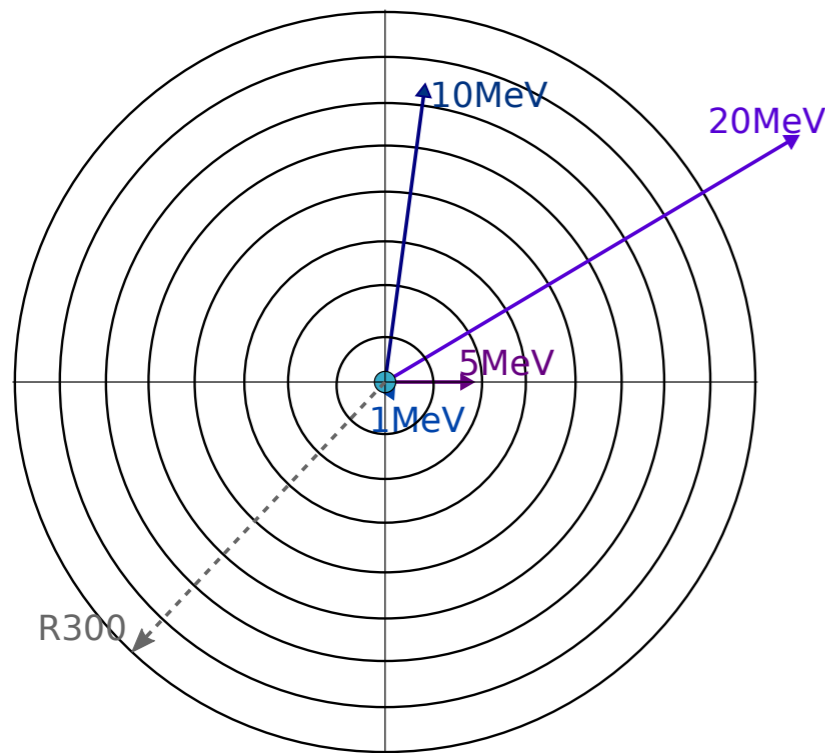


# Detection of Low- $Q^2$ Recoil-Protons

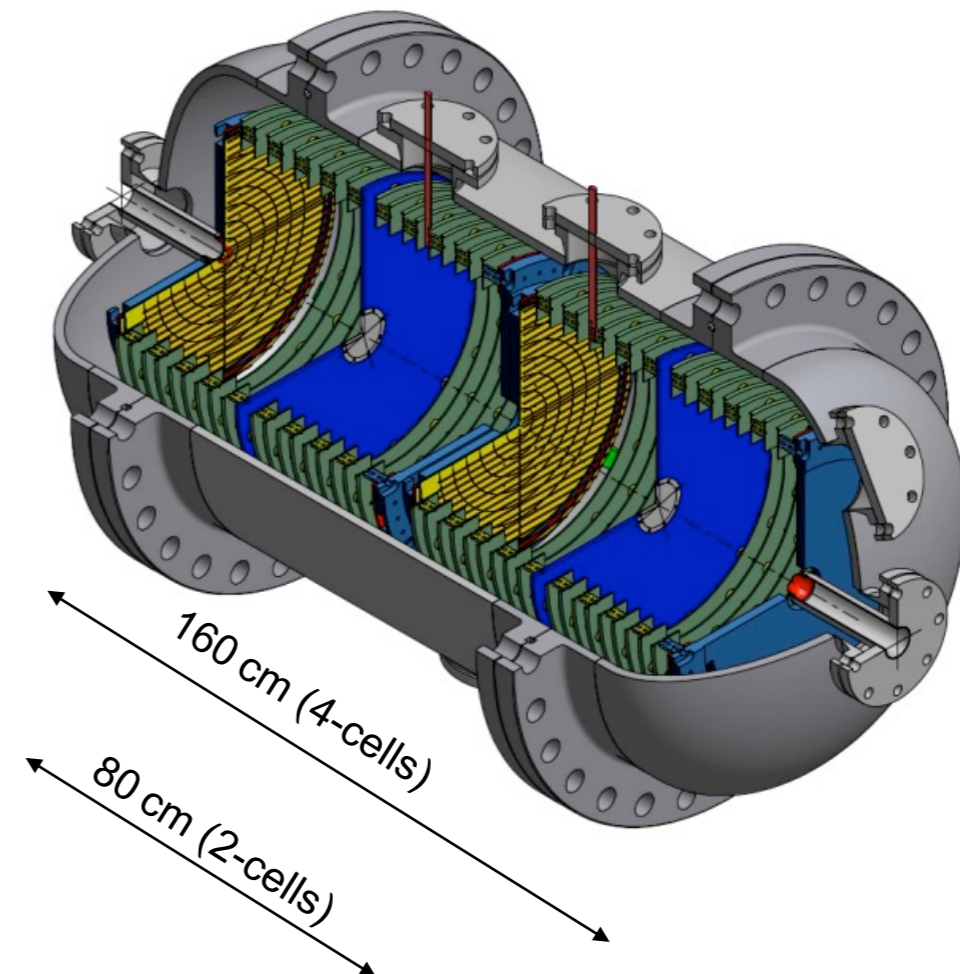
## Pressurised hydrogen active-target TPC

Range of proton depends on momentum transfer.

- Low- $Q^2$  range
  - recoil-proton ranges of 70 - 300 mm
  - segmented read out structure
- Optimisation of geometry ongoing
  - optimal pressure settings for  $Q^2$ -range
  - optimal length of hydrogen target



- Two pressure settings required
  - 20 bar ( $0.0025 \text{ GeV}^2/c^2 < Q^2 < 0.04$ )
  - 4 bar ( $Q^2 < 0.0025 \text{ GeV}^2/c^2$ )



# Control of Systematic Effects

## Absolut calibration, inefficiencies, and background

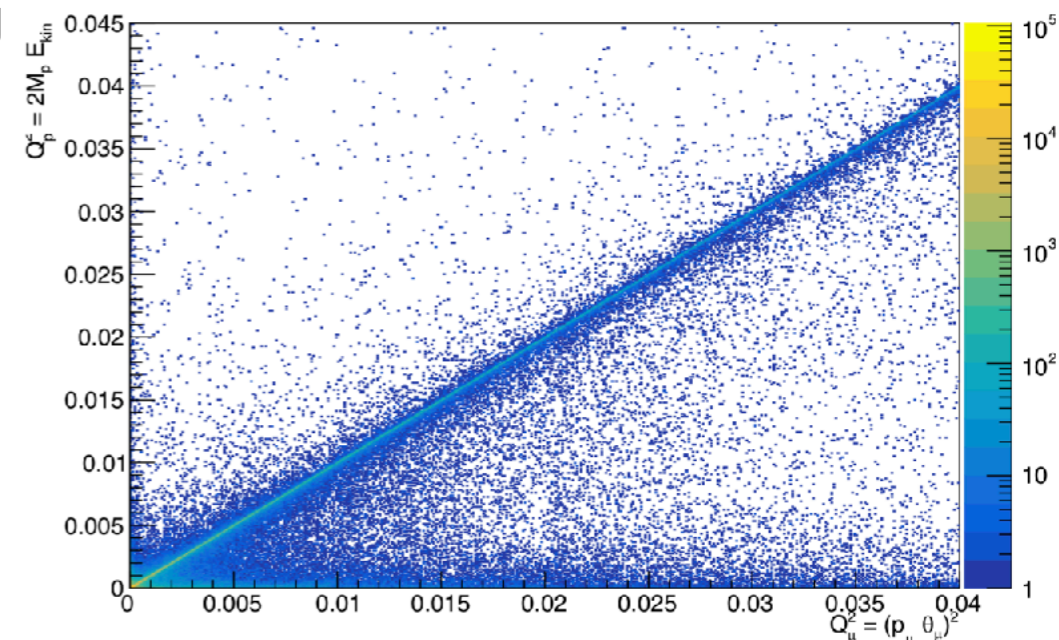
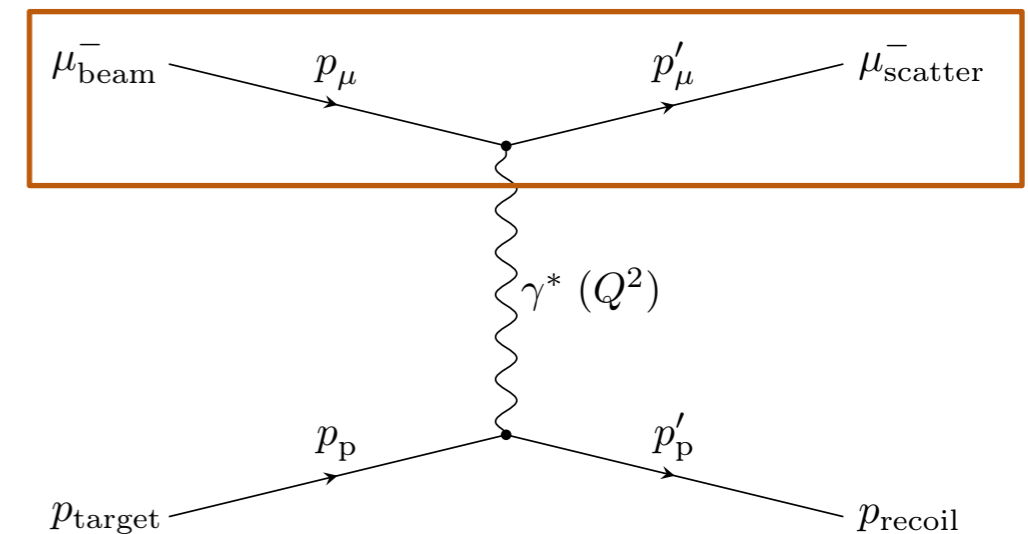
Understanding of systematic effects is crucial for precision.

- Absolut calibration of the TPC recoil-proton energy-scale
- Inefficiencies in recoil-proton measurement
- Cross check of TPC measurement

Redundant measurement to control systematics  
 → measurement of scattered muon kinematics

- Lepton-proton scattering accompanied by bremsstrahlung  
 → NLO process on  $\mathcal{O}(10^{-4})$  level for  $E_\gamma > 500$  MeV  
 → distortion of  $Q^2$ -spectrum

Usage of COMPASS spectrometer  
 → understanding of background  
 → muon momentum measurement



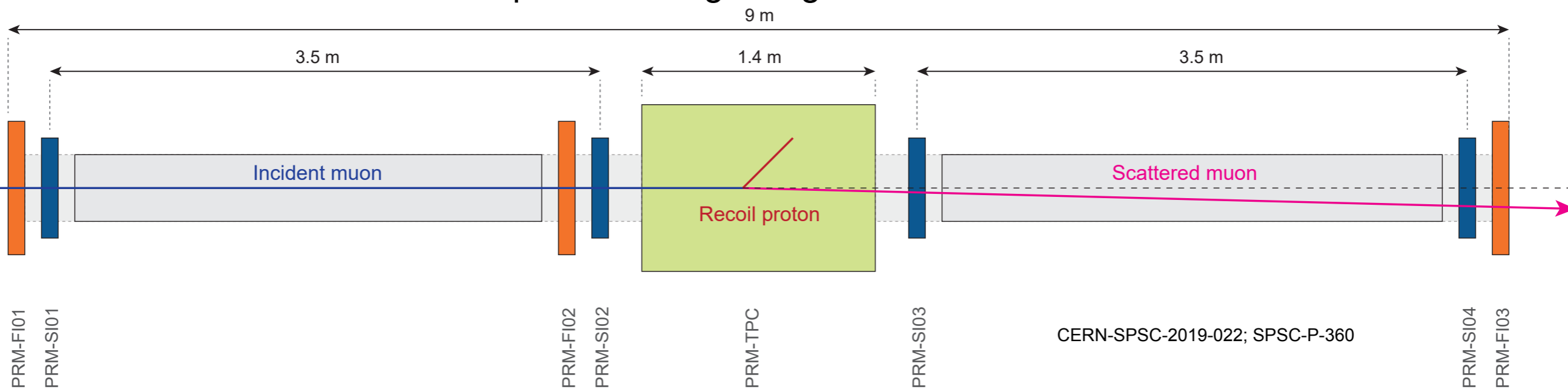


# Layout of the Proton-Radius Setup

## Components of the core setup

Precise recoil-proton and muon measurement with trigger on elastic events.

- Detect  $Q^2$ -values in the range of  $0.001 - 0.04 \text{ GeV}^2/c^2$   
 → pressurised hydrogen TPC as active target
- Redundant measurement: silicon detectors for measurement of scattered muon angle
- Trigger on scattered muons: scintillating-fiber detector to select elastic scattering events
- Vacuum tubes to minimise multiple scattering along the beam axis



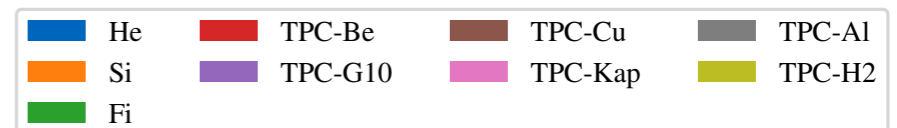
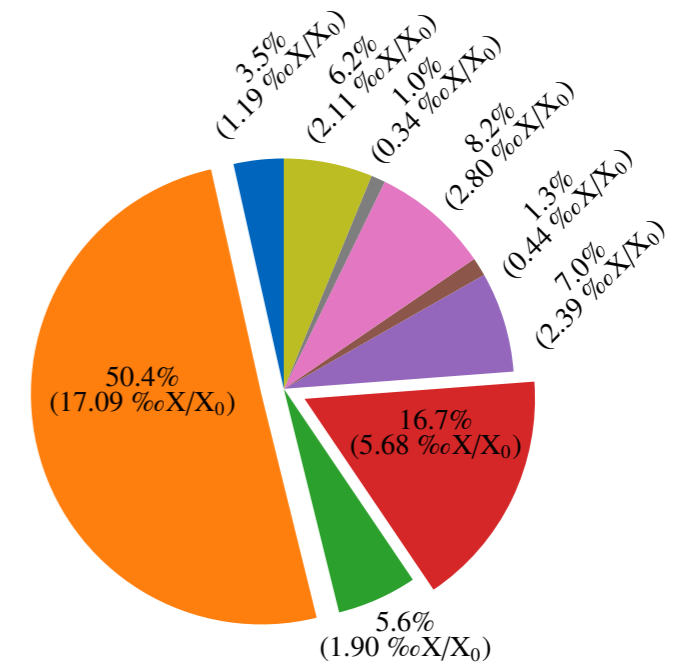
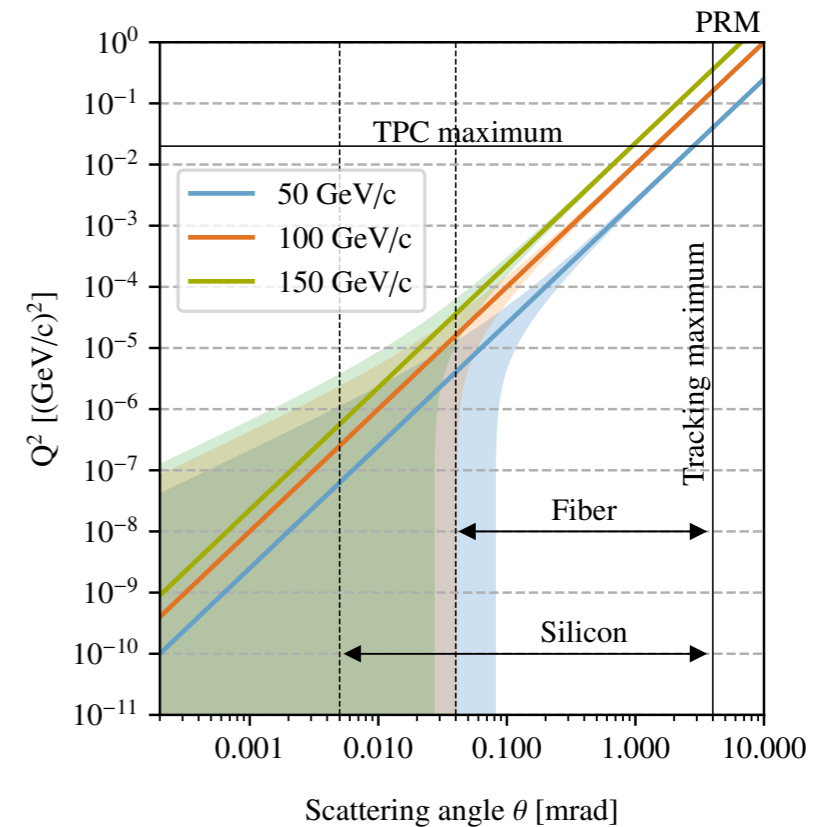
Scintillating-fiber tracker  
  Silicon tracker  
  High-pressure hydrogen time-projection chamber  
  Helium/vacuum beam pipe

# Influence of Multiple Scattering

## Scattering angle distorted by multiple scattering

Low- $Q^2$  values require a precise measurement of the small scattering angle.

