

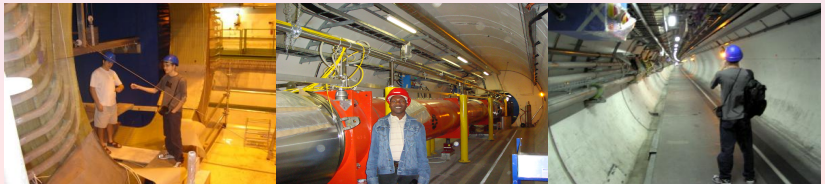


Foundations of Nuclear and Particle Physics.

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2/3 August 2010 / Stellenbosch, South Africa



Outline

- 1 High Energy Physics
- 2 High Energy Collisions
- 3 Natural Units
- 4 Kinematic Variables
- 5 An Example: Rapidity in a Thermal Model
- 6 Strangeness
- 7 Comparison of Chemical Freeze-Out Criteria
- 8 If everything is smooth why is there such a roller-coaster in the particle ratios?
- 9 Summary
- 10 A simple Bag model for the phase transition.



A vast subject which can easily cover a whole lecture series.
I will focus on the high energy physics aspects of nuclear and
particle physics covered at CERN in Europe and at the
Brookhaven National Lab in USA.



I will emphasize the difference between high energy particle physics and high energy nuclear physics.
Some aspects of quantum chromodynamics can only be unraveled in heavy ion collisions.



CERN



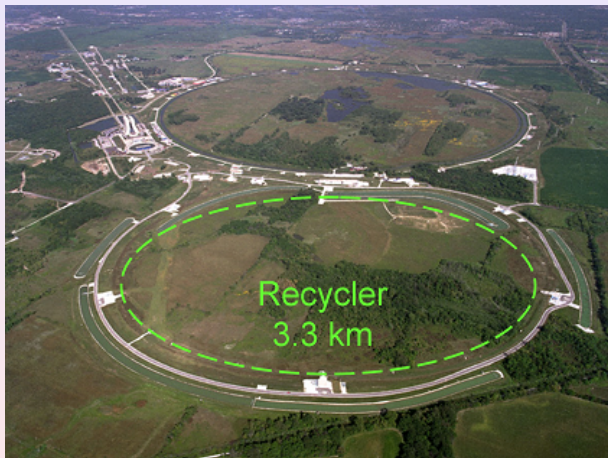
CERN

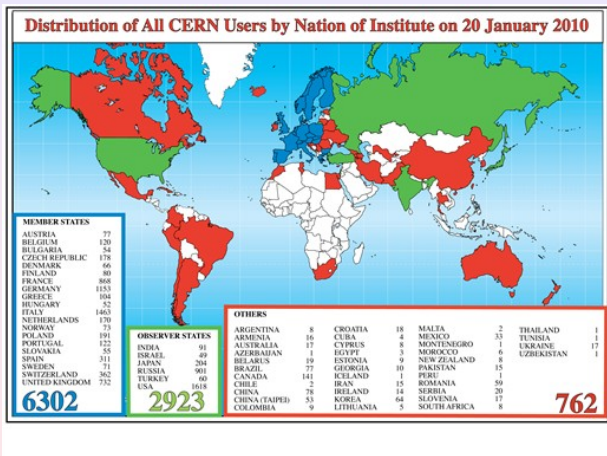


BNL-RHIC

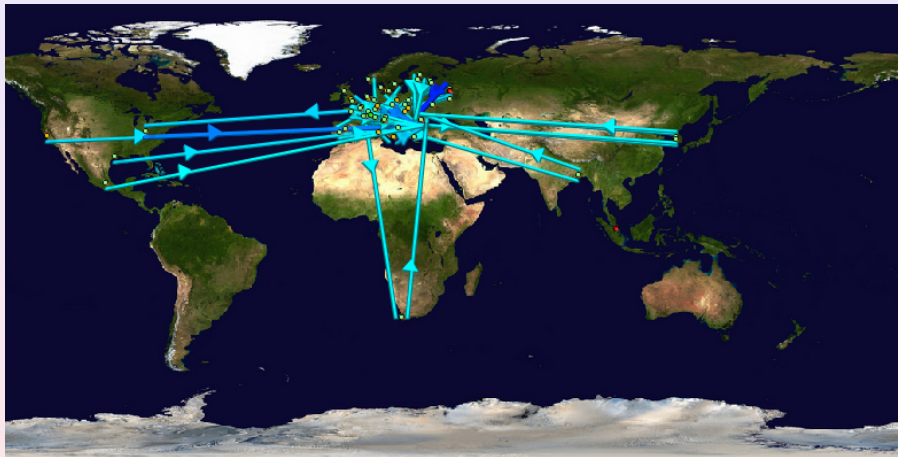


FermiLab

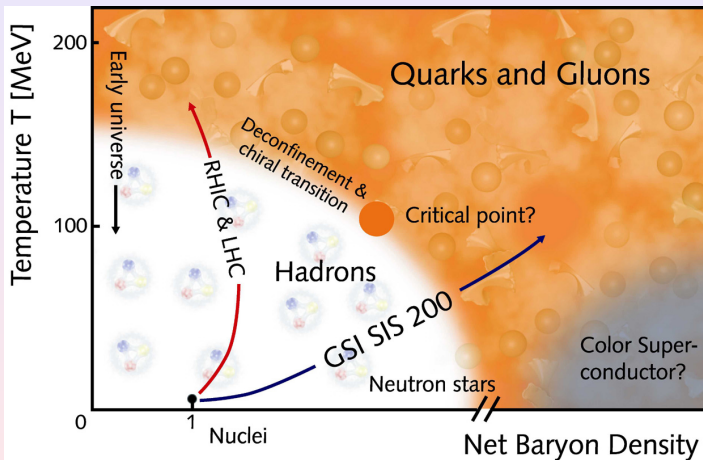




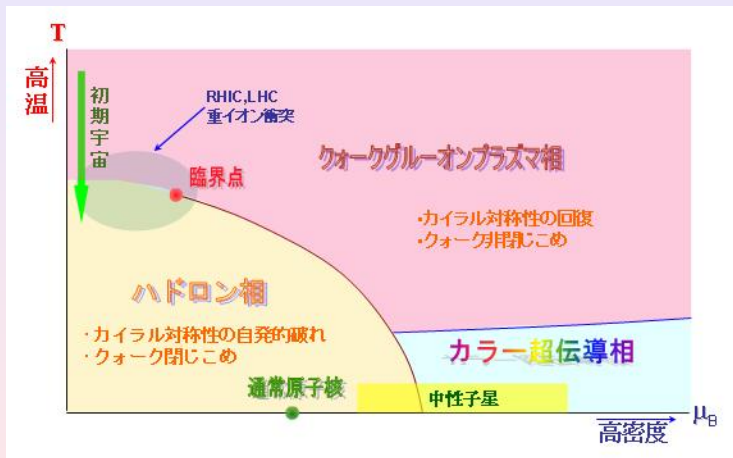
Grid Computing



Phase Diagramme



Phase Diagramme



Phase Diagramme



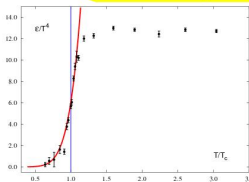
Critical behaviour in dense matter Hagedorn's Resonance Gas

