

Calibration of the PSPMT (LJU diary 8)

A. Studen H. Kagan N. Clinthorne

Department of Physics,
Ohio State University,
Columbus, OH

Institut Jožef Stefan
Odsek za eksperimentalno fiziko osnovnih delcev
andrej.studen@ijs.si



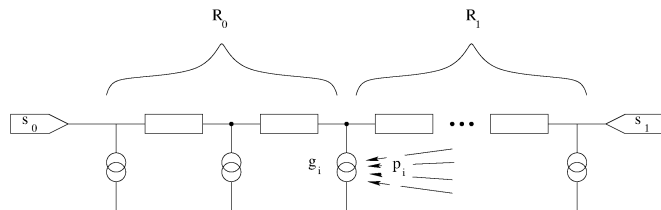
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LYSO module study

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/mnt/hrpet1/data1/pet/test/20171214/ants2Flood/run0/root
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LYSO position decoding



- Light p_i incident on tube i out of N tubes with gain g_i connected through resistor chain to outputs s_0 and s_1 , i numbering from 0 at s_0 to $N - 1$ at s_1
- For a single hit in i -th PSPMT, we get

$$s_0 = (1 - \alpha_i)g_i p_i \quad s_1 = \alpha_i g_i p_i$$

where α_i is the ratio of resistivity

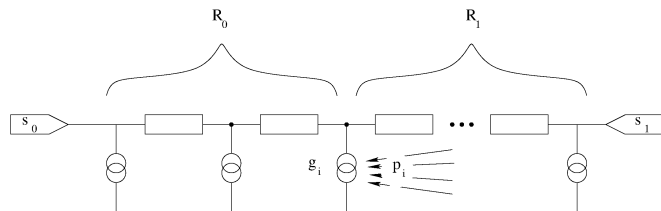
$$\alpha_i = \frac{R_0}{R_1 + R_0} = i/(N - 1)$$

- In actual events, more than 1 PMT is hit, hence

$$s_0 = \sum_i (1 - \alpha_i)g_i p_i \quad s_1 = \sum_i \alpha_i g_i p_i$$

- Asymmetry in expressions prevents from absorbing g_i in resistor values. Equivalently - cannot separate low energy event in high gain tube from high energy event in low gain tube.

LYSO position decoding



- Convert to linear algebra by writing:

$$G = \text{diag}\{g_i\}$$

$$\mathbf{e} = \text{ones}(\text{size}(\mathbf{p}))$$

$$\mathbf{p} = \{p_i\}, \quad \boldsymbol{\alpha} = \{\alpha_i\}$$

- Coordinate in Anger's algebra:

$$x = \frac{s_1 - s_0}{s_1 + s_0} = \frac{(\mathbf{e} - 2\boldsymbol{\alpha})^T G \mathbf{p}}{\mathbf{e}^T G \mathbf{p}}$$