- Influence on scattering angle of muon  
 → change in  $Q^2$ -spectrum
- Relative resolution at lowest proposed  $Q^2 = 0.001 \text{ GeV}^2/c^2$ :  
 →  $(\Delta Q^2/Q^2)_{2\text{-cell}} = 13.8 \%$  with  $(X/X_0)_{2\text{-cell}} = 33.9 \%$   
 →  $(\Delta Q^2/Q^2)_{4\text{-cell}} = 15.4 \%$  with  $(X/X_0)_{4\text{-cell}} = 41.5 \%$
- Fix contribution due to beryllium window of TPC
- Main contribution due to silicon detector material



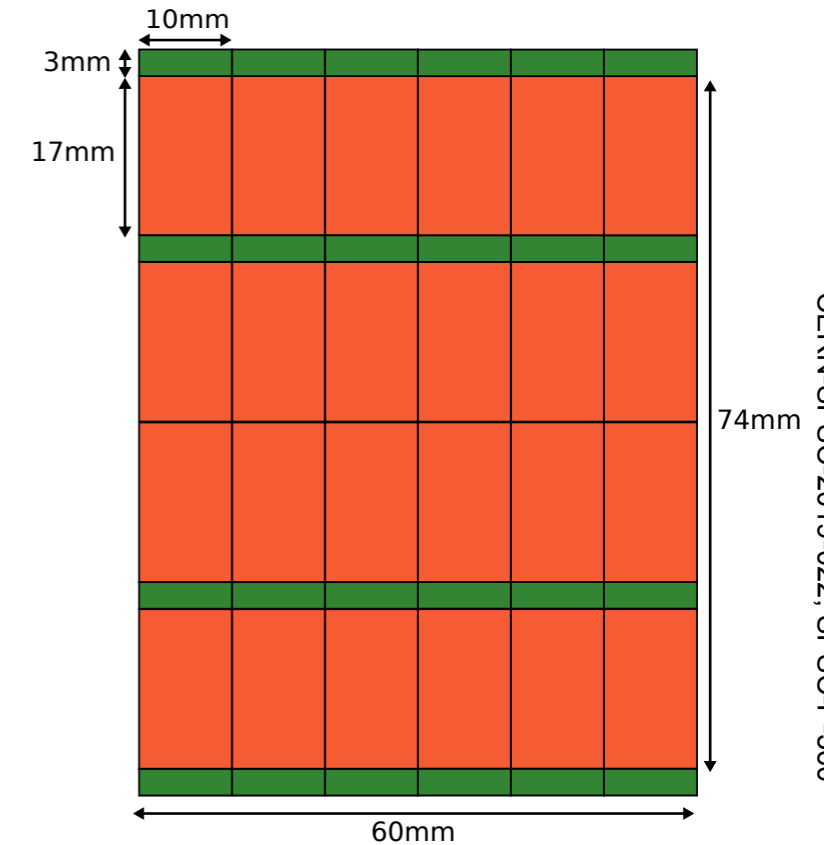
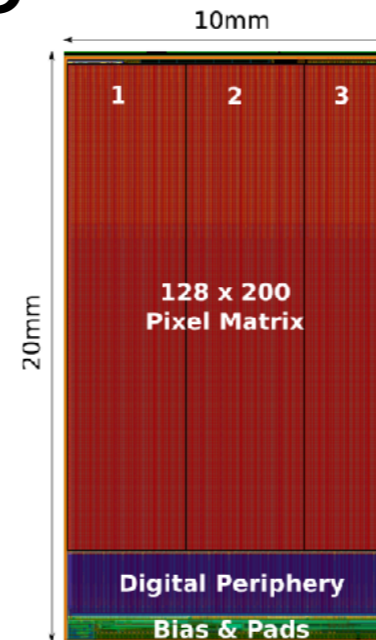
Material budget must be precisely under control  
 → detector geometries must be optimised

# Muon Trigger and Tracking Detectors

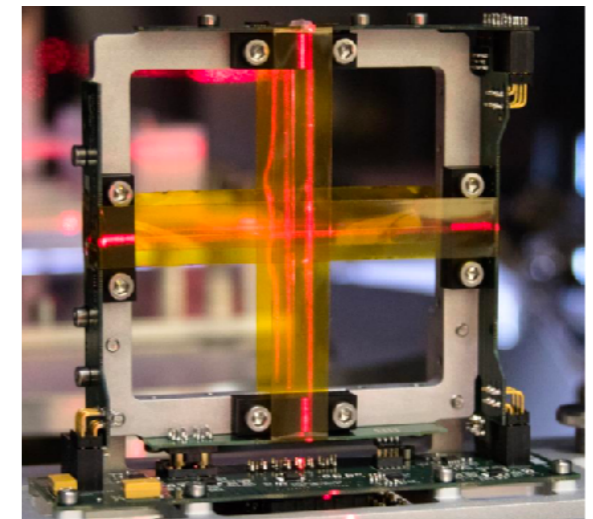
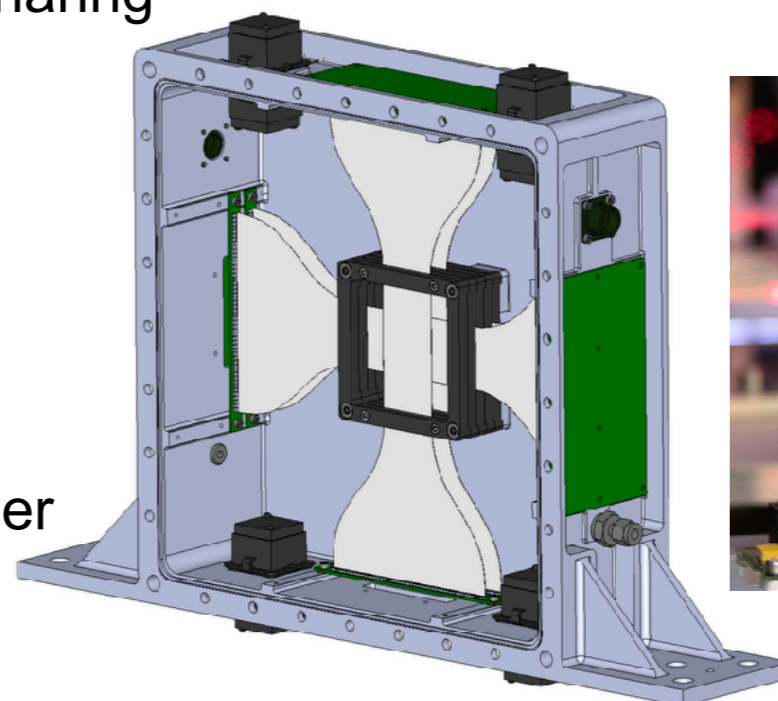
## Current solutions for detectors

Silicon detectors for precise muon tracking triggered by scintillating-fiber triggers.

- Silicon detector - MuPix under investigation:
  - produced at KIT and used at Mu3e
  - MuPix8 prototype: 1 x 2 cm<sup>2</sup>, 128 x 200 pixels
  - thickness down to only 50 μm
  - 20-ns time resolution and 80-μm pixel size
  - combination of several layers required
  - spatial resolution of 5 μm with charge sharing
  - talk by I. Konorov (tomorrow)
- Scintillating-fiber trigger:
  - 200-μm scintillating-plastic fibers
  - each fiber read out via SiPMT
  - four layers combined per station
  - challenge: only 6 photoelectrons per fiber



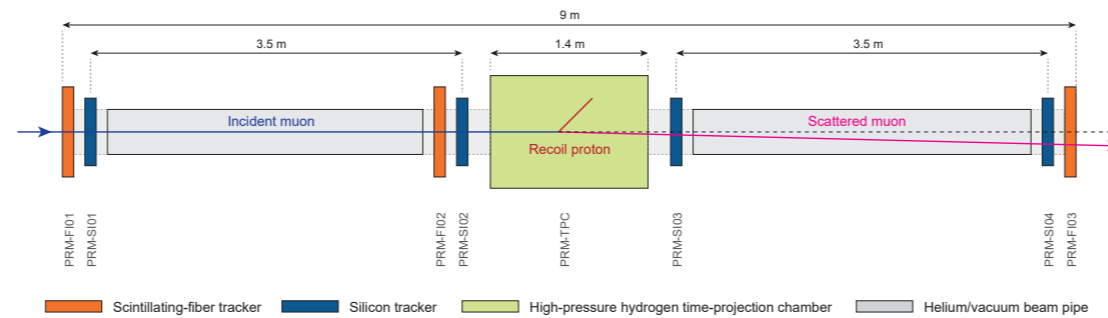
CERN-SPSC-2019-022; SPSC-P-360



# Layout of the Proton-Radius Setup

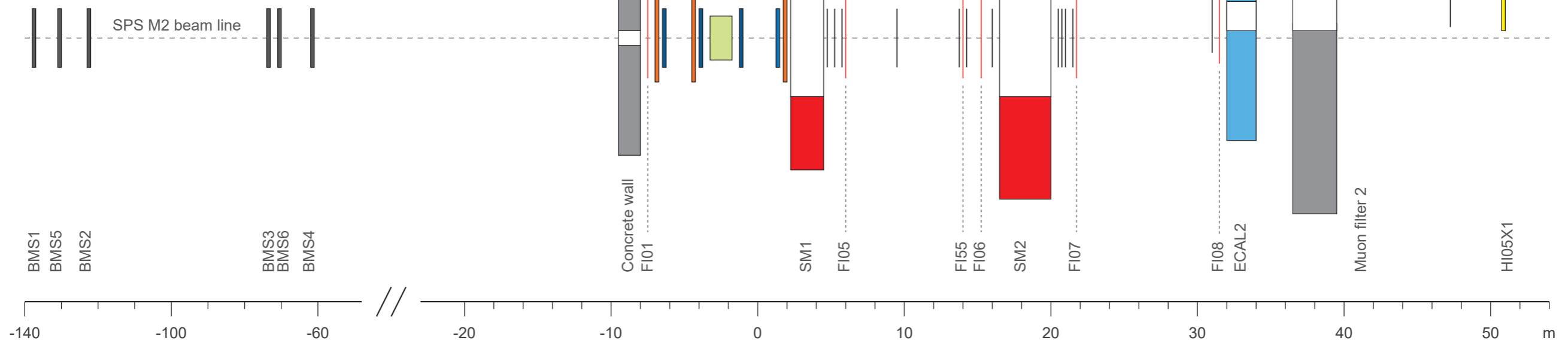
## Advantages of using the COMPASS spectrometer

Measurement of muon momentum and understanding of background.



- Scintillating-fiber tracker
- GEMs / Pixel-GEMs
- Electromagnetic calorimeter
- Hodoscope
- Magnet
- Concrete

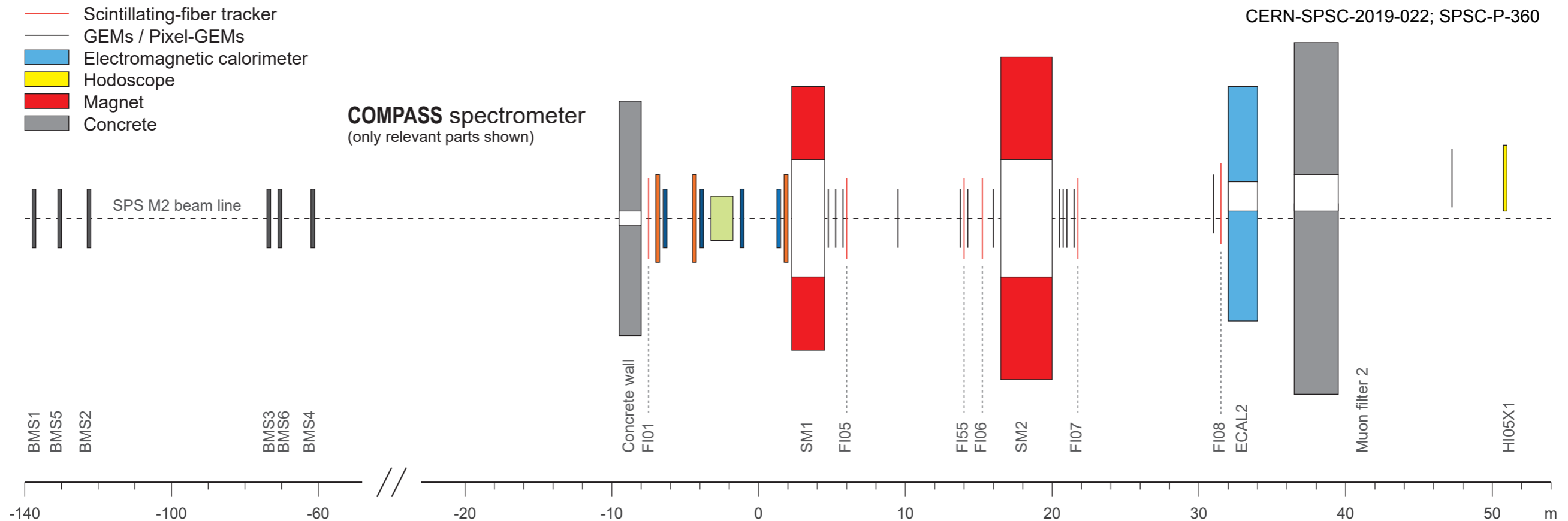
COMPASS spectrometer  
 (only relevant parts shown)



# Layout of the Proton-Radius Setup

## Advantages of using the COMPASS spectrometer

Measurement of muon momentum and understanding of background.