R. Hagedorn, Nuovo Cimento 35 (1965) 395

strong interactions \Rightarrow exponentially rising spectrum of resonances

Hagedorn spectrum : $\rho(m_H) \sim c m_H^a e^{m_H/T_H}$

$$Z(T, \mu_B) = \int dm_H \rho(m_H) e^{-m_H/T}$$



\Rightarrow critical behaviour: $T_c \equiv T_H$
(end of hadronic physics)

resonance gas (adjusted mass spectrum):

~ 1000 resonance d.o.f.

lattice calculation:

(2+1)-flavor QCD, $m_q/T = 0.4$, $\mu_B = 0$

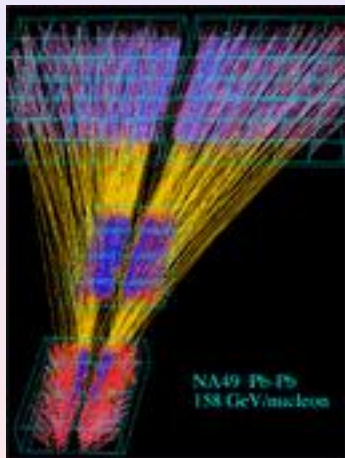
continuous transition at T_c

FK, K. Redlich, A. Tawfik, hep-ph/0303108

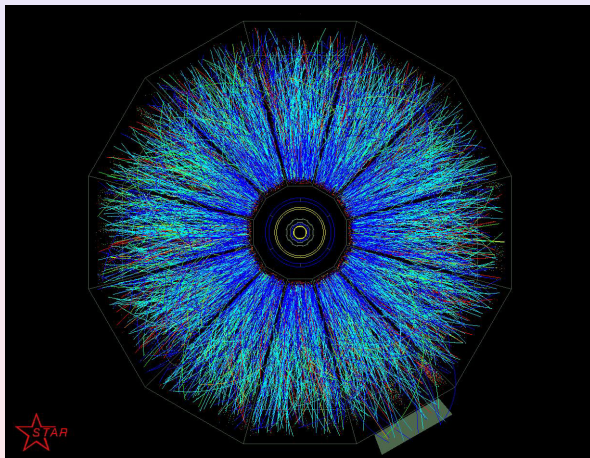
© Kersch, Strange Quark Matter 2004 - p.23/20



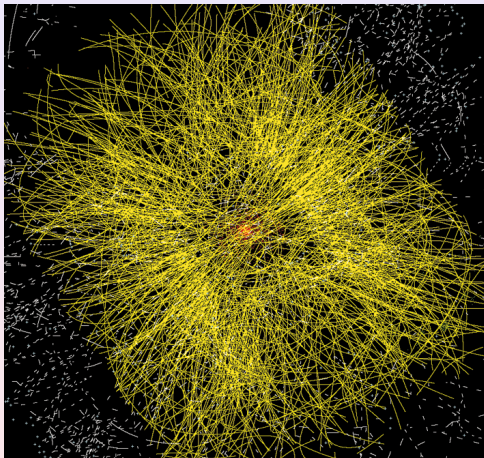
Event Simulation Pb-Pb at the SPS.



RHIC, Brookhaven



Event Simulation Pb-Pb at the LHC.



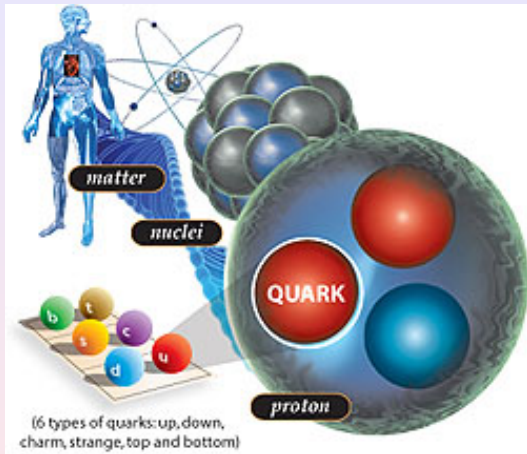
What are all those tracks?

g_i	m_i	stat	S_i	B_i	Q_i	Particle i
1	0.140	boson	0	0	1.	π^+
1	0.140	boson	0	0	-1.	π^-
2	0.938	fermion	0	1	1.	proton
2	0.938	fermion	0	-1	-1.	anti-proton
1	0.494	boson	1	0	1.	K^+
1	0.494	boson	-1	0	-1.	K^-



RHIC





In terms of quarks (and anti-quarks):

u-quark : charge $+2/3$

d-quark : charge $-1/3$

s-quark : charge $-1/3$

g_i	m_i	stat	S_i	B_i	Q_i	Particle i	
1	0.140	boson	0	0	1.	π^+	$u\bar{d}$
1	0.140	boson	0	0	-1.	π^-	$d\bar{u}$
2	0.938	fermion	0	1	1.	proton	uud
2	0.938	fermion	0	-1	-1.	anti-proton	$\bar{u}\bar{u}\bar{d}$
1	0.494	boson	1	0	1.	K^+	$u\bar{s}$
1	0.494	boson	-1	0	-1.	K^-	$s\bar{u}$



Natural Units

$$c = \hbar = 1 \quad (1)$$

$$c \equiv 299792458 \frac{m}{s} \quad \text{exact}$$

$$\hbar c \approx 197 \text{ MeV} \cdot \text{fm} \quad (2)$$

As an example:

$$\begin{aligned} 140 \text{ MeV} &= 140 \text{ MeV} \frac{1}{197 \text{ MeV} \cdot \text{fm}} \\ &= 0.71 \text{ fm}^{-1} \end{aligned} \quad (3)$$



Natural Units for Temperature

Boltzmann's constant

$$\begin{aligned}k_B &= 1 \\k_B &= 8.6173 \times 10^{-14} \text{ GeV}/^\circ\text{K}\end{aligned}\tag{4}$$

As an example:

$$1 \text{ eV} = 1.16 \times 10^5 \text{ }^\circ\text{K}\tag{5}$$



Kinematic variables

$$\begin{aligned} E^2 &= |\vec{p}|^2 + m^2 \\ &= p_x^2 + p_y^2 + p_z^2 + m^2 \\ &= p_T^2 + p_z^2 + m^2 \end{aligned} \tag{6}$$

$p_T^2 + m^2 \equiv m_T^2$ is called the **transverse mass**.

Hence

$$E^2 = p_z^2 + m_T^2 \tag{7}$$

$$E = m_T \cosh y$$

$$p_z = m_T \sinh y$$

y is called the rapidity.



Rapidity

$$E = m_T \cosh y = m_T \frac{1}{2} (e^y + e^{-y})$$
$$p_z = m_T \sinh y = m_T \frac{1}{2} (e^y - e^{-y})$$

$$m_T e^y = E + p_z$$
$$m_T e^{-y} = E - p_z$$

(8)

and

$$y = \frac{1}{2} \ln \frac{E+p_z}{E-p_z}$$



Tutorial 1: calculate the maximum value of the rapidity y at the highest beam energy at CERN $E = 7000$ GeV and at BNL $E = 200$ GeV. What is the corresponding γ factor?