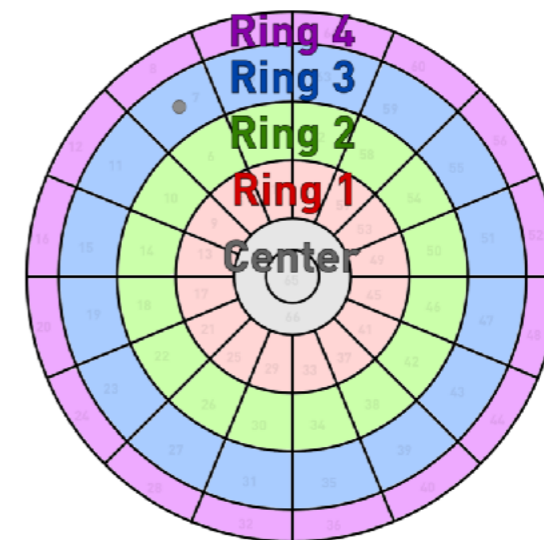
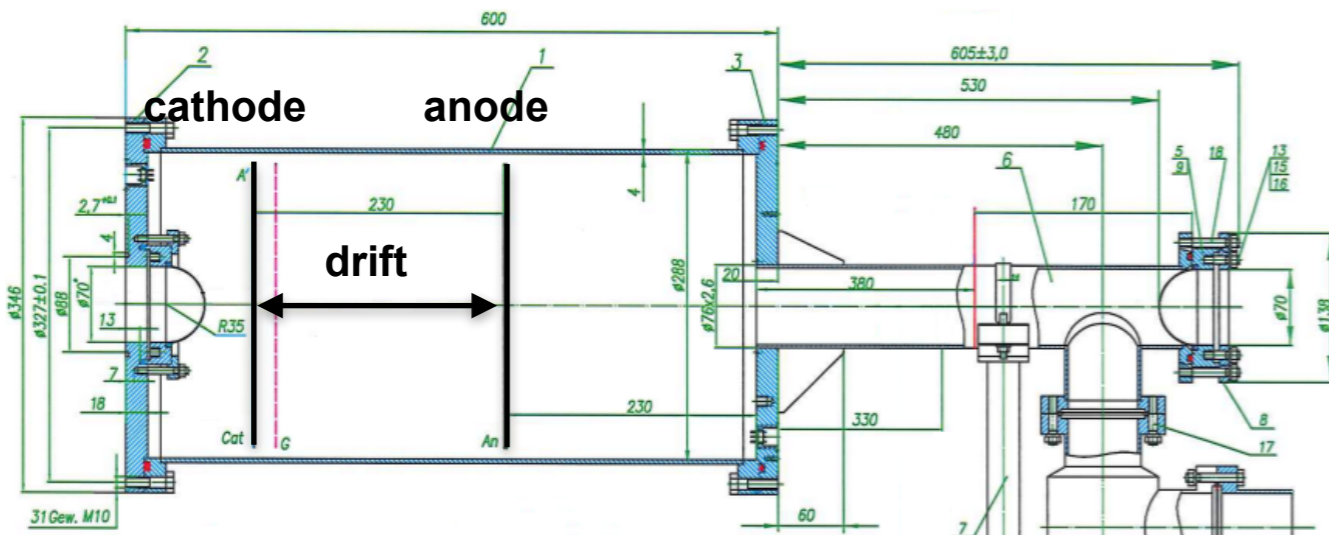
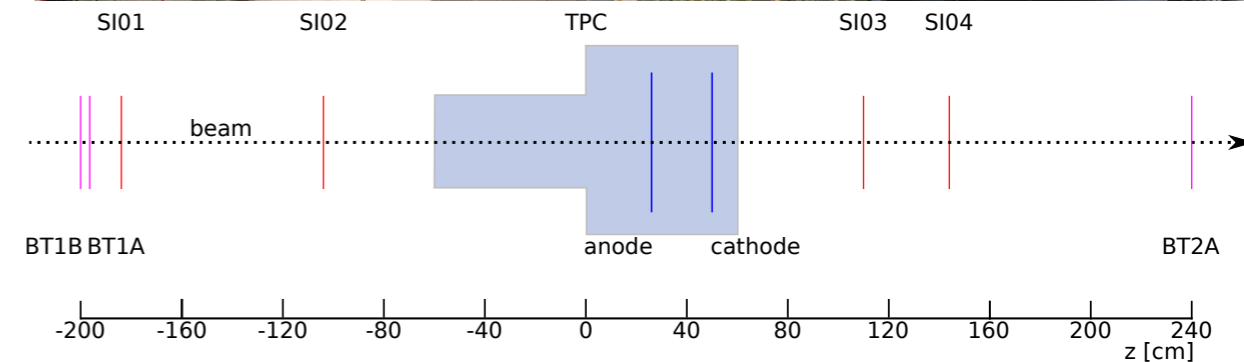
- COMPASS spectrometer
  - momentum measurement of scattered muon
  - radiative background using electromagnetic calorimeter
  - muon identification with muon filter and hodoscope

# Beam Test in 2018

## Feasibility test using TPC and silicon detectors

Two-month beam test parallel to COMPASS run with TPC and silicon trackers.

- Parasitically to COMPASS Drell-Yan run  
 → remaining muons of 190 GeV pion beam
- TPC: 8 bar hydrogen and 23 cm drift
- Four silicon stations with a size of 7x5 cm<sup>2</sup>
- Two distinct DAQ systems  
 → event matching via time stamp

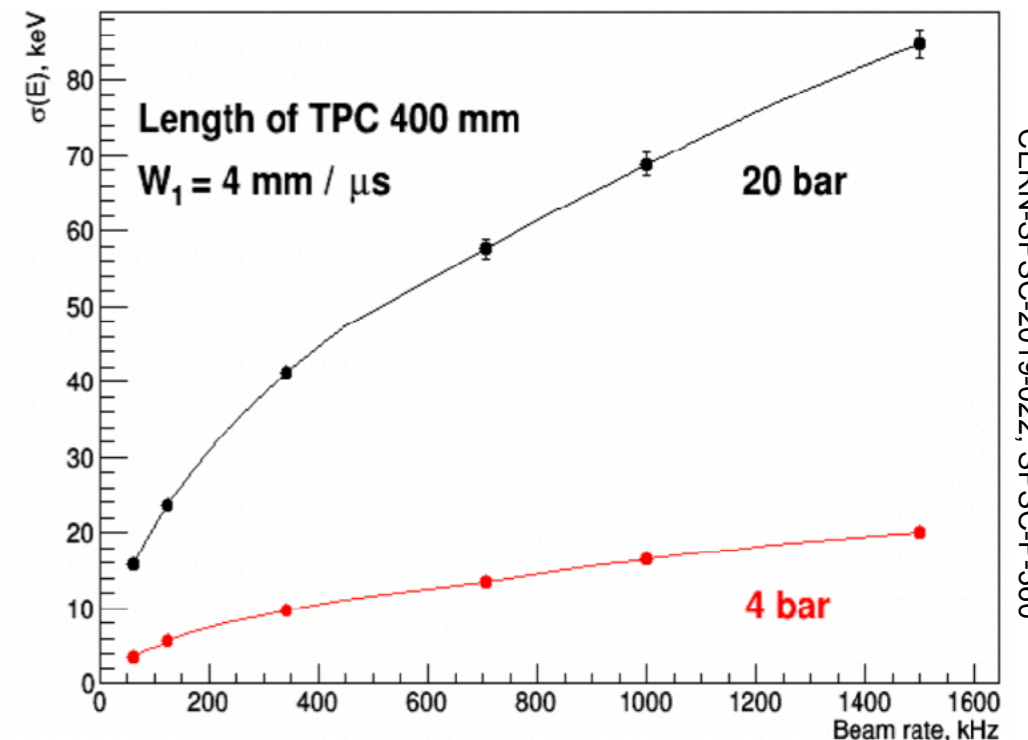
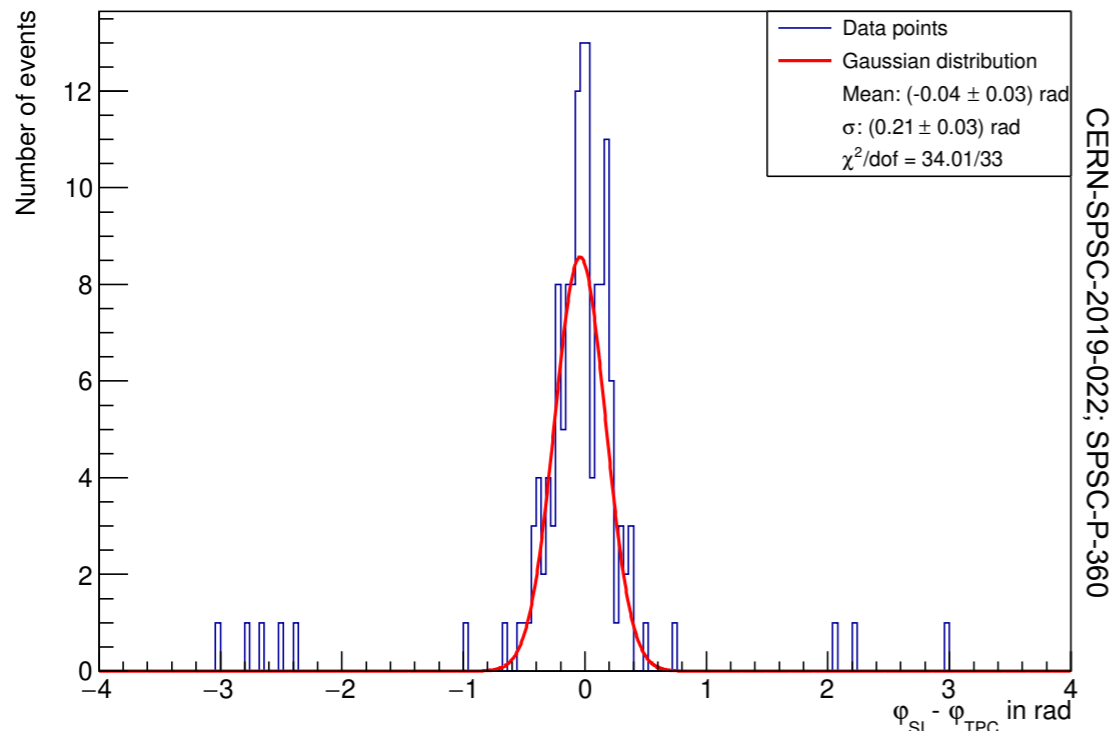
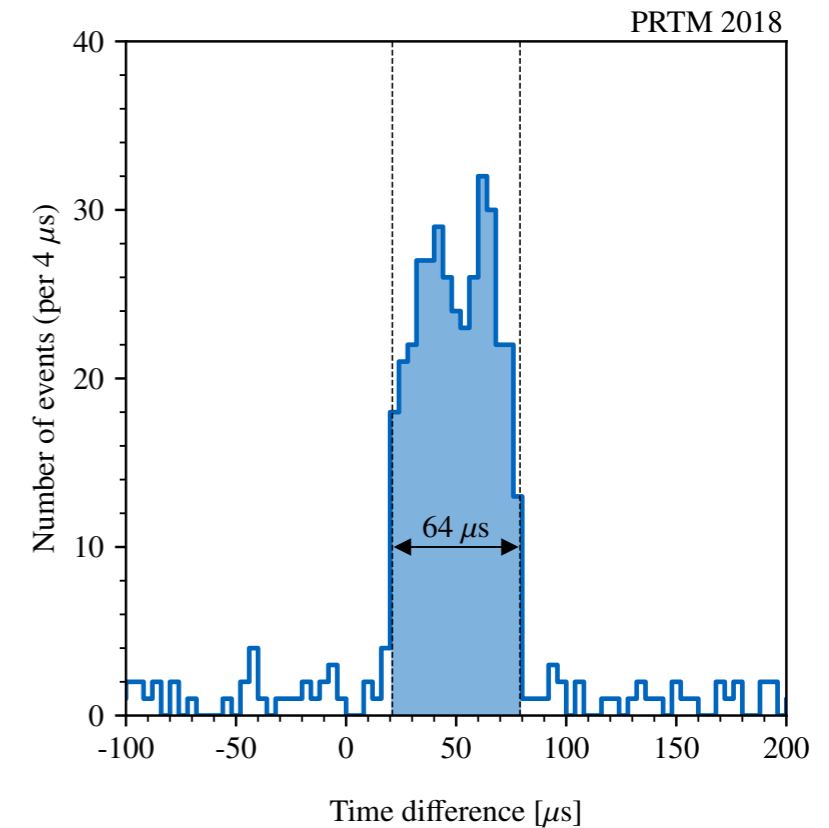


# Results of the Beam Test in 2018

## Feasibility test using TPC and silicon detectors

Two-month beam test parallel to COMPASS run with TPC and silicon trackers.

- Time correlation of TPC and silicon events  
 → 23 cm drift correspond to 64  $\mu\text{s}$  drift time
- High purity of events in reconstructed polar angle  $\varphi$   
 → width corresponds to readout segmentation
- “Beam noise” due to beam intensity crucial for TPC

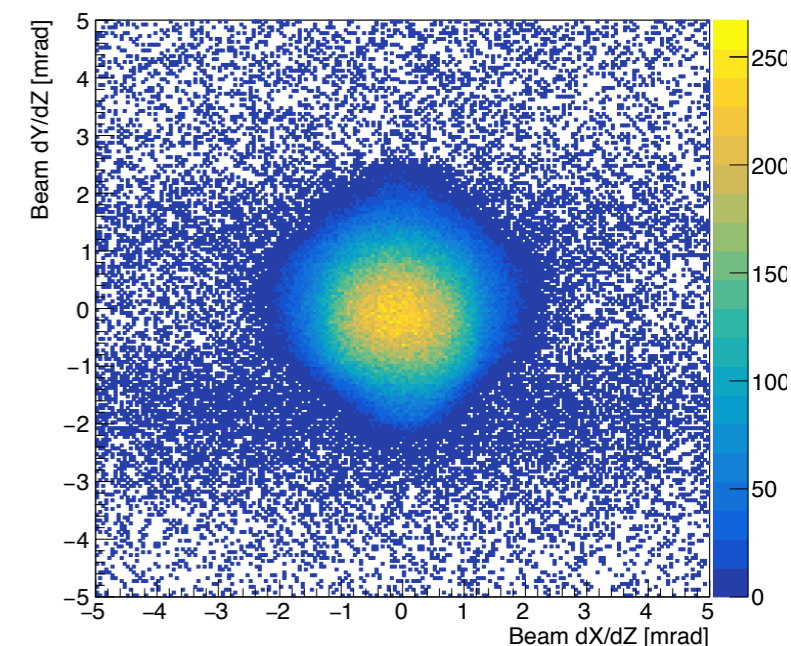
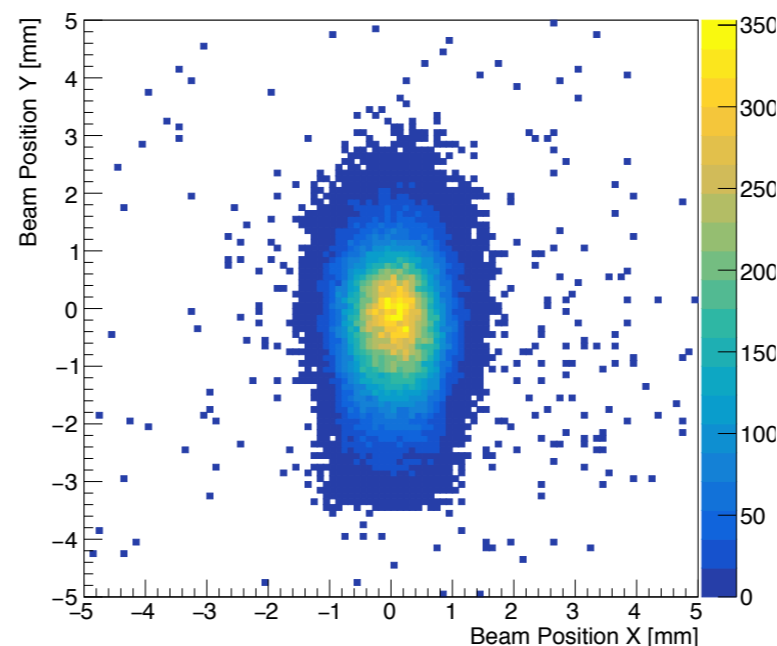
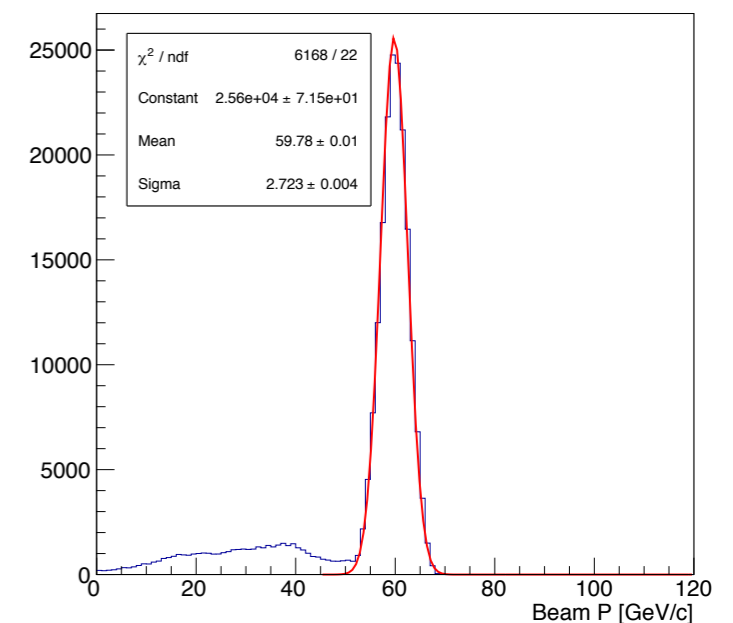
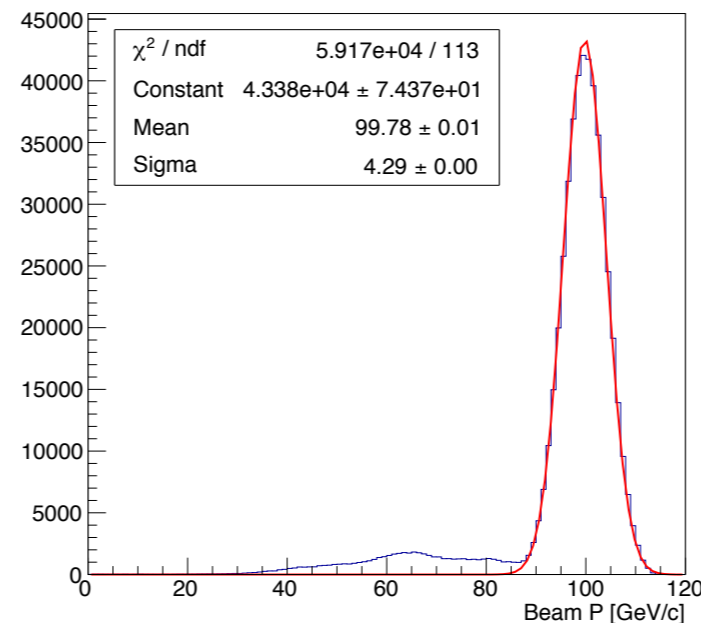


# Beam Properties

## Intensity and size of muon beam

Beam properties are defined by geometry and detector properties.

- Maximum beam rate for TPC  
 → Beam flux  $\Phi_\mu = 2 \cdot 10^6/\text{s}$
- Beam energy scenarios  
 →  $E_\mu = 100 \text{ GeV}$  - measurement  
 →  $E_\mu = 60 \text{ GeV}$  - systematic studies
- Narrow beam at target position  
 →  $\sigma_{x,y} < 1 \text{ cm}$
- Small dispersion along target region  
 →  $\sigma_{dx/dz, dy/dz} < 0.5 \text{ mrad}$

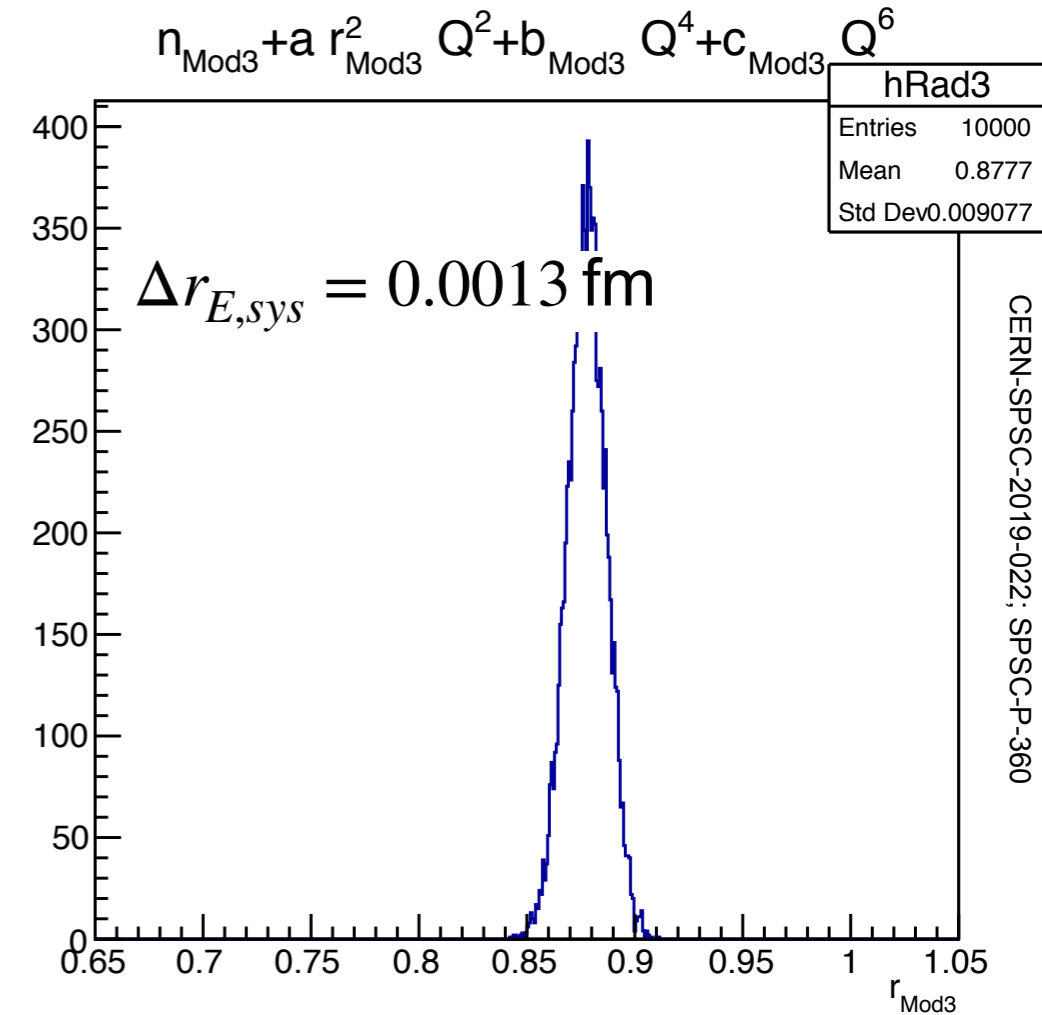
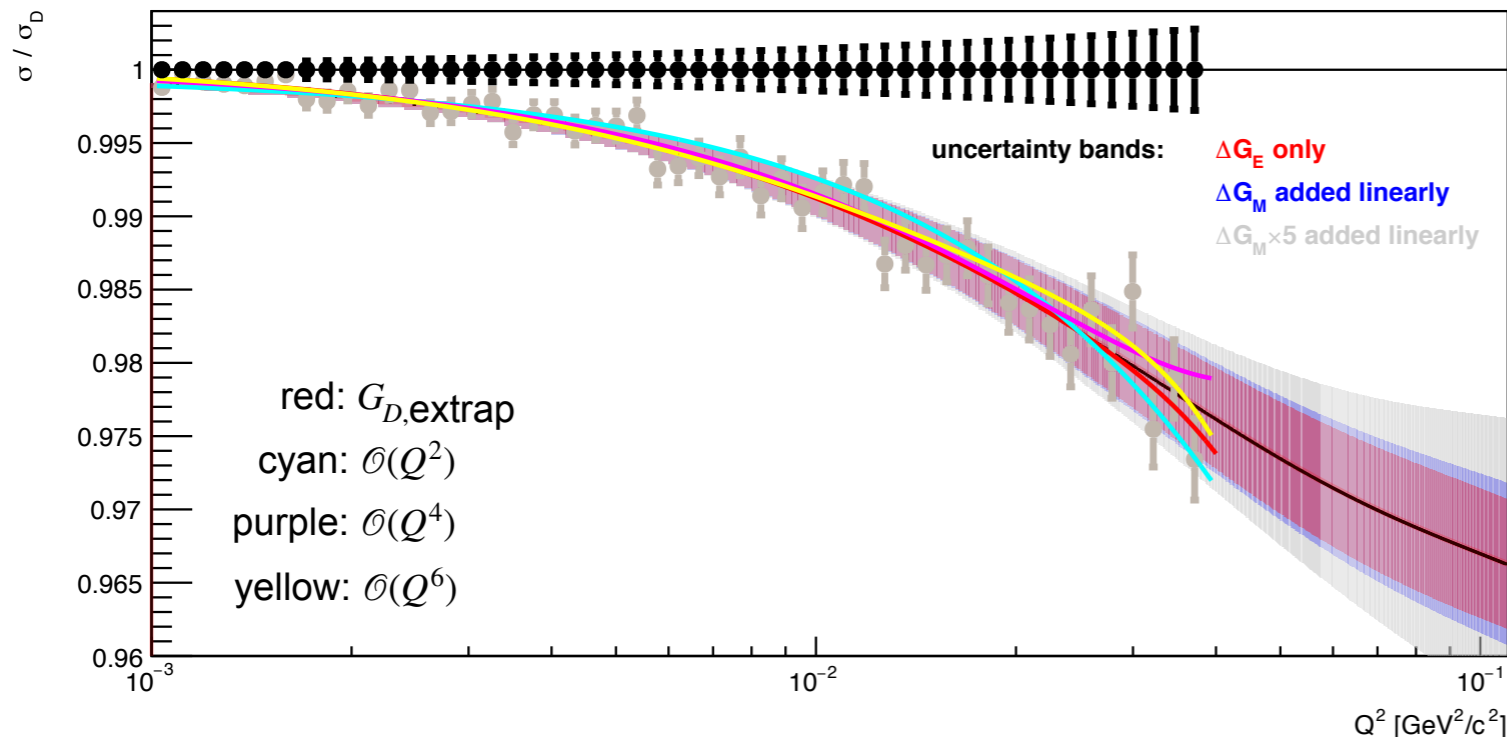




# Test of Statistical Precision and Beam Time

## Example using a model

MAMI A1 data as input and replicas in bins fitted with polynomials up to  $\mathcal{O}(Q^{2n})$ .



- Polynomial fit with  $\mathcal{O}(Q^6)$  and four free parameters:  
 → statistical precision 0.0090 fm
- 70 million events required for statistical precision of 1 %  
 → about 140 days of data taking depending on final geometry

# Summary

- Discrepancy between scattering and spectroscopy experiments - Proton Radius Puzzle
- Many performed, some running and several proposed experiments:
  - missing: measurement of the proton charge radius via **high-energy  $\mu$ -p elastic scattering**
- Unique location: CERN M2 beamline in combination with the COMPASS spectrometer
- Providing a high-energy  $\mu$ -p elastic scattering data set of about 70 million events
  - $Q^2$ -range: 0.001 - 0.04 GeV<sup>2</sup>/c<sup>2</sup>
  - aimed statistical precision for this measurement of the proton charge radius: 1 %
- Estimated beam time about 140 days depending on final geometry
- New development ongoing - TPC, silicon detectors, fiber triggers and DAQ (*Talk by I. Konorov*)
- Test beam in 2018 provided promising results and experience

Proposal was handed in end of May to SPS Experiments Committee (CERN)  
(CERN-SPSC-2019-022, SPSC-P-360)

# Outlook

- More detailed studies of systematics required to support the aimed precision
- Full Monte-Carlo description of final setup to study driving parameters for geometry and detector development
- Comparison of this measurement with other upcoming measurements like MUSE at PSI
- Further development and studies of prototypes for silicon detector and fiber trigger
- Absolute energy scale of beam and measured  $Q^2$  required - different approaches under study
- First beam tests foreseen in 2021
  - 20 days dedicated tests in addition to the transverse-deuteron run of COMPASS
  - further testing downstream of COMPASS in parallel
- First data taking proposed in 2022 / 2023

Update of proposal until next SPSC meeting (15<sup>th</sup> October 2019)

Thank you for your attention

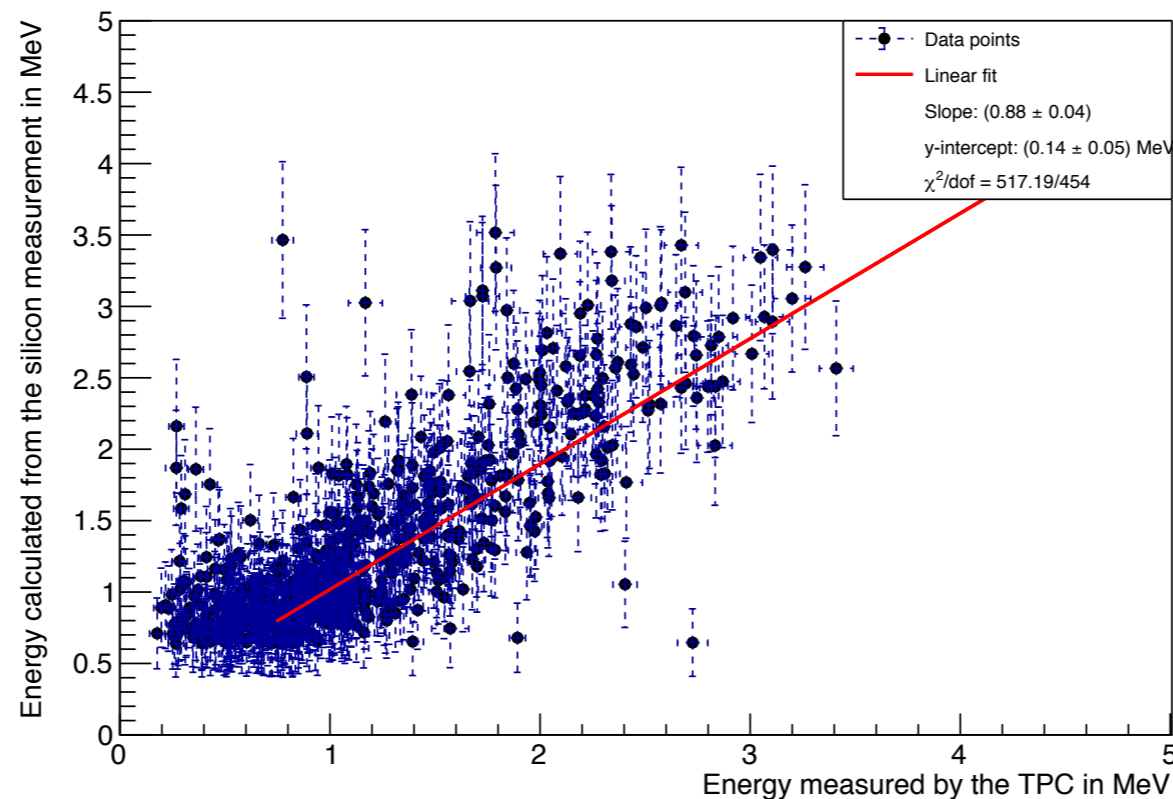
## Further information

# Results of the Beam Test in 2018

## Basic detector setup for tested in 2018

Two month test parallel to COMPASS run with TPC and silicon tracking stations.