Tutorial 2 : Show that $\frac{d^3\rho}{E}$ is invariant under Lorentz transformations.

Tutorial 3 : What is the temperature of the sun expressed in eV?

Rapidity

d^3p/E is invariant under Lorentz transformations.

$$\begin{aligned}\frac{d^3p}{E} &= p_T dp_T d\phi \frac{dp_z}{E} \\ &= m_T dm_T d\phi \frac{m_T \cosh y dy}{m_T \cosh y} \\ &= m_T dm_T d\phi dy\end{aligned}\tag{9}$$



Pseudo-Rapidity

Disadvantage of rapidity: need to know mass m of particle.

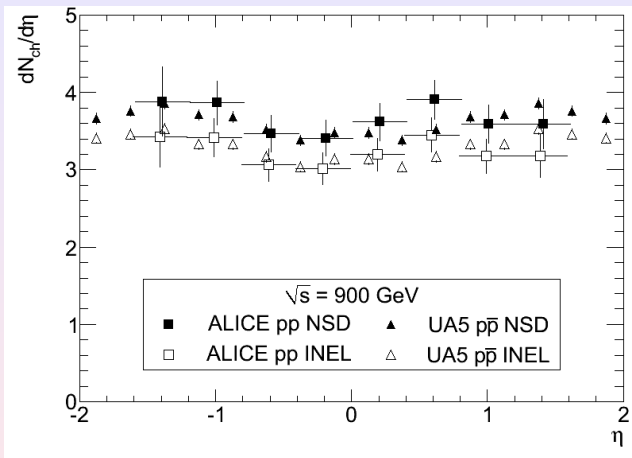
Pseudo-rapidity

$$\eta = \frac{1}{2} \ln \frac{|\vec{p}| + p_z}{|\vec{p}| - p_z}$$

$$\begin{aligned}\eta &= \frac{1}{2} \ln \frac{|\vec{p}| + p_z}{|\vec{p}| - p_z} \\ &= \frac{1}{2} \ln \frac{|\vec{p}| + |\vec{p}| \cos \theta}{|\vec{p}| - |\vec{p}| \cos \theta} \\ &= \frac{1}{2} \ln \frac{1 + \cos \theta}{1 - \cos \theta} \\ &= \frac{1}{2} \ln \frac{\cos^2(\theta/2)}{\sin^2(\theta/2)} \\ &= \ln \cot(\theta/2) \\ &= -\ln \tan(\theta/2)\end{aligned}\tag{10}$$

Hence one only needs to know the angle.

Pseudorapidity at the LHC



Conclusion: at 900 GeV p-p collisions at the LHC there is NOTHING NEW!!!

(This will not be true for heavy-ion collisions in November 2010.)



Momentum Distribution in a Thermal Model

$$N_i = g_i V \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E_i}{T} + \frac{\mu_i}{T}\right)$$

$$E_i \frac{dN_i}{d^3 p} = \frac{g_i}{(2\pi)^3} V E_i \exp\left(-\frac{E_i}{T} + \frac{\mu_i}{T}\right)$$

Momentum Distribution in a Thermal Model

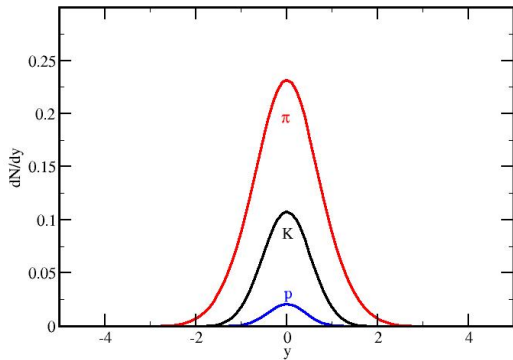
$$\frac{dN_i}{dy m_T dm_T} = \frac{g_i}{(2\pi)^2} V m_T \cosh y e^{-\frac{m_T}{T} \cosh y + \frac{\mu_i}{T}}$$

$$\frac{dN_i}{dy} = \frac{g_i V}{2\pi^2} \left[\frac{2T^3}{\cosh^2 y} + \frac{2mT^2}{\cosh y} + m^2 T \right] e^{\frac{\mu_i}{T}} e^{-\frac{m}{T} \cosh y}$$

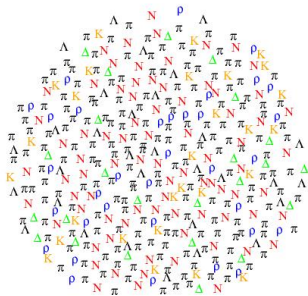
Narrow Distribution in Rapidity

Approximately Gaussian

Rapidity Distribution in the Thermal Model



Hadronic Gas



Thermal Equilibrium

In thermal equilibrium

$$Z = \text{Tr} e^{-\frac{H}{T} + \frac{\mu N}{T}}$$

$$\langle N \rangle = \frac{\text{Tr} N e^{-\frac{H}{T} + \frac{\mu N}{T}}}{\text{Tr} e^{-\frac{H}{T} + \frac{\mu N}{T}}}$$

$$\langle E \rangle = \frac{\text{Tr} E e^{-\frac{H}{T} + \frac{\mu N}{T}}}{\text{Tr} e^{-\frac{H}{T} + \frac{\mu N}{T}}}$$



Full Hydrodynamic Flow

Bjorken scaling + Transverse expansion

After integration over m_T

$$\frac{dN_i/dy}{dN_j/dy} = \frac{N_i^0}{N_j^0}$$

where N_i^0 is the particle yield
as calculated in a fireball **AT REST!**

Effects of hydrodynamic flow cancel out in ratios.



Thermal Equilibrium

Particle Number

$$\begin{aligned}\langle N \rangle &= \frac{\text{Tr} N e^{-\frac{H}{T} + \frac{\mu N}{T}}}{\text{Tr} e^{-\frac{H}{T} + \frac{\mu N}{T}}} \\ &= \frac{T}{Z} \frac{\partial}{\partial \mu} \text{Tr} e^{-\frac{H}{T} + \frac{\mu N}{T}} \\ &= T \frac{1}{Z} \frac{\partial Z}{\partial \mu} \\ &= T \frac{\partial}{\partial \mu} \ln Z\end{aligned}$$



Thermal Equilibrium

Average Energy

$$\begin{aligned}\langle E \rangle &= \frac{\text{Tr } H e^{\frac{-H}{T} + \frac{\mu N}{T}}}{\text{Tr } e^{\frac{-H}{T} + \frac{\mu N}{T}}} \\ &= -\frac{1}{Z} \frac{\partial Z}{\partial \beta} + \mu \langle N \rangle \\ &= T^2 \frac{\partial}{\partial T} \ln Z + \mu \langle N \rangle\end{aligned}$$