- Recoil proton energies determined by both detector systems
  - Resolution obtained by TPC 3x better
  - Proposed setup: increase resolution by factor 2
- Important experience was gathered along with know-how of a future analysis of the proposed measurement



# Goal of this Measurement and Requirements

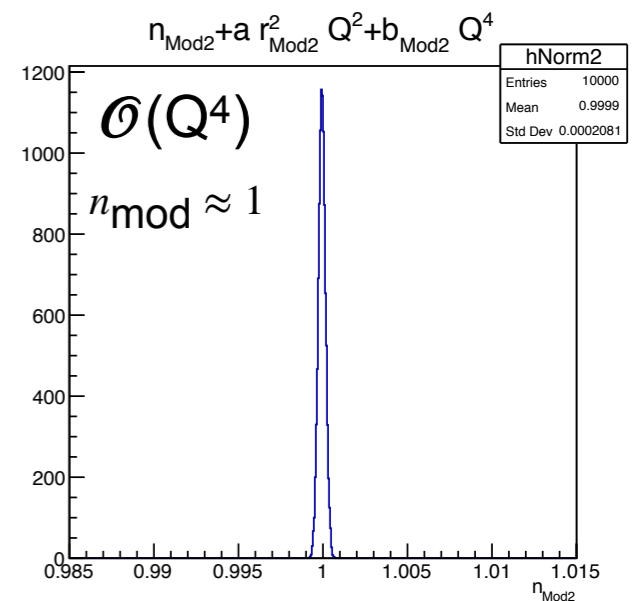
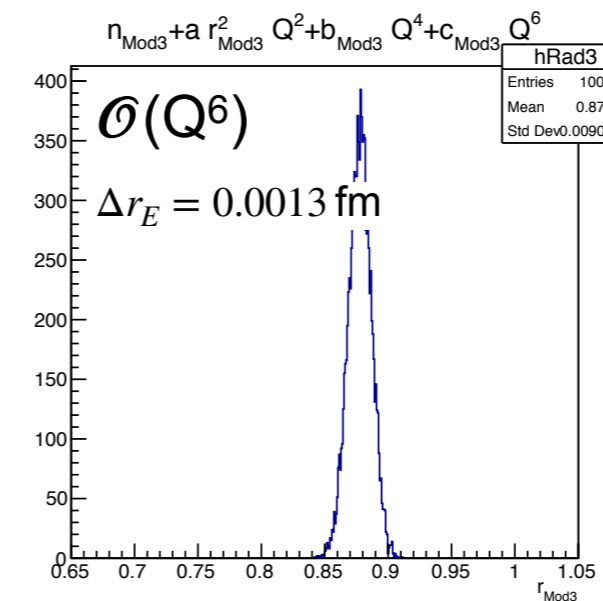
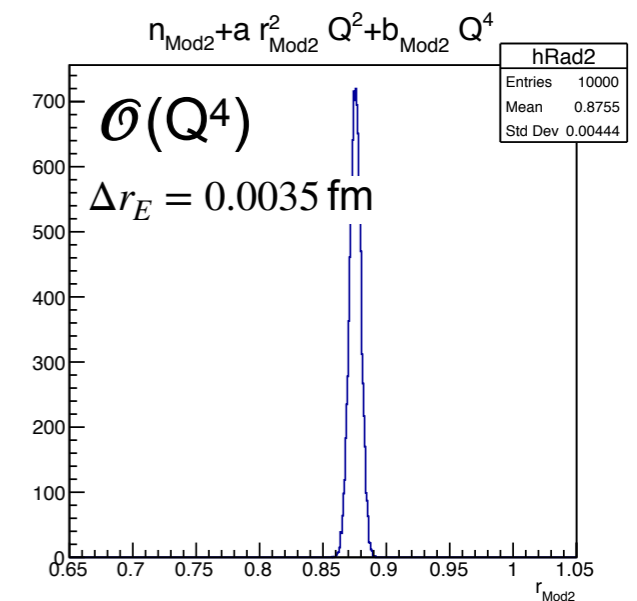
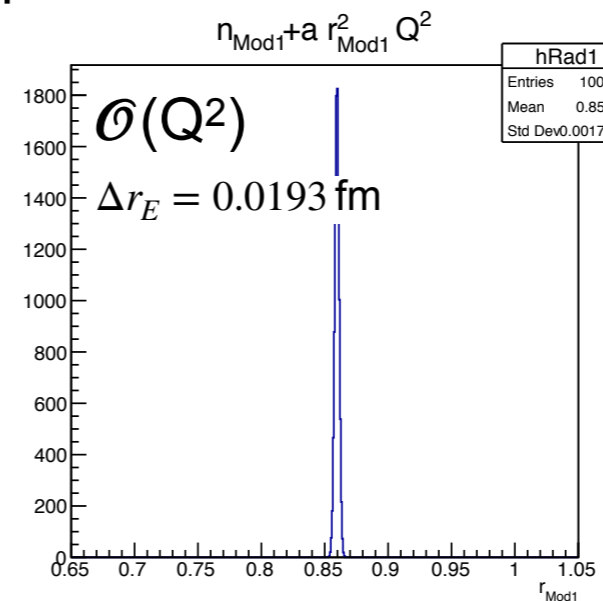
## Different models for the radius extraction

$Q^2$ -dependency of cross section can be fitted with polynomials up to  $\mathcal{O}(Q^{2n})$ .

- 70 million elastic events in proposed  $Q^2$ -range fitted to MAMI data ( $r_{E,MAMI} = 0.879$  fm)
- Truncated series of  $G_E(Q^2)$ :  

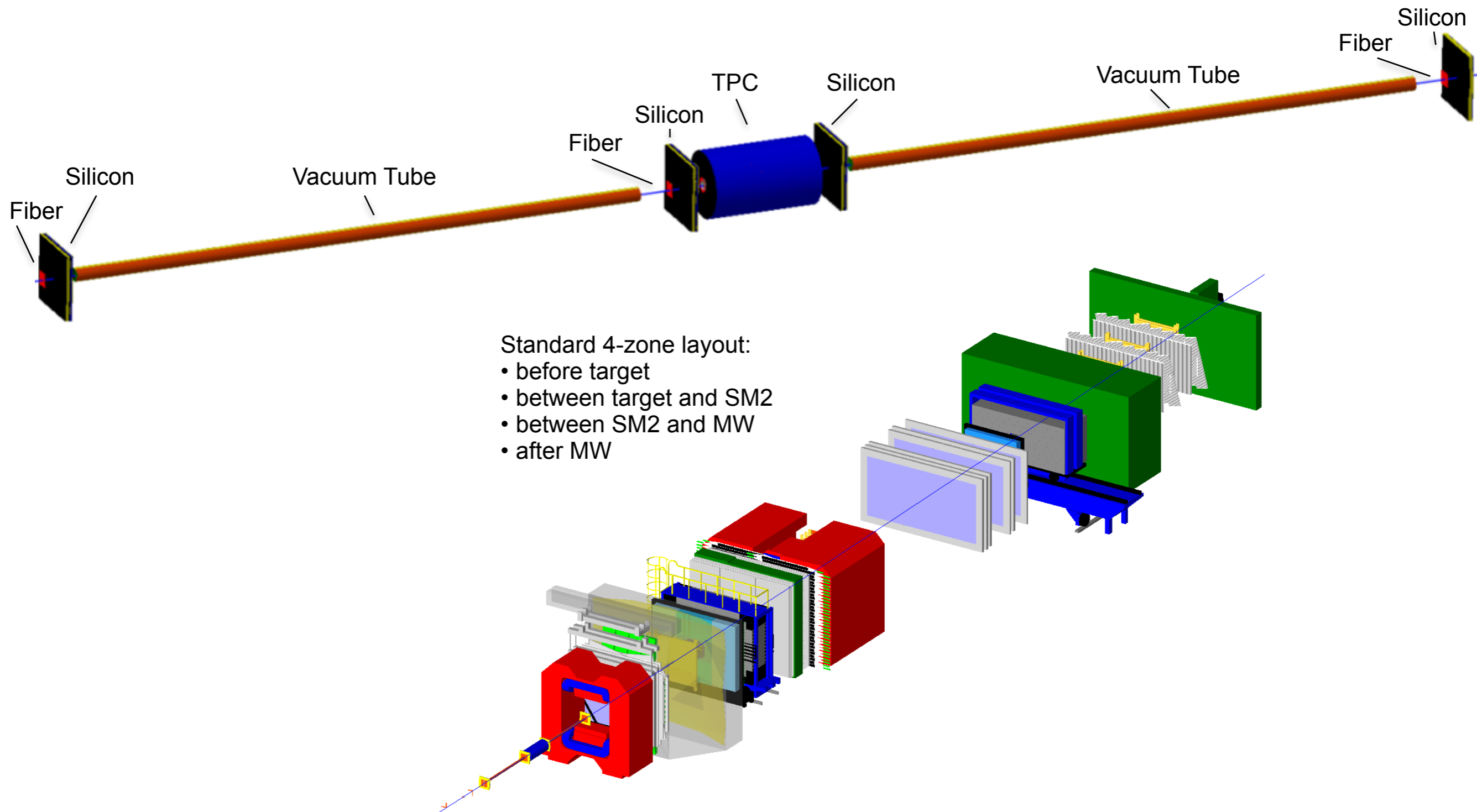
$$G_E(Q^2) = n (1 + a_2' Q^2 + a_4' Q^4 + a_6' Q^6 + a_8' Q^8 + \dots)$$
- 3 parameters  $\mathcal{O}(Q^4)$ :  $n, a_2, a_4$   
 → sys 0.0035 fm, stat 0.0040 fm
- 4 parameters  $\mathcal{O}(Q^6)$ :  $n, a_2, a_4, a_6$   
 → sys 0.0013 fm, stat 0.0090 fm

Measurement the proton radius with a statistical precision on the level of 1% achieved with 70 million events



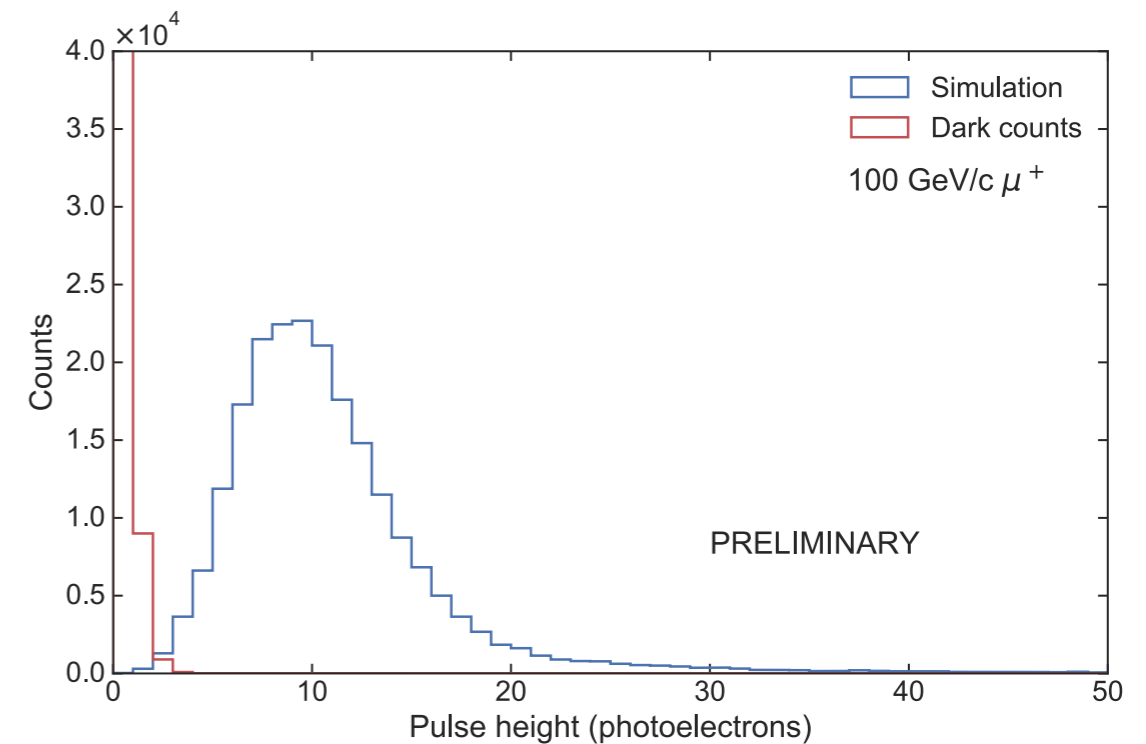
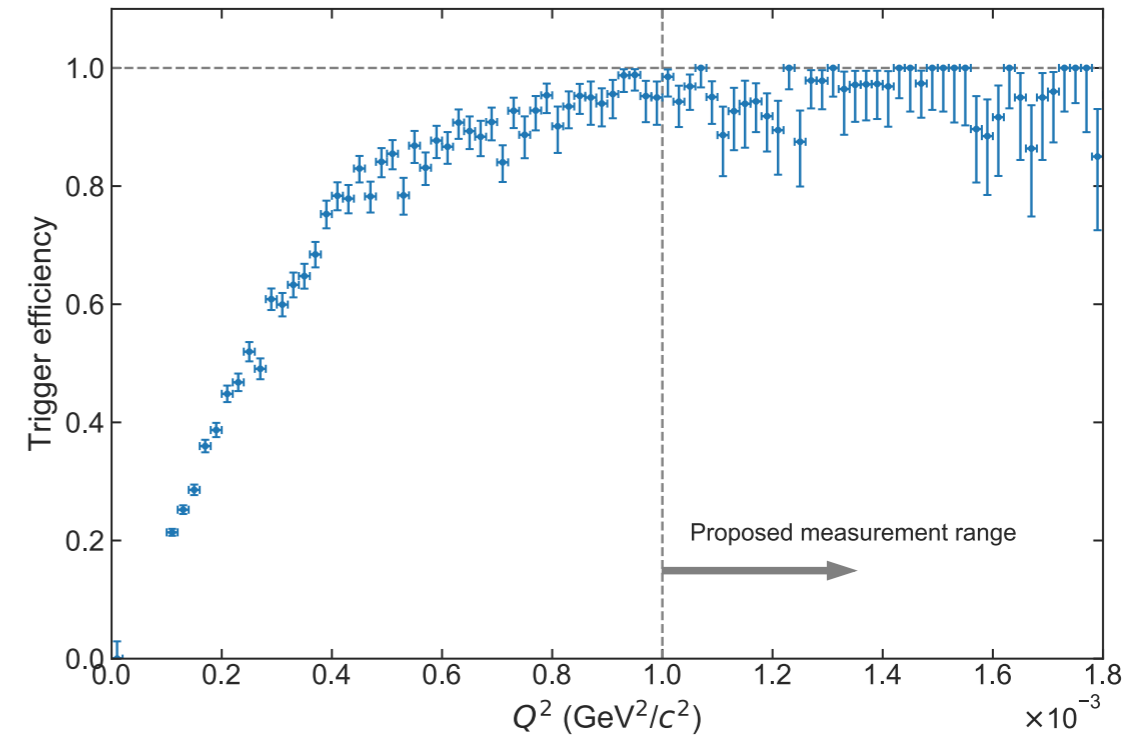
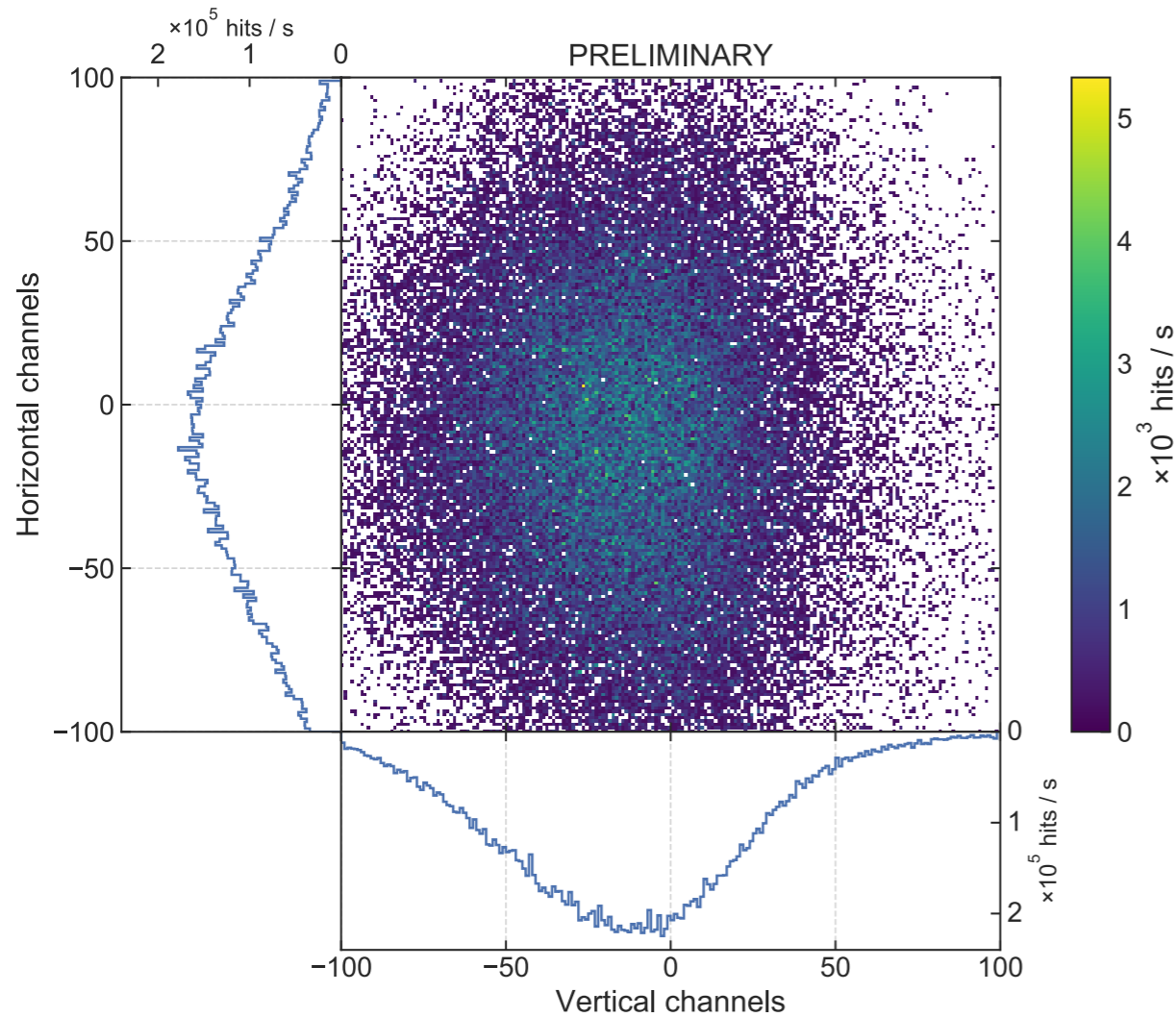
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# Layout of the Setup

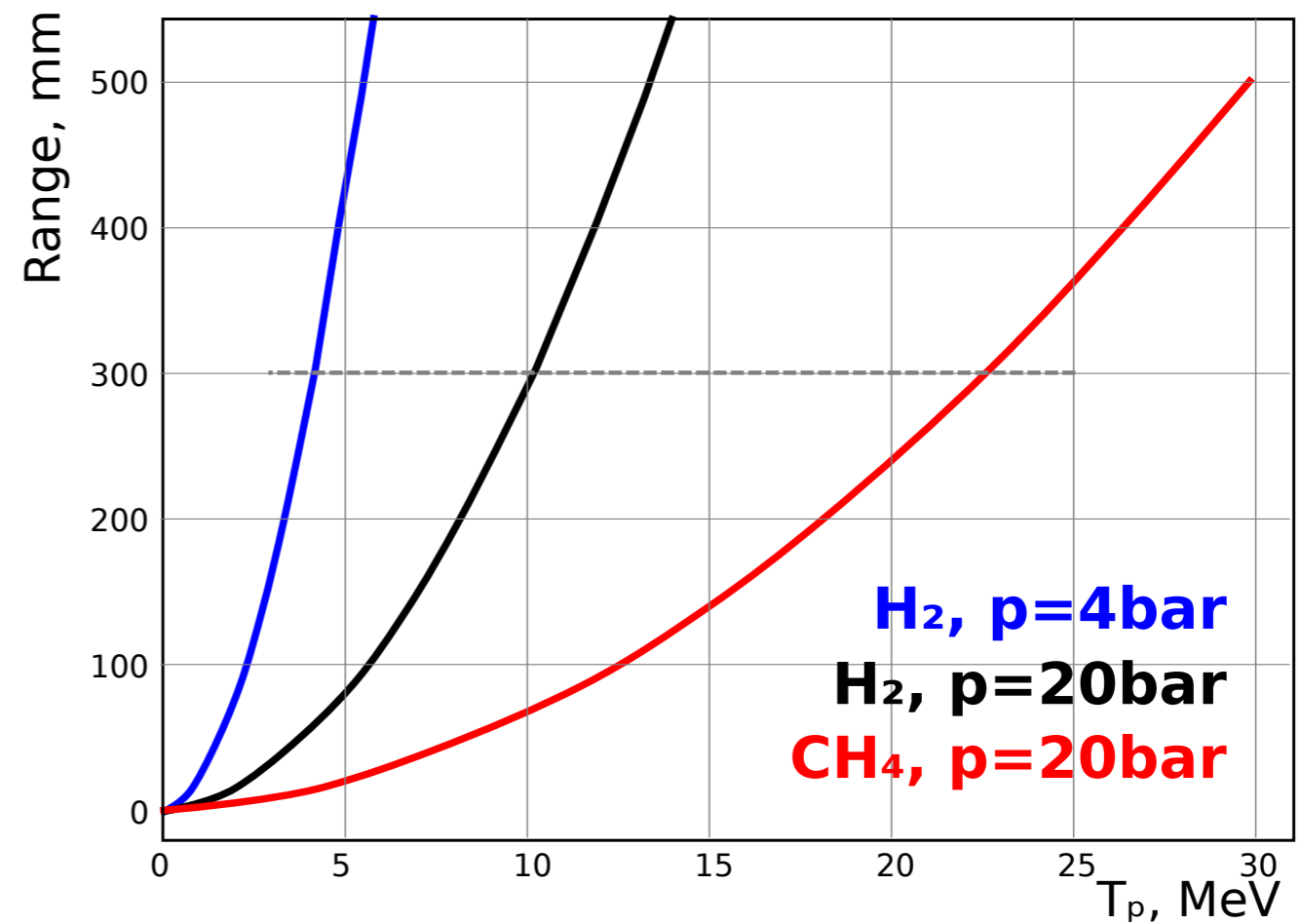
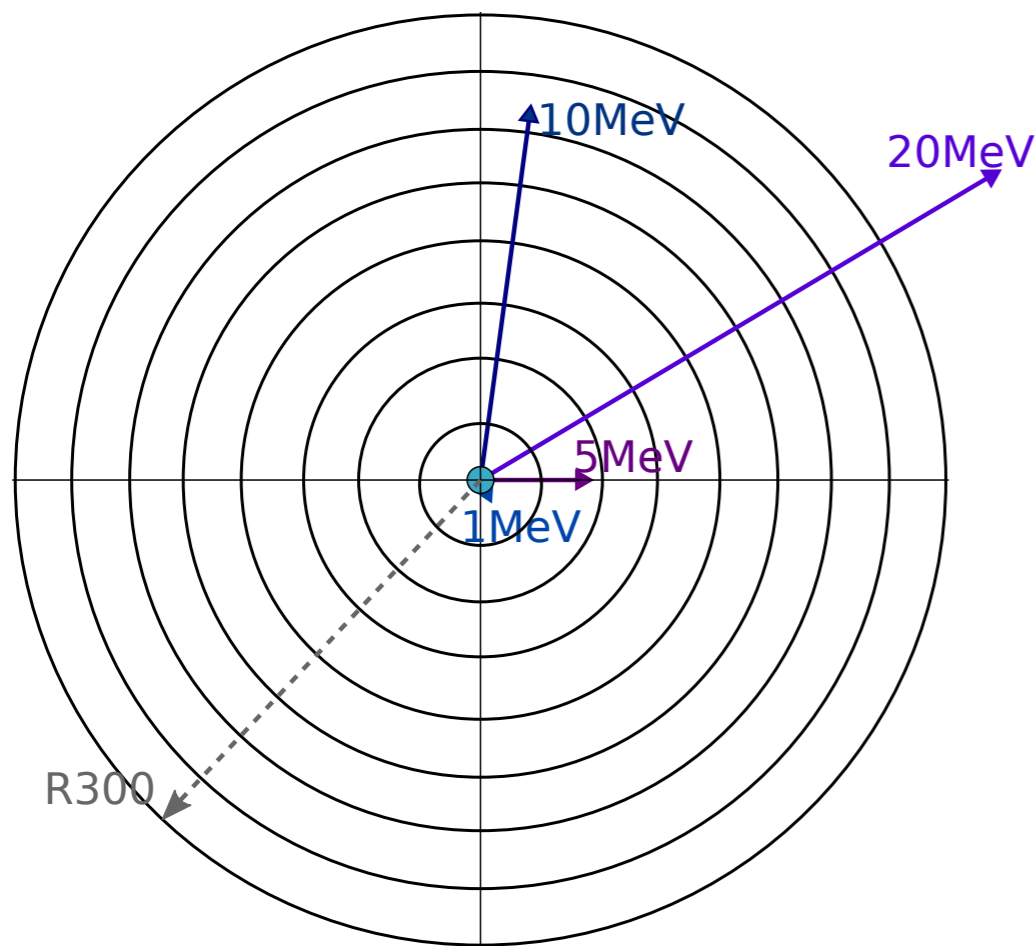




# Fiber Trigger Efficiency



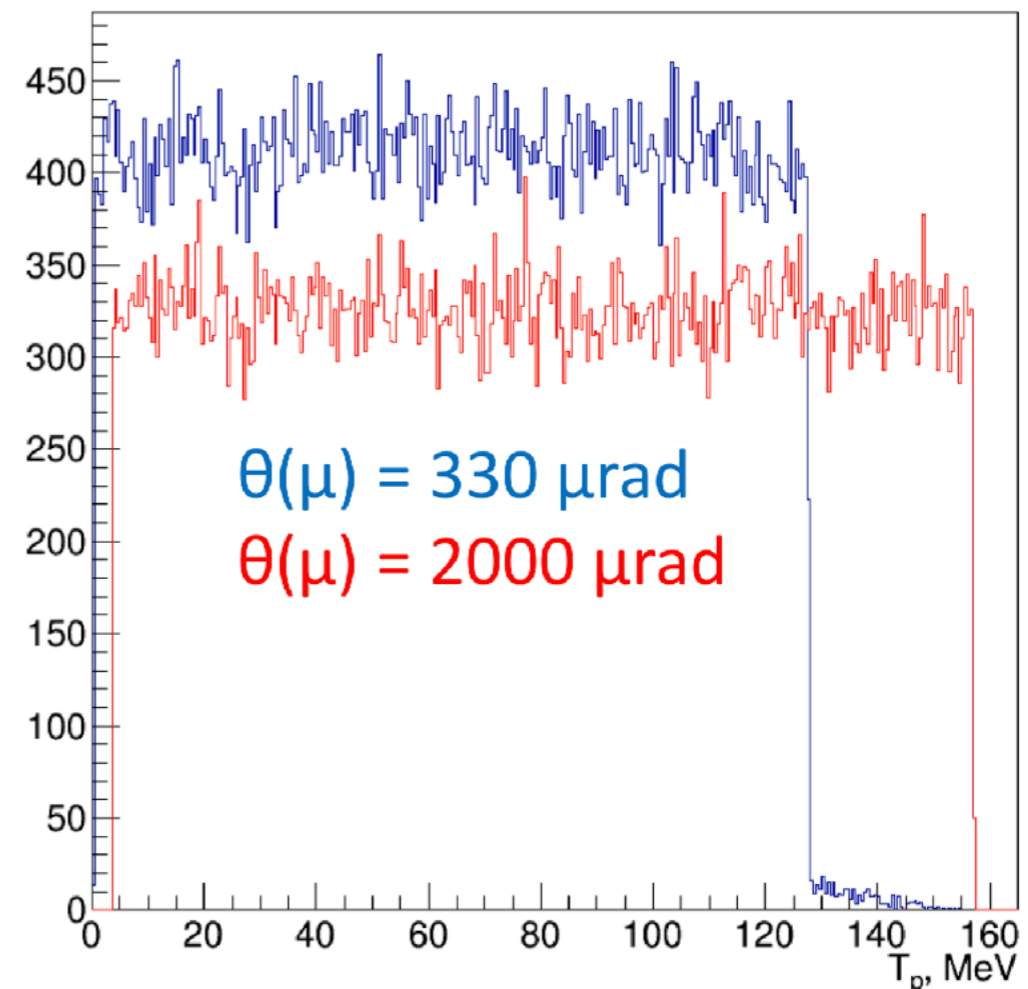
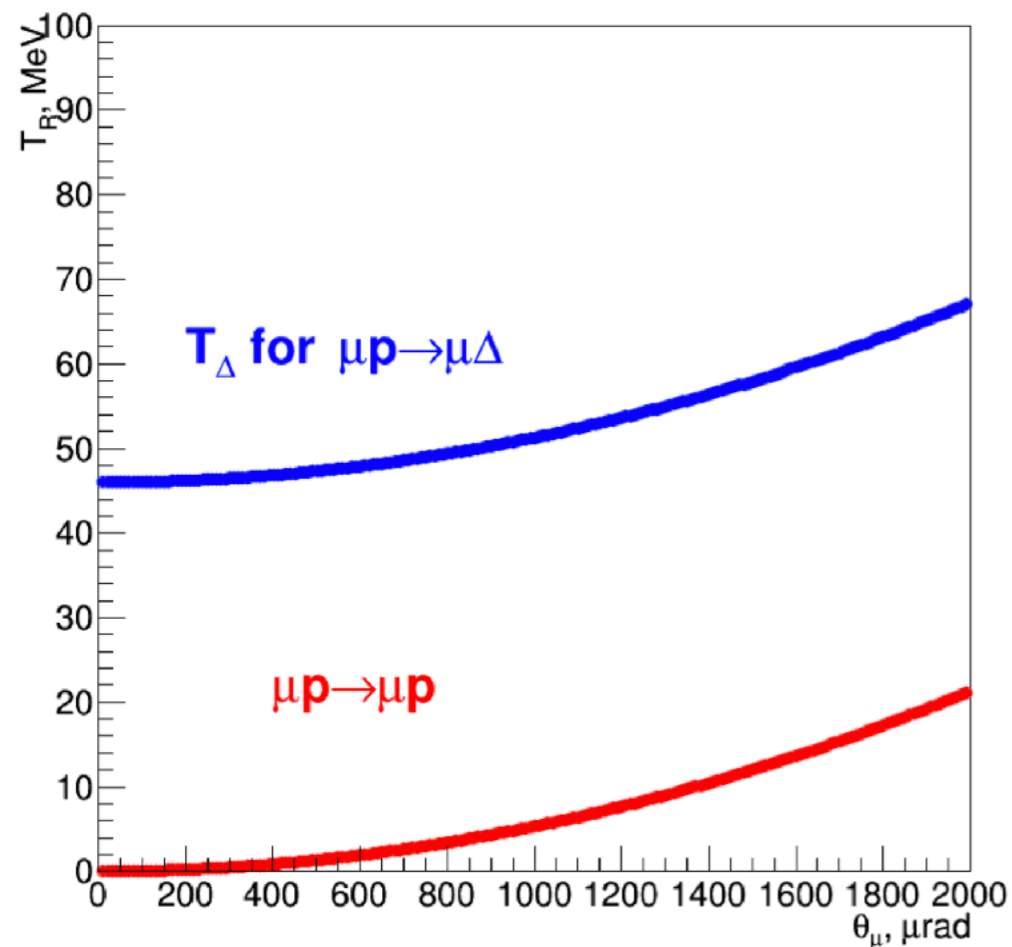
# TPC Proton Ranges