Thermal Equilibrium

$$\begin{aligned} N_i &= g_i V \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E}{T}\right) e^{\frac{\mu_i}{T}} \\ &= g_i V \frac{4\pi}{(2\pi)^3} \int p^2 dp \exp\left(-\frac{\sqrt{p^2 + m_i^2}}{T}\right) e^{\frac{\mu_i}{T}} \\ &= g_i V \frac{4\pi}{(2\pi)^3} T^3 \int x^2 dx \exp\left(-\sqrt{x^2 + m_i^2/T^2}\right) e^{\frac{\mu_i}{T}} \\ &= g_i V \frac{1}{2\pi^2} T m_i^2 K_2\left(\frac{m_i}{T}\right) e^{\frac{\mu_i}{T}} \end{aligned}$$



Thermal Equilibrium

$$n_i = g_i \frac{1}{2\pi^2} T m_i^2 K_2 \left(\frac{m_i}{T} \right) e^{\frac{\mu_i}{T}}$$

$$\epsilon_i = g_i \frac{1}{2\pi^2} T m_i^3 \left[K_1 \left(\frac{m_i}{T} \right) + 3 \frac{T}{m} K_2 \left(\frac{m_i}{T} \right) \right] e^{\frac{\mu_i}{T}}$$

$$s_i = g_i \frac{1}{2\pi^2} m_i^3 \left[K_1 \left(\frac{m_i}{T} \right) + \frac{4T}{m} K_2 \left(\frac{m_i}{T} \right) - \frac{\mu_i}{m} K_2 \left(\frac{m_i}{T} \right) \right] e^{\frac{\mu_i}{T}}$$

$$P_i = g_i \frac{1}{2\pi^2} T^2 m_i^2 K_2 \left(\frac{m_i}{T} \right) e^{\frac{\mu_i}{T}}$$



Chemical Equilibrium

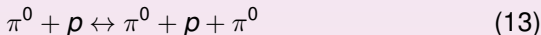
In equilibrium

$$E_1 + E_2 + \dots = E_3 + E_4 + E_5 + \dots \quad (11)$$

for the chemical potentials

$$\mu_1 + \mu_2 + \dots = \mu_3 + \mu_4 + \mu_5 + \dots \quad (12)$$

As an example



leads to

$$\mu_{\pi^0} + \mu_p = \mu_{\pi^0} + \mu_p + \mu_{\pi^0} \quad (14)$$

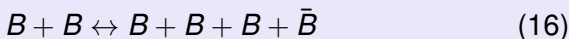
which leads to

$$\mu_{\pi^0} = 0 \quad (15)$$



Chemical Equilibrium

In equilibrium



$$dE = -pdV + TdS + \mu_B dN_B + \mu_{\bar{B}} dN_{\bar{B}}$$

Due to baryon number conservation one has

$$N_B - N_{\bar{B}} = \text{constant}$$

and

$$dN_B = dN_{\bar{B}}$$

The energy is a minimum for

$$dE = (\mu_B + \mu_{\bar{B}})dN_B = 0 \quad (17)$$

$$\mu_B = -\mu_{\bar{B}} \quad (18)$$



Chemical Equilibrium

In equilibrium

$$N_B = g V \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E}{T} + \frac{\mu_B}{T}\right)$$

$$N_{\bar{B}} = g V \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E}{T} - \frac{\mu_B}{T}\right)$$

$$N_B = N_{\bar{B}} \rightarrow \mu_B = 0$$

$$N_B \geq N_{\bar{B}} \rightarrow \mu_B \geq 0$$

$$N_B \leq N_{\bar{B}} \rightarrow \mu_B \leq 0$$



	Chemical Equilibrium	No Chem. Equil.
π	$\exp\left[-\frac{E_\pi}{T}\right]$	$\exp\left[-\frac{E_\pi}{T} + \frac{\mu_\pi}{T}\right]$
N	$\exp\left[-\frac{E_N}{T} + \frac{\mu_B}{T}\right]$	$\exp\left[-\frac{E_N}{T} + \frac{\mu_N}{T}\right]$
\bar{N}	$\exp\left[-\frac{E_N}{T} - \frac{\mu_B}{T}\right]$	$\exp\left[-\frac{E_N}{T} + \frac{\mu_{\bar{N}}}{T}\right]$
Λ	$\exp\left[-\frac{E_\Lambda}{T} + \frac{\mu_B}{T} - \frac{\mu_S}{T}\right]$	$\exp\left[-\frac{E_\Lambda}{T} + \frac{\mu_\Lambda}{T}\right]$
$\bar{\Lambda}$	$\exp\left[-\frac{E_\Lambda}{T} - \frac{\mu_B}{T} + \frac{\mu_S}{T}\right]$	$\exp\left[-\frac{E_\Lambda}{T} + \frac{\mu_{\bar{\Lambda}}}{T}\right]$
K	$\exp\left[-\frac{E_K}{T} + \frac{\mu_S}{T}\right]$	$\exp\left[-\frac{E_K}{T} + \frac{\mu_K}{T}\right]$
\bar{K}	$\exp\left[-\frac{E_K}{T} - \frac{\mu_S}{T}\right]$	$\exp\left[-\frac{E_K}{T} + \frac{\mu_{\bar{K}}}{T}\right]$



The number of particles of type i is determined by:

$$N_i = V g_i \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E_i}{T} + \frac{\mu_i}{T}\right)$$

For bosons:

$$N_i = V g_i \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\exp\left(\frac{E_i}{T} - \frac{\mu_i}{T}\right) - 1}$$

For fermions:

$$N_i = V g_i \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\exp\left(\frac{E_i}{T} - \frac{\mu_i}{T}\right) + 1}$$



Chemical Equilibrium

Only conserved quantum numbers matter for chemical equilibrium: In equilibrium

$$\mu_i = B_i\mu_B + Q_i\mu_Q + S_i\mu_S + C_i\mu_C + \dots \quad (19)$$

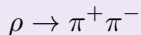


g_i	m_i	stat	S_i	B_i	Q_i	Particle i
1	0.140	-1	0	0	1.	π^+
1	0.135	-1	0	0	0.	π^0
1	0.140	-1	0	0	-1.	π^-
1	0.547	-1	0	0	0.	η
3	0.770	-1	0	0	1.	ρ^+
3	0.770	-1	0	0	0.	ρ^0
3	0.770	-1	0	0	-1.	ρ^-
3	0.782	-1	0	0	0.	ω
1	0.958	-1	0	0	0.	η'
1	0.980	-1	0	0	0.	f_0
1	0.982	-1	0	0	1.	a_0^+
1	0.982	-1	0	0	0.	a_0^0
1	0.982	-1	0	0	-1.	a_0^-
3	1.019	-1	0	0	0.	ϕ
3	1.170	-1	0	0	0.	
3	1.230	-1	0	0	1.	
3	1.230	-1	0	0	0.	
3	1.230	-1	0	0	-1.	
3	1.229	-1	0	0	1.	
3	1.229	-1	0	0	0.	
3	1.229	-1	0	0	-1.	
5	1.275	-1	0	0	0.	
3	1.282	-1	0	0	0.	
1	1.297	-1	0	0	0.	
1	1.300	-1	0	0	1.	
1	1.300	-1	0	0	0.	