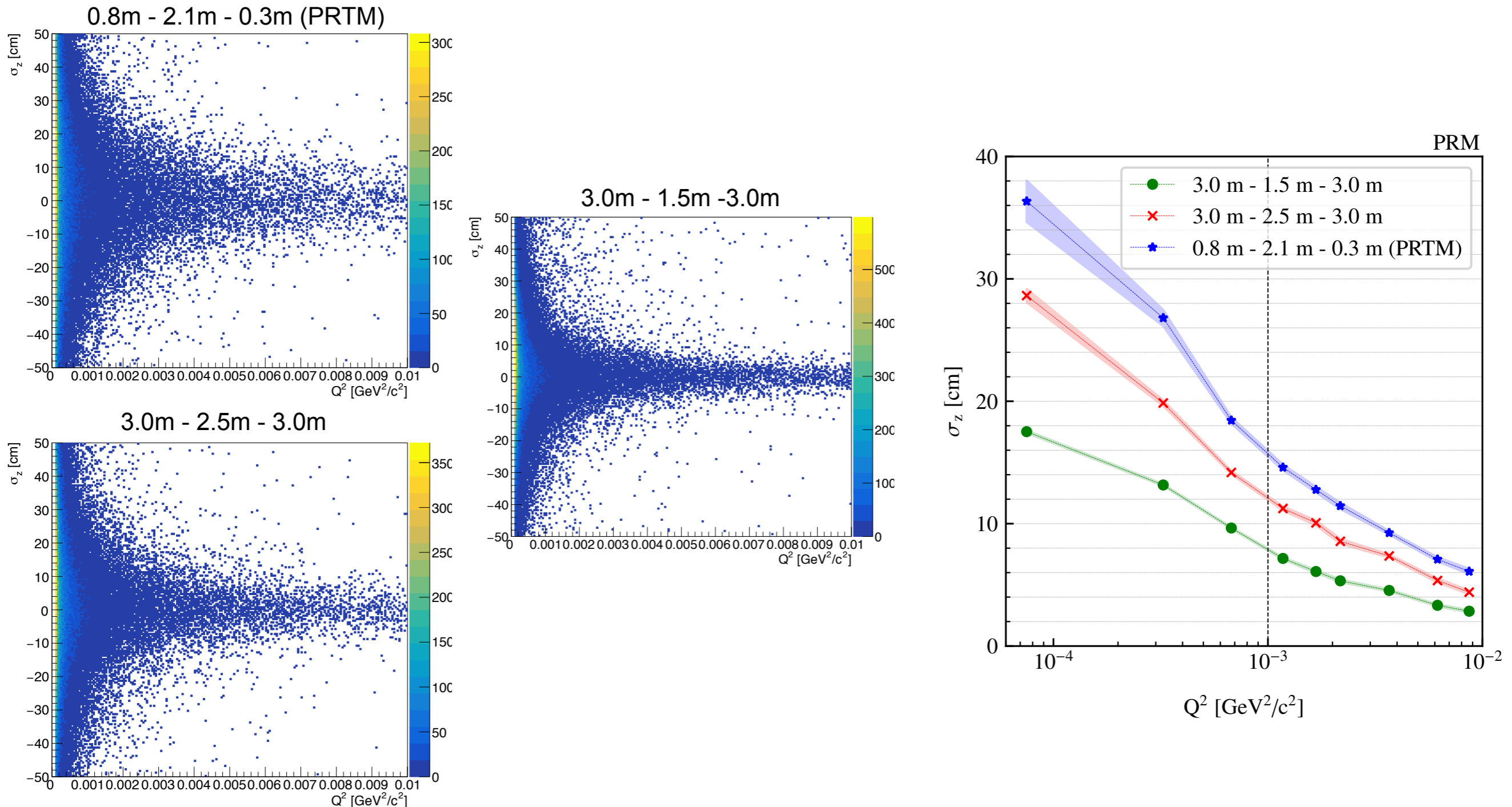
# Inelastic Background

## Example of $\Delta$ -production

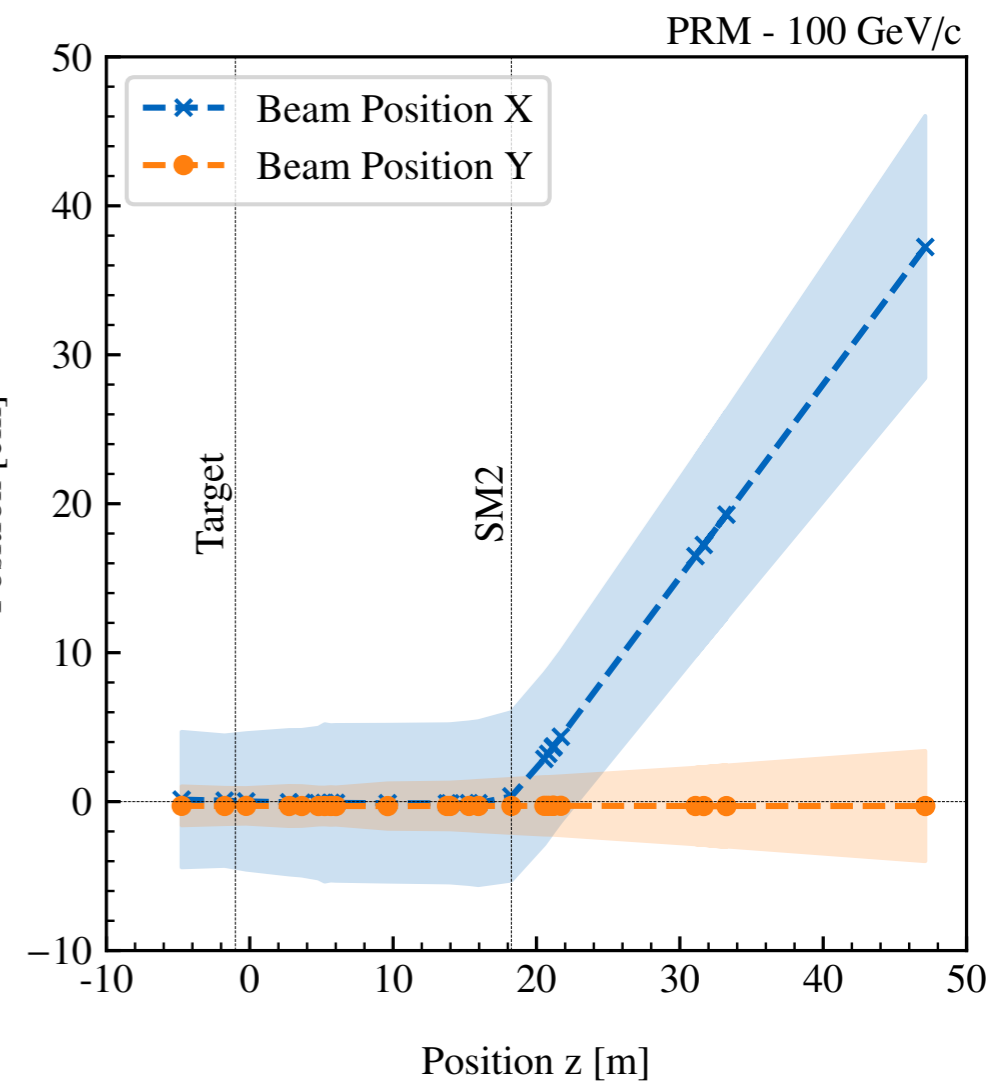
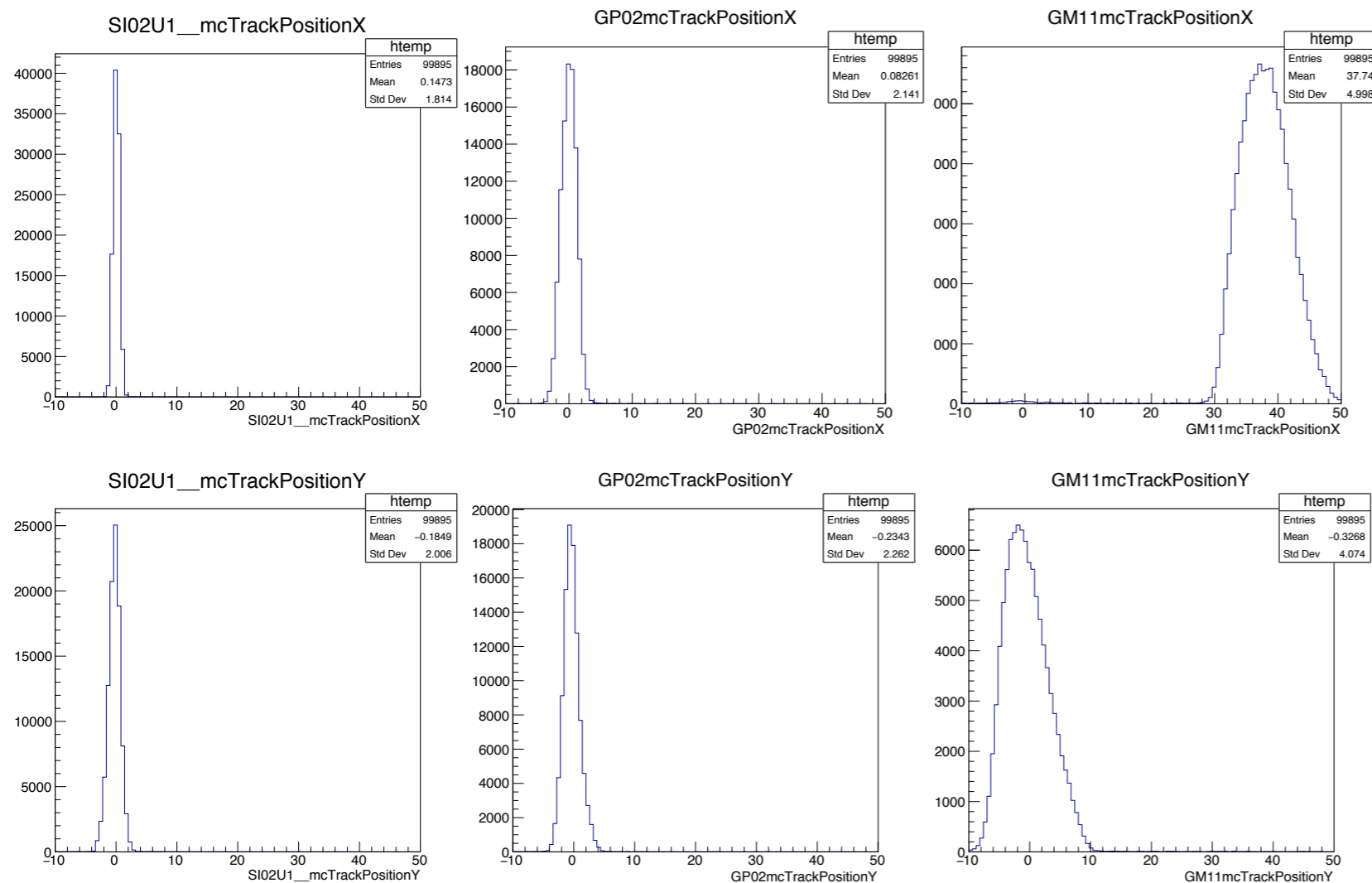
- 2-body  $\Delta(1232)$  production as proxy process for inelastic reactions
- Only a fraction of protons from  $\Delta$  decay have energies below 20 MeV
- Angular distributions from  $\Delta$  decays can be separated from elastic process  
→ kinematics of angle and energy can be used for separation