The Role of Resonances

Example: ρ 's



Final, observed, number of π^+ is given by

$$N_{\pi^+} = N_{\pi^+}(\text{thermal}) + N_{\pi^+}(\text{resonance decays})$$

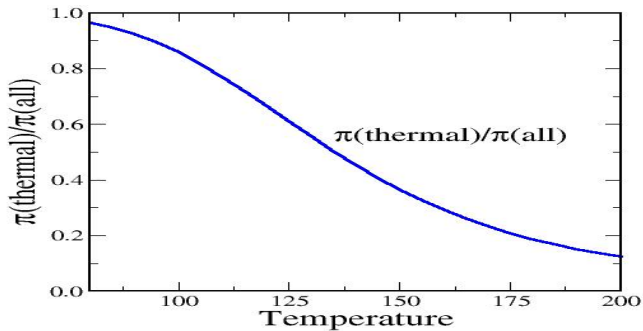
depending on the temperature, over 80% of observed pions are due to resonance decays



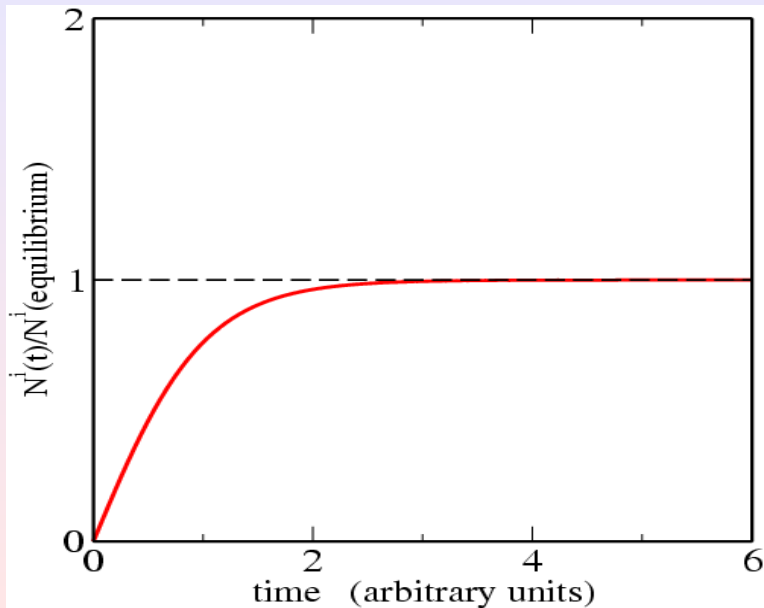
g_j	m_j	stat	S_j	B_j	Q_j	$BR \rightarrow \pi^+$	Particle i
1	0.140	-1	0	0	1.	1.000	π^+
1	0.135	-1	0	0	0.	0.000	π^0
1	0.140	-1	0	0	-1.	0.000	π^-
1	0.547	-1	0	0	0.	0.285	η
3	0.770	-1	0	0	1.	1.000	ρ^+
3	0.770	-1	0	0	0.	1.000	ρ^0
3	0.770	-1	0	0	-1.	0.000	ρ^-
3	0.782	-1	0	0	0.	0.910	ω
1	0.958	-1	0	0	0.	0.965	η'
1	0.980	-1	0	0	0.	0.521	f_0
1	0.982	-1	0	0	1.	1.285	a_0^+
1	0.982	-1	0	0	0.	0.285	a_0^0
1	0.982	-1	0	0	-1.	0.285	a_0^-
3	1.019	-1	0	0	0.	0.155	ϕ
3	1.170	-1	0	0	0.	1.000	h_1
3	1.230	-1	0	0	1.	1.500	
3	1.230	-1	0	0	0.	0.50	
3	1.230	-1	0	0	-1.	0.50	
3	1.229	-1	0	0	1.	1.91	
3	1.229	-1	0	0	0.	0.91	
3	1.229	-1	0	0	-1.	0.91	
5	1.275	-1	0	0	0.	0.69	
3	1.282	-1	0	0	0.	1.00	
1	1.297	-1	0	0	0.	1.11	
1	1.300	-1	0	0	1.	2.00	
1	1.300	-1	0	0	0.	1.50	



Importance of Resonances.



Strangeness saturation?



Strangeness saturation?

$$N_i = \boxed{\gamma_s^{|S|}} V g_i \int \frac{d^3 p}{(2\pi)^3} \exp\left(-\frac{E_i}{T} + \frac{\mu_i}{T}\right)$$

with

$\gamma_s < 1$ strangeness under-saturation

$\gamma_s = 1$ strangeness in chemical equilibrium

$\gamma_s > 1$ strangeness over-saturation



SPS data.

	Measurement
Pb–Pb 158A GeV	
$(\pi^+ + \pi^-)/2.$	600 ± 30
K^+	95 ± 10
K^-	50 ± 5
K_S^0	60 ± 12
p	140 ± 12
\bar{p}	10 ± 1.7
ϕ	7.6 ± 1.1
Ξ^-	4.42 ± 0.31
Ξ^-	0.74 ± 0.04
$\bar{\Lambda}/\Lambda$	0.2 ± 0.04



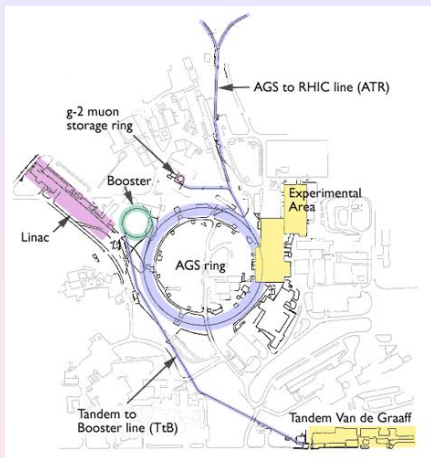
SPS data.

SPS: Chemical Freeze-Out Parameters:

$$\begin{aligned}T &= 156.0 \pm 2.4 \text{ MeV} \\ \mu_B &= 239 \pm 12 \text{ MeV} \\ \gamma_s &= 0.862 \pm 0.036\end{aligned}$$



AGS



AGS data.

	Measurement
Au–Au 11.6A GeV	
Participants	363 ± 10
K^+	23.7 ± 2.9
K^-	3.76 ± 0.47
π^+	133.7 ± 9.9
Λ	20.34 ± 2.74
p/π^+	1.234 ± 0.126
\bar{p}	$>0.0185 \pm 0.0018$



AGS data.

AGS: Chemical Freeze-Out Parameters:

$$\begin{aligned}T &= 130.6 \pm 5.5 \text{MeV} \\ \mu_B &= 594 \pm 26 \text{MeV} \\ \gamma_s &= 0.883 \pm 0.124\end{aligned}$$



SIS data.

	Measurement
Au–Au 1.7A GeV	
π^+/p	0.052 ± 0.013
K^+/π^+	0.003 ± 0.00075
π^-/π^+	2.05 ± 0.51
η/π^0	0.018 ± 0.007



SIS data.