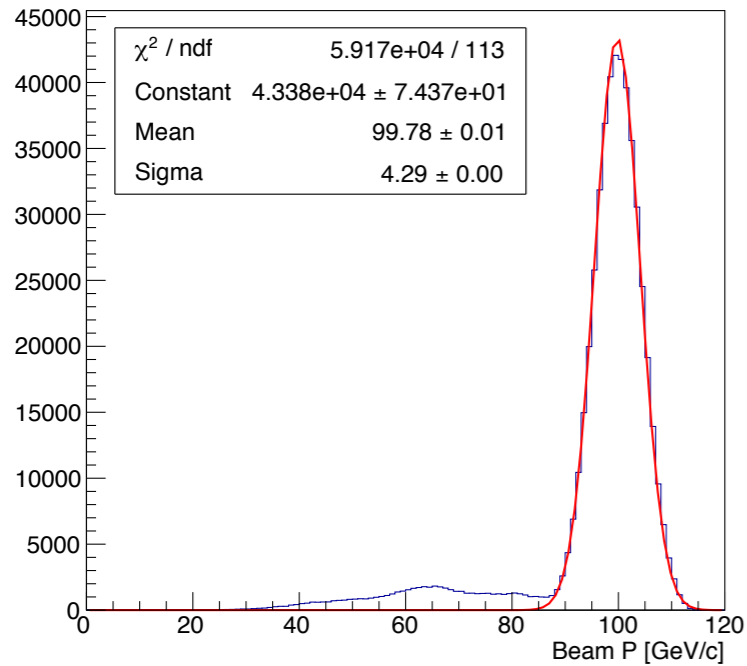
# Studies on Geometries



# Studies on Beam Properties

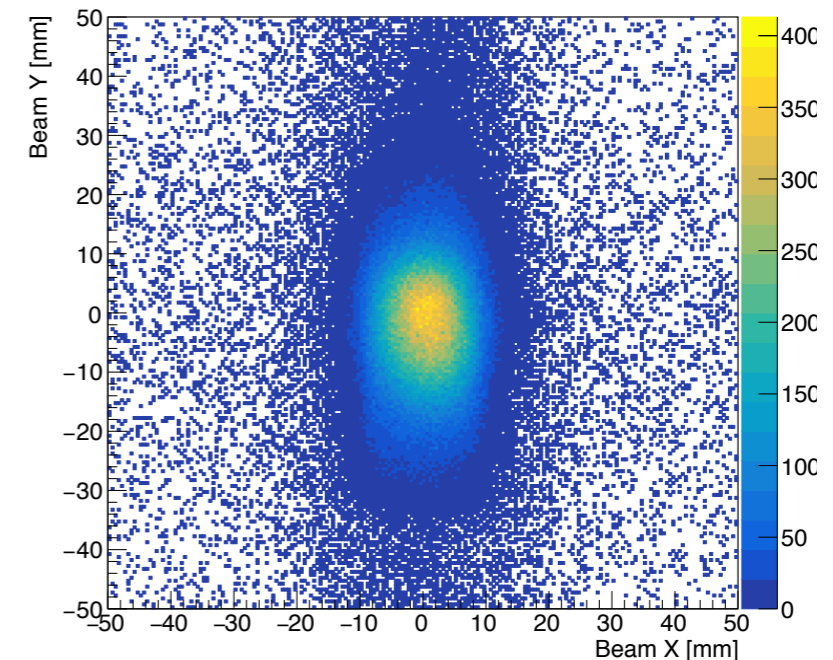
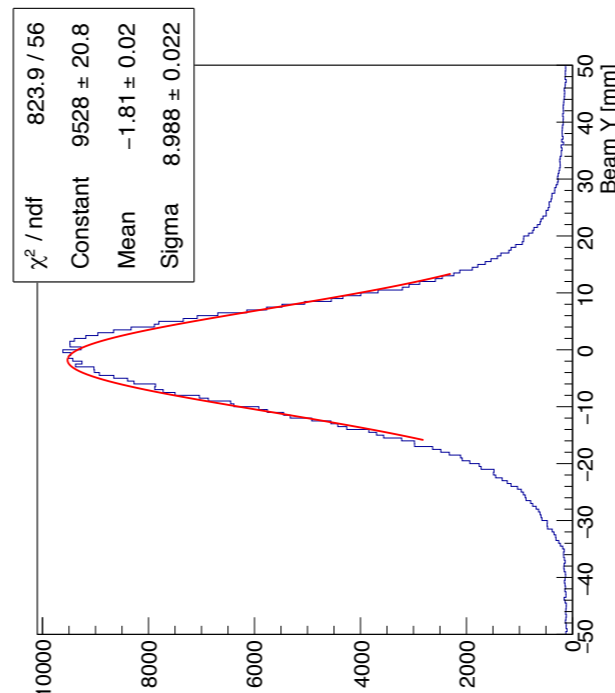
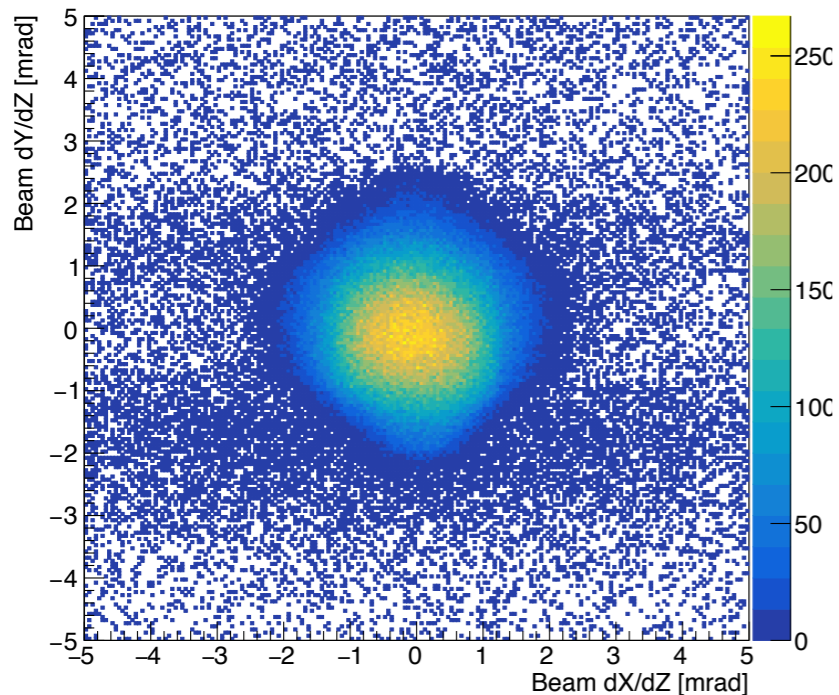
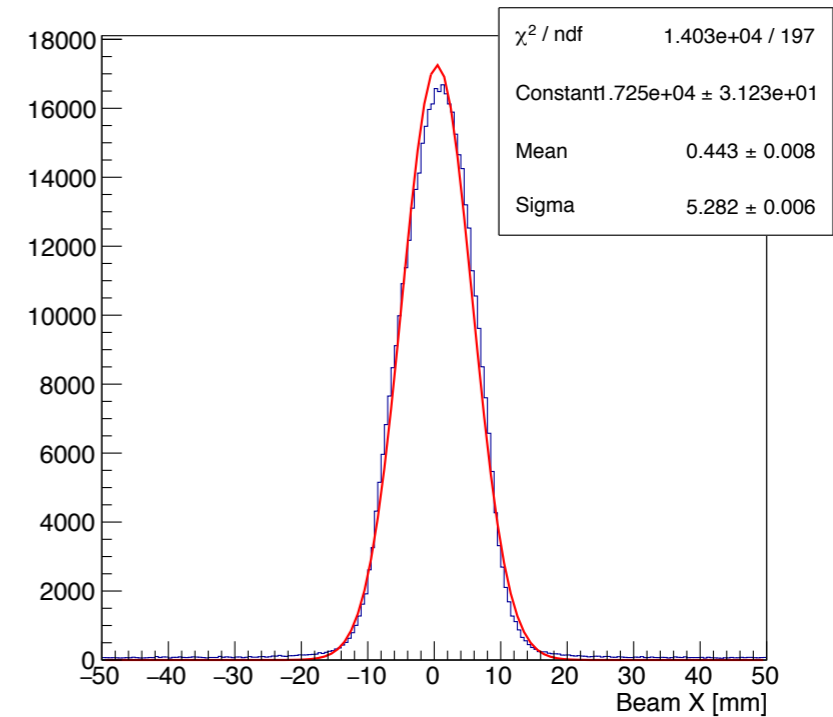


# Beam Properties (100 GeV/c)

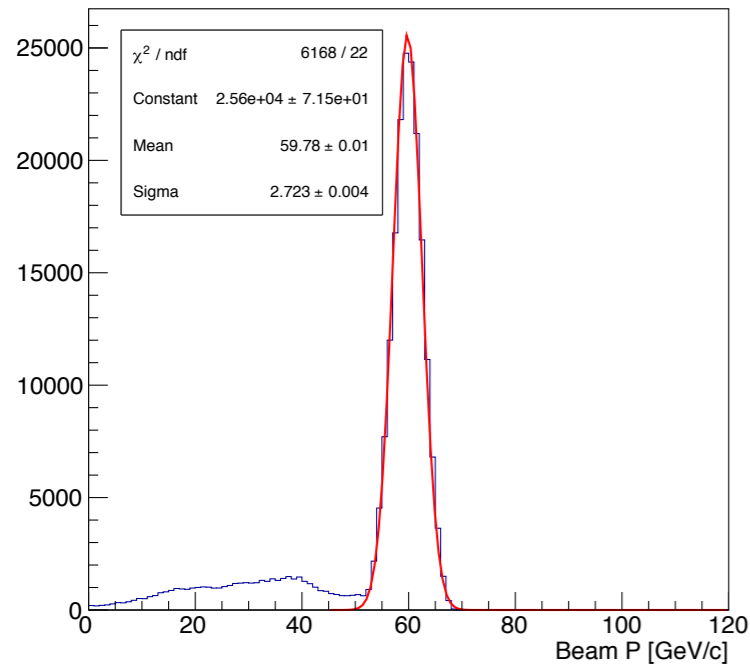


Beam file available:

- Focused at  $z = -1000$  mm
- Mostly parallel over 8 meters
- Contains tagged halo component

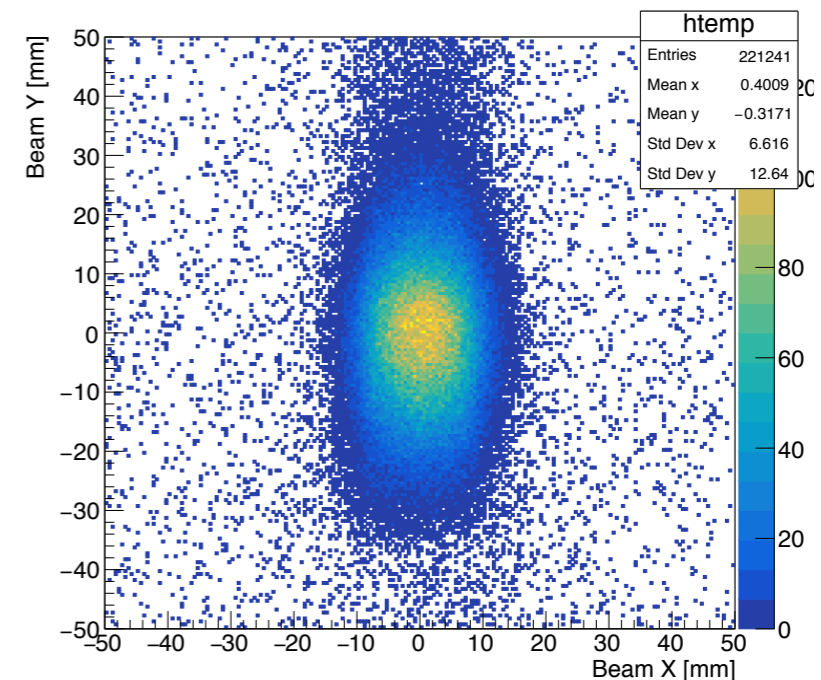
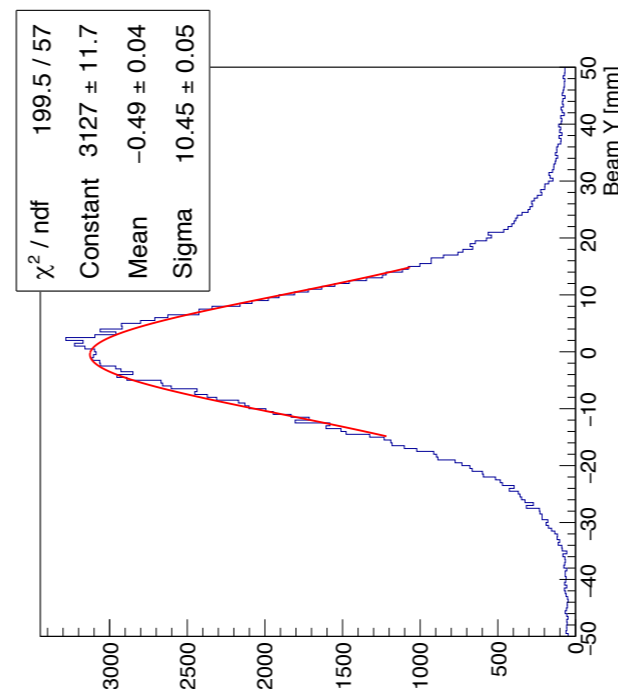
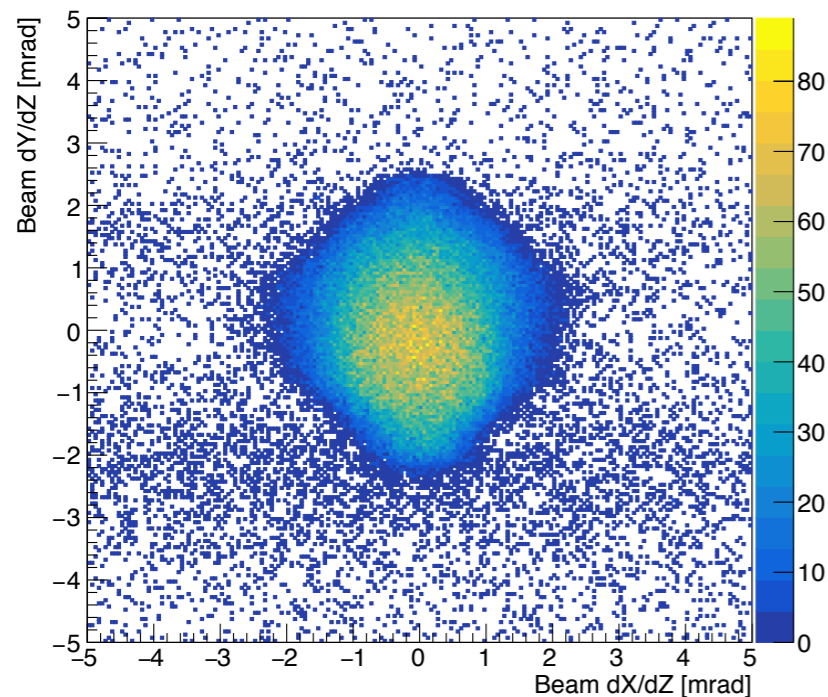
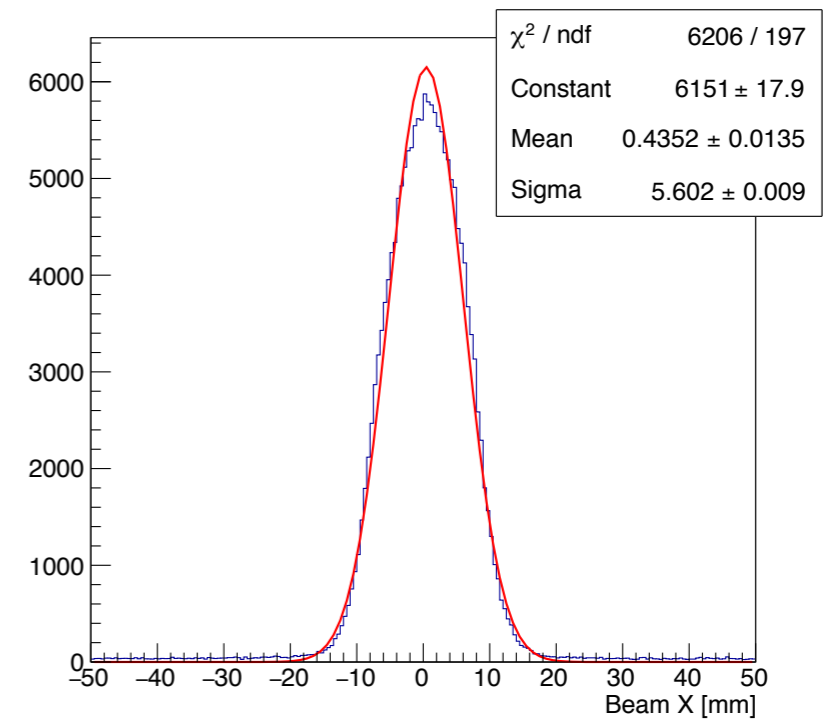


# Beam Properties (60 GeV/c)



Beam file available:

- Focused at  $z = -1000$  mm
- Mostly parallel over 8 meters
- Contains tagged halo component



# Material Budget

| material                         | planes | $d/\text{plane}$<br>[cm] | density $\rho$<br>[g/cm <sup>3</sup> ] | $X_0$<br>[g/cm <sup>2</sup> ] | $x/X_0$<br>[%o] | contribution<br>[%] |
|----------------------------------|--------|--------------------------|--|-------------------------------|-----------------|---------------------|
| Environment and tracking:        |        |                          |  |                               |                 |                     |
| Dry Air                          | 2      | 300.00                   | 0.00120                                | 36.62                         | 22.94           |                     |
| Helium*                          | 2      | 300.00                   | 0.00016                                | 94.32                         | 1.19            | 3.02                |
| Fibre (polystyrene)*             | 4      | 0.02                     | 1.04                                   | 43.79                         | 1.90            | 5.63                |
| Silicon*                         | 8      | 0.02                     | 2.33                                   | 21.82                         | 21.82           | 50.63               |
| TPC components (2-cell version): |        |                          |  |                               |                 |                     |
| Hydrogen (4 bar)                 | 2      | 40.00                    | 0.00033                                | 63.05                         | 0.52            |                     |
| Hydrogen (20 bar)*               | 2      | 40.00                    | 0.00166                                | 63.05                         | 2.63            | 6.24                |
| TPC-Anode (Kapton)*              | 2      | 0.040                    | 1.42                                   | 40.58                         | 2.80            | 8.30                |
| TPC-Anode (Cu)*                  | 2      | 0.002                    | 1.40                                   | 12.86                         | 0.44            | 1.29                |
| TPC-Anode (G10)*                 | 2      | 0.020                    | 1.80                                   | 30.17                         | 2.39            | 7.07                |
| TPC-Cathode (Al)*                | 1      | 0.003                    | 2.70                                   | 24.01                         | 0.34            | 1.00                |
| TPC-Window (Be)*                 | 2      | 0.100                    | 1.85                                   | 65.19                         | 5.68            | 16.82               |
| Total:                           |        |                          |  |                               | 33.74           | 100.00              |



# Vertex Distributions of Test Setup 2018