SIS: Chemical Freeze-Out Parameters:

$$\begin{aligned} T &= 49.7 \pm 1.1 \text{MeV} \\ \mu_B &= 818 \pm 15 \text{MeV} \\ \gamma_s &= 1 \text{ (fixed)} \end{aligned}$$



RHIC data.

Ratio	Experiment	Central	Mid-Central	Peripheral
$\pi_{(2)}^- / \pi_{(2)}^+$	BRAHMS	0.990±0.100		
	PHENIX	0.960±0.177	0.920±0.170	0.933±0.172
	PHOBOS	1.000±0.022		
	STAR	1.000±0.073	1.000±0.073	1.000 ± 0.073
$K_{(2)}^+ / K_{(2)}^-$	PHENIX	1.152±0.240	1.292±0.268	1.322±0.284
	PHOBOS	1.099±0.111		
	STAR	1.109±0.022	1.105±0.036	1.120±0.040
$\bar{p}_{(1)} / p_{(1)}$	PHENIX	0.680±0.149	0.671±0.142	0.717±0.157
$\bar{p}_{(2)} / p_{(2)}$	BRAHMS	0.650±0.092		
	PHOBOS	0.600±0.072		
	STAR	0.714±0.050	0.724±0.050	0.764±0.053
$\bar{\Lambda}_{(1)} / \Lambda_{(1)}$	PHENIX	0.750±0.180	0.798±0.197	0.795±0.197
$\bar{\Lambda}_{(2)} / \Lambda_{(2)}$	STAR	0.719±0.090	0.739±0.092	0.744±0.100
$\Xi_{(2)}^+ / \Xi_{(2)}^-$	STAR	0.840±0.053	0.822±0.114	0.815±0.096
$\bar{\Omega}^+ / \Omega^-$	STAR	1.062±0.410		
$K_{(2)}^- / \pi_{(2)}^-$	PHENIX	0.151±0.030	0.134±0.027	0.116±0.023
	STAR	0.151±0.022	0.147±0.022	0.130±0.019
$K_S^0 / \pi_{(2)}^-$	STAR	0.134±0.022	0.131±0.022	0.108±0.018
$\bar{p}_{(1)} / \pi_{(2)}^-$	PHENIX	0.049±0.010	0.047±0.010	0.045±0.009
$\bar{p}_{(2)} / \pi_{(2)}^-$	STAR	0.069±0.019	0.067±0.019	0.067±0.019
$\Lambda_{(1)} / \pi_{(2)}^-$	STAR	0.043±0.008	0.043±0.008	0.039±0.007
$\Lambda_{(2)} / \pi_{(2)}^-$	PHENIX	0.072±0.017	0.068±0.016	0.074±0.017
$< K^{*0} > / \pi_{(2)}^-$	STAR	0.039±0.011		
$\phi / \pi_{(2)}^-$	STAR	0.022±0.003	0.021±0.004	0.022±0.004
$\Xi_{(2)}^- / \pi_{(2)}^-$	STAR	0.0093±0.0012	0.0072±0.0011	0.0060±0.0008
$\Omega^- / \pi_{(2)}^-$	STAR	0.0014±0.0004		



RHIC data.

RHIC: Chemical Freeze-Out Parameters:

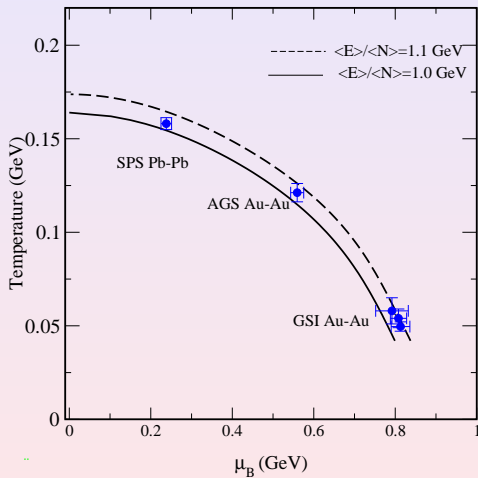
$$T = 169 \pm 4.2 \text{ MeV}$$

$$\mu_B = 39.6 \pm 6 \text{ MeV}$$

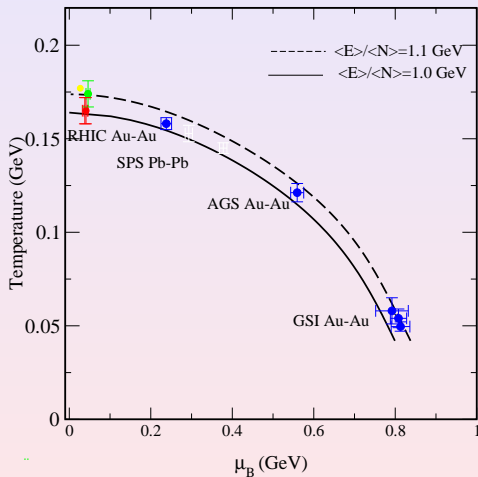
$$\gamma_s = 0.9 \pm 0.1$$



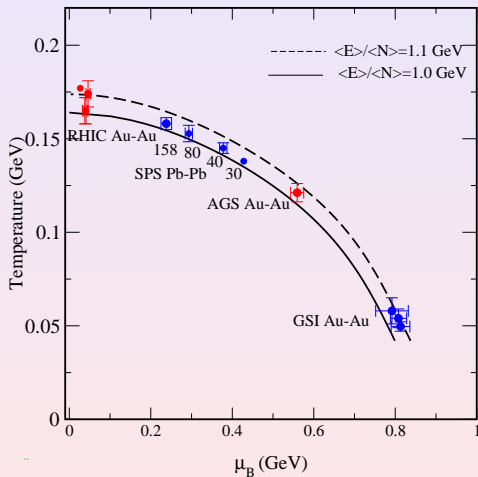
E/N in 1999



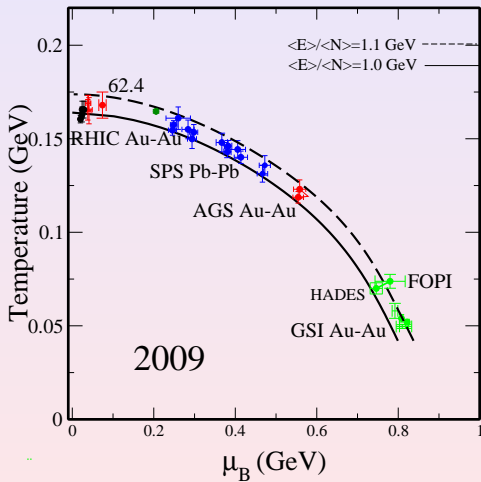
E/N in 2000



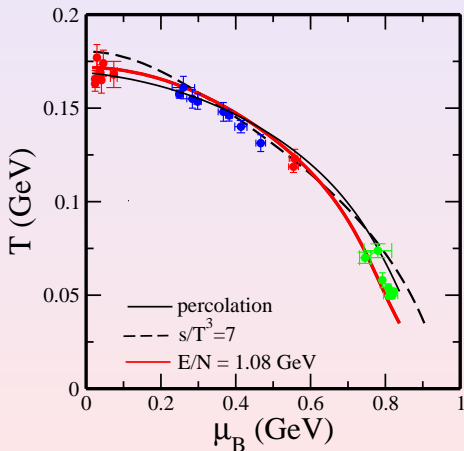
E/N in 2005



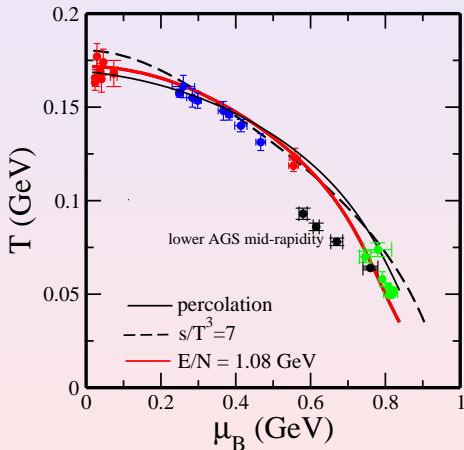
E/N in 2009



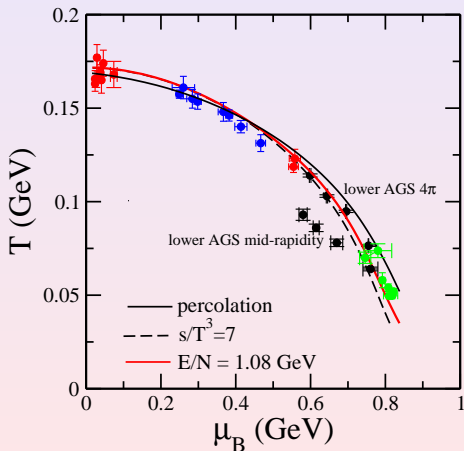
Chemical Freeze-Out: Criteria



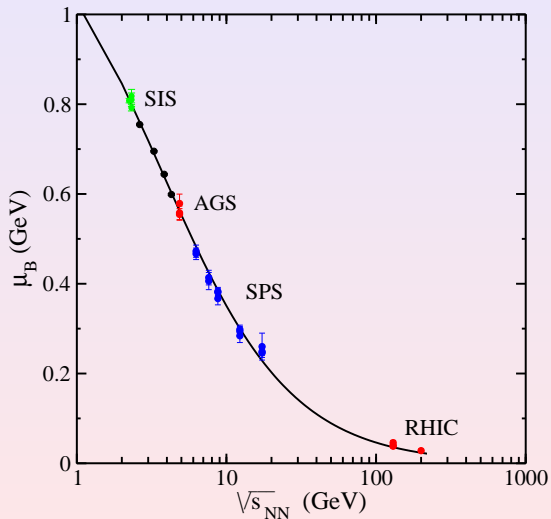
Chemical Freeze-Out: Criteria



Chemical Freeze-Out: Status in 2010



μ_B as a function of $\sqrt{s_{NN}}$



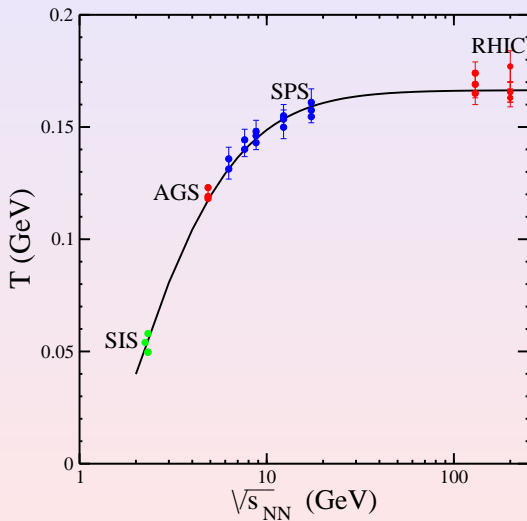
μ_B as a function of $\sqrt{s_{NN}}$

$$\mu_B(\sqrt{s}) = \frac{1.308 \text{ GeV}}{1 + 0.273 \text{ GeV}^{-1} \sqrt{s}}.$$

This predicts at LHC $\mu_B \approx 1 \text{ MeV}$.



T as a function of $\sqrt{s_{NN}}$



ALICE: presentations at 72 conferences in 2010!

Publications

- *“First proton-proton collisions at the LHC as observed with the ALICE detector: measurement of the charged-particle pseudorapidity density at $\sqrt{s} = 900$ GeV.”*
European Physics Journal C65 (2010) 111-125
- *“Charged-particle multiplicity measurement in proton-proton collisions at $\sqrt{s} = 0.9$ and 2.36 TeV with ALICE and LHC.”*
European Physics Journal C68 (2010) 89-108
- *“Charged-particle multiplicity measurement in proton-proton collisions at $\sqrt{s} = 7$ TeV with ALICE and LHC.”*
European Physics Journal (submitted)
- *“Midrapidity antiproton-to-proton ratio in pp collisions at $\sqrt{s} = 0.9$ and 7 TeV measured by the ALICE experiment.”*
Physical Review Letters (accepted for publication)

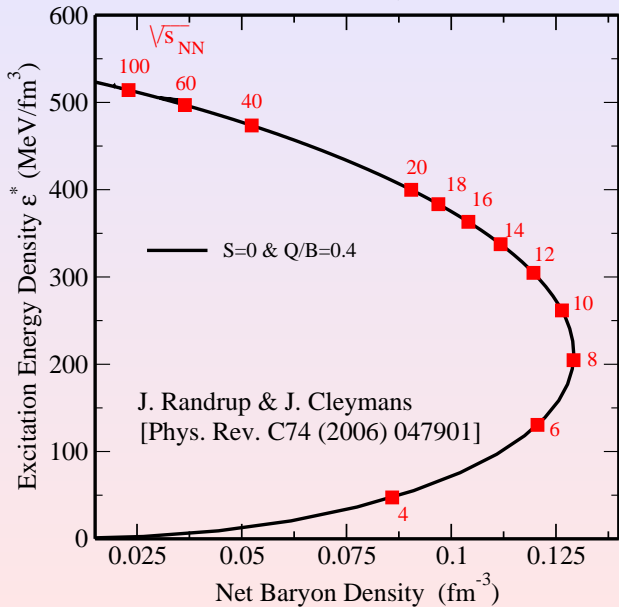


- *“Two-pion Bose-Einstein correlations in pp collisions at $\sqrt{s} = 900 \text{ GeV}$.”*
- *“Transverse momentum spectra of charged particles in proton-proton collisions at $\sqrt{s} = 900 \text{ GeV}$ with ALICE and LHC.”*

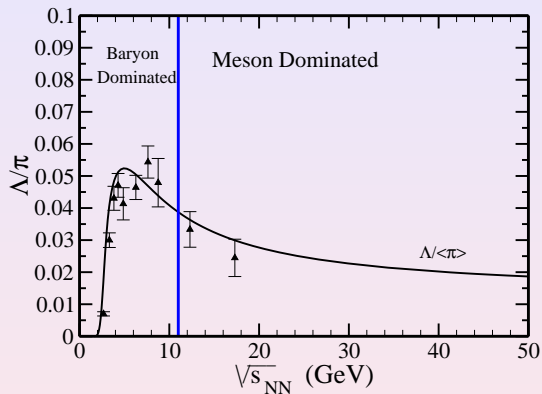


Hadronic Freeze-Out

$$\varepsilon^* = \varepsilon - m_N \rho$$



Roller-coaster Λ/π Ratio

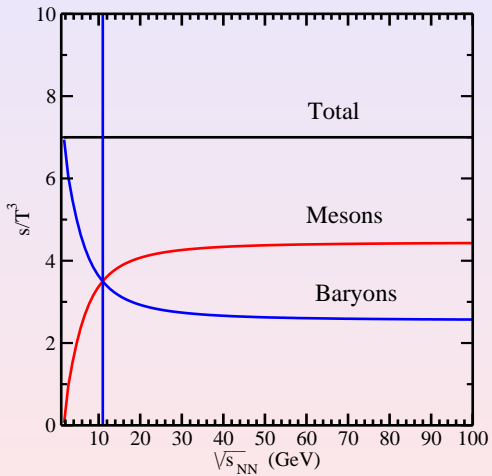


THERMUS

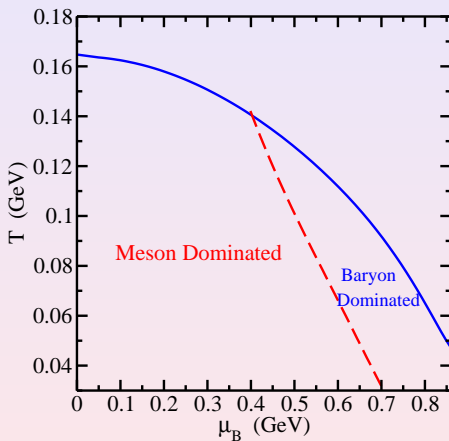
S. Wheaton, J. Cleymans, M. Hauer

Comp. Phys. Comm. 180 (2009) 84-106

$$s/T^3$$



Transition



Strangeness in Heavy Ion Collisions

vs

Strangeness in pp - collisions

Use the Wroblewski factor

$$\lambda_s = \frac{2 \langle s\bar{s} \rangle}{\langle u\bar{u} \rangle + \langle d\bar{d} \rangle}$$

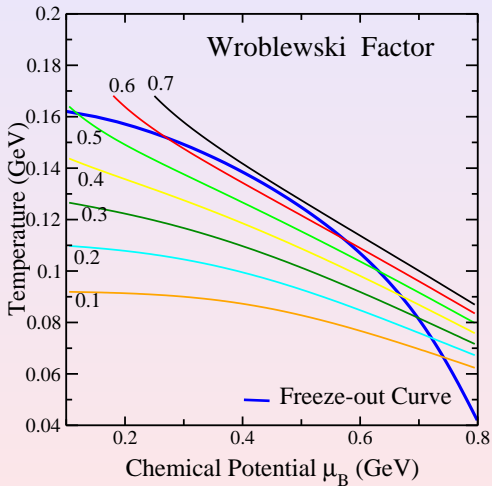
This is determined by the number of **newly** created quark – anti-quark pairs and **before** strong decays, i.e. before ρ 's and Δ 's decay.

Limiting values :

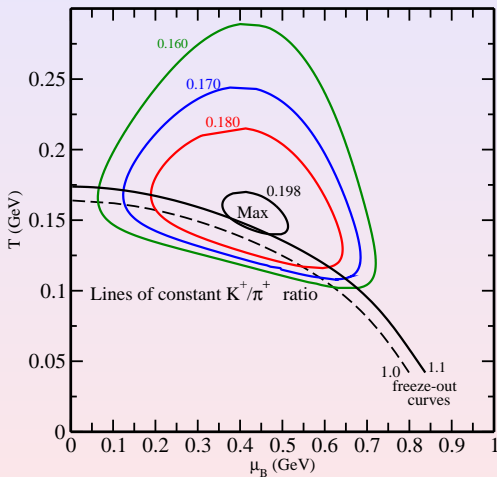
$\lambda_s = 1$ all quark pairs are equally abundant, SU(3) symmetry.

$\lambda_s = 0$ no strange quark pairs.

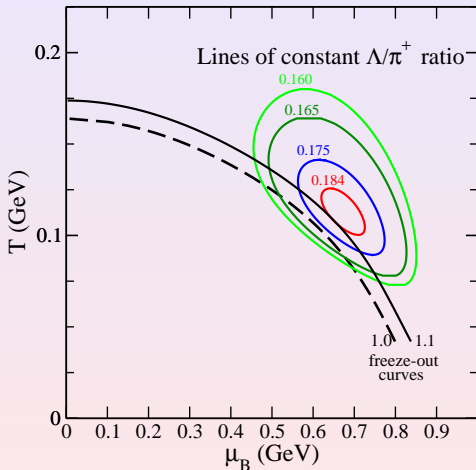
Maxima in particle ratios : K^+/π^+

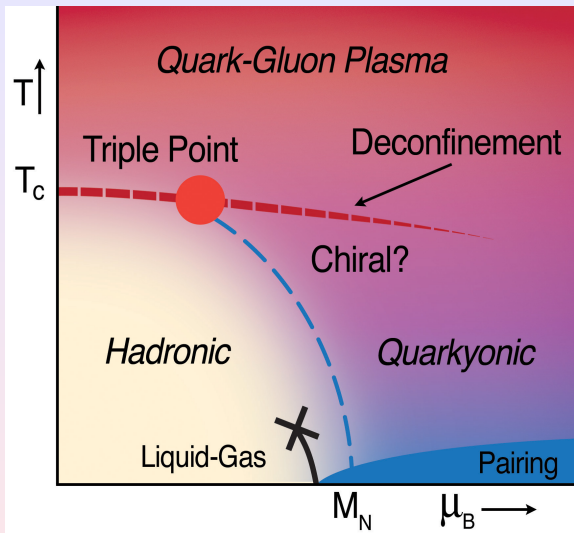


Maxima in particle ratios : K^+/π^+



Maxima in particle ratios : K^+/π^+





R. Pisarski and L. McLerran



RHIC



In conclusion, the roller-coaster seen in the particle ratios corresponds to a transition from a baryon-dominated to a meson-dominated hadronic gas. This transition occurs at a

- temperature $T = 151$ MeV,
- baryon chemical potential $\mu_B = 327$ MeV,
- energy $\sqrt{s_{NN}} = 11$ GeV.

In the statistical model this transition leads to peaks in the $\Lambda / \langle \pi \rangle$, K^+ / π^+ , Ξ^- / π^+ and Ω^- / π^+ ratios.



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Hadronic sector : Massless Pions

$$P_{\pi}/T^4 = \pi^2/30 \approx 1/3$$

$$\epsilon_{pi}/T^4 = \pi^2/10 \approx 1$$

QGP sector : Massless Quarks and Gluons

$$P_Q/T^4 = (37\pi^2/90) \approx 4$$

$$\epsilon_{pi}/T^4 = (37\pi^2/30) \approx 12$$